TOTEM: Tokenized Time Series Embeddings for General Time Series Analysis

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ABSTRACT

Learning with time series health data poses many challenges such as variability in sensor semantics (e.g. neural voltage recordings vs US birth rate), difficulty in accessing data, and the relatively smaller data volume compared to other time series domains. Given these limitations, and the fact that the field of general time series analysis has recently begun to explore unified modeling, we approach unification from a complementary vantage point to ultimately benefit zero-shot performance to health time series. Historically general time series analysis unification entails when a common architectural backbone is retrained on a specific task for a specific dataset; we study the unification of time series data representations across domains in many tasks. To this end, we explore the impact of discrete, learnt, time series data representations that enable generalist, cross-domain training. Our method, TOTEM, or Tokenized Time Series Embeddings, proposes a simple tokenizer architecture that embeds time series data from varying domains using a discrete vectorized representation learned in a self-supervised manner. TOTEM works across multiple tasks and domains with minimal to no tuning. We study TOTEM's efficacy with an extensive evaluation on 17 real world time series datasets across 3 tasks. Notably, the majority of our zero-shot datasets are time series health datasets from the neuroscience and birth domains. We evaluate both the specialist (i.e., train a model on each domain) and generalist (i.e., train a single model on many domains), and show that TOTEM matches or outperforms previous best methods on several popular benchmarks. Please find the full paper here: https://arxiv.org/pdf/2402.16412.pdf, and the code here: https://github.com/SaberaTalukder/TOTEM.

1 Introduction

Time series analysis, both for health and more generally, encompasses a wide range of datasets, tasks, and applications in the real world. When considering training paradigms, time series analysis has historically been conducted via *specialist-training*, meaning that models are trained on a single time series domain (Zhou et al., 2023; Wu et al., 2022a; Nie et al., 2022; Zhang & Yan, 2022). *Generalist-training*, where models are simultaneously trained on multiple time series domains, contrasts the specialist paradigm. Both specialist and generalist models can be tested under various regimes. Within *in-domain-testing*, a model is tested on the same domain(s) it was trained on. In *zero-shot-testing*, a model is tested on different domains(s) than it was trained on. Some methods have begun to explore the idea of zero-shot forecasting where (1) a forecaster trains on one dataset then predicts on a separate dataset (Zhou et al., 2023), or (2) a forecaster trains on a subset of channels (which we call *sensors*) from one dataset then zero-shot forecasts on the remaining sensors in the same dataset (Liu et al., 2023). Both of these models would be considered specialists, as they were trained on only one (or a subset of one) dataset. In order to fully enable generalist training and zero shot testing we explore the value of unified time series data representations.

Further, time series analysis has typically been restricted by task, where methods study only *fore-casting* (Wu et al., 2021; Woo et al., 2022), *anomaly detection* (Xu et al., 2021; He & Zhao, 2019), or *imputation* (Luo et al., 2018; 2019), among others. Recently, the field has become increasingly unified with respect to model architecture, with methods (Zhou et al., 2023; Wu et al., 2022a) ex-

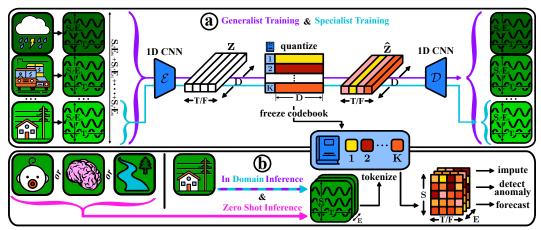


Figure 1: **TOTEM & Evaluation Regimes.** (a) The TOTEM VQVAE architecture consists of an 1D strided CNN encoder \mathcal{E} , quantizer, latent codebook, and 1D strided transpose CNN decoder \mathcal{D} . TOTEM's VQVAE enables generalist training, i.e. on all datasets jointly, and specialist training, i.e. on one dataset at a time. (b) TOTEM's discrete, self-supervised codebook can be leveraged for both in domain and zero shot testing. We utilize US birth and neuroscience domains for zero-shot testing.

ploring language and vision backbones on various time series tasks. These backbones, like previous methods, utilize specialist training (e.g., training separate anomaly detectors on each dataset).

The field has also become increasingly unified with respect to data representation, with growing emphasis on learning performant data representations. For instance, Franceschi et al. (2019) utilize an exponentially dilated causal convolutional encoder to discover in-domain embeddings, Tonekaboni et al. (2021) leverage temporal neighborhood coding, Yang & Hong (2022) utilize temporal-spectral fusion, and Yue et al. (2022) employs hierarchical contrasting across time and batch dimensions.

At a technical level, our approach bears closest affinity to methods that use vector quantized variational autoencoders (VQVAEs) (Van Den Oord et al., 2017; Duan et al., 2023; Rasul et al., 2022b;a). As we discuss further in Section 2, Our goal is to develop a streamlined framework for learning a tokenized data representation (using VQVAEs) in a way that permits easy applicability and holistic empirical evaluation on a broad range of time series modeling tasks and data domains (including zero-shot generalization to new test domains) with minimal to no tuning. \(^1\)

Motivated by the difficulty of training on health time series and the trend of time series analysis unification, we explore the value of a VQVAE-based tokenizer for time series imputation, anomaly detection (Appendix E), and forecasting (Appendix F). Unlike previous methods, we utilize self-supervised, discrete tokens, and extensively explore their utility in varied training and testing regimes. Neuro2 [N2], Neuro5 [N5], and US Births [B] are health datasets we utilize to test zero-shot performance, see Appendix D for more discussion. Our contributions are as follows:

- 1. We present TOTEM, a simple tokenizer architecture for time series analysis that works across domains and tasks with minimal to no tuning.
- Despite its simplicity, TOTEM matches or outperforms the state-of-the-art on several popular benchmark datasets and tasks.
- 3. With an extensive evaluation in the generalist setting (training a single model on multiple domains), we show that TOTEM outperforms the leading state-of-the-art model in both in-domain and zero-shot testing regimes.

2 Method

Our proposed discrete time series tokenization enables the design of general models across a variety of time series domains, tasks, and evaluation schemas, Figure 1. We design a single tokenizer architecture that is generally applicable without extensive data engineering while being suitable for varying data dimensionalities across different tasks. There are many possibilities for how to introduce a discrete time series tokenizer, we extensively study one such methodology that satisfies the aforementioned design criteria.

¹As an aside, our approach to studying what is a performant general time series data representation shares a philosophical alignment with the development of large generalist models in natural language processing, which are also based on having a common tokenized representation (Gage, 1994; Radford et al., 2018).

Data Engineering. Prior work leverages data engineering such as the use of auxiliary features (e.g. day of the month, or minute in the hour, etc.) (Chen et al., 2023; Salinas et al., 2020), or frequency transformations (Wu et al., 2022a; Zhou et al., 2022). We forego any data engineering and operate directly on time steps. This enables generalist-training as differing data domains have widely varying sampling rates leading to distinct auxiliary features and frequency profiles.

Varying Dimensionality. A time series dataset consists of E examples (i.e. number of distinct recordings), S sensor channels, and T time steps, and can be formally expressed as $\{\mathbf{x}_j\}_{j=1}^E \subset \mathbb{R}^{S \times T}$. Even within a single task and single data domain where S does not change, E and E take on a wide range of values. As an example, canonical forecasting predictions lengths range from 96 to 720 time steps. When moving to generalist-training, datasets additionally have wide ranging sensor dimensionalities E. Our tokenizer handles varying dimensionality across E, E, and E0 by creating non-overlapping tokens along the time-dimension that are smaller than the dimension E1.

Differing Tasks. There are numerous tasks to tackle in health time series analysis. Three significant ones are imputation, anomaly detection (Appendix E), and forecasting (Appendix F). In *imputation*, models intake a masked time series $\mathbf{x_m} \in \mathbb{R}^{S \times T_{\text{in}}}$, and then reconstruct and impute $\mathbf{x} \in \mathbb{R}^{S \times T_{\text{in}}}$. In *anomaly detection*, models intake a corrupted time series $\mathbf{x_{corr}} \in \mathbb{R}^{S \times T_{\text{in}}}$ and reconstruct the data $\mathbf{x} \in \mathbb{R}^{S \times T_{\text{in}}}$. The amount of corruption is considered known, at A%. In *forecasting*, models intake a time series $\mathbf{x} \in \mathbb{R}^{S \times T_{\text{in}}}$ and predict future readings $\mathbf{y} \in \mathbb{R}^{S \times T_{\text{out}}}$, where S is the number of sensors and $T_{\text{in}}, T_{\text{out}}$ signify the durations of the preceding and succeeding time series, respectively. Our tokenizer is performant across all tasks despite their distinct representational requirements.

TOTEM Implementation. To realize a single tokenizer architecture that enables generalist modeling across differing domains and tasks we take inspiration from the VQVAE (Van Den Oord et al., 2017). The original VQVAE leverages a dilated convolutional architecture with a stride of 2 and window-size of 4, similar to the WaveNet (Oord et al., 2016) dilated, causal, convolutional decoder. A dilated convolution skips inputs allowing a filter to operate on a larger input area / coarser scale. Utilizing dilated convolutions is an architectural decision rooted in the high sampling rates of raw audio waveforms (Oord et al., 2016; Van Den Oord et al., 2017). High sampling rates are not a trait shared by many time series domains.

When adapting the VQVAE for general time series analysis, the TOTEM VQVAE:

- 1. Operates directly on time steps; no data engineering.
- 2. Creates discrete, non-overlapping tokens along the time dimension of length F, where F < T, thereby promoting training and testing on variable length examples, E, sensors, S, and time steps T.
- 3. Maintains the same architecture and objective regardless of the downstream task.
- 4. Aims to capture maximal information within a large receptive field by: (1) using a strided non-causal convolutional architecture with no dilation, (2) training on long time series inputs, (3) pre-striding the data by a stride of 1 so the tokenizer learns from maximal inputs.

The TOTEM VQVAE consists of an encoder, quantizer, latent codebook, and decoder. It takes in a univariate time series $\{\mathbf{x}_i \in \mathbb{R}^T\}_{i=1}^{E\cdot S}$ obtained by flattening the multivariate sensor channel. This makes TOTEM's VQVAE sensor-agnostic, enabling TOTEM's generalist-training and zero-shot-testing. The encoder \mathcal{E} consists of strided 1D convolutions compressing the time series by a cumulative stride of F. \mathcal{E} maps a univariate time series $\mathbf{x} \in \mathbb{R}^T$ to a latent representation $\mathbf{z} = \mathcal{E}(\mathbf{x}) \in \mathbb{R}^{T/F \times D}$, where D is the he hidden dimension. The latent codebook $\mathcal{C} = \{\mathbf{c}_i\}_{i=1}^K$ consists of K D-dim codewords $\mathbf{c}_i \in \mathbb{R}^D$. During quantization, the codebook is used to replace \mathbf{z} with $\hat{\mathbf{z}} \in \mathbb{R}^{T/F \times D}$ such that $\hat{\mathbf{z}}_j = \mathbf{c}_k$, where $k = \arg\min_i ||\mathbf{z}_j - c_i||_2$. The decoder \mathcal{D} follows the reverse architecture of the encoder \mathcal{E} , consisting of 1D transpose convolutions with a cumulative stride of 1/F mapping the quantized $\hat{\mathbf{z}}$ to a reconstructed time series $\hat{\mathbf{x}} = \mathcal{D}(\hat{\mathbf{z}}) \in \mathbb{R}^T$. We learn \mathcal{E}, \mathcal{D} , and \mathcal{C} by optimizing the objective $\mathcal{L} = \mathcal{L}_{\text{rec}} + \mathcal{L}_{\text{cmt}}$ consisting of a reconstruction loss $\mathcal{L}_{\text{rec}} = \frac{1}{E\cdot S} \sum_i ||\mathbf{x}_i - \hat{\mathbf{x}}_i||_2^2$ and a commitment loss \mathcal{L}_{cmt} , which allows the codebook to update despite the the non-differentiable arg min operation during quantization. The final objective is $\mathcal{L} = \mathcal{L}_{\text{rec}} + \alpha \cdot \mathcal{L}_{\text{cmt}}$, where α is a scalar that weights the two losses. This objective does not change even when the underlying task, time series length, data masking, normalization schema, or data domain changes.

Table 1: **Specialist Imputation** (\downarrow). Across all datasets, metrics, and masking percentages, TOTEM has the highest AvgWins (**52.1%**), followed by GPT2 (**35.4%**). TOTEM values are means from 3 seeds; baseline values are from Zhou et al. (2023); Wu et al. (2022a).

