#### 000 HI-MAMBA: HIERARCHICAL MAMBA FOR EFFICIENT 001 IMAGE SUPER-RESOLUTION 002 003

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### ABSTRACT

State Space Models (SSM), such as Mamba, have shown strong representation ability in modeling long-range dependency with linear complexity, achieving successful applications from high-level to low-level vision tasks. However, SSM's sequential nature necessitates multiple scans in different directions to compensate for the loss of spatial dependency when unfolding the image into a 1D sequence. This multi-direction scanning strategy significantly increases the computation overhead and is unbearable for high-resolution image processing. To address this problem, we propose a novel Hierarchical Mamba network, namely, Hi-Mamba, for image super-resolution (SR). Hi-Mamba consists of two key designs: (1) The Hierarchical Mamba Block (HMB) assembled by a Local SSM (L-SSM) and a Region SSM (R-SSM) both with the single-direction scanning, aggregates multiscale representations to enhance the context modeling ability. (2) The Direction Alternation Hierarchical Mamba Group (DA-HMG) allocates the isomeric singledirection scanning into cascading HMBs to enrich the spatial relationship modeling. Extensive experiments demonstrate the superiority of Hi-Mamba across five benchmark datasets for efficient SR. For example, Hi-Mamba achieves a significant PSNR improvement of 0.29 dB on Manga109 for  $\times 3$  SR, compared to the strong lightweight MambaIR.

1 INTRODUCTION

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Single Image Super-Resolution Yang et al. (2019); He et al. (2019); Zhang et al. (2018); Chen 032 et al. (2022); Zhang et al. (2021) (SISR) aims to restore an authentic high-resolution (HR) image 033 from a single degraded low-resolution (LR) one, which benefits plentiful downstream applications 034 such as magnetic resonance imaging (MRI), mobile device photography, and video surveillance. Various studies have proposed Convolutional Neural Networks (CNNs) Ahn et al. (2018); Li et al. (2021b); Zhang et al. (2019b) to learn a mapping from LR inputs to HR outputs. Despite their efficacy 037 and remarkable advances in the past, CNN-based SR models are reaching their upper-performance 038 limits even with continuously increasing model sizes, due to CNNs' limited capability on long-range dependency modeling.

040 Transformer-based SR methods Liang et al. (2021); Chen et al. (2023b;a); Ray et al. (2024); Zhang 041 et al. (2024) introduce self-attention mechanisms with extraordinary long-range modeling capabilities 042 to remarkably improve SR performance, while at the cost of quadratic computational complexity. 043 Numerous subsequent works have been proposed to make the vanilla Transformers more efficient 044 and powerful via shifted window attention Liang et al. (2021); Zhang et al. (2022b), transposed attentions Zamir et al. (2022); Li et al. (2023b) and anchored stripe self-attention Li et al. (2023c), etc. However, these studies are difficult to relieve the quadratic complexity of attention mechanisms 046 at inference in practice. 047

048 Recently, Mamba Gu & Dao (2024) architecture constructed on Structured State Space Models (S4) has emerged as a promising technique due to its high potential in long-sequence modeling with linear complexity. As S4 was originally proposed in the field of natural language processing (NLP) Gu et al. 051 (2021a); Gu & Dao (2024), several succeeding works have introduced S4 into vision recognition tasks Liu et al. (2024); Zhu et al. (2024) and image processing tasks Shi et al. (2024), demonstrating 052 impressive results. For example, Vision Mamba Zhu et al. (2024) was proposed for image recognition tasks, manifesting that Vision Mamba can overcome the computation & memory constraints on

using the number of $n$ scan	ning.							
Method	GPU(ms)	Params	FLOPs	Set5	Set14	B100	Urban100	Mang
MambaIR-1 Guo et al. (2024)	519	987K	291G	38.13	33.86	32.31	32.82	39.
MambaIR-2 Guo et al. (2024)	653	1.11M	383G	38.15	33.94	32.31	32.86	39.
MambaIR-4 Guo et al. (2024)	982	1.36M	568G	38.16	34.00	32.34	32.92	39.
Hi-Mamba-S (Ours)	379	1.34M	274G	38.24	34.08	32.38	33.13	39.

n 062 state-space module (VSSM) from Vmamba Liu et al. (2024) for image super-resolution and achieves 063 performance comparable to Transformer-based SR baselines.

064 Previous vision Mamba architectures typically employ a multi-direction scanning strategy to compen-065 sate for the loss of spatial dependencies when unfolding the image into a 1D sequence. Unfortunately, 066 the repetitive multiple-sequence scanning overshadows the essential linear computational complexity 067 of SSMs primarily designed with single-sequence scanning to model 1D sequential relationships. 068 It significantly increases the computation overhead and is unacceptable for high-resolution image 069 processing tasks. As shown in Tab. 1, the four-sequence scanning approach effectively improves the performance by 0.10 dB and 0.12 dB on Urban100 and Manga109, respectively. However, this enhancement comes at a significant computational cost, increasing FLOPs by 95.2% and parameters 071 by 37.8% compared to the single-sequence scanning approach in MambaIR. 072

073 To address this problem, we propose a novel Hierarchical Mamba architecture, termed Hi-Mamba, 074 for image super-resolution (SR). We first propose the hierarchical Mamba block (HMB) which is 075 constructed by a local SSM and a region SSM with single-direction scanning to conduct multi-076 scale data-dependent visual context modeling. Furthermore, we propose the direction alternation 077 hierarchical Mamba group (DA-HMG) that allocates the isomeric single-direction scanning into cascaded HMBs to enrich the spatial relationship modeling. Our DA-HMG improves the reconstruction performance with no extra FLOPs or parameter increases. In addition, we propose that the 079 gate feed-forward network (G-FFN) introduce additional non-linear information through a simple gate mechanism in the feed-forward network. We verify the effectiveness of Hi-Mamba on several 081 classical SR benchmarks with three released versions, which makes fair comparisons with various 082 SR models with different capacities. 083

- We summarize our main contributions as follows: 084
  - We propose Hi-Mamba for efficient SR, incorporating hierarchical Mamba block (HMB), specifically the Local-SSM and the Region-SSM for multi-scale data-dependent visual context modeling.
  - The direction alternation hierarchical Mamba group (DA-HMG) is simple yet effective in enriching the spatial relationship modeling, which allocates the isometric single-direction scanning into cascaded HMBs to improve performance without incurring extra computation and memory costs.
  - Extensive experiments demonstrate the superiority of the proposed Hi-Mamba. For example, our Hi-Mamba achieves significant PSNR gains of 0.37dB on Urban100 for  $\times 3$  SR compared to SRFormer Zhou et al. (2023).

#### **RELATED WORK** 2

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2.1 EFFICIENT CNNs AND TRANSFORMERS FOR SUPER-RESOLUTION

100 Since SRCNNDong et al. (2015) first introduced convolutional neural networks (CNNs) for SR, 101 various works Dong et al. (2016); Lim et al. (2017); Ledig et al. (2017); Zhang et al. (2018) have 102 explored CNN-based SR architectures to improve SR performance. To improve model efficiency, 103 CARN Ahn et al. (2018) proposes a cascading mechanism at both the local and global levels. 104 IMDN Hui et al. (2019) adopts feature splitting and concatenation operations to progressively 105 aggregate features, further reducing parameters. SAFMN Sun et al. (2023) utilizes a feature pyramid to generate spatially-adaptive feature attention maps. However, these CNN-based SR methods are 106 limited by the size of the convolutional kernels and cannot effectively model long-term dependencies 107 between pixels.

