Explaining Soft-Goal Conflicts through Constraint Relaxations

Submission #3

Abstract

Recent work suggests to explain trade-offs between soft goals in terms of their conflicts, i.e., minimal unsolvable soft-goal subsets. But this does not explain the conflicts themselves: Why can a given set of soft-goals not be jointly achieved? Here we approach that question in terms of the underlying constraints on plans in the task at hand, namely resource availability and time windows. In this context, a natural form of explanation for a soft-goal conflict is a minimal constraint relaxation under which the conflict disappears (“if the deadline was 1 hour later, it would work”). We explore algorithms for computing such explanations. A baseline is to simply loop over all relaxed tasks and compute the conflicts for each separately. We improve over this by two algorithms that leverage information – conflicts, reachable states – across relaxed tasks. We show that these algorithms can exponentially outperform the baseline in theory, and we run experiments confirming that advantage in practice.

Introduction

Imagine planning the next Mars Rover Mission. Due to the rovers’ limited resources and timing constraint for data collection and uploads, only some of the rovers’ tasks can be planned. Recent work by Eifler et al. (2020a; 2020b) suggests to explain trade-offs between such soft goals in terms of conflicts, i.e., minimal unsolvable soft-goal subsets. However, this does not give further insights into why the soft-goals can not be jointly achieved. Understanding the cause of these conflicts and possible resolutions are crucial to reasoning about different options and finding the best trade-offs.

Here, we explore the question of what causes soft-goal conflicts in tasks with constraints such as resource availability and time windows. In this context, soft-goal conflicts can naturally be explained by identifying the minimal constraint relaxations under which the conflict disappears. For example the conflict \{x-ray image, soil sample\} could be explained by :“The rover needs 2 more units of energy or the upload window to relay X needs to be 3 time units longer, to perform both tasks”. A similar approach is used in constraint programming (Lauffer and Topcu 2019; Senthooran et al. 2021), where they introduce soft constraints, to provide suggestions on how to modify an infeasible subset of constraints to make it feasible. We investigate algorithms for computing such explanations based on minimal relaxations in a set of given relaxations, which we instantiate with resource and time window constraint relaxations.

Eifler et al. (2020b) introduced an algorithm which computes all minimal unsolvable goal subsets of a task by expanding the whole search space while tracking all maximal solvable goal subsets. To reduce the search space size they prune all states from which, according to a given heuristic, no superset of the current incumbent solution is reachable. The basic adaption of this procedure is to iteratively call it for each relaxed task separately and compute the minimal relaxed task where each conflict disappears in a post processing step.

We introduce two algorithms which improve over this baseline by taking advantage of the fact that information like reachable goal subsets and states can be propagated from one relaxed task to another if the latter is more relaxed. The first algorithm, Internal Constraint Reuse (ICR), iteratively computes the conflicts for each increasingly relaxed planning task, and reuses the reachable subgoals from less relaxed tasks. This provides the pruning function with a growing set of reachable subgoals that it can use to prune parts of the search space that do not contain any subgoals that have not yet been achieved. The second algorithm, Search Space Reuse (SSR), reduces duplicate work by iteratively increasing one search space instead of generating a new one per relaxed task. This is done by storing the search frontier of unreachable states for each task, and using it as the starting point for more relaxed tasks. Thus for each relaxed task only the newly reachable states are generated.

We show that these algorithms can exponentially outperform the baseline, with respect to number of generated states, in theory. Experiments on 4 resource-centric domains and 3 domains with time windows show that both algorithms perform significantly better than the baseline in practice, and that they are complementary to each other with respect to finding explanations on resource- and time- centric domains.

Related Work

Sreedharan et al. (2019) explain the unsolvability of a task by identifying a necessary subgoal of a relaxed task, which is
unachievable in the original task. They use relaxations based on projections on subsets of the state variables. Thus, this approach is not suited to quantify the relaxation necessary to make the task solvable. An ‘excuse’ for unsolvability, as defined by (Göbelbecker et al. 2010), is a series of value changes in the initial state and addition of objects to make a task solvable. Their approach is not aimed at providing an intuitive explanation of why the task is not solvable, but rather to point out errors in the model description. The automated scheduling system by Agraval et al. (2020) is able to provide information on constraint relaxations for activities that could not be scheduled. Their main focus is to identify all unsatisfied constraints of an activity and present them alongside the schedule to help the user to inspect them. So far, their analysis does not include any reasoning on the extent to which a constraint needs to be relaxed to schedule the activity. The unsolvability certificates provided by the proof system of Eriksson et al. (2017; 2018) are not intended to be human readable and do not provide information on how the task could be rendered solvable.