Model Metric	TOTEM MSE MAE	GP MSE		TiN MSE		Pat MSE		E7 MSE		FE MSE		St MSE	at MAE		uto MAE		I nf MAE		Re MAE		iTS MAE	Dlin MSE MAE
≥ 12.5% 25% 37.5% 50%	0.028 0.046 0.029 0.047 0.031 0.048 0.033 0.052	0.026 0.028 0.033 0.037	0.049 0.052 0.060 0.065).025).029).031).034	0.045 0.052 0.057 0.062	0.029 0.031 0.035 0.038	0.049 0.053 0.058 0.063	0.057 0.065 0.081 0.102	0.141 0.155 0.180 0.207	$0.041 \\ 0.064 \\ 0.107 \\ 0.183$	0.107 0.163 0.229 0.312	0.027 0.029 0.033 0.037	0.051 0.056 0.062 0.068	0.026 0.030 0.032 0.037	0.04 0.05 0.06 0.06	7 0.03 4 0.04 0 0.04 7 0.05	7 0.092 2 0.100 9 0.11 3 0.114	3 0.03 0 0.035 1 0.040 4 0.046	0.076 5 0.08 6 0.09 6 0.09	5 0.04 2 0.05 1 0.05 9 0.06	7 0.101 2 0.111 8 0.121 5 0.133	0.039 0.084 0.048 0.103 0.057 0.117 0.066 0.134
50%	0.054 0.154 0.059 0.160 0.067 0.169 0.079 0.183	0.080 0.087 0.094 0.101																				0.092 0.214 0.118 0.247 0.144 0.276 0.175 0.305
E 12.5% E 37.5% 50%	0.049 0.125 0.052 0.128 0.055 0.132 0.061 0.139	$\begin{array}{c} 0.017 \\ 0.022 \\ 0.029 \\ 0.040 \end{array}$).085).096).111).128 ().019).023).029).036	$\begin{array}{c} 0.092 \\ 0.101 \\ 0.111 \\ 0.124 \end{array}$	0.041 0.044 0.049 0.055	0.130 0.135 0.143 0.151	0.067 0.096 0.133 0.186	0.188 0.229 0.271 0.323	$0.035 \\ 0.052 \\ 0.069 \\ 0.089$	0.135 0.166 0.191 0.218	$\begin{array}{c} 0.026 \\ 0.032 \\ 0.039 \\ 0.047 \end{array}$	0.107 0.119 0.131 0.145	0.034 0.046 0.057 0.067	0.12 0.14 0.16 0.16	4 0.04 4 0.06 1 0.07 4 0.09	7 0.15 3 0.18 9 0.20 3 0.21	5 0.032 0 0.042 0 0.063 8 0.082	2 0.120 2 0.140 3 0.18 2 0.20	5 0.07 5 0.09 2 0.11 8 0.13	5 0.180 3 0.206 3 0.231 4 0.255	0.058 0.162 0.080 0.193 0.103 0.219 0.132 0.248
E 12.5% E 25% 50%	$ \begin{smallmatrix} 0.016 & 0.078 \\ 0.017 & 0.081 \\ 0.018 & 0.084 \\ 0.020 & 0.088 \end{smallmatrix} $	0.020	0.076 0.080 0.087 0.095	0.018 0.020 0.023 0.026	0.080 0.085 0.091 0.098	0.026 0.028 0.030 0.034	0.094 0.099 0.104 0.110	0.108 0.164 0.237 0.323	0.239 0.294 0.356 0.421	0.056 0.080 0.110 0.156	0.159 0.195 0.231 0.276	0.021 0.024 0.027 0.030	0.088 0.096 0.103 0.108	0.023 0.026 0.030 0.035	0.09 0.10 0.10 0.11	2 0.13 1 0.13 8 0.15 9 0.20	3 0.270 5 0.277 5 0.29 6 0.33	0 0.108 2 0.136 3 0.175 3 0.211	3 0.22 5 0.26 5 0.30 1 0.32	8 0.03 2 0.04 0 0.05 9 0.05	4 0.127 2 0.143 1 0.159 9 0.174	0.062 0.166 0.085 0.196 0.106 0.222 0.131 0.247
⊒ 12.5% □ 25% 37.5% 50%	0.119 0.212 0.127 0.220 0.138 0.230 0.157 0.247	0.043 0.054 0.072 0.107	0.140 0.156 0.180 0.216																			0.151 0.267 0.180 0.292 0.215 0.318 0.257 0.347
일 12.5% 일 25% 37.5% 50%	0.040 0.129 0.041 0.131 0.043 0.136 0.047 0.142	0.039 0.044 0.051 0.059).125 .135 .147 .158).040).046).052).060	$\begin{array}{c} 0.130 \\ 0.141 \\ 0.151 \\ 0.162 \end{array}$	0.057 0.061 0.067 0.073).152).158).166).174	0.187 0.279 0.400 0.602	0.319 0.390 0.465 0.572	0.095 0.137 0.187 0.232	0.212 0.258 0.304 0.341	0.042 0.049 0.056 0.065	0.133 0.147 0.158 0.170	0.044 0.050 0.060 0.068	0.13 0.14 0.16 0.16	8 0.30; 9 0.32; 3 0.35; 3 0.36;	5 0.43 2 0.44 3 0.46 9 0.47	1 0.163 4 0.206 2 0.252 2 0.316	3 0.28 9 0.33 9 0.37 5 0.41	9 0.10 1 0.11 0.12 9 0.13	1 0.231 5 0.246 5 0.257 6 0.268	0.100 0.216 0.127 0.247 0.158 0.276 0.183 0.299
AvgWins	52.1%	35.4	%	18.8		09		0		09			%		%)%		%)%	0%

For further discussion see: reproducibility (A), ethical considerations (B), related work (C), experimental setup (D), anomaly detection (E), forecasting (F), ablations (G), exploratory studies in generalist modeling (H), and std. devs. (I). Following the field standard, we bold the **best**, **second** best, and **third** best and calculate the average number of best results, or AvgWins, for each method. We compare to two approach families: methods designed for multiple tasks (**multitask**) – TOTEM's category – and methods designed for a specific task (**singletask**), and are adapted to other tasks.

3 IMPUTATION

In imputation, models intake a masked time series $\mathbf{x_m} \in \mathbb{R}^{S \times T_{\text{in}}}$, and then reconstruct and impute $\mathbf{x} \in \mathbb{R}^{S \times T_{\text{in}}}$ We experiment with four canonical masking percentages at 12.5%, 25%, 37.5%, 50%, and report MSE and MAE; lower is better (\downarrow) . **Specialist.** In Table 1 we compare TOTEM to baselines. All models are trained and evaluated on the same dataset (indomain). TOTEM has the highest AvgWins with 52.1%, followed by GPT2 at 35.4%, and TiNet at 18.8%. TOTEM performance for m1 and h1 is lower; notably these datasets are the minute and hour resampling of the same raw data respectively. We investigate and discuss TOTEM's success across different domains in Table 9. Generalist. In Table 2 we compare TOTEM to GPT2 (best performing models above), when both models are trained on the aggregate of W, E, m1, m2, h1, h2. We test them on the in-domain and zero-shot test sets. TOTEM outperforms GPT2 in-domain, 58.3%

Table 2: **Generalist Imputation** (↓). TOTEM & GPT2 simultaneously train on all in domain datasets, 3 seeds each. **A. In-Domain Performance.** TOTEM has the highest AvgWins at **58.3%**. **B. Zero-Shot Performance.** We test on unseen datasets zero-shot. TOTEM again has the highest AvgWins at **80.0%**.

A. In-Domain Performance	
Model TOTEM GPT2 Metric MSE MAE MSE MAE	
$\geqslant \begin{array}{cccccccccccccccccccccccccccccccccccc$	B. Zero-Shot Performance Model TOTEM GPT2 Metric MSE MAE MSE MAE
12.5% 0.051 0.179 0.091 0.186 0.197 0.375 0.080 0.189 0.189 0.123 0.080 0.189 0.132 0.233 0.080 0.189 0.132 0.233	12.5% 0.029 0.120 0.047 0.145 25% 0.033 0.127 0.064 0.164 237.5% 0.041 0.139 (0.990 0.191 50% 0.056 0.160 0.131 0.228
= 12.5% 0.041 0.132 0.052 0.141 25% 0.044 0.135 0.065 0.154 37.5% 0.048 0.139 0.015 0.177 0.196	25% 0.017 0.085 0.021 0.095 25% 0.019 0.090 0.028 0.107 0.039 0.039 0.123 0.039 0.123 0.039 0.123 0.039 0.123 0.039 0.123 0.039 0.123 0.039 0.123 0.039 0.123 0.039 0.123 0.039 0.123 0.039 0.123 0.039 0.123 0.039 0.123 0.039 0.123 0.039 0.123 0.039 0.123 0.039 0.123 0.039 0.123 0.039 0.123 0.039 0.
B 37.5% 0.040 0.125 0.029 0.095	
= 12.5% 0.100 0.201 0.113 0.217 25% 0.108 0.209 0.131 0.231 37.5% 0.122 0.229 0.153 0.247 50% 0.124 0.237 0.182 0.266	m 12.5% 0.632 0.642 0.392 0.496 25% 0.693 0.665 0.444 0.523 37.5% 0.761 0.692 0.498 0.533 50% 0.827 0.718 0.591 0.589
12.5% 0.075 0.175 0.067 0.155 25% 0.076 0.177 0.071 0.160 37.5% 0.093 0.195 0.077 0.167 50% 0.089 0.192 0.086 0.179	25% 0.061 0.168 0.070 0.173 25% 0.061 0.168 0.084 0.189 37.5% 0.069 0.178 0.103 0.209 50% 0.082 0.193 0.128 0.234
AvgWins 58.3% 43.8%	AvgWins 80.0% 20.0%

vs. 43.8%, and by a much larger margin in zero-shot, 80% vs. 20%. TOTEM's performance across all experiments demonstrate that tokens are a performant representation for imputation.

4 CONCLUSIONS, LIMITATIONS & FUTURE WORK

We present TOTEM: a simple, performant tokenizer that creates unified time series data representations across domains in many tasks thereby enabling generalist modeling. TOTEM demonstrates strong in-domain and zero-shot capabilities that match or outperform existing state-of-the-art approaches. Through dataset selection we emphasize the ability to train on varying domains and test on health domains. We leave discussion of anomaly detection E, forecasting F, ablations G, and further studies of generalist modeling H to the Appendix. Moving forward, an interesting limitation

is that TOTEM does not support variable token lengths. Future work includes exploring dynamic token lengths as they could enhance unified representations and further improve task performance.

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APPENDIX

A REPRODUCIBILITY STATEMENT

To ensure reproducibility all results are run on three seeds; see section I for standard deviations. All code will be released. All datasets are already popular, public time series benchmark datasets. In imputation, anomaly detection, and forecasting the VQVAE is trained with a learning rate of 0.001, embedding dimension of 64, commitment cost of 0.25, and compression factor of 4. In forecasting the downstream model is a transformer encoder with 4 layers and 4 attention heads and a feed-forward hidden dimension of 256. We train using Adam with a base learning rate of 0.0001 and a one cycle learning rate scheduler in accordance with Nie et al. (2022) on A100s.

B ETHICAL CONSIDERATIONS

There are no immediate ethical concerns that arise from our work. However, as with all data driven methods, certain societal consequences are important to be discussed, in this case surrounding time series modeling. A few are reported below:

Privacy Concerns. Time series data, especially when sourced from personal devices or applications, can contain sensitive information about individuals, e.g. for health domains. In this work, no time series were sourced from personal devices, and all data is publicly available.

Reliability. Time series models can be unreliable. For instance, if a model forecasts incorrect health predictions, it could cause undue patient concern. In this work, we focused on unified data representations across many tasks as opposed to a single task.

C RELATED WORK

Time series modeling methods utilize many techniques, ranging from statistical methods (Winters, 1960; Holt, 1957; Anderson, 1976; Hyndman & Athanasopoulos, 2018; Taylor & Letham, 2018) to multilayer perceptrons (MLPs) (Zeng et al., 2023; Li et al., 2023; Das et al., 2023; Challu et al., 2023; Chen et al., 2023; Zhang et al., 2022; Oreshkin et al., 2019) to convolutional neural networks (CNNs) (Wu et al., 2022a; Liu et al., 2022a; He & Zhao, 2019; Franceschi et al., 2019; Bai et al., 2018) to recurrent neural networks (RNNs) (Salinas et al., 2020; Shen et al., 2020; Hochreiter & Schmidhuber, 1997) to transformers (Zhou et al., 2023; Liu et al., 2023; Nie et al., 2022; Zhang & Yan, 2022; Woo et al., 2022; Zhou et al., 2022; Liu et al., 2022b; Wu et al., 2022b; Xu et al., 2021; Wu et al., 2021; Liu et al., 2021; Many models are hybrid solutions that blend aforementioned approaches.

Most of these methods intake time and then perform various combinations of normalization (Kim et al., 2021), frequency transformations (Wu et al., 2022a; Zhou et al., 2022), and patchification either along the time dimension (Liu et al., 2023; Zhang & Yan, 2022; Nie et al., 2022), or sensor dimension (Li et al., 2019; Zhou et al., 2021; Wu et al., 2021; Liu et al., 2021). Patch lengths range from a single time-step / sensor, also known as point-wise, to the length of the entire time series / all sensors. Time and sensor patch dependencies are then learned, via an attention mechanism, convolution, recurrence, or linear layer, across the temporal dimension, sensor dimension, or both the temporal and sensor dimensions (Zhang & Yan, 2022). For multisensor modeling, one can model all sensors jointly or independently (i.e., forecast each sensor independently) (Nie et al., 2022). These methods learn the underlying data representations end-to-end with the downstream task (e.g., forecasting).

