Exploring Quantization for Efficient Pre-Training of Transformer Language Models

Anonymous ACL submission

Abstract

 The increasing scale of Transformer models has led to an increase in their pre-training compu- tational requirements. While quantization has proven to be effective after pre-training and during fine-tuning, applying quantization in Transformers during pre-training has remained largely unexplored at scale for language model- ing. This study aims to explore the impact of quantization for efficient pre-training of Trans- formers, with a focus on linear layer compo- nents. By systematically applying straightfor- ward linear quantization to weights, activations, gradients, and optimizer states, we assess its effects on model efficiency, stability, and perfor-015 mance during training. By offering a compre- hensive recipe of effective quantization strate- gies to be applied during the pre-training of Transformers, we promote high training effi- ciency from scratch while retaining language modeling ability.

⁰²¹ 1 Introduction

 Transformers [\(Vaswani et al.,](#page-9-0) [2017\)](#page-9-0) have become the dominant model for natural language process- ing, with the GPT family of models [\(Radford et al.,](#page-9-1) [2019\)](#page-9-1) showcasing their effectiveness across vari- ous tasks, from language understanding to code generation. As the performance of Transformers scales nicely with the number of parameters and the data size, the current state-of-the-art models have reached unprecedented computational require- ments both during training and inference [\(Tay et al.,](#page-9-2) [2020\)](#page-9-2). For instance, pre-training a 175B param- eter GPT-3 model requires a staggering number [o](#page-9-3)f 10,000 V100 GPUs for 14.8 days [\(Patterson](#page-9-3) [et al.,](#page-9-3) [2021\)](#page-9-3). As a result, pre-training has become extremely expensive, beyond the reach of most research groups, and has raised concerns over sus- tainability due to CO2 emissions from extensive GPU usage [\(Luccioni et al.,](#page-8-0) [2023\)](#page-8-0).

040 To improve the efficiency of Transformers, quan-**041** tization has gained significant traction due to its

[r](#page-8-1)ecent successes in both post-training [\(Ashkboos](#page-8-1) **042** [et al.,](#page-8-1) [2024;](#page-8-1) [Dettmers et al.,](#page-8-2) [2022;](#page-8-2) [Frantar et al.,](#page-8-3) **043** [2022\)](#page-8-3) and during fine-tuning [\(Li et al.,](#page-8-4) [2023\)](#page-8-4). **044** Quantized pre-training, where certain parts of the **045** computational graph and model parameters are **046** quantized from the beginning of training, remains **047** a challenging problem. In such scenarios, the train- **048** ing instabilities caused by substantial changes in **049** model parameters and emerging model behaviors **050** do not pair well with the added noise introduced **051** by quantization [\(Nagel et al.,](#page-9-4) [2022\)](#page-9-4). Additionally, **052** quantizing model components without compromis- **053** ing performance becomes increasingly difficult at **054** larger scales [\(Dettmers and Zettlemoyer,](#page-8-5) [2023\)](#page-8-5). **055** Despite its importance, quantized pre-training of **056** Transformer language models remains largely un- **057** explored at scale. **058**

In this paper, we present the first in-depth study **059** on the effects of quantizing Transformer language **060** models during pre-training and at scale. Our pri- **061** mary aim is to provide a recipe for quantized pre- **062** training by conducting a controlled study that inves- **063** tigates the impact of quantization on weights, acti- **064** vations, gradients, and optimizer states on model ef- **065** ficiency, stability, and performance, using a simple **066** linear quantization with 4 and 8 bits. Our findings **067** demonstrate that 8-bit quantization for weights and **068** activations can be effectively combined to provide **069** significant memory savings and potential speedup, 070 achieving performance comparable to the baseline **071** model. However, extending quantization to gradi- **072** ents to utilize computational speedup in backward **073** matrix multiplications or reducing precision to 4 074 bits results in notable training instability. **075**

Specifically, 4-bit quantization introduces a 076 sharper loss landscape for weights ([§4.1\)](#page-3-0) and per- **077** sistent outliers in the channel dimension of activa- **078** tions ([§4.2\)](#page-4-0), significantly degrading performance **079** despite attempts to manage them through per- **080** channel quantization. Additionally, gradient quan- **081** tization is particularly problematic due to spikes in **082**

 gradient norms during early training phases and the unstructured and sparse nature of gradients through- out training ([§4.3\)](#page-5-0). While 8-bit gradient quantiza-086 tion does not hurt model convergence, transitioning to 4 bits results in non-convergence. Finally, quan- tizing the first-order moments of Adam to even 4 bits is feasible without significant performance loss, but the second-order moments require a more complex quantization scheme to avoid instabilities in the Adam update, even when using 8-bits qaun-tization ([§4.4\)](#page-6-0).

⁰⁹⁴ 2 Related Work

 In recent years, numerous methods have been stud- ied to improve the efficiency of neural networks. Among these, Quantization-aware training (QAT) emerges as an acceleration technique for inference, as parameters are stored and operations are con- ducted with higher precision during training. The induced quantization error during training serves as a regularizer, as demonstrated in [Gholami et al.](#page-8-6) [\(2022\)](#page-8-6), ultimately facilitating the development of a more quantization-friendly model.

 In contrast, Fully Quantized Training (FQT) har- nesses the accelerated gains derived from higher throughput in INT8 or INT4 operations supported by modern GPUs during training. Additionally, FQT capitalizes on memory savings by storing pa- rameters in lower precisions. As exemplified by [Li et al.](#page-8-7) [\(2024\)](#page-8-7) and [Dettmers et al.](#page-8-8) [\(2021\)](#page-8-8), states of the Adam optimizer are stored in 4 and 8 bits, respectively, to minimize memory footprint. An- other strategy introduced by [Markov et al.](#page-8-9) [\(2023\)](#page-8-9) involves quantizing both weights and gradients to reduce bandwidth usage in distributed training. Fur-117 thermore, [\(Wortsman et al.,](#page-9-5) [2024\)](#page-9-5) and [\(Kim et al.,](#page-8-10) [2021\)](#page-8-10) advocate the replacement of linear opera- tions with INT8 matrix multiplications to achieve substantial speedups.

 Despite the considerable advantages in acceler- ating the training process, FQT poses challenges attributable to numerical stability and optimiza- tion issues inherent in training quantized networks. Many existing methods predominantly focus on fine-tuning Large Language Models (LLMs) using FQT, leveraging the inherent stability of pre-trained models in each gradient update. The evolution from 16-bit to FP8 data formats, as evidenced by remarkable results in mixed precision training on LLMs [\(Peng et al.,](#page-9-6) [2023\)](#page-9-6), showcases the potential of FQT. However, the scarcity and difficulty in obtaining hardware that supports FP8 formats pose **133** significant challenges to its widespread adoption.