Preliminaries

Planning Formalism

A finite-domain representation (FDR) (Bäckström and Nebel 1995) planning task with soft-goals is a tuple \( \tau = (V, A, I, G^{soft}, G^{hard}) \), where \( V \) is a finite set of state variables \( v \) with domain \( D(v) \), \( A \) is a finite set of actions, and \( I \) is a complete assignment to \( V \) called initial state. \( G^{soft} \) and \( G^{hard} \) are disjoint partial assignment to \( V \) called soft and hard-goal. A state is a complete assignment to \( V \). Variable-value pairs \( v = d \) are referred to as facts, and (partial) variable assignments are identified by sets of facts. The value of \( v \) in the (partial) variable assignments \( s \) is referred to as \( s(v) \). Each action consists of a precondition and effect \( (\text{pre}_a, \text{eff}_a) \) defined as partial assignments to \( V \). A action \( a \) is applicable in a state \( s \) (\( \text{app}(a, s) \)) if \( \text{pre}_a \subseteq s \). Applying \( a \) to \( s \), denoted by \( s[[a]] = s' \), changes the values of \( s \) to \( s'(v) := \text{eff}_a(v) \) if \( \text{eff}_a(v) \) is defined and leaves them the same \( s'(v) := s(v) \) otherwise. The resulting state of an iteratively applicable action sequence \( \pi \) is denoted by \( s[[\pi]] \). A plan is an action sequence where \( G^{hard} \subseteq I[[\pi]] \). \( \Pi(\tau) \) denotes the set of all possible plans for task \( \tau \). The prefix \( a_0 \cdots a_n \) of plan \( \pi = a_0 \cdots a_i, a_j \cdots a_n \) up to action \( a_j \) is denoted by \( \text{prefix}(\pi, a_j) \).

Running Example Our running example is based on the IPC Rovers domain. One rover must collect up to three samples \( S_0, S_1, S_2 \) and upload the data to a relay satellite. The rover can perform three different actions: move between two locations, take a sample if it is at the corresponding location, and upload the collected data at \( l_0 \) or \( l_3 \). The road map and the initial location of the rover are depicted on the left in Figure 1.

Planning with Consumed Resources

A consumed resource \( \rho \) with domain \( D(\rho) = [0, \rho_{max}] \subset \mathbb{N} \) has an initial value \( \text{init}_\rho \in D(\rho) \) and a function \( \delta_\rho : A \rightarrow \mathbb{N} \) that maps each action to the amount of resource consumed by that action. A state represents a complete assignment to \( V \cup \{ \rho \} \). An action \( a \) is applicable in a state \( s \) if \( \text{pre}_a \subseteq s \) and the remaining value of \( \rho \) is sufficient to execute the action \( s(\rho) \geq \delta_\rho(a) \). Applying \( a \) in state \( s \) decreases the resource by \( \delta_\rho(a) : s[[a]](\rho) = s(\rho) - \delta_\rho(a) \). The amount of resource \( \rho \) consumed by an action sequence \( \pi \) is given by \( \text{con}(\pi) = \sum_{a \in \pi} \delta_\rho(a) \). An extension to multiple resources is defined accordingly, where the set of all resources is denoted by \( R \). In our running example there is one resource \( B \), battery energy.

Planning with Simple Time Windows

We restrict ourselves to an extension with a concept of time that can be compiled to classical planning. This means discrete time units and no parallel execution of actions.

