Guiding Explanation-based NLI through Symbolic Inference Types

Anonymous ACL submission

Abstract

In this work, we investigate the localised, quasisymbolic inference behaviours in distributional representation spaces by focusing on the 004 Explanation-based Natural Language Inference (NLI), exemplified by the syllogistic-deductive NLI, where two explanations (premises) are provided to derive a single conclusion. We first establish the connection between natural language and symbolic inferences by characterising quasi-symbolic NLI behaviours, named symbolic inference types. Next, we establish the theoretical connection between distribu-013 tional and symbolic inferences by formalising the Transformer encoder-decoder NLI model as a latent variable model. We provide extensive experiments to reveal that the symbolic in-017 ference types can enhance model training and inference dynamics, and deliver localised, symbolic inference control. Based on these findings, we conjecture the different inference behaviours are encoded as functionally separated subspaces in latent parametric space, as the fu-023 ture direction to probe the composition and generalisation of symbolic inference behaviours in 024 distributional representation spaces.

1 Introduction

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Explanatory sentences (Jansen et al., 2018b), such as *animal is a kind of living thing*, can encode hierarchical, taxonomic, and causal relations between concepts (Gardenfors and Zenker, 2015). By understanding and reasoning over these concepts expressed by explanations, humans can make intricate decisions, which is significant in scientific, cognitive, and AI domains. In this work, we centre on the Explanation-based Natural Language Inference (NLI) task, exemplified by syllogisticdeductive NLI, where two explanations (premises) are provided to derive a single conclusion. Within this task, a central challenge involves achieving localised and (quasi-)symbolic inference behaviour. E.g., given the two premises: *milk is a kind of*



Figure 1: Conceptual visualisation for the proposed *Quasi-symbolic NLI Representation* approach. Inference types can be encoded as functional subspaces, which are separated or disentangled in parametric space. Thus, by manipulating the inference types, we can deliver localised, symbolic inference control.

liquid and *liquid can flow*, one may derive the conclusion *milk can flow* by localising *can flow* and substituting the concept *liquid* with *milk*.

A key question then arises: How can we train current Transformer-based NLI models to learn and generalise this quasi-symbolic behaviour in the distributional representation space? Investigating this question allows us to shorten the gap between deep latent semantics and formal linguistic representations (Gildea and Jurafsky, 2000; Banarescu et al., 2013), integrating the flexibility of distributionalneural models with the properties of linguistically grounded representations, facilitating both interpretability and generative control.

Recent studies have demonstrated that the Argument Structure Theory (AST) representation (Jackendoff, 1992) from explanations can be effectively represented, localised, and disentangled in the latent space of Transformer-based models (Zhang et al., 2024a,c). A particular instance of an AST representation is the Abstract Meaning Representation (AMR) (Banarescu et al., 2013), which represents the relations between semantic variables, allowing us to first establish the con042

nection between natural and symbolic language inferences. Specifically, we leverage the AMR to *systematically characterise quasi-symbolic inference behaviours, named symbolic inference types, grounded on AMR symbolic graphs.* Using the explanation-based NLI dataset (EntailmentBank, Dalvi et al. (2021)), we identify ten categories of symbolic transformations and provide annotations for 5,134 premise-conclusion pairs. Illustrative examples are presented in Section 3 and Table 1.

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Next, we aim to establish the theoretical connection between distributional and symbolic inferences from the perspective of neural representation space (see Section 4). An ideal neuro-symbolic NLI model should demonstrate two core representational capabilities: (i) the capacity to encode and utilise inference rules and (ii) the ability to extract semantic features.

As for the former, we formalise the Transformerbased encoder-decoder NLI architecture (e.g., T5) as a latent variable NLI framework, in which *the symbolic inference types are injected to guide the dynamics of symbolic inference behaviours within the latent parametric space*. With respect to the latter, we introduce a feature space (i.e., sentence bottleneck) in the middle of the latent variable NLI architecture. Ideally, this low-dimensional feature space encodes sufficiently abstract, high-level semantic representations during inference.

We provide extensive experiments to evaluate the training and inference dynamics (Section 5.1), localised inference control (Section 5.2), and feature representation with explanation inference retrieval task (Section 5.3). Experimental results reveal that the symbolic inference type can assist model training, inference, and deliver localised inference control. Based on these observations, we conjecture that *in Transformers, different inference behaviours are encoded as functional subspaces which are separated or disentangled in the latent parametric space.*

In summary, this work provides a complete initial step in investigating the quasi-symbolic inference over distributional semantic space, with the following contributions: (1) We first establish the connection between natural and symbolic language inferences from the perspective of linguistics by systematically characterising quasi-symbolic inference behaviours, named symbolic inference types, grounded on the AMR graph. (2) We establish the distributional-symbolic connection from the perspective of neural representation space: (3) We frame the Transformer-based encoder-decoder NLI model as a latent variable model where the dynamics of inference behaviours are guided via our symbolic inference types in the latent space. (4) We investigate the latent space for encoding abstract, high-level features during inference. Experimental results showed that the injected symbolic inference type can improve model training dynamics, inference, and localisation. Based on those findings, we conjecture that different inference types are encoded as functional subspaces which are separated or disentangled in the parametric space, as a future direction to probe the composition and generalisation of symbolic inference behaviours in distributional representation spaces. The experimental pipelines are released¹.

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2 Related Work

In this section, we review the related work around two topics: *neuro-symbolic representation* and *latent variable model and control*, to highlight the current research limitation and elucidate the motivation underlying our work.

Neuro-symbolic representation. A longstanding goal in NLP is to blend the representational strengths of neural networks with the interpretability of symbolic systems to build more robust NLI models. Current methods usually inject symbolic behaviour through explicit symbolic representations, including graph (Khashabi et al., 2018; Khot et al., 2017; Jansen et al., 2017; Kalouli et al., 2020; Thayaparan et al., 2021), linear programming (Valentino et al., 2022b; Thayaparan et al., 2024), adopting iterative methods, using sparse encoding mechanisms (Valentino et al., 2020; Lin et al., 2020), synthetic natural language expression (Clark et al., 2020; Yanaka et al., 2021; Fu and Frank, 2024; Weir et al., 2024), symbolicrefined LLMs (Olausson et al., 2023; Quan et al., 2024), etc. Those studies ignore the underlying neuro-symbolic behaviour in neural representation space. From the Explainable AI domain, many studies have shown that neural networks can encode sparse neural-symbolic concepts without explicit symbolic injection across areas like image embedding (Ren et al., 2022; Deng et al., 2021; Li and Zhang, 2023), word embedding (Ethayarajh et al., 2018; Allen et al., 2019; Ri et al., 2023),

¹https://anonymous.4open.science/r/Inference_ type-5E07/

165contextual embedding (Gurnee et al., 2023; Nanda166et al., 2023; Li et al., 2024), and LLM interpre-167tation (Park et al., 2024; Templeton et al., 2024).168To address this research gap, we draw on neuro-169symbolic NLI objectives within distributional neu-170ral models, employing AMR-grounded inference171types to integrate distributional and symbolic forms172of inference.

