

AN EFFECTIVE VARIANCE CHANGE DETECTION METHOD UNDER CONSTANTLY CHANGING MEAN

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Paper under double-blind review

ABSTRACT

1 Effectively evaluating the viability of a procured organ in the transplant patient
2 prior the procedure is of critical importance. Current viability assessment methods
3 rely on evaluating the organ’s morphology and/or laboratory biopsy results with
4 limited effectiveness. A recently proposed, well-designed noninvasive method
5 evaluated the viability status of organs by detecting the variance change point
6 of their surface temperature through exploring the entire data profile. However,
7 most part of the data in a temperature profile barely contains the change informa-
8 tion, which yields a waste of computational resources of their method. This paper
9 proposes an accelerating algorithm with a well-designed dual control windows
10 scheme that can be extended to online change detection. The proposed method
11 significantly improves the computational speed and retains the same change de-
12 tection power as the method Gao19 through the removal of redundant data. Simu-
13 lation and application results demonstrate the robust performance of the proposed
14 method.

15 1 INTRODUCTION

16 Organ transplantation is an effective method to treat end-stage diseases of various organs. Due
17 to the limitation of storage and transportation techniques, the viability of organs cannot be fully
18 guaranteed. Therefore, the quality of procured organs must be evaluated before transplantation.
19 Different organs can accept different cold ischemia time. For example, the upper limit of the cold
20 ischemia time of the liver is about 12 hours, and that of the heart is only 8 hours. Therefore, in an
21 organ transplantation operation, both doctors and patients are racing against time. The traditional
22 evaluation often relies on subjective experience in the viability of the organ based on the physical
23 shape and some functional data. In many cases, it is impossible to clearly distinguish the viable
24 organs from nonviable organs. Laboratory biopsy usually cut off a small piece of the organ for an
25 integrity test of the transplanted organs. However, the test results of samples cannot represent the
26 viability state of the entire organ, which leads to a missing identification of the transplantable organ
27 areas, and results in a waste of valuable organs. Therefore, in order to further improve the utilization
28 rate of transplanted organs, a more accurate and convenient organ viability change detection method
29 is desired.

30 It has been proved that there is a strong correlation between surface temperature of organs and
31 their viability (Skowno & Karpelowsky, 2014; Vidal et al., 2014; Kochan et al., 2015), where the
32 surface temperature of the viable organ fluctuates greatly. A research team of clinical scientists and
33 engineers at Virginia Tech designed a set of noninvasive organ viability evaluation methods (Bhonsle
34 et al., 2016; O’Brien et al., 2017; Gao et al., 2019). A porcine liver was used in the experiment.
35 The organ surface was divided into a dense grid covering the entire liver surface. A noninvasive,
36 high-precision thermal imaging system was used to measure the surface temperature of the liver.
37 Temperatures were collected every ten minutes for 24 hours. Figure 1 is the temperature profile
38 of a randomly selected spot on the organ surface. From the plots we see that the mean trend of
39 the temperature changes slowly and smoothly in the perfusion process. The surface temperature
40 fluctuates strongly in the first 12 hours, which indicates a high viability of the organ. After 12
41 hours’ perfusion, a sudden viability drop appears, and the organ gradually loses its viability. The red
42 vertical line is the potential viability change point. Then, the viability evaluation of a procured organ
43 is transformed from a medical problem into a statistical problem of variance change point detection
44 under a smoothly changing mean trend.

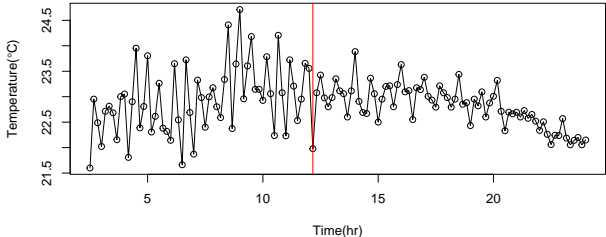


Figure 1: Temperature profile at a randomly selected spot of the liver. The red vertical line is the approximated location of the variance change point.

45 Recent research on the change point detection are mainly based on the parametric methods and
 46 the nonparametric methods. The parametric method assumes that the data distribution belongs to
 47 a certain distribution family, and infers sudden changes in one or several parameters of the data
 48 distribution (Inclan & Tiao, 1994; Chen & Gupta, 1997; Pan & Chen, 2006; Kang et al., 2018; Dette
 49 & Gösmann, 2020; Wang et al., 2021). However, these existing methods cannot be applied in our
 50 liver experiment, since not only the variance change suddenly, the mean function of the temperature
 51 profile also changes smoothly. The nonparametric change point detection method does not depend
 52 on an overall distribution (Hariz et al., 2007; Matteson & James, 2014; Zou et al., 2014; Yu & Chen,
 53 2022). These methods can effectively detect sudden changes. However, the data obtained from
 54 the liver experiment not only has a sudden change in variance, but also has constant changes in the
 55 mean function. This constantly changing mean will affect the detection effect of the variance change
 56 point. Directly applying these methods to the liver data will lead to an ironic detection result. For
 57 the smooth mean estimation in the liver data, the smoothing spline is one of the common method
 58 (Shang & Cheng, 2013; 2017; Xu & Wang, 2018). There are also some methods combining mean
 59 function estimation and change detection together (Loader, 1996; Liao & Meyer, 2017; Grégoire &
 60 Hamrouni, 2002). However, all these methods are about to estimate the sudden changes in the mean
 61 curve. They are not suitable for our scenario, where the mean function changes constantly in our
 62 scenario.

