Context-aware Learned Mesh-based Simulation via Trajectory-Level Meta-Learning

Anonymous authors
Paper under double-blind review

Abstract

Simulating object deformations is a critical challenge across many scientific domains, including robotics, manufacturing, and structural mechanics. Learned Graph Network Simulators (GNSs) offer a promising alternative to traditional mesh-based physics simulators. Their speed and inherent differentiability make them particularly well suited for applications that require fast and accurate simulations, such as robotic manipulation or manufacturing optimization. However, existing learned simulators typically rely on single-step observations, which limits their ability to exploit temporal context. Without this information, these models fail to infer, e.g., material properties. Further, they rely on auto-regressive rollouts, which quickly accumulate error for long trajectories. We instead frame mesh-based simulation as a trajectory-level meta-learning problem. Using Conditional Neural Processes, our method enables rapid adaptation to new simulation scenarios from limited initial data while capturing their latent simulation properties. We utilize movement primitives to directly predict fast, stable and accurate simulations from a single model call. The resulting approach, Movement-primitive Meta-Meshgraphnet (M3GN), provides higher simulation accuracy at a fraction of the runtime cost compared to state-of-the-art GNSs across several tasks.

1 Introduction

The simulation of complex physical systems is crucial to a wide variety of engineering disciplines, including solid mechanics (Yazid et al., 2009; Zienkiewicz & Taylor, 2005; Stanova et al., 2015), fluid dynamics (Chung, 1978; Zienkiewicz et al., 2013; Connor & Brebbia, 2013), and electromagnetism (Jin, 2015; Polycarpou, 2022; Reddy, 1994). In particular, the simulation of object deformations under external forces finds widespread application in, e.g., robotic applications (Scheikl et al., 2022; Wang & Zhu, 2023; Linkerhägner et al., 2023). Mesh-based simulations are appealing for such problems due to the computational efficiency and accuracy of the underlying finite element method (Brenner & Scott, 2008; Reddy, 2019). However, the diversity of the problems to be modeled usually demands task-specific simulators in order to accurately capture the relevant physical quantities (Reddy & Gartling, 2010). Such specialized simulators can be slow and cumbersome to use, especially for large-scale simulations (Paszynski, 2016; Hughes et al., 2005).

Thus, data-driven surrogate models trained on reference simulations have become an appealing alternative (Guo et al., 2016; Da Wang et al., 2021; Li et al., 2022). Among them, general-purpose Graph Network Simulators (GNSs) have recently become increasingly popular (Battaglia et al., 2018; Pfaff et al., 2021; Allen et al., 2022b; 2023; Lippe et al., 2023; Linkerhägner et al., 2023; Yu et al., 2024; Würth et al., 2025). GNSs encode the simulated system as a graph of interacting entities whose dynamics are predicted using GNNs (Bronstein et al., 2021). GNS are one to two orders of magnitude faster than classical simulators (Pfaff et al., 2021) while being fully differentiable. These properties make them highly effective for, e.g., inverse design problems (Allen et al., 2022b; Xu et al., 2021), robotics (Shi et al., 2023; Hoang et al., 2025), and other engineering applications that benefit from fast simulation surrogates (Simon, 2021). However, existing GNS-based models rarely exploit historical context, limiting their ability to infer material properties or long-term system behavior.

Consider, for example, a robotic manipulation task, where the robot needs to maintain an accurate model of some deformable object with unknown material properties to achieve a certain goal (Antonova et al.,

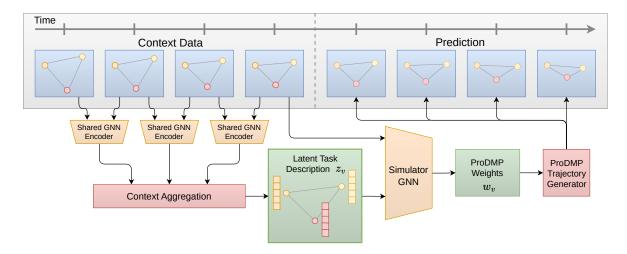


Figure 1: Movement-Primitive Meta-MESHGRAPHNET (M3GN) aims to learn accurate simulation dynamics from a few initial observations, enabling it to infer material properties from limited historical data. Given a context set of initial system states, node-level latent features are computed for every pair of states using a shared Graph Neural Network (GNN) encoder. These features are then aggregated to form a node-level latent task description z_v . This description is concatenated with the last system state to predict Probabilistic Dynamic Movement Primitive (ProDMP) weights, which are used to compute per-node trajectories.

2022; Shi et al., 2023; Hoang et al., 2025). Current learned models rely mainly on the current observation, preventing them from using the historical context to infer knowledge about the material or other relevant behaviors (Linkerhägner et al., 2023). To alleviate this issue, we propose to provide a few initial mesh states to learned simulators, allowing the model to observe how the given system behaves before having to simulate subsequent steps. Equipped with this knowledge, the model may infer latent material properties, facilitating for more accurate simulations that precisely extend the previous context. To the best of our knowledge, we are the first to study this specific experimental setup.

This setting naturally fits into a meta-learning framework (Schmidhuber, 1992; Thrun & Pratt, 1998; Vilalta & Drissi, 2005; Hospedales et al., 2022), where the sequence of initial states induces the unique task of predicting its subsequent simulated trajectory. Concretely, we employ Conditional Neural Processs (CNPs) (Garnelo et al., 2018a) to aggregate the provided context sets and the dynamics inferred from them into a latent descriptor, which is then used to predict the rest of the trajectory. This formulation reveals opportunities to better adapt the standard GNS training setup to meta-learning scenarios, particularly when models must condition on initial context.

GNSs are typically trained through simple next-step supervision (Battaglia et al., 2018; Pfaff et al., 2021; Allen et al., 2023). During inference, entire trajectories are simulated by iteratively predicting per-node dynamics from an initial system state in an autoregressive manner, only ever considering the previous system state or a fixed-size history. This approach is prone to error accumulation over time, decreasing accuracy for longer time horizons (Brandstetter et al., 2022; Han et al., 2022; Radler et al., 2025).

Since the initial context set influences the full trajectory, we decide to utilize trajectory-level predictions, where our model consumes the context steps and directly outputs the remaining simulation in a single forward pass. This formulation offers several advantages over alternatives such as recurrent architectures (Hochreiter & Schmidhuber, 1997; Ruiz et al., 2020; Mienye et al., 2024) or multi-step training (Shi et al., 2023). By predicting the entire trajectory in a single forward pass, we improve training stability and memory efficiency by avoiding gradient updates across multiple passes. This single-pass approach also increases inference speed and completely sidesteps the error accumulation common in autoregressive rollouts.

To this end, we employ node-level Probabilistic Dynamic Movement Primitives (ProDMPs) (Schaal, 2006; Paraschos et al., 2013; Li et al., 2023), which allow us to output complete trajectories using only the latent descriptor as inputs. By representing trajectories with basis functions, ProDMPs neither require autoregressive

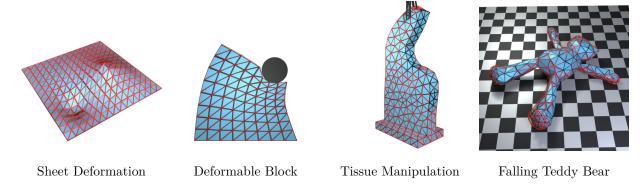


Figure 2: Final M3GN simulation steps for different evaluation tasks. From left to right: a sheet deforms under two orthogonal forces, a falling collider deforming a block in 2D, a surgical tool dragging tissue, and a falling teddy bear. All visualizations present the **predicted mesh** (blue) alongside a reference **wireframe** (red) of the ground-truth simulation. M3GN takes the deformable object positions from a few initial time steps to predict the remaining simulation steps using per-node movement primitives.

rollouts, which is costly and error-prone for long horizons, nor large memory for constructing temporal convolutions, unlike prior works (Dahlinger et al., 2025; Xu et al., 2024; Cini et al., 2025). These components enable efficient training and rapid adaptation to trajectory-specific simulation parameters, such as unknown material properties, without requiring explicit parameter knowledge during training or inference.

The resulting method, called Movement-Primitive Meta-MeshGraphNet (M3GN), allows the generation of context-dependent simulation trajectories that accurately infer and integrate unknown system properties. Figure 1 provides an overview of our approach, while Figure 2 shows examples for different tasks. To validate the effectiveness of M3GN, we adapt existing experiment suites (Linkerhägner et al., 2023; Dahlinger et al., 2025) to our trajectory-based meta-learning setup, and additionally introduce two novel tasks based on challenging deformable object simulations with varying object materials. Our results show that our method provides superior simulation accuracy compared to several variants of MeshGraphNet (MGN) (Pfaff et al., 2021) and recent trajectory-based learned simulators (Xu et al., 2024; Dahlinger et al., 2025)¹. Further, M3GN's ProDMPs trajectory representation reduces the number model calls at inference, improving inference runtime by up to 32 times compared to MGN.

In summary, we propose M3GN, a novel GNS that (i) extracts a latent descriptor from initial states and uses it to generate the remaining node-level trajectory in a single shot, while rapidly adapting to varying material properties; (ii) achieves state-of-the-art inference speed by coupling CNP-based context aggregation with a physically consistent trajectory formulation via ProDMPs; and (iii) surpasses recent GNSs on challenging deformation benchmarks, yielding superior long-horizon accuracy and stability. To support our claims, we introduce a new experimental setup in which the initial part of each trajectory serves as context data for the model.

2 Related Work

Graph Network Simulators. Deep neural networks for physical simulations can provide significant speedups over traditional simulators while being fully differentiable (Pfaff et al., 2021; Allen et al., 2022a), making them a natural choice for applications like model-based Reinforcement Learning (Mora et al., 2021) and Inverse Design problems (Baqué et al., 2018; Durasov et al., 2021; Allen et al., 2022a). A popular class of learned neural simulators are Graph Network Simulators (GNSs) (Battaglia et al., 2016; Sanchez-Gonzalez et al., 2020). GNSs utilize Message Passing Networks (MPNs), a special type of GNN (Scarselli et al., 2009; Bronstein et al., 2021) that representationally encompasses the function class of many classical solvers (Brandstetter et al., 2022). GNS handle physical data by modeling arbitrary entities and their relations as a graph. Applications

 $^{^{1}}$ Code is provided in the supplement. Here, the reviewers can also find videos showing the qualitative results of M3GN predictions and comparisons to existing baselines.

of GNSs include particle-based simulations (Li et al., 2019; Sanchez-Gonzalez et al., 2020; Whitney et al., 2023), atomic force prediction (Hu et al., 2021), and fluid dynamic problems (Brandstetter et al., 2022). These models have additionally been applied to the mesh-based prediction of deformable objects (Pfaff et al., 2021; Weng et al., 2021; Han et al., 2022; Fortunato et al., 2022; Linkerhägner et al., 2023). Recent extensions handle rigid objects (Allen et al., 2022b; 2023; Lopez-Guevara et al., 2024) and integrate learned adaptive meshing strategies (Plewa et al., 2005; Freymuth et al., 2023; 2025) into the simulator (Wu et al., 2023).

Existing work that considers unknown material properties in simulations of deformable objects combines the GNS prediction with point cloud information to improve long-term predictions Linkerhägner et al. (2023). This method requires a constant stream of point clouds to ground the simulation in, but can not aggregate this information into a description of the material properties. Additionally, the DEL method (Wang et al., 2024) integrates physical priors from the Discrete Element Analysis (DEA) framework with learnable graph kernels, addressing the challenges of simulating 3D particle dynamics from 2D images.

In the context of larger-scale simulations, foundation models are gaining traction in neural simulation tasks, as exemplified by Aurora (Bodnar et al., 2024), a large-scale model trained on extensive climate data. While Aurora demonstrates impressive performance on atmospheric predictions, including global air pollution and weather forecasts, it requires significantly more data for fine-tuning compared to our approach, which focuses on efficient adaptation with fewer data points. Notably, all previously mentioned GNSs predict system dynamics iteratively from a given state, whereas we directly estimate entire trajectories, improving rollout stability and reducing function calls. Related to our approach is the Equivariant Graph Neural Operator (EGNO) (Xu et al., 2024), which also predicts full trajectories using SE(3) equivariance to model 3D dynamics and capture spatial and temporal correlations.

All previously discussed approaches rely on supervised learning or fine-tuning large foundation models, whereas we employ meta-learning to enable efficient adaptation to new simulation conditions. Recently, the Meta Neural Graph Operator (MaNGO) (Dahlinger et al., 2025) introduced meta-learning into Graph Network Simulators. Our work differs in several key aspects: MaNGO requires access to simulation parameters at least for the training set, while our method remains fully parameter-agnostic during both training and inference. Moreover, the meta-learning setup in MaNGO uses different simulation trials with the same material properties as context, whereas we exploit the temporal evolution within a single simulation to infer latent material characteristics. Finally, MaNGO's trajectory representation is less memory-efficient, as it does not employ a compact formulation such as ProDMPs.

Meta-Learning. Meta-learning (Schmidhuber, 1992; Thrun & Pratt, 1998; Vilalta & Drissi, 2005; Hospedales et al., 2022) extracts inductive biases from a training set of related tasks in order to increase data efficiency on unseen tasks drawn from the same task distribution. In contrast to other multi-task learning methods, such as transfer learning (Krizhevsky et al., 2012; Golovin et al., 2017; Zhuang et al., 2020), which merely fine-tune or combine standard single-task models, meta-learning makes the multi-task setting explicit in the model architecture (Bengio et al., 1991; Ravi & Larochelle, 2017; Andrychowicz et al., 2016; Volpp et al., 2019; Santoro et al., 2016; Snell et al., 2017). This explicit architecture allows the resulting meta-models to learn how to learn new tasks from a small number of example contexts. A popular variant is Model-Agnostic Meta-Learning (MAML) (Finn et al., 2017; Grant et al., 2018; Finn et al., 2018; Kim et al., 2018), which employs standard single-task models and formulates a multi-task optimization procedure.