Latent variable models and control. Latent 173 variable models, such as VAE (Kingma and 174 Welling, 2013), have shown the capability of sym-175 bolic representation, control, and interpretation 176 over the distributional space, which are widely 177 deployed in the NLP domain, such as disentangled representation learning (Zhang et al., 2024a,c), 179 style-transfer (Liu et al., 2023; Gu et al., 2023; 180 181 Zhang et al., 2024b), etc. Thus, we establish the connection between distributional and symbolic in-182 ferences by formalising the neural NLI models as latent variable models where the symbolic infer-184 ence type label can guide the dynamics of latent 185 variables in parametric space. This guidance has been widely investigated to improve training and inference dynamics, such as Conditional VAE (Car-188 valho et al., 2023), Diffusion (Dhariwal and Nichol, 189 2021; Ho and Salimans, 2022), normalising flow 190 (Rombach et al., 2020) etc.

In the next section, we start by defining the symbolic inference types for semantically bridging the natural language and symbolic inferences.

3 Defining Symbolic Inference Types

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Valentino et al. (2021) has demonstrated that stepwise explanation-based NLI cannot be directly framed as pure logical reasoning. Explanatory chains, while looking plausible at first inspection, commonly have subtler incompleteness and consistency problems from a logical point of view. Meanwhile, explanatory chains corresponding to definable inference patterns and symbolic operations can be localised over the sentence structure. Motivated by this middle ground between logical representations and lexico-semantic inference patterns, we introduce granular inference types based on explanatory sentences, using AMR to define the symbolic operations involved in step-wise inference, linking transformations from premises to conclusions². Table 1 describes the AMR-grounded inference types and examples from the EntailmentBank212corpus. Next, we define each lexico-semantic infer-
ence type and the corresponding symbolic forms.213



Figure 2: AMR argument substitution: the inference behaviour is defined as subgraph substitution.

The substitution category refers to obtaining a conclusion by replacing a predicate/argument term from one premise with a predicate/argument term from the other premise. Possible variations of this category include (1) argument (ARG) substitution, (2) predicate (PRED) substitution, and (3) frame (PRED+ARG) substitution. In this category, one premise is used to connect two terms which are usually connected by is a kind of, is a source of, etc. Conceptualising the AMR representation as a graph, this can be symbolically represented as a subgraph substitution operation over the premise graphs, as illustrated in Figure 2. The PRED substitution category works in a similar manner, but replacing a predicate term. The two predicates are usually linked by the following patterns: " v_1 is a kind of v_2 ", "to v_1 something means to v_2 something", etc. The frame (PRED+ARG) substitution category combines both previous categories by replacing a frame (predicate subgraph) of one of the premises with one from the other premise.

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²Please note that AMR is not used as a representation mechanism in the proposed architecture, but only to precisely ground these symbolic operations within a well-defined se-

mantic representation structure.

Original type	Symbolic type	Prop.	Example entailment relation
	ARG substitution		P1: a scar on the knee is a kind of scar
	(ARG-SUB)	19%	P2: a scar is an acquired characteristic
	(ARG-SOD)		C: a scar on the knee is an acquired characteristic
	PRED substitution		P1: food contains nutrients and energy for living things
Substitution	(PRED-SUB)	5%	P2: to contain something can mean to store something
	(IRED-SOD)		C: food stores nutrients and energy for living things
	Frame substitution		P1: the formation of diamonds requires intense pressure
	(FRAME-SUB)	20%	P2: the pressure is intense deep below earth 's crust
	(IRAML-SOD)		C: the formation of diamonds occurs deep below the crust of the earth
	Conditional frame		P1: if something is renewable then that something is not a fossil
Inference from Rule	insertion/substitution (COND-FRAME)	12%	P2: fuel wood is a renewable resource
			C: wood is not a fossil fuel
	ARG insertion (ARG-INS)		P1: solar energy comes from the sun
		18%	P2: solar energy is a kind of energy
Further Specification			P3: solar energy is a kind of energy that comes from the sun
or Conjunction	Frame conjunction (FRAME-CONJ)	6%	P1: photosynthesis stores energy
			P2: respiration releases energy
	(FRAME-CONJ)		C: photosynthesis stores energy and respiration releases energy
Infer Class	ARG/PRED		P1: rock is a hard material
from Properties	generalisation	1%	P2: granite is a hard material
fioni i toperues	(ARG/PRED-GEN)		C: granite is a kind of rock
	ARG substitution		P1: blacktop is made of asphalt concrete
Property Inheritance	(Property Inheritance)	0.4%	P2: asphalt has a smooth surface
	(ARG-SUB-PROP)		C: a blacktop has a smooth surface
			an optical telescope requires visible light for human to use
Causal Expression	Causality (IFT)	0.8%	clouds / dusts block visible light
-			if there is clouds or dusts, then the optical telescope cannot be used
			a shelter can be used for living in by raccoons
Example-based Inference	Example (EXAMPLE)	0.9%	some raccoons live in hollow logs
-			an example of a shelter is a raccoon living in a hollow log

Table 1: Examples of symbolic inference types, with their corresponding abbreviations provided in parentheses and used consistently throughout the paper. The EntailmentBank utilised for this task comprises 5,134 instances, with our annotations covering 84% of the (premises, conclusion) cases. These annotations are planned for public release.

The *further specification or conjunction* category allows for obtaining a conclusion by joining both premises. It includes (4) *ARG insertion* and (5) *frame conjunction*. In the case of *ARG insertion*, the conclusion is obtained by connecting an argument from one of the premises to a frame of the other. As for *frame conjunction/disjunction*, the conclusion is obtained by joining the premises graphs through a conjunction/disjunction node (*and*) or (*or*).

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The *inference from rule* category from (Dalvi et al., 2021) encompasses a specific instance of insertion or substitution, identified as (6) *conditional frame insertion/substitution*. In this category, a frame is either inserted or replaced as an argument of a premise, following a conditional pathway present in the other premise. This process is illustrated in Figure 5.

The inference type *infer class from properties* has been re-categorised as (7) *ARG or PRED generalisation*, where a new *:domain* relation frame is created if both premise graphs differ by a single predicate/argument term. (8) *Property inheritance*, on the other hand, is a special case of *ARG sub-* *stitution*, where one of the premises describes a *is made of* relationship between the entity in the other premise and its replacement.

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Finally, (9) *Causal Expression* and (10) *Examplebased Inference* categories are defined according to the key lexical characteristic of the conclusion, as systematic AMR transformations which could be applied without rephrasing the underlying explanatory sentences could not be determined. More details about the annotation procedure are provided in Appendix A.

Thus far, we have established a connection between natural and symbolic language inferences from the perspective of semantic representations through the AMR symbolic graph. In the next section, we aim to establish the distributionalsymbolic NLI connection from the point of neural representation space.