Specialist-training, where models are only trained on a single time series domain, is the most common regime amongst prior work (Zhou et al., 2023; Wu et al., 2022a; Nie et al., 2022; Zhang & Yan, 2022). These specialist models are primarily evaluated via in-domain-testing, where the test set is from the same domain as the train set. Recently, some methods (Zhou et al., 2023; Liu et al., 2023) have begun to explore specialist zero-shot forecasting capabilities.

²In time series analysis, sensors, channels, and variates are synonymous terms; in this paper we adopt the sensor terminology.

The time series analysis field is undergoing unification along both the modeling axis (Zhou et al., 2023; Wu et al., 2022a) and data representation axis (Franceschi et al., 2019; Tonekaboni et al., 2021; Yang & Hong, 2022; Yue et al., 2022). Unified data representations, both statistical and learnt, have been more extensively studied in language and vision modeling (Gage, 1994; Van Den Oord et al., 2017; Esser et al., 2021; Rombach et al., 2022). The vision modeling field distinguishes between discrete, learnt, tokens (Van Den Oord et al., 2017; Esser et al., 2021; Rombach et al., 2022) and patches (Dosovitskiy et al., 2020). Patches have been studied in time series modeling (Zhou et al., 2023; Nie et al., 2022; Zhang & Yan, 2022). In this work, we propose to use discrete, learnt tokenized representations, which we show lead to strong performance in both specialist and generalist settings, as well as in-domain and zero-shot testing regimes.

D EXPERIMENTAL SETUP

Through experiments in imputation (§3), anomaly detection (§E), and forecasting (§F), our goal is to explore the efficacy of TOTEM on standard benchmark datasets and tasks, and domain general settings. To briefly refresh: specialist refers to training on a single domain (Tables 1, 3, 5). Generalist refers to training on multiple domains (Tables 2, 4, 6). Finally, in-domain refers to testing on the training domain, and zero-shot to testing on a separate domain from training.

For all experiments & models, we run three seeds and report the mean; standard deviations are reported in section I. Following the field standard, we bold the **best** metric in all tables. Evaluation metrics differ across tasks. We report mean squared error MSE (\downarrow), mean absolute error MAE (\downarrow), precision P (\uparrow), recall R (\uparrow), and F1 score (\uparrow); (\downarrow) means lower is better, (\uparrow) means higher performance is better. Given the varied metrics we calculate the average number of best results, or AvgWins , for each method and highlight the **best**, **second** best, and **third** best methods.

Notably imputation and anomaly detection can be directly solved with just TOTEM's VQVAE, as they are fundamentally data representation tasks, whereas in forecasting further modeling is required, Figure 2. In forecasting, the trained, frozen, codebook representation converts a sensor's observed measurements $\mathbf{x}_s \in \mathbb{R}^{T_{\text{in}}}$ to a sequence of T_{in}/F discrete tokens.

Baselines. We compare to two families of approaches: methods designed for multiple tasks (multitask) – TOTEM belongs in this category – and methods designed for a specific task (singletask), and are adapted to other tasks.

We compare against two recent multitask models, the transformer based GPT2 Zhou et al. (2023) and the convolutional TimesNet[TiNet] Wu et al. (2022a). For singletask models we compare against PatchTST Patch] Nie et al. (2022), ETSFormer[ETS] Woo et al. (2022), Fedformer[FED] Zhou et al. (2022), Non-stationary trans.[Stat] Liu et al. (2022b), Autoformer[Auto] Wu et al. (2021), Informer[Inf] Zhou et al. (2021), Reformer[Re] Kitaev et al. (2020), LightTS[LiTS] Zhang et al. (2022), DLinear[DLin] Zeng et al. (2023), Anomaly trans.[ATran]Xu et al. (2021), Pyraformer[Pyra] Liu et al. (2021), LogTrans.[LogTr] Li et al. (2019), Trans.[Trans] Vaswani et al. (2017), Crossformer[Cross] Zhang & Yan (2022), TiDE Das et al. (2023), RLinear[RLin] Li et al. (2023), SciNet[SCi] Liu et al. (2022a), & iTrans.[iTrans] Liu et al. (2023).

Datasets. We leverage 12 benchmark datasets: weather[W], electricity[E], traffic[T], ETTm1[m1], ETTm2[m2], ETTh1[h1], ETTh2[h2], SMD, MSL, SMAP, SWAT, PSM that are commonly used for imputation, anomaly detection and forecasting Zhou et al. (2023); Wu et al. (2022a); Xu et al. (2021); Zhang & Yan (2022); Nie et al. (2022). For the zero shot settings, we leverage 5 benchmark datasets: neuro2[N2], neuro5[N5] (from Peterson et al. (2022)), and saugeen river flow[R], U.S. births[B], and sunspot[S] (from Godahewa et al. (2021)). 17 datasets in total.

E ANOMALY DETECTION

In anomaly detection, models intake a corrupted time series $\mathbf{x_{corr}} \in \mathbb{R}^{S \times T_{in}}$ and reconstruct the data $\mathbf{x} \in \mathbb{R}^{S \times T_{in}}$, where the amount of corruption is considered known, at A%. We report % Precision P (\uparrow), Recall R (\uparrow), and F1 Score (\uparrow); higher is better (\uparrow).

The standard practice in machine learning, which we adopt, is to have a held out test set that is not used for tuning the model or learning algorithm. One aspect that makes comparing with several prior works challenging is that they use the test set as a validation set for early stopping of the learning algorithm, which can often inflate their performance. Despite this inconsistency, we compare our performance against these reported performances, whenever available.

Specialist. In Table 3 we evaluate TOTEM against numerous specialist baselines. TOTEM has the highest AvgWins at 26.7% followed by a five-way tie between GPT2, TiNet, ATrans, ETS, and LogTr at 13.3%. **Generalist.** In Table 4 we compare generalist-trained TOTEM and GPT2. On the in-domain test sets TOTEM outperforms GPT2: 80% vs. 20%. In the zero-shot test sets TOTEM outperforms GPT2: 73.3% vs. 26.7%.

TOTEM's AvgWins across the specialist and generalist settings demonstrate that tokens are a performant representation for anomaly detection.

Table 3: **Specialist Anomaly Detection** (↑). TOTEM has the highest AvgWins at **26.7**% followed by a five-way tie between GPT2, TiNet, ATrans, ETS, and LogTr at **13.3**%. Some prior methods use the test set as a validation set for early stopping of the learning algorithm, which can inflate performance. We do not adopt this practice and train TOTEM for a set number of iterations.

Model	TOTEM	GPT2	TiNet	ATran	Patch	ETS	FED	Stat	Auto	Pyra	Inf	Re	LogTr	Trans LiTS DLi
SMD ⊢ MSL □ SMAP SWAT PSM	79.62 82.58 94.02 94.27 95.87	86.89 82.45 72.88 94.23 97.13	84.61 81.84 69.39 93.02 97.34	85.49 83.31 71.18 83.10 79.40	84.62 78.70 68.82 85.72 96.08	83.13 85.03 69.50 84.91 91.76	85.08 78.57 70.76 93.19 97.23	84.62 77.50 71.09 79.88 97.29	85.11 79.05 71.12 92.74 93.29	83.04 84.86 71.09 91.78 82.08	69.92 81.43	75.32 84.40 70.40 82.80 73.61	76.21 79.57 69.97 80.52 76.74	79.56 82.53 77.1 78.68 78.95 84.8 69.70 69.21 69.2 6
SMD MSL SMAP SWAT PSM	76.06 82.85 94.04 95.91 94.21	84.98 82.91 60.95 96.34 95.68	81.54 75.36 56.40 95.40 96.20	82.23 87.37 58.11 97.32 94.72	82.14 70.96 55.46 80.94 93.47	79.23 84.93 55.75 80.36 85.28	82.39 80.07 58.10 96.42 97.16	81.21 89.14 59.02 96.75 96.76	58.62 95.81	80.61 85.93 57.71 96.00 96.02	77.23 86.48 57.13 96.75 96.33	69.24 83.31 57.44 96.53 95.38	70.13 87.37 57.59 97.32 98.00	76.13 78.42 71.5 87.37 75.78 85.4 96.53 94.72 95.3 96.56 95.97 89.2
SMD MSL SMAP SWAT PSM	83.54 82.32 94.00 92.68 97.58	88.89 82.00 90.60 92.20 98.62	87.91 89.54 90.14 90.75 98.51	88.91 79.61 91.85 72.51 68.35	87.26 88.34 90.64 91.10 98.84	87.44 85.13 92.25 90.02 99.31	87.95 77.14 90.47 90.17 97.31	68.55 89.37	88.06 77.27 90.40 89.85 99.08	83.81	81.77 90 11	85.51 90 91	83.46 73.05 89.15 68.67 63.06	83.58 87.10 83.6 71.57 82.40 84.3 89.37 92.58 92.3 68.84 91.98 80.9 62.75 98.37 98.2
AvgWins	26.7%	13.3%	13.3%	13.3%	0%	13.3%	0%	6.7%	0%	0%	0%	0%	13.3%	

Table 4: **Generalist Anomaly Detection** (↑). We train TOTEM & GPT2 on all datasets and then perform in-domain and zero-shot evaluations. **A. In-Domain Performance.** TOTEM outperforms GPT2: **80.0**% vs. 20.0%. **B. Zero-Shot Performance.** TOTEM again outperforms GPT2: **73.3**% vs. 26.7%.

A. In-Do	omain Per	rformance	<u>B.</u>	Zero-	Shot Per	formance
<u>Model</u>	TOTEM	GPT2	_ <u>N</u>	<u>Iodel</u>	TOTEM	GPT2
SMD ⊢ MSL III SMAP SWAT PSM	78.64 83.29 92.51 94.37 95.78	79.73 80.17 67.05 89.62 90.47	F.1	N2 N5 R B S	51.29 51.28 49.39 49.15 52.17	39.02 42.19 36.14 20.81 38.12
≃ SMD MSL SMAP SWAT PSM	72.07 82.96 91.48 96.13 93.90	73.42 78.48 53.42 87.53 87.76	М	N2 N5 R B S	76.88 76.84 70.49 73.71 77.36	33.69 36.77 29.66 17.67 31.83
SMD MSL SMAP SWAT PSM	86.66 83.64 93.56 92.68 97.74	87.44 81.95 90.01 91.83 93.39	Д	N2 N5 R B S	38.49 38.48 38.02 36.86 39.35	46.43 49.58 46.30 25.33 47.72
AvgWins	80.0%	20.0%	Av	gWins	73.3%	26.7%

F FORECASTING

The forecaster transformer encoder processes the tokenized time series independently for each sensor, adding time-based positional encodings to each token along the time dimension. Using a series of multihead attention layers, the model predicts the forecasted measurements $\bar{\mathbf{y}}_s \in \mathbb{R}^{T_{\text{out}}} \text{ for } s = 1,...,S, \text{ ap-}$ plying the attention mechanism along the time dimension T. In parallel, the forecaster takes in x_s and predicts the future's mean, μ_s , and standard deviation, σ_s , for each sensor s = 1, ..., S to unnormalize the data. The final forecasted prediction is $\mathbf{y}_s = \sigma_s \cdot \bar{\mathbf{y}}_s + \mu_s$. The forecaster is trained in a supervised fashion by minimizing three smooth L1 losses between predictions $\{\bar{\mathbf{y}}_s, \mu_s, \sigma_s\}$ and their ground truth respectively.

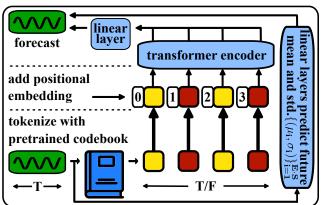


Figure 2: Forecaster Modeling. The forecasting task requires modeling beyond the VQVAE. We leverage TOTEM's pretrained, learnt, discrete codes as a the input data representation and train a transformer encoder. We add positional embeddings along the time dimension, and use linear layers before the final output as well as to unnormalize the resulting forecast.

In forecasting, models intake a time series $\mathbf{x} \in \mathbb{R}^{S \times T_{\text{in}}}$ and predict future readings $\mathbf{y} \in \mathbb{R}^{S \times T_{\text{out}}}$, where S is the number of sensors and $T_{\text{in}}, T_{\text{out}}$ signify the durations of the preceding and succeeding time series, respectively. The pairs (\mathbf{x}, \mathbf{y}) are generated by striding the original time series data.

All models have a lookback of $T_{\rm in}=96$, with prediction lengths $T_{\rm out}=\{96,192,336,720\}$. Numbers for other methods are from Liu et al. (2023). We run GPT2 with $T_{\rm in}=96$ as they originally report varying, dataset-specific, lookback lengths. We report MSE (\downarrow) and MAE (\downarrow); lower is better.

Specialist. From Table 5 we find that TOTEM achieves the highest AvgWins at 28.6% followed by iTrans at 26.8%. TOTEM has first finishes in five datasets while iTrans' first finishes are only electricity and traffic. **Generalist.** In Table 6 we compare generalist TOTEM and GPT2. TOTEM outperforms GPT2 for both in-domain (67.9% vs. 33.9%) and zero-shot (90.0% vs. 12.5%).

