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## **Debiased Orthogonal Boundary-driven Efficient Noise Mitigation**

#### Anonymous Authors<sup>1</sup>

#### **Abstract**

Mitigating the detrimental effects of noisy labels on the training process has become increasingly critical, as obtaining entirely clean or humanannotated samples for large-scale pre-training tasks is often impractical. Nonetheless, existing noise mitigation methods often encounter limitations in practical applications due to their taskspecific design, model dependency, and significant computational overhead. In this work, we exploit the properties of high-dimensional orthogonality to identify a robust and effective boundary in cone space for separating clean and noisy samples. Building on this, we propose One-Step Anti-noise (OSA), a model-agnostic noisy label mitigation paradigm that employs an estimator model and a scoring function to assess the noise level of input pairs through just one-step inference. We empirically validate the superiority of OSA, demonstrating its enhanced training robustness, improved task transferability, streamlined deployment, and reduced computational overhead across diverse benchmarks, models, and tasks. Our code is released at https://anonymous.4open. science/r/CLIP\_OSN-E86C.

#### 1. Introduction

Noise mitigation aims to handle the detriment of noisy labels encountered during the training process. The advancement of large-scale pre-training has significantly increased data scale to the trillion level, but also inevitably introduced considerable noise due to the collection from the internet, severely impeding the training process. This poses a substantial challenge for robust model training in various tasks, such as cross-modal matching (Huang et al., 2021; Zhang et al., 2024), image classification (Sun et al., 2021; Yu et al., 2019), and image retrieval (Liu et al., 2021).

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Traditional noise mitigation approaches encounter several limitations that constrain their practical applicability: 1) **Task specificity:** Existing methods (Huang et al., 2021; Sun et al., 2021; Ibrahimi et al., 2022a) are tailored to specific tasks, limiting their applicability across different tasks. 2) Model dependency: Most noise mitigation techniques (Liu et al., 2021; Yang et al., 2023a) are tightly coupled with specific models, requiring extensive modifications for adaptation to different models. 3) Computational cost: Numerous existing methods necessitate dual-model collaborations (Huang et al., 2021; Yu et al., 2019) or multiple training passes (Huang et al., 2021), i.e., they require at least two backward passes per training step, effectively doubling the computational expense and substantially increasing the training burden (see Figure. 1a). Benefiting from the remarkable generalization capabilities demonstrated by multimodal pre-trained models such as CLIP (Radford et al., 2021), several studies (Feng et al., 2024; Wei et al., 2024; Zhang et al., 2024; Liang et al., 2023) have emerged to leverage these pre-trained models for noise mitigation. However, these approaches still suffer from aforementioned limitations, including task specificity (Feng et al., 2024; Wei et al., 2024; Liang et al., 2023), model dependency (Wei et al., 2024) and excessive computational demands (Zhang et al., 2024), making them hard to utilize in practical scenarios. Most importantly, these methods share a common oversight in that they do not fully explore the potential of pre-trained models for noise detection.

To tackle these challenges, we use an external estimator to assess the noise level of each sample, ensuring the target model-agnostic. This estimator reduces the influence of noisy samples by reducing their weights of training loss closer to zero. We leverage multimodal pre-trained models as the estimator due to their revealed strong semantic capabilities and task transferability. For instance, CLIP (Radford et al., 2021) unifies the paradigms of image-text retrieval and image classification through a shared embedding space (see Figure. 1b). It converts category labels into sentences and then calculates the cosine similarity with the image representation to perform image classification. In this case, only one additional inference process is required for each sample, significantly reducing the computational overhead compared to performing an extra backward pass.

Nonetheless, this paradigm introduces a new challenge: how

<sup>&</sup>lt;sup>1</sup>Anonymous Institution, Anonymous City, Anonymous Region, Anonymous Country. Correspondence to: Anonymous Author <anon.email@domain.com>.

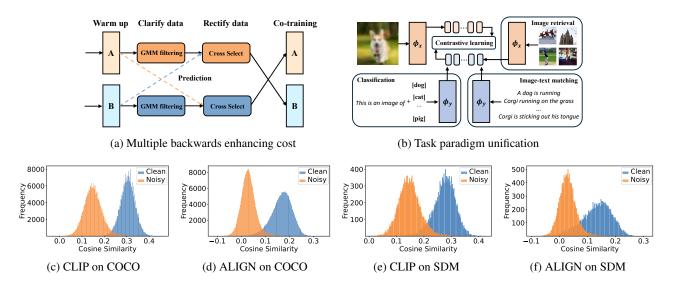


Figure 1: (a) The current anti-noise paradigm with multiple backward significantly enhances the training overhead. (b) CLIP unifies the framework of image-text matching and image classification through a shared space. (c-f) Cosine similarity distribution of noise and clean data with 50% noise.

to accurately identify noise based solely on cosine similarity scores inferenced by estimators. An ideal solution is to find a decision boundary in cosine space that can separate clean and noisy samples. Existing methods (Huang et al., 2021; Li et al., 2020; Feng et al., 2024; Zhang et al., 2024) typically attempt to build this boundary within the loss space, an isotropic space with uniform distribution, which creates only a narrow gap between noisy and clean samples. More critically, the coarse handling of overlaps by integrating multi-model predictions often results in an unstable decision boundary. In contrast, the shared embedding space of pre-trained models is a high-dimensional space, and its corresponding cosine similarity space is an anisotropic space with an imbalanced distribution. Thus, a consideration is whether the properties of imbalanced anisotropic space can help to identify a more precise and robust decision boundary.