Neural Processes (NPs) (Garnelo et al., 2018a;b; Kim et al., 2019; Gordon et al., 2019; Louizos et al., 2019; Volpp et al., 2021; 2023) instead build on a multi-task model architecture (Heskes, 2000; Bakker & Heskes, 2003) but employ standard gradient based optimization algorithms (Kingma & Ba, 2015; Kingma & Welling, 2014; Rezende et al., 2014; Zaheer et al., 2017). Here, we use Conditional Neural Processes (CNPs) (Garnelo et al., 2018a), which aggregate learned features over a variable-sized context set to yield a latent task description that our downstream GNS is conditioned on. Compared to regular NPs, CNPs assume a deterministic task description, eliminating the need for a distribution over latent variables. This assumption simplifies and accelerates the training process, as our objective is to predict a single precise simulation trajectory from the context set. While epistemic uncertainty cannot be fully eliminated, the simulation data itself is deterministic and lacks aleatoric noise, making a distributional latent formulation less appealing and inconsistent with the probabilistic assumptions that motivate Neural Processes.

3 Movement-Primitive Meta-MeshGraphNets

In this section, we present the theoretical foundation of the M3GN method, detailing the algorithmic design choices that guided its development.

Graph Network Simulators. Consider a graph $\mathcal{G} = (\mathcal{V}, \mathcal{E}, \mathbf{X}_{\mathcal{V}}, \mathbf{X}_{\mathcal{E}})$ with nodes \mathcal{V} , edges \mathcal{E} , and associated vector-valued node and edge features $\mathbf{X}_{\mathcal{V}}$ and $\mathbf{X}_{\mathcal{E}}$. An MPN (Sanchez-Gonzalez et al., 2020; Pfaff et al., 2021) consists of M message passing steps, which iteratively update the node and edge features based on the graph topology. Each such step is given as

$$\begin{split} \mathbf{h}_e^{m+1} &= f_{\mathcal{E}}^m(\mathbf{h}_v^m, \mathbf{h}_e^m), \\ \mathbf{h}_v^{m+1} &= f_{\mathcal{V}}^m(\mathbf{h}_v^m, \bigoplus_{e \in \mathcal{E}_v} \mathbf{h}_e^{m+1}), \end{split}$$

where \mathbf{h}_v^m and \mathbf{h}_e^m denote embeddings of the system state per node and edge at message passing iteration m, respectively. $\mathcal{E}_v \subset \mathcal{E}$ are the edges connected to v. Further, \bigoplus denotes a permutation-invariant aggregation operation such as the sum, the max, or the mean. The functions $f_{\mathcal{V}}^m$ and $f_{\mathcal{E}}^m$ are learned Multilayer Perceptrons (MLPs). The network's final output are the node-wise learned representations $\mathbf{h}_v := \mathbf{h}_v^M$ that encode local information of the initial node and edge features.

Conventional GNSs encode the state of the simulated system as a graph, feed it through the MPN, and interpret the per-node outputs as velocities or accelerations (Pfaff et al., 2021). These dynamics are used to forward the simulation in time using, e.g., a forward-Euler integrator (Sanchez-Gonzalez et al., 2020). The graph encodes relative distances and velocities between entities instead of absolute ones, as the resulting equivariance to translation improves generalization (Sanchez-Gonzalez et al., 2020). GNSs usually minimize a next-step Mean Squared Error (MSE) per node during training, adding carefully tuned implicit denoising strategies (Pfaff et al., 2021; Brandstetter et al., 2022) to stabilize long-term predictions. During inference, they compute trajectories by iteratively predicting and integrating their output in an autoregressive fashion. If some simulated objects, like the collider, are known, only the remaining nodes are predicted. Our method instead uses a ProDMP to predict a compact representation of a whole trajectory per system node.

Probabilistic Dynamic Movement Primitives. Movement Primitives (MPs) (Schaal, 2006; Paraschos et al., 2013) allow for compact and smooth trajectory representations y via a set of basis functions parameterized by a set of weights w. This temporal smoothness is highly beneficial for, e.g., robotic applications (Li et al., 2024; Otto et al., 2022). Recent methods integrate MPs with neural networks to enhance their expressive capabilities (Seker et al., 2019; Bahl et al., 2020; Li et al., 2023). Dynamic Movement Primitives (DMPs) (Schaal, 2006) use a spring-damper dynamical system governed by parameters α and β . To manipulate the trajectory, an external forcing term f is added, before the system converges to a predefined goal g:

$$\tau^2 \ddot{y} = \alpha \left(\beta (g - y) - \tau \dot{y} \right) + f(x), \quad f(x) = x \varphi^{\mathsf{T}} w. \tag{1}$$

Here, τ influences execution speed, while f depends on the basis functions φ in force-space, the weights w and the exponential decaying phase x. Solving this equation typically is computationally intensive, particularly when the gradient dy/dw is required (Bahl et al., 2020). ProDMPs (Li et al., 2023) instead solve Equation (7) with pre-computed basis functions Φ in position-space as

$$y(t) = c_1 y_1(t) + c_2 y_2(t) + \mathbf{\Phi}(t)^{\top} \mathbf{w}.$$

The term $c_1y_1(t) + c_2y_2(t)$ only depends on the initial conditions $[y(t_0), \dot{y}(t_0)]$. ProDMPs thus generate smooth trajectories at an arbitrary temporal resolution from low-dimensional weights \boldsymbol{w} . They crucially allow for efficient gradient computation, and can respect different initial conditions such as positions or velocities. We provide an extensive mathematical background of ProDMPs in Appendix A.

Meta-Learning and Graph Network Simulators. To enable generalization across tasks with varying properties, we frame GNS as a meta-learning problem. In this setup, each task corresponds to a simulation of a deformable object with unknown material properties. The goal is to learn a simulator that can adapt quickly to a specific scenario using a limited amount of context data. Following the notation of Volpp et al.

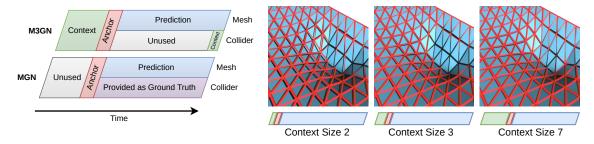


Figure 3: **Left:** M3GN and MGN task setup. Both methods predict mesh positions based on the initial mesh at the anchor time step. M3GN utilizes previous mesh positions and the last step of the collider trajectory for its latent task description, whereas MGN disregards past information and integrates the ground truth collider trajectory into its step-based model. **Right:** Exemplary final simulation steps on the Sheet Deformation task of M3GN given different context set sizes. A larger context size results in a more accurate **prediction** (blue) of the **ground truth** (red wireframe) simulation.

(2021), the meta-dataset $\mathcal{D} = \mathcal{D}_{1:L}$ consists of simulation trajectories $\mathcal{D}_l = \{\mathcal{G}_{l,1} \dots \mathcal{G}_{l,T}\}$, where T is the trajectory length. Each simulation step $\mathcal{G}_{l,t} = (\boldsymbol{m}_{l,t}, \boldsymbol{u}_{l,t})$ represents a graph capturing both the deformable object mesh $\boldsymbol{m}_{l,t}$ (describing its position and topology) and an optional rigid collider $\boldsymbol{u}_{l,t}$. Physical proximity is used to define graph edges that model interactions between the deformable object and the collider. At test time, the first $T^c \ll T$ simulation frames, $\mathcal{G}_{l,1:T^c}$, are observed as a context set to predict the remaining trajectory. Following prior work (Pfaff et al., 2021), we assume access to the full collider trajectory during prediction², resulting in the complete context set:

$$\mathcal{D}_{l}^{c} = \{\mathcal{G}_{l,1}, \dots \mathcal{G}_{l,T^{c}}\} \cup \{\mathbf{u}_{l,T^{c}+1}, \dots, \mathbf{u}_{l,T}\}.$$
(2)

To provide a clear reference point for discussion, we define the anchor time step as the final time step T^c of the context set. The corresponding anchor graph, \mathcal{G}_{l,T^c} , represents the system's state at this point and serves as the starting state for trajectory prediction by the GNSs. Notably, the anchor graph \mathcal{G}_{l,T^c} alone does not capture the complete system state, as the material properties of the deformable object remain unknown. These properties must be inferred from the prior simulation steps, $\mathcal{G}_{l,1:T^c}$, to enable accurate simulation predictions. Figure 3 illustrates this setup.

Model Architecture. Our model architecture, M3GN, is designed to learn from context data and predict future simulation steps by leveraging a combination of graph network simulation and meta-learning techniques. The architecture consists of two parts: the computation of the latent task description from the context data and the actual graph network simulation of future simulation steps. We base our context processing on the Conditional Neural Process (CNP) (Garnelo et al., 2018a), as it efficiently encodes a latent description over tasks given a set of context observations. Omitting the task index l to avoid clutter, CNPs expect a context set $\{(x_1, y_1), \ldots, (x_{T^c}, y_{T^c})\}$ consisting of inputs x_t and corresponding targets y_t . We translate our context set \mathcal{D}^c from Equation 2 to this format by using each graph \mathcal{G}_t as an input, and setting its labels as the node-wise velocities. This approach allows the model to focus on dynamics rather than absolute positions, which are more task-specific. Assuming a forward-Euler integration scheme with a time step of 1, we numerically approximate the velocities as the difference between the node positions of two consecutive simulation steps. The input graph x_t represents the simulation state at time step t, including mesh and collider, while y_t encodes the change in positions between consecutive time steps.

$$x_t = \mathcal{G}_t, \quad y_t = pos(\mathcal{G}_{t+1}) - pos(\mathcal{G}_t).$$

To account for the known collider trajectory, we add its relative position as an additional node feature. Specifically, we include the position of the collider at the last time step T of the simulation, $pos(\boldsymbol{u}_T)$, relative to its current position, $pos(\boldsymbol{u}_t)$. Preliminary testing indicated that incorporating the complete future collider

²This assumption is commonly satisfied in practical scenarios. For instance, in robotic planning tasks, the robot generates multiple candidate future end-effector trajectories and requires predictions of the resulting deformation to select the most suitable plan.

trajectory $pos(\boldsymbol{u}_{T^c}),...pos(\boldsymbol{u}_T)$ did not improve the results on our tasks. Given a context set \mathcal{D}^c with anchor time step T^c , this results in $T^c - 1$ tuples $(\boldsymbol{x}_t, \boldsymbol{y}_t)$. A shared GNN encoder $h_{\boldsymbol{\theta}}$ computes node-level latent features

$$\boldsymbol{z}_{t,v} = h_{\boldsymbol{\theta}}(\boldsymbol{x}_t, \boldsymbol{y}_t) \in \mathbb{R}^{T^c \times |\mathcal{V}| \times d_z}$$
(3)

for each context time step with feature dimension d_z . We then aggregate over the time domain of the context set to obtain $\mathbf{z}_v = \bigoplus_t \mathbf{z}_{t,v} \in \mathbb{R}^{|\mathcal{V}| \times d_z}$, using $\bigoplus = \max$ as the aggregation operator. Intuitively, \mathbf{z}_v is a representation of the task inferred from the context data \mathcal{D}^c , and encodes material properties, future collider movements, and high-level deformations of the simulation. While we use node-level latent features for M3GN, one could additionally aggregate over the nodes to obtain a graph-global task descriptor $\mathbf{z} = \bigotimes \mathbf{z}_v \in \mathbb{R}^{d_z}$. We explore this choice and different aggregation functions \bigoplus , \bigotimes in Section 4.

Once the task descriptor has been computed, it serves as the input to the predictive stage, enabling simulation of future trajectories. We concatenate the latent description z_v with the node features of the anchor graph \mathcal{G}_{T^c} and subsequently use a GNN g_{θ} to predict per-node ProDMP weights

$$\boldsymbol{w}_v = q_{\boldsymbol{\theta}}(\mathcal{G}_{T^c}, \boldsymbol{z}_v) \in \mathbb{R}^{|\mathcal{V}| \times d_w}. \tag{4}$$

GNNs provide the flexibility to incorporate arbitrary node features. To better capture short-term dynamics, we augment the input with node velocities from the anchor time step (T^c) ; the inclusion of velocity information was determined through hyperparameter optimization on a per-task basis. The ProDMP trajectory generator $f(\boldsymbol{w}_v) \in \mathbb{R}^{T \times |\mathcal{V}| \times d_{\text{world}}}$ transforms the predicted outputs of the simulator GNN into per-node object trajectories over the entire simulation horizon. This approach can be seen as a form of temporal bundling (Brandstetter et al., 2022), requiring a single function call. In comparison, existing GNS train mostly on next-step dynamics and require one call per step during their auto-regressive inference scheme (Pfaff et al., 2021; Allen et al., 2023). The trajectory-level view further allows us to omit noise injection during training, which MGN requires to generalize from learned next-step predictions to multi-step rollouts during inference. We provide a visualization of our model architecture in Figure 1 and refer to Appendix B for further details.

Meta Training. The goal of meta-learning is to automatically encode inductive biases towards the task distribution extracted from the meta-dataset \mathcal{D} into the task-global parameter $\boldsymbol{\theta}$. To this end, we minimize the negative conditional log probability (Garnelo et al., 2018a)

$$\mathcal{L}(\boldsymbol{\theta}) = -\mathbb{E}_{l \sim 1:L} \Big[\mathbb{E}_{T^c \sim T_{\min}: T_{\max}} \Big[\log p_{\boldsymbol{\theta}} (pos(\boldsymbol{m}_{l,1:T}) \mid \mathcal{D}_l^c) \Big] \Big].$$
 (5)

Each training batch consists of a task \mathcal{D}_l for which we sample a context size T^c uniformly between T_{\min} and T_{\max} to ensure that the model learns to handle different context set sizes. We then compute the latent task descriptor \mathbf{z}_v and subsequently the predicted node trajectories $f(g_{\theta}(\mathcal{G}_{l,T^c},\mathbf{z}_v))$ as described in Equation 3 and Equation 4. The likelihood p_{θ} is defined to be the Gaussian

$$p_{\boldsymbol{\theta}}(\operatorname{pos}(\boldsymbol{m}_{l,1:T}) \mid \mathcal{D}_{l}^{c}) = \mathcal{N}(\operatorname{pos}(\boldsymbol{m}_{l,1:T}) \mid f(g_{\boldsymbol{\theta}}(\mathcal{G}_{l,T^{c}}, \boldsymbol{z}_{v})), \boldsymbol{\sigma}_{o}). \tag{6}$$

Since the training simulations are not affected by noise, we are not modeling the output variance and set it to $\sigma_0 = 1$. Together with taking the mean over the nodes and time steps to stabilize training, optimizing the Gaussian log likelihood from Equation 6 is equivalent to minimizing the MSE

$$\log p_{\boldsymbol{\theta}}(\operatorname{pos}(\boldsymbol{m}_{l,1:T}) \mid \mathcal{D}_{l}^{c}) \simeq \frac{1}{T \mid \mathcal{V} \mid d_{\operatorname{world}}} \sum_{t,v,i} \left(\operatorname{pos}(\boldsymbol{m}_{l,t})_{v,i} - f(g_{\boldsymbol{\theta}}(\mathcal{G}_{l,T^{c}}, \boldsymbol{z}_{v}))_{t,v,i} \right)^{2}.$$

The whole architecture is trained end-to-end using the loss $\mathcal{L}(\theta)$ from Equation 5. After the meta-training, we fix θ , which now encodes inductive biases towards the meta-data \mathcal{D} .

