# RMAAT: A BIO-INSPIRED APPROACH FOR EFFICIENT LONG-CONTEXT SEQUENCE PROCESSING IN TRANS FORMERS

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## Abstract

Astrocytes, an essential component of the brain's neural circuitry, demonstrate learning capabilities through bioplausible mechanisms such as presynaptic plasticity and hebbian plasticity. However, their integration into computational models remains underexplored. This paper advances astromorphic computing techniques to emulate transformer self-attention mechanisms, leveraging astrocytic nonlinearity and memory retention to improve long-range dependency processing in machine learning and natural language processing (NLP) tasks. Existing transformer models have difficulty handling lengthy contexts with thousands of tokens, even with substantial computational resources. We propose Recurrent Memory Augmented Astromorphic Transformers (RMAAT), integrating astrocytic memory and recurrent processing into self-attention, enabling longer context handling without quadratic complexity growth. Our bioplausible model has been found to outperform traditional transformers in experimental tests conducted on the Long Range Arena benchmark and IMDB dataset. Specifically, our model achieves a significant reduction in memory utilization and computational latency. This paves the way for biologically inspired AI models by illustrating how astrocytic characteristics may enhance the performance and efficiency of computational models.

# 1 INTRODUCTION

032 The human brain, a marvel of biological engineering, relies on a network of diverse cell types to 033 perform complex functionalities. Among these cells, astrocytes are ubiquitous in critical regions es-034 sential for cognitive functions. Astrocytes, which are star-shaped glial cells, have long been thought to support neurons, but recent research has revealed that they also play an active role in various brain 035 processes. They control synaptic activity, assist in learning and memory, and alter how information is processed and stored in the brain (Gibbs et al., 2008; Bohmbach et al., 2022; Oliveira & Araque, 037 2022). The diverse range of functions performed by astrocytes presents intriguing opportunities for incorporating their roles into computational models, providing novel pathways for enhancing artificial intelligence and machine learning (Kozachkov & Michmizos, 2017; 2020; González et al., 040 2012; Porto-Pazos et al., 2011). 041

Astromorphic computing aims to improve the efficiency and effectiveness of machine learning mod-042 els by emulating the nonlinear processing and memory retention capabilities of astrocytes, (Mia 043 et al., 2023; Kozachkov et al., 2023a). Integrating the principles of astromorphic computing with 044 transformer architectures presents a novel approach to advancing artificial intelligence. Transform-045 ers have significantly impacted the domain of machine learning, specifically in natural language 046 processing (NLP) (Vaswani et al., 2017). The self-attention mechanism is the key innovation of 047 transformers; it allows models to determine the importance of each word in a sentence indepen-048 dent of their position. However, despite the remarkable success of transformers, challenges persist in efficiently handling long sequences. Conventional neural networks, including transformers, often struggle with lengthy data sequences due to architectural limitations (Wu et al., 2020; Bulatov 051 et al., 2022). Similarly, brain-inspired models like spiking neural networks (SNNs) have advanced by emulating neuronal spiking behaviors and incorporating various bio-plausible synaptic learn-052 ing rules—such as spike-timing-dependent plasticity, e-prop, DECOLLE, equilibrium propagation, among others (Lu & Sengupta, 2024; Bellec et al., 2020; Kaiser et al., 2020; Bal & Sengupta,

2022)—but they generally fail to fully integrate the essential role of astrocytes and the complex interactions within the tripartite synapse. These models frequently overlook astrocytes' capacity for recurrent processing and memory retention, as well as their function as temporal and spatial integrators (Kozachkov et al., 2023; Mia et al., 2023; Han et al., 2023; Lines, 2025).

058 In this work, we leverage the memory retention and recurrent processing capabilities of astrocytes, macro-modeled through short- and long-term processes in the neuron-astrocyte network, to tempo-060 rally integrate astrocytic functions within transformer architectures. We explicitly map astrocytic 061 short-term plasticity to spatial relative information, an aspect previously overlooked. This mapping 062 of short-term processes facilitates the integration of long-term plasticity, which is then incorporated 063 to form temporal astrocytic memory, enabling the model to process long sequences by compressing 064 context into memory tokens. We implement this compression mechanism derived from the neuroscience macro-model as a memory retention factor. Furthermore, leveraging astrocytic memory, 065 we introduce the Astrocytic Memory Replay Backpropagation (AMRB) algorithm, which signifi-066 cantly reduces hardware computational burden. Through this neuroscience-algorithm co-design, we 067 propose the Recurrent Memory Augmented Astromorphic Transformer (RMAAT), which offers a 068 unique learning approach, achieving higher accuracy in long-context machine learning tasks with a 069 fivefold reduction in hardware memory utilization. 070

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# 2 RELATED WORKS AND MAIN CONTRIBUTIONS

While transformers have transformed sequence modeling with self-attention, their quadratic complexity limits scalability for long sequences (Vaswani et al., 2017). Efficient variants like Reformer (Kitaev et al., 2020) and Longformer (Beltagy et al., 2020) address this but often compromise model capacity and long-term dependency capture. Spiking Neural Networks (SNNs) offer energy-efficient alternatives (Pfeiffer & Pfeil, 2018), with advanced learning rules like e-prop (Bellec et al., 2020), DECOLLE (Kaiser et al., 2020), and surrogate gradients (Neftci et al., 2019). However, SNNs typically lack the capacity to handle long-term dependencies without major architectural changes and do not incorporate astrocytic functions or tripartite synapse interactions.

Research on integrating astrocytes into neural networks has predominantly focused on small-scale 084 models for specific functions such as synaptic modulation and homeostasis. For example, Nad-085 karni & Jung (2007) explored astrocyte-mediated synaptic transmission, and Postnov et al. (2009) 086 investigated astrocytic influence on neuronal synchronization. In addition, astrocytic models have 087 been instrumental in advancing neuromorphic systems by enabling self-repair and improving robotic 088 locomotion through homeostatic control of Central Pattern Generators (CPG). In self-repair mech-089 anisms, astrocytes play a crucial role in restoring synaptic functions, as explored by (Wade et al., 090 2012) and (Han et al., 2023), where astrocytic retrograde signaling is used to repair damaged neural 091 pathways. In CPG systems, astrocytes regulate neuronal synchronization and plasticity, facilitat-092 ing gait generation and learning in robotic systems, as shown by (Han & Sengupta, 2023). Some 093 other works in astromorphic computing have begun to explore astrocytic functions within machine learning models. Kozachkov et al. (2023a) introduced astrocyte-inspired neural networks focusing 094 on tripartite synaptic plasticity, while Mia et al. (2023) leveraged astrocytic calcium dynamics to 095 introduce nonlinearity into the self-attention mechanism of transformers, allowing the processing of 096 information based on relative input positioning. However, they do not explicitly associate short-term plasticity with self-attention. Consequently, existing approaches tend to address isolated aspects of 098 astrocytic function and fail to explicitly map both short-term and long-term plasticity onto machine learning models or integrate the temporal astrocytic plasticity necessary for efficient handling of 100 long sequences. 101

Our work introduces a novel RMAAT architecture that leverages astrocytic plasticity for efficient processing of long-context sequences. The main contributions of this work are:

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- Temporal Memory via Long-Term Astrocytic Plasticity: By integrating long-term astrocytic plasticity, we form temporal memory that retains context during sequential processing, enabling the model to handle long sequences by retaining contexts into memory tokens.

- Innovative Astrocytic Memory Compression Mechanism: We introduce a novel astrocytic compression mechanism that efficiently condenses contextual information into residual temporal memories.
- Hardware Efficiency via Astrocytic Memory Replay Backpropagation (AMRB): By employing the AMRB learning technique, the proposed model achieves a 5× reduction in hardware memory utilization compared to conventional transformers, enhancing practicality for resource-constrained applications.
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# 3 Methodology

In order to introduce the Recurrent Memory Augmented Astromorphic Transformer (RMAAT), we first discuss the computational neuroscience backbone that forms the foundation of our model. This backbone creates the macro-model responsible for translating short and long-term synaptic plasticities into the astromorphic self-attention mechanism. We then leverage these plasticities within a machine learning framework to efficiently handle long-range dependencies, forming the RMAAT architecture that combines biologically-inspired mechanisms with transformer-based processing.