In this work, we delve into the issue of decision boundary selection in anisotropic cosine spaces for pre-trained models being efficient noise estimators. Theoretically, a cosine similarity of zero—*i.e.*, an orthogonal boundary—should serve as a natural decision threshold in isotropic cosine spaces to separate clean and noisy samples. To validate this hypothesis, we empirically analyze the cosine similarity distributions of clean and noisy samples using multimodal pre-trained models CLIP (Radford et al., 2021) and ALIGN (Jia et al., 2021) across two datasets: MSCOCO and SDM (Stable Diffusion Model (Rombach et al., 2022)), both with a 50% noise ratio. The SDM dataset, comprising images generated in uncommon artistic styles (see Figure 4), is designed to test the robustness of pre-trained models in distinguishing noisy samples from unseen domains.

Surprisingly, as shown in Figure. 1c-1f, the empirically optimal decision boundary deviates significantly from the theoretical orthogonal threshold zero, limiting its usage in practical applications. Despite this deviation, there are also two interesting observations: (1) the intersection points of clean and noisy distributions remain consistent for the same model across different datasets, suggesting the existence of a stable, dataset-irrelevant boundary. (2) even on the SDM dataset—where models encounter unfamiliar domains—the overlap between clean and noisy distributions remains minimal, indicating the boundary's robustness in distinguishing noisy samples.

Building on these two observations, we aim to reveal the underlying mechanisms and provide a theoretical guidance for fully exploiting the potential of pre-trained models in noise mitigation. Our key contributions are as follows:

- 1. We figure out the origin of the intersection, attributing it to the shift of orthogonal boundaries induced by the cone effect. Furthermore, we provide a theoretical framework that proves and elaborates the stability and accuracy of this boundary in separating noisy and clean samples.
- 2. Building on our findings, we develop One-Step Antinoise (OSA), an efficient and model-agnostic paradigm for noise recognition that requires just one-step inference. Specifically, we utilize a pre-trained model as the estimator to maintain a task unification and model-agnostic framework. Then, we design a non-linear scoring function based on the shifted orthogonal boundary properties to balance the training process of overlapped ambiguous samples and positive samples by re-weighting their loss. This inference-based approach could significantly reduce the additional

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overhead in noise mitigation.

3. We conduct comprehensive experiments across a variety of challenging benchmarks, models, and tasks, demonstrating the effectiveness, generalization capabilities, and efficiency of our findings and introduced methods.

## 2. Boundary Principle Analysis

In Figure. 1c-1f, we observe a natural boundary emerging in the pre-trained model's ability to distinguish between clean and noisy samples. In this section, we explain the principle of boundary forming from high-dimensional perspectives, and how robust it is in general noise mitigation.

## 2.1. Hypothesis: Intersection Boundary is Shifted from Orthogonal Boundary

We first elaborate on the gap extent between the positive and negative sides kept by the orthogonal boundary. Then, we present the reasoning behind the hypothesis that the intersection boundary in Figure. 1 is a shifted orthogonal boundary in the cone space.

The orthogonal boundary largely separates the positive and negative sides. High-dimensional orthogonality is a general phenomenon caused by dimension disaster, where the angles between randomly selected vectors typically approximate 90 degrees, suggesting the cosine similarity that trends toward zero. For instance, in a 1024-dimensional space, the probability of two random vectors having a cosine similarity within [-0.1, 0.1] is approximately 99.86% (details in Appendix. D.1). This creates a natural boundary at zero cosine similarity, effectively separating the positive and negative sides with a large gap.

Table 1: The mean and variance of cosine similarity between randomly generated pairs.

Model	Mean	Var
CLIP	0.215	0.024
ALIGN	0.087	6e-4

Cone effect may induce orthogonal boundary shift. Recent literature (Liang et al., 2022a; Bogolin et al., 2022; Ethayarajh, 2019) has demonstrated that the cone effect is a general phenomenon in deep neural networks, where the learned embedding subspace forms a narrow cone and the orthogonal boundary encounters a positive shift. Based on this, a hypothesis is that the intersection boundary in Figure. 1 is the shifted orthogonal boundary. To prove this, we simulate the process of selecting random vectors in high-dimensional space and randomly generate thousands of pairs mapped into the shared embedding space. We find that all similarity of these random vector pairs tends to a fixed value, with the

low-variance cosine similarity almost lying in the middle of clean and noise distributions (see Table. 1). An interesting phenomenon is that if we compare the mean with the intersection points in Figure. 1c-1f, we find they are almost identical, suggesting that the intersection boundary is highly likely to be a shifted orthogonal boundary in cone space.