4 Experiments

Setup. We model mesh vertices as graph nodes and establish edges according to the mesh topology, using additional edges between different objects based on Euclidean distance. We employ one-hot encoding to

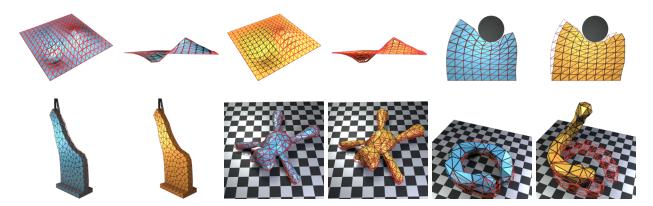


Figure 4: Comparison of the final simulation step between M3GN (blue) and MGN (orange) on all datasets. From (Left) to (Right): (Top) Sheet Deformation and Deformable Block with an anchor time step of 2. (Bottom) Tissue Manipulation with a context size of 5, and Falling Teddy Bear and Mixed Objects Falling with an anchor time step of 20. M3GN provides much better alignment to the ground truth (red wireframe) simulation on all tasks, except for Tissue Manipulation, where MGN also solves the task well.

distinguish deformable objects from colliders, using a homogeneous graph representation (Pfaff et al., 2021). The edges additionally encode the relative distances between their connected nodes. Compared to existing work (Linkerhägner et al., 2023), we include a small initial context sequence covering time steps $1, \ldots, T^c$ for each simulation, with T^c being the anchor time step. Both the context and simulator MPNs use 15 message passing steps. Each message passing step uses separate 1-layer MLPs with a latent dimension of 128 and LeakyReLU activations for its node and edge updates.

We evaluate the *Full-rollout MSE*, computed as the average simulation MSEs following all time steps after the anchor time step, and the *Per-timestep MSE*, defined as the MSE at each individual time step. Both metrics are averaged over all trajectories in the test set. For each experiment, we report the mean and bootstrapped confidence intervals (Agarwal et al., 2021) over 8 random seeds. We evaluate both metrics for various context sizes ranging from 2 to 30 steps. Appendix C provides additional details on our experimental setup.

Datasets. We validate our method on five different simulation datasets based on three different mesh-based physics simulators. These include a *Deformable Block* (DB) task in 2D and a 3D *Tissue Manipulation* (TM) task (Linkerhägner et al., 2023), generated using Simulation Open Framework Architecture (SOFA) (Faure et al., 2012). In both datasets, the Poisson's ratio (Lim, 2015) acts as the randomized material property. *Deformable Block* simulates different trapezoids that are deformed by a circular collider with constant velocity and varying size and starting position. Each trajectory consists of a mesh with 81 nodes that is deformed over 39 time steps. *Tissue Manipulation* considers a surgical robotics scenario where a piece of tissue is deformed by a gripper. The gripper is attached to a fixed object position and moves in a random direction with constant velocity. The mesh comprises 361 nodes and the simulation has 100 steps.

We further consider the *Sheet Deformation* (SD) dataset (Dahlinger et al., 2025), which simulates how a sheet deforms under two constant forces that are applied at different positions of the sheet plane. As the Young's modulus is varied between sheets, this dataset constitutes a simplified stamp forming process, as common in mechanical engineering (Zimmerling et al., 2022). The simulations are generated with Abaqus (Smith, 2009), comprising 50 time steps and a plate with 225 nodes. We test two different data splits: The in-distribution (ID) split tests on material properties that the model has seen during training, while the out-of-distribution (OOD) split evaluates Young's modulus values outside the training domain.

The final two tasks place a randomly rotated deformable object at a specific height and let it fall to and collide with the ground. Falling Teddy Bear (FTB) considers the titular teddy bear as its only object, whereas six different objects are considered for Mixed Objects Falling (MOF). Each trajectory assigns a random Poisson's ratio and random Young's modulus to the falling object, thus influencing its deformation upon contact with the floor. Each trajectory in the last two tasks consists of 200 time steps. The object meshes have up to 350 nodes and are shown in Figure 11 in the appendix. For simplicity, we only consider the triangular surface

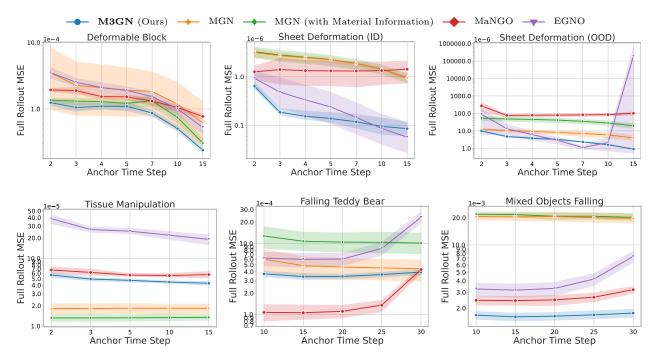


Figure 5: MSE (on a log scale) over full rollouts for different methods across all tasks, including an additional plot for the *Sheet Deformation* task evaluated on an out-of-distribution (OOD) test set of material properties. Overall, M3GN steadily improves its performance when provided with additional context information. Our method generally outperforms both MGN variants, likely due to the MP-based trajectory formulation and the latent material property representation, with the exception of the Tissue Manipulation task. Equivariant Graph Neural Operator (EGNO) exhibits instability for later anchor time steps and only performs competitively on the *Sheet Deformation (ID)* task.

meshes for the experimental setup. All task spaces are normalized to $[-1,1]^3$. Appendix B.1 details the graph encoding, while Appendix D provides further information on dataset sizes and preprocessing.

Baselines and Ablations. We compare to MGN(Pfaff et al., 2021), evaluating its performance both with and without additional *material information* provided as a node feature. Importantly, we never supply this feature to M3GN.

MGN generates the next mesh state by iteratively predicting the velocities for the current simulation step. It is trained to minimize the 1-step MSE over node velocities, incorporating Gaussian input noise during training (Brandstetter et al., 2022). This noise serves to mitigate error accumulation and stabilize autoregressive rollouts during inference. To ensure a fair comparison, we adopt the same hyperparameters as our method and optimize the input noise level per task.

We also explore the effect of incorporating historical information, specifically previous velocities, as node features for both MGN and M3GN. For MGN, using both the current and previous velocities improves performance significantly on many tasks. For M3GN, including only the current velocity yields similar benefits. Figure 12 in the Appendix presents the results of preliminary tuning experiments on a validation split. Additionally, Table 1 summarizes the specific history configurations and other relevant hyperparameter for each method and task. As a comparison to a graph-based meta-learning method, we evaluate M3GN against the Meta Neural Graph Operator (MaNGO) (Dahlinger et al., 2025). To adapt MaNGO to our trajectory-based meta-learning setup, we modify its architecture accordingly. Specifically, we remove the MaNGO encoder, which aggregates information across multiple trajectories. Instead, we provide the context data as the initial position in the unprocessed input trajectory of the MaNGO decoder and repeat the anchor-timestep data until the end of the trajectory. MaNGO then processes this sequence using spatial message passing and temporal convolution to produce its predicted trajectory. We discard the predicted portion corresponding to the context time steps and use the remaining time steps as the MaNGO prediction.

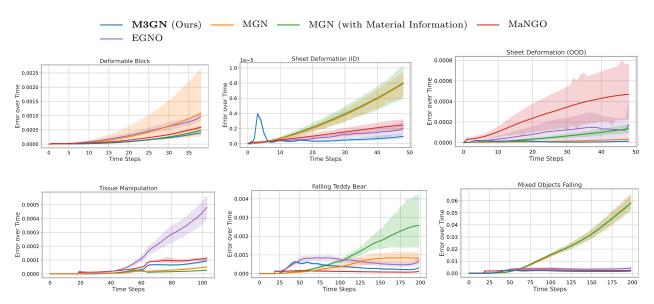


Figure 6: Per-timestep MSE for different methods across all tasks, showing the temporal evolution of prediction error averaged over all test trajectories. For DB, SD (ID), and SD (OOD), the context size is set to 2, whereas TM, FTB, and MOF use a context size of 20. The step-based MGN variants exhibit clear error accumulation over time, whereas M3GN maintains stable accuracy throughout the rollout likely due to its temporally consistent MP-based trajectory formulation.

As an additional baseline, we compare our approach to the Equivariant Graph Neural Operator (EGNO) (Xu et al., 2024), which employs equivariant message-passing layers and predicts the remaining simulation steps in a single pass, closely aligning with our setup. However, training EGNO proved unstable with 15 message-passing steps, and the best results were achieved using only 5 steps. We hypothesize that this instability may stem from the longer prediction horizon of up to 200 steps in our experiments, as the baseline was originally evaluated on tasks with a much shorter prediction horizon of only 8 steps. Further details on the implementation of these baselines can be found in Appendix C.

We further study different design choices of M3GN on Sheet Deformation and Deformable Block. To investigate the effect of the meta-learning approach, we train an MGN (MP) variant that uses ProDMPs predictions, but omits a context aggregation and thus has no latent task description z_v . Similarly, we compare to M3GN (Step-based), which performs a next-step prediction of the dynamics instead of predicting ProDMP parameters, but otherwise follows the CNP training scheme to learn a latent task description. Finally, we compare the deterministic CNP approach to both MP and step-based probabilistic Neural Process (NP) approaches. Here, we get diagonal Gaussian distributions as the outputs of the context MPN, which we aggregate using Bayesian context aggregation (Volpp et al., 2021). We further investigate if node aggregation of the latent task description is beneficial by applying a maximum aggregation of the node features before the context aggregation. While standard CNPs require a permutation-invariant context aggregation, our context has a temporal structure. We thus experiment with a small transformer model with 4 transformer blocks, 4 attention heads, temporal encoding and a latent dimension of 32 as an aggregator. The transformer takes the sequence of outputs of the context MPN and predicts the aggregated node-level task description z_v .

Main Results. Figure 4 visualizes exemplary final simulation steps for M3GN and MGN for all tasks. M3GN aggregates context information to condition node-level ProDMP representations of the simulated trajectory. This approach leads to accurate simulations, providing much better alignment to the ground truth simulation than the step-based MGN on all tasks. Appendix E.3 shows visualizations of full simulation rollouts for all tasks and methods.³

Figure 5 provides the full-rollout MSE for M3GN, MGN, and MGN (with Material Information) across tasks. Adding material information improves performance only on the *Deformable Block* and *Tissue Manipulation*

³Videos of these simulations are in the supplementary material.

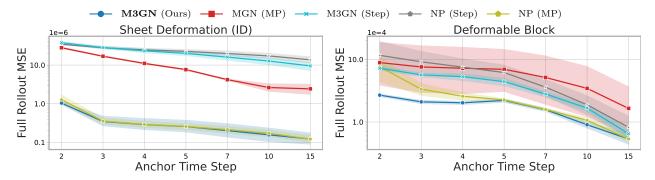


Figure 7: Log-scale MSE over full rollouts for the *Sheet Deformation* (**Left**) and *Deformable Block* (**Right**) tasks for different meta-learning and MP variants. Using a ProDMP representation for MGN improves performance. CNPs and NPs with a next-step prediction do not improve over standard MGN. A NP instead of an CNP architecture for M3GN slightly reduces performance.

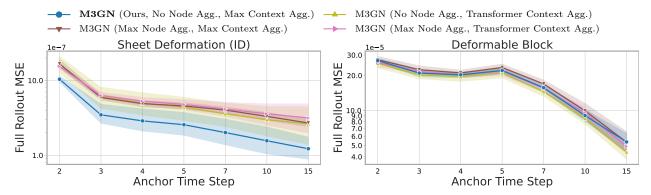


Figure 8: Log-scale MSE over full rollouts for the *Sheet Deformation* (**Left**) and *Deformable Block* (**Right**) tasks for different context and node aggregation methods. The node-level maximum context aggregation of M3GN performs best for *Sheet Deformation*, while all methods work roughly equally well on the *Deformable Block* task.

datasets. In contrast, on the Falling Teddy Bear and Sheet Deformation (OOD) tasks, MGN (with Material Information) tends to overfit, likely resulting in decreased performance when material information was provided. In general, using a later anchor time step improves performance across all methods, presumably due to a shorter prediction horizon. The main exception is EGNO on Sheet Deformation (OOD), which becomes unstable for later anchor time steps.

M3GN surpasses all baselines *Deformable Block*. For *Sheet Deformation*, M3GN and EGNO significantly outperform the other baselines across context sizes. Furthermore, M3GN generalizes well to unseen material properties in the *OOD* setup, whereas, e.g., MGN and MaNGO fail to properly extrapolate. For *Tissue Manipulation*, the step-based baselines slightly outerperform M3GN in terms of MSE. Yet, M3GN and MaNGO provide plausible and visually consistent simulations, with the step-based baselines primarily capturing finer details more accurately. In contrast, EGNO performs significantly worse in this setting, achieving an MSE that is an order of magnitude higher than that of M3GN.

On Falling Teddy Bear and Mixed Objects Falling, the step-based MGN without material information performs well on the former but, along with the other step-based method, fails to provide accurate long-term simulations on the latter. For Mixed Objects Falling, the predicted trajectories of both MGN variants qualitatively deviate from the ground truth. Both MGN and MGN (with Material Information) exhibit object drift or misalignment, e.g., between colliding bodies. In contrast, for M3GN, the ProDMP's temporally consistent movements combined with context aggregation produce stable and coherent simulations, substantially improving over the step-based baselines. Examples of these behaviors are shown at the bottom of Figure 4. MaNGO achieves exceptional good results on Falling Teddy Bear, but it is surpassed by M3GN on Mixed Objects Falling.