125 3.1 SHORT-TERM AND LONG-TERM PLASTICITY

To capture the spatial and temporal aspects of astrocytic plasticities, we focus on short-term plasticity (STP) and long-term plasticity (LTP). STP involves rapid synaptic adjustments, while LTP refers to lasting changes over hours to days, both critical for memory and learning (Min et al., 2012; Perez-Catalan et al., 2021; Pittà et al., 2015; Li, 2024; Alberini et al., 2018; Gordleeva et al., 2023; 2021).
These plasticities integrate neuronal, synaptic, and astrocytic dynamics across different temporal and spatial scales (Kozachkov et al., 2023b; Kozachkov & Michmizos, 2017).

**Neuron-Astrocyte Network Dynamics:** The neuron-astrocyte network integrates the dynamics of 133 neurons, synapses, and astrocytic processes shaped by short and long-term plasticities. Astrocytes 134 modulate synaptic transmission and plasticity via gliotransmitter release and ionic concentration, 135 stabilizing neuronal activity and forming attractor states-stable brain activity configurations encod-136 ing memories and behaviors (Becker et al., 2022; Mongillo et al., 2008). Using short-term plasticity, 137 the network quickly adjusts to new information. These neuron-astrocyte interactions are modeled 138 through differential equations, capturing the temporal evolution of synaptic weights and astrocytic 139 influence (Kozachkov et al., 2023b). 140

Short-term Process Dynamics: We begin by examining the short-term processes that regulate synaptic weights via interactions between neurons, synapses, and astrocytes.

(*i*) Neural Dynamics: In the context of a spiking neuron model, the neuron-astrocyte network can be described by discrete events of neuron spikes and continuous synaptic interactions influenced by astrocytes. The membrane potential  $V_i(t)$  of neuron *i* evolves according to the following Eqn. 1:

$$\tau_n \frac{dV_i(t)}{dt} = -\lambda (V_i(t) - V_{\text{reset}}) + I_i(t)$$
(1)

Here,  $\tau_n = R_m C_m$  is the neural dynamics timescale, which is the product of the membrane resistance  $R_m$  and the membrane capacitance  $C_m$ . This timescale is in the order of short-term effects.  $\lambda$ is the decay rate for the membrane potential.  $V_{\text{reset}}$  is the reset potential, and  $I_i(t)$  is the input current to neuron *i* (Diehl et al., 2015). The input current  $I_i(t)$  is determined by the synaptic inputs and an intrinsic bias as noted in Eqn. 2:

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$$I_i(t) = \sum_{j=1}^N g(s_{ij})S_j(t) + b_i, \ S_j(t) = \sum_k \delta(t - t_k)$$
(2)

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157 where,  $S_j(t)$  represents the spike train from neuron j, defined as a sum of Dirac delta functions at 158 spike times  $t_k$ . The synaptic weight  $g(s_{ij})$  and the input bias  $b_i$  influence the membrane potential 159 dynamics. When the membrane potential  $V_i(t)$  reaches a threshold  $V_{th}$ , the neuron fires a spike and 160 the potential is reset to a reset potential  $V_{reset}$ . The activity of neuron i, denoted as  $x_i$ , is a function of 161 its membrane potential  $V_i$ . Specifically,  $x_i$  represents the firing rate or the probability of the neuron 171 firing a spike at a given time, which is influenced by the membrane potential  $V_i$ . 162 (ii) Synaptic Dynamics: The variable  $s_{ij}$  represents the level of synaptic facilitation, indicating the 163 extent to which presynaptic spiking activity influences the postsynaptic neuron. Synaptic strength 164 can either increase or decrease based on pre- and postsynaptic activity. Astrocytes modulate these 165 synaptic interactions through mechanisms such as gliotransmitter release and ionic concentration 166 changes, which in turn affect the synaptic weights  $g(s_{ij})$ . In accordance with studies on neuronglial interactions (Kozachkov et al., 2023b; Gong et al., 2024), we consider tripartite synapses, 167 where synaptic plasticity is regulated by an associated short-term astrocytic parameter,  $p_{ij}^s$ . The 168 dynamics of synaptic facilitation are given by: 169

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$$\tau_s \frac{ds_{ij}}{dt} = -\beta s_{ij} + \theta(x_i)\theta(x_j) + \psi(p_{ij}^s) + c_{ij}$$
(3)

172 In this equation,  $\tau_s$  is the synaptic dynamics timescale.  $\beta$  represents the decay rate of synaptic facili-173 tation. The function  $\theta(x)$  captures the nonlinear interactions between these biological variables. The 174 variables  $x_i$  and  $x_j$  represent the activity levels of neurons i and j, respectively. The constant  $c_{ij}$  acts 175 as a bias, setting the baseline rate of synaptic facilitation in the absence of external input.  $p_{ij}^s$  can be 176 understood as the concentration of intracellular  $Ca^{2+}$  ions in the astrocytic process surrounding the 177 synapse. Astrocytes modulate neural activity through  $Ca^{2+}$ -dependent release of gliotransmitters 178 such as GABA, D-serine, ATP, and glutamate (de Ceglia et al., 2023)-this modulation is captured 179 by the function  $\psi(p_{ij}^s)$ .

(iii) Short-Term Astrocytic Process Dynamics: The state of a particular astrocytic process is influenced by its interactions with neurons at the tripartite synapse and with other astrocytic processes via intracellular calcium transport. This relationship is described by the equation:

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$$\tau_p^s \frac{dp_{ij}^s}{dt} = -\gamma^s p_{ij}^s + \sum_{k,l=1}^N T_{ijkl} \psi(p_{kl}^s) + d_{ij} \tag{4}$$

Here,  $\tau_p^s$  represents the timescale for short-term astrocyte dynamics, and  $\gamma^s > 0$  is a decay term for the intracellular calcium in the astrocytic process. The double sum captures the interactions between the process  $p_{ij}^s$  and all other processes. In the simplest case, calcium can diffuse between processes, represented by a non-linear function  $\psi(p)$  and the tensor  $T_{ijkl}$  describing concentration fluxes. The term  $T_{ijkl}$  is a parameter that captures the spatial positions for the multiple neurons connected to that tripartite synapse. and encodes the spatial distance between the processes  $p_{ij}^s$  and  $p_{kl}^s$ .

While previous efforts have implicitly incorporated short-term process dynamics, we are the first to explicitly propose and map these processes to a neuron-astrocyte network, which subsequently enable us to integrate astrocytic temporal dynamics into the proposed RMAAT architecture. Next, we address the *long-term process dynamics*, a key contribution that enables the temporal integration of astrocytes within the RMAAT architecture.

Long-Term Process Dynamics: The state of a particular astrocytic process for long-term dynamics is described by the equation:

$$\int_{p}^{l} \frac{dp_{ij}^{l}}{dt} = -\gamma^{l} p_{ij}^{l} + \kappa(s_{ij})$$
(5)

Here,  $\tau_p^l$  represents the timescale for long-term astrocyte dynamics and is greater than the timescale for short-term astrocyte dynamics.  $\gamma^l > 0$  is a decay term for the intracellular calcium in the astrocytic process. The nonlinear function  $\kappa(s_{ij})$  represents the synapse-to-astrocyte signaling pathway at the tripartite synapse level, capturing the effects of synaptic activity on astrocytic processes.

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In long-term dynamics, the astrocyte process is performing a form of temporal integration, where it accumulates and integrates the effects of sustained synaptic activity over time. This is essential for the persistent changes associated with long-term plasticity (LTP) and is driven by complex biochemical pathways influenced by the history of synaptic activity. This temporal integration is supported by research showing that long-term changes in astrocytic function involve prolonged biochemical signaling and gene expression changes, which are critical for maintaining long-term synaptic plasticity (Nedergaard et al., 2003; Perea et al., 2009).

**Synergy of Short-Term and Long-Term Dynamics:** We developed a macro-model to simulate the interaction between short-term plasticity (STP) and long-term plasticity (LTP) using a multi-neuron astrocyte network, consisting of 3 presynaptic  $(V_j)$  and 3 postsynaptic neurons  $(V_i)$  connected by 9 synapses  $(s_{ij})$ . The network includes a single astrocyte governing 9 processes in both short-term ( $p_{ij}^s$ ) and long-term dynamics  $(p_{ij}^l)$ . We map these process parameters as attractor states in this macro-model. Neural  $(V_{i,j})$ , synaptic  $(s_{ij})$ , and short-term astrocytic processes  $(p_{ij}^s)$  are modeled with the STP timescale, while long-term astrocytic processes  $(p_{ij}^l)$  follow the LTP timescale. The details of hyperparameters describing the timescale, membrane potential threshold, etc. are discussed in Appendix C.