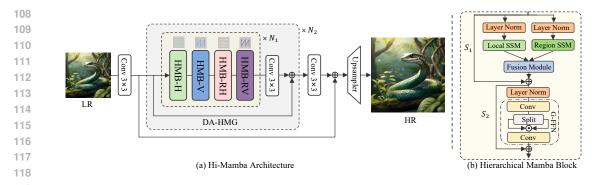


Figure 1: Illustration of the proposed Hi-Mamba. (a) The overview of Hi-Mamba architecture with  $N_2$  Hierarchical Mamba Groups (DA-HMG), where each DA-HMG contains the number of  $N_1$  Hierarchical Mamba blocks (HMB), which consist of four isomeric single-direction scanning SSM denoted by HMB-H/V/RH/RV. (b) Hierarchical Mamba Block (HMB) consists of a Local-SSM, a Region-SSM, and a Gate Feed-Forward Network (G-FFN).

124 To capture long-range pixel dependencies, Transformer-based methods Liang et al. (2021); Chen 125 et al. (2023b;a); Ray et al. (2024); Zhang et al. (2024) have introduced self-attention mechanisms 126 into SR tasks, achieving significant performance improvements. To facilitate practical deployment, 127 various efficient attention mechanisms Li et al. (2023c); Zhou et al. (2023) have been proposed to reduce computational and memory costs. ESRT Zhisheng et al. (2021) computes attention maps 128 in a group manner to reduce memory usage. N-Gram Choi et al. (2023) proposed an asymmetric 129 U-Net architecture that downsamples features to reduce computational cost. DLGSANet Li et al. 130 (2023b) utilizes channel-wise self-attention, which has lower computational costs compared to spatial 131 self-attention. SRFormer Zhou et al. (2023) minimizes the size of the attention map by compressing 132 the channel dimensions of the key and value in self-attention. However, these methods do not directly 133 address the quadratically growing complexity of attention mechanisms with the increase in token 134 sequence length. Moreover, they typically compute self-attention based on windows, which confines 135 the receptive field for high-quality image reconstruction.

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#### 2.2 MAMBA AND APPLICATIONS FOR SUPER-RESOLUTION

139 State space models (SSM) Gu et al. (2021a;b); Smith et al. (2022), originating from classical control theory Kalman (1960), are rising as novel backbones in Deep Learning. Successful applications 140 of SSM include Mamba Gu & Dao (2024), Vim Zhu et al. (2024), and VMamba Liu et al. (2024), 141 which are all tailored toward high-level image understanding tasks. Overall, the implementations 142 of SSM in low-level vision tasks remain few. MambaIR Guo et al. (2024) first introduced the 143 Mamba architecture to image super-resolution tasks, achieving impressive image restoration results. 144 MMA Cheng et al. (2024) introduced Vision Mamba (ViM) Zhu et al. (2024) and combined it 145 with convolutional structures to activate a wider pixel area, thereby enhancing SR performance. 146 DVMSR Lei et al. (2024) was the first to attempt distilling the Mamba architecture to achieve 147 an ultra-lightweight SR Mamba model. FMSR Xiao et al. (2024) introduced Mamba for remote 148 sensing image super-resolution, which uses frequency information to assist the Mamba architecture, 149 achieving performance surpassing Transformer methods. However, these methods all use multi-150 sequence scanning strategies to model the image spatial relationships, which significantly increases 151 computational costs compared to the single-sequence scanning of vanilla Mamba. Different from these methods, our Hi-Mamba uses only single-sequence scanning and proposes HMB to compensate 152 for SSM's inadequacy in modeling 2D-pixel relationships. Additionally, the DA-HMG is proposed to 153 enrich spatial relationship modeling by alternatively changing the single-sequence scanning direction 154 in HMB without additional computational costs. 155

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#### 3 HIERARCHICAL MAMBA NETWORKS

- 159 3.1 PRELIMINARIES
- 161 SSM can be viewed as a Linear Time-Invariant (LTI) system, which maps the input one-dimensional function or sequence  $x(t) \in \mathbb{R}$  to the output response  $y(t) \in \mathbb{R}$  through a hidden state  $h(t) \in \mathbb{R}^N$ .

162 They are typically represented as linear ordinary differential equations:

$$h'(t) = Ah(t) + Bx(t), \quad y(t) = Ch(t) + Dx(t),$$
(1)

where  $A \in \mathbb{R}^{N \times N}$ ,  $B \in \mathbb{R}^{N \times 1}$ ,  $C \in \mathbb{R}^{1 \times N}$ , and  $D \in \mathbb{R}$  are weight parameters, and N represents the state size.

The discretization process is commonly used to process Eq. 1, which can be applied in deep learning scenarios. In particular, the timescale parameter  $\Delta$  is used to convert the continuous parameters Aand B into discrete ones  $\overline{A}$  and  $\overline{B}$ . The widely used discretization method adheres to the Zero-Order Hold (ZOH) rule, which is formulated as:

$$\overline{A} = \exp(\Delta A), \quad \overline{B} = (\Delta A)^{-1}(\exp(A) - I) \cdot \Delta B.$$
 (2)

<sup>173</sup> Therefore, after discretization, Eq. 1 can be rewritten as:

$$h_k = \overline{A}h_{k-1} + \overline{B}x_k, \quad y_k = Ch_k + Dx_k. \tag{3}$$

To further accelerate computation, Gu et al. Gu et al. (2021a) expanded the SSM computation into a convolution with a structured convolutional kernel  $\overline{K} \in \mathbb{R}^L$ :

$$\overline{K} \triangleq \left( C\overline{B}, C\overline{AB}, \cdots, C\overline{A}^{L-1}\overline{B} \right), \quad y = x * \overline{K}, \tag{4}$$

where L is the length of the input sequence and \* denotes the convolution operation. A recent state space model, Mamba Gu & Dao (2024), introduces Selective State Space Models (S6) by relaxing the time-invariance constraints on B, C, and  $\Delta$  depending on the input x, which selectively propagates information for 1D language sequence modeling.

To expand Mamba from 1D language sequences to 2D visual inputs, various works Liu et al. (2024);
Liang et al. (2024); Deng & Gu (2024); Guo et al. (2024) employ 2D selective scan (SS2D) mechanism to capture spatial correlations with 2D feature sequences. For example, VMamba Liu et al. (2024) employs SS2D by scanning four directed input sequences and generating the 2D feature map by independently combining four feature sequences via an S6 block. Similarly, MambaIR Guo et al. (2024) introduces the Vision State-Space Module (VSSM) into image restoration for information interaction at the whole-image level. However, these methods employ repetitive multi-direction scanning to adapt to 2D image inputs, significantly increasing computational costs.

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#### **193 3.2** ARCHITECTURE OVERVIEW

As shown in Fig. 1 (a), the proposed Hierarchical Mamba (Hi-Mamba) architecture comprises three parts: shallow feature extraction, deep feature extraction, and image reconstruction. Given a lowresolution (LR) input image  $I_{LR} \in \mathbb{R}^{C_{in} \times H \times W}$ , where  $C_{in}$ , H, and W are the input channels, height, and width, respectively. We first use a simple convolution for shallow feature extraction  $H_{SF}$  to generate local features  $F_l \in \mathbb{R}^{C \times H \times W}$ :

$$F_l = H_{SF}(I_{LR}),\tag{5}$$

where C is the embedding channel dimension. Subsequently, the local features  $F_l$  are processed in the deep feature extraction module  $H_{DF}$  to obtain deep features  $F_d \in \mathbb{R}^{C \times H \times W}$ :

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$$F_d = H_{DF}(F_l),\tag{6}$$

where the deep feature extraction module  $H_{DF}$  consists of multiple direction alternation hierarchical Mamba groups (DA-HMG) with a total number of  $N_2$ . To ensure training stability, a residual strategy is adopted within each group. Each DA-HMG contains the number of  $N_1$  Hierarchical Mamba blocks (HMB), which consist of four isomeric single-direction scanning SSM denoted by HMB-H/V/RH/RV. At the end of each DA-HMG, convolutional layers are introduced to refine the features.