TOTEM's AvgWins forecasting performance across the training and testing regimes demonstrates that tokens are a performant representation for forecasting.

Table 5: **Specialist Forecasting** (\downarrow). TOTEM has the best AvgWins (28.6%), followed by iTrans (26.8%). Notably, TOTEM has first place finishes in 5 datasets, while iTrans' first places are concentrated in only electricity and traffic. All models have lookback $T_{in} = 96$.

Model Metric	TOTEM MSE MAE N	GPT2 MSE MAE	TiNe MSE M		ans P	atch MAE	Cross MSE MAE	FE MSE		Stat SE MAE	TiDE MSE MA	RLin		SCi MSE MAE
≥ 96 192 336 720	0.165 0.208 0 0.207 0.250 0 0.257 0.291 0 0.326 0.340 0	.184 0.22 .231 0.26 .285 0.30 .362 0.35	4 <mark>0.172</mark> 0 3 <mark>0.219</mark> 0 2 0.280 0 1 0.365 0	220 0.174 261 0.221 306 <mark>0.278</mark> 359 0.358	0.214 0.17 0.254 0.22 0.296 0.27 0.349 0.35	7 0.218 5 0.259 8 0.297 4 0.348	0.158 0.23 0.206 0.27 0.272 0.33 0.398 0.41	0 0.217 (7 0.276 (5 0.339 (8 0.403 (0.296 0. 0.336 0. 0.380 0. 0.428 0.4	173 0.223 245 0.285 321 0.338 414 0.410	0.202 0.20 0.242 0.20 0.287 0.30 0.351 0.30	61 0.192 0.2 98 0.240 0.3 35 0.292 0.3 86 0.364 0.3	232 0.196 0.25 271 0.237 0.29 807 0.283 0.33 853 <mark>0.345</mark> 0.38	5 0.221 0.306 6 0.261 0.340 5 0.309 0.378 1 0.377 0.427
四 192 336 720	0.178 0.263 0 0.187 0.272 0 0.199 0.285 0 0.236 0.318 0	1.190 0.27 1.204 0.29 1.245 0.32											281 0.197 0.28 283 0.196 0.28 298 0.209 0.30 331 0.245 0.33	
⊢ 192 336 720	0.523 0.303 0 0.530 0.303 0 0.549 0.311 0 0.598 0.331 0	.471 0.31 .479 0.31 .490 0.31 .524 0.33	1 0.593 0. 2 0.617 0. 7 0.629 0. 6 0.640 0.	321 0.395 336 0.417 336 0.433 350 0.467	0.268 0.54 0.276 0.54 0.283 0.55 0.302 0.58	4 0.359 0 0.354 1 0.358 6 0.375	0.522 0.29 0.530 0.29 0.558 0.30 0.589 0.32	0 0.587 (3 0.604 (5 0.621 (8 0.626 (0.366 0.0 0.373 0.0 0.383 0.0 0.382 0.0	612 0.338 613 0.340 618 0.328 653 0.355	0.805 0.4 0.756 0.4 0.762 0.4 0.719 0.4	93 0.649 0.; 74 0.601 0.; 77 0.609 0.; 49 0.647 0.	389 0.650 0.39 366 0.598 0.37 369 0.605 0.37 387 0.645 0.39	6 0.788 0.499 0 0.789 0.505 3 0.797 0.508 4 0.841 0.523
= 96 = 192 336 720	0.320 0.347 0 0.379 0.382 0 0.406 0.402 0 0.471 0.438 0	328 0.36 368 0.38 .400 0.40 .462 0.44	3 0.338 0. 2 0.374 0. 4 0.410 0. 0 0.478 0.	375 0.334 387 0.377 411 0.426 450 0.491	0.368 <mark>0.32</mark> 0.391 <mark>0.36</mark> 0.420 0.39 0.459 0.45	9 0.367 7 0.385 9 0.410 4 0.439).404 0.42).450 0.45).532 0.51).666 0.58	6 0.379 (1 0.426 (5 0.445 (9 0.543 (3.419 0.4 3.441 0.4 3.459 0.4 3.490 0.5	386 0.398 459 0.444 495 0.464 585 0.516	0.364 0.3 0.398 0.4 0.428 0.4 0.487 0.4	87 0.355 0.3 04 0.391 0.3 25 0.424 0.4 61 0.487 0.4	376 0.345 0.37 392 0.380 0.38 415 0.413 0.41 450 0.474 0.45	2 0.418 0.438 9 0.439 0.450 3 0.490 0.485 3 0.595 0.550
전 변 192 336 720	0.176 0.253 0 0.247 0.302 0 0.317 0.348 0 0.426 0.410 0	.178 0.26 .245 0.30 .307 0.34 .410 0.40	3 0.187 0.2 7 0.249 0.6 6 0.321 0.9 9 0.408 0.	267 0.180 309 0.250 351 0.311 403 0.412	0.264 0.17 0.309 0.24 0.348 0.30 0.407 0.40	0.259 0.302 0.343 0.400	0.287 0.36 0.414 0.49 0.597 0.54 1.730 1.04	6 0.203 (2 0.269 (2 0.325 (2 0.421 (0.287 0. 0.328 0. 0.366 0. 0.415 0.4	192 0.274 280 0.339 334 0.361 417 0.413	0.207 0.3 0.290 0.3 0.377 0.4 0.558 0.5	05 0.182 0.2 64 0.246 0.2 22 0.307 0.2 24 0.407 0.	265 0.193 0.29 304 0.284 0.36 342 0.369 0.42 398 0.554 0.52	2 0.286 0.377 2 0.399 0.445 7 0.637 0.591 2 0.960 0.735
= 192	0.380 0.394 0 0.434 0.427 0 0.490 0.459 0 0.539 0.513 0	1.379 0.39 1438 0.42	7 0.384 0.4 7 0.436 0.4 8 0.491 0.5 5 0.521 0.5	402 0.386 429 0.441 469 0.487 500 0.503	0.405 0.414 0.436 0.466 0.458 0.50 0.491 0.50	4 0.419 0 0 0.445 0 1 0.466 0 0 0.488 0	0.423 0.44 0.471 0.47 0.570 0.54 0.653 0.62	8 0.376 (0.420 (0.459 (1 0.506 (0.419 0.: 0.448 0.: 0.465 0.: 0.507 0.:	513 0.491 534 0.504 588 0.535 643 0.616	0.479 0.4 0.525 0.4 0.565 0.5 0.594 0.5	64 0.386 0. 92 0.437 0. 15 0.479 0. 58 0.481 0.	395 0.386 0.40 124 0.437 0.43 146 0.481 0.45 170 0.519 0.51	0 0.654 0.599 2 0.719 0.631 9 0.778 0.659 6 0.836 0.699
일 192 336 720	0.293	.295 0.34 .384 0.40 .418 0.43 .423 0.44											38 0.333 0.38 90 0.477 0.47 26 0.594 0.54 40 0.831 0.65	
AvgWins	28.6%	1.8%	1.8%			.3%	3.6%	5.4		0%	0%	25%		0%

Table 6: **Generalist Forecasting** (↓). We evaluate generalist TOTEM and GPT2. **A. In-Domain.** TOTEM outperforms GPT2: 67.9% to 33.9%. **B. Zero-Shot.** TOTEM outperforms GPT2: 90.0% to 12.5%.

Α.	In-D	omain	Perf	orma	ance						
M	lodel letric	MSE N		GP MSE	T2 MAE						
<u>×</u>	96 192 336 720		.216	0.201	0.237 0.275 0.311 0.360						
ш	96 192	0.179 0	.264 0.267	0.194	0.278 0.284		<u>Zero</u>				
_	192 336 720	0.196 0 0.230 0	.283 .314	0.214 0.255	0.300	_M	odel etric	MSE	TEM MAE	GI MSE	MAE
L	96 192 336 720	0.507 0.511 0.535 0.580	.284 .282 .292 .309	0.484 0.488 0.502 0.534	0.320 0.320 0.326 0.343	N2	96 192 336 720	1.138 1.149 1.092 1.045	0.777 0.785 0.770 0.754	1.332 1.416 1.358 1.308	$\begin{array}{c} 0.830 \\ 0.863 \\ 0.851 \\ 0.840 \end{array}$
m	96 192 336 720	0.374 0 0.400 0 0.432 0 0.487 0	1.384 1.399 1.424 1.460	0.487 0.516 0.548 0.581	0.468 0.480 0.499 0.511	N2	96 192 336 720	0.483 0.495 0.468 0.451	0.484 0.491 0.483 0.477	0.528 0.578 0.548 0.537	0.499 0.524 0.515 0.511
m2	96 192 336 720	0.198 0 0.266 0 0.365 0 0.588 0			0.315 0.346 0.376 0.423	~	96 192 336 720	1.120 1.242 1.237 1.182	0.635	1.465 1.638 1.601 1.552	0.785
h1	96 192 336 720	0.382 0 0.463 0 0.507 0 0.517	.404 .435 0.463 0.500	0.421 0.480 0.518 0.517	0.408 0.436 0.453 0.467	В	96 192 336 720	0.805 0.836 0.809 0.896	0.739 0.752 0.748 0.794	0.838 0.837 0.792 0.927	0.762 0.752 0.738 0.806
h2	96 192 336 720	0.307 0 0.406 0 0.505 0 0.661 0).345).403).460).557	0.298 0.381 0.406 0.423	0:343 0:392 0:419 0:438	S	96 192 336 720	$0.446 \\ 0.462 \\ 0.521 \\ 0.717$	0.482 0.491 0.525 0.625	0.443 0.481 0.541 0.773	0.478 0.499 0.533 0.643
Ave	gWins	67.9	%	33.	9%	Avç	gWins	90.	0%	12.	.5%

G ABLATIONS

Tokens vs. Time. To evaluate if tokens enable TOTEM's performance, we implement TimeTOTEM. TimeTOTEM has the identical architecture to TOTEM, except we replace the VQVAE with an MLP trained end-to-end with the downstream forecaster. We compare Totem vs. TimeTOTEM in the specialist in-domain, and generalist in-domain and zero-shot regimes (Table 7). In all cases TOTEM outperforms TimeTOTEM - specialist: 67.9% vs. 39.3%, generalist in-domain: 78.6% vs. 23.2%, generalist zero-shot: 67.5% vs. 35.0%. TOTEM's performance demonstrates that tokens, when compared to time, lead to better performance.

Codebook Size. In Table 7 we explore the affect of the codebook size, K, on the VQVAE's MSE and MAE reconstruction performance. As expected, we find that as K increases from 32 to 256 to 512 the reconstruction performance improves.

Table 7: **Ablations** (\downarrow). Across the Tokens vs. Time (TvT) experiments tokens out perform time. (A) specialist: 67.9% to 39.93%, (B) in-domain generalist: 78.6% to 23.2%, and (C) zero-shot generalist: 67.5% to 35%. (D) As the codebook size K increases the VQVAE reconstruction performance improves.

	A.	TvT Sp	ecialist	
M M	lodel letric	TOTEM MSE MA		
M	96 192 336 720	0.165 0.20 0.207 0.2 0.257 0.2 0.326 0.3	0.164 0.2 0 0.209 0.2 1 0.261 0.2 1 0.332 0.3	
田	96 192 336 720	0.178 0.20 0.187 0.20 0.199 0.20 0.236 0.3	63 0.179	62 69 89 25
Н	96 192 336 720		03 0.528 0.3 03 0.500 0.3 11 0.531 0.3	10 49 65 98
m1	96 192 336 720	0.320 0.3 0.379 0.3 0.406 0.4 0.471 0.4	17 0.326 0.3 32 0.377 0.3 12 0.409 0.4 38 0.469 0.4	55 86 09 41
m2	96 192 336 720	0.176 0.2 0.247 0.3 0.317 0.3 0.426 0.4	53 0.176 0.2 12 0.247 0.3 18 0.3 8 0.3 10 0.419 0.4	54 03 50 11
h1	96 192 336 720	0.380 0.3 0.434 0.4 0.490 0.4 0.539 0.5	94 0.377 0.3	95 28 62 22
h2	96 192 336 720	0.293 0.3 0.375 0.39 0.422 0.4 0.610 0.56	38 0.294 0.3 90 0.373 0.3 31 0.423 0.4 57 0.591 0.5	38 89 33 56
Ave	gWins	67.9%		,
C.	TvT	Zero-Sh	ot General	ist
M	lodel letric	TOTEM	TimeTOT	EM E
N2	96 192 336 720	1.138 0.77 1.149 0.73 1.092 0.77 1.045 0.75	77 1.127 0.7 35 1.169 0.7 70 1.115 0.7 54 1.070 0.7	73 93 80 66
N5	96 192 336 720	0.483 0.4 0.495 0.4 0.468 0.4 0.451 0.4	34 0.481 0.4 01 0.508 0.5 33 0.481 0.4 77 0.467 0.4	83 00
R	96 192 336 720	1.120 0.55 1.242 0.65 1.237 0.65 1.182 0.66	32 1.102 0.5 35 1.207 0.6 26 1.190 0.6	78 28 13 96
В	96 192 336		39 0.825 0.7 2 0.847 0.7 8 0.831 0.7	51 61 64