4 Latent Variable NLI Framework

Recent studies revealed that transformer-based language models can linearly encode abstract-level semantic concepts (latent variables, denoted by z) (Park et al., 2023; Li et al., 2024; Wang et al., 2024; Jiang et al., 2024). Following prior studies, we frame gradient-based neural NLI models as conditional latent variable models that can realise quasisymbolic inference dynamics. Assuming premises and conclusions share the same latent space where the explanatory entailment relation is computed in a probabilistic fashion, this allows for the framing of the entailment determination as the problem of learning a set of conditional probabilities among the latent variables. Figure 3 depicts an abstraction of the computational graph of the latent NLI/explanatory entailment framework.



Figure 3: Latent variable NLI framework, where x, z, and π are the observation space, latent space, and symbolic inference type label, respectively.

Latent variables and relations. We first propose a set of latent variables based on prior studies of Zhang et al. (2024a), which revealed that explanatory sentence semantics can be decomposed into semantic role - word content sets (denoted by rolecontent) according to Argument Structure Theory (AST) (Jackendoff, 1992). E.g., the sentence, 'animals require oxygen for survival', can be represented as:

$$\underbrace{animals}_{ARG0} \oplus \underbrace{require}_{PRED} \oplus \underbrace{oxygen}_{ARG1} \oplus \underbrace{for \ survival}_{ARGM-PRP}$$

where \oplus represents the composition operation under a compositional-distributional model (Clark et al., 2008). Each role-content set, such as ARGO-animals, is encoded as a convex cone in the latent space. Therefore, we consider each role-content as a latent variable. The latent representation of observed sentence x can be formalised as a set of latent variables: $x \leftrightarrow z^{(x)} =$ $\{(c_1, r_1), \ldots, (c_i, r_i), \ldots\}$ where \leftrightarrow represent the deterministic mapping between x and $z^{(x)}$ through the embedding layer, $c_i \in C$ and $r_i \in R$ represent the word content and semantic role at position i, C and R are the vocabularies of word content and semantic role category, predefined based on training corpus. Since an AMR representation is a particular instance of an AST representation, which

represents the relation between latent variables, by defining and manipulating the inference patterns over the AMR representation in the context of inference types, we can provide quasi-symbolic interpretation and control to the latent NLI model. In the next section, the targeted NLI task supported by the AMR-grounded inference types is formalised under a Bayesian inference framework.

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Latent **Bayesian** inference. Given а (premises, conclusion) explanatory sentence pair $\langle x_{p_0}, x_{p_1}, x_c \rangle$, an inference type $\pi \in \Pi$ can be associated, if exists a transformation $amr(x_{p_0}), amr(x_{p_1}) \rightarrow amr(x_c)$ defined over the set of transformations Π . The NLI process can be described as a Bayesian inference: $P(x_c|x_{p_0}, x_{p_1}) = P(x_c|z^{(x_c)})P(z^{(x_c)}|x_{p_0}, x_{p_1})$ where $P(z^{(x_c)}|x_{p_0}, x_{p_1})$ approximates the posterior inference via the encoder. Specifically, it first transform x_{p_0}, x_{p_1} into latent representations $z^{x_{p_0}}, z^{x_{p_1}}$. Subsequently, inference behaviour π is performed over the set of latent variables (e.g., substitution over latent variables set). The latent variables $z^{(x_c)}$ are retained for generation conclusion via decoder $P(x_c|z)$. To validate this inference process, we propose Proposition 1.

Proposition 1: The inference behaviour is materialised during the posterior inference stage and can be controlled by the injection of the associated inference type labels, Π , into the posterior. That is the conditional inference process:

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$$P(x_c|x_{p_0}, x_{p_1}, \pi) = P(x_c|z^{(x_c)})P(z^{(x_c)}|x_{p_0}, x_{p_1}, \pi)$$
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The inference type can be injected into the model at different points (e.g. at the encoder or decoder) and can be manipulated over different inference types to validate Proposition 1, as evaluated in Section 5.1. Finally, optimising the language modelling task approximates the latent variable space Z. This can be formalised as: $P(x_c) =$ $\prod_{i=1}^{N} P(c_i | c_{i-1}, \dots, c_1, Z)$ where c_i represent the *i*-th token.

Latent sentence space. To evaluate the feature representation capability, we next describe the methodological framework behind the construction of the latent sentence-level feature space within T5 (named T5 bottleneck). As for the encoding stage, $P(z|x_1, x_2)$, we calculate the mean of each dimension on all token embeddings and feed the resulting vector into a multi-layer perceptron

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to obtain the sentence embedding. As for the decoding stage, $(x_c|z)$, we reconstruct the token embeddings from a sentence representation with a linear MLP network and directly feed them into the cross-attention layers of the decoder: $\hat{Y} =$ MultiHead $(YW^q, MLP(z)W^k, MLP(z)W^v)$

> where \hat{Y} is the reconstruction of decoder input sequence $Y = [y_1, ..., y_K]$. Here, we only describe the optimal setup. We provide a systematic way to choose the best setup in the Appendix B.

5 Empirical Analysis

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The experiment is designed to address three key questions: Section 5.1: (i) Do symbolic inference types enhance model training and inference performance? Section 5.2: (ii) Can these inference types be utilised for prescriptive inference control? Section 5.3: (iii) Does the incorporation of a sentence bottleneck contribute to improved feature representation? All experimental details are provided in Appendix B.

5.1 Training and Inference Evaluation

Firstly, we evaluate (i) if symbolic inference types enhance model training and inference performance. We consider three mechanisms to conditionally inject the symbolic inference types into the latent space, which are described below, where p1, p2, and *con* are the premises and conclusion, respectively, and </s> is a special token for sentence separation.

i. The inference type as the prefix for the premises at the Encoder: *the inference type is* [*type*] </s> *p1* </s> *p2* ii. The inference type as the prefix for the conclusion in the Decoder: </s> the inference type is [*type*]. *con* iii. The inference type at the end of the conclusion in the Decoder: </s> con. the inference type is [*type*]

Training dynamics. We first quantitatively evaluate training performance based on five metrics: test loss (cross-entropy), perplexity (PPL), BLEURT (Sellam et al., 2020), BLEU (Papineni et al., 2002), and cosine similarity against sentenceT5 (Ni et al., 2021). We choose the T5, Bart (Lewis et al., 2019), GPT2 (Radford et al., 2019), our T5 bottleneck and Optimus (Li et al., 2020) with 768 latent dimensions as testbed. The performances are measured from the Entailment testset.

As illustrated in Table 2, all baselines with inference types always have lower test losses and PPLs, which means the inference type can help the model training. Furthermore, across all baseline models, incorporating inference types into the encoder consistently results in improved performance as measured by BLEU, Cosine, and BLEURT metrics. This finding suggests that the conditionalisation on inference types can support the inference representation, and the inference process has been performed inside the encoder (*Proposition1*).