Finally, we use  $F_l$  and  $F_d$  as the inputs and reconstruct the high-resolution (HR) output image  $H_R$ through the reconstruction module, which can be formulated as:

$$I_r = H_R(F_l + F_d),\tag{7}$$

where  $H_R$  involves a single 3×3 convolution followed by a pixel shuffle operation. We optimize the parameters  $\theta$  of Hi-Mamba by the pixel-wise L1 loss between the reconstruction output  $I_r$  and the ground truth (GT)  $I_{at}$ . In the following, we will introduce the key blocks and modules in Hi-Mamba.

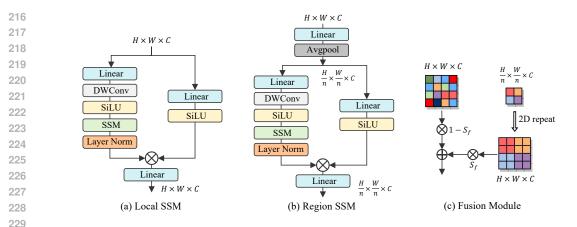


Figure 2: Illustration of the key components in HMB.

#### 3.3 HIERARCHICAL MAMBA BLOCK

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The original visual Mamba blocks Liu et al. (2024); Zhu et al. (2024) typically employ multi-direction scanning, which significantly increases the computation overhead. To address this problem, we design a novel hierarchical mamba block (HMB) with only single-direction scanning and alternatively change the scanning direction to enrich the spatial relationship modeling to construct DA-HMG.

As illustrated in Fig. 1 (b), HMB primarily consists of two branches: Local SSM (L-SSM) and Region SSM (R-SSM). Given the local input feature  $I_l^i \in \mathbb{R}^{C \times H \times W}$  and the region input feature  $I_r^i \in \mathbb{R}^{C \times \frac{H}{n} \times \frac{W}{n}}$  at the *i*-th layer, we first employ Layer Normalization (LN) and go through two branches to capture long-range dependencies. Additionally, we incorporate learnable scaling factors  $S_1 \in \mathbb{R}^C$  to regulate the information within skip connections:

$$F_l^i = \text{L-SSM}(\text{LN}(I_l^i)), F_r^i = \text{R-SSM}(\text{LN}(I_r^i)),$$
  

$$F^i = (F_l^i \otimes F_r^i) + (S_1 \cdot I_l^i).$$
(8)

where  $F_l^i$ , and  $F_r^i$  are the outputs of these two branches, respectively.  $\otimes$  denotes the fusion module. The L-/R-SSM and fusion modules will be described in Sec. 3.3.1 and Sec. 3.3.2, respectively.

Subsequently, the intermediate features  $F^i$  will subsequently undergo the proposed gate feed-forward network (G-FFN) followed by another learnable scale factor  $S_2$  in the residual connection to obtain the input features at the i + 1-th layer and  $F_r^i$  is directly used as the regional input for the next layer:

$$F_l^{i+1} = \operatorname{G-FFN}\left(\operatorname{LN}(F^i)\right) + S_2 \cdot F^i, \quad F_r^{i+1} = F_r^i.$$
(9)

In G-FFN, we enhance the modeling capacity for spatial information by introducing a gate mechanism
 into the FFN. This also reduces redundant information in the channels. G-FFN first extracts features
 through convolution and splits the feature map along the channel dimension into two parts for
 element-wise multiplication. Specifically, G-FFN is computed as:

$$\hat{F} = w^{1} * \text{LN}(F^{i}), [\hat{F}_{1}, \hat{F}_{2}] = \text{Split}(\hat{F}),$$
  
G-FFN( $F^{i}$ ) =  $w^{2} * (\hat{F}_{1} \odot \hat{F}_{2}),$  (10)

where  $w^1$  and  $w^2$  are the convolution weights.  $\odot$  is an element-wise multiplication operation. Note that, we only use a single-direction scanning in one HMB, *i.e.*, one selection from the horizontal, vertical, reverse horizontal, and reverse vertical directions.

# 264 3.3.1 LOCAL / REGION SSM 265

Following the VSSM of MambaIR Guo et al. (2024), L-SSM and R-SSM use a similar computational sequence. Instead of VSSM with multiple-sequence scanning, L-SSM and R-SSM employ singlesequence scanning to reduce the computation costs. The architecture of L-SSM and R-SSM are illustrated in Fig. 2 (a) and (b), respectively. L-SSM and R-SSM take the local feature  $I_l \in \mathbb{R}^{C \times H \times W}$ and the region feature  $I_r \in \mathbb{R}^{C \times \frac{H}{n} \times \frac{W}{n}}$  as the inputs, respectively. Here,  $I_r$  is generated by a simple projection operation with a region size of n to the local feature  $I_l$ . For simplicity, we denote the input uniformly as X, due to the same computation process to L-SSM and R-SSM.

In the first branch of L-SSM, feature channels are expanded to  $\lambda C$  via a linear layer, where  $\lambda$  is a predefined channel expansion factor, followed by depthwise convolution, SiLU Shazeer (2020) activation function, SSM and LayerNorm. In the second branch, feature channels are also expanded to  $\lambda C$  with a linear layer and SiLU activation function. Finally, the features from both branches are merged and projected back to C to generate an output  $X_{out}$  with the same shape as the input. The above computation process can be formulated as:

 $X_{b1} = \text{LN}(\text{SSM}(\text{SiLU}(\text{DWConv}(\text{Linear}(X))))),$   $X_{b2} = \text{SiLU}(\text{Linear}(X)),$   $X_{out} = \text{Linear}(X_{b1} \odot X_{b2}),$ (11)

where DWConv( $\cdot$ ), SSM( $\cdot$ ) and  $\odot$  represent depthwise convolution, SS2D Liu et al. (2024) with single-direction scanning and element-wise multiplication, respectively.

# 285 3.3.2 FUSION MODULE

To reinforce spatial dependencies in the 2D domains, we use the fusion module to leverage region information from adjacent pixels in the R-SSM to guide the single-sequence local feature modeling. As illustrated in Fig. 2 (c), we first repeat the region features along the spatial dimension to match the size of the local features, ensuring that each region token is mapped to the corresponding local token. This operation implicitly incorporates spatial positional information. To dynamic control the fusion results, we introduce learnable fusion scaling factors  $S_f \in \mathbb{R}^C$  to fuse the outputs of L-SSM and R-SSM in Eq. 11, which is formulated as:

$$F_{out} = S_f \cdot X_{out}^l + (1 - S_f) \cdot f_{re}(X_{out}^r).$$

$$\tag{12}$$

where  $X_{out}^l$  and  $X_{out}^r$  denote the outputs of the L-SSM and R-SSM, respectively.  $f_{re}$  represents the repeat operation along the 2D spatial dimension.

# 298 3.4 DIRECTION ALTERNATION HIERARCHICAL MAMBA GROUP

As depicted in Fig. 1, DA-HMG is easy to implement by alternatively allocating the isomeric single direction scanning to different HMBs. By default, we apply Horizontal HMB (HMB-H), Vertical
 HMB (HMB-V), Reverse Horizontal HMB (HMB-RH), and Reverse Vertical HMB (HMB-RV)
 orders to enrich the spatial relationship modeling further. DA-HMG does not incur extra parameters
 and computational costs, compared to the HMB with the same direction, denoted by base-single.