A (start) time window is a tuple \( W = (A_W, o, c) \) with \( 0 \leq o \leq c \leq t_{\text{max}} \). The application of the actions in \( A_W \subset A \) is constrained by the opening time \( o \) and closing time \( c \). The function \( \delta_t : A \rightarrow \mathbb{N} \) maps each action to its execution duration. The passed time units are represented by the variable \( t \) with domain \( D(t) = [0, t_{\text{max}}] \). A state represents a complete assignment to \( V \cup \{ t \} \). An action \( a \) is applicable in a state \( s \) if \( \text{pre}_a \subseteq s \) and if \( a \in A_W \), then \( o \leq s(t) \leq c \) holds. Applying an action \( a \) in state \( s \) increases the passed time by \( \delta_t(a) : s[[a]](t) = s(t) + \delta_t(a) \). The execution duration of an action sequence \( \pi \) is given by \( \text{dur}(\pi) = \sum_{a \in \pi} \delta_t(a) \) and the execution time point of action \( a \) in \( \pi \) is given by \( \text{exec}(\pi, a) = \text{dur}(\text{prefix}(\pi, a)) \). An extension to multiple time windows is defined accordingly, where the set of all time windows is denoted with \( W \). In the running example there is one time window \( W_U = \{ \{\text{upload}(S_1)\} \cup \{\text{upload}(S_2)\}, 4, 6 \} \) which allows to upload data to the relay satellite only between the time points 4 and 6.

Explanation Framework

In Eif20 framework \( G^{soft} \) represents a set of plan properties, specifically LTLf plan-preference formulas compiled into (soft-)goal facts (Baier and McIlraith 2006; Edelkamp 2006; Eifler et al. 2020b). The explanation facility uses exclusion dependencies between these plan properties to generate answers to the users question. The soft-goals \( X, Y \subseteq G^{soft} \) exclude each other if all plans of \( \tau \) that achieve all \( g \in X \), do not achieve all \( g \in Y \). The strongest dependencies of this kind are given by the minimal unsolvable goal subsets (MUGS) \( X \cup Y = G \subseteq G^{soft} \) where \( G \) cannot be achieved but every \( G' \subseteq G \) can. The set of all MUGS for a task \( \tau \) is denoted by \( \text{MUGS}(\tau) \).

Conflict Explanation Through Relaxations

We provide explanations for a soft-goal conflict based on minimal constraint relaxations under which the conflict dis-
appears. In the following sections we define the relaxations that are considered and how we identify explanations based on a given set of relaxed tasks.

**Relaxation Orders**

In planning, the most general property of an abstraction or relaxation $T'$ of a planning task $T$ is that all plans of $T$ are preserved (Culberson and Schaeffer 1998; Edelkamp 2001; Seipp and Helmert 2013). This gives the most general definition of a relaxed task as:

**Definition 1 (Relaxed Task).** Let $T$ be a planning task. Then $T'$ is a relaxed task of $T$ (denoted by $T \subseteq T'$) iff $\Pi(T) \subseteq \Pi(T')$.

Our explanation approach and algorithms make no further assumptions about the specific implementation of relaxation.

To compute the explanation for a conflict in task $T$, we assume a finial set of relaxed tasks $T$ for $T$, where $T \subseteq {T_1, \ldots, T_n}$, and for all $T' \in T$, $T \subseteq T'$, is given.

For $T'$ the relation $T_r \subseteq T'_r$ represents a partial order, which we will use to define a *minimal* relaxed task that resolves a conflict. The partially ordered set $T = (T, \subseteq)$ we call in the following a relaxation order for $T$.

The functions $C_U(T)$ and $C_L(T)$ denote the upper and lower covers of $T$ within $T$. Given a partially ordered set $S$ then the upper cover of an element $e \in S$ is the set $C_U(e) = \{e' \in S \mid e' > e \land \exists e'' \in S : e' > e'' > e\}$, and the lower cover the set $C_L(e) = \{e' \in S \mid e' < e \land \exists e'' \in S : e' < e'' < e\}$. One of our algorithms additionally assumes, that $T$ has a supremum.

**Resource and Time Constraint Relaxations**

Now we instantiate the above with Resource and Time Window Constraint Relaxations.

**Resource Constraint Relaxations** A task with consumed resources can be relaxed by increasing the initial resource value.

**Definition 2 (Resource Relaxed Task).** Let $T = (\tau, R)$ be a planning task $\tau$ with resources $R$. Then a resource relaxed task with respect to a resource $\rho \in R$ is defined as $T' = (\tau, R')$ where $R'$ is the relaxed resource $\rho$ replaced by resource $\rho'$ with $D(\rho) = D(\rho') = [0, \rho_{max}]$, $\delta(\rho) = \delta(\rho')$ and $\rho_{max} \geq init(\rho) \geq init(\rho')$.