Interestingly, trajectory-based methods do not benefit from later anchor steps on these tasks. We suspect the increase in MSE is a consequence of how the metric is averaged: early timesteps are trivial (the object is simply falling), so including them lowers the mean error. When anchoring later, these easy steps are removed, and the MSE is computed only over the harder, post-impact segment, leading to a higher average error.

Additional Experiments. Figure 6 shows representative *Pertimestep MSE* results, while Appendix E provides the complete set of evaluations for different context sizes. These figures highlight the error accumulation common in step-based learned simulatiors. In contrast, M3GN maintains stable accuracy throughout the rollout. In *Sheet Deformation (ID)*, we observe a temporary increase in error for M3GN around time steps 2 to 5. This behavior seems to stem from a rapid change in node velocities, which our ProDMP representation smooths over. While additional basis functions would increase the ProDMP's capacity and thus likely mitigate this issue, we deliberately avoided excessive hyperparameter tuning to ensure a fair comparison and comparable optimization budgets across methods.

Next, Figure 7 finds that both MP representations and a metalearning objective are crucial for accurate simulations. Interestingly, using NPs with ProDMPs only slightly degrades performance compared to M3GN, suggesting that the NP's latent distribution does not benefit our GNS setup. Figure 8 additionally compares different methods to aggregate the context set. The node-level maximum context aggregation works best for *Sheet Deformation*. For *Deformable Block*, there is no significant difference between aggregations, causing us to use the comparatively simple node-level maximum context aggregation for all experiments.

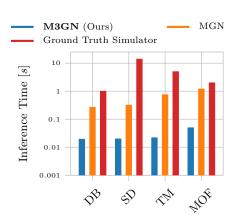


Figure 9: Runtime comparison on four tasks between the learned methods and the different ground truth simulators. Note the log scale on the y-axis. The complete runtime and memory usage evaluation is in Appendix, Table 3.

We additionally present a visualization of the latent space for M3GN in Figure 19 in the Appendix, showing that simulations with similar material properties are clustered together. This latent structure highlights the model's ability to differentiate between material behaviors while preserving the relationships between similar properties.

Figure 9 compares the inference speed of M3GN to that of the step-based MGN. M3GN's ProDMP trajectory representation significantly decreases the amount of required model calls for the simulation, since, after encoding, a single GNN forward pass can is used to compute the full trajectory. Additionally, the context set is easily encoded in parallel, resulting in a relatively minor cost for the context computation and aggregation for all tasks. While MGN does not perform any context processing, it requires one forward pass per timestep, making its rollout inherently sequential. Together, these properties result in an inference-time speedup of up to a factor of 32 for M3GN compared to MGN (for the *Tissue Manipulation* task), and up to a factor of 700 compared to the ground-truth simulators (for the *Sheet Deformation* task). A complete comparison of execution time and memory consumption during inference is provided in Table 3 in the Appendix. Improving over existing learned simulators by more than one, and over classical simulators by more than two orders of magnitude enables rapid development for downstream engineering applications, such as manufacturing optimization.

5 Conclusion

We introduce Movement-Primitive Meta-MESHGRAPHNET (M3GN), a novel Graph Network Simulator that combines movement primitives with trajectory-level meta-learning for efficient and accurate long-term predictions in physical simulations. Our method dynamically adapts to available context information during inference, enabling accurate prediction of deformations under unknown object properties. Additionally, it effectively mitigates error accumulation while reducing the number of required learned simulator function calls. To validate the effectiveness of M3GN, we propose two new deformation prediction tasks with uncertain material properties. Results on these tasks and existing datasets demonstrate that our method consistently

outperforms two strong Graph Network Simulator baselines, even when the baselines are provided with oracle information about the material properties.

Limitations and Future Work. Our method may struggle to capture rapid, high-frequency dynamics, as the smooth ProDMP formulation can lead to temporary errors when node velocities change abruptly. We also plan to integrate online re-planning of trajectories, predicting trajectory segments with every model forward pass. This process may enhance coordination between simulated nodes across segments while maintaining the benefits of a compact multi-step trajectory representation. In addition, the M3GN framework is not limited to deformation tasks; it can be extended to new settings such as fluid simulations or other non-mesh-based environments, provided that an appropriate graph structure can be constructed from the underlying data.

Broader Impact Statement Our proposed Graph Network Simulator can positively impact various fields relying on computational modeling and simulation by significantly reducing computational cost compared to traditional simulators while providing accurate simulations. However, efficient and accurate simulation of physical systems also comes with potential negative impacts, such as, e.g., the development of advanced weapon models.

References

- Rishabh Agarwal, Max Schwarzer, Pablo Samuel Castro, Aaron C Courville, and Marc Bellemare. Deep reinforcement learning at the edge of the statistical precipice. In M. Ranzato, A. Beygelzimer, Y. Dauphin, P.S. Liang, and J. Wortman Vaughan (eds.), *Advances in Neural Information Processing Systems*, volume 34, pp. 29304–29320. Curran Associates, Inc., 2021. URL https://proceedings.neurips.cc/paper_files/paper/2021/file/f514cec81cb148559cf475e7426eed5e-Paper.pdf.
- Kelsey Allen, Tatiana Lopez-Guevara, Kimberly L Stachenfeld, Alvaro Sanchez Gonzalez, Peter Battaglia, Jessica B Hamrick, and Tobias Pfaff. Inverse design for fluid-structure interactions using graph network simulators. In S. Koyejo, S. Mohamed, A. Agarwal, D. Belgrave, K. Cho, and A. Oh (eds.), Advances in Neural Information Processing Systems, volume 35, pp. 13759–13774. Curran Associates, Inc., 2022a. URL https://proceedings.neurips.cc/paper_files/paper/2022/file/59593615e358d52295578e0d8e94ec4a-Paper-Conference.pdf.
- Kelsey R Allen, Tatiana Lopez Guevara, Yulia Rubanova, Kimberly Stachenfeld, Alvaro Sanchez-Gonzalez, Peter Battaglia, and Tobias Pfaff. Graph network simulators can learn discontinuous, rigid contact dynamics. Conference on Robot Learning (CoRL)., 2022b.
- Kelsey R Allen, Yulia Rubanova, Tatiana Lopez-Guevara, William F Whitney, Alvaro Sanchez-Gonzalez, Peter Battaglia, and Tobias Pfaff. Learning rigid dynamics with face interaction graph networks. In *The Eleventh International Conference on Learning Representations*, 2023.
- Marcin Andrychowicz, Misha Denil, Sergio Gomez Colmenarejo, Matthew W. Hoffman, David Pfau, Tom Schaul, and Nando de Freitas. Learning to Learn by Gradient Descent by Gradient Descent. Advances in Neural Information Processing Systems, 2016.
- Rika Antonova, Jingyun Yang, Priya Sundaresan, Dieter Fox, Fabio Ramos, and Jeannette Bohg. A bayesian treatment of real-to-sim for deformable object manipulation. *IEEE Robotics and Automation Letters*, 7(3): 5819–5826, 2022.
- Shikhar Bahl, Mustafa Mukadam, Abhinav Gupta, and Deepak Pathak. Neural dynamic policies for end-to-end sensorimotor learning. Advances in Neural Information Processing Systems, 33:5058–5069, 2020.
- Bart Bakker and Tom Heskes. Task clustering and gating for Bayesian multitask learning. *Journal of Machine Learning Research*, 2003.
- Pierre Baqué, Edoardo Remelli, François Fleuret, and Pascal Fua. Geodesic convolutional shape optimization. In Jennifer G. Dy and Andreas Krause (eds.), *Proceedings of the 35th International Conference on Machine Learning, ICML 2018, Stockholmsmässan, Stockholm, Sweden, July 10-15, 2018*, volume 80 of *Proceedings of Machine Learning Research*, pp. 481–490. PMLR, 2018. URL http://proceedings.mlr.press/v80/baque18a.html.

- Peter Battaglia, Razvan Pascanu, Matthew Lai, Danilo Jimenez Rezende, and koray kavukcuoglu. Interaction networks for learning about objects, relations and physics. In D. Lee, M. Sugiyama, U. Luxburg, I. Guyon, and R. Garnett (eds.), Advances in Neural Information Processing Systems, volume 29. Curran Associates, Inc., 2016. URL https://proceedings.neurips.cc/paper/2016/file/3147da8ab4a0437c15ef51a5cc7f2dc4-Paper.pdf.
- Peter W. Battaglia, Jessica B. Hamrick, Victor Bapst, Alvaro Sanchez-Gonzalez, Vinícius Flores Zambaldi, Mateusz Malinowski, Andrea Tacchetti, David Raposo, Adam Santoro, Ryan Faulkner, Çaglar Gülçehre, H. Francis Song, Andrew J. Ballard, Justin Gilmer, George E. Dahl, Ashish Vaswani, Kelsey R. Allen, Charles Nash, Victoria Langston, Chris Dyer, Nicolas Heess, Daan Wierstra, Pushmeet Kohli, Matthew Botvinick, Oriol Vinyals, Yujia Li, and Razvan Pascanu. Relational inductive biases, deep learning, and graph networks. *CoRR*, abs/1806.01261, 2018. URL http://arxiv.org/abs/1806.01261.
- Yoshua Bengio, Samy Bengio, and Jocelyn Cloutier. Learning a synaptic learning rule. *International Joint Conference on Neural Networks*, 1991.
- Cristian Bodnar, Wessel P. Bruinsma, Ana Lucic, Megan Stanley, Johannes Brandstetter, Patrick Garvan, Maik Riechert, Jonathan A. Weyn, Haiyu Dong, Anna Vaughan, Jayesh K. Gupta, Kit Thambiratnam, Alex Archibald, Elizabeth Heider, Max Welling, Richard E. Turner, and Paris Perdikaris. Aurora: A foundation model of the atmosphere. CoRR, abs/2405.13063, 2024. doi: 10.48550/ARXIV.2405.13063. URL https://doi.org/10.48550/arXiv.2405.13063.
- Johannes Brandstetter, Daniel E Worrall, and Max Welling. Message passing neural pde solvers. In *International Conference on Learning Representations*, 2022.
- Susanne C Brenner and L Ridgway Scott. The mathematical theory of finite element methods, volume 3. Springer, 2008.
- Michael M. Bronstein, Joan Bruna, Taco Cohen, and Petar Velickovic. Geometric deep learning: Grids, groups, graphs, geodesics, and gauges. *CoRR*, abs/2104.13478, 2021. URL https://arxiv.org/abs/2104.13478.
- TJ Chung. Finite element analysis in fluid dynamics. NASA STI/Recon Technical Report A, 78:44102, 1978.
- Andrea Cini, Ivan Marisca, Daniele Zambon, and Cesare Alippi. Graph deep learning for time series forecasting. *ACM Comput. Surv.*, 57(12), July 2025. ISSN 0360-0300. doi: 10.1145/3742784. URL https://doi.org/10.1145/3742784.
- Jerome J Connor and Carlos Alberto Brebbia. Finite element techniques for fluid flow. Newnes, 2013.
- Ying Da Wang, Martin J Blunt, Ryan T Armstrong, and Peyman Mostaghimi. Deep learning in pore scale imaging and modeling. *Earth-Science Reviews*, 215:103555, 2021.
- Philipp Dahlinger, Tai Hoang, Denis Blessing, Niklas Freymuth, and Gerhard Neumann. Mango adaptable graph network simulators via meta-learning. arXiv preprint arXiv:2510.05874, 2025.
- Nikita Durasov, Artem Lukoyanov, Jonathan Donier, and Pascal Fua. Debosh: Deep bayesian shape optimization. arXiv preprint arXiv:2109.13337, 2021.
- François Faure, Christian Duriez, Hervé Delingette, Jérémie Allard, Benjamin Gilles, Stéphanie Marchesseau, Hugo Talbot, Hadrien Courtecuisse, Guillaume Bousquet, Igor Peterlik, and Stéphane Cotin. SOFA: A Multi-Model Framework for Interactive Physical Simulation. In Yohan Payan (ed.), Soft Tissue Biomechanical Modeling for Computer Assisted Surgery, volume 11 of Studies in Mechanobiology, Tissue Engineering and Biomaterials, pp. 283–321. Springer, June 2012. doi: 10.1007/8415_2012_125. URL https://hal.inria.fr/hal-00681539.
- Chelsea Finn, Pieter Abbeel, and Sergey Levine. Model-agnostic meta-learning for fast adaptation of deep networks. *International Conference on Machine Learning*, 2017.
- Chelsea Finn, Kelvin Xu, and Sergey Levine. Probabilistic Model-Agnostic Meta-Learning. Advances in Neural Information Processing Systems, 2018.