63 Gao et al. (2019; 2020) proposed algorithms that can do the smooth mean function estimation and
 64 the variance change point detection simultaneously. However, limited by the practical meaning of
 65 the application scenario, it is very common that the location of the change point is normally in a
 66 certain range. In the liver experiment, we found that the variance change point of the temperature
 67 profile is basically distributed in 10-16 hours. However, the computational logic of their methods
 68 needs to scan the entire data profile, in which most parts of the data series have no change point.
 69 Therefore, scanning the whole time series to detect variance change points is unnecessary. There are
 70 more than 36,000 temperature profiles need to be analyzed in the scene of time competition. Clearly
 71 their methods are highly lack of efficiency.

72 In this paper, we propose a new variance change point detection approach with dual control windows
 73 to improve the computational efficiency of the method proposed by Gao et al. (2019) to simultane-
 74 ously improve the accuracy and speed of the change detection. In our proposed method one control
 75 window CW_α is designed for the mean estimation and the other control window CW_β is designed
 76 for the variance change point detection. In the liver procurement experiment, the variance change
 77 point of the liver surface temperature generally conforms to a normal distribution. We obtain the
 78 preliminary variance change points information by randomly scanning a group of temperature pro-
 79 files in the early stage, and construct a model for the mean estimation based on the distribution
 80 information of the variance change point. Our proposed method reduces the redundant data infor-
 81 mation sufficiently and allows to address an accurate estimate of the change point fleetly, which
 82 significantly improves the computational efficiency of the algorithm, and saves plenty of time in
 83 detection for urgent life saving circumstances.

84

2 METHOD

85

2.1 MODEL AND NOTATION

86 Suppose that y_t are the independent observations generated from the following model:

$$y_t = f_0(t/n) + \epsilon_t, \quad t = 1, \dots, n,$$

87 where f_0 is an unknown smoothing function, $\epsilon_t \sim N(0, \sigma_t^2)$ is the error term. Let τ be the position
88 of the variance change point. σ_0^2 and δ_0^2 are variances. For $t \leq \tau$, $\sigma_t^2 = \sigma_0^2$. For $t > \tau$, $\sigma_t^2 = \delta_0^2$.89 Algorithm 1 is the computational framework of our proposed method. This algorithm begins with
90 an initialization of the dual control windows. To obtain a possible range of the potential variance
91 change points, we firstly perform a preliminary variance change point detection procedure and con-
92 struct an initialized control window CW_α^0 for the mean estimation and a control window CW_β^0 for
93 the variance change point detection based on the randomly selected K data profiles. [The variance
94 change point detection procedures of these \$K\$ randomly selected data profiles are the method by
95 Gao et al. \(2019\)](#). Since the sample space of determining the control window CW_α^0 will be updated
96 iteratively in Algorithm 1, the choice of K is arbitrary as long as it satisfies the minimum statistical
97 requirement. Then we estimate the mean function and detect the variance change point within the
98 control windows. The dual control windows CW_α and CW_β are updated iteratively and simultane-
99 ously based on the information of the newly detected variance change points. The details of the dual
100 control windows are shown in Section 2.2.

101 All parameters' estimates are obtained by minimizing the following objective function,

$$\frac{1}{n}(\mathbf{y} - \mathbf{f})^\top \Sigma_{n,\tau,\sigma,\delta}^{-1}(\mathbf{y} - \mathbf{f}) + \lambda J(f), \quad (1)$$

102 where $\mathbf{y} = (y_1, y_2, \dots, y_n)^\top$, $\mathbf{f} = (f(1/n), f(2/n), \dots, f(1)^\top)$, $\Sigma_{n,\tau,\sigma,\delta}$ is a diagonal matrix,
103 where the first τ diagonals are σ_0^2 , and the rest are δ_0^2 . $J(f)$ is the roughness penalty with the
104 smoothing parameter $\lambda > 0$ balancing the tradeoff between the smoothness of the estimated mean
105 function and the goodness of fit represented by the weighted sum of squared errors. Since the objec-
106 tive function Equation 1 tends to zero as σ^2 goes to infinity, the global minimizer of Equation 1 does
107 not exist. Therefore an iterative parameter estimation procedure is designed to obtain a local optimal
108 solution. The parameter estimation starts with the initialization of the mean function $\hat{f}^{(0)}$ assuming
109 constant variance. Therefore, the covariance matrix in Equation 1 reduces to $\sigma^2 I$, and σ^2 can be
110 absorbed into the smoothing parameter λ . Given the mean function estimate, the variance change
111 point $\hat{\tau}$, and the variances $\hat{\sigma}^2$ and $\hat{\delta}^2$ are obtained in the change detection procedures. The mean
112 function estimates and the detected variance change points are updated iteratively. [The convergence
113 criterion of our proposed algorithm is the maximum absolute difference between the residuals of
114 the current iteration and the previous iteration. In the numerical experiments conducted in the later
115 sections, our algorithm can converge in a few iterations.](#) The consistency of parameter estimates has
116 been proved by Gao et al. (2019).117