[Wortsman et al.](#page-9-5) [\(2024\)](#page-9-5) employ 8-bit quantiza- **135** tion for linear operations in both forward and back- **136** ward passes, achieving remarkable results in pre- **137** training large-scale vision language models. Their **138** approach incorporates row-wise quantization for **139** activations and gradients, mitigating the impact of **140** quantization errors on other parameters. However, **141** vision language models significantly differ from **142** large textual language models. [Xi et al.](#page-9-7) [\(2024b\)](#page-9-7) **143** proposed 4-bit quantization in FQT with Hadamard **144** transformation to address outliers in activations. **145** Acknowledging the sparsity of gradients during **146** training, they propose bit splitting for quantizing **147** gradients in 4-bit precision. However, they predom- **148** inantly focus on fine-tuning, and their experiments **149** on pre-training only consider small models (60M) **150** on a limited dataset (WMT 14 En-De). **151**

The generalization of these findings to large- **152** scale language models (LLMs) remains a challenge, **153** especially considering that training such models **154** involves unique complexities. Additionally, their **155** reliance on Hadamard transformations imposes re- **156** strictions on activation dimensions, limiting appli- **157** cability to power-of-two dimensions, a constraint **158** not easily met by recent LLM architectures such as **159** LLaMa. **160**

In contrast to the aforementioned complex quan- **161** tization methods, such as quantile quantization and 162 learnable quantization parameters, this study fo- **163** cuses on a more straightforward implementation. **164** The objective is to investigate the effects of quanti- **165** zation and explore the feasibility of training LLMs **166** with full integer operations. The primary goal of 167 this paper is to offer detailed insights into quantiz- **168** ing different components of the model. While more **169** sophisticated quantization methods have the poten- **170** tial to enhance the final performance, our work **171** serves as a foundational investigation, providing **172** valuable insights and paving the way for further **173** exploration in the realm of quantization for LLMs. **174**

3 Quantization Methodology **¹⁷⁵**

In this work, we explore various quantization **176** schemes $(\S3.1)$ and granularities $(\S3.2)$ on model 177 components. This controlled approach during pre- **178** training allows us to examine the impacts on lan- **179** guage modeling and downstream task performance. **180**

181 3.1 Quantization Scheme

 We start by introducing the quantization procedure used in our study, which is applied to all linear layers of Transformers. We perform fake quantiza- tion, where all values and computations are stored with higher precision, and every quantization oper- ation is followed by de-quantization to introduce quantization error. Simulating low-precision pre- training fits the purpose of this study since we aim to analyze the effects of quantizing different model components without focusing on actual training speedups that can be obtained by implementing custom GPU kernels.

Figure 1: Overview of the quantization process in forward and backward passes.

 Figure [1](#page-2-2) illustrates how quantization error is in- troduced during both the forward and backward passes. Specifically, the quantization error is in- jected into either the weights or input activations during the forward pass. In the backward pass, quantization is applied to the output gradient for computing weight updates due to only the gra- dient of the weight is stored. Nonetheless, the real-valued output gradient is used to compute the quantized input gradient since we observed an in- crease in training instability when propagating the quantization error through the entire backward path. Additional details about gradient quantization are presented in Section [4.3.](#page-5-0)

 We employ linear quantization for our experi- ments since this is a popular approach compatible with existing hardware, and using more complex methods could potentially hinder the practical rel- evance of our study. Specifically, we map real-213 valued vectors X to a discrete grid of integers as

follows: **214**

$$
X_{\text{int}} = \text{clip}\left(\left\lfloor \frac{X}{s} \right\rfloor - z; N, P\right),\qquad(1)
$$

$$
\widehat{\mathbf{X}} = s(X_{\text{int}} + z),
$$

where $|\cdot|$ is the round-to-nearest integer operator, 216 N and P represent the quantization range, with **217** $N = -2^{b-1}$, $P = 2^{b-1} - 1$, and b is the bitwidth, 218 since we deal with signed data in our experiments. 219 The scaling factor s is set to the maximum abso- **220** lute value of X/P . Unless specified, we perform 221 symmetric quantization by setting the offset z to 0, 222 which has less overhead than asymmetric quanti- 223 zation where z is set to $|\min(X)/s|$ [\(Nagel et al.,](#page-8-11) 224 [2021\)](#page-8-11). During backpropagation, we employ the **225** [w](#page-8-12)ell-known straight-through estimator (STE) [\(Ben-](#page-8-12) **226** [gio et al.,](#page-8-12) [2013\)](#page-8-12) mechanism to update the weights. **227**

3.2 Quantization Granularity **228**

We can choose scaling factors with different granu- **229** larity: per-tensor, per-channel, and per-token quan- **230** tization, where each quantization granularity leads **231** to a specific trade-off between efficiency and perfor- **232** mance. Specifically, per-tensor quantization offers **233** the highest efficiency since it performs a single **234** element-wise floating-point multiplication for the **235** de-quantization step. However, since only a single **236** value is used to rescale the entire tensor, perfor- **237** mance degradation is likely to occur due to such **238** uniform scaling across the tensor elements. **239**

On the other hand, per-channel and per-token **240** quantization offer a finer-grained scaling, where **241** different scaling factors are tailored to specific ten- **242** sor element groups (*i.e.* channels and tokens, re- **243** spectively). Even though such approaches help 244 in terms of performance, they introduce an over- **245** head during the de-quantization step. It is worth **246** noting that, in certain instances, these quantiza- **247** tion granularities cannot be efficiently implemented **248** by hardware-accelerated GEMM kernels. For ex- **249** ample, using per-channel quantization for both **250** weights and activations can not be efficiently implemented. **252**

3.3 Quantization Efficiency **253**

To show the potential memory saving in quantized **254** pre-training, we explore the memory consumption **255** of various components within GPT-2 models dur- **256** ing training using the PyTorch Memory Profiler. **257** We analyze peak memory usage, as shown in Fig- **258** ure [2,](#page-3-1) which illustrates memory usage for different **259**

(1) **²¹⁵**

Figure 2: Distribution of peak memory usage across different model sizes (GPT-2 Small, Medium, and Large) for a constant context length of 1024, with varying batch sizes. Memory usage for model components other than activations is hatched.

 batch sizes with a fixed context length of 1024 across various model sizes. We observe that when a model can fit within the GPU memory, the ma- jority of the memory at peak times is consumed by activations, particularly with large batch sizes and sequence lengths. Under these conditions, gradi- ents do not contribute to peak memory usage. More details are in Appendix [B.](#page-10-0)

Figure 3: Proportion of total execution time consumed by linear layers in the attention block of GPT-2 models (Small, Medium, Large, and X-Large) across different sequence lengths.