Baseline	INJ	BLEU	Cosine	BLEURT	Loss↓	$PPL\downarrow$
S	eq2seq.	LM: enco	der-decod	ler architect	ure	
	DE	0.55	0.96	0.30	0.53	1.44
T5 original	DP	0.59	0.96	0.34	0.58	1.57
(small)	EP	0.65	0.97	0.45	0.52	1.41
(sman)	NO	0.54	0.96	0.22	0.69	2.22
	DE	0.46	0.96	0.23	0.49	1.33
T5 original	DP	0.53	0.96	0.25	0.51	1.38
(base)	EP	0.61	0.97	0.39	0.45	1.22
(buse)	NO	0.57	0.96	0.33	0.61	1.65
	DE	0.44	0.94	0.03	0.55	1.49
Bart	DP	0.38	0.93	-0.42	0.48	1.30
(base)	EP	0.57	0.96	0.23	0.58	1.57
	NO	0.54	0.96	0.17	0.63	1.71
ΤC	DE	0.60	0.97	0.46	0.40	1.49
T5 original	DP	0.64	0.97	0.44	0.46	1.58
(large)	EP	0.67	0.97	0.50	0.59	1.80
(imge)	NO	0.57	0.96	0.31	0.61	1.84
	DE	0.01	0.73	-1.34	6.91	10.2
Flan-T5	DP	0.01	0.73	-1.34	7.00	15.4
(large)	EP	0.21	0.87	-1.04	1.30	3.66
	NO	0.20	0.87	-1.14	1.34	3.81
Т5	DE	0.60	0.96	0.44	0.68	1.97
original	DP	0.66	0.96	0.49	0.65	1.91
(3b)	EP	0.70	0.97	0.57	0.51	1.66
()	NO	0.68	0.97	0.55	0.63	1.87
	Cause	ulLM: deo	coder only	v architecture	2	
GPT2	DE	0.02	0.87	-1.15	0.73	2.07
(large)	DP	0.08	0.90	-0.91	0.73	2.07
(NO	0.07	0.90	-0.93	0.76	2.06
GPT2	DE	0.20	0.88	-1.10	0.63	1.87
(xl)	DP	0.28	0.91	-0.90	0.60	1.82
()	NO	0.27	0.90	-0.97	0.68	1.97
	seq2s	-		e bottleneck		
Т5	DE	0.35	0.91	-0.15	0.84	2.31
15 bottleneck	DP	0.39	0.91	-0.13	0.86	2.36
(base)	EP	0.42	0.92	-0.07	1.23	3.42
	NO	0.35	0.91	-0.20	1.24	3.45
	DE	0.26	0.80	-1.11	0.87	2.38
Optimus	DP	0.25	0.79	-1.14	0.85	2.33
(BERT-GPT2)	EP	0.09	0.74	-1.17	1.11	3.03
	NO	0.07	0.74	-1.20	1.13	3.09

Table 2: Quantitative evaluation on testset, where best results are highlighted in **bold**. Specification for abbreviation. INJ: ways for injecting the information of inference types into the model, it includes DE: decoder end, DP: decoder prefix, EP: encoder prefix, NO: no inference type. PPL is perplexity, Loss is cross entropy.

In-context learning. Next, we quantitatively evaluate the symbolic inference types within incontext learning (ICL) in contemporary large language models (LLMs). As illustrated in Table 3, prompting with inference types can improve the performance of ICL in both seq2seq and causal LLMs. Besides, within the context of causal LLMs, 409

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an increase in f	few shot examples	³ , improves the
performance.		

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Baseline	INJ	Num	BLEU	Cosine	BLEURT
Seq2seqLL					
	Yes	10	0.51	0.97	0.39
CoT-T5 (11b)	Yes	5	0.51	0.97	0.39
(Kim et al., 2023)	Yes	0	0.50	0.97	0.36
	NO	0	0.46	0.96	0.31
	Yes	10	0.49	0.96	0.40
Flan-T5 (xl)	Yes	5	0.48	0.96	0.39
Fidil-15 (XI)	Yes	0	0.52	0.96	0.39
	NO	0	0.44	0.95	0.24
	Yes	10	0.51	0.97	0.41
Flan-T5 (xxl)	Yes	5	0.53	0.97	0.43
Fiall-13 (XXI)	Yes	0	0.50	0.96	0.37
	NO	0	0.48	0.96	0.36
CausalL	LM: d	ecoder	only arch	itecture	
	Yes	10	0.52	0.96	0.40
GPT-3.5-turbo-0125	Yes	5	0.48	0.96	0.35
GP1-5.5-turb0-0125	Yes	0	0.46	0.96	0.31
	NO	0	0.42	0.96	0.33
	Yes	10	0.53	0.97	0.50
GPT-4-0613	Yes	5	0.52	0.97	0.47
GP1-4-0015	Yes	0	0.52	0.97	0.50
	NO	0	0.47	0.96	0.40
	Yes	10	0.48	0.96	0.33
llama3-8b-8192	Yes	5	0.45	0.96	0.32
nama5-80-8192	Yes	0	0.37	0.95	0.22
	NO	0	0.34	0.95	0.19
	Yes	10	0.54	0.97	0.54
11	Yes	5	0.52	0.97	0.52
llama3-70b-8192	Yes	0	0.51	0.97	0.47
	NO	0	0.44	0.96	0.40

Table 3: ICL evaluation of test cases, where worst results are highlighted in **bold**. The prompt is "*performing natural language inference [where the inference type is type, description],* $[p1; p2; c]_{\times num}$. p1, p2, what is the conclusion?". num is the number of examples. The*description*is based on the definition of inference types in Section 3.

5.2 Quasi-symbolic Inference Evaluation

Secondly, we evaluate (ii) if these inference types can be utilised for prescriptive inference control.

Qualitative evaluation. We qualitatively evaluate the quasi-symbolic inference control on the generation of conclusions by systematically intervening on the inference type prior to the encoder. As illustrated in Table 4, we can observe that the associated linguistic properties of the conclusion can be controlled consistently with the inference type modifications, which indicates that the representation mechanisms can improve inference control with regard to symbolic/lexico-semantic properties. For example, when the type is ARG substitution (ARG-SUB), the model can generate *the blacktop is made of a smooth surface* by replacing the argument *asphalt concrete* with *smooth surface*. The conclusions are changed to *asphalt and blacktop have the same surface* when the inference type is the conjunction (FRAME-CONJ). More examples are provided in Table 13.

Quasi-symbolic NLI control
P1: blacktop is made of asphalt concrete P2: asphalt has a smooth surfaceARG-SUB: the blacktop is made of smooth surfaceARG-SUB-PROP: blacktop has a smooth surface ARG/PRED-GEN: a blacktop is a kind of asphalt ARG-INS: asphalt concrete blacktop has a smooth surfaceFRAME-CON: asphalt and blacktop have the same surfaceIFT: if the asphalt has a smooth surface blacktop will have a smooth surface

Table 4: Controllable generation over original T5 (base) (ARG-SUB: argument substitution, ARG/PRED-GEN: argument/predicate generalisation. ARG-SUB-PROP: property inheritance. ARG-INS: argument insertion, FRAME-CON: frame conjunction, IFT: casual expression.). The example of the T5 bottleneck is provided in Table 11.