67.5%

AvgWins

<u>B. 7</u>	[vT]	n-Do	mair	Gen	<u>eralist</u>
Mo Me	odel etric	TO:	ΓEM MAE	Time7	OTEM MAE
≽	96 192 336 720	0.172 0.217 0.266 0.334	$\begin{array}{c} 0.216 \\ 0.256 \\ 0.295 \\ 0.342 \end{array}$	$\begin{array}{c} 0.173 \\ 0.218 \\ 0.267 \\ 0.337 \end{array}$	0.218 0.261 0.299 0.347
ш	96 192 336 720	$\begin{array}{c} 0.179 \\ 0.181 \\ 0.196 \\ 0.230 \end{array}$	0.264 0.267 0.283 0.314	0.183 0.189 0.204 0.242	0.267 0.275 0.291 0.325
L	96 192 336 720	0.507 0.511 0.535 0.580	0.284 0.282 0.292 0.309	0.517 0.526 0.552 0.602	0.293 0.296 0.304 0.326
m1	96 192 336 720	$\begin{array}{c} 0.374 \\ 0.400 \\ 0.432 \\ 0.487 \end{array}$	0.384 0.399 0.424 0.460	$\begin{array}{c} 0.428 \\ 0.438 \\ 0.469 \\ 0.546 \end{array}$	0.420 0.427 0.447 0.493
m2	96 192 336 720	0.198 0.266 0.365 0.588	0.275 0.319 0.377 0.511	0.207 0.269 0.358 0.521	0.286 0.325 0.377 0.482
h1	96 192 336 720	0.382 0.463 0.507 0.517	0.404 0.435 0.463 0.500	0.401 0.453 0.496 0.518	0.410 0.441 0.468 0.510
h2	96 192 336 720	0.307 0.406 0.505 0.661	0.403 0.403 0.460 0.557	0.305 0.396 0.492 0.599	0.346 0.402 0.458 0.531
Avgl	Wins	78.	6%	23	.2%

D. Code	book	Size A	<u>blations</u>
		debook S	
	32	256	512
		MSE	
All	0.0451	0.0192	0.0184
W		0.0161	0.0128
Е	0.0463	0.0209	0.0152
T	0.0312	0.0120	0.0101
		MAE	
All	0.1460	0.0937	0.0913
\mathbf{W}		0.0673	0.0607
\mathbf{E}	0.1520	0.1027	0.0878
T	0.1204	0.0749	0.0685
AvgWins	0%	0%	100%

H EXPLORATORY STUDIES IN GENERALIST MODELING

Generalist Codebooks. To further explore the capabilities of a generalist codebook data representation we train models that utilize a general codebook but dataset-specific transformer forecasters, e.g. a TOTEM VQVAE trained on multiple domains with a forecaster trained only on electricity, Table 8. We compare these mixed models to generalist and specialist models trained on the same domains. All models use the same the codebook hyperparameters (number of codewords K=256, compression factor F=4, code dimensionality D=64) as well as the forecaster transformer architecture to ensure a fair comparison.

Since we are evaluating the specialists, mixed-models, and generalist on in-domain test data one might expect that the TOTEM specialists will significantly outperform all models. Surprisingly this intuition is not correct. When comparing models trained using specialist codebooks to models trained using a single generalist codebook we find that generalist codebook models outperform specialist codebook models: 66.1% vs. 57.1%. Upon further inspection we find that the fully-generalist model (far right column Table 8) significantly outperforms the mixed-models (middle column Table 8) in traffic (T) and electricity (E). This dominant performance is puzzling until considering the training sizes.

The largest training set across domains belongs to traffic (T) at 10.2M training examples. In dataset T, the fully generalist models achieves 100% AvgWins. The second largest training set belongs to electricity (E) at 5.8M training examples, with 75% AvgWins for the fully-generalist model. Unfortunately there is a sharp drop off in training set sizes, with the rest of the data domains collectively comprising 1.6M training examples. These results evoke questions. For instance: does training on the smaller datasets act like form of regularization? Or: how does in-domain generalist performance scale with dataset size? We leave these exciting directions for future work. The generalist codebook's performance across datasets highlights the potential of unified, discrete, token representations for in-domain evaluations.

Zero Shot Vignette: Training Size & Data Diversity. Here we further explore generalist and specialist zero-shot testing capabilites, Table 9. We take the two largest TOTEM specialist, traffic at 10.2M and electricity at 5.8M training examples, and test their zero-shot capabilities compared to the TOTEM generalist. We expect that the generalist will perform best as it was trained on the most data at 17.6M training examples as well as the most domains. We predict the generalist will be followed by TOTEM-traffic then TOTEM-electricity as they are both trained on only one domain but traffic has 4.4M more training examples than electricity. As expected the generalist outperforms both TOTEM-traffic and TOTEM-electricity with 85.0% AvgWins. However, curiously TOTEM-electricity outperforms TOTEM-traffic: 12.5% vs. 2.5% despite having 4.4M fewer training examples. Why is the smaller training set outperforming the larger training set? One possible explanation is that the electricity domain is more similar than the traffic domain to neuro, river, births, and sunspot. Another possible explanation comes from the raw time series dimensionality. Despite having fewer training examples, electricity has a higher number of raw time steps³ compared to traffic: 26304 vs. 17544. However, traffic has a larger number of sensors: 862 vs. 321. This limited analysis suggests that a higher number of raw time steps is more valuable than more sensor readings. Untangling these possibilities and beginning to answer the questions: what is a unit of data in time series? And how this unit scale as the time steps, sensors, and examples scale? are valuable future directions. The zero shot vignette has demonstrated the power of the token-enabled generalist over the traffic and electricity specialists, and has opened up exciting training size and data diversity questions.

³Raw time steps for all data. The train:val:test ratio is 7:1:2.

Table 8: Generalist codes beat specialist codes: 66.1% vs 57.1%.

Codebook Forecaster Metric	1 1	Generalist Specialist MSE MAE	Generalist Generalist MSE MAE
≥ 96	0.165 0.208	0.164 0.208	0.172 0.216
≥ 192	0.207 0.250	0.208 0.251	0.217 0.256
336	0.257 0.291	0.258 0.290	0.266 0.295
720	0.326 0.340	0.329 0.338	0.334 0.342
96	0.178 0.263	0.178 0.263	0.179 0.264
山 192	0.187 0.272	0.187 0.273	0.181 0.267
336	0.199 0.285	0.199 0.285	0.196 0.283
720	0.236 0.318	0.238 0.320	0.230 0.314
96	0.523 0.303	0.521 0.301	0.507 0.284
192	0.530 0.303	0.530 0.303	0.511 0.282
336	0.549 0.311	0.555 0.313	0.535 0.292
720	0.598 0.331	0.605 0.337	0.580 0.309
96	0.320 0.347		0.374 0.384
192	0.379 0.382		0.400 0.399
336	0.406 0.402		0.432 0.424
720	0.471 0.438		0.487 0.460
796	0.176 0.253		0.198 0.275
E 192	0.247 0.302		0.266 0.319
336	0.317 0.348		0.365 0.377
720	0.426 0.410		0.588 0.511
96	0.380 0.394		0.382 0.404
192	0.434 0.427		0.463 0.435
336	0.490 0.459		0.507 0.463
720	0.539 0.513		0.517 0.500
72 96 192 336 720	0.293 0.338 0.375 0.390 0.422 0.431 0.610 0.567	0.294 0.339 0.375 0.391 0.421 0.431 0.610 0.567	0.307 0.345 0.406 0.403 0.505 0.460 0.661 0.557
AvgWins	57.1%	66.	1%

Table 9: Zero Shot Vignette: Training Size & Diversity

Model Train Domain	TOTEM	TOTEM	TOTEM
	Generalist	Specialist	Specialist
	ALL	Traffic	Electricity
Sensor Num (S)	-	862	321
Raw Length (T)		17544	26304
Train Size Metric	17.6M	10.2M	5.8M
	MSE MAE	MSE MAE	MSE MAE
S 192 336 720	1.138 0.777 1.149 0.785 1.092 0.770 1.045 0.754	1.194 0.798 1.218 0.808 1.190 0.804 1.117 0.784	1.193 0.802 1.300 0.845 1.260 0.837 1.234 0.832
96	0.483 0.484	0.515 0.505	0.489 0.490
192	0.495 0.491	0.535 0.514	0.555 0.527
336	0.468 0.483	0.524 0.513	0.538 0.525
720	0.451 0.477	0.500 0.507	0.533 0.527
96	1.120 0.582	1.171 0.635	1.141 0.579
192	1.242 0.635	1.273 0.673	1.297 0.652
336	1.237 0.626	1.232 0.653	1.247 0.628
720	1.182 0.604	1.198 0.642	1.236 0.633
96	0.805 0.739		0.820 0.756
192	0.836 0.752		0.843 0.759
336	0.809 0.748		0.791 0.741
720	0.896 0.794		0.886 0.790
96	0.446 0.482	0.476 0.508	0.460 0.487
192	0.462 0.491	0.511 0.528	0.505 0.511
336	0.521 0.525	0.576 0.568	0.569 0.545
720	0.717 0.625	0.795 0.685	0.764 0.641
AvgWins	85.0%	2.5%	12.5%

I MEANS AND STANDARD DEVIATIONS

I.1 IMPUTATION RESULTS - MEANS AND STANDARD DEVIATIONS

Table 10: **TOTEM - Specialist Imputation** (\downarrow)

Metric	MSE	MAE
≥ 25% 0.	028 ± 0.0000 028 ± 0.0000 029 ± 0.0000 031 ± 0.0006	0.046 ± 0.0006
□ 25% 0. 37.5% 0	054 ± 0.0006 059 ± 0.0006 $.067 \pm 0.006$ 079 ± 0.0012	0.160 ± 0.0010 0.169 ± 0.0012
E 25% 0. 37.5% 0. 50% 0.	049 ± 0.0000 052 ± 0.0006 055 ± 0.0000 061 ± 0.0006	$\begin{array}{c} 0.125 \pm 0.0006 \\ 0.128 \pm 0.0006 \\ 0.132 \pm 0.0006 \\ 0.139 \pm 0.0006 \end{array}$
25% 0. E 37.5% 0.	016 ± 0.0006 017 ± 0.0006 018 ± 0.0000 020 ± 0.0000	0.081 ± 0.0006 0.084 ± 0.0006
∃ 25% 0.	119 ± 0.0010 127 ± 0.0015 138 ± 0.0012 157 ± 0.0006	0.220 ± 0.0006 0.230 ± 0.0006
≥ 25% 0. 37.5% 0.	040 ± 0.0006 041 ± 0.0010 043 ± 0.0006 047 ± 0.0006	0.131 ± 0.0012 0.136 ± 0.0006

Table 11: **TOTEM - Generalist Imputation** (\downarrow)

N	l etric	MSE	MAE
≱	12.5% 25% 37.5% 50%	$\begin{array}{c} 0.029 \pm 0.0012 \\ 0.030 \pm 0.0006 \\ 0.032 \pm 0.0006 \\ 0.036 \pm 0.0006 \end{array}$	$\begin{array}{c} 0.060 \pm 0.0047 \\ 0.060 \pm 0.0047 \\ 0.062 \pm 0.0030 \\ 0.067 \pm 0.00036 \end{array}$
ш	12.5% 25% 37.5% 50%	$\begin{array}{c} 0.065 \pm 0.0020 \\ 0.071 \pm 0.0015 \\ 0.080 \pm 0.0025 \\ 0.095 \pm 0.0026 \end{array}$	$\begin{array}{c} 0.171 \pm 0.0032 \\ 0.179 \pm 0.0031 \\ 0.189 \pm 0.0032 \\ 0.205 \pm 0.0032 \end{array}$
m	12.5% 25% 37.5% 50%	10.044 ± 0.0000	$\begin{array}{c} 0.132 \pm 0.0015 \\ 0.135 \pm 0.0010 \\ 0.139 \pm 0.0040 \\ 0.152 \pm 0.0000 \end{array}$
m2	12.5% 25% 37.5% 50%	10.041 ± 0.0015	$\begin{array}{c} 0.125 \pm 0.0067 \\ 0.126 \pm 0.0058 \\ 0.129 \pm 0.0049 \\ 0.136 \pm 0.0038 \end{array}$
h1	12.5% 25% 37.5% 50%	10.108 ± 0.0049	$\begin{array}{c} 0.201 \pm 0.0049 \\ 0.209 \pm 0.0038 \\ 0.220 \pm 0.0044 \\ 0.237 \pm 0.0049 \end{array}$
h2	12.5% 25% 37.5% 50%	$\begin{array}{c} 0.075 \pm 0.0012 \\ 0.076 \pm 0.0006 \\ 0.093 \pm 0.0222 \\ 0.089 \pm 0.0010 \end{array}$	$\begin{array}{c} 0.175 \pm 0.0053 \\ 0.177 \pm 0.0036 \\ 0.195 \pm 0.0200 \\ 0.192 \pm 0.0035 \end{array}$
Ξ		Zero-Sho	ot
NZ	12.5% 25% 37.5% 50%		$\begin{array}{c} 0.120 \pm 0.0045 \\ 0.127 \pm 0.0035 \\ 0.139 \pm 0.0025 \\ 0.160 \pm 0.0012 \end{array}$
NS	12.5% 25% 37.5% 50%	$\begin{array}{c} 0.017 \pm 0.0010 \\ 0.019 \pm 0.0010 \\ 0.022 \pm 0.0006 \\ 0.029 \pm 0.0006 \end{array}$	$\begin{array}{c} 0.085 \pm 0.0030 \\ 0.090 \pm 0.0030 \\ 0.098 \pm 0.0025 \\ 0.110 \pm 0.0025 \end{array}$
В	12.5% 25% 37.5% 50%	10.087 ± 0.0064	$\begin{array}{c} 0.109 \pm 0.0040 \\ 0.117 \pm 0.0031 \\ 0.129 \pm 0.0035 \\ 0.147 \pm 0.0023 \end{array}$
В	12.5% 25% 37.5% 50%	$\begin{array}{c} 0.632 \pm 0.0087 \\ 0.693 \pm 0.0070 \\ 0.761 \pm 0.0055 \\ 0.827 \pm 0.0044 \end{array}$	$\begin{array}{c} 0.642 \pm 0.0068 \\ 0.665 \pm 0.0047 \\ 0.692 \pm 0.0023 \\ 0.718 \pm 0.0000 \end{array}$
S	12.5% 25% 37.5% 50%	10.061 ± 0.0006	$\begin{array}{c} 0.160 \pm 0.0023 \\ 0.168 \pm 0.0021 \\ 0.178 \pm 0.0021 \\ 0.193 \pm 0.0015 \end{array}$