Compared to the stacked multi-sequence scanning in the 2D-SSM module of MambaIR, DA-HMG
 significantly reduces the computational and parameter overhead while achieving superior performance.
 The more detailed difference between base-single, 2D-SSM and DA-HMG on the sequence scanning
 strategy is presented in Fig. 7 of Appendix.

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### 4 EXPERIMENTS

# 312 4.1 EXPERIMENTAL SETTINGS313

314 Datasets. Following Liang et al. (2021); Guo et al. (2024); Li et al. (2023a); Chen et al. (2023b), we train our model on two widely-used datasets, DIV2K Agustsson & Timofte (2017) and Flicker2K Lim 315 et al. (2017), and only use DIV2K dataset to train the lightweight version of our model. We evaluate 316 our method on five standard SR benchmarks: Set5 Bevilacqua et al. (2012), Set14 Zeyde et al. (2012), 317 BSD100 Martin et al. (2001), Urban100 Huang et al. (2015), and Manga109 Matsui et al. (2017) 318 across three scaling factors,  $\times 2$ ,  $\times 3$ , and  $\times 4$ . For the evaluation metric, we calculate PSNR and 319 SSIM Wang et al. (2004) on the Y channel in the YCbCr space and also report the average inference 320 time (20 runs) on one NVIDIA V100, parameters and FLOPs. 321

**Implementation details.** Following the general setting Liang et al. (2021); Zhang et al. (2022a); Chen et al. (2022), each training sample is augmented through flipping and rotations of 90°, 180° and 270°. During training, we randomly crop images into  $64 \times 64$  patches, with a total iteration number of

Scale	Model	Params (M)	FLOPs (G)	PSNR S	et5 SSIM	PSNR S	et14 SSIM	PSNR BS	D100 SSIM	PSNR	an100 SSIM	Ma PSNR
	CARN Ahn et al. (2018)	1.45	223	37.76	0.9590	33.52	0.9166	32.09	0.8978	31.92	0.9256	38.36
	EDSR-baseline Lim et al. (2017)	1.37	316	37.99	0.9604	33.57	0.9175	32.16	0.8994	31.98	0.9272	38.54
	IMDN Hui et al. (2019)	0.69	159	38.00	0.9605	33.63	0.9177	32.19	0.8996	32.17	0.9283	38.88
	LAPAR-A Li et al. (2020)	0.55	171	38.01	0.9605	33.62	0.9183	32.19	0.8999	32.10	0.9283	38.67
	LatticeNet Luo et al. (2020)	0.76	170	38.15	0.9610	33.78	0.9193	32.25	0.9005	32.43	0.9302	-
	ESRT Zhisheng et al. (2021)	0.67	-	38.03	0.9600	33.75	0.9184	32.25	0.9001	32.58	0.9318	39.12
x2	SwinIR-Light Liang et al. (2021)	0.90	235	38.14	0.9611	33.86	0.9206	32.31	0.9012	32.76	0.9340	39.12
	N-Gram Choi et al. (2023)	1.01	140	38.05	0.9610	33.79	0.9199	32.27	0.9008	32.53	0.9324	38.9
	SRFormer-Light Zhou et al. (2023)	0.83	236	38.23	0.9613	33.94	0.9209	32.36	0.9019	32.91	0.9353	39.28
	MambalR Guo et al. (2024)	1.36	568	38.16	0.9610	34.00	0.9212	32.34	0.9017	32.92	0.9356	39.3
	Hi-Mamba-T	0.87	178	38.24	0.9613	34.06	0.9215	32.35	0.9019	33.04	0.9358	39.2
	Hi-Mamba-S	1.34	274	38.24	0.9614	34.08	0.9217	32.38	0.9021	33.13	0.9368	39.35
	CARN Ahn et al. (2018)	1.59	119	34.29	0.9255	30.29	0.8407	29.06	0.8034	28.06	0.8493	33.50
	EDSR-baseline Lim et al. (2017)	1.56	160	34.37	0.9270	30.28	0.8417	29.09	0.8052	28.15	0.8527	33.4
	IMDN Hui et al. (2019)	0.70	72	34.36	0.9270	30.32	0.8417	29.09	0.8046	28.17	0.8519	33.6
	LAPAR-A Li et al. (2020)	0.54	114	34.36	0.9267	30.34	0.8421	29.11	0.8054	28.15	0.8523	33.5
	LatticeNet Luo et al. (2020)	0.77	76	34.53	0.9281	30.39	0.8424	29.15	0.8059	28.33	0.8538	-
	ESRT Zhisheng et al. (2021)	0.77	-	34.42	0.9268	30.43	0.8433	29.15	0.8063	28.46	0.8574	33.9
x3	SwinIR-Light Liang et al. (2021)	0.89	87	34.62	0.9289	30.54	0.8463	29.20	0.8082	28.66	0.8624	33.9
	N-Gram Choi et al. (2023)	1.01	67	34.52	0.9282	30.53	0.8456	29.19	0.8078	28.52	0.8603	33.8
	SRFormer-Light Zhou et al. (2023)	0.86	105	34.67	0.9296	30.57	0.8469	29.26	0.8099	28.81	0.8655	34.1
	MambalR Guo et al. (2024)	1.37	253	34.72	0.9296	30.63	0.8475	29.29	0.8099	29.00	0.8689	34.3
	Hi-Mamba-T	0.88	80	34.76	0.9298	30.61	0.8472	29.27	0.8091	29.05	0.8693	34.4
	Hi-Mamba-S	1.35	123	34.77	0.9303	30.68	0.8493	29.33	0.8111	29.18	0.8716	34.6
	CARN Ahn et al. (2018)	1.59	91	32.13	0.8937	28.6	0.7806	27.58	0.7349	26.07	0.7837	30.4
	EDSR-baseline Lim et al. (2017)	1.52	114	32.09	0.8938	28.58	0.7813	27.57	0.7357	26.04	0.7849	30.3
	IMDN Hui et al. (2019)	0.72	41	32.21	0.8948	28.58	0.7811	27.56	0.7353	26.04	0.7838	30.4
	LAPAR-A Li et al. (2020)	0.66	94	32.15	0.8944	28.61	0.7818	27.61	0.7366	26.14	0.7871	30.4
	LatticeNet Luo et al. (2020)	0.78	44	32.30	0.8962	28.68	0.7830	27.62	0.7367	26.25	0.7873	-
	ESRT Zhisheng et al. (2021)	0.75	64	32.19	0.8947	28.69	0.7833	27.69	0.7379	26.39	0.7962	30.7
x4	SwinIR-Light Liang et al. (2021) N-Gram Choi et al. (2023)	0.90	50 36	32.44 32.33	0.8976 0.8963	28.77 28.78	0.7858 0.7859	27.69 27.66	0.7406 0.7396	26.47	0.7980 0.7963	30.9 30.8
										26.45		
	SRFormer-Light Zhou et al. (2023) MambaIR Guo et al. (2024)	0.87	63 143	32.51 32.51	0.8988	28.82 28.82	0.7872	27.73	0.7422	26.67	0.8032	31.1
	Hi-Mamba-T	0.89			0.8995	28.82						
		1.36	45 69	32.52 32.60	0.8995	28.80	0.7873 0.7895	27.75 27.78	0.7429 0.7436	26.81 26.86	0.8072 0.8086	31.3
	Hi-Mamba-S	1.30	69	32.00	0.8999	28.91	0.7895	27.78	0.7430	20.80	0.8080	31.4

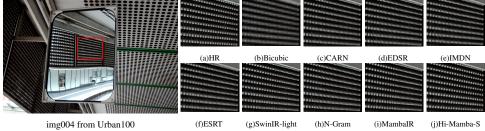


Figure 3: Qualitative comparison on the "img004" image of Urban100 for  $\times 4$  SR.