 We also profile the execution time of kernels using the Nvidia Nsight Profiler to assess the poten- tial speedup from quantizing linear layers. Figure [3](#page-3-2) shows the proportion of total execution time con- sumed by linear layers in the attention block of GPT-2 models of varying sizes across different se- quence lengths. This profiling includes both the forward and backward passes. We observe that for small sequence lengths, linear layers consume a significant portion (more than 80%) of the execution time. As the model size increases, this **278** proportion typically rises, but as sequence lengths **279** increase, the proportion of time spent in linear lay- **280** ers decreases, suggesting that self-attention, due to **281** its quadratic computational complexity, becomes **282** the dominant factor in execution time. This indi- **283** cates that while quantizing linear layers can offer **284** substantial speedup, the potential gains are more **285** pronounced with smaller sequence lengths. **286**

4 Experimental Results **²⁸⁷**

We used GPT-2 small [\(Radford et al.,](#page-9-1) [2019\)](#page-9-1) (124M) **288** with FlashAttention2 [\(Dao et al.,](#page-8-13) [2022\)](#page-8-13) for our 289 experiments due to its popularity and remarkable **290** performance-to-compute ratio. For the follow- **291** ing experiments, we pre-trained 30 models from **292** scratch on OpenWebText [\(Gokaslan and Cohen,](#page-8-14) **293** [2019\)](#page-8-14) for 300k gradient steps with a global batch **294** size of 512 samples and a context length of 1024 **295** tokens. For our evaluation setup, we evaluate **296** the performance of the models on a range of lan- **297** guage tasks, including ARC-Easy [\(Yadav et al.,](#page-9-8) **298** [2019\)](#page-9-8), ARC-Challenge [\(Yadav et al.,](#page-9-8) [2019\)](#page-9-8), Hel- **299** [l](#page-9-10)aswag [\(Zellers et al.,](#page-9-9) [2019\)](#page-9-9), LAMBADA [\(Paperno](#page-9-10) **300** [et al.,](#page-9-10) [2016\)](#page-9-10), and GLUE score [\(Wang et al.,](#page-9-11) [2018\)](#page-9-11). **301** Additional details about our training and evaluation **302** setups are provided in Appendix [A.](#page-9-12)^{[1](#page-3-3)}

303

4.1 Weight Quantization 304

The validation loss curves of applying per-tensor **305** and per-channel quantization to weights with 4 and **306** 8 bits are presented in Figure [4](#page-4-1) (down). We observe **307** that per-channel weight quantization with 8 bits **308** outperforms the floating-point baseline since the **309** beginning of training in terms of validation loss, **310** while per-tensor weight quantization with 8 bits 311 shows competitive performance. When quantizing **312** to 4 bits, there is a substantial difference between **313** the different granularities, with per-channel weight **314** quantization significantly outperforming per-tensor **315** quantization, as previously discussed in § [3.2.](#page-2-1) **316**

We also evaluate the downstream task perfor- **317** mance of the quantized pre-trained models in Fig- **318** ure [4](#page-4-1) (top). We observe that 8-bit weight quanti- **319** zation outperforms 4-bit and achieves competitive **320** performance compared to the floating point base- **321** line, independently of the granularity used. Once **322** again, per-channel weight quantization with 8 bits **323** achieves the best performance among the tested **324** quantization schemes. Overall, we observe similar **325**

¹We will release the code upon the acceptance of the paper.

Figure 4: Comparison of different Weight Quantization schemes. (Down) Validation loss across training iterations for 4-bit and 8-bit quantization, both per-tensor and per-channel, alongside the baseline. (Top) Performance on downstream tasks for the corresponding quantization approaches, demonstrating the efficacy of 8-bit per-channel weight quantization.

 findings when comparing the performance of the different methods during the pre-training and down- stream phases. Despite the success in quantizing weights to 8 bits from scratch, we note that only per- forming 8-bit quantization post-training also works well, as shown in Appendix [C](#page-11-0) (Table [10\)](#page-13-0). However, when it comes to 4-bit quantization, applying quan- tization from scratch leads to significantly better performance.

 We note a pronounced drop in validation loss at the end of training with the 4-bit weight quan- tization schemes, as seen in the final training it- erations in Figure [4](#page-4-1) (down). We hypothesize that this is related to reducing the learning rate below 1e − 6 in the final steps of training in our setup. However, this is not observed in all the schemes. [Nagel et al.](#page-9-4) [\(2022\)](#page-9-4) suggested that the oscillations in weights originated from performing quantiza- tion with STE during training may result in weight movements around decision thresholds. Hence, in our use case, we hypothesize that the drop in valida- tion loss stems from the presence of sharp minima when quantizing weights to lower bit-widths and that the lower learning rate regime at the end of training helps convergence to minima with lower **351** loss.

352 To further investigate this, we compare the sharp-**353** ness of the different models at the end of pre-

Figure 5: Sharpness comparison between baseline model and 4-bit weight quantization. (Top) m sharpness. (Down) Loss surfaces.

training using m-sharpness [\(Foret et al.,](#page-8-15) [2021\)](#page-8-15) with **354** varying radii in Figure [5](#page-4-2) (down). We observe that **355** all quantized models converge to sharper minima **356** compared to the floating-point, unquantized base- **357** line. Moreover, there is a direct relation between **358** the sharpness of each quantized model and the rel- **359** ative drop in validation loss observed in Figure [4](#page-4-1) **360** (down). Specifically, per-tensor weight quantiza- **361** tion with 4 bits shows the highest sharpness and **362** also the highest drop in validation loss. This cor- **363** relation is also observed on a smaller scale for the **364** per-tensor weight quantization model to 4 bits and **365** the per-tensor weight quantization model to 8 bits. **366** To visualize the loss surfaces, we employ the vi- **367** sualization method introduced by [Li et al.](#page-8-16) [\(2018\)](#page-8-16). **368** The loss surfaces of the baseline and the per-tensor **369** weight quantization model to 4-bits are shown in 370 Figure [5](#page-4-2) (right), further illustrating the impact that **371** quantization during pre-training has on the sharp- **372** ness of the final pre-trained model. **373**

4.2 Activation Quantization **374**

We present the validation loss when quantizing acti- **375** vations during pre-training in Figure [7](#page-5-1) (down). We **376** note that quantizing activations to 4 bits is more **377** challenging than training with 4-bit weights, as no- **378** ticed by previous work [\(Xiao et al.,](#page-9-13) [2023\)](#page-9-13) and as **379** seen by the divergence behavior of per-token and **380** per-tensor activation quantization. On the other **381** hand, quantizing activations to 8 bits works well, **382** especially if performed per-token, which achieves **383**

Figure 6: Training progression of activation distributions across selected iterations, showing persistent channelspecific outliers

 lower validation loss than the floating-point base- line. The performance of downstream tasks of the baseline and quantized models is presented in Fig- ure [7](#page-5-1) (top). We notice a similar performance trend across the models, with 8-bit per-token activation reaching competitive performance with the base-line model.