#### 2.2. Theoretical Verification of Intersection Origin

Here, we theoretically investigate whether the origin of the intersection boundary is a shifted orthogonal boundary. We first show that (i) contrastive learning separates clean and noisy samples on opposite sides of the orthogonal boundary and (ii) The relative relationships of pairs' cosine similarity stays unchanged after transmitting into the narrow cone space. Based on (i) and (ii), we can confirm that the intersection boundary at the center of the clean and noisy distributions is the shifted orthogonal boundary.

Contrastive learning empowers the separation of clean and noisy samples. For an initialized model to learn an embedding space, both clean and noisy samples are treated as orthogonal random vectors since lacking semantic perception ability in the initial space. During contrastive training process, given N sample pairs  $\{(x_i, y_i)\}_{i=1}^N$ , the embedding space is optimized through the cross-entropy loss:

$$\mathcal{L}_{ce} = \frac{1}{N} \sum_{i=1}^{N} \log \frac{\exp(m_{ii})}{\sum_{j=1}^{N} \exp(m_{ij})},$$
 (1)

where  $M \in \mathbb{R}^{N \times N}$  represents the cosine similarity matrix of N sample pairs during training process. Each element  $m_{ij} \in M$  denote the cosine similarity between  $x_i$  and  $y_j$ . The diagonal elements  $m_{ii}$  denote the cosine similarities of positive pairs, while the non-diagonal elements  $m_{ij}$  represent the cosine similarities of negative pairs.

To minimize  $\mathcal{L}_{ce}$  during training, two subprocesses occur: the diagonal elements of the matrix (*i.e.*, clean pairs) are optimized to the positive side of the orthogonal boundary, while the non-diagonal elements (equivalent to noise pairs) are optimized to the negative side. Consequently, the distributions of these two types of samples are on opposite sides of the orthogonal boundary.

#### Relative relationship unchanged in transmitting process.

We study how the boundary shifts from the entire space to the narrow cone in the neural network. The following theorem shows that the cosine similarity will be proportionally scaled to the target narrow cone, while still maintaining a boundary with properties similar to the orthogonal boundary. In other words, vectors with cosine similarity smaller than the orthogonal boundary in the original space remain smaller than the shifted boundary in the narrow cone space, while those larger remain larger.

**Theorem 2.1** (Proportional shift of boundary). Let  $\mathbb{R}^{d_{in}}$ 

be the original space before being transmitted in a neural network. Suppose  $u,v\in\mathbb{R}^{d_{in}}$  are any two random vectors with  $\cos(u,v)\approx 0$ .  $u_c,v_c\in\mathbb{R}^{d_{in}}$  is a pair of clean vectors with  $\cos(u_c,v_c)>0$ , while  $u_n,v_n\in\mathbb{R}^{d_{in}}$  is a noisy pair with  $\cos(u_n,v_n)<0$ . Given a Neural Network  $F(x)=f_t(f_{t-1}(\dots f_2(f_1(x))))\in\mathbb{R}^{d_{out}}$  with t layers.  $f_i(x)=\sigma_i(\mathbf{W}_ix+\mathbf{b}_i)$  denotes  $i^{th}$  layer, where  $\sigma(\cdot)$  indicates activation function.  $\mathbf{W}_i\in\mathbb{R}^{d_{out}^i\times d_{in}^i}$  is a random weight matrix where each element  $\mathbf{W}_i^{k,l}\sim\mathcal{N}(0,1/d_{out}^i)$  for  $k\in[d_{out}^i]$ ,  $l\in[d_{in}^i]$ , and  $\mathbf{b}_i\in\mathbb{R}^{d_{out}^i}$  is a random bias vector such that  $\mathbf{b}_i^k\sim\mathcal{N}(0,1/d_{out}^i)$  for  $k\in[d_{out}^i]$ . Then, there always be a boundary  $\beta$ , satisfying:

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$$\cos(F(u_n), F(v_n)) < \cos(F(u), F(v))$$

$$\approx \beta < \cos(F(u_c), F(v_c)). \tag{2}$$

Theorem. 2.1 shows the pairs' relative relationship in the original entire space remain unchanged after transmitting to the narrow cone space of the trained model, and there is always a boundary  $\beta$  concentrated on most random vectors. Appendix. D.2 provides a detailed statement and proof.

#### 2.3. Qualitative analysis of robustness and applicability

Next, we perform a qualitative analysis to explore (i) the robustness and generality of the boundary in distinguishing between clean and noisy samples, and (ii) how the boundary's properties can be leveraged to achieve more reasonable and precise overlap handling.

How about the boundary robustness even in unfamiliar domains? Although the boundary's ability to distinguish clean and noisy samples is proven, its robustness and generality still require further exploration. For practical pre-training, it must maintain accuracy and robustness even in unfamiliar domain datasets. Since the capabilities of the pre-trained model are difficult to quantify, we conduct a qualitative analysis from the perspective of pre-trained model inference. The models pre-trained on millions of samples already possess somewhat semantic understanding capabilities. Given a positive pair from an unseen domain, due to the contrastive learning process during pre-training, it still has a strong likelihood of moving toward the positive side of the boundary, while the negative pair tends toward the negative side. Although the cosine similarity difference might be slight, as we have shown in Section. 2.1, the boundary constructs a significant gap from the perspective of high-dimensional orthogonality.