Quantitative evaluation. Next, we perform a quantitative evaluation using a large language model (LLM) evaluator, specifically ChatGPT4o. For each pair of premises in the EntailmentBank test set, we apply various inference types to generate a diverse set of conclusions using the finetuned T5 (base) model. We then assess the resulting (premises, conclusion, inference type) tuples based on two criteria: (i) whether the generated conclusion contradicts the premises, and (ii) whether the (premises, conclusion) pair is consistent with the specified inference type. Utilising the prompt detailed in Table 14, we report the accuracy for each criterion. As illustrated in Table 5, the T5 (base) model with controlled symbolic inference types achieves accuracies exceeding 60% for both evaluation dimensions.

Evaluators	logicality	alignment
ChatGPT4o	67%	63%

Table 5: Quantitative evaluation via ChatGPT40.

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³We randomly sample the examples with the same inference type as the current test example from the training set. We perform ten times and calculate the average for each metric.

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5.3 Latent Feature Space Evaluation

Finally, we evaluate (iii) whether the incorporation of feature space (i.e., sentence bottleneck) con-466 tributes to improved feature representation. 467

Explanation-based NLI. We quantitatively evaluate the NLI performance of different baselines on the Entailment testset. We specifically choose the VAE baselines, including the Transformer VAE model: Optimus (Li et al., 2020) and Della (Hu et al., 2022) with two different sentence dimensions (32 and 768), and five LSTM language autoencoders with 768 latent dimensions: denoising AE (Vincent et al. (2008), DAE), β -VAE (Higgins et al., 2016), adversarial AE (Makhzani et al. (2015), AAE), label adversarial AE (Rubenstein et al. (2018), LAAE), and denoising adversarial autoencoder (Shen et al. (2020), DAAE). In Table 6 (bottom), we can observe that our T5 bottleneck can outperform all baselines on BLEU, BLEURT, and cosine similarity from pre-trained sentence T5.

Test: EntailmentBank								
Metrics	BLEU	Cosine	BLEURT	Loss \downarrow	$PPL\downarrow$			
Optimus(32)	0.07	0.74	-1.20	1.13	2.31			
Optimus(768)	0.08	0.74	-1.21	0.82	2.27			
DELLA(32)	0.08	0.85	-1.23	1.69	5.41			
DELLA(768)	0.09	0.87	-1.09	1.54	4.66			
DAE(768)	0.15	0.89	-0.95	1.33	3.78			
AAE(768)	0.11	0.88	-0.95	1.35	3.85			
LAAE(768)	0.09	0.74	-1.12	1.38	3.97			
DAAE(768)	0.07	0.74	-1.20	1.43	4.17			
β -VAE(768)	0.07	0.74	-1.20	1.43	4.17			
T5 bottleneck	0.35	0.91	-0.20	1.24	3.45			

Table 6: Comparison of different baselines on EntailmentBank testset, T5 bottleneck has 768 dimensions.

Explanation inference retrieval. We next evaluate the sentence embedding using as an associated explanation retrieval task (explanationregeneration - i.e. retrieving the associated explanatory facts relevant to a claim) (Valentino et al., 2022a). Given a question-and-answer pair, it reconstructs the entailment tree by searching the explanations from a fact bank (i.e., WorldTree (Jansen et al., 2018a)) in an iterative fashion using a dense sentence encoder. In this framework, we can replace the dense sentence encoder with the proposed T5 bottleneck baseline to evaluate its sentence embeddings. We compare the T5 bottleneck with sentence VAEs: Optimus and five LSTM VAEs, and evaluate them via mean average precision (MAP). As illustrated in Table 7, the T5 bottleneck outperforms all baselines, indicating that it can deliver a better representation of explanatory sentences and entailment relations in a retrieval setting.

depth	t=1	t=2	t=3	t=4
DAE(768)	30.27	31.74	30.65	30.74
AAE(768)	29.13	30.47	29.33	29.14
LAAE(768)	19.13	20.86	18.32	18.01
DAAE(768)	13.16	15.42	14.30	13.97
β -VAE(768)	10.03	10.07	10.05	10.05
Optimus(768)	28.21	29.35	28.35	28.27
T5 bottleneck(768)	34.47	35.28	34.50	34.47

Table 7: Explanatory inference retrieval task where t represents the depth of entailment tree.

6 **Conclusion and Future Work**

This study serves as a foundational step in exploring quasi-symbolic inference within distributional semantic spaces. We establish the connection between natural and symbolic language inferences by (1) characterizing quasi-symbolic inference behaviours, termed symbolic inference types, based on the AMR graph. From a neural representation perspective, we introduce parameter and feature spaces to bridge distributional and symbolic inferences. Specifically, (2) we model Transformerbased encoder-decoder NLI systems as latent variable models, using symbolic inference types to guide latent space dynamics, and (3) explore the feature space for encoding abstract, high-level features. Experimental results reveal that integrating symbolic inference types enhances training dynamics, inference precision, and explanation retrieval, suggesting the potential for neuro-symbolic NLI.

Building upon these findings, we hypothesise that distinct inference types can be represented as functional subspaces that are either separated or disentangled within the parametric space. During the training phase, different inference types result in divergent training trajectories, thereby enhancing both model training and inference dynamics. Furthermore, by manipulating various inference types during the inference stage, semantic features are integrated into specific parametric subspaces corresponding to each inference type, thereby enabling precise inference control.

In future research, we will examine this hypothesis and investigate the composition and generalization of symbolic inference behaviours within distributional representation spaces to develop an explainable and controllable NLI model.

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540 Limitations

This study empirically explores quasi-symbolic in-541 ference behaviours within distributional semantic 542 spaces. Our findings indicate that symbolic inference types can enhance model training, facilitate inference processes, and enable localised in-545 546 ference control. However, we have not yet provided a formal explanation for these observations. 547 We hypothesise that quasi-symbolic inference be-548 haviour arises from the segregation of inference types within the parametric space. This hypothesis 550 may be linked to the results presented in Ortiz-551 Jimenez et al. (2023), which demonstrated that dif-552 ferent tasks are disentangled in the visual embed-553 554 ding space of CLIP (Radford et al., 2021). Future research will address this hypothesis by examining 555 the geometric properties of the parametric space with the target of better composition, generalisation, and interpretation in the neuro-symbolic NLI domain.

> Moreover, while the work focuses on the symbolic control of explanatory inference, complementary methods need to be employed to deliver more strict safety guarantees. While we conduct a quantitative assessment of the logical consistency of the deduction process using ChatGPT40, this evaluation may be unreliable due to the limited proficiency of large language models in logical reasoning. It is essential that control and safety mechanisms remain distinct and are implemented through independent processes.