500K. The patch size is set to 32. We employ the Adam optimizer with training parameters  $\beta_1 = 0.9$ ,  $\beta_2 = 0.999$ , and zero weight decay. The initial learning rate was 2e-4, which was halved at iterations [250K, 400K, 450K, 475K]. The experiments are implemented by PyTorch using 8 NVIDIA V100 GPUs. We provide three versions of Hi-Mamba with varying complexities, denoted as Hi-Mamba-T, Hi-Mamba-S and Hi-Mamba-L. The details of the three versions can be found in the Appendix.

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4.2 COMPARISON WITH LIGHTWEIGHT SR MODELS.

Quantitative evaluations. Tab. 2 summarizes the quantitative results at three SR scale factors 366 of  $\times 2, \times 3$  and  $\times 4$ . The parameter and computational costs of MambalRGuo et al. (2024) are 367 modified by the tool<sup>1</sup>Compared to CNN-based methods, Transformer-based approaches (such as 368 IMDN Hui et al. (2019) and SRFormer-Light Zhou et al. (2023)) introduce self-attention mechanisms 369 to model long-range dependencies, exhibiting superior performance in terms of PSNR and SSIM. 370 Notably, transformer-based methods often utilize window-based self-attention mechanisms in the 371 super-resolution task to reduce computational but limit the receptive field within the window. In 372 contrast, MambaIR employs the SSM to model long-range dependencies, which outperforms the 373 SOTA SRFormer Zhou et al. (2023) by 0.09 PSNR on Urban100 for  $3 \times$  SR. However, MambaIR 374 requires  $1.59 \times$  parameter and  $2.41 \times$  FLOPs compared to SRFormer. This is due to the usage of 375 computation-heavy multi-sequence directional scanning in SSM and the redundant structural design. 376 For a fair comparison, we compare the proposed Hi-Mamba-T and Hi-Mamba-S with state-of-the-art

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<sup>&</sup>lt;sup>1</sup>https://github.com/MzeroMiko/VMamba/blob/main/classification/models/vmamba.py#L1372

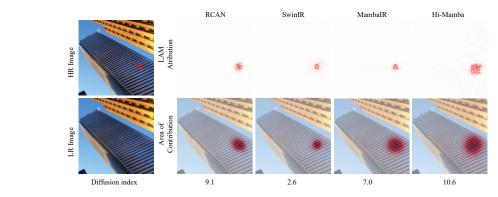


Figure 4: LAM visualization Gu & Dong (2021) on  $\times 2$  SR task. LAM indicates the correlation between the significance of each pixel in LR and the SR patch outlined with the red box. Hi-Mamba utilizes a broader range of information to obtain better performance.

Table 3: Comparison of different PSNR-oriented SR models on five benchmarks. Methods with "\*" are replicated with standard setting, detailed in the Appendix. Methods with "+" denote the use of a self-ensemble strategy.

396	self-ensemble strategy	<b>'</b> .										
007	Model	Scale		et5	Se	t14	BSI	D100		an100	Man	ga109
397		State	PSNR	SSIM								
398	EDSR Lim et al. (2017)	$\times 2$	38.11	0.9602	33.92	0.9195	32.32	0.9013	32.93	0.9351	39.10	0.9773
	RCAN Zhang et al. (2018)	$\times 2$	38.27	0.9614	34.12	0.9216	32.41	0.9027	33.34	0.9384	39.44	0.9786
399	SAN Dai et al. (2019)	$\times 2$	38.31	0.9620	34.07	0.9213	32.42	0.9028	33.10	0.9370	39.32	0.9792
400	HAN Niu et al. (2020)	$\times 2$	38.27	0.9614	34.16	0.9217	32.41	0.9027	33.35	0.9385	39.46	0.9785
400	IGNN Zhou et al. (2020)	$\times 2$	38.24	0.9613	34.07	0.9217	32.41	0.9025	33.23	0.9383	39.35	0.9786
401	CSNLN Mei et al. (2020)	$\times 2$	38.28	0.9616	34.12	0.9223	32.40	0.9024	33.25	0.9386	39.37	0.9785
100	NLSN Mei et al. (2021)	$\times 2$	38.34	0.9618	34.08	0.9231	32.43	0.9027	33.42	0.9394	39.59	0.9789
402	ELAN Zhang et al. (2022b)	$\times 2$	38.36	0.9620	33.20	0.9228	32.45	0.9030	33.44	0.9391	39.62	0.9793
403	DLGSANet Li et al. (2023b)	$\times 2$	38.34	0.9617	34.25	0.9231	32.38	0.9025	33.41	0.9393	39.57	0.9789
	IPT Chen et al. (2021)	$\times 2$	38.37	-	34.43	-	32.48	-	33.76	-	-	-
404	SwinIR Liang et al. (2021)	$\times 2$	38.42	0.9623	34.46	0.9250	32.53	0.9041	33.81	0.9427	39.92	0.9797
405	EDT Li et al. (2021a)	$\times 2$	38.45	0.9624	34.57	0.9258	32.52	0.9041	33.80	0.9425	39.93	0.9800
405	GRL-B* Li et al. (2023c)	$\times 2$	38.48	0.9627	34.64	0.9265	32.55	0.9045	33.97	0.9437	40.06	0.9804
406	SRFormer Zhou et al. (2023)	$\times 2$	38.51	0.9627	34.44	0.9253	32.57	0.9046	34.09	0.9449	40.07	0.9802
	MambaIR Guo et al. (2024)	$\times 2$	38.57	0.9627	34.67	0.9261	32.58	0.9048	34.15	0.9466	40.28	0.9806
407	Hi-Mamba-L	$\times 2$	38.58	0.9633	34.70	0.9264	32.60	0.9054	34.22	0.9475	40.38	0.9820
408	Hi-Mamba-L+	$\times 2$	38.60	0.9634	34.78	0.9269	32.63	0.9058	34.34	0.9483	40.49	0.9822
400	EDSR Lim et al. (2017)	$\times 4$	32.46	0.8968	28.80	0.7876	27.71	0.7420	26.64	0.8033	31.02	0.9148
409	RCAN Zhang et al. (2018)	$\times 4$	32.63	0.9002	28.87	0.7889	27.77	0.7436	26.82	0.8087	31.22	0.9173
	SAN Dai et al. (2019)	$\times 4$	32.64	0.9003	28.92	0.7888	27.78	0.7436	26.79	0.8068	31.18	0.9169
410	HAN Niu et al. (2020)	$\times 4$	32.64	0.9002	28.90	0.7890	27.80	0.7442	26.85	0.8094	31.42	0.9177
411	IGNN Zhou et al. (2020)	$\times 4$	32.57	0.8998	28.85	0.7891	27.77	0.7434	26.84	0.8090	31.28	0.9182
	CSNLN Mei et al. (2020)	$\times 4$	32.68	0.9004	28.95	0.7888	27.80	0.7439	27.22	0.8168	31.43	0.9201
412	NLSN Mei et al. (2021)	$\times 4$	32.59	0.9000	28.87	0.7891	27.78	0.7444	26.96	0.8109	31.27	0.9184
440	ELAN Zhang et al. (2022b)	$\times 4$	32.75	0.9022	28.96	0.7914	27.83	0.7459	27.13	0.8167	31.68	0.9226
413	DLGSANet Li et al. (2023b)	$\times 4$	32.80	0.9021	28.95	0.7907	27.85	0.7464	27.17	0.8175	31.68	0.9219
414	IPT Chen et al. (2021)	$\times 4$	32.64	-	29.01	-	27.82	-	27.26	-	-	-
	SwinIR Liang et al. (2021)	$\times 4$	32.92	0.9044	29.09	0.7950	27.92	0.7489	27.45	0.8254	32.03	0.9260
415	EDT Li et al. (2021a)	$\times 4$	32.82	0.9031	29.09	0.7939	27.91	0.7483	27.46	0.8246	32.05	0.9254
416	GRL-B* Li et al. (2023c)	$\times 4$	32.90	0.9039	29.14	0.7956	27.96	0.7497	27.53	0.8276	32.19	0.9266
416	SRFormer Zhou et al. (2023)	$\times 4$	32.93	0.9041	29.08	0.7953	27.94	0.7502	27.68	0.8311	32.21	0.9271
417	MambaIR Guo et al. (2024)	$\times 4$	33.03	0.9046	29.20	0.7961	27.98	0.7503	27.68	0.8287	32.32	0.9272
	Hi-Mamba-L	$\times 4$	33.05	0.9049	29.23	0.7966	28.01	0.7531	27.72	0.8296	32.43	0.9280
418	Hi-Mamba-L+	$\times 4$	33.08	0.9051	29.26	0.7969	28.02	0.7534	27.81	0.8304	32.56	0.9300