Table 12: **GPT2 - Generalist Imputation** (\downarrow)

Μ	letric	MSE	MAE
≱	12.5% 25% 37.5% 50%	$\begin{array}{c} 0.029 \pm 0.0000 \\ 0.033 \pm 0.0006 \\ 0.037 \pm 0.0006 \\ 0.043 \pm 0.0012 \end{array}$	$\begin{array}{c} 0.045 \pm 0.0006 \\ 0.048 \pm 0.0006 \\ 0.054 \pm 0.0012 \\ 0.061 \pm 0.0001 \end{array}$
ш	12.5% 25% 37.5% 50%	$\begin{array}{c} 0.008 \pm 0.0020 \\ 0.091 \pm 0.0020 \\ 0.108 \pm 0.0021 \\ 0.132 \pm 0.0026 \end{array}$	$\begin{array}{c} 0.186 \pm 0.0035 \\ 0.197 \pm 0.0025 \\ 0.213 \pm 0.0026 \\ 0.236 \pm 0.0026 \end{array}$
m	12.5% 25% 37.5% 50%	$\begin{array}{c} 0.052 \pm 0.0012 \\ 0.065 \pm 0.0021 \\ 0.085 \pm 0.0038 \\ 0.117 \pm 0.0052 \end{array}$	$\begin{array}{c} 0.141 \pm 0.0016 \\ 0.154 \pm 0.0021 \\ 0.171 \pm 0.0026 \\ 0.196 \pm 0.0026 \end{array}$
m2	12.5% 25% 37.5% 50%	$\begin{array}{c} 0.029 \pm 0.0000 \\ 0.033 \pm 0.0006 \\ 0.038 \pm 0.0006 \\ 0.045 \pm 0.0006 \end{array}$	$\begin{array}{c} 0.095 \pm 0.0006 \\ 0.101 \pm 0.0006 \\ 0.110 \pm 0.0012 \\ 0.121 \pm 0.0012 \end{array}$
귤	12.5% 25% 37.5% 50%	10.131 ± 0.0010	$\begin{array}{c} 0.217 \pm 0.0021 \\ 0.231 \pm 0.0015 \\ 0.247 \pm 0.0017 \\ 0.266 \pm 0.0012 \end{array}$
h2	12.5% 25% 37.5% 50%	$egin{array}{l} 0.067 \pm 0.0010 \\ 0.071 \pm 0.0006 \\ 0.077 \pm 0.010 \\ 0.086 \pm 0.0032 \end{array}$	$\begin{array}{c} 0.155 \pm 0.0015 \\ 0.160 \pm 0.0015 \\ 0.167 \pm 0.0015 \\ 0.179 \pm 0.0038 \end{array}$
		Zero-Sh	ot
NZ	12.5% 25% 37.5% 50%	$ \begin{vmatrix} 0.047 \pm 0.0006 \\ 0.064 \pm 0.0017 \\ 0.090 \pm 0.0036 \\ 0.131 \pm 0.0051 \end{vmatrix} $	$\begin{array}{c} 0.145 \pm 0.0015 \\ 0.164 \pm 0.0015 \\ 0.191 \pm 0.0032 \\ 0.228 \pm 0.0044 \end{array}$
N2	12.5% 25% 37.5% 50%	$egin{array}{l} 0.021 \pm 0.0006 \\ 0.028 \pm 0.0006 \\ 0.039 \pm 0.0015 \\ 0.055 \pm 0.0015 \end{array}$	$\begin{array}{c} 0.095 \pm 0.0012 \\ 0.107 \pm 0.0010 \\ 0.123 \pm 0.0015 \\ 0.145 \pm 0.0023 \end{array}$
R	12.5% 25% 37.5% 50%	$ \begin{array}{c} 0.093 \pm 0.0010 \\ 0.125 \pm 0.0006 \\ 0.167 \pm 0.0021 \\ 0.220 \pm 0.0045 \end{array} $	$\begin{array}{c} 0.119 \pm 0.0015 \\ 0.134 \pm 0.0026 \\ 0.154 \pm 0.0042 \\ 0.182 \pm 0.0057 \end{array}$
В	12.5% 25% 37.5% 50%	$egin{array}{l} 0.392 \pm 0.0064 \\ 0.444 \pm 0.0071 \\ 0.498 \pm 0.0080 \\ 0.591 \pm 0.0700 \end{array}$	$\begin{array}{c} 0.496 \pm 0.0023 \\ 0.523 \pm 0.0029 \\ 0.553 \pm 0.0023 \\ 0.599 \pm 0.0275 \end{array}$
s	12.5% 25% 37.5% 50%	10.084 ± 0.0010	$\begin{array}{c} 0.173 \pm 0.0017 \\ 0.189 \pm 0.0015 \\ 0.209 \pm 0.0021 \\ 0.234 \pm 0.0021 \end{array}$

I.2 Anomaly Detection Results - Means and Standard Deviations

Table 13: **TOTEM - Specialist Anomaly Detection** (\uparrow)

	$\mathbf{Mean} \pm \mathbf{Std}$
SMD	0.796 ± 0.0137
MSL	0.826 ± 0.0052
☐ SMAP	0.940 ± 0.0008
SWAT	0.943 ± 0.0006
PSM	0.959 ± 0.0008
SMD	0.761 ± 0.0207
MSL	0.829 ± 0.0071
\cong SMAP	0.940 ± 0.0013
SWAT	0.959 ± 0.0012
PSM	0.942 ± 0.0004
SMD	0.835 ± 0.0054
MSL	0.823 ± 0.0033
□ SMAP	0.940 ± 0.0004
SWAT	0.927 ± 0.0003
PSM	0.976 ± 0.0012

Table 14: **TOTEM - Generalist Anomaly Detection** (\uparrow)

_		$\mathbf{Mean} \pm \mathbf{Std}$
	SMD	0.786 ± 0.0386
	MSL	0.833 ± 0.0020
	SMAP	0.925 ± 0.0014
	SWAT	0.944 ± 0.0005
\vdash	PSM	0.958 ± 0.0002
ш	N2	0.513 ± 0.0397
	N5	0.513 ± 0.0390
	R	0.494 ± 0.0625
	В	0.492 ± 0.0229
_	S	0.522 ± 0.0418
	SMD	0.721 ± 0.0565
	MSL	0.830 ± 0.0046
	SMAP	0.915 ± 0.0020
	SWAT	0.961 ± 0.0010
γ.	PSM	0.939 ± 0.0004
щ	N2	0.769 ± 0.0594
	N5	0.768 ± 0.0582
	R	0.705 ± 0.0825
	В	0.737 ± 0.0340
	S	0.774 ± 0.0581
	SMD	0.867 ± 0.0114
	MSL	0.836 ± 0.0014
	SMAP	0.936 ± 0.0009
	SWAT	0.927 ± 0.0001
Д	PSM	0.977 ± 0.0002
щ	N2	0.385 ± 0.0299
	N5	0.385 ± 0.0294
	R	0.380 ± 0.0502
	В	0.369 ± 0.0172
	S	0.394 ± 0.0325
_		

Table 15: **GPT2 - Generalist Anomaly Detection** (\uparrow)

_		
		$\mathbf{Mean} \pm \mathbf{Std}$
	SMD	0.797 ± 0.0326
	MSL	0.802 ± 0.0205
	SMAP	0.671 ± 0.0041
	SWAT	0.896 ± 0.0016
\vdash	PSM	0.905 ± 0.0759
ഥ	N2	0.390 ± 0.0596
	N5	0.422 ± 0.0047
	R	0.361 ± 0.0204
	В	0.208 ± 0.0462
	S	0.381 ± 0.0621
	SMD	0.734 ± 0.0559
	MSL	0.785 ± 0.0277
	SMAP	0.534 ± 0.0051
	SWAT	0.875 ± 0.0033
ĸ.	PSM	0.878 ± 0.0624
щ	N2	0.337 ± 0.0592
	N5	0.368 ± 0.0498
	R	0.297 ± 0.0218
	В	0.177 ± 0.0426
_	S	0.318 ± 0.0648
	SMD	0.874 ± 0.0029
	MSL	0.820 ± 0.0130
	SMAP	0.900 ± 0.0007
	SWAT	0.918 ± 0.0006
۵	PSM	0.934 ± 0.0925
Щ	N2	0.464 ± 0.0561
	N5	0.496 ± 0.0396
	R	0.463 ± 0.0139
	В	0.253 ± 0.0498
	S	0.477 ± 0.5000
_		

I.3 FORECASTING RESULTS - MEANS AND STANDARD DEVIATIONS

Table 16: TOTEM - Specialist Forecasting (\downarrow)

Mean ± Std					
<u>Metric</u>	MSE MAE				
≥ 192 336 720	$\begin{array}{c} 0.165 \pm 0.0015 0.208 \pm 0.0012 \\ 0.207 \pm 0.0006 0.250 \pm 0.0012 \\ 0.257 \pm 0.0002 0.291 \pm 0.0006 \\ 0.326 \pm 0.0035 0.340 \pm 0.0023 \end{array}$				
96 192 336 720	$\begin{array}{c} 0.178 \pm 0.0015 0.263 \pm 0.0010 \\ 0.187 \pm 0.0015 0.272 \pm 0.0015 \\ 0.199 \pm 0.0012 0.285 \pm 0.0012 \\ 0.236 \pm 0.0035 0.318 \pm 0.0031 \\ \end{array}$				
⊢ 192 336 720	$\begin{array}{c} 0.523 \pm 0.0010 0.303 \pm 0.0006 \\ 0.530 \pm 0.0030 0.303 \pm 0.0017 \\ 0.549 \pm 0.0017 0.311 \pm 0.0021 \\ 0.598 \pm 0.0095 0.331 \pm 0.0062 \end{array}$				
E 192 336 720	$\begin{array}{c} 0.320 \pm 0.0006 0.347 \pm 0.0006 \\ 0.379 \pm 0.0017 0.382 \pm 0.0012 \\ 0.406 \pm 0.0040 0.402 \pm 0.0026 \\ 0.471 \pm 0.0006 0.438 \pm 0.0010 \end{array}$				
SE 192 192 336 720	$\begin{array}{c} 0.176 \pm 0.0006 0.253 \pm 0.0010 \\ 0.247 \pm 0.0012 0.302 \pm 0.0015 \\ 0.317 \pm 0.0046 0.348 \pm 0.0031 \\ 0.426 \pm 0.0085 0.410 \pm 0.0062 \end{array}$				
⊒ 192 336 720	$\begin{array}{c} 0.380 \pm 0.0006 0.394 \pm 0.0000 \\ 0.434 \pm 0.0010 0.427 \pm 0.0006 \\ 0.490 \pm 0.0023 0.459 \pm 0.0015 \\ 0.539 \pm 0.0031 0.513 \pm 0.0020 \end{array}$				
2 192 336 720	$\begin{array}{c} 0.293 \pm 0.0015 0.338 \pm 0.0006 \\ 0.375 \pm 0.0031 0.390 \pm 0.0026 \\ 0.422 \pm 0.0046 0.431 \pm 0.0031 \\ 0.610 \pm 0.0095 0.567 \pm 0.0081 \end{array}$				

Table 17: GPT2 - Specialist Forecasting, Lookback Window of 96 (\downarrow)