One STP cycle is defined as complete when the attractor states of the network stabilize, which, 224 in this model, takes 50 seconds. The dynam-225 ics, described by Eqns. 1 - 5, were simulated 226 for 300 seconds, encapsulating 6 STP cycles 227 within one LTP cycle. The long-term astrocytic 228 process parameter  $p_{ij}^l$  reaches a stable attractor 229 state at the 300s mark, accumulating informa-230 tion from the short-term parameters as calcium ions build up during each STP cycle. Depend-231 ing on the LTP timescale  $(\tau_p^l)$ , a varying num-232 ber of STP cycles can fit within one LTP cy-233 cle. We later map the characteristics of STP and 234 LTP in RMAAT, where each STP represents a 235 segmented forward pass within a sequence in-236 volving long-range context. To conceptualize 237 segmented processing, the current STP cycle is 238 reset upon reaching a stable attractor state, after 239 which a new STP cycle is initiated. As depicted 240



Figure 1: Simulated dynamics of synaptic facilitation  $s_{ij}$  (STP) and astrocyte process  $p_{ij}^l$  (LTP) in the macro-model. The figure highlights the rapid stabilization of STP, while LTP gradually builds up over multiple cycles, ultimately reaching a stable attractor state, with cumulative STP effects contributing to the LTP process.

in Fig. 1, after every 50 seconds, a new STP cycle begins, with  $p_{ij}^l$  continuing to accumulate information from short-term parameters  $(s_{ij}, p_{ij}^s)$ . As  $p_{ij}^s$  and  $s_{ij}$  show similar characteristics in STP, for simplicity, only  $s_{ij}$  and  $p_{ij}^l$  are depicted in Fig. 1. Although arbitrary units have been used to plot the parameters,  $s_{ij}$  and  $p_{ij}^l$  can be mapped to synaptic weights and calcium concentration respectively.

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# 3.2 NEURON-ASTROCYTE NETWORK

To utilize STP and LTP 248 processes of the neu-249 roscience macro-model 250 in machine learning, а 251 neuroscience-algorithm co-design framework must 253 be established, and neuron-254 astrocyte networks offer a 255 viable approach for this in-256 tegration. Recent works on neuron-astrocyte networks 257 have proposed decompos-258 ing the softmax attention 259 into linearized kernels by 260 drawing inspiration from 261 biologically plausible plas-262 ticities and nonlinearities observed in astrocytes 264 (Kozachkov et al., 2023a; 265 Mia et al., 2023). This 266 approach decomposes the self-attention formulation 267 into a kernelized operation 268



Figure 2: Overview of the Astromorphic Transformer architecture. This diagram illustrates the integration of bioplausible bi-directional feedback mechanisms within a two-layered neuron-astrocyte network, emulating the self-attention of the transformer encoder. The tripartite synapse between the hidden and output layers is shown, with a detailed depiction of the biological tripartite synapse on the right. The synaptic weights  $W_K$ ,  $W_Q$  and  $W_V$  are corresponding to K, Q and Vof the transformer. 2 - AG initiates the bidirectional communication between astrocyte and neuron which is linked to the direct and indirect feedback evoked by the  $Ca^{2+}$  concentration.

in transformers. The decomposition is carried out by a two-layer neuron-astrocyte network that operates in both write and read modes. In the write mode, information is encoded as keys and

values, while in the read mode, it is decoded using queries within the transformer architecture. The
depiction in Fig. 2 illustrates how bioplausible plasticities influence the network during both the
write and read modes.

In the tripartite synapse of Fig. 2, the presynaptic action potential activates both the postsynaptic neuron and the astrocyte, triggering a calcium response in the astrocyte. This results in direct feedback from the postsynaptic neuron and indirect feedback mediated by the astrocyte. The dynamics of neuron-astrocyte communication can be referenced from Li and Rinzel  $Ca^{2+}$  dynamics (Li & Rinzel, 1994), gatekeeper model (Volman et al., 2007), Nadkarni and Jung model (Nadkarni & Jung, 2004; 2007), and bidirectional study on astrocytic glutamate binding to postsynaptic neurons (AN model) (Wade et al., 2011). The comprehensive description of the computational model can be found in the works of (Wade et al., 2012; 2011; De Pittà et al., 2009; Navarrete & Araque, 2010).

281 In the neuron-astrocyte network of Fig. 2, the write mode encodes input sequences by adjusting 282 synaptic weights through biologically inspired plasticity mechanisms. During the write mode, the 283 input for token t is processed in the neuron-astrocyte network (Fig. 2) as follows:  $i_t = x_t, h_t =$ 284  $\phi(i_t W_K) = \phi(k_t), o_t = i_t W_V = v_t$ . During the write mode, the input layer sequentially transmits 285 the keys  $k_t = i_t W_K$  to the hidden layer and the values  $v_t = i_t W_V$  to the output layer. The hidden layer neurons activate a non-linear feature map  $\phi(.)$  on the keys to create outputs  $h_t = \phi(k_t)$ , and 286 287 the values  $v_t$  are transmitted to the output layer.  $\phi(.)$  can be implemented using radial basis function (RBF) (Peng et al., 2021), rectified, or exponent-based (Katharopoulos et al., 2020) kernels. We employ the feature map  $\phi(x) = elu(x) + 1$  due to its superior performance compared to alternative 289 kernels. 290

In the following subsections, we explain in detail how these astrocytic plasticities, specifically hebbian and presynaptic plasticites, are incorporated during the write mode and their role in enabling the self-attention mechanism in the read mode. Moreover, we emphasize our contribution in mapping short-term processes through the spatial integration of astrocytes within the neuron-astrocyte network, culminating in the development of the RMAAT architecture. To map STP into astromyphic computing, we first outline the specific plasticity mechanisms associated with the neuron-astrocyte network.

298 **Hebbian Plasticity:** Hebbian plasticity adjusts synaptic weights based on the co-activation of pre and postsynaptic neurons along with astrocytes. Two forms of Hebbian plasticity are modeled: (i) 299 Neuronal Hebbian Plasticity: The synaptic weight between these neurons,  $H_{neuron}$ , is updated 300 based on the co-activation of these neuron layers:  $H_{neuron,t} = H_{neuron,t-1} + \frac{1}{m}h_t^T o_t$ . where, m represents the number of neurons in the hidden layer for each token. We map this  $H_{neuron,t}$  to 301 302  $\theta(x_i) \cdot \theta(x_i)$  in the synaptic dynamics of our proposed macro-model (Eqn. 3), representing the inter-303 action between the activations of neurons i and j, capturing the essence of hebbian learning where 304 the connection strength increases as the neurons co-activate. (ii) Astrocytic Hebbian Plasticity: As-305 trocytes modulate synaptic efficacy through gliotransmitter release, which is modeled by the weight 306  $H_{astro}$ . This weight is updated as follows:  $H_{astro,t} = H_{astro,t-1} + \frac{1}{m}\phi(R)^T o_t$ , where R represents the astrocytic activity, influenced by calcium dynamics.  $\phi(R)$  reflects the indirect feedback 307 308 from astrocytes to postsynaptic neurons. We propose to associate  $H_{\text{astro}}$  with the term  $\psi(p_{ij}^s)$  in the 309 synaptic dynamics of the neuroscience macro-model, where the activation of  $p_{ii}^s$  ( $\psi(p_{ij}^s)$ ) processes 310 the inherent information of  $T_{ijkl}$ .