lightweight SR methods. Benefiting from the multi-scale mechanism and DA-HMG, Hi-Mamba-T
and Hi-Mamba-S outperform SRFormer and MambaIR in terms of PSNR and SSIM across multiple
benchmark datasets with comparable parameters and FLOPs. For example, compared to MambaIR,
Hi-Mamba-S and Hi-Mamba-T reduce FLOPs by 294G and 390G, while improving the PSNR for
×2 SR on Urban100 by 0.21 dB and 0.12 dB, respectively. Meanwhile, Hi-Mamba-T significantly
outperforms SRFormer by 0.24 dB on ×3 scale SR on Urban100, while reducing 25 GFLOPs and
maintaining relatively consistent parameters.

Qualitative Comparison. In Fig. 3, we present the visual comparisons for ×4 SR. We can observe
 that previous CNN-based or Transformer-based methods suffer from blurry artifacts, distortions, and
 inaccurate texture restoration. In contrast, our method effectively reduces these artifacts, preserving
 more structural and clear details. More visual examples can be referred to in the Appendix. Moreover,
 as shown in Fig.4, we also visualize the Local Attribution Map (LAM) Gu & Dong (2021) to
 demonstrate the strong ability for long-range modeling using our Hi-Mamba-S.

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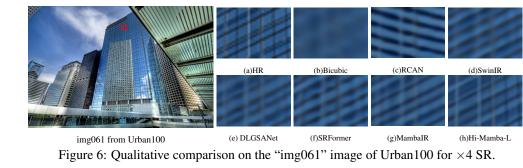


Table 4: Model complexity comparisons ( $\times$ 2). PSNR (dB) on Urban100 and Manga109, FLOPs, and Params are reported. Methods with "\*" are replicated with standard settings.

i aranis are reported	. memo	us with	are reprivated with standard settings.						
Method	EDSR	RCAN	SAN	HAN	NLSA	SwinIR	GRL-B*	MambaIR	Hi-Mamba-L
Params(M)	43.09	15.59	15.87	63.61	41.80	11.90	20.20	20.42	21.58
FLOPs(G)	11,130	3,530	3,050	14,551	9,632	3,213	12,036	6,215	4,334
PSNR-Urban100(dB)	32.93	33.34	33.10	33.35	33.42	33.81	33.97	34.15	34.22
PSNR-Managa109(dB)	39.10	39.44	39.32	39.46	39.59	39.92	40.06	40.28	40.38

4.3 COMPARISON WITH PSNR-ORIENTED SR MODELS

To validate the scalability of Hi-Mamba, we further compare our Hi-Mamba-L with state-of-the-art PSNR-oriented SR models.

**Quantitative evaluations.** Tab. 3 summarizes the SR results at the scales of  $\times 2$  and  $\times 4$ .

454 Our Hi-Mamba-L demonstrates superior performance 455 compared to previous methods. In addition, the perfor-456 mance of Hi-Mamba-L can be further improved by using the self-ensemble strategy, denoted by Hi-Mamba-457 L+. For example, compared to SRFormer Zhou et al. 458 (2023) and MambaIR Guo et al. (2024), our Hi-Mamba-459 L+ achieves significant PSNR gains of 0.42 dB and 460 0.21 dB on Manga109 for  $\times 2$  SR, respectively. For  $\times 4$ 461 SR, our Hi-Mamba-L+ outperforms SRFormer by the 462 PSNR of 0.18 dB and 0.35 dB on Set14 and Manga109, 463 respectively.  $\times 3$  SR result is presented in the Appendix. 464

Qualitative comparison. We present the visual comparison of classic SR (×4) in Fig. 6. Compared with CNNs (e.g., RCAN) and Transformers (e.g., SwinIR, SRFormer, DLGSANet), as well as SSM-based MambaIR, Hi-Mamba reconstructs the most photo-realistic building texture compared to these models.

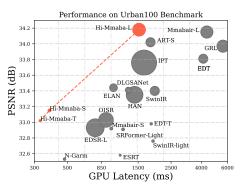


Figure 5: Performance on Urban100 for  $\times 2$  SR. The larger circles present larger computation costs on Params.

Model Complexity Comparison. Tab. 4 further makes our Hi-Mamba-L with CNNs and Transformers in terms of parameters and FLOPs. Our Hi-Mamba-L significantly reduces GFLOPs by 7,702 and 1,881, and achieves 0.22dB and 0.10dB PSNR gains on Manga109 over GRL-B and MambaIR. To evaluate the practical inference time, we conduct the experiments on the PSNR and speed results of different methods as shown in Fig. 5. We can observe that Hi-Mamba achieves the best latency-PSNR trade-off.

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478 4.4 ABLATION STUDIES

In the ablation study, we train the models on DIV2K evaluated on Urban100 for  $2 \times$  SR, as it contains images with rich structural details. For a fair comparison, we train the *baseline* composed of only L-SSM and MLP stacks with a depth number equal to Hi-Mamba-S.

Ablation for key components of Hi-Mamba. We first conduct the ablation study on the effect of
 R-SSM, G-FFN, and DA-HMG. As shown in Tab. 5, the R-SSM significantly improves PSNR by 0.19
 dB. With the FFN replaced by G-FFN, this model achieves a gain of 0.04 dB over baseline+R-SMM
 while reducing 0.1M parameters and 15G FLOPs. Finally, by utilizing DA-HMG, we further improve

Tabl	e 5: Ał	olation st	udy of the	e key con	nponer	nts.	Table 7: Effect of fusion module in R-SS				
R-SSM	G-FFN	DA-HMG	Params(M)	FLOPs(G)	PSNR	SSIM	Fusion method	Upsampling	Repeat	Repeat $S_f = 0.5$	
			1.29	252	32.76	0.9339	Params(M)	1.34	1.34	1.33	
1			1.44	289	32.95	0.9354	FLOPs(G)	275	274	274	
	./		1.34	274	32.99	0.9356	GPU(ms)	387	379	371	
•	•	/					PSNR(dB)	33.06	33.13	33.08	
<b>√</b>	✓	~	1.34	274	33.13	0.9368	SSIM	0.9352	0.9368	0.9360	

PSNR by 0.14 dB without incurring additional computational costs. This indicates that all the key components of Hi-Mamba show their effectiveness.