A resource relaxed task indeed represents a relaxed task according to Definition 1:

**Proposition 1.** Let $T'$ be a resource relaxed task of $T$. Then, $\Pi(T) \subseteq \Pi(T')$.

**Proof sketch:** $\Pi(T) \subseteq \Pi(T')$, because every action sequence $\pi = a_0 \ldots a_n$ applicable in $I$ of $T$ is also applicable in $I'$ of $T'$. For all actions $a_i \in \pi$ with $a_i = \text{prefix}(\pi, a_i)$, $s = I[|\pi_i|]$, $s' = I'[|\pi_i|]$ and $c = \text{con}(\pi_i)$, $a_i$ is applicable in $s'$ because $a_i$ is applicable in $s$ and $s(V) = s'(V)$ and $\text{init}(\rho) = s(\rho) < s'(\rho) = \text{init}(\rho') - c$.

Making the application of an action cheaper by reducing $\delta(\rho)$ is another option to relax a task with respect to a resource. This is almost equivalent to increasing the initially available resource, given that the resource is depletable and the action appears once in the plan. We use increasing resource availability as a proxy for any reduction in resource consumption.

Using the set $T_\rho$ of all resource relaxed tasks of task $T$ with respect to $\rho$, we get a well defined relaxation order $T_\rho = (T_\rho, \subseteq)$ for $T$. Since all $T_i \in T_\rho$ are exclusively distinguished by $\text{init}(\rho)$, we have $T \subseteq T'$ iff $\text{init}(\rho') < \text{init}(\rho)$, which results in a total order for $T_\rho$. The task $T'$ where $\text{init}(\rho') = \rho_{max}$ represents the supremum of $T_\rho$. The upper/lower cover of $T'$ is the relaxed task where the initial resource value is one unit larger/smaller than in $T'$.

For our running example we have four relaxed tasks for the battery $T_B = \{T_i \mid i \in \{7, 8, 9, 10\}\}$, where in $T_i$ the initial battery level is $i$.

**Time Constraint Relaxations** A task with simple time windows can be relaxed by increasing the time window, either by decreasing the open time or by increasing the closing time.

**Definition 3 (Time-Window Relaxed Task).** Let $T = (\tau, W)$ be a planning task $\tau$ with simple time windows $W$. Then a relaxed task with respect to time window $W' = (A_W, o', c)$ is defined as $T' = (\tau, W')$ where $W$ is replaced by $W' = (A_W, o', c')$ with $0 \leq o' < o \leq c \leq c' \leq t_{max}$.

A time-window relaxed task indeed represents a relaxed task according to Definition 1:

**Proposition 2.** Let $T'$ be a time-window relaxed task of $T$. Then, $\Pi(T) \subseteq \Pi(T')$.

**Proof sketch:** $\Pi(T) \subseteq \Pi(T')$, because every action sequence $\pi = a_0 \ldots a_n$ applicable in $I$ of $T$ is also applicable in $I'$ of $T'$. For all actions $a_i \in \pi$, $\text{exec}(\pi, a_i)$ is the same in both tasks and with $a_i = \text{prefix}(\pi, a_i)$, $s = I[|\pi_i|]$ and $s' = I'[|\pi_i|]$, $a_i$ is applicable in $s'$ because $a_i$ is applicable in $s$ and if $a_i \in A_W$ then $0 \leq o \leq \text{exec}(\pi, a_i) \leq c'$.

An alternative approach to relax a task with respect to time constraints is the reduction of the execution time of an action by decreasing $\delta(\tau)$. However, in addition to managing the influence on multiple time windows, handling the explosion of possible relaxed tasks is not trivial, which is why we leave this for future work.

The subsumption relation of the intervals $[o', c']$ for time window $W$ yields the partial order for $T_W = (T_W, \subseteq)$, where $T_W$ is the set of all time-window relaxed tasks of $T$ with respect to $W$. The task with $W'' = (A_W, 0, t_{max})$ is the supremum of $T_W$. The upper/lower cover of $T' \in T_W$ are the relaxed tasks where either $o$ is decreased/increased or $c$ is increased/decreased by one compared to $T'$.

For our running example we have 25 different relaxed tasks for the upload window $T_{WU} = \{T_{i,j} \mid i \in \{0, 1, 2, 3, 4\} \land j \in \{6, 7, 8, 9, 10\}\}$, where in $T_{i,j}$ the open time is at $i$ and the closing time at $j$.