How to handle the overlaps through imbalanced probability? Since orthogonal boundary properties, as cosine similarity decreases and approaches zero from the positive side, the probability of positive samples sharply decreases. Therefore, we can design a scoring function to annotate the cleanliness of samples. This function should satisfy

two requirements: for samples with cosine similarity less than or equal to zero, which are almost certainly noise, the function should assign them a weight of zero. For samples with cosine similarity greater than zero, the function gradient should increase rapidly as the cosine similarity moves further from zero.

#### 3. Method

In this section, we present our One-Step Anti-noise (OSA) paradigm with a workflow shown in Figure. 2. We first define the pair-based noise mitigation tasks in Sec. 3.1. Afterward, we clarify OSA in Sec. 3.2.

#### 3.1. Task Definition

Let  $\mathcal{D} = \{(x_i, y_i, c_i)\}_{i=1}^N$  denote a paired dataset, where  $(x_i, y_i)$  represents the *i*-th pair in the dataset, and  $c_i$  indicates a noise label for that pair. Specifically, when  $c_i = 0$ ,  $(x_i, y_i)$ forms a correct (paired) match, while  $c_i = 1$  denotes an incorrect (unpaired) match. The objective of noise mitigation in contrastive learning is to construct a shared embedding space that brings  $x_i$  and  $y_i$  closer when  $c_i = 1$ . In different tasks,  $x_i$  and  $y_i$  are distinct data types. For instance, in the image-text retrieval task,  $x_i$  and  $y_i$  represent images and texts, respectively. In the image classification task,  $x_i$  and  $y_i$  represent images and categories, respectively. In the image retrieval task,  $x_i$  and  $y_i$  represent images and relevant images, respectively. The paired sample (x, y) could be encoded into a shared embedding space by corresponding encoders  $\phi_x(\cdot)$  and  $\phi_y(\cdot)$ . Afterward, the cosine similarity s(x,y) is calculated through Eq. 3 as semantic relevance of (x,y) to guide the training.

$$s(x,y) = \frac{\phi_x(x)}{\|\phi_x(x)\|} \cdot \frac{\phi_y(y)}{\|\phi_y(y)\|}.$$
 (3)

#### 3.2. One-step Anti-Noise

The workflow of our noise mitigation approach OSA is depicted in Figure. 2. Initially, we utilize an estimator model to encode the input pair to a shared embedding space and continue to compute the cosine similarity between the paired embedding. Afterward, the cosine similarity is converted to a cleanliness score  $w_i$ ,  $(0 \le w_i \le 1)$  through a scoring function designed based on orthogonal properties (Section. 2.3). This score quantifies the clean degree of the sample, the smaller  $w_i$  is, the noisier the sample.

During the target model training phase, this cleanliness score is used as a weight, directly multiplied by the loss of the corresponding sample to facilitate selective learning. This noise mitigation process, being solely dependent on the estimator model, is readily adaptable to the training of various target models by simply adding an extra coefficient to the loss function, ensuring the model-agnostic property.

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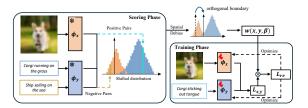


Figure 2: Two phases in the OSA workflow: In the Scoring Phase, a pair is mapped to a shared space by estimators. Then the cosine similarity is debiased based on the orthogonal boundary and transformed to a weight w by a scoring function. In the Training Phase, the weight w is directly multiplied with the loss to instruct the optimization.

Therefore, the key of our noise mitigation approach revolves around the estimator model and noise score assessment.

#### 3.2.1. ESTIMATOR MODEL

**Estimator model selection.** In our approach, the Estimator Model must satisfy two critical requirements: 1) effectively mapping input pairs into a unified embedding space and 2) possessing basic semantic understanding capabilities. To meet these requirements, we employ CLIP (Radford et al., 2021), a commonly used multimodal pre-trained models, as our estimator model. It is equipped with a text encoder  $\phi_t(\cdot)$  and an image encoder  $\phi_v(\cdot)$ , enabling it to perform basic zero-shot tasks efficiently.

**Domain adaptation (Optional).** While we have performed a qualitative analysis of the zero-shot pre-trained model's robustness on out-of-domain data in Section. 2.3, and shown strong robustness for edge cases in Figure. 1, considering the domain diversity in real-world scenarios, we provide an optional Domain Adaptation (DA) approach to enhance the estimator model's adaptability when encountering edge domains. Following NPC (Zhang et al., 2024), we first employ a Gaussian Mixture Model (GMM) coupled with strict selection thresholds to ensure the absolute cleanliness of the chosen samples. We afterward implement a warm-up phase with few steps, allowing the estimator model to better understand the semantics of the target domain. Notably, this trick is only optional for our methods. Through multiple experiments, we found that even without domain adaptation, the zero-shot CLIP model performs exceptionally well across various scenarios.