2.2 THE DUAL CONTROL WINDOWS

118 Suppose we have detected K data profiles, and $\{\iota_1, \dots, \iota_K\}$ is the set of detected variance change
119 points. To build a proper control window CW_α for the mean estimation, we have verified that the
120 asymptotic distribution of the variance change point is normal. According to the empirical rule,
121 about 95% of the data falls into the range of the mean plus or minus two standard deviations. More
122 general, we use the upper quantiles of the standard normal distribution as an approximate substitute
123 to get CW'_α .

$$CW'_\alpha = [CLL'_\alpha, CLU'_\alpha], \quad CLL'_\alpha = \mu - W, \quad CLU'_\alpha = \mu + W,$$

Algorithm 1: Variance Change Point Detection with Dual Control Windows

Input: Data set $\mathcal{D} \in \mathbb{R}^{M \times n}$, where M is the number of data profiles, n is the length of each data profile

Output: $\{\hat{\tau}_1, \dots, \hat{\tau}_M\}$

Step1 Initialize the dual control windows. Randomly select K data profiles from \mathcal{D} , detect the variance change points $\hat{l}_1, \dots, \hat{l}_K$ to initialize the control window $CW_\alpha^{(0)}$ and $CW_\beta^{(0)}$.

Step2 Variance change detection within dual control windows. For the m^{th} data profile,

Step2.1 capture the reduced data profile $\mathbf{y}_m^* = \{y_i | i \in CW_\alpha^{(m-1)}\}$.

Step2.2 Initialize the mean function estimate $\hat{f}_m^{(0)}$ assuming constant variance.

$\hat{f}_m^{(0)}$ minimizes $\frac{1}{n}(\mathbf{y}_m - \mathbf{f}_m)^\top (\mathbf{y}_m - \mathbf{f}_m) + \lambda J(\mathbf{f}_m)$.

Step2.3 Estimate the variance change point iteratively. Each iteration consists of two steps. At the j^{th} iteration,

Step-A Given the mean estimate $\hat{f}^{(j-1)}$, the data profile

$\mathbf{y}_m^{**} = \{y_i | i \in CW_\beta^{(m-1)}\}$ is validated to yield estimates of $\hat{\tau}^{(j)}$,

$[\hat{\sigma}^2]^{(j)}$ and $[\hat{\delta}^2]^{(j)}$.

Step-B Substitute the current parameters estimates from Step-A into

Equation 1 to update the mean function estimate $\hat{f}^{(j)}$.

Step2.4 Iterate until the algorithm converges, and obtain the estimates

$\hat{\tau}_m, \hat{\sigma}_m^2, \hat{\delta}_m^2$, and \hat{f}_m .

Step2.5 Update $CW_\alpha^{(m)}$ and $CW_\beta^{(m)}$ by $\{\hat{l}_1, \dots, \hat{l}_K, \hat{\tau}_1, \dots, \hat{\tau}_m\}$.

124 where $\mu = \frac{1}{K} \sum_{i=1}^K \tau_i$, $W = z_q \sqrt{\frac{1}{K-1} \sum_{i=1}^K (\tau_i - \mu)^2}$, K is the number of detected change points,
 125 τ is the known change point data, and z_q is the upper quantile of the standard normal distribution
 126 corresponding to the desired accuracy.

127 In our method, we use the cubic splines method to estimate the mean functions. The computational
 128 efficiency of the smoothing spline method is highly affected by the sample size of the data. The
 129 minimizer f_λ of Equation 1 resides in the n -dimensional space, and the computation in multivariate
 130 settings is generally of the order $O(n^3)$ (Kim & Gu, 2004). Therefore, large sample size will ex-
 131 tremely slow down the computational speed. However, the accuracy of the mean function estimation
 132 using the nonparametric method highly relies on the sufficiency of the quantity of the data. In or-
 133 der to improve the speed of the algorithm without reducing the accuracy of parameter estimates, we
 134 need to choose an appropriate radius of the control window CW_α . We define a hyper parameter W_α ,
 135 which is the minimum size of the control window CW_α . The determination of W_α refers to the rule
 136 of elbow in the K-means clustering. The minimum window size can be estimated by balancing the
 137 tradeoff between the accuracy of the estimation and computational speed. For example, in the liver
 138 experiment, if we want the accuracy of the change detection to be above 0.95, we should ensure that
 139 the control window contains at least 100 data points. In that case, to make the calculations as fast as
 140 possible, we can choose $W_\alpha = 50$. Considering the above two factors, the definition for CW_α is

$$CW_\alpha = [CLL_\alpha, CLU_\alpha], \quad CLL_\alpha = \mu - \max\{W_\alpha, W\}, \quad CLU_\alpha = \mu + \max\{W_\alpha, W\},$$

141 where $\mu = \frac{1}{n} \sum_{i=1}^n \tau_i$, and $W = z_q \sqrt{\frac{1}{n-1} \sum_{i=1}^n (\tau_i - \mu)^2}$.

142 CW_β is designed for variance change point detection. Generally, the mean function estimation
 143 requires more data information than the variance change points detection. Therefore, a portion of
 144 the data contained in CW_α is redundant for variance change detection. Generally speaking, the
 145 change point location presents a high degree of concentration. This is a common situation in many
 146 change point detection problems, such as the change of the daily traffic flow data set of the same
 147 road section, the change of the stock market, and the change of the sales of an industry company.