**Conflict Explanation**

We aim to generate explanations for the MUGS of $T$. Given a relaxation order, we can now define for each MUGS whether a task is minimal relaxed with respect to the MUGS.
Definition 4 (Minimally Relaxed Task). Let \( \hat{T} = (T, \sqsubseteq) \) be a relaxation order for task \( T \). Then \( T' \in T \) is minimally relaxed for conflict \( G \notin \text{MUGS}(T') \) if for all \( T'' \in T : T'' \sqsubseteq T' \rightarrow G \in \text{MUGS}(T'') \).

So a minimally relaxed task for conflict \( G \) is a minimally relaxed task where \( G \) is no conflict anymore. All MUGS in \( \{ \text{MUGS}(T'' \mid T'' \in T) \} \), for which \( T' \) is minimally relaxed with respect to the relaxation order \( \hat{T} \) are denoted by \( \text{mr-MUGS}(\hat{T}, T') \). The explanation for a conflict in \( T \) can then be defined as:

Definition 5 (Conflict Explanation). Let \( T \) be a task with conflict \( G \in \text{MUGS}(T) \). Given a relaxation order \( \hat{T} \) for \( T \), then the set of all minimally relaxed tasks for \( G \), \( E(\hat{T}, G) = \{ T' \mid G \in \text{mr-MUGS}(\hat{T}, T') \} \), is the set of conflict explanations for \( G \).

To illustrate the explanation for conflict \( G = \{ S_0, S_2 \} \) in our running example we use the diagram in Figure 2. The minimal relaxed tasks and the explanations are given as \( E = \{ T_{1.6}, T_{4.7} \} \): “Sample \( S_0 \) and \( S_2 \) can not both be uploaded, because the upload window, needs either to start 3 units earlier or end 1 unit later”.

Figure 2: Part of hasse diagram for time relaxed tasks of running example. \([S_1, T_1] \rightarrow [S_2, T_2]\) means \( T_{i_1,j_1} \leq T_{i_2,j_2}, T_{3.7} \notin E(\hat{T}, G) \) because \( T_{4.7} \sqsubseteq T_{3.7} \).

Internal Constraint Reuse (ICR)

In the following we introduce two algorithms which given a relaxation order \( \hat{T} \) compute the mr-MUGS for each task. Thereby, the mr-MUGS are not directly computed, but via the maximal solvable goal subsets (MSGS) of each task.

From MSGS to mr-MUGS A MSGS is a soft-goal subset \( G \subseteq G^{\text{soft}} \) where \( G \) can be achieved but every \( G' \supseteq G \) cannot. They serve as the foundation to compute mr-MUGS(\( \hat{T}, T' \)) for each task \( T' \in T \) in two post-processing steps. In a first step, we compute the MSGS for every \( T' \) by performing a bottom up tree search over all subsets of \( G^{\text{soft}} \) and use the MSGS as a fast solvability check as introduced by Eifler 20. Then, the MUGS for which \( T' \) is minimally relaxed are computed as mr-MUGS(\( \hat{T}, T' \)) = \( (\bigcap_{T'' \in \text{CL}(T')} \text{MUGS}(T'')) \setminus \text{MUGS}(T') \).

MSGS Computation Eifler et al. (2020b) compute the MSGS for a task by exhaustively exploring the state space while tracking all reached MSGS. To reduce the search space size they introduce a pruning function, which prunes all states from which no superset of the current MSGS is reachable.

Extending this algorithm, given a relaxation order \( \hat{T} = (T, \sqsubseteq) \) for \( T \), we compute the MSGS for all \( T' \in T \) by iterating over \( T' \) according to the partial ordering, starting with \( T \), and computing the MSGS for each task individually.

Since all plans are preserved when relaxing a task, for all \( T_i, T_j \in T \) with \( T_i \sqsubseteq T_j \), all soft-goals \( G \subseteq G^{\text{soft}} \) that are reachable in \( T_i \) are also reachable in \( T_j \). Thus, the MSGS of \( T_i \) can be propagated to \( T_j \).