Figure 7: Pre-training Activation Quantization effects: (Down) Validation loss curves for various quantization schemes; (Top) Downstream task Performance across Datasets, showing 8-bit quantization closely aligns with baseline performance.

 To investigate 4-bit activation quantization fur- ther, we also tried applying an asymmetric scheme. The intuition is that, while most activations exhibit symmetry around zero, this is not the case for acti- [v](#page-8-17)ation after GELU activation functions [\(Hendrycks](#page-8-17) [and Gimpel,](#page-8-17) [2016\)](#page-8-17). Hence, having an asymmet- ric scheme can lead to a better utilization of the available bits for representation. However, we ob- serve that while the asymmetric scheme provides an improvement over 4-bit per-token symmetric quantization, the model still diverges. We analyze the activation distributions of the output projection layer within the attention block of layer 7 in Figure [6.](#page-5-2) We see that outliers predominantly reside **404** within specific channels and persistently affect the 405 same channels throughout training. Given our use 406 of per-tensor and per-token quantization for activa- **407** tions, it is evident that such outliers can influence **408** all tokens, given their consistent pattern across the **409** channel dimension. 410

Figure 8: Validation loss and activation outliers for 4-bit per-channel quantization. (Left) Validation loss shows convergence but underperforms compared to the baseline. (Right) Histogram of activation with massive outliers.

Since activation outliers are mostly predominant **411** in particular channels during training, we explore **412** the efficacy of per-channel 4-bit activation quantiza- **413** tion in Figure [8](#page-5-3) (left). We observe that this variant **414** does converge, even though it fails to be competi- **415** tive with the floating-point baseline. Such degra- **416** dation in validation loss can be attributed to the **417** presence of massive outlier activations in specific **418** layers. Despite being important for the model's per- **419** formance [\(Sun et al.,](#page-9-14) [2024\)](#page-9-14), these big activations **420** pose a challenge for both per-token and per-channel **421** quantization. An example of these is presented in **422** Figure [8](#page-5-3) (right), showing the presence of large acti- **423** vations in the FC2 layer in the final attention block. **424**

4.3 Gradient Quantization **425**

We perform gradient quantization and present the **426** validation losses obtained during pre-training in **427** Figure [9](#page-6-1) (down). We observe that, with 4-bit gra- 428 dient quantization, training becomes highly un- **429** stable or completely fails to converge. With 8 **430**

 bits, only per-token quantization converges despite showing worse performance compared to our base- line model. The observations are similar when measuring the performance of the different models on downstream tasks, as shown in Figure [9](#page-6-1) (top).

Figure 9: Gradient Quantization. (Down) Validation loss showing non-convergence for 4-bit and 8-bit pertensor quantization. (Top) Performance on downstream tasks, with only 8-bit per-token approaching baseline performance.

 As previously discussed in [§3.1,](#page-2-0) we quantize the output gradients only for the weight updates, avoid- ing the instability in training that can result from propagating quantization errors when quantizing activation gradients. This is illustrated in Figure [10](#page-6-2) (top), where quantizing activation gradients in the initial training stages leads to an explosion in the validation loss, followed by divergence. Moreover, we observe an increase in the L2 norm between the floating-point gradients and the quantized coun- terparts when quantizing activation gradients com-pared to weight gradients.

 To further analyze the subpar performance of 8-bit per-token gradient quantization, even when only applied to weight gradients, we analyze the gradients for the QKV projection at the first layer of the model early on in training in Figure [10](#page-6-2) (down). We observe that gradients are mostly sparse during training and are prone to induce high quantization errors, rendering instabilities.

456 4.4 Optimizer States Quantization

457 We quantize optimizer states, particularly the **458** first and second moments in the Adam optimizer.

Figure 10: (Top) Validation loss spike illustrating instability from quantizing activation gradients. (Down) Gradient magnitude histogram for a linear layer, highlighting sparsity and potential for quantization error.

Figure 11: Quantization of Adam optimizer's firstorder moments. (Down) Comparison of validation loss for different quantization approaches; (Top) Performance on downstream tasks, with 8-bit per-channel closely matching baseline.

stored until the next training iteration, which are **460** then dequantized and used for Adam's update. To **461** better assess the effect of quantizing each state, we **462** quantize them separately and individually. The val- **463** idation losses when quantizing Adam's first state **464** are presented in Figure [11](#page-6-3) (down). We observe **465** that per-channel quantization to 8 bits works well, **466** achieving performance similar to that of the base- **467**

 line model. Notably, only per-tensor quantization to 4 bits failed to converge out of all tested configu- rations. Similar findings are found when evaluating the downstream performance of the different quan-tization schemes in Figure [11](#page-6-3) (right).

Figure 12: Second-order moments of Adam quantization. (Top) Validation loss quickly diverges. (Down) Histogram showing the concentration of quantized values in the zero bin, which contributes to instability in weight updates.

 The results of quantizing Adam's second state are presented in Figure [12](#page-7-0) (left). We observe that the quantized model failed to converge smoothly throughout training, even when applying per- channel quantization with 8 bits. This can be ex- plained by the usage of a linear symmetric quan- tization function around zero in our scheme. This causes all small values to be set to zero after quan- tization, hurting performance, as presented in Fig- ure [12](#page-7-0) (right). Given that the second state plays a pivotal role in the denominator of Adam's update, such clustering to zero leads to excessively large weight updates, causing training to diverge from the onset, as observed in Figure [12](#page-7-0) (left).

487 4.5 Multiple Components Quantization

 As our last studied components, we trained models using 8-bit quantization for weights, activations, and gradients, as well as isolating quantization to only weights and activations with per-channel granularity for weights and per-token granularity for activations and gradients. Our findings, as de- picted in Figure [13,](#page-7-1) demonstrate that quantizing both weights and activations to 8-bit allows per-formance to closely align with the baseline model.