- Meire Fortunato, Tobias Pfaff, Peter Wirnsberger, Alexander Pritzel, and Peter Battaglia. Multiscale meshgraphnets. In *ICML 2022 2nd AI for Science Workshop*, 2022. URL https://openreview.net/forum?id=G3TRIsmMhhf.
- Niklas Freymuth, Philipp Dahlinger, Tobias Würth, Luise Kärger, and Gerhard Neumann. Swarm reinforcement learning for adaptive mesh refinement. *Neural Information Processing Systems*, 37, 2023.
- Niklas Freymuth, Tobias Würth, Nicolas Schreiber, Balazs Gyenes, Andreas Boltres, Johannes Mitsch, Aleksandar Taranovic, Tai Hoang, Philipp Dahlinger, Philipp Becker, et al. Amber: Adaptive mesh generation by iterative mesh resolution prediction. *Neural Information Processing Systems*, 39, 2025.
- Marta Garnelo, Dan Rosenbaum, Christopher Maddison, Tiago Ramalho, David Saxton, Murray Shanahan, Yee Whye Teh, Danilo Rezende, and S. M. Ali Eslami. Conditional neural processes. *International Conference on Machine Learning*, 2018a.
- Marta Garnelo, Jonathan Schwarz, Dan Rosenbaum, Fabio Viola, Danilo Jimenez Rezende, S. M. Ali Eslami, and Yee Whye Teh. Neural processes. *ICML Workshop on Theoretical Foundations and Applications of Deep Generative Models*, 2018b.
- Daniel Golovin, Benjamin Solnik, Subhodeep Moitra, Greg Kochanski, John Karro, and D. Sculley. Google vizier: a service for black-box optimization. *International Conference on Knowledge Discovery and Data Mining*, 2017.
- Jonathan Gordon, John Bronskill, Matthias Bauer, Sebastian Nowozin, and Richard E. Turner. Meta-Learning Probabilistic Inference for Prediction. *International Conference on Learning Representations*, 2019.
- Erin Grant, Chelsea Finn, Sergey Levine, Trevor Darrell, and Thomas L. Griffiths. Recasting Gradient-Based Meta-Learning as Hierarchical Bayes. *International Conference on Learning Representations*, 2018.
- Xiaoxiao Guo, Wei Li, and Francesco Iorio. Convolutional neural networks for steady flow approximation. In *Proceedings of the 22nd ACM SIGKDD International Conference on Knowledge Discovery and Data Mining*, KDD '16, pp. 481–490, New York, NY, USA, 2016. Association for Computing Machinery. ISBN 9781450342322. doi: 10.1145/2939672.2939738. URL https://doi.org/10.1145/2939672.2939738.
- Xu Han, Han Gao, Tobias Pfaff, Jian-Xun Wang, and Liping Liu. Predicting physics in mesh-reduced space with temporal attention. In *The Tenth International Conference on Learning Representations, ICLR 2022, Virtual Event, April 25-29, 2022.* OpenReview.net, 2022. URL https://openreview.net/forum?id=XctLdNfCmP.
- Tom Heskes. Empirical Bayes for learning to learn. International Conference on Machine Learning, 2000.
- Tai Hoang, Huy Le, Philipp Becker, Vien Anh Ngo, and Gerhard Neumann. Geometry-aware RL for manipulation of varying shapes and deformable objects. In *The Thirteenth International Conference on Learning Representations*, 2025. URL https://openreview.net/forum?id=7BLXhmWvwF.
- Sepp Hochreiter and Jürgen Schmidhuber. Long short-term memory. Neural computation, 9:1735–80, 12 1997. doi: 10.1162/neco.1997.9.8.1735.
- T. Hospedales, A. Antoniou, P. Micaelli, and A. Storkey. Meta-learning in neural networks: a survey. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 2022.
- Weihua Hu, Muhammed Shuaibi, Abhishek Das, Siddharth Goyal, Anuroop Sriram, Jure Leskovec, Devi Parikh, and C Lawrence Zitnick. Forcenet: A graph neural network for large-scale quantum calculations. In *ICLR 2021 SimDL Workshop*, volume 20, 2021.
- Thomas JR Hughes, John A Cottrell, and Yuri Bazilevs. Isogeometric analysis: Cad, finite elements, nurbs, exact geometry and mesh refinement. *Computer methods in applied mechanics and engineering*, 194(39-41): 4135–4195, 2005.
- Jian-Ming Jin. The finite element method in electromagnetics. John Wiley & Sons, 2015.

- Hyunjik Kim, Andriy Mnih, Jonathan Schwarz, Marta Garnelo, Ali Eslami, Dan Rosenbaum, Oriol Vinyals, and Yee Whye Teh. Attentive neural processes. *International Conference on Learning Representations*, 2019.
- Taesup Kim, Jaesik Yoon, Ousmane Dia, Sungwoong Kim, Yoshua Bengio, and Sungjin Ahn. Bayesian Model-Agnostic Meta-Learning. Advances in Neural Information Processing Systems, 2018.
- Diederik P. Kingma and Jimmy Ba. Adam: A method for stochastic optimization. In Yoshua Bengio and Yann LeCun (eds.), 3rd International Conference on Learning Representations, ICLR 2015, San Diego, CA, USA, May 7-9, 2015, Conference Track Proceedings, 2015. URL http://arxiv.org/abs/1412.6980.
- Diederik P. Kingma and Max Welling. Auto-encoding variational bayes. *International Conference on Learning Representations*, 2014.
- Alex Krizhevsky, Ilya Sutskever, and Geoffrey E Hinton. Imagenet classification with deep convolutional neural networks. In F. Pereira, C. J. C. Burges, L. Bottou, and K. Q. Weinberger (eds.), *Advances in Neural Information Processing Systems*, volume 25. Curran Associates, Inc., 2012.
- Ge Li, Zeqi Jin, Michael Volpp, Fabian Otto, Rudolf Lioutikov, and Gerhard Neumann. Prodmp: A unified perspective on dynamic and probabilistic movement primitives. *IEEE Robotics and Automation Letters*, 8 (4):2325–2332, 2023.
- Ge Li, Hongyi Zhou, Dominik Roth, Serge Thilges, Fabian Otto, Rudolf Lioutikov, and Gerhard Neumann. Open the black box: Step-based policy updates for temporally-correlated episodic reinforcement learning, 2024.
- Jichao Li, Xiaosong Du, and Joaquim RRA Martins. Machine learning in aerodynamic shape optimization. *Progress in Aerospace Sciences*, 134:100849, 2022.
- Yunzhu Li, Jiajun Wu, Russ Tedrake, Joshua B. Tenenbaum, and Antonio Torralba. Learning particle dynamics for manipulating rigid bodies, deformable objects, and fluids. In *International Conference on Learning Representations*, 2019. URL https://openreview.net/forum?id=rJgbSn09Ym.
- Teik-Cheng Lim. Auxetic Materials and Structures. Springer Singapore, 01 2015. ISBN 978-981-287-274-6. doi: 10.1007/978-981-287-275-3. URL https://doi.org/10.1007/978-981-287-275-3.
- Jonas Linkerhägner, Niklas Freymuth, Paul Maria Scheikl, Franziska Mathis-Ullrich, and Gerhard Neumann. Grounding graph network simulators using physical sensor observations. In *The Eleventh International Conference on Learning Representations*, 2023.
- Phillip Lippe, Bas Veeling, Paris Perdikaris, Richard E. Turner, and Johannes Brandstetter. Pde-refiner: Achieving accurate long rollouts with neural PDE solvers. In Alice Oh, Tristan Naumann, Amir Globerson, Kate Saenko, Moritz Hardt, and Sergey Levine (eds.), Advances in Neural Information Processing Systems 36: Annual Conference on Neural Information Processing Systems 2023, NeurIPS 2023, New Orleans, LA, USA, December 10 16, 2023, 2023. URL http://papers.nips.cc/paper_files/paper/2023/hash/d529b943af3dba734f8a7d49efcb6d09-Abstract-Conference.html.
- Tatiana Lopez-Guevara, Yulia Rubanova, William F Whitney, Tobias Pfaff, Kimberly Stachenfeld, and Kelsey R Allen. Scaling face interaction graph networks to real world scenes. arXiv preprint arXiv:2401.11985, 2024.
- Christos Louizos, Xiahan Shi, Klamer Schutte, and M. Welling. The functional neural process. *Advances in Neural Information Processing Systems*, 2019.
- Ibomoiye Domor Mienye, Theo G. Swart, and George Obaido. Recurrent neural networks: A comprehensive review of architectures, variants, and applications. *Information*, 15(9), 2024. ISSN 2078-2489. doi: 10.3390/info15090517. URL https://www.mdpi.com/2078-2489/15/9/517.

- Miguel Angel Zamora Mora, Momchil Peychev, Sehoon Ha, Martin Vechev, and Stelian Coros. Pods: Policy optimization via differentiable simulation. In Marina Meila and Tong Zhang (eds.), *Proceedings of the 38th International Conference on Machine Learning*, volume 139 of *Proceedings of Machine Learning Research*, pp. 7805–7817. PMLR, 18–24 Jul 2021. URL http://proceedings.mlr.press/v139/mora21a.html.
- NVIDIA. Isaac sim, 2022a. URL https://developer.nvidia.com/isaac-sim.
- NVIDIA. Nvidia physx sdk, 2022b. URL https://developer.nvidia.com/physx-sdk.
- Fabian Otto, Onur Celik, Hongyi Zhou, Hanna Ziesche, Ngo Anh Vien, and Gerhard Neumann. Deep black-box reinforcement learning with movement primitives. In Karen Liu, Dana Kulic, and Jeffrey Ichnowski (eds.), Conference on Robot Learning, CoRL 2022, 14-18 December 2022, Auckland, New Zealand, volume 205 of Proceedings of Machine Learning Research, pp. 1244–1265. PMLR, 2022. URL https://proceedings.mlr.press/v205/otto23a.html.
- Alexandros Paraschos, Christian Daniel, Jan R Peters, and Gerhard Neumann. Probabilistic movement primitives. Advances in neural information processing systems, 26, 2013.
- Maciej Paszynski. Fast solvers for mesh-based computations. CRC Press, 2016.
- Tobias Pfaff, Meire Fortunato, Alvaro Sanchez-Gonzalez, and Peter W. Battaglia. Learning mesh-based simulation with graph networks. In *International Conference on Learning Representations*, 2021. URL https://arxiv.org/abs/2010.03409.
- Tomasz Plewa, Timur Linde, V Gregory Weirs, et al. Adaptive mesh refinement-theory and applications. Springer, 2005.
- Anastasis C Polycarpou. Introduction to the finite element method in electromagnetics. Springer Nature, 2022
- Andreas Radler, Vincent Seyfried, Stefan Pirker, Johannes Brandstetter, and Thomas Lichtenegger. Paint: Parallel-in-time neural twins for dynamical system reconstruction, 2025. URL https://arxiv.org/abs/2510.16004.
- Sachin Ravi and Hugo Larochelle. Optimization as a model for few-shot learning. *International Conference on Learning Representations*, 2017.
- CJ Reddy. Finite element method for eigenvalue problems in electromagnetics, volume 3485. NASA, Langley Research Center, 1994.
- Junuthula Narasimha Reddy. Introduction to the finite element method. McGraw-Hill Education, 2019.
- Junuthula Narasimha Reddy and David K Gartling. The finite element method in heat transfer and fluid dynamics. CRC press, 2010.
- Danilo Jimenez Rezende, Shakir Mohamed, and Daan Wierstra. Stochastic backpropagation and approximate inference in deep generative models. *International Conference on Machine Learning*, 2014.
- Luana Ruiz, Fernando Gama, and Alejandro Ribeiro. Gated graph recurrent neural networks. *IEEE Transactions on Signal Processing*, 68:6303–6318, 2020.
- Alvaro Sanchez-Gonzalez, Nicolas Heess, Jost Tobias Springenberg, Josh Merel, Martin Riedmiller, Raia Hadsell, and Peter Battaglia. Graph networks as learnable physics engines for inference and control. In Jennifer Dy and Andreas Krause (eds.), *Proceedings of the 35th International Conference on Machine Learning*, volume 80 of *Proceedings of Machine Learning Research*, pp. 4470–4479. PMLR, 10–15 Jul 2018. URL https://proceedings.mlr.press/v80/sanchez-gonzalez18a.html.
- Alvaro Sanchez-Gonzalez, Jonathan Godwin, Tobias Pfaff, Rex Ying, Jure Leskovec, and Peter Battaglia. Learning to simulate complex physics with graph networks. In *Proceedings of the 37th International Conference on Machine Learning*, pp. 8459–8468. PMLR, 2020.

- Adam Santoro, Sergey Bartunov, Matthew M. Botvinick, Daan Wierstra, and Timothy P. Lillicrap. Metalearning with memory-augmented neural networks. *International Conference on Machine Learning*, 2016.
- Franco Scarselli, Marco Gori, Ah Chung Tsoi, Markus Hagenbuchner, and Gabriele Monfardini. The graph neural network model. *IEEE Transactions on Neural Networks*, 20(1):61–80, 2009. doi: 10.1109/TNN.2008. 2005605.
- Stefan Schaal. Dynamic movement primitives-a framework for motor control in humans and humanoid robotics. In *Adaptive motion of animals and machines*, pp. 261–280. Springer, 2006.
- Paul Maria Scheikl, Eleonora Tagliabue, Balázs Gyenes, Martin Wagner, Diego Dall'Alba, Paolo Fiorini, and Franziska Mathis-Ullrich. Sim-to-real transfer for visual reinforcement learning of deformable object manipulation for robot-assisted surgery. *IEEE Robotics and Automation Letters*, 8(2):560–567, 2022.
- Jürgen Schmidhuber. Learning to control fast-weight memories: an alternative to dynamic recurrent networks. Neural Computation, 1992.
- Muhammet Yunus Seker, Mert Imre, Justus H Piater, and Emre Ugur. Conditional neural movement primitives. In *Robotics: Science and Systems*, volume 10, 2019.
- Haochen Shi, Huazhe Xu, Samuel Clarke, Yunzhu Li, and Jiajun Wu. Robocook: Long-horizon elasto-plastic object manipulation with diverse tools. In *Conference on Robot Learning*, pp. 642–660. PMLR, 2023.
- Jaan-Willem Simon. A review of recent trends and challenges in computational modeling of paper and paper-board at different scales. *Archives of Computational Methods in Engineering*, 28(4):2409–2428, 2021. ISSN 1886-1784. doi: 10.1007/s11831-020-09460-y. URL https://doi.org/10.1007/s11831-020-09460-y.
- Michael Smith. ABAQUS/Standard User's Manual, Version 6.9. Dassault Systèmes Simulia Corp, United States, 2009.
- Jake Snell, Kevin Swersky, and Richard S. Zemel. Prototypical networks for few-shot learning. Advances in Neural Information Processing Systems, 2017.
- Eva Stanova, Gabriel Fedorko, Stanislav Kmet, Vieroslav Molnar, and Michal Fabian. Finite element analysis of spiral strands with different shapes subjected to axial loads. *Advances in engineering software*, 83:45–58, 2015.
- Sebastian Thrun and Lorien Pratt. Learning to Learn. Kluwer Academic Publishers, 1998.
- Laurens van der Maaten and Geoffrey Hinton. Visualizing data using t-sne. *Journal of Machine Learning Research*, 9(86):2579–2605, 2008. URL http://jmlr.org/papers/v9/vandermaaten08a.html.
- Ricardo Vilalta and Youssef Drissi. A Perspective View and Survey of Meta-Learning. *Artificial Intelligence Review*, 2005.
- Michael Volpp, Lukas P. Fröhlich, Kirsten Fischer, Andreas Doerr, Stefan Falkner, Frank Hutter, and Christian Daniel. Meta-learning acquisition functions for transfer learning in Bayesian optimization. *International Conference on Learning Representations*, 2019.
- Michael Volpp, Fabian Flürenbrock, Lukas Großberger, Christian Daniel, and Gerhard Neumann. Bayesian context aggregation for neural processes. *International Conference on Learning Representations*, 2021.
- Michael Volpp, Philipp Dahlinger, Philipp Becker, Christian Daniel, and Gerhard Neumann. Accurate bayesian meta-learning by accurate task posterior inference. In *The Eleventh International Conference on Learning Representations, ICLR 2023, Kigali, Rwanda, May 1-5, 2023.* OpenReview.net, 2023. URL https://openreview.net/pdf?id=sb-IkS8DQw2.
- Jiaxu Wang, Jingkai SUN, Ziyi Zhang, Junhao He, Qiang Zhang, Mingyuan Sun, and Renjing Xu. DEL: Discrete element learner for learning 3d particle dynamics with neural rendering. In *The Thirty-eighth Annual Conference on Neural Information Processing Systems*, 2024. URL https://openreview.net/forum?id=2nvkD0sP0k.