#### 3.3. Comparisons with State of The Arts

#### 3.3.1. Noise Score Assessment

**Spatial Debiasing.** The cone effect phenomenon has been demonstrated as a general phenomenon for deep neural networks, typically resulting in a narrow embedding space that causes a shift of space center to a narrow cone center (Liang

et al., 2022a). Specifically, when paired randomly generated inputs are mapped into a shared embedding space through model encoders, the resultant vectors exhibit an average cosine similarity that deviates from zero and tends to another fixed angle. To counteract this shift and mitigate its impact on the estimator's ability to accurately recognize noises through high-dimensional orthogonality, a random sampling method is developed. We begin by constructing K random sample pairs  $\mathcal{R} = \{(x_j, y_j) \mid j=1, 2, \ldots, K\}$  and processing them through the estimator's encoder to generate a set of vectors. Then the average cosine similarity among these vectors will be calculated as the space shift  $\beta$  through:

$$\beta = \frac{\sum_{j=1}^{K} s(x_j, y_j)}{K}.$$
 (4)

**Scoring Function.** After spatial debiasing, we employ a scoring function  $w(\cdot)$  to evaluate the cleanliness of the input pair (x, y). In section. 2.3, we have elaborate how to handle overlaps based on the orthogonal boundary property. For an estimator model trained on millions of samples using contrastive learning, clean pairs (diagonal elements) are optimized to positive side, while noise pairs (non-diagonal elements) are optimized to negative side. Given unfamiliar pairs, the model also tends to map clean pairs towards positive and noisy pairs towards negative. Despite the potentially slight similarity difference between clean and noisy pairs, high-dimensional orthogonality ensures a substantial gap between them. In this case, a negative cosine similarity s(x,y) computed by the estimator, indicating the pair is almost certainly noise, should be assigned a weight of zero. For samples with s(x, y) greater than the orthogonal boundary  $\beta$ , the probability of the sample being positive sharply decreases as the cosine similarity approaches orthogonal boundary from the positive side. Therefore, the function gradient should increase rapidly as the cosine similarity moves further from  $\beta$ . To systematically score the noise, we utilize  $\tilde{s}_{x,y} = s(x,y) - \beta$  to indicate the debiased cosine similarity score, and then, the scoring function for re-weighting can be designed as (more scoring function exploration in Appendix. F.1):

$$w(x, y, \beta) = \begin{cases} 0 & , \tilde{s}_{x,y} \le 0 \\ -(\tilde{s}_{x,y})^2(\tilde{s}_{x,y} - 1) & , otherwise \end{cases}$$
 (5)

**Re-weight Training.** After scoring, the target model can selectively learn from the samples by re-weighting the loss. Noise samples with smaller weights will have a reduced impact on model updates and will be effectively mitigated. For a sample (x,y), let  $\mathcal{L}_{x,y}$  denote its loss, the re-computed loss  $\mathcal{L}_{re}$  is defined as:

$$\mathcal{L}_{re} = w(x, y, \beta) \times \mathcal{L}_{x,y}. \tag{6}$$

Table 2: Comparison on noisy MS-COCO.

	<u> </u>	ı		MS-CC	CO 11/			1		MS-CC	CO 5V	,	
Noise ratio	Method		i2t	MS-CC	COIK	t2i			i2t	MS-CC	COSK	t2i	
rioise ratio	Wichiod	R@1	R@5	R@10	R@1	R@5	R@10	R@1	R@5	R@10	R@1	R@5	R@10
	VSE∞	82.0	97.2	98.9	69.0	92.6	96.8	62.3	87.1	93,3	48.2	76.7	85.5
	PCME++	81.6	97.2	99.0	69.2	92.8	97.1	62.1	86.8	93.3	48.1	76.7	85.5
	PAU	80.4	96.2	98.5	67.7	91.8	96.6	63.6	85.2	92.2	46.8	74.4	83.7
0%	NPC	82.2	96.5	98.7	68.3	92.0	98.7	65.4	87.3	93.1	48.5	75.4	84.4
	CLIP	80.1	95.7	98.2	67.1	91.4	96.6	62.9	84.9	91.6	46.5	73.8	82.9
	+OSA	82.2	96.5	98.7	68.8	92.1	96.7	65.6	86.8	92.9	49.1	76.2	84.8
	ALIGN	84.9	97.3	99.0	70.5	92.8	97.2	69.6	89.9	94.5	50.5	77.5	85.7
	+OSA	85.3	97.4	99.0	71.4	93.1	97.3	69.8	89.9	94.8	51.4	78.2	86.3
	$VSE\infty$	78.4	94.3	97.0	65.5	89.3	94.1	58.6	83.4	89.9	45.0	72.9	81.7
	PCME++	78.4	95.9	98.4	64.9	90.8	96.1	57.7	83.9	91.0	43.2	72.3	82.4
	PAU	78.2	95.2	98.1	64.5	90.0	95.4	59.3	82.9	90.4	44.2	71.3	81.3
20%	NPC	79.9	95.9	98.4	66.3	90.8	98.4	61.6	85.4	91.6	46.0	73.4	82.9
	CLIP	76.0	94.3	97.5	63.4	89.0	94.8	55.3	79.1	86.9	41.0	68.8	79.3
	+OSA	81.6	96.2	98.5	68.9	92.0	96.6	65.8	86.4	92.5	48.7	76.1	84.5
	ALIGN	79.4	95.7	98.2	66.2	90.8	96.1	60.9	84.5	91.0	46.3	73.6	82.3
	+OSA	85.1	97.4	99.1	70.9	93.0	97.3	69.7	90.0	94.7	50.9	77.8	86.2
	VSE∞	44.3	76.1	86.9	34.0	69.2	84.5	22.4	48.2	61.1	15.8	38.8	52.1
	PCME++	74.8	94.3	97.7	60.4	88.7	95.0	52.5	79.6	88.4	38.6	68.0	79.0
	PAU	76.4	94.1	97.6	62.3	88.5	94.6	57.3	81.5	88.8	41.9	69.4	79.6
50%	NPC	78.2	94.4	97.7	63.1	89.0	97.7	59.9	82.9	89.7	43.0	70.2	80.0
	CLIP	73.9	93.0	97.2	60.1	87.3	94.0	54.1	78.5	86.6	39.7	67.2	77.5
	+OSA	81.4	96.5	98.6	68.4	92.0	96.6	64.7	86.8	92.4	48.6	75.9	84.6
	ALIGN	78.0	95.8	98.5	65.4	90.3	96.0	60.1	84.3	91.2	45.2	72.8	82.1
	+OSA	84.3	97.0	98.9	70.0	92.5	97.0	68.5	89.2	94.2	50.0	77.0	85.4