311 **Presynaptic Plasticity:** Presynaptic plasticity is influenced by the presynaptic activity (neurotrans-312 mitter release) and the astrocytic calcium dynamics, which regulates the release of neurotransmit-313 ters. The presynaptic plasticity parameter  $g_t$  is the link between these two entities that captures the 314 concentration of neurotransmitter in the synaptic cleft based on the neuron firing activity,  $x_i$  ( $x_i$  is 315 modulated by membrane potential,  $V_i$  in Eqn. 1). Thus,  $g_t$  accumulates the presynaptic activity as 316 input tokens are processed:  $g_t = g_{t-1} + h_t = g_{t-1} + \phi(k_t)$ . The non-linear response of astrocytes to presynaptic activity is modeled by raising this sum to the power of  $\alpha$ , a hyperparameter that encodes the non-linearity of calcium dynamics (Mia et al., 2023):  $g = \left(\sum_{t=1}^{N} \phi(k_t)\right)^{\alpha}$ . This 317 318 319 non-linear presynaptic plasticity reflects the slowing of calcium accumulation as presynaptic activity 320 intensifies. 321

Both plasticities are encoded sequentially in the write mode through keys and values. However, in the read mode, the queries are presented in a parallel manner, where  $Q = \begin{pmatrix} q_1 \\ q_2 \\ \vdots \\ q_N \end{pmatrix}$  is a matrix of shape  $\begin{array}{ll} 324 \\ R^{N \times d}, \text{ with } N \text{ representing the number of tokens and } d \text{ as the embedding dimension for each token.} \\ 325 \\ 326 \\ 326 \\ 326 \\ 327 \end{array}$ 

**Realization of Astromorphic Self-attention:** As discussed previously, after the Hebbian and presynaptic plasticities are encoded in the write mode, the read mode retrieves the stored information to compute self-attention. The hidden layer activates queries,  $(h = \phi(Q))$  and the encoded information is accessed through the combined hebbian weight H and the presynaptic plasticity parameter g. In Eqn. 6, H, which is the sum of both neuronal and astrocytic hebbian plasticities, captures the plasticities for all the N tokens, thus is represented by matrix form.

$$H = H_{neuron} + H_{astro} = \frac{1}{m} \left( \phi(K)^T V + \phi(R)^T V \right)$$
(6)

Here,  $\phi(R)$  captures the relative position information between tokens which we map to  $T_{ijkl}$  in the neuroscience macro-model. The read mode computes the calcium response  $C = hg^T$  and the weight P, modulated by astrocytic activity, is computed based on calcium response  $P = \frac{1}{C}$  for N tokens in Eqn. 7.

$$P = \frac{1}{\phi(Q) \left(\sum_{t=1}^{N} \phi(k_t)\right)^{\alpha}} \tag{7}$$

Finally, the output of the network during the read mode is computed by applying the learned hebbian weight H and the presynaptic weight P to the hidden-to-output layer connection, with a residual connection from the input layer:  $L = \phi(Q)(H \odot P) + I$ , where  $\odot$  denotes element-wise multiplication, and I = X represents the direct residual connection from the input layer. By integrating the Hebbian plasticity H and presynaptic plasticity P, we illustrate the final output of the astromorphic self-attention mechanism in Eqn. 8:

$$L = \frac{\phi(Q)(\phi(K)^{T}V + \phi(R)^{T}V)}{m \times \phi(Q) \sum_{t=1}^{N} [\phi(k_{t})]^{\alpha}} + X$$
(8)

To complete the transformer operation, layer normalization is applied to the self-attention output L, followed by a feedforward network (FFN) to produce the final logits in Eqn. 9.

$$Y = \text{LayerNorm}(L), \text{ logits} = \text{Softmax}(\text{Linear}(\text{FFN}(Y) + Y))$$
(9)

The final output logits represent the classification probabilities or other task-specific outputs, depending on the application of the astromorphic transformer.

355 **Spatial Mapping:** In the macro-model,  $T_{ijkl}$  is responsible for spatial encoding, which is utilized 356 through R in  $H_{astro}$ . We capture this spatial mapping by simulating the macro-model for various 357 spatial orientations of neurons in  $T_{ijkl}$  and tracking the resulting outputs of  $p_{ij}^s$ . Different spatial 358 configurations produce varying responses in  $p_{ij}^s$  and neuron spiking activity. However, when spatial distances remain constant,  $p_{ij}^s$  shows no variation, and neuron spiking activity remains uniform. So, 359 we can deduce an impact of relative spatial position on the neuron-astrocyte network that is mapped 360 by  $T_{iikl}$  to  $H_{astro}$  and then to R. Consequently, we establish a previously unexplored connec-361 tion between the neuroscience macro-model and relative positional encoding in astromorphic self-362 attention. Prior approaches did not explicitly investigate how short-term processes could be mapped to spatial information. By addressing this gap, we have enabled our model to exploit long-term pro-364 cesses for the integration of temporal information, achieving a more comprehensive representation 365 in our current approach. In the following sections, we explore the temporal integration of astrocytes 366 into astromorphic computing by introducing astrocytic memory as memory tokens. Additionally, 367 we propose the RMAAT architecture, which effectively handles long-context sequences using as-368 trocytic memories within a machine learning framework, incorporating an astrocytic compression 369 algorithm and the AMRB learning rule.

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# 3.3 TEMPORAL INTEGRATION OF ASTROCYTES IN TRANSFORMERS

Temporal integration in astrocytes originates from long-term tripartite synaptic plasticity, represented by the long-term astrocytic process parameter  $p_{ij}^l$  in Eqn. 5. The timescale  $\tau_p^l$ , being significantly longer than  $\tau_p^s$  in Eqn. 4, allows for extended retention of information. This accumulation of  $Ca^{2+}$  responses constitutes the long-term astrocytic process,  $p_{ij}^l$ , which gives rise to the concept of astrocytic memories. To incorporate this feature into transformer architectures, we introduce the notion of memory tokens based on these astrocytic processes. 378 Memory tokens: Memory tokens are designed 379 to persist through multiple processing stages 380 of serialized sequences. Traditional memoryaugmented transformer architectures initialize 382 and learn these tokens externally, passing them from one segment to another in segmented sequence propagation (Bulatov et al., 2022; Wu 384 et al., 2020). However, they often lack the 385 context needed to establish a cohesive mean-386 ing. These architectures incur greater compu-387 tational costs due to BPTT and external mem-388 ory initialization. In contrast, our approach 389 uses astrocytic memories as naturally integrated 390 tokens within the neuron-astrocyte network's 391 long-term processes, eliminating the need for 392 external initialization and reducing computational overhead.



Figure 3: Memory retention factor of astrocytes demonstrating the compression mechanism to emulate long-term plasticity based on the macromodel. The graph illustrates how the retention factor decreases as the number of segments (STP cycles) increases, indicating that more segments lead to higher compression for each segment.

Astrocytic Memory: Our proposed neuro-

science macro-model simulates the behavior of the synaptic facilitation  $s_{ij}$  and the long-term astrocytic process parameter,  $p_{ij}^l$ , which represents the astrocytic memory accumulation over time. This macro-model accounts for all the neural, synaptic, and astrocytic dynamics described in Eqns. 1 - 5. Based on the behavior of  $p_{ij}^l$  in Fig. 1, we observe that with repeated short-term plasticity (STP) events, the parameter gradually saturates, as calcium ions are finite, leading to a stabilized state in the calcium response. We model the behavior of  $p_{ij}^l$  by interpolating the LTP response from Fig. 1, allowing us to map bioplausibility onto the astrocytic memory tokens.

402 Based on the interpolated LTP dynamics in Fig. 1, we propose an algorithm that compresses stored 403 information by scaling the memory tokens. The compression is directly influenced by the number 404 of STP cycles encoded within a single LTP cycle. A model is fitted to the interpolated LTP curve, 405 where the area under the curve is normalized to 1, representing the total available  $Ca^{2+}$  ion con-406 centration. For each STP cycle, the  $Ca^{2+}$  response constitutes a fraction of this total calcium, with the fraction decreasing as the number of STP cycles increases. If all STP fractions are integrated, 407 they sum to the total  $Ca^{2+}$  ion concentration of 1. This fraction is termed the memory retention 408 factor, as it represents the  $Ca^{2+}$  ion concentration corresponding to the long-term astrocytic process 409 parameter,  $p_{ij}^{l}$ . This compressed astrocytic memory effectively manages long-range dependencies 410 without requiring external memory initialization, reducing computational overhead and improving 411 scalability. As the number of STP cycles increases, the memory retention factor decreases, resulting 412 in a more compressed form of astrocytic memory, as shown in Fig. 3. The number of STP cycles 413 corresponds to the number of segments used for a given machine learning dataset in RMAAT. The 414 approach for dividing long input sequences into multiple segments, based on the RMAAT's model 415 capacity, is explained in the next section.