Figure 13: Validation loss across training iterations for weight, activation, and gradient quantization together.

However, extending quantization to include gradi- **497** ents results in a notable decrease in performance. **498** This observation is consistent with earlier results **499** from our independent quantization of gradients, **500** highlighting the significant challenges this intro- 501 duces. 502

5 Conclusion **⁵⁰³**

This study presents an extensive analysis of the **504** impact of quantizing specific Transformer compo- **505** nents in 4 and 8 bits during pre-training, in con- **506** trast to concurrent work that focuses on individual **507** methods without comprehensive ablations [\(Xi et al.,](#page-9-15) **508** [2024a\)](#page-9-15). Our study reveals that quantizing weights **509** to 8-bits from the beginning of pre-training is gen- **510** erally successful. However, 4-bit weight quanti- **511** zation can significantly affect model convergence **512** due to a sharper loss landscape. We also found that **513** carefully managing activation outliers is crucial **514** to avoid performance drops with lower-precision **515** quantization. Additionally, we explain the sensitive **516** nature of gradient quantization and its potential to 517 fail at lower bit-widths. We observed that while **518** the first-order moments of the Adam optimizer can **519** be effectively quantized to 4-bits, the second-order **520** moments pose a greater challenge even for 8-bit 521 quantization. Overall, our work establishes an im- **522** portant foundation for future developments in quan- **523** tization approaches tailored to Transformers, open- **524** ing the door to efficiently train large-scale models **525** from scratch for improved accessibility. **526**

⁵²⁷ Limitation

528 We acknowledge the limitations of our work:

 • We employed linear quantization for our ex- periments. While this approach is widely used and allows for a controlled study, it may not capture the full potential of more sophisticated quantization methods.

 • Due to the cost of pre-training and the number of experiments, we limited our study to GPT-2 small, and our findings may not generalize to larger models.

 • The efficiency gains discussed are estimated using profiling data, and implementing these improvements in practice is challenging due to the complexity of kernel optimizations.

⁵⁴² References

- **543** Saleh Ashkboos, Amirkeivan Mohtashami, Maximil-**544** ian L Croci, Bo Li, Martin Jaggi, Dan Alistarh, **545** Torsten Hoefler, and James Hensman. 2024. Quarot: **546** Outlier-free 4-bit inference in rotated llms. *arXiv* **547** *preprint arXiv:2404.00456*.
- **548** Yoshua Bengio, Nicholas Léonard, and Aaron Courville. **549** 2013. Estimating or propagating gradients through **550** stochastic neurons for conditional computation. **551** *arXiv preprint arXiv:1308.3432*.
- **552** Ciprian Chelba, Tomas Mikolov, Mike Schuster, Qi Ge, **553** Thorsten Brants, Phillipp Koehn, and Tony Robinson. **554** 2014. [One billion word benchmark for measuring](https://arxiv.org/abs/1312.3005) **555** [progress in statistical language modeling.](https://arxiv.org/abs/1312.3005) *Preprint*, **556** arXiv:1312.3005.
- **557** Tri Dao, Dan Fu, Stefano Ermon, Atri Rudra, and **558** Christopher Ré. 2022. Flashattention: Fast and **559** memory-efficient exact attention with io-awareness. **560** *Advances in Neural Information Processing Systems*, **561** 35:16344–16359.
- **562** Tim Dettmers, Mike Lewis, Younes Belkada, and Luke **563** Zettlemoyer. 2022. [GPT3.int8\(\): 8-bit matrix mul-](https://openreview.net/forum?id=dXiGWqBoxaD)**564** [tiplication for transformers at scale.](https://openreview.net/forum?id=dXiGWqBoxaD) In *Advances in* **565** *Neural Information Processing Systems*.
- **566** Tim Dettmers, Mike Lewis, Sam Shleifer, and Luke **567** Zettlemoyer. 2021. 8-bit optimizers via block-wise **568** quantization. *arXiv preprint arXiv:2110.02861*.
- **569** Tim Dettmers and Luke Zettlemoyer. 2023. The case **570** for 4-bit precision: k-bit inference scaling laws. In **571** *Proceedings of the 40th International Conference on* **572** *Machine Learning*, ICML'23. JMLR.org.
- Pierre Foret, Ariel Kleiner, Hossein Mobahi, and **573** Behnam Neyshabur. 2021. [Sharpness-aware mini](https://openreview.net/forum?id=6Tm1mposlrM) [mization for efficiently improving generalization.](https://openreview.net/forum?id=6Tm1mposlrM) In **575** *International Conference on Learning Representa-* **576** *tions*. **577**
- Elias Frantar, Saleh Ashkboos, Torsten Hoefler, and **578** Dan Alistarh. 2022. GPTQ: Accurate post-training **579** compression for generative pretrained transformers. **580** *arXiv preprint arXiv:2210.17323*. **581**
- Amir Gholami, Sehoon Kim, Zhen Dong, Zhewei Yao, **582** Michael W Mahoney, and Kurt Keutzer. 2022. A survey of quantization methods for efficient neural **584** network inference. In *Low-Power Computer Vision*, **585** pages 291–326. Chapman and Hall/CRC. **586**
- Aaron Gokaslan and Vanya Cohen. 2019. Openwebtext corpus. [http://Skylion007.github.io/](http://Skylion007.github.io/OpenWebTextCorpus) **588** [OpenWebTextCorpus](http://Skylion007.github.io/OpenWebTextCorpus). **589**
- Dan Hendrycks and Kevin Gimpel. 2016. Gaussian error linear units (gelus). *arXiv preprint* $arXiv:1606.08415.$
- Sehoon Kim, Amir Gholami, Zhewei Yao, Michael W **593** Mahoney, and Kurt Keutzer. 2021. I-bert: Integeronly bert quantization. In *International conference* **595** *on machine learning*, pages 5506–5518. PMLR.
- Bingrui Li, Jianfei Chen, and Jun Zhu. 2024. Memory **597** efficient optimizers with 4-bit states. Advances in *Neural Information Processing Systems, 36.*
- Hao Li, Zheng Xu, Gavin Taylor, Christoph Studer, and **600** Tom Goldstein. 2018. [Visualizing the loss landscape](https://arxiv.org/abs/1712.09913) [of neural nets.](https://arxiv.org/abs/1712.09913)
- Zhikai Li, Xiaoxuan Liu, Banghua Zhu, Zhen Dong, **603** Qingyi Gu, and Kurt Keutzer. 2023. Qft: Quan- **604** tized full-parameter tuning of llms with affordable **605** resources. *arXiv preprint arXiv:2310.07147*.
- Alexandra Sasha Luccioni, Sylvain Viguier, and Anne- **607** Laure Ligozat. 2023. Estimating the carbon footprint of bloom, a 176b parameter language model. *Journal* **609** *of Machine Learning Research*, 24(253):1–15. **610**
- Mitchell P. Marcus, Beatrice Santorini, and Mary Ann **611** Marcinkiewicz. 1993. [Building a large annotated cor](https://www.aclweb.org/anthology/J93-2004) [pus of English: The Penn Treebank.](https://www.aclweb.org/anthology/J93-2004) *Computational* **613** *Linguistics*, 19(2):313–330. **614**
- Ilia Markov, Adrian Vladu, Qi Guo, and Dan Alis- **615** tarh. 2023. Quantized distributed training of large models with convergence guarantees. *arXiv preprint* **617** *arXiv:2302.02390*. **618**
- Stephen Merity, Caiming Xiong, James Bradbury, and **619** Richard Socher. 2016. [Pointer sentinel mixture mod](https://arxiv.org/abs/1609.07843) [els.](https://arxiv.org/abs/1609.07843) *Preprint*, arXiv:1609.07843. **621**
- Markus Nagel, Marios Fournarakis, Rana Ali Amjad, **622** Yelysei Bondarenko, Mart Van Baalen, and Tijmen Blankevoort. 2021. A white paper on neural network quantization. *arXiv preprint arXiv:2106.08295*. **625**
-
-
-
-
-
-
-
-
-
-
-
-
-
-
-
-
-
-
-