Pseudo Code of ICR The pseudo code of the Internal Constraint Reuse (ICR) algorithm is given in Algorithm 1. The underlying search algorithm for the state space exploration of one task is depth first search (DFS) guided by a heuristic (see Eifler et al. 2020b). This is abstracted by the function NEXT(\( O, h \)) which mimics the expansion order of DFS. \( M \) (line 3) is a map from task to a set of soft-goal subsets storing the MSGS for each visited task. The aforementioned propagation of MSGS is achieved by initializing \( M[\hat{T}] \) with all MSGS reached in the lower cover of \( \hat{T} \) (line 6). Iterating over the relaxed tasks according to the partial ordering is represented by the functions HASNEXT(\( \hat{T} \)) and NEXT(\( \hat{T} \)). The order of incomparable elements is resolved randomly. In order to take the already reached MSGS for a given task into account when updating \( M \) (line 11), the function EXTEND(\( M, G \)) returns \( M \) if there is a \( G' \in M : G \subseteq G' \) and \( \{G' \in M \mid G' \not\subseteq G\} \cup \{G\} \) otherwise. The generation of successor states of state \( s \) according to the semantics of task \( T \) (\( \text{SUCC}(T, s) \)) is based on standard progression (see Sections and ). States are pruned (line 15) if no superset of soft-goals or the hard goal cannot be reached based on the heuristic estimation. This means \( \text{prune}(T', M, h, s) \) returns true if \( G^{\text{hard}} \not\subseteq R \) \( \forall G' \in M : R \cap G' \subseteq \) \( G \), where \( R \) is the set of facts reachable from state \( s \) in task \( T' \) according to heuristic \( h \) and false otherwise. For possible implementations we refer to (Eifler et al. 2020b). If a state satisfies all hard and soft goals the search space exploration for the current relaxed task can be terminated early (line 13). All more relaxed tasks than the current task are also solvable and their MSGS are updated accordingly (line 14). Tasks whose MSGS have already been determined are skipped by HASNEXT/NEXT.

Algorithm 1: Internal Constraint Reuse (ICR)

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1: Given: relaxation order \( \hat{T} \), heuristic \( h \)
2: function computeMSGS(\( \hat{T}, h \))
3: \( M \leftarrow \{\} \) \( \triangleright \) map of states
4: while hasNext(\( \hat{T} \)) do
5: \( T \leftarrow \text{next}(\hat{T}) \) \( \triangleright \) current relaxed task
6: \( \hat{M}[\hat{T}] \leftarrow \bigcup_{T' \in \text{CL}(\hat{T})} \hat{M}[\hat{T}'] \) \( \triangleright \) propagate MSGS
7: \( O \leftarrow \{\text{init}(T)\} \) \( \triangleright \) initial state of relaxed task
8: while \( |O| \neq 0 \) do
9: \( s \leftarrow \text{next}(O, h) \) \( \triangleright \) next state according to expansion order
10: if \( G^{\text{soft}} \not\subseteq s \) then \( \triangleright \) update MSGS
11: \( M[\hat{T}] \leftarrow \text{extend}(M[\hat{T}], s \cap G^{\text{soft}}) \)
12: if \( G^{\text{hard}} \cup G^{\text{soft}} \not\subseteq s \) then \( \triangleright \) check and propagate solvability
13: \( \forall T' \in \hat{T} \land \hat{T} \subseteq T' : M[T'] \leftarrow G^{\text{hard}} \cup G^{\text{soft}} \) \( \triangleright \) break
14: \( O \leftarrow O \cup \{s' \in \text{SUCC}(T, s) \mid \neg \text{prune}(T', M[\hat{T}], h, s')\} \)
15: return \( M \)
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Search Space Reuse (SSR)

The algorithm introduced in the previous section has an overhead, because equivalent states are generated multiple times in the separate search spaces. Instead of only reusing the MSGS it can be beneficial to also reuse the search space.

As all plans are preserved in the relaxation of a task, for all \( T' \in \mathcal{T} \) and maximal relaxed task \( T_e = \supremum(\mathcal{T}) \) holds \( \left( \bigcup_{T' \in CL(\mathcal{T}')} S_{T'} \right) \subseteq S_{T'} \), where \( S_{T'} \) are the states reachable from the initial state \( I_s \) of \( T_e \) by plans of \( T' \). Thus, we can base the computation of the MSGS for all relaxed tasks on the search space of \( T_e \). We start with exploring the reachable state space with respect to \( T \). All states that are generated in the meantime, but which are not reachable in \( \hat{T} \), are stored in a search frontier. To decide whether a state \( s \) is reachable in a task \( T' \) or not, we check whether the action sequence \( \pi(s) \) leading to \( s \) is applicable in \( T' \) (APPL\( (T',\pi(s)) \)). In the following iterations the search frontier of less relaxed tasks are further extended for more relaxed tasks. This limits the states generated for each task to the newly reachable states.