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### 417 418 3.4 THE RECURRENT MEMORY AUGMENTED ASTROMORPHIC TRANSFORMER (RMAAT)

The Recurrent Memory Augmented Astromorphic Transformer (RMAAT) is specifically engineered
to effectively process lengthy sequences by partitioning them into smaller segments. The maximum
sequence length for each segment is established according to the model's token handling capacity.
These segments are then processed in a temporally recurring manner, beginning with the first segment. These segments map to the STP cycles in the neuroscience macro-model in Fig. 1. As the
RMAAT processes each segment, it utilizes the astrocytic memory compression algorithm discussed
above and propagates the compressed contexts in form of memory tokens, as depicted in Fig. 4.

Temporal Recurrence and Context Propagation: As subsequent segments are processed, the in herent compressed memory stored in the astrocytes facilitates the transition of context from one
 segment to the next. The recurrent nature of the processing guarantees that the context from prior
 segments is consistently transmitted, preserving a unified comprehension of the entire sequence. By
 employing this technique of connecting astrocytic memory tokens, the model is able to effortlessly
 include information from different segments, efficiently handling distant connections without sacrificing important contextual details. The time-unrolled diagram in Fig. 4 illustrates the progression

of compressed astrocytic memories throughout the sequence. The  $mem_t$  tokens represent the compressed memories, following the compression algorithm outlined in Fig. 3, where t denotes the identity of STP cycles, corresponding to the segments in RMAAT. Astrocytic memories also enable the development of an efficient learning algorithm by utilizing the stored memory tokens.

#### 436 Resource-Efficient Learning with AMRB:

437 The Recurrent Memory Augmented Astro-438 morphic Transformer (RMAAT) employs an 439 innovative approach to learning known as 440 Astrocytic Memory Replay Backpropagation 441 (AMRB), which draws inspiration from the 442 learning algorithms used by recurrent neural networks (Wu et al., 2020; Wan et al., 2023). 443 In AMRB, all memory tokens are saved and 444 replayed backward during the gradient calcu-445 lation phase (See Appendix A for the detailed 446 algorithm). AMRB aligns closely with biologi-447 cal systems through its use of localized compu-448 tation, where neurons and astrocytes interact lo-449 cally to manage memory and learning. Unlike 450 BPTT, which propagates information globally 451 across all time steps, AMRB leverages local-452 ized astrocytic memories that store compressed 453 information from previous interactions. This localized approach mirrors the way biological 454 systems handle information, as astrocytes mod-455 ulate synaptic activity based on local neural 456 activity without retaining the entire sequence 457 state. As a result, AMRB not only enhances 458 bio-plausibility but also significantly reduces 459



Figure 4: Illustration of the Recurrent Memory Augmented Astromorphic Transformer (RMAAT) processing through time unrolling. The diagram demonstrates how segments are processed sequentially with recurrent processing, where astrocytic memory  $(mem_t)$  flows from one segment to the next, preserving context throughout. Short-term plasticity (STP) modulates information within each segment, while long-term plasticity (LTP) supports the recurrent processing and memory flow.

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AMRB reduces hardware memory usage by a factor of five, significantly lowering the memory bur den during the backward pass. Additionally, as the memory tokens are stored inherently in astrocytes
 rather than externally provided, AMRB improves computational efficiency, running approximately
 15% faster than BPTT, which results in higher processing speeds without sacrificing accuracy.

4 Results

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In this section, we present the performance evaluation of RMAAT across two key benchmarks: the 470 IMDB dataset for sentiment classification (Maas et al., 2011) and the Long Range Arena (LRA) 471 for text classification (Tay et al., 2020). These benchmarks were chosen to assess the model's abil-472 ity to handle tasks requiring both short-term and long-term context understanding. The detailed 473 experimental setup is outlined in Appendix B. The models' performance was evaluated using key 474 metrics: accuracy, memory usage, and computational speed. Accuracy reflects the proportion of 475 correct predictions, indicating model performance. Memory utilization assesses hardware efficacy 476 during training and inference, while computational speed evaluates data processing in relation to the 477 Softmax Transformer baseline (1x). RMAAT's comparison with other transformers underscores its 478 enhanced precision and resource efficiency, particularly for long-range assignments.

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# 4.1 SENTIMENT CLASSIFICATION ON IMDB

To evaluate the performance of RMAAT on sentiment classification, we conducted experiments using the IMDB dataset. We used 256 as the maximum sequence length allowed for each RMAAT block depicted in Fig. 4. The results are summarized in Table 1, comparing the performance of various transformer models and memory-augmented variants (The hyperparameters are listed in Appendix C).

486 When processing a single 487 segment, the astromor-488 phic transformer demon-489 strates comparable per-490 formance to the Softmax and Linear Trans-491 formers. However, its 492 true advantage emerges 493 with longer sequences, 494 where the RMAAT out-495 performs both the RMT 496 and Linear Transformer 497 variants. Additionally, 498

Model	Seg- ments	Recur- rency	Accuracy (% ± std)	Memory (GB)	Speed
Softmax Transformer	1	No	$85.5 \pm 0.1$	6.1	1x
Astromorphic Transformer(Mia et al., 2023)	1	No	$85.8 \pm 0.2$	7.1	0.92x
Linear Transformer(Kozachkov et al., 2023a)	1	No	$85.7 \pm 0.2$	6.6	0.95x
Spike-Transformer(Mueller et al., 2021)	1*	No	86.36	-	-
Recurrent SNN (Wang et al., 2022)	1*	No	86.82	-	-
CoRNN (Rusch & Mishra, 2020)	1*	No	87.4	-	-
LSTM (Aswani et al., 2021)	1*	No	87.48	-	-
SNN (Agrawal et al., 2021)	1*	No	88.15	-	-
RMT variant (Softmax) (Bulatov et al., 2022)	6	Yes	$88.4 \pm 0.2$	20.2	1x
Linear Transformer	6	Yes	$88.2 \pm 0.2$	22.5	1.03x
RMAAT (Our Model)	6	Yes	88.9 ± 0.1	4.4	1.15x
* These models are not iso-architecture	and may 1	process lo	nger seauence	e lengths	

Table 1: IMDB Sentiment Classification Results

RMAAT shows significant memory efficiency, achieving approximately a fivefold reduction in mem-499 ory usage compared to other models while retaining superior contextual information. RMAAT also 500 processes data 15% faster than the RMT variant and 10% faster than the Linear Transformer. Com-501 pared to models like Spike-Transformer, Recurrent SNN, and LSTM, RMAAT offers clear advantages in both accuracy and efficiency. These models have varying architectures compared to ours as 502 they are taken from different literature. 503

# 4.2 TEXT CLASSIFICATION ON LONG RANGE ARENA BENCHMARK

The Long Range Arena 507 (LRA) benchmark eval-508 uates models on their 509 ability to handle long-510 range dependencies. 511 The text classification 512 task involves sequences 513 much longer than typical 514 benchmarks. making 515 it ideal for assessing RMAAT's capacity to 516 maintain context over 517 extended lengths. Se-518 quences were tokenized 519