-
-
- **626** Markus Nagel, Marios Fournarakis, Yelysei Bon-**627** darenko, and Tijmen Blankevoort. 2022. [Overcom-](https://proceedings.mlr.press/v162/nagel22a.html)**628** [ing oscillations in quantization-aware training.](https://proceedings.mlr.press/v162/nagel22a.html) In **629** *Proceedings of the 39th International Conference* **630** *on Machine Learning*, volume 162 of *Proceedings* **631** *of Machine Learning Research*, pages 16318–16330. **632** PMLR.
- **633** Denis Paperno, Germán Kruszewski, Angeliki Lazari-**634** dou, Ngoc Quan Pham, Raffaella Bernardi, Sandro **635** Pezzelle, Marco Baroni, Gemma Boleda, and Raquel **636** Fernandez. 2016. [The LAMBADA dataset: Word](http://www.aclweb.org/anthology/P16-1144) **637** [prediction requiring a broad discourse context.](http://www.aclweb.org/anthology/P16-1144) In **638** *Proceedings of the 54th Annual Meeting of the As-***639** *sociation for Computational Linguistics (Volume 1:* **640** *Long Papers)*, pages 1525–1534, Berlin, Germany. **641** Association for Computational Linguistics.
- **642** David Patterson, Joseph Gonzalez, Quoc Le, Chen **643** Liang, Lluis-Miquel Munguia, Daniel Rothchild, **644** David So, Maud Texier, and Jeff Dean. 2021. Carbon **645** emissions and large neural network training. *arXiv* **646** *preprint arXiv:2104.10350*.
- **647** Houwen Peng, Kan Wu, Yixuan Wei, Guoshuai Zhao, **648** Yuxiang Yang, Ze Liu, Yifan Xiong, Ziyue Yang, **649** Bolin Ni, Jingcheng Hu, et al. 2023. Fp8-lm: Train-**650** ing fp8 large language models. *arXiv preprint* **651** *arXiv:2310.18313*.
- **652** Alec Radford, Jeffrey Wu, Rewon Child, David Luan, **653** Dario Amodei, Ilya Sutskever, et al. 2019. Language **654** models are unsupervised multitask learners. *OpenAI* **655** *blog*, 1(8):9.
- **656** Mingjie Sun, Xinlei Chen, J Zico Kolter, and Zhuang **657** Liu. 2024. Massive activations in large language **658** models. *arXiv preprint arXiv:2402.17762*.
- **659** Yi Tay, Mostafa Dehghani, Dara Bahri, and Donald Met-**660** zler. 2020. Efficient transformers: A survey.(2020). **661** *arXiv preprint cs.LG/2009.06732*.
- **662** Ashish Vaswani, Noam Shazeer, Niki Parmar, Jakob **663** Uszkoreit, Llion Jones, Aidan N Gomez, Łukasz **664** Kaiser, and Illia Polosukhin. 2017. Attention is all **665** you need. *Advances in neural information processing* **666** *systems*, 30.
- **667** Alex Wang, Amanpreet Singh, Julian Michael, Felix **668** Hill, Omer Levy, and Samuel R Bowman. 2018. **669** Glue: A multi-task benchmark and analysis platform **670** for natural language understanding. *arXiv preprint* **671** *arXiv:1804.07461*.
- **672** Mitchell Wortsman, Tim Dettmers, Luke Zettlemoyer, **673** Ari Morcos, Ali Farhadi, and Ludwig Schmidt. 2024. **674** Stable and low-precision training for large-scale **675** vision-language models. *Advances in Neural Infor-***676** *mation Processing Systems*, 36.
- **677** Haocheng Xi, Yuxiang Chen, Kang Zhao, Kaijun Zheng, **678** Jianfei Chen, and Jun Zhu. 2024a. Jetfire: Effi-**679** cient and accurate transformer pretraining with int8 **680** data flow and per-block quantization. *arXiv preprint* **681** *arXiv:2403.12422*.
- Haocheng Xi, Changhao Li, Jianfei Chen, and Jun Zhu. **682** 2024b. Training transformers with 4-bit integers. **683** *Advances in Neural Information Processing Systems*, **684** 36. **685**
- Guangxuan Xiao, Ji Lin, Mickael Seznec, Hao Wu, **686** Julien Demouth, and Song Han. 2023. Smoothquant: **687** Accurate and efficient post-training quantization for **688** large language models. In *International Conference* **689** *on Machine Learning*, pages 38087–38099. PMLR. **690**
- Vikas Yadav, Steven Bethard, and Mihai Surdeanu. **691** 2019. Quick and (not so) dirty: Unsupervised selec- **692** tion of justification sentences for multi-hop question **693** answering. *arXiv preprint arXiv:1911.07176*. **694**
- Rowan Zellers, Ari Holtzman, Yonatan Bisk, Ali **695** Farhadi, and Yejin Choi. 2019. Hellaswag: Can a **696** machine really finish your sentence? *arXiv preprint* **697** *arXiv:1905.07830*. **698**