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A Annotation Details

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Annotation procedure. Annotation was performed manually for 5134 entailment triples (two premises, one conclusion) from the Entailment-Bank (Dalvi et al., 2021), according to Algorithm 1. Graph subset relations and root matching are relaxed for non-argument (:ARG*, op*) edges, meaning relations such as :manner or :time can be ignored for this purpose. Two independent annotators with post-graduate level backgrounds in Computational Linguistics were used in this process, on a consensus-based annotation scheme where a first annotator defined the transformations and a second annotator verified and refined the annotation scheme, in two iterations. The annotation of the AMR graph is based on an off-the-shelf parser (Damonte et al., 2017). The descriptions for each inference type category are as follows:

ARG-SUB (Figure 2): the conclusion is obtained by replacing one argument with another argument.

PRED-SUB: the conclusion is obtained by replacing one verb with another verb.

FRAME-SUB: the conclusion is obtained by replacing a frame of one of the premises with one from the other premise.

COND-FRAM (Figure 5): the conclusion is obtained according to the conditional premise with keyword "if".

ARG-INS (Figure 4): the conclusion is obtained by connecting an argument from one of the premises to a frame of the other.

FRAME-CONJ: the conclusion is obtained by using connectives to connect two premises.

ARG/PRED-GEN (Figure 6): a new *:domain* relation frame is created in the conclusion if both premise graphs differ by a single predicate/argument term.

ARG-SUB-PROP (Figure 7): one of the premises describes a "*is made of*" relationship between the entity in the other premise and its replacement.

IFT: the conclusion should be a conditional sentence.

EXAMPLE: the conclusion should contain the keyword "example".

Unknown (UNK) category. In this work, our annotation occupies 84% based on the Entailment-Bank corpus. As for other unknown categories, we do not further specify them, as they either require



Figure 4: AMR argument insertion (ARG-INS).

P1: inventing paper allows paper to be used



C: inventing paper might increase the use of paper



Figure 5: AMR conditional frame insertion (COND-FRAME).

knowledge outside of the scope of the premises or do not have a consistent symbolic transformation expression. An additional subtype called *premise copy* was included for the cases where the conclusion has the same graph as one of the premises.

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Figure 6: AMR argument generalisation (ARG-GEN).

P1: blacktop is made of asphalt concrete



Figure 7: AMR argument substitution (property inheritance) (ARG-SUB-PROP).

B Experimental Details

B.1 Dataset

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Table 8 describes the statistical information of the corpus used in the experiment. For experiments: Section 5.1, 5.2, and 5.3, the Entailment-Bank dataset is split into train 60%, valid 20%, and test 20% sets. For the explanation inference retrieval task in Section 5.3, we follow the same experimental setup provided online. ⁴

Corpus	Num data.	Avg. length
WorldTree (Jansen et al., 2018a)	11430	8.65
EntailmentBank (Dalvi et al., 2021)	5134	10.35

Table 8: Statistics from explanations datasets.WorldTree is used in the Explanation Inference Retrievaltask.

B.2 T5 Bottleneck Architecture

Figure 8 shows the architecture of the T5 bottleneck for learning latent sentence space. It includes two stages: sentence embedding and decoder connection. The sentence embedding aims to transform token embeddings into a sentence (single) embedding. Decoder connection aims to connect the encoder and decoder.

Latent sentence space: $P(z|x_1, x_2)$. While designing the sentence bottleneck, we compare the four most frequently used mechanisms to transform token embeddings into sentence embeddings:

(1) Mean pooling: calculating the mean of each dimension on all token embeddings and feeding the resulting vector into a multi-layer perceptron to obtain the sentence embedding. (2) multi-layer perceptron (MLP): applying an MLP to reduce the dimensionality of token embeddings, and the resulting embeddings are concatenated to form a single sentence embedding: $z = \operatorname{concat} |\operatorname{MLP}_1(x_1); ...; \operatorname{MLP}_T(x_T)|$ where $MLP_i(x_i)$ represents the *i*-th neural network for input representation of token x_i , z is the latent sentence representation, and T is the maximum token length for a sentence. (3) multi-head attention: feeding each token embedding into the multi-head attention and considering the first output embedding as the sentence embedding (Montero et al., 2021): z =MultiHead (XW^q, XW^k, XW^v) [0] where $X = [x_1, ..., x_T]$ and W^q , W^k , and W^{v} are the weights for learning q, k, v embeddings in selfattention, respectively. (4) Sentence T5: re-loading the pre-trained sentence T5 (S-T5, Ni et al. (2021)).

Conditional generation: $P(x_c|z)$. Next, we consider four strategies to inject sentence embeddings into the decoder. (1) Cross-attention input embedding (CA Input): reconstructing the token embeddings from a sentence representation and directly feeding them into the

⁴https://github.com/ai-systems/hybrid_ autoregressive_inference

1009 cross-attention layers of the decoder: $\hat{Y} =$ 1010 MultiHead $(YW^q, MLP(z)W^k, MLP(z)W^v)$

where \hat{Y} is the reconstruction of decoder input 1011 sequence $Y = [y_1, ..., y_K]$. (2) Cross-attention 1012 KV embedding (CA KV): instead of recon-1013 structing the token embeddings, it consists of 1014 directly learning the Key and Value (Hu et al., 1015 2022; Li et al., 2020), which is formalised as $\hat{Y} =$ MultiHead $(YW^q, MLP_k(z), MLP_v(z)),$ 1017 where MLP_k and MLP_v are neural layers for learning k v embeddings. (3) Non-cross-attention input connection (NCA Input): reconstructing 1020 1021 the token embeddings and element-wisely adding them with the input embeddings of the decoder 1022 (Fang et al., 2021). (4) Non-cross-attention 1023 output connection (NCA Output): adding the 1024 reconstructed token embeddings to the output 1025 1026 embedding of the decoder.

Train: architecture							
Decoder Co	nnection	CA Input	CA KV	NCA Input	NCA Output		
	Pooling	1.41	1.44	1.86	2.42		
Sentence	MLP	1.71	1.94	2.09	2.62		
Embedding	MHA	1.51	2.24	2.31	3.03		
	S-T5	1.24	1.42	1.81	2.22		

Table 9: Comparison of different setups on test loss via cross-entropy (CA: cross-attention, NCA: non-cross-attention), bottom: comparison of different baselines on EntailmentBank testset.

B.3 Implementation Details

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Hyper-parameters. 1. Size of Sentence Representation: in this work, we consider 768 as the size of the sentence embedding. Usually, the performance of the model improves as the size increases.
2. Multi-head Attention (MHA): in the experiment, MHA consists of 8 layers, each layer containing 12 heads. The dimensions of Query, Key, and Value are 64 in each head. The dimension of token embedding is 768. Training hyperparameters are: 3. For all models, the max epoch: 40, learning rate: 5e-5. During fine-tuning the T5 bottleneck, we first freeze the pre-trained parameters in the first epoch and fine-tune all parameters for the remaining epochs. 4. All models are trained on a single A6000 GPU device.