Table 2: LRA Text 0	Classifi	cation	Results		
Model	Seg-	Recur-	Accuracy	Memor	ry <sub>Sneed</sub>
ments rency $(\% \pm std)$	(GB)	Specu			
Softmax Transformer (Mia et al., 2023)	1	No	$61.5 \pm 0.1$	6.3	1x
Astromorphic Transformer (Mia et al., 2023)	1	No	$61.5 \pm 0.1$	7.6	1.9x
Linear Transformer (Mia et al., 2023)	1	No	$61.0 \pm 0.1$	5.9	1.01x
Local Attention (Vaswani et al., 2017)	1*	No	52.98	-	-
Sparse Transformer (Child et al., 2019)	1*	No	63.58	-	-
Longformer (Beltagy et al., 2020)	1*	No	62.85	-	-
Linformer (Wang et al., 2020)	1*	No	53.94	-	-
Reformer (Kitaev et al., 2020)	1*	No	56.10	-	-
Synthesizer (Tay et al., 2021)	1*	No	61.68	-	-
BigBird (Zaheer et al., 2020)	1*	No	64.02	-	-
Performer (Choromanski et al., 2020)	1*	No	65.40	-	-
RMT variant (Softmax) (Bulatov et al., 2022)	8	Yes	$65.0 \pm 0.2$	24.0	1x
Linear Transformer	8	Yes	$64.8 \pm 0.1$	22.6	1.13x
RMAAT (Our Model)	8	Yes	$65.9 \pm 0.1$	5.1	1.5x
* These models are not iso-architecture	and may	process la	onger sequenc	e lengths	

at the byte level with up to 512 tokens per segment, and a total of 4096 tokens (8 segments). All 520 the hyperparameters are listed in Appendix C. Table 2 summarizes the results, comparing RMAAT 521 with other transformer models and memory-augmented variants on the LRA text dataset. In the 522 evaluation with 8 segments, RMAAT demonstrates superior performance, operating 50% faster 523 than the RMT variant and 30% faster than the Linear Transformer, while also significantly reducing 524 memory usage to 5.1 GB. Compared to other efficient transformers like Longformer, Linformer, 525 and Sparse Transformer, RMAAT excels in handling long-range dependencies with enhanced 526 computational efficiency. The inclusion of Astrocytic Memory Replay Backpropagation (AMRB) 527 strengthens the model's ability to manage complex, long-context sequences effectively, showcasing the impact of bioplausible mechanisms in transformer architectures. 528

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#### 5 CONCLUSIONS

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This research introduces the RMAAT, a transformer enhanced by bioplausible astrocytic mech-533 anisms. By integrating short and long-term astrocytic plasticity, RMAAT addresses long-range 534 dependencies in sequential data, outperforming standard transformers in both accuracy and effi-535 ciency. With AMRB, the model reduces memory usage and enhances computational speed, making 536 it well-suited for resource-limited systems. Moving forward, further biological inspiration, such as 537 astrocyte-astrocyte communication through gap junctions, can be explored as potential avenues to parallelize sequential processing and enhance computational efficiency. Future work can also ex-538 tend RMAAT to more challenging domains like computer vision and machine translation, aiming to 539 create more efficient, biologically inspired AI systems that closely emulate human cognition.

# 540 REFERENCES

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- Amogh Agrawal, Mustafa Ali, Minsuk Koo, Nitin Rathi, Akhilesh Jaiswal, and Kaushik Roy. Impulse: A 65-nm digital compute-in-memory macro with fused weights and membrane potential for spike-based sequential learning tasks. *IEEE Solid-State Circuits Letters*, 4:137–140, 2021.
- 545 Cristina M Alberini, Emmanuel Cruz, Giannina Descalzi, Benjamin Bessières, and Virginia Gao.
  546 Astrocyte glycogen and lactate: New insights into learning and memory mechanisms. *Glia*, 66
  547 (6):1244–1262, 2018.
- AR Aswani, Rohan Kumar, Jai Narayan Tripathi, and Alex James. Performance of crossbar based long short term memory with aging memristors. In 2021 IEEE 3rd International Conference on Artificial Intelligence Circuits and Systems (AICAS), pp. 1–4. IEEE, 2021.
- Malyaban Bal and Abhronil Sengupta. Sequence learning using equilibrium propagation. arXiv preprint arXiv:2209.09626, 2022.
- Sophia Becker, A. Nold, and T. Tchumatchenko. Modulation of working memory duration by synaptic and astrocytic mechanisms. *PLoS Computational Biology*, 18, 2022. doi: 10.1371/journal.pcbi.1010543.
- Guillaume Bellec, Franz Scherr, Anand Subramoney, Elias Hajek, Darjan Salaj, Robert Legenstein, and Wolfgang Maass. A solution to the learning dilemma for recurrent networks of spiking neurons. *Nature communications*, 11(1):3625, 2020.
- Iz Beltagy, Matthew E Peters, and Arman Cohan. Longformer: The long-document transformer.
   *arXiv preprint arXiv:2004.05150*, 2020.
  - K. Bohmbach, C. Henneberger, and J. Hirrlinger. Astrocytes in memory formation and maintenance. *Essays in biochemistry*, 2022. doi: 10.1042/EBC20220091.
- Aydar Bulatov, Yuri Kuratov, and M. Burtsev. Recurrent memory transformer. ArXiv, abs/2207.06881, 2022. doi: 10.48550/arXiv.2207.06881.
- Rewon Child, Scott Gray, Alec Radford, and Ilya Sutskever. Generating long sequences with sparse transformers. *arXiv preprint arXiv:1904.10509*, 2019.
- Krzysztof Choromanski, Valerii Likhosherstov, David Dohan, Xingyou Song, Andreea Gane, Tamas Sarlos, Peter Hawkins, Jared Davis, David Belanger, Lucy Colwell, et al. Masked language modeling for proteins via linearly scalable long-context transformers. *arXiv preprint arXiv:2006.03555*, 2020.
- Roberta de Ceglia, Ada Ledonne, David Gregory Litvin, Barbara Lykke Lind, Giovanni Carriero,
  Emanuele Claudio Latagliata, Erika Bindocci, Maria Amalia Di Castro, Iaroslav Savtchouk, Ilaria
  Vitali, et al. Specialized astrocytes mediate glutamatergic gliotransmission in the cns. *Nature*, 622
  (7981):120–129, 2023.
- Maurizio De Pittà, Mati Goldberg, Vladislav Volman, Hugues Berry, and Eshel Ben-Jacob. Glutamate regulation of calcium and ip 3 oscillating and pulsating dynamics in astrocytes. *Journal of biological physics*, 35:383–411, 2009.
- Peter U Diehl, Daniel Neil, Jonathan Binas, Matthew Cook, Shih-Chii Liu, and Michael Pfeiffer.
  Fast-classifying, high-accuracy spiking deep networks through weight and threshold balancing. In 2015 International joint conference on neural networks (IJCNN), pp. 1–8. ieee, 2015.
- Marie E Gibbs, Dana Hutchinson, and Leif Hertz. Astrocytic involvement in learning and memory
   consolidation. *Neuroscience & Biobehavioral Reviews*, 32(5):927–944, 2008.
- Lulu Gong, Fabio Pasqualetti, Thomas Papouin, and ShiNung Ching. Astrocytes as a mechanism for contextually-guided network dynamics and function. *PLOS Computational Biology*, 20(5): e1012186, 2024.
- A. A. González, A. Pazos, and A. Pazos. Computational models of neuron-astrocyte interactions lead to improved efficacy in the performance of neural networks. *Computational and Mathematical Methods in Medicine*, 2012, 2012. doi: 10.1155/2012/476324.