A **Experimental Setup** 699

A.1 Model and Training Configuration **700**

Our experiments leverage the computational en- **701** [h](#page-8-13)ancements of the FlashAttention library [\(Dao](#page-8-13) 702 [et al.,](#page-8-13) [2022\)](#page-8-13), utilizing its GPT-2 implementation **703** within the HuggingFace Trainer framework^{[2](#page-9-16)} for 704 our training processes. **705**

Training was conducted on the OpenWebText **706** corpus [\(Gokaslan and Cohen,](#page-8-14) [2019\)](#page-8-14), adopting a set **707** of training configurations similar to [\(Dao et al.,](#page-8-13) **708** [2022\)](#page-8-13) and nanoGPT [3](#page-9-17) , without hyperparameter **709** tuning due to computational constraints. We use **710** AdamW optimizer with a learning rate of $6e - 4$, 711 combined with a cosine learning rate scheduler set **712** to a half cycle. We adopt mixed precision training **713** in bfloat16. The experiments are conducted with **714** a fixed batch size of 512, employing gradient ac- **715** cumulation as necessary to accommodate the com- **716** putational constraints of our setup across 4xA100 **717** 80G GPUs. This training configuration remains **718** consistent across all experiments, culminating in a **719** training duration averaging 4.3 days for completion **720** of 300k steps. **721**

A.2 Data and Evaluation Metrics **722**

The OpenWebText corpus was randomly split into **723** training and validation sets, with 0.5% of the data **724** reserved for validation. Following the methodology **725** of [Radford et al.](#page-9-1) [\(2019\)](#page-9-1), the performance of our pre- **726** trained models was evaluated on several benchmark **727** datasets. These evaluations focused on perplexity **728**

² [https://huggingface.co/docs/transformers/en/](https://huggingface.co/docs/transformers/en/main_classes/trainer) [main_classes/trainer](https://huggingface.co/docs/transformers/en/main_classes/trainer)

³ <https://github.com/karpathy/nanoGPT>

 measurements on well-known datasets including WikiText [\(Merity et al.,](#page-8-18) [2016\)](#page-8-18), PTB [\(Marcus et al.,](#page-8-19) [1993\)](#page-8-19), and 1BW [\(Chelba et al.,](#page-8-20) [2014\)](#page-8-20). Our models were further evaluated using a range of downstream **733** tasks:

- **734** GLUE [\(Wang et al.,](#page-9-11) [2018\)](#page-9-11): A collection of **735** natural language understanding tasks includ-**736** ing question answering, sentiment analysis, **737** and textual entailment, designed to bench-**738** mark the generalization capabilities of models **739** across a diverse range of linguistic challenges.
- **740** ARC [\(Yadav et al.,](#page-9-8) [2019\)](#page-9-8): Comprising **741** the ARC-Easy and ARC-Challenge, these **742** datasets test the model's reasoning abil-**743** ity through science-based question answer-**744** ing. ARC-Easy contains simpler questions, **745** while ARC-Challenge includes more complex **746** queries demanding deeper reasoning.
- **747** Hellaswag [\(Zellers et al.,](#page-9-9) [2019\)](#page-9-9): This dataset **748** challenges models to predict the most plau-**749** sible continuation of a narrative from a large **750** corpus of everyday contexts and movie scripts, **751** testing the commonsense reasoning ability of **752** the models.
- **753** LAMBADA [\(Gokaslan and Cohen,](#page-8-14) [2019\)](#page-8-14): **754** Evaluates the model's capability to predict the **755** final word of a textual passage, focusing on **756** the contextual understanding of the language.

 For evaluation on downstream tasks, we adopted a few-shot approach, utilizing a 5-shot prompting method with greedy decoding. Each prompt was structured with a task instruction followed by the five examples of training data and we compute ac- curacy on validation set. We implemented our few- shot evaluation protocol following the guidelines provided by the lm_evaluation_harness library [4](#page-10-1) **764** .

765 A.3 Comparison of Baseline and Pre-trained **766** Model

Table 1: Comparison of Baseline and Pre-trained Models: The latter trained for at least twice the duration.

4 [https://github.com/zphang/lm_evaluation_](https://github.com/zphang/lm_evaluation_harness) [harness](https://github.com/zphang/lm_evaluation_harness)

To establish a solid baseline for our experiments, **767** we benchmark our trained model against the pre- **768** trained GPT-2 weights provided by OpenAI across **769** several downstream tasks. The comparison, de- 770 tailed in Table [1,](#page-10-2) reveals that our model achieves **771** results closely aligned with the original, validating **772** the efficacy of our training approach. In the fol- **773** lowing sections, we will delve into the individual **774** components of the model, discussing the impact **775** and outcomes of our quantization experiments on **776** each. **777**

B Memory Analysis **⁷⁷⁸**

In this section, we explore the memory consump- **779** tion patterns of various components within GPT-2 **780** models during training, using the PyTorch Mem- **781** ory Profiler. This profiling tool allows for precise **782** monitoring of memory usage throughout the lifecy- **783** cle of a model's operation, particularly during the **784** forward and backward passes, and during optimiza- **785** tion steps. "Peak memory" in this context refers to **786** the maximum memory usage observed at any point **787** in these stages, providing insights into how differ- **788** ent model configurations impact overall memory **789** requirements. We profiled all attention blocks as **790** well as lm head of the Transformer model. **791**

Figure [14](#page-11-1) shows how memory usage changes 792 with different batch sizes for a fixed context length 793 of 1024, across various model sizes. Notably, as **794** the batch size increases, the memory allocated for **795** activations becomes more dominant, especially in **796** larger models. This trend is primarily due to the **797** need to store activations for the computation of gra- **798** dients during the backward pass, which increases **799** with larger batch sizes. 800

Figure [15](#page-11-2) examines the memory usage across 801 various sequence lengths while keeping the batch **802** size constant at 4. When both batch size and sequence length are small, peak memory typically oc- **804** curs towards the end of the backward propagation **805** phase. At this stage, memory includes the parame- **806** ters, optimizer states, gradients from all layers, and **807** activations from the initial layers. However, as the **808** sequence length and batch size increase, peak mem- **809** ory usage shifts to the beginning of the backward **810** propagation. At this point, the memory comprises **811** parameters, optimizer states, all activations, and no- **812** tably, the output gradient of the final layers, which **813** matches the size of the logits (proportional to batch **814** size * sequence length * vocabulary size). 815

In conclusion, the analysis reveals that when a **816**

Figure 14: Distribution of peak memory usage across different model sizes (GPT-2 Small, Medium, and Large) for a constant context length of 1024, with varying batch sizes. This figure demonstrates how memory dedicated to activations increases as batch size increases, highlighting the impact of batch size on memory allocation dynamics in large-scale models.