## 4. Experiments

In this section, we present experiments on multiple datasets with label noise, demonstrating the effectiveness of our methods. Firstly, we describe the datasets, metrics, and implementation details. Then, we report our results on several downstream tasks. Lastly, we conduct ablation studies to show how each part of our method contributes and examine how these parts interact. The literature involved in our experiments and richer related work are detailed in Appendix. C.

#### 4.1. Evaluation Setting

In this section, we briefly introduce the datasets and evaluation metrics used in the experiments. For more dataset and implementation details, please refer to Appendix. B. **Datasets.** We evaluate our method on three downstream tasks with noisy labels, including one multimodal task and two visual tasks. For the cross-modal matching task, we perform experiments on the MSCOCO (Lin et al., 2014) and Flickr30K (Young et al., 2014) datasets. Following NPC (Zhang et al., 2024), we further carry out evaluations on a real-world noisy dataset CC120K. For image classification tasks, experiments are conducted under three subsets of WebFG-496 (Sun et al., 2021)—Aircraft, Bird, and Car. For image retrieval tasks, we conduct experiments on the CARS98N dataset under PRISM (Liu et al., 2021) setting.

**Evaluation Metrics.** For the image-text matching task, the recall value of the top-K retrieved results (R@K) is used. For classification tasks, accuracy serves as the evaluation metric. For the image retrieval task, we use Precision@1

and mAP@R for evaluation.

**Results on MSCOCO.** To fairly demonstrate the effectiveness of our method, we compare OSA with various robust learning image-text matching approaches using the same ViT-B/32 CLIP as backbone, including VSE∞ (Chen et al., 2021), PCME++ (Chun, 2023), PAU (Li et al., 2023), NPC (Zhang et al., 2024). Besides, we separately employ OSA on both CLIP (Radford et al., 2021) and ALIGN (Jia et al., 2021). The results in Table. 2 show that OSA outperforms all previous approaches on all metrics with a huge gap. In the more challenging MS-COCO 5K set with 50% noise ratio, OSA surpasses the SOTA method NPC in the R@1 for both image-to-text (i2t) and text-to-image (t2i) matching by 8.6% and 7.0%, respectively. Another phenomenon is that as the noise ratio increases from 0% to 50%, all other methods encounter severe performance drop, with an averaging drop of 5.05% for NPC across four R@1 metrics. In contrast, OSA exhibits only a slight decrease of 1.275%, showcasing the accuracy and robustness of OSA in anti-noise tasks.

Results on Flickr30K. To further demonstrate the generalization ability of OSA, we evaluate on the Flickr30K dataset and compare with several anti-noise methods, including NCR (Huang et al., 2021), DECL (Qin et al., 2022), Bi-Cro (Yang et al., 2023a), and NPC (Zhang et al., 2024). The results are presented in Table. 7 of Appendix. It is evident that OSA consistently outperforms all models on the R@1 metric. Notably, compared with the baseline CLIP, training with OSA at a 60% noise ratio achieves 20.9% R@1 im-

provement for i2t and a 22.3% R@1 improvement in t2i, further indicating the effectiveness of OSA on noise mitigation. Additionally, OSA demonstrates similar noise robustness on the Flickr30K dataset as observed on MSCOCO, with only 1.4% R@1 drop on i2t and 1.2% R@1 drop on t2i ranging from 0% noise to 60% noise, while all of the other antinoise approaches hardly resist the detriment from high-ratio noise. All of these results demonstrate the effectiveness and robustness of OSA on anti-noise tasks.