- 594 S. Gordleeva, Yuliya Tsybina, M. Krivonosov, I. Tyukin, Victor B. Kazantsev, Alexey Zaikin, and 595 Alexander N. Gorban. Situation-based neuromorphic memory in spiking neuron-astrocyte net-596 work. IEEE transactions on neural networks and learning systems, PP, 2023. doi: 10.1109/ 597 TNNLS.2023.3335450. 598 Susanna Yu Gordleeva, Yuliya A Tsybina, Mikhail I Krivonosov, Mikhail V Ivanchenko, Alexey A Zaikin, Victor B Kazantsev, and Alexander N Gorban. Modeling working memory in a spiking 600 neuron network accompanied by astrocytes. Frontiers in Cellular Neuroscience, 15:631485, 2021. 601 Zhuangyu Han and Abhronil Sengupta. Astrocyte regulated neuromorphic cpg control of legged 602 robotic locomotion. arXiv preprint arXiv:2312.15805, 2023. 603 604 Zhuangyu Han, ANM Nafiul Islam, and Abhronil Sengupta. Astromorphic self-repair of neuro-605 morphic hardware systems. In Proceedings of the AAAI Conference on Artificial Intelligence, 606 volume 37, pp. 7821-7829, 2023. 607 Jacques Kaiser, Hesham Mostafa, and Emre Neftci. Synaptic plasticity dynamics for deep continu-608 ous local learning (decolle). Frontiers in Neuroscience, 14:424, 2020. 609 610 Angelos Katharopoulos, Apoorv Vyas, Nikolaos Pappas, and François Fleuret. Transformers are 611 rnns: Fast autoregressive transformers with linear attention. In International Conference on Ma-612 chine Learning, pp. 5156–5165. PMLR, 2020. 613 Nikita Kitaev, Łukasz Kaiser, and Anselm Levskaya. Reformer: The efficient transformer. arXiv 614 preprint arXiv:2001.04451, 2020. 615 616 L. Kozachkov and K. Michmizos. A computational role for astrocytes in memory. arXiv: Neurons 617 and Cognition, 2017. 618 Leo Kozachkov and Konstantinos P Michmizos. Sequence learning in associative neuronal-619 astrocytic networks. In Brain Informatics: 13th International Conference, BI 2020, Padua, Italy, 620 September 19, 2020, Proceedings 13, pp. 349-360. Springer, 2020. 621 622 Leo Kozachkov, Ksenia V Kastanenka, and Dmitry Krotov. Building transformers from neurons and astrocytes. Proceedings of the National Academy of Sciences, 120(34):e2219150120, 2023a. 623 624 Leo Kozachkov, Jean-Jacques Slotine, and Dmitry Krotov. Neuron-astrocyte associative memory. 625 *arXiv preprint arXiv:2311.08135*, 2023b. 626 Qin Li. Astrocytes: The rising stars that regulate synaptic plasticity and long-term memory for-627 mation. In Synaptic Tagging and Capture: From Synapses to Behavior, pp. 309-320. Springer, 628 2024. 629 630 Yue-Xian Li and John Rinzel. Equations for InsP3 receptor-mediated  $Ca^{2+}$  i oscillations derived 631 from a detailed kinetic model: a Hodgkin-Huxley like formalism. Journal of theoretical Biology, 632 166(4):461-473, 1994. 633 Justin Lines. Astrocytes integrate time and space. Neural Regeneration Research, 20(2):467–468, 634 2025. 635 636 Sen Lu and Abhronil Sengupta. Deep unsupervised learning using spike-timing-dependent plastic-637 ity. *Neuromorphic Computing and Engineering*, 4(2):024004, 2024. 638 Andrew Maas, Raymond E Daly, Peter T Pham, Dan Huang, Andrew Y Ng, and Christopher Potts. 639 Learning word vectors for sentiment analysis. In Proceedings of the 49th annual meeting of the 640 association for computational linguistics: Human language technologies, pp. 142–150, 2011. 641 Md Zesun Ahmed Mia et al. Delving deeper into astromorphic transformers. arXiv preprint 642 arXiv:2312.10925, 2023. 643 644 Rogier Min, Mirko Santello, and Thomas Nevian. The computational power of astrocyte mediated 645 synaptic plasticity. Frontiers in computational neuroscience, 6:93, 2012. 646
- 647 Gianluigi Mongillo, Omri Barak, and Misha Tsodyks. Synaptic theory of working memory. *Science*, 319(5869):1543–1546, 2008.

648 649 650	Etienne Mueller, Viktor Studenyak, Daniel Auge, and Alois Knoll. Spiking transformer networks: A rate coded approach for processing sequential data. In 2021 7th International Conference on Systems and Informatics (ICSAI), pp. 1–5. IEEE, 2021.
652 653	Suhita Nadkarni and Peter Jung. Dressed neurons: modeling neural-glial interactions. <i>Physical biology</i> , 1(1):35, 2004.
654 655 656	Suhita Nadkarni and Peter Jung. Modeling synaptic transmission of the tripartite synapse. <i>Physical biology</i> , 4(1):1, 2007.
657 658	Marta Navarrete and Alfonso Araque. Endocannabinoids potentiate synaptic transmission through stimulation of astrocytes. <i>Neuron</i> , 68(1):113–126, 2010.
659 660 661	Maiken Nedergaard, Bruce Ransom, and Steven A Goldman. New roles for astrocytes: redefining the functional architecture of the brain. <i>Trends in Neurosciences</i> , 26(10):523–530, 2003.
662 663 664	Emre O Neftci, Hesham Mostafa, and Friedemann Zenke. Surrogate gradient learning in spiking neural networks: Bringing the power of gradient-based optimization to spiking neural networks. <i>IEEE Signal Processing Magazine</i> , 36(6):51–63, 2019.
665 666 667	J. Oliveira and A. Araque. Astrocyte regulation of neural circuit activity and network states. <i>Glia</i> , 70:1455 – 1466, 2022. doi: 10.1002/glia.24178.
668 669 670	Hao Peng, Nikolaos Pappas, Dani Yogatama, Roy Schwartz, Noah A Smith, and Lingpeng Kong. Random feature attention. <i>arXiv preprint arXiv:2103.02143</i> , 2021.
671 672	Gertrudis Perea, Mriganka Sur, and Alfonso Araque. The tripartite synapse: astrocytes process and control synaptic information. <i>Trends in Neurosciences</i> , 32(8):421–431, 2009.
673 674 675 676	Nelson A. Perez-Catalan, C. Doe, and Sarah D. Ackerman. The role of astrocyte-mediated plasticity in neural circuit development and function. <i>Neural Development</i> , 16, 2021. doi: 10.1186/s13064-020-00151-9.
677 678	Michael Pfeiffer and Thomas Pfeil. Deep learning with spiking neurons: opportunities and challenges. <i>Frontiers in neuroscience</i> , 12:409662, 2018.
679 680 681	M. Pittà, N. Brunel, and A. Volterra. Astrocytes: Orchestrating synaptic plasticity? <i>Neuroscience</i> , 323:43–61, 2015. doi: 10.1016/j.neuroscience.2015.04.001.
682 683 684	<ul> <li>Ana B. Porto-Pazos, Noha Veiguela, P. Mesejo, M. Navarrete, Alberto Alvarellos, Óscar Ibáñez,</li> <li>A. Pazos, and A. Araque. Artificial astrocytes improve neural network performance. <i>PLoS ONE</i>,</li> <li>6, 2011. doi: 10.1371/journal.pone.0019109.</li> </ul>
685 686 687 688	Dimitry E Postnov, RN Koreshkov, Nadezda A Brazhe, Alexey R Brazhe, and Olga V Sosnovtseva. Dynamical patterns of calcium signaling in a functional model of neuron–astrocyte networks. <i>Journal of biological physics</i> , 35:425–445, 2009.
689 690 691	T Konstantin Rusch and Siddhartha Mishra. Coupled oscillatory recurrent neural network (cornn): An accurate and (gradient) stable architecture for learning long time dependencies. <i>arXiv preprint</i> <i>arXiv:2010.00951</i> , 2020.
692 693 694 695	Yi Tay, Mostafa Dehghani, Samira Abnar, Yikang Shen, Dara Bahri, Philip Pham, Jinfeng Rao, Liu Yang, Sebastian Ruder, and Donald Metzler. Long range arena: A benchmark for efficient transformers. <i>arXiv preprint arXiv:2011.04006</i> , 2020.
696 697 698	Yi Tay, Dara Bahri, Donald Metzler, Da-Cheng Juan, Zhe Zhao, and Che Zheng. Synthesizer: Re- thinking self-attention for transformer models. In <i>International conference on machine learning</i> , pp. 10183–10192. PMLR, 2021.
700 701	Ashish Vaswani, Noam Shazeer, Niki Parmar, Jakob Uszkoreit, Llion Jones, Aidan N Gomez, Łukasz Kaiser, and Illia Polosukhin. Attention is all you need. <i>Advances in neural information processing systems</i> , 30, 2017.