148 Therefore, the variance change point detection interval CW_β should be further controlled to make
 149 the probability of variance change points in the interval reaches to a certain value or more, and
 150 those points that are not likely to become variance change points are eliminated as much as possible.
 151 According to the Glivenko-Cantelli Theorem, we have

$$P \left\{ \lim_{m \rightarrow \infty} \sup_{-\infty < \tau < \infty} |F_m(\tau) - F(\tau)| = 0 \right\} = 1,$$

152 where $F_m(\tau)$ is the empirical distribution function of the dataset $\{\tau_1, \dots, \tau_m\}$ and $F(\tau)$ is the real
 153 distribution function of the variance change points. When the sample size is large enough, we adopt
 154 the concepts of the probability interval to control the likelihood of the change point positions ac-
 155 cording to the empirical distribution function. We get $CW_\beta = [CLL_\beta, CLU_\beta]$, where the potential
 156 variance change points fall into this interval with a probability of at least q . The upper and lower
 157 bounds of CW_β satisfy $F_m(CLU_\beta) - F_m(CLL_\beta) \geq q$. Since the asymptotic distribution of the
 158 variance change point is normal, we can do it in terms of the quantile of the sample

$$CW_\beta = [CLL_\beta, CLU_\beta], \quad CLL_\beta = \tau_{\frac{1-q}{2}}, \quad CLU_\beta = \tau_{\frac{1+q}{2}},$$

159 where $\tau_{\frac{1\pm q}{2}}$ is the $\frac{1\pm q}{2}$ percentile of the detected variance change points. By using the control
 160 window $\hat{C}W_\beta$, we further reduce the amount of data used for variance change point detection.

161 2.3 SMOOTHING SPLINES ESTIMATION FOR MEAN FUNCTION

162 The mean estimation in this article uses the cubic smoothing splines. Before introducing the es-
 163 timation method for the mean function, it is necessary to first introduce the polynomial smooth-
 164 ing spline with period 1 on the interval $[0, 1]$. The mean function f_0 is estimated by minimiz-
 165 ing the objective function $\frac{1}{n} \sum_{i=1}^n (y_i - f_0(t_i))^2 + \lambda \int_0^1 (f_0^{(m)}(t))^2 dt$ in the space $C^{(m)}[0, 1] =$
 166 $\{f : f^{(m)} \in \mathcal{L}_2[0, 1]\}$, where $C^{(m)}[0, 1]$ is a reproducing kernel Hilbert space (RKHS). The true
 167 mean function f_0 is an unknown smoothing function and is a function in the reproducing kernel
 168 Hilbert space $\mathcal{C} = \{f \mid f : [0, 1] \rightarrow R, J(f) < \infty\}$. When σ^2, δ^2 and τ are given, the estimate of f_0
 169 is the minimizer of the penalized weighted least squares Equation 1, where the smoothness param-
 170 eter $\lambda > 0$ is chosen by the generalized cross-validation. Note that since \mathcal{C} is of infinite dimension,
 171 it is not possible to optimize Equation 1 on \mathcal{C} directly. However, since the weighted least squares
 172 part in Equation 1 depends on f_0 only at the observation $y_i, i \in [CLL_\alpha, CLU_\alpha]$, the representation
 173 theorem guarantees that the exact minimizer exists in a finite dimensional subspace of \mathcal{C} . Therefore,
 174 the minimizer of the objective function Equation 1 can be analytically obtained.

175 2.4 VARIANCE CHANGE POINT DETECTION

176 When the mean function estimate \hat{f} is given, the variance change point $\hat{\tau}$ is detected within the
 177 control window CW_β through a well designed hypothesis test procedure. The estimates of the
 178 variances are $\hat{\sigma}^2 = \hat{\tau}^{-1} \sum_{t=1}^{\hat{\tau}} \{y_t - \hat{f}(t/n)\}^2$ and $\hat{\delta}^2 = (n - \hat{\tau})^{-1} \sum_{t=\hat{\tau}+1}^n \{y_t - \hat{f}(t/n)\}^2$. For
 179 variance change point detection, establish the null and alternative hypotheses.

$$H_0 : \sigma_1^2 = \dots = \sigma_n^2 \quad vs \quad H_1 : \sigma_1^2 = \dots = \sigma_\tau^2 \neq \sigma_{\tau+1}^2 = \dots = \sigma_n^2$$

180 For a potential variance change point $\hat{\tau} = k, k \in \{1, \dots, n\}$, the likelihood function is

$$L(k) = k \left[\log \frac{1}{k} \sum_{t=1}^k \{y_t - \hat{f}(t/n)\}^2 \right] + (n - k) \left[\log \frac{1}{n - k} \sum_{t=k+1}^n \{y_t - \hat{f}(t/n)\}^2 \right],$$

181 then we have $L(n) = -2L_0(\hat{\sigma}^2) - n - n \log 2\pi$, and $L(\tau) = -2L_1(\hat{\sigma}^2, \hat{\delta}^2) - n - n \log 2\pi$. Where
 182 L_0 and L_1 are the log-likelihood functions under the hypotheses H_0 and H_1 . Then we have the
 183 definition of the test statistic: $\Delta_n^2 = \max_{1 < k < n} \{L(n) - L(k)\}$. By the principle of the minimum