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**Results on CC120K.** To further verify the reliability of OSA in real scenarios, we conduct evaluations on a large-scale real-world noisy dataset, CC120K, with 3%-20% noise ratio. The results in Table. 8 of Appendix indicate that OSA outperforms the current state-of-the-art method NPC, even in real-world domains. This demonstrates the feasibility and generality of OSA even in practical training scenarios.

Results on Other Downstream Tasks. To validate the transferability of OSA across different tasks, we evaluate it on two additional tasks: image classification and image retrieval. The results are presented in Table. 3. The baseline method for both tasks leverages contrastive learning. In the image classification task, OSA outperforms the baseline by 7.74%, 8.21%, and 4.28% on the Aircraft, Bird, and Car subsets, respectively. In the image retrieval task, OSA improves performance by 6.76% in precision and 6.83% in mAP. These improvements demonstrate the strong task transferability and generality of OSA.

Table 3: Results of other image-based tasks.

				Image Retrieval			
Method	Aircraft	Bird	Car	Drac	m A D		
					ШАГ		
Baseline +OSA	65.44	62.29	75.90	71.69	18.16		
+OSA	73.18	70.50	80.19	78.45	24.99		

#### 4.2. Target Model-Agnostic Analysis

OSA is an architecture-agnostic paradigm easily adaptable to various models. To verify this, we evaluate it across different architectures and apply it to other anti-noise models to demonstrate its generalization in noise mitigation.

Architecture-agnostic Analysis. The effectiveness of OSA on Vision Transformer (ViT) has been proven in Section. 3.3. We further explore the generality of OSA on target models with other architectures. Specifically, we deploy OSA above the VSE++ (Faghri et al., 2018) model with two different architecture types: ResNet-152 (He et al., 2016) and VGG-19 (Simonyan & Zisserman, 2014). These two architectures are highly sensitive to noise (Huang et al., 2021). In this experiment, all estimator models employ zero-shot CLIP and we utilize the original VSE++ as our baseline. The results in Table. 4 indicate a significant performance

Table 4: The results of the target model with different architectures on noisy MSCOCO 1K.

NT : .:	N. 4. 1			i2t			t2i	
Noise ratio	Method	Architecture	R@1	R@5	R@10	R@1	R@5	R@10
	Baseline +OSA	ResNet-152	58.9 <b>58.9</b>	<b>86.9</b> 86.2	<b>93.8</b> 93.7	44.2 44.3		<b>88.3</b> 87.9
0%	+05A		30.9	00.2		44.3	11.9	
	Baseline	VGG-19		79.4	89.1	38.0		84.7
	+OSA	1 , 00 17	50.1	80.0	89.3	38.3	73.0	84.6
	Baseline	ResNet-152	45.8	70.3	83.7	36.1	68.4	79.7
20%	+OSA	Kesnet-132	58.1	86.1	93.2	43.4	76.8	87.2
2070	Baseline	VGG 10	33.2	67.1	81.5	25.9	58.0	71.4
	+OSA	VGG-19	49.3	79.1	88.6	37.2	71.9	83.8
	Baseline	D N 150	28.4	61.2	75.2	5.2	14.0	19.5
50%	+OSA	ResNet-152	55.0	84.0	92.0	40.7	74.7	85.6
2370	Baseline	VGG-19	2.5	9.8	16.2	0.1	0.5	1.0
	+OSA	VGG-19	47.1	77.7	87.6	35.7	70.3	82.8

degradation emerged for the baseline methods in noisy setting, while a stable performance is achieved after employing OSA. The stable performance on these two noise-vulnerable architectures fully demonstrates that OSA possesses the architecture-agnostic property.

Adaptability to Other Anti-Noise Models. Theoretically, OSA is adaptable to any target model. However, can OSA further enhance the robustness of models specifically designed for noise mitigation? To investigate this, we applied OSA to the current state-of-the-art model, NPC (Zhang et al., 2024). As shown in Table. 9 of Appendix, even for noise-mitigating models, OSA consistently improves training robustness. This finding further demonstrates the broad adaptability of OSA across different model types.

#### 4.3. Estimator Model Analysis.

The estimator model is the basis of OSA's anti-noise capability. In this section, we explore the impact of different estimator models on noise mitigation, and examine the impact of domain adaptation in noise mitigation. In Table. 10 of Appendix, we investigate four types of estimators: "None" refers to training CLIP directly without using OSA. "CLIP (w/o DA)" and "ALIGN (w/o DA)" represent using CLIP and ALIGN without domain adaptation as estimators, respectively, i.e., zero-shot CLIP and ALIGN. "CLIP (w DA)" indicates the CLIP with domain adaptation. The target models are all CLIP. We can observe that both of CLIP and ALIGN as estimators significantly enhance the target model performance stability when learning with noise, indicating that the choice of estimator is very flexible. Both CLIP and ALIGN demonstrate exceptional performance when served as estimators. The other phenomenon is that the zero-shot CLIP model shows comparable performance to the domainadapted CLIP with a even better performance at lower noise ratios. This indicates that zero-shot CLIP, as an estimator, already performs exceptionally well in noise mitigation. The domain adaptation is unnecessary. This further enhances

the deployment convenience of OSA.