1043**Baselines.** In the experiment, we implement five1044LSTM-based autoencoders, including denoising1045AE (Vincent et al. (2008), DAE), β -VAE (Hig-1046gins et al., 2016), adversarial AE (Makhzani et al.

(2015), AAE), label adversarial AE (Rubenstein 1047 et al. (2018), LAAE), and denoising adversarial 1048 autoencoder (Shen et al. (2020), DAAE). Their im-1049 plementation relies on the open-source codebase 1050 available at the URL⁵. As for transformer-based 1051 VAEs, we implement Optimus (Li et al., 2020)⁶ 1052 and Della (Hu et al., 2022)⁷. All baseline models 1053 undergo training and evaluation with the hyper-1054 parameters provided by their respective sources. 1055 A latent dimension of 768 is specified to ensure a 1056 uniform and equitable comparative analysis. 1057

Metrics. To evaluate the generated conclusions against the reference conclusions, we employ BLEU scores for 1- to 3-gram overlaps and report the average score. Additionally, to assess semantic similarity, we calculate the cosine similarity between the generated and reference conclusions by encoding both using the pretrained Sentence-T5 model⁸ and computing the cosine similarity of their resulting embeddings.

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C Complementary Results

Remove	T5	BLEU	BLEURT	Cosine	Loss \downarrow	$\text{PPL}\downarrow$
FRAME-	small	0.50	0.19	0.95	0.95	2.58
SUB	base	0.60	0.33	0.96	0.72	1.95
ARG-INS	small	0.54	0.27	0.95	0.82	2.22
AKO-IINS	base	0.63	0.46	0.97	0.64	1.73
FRAME-	small	0.53	0.26	0.96	0.84	2.28
CONJ	base	0.60	0.35	0.96	0.65	1.76
COND-	small	0.55	0.25	0.96	0.88	2.39
FRAME	base	0.59	0.36	0.96	0.69	1.87
UNK	small	0.55	0.23	0.95	0.53	1.44
UNK	base	0.62	0.40	0.96	0.58	1.57
No	small	0.54	0.22	0.96	0.69	2.22
No	base	0.57	0.33	0.96	0.61	1.65

Table 10: Ablation study over inference type (No: no inference types are removed).

Ablation studies. We remove the inference types from the dataset and evaluate the T5 model performance using the same metrics. In this case, we can compare the model performance trained with or without that inference-type. From Table 10, we can observe that the baselines (T5 small and base) achieve higher BLEU and BLEURT scores without the data with ARG-INS, COND-FRAME, and

text-autoencoders

⁵https://github.com/shentianxiao/

⁶https://github.com/ChunyuanLI/Optimus

⁷https://github.com/OpenVLG/DELLA

⁸https://huggingface.co/sentence-transformers/ sentence-t5-base



Figure 8: The architectural configuration of T5 bottleneck, it consists of two stages: sentence embedding and decoder connection.

UNK inference type, respectively. This result indicates that the T5 cannot generalize well over those inference types. Also, removing the UNK inference type from data can achieve lower loss and PPL, which indicates that it has a negative impact on model training.

More controllable inference examples. We provide more controlled examples based on both the Original T5 and T5 bottleneck in Table 11, 12, and 13. All examples reveal that the inference type can provide quasi-symbolic inference control to language models.

Quasi-symbolic NLI control
P1: a pumpkin contains seeds P2: fruit contains seeds
Original T5: ARG-INS: a fruit in a pumpkin contains seeds FRAME-CONJ: a pumpkin and fruit both contains seeds FRAME-SUB: fruit is a kind of pumpkin
T5 bottleneck: ARG-INS: fruit is a part of pumpkin that contains seeds FRAME-CONJ: a fruit contains seeds FRAME-SUB: a pumpkin is a kind of plant

Table 11: Controlled generation. original T5(base) (top) and T5 bottleneck (bottom).

Quasi-symbolic NLI control
 P1: eating something has a negative impact on that something P2: some animals eat cacti ARG-INS: some animals have a negative impact on cacti by eating cacti PRED-SUB: some animals may have a negative impact on cacti FRAME-SUB: eating cacti has a negative impact on that cacti
ARG-INS: some animals have a negative impact on cacti by eating cacti PRED-SUB: animals have a negative impact on cacti FRAME-SUB: eating cacti has a negative impact on that cacti

Table 12: Controlled generation. original T5(base) (top) and T5 bottleneck (bottom).

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Premises	Inference Type		Original T5		
P1: a pumpkin contains seeds	ARG-INS		a fruit in a pumpkin contains seeds		
P2: fruit contains seeds	FRAME-CONJ			and fruit both contain seeds	
	IFT		if a pumpkin contains fruit then the fruit may contain seeds		
	EXAMPLE		fruit is an example of pumpkins being sown		
	ARG/PRED-GEN		a pumpkin is a kind of fruit		
	ARG-SUB		fruit can contain pumpkin seeds		
	UNK		a pumpkin can contain seeds		
FRAME-SUB P1: sunlight is a kind of solar en- ARG-INS			fruit is a kind of pumpkin solar energy is a kind of resource for plants that uses water		
ergy		T		-	
P2: water and sunlight are re- sources for plants	FRAME-CONJ		water and sunlight are resources for plants and are kinds of sola energy		
	UNK ARG-SUB		the resources for plants include water and solar energy water and solar energy are resources for plants		
P1: to may a something can mean					
P1: to move something can mean to transfer something	ARG-SUB		flowing can mean to transfer energy		
P2: flowing is a kind of movement for energy	INF		if something flows, then that energy will flow		
tor energy	FRAME-CON	IJ	moving can	transfer energy and mean flowing	
	ARG-INS		flowing can be a kind of transfer of energy to another entity		
	ARG/PRED-GEN		transferring energy with flowing can be seen as transferring energy		
P1: if a pot is exposed to a stove	COND-FRAM			become hot	
then that pot may become hot					
2: the pot is exposed to a stove EXAMPLE			an example	of hot pot is a pot exposed to a stove	
P1: eating something has a nega-	FRAME-SUB		eating cacti	has a negative impact on that cacti	
tive impact on that something					
P2: some animals eat cacti	PRED-SUB		some animals may have a negative impact on cacti		
	ARG-INS		some animals have a negative impact on cacti by eating cacti		
	EXAMPLE		cooking cacti is an example of a negative impact on a cactus		
	INF		if a cactus has a negative impact on an animal, that cactus could be devoured		
P1: seeing requires light	ARG-SUB		reading req		
P2: reading requires seeing		ARG-INS		nd of requirement for reading	
	INF		if light is moving then reading may be taken		
	EXAMPLE	EXAMPLE		a light bulb will be used for reading	
	UNK		-	elp you read	
Premises		Inference T	ype	T5 bottleneck	
P1: a pumpkin contains seeds		ARG-INS		fruit is part of a pumpkin that contains seeds	
P2: fruit contains seeds		FRAME-C	ONJ	a fruit contains seeds	
		FRAME-SU	UB	a pumpkin is a kind of plant	
P1: sunlight is a kind of solar energy		ARG-INS		water is a kind of resource that is used by plant for growth	
P2: water and sunlight are resources for plants		FRAME-CONJ		plants and water are resources that require wate and energy	
		ARG-SUB		plants use water and sunlight to produce energy	
P1: to move something can mean to	ARG-SUB		flowing can mean to transfer energy		
thing					
P2: flowing is a kind of movement for energy		INF		if something flows, then that energy will flow	
		FRAME-CONJ		moving can transfer energy and mean flowing	
		ARG-INS		flowing can be a kind of transfer of something	
		ARG/PRED-GEN		transferring energy with flowing can be seen a transferring energy	
P1: if a pot is exposed to a stove then that pot may become hot		COND-FRAME		the pot may become hot	
P2: the pot is exposed to a stove		ARG/PRED-GEN		the pot may be a source of heat	
	P1: eating something has a negative impact on		UB	eating cacti has a negative impact on that cacti	
P1: eating something has a negat	tive impact on	FRAME-SI			
P1: eating something has a negat that something	tive impact on	PRED-SUE	3	animals have a negative impact on cacti	
P1: eating something has a negat that something	tive impact on		3	some animals have a negative impact on cacti b	
P1: eating something has a negat that something P2: some animals eat cacti	tive impact on	PRED-SUE ARG-INS	3	some animals have a negative impact on cacti b eating cacti	
 P1: eating something has a negat that something P2: some animals eat cacti P1: seeing requires light 	ive impact on	PRED-SUE ARG-INS ARG-SUB		some animals have a negative impact on cacti b eating cacti reading requires light	
	ive impact on	PRED-SUE ARG-INS		some animals have a negative impact on cacti b eating cacti	