- Liman Wang and Jihong Zhu. Deformable object manipulation in caregiving scenarios: A review. *Machines*, 11(11):1013, 2023.
- Zehang Weng, Fabian Paus, Anastasiia Varava, Hang Yin, Tamim Asfour, and Danica Kragic. Graph-based task-specific prediction models for interactions between deformable and rigid objects. In 2021 IEEE/RSJ International Conference on Intelligent Robots and Systems (IROS), pp. 5741–5748, 2021. doi: 10.1109/IROS51168.2021.9636660. URL https://arxiv.org/abs/2103.02932.
- William F Whitney, Tatiana Lopez-Guevara, Tobias Pfaff, Yulia Rubanova, Thomas Kipf, Kimberly Stachenfeld, and Kelsey R Allen. Learning 3d particle-based simulators from rgb-d videos. arXiv preprint arXiv:2312.05359, 2023.
- Tailin Wu, Takashi Maruyama, Qingqing Zhao, Gordon Wetzstein, and Jure Leskovec. Learning controllable adaptive simulation for multi-resolution physics. In *The Eleventh International Conference on Learning Representations*, 2023.
- Tobias Würth, Niklas Freymuth, Gerhard Neumann, and Luise Kärger. Diffusion-based hierarchical graph neural networks for simulating nonlinear solid mechanics. In *The Thirty-ninth Annual Conference on Neural Information Processing Systems*, 2025. doi: 10.48550/arXiv.2506.06045. URL https://arxiv.org/abs/2506.06045. Spotlight, NeurIPS 2025.
- Jie Xu, Tao Chen, Lara Zlokapa, Michael Foshey, Wojciech Matusik, Shinjiro Sueda, and Pulkit Agrawal. An end-to-end differentiable framework for contact-aware robot design. In *Robotics: Science & Systems*, 2021.
- Minkai Xu, Jiaqi Han, Aaron Lou, Jean Kossaifi, Arvind Ramanathan, Kamyar Azizzadenesheli, Jure Leskovec, Stefano Ermon, and Anima Anandkumar. Equivariant graph neural operator for modeling 3d dynamics. In Forty-first International Conference on Machine Learning, ICML 2024, Vienna, Austria, July 21-27, 2024. OpenReview.net, 2024. URL https://openreview.net/forum?id=dccRCYmL5x.
- Abdelaziz Yazid, Nabbou Abdelkader, and Hamouine Abdelmadjid. A state-of-the-art review of the x-fem for computational fracture mechanics. *Applied Mathematical Modelling*, 33(12):4269–4282, 2009.
- Youn-Yeol Yu, Jeongwhan Choi, Woojin Cho, Kookjin Lee, Nayong Kim, Kiseok Chang, ChangSeung Woo, Ilho Kim, SeokWoo Lee, Joon-Young Yang, Sooyoung Yoon, and Noseong Park. Learning flexible body collision dynamics with hierarchical contact mesh transformer. In *The Twelfth International Conference on Learning Representations, ICLR 2024, Vienna, Austria, May 7-11, 2024.* OpenReview.net, 2024. URL https://openreview.net/forum?id=90yw2uM6J5.
- Manzil Zaheer, Satwik Kottur, Siamak Ravanbakhsh, Barnabás Póczos, Ruslan Salakhutdinov, and Alexander J. Smola. Deep sets. *Advances in Neural Information Processing Systems*, 2017.
- Fuzhen Zhuang, Zhiyuan Qi, Keyu Duan, Dongbo Xi, Yongchun Zhu, Hengshu Zhu, Hui Xiong, and Qing He. A comprehensive survey on transfer learning. *Proceedings of the IEEE*, 2020.
- Olek C Zienkiewicz and Robert Leroy Taylor. The finite element method for solid and structural mechanics. Elsevier, 2005.
- Olek C Zienkiewicz, Robert Leroy Taylor, and Perumal Nithiarasu. The finite element method for fluid dynamics. Butterworth-Heinemann, 2013.
- Clemens Zimmerling, Christian Poppe, Oliver Stein, and Luise Kärger. Optimisation of manufacturing process parameters for variable component geometries using reinforcement learning. *Materials and Design*, 214:Art.–Nr.: 110423, 2022. ISSN 0264-1275, 0141-5530, 0261-3069, 1873-4197, 1878-2876. doi: 10.1016/j.matdes.2022.110423.

A Mathematical formulations of Movement Primitives

We provide an overview of the probabilistic dynamic movement primitives (ProDMP) formulations utilized in this paper, starting with the foundational methods: Dynamic Movement Primitives (DMPs) and Probabilistic Movement Primitives (ProMPs).

A.1 DMPs

Schaal (2006) introduced Dynamic Movement Primitives (DMPs), which integrate a forcing term into a dynamical system to generate smooth trajectories from given initial conditions⁴, such as a robot's position and velocity at a particular time. A DMP trajectory is governed by a second-order linear ordinary differential equation (ODE) as follows:

$$\tau^{2}\ddot{y} = \alpha(\beta(g-y) - \tau\dot{y}) + f(x), \quad f(x) = x \frac{\sum \varphi_{i}(x)w_{i}}{\sum \varphi_{i}(x)} = x \varphi_{x}^{\mathsf{T}} \boldsymbol{w}, \tag{7}$$

where y = y(t), $\dot{y} = \mathrm{d}y/\mathrm{d}t$, and $\ddot{y} = \mathrm{d}^2y/\mathrm{d}t^2$ denote the position, velocity, and acceleration of the system at a specific time t, respectively. Constants α and β are spring-damper parameters, g is the goal attractor, and τ is a time constant modulating the speed of trajectory execution.

The functions $\varphi_i(x)$ represent the basis functions for the forcing term, as shown in Fig. 10a, while the phase variable $x = x(t) \in [0, 1]$ captures the execution progress. The trajectory's shape is determined by the weight parameters $w_i \in \mathbf{w}$ for i = 1, ..., N and the goal term g. The trajectory $[y_t]_{t=0:T}$ is typically computed by numerically integrating the dynamical system from the start to the endpoint. However, this numerical process is computationally expensive (Bahl et al., 2020; Li et al., 2023), as its cost scales with the trajectory length and the resolution of the numerical integration.

A.2 ProMPs

Paraschos et al. (2013) introduced the Probabilistic Movement Primitives (ProMPs) framework for modeling trajectory distributions, effectively capturing both temporal and inter-dimensional correlations. Unlike DMPs, which rely on a forcing term, ProMPs directly model the desired trajectory and its distribution using a linear basis function representation. Given a weight vector \boldsymbol{w} or a weight vector distribution $p(\boldsymbol{w}) \sim \mathcal{N}(\boldsymbol{w}|\boldsymbol{\mu_w}, \boldsymbol{\Sigma_w})$, the corresponding trajectory or trajectory distribution is computed as follows:

Compute Trajectory:
$$[y_t]_{t=0:T} = \mathbf{\Phi}^{\mathsf{T}} \mathbf{w},$$
 (8)

Compute Distribution:
$$p([y_t]_{t=0:T}; \ \boldsymbol{\mu_u}, \boldsymbol{\Sigma_u}) = \mathcal{N}(\boldsymbol{\Phi}^{\mathsf{T}} \boldsymbol{\mu_w}, \ \boldsymbol{\Phi}^{\mathsf{T}} \boldsymbol{\Sigma_w} \boldsymbol{\Phi}).$$
 (9)

Here, the matrix Φ contains the basis functions for each time step $t \in [0, T]$, shown in Fig. 10a. The trajectory shape is determined by the weight parameters $w_i \in \boldsymbol{w}$ through matrix-vector multiplication. Despite their simplicity and computational efficiency, ProMPs lack an intrinsic dynamic system, limiting their ability to specify a given initial condition for a trajectory or predict smooth transitions between two ProMP trajectories with differing parameter vectors.

A.3 ProDMPs

Solving the ODE underlying DMPs Li et al. (2023) observed that the governing equation of DMPs, as described in Eq. (7), admits an analytical solution. We re-express the original ODE from Eq. (7) and its homogeneous counterpart in standard ODE forms as follows:

Non-homo. ODE:
$$\ddot{y} + \frac{\alpha}{\tau}\dot{y} + \frac{\alpha\beta}{\tau^2}y = \frac{f(x)}{\tau^2} + \frac{\alpha\beta}{\tau^2}g \equiv F(x,g),$$
 (10)

Homo. ODE:
$$\ddot{y} + \frac{\alpha}{\tau}\dot{y} + \frac{\alpha\beta}{\tau^2}y = 0.$$
 (11)

⁴In mathematics, an initial condition refers to the value of a function or its derivatives at a starting point, which can be specified at any time, not necessarily at t = 0.

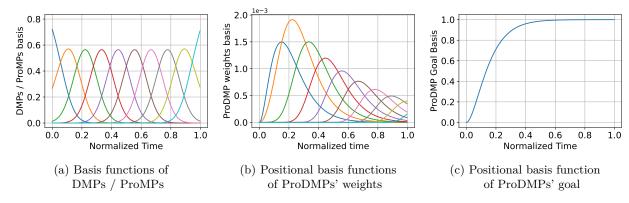


Figure 10: Illustration of basis functions used in MP methods. (a) Normalized radial basis functions used in DMPs in Eq.(7) and ProMPs in Eq.(8), respectively. (b) Positional basis functions of ProDMPs' weights \boldsymbol{w} and (c) ProDMPs' goal g in Eq.(17). In ProDMPs, g is concatenated with the weights vector \boldsymbol{w} and treated as one dimension of the resulting vector \boldsymbol{w}_g . Both weights and goal basis functions are computed from solving the DMPs' underlying ODE, following the procedure from Eq.(12) to Eq.(16)

The solution to this ODE is essentially the position trajectory, and its time derivative yields the velocity trajectory. They are formulated through several time-dependent function as:

$$y = \begin{bmatrix} y_2 \boldsymbol{p_2} - y_1 \boldsymbol{p_1} & y_2 q_2 - y_1 q_1 \end{bmatrix} \begin{bmatrix} \boldsymbol{w} \\ g \end{bmatrix} + c_1 y_1 + c_2 y_2$$
 (12)

$$\dot{y} = \begin{bmatrix} \dot{y}_2 \boldsymbol{p_2} - \dot{y}_1 \boldsymbol{p_1} & \dot{y}_2 q_2 - \dot{y}_1 q_1 \end{bmatrix} \begin{bmatrix} \boldsymbol{w} \\ g \end{bmatrix} + c_1 \dot{y}_1 + c_2 \dot{y}_2. \tag{13}$$

Here, the learnable parameters $[\boldsymbol{w}, g]^T$ which control the shape of the trajectory, are separable from the remaining time-dependent functions $y_1, y_2, \boldsymbol{p}_1, \boldsymbol{p}_2, q_1, q_2$. These functions are computed by solving the ODE in Eq. (10), (11):

$$y_1(t) = \exp\left(-\frac{\alpha}{2\tau}t\right),$$
 $y_2(t) = t\exp\left(-\frac{\alpha}{2\tau}t\right),$ (14)

$$\boldsymbol{p}_{1}(t) = \frac{1}{\tau^{2}} \int_{0}^{t} t' \exp\left(\frac{\alpha}{2\tau}t'\right) x(t') \boldsymbol{\varphi}_{x}^{\mathsf{T}} dt', \qquad \boldsymbol{p}_{2}(t) = \frac{1}{\tau^{2}} \int_{0}^{t} \exp\left(\frac{\alpha}{2\tau}t'\right) x(t') \boldsymbol{\varphi}_{x}^{\mathsf{T}} dt', \tag{15}$$

$$q_1(t) = \left(\frac{\alpha}{2\tau}t - 1\right)\exp\left(\frac{\alpha}{2\tau}t\right) + 1, \qquad q_2(t) = \frac{\alpha}{2\tau}\left[\exp\left(\frac{\alpha}{2\tau}t\right) - 1\right].$$
 (16)

Here, the function y_1, y_2 are the complementary solutions to the homogeneous ODE presented in Eq.(11), with \dot{y}_1, \dot{y}_2 their time derivatives respectively.

It's worth noting that p_1 and p_2 cannot be derived analytically due to the complexity of the forcing basis terms φ_x . Consequently, these terms must be computed numerically. However, isolating the learnable parameters, namely w and g, enables the reuse of other time-dependent functions across all generated trajectories.

ProDMPs identify these reusable terms as the position and velocity basis functions, denoted by $\Phi(t)$ and $\dot{\Phi}(t)$, respectively. Fig. 10b and Fig. 10c illustrate the resulting position basis functions for the weights \boldsymbol{w} and the goal g, respectively. These functions are pre-computed offline and treated as constants during online learning. When \boldsymbol{w} and g are combined into a concatenated vector, represented as \boldsymbol{w}_g , the position and velocity trajectories can be expressed in a manner similar to that used by ProMPs:

Position:
$$y(t) = \Phi(t)^{\mathsf{T}} w_q + c_1 y_1(t) + c_2 y_2(t),$$
 (17)

Velocity:
$$\dot{y}(t) = \dot{\boldsymbol{\Phi}}(t)^{\mathsf{T}} \boldsymbol{w}_q + c_1 \dot{y}_1(t) + c_2 \dot{y}_2(t).$$
 (18)

In the main paper, for simplicity and notation convenience, we use w instead of w_g to describe the parameters and goal of ProDMPs.