Table 6: Ablation study of DA-HMG.									
Model	PSNR(dB)	SSIM	Params(M)	FLOPs(G)					
Single-direction w/o alternation	32.99	0.9356	1.34	274					
Two-direction alternation	33.07	0.9361	1.34	274					
Four-direction alternation	33.13	0.9368	1.34	274					

Table 8	: Abali	ton of R	R-SSM o	hannel nu	mber.
	#Channel	FLOPs(G)	Params(M)	PSNR(dB)	
	15	252	1.30	33.01	
	30	274	1.34	33.13	
	60	296	1.76	33.14	

	Table 9: Effect of region size in R-SSM.									
Region size	Params(M)	FLOPS(G)	GPU(ms)	PSNR(dB)	SSIM					
$1 \times 1$	1.52	312	662	33.13	0.9369					
$4 \times 4$	1.34	274	379	33.13	0.9368					
$8 \times 8$	1.34	271	365	33.01	0.9358					

504 Ablation for different scan modes in DA-HMG. To investigate the effect of different scan modes 505 in DA-HMG, we compare four-direction alternative scanning with single-direction without alternation(i.e., base-single), and two-direction alternative scanning, as summarized in Tab. 6. By default, 506 single-direction without alternation only uses HMB-H, and two-direction alternative scanning uses 507 HMB-H and HMB-V. We observe that the model using four-direction alternation achieves the best 508 performance with an improvement of 0.14 dB PSNR and 0.06 dB PSNR over single-direction without 509 alternation and two-direction alternation, respectively. Note that alternative direction scanning does 510 not incur additional computational and memory costs. This indicates that direction alternation in 511 DA-HMG can aggregate spatial information from different positions to improve reconstruction 512 performance. 513

**Effect of fusion module in R-SSM.** As shown in Tab. 7, the repeat method implicitly incorporates the 2D spatial position information of features, achieving a PSNR of 0.07 dB higher than the upsampling method. It demonstrates the effectiveness of our 2D repeat fusion method. We also conduct additional ablation experiments on the learnable parameters  $S_f$ . We observed that the learnable parameter  $S_f$  achieves only a slight increase of 0.01M parameters and 8ms GPU while outperforming fixed  $S_f$  by 0.05dB PSNR. Thus, we default use the learnable  $S_f$  for the fusion module.

Ablation of R-SSM channel number. We analyze the computational complexity of hierarchical design to achieve the best PSNR-FLOPs trade-off by changing the channel number of R-SSM. In Tab. 8, the channel number of 30 in R-SSM (*i.e.*, a half of L-SSM) achieves the best trade-off between performance and computation complexity.

**Ablation for the region size**  $n \times n$  **in R-SSM.** As presented in Tab. 9, we find that a region patch size of  $1 \times 1$  achieves the highest SSIM of 0.9369, but the inference time significantly increases, compared to patch sizes of  $4 \times 4$  and  $8 \times 8$ . The region size of  $4 \times 4$  yields the best trade-off between PSNR and inference speed. Thus, we set the region size to  $4 \times 4$  for our experiments.

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### 5 CONCLUSION

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We present the Hierarchical Mamba Network (Hi-Mamba) in this paper for image super-resolution.
Hi-Mamba is built on multiple-direction alternation hierarchical Mamba groups (DA-HMG), which
allocates the isomeric single-direction scanning into cascading HMBs, enriching the modeling
of spatial relationships. Each HMB consists of a Local SSM and a Region SSM, utilizing unidirectional scanning to aggregate multi-scale representations and enhance 2D spatial perception.
Extensive experiments demonstrate that our Hi-Mamba has high potential compared to CNN-based
and transformer-based methods.

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## 540 REPRODUCIBILITY STATEMENT

In this section, we provide a reproducibility statement for our proposed method. We detail the model
architecture and core designs in Sec. 3, including the hierarchical mamba block (HMB) and Direction
Alternation HMB Group (DA-HMG). Additionally, we present implementation details and elaborate
on the experimental setup in Sec. 4.1. To ensure reproducibility, we will release the source code and
pre-trained models. For more details, please refer to the Appendix.

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### 756 A APPENDIX

In this supplementary material, we provide additional information on the model analysis and experimental results of the Hierarchical Mamba (Hi-Mamba). In Section A.1, we report more information on the model details of different versions of Hi-Mamba. In Section A.2, We show the details of different scanning methods. In Section A.3, we present more extensive quantitative results on Hi-Mamba-L. In Section A.4, we provide additional qualitative comparisons. In Section A.5, we report the results of Hi-Mamba on other low-level vision tasks.

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  - A.1 MODEL DETAILS

766 We introduce Hi-Mamba model variants, scaled appropriately for different model sizes. We propose 767 three sizes: Hi-Mamba-T (0.87M parameters), Hi-Mamba-S (1.34M parameters), and Hi-Mamba-L 768 (22.58M parameters). Each Hi-Mamba variant is defined by its depth and width. Specifically, for 769 Hi-Mamba-T and Hi-Mamba-S, there are 5 DA-HMGs, each containing 4 HMBs. The channel 770 dimensions are set to 60 and 48 for Hi-Mamba-T and Hi-Mamba-S, respectively. The channel size 771 for R-SSM is set to half of the respective channel dimensions. The channel expansion factor in 772 G-FFN is set to 1.5. For Hi-Mamba-L, we increase the number of DA-HMGs to 7, with HMB 773 numbers configured as [4, 4, 8, 8, 8, 4, 4]. Additionally, the channel dimension is increased to 180, 774 and the expansion factor is set to 2. In addition, Hi-Mamba-L also introduces the channel attention 775 mechanism. Other settings remain the same as Hi-Mamba-S. The model variants are summarized in the table 10. 776

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Table 10: Hi-Mamba family. Channel Dimension indicates the number of channels for L-SSM/R-SSM.

Method	Params(M)	FLOPs(G)	GPU(ms)	DA-HMG	HMB	Channel Dimension	Expansion Factor	Channel Attention
Hi-Mamba-T	0.87	178	324	5	[4, 4, 4, 4, 4]	48/24	1.5	No
Hi-Mamba-S	1.34	274	379	5	[4, 4, 4, 4, 4]	60/30	1.5	No
Hi-Mamba-L	21.58	4334	1593	7	[4, 4, 8, 8, 8, 4, 4]	180/90	2	Yes

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### A.2 COMPARISON OF DIFFERENT SCANNING METHODS IN SSM

In NLP tasks, data often contains causal relationships, so a base-single scanning approach is typically 786 used, as shown in Fig. 7 (a). This single-directional scanning method has low complexity, but it is 787 designed for text data and struggles to construct 2D spatial relationships in image tasks. VMamba Liu 788 et al. (2024) and MambaIR Guo et al. (2024) designed the 2D-SSM scanning method for image tasks 789 to model pixel information from various directions, as shown in Fig. 7 (b). 2D-SSM performs four 790 different directional scanning sequences in parallel at each layer, achieving multi-directional paral-791 lelism. However, in visual SSM architectures, parallel scanning across four sequences significantly 792 increases computational overhead, making it less efficient for processing high-resolution images. 793 This compromises the speed advantage of the Mamba architecture. To address this issue, we designed 794 the DA-HMG, as shown in Fig. 7 (c). In each layer, only a single directional scanning sequence is 795 computed. Compared to the base-single approach, the use of different directional scanning sequences 796 in DA-HMG allows pixels to integrate neighboring information from multiple directions. In contrast to 2D-SSM, DA-HMG selects only one scanning direction per layer, significantly improving inference 797 speed while reducing computational and parameter overhead. 798

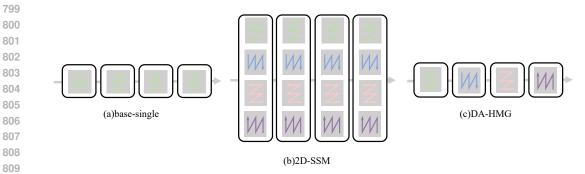


Figure 7: Visualization of different scanning methods.