702 Vladislav Volman, Eshel Ben-Jacob, and Herbert Levine. The astrocyte as a gatekeeper of synaptic 703 information transfer. Neural computation, 19(2):303-326, 2007. 704 John Wade, Liam J McDaid, Jim Harkin, Vincenzo Crunelli, and Scott Kelso. Self-repair in a 705 bidirectionally coupled astrocyte-neuron (AN) system based on retrograde signaling. Frontiers in 706 computational neuroscience, 6:76, 2012. 707 708 John J Wade, Liam J McDaid, Jim Harkin, Vincenzo Crunelli, and JA Scott Kelso. Bidirectional cou-709 pling between astrocytes and neurons mediates learning and dynamic coordination in the brain: a 710 multiple modeling approach. *PloS one*, 6(12):e29445, 2011. 711 712 Zhen Wan, Xiao Wang, Cheng Liu, Syed Alam, and Yi Zheng. Efficient large language models: 713 A survey. arXiv preprint arXiv:2306.15497, 2023. URL https://www.researchgate. 714 net/profile/Mi-Zhang-13/publication/376796054\_Efficient\_ Large\_Language\_Models\_A\_Survey/links/65e87d87c3b52a11701b815c/ 715 Efficient-Large-Language-Models-A-Survey.pdf. 716 717 Sinong Wang, Belinda Z Li, Madian Khabsa, Han Fang, and Hao Ma. Linformer: Self-attention 718 with linear complexity. arXiv preprint arXiv:2006.04768, 2020. 719 720 Zijian Wang, Yanting Zhang, Haibo Shi, Lei Cao, Cairong Yan, and Guangwei Xu. Recurrent spik-721 ing neural network with dynamic presynaptic currents based on backpropagation. International 722 Journal of Intelligent Systems, 37(3):2242–2265, 2022. 723 Qingyang Wu, Zhenzhong Lan, Jing Gu, and Zhou Yu. Memformer: The memory-augmented 724 transformer. ArXiv, abs/2010.06891, 2020. 725 726 Manzil Zaheer, Guru Guruganesh, Kumar Avinava Dubey, Joshua Ainslie, Chris Alberti, Santiago 727 Ontanon, Philip Pham, Anirudh Ravula, Qifan Wang, Li Yang, et al. Big bird: Transformers for 728 longer sequences. Advances in neural information processing systems, 33:17283–17297, 2020. 729

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# A ASTROCYTIC MEMORY REPLAY BACKPROPAGATION (AMRB)

This algorithm describes the Astrocytic Memory Replay Backpropagation (AMRB), which efficiently manages and updates memory states across multiple segments. By leveraging the bioplausible properties of astrocytes, AMRB ensures the preservation and propagation of context throughout the network, thereby enhancing the model's ability to handle long-range dependencies. The algorithm is outlined in Alg. 1.

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# **B** EXPERIMENT SETUP

741 Hardware Specifications & Network Architecture: All experiments were conducted on a server 742 equipped with Linux 5.15.0-113-generic x86\_64 with glibc2.31. The server featured an AMD EPYC 743 7742 64-Core Processor with 32 CPU cores, 1TB of RAM, and 8 NVIDIA RTX A5000 GPUs, each 744 with 24GB of memory. The RMAAT network architecture, depicted in Fig. 4, can have varying 745 numbers of encoder layers depending on the ML task. The model leverages the inherent memory 746 and processing capabilities of astrocytes, with recurrent processing as depicted in Fig. 4. The 747 specific hyperparameters, such as the number of layers, heads, and size of the hidden states, etc. are detailed in the supplementary section. 748

749 Datasets: The IMDB dataset consists of 50,000 movie reviews, split evenly into 25,000 training
 750 and 25,000 testing samples. Each review is labeled as either positive or negative, providing a bal 751 anced dataset for sentiment classification. This dataset is particularly useful for evaluating how well
 752 models can capture and retain context over relatively long sequences, as movie reviews often con 753 tain nuanced and varied language. The LRA benchmark includes several tasks designed to test the
 754 ability of models to handle long-range dependencies. For the text classification task, sequences are
 rs55 significantly longer than those in standard benchmarks, making it an ideal test for evaluating the
 RMAAT's capability to maintain context over extended lengths.

756				
757	Algorithm 1: Astrocy	tic Memory Replay Backpropagation (A	MRB)	
758	<b>Input:</b> $rollout = [x_0, $	$x_1, \ldots, x_T$ ]: A list containing each time	estep t's input	$\overline{x_t}$
759	Input: prev_memory	: Memory from the previous rollout	1 1	U
760	<b>Result:</b> Updated mem	ory for the next rollout		
761	1 Initialize $replay_buf$	fer = [];		
762	2 Append prev_memor	y to $replay\_buffer;$		
763	3 Forward Pass:;			
764	4 for $t = 0, 1, 2, \dots, T$	— 1 <b>do</b>		
765	5   $m_{t+1} = \operatorname{Model}(x_t)$	$(m_t);$ // N	o gradien	t computation
766	6 $m_{t+1} = \text{astro}\_\text{men}$	$m_{\text{retention}}(m_{t+1});$ // A	pply astr	ocytic memory
767	retention			
760	7   Append $m_{t+1}$ to r	eplay_buffer;		
700	8 end			
769	9 Backward Pass:;			
770	10 Initialize $\nabla m_{t+1} = 0$			
771	11 for $t = T, T - 1, \ldots,$	0 <b>do</b>		
772	12 $m_{t+1}, o_t = \text{Model}$	$l(x_t, m_t);$	// Reco	mpute outputs
773	13 Compute $loss = 1$	oss_function $(o_t)$ ;		
774	14   Perform backprop	agation loss.backward();	· ·	
775	15   Backpropagate thr	ough memory $m_{t+1}$ .backward( $\nabla m_{t+1}$ )	); //	Compute $ abla m_t$
776	16 end			
777	17 Save $m_T$ for the next 1	rollout's update;		
778				
779				
780	-			
781		Table S1: Neuroscience Macro-model Hy	yperparameter	S
782		Parameter	Value	
783		Network Details	0	
784		Number of presynaptic neurons	3	
785		Number of presynaptic neurons	3	
705		Number of astrocytes	1	
700		Timescale	300 s	
/8/		limestep, dt	$0.04 \ s$	
788		Neural Dynamics		
789		Neural dynamics timescale, $\tau_n$	0.5 s	
790		Membrane potential threshold, $V_{th}$	1 mV	
791		Reset potential, V <sub>reset</sub>	-1 mV	
792		Decay parameter, $\lambda$	0.2	
793		Bias parameter, b		
794		Non-linearity, $\phi$	tanh	
795		Synaptic Dynamics	0.75	
796		Synaptic dynamics timescale, $\tau_s$	0.75 s	
797		Decay parameter, $\beta$	0.25	
798		Bias parameter, c	0	
799		Non-linearity, $\theta$	tanh	
800		Astrocytic STP Dynamics		
801		Short-term astrocytic process dynam-	1 s	
001		ics timescale , $\tau_p^s$		
002		Decay parameter, $\gamma^s$	0.2	
803		Bias parameter, d	0	
804		Non-linearity, $\psi$	tanh	
805		Astrocytic LTP Dynamics		
806		Long-term astrocytic process dynam-	6.8	
807		ics timescale , $ au_p^l$	0.8	
808		Decay parameter, $\gamma^l$	0.1	
809		Non-linearity, $\kappa$	sigmoid	

#### С HYPERPARAMETER DETAILS

We develop the neuroscience macro-model and simulate the neural, synaptic and short and long-term astrocytic dynamics to realize the neuroscience-algorithm co-design framework achieved by the RMAAT structure. Table S1 shows the hyperparameters involved in simulating the model. For the RMAAT framework, Table S2 presents the hyperparameters used for training and evaluating the IMDB Dataset, while Table S3 details the hyperparameters for the LRA Text Dataset.

Table S2: IMDB Dataset Hyperpar	ameters
Parameter	Value
Training Parameters	
Batch size	64
Maximum sequence length in a segment, $N$	256
Number of epochs	20
Learning rate	$1.5e^{-5}$
Model Architecture	
Embedding dimension, d	768
Number of heads	6
Number of neurons of feed forward network	1024
Number of encoder layers	3
Dropout	0.1
AMRB Parameters	
Number of segments	6
Number of memory tokens	32
Astromorphic Self-Attention Parame	eters
Hidden layer neuron number, m	100
Nonlinearity, $\alpha$	0.25

Parameter	Value
Training Parameters	
Batch size	64
Maximum sequence length in a seg-	519
ment, N	012
Number of epochs	40
Learning rate	$1.2e^{-}$
Model Architecture	
Embedding dimension, d	256
Number of heads	2
Number of neurons of feed forward	1094
network	1024
Number of encoder layers	1
Dropout	0.1
AMRB Parameters	
Number of segments	8
Number of memory tokens	32
Astromorphic Self-Attention Parame	eters
Hidden layer neuron number, m	100
Nonlinearity, $\alpha$	0.25