Pseudo Code of SSR  The pseudo-code of our Search Space Reuse (SSR) algorithm is depicted by Algorithm 2. If not mentioned explicitly, the algorithm parts work as described for Algorithm 1. The map \( \mathcal{F} \) (line 5) stores for each task \( \hat{T} \) the states which were generated during the search for \( \hat{T} \) but were not reachable (line 17). In the first iteration the openlist is initialized with the initial state of the maximal relaxed task \( \hat{T} \) (line 6). In each further iteration it is initialized with the states in \( \mathcal{F} \) of all tasks in the lower cover of \( \hat{T} \) that are reachable in \( \hat{T} \) (line 23-25). States are pruned by following the same approach as in Algorithm 1 (line 16/23). However, instead of basing the pruning on the current relaxed task \( \hat{T} \) it is based on the maximal relaxed task \( T_e \), because otherwise states which could be reachable in more relaxed tasks, would be pruned.

Theoretical Comparison

The propagation of the MSGS can improve the pruning function, which is beneficial to both ICR and SSR. Although reusing the search space in SSR reduces duplicate work, it prunes states only with respect to their reachability in the maximal relaxed task, not the current relaxed task. In the following we compare the overall number of generated states by each algorithm as a measure to decide whether they are exponentially separated. As the baseline algorithm we consider ICR without the propagation of MSGS.

Definition 6  (Exponential Separation). Let \( \{ T^n | n \in \mathbb{N} \} \) be a family of planning tasks of size (number of facts and actions) polynomially related to \( n \) and \( S(X) \) the number of states generated by search method \( X \). Then, search method \( X \) is exponentially separated from search method \( Y \) if \( \left| S(Y) - S(X) \right| \) is exponential in \( n \).

To give a family of planning tasks to prove the exponential separations of the algorithms we use the following domain:

Domain  Consider a planning task, where a robot has to visit different locations. The robot’s movement is restricted by the resource \( \rho \), which can have the values \( \{0, 1, 2\} \), with initial value 1. Moving between connected locations consumes the amount of resources depicted in the map in Figure 3. There is one location annotated with \( K \) which holds a set of \( n \) keys. The robot can pick up one key at a time (without using any resources) if it is in the same location as the key. To take the dashed connection the robot has to hold all keys. Since the robot can pick up any combination of keys, there can be exponentially many search states.

Figure 3: left: Map of example for exponential separation of ICR and SSR from baseline. Initial location \( L_0 \), locations to visit \( L_1 \) and \( L_2 \). right: Map of example for exponential separation of ICR from SSR. Initial location \( L_0 \), goal visit \( L_3 \).  

In the following examples the pruning function uses the \( h^2 \) heuristic (Haslum and Geffner 2000) to decide reachability.

Theorem 1. ICR and SSR are exponentially separated from the baseline.

Example  Consider the map depicted on the left in Figure 3.

In the first iteration with \( init_\rho = 1 \) ICR and the baseline generate 2 states (R at \( L_0 \) and \( L_1 \)). SSR, with \( init_\rho = 2 \), generates the same two states and 2 additional states (R at \( L_2 \) and \( L_3 \)), which are not reachable and stored in the fron-
tier. For both ICR and SSR MSGS = \{\{L_1\}\} is propagated. In the next iteration of ICR (init_\rho = 2), moving to L_3 is pruned because no new locations are reachable from there. The same holds for SSR. This leads to 2 + 3 and 4 + 1 states for ICR and SSR respectively. For the baseline, reachability of L_1 is not propagated and moving to L_3 is not pruned. Thus, we get 2 + 3 + 2 * 2^n states, for picking up any combination of keys.