184 information criterion, there is no evidence of the existence of the variance change point within the
 185 control window CW_β if $L(n) \leq \min_k L(k), k \in [CLL_\beta, CLU_\beta]$. The null hypothesis is failed to
 186 reject if $\exists k \in [CLL_\beta, CLU_\beta],$ we have $L(n) > L(k)$, then the null hypothesis is rejected, and there
 187 exists a variance change point. Therefore the position of the estimated variance change point is

$$\hat{\tau} = \arg \min_{CLL_\beta \leq k \leq CLU_\beta} L(k).$$

188 **3 SIMULATION**

189 In this section, we compare the performance of our proposed change detection method, which is
 190 denoted by the New method hereafter, with one of the most sufficient method in Gao et al. (2019)
 191 hereafter denoted by the Gao19 method. We conduct the comprehensive simulation studies using
 192 the same data generating schemes in Gao et al. (2019). Two mean functions $f_{01}(t) = 20 + 12t(1-t)$
 193 and $f_{02}(t) = \sin(t) + t^5 - 8t^3 + 10t + 6$ are considered. The first mean function f_{01} mimics the trend
 194 of the temperature profile obtained in the porcine liver procurement experiment, while the second
 195 function f_{02} represents a more complex smooth mean trend. We use two sample sizes $n = 130$
 196 and $n = 500$. When $n = 130$, the true variance change point is $\tau_0 = 65$ and the parameter of the
 197 control window $W_\alpha = 50$. When $n = 500$, we have $\tau_0 = 250$ and $W_\alpha = 190$. The true variances
 198 are $\sigma_0^2 = 0.24$ and $\delta_0^2 = 0.06$ when f_{01} is the mean function, and $\sigma_0^2 = 8$ and $\delta_0^2 = 2$ when f_{02}
 199 is the mean function. We simulated 1000 data replicates for each combination of simulation settings.
 200 We also conduct the sensitivity and power analysis of the proposed method. However, due to the
 201 limitation of the space, we include these studies in Appendix.

202 Figure 2 is the boxplots of the change point estimates of the proposed algorithm and the method
 203 of Gao19. New is our proposed algorithm. Gao19 and New are tested with sample size $n = 130$.
 204 New500 represents the change point estimates of the proposed algorithm with sample size $n = 500$.
 205 We can see that the accuracy of the change estimates is the same for the proposed method and Gao19.
 206 However, the number of the extreme change estimates is greatly reduced by the proposed method.
 207 This is due to the fact that Gao19 identifies pseudo change points far from the actual position of
 208 the change point if there are strong abnormal data fluctuation behaviors near the boundaries of the
 209 data profiles. The new algorithm, however, restricts the data to the interval where the change points
 210 have a high probability of existence, which reduces the influence of the extreme pseudo change
 211 points and thus reduces the extreme change estimates. When the sample size increases from 130 to
 212 500, the estimation accuracy is significantly improved and the extreme change estimates are further
 213 reduced, which indicates that the proposed method has a better effect on improving the accuracy of
 214 the change estimates.

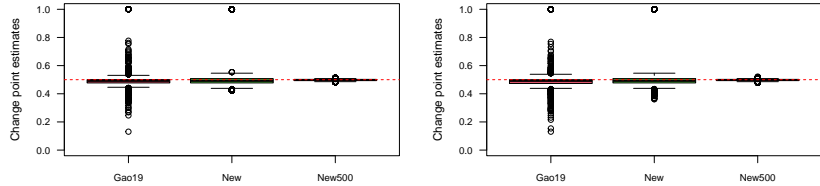


Figure 2: Boxplots of the change point estimates. The left panel is the simulation result with the true mean function $f_{01}(t)$; the right side panel is the result with f_{02} . Both methods are tested with sample size $n = 130$. New500 represents the change point estimates of the proposed algorithm with sample size $n = 500$. The red dashed line is the true change point $\tau_0/n = 0.5$.

215 To compare the computational efficiency of our proposed algorithm with Gao19, we conduct sim-
 216 ulations with the mean function f_{01} and the sample size $n = 130$. We generate $m = 5,000$ and
 217 $m = 50,000$ replicates. The experiments are repeated for five times, and the average results are
 218 shown in the Table 1. We can see that the average time consumed by the method of Gao19 is
 219 280.92s for $m = 5,000$ data profiles, and is only 156.96s for our proposed algorithm. This is a

220 significant improvement in computational speed. The difference of the time consumption for these
 221 two methods are linearly increased as the amount of data increases. Combining the results of Fig-
 222 ure 2 and Table 1, we can draw a conclusion that our proposed algorithm achieves a significant
 223 improvement in computational efficiency on the basis of guaranteed estimation accuracy.

Table 1: Computational efficiency Comparison.

Method	Gao19	New
m=5,000	280.92s	156.96s
m=50,000	2,634.93s	1,601.53s

224 Figure 3 evaluates the performance of the mean estimates of the proposed method. We compute
 225 the mean squared errors and plot the boxplots. The left side panels show the 25th, 50th, and 75th
 226 percentiles of the MSEs for sample sizes $n = 130$ and 500. We can see that within the control
 227 window CW_α , the mean function estimates match the true mean function well. In addition, the
 228 MSE of the mean estimation improves as the sample size increases.