Table 13: controllable NLI via inference type (Top: original T5, bottom: T5 bottleneck).

Algorithm 1 Annotation procedure

1: Find premise P_x most similar to the conclusion C, $P_{\bar{x}}$ being the other premise. 2: $G_{x,\bar{x},C} \leftarrow \text{AMR graph of } P_x, P_{\bar{x}}, C$, respectively. 3: #----- common ARG-SUB, PRED-SUB ------4: if $G_x = G_c$ or $G_{\bar{x}} = G_c$ then type = PREM-COPY # Comment: no reasoning happen. 5: 6: else if P_x and C differ by one word w then # Comment: common ARG(PRED)-SUB. if w is a verb then 7: type = PRED-SUB8: 9: else 10: type = ARG-SUBend if 11: 12: else 13: # - - ------ COND-FRAME, FRAME-SUB, ARG-SUB-PROP -----Get AMR graphs G_1, G_2, G_c for P_1, P_2 and C respectively. $P_x \to G_x$. $14 \cdot$ if \exists :ARG* $(x, a) \in C$ and $a \in P_{\bar{x}}$ then 15: if \exists :condition($root(G_x)$, $root(G_{\bar{x}})$) then 16: # Comment: see Figure 5, two root nodes are connected by :condition edge 17: type = COND-FRAME 18: 19: else if root(a) is a noun then if $root(G_{\bar{x}}) =$ "make-01" and \exists :ARG*($root(G_{\bar{x}})$, a) then 20: # Comment: "make" as a trigger to classify ARG-SUB and property inheritance. 21: type = ARG-SUB-PROP22: else 23: type = ARG-SUB # ARG-SUB that was not caught by the simpler rule on line 10, 24: due to Px differing from C by more than a single word end if 25: 26: else 27: type = FRAME-SUBend if 28: ----- Further-specification and Conjunction ------29: # - - - else if $G_x \subset G_c$ and $G_{\bar{x}} \subset G_C$ then 30: 31: type = FRAME-CONJelse if $\exists x, y : \text{domain}(root(G_x), x)$ and $: \text{domain}(root(G_{\bar{x}}, y) \text{ and } : \text{op*}(\text{``and''}, x) \in G_c$ and 32: $:op*(``and", y) \in G_c$ then # Comment: using connectives 'and' to connect two premises type = FRAME-CONJ33: else if $G_x \subset G_c$ then 34: 35: $d \leftarrow G_c - G_x$ if root(d) is a noun then 36: type = ARG-INS # Comment: inserting an argument. 37: 38: else type = FRAME-INS # Comment: inserting a phase (also annotated as ARG-INS). 39: end if 40: ---- ARG/PRED-GEN and Others -----41: # else if \exists :domain($root(G_c), y$) and ($root(G_c) \in G_x$ and $y \in G_{\bar{x}}$) or ($root(G_c) \in G_{\bar{x}}$ and $y \in G_x$) 42: then type = ARG/PRED-GEN 43: else 44: type = UNK45: end if 46: 47: end if

Prompts for automatic evaluation

Logicality:

You are a scoring expert in natural language reasoning. Given two premises and a conclusion, your goal is to evaluate whether the conclusion violates the premises. During your inference process, please only consider the information from the premises.

you can directly give your score (0 or 1) based on the following criteria:

0: the conclusion violates the premises.

1: the conclusion doesn't violate the premises.

The output format is just the score. You don't need to analyse the reasoning process.

Alignment:

You are a scoring expert. Given two premises, a conclusion, and an inference type, your goal is to evaluate whether the (premises, conclusion) pair is aligned with the inference type.

The following is the description of 10 inference types:

1. ARG-SUB: the conclusion is obtained by replacing one argument with another argument.

2. PRED-SUB: the conclusion is obtained by replacing one verb with another verb.

3. FRAME-SUB: the conclusion is obtained by replacing a frame of one of the premises with one from the other premise.

4. COND-FRAM: the conclusion is obtained according to the conditional premise with keyword "if".

5. ARG-INS: the conclusion is obtained by connecting an argument from one of the premises to a frame of the other.

6. FRAME-CONJ: the conclusion is obtained by using connectives to connect two premises.

7. ARG/PRED-GEN: a new ":domain" relation frame is created in the conclusion if both premise graphs differ by a single predicate/argument term.

8. ARG-SUB-PROP: one of the premises describes a "is made of" relationship between the entity in the other premise and its replacement.

9. IFT: the conclusion should be a conditional sentence.

10. EXAMPLE: the conclusion should contain the keyword "example".

When evaluating, some premises might not be able to deduce more than one conclusions. You can ignore those cases.

Finally, you can directly give your score (0 or 1) based on the following criteria:

0: the (premises, conclusion) pair is not aligned with the inference type.

1: the (premises, conclusion) pair is aligned with the inference type.

The output format is just the score. You don't need to analyse the reasoning process.

Table 14: Empirically designed prompt for automatically evaluating the controllability in Section 5.2.