Trajectory's Initial Condition The coefficients c_1 and c_2 are solutions to the initial value problem defined by Eqs.(17)(18). Assuming the trajectory starts at time t_b with position y_b and velocity \dot{y}_b , we denote the values of the complementary functions and their derivatives at the condition time t_b as $y_{1_b}, y_{2_b}, \dot{y}_{1_b}$ and \dot{y}_{2_b} . Similarly, the values of the position and velocity basis functions at t_b are denoted as Φ_b and $\dot{\Phi}_b$ respectively. Using these notations, c_1 and c_2 are computed as:

$$\begin{bmatrix} c_1 \\ c_2 \end{bmatrix} = \begin{bmatrix} \frac{\dot{y}_{2_b} y_b - y_{2_b} \dot{y}_b}{y_{1_b} \dot{y}_{2_b} - y_{2_b} \dot{y}_{1_b}} + \frac{y_{2_b} \dot{\Phi}_b^{\mathsf{T}} - y_{2_b} \Phi_b^{\mathsf{T}}}{y_{1_b} \dot{y}_{2_b} - y_{2_b} \dot{y}_{1_b}} \boldsymbol{w}_g \\ \frac{y_{1_b} \dot{y}_{2_b} - y_{2_b} \dot{y}_{1_b}}{y_{1_b} \dot{y}_{2_b} - y_{2_b} \dot{y}_{1_b}} + \frac{\dot{y}_{1_b} \Phi_b^{\mathsf{T}} - y_{1_b} \dot{\Phi}_b^{\mathsf{T}}}{y_{1_b} \dot{y}_{2_b} - y_{2_b} \dot{y}_{1_b}} \boldsymbol{w}_g \end{bmatrix}.$$
(19)

Set Goal Convergence Relative to Initial Condition The goal attractor g in the ProDMPs framework represents an asymptotic convergence point for the dynamical system as $t \to \infty$, typically defined as an absolute coordinate. However, the goal term can also be modeled relative to the initial position y_b . In this approach, the relative goal $g_{\rm rel}$ is predicted, and its absolute counterpart is computed as $g_{\rm abs} = g_{\rm rel} + y_b$. This approach is particularly useful for predicting the goal in the coordinate system relative to a node's starting position. Since we aim to achieve a translation-equivariant approach (where absolute node positions are encoded as relative edge features between nodes), predicting relative goal positions aligns well with this design principle.

B Architecture and Method Details

This section offers detailed insights into our methodology and the architectural decisions guiding our approach.

B.1 Graph Encodings

In processing the initial graph \mathcal{G}_{*,T^c} , we create edges between the mesh and the collider based on a radius graph. Specifically, we connect mesh and collider nodes for *Deformable Block* and *Tissue Manipulation* if their euclidean distance is smaller than 0.3. In the *Tissue Manipulation* task, the collider is given as a single node which is connected to the tip of the tissue. It marks the grasping point of a gripper. In the *Sheet Deformation* task, we add an additional node feature to the nodes which get directly influenced by the external force. Therefore, no collider is used in this task. For the *Falling Teddy Bear* and the *Mixed Objects Falling* task, we implicitly model the ground as a collider by adding the current z position of every node to its node features (Sanchez-Gonzalez et al., 2018). This quantity gets updated for the step-based methods.

B.2 ProDMP Details

Initialization of ProDMPs necessitates node velocities for the anchor time step T^c . We employ a linear approximation, leveraging data from the previous time step $T^c - 1$.

Similar to the relative encoding of node positions in the MPN, we employ a technique in ProDMP to derive relative trajectories. Initially, we integrate a relative goal position as part of the node weights \mathbf{w}_v . Utilizing this approach, trajectories commence from the origin and traverse towards their respective relative goals. Subsequently, we adjust all positions by the initial position. This strategy fosters model generalization across various nodes.

The parameter τ , as described in Equation 7, is learned globally across all tasks using a compact MLP. The model's final layer employs a scaled sigmoid function for parameter estimation.

C Experimental Protocol

In order to promote reproducibility, we provide details of our experimental methodology. Table 1 presents the hyperparameters used in our experiments. For a comprehensive description of the creation of all datasets, please refer to Appendix D.

The training took place on an NVIDIA A100 GPU, with each method given the same computation budget of 48 hours, except for the *Sheet Deformation* task, where the computation budget was set to 24 hours. Consequently, the number of epochs varied, as the batching differed significantly between the trajectory-based method M3GN and the step-based MGN. We adapted the batchsize of the step-based methods in order to use the GPU memory efficiently. M3GN is always trained on one full trajectory per batch. Here, the whole context is processed in parallel and the remaining trajectory is predicted and compared to the ground truth.

We conducted a multi-staged grid-based hyperparameter search for the learning rate, input noise, and other hyperparameters as the latent task description dimension. In general, we optimized all methods on all tasks separately, however, we noticed that over different tasks and methods some parameters had the same best configuration. We did not use the test data for this, but tuned all hyperparameters on a separate validation split. This split was also used to determine the best epoch checkpoint to mitigate any overfitting effects.

In the end, all methods worked well with a learning rate of 5.0×10^{-4} except in the *Sheet Deformation* task. Here, our hyperparameter optimization indicated that the trajectory based methods benefit from a smaller learning rate of 1.0×10^{-5} . For MGN, we experimented with different input noise scales. Notably, for the *Deformable Block* and the *Sheet Deformation* task, a smaller noise scale improved performance significantly. In the falling objects tasks, we also explored second-order predictions, such as node accelerations, instead of velocity predictions. Following the approach in Pfaff et al. (2021), we adjusted the labels accordingly and conducted preliminary evaluations. However, since direct velocity predictions yielded superior results, we opted for them as our final approach, as presented in the main paper.

C.1 EGNO Training

For the Equivariant Graph Neural Operator (EGNO) method, we used the original code from Xu et al. (2024) for the model implementation. Since EGNO can only predict for a fixed next horizon, we cut the remaining prediction when using a later anchor time step. This is done during training and evaluation.

C.2 MGN Training

We mainly follow Pfaff et al. (2021) for the training of the MGN baseline. The only difference is the incorporation of current and historic velocity node features. Pfaff et al. (2021) consider this in their experiments but they show in their experiment suite that it does not improve the results and can lead to overfitting. This is different to our results. For us, on all tasks except *Mixed Objects Falling*, adding the current and historic velocities of nodes improves the results. We follow the Gaussian random walk noise injection for the velocity features from Sanchez-Gonzalez et al. (2020).

D Datasets and Preprocessing information

In this section, we give detailed information about the datasets we used. We report a general overview of all datasets in Table 2. Here each dataset is abbreviated for brevity as the following:

Table 2 lists in detail the datasets used in the paper. Each dataset is abbreviated for brevity and explained as follows:

• SD.: Sheet Deformation

• **DB**: Deformable Block

• TM.: Tissue Manipulation

• FTB.: Falling Teddy Bear

• MOF.: Mixed Objects Falling

Table 1: Table listing the hyperparameters and configurations of the experiments

Parameter	Value
Node feature dimension	128
Latent task description dimension	64
Decoder hidden dimension	128
Message passing blocks	15
Message passing blocks (EGNO)	5
GNN Aggregation function	Mean
GNN Activation function	Leaky ReLU
M3GN Context Aggregation method	Max Aggr.
M3GN Latent Node Aggregation method	No Aggr.
Learning rate	5.0×10^{-4}
Learning rate (Sheet Def. MP-based methods)	1.0×10^{-5}
Number of ProDMP basis functions	30
ProDMP $ au$	learned
	range: $[0.3, 3.0]$
ProDMP Relative start position	True
MGN input mesh noise	0.01
MGN input mesh noise (Def. Block)	0.001
MGN input mesh noise (Sheet Def.)	0.0001
MGN history length (all tasks except Mixed Objects Fall)	2
MGN history length (Mixed Objects Fall)	0
M3GN history length (all tasks except <i>Tiss. Man.</i> and <i>Sheet Def. (OOD)</i>)	1
M3GN history length (Tiss. Man. and Sheet Def. (OOD))	0
Minimum/Maximum Train Context Size (Sheet Deformation)	2 / 15
Minimum/Maximum Train Context Size (Deformable Block)	2 / 15
Minimum/Maximum Train Context Size (Tissue Manipulation)	2 / 40
Minimum/Maximum Train Context Size (Falling Teddy Bear)	10 / 50
Minimum/Maximum Train Context Size (Mixed Objects Fall)	10 / 50
Threshold to create collider-mesh edge	0.3

Table 2: Table listing the datasets and their configurations

Name	Train/Val/Test Splits	Number of steps	Number of Nodes	Collider interaction
SD.	630/135/135	50	225	External Force
DB.	675/135/135	39	81	Rigid Collider
TM.	600/120/120	100	361	Grasping point
FTB.	700/150/150	200	304	Boundary Condition
MOF.	1800/360/360	200	up to 350	Boundary Condition

D.1 Sheet deformation

We select 9 different Young's modulus ranging between 10 and 1000 from a very deformable to an almost stiff sheet. Then, per material, we compute 100 simulations using Abaqus where the positions of the two acting forces are randomized. The boundary nodes of the sheet are kept in place. From every material configuration, we take 70 simulations for training and 15 simulations for validation and testing respectively. For the out-of-distribution task, we trained using Young's modulus values ranging from 60 to 500 and tested using values of 10, 30, 750, and 1000.

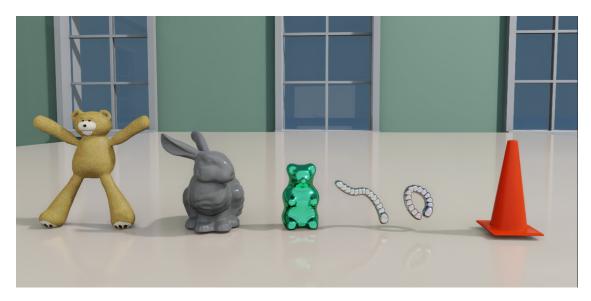


Figure 11: Six objects used in the *Mixed Objects Falling* task. From left to right: Teddy Bear, Bunny, Gummy Bear, Gummy Worm 1, Gummy Worm 2, and Traffic Cone.

D.2 Deformable Block

The original task was introduced in Linkerhägner et al. (2023), generated using SOFA (Faure et al., 2012). It uses 3 different Poisson's ratios and 9 different trapezoidal meshes. We increase the difficulty of this dataset by introducing more complex initial starting conditions. This is done by selecting a random Poisson's ratio, simulating for 11 steps, and then switching to another Poisson's ratio. Then, the simulation continues for 39 steps. The first 11 steps are then discarded and step 12 is then the initial step for the dataset (and is referred to step 0 throughout the paper).

D.3 Tissue Manipulation

We use the original task introduced in Linkerhägner et al. (2023) without alterations. This dataset was also generated using SOFA (Faure et al., 2012).

D.4 Falling Teddy Bear

Each trajectory of the dataset was created by choosing an angle from $[0^{\circ}, 360^{\circ}]$ for the first time step. To vary the material properties, we randomly select combinations of Young's modulus and Poisson's ratio from 1000 uniformly spaced values of the Young's modulus in $[1 \times 10^{5}, 1 \times 10^{6}]$ and 100 uniformly spaced values of the Poisson's ratio in [0.0, 0.499]. This dataset is generated using NVIDIA Isaac Sim (NVIDIA, 2022a), which utilizes PhysX 5.0 (NVIDIA, 2022b) to simulate tetrahedral meshes based on initial CAD models.

D.5 Mixed Objects Falling

The simulation uses the setup from *Falling Teddy Bear*. In addition to the Teddy, we include other objects to encourage diversity. In total, there are six different objects presented in the dataset. We report an image of their high-resolution meshes in Figure 11. From every object, we use 300 simulations for the training split and 60 simulations for the test and validation split respectively.

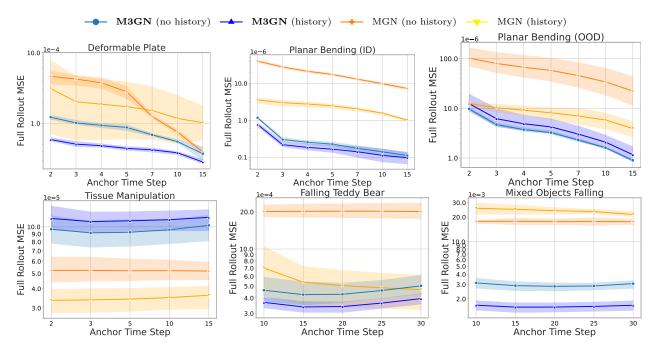


Figure 12: Log-scale MSE over full rollouts on the validation split for M3GN and MGN comparing history features. The better performing hyperparameter configuration was chosen for the final evaluation on the test dataset.

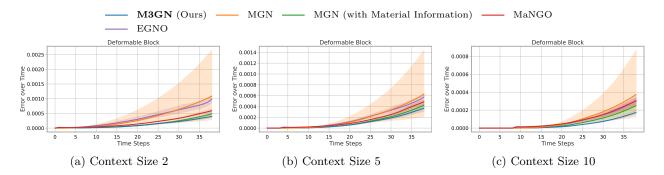


Figure 13: Per-timestep MSE for the *Deformable Block* task.

E Additional Results

E.1 Hyperparameter Optimization

We observed that the history inclusion of previous velocities has a big impact on the result of the simulation, depending on the task. To obtain optimal performance, we did an hyperparameter optimization on the validation split comparing history features. The results for M3GN and MGN are given in Figure 12.

E.2 Evaluations.

MSE over time To gain better insights into the rollout stability of the model predictions, we report the Mean Squared Error (MSE) over timesteps in Figure 13, 14, 15, 16, 17, and Figure 18. Overall, our model M3GN demonstrates great robustness against error accumulation, benefiting from the inherent trajectory representation provided by the ProDMP method. MGN works well on the *Tissue Manipulation* task, but fails to incorporate the correct context information on other tasks. EGNO performs in general worse except on the *Sheet Deformation* tasks.

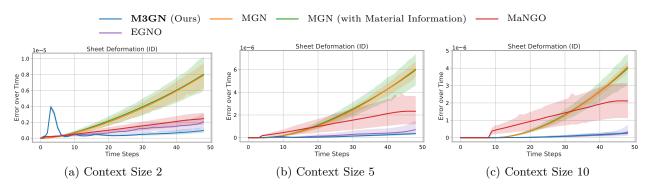


Figure 14: Per-timestep MSE for the Sheet Deformation (ID) task.

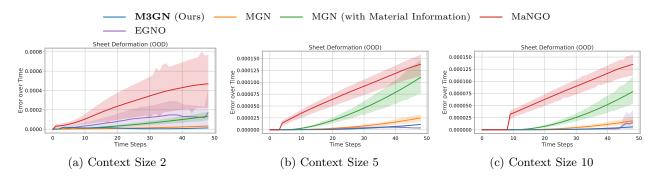


Figure 15: Per-timestep MSE for the Sheet Deformation (OOD) task.