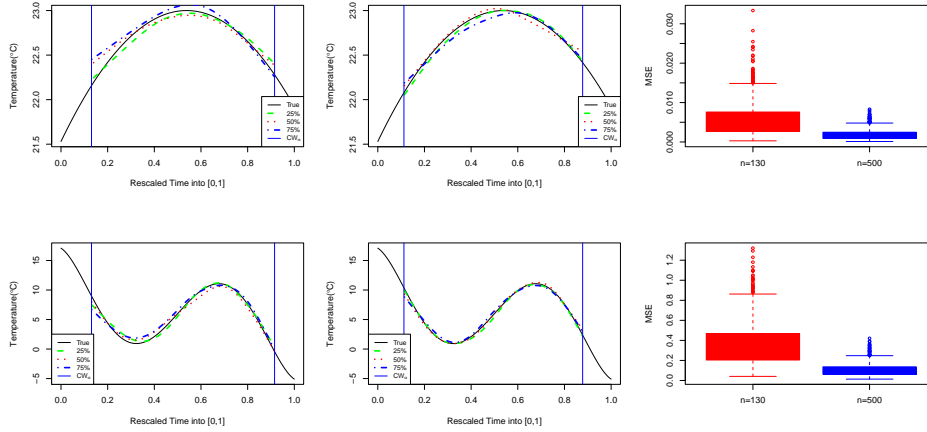


Figure 3: Performance of the mean estimation. The top panels show the simulation results when the mean function is f_{01} . The bottom panels show the simulation results when the mean function is f_{02} . The sample size of the left side panels is $n = 130$ whose MSE are the 25th (dashed green), 50th (dotted red), and 75th (dot-dashed blue) percentiles of the 1,000 MSEs obtained in each setting. The middle panels are the same as the left side panels but with $n = 500$. The vertical blue lines are the upper and lower boundaries of the control window CW_α . The right side panels are the boxplots of the 1,000 MSEs in each setting.

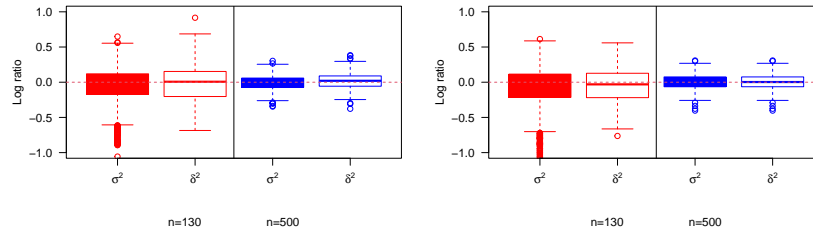


Figure 4: Boxplots of the log ratios of the variance estimates versus the true variances. The left panel shows the simulation results when the mean function is f_{01} . The right panel shows the simulation results when the mean function is f_{02} . Red: $n = 130$; Blue: $n = 500$.

229 Figure 4 uses the log ratio of the variance estimates versus the true variances to evaluate the esti-
 230 mation performance for the two variances. We can see that both variances are estimated accurately.
 231 The estimation performances are improved as the sample size increases from 130 to 500.

232 4 APPLICATION

233 The data were collected through a well designed noninvasive biomedical experiment conducted by
 234 a research team from Virginia Tech. In the mechanical perfusion process, they measured the sur-
 235 face temperature of each profile over 24 hours using a noninvasive, high precision thermal imaging
 236 system. They divided a porcine liver’s surface into a dense grid composed by 36,795 spots. Tem-
 237 perature measurements were collected every 10 minutes producing a 24 hours surface temperature
 238 profile with 145 points in each profile. We discarded the data in the first 2.5 hours, since the perfu-
 239 sion fluid needs one to two hours to completely infuse and stabilize the liver. Finally, there were 130
 240 points left in each profile. Previously, (Gao et al., 2019) conducted a spot-wise analysis method on
 241 each of these 36,795 temperature profiles and obtained a heat map of the estimates of the variance
 242 change points on the liver surface. We repeat their experiments, and compare their results (Gao19)
 243 with our proposed method (New).

244 Figure 5 is the heat maps of the variance change point detection results of Gao19 and our proposed
 245 method. Different color indicates that different areas of the organ have different viability deterio-
 246 ration time. An earlier change in variance means an earlier drop in the viability of the cells around
 247 the spot. Two maps share the similar color patterns of regional hierarchical structure, which is the
 248 viability of the top half and the middle bottom parts of the liver deteriorated around 12 hours while
 249 the left and right bottom corners of the liver last beyond 14 hours. There are also several clearly vis-
 250 ible straight green line type boundaries between the early and late failure areas. These may be parts
 251 where the porcine liver lobe was deformed during dissection and perfusion. The detection results of
 252 Gao19 have been validated by the biomedical scientists. Similar regional color patterns of these two
 253 heat maps suggest that the results of our proposed algorithm are accurate in a practical sense. How-
 254 ever, there are still macroscopic differences. In the bottom left and right areas of the heat map, there
 255 are less green dots of our New method. That means our proposed algorithm discovers more earlier
 256 deteriorated change points distributed around 12 hours than Gao19. Our results are more consistent
 257 with the biological and biomedical conclusions. We also compare the computational efficiency of
 258 these two methods. The computational time of Gao19 is 3,589.66s, while the new algorithm only
 259 takes 2,099.45s. The proposed method can greatly reduce the detection time. This makes the online
 260 organ viability assessment in realtime possible.