Figure 15: Peak memory usage profile for different sequence lengths while maintaining a constant batch size of 4, across different model sizes (GPT-2 Small, Medium, and Large). This figure illustrates the shift in peak memory usage from gradients to activations as sequence length increases, and the significant impact of sequence length on memory dynamics during training.

 model can fit within the GPU memory, the ma- jority of the memory at peak times is consumed by activations, especially when working with suf- ficiently large batch sizes and sequence lengths. Under these conditions, gradients do not contribute to peak memory usage. Consequently, quantizing gradients will not lead to significant memory sav-**824** ings.

⁸²⁵ C Quantization Results

 This appendix presents the granular results from our experiments on weight, activation, gradient, and optimizer states quantization. The tables detail the performance metrics, like perplexity and accu- racy, under various quantization settings. Finally, we present post-training quantization results of our baseline model in Tables [10](#page-13-0)[,11.](#page-13-1)

#bit	granularity	WikiText103	WikiText2	PTB	1BW
baseline		39.94	34.32	35.13	44.03
4 bit	per-tensor	55.50	46.70	52.38	59.14
	per-channel	56.43	47.32	38.18	46.30
8 bit	per-tensor	48.52	40.01	37.02	45.04
	per-channel	42.43	35.94	34.81	43.47

Table 2: Weight Quantization: evaluation of perplexity across multiple datasets.

Table 3: Activation Quantization: evaluation of perplexity across multiple datasets.

#bit	granularity	WikiText103	WikiText2	PTR	1BW
baseline		39.94	34.32	35.13	44.03
4 bit	per-tensor	418.63	264.07	261.64	310.43
	per-token	69.82	54.53	56.58	72.06
8 bit	per-tensor	64.77	51.06	37.96	45.26
	per-token	42.86	37.17	35.43	43.38

Table 4: Gradient Quantization: evaluation of perplexity across multiple datasets.

#bit	granularity	WikiText103	WikiText2	PTB	1BW
	baseline	39.94	34.32	35.13	44.03
4 bit	per-tensor	17990.70	15560.03	6632.20	6393.07
	per-token	128.71	92.74	106.73	110.14
8 bit	per-tensor	123.08	87.81	104.90	111.51
	per-token	59.24	47.50	42.28	51.89

Table 5: Adam Optimizer's First Moments: evaluation of perplexity across multiple datasets.

#bit	granularity	WikiText103	WikiText2	PTB	1BW
baseline		39.94	34.32	35.13	44.03
4 bit	per-tensor	78.78	62.08	66.50	85.60
	per-channel	43.02	36.70	38.57	47.90
8 bit	per-tensor	42.93	36.91	39.72	46.63
	per-channel	39.84	33.78	35.67	44.29

Table 6: Weight Quantization: accuracy on downstream tasks.

			GLUE Score						ARC			
# of bit	granularity	MNLI	MRPC	RTE	ONLI	SST	WNLI	Easy	Challenge	LAMBADA	Hellaswag	Average
	baseline	33.31	64.46	49.82	49.13	52.06	50.70	46.14	22.07	36.17	29.12	43.30
4 bit	per-tensor per-channel	31.76 33.51	50.49 59.07	45.49 50.90	49.13 49.70	50.46 52.29	36.62 56.34	40.70 45.09	19.40 22.07	27.03 34.21	27.25 28.86	37.83 43.20
8 bit	per-tensor per-channel	33.12 34.78	59.07 67.16	46.57 53.07	48.95 49.42	54.24 54.01	49.30 50.70	46.84 44.21	21.40 22.07	34.81 36.43	28.80 29.17	42.31 44.10

Table 7: Activation Quantization: accuracy on downstream tasks.

			GLUE Score						ARC			
$#$ of bit	granularity		MNLI MRPC	RTE						QNLI SST WNLI Easy Challenge LAMBADA Hellaswag		Average
	baseline	33.31	64.46	49.82	49.13	52.06	50.70	46.14	22.07	36.17	29.12	43.30
4 hit	per-token	34.19	35.29				49.10 49.46 49.54 49.30	33.68	19.40	19.06	26.11	36.51
8 bit	per-token per-tensor	33.35 35.25	42.89 31.13	52.71 45.85	49.42 49.48	50.80 50.34	25.35 54.93	45.09 33.33	18.39 20.40	33.81 18.22	28.81 26.15	38.06 36.51

Table 8: Gradient Quantization: accuracy on downstream tasks.

Table 9: Quantization of Adam Optimizer's First-Order Moments: accuracy on downstream tasks.

			GLUE Score						ARC			
# of bit	granularity	MNLI	MRPC	RTE	QNLI	SST	WNLI	Easy	Challenge	LAMBADA	Hellaswag	Average
	baseline	33.31	64.46	49.82	49.13	52.06	50.70	46.14	22.07	36.17	29.12	43.30
4 bit	per-channel per-tensor	33.98 32.36	66.42 66.42	52.35 46.93	49.46 50.32	51.03 50.92	53.52 42.25	46.67 35.44	21.07 22.07	33.15 20.12	28.47 26.49	43.61 39.33
8 bit	per-channel per-tensor	33.25 34.15	67.40 61.76	50.18 50.18	49.48 49.53	52.87 54.70	50.70 60.56	46.67 45.61	20.40 18.39	36.52 32.91	28.91 28.80	43.64 43.66

Table 10: Post-training weight quantization results

#bit	granularity	WikiText103	WikiText2	PTB	1 _{BW}
		(ppl)	(ppl)	(ppl)	(ppl)
	baseline	39.94	34.32	35.13	44.03
4 bit	per-tensor	16196.10	17256.89	17471.35	13761.79
	per-column	98.39	75.56	81.28	94.40
8 bit	per-tensor	46.45	39.23	41.18	52.15
	per-column	40.15	34.45	35.23	44.11

Table 11: Post-training activation quantization results

#bit	granularity	WikiText103	WikiText2	PTB	1 _{BW}
		(ppl)	(ppl)	(ppl)	(ppl)
baseline		39.94	34.32	35.13	44.03
4 bit	per-tensor				
	per-column	14022.78	17933.29	13392.28	8763.06
8 bit	per-tensor	70.07	58.45	64.99	149.35
	per-column	40.09	34.44	35.43	44.37