Metric	Mean ± Std MSE MAE				
≥ 192 336 720	0.184 ± 0.0013	0.224 ± 0.0014			
四 192 336 720	$\begin{array}{c} 0.186 \pm 0.0004 \\ 0.190 \pm 0.0007 \\ 0.204 \pm 0.0003 \\ 0.245 \pm 0.0012 \\ \end{array}$	0.278 ± 0.0008 0.291 ± 0.0005			
⊢ 192 336 720	$\begin{array}{c} 0.471 \pm 0.0016 \\ 0.479 \pm 0.0017 \\ 0.490 \pm 0.0009 \\ 0.524 \pm 0.0019 \end{array}$	$\begin{array}{c} 0.311 \pm 0.0016 \\ 0.312 \pm 0.0010 \\ 0.317 \pm 0.0010 \\ 0.336 \pm 0.0018 \end{array}$			
E 192 336 720	$\begin{array}{c} 0.328 \pm 0.0022 \\ 0.368 \pm 0.0006 \\ 0.400 \pm 0.0013 \\ 0.462 \pm 0.0010 \end{array}$	0.404 ± 0.0011			
720 96 E 192 336 720	$\begin{array}{c} 0.178 \pm 0.0000 \\ 0.245 \pm 0.0000 \\ 0.307 \pm 0.0000 \\ 0.410 \pm 0.0000 \end{array}$	$egin{array}{l} 0.263 \pm 0.0000 \ 0.307 \pm 0.0000 \ 0.346 \pm 0.0000 \ 0.409 \pm 0.0000 \end{array}$			
∃ 192 336 720	$\begin{array}{c} 0.379 \pm 0.0032 \\ 0.438 \pm 0.0037 \\ 0.474 \pm 0.0045 \\ 0.496 \pm 0.0066 \end{array}$	0.427 ± 0.0004 0.448 ± 0.0004			
≥ 96 192 336 720	$\begin{array}{c} 0.295 \pm 0.0000 \\ 0.384 \pm 0.0000 \\ 0.418 \pm 0.0000 \\ 0.423 \pm 0.0000 \\ \end{array}$	0.402 ± 0.0000 0.432 ± 0.0000			

Table 18: TOTEM - Generalist and Zero-Shot Forecasting (\downarrow)

М	etric	Mean ± Std MSE MAE
M	96 192 336 720	$\begin{array}{c} 0.172 \pm 0.0010 0.216 \pm 0.0000 \\ 0.217 \pm 0.0006 0.256 \pm 0.0006 \\ 0.266 \pm 0.0015 0.295 \pm 0.0015 \\ 0.334 \pm 0.0010 0.342 \pm 0.0012 \\ \end{array}$
Э	96 192 336 720	$\begin{array}{c} 0.179 \pm 0.0006 0.264 \pm 0.0012 \\ 0.181 \pm 0.0006 0.267 \pm 0.0000 \\ 0.196 \pm 0.0020 0.283 \pm 0.0013 \\ 0.230 \pm 0.0035 0.314 \pm 0.0023 \\ \end{array}$
T	96 192 336 720	$\begin{array}{c} 0.507 \pm 0.0020 0.284 \pm 0.0006 \\ 0.511 \pm 0.0030 0.282 \pm 0.0006 \\ 0.535 \pm 0.0076 0.292 \pm 0.0012 \\ 0.580 \pm 0.0046 0.309 \pm 0.0006 \end{array}$
m1	96 192 336 720	$\begin{array}{c} 0.374 \pm 0.0000 0.384 \pm 0.0006 \\ 0.400 \pm 0.0015 0.399 \pm 0.0025 \\ 0.432 \pm 0.0040 0.424 \pm 0.0015 \\ 0.487 \pm 0.0081 0.460 \pm 0.0017 \end{array}$
m ₂	96 192 336 720	$\begin{array}{c} 0.198 \pm 0.0006 0.275 \pm 0.0012 \\ 0.266 \pm 0.0035 0.319 \pm 0.0021 \\ 0.365 \pm 0.0115 0.377 \pm 0.0038 \\ 0.588 \pm 0.0699 0.511 \pm 0.0281 \end{array}$
h1	96 192 336 720	$\begin{array}{c} 0.382 \pm 0.0364 0.404 \pm 0.0012 \\ 0.463 \pm 0.0025 0.435 \pm 0.0006 \\ 0.507 \pm 0.0025 0.463 \pm 0.0016 \\ 0.517 \pm 0.0010 0.500 \pm 0.0017 \end{array}$
h2	96 192 336 720	$\begin{array}{c} 0.307 \pm 0.0012 0.345 \pm 0.0015 \\ 0.406 \pm 0.0038 0.403 \pm 0.0025 \\ 0.505 \pm 0.0114 0.460 \pm 0.0035 \\ 0.661 \pm 0.0514 0.557 \pm 0.0215 \\ \end{array}$
		Zero-Shot
Z2	96 192 336 720	$\begin{array}{c} 1.138 \pm 0.0032 \mid 0.777 \pm 0.0012 \\ 1.149 \pm 0.0026 \mid 0.785 \pm 0.0012 \\ 1.092 \pm 0.0062 \mid 0.770 \pm 0.0026 \\ 1.045 \pm 0.0040 \mid 0.754 \pm 0.0026 \end{array}$
SN.	96 192 336 720	$\begin{array}{c} 0.483 \pm 0.0012 0.484 \pm 0.0012 \\ 0.495 \pm 0.0021 0.491 \pm 0.0015 \\ 0.468 \pm 0.0035 0.483 \pm 0.0025 \\ 0.451 \pm 0.0023 0.477 \pm 0.0025 \end{array}$
м	96 192 336 720	$\begin{array}{c} 1.120 \pm 0.0081 \mid 0.582 \pm 0.0036 \\ 1.242 \pm 0.0151 \mid 0.635 \pm 0.0074 \\ 1.237 \pm 0.0153 \mid 0.626 \pm 0.0076 \\ 1.182 \pm 0.0151 \mid 0.604 \pm 0.0056 \end{array}$
В	96 192 336 720	$\begin{array}{c} 0.805 \pm 0.0070 0.739 \pm 0.0035 \\ 0.836 \pm 0.0040 0.752 \pm 0.0021 \\ 0.809 \pm 0.0038 0.748 \pm 0.0021 \\ 0.896 \pm 0.0137 0.794 \pm 0.0085 \end{array}$
S	96 192 336 720	$\begin{array}{c} 0.446 \pm 0.0032 0.482 \pm 0.0017 \\ 0.462 \pm 0.0015 0.491 \pm 0.0016 \\ 0.521 \pm 0.0122 0.525 \pm 0.0068 \\ 0.717 \pm 0.0096 0.625 \pm 0.0046 \end{array}$

Table 19: GPT2 - Generalist and Zero-Shot Forecasting (\downarrow)

_										
M	etric		MSE		ean	±		ИAЕ	,	
×	96 192 336 720	$ \begin{array}{c} 0.201 \\ 0.247 \\ 0.298 \\ 0.372 \\ \end{array} $	± 7 ± ± ± ± ±	0.00 0.00 0.00)17)20)06)10	0.2 0.2 0.3	237 275 311 360	\pm (Q.Ç	$\begin{array}{c} 012 \\ 015 \\ 006 \\ 006 \end{array}$
ш	96 192 336 720	$ \begin{array}{c} 0.194 \\ 0.199 \\ 0.214 \\ 0.255 \\ \end{array} $	1 ± 1 ± 1 ± 5 ±	0.00 0.00 0.00)12)06)12)06	0.2 0.2 0.3	278 284 300 331	±±±±±	0.0	$\begin{array}{c} 021 \\ 006 \\ 015 \\ 012 \end{array}$
L	96 192 336 720	$\begin{array}{c} 0.484 \\ 0.488 \\ 0.502 \\ 0.534 \end{array}$		0.00 0.00 0.00 0.00				± (± (0.0 0.0	$ \begin{array}{c} 042 \\ 006 \\ 021 \\ 021 \\ \end{array} $
m1	96 192 336 720	$\begin{array}{c} 0.487 \\ 0.516 \\ 0.548 \\ 0.581 \end{array}$	± 1	0.01 0.00 0.00 0.00	$^{171}_{15}$	0.4	168 180 199 511	± (J.U	$\begin{array}{c} 035 \\ 021 \\ 015 \\ 012 \end{array}$
_ m2	96 192 336 720	$\begin{array}{c} 0.243 \\ 0.297 \\ 0.349 \\ 0.439 \end{array}$	3 ± 7 ± 9 ± 9 ±	0.00 0.00 0.00 0.00)21)12)25)10	0.3 0.3 0.4	315 346 376 423	± (0.00	$\begin{array}{c} 021 \\ 010 \\ 020 \\ 010 \end{array}$
h1	96 192 336 720	$\begin{array}{c} 0.421 \\ 0.480 \\ 0.518 \\ 0.517 \end{array}$) ±) ± 3 ± 7 ±	0.00 0.00 0.01 0.00	LOI	IU.4	153	± (0.00	$\begin{array}{c} 010 \\ 020 \\ 070 \\ 035 \end{array}$
h2	96 192 336 720	$ 0.298 \\ 0.381 \\ 0.406 \\ 0.423$	8 ± 1 ± 3 ±	0.00 0.01 0.02 0.00)90 53 271)78	0.3 0.3 0.4 0.4	343 392 419 438	± ().0).0	$049 \\ 072 \\ 144 \\ 051$
			Zeı	:o-s	Sho	ot				
Z	96 192 336 720	$\begin{vmatrix} 1.332 \\ 1.416 \\ 1.358 \\ 1.308 \end{vmatrix}$	2 ± 3 ± 3 ± 3 ± 3 ±	0.00	$\begin{array}{c} 012 \\ 080 \\ 123 \\ 026 \end{array}$	8.0 8.0 8.0	830 863 851 840	± ().U).O	$010 \\ 025 \\ 042 \\ 010$
N2	96 192 336 720	$ \begin{array}{c} 0.528 \\ 0.578 \\ 0.548 \\ 0.537 \end{array} $	3 ± 3 ± 3 ± 7 ±	0.00 0.00 0.00 0.00	006 015 040 006	0.4 0.5 0.5	199 524 515 511	± (0.00	$\begin{array}{c} 010 \\ 006 \\ 015 \\ 006 \end{array}$
~	96 192 336 720	$\begin{array}{c} 1.465 \\ 1.638 \\ 1.601 \\ 1.552 \end{array}$	5 ± 3 ± 1 ± 2 ±	0.01 0.02 0.02 0.01	185 280 244 110	0. 0. 0. 0.	725 785 769 760	±8	0.00	$\begin{array}{c} 031 \\ 078 \\ 060 \\ 035 \end{array}$
В	96 192 336 720	$ \begin{array}{c} 0.838 \\ 0.837 \\ 0.792 \\ 0.927 \end{array} $	3 ± 7 ± 2 ± 7 ±	0.01 0.00 0.01 0.00	104	8:	738	± (0.00	$071 \\ 040 \\ 050 \\ 038$
S	96 192 336 720	$\begin{array}{c} 0.443 \\ 0.481 \\ 0.541 \\ 0.773 \end{array}$	3 ± 1 ± 1 ± 3 ±	0.00 0.00 0.00 0.00)10)06)10)20	0.4 0.4 0.5 0.6	178 199 533 543	± (0.0 0.0	006 006 006 010

I.4 Additional Ablations

Table 20: TimeTOTEM Ablation - Specialist Forecasting

Mean ± Std
$\geqslant \begin{array}{c} 96 \mid 0.164 \pm 0.0006 \mid 0.209 \pm 0.0006 \\ \geqslant 192 \mid 0.209 \pm 0.0017 \mid 0.251 \pm 0.0023 \\ 336 \mid 0.261 \pm 0.0012 \mid 0.293 \pm 0.0017 \\ 720 \mid 0.332 \pm 0.0023 \mid 0.340 \pm 0.0006 \\ \end{array}$
$ \begin{array}{c} 96 \mid 0.179 \pm 0.0015 \mid 0.262 \pm 0.0015 \\ \bowtie 192 \mid 0.185 \pm 0.0006 \mid 0.269 \pm 0.0000 \\ 336 \mid 0.204 \pm 0.0055 \mid 0.289 \pm 0.0061 \\ 720 \mid 0.244 \pm 0.0040 \mid 0.325 \pm 0.0036 \\ \end{array} $
$ \begin{array}{c} 96 \mid \! 0.528 \pm 0.0081 \mid \! 0.310 \pm 0.0092 \\ \vdash 192 \mid \! 0.500 \pm 0.0606 \mid \! 0.349 \pm 0.0699 \\ 336 \mid \! 0.531 \pm 0.0424 \mid \! 0.365 \pm 0.0852 \\ 720 \mid \! 0.578 \pm 0.0361 \mid \! 0.398 \pm 0.1103 \end{array} $
$\begin{array}{c} -96 \mid 0.326 \pm 0.0006 \mid 0.355 \pm 0.0006 \\ \hline \text{E} \mid 392 \mid 0.377 \pm 0.0023 \mid 0.386 \pm 0.0012 \\ \hline \text{E} \mid 336 \mid 0.409 \pm 0.0006 \mid 0.409 \pm 0.0006 \\ \hline 720 \mid 0.469 \pm 0.0015 \mid 0.441 \pm 0.0000 \\ \end{array}$
$\begin{array}{c} 96 \mid 0.176 \pm 0.0010 \mid 0.254 \pm 0.0006 \\ \exists \mid 192 \mid 0.247 \pm 0.0031 \mid 0.303 \pm 0.0026 \\ \exists \mid 336 \mid 0.318 \pm 0.0006 \mid 0.350 \pm 0.0021 \\ 720 \mid 0.419 \pm 0.0067 \mid 0.411 \pm 0.0044 \end{array}$
$\begin{array}{c} 96 \mid 0.377 \pm 0.0010 \mid 0.395 \pm 0.0006 \\ 192 \mid 0.428 \pm 0.0015 \mid 0.428 \pm 0.0015 \\ 336 \mid 0.480 \pm 0.0021 \mid 0.462 \pm 0.0012 \\ 720 \mid 0.530 \pm 0.0110 \mid 0.522 \pm 0.0108 \end{array}$
$\begin{array}{c} 96 \mid 0.294 \pm 0.0021 \mid 0.338 \pm 0.0010 \\ 9192 \mid 0.373 \pm 0.0023 \mid 0.389 \pm 0.0032 \\ 3360 \cdot 4.23 \pm 0.0031 \mid 0.433 \pm 0.0051 \\ 720 \mid 0.591 \pm 0.0145 \mid 0.556 \pm 0.0051 \end{array}$