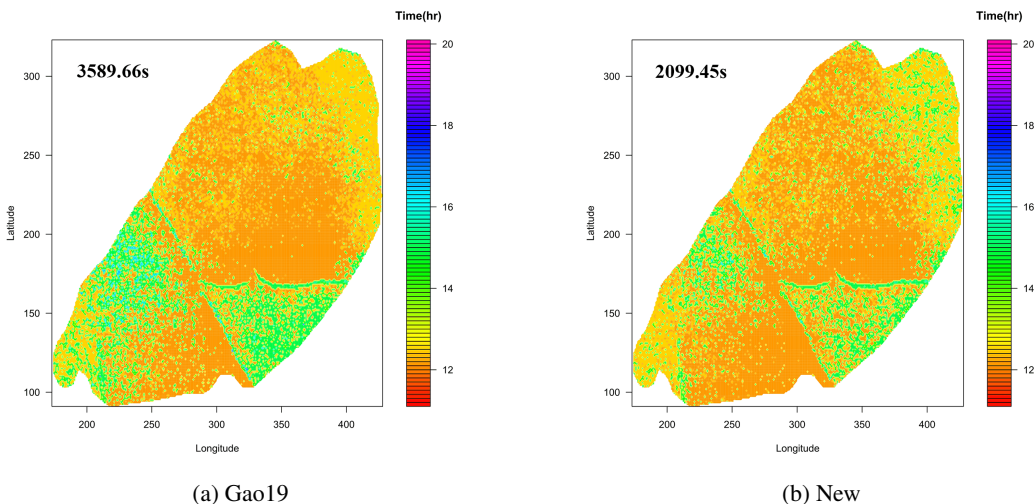


Figure 5: Heat map of the estimated variance change points on the surface of porcine liver.

261 Figure 6 is the mean function and variance change point estimates of our proposed method applied
 262 respectively on the raw and de-trended temperature profiles at three randomly selected spots on the

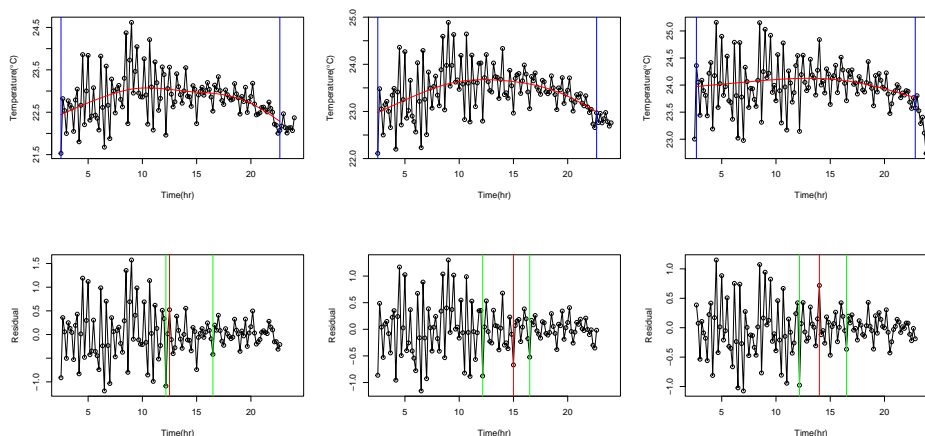


Figure 6: Mean and variance change point estimates imposed respectively on the raw temperature profiles (top panels) and de-trended temperature profiles (bottom panels) at three randomly selected spots on the liver surface. The smooth red curves are the estimated mean function. The blue vertical lines are the upper and lower bounds of the control window CW_{α} . The green vertical lines are the upper and lower bounds of the control window CW_{β} . The red vertical lines are the estimated variance change points.

263 liver surface. All mean estimates fit well with the potential trends hidden in the data. All detected
 264 variance change points reasonably locate at the proper locations in the data profiles. In the first 12
 265 hours or so, the average temperature at these three spots rises at different speeds and has a faster
 266 downward trend after 12 hours. The variance change points of these three spots are all around 12
 267 hours, which is consistent with the biomedical conclusion.

268 5 CONCLUSION

269 The viability detection of the transplanted organs is an important biomedical issue. In organ trans-
 270 plantation, timelines are the most important thing. The noninvasive viability change detection algo-
 271 rithm proposed by Gao et al. (2019) can well solve the existing problems and provide a reasonable
 272 viability assessment of the organ. However, their method spends a lot of time to explore the ar-
 273 eas where change points unlikely exist, thus losses the computational efficiency. It is necessary to
 274 improve the computational efficiency of the algorithm. Motivated by this, we propose an evolution-
 275 ary algorithm with a well designed double-layer control windows to filter out these noninformative
 276 data. The simulation shows that the proposed algorithm reduces the computational time significantly
 277 without losing detection accuracy. In the application, the heat map of the detected viability change
 278 points on the organ surface obtained by the proposed algorithm discovers earlier deteriorated areas
 279 on the liver surface, which is more consistent with the biomedical conclusions. The proposed change
 280 detection method has a very high application value in the field of online change detection.