E.3 Visualizations.

In Figure 19, we include a latent space visualization of the *Sheet Deformation* task, where simulations with 9 different Young's Modulus values are clustered according to their material properties. The t-SNE projection of the 64-dimensional latent node vectors demonstrates clear clustering, indicating that the model effectively captures and differentiates material characteristics based on learned task representations.

We further provide additional visualizations for M3GN, MGN and MGN (with Material Information) for exemplary simulations of all tasks. Each visualization shows the same simulated trajectory for different time steps (columns) and different methods (rows).

- Figure 20 shows a simulation of the Sheet Deformation task for a context set size of 5.
- Figure 21 visualizes the *Deformable Block* task for a context set size of 6.
- Figure 22 shows a *Tissue Manipulation* visualization for a context set size of 6.
- Figure 23 provides an examplary *Teddy Bear Falling* for a context set size of 20.
- Figure 24 and Figure 25 show two different simulated *Mixed Objects Falling* for a context set size of 20.

Across tasks, M3GN provides accurate simulations, whereas MGN, especially when not provided the additional material information as oracle knowledge, sometimes fails to respect the material properties or predicts a drift in the solution for later time steps.

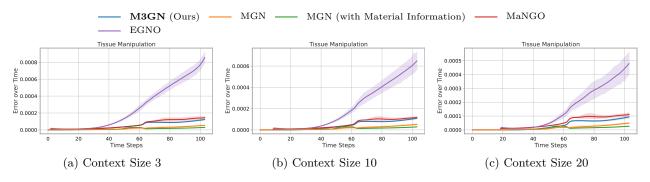


Figure 16: Per-timestep MSE for the Tissue Manipulation task.

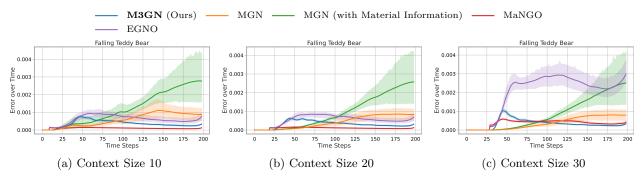


Figure 17: Per-timestep MSE for the Falling Teddy Bear task.

E.4 Runtime, memory and parameter comparison.

In Table 3, we provide the runtime, memory, and parameter comparison of all methods on the four benchmark task during inference. We split up the total inference time into context encoding and simulation time for M3GN.

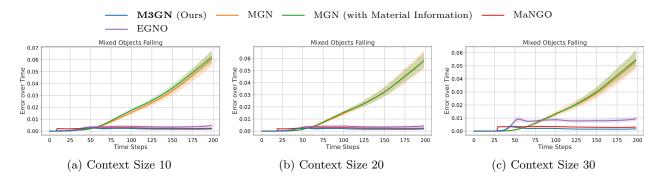


Figure 18: Per-timestep MSE for the $\it Mixed Objects Falling task.$

Table 3: Runtime, memory, and parameter comparison of all methods on the four benchmark tasks.

Task	Metric	M3GN (Ours)	MGN	EGNO	Mango
Deformable Block	Context Encoding Time [s]	0.0062	0.0000	0.0000	0.0000
	Simulation Time [s]	0.0132	0.2673	0.0134	0.0628
	Total Inference Time [s]	0.0194	0.2673	0.0134	0.0628
	GPU Memory Usage [MB]	68.33	26.94	121.43	126.10
	# Parameters	2542847	1259394	1000026	2990082
Sheet Deformation	Context Encoding Time [s]	0.0066	0.0000	0.0000	0.0000
	Simulation Time [s]	0.0132	0.3177	0.0242	0.1247
	Total Inference Time [s]	0.0198	0.3177	0.0242	0.1247
	GPU Memory Usage [MB]	170.27	29.12	210.69	324.03
	# Parameters	2546206	1259779	999258	2990211
	Context Encoding Time [s]	0.0083	0.0000	0.0000	0.0000
	Simulation Time [s]	0.0135	0.7531	0.0802	0.4705
Tissue Manipulation	Total Inference Time [s]	0.0218	0.7531	0.0802	0.4705
	GPU Memory Usage [MB]	569.70	45.40	759.84	748.71
	# Parameters	2547614	1259907	1000794	2990723
Mixed Objects Falling	Context Encoding Time [s]	0.0354	0.0000	0.0000	0.0000
	Simulation Time [s]	0.0143	1.1961	0.1347	0.7442
	Total Inference Time [s]	0.0497	1.1961	0.1347	0.7442
	GPU Memory Usage [MB]	1340.79	42.56	1406.92	1405.34
	# Parameters	2 545 950	1259651	999 130	2990083

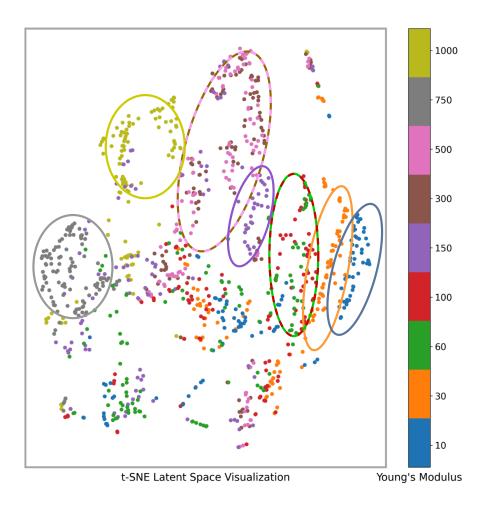


Figure 19: This figure shows a latent space visualization of the Sheet Deformation task for trajectories with 9 different Young's Modulus values, using a context size of 10. Each dot represents a 64-dimensional latent node vector projected to 2D using the t-SNE algorithm (van der Maaten & Hinton, 2008). Dots of the same color correspond to latent node descriptions for the same task, each simulated with a unique Young's Modulus. The visualization reveals distinct clustering in the latent space, with similar material properties grouped closer together, highlighting the relationship between material characteristics and the learned task representations. To improve clarity, points corresponding to nodes on the plate's edge were excluded, as their constant boundary condition resulted in unvarying latent descriptions.

Sheet Deformation

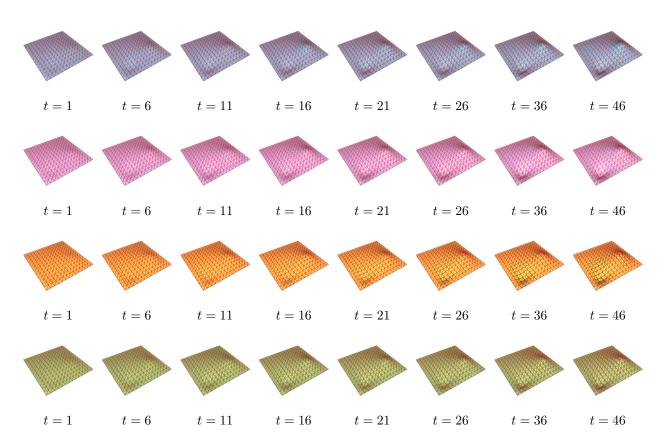


Figure 20: Simulation over time of an exemplary test trajectory from the **Sheet Deformation** task by M3GN (blue), EGNO (purple), MGN (orange), and MGN with material information (green). The **context set size** is set to 5. All visualizations show the colored **predicted mesh**, a **collider** or floor, and a **wireframe** (red) of the ground-truth simulation. M3GN can accurately predict the correct material properties, resulting in a highly accurate simulation.

Deformable Block

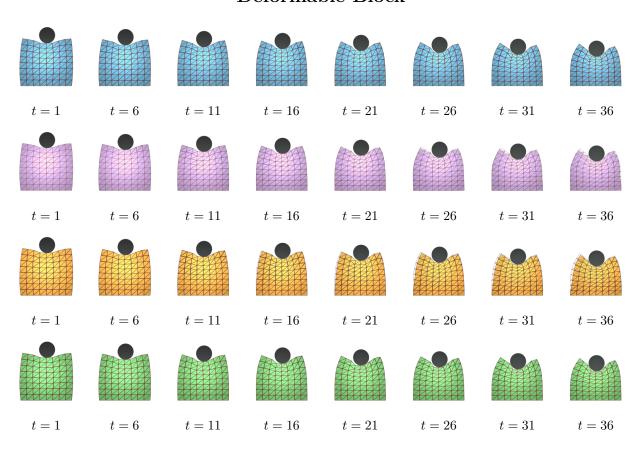


Figure 21: Simulation over time of an exemplary test trajectory from the **Deformable Block** task by M3GN (blue), EGNO (purple), MGN (orange), and MGN with material information (green). The **context set size** is set to 5. All visualizations show the colored **predicted mesh**, a **collider or floor**, and a **wireframe** (red) of the ground-truth simulation. M3GN can accurately predict the correct material properties, resulting in a highly accurate simulation.

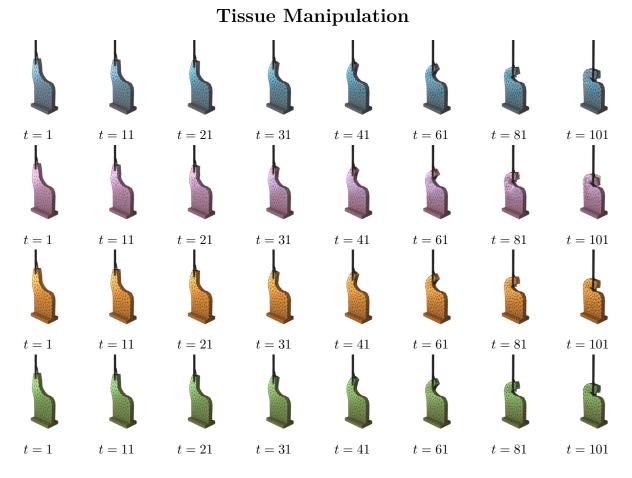


Figure 22: Simulation over time of an exemplary test trajectory from the **Tissue Manipulation** task by M3GN (blue), EGNO (purple), MGN (orange), and MGN with material information (green). The **context** set size is set to 5. All visualizations show the colored **predicted mesh**, a collider or floor, and a wireframe (red) of the ground-truth simulation. All methods can solve the task, however MGN is drifting a tiny bit to the left over time.

Falling Teddy Bear

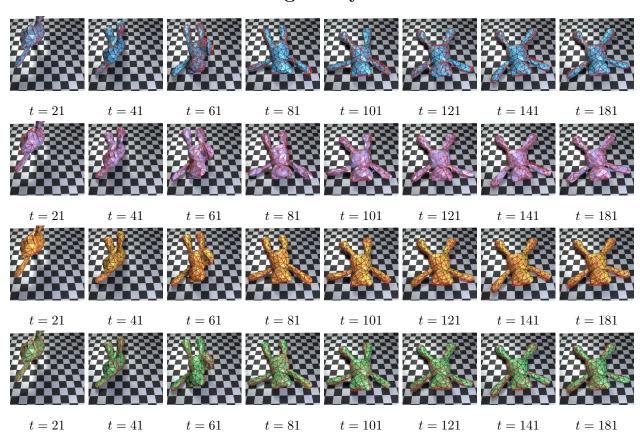


Figure 23: Simulation over time of an exemplary test trajectory from the Falling Teddy Bear task by M3GN (blue), EGNO (purple), MGN (orange), and MGN with material information (green). The context set size is set to 20. All visualizations show the colored predicted mesh, a collider or floor, and a wireframe (red) of the ground-truth simulation. M3GN significantly outperforms both step-based baselines.

Mixed Objects Fall (Bunny)

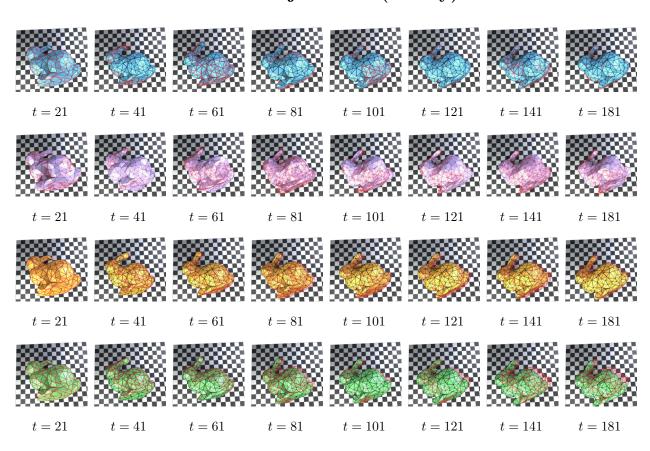


Figure 24: Simulation over time of a bunny from the **Mixed Objects Fall** task by M3GN (blue), MGN (orange), EGNO (purple), and MGN with material information (green). The **context set size** is set to 20. All visualizations show the colored **predicted mesh**, a **collider or floor**, and a **wireframe** (red) of the ground-truth simulation. M3GN significantly outperforms both step-based baselines.

Mixed Objects Fall (Traffic Cone)

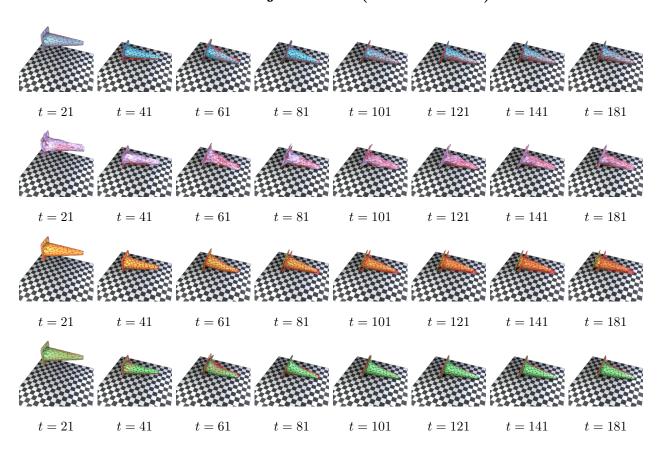


Figure 25: Simulation over time of a traffic cone from the **Mixed Objects Fall** task by M3GN (blue), EGNO (purple), MGN (orange), and MGN with material information (green). The **context set size** is set to 20. All visualizations show the colored **predicted mesh**, a **collider or floor**, and a **wireframe** (red) of the ground-truth simulation. M3GN significantly outperforms both step-based baselines. The simulation generated by MGN is severly affected by drift.