Table 21: TimeTOTEM Ablation - Generalist and Zero-Shot Forecasting

М	etric	Mean ± Std MSE MAE
<u>IVI</u>	96 192 336 720	$\begin{array}{ c c c c c }\hline \text{MSE} & \text{MAE}\\\hline 0.173 \pm 0.0012 0.218 \pm 0.0006\\0.218 \pm 0.0006 0.261 \pm 0.0006\\0.267 \pm 0.0006 0.299 \pm 0.0006\\0.337 \pm 0.0010 0.347 \pm 0.0006\\\hline \end{array}$
ш	96 192 336 720	$\begin{array}{c} 0.183\pm0.0012 0.267\pm0.0012\\ 0.189\pm0.0006 0.275\pm0.0000\\ 0.204\pm0.0010 0.291\pm0.0010\\ 0.242\pm0.0006 0.325\pm0.0006 \end{array}$
L	96 192 336 720	$\begin{array}{c} 0.517\pm0.0000 0.293\pm0.0029\\ 0.526\pm0.0030 0.296\pm0.0006\\ 0.552\pm0.0015 0.304\pm0.0015\\ 0.602\pm0.0046 0.326\pm0.0015 \end{array}$
ml	96 192 336 720	$\begin{array}{c} 0.428\pm0.0090 0.420\pm0.0040\\ 0.438\pm0.0015 0.427\pm0.0010\\ 0.469\pm0.0062 0.447\pm0.0042\\ 0.546\pm0.0081 0.493\pm0.0017 \end{array}$
m2	96 192 336 720	$\begin{array}{c} 0.207\pm0.0015 0.286\pm0.0020\\ 0.269\pm0.0015 0.325\pm0.0010\\ 0.358\pm0.0199 0.377\pm0.0091\\ 0.521\pm0.0165 0.482\pm0.0026 \end{array}$
h1	96 192 336 720	$\begin{array}{c} 0.401 \pm 0.0006 0.410 \pm 0.0006 \\ 0.453 \pm 0.0010 0.441 \pm 0.0010 \\ 0.496 \pm 0.0017 0.468 \pm 0.0006 \\ 0.518 \pm 0.0020 0.510 \pm 0.0017 \end{array}$
h2	96 192 336 720	$\begin{array}{c} 0.305\pm0.0006 0.346\pm0.0006\\ 0.396\pm0.0015 0.402\pm0.0001\\ 0.492\pm0.0310 0.458\pm0.0131\\ 0.599\pm0.0105 0.531\pm0.0026 \end{array}$
N2	96 192 336 720	$\begin{array}{c} 1.127 \pm 0.0017 0.773 \pm 0.0006 \\ 1.169 \pm 0.0032 0.793 \pm 0.0010 \\ 1.115 \pm 0.0010 0.780 \pm 0.0006 \\ 1.070 \pm 0.0035 0.766 \pm 0.0010 \\ \end{array}$
N5	96 192 336 720	$\begin{array}{c} 0.481\pm0.0015 0.483\pm0.0006\\ 0.508\pm0.0012 0.500\pm0.0000\\ 0.481\pm0.0006 0.491\pm0.0006\\ 0.467\pm0.0010 0.488\pm0.0010 \end{array}$
~	96 192 336 720	$\begin{array}{c} 1.102\pm0.0031 0.578\pm0.0021\\ 1.207\pm0.0036 0.628\pm0.0017\\ 1.190\pm0.0021 0.613\pm0.0010\\ 1.149\pm0.0017 0.596\pm0.0020 \end{array}$
В	96 192 336 720	$\begin{array}{c} 0.825\pm0.0079 0.751\pm0.0076\\ 0.847\pm0.0021 0.761\pm0.0012\\ 0.831\pm0.0066 0.764\pm0.0042\\ 0.928\pm0.0131 0.813\pm0.0050 \end{array}$
S	96 192 336 720	$\begin{array}{c} 0.446\pm0.0015 0.481\pm0.0010\\ 0.478\pm0.0015 0.499\pm0.0000\\ 0.535\pm0.0012 0.532\pm0.0006\\ 0.736\pm0.0025 0.631\pm0.0006 \end{array}$

Table 22: **Detailed Codebook Ablation** (\downarrow)

K	Mean =	
≥ 256 0. ≥ 512 0. 32 0.	016 ± 0.00040 013 ± 0.00110 039 ± 0.00050	0.067 ± 0.0011 0.061 ± 0.0032 0.112 ± 0.0064
		0.103 ± 0.0029 0.088 ± 0.0014 0.152 ± 0.0016
		0.075 ± 0.0007 0.069 ± 0.0044 0.120 ± 0.0008
		0.094 ± 0.0007 0.091 ± 0.0062 0.146 ± 0.0030

I.5 EXPLORATORY RESULTS

Table 23: Mixed Models - Forecasting (\downarrow)

_				
Metric		Mean \pm Std		
IVI	eunc	MSE MAE		
<u>≽</u>	96 192 336 720	$\begin{array}{c} 0.164 \pm 0.0010 0.208 \pm 0.0012 \\ 0.208 \pm 0.0010 0.251 \pm 0.0015 \\ 0.258 \pm 0.0012 0.290 \pm 0.0015 \\ 0.329 \pm 0.0021 0.338 \pm 0.0015 \end{array}$		
ш	96 192 336 720	$\begin{array}{c} 0.178 \pm 0.0006 \mid 0.263 \pm 0.0010 \\ 0.187 \pm 0.0021 \mid 0.273 \pm 0.0017 \\ 0.199 \pm 0.0012 \mid 0.285 \pm 0.0017 \\ 0.238 \pm 0.0012 \mid 0.320 \pm 0.0012 \\ \end{array}$		
L	96 192 336 720	$\begin{array}{c} 0.521 \pm 0.0010 0.301 \pm 0.0010 \\ 0.530 \pm 0.0023 0.303 \pm 0.0012 \\ 0.555 \pm 0.0080 0.313 \pm 0.0072 \\ 0.605 \pm 0.0097 0.337 \pm 0.0075 \end{array}$		
ml	96 192 336 720	$\begin{array}{c} 0.328 \pm 0.0036 0.352 \pm 0.0006 \\ 0.377 \pm 0.0021 0.383 \pm 0.0012 \\ 0.408 \pm 0.0035 0.404 \pm 0.0021 \\ 0.470 \pm 0.0035 0.440 \pm 0.0021 \end{array}$		
m2	96 192 336 720	$\begin{array}{c} 0.175 \pm 0.0006 \mid 0.253 \pm 0.0010 \\ 0.247 \pm 0.0006 \mid 0.302 \pm 0.0010 \\ 0.318 \pm 0.0006 \mid 0.348 \pm 0.0031 \\ 0.427 \pm 0.0012 \mid 0.410 \pm 0.0067 \end{array}$		
PI	96 192 336 720	$\begin{array}{c} 0.382 \pm 0.0025 \mid 0.395 \pm 0.0015 \\ 0.437 \pm 0.0012 \mid 0.427 \pm 0.0006 \\ 0.490 \pm 0.0015 \mid 0.460 \pm 0.0021 \\ 0.536 \pm 0.0031 \mid 0.512 \pm 0.0032 \end{array}$		
h2	96 192 336 720	$\begin{array}{c} 0.294 \pm 0.0010 \mid 0.339 \pm 0.0012 \\ 0.375 \pm 0.0025 \mid 0.391 \pm 0.0023 \\ 0.421 \pm 0.0050 \mid 0.431 \pm 0.0031 \\ 0.610 \pm 0.0089 \mid 0.567 \pm 0.0075 \end{array}$		

Table 24: Traffic Only - Specialist Zero-Shot Performance (\downarrow)

M	etric	Mean MSE	\pm Std MAE
N2	96 192 336 720	$\begin{array}{c} 1.194 \pm 0.0062 \\ 1.218 \pm 0.0074 \\ 1.190 \pm 0.0153 \\ 1.117 \pm 0.0137 \end{array}$	$\begin{array}{c} 0.798 \pm 0.0020 \\ 0.808 \pm 0.0023 \\ 0.804 \pm 0.0052 \\ 0.784 \pm 0.0056 \end{array}$
N5	96 192 336 720	$\begin{array}{c} 0.515 \pm 0.0026 \\ 0.535 \pm 0.0051 \\ 0.524 \pm 0.0071 \\ 0.500 \pm 0.0064 \end{array}$	$\begin{array}{c} 0.505 \pm 0.0012 \\ 0.514 \pm 0.0028 \\ 0.513 \pm 0.0030 \\ 0.507 \pm 0.0032 \end{array}$
2	96 192 336 720	11.232 ± 0.0055	$\begin{array}{c} 0.635 \pm 0.0019 \\ 0.673 \pm 0.0042 \\ 0.653 \pm 0.0022 \\ 0.642 \pm 0.0041 \end{array}$
В	96 192 336 720	$\begin{array}{c} 0.812 \pm 0.0037 \\ 0.858 \pm 0.0025 \\ 0.826 \pm 0.0041 \\ 0.919 \pm 0.0063 \\ \end{array}$	$\begin{array}{c} 0.749 \pm 0.0025 \\ 0.767 \pm 0.0015 \\ 0.759 \pm 0.0030 \\ 0.803 \pm 0.0037 \end{array}$
S	96 192 336 720	$\begin{array}{c} 0.476 \pm 0.0012 \\ 0.511 \pm 0.0005 \\ 0.576 \pm 0.0024 \\ 0.795 \pm 0.0017 \end{array}$	$\begin{array}{c} 0.508 \pm 0.0012 \\ 0.528 \pm 0.0005 \\ 0.568 \pm 0.0009 \\ 0.685 \pm 0.0012 \end{array}$

Table 25: Electricity Only - Specialist Zero-Shot Performance (\downarrow)

M	etric	Mean ± Std MSE MAE	
N2	96 192 336 720	$\begin{array}{c} 1.193 \pm 0.0059 0.802 \pm 0.002 \\ 1.300 \pm 0.0016 0.845 \pm 0.006 \\ 1.260 \pm 0.0162 0.837 \pm 0.003 \\ 1.234 \pm 0.0054 0.832 \pm 0.003 \end{array}$)3 55
NS	96 192 336 720	$\begin{array}{c} 0.489 \pm 0.0024 \mid \! 0.490 \pm 0.001 \\ 0.555 \pm 0.0012 \mid \! 0.527 \pm 0.000 \\ 0.538 \pm 0.0064 \mid \! 0.525 \pm 0.003 \\ 0.533 \pm 0.0010 \mid \! 0.527 \pm 0.000 \end{array}$	$\frac{1}{3}$
R	96 192 336 720	$\begin{array}{c} 1.141 \pm 0.0056 \mid 0.579 \pm 0.002 \\ 1.297 \pm 0.0162 \mid 0.652 \pm 0.007 \\ 1.247 \pm 0.0108 \mid 0.628 \pm 0.003 \\ 1.236 \pm 0.0053 \mid 0.633 \pm 0.007 \end{array}$	79 59
В	96 192 336 720	$\begin{array}{c} 0.820 \pm 0.0065 0.756 \pm 0.003 \\ 0.843 \pm 0.0042 0.759 \pm 0.002 \\ 0.791 \pm 0.0023 0.741 \pm 0.002 \\ 0.886 \pm 0.0059 0.790 \pm 0.002 \end{array}$	22 19
S	96 192 336 720	$\begin{array}{c} 0.460 \pm 0.0017 0.487 \pm 0.001 \\ 0.505 \pm 0.0017 0.511 \pm 0.001 \\ 0.569 \pm 0.0020 0.545 \pm 0.001 \\ 0.764 \pm 0.0046 0.641 \pm 0.001 \\ \end{array}$)8 11