281 AUTHOR CONTRIBUTIONS

282 ACKNOWLEDGMENTS

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349 APPENDIX

350 A SENSITIVITY ANALYSIS OF THE METHOD WITH RESPECT TO THE SAMPLE SIZE

351 The performance of our proposed change detection method is affected by the sample size of the data
 352 profile. Here we perform the test on the data with mean function $f_{01}(t)$. The sample size n is set
 353 to be $\{20, 25, 30, 35, \dots, 130\}$. The true variance change point $\tau = \frac{n}{2}$. The variances before and
 354 after the change point are $\sigma_0^2 = 0.24$ and $\delta_0^2 = 0.06$. We simulate 10,000 data profiles for each
 355 sample size. The change point estimation accuracy and the computational efficiency of the proposed
 356 algorithm are shown in Figure 7. We can see that the accuracy of the proposed algorithm increases
 357 rapidly as the sample size increases. The accuracy has a steeper curve before $n = 100$ and slows
 358 down afterwards. The computational cost is linearly related to the sample size. According to the
 359 rule of elbow, we choose $n = 100$ in the mean function estimation stage, which makes the minimum
 360 window size $W_\alpha = 50$. By choosing $n = 100$ the accuracy of the proposed algorithm exceeds 90%,
 361 and the time consuming is about 400 seconds per 10,000 data profiles.

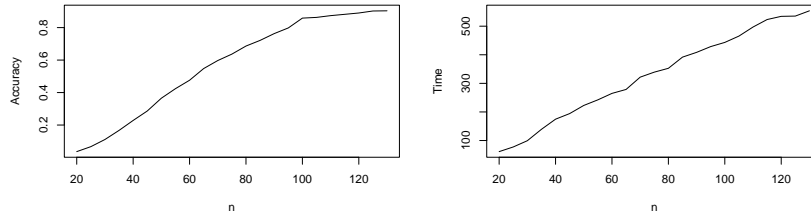


Figure 7: The accuracy and computational speed of the proposed method against the sample size.

362 B POWER ANALYSIS

363 We also present a power analysis study on the change point testing procedure. We considered the
 364 data simulated from the mean function $f_{01}(t)$. The variance $\delta_0^2 = 0.06$ and $\sigma_0^2 = \theta\delta_0^2$, where $\theta \geq 1$
 365 was the ratio of σ_0^2 over δ_0^2 .

366 When $\theta = 1$, $\delta_0^2 = \sigma_0^2$ indicates there is no variance change point in the data profile. Therefore we
 367 can investigate the size of the test under this setting. Two levels $\alpha = \{0.05, 0.1\}$ and four sample
 368 sizes $n = \{130, 500, 2000, 10000\}$ are considered. For each combination of α and n , we simulated
 369 10,000 replicated data profiles. Table 2 summarizes the results about the size of the test. We see
 370 that the empirical sizes of the test are smaller than the levels of the test indicating that the test is a
 371 bit more conservative than expected in claiming a change point when there is no change point. The
 372 reason is that the asymptotic null distribution is a heavy-tailed extreme value distribution and may
 373 require a larger sample size to achieve the desired size of the hypothesis test.

Table 2: Proportions of rejections when H_0 is true under different levels of α . The true mean function is $f_{01}(t)$.

Test Level α	Sample Size n			
	130	500	2000	10000
0.05	0.0000	0.0002	0.0010	0.0107
0.1	0.0325	0.0336	0.0356	0.0401

374 When $\theta > 1$, we investigate the power of the proposed change detection method in the simulation.
 375 The power plots are shown in Figure 8. Consider the data generated with the mean function $f_{01}(t)$.
 376 The variances $\delta^2 = 0.06$ and $\sigma^2 = \theta\delta^2$, where $\theta \geq 1$ is the ratio of σ^2 over δ^2 . Two sample sizes
 377 $n = 130$ and 500 are considered. When $n = 130$, θ takes the value of $\{1, 1.25, 1.5, \dots, 5\}$. When
 378 $n = 500$, the grid points of θ are $\{1, 1.2, 1.4, \dots, 5\}$. For each combination of θ and n , we simulate
 379 10,000 data replicates. For $n = 130$, the power is greater than 0.8 when the variance ratio is 3. For
 380 $n = 500$, the power is higher than 0.9 before the variance ratio reaches 2.

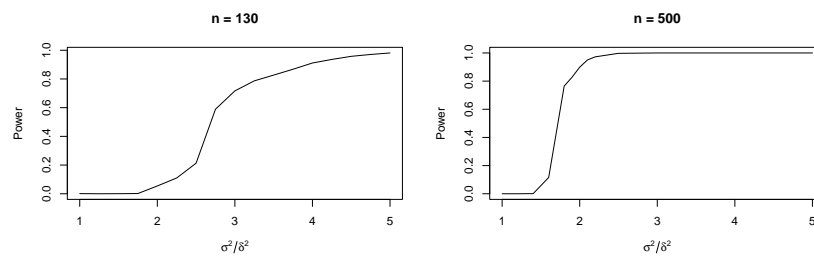


Figure 8: Plots of detection power against the ratio of the variances.