**Theorem 2.** ICR is exponentially separated from SSR.

**Example** Consider the map depicted on the right in Figure 3. In the first iteration with init_\rho = 1, ICR generates only one state. Moving to L_1 is pruned because h^2 recognizes that L_2 is not reachable with \rho = 1. In SSR, init_\rho = 2 prevents pruning L_1 and picking up any combination of keys. Thus, 1 + 2^n reachable and 2^n (at L_2 with any combination of keys) unreachable states are generated. In the last iteration in ICR with init_\rho = 2 visiting L_2 via the upper connection and extending the MSGS to \{\{L_2\}\} leads to an early termination. The same holds for SSR. This results in 1 + 3 states for ICR and 1 + 2 * 2^n for SSR.

**Experiments**

We implemented both algorithms in the Fast Downward planning system (Helmert 2006), extending the code base of Eifler et al. (2020b). The experiments were run on Intel E5-2660 machines running at 2.20 GHz, with a time (memory) limit of 2h (4GB) per benchmark instance.

**Benchmark**

Our benchmark consists of 4 resource-constraint domains (Blocksworld, NoMystery, Rovers R, TPP) and 3 domains (Parent’s Afternoon, Rovers T, Satellite) with time-constraints. The former part builds on a subset of the resource constraint benchmark by Eifler et al. (2020b). In each instance there are 2 individual resources R. For each resource \rho \in R we generated one benchmark instance, scaling init_\rho between 0 and two times the initial value in the original task.

Rover T and Satellite are extension of the corresponding IPC domains with data upload windows for Rovers and time windows to take the images for Satellite. Parents’ Afternoon is a new domain, that models a parent’s afternoon routine, including shopping and various family member activities. The execution of these activities is partially constraint by time windows. For each time window W \in W we generated one benchmark instance. For Parent’s Afternoon and Satellite, each time window is relaxed between its original size and the maximal value of the time variable domain in the original task. For Rovers the relaxation of a upload window is additionally bounded by the other upload windows.

Each benchmark instance has up to 5 plan properties that, for example, restrict the order in which two goal facts are to be achieved. All plan properties and the original goal facts of the instance are soft goals. There are no hard goals.

**Evaluation**

The coverage results for the baseline (ICR without MSGS propagation), ICR and SSR are given in Table 1. An instance is considered to be solved, when the MUGS for all relaxed tasks are computed. Comparing the ICR to the baseline shows propagating the MSGS increases the coverage in 5 domains, while not decreasing it in any. SSR solves more instances in 4 domains, while it is worse than the baseline in 2. ICR clearly has the advantage over SSR in the resource constraint domains, while it is the other way around for the time constraint domains.

The increase in reachable states achieved by relaxing a time window is typically much smaller than the increase by relaxing a resource constraint. Increasing a time window only adds few more times at which a single action a \in A_W could start. However, as a is also constrained by all other time dependent actions, there may not be many added reachable states. By contrast, relaxing a resource allows you to add new actions and increases the number of action orderings, which would otherwise be constrained by too few resources. This is in favor for SSR, because it only considers the newly reachable states. Comparing the number of expansions needed by each algorithm per relaxed task, as depicted in Figure 4, confirms this assumption. In the time constraint...
domains SSR expands more states than ICR in the first task, but has much fewer expansions than ICR from then on. For the resource-constraint task, the stronger pruning function in ICR is advantageous for a wider span of relaxed tasks, such that SSR only needs fewer expansions in more relaxed tasks.

Problems may not be solved either due to the exhaustion of the time limit or the memory limit. For Blocksworld and all time constraint domains, all algorithms ran out of time. For the other resource constraint domains SSR failed due to the memory limit. In TPP ICR failed due to the time limit and in rovers due to the memory. Nomystery is the only domain with a mixed reason for failure of ICR, with about 25% timeouts and 75% memory limit exhaustion. Overall, timeout is most common. This could be addressed by parallelizing the computation of MSGS which have no strict order.

**Conclusion**

Our approach addresses the question why soft-goal conflicts exist by identifying the minimal relaxation under which a conflict disappears. Combined with the work of Eifler et al. (2020a), this provides an explanation framework that can explain trade-offs between soft goals by identifying not only conflicting soft goals, but also options for resolving them. This not only helps to better understand why a conflict exists, but also whether it can be resolved. In addition it enables the user to evaluate the trade-offs and benefits of a relaxation.

Future work includes the evaluation in an application setting and automatically identifying relevant relaxations for a user and conflict.

**References**