#### A.3 MORE EXTENSIVE QUANTITATIVE RESULTS

We further report the results compared to PSNR-oriented SR Models at scale  $\times 3$ . In the main paper, we have evaluated the effectiveness for  $\times 2$  and  $\times 4$  SR performance. As shown in Tab. 11, Hi-Mamba-L achieves the best PSNR across all datasets, surpassing the second-place MambaIR by 0.11 dB and the transformer-based method SR former by 0.28 dB on Manga109 with comparable parameter and FLOPs. 

Table 11: Comparison of different PSNR-oriented SR models on five benchmarks with scale  $\times 3$ .

Model	Scale	S	et5	Se	et14	BSI	D100	Urb	an100	Man	ga109
would	Scale	PSNR	SSIM								
EDSR Lim et al. (2017)	$\times 3$	34.65	0.9280	30.52	0.8462	29.25	0.8093	28.80	0.8653	34.17	0.9476
RCAN Zhang et al. (2018)	$\times 3$	34.74	0.9299	30.65	0.8482	29.32	0.8111	29.09	0.8702	34.44	0.9499
SAN Dai et al. (2019)	$\times 3$	34.75	0.9300	30.59	0.8476	29.33	0.8112	28.93	0.8671	34.30	0.9494
HAN Niu et al. (2020)	$\times 3$	34.75	0.9299	30.67	0.8483	29.32	0.8110	29.10	0.8705	34.48	0.9500
IGNN Zhou et al. (2020)	$\times 3$	34.72	0.9298	30.66	0.8484	29.31	0.8105	29.03	0.8696	34.39	0.9496
CSNLN Mei et al. (2020)	$\times 3$	34.74	0.9300	30.66	0.8482	29.33	0.8105	29.13	0.8712	34.45	0.9502
NLSN Mei et al. (2021)	$\times 3$	34.85	0.9306	30.70	0.8485	29.34	0.8117	29.25	0.8726	34.57	0.9508
ELAN Zhang et al. (2022b)	$\times 3$	34.90	0.9313	30.80	0.8504	29.38	0.8124	29.32	0.8745	34.73	0.9517
DLGSANet Li et al. (2023b)	$\times 3$	34.95	0.9310	30.77	0.8501	29.38	0.8121	29.43	0.8761	34.76	0.9517
IPT Chen et al. (2021)	$\times 3$	34.81	-	30.85	-	29.38	-	29.49	-	-	-
SwinIR Liang et al. (2021)	$\times 3$	34.97	0.9318	30.93	0.8534	29.16	0.8145	29.75	0.8826	35.12	0.9537
EDT Li et al. (2021a)	$\times 3$	34.97	0.9316	30.89	0.8527	29.44	0.8142	29.72	0.8814	35.13	0.9534
GRL-B* Li et al. (2023c)	$\times 3$	35.05	0.9323	31.00	0.8543	29.49	0.8153	29.83	0.8837	35.24	0.9541
SRFormer Zhou et al. (2023)	$\times 3$	35.02	0.9323	30.94	0.8540	29.48	0.8156	30.04	0.8865	35.26	0.9543
MambaIR Guo et al. (2024)	$\times 3$	35.08	0.9323	30.99	0.8536	29.51	0.8157	29.93	0.8841	35.43	0.9546
Hi-Mamba-L	$\times 3$	35.10	0.9329	31.08	0.8545	29.54	0.8173	29.99	0.8846	35.47	0.9548
Hi-Mamba-L+	$\times 3$	35.15	0.9332	31.16	0.8547	29.55	0.8176	30.08	0.8871	35.54	0.9553

### A.4 MORE VISUALIZATION RESULTS

We add more visualization results of our Hi-Mamba-S and Hi-Mamba-L, making comparisons with other models on different datasets for  $\times 4$  SR in Fig. 8, and Fig. 9, respectively. In img078, ESRT and MambaIR exhibit artifacts in their restorations, whereas Hi-Mamba-S successfully recovers the structural detail contours.

#### A.5 MORE IMAGE RESTORATION TASKS

We further evaluate the performance of our Hi-Mamba on image deblurring with state-of-the-art image deblurring models. including SRN Tao et al. (2018), DMPHN Zhang et al. (2019a), MPRNet Zamir et al. (2021), IPT Chen et al. (2021), Restormer Zamir et al. (2022), Uformer Wang et al. (2022) and Stripformer Tsai et al. (2022) In Tab. 12, our Hi-Mamba achieves the highest 33.27dB PSNR, outperforming the previous best SOTA Stripformer with 0.19dB.

[	Table 12: Quantitative evaluations on GoPro dataset for image deblurring.										
Method	SRN	DMPHN	MPRNet	IPT	Restormer	Uformer	Stripformer	Hi-Mamba			
PSNR	30.26	31.20	32.66	32.52	32.92	33.06	33.08	33.27			
SSIM	0.9342	0.9453	0.9589	-	0.9611	0.9670	0.9624	0.9651			
Params(M)	6.8	21.7	20.1	114	26.1	50.9	19.7	23.6			

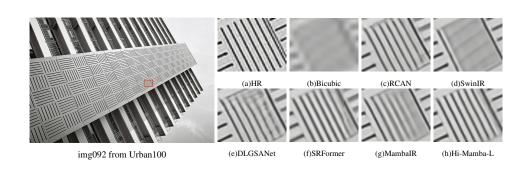


Figure 8: Qualitative comparison on the "img092" image of Urban100 for ×4 classical SR.

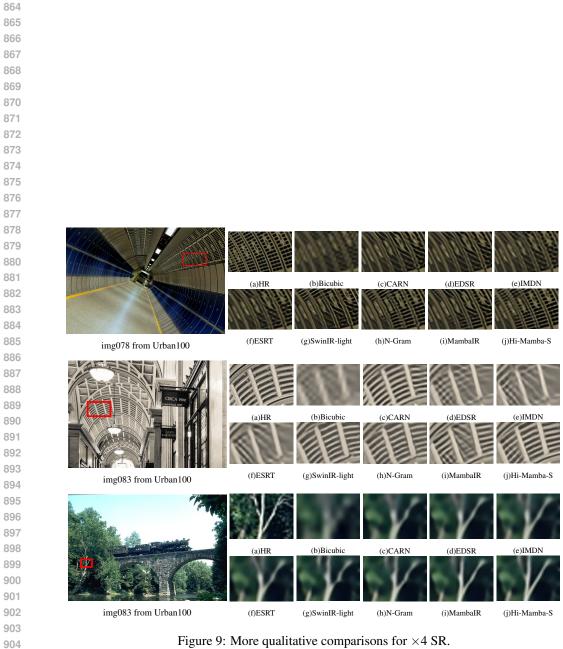


Figure 9: More qualitative comparisons for  $\times 4$  SR.