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Table 5: ACC and recall of noise detection.

Estimator Type	20%	noise	50% Noise			
Dominuter Type	Acc.	Recall	Acc.	Recall		
CLIP (w/o DA)	93.88	97.49	93.91	99.35		
CLIP (w DA)	97.68	97.18	98.14	99.24		

#### 4.4. Noise Assessment Accuracy

Noise Detection Accuracy Analysis. To figure out how accurate OSA is in recognizing noise, we evaluate the accuracy and recall on CLIP without Domain-Adaptation (w/o DA) and CLIP with Domain-Adaptation (w DA) on noisy MSCOCO. We utilize zero as the threshold to roughly divide pairs into noise and clean sets, respectively. Concretely, we classify scores less than or equal to 0 as noise, and scores greater than 0 as clean. The Accuracy means the proportion of the clean pairs correctly classified into the clean set, while the Recall indicates the noisy pairs correctly classified into the noisy set. The results presented in Table. 5 indicates the powerful noise recognizing capability of OSA. The remarkable performance on CLIP (w/o DA) fully demonstrates the generality of OSA. Another notable phenomenon is that all recall scores converge towards 100, suggesting that OSA can almost entirely eliminate the impact of noise on training.

Noise Re-weighting Accuracy Comparison. Some antinoise methods, like NPC, also employ loss re-weighting for optimization. To assess whether our method assigns relatively smaller weights to noise than these methods, we first analyze the weights generated by NPC and OSA. Due to differences in weight scales across methods, a direct comparison is unfair. We therefore adopt a ranking-based approach, sorting weights in descending order and calculating the Mean Noise Rank to unify the scale. This metric evaluates whether smaller weights are consistently assigned to noisy samples relative to clean ones. Our experiments use 2,000 randomly selected samples from the MSCOCO dataset under two noise conditions: 20% noise (370 noisy samples) and 50% noise (953 noisy samples). The theoretical optimal Mean Noise Ranks, where all noisy weights are ranked last, are 1815.5 and 1524.0, respectively. Results presented in Table. 11 of Appendix show that OSA achieves a higher Mean Noise Rank compared to NPC, demonstrating greater accuracy in re-weighting. Moreover, OSA's rankings are nearly optimal (20% noise: 1809.1 for OSA vs. 1815.5 optimal; 50% noise: 1520.7 for OSA vs. 1524.0 optimal). This near-perfect alignment indicates that OSA effectively places almost all noisy samples behind the clean ones.

#### 4.5. Computational Cost Analysis

Cost in Pre-training. To evaluate the practicality of OSA in a real-world pre-training scenario, we estimate the additional computational cost for processing 1 billion data points. Using an NVIDIA RTX 3090 with an inference batch size of 4096, utilizing about 24 GB of GPU memory, processing the MS-COCO dataset consisting of 566,435 pairs takes approximately 153 seconds. At this inference rate, processing 1 billion data points would require approximately 75 hours on a single RTX 3090. This cost is negligible for large-scale pre-training, especially with multiple GPUs for parallel inference.

Time Cost Comparison. To further examine the computational efficiency of our method compared to other anti-noise techniques, we evaluate training time against two representative approaches: CLIP and NPC. CLIP, which serves as the baseline, is trained directly without any additional technique. NPC, the current state-of-the-art, also uses CLIP as its backbone but applies an anti-noise technique by estimating the negative impact of each sample, necessitating double backward passes. The training time comparison, presented in Table. 12 of Appendix, shows that our method introduces only a minimal increase in training time compared to direct training, requiring just one-tenth of the additional time needed by NPC. This highlights the efficiency of OSA, making it well-suited for large-scale robust training tasks.

#### 5. Conclusion

In this work, we investigated the potential of anti-noise techniques for practical large-scale training, uncovering the underlying mechanisms of orthogonal boundary shifts in pre-trained models. We provide theoretical guidance for fully harnessing the capabilities of pre-trained models in noise mitigation. Building on these insights, we introduced a novel model-agnostic anti-noise paradigm that offers key advantages, including task transferability, model adaptability, and minimal computational overhead. By leveraging the properties of high-dimensional orthogonality, we designed a robust decision boundary to effectively distinguish between noisy and clean samples. Through rigorous theoretical analysis and comprehensive experiments, we demonstrated the efficacy and robustness of OSA for general noise mitigation. While our primary focus was on adapting to largescale training scenarios, OSA also achieves state-of-the-art performance in standard anti-noise settings. To our knowledge, this is the first work to explore noise mitigation in large-scale training and to fully leverage the potential of pre-trained models in this context, as well as the first to propose a general anti-noise approach.

## **Impact Statement**

This paper presents work whose goal is to advance the field of robust learning in noisy correspondences. There are many potential societal consequences of our work, none which we feel must be specifically highlighted here.

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## **Appendix**

#### A. Limitations and Future Works

Limited by the significant computational cost of pre-training, it is difficult for us to evaluate in a real pre-training process. Instead, we simulate large-scale pre-training processes to the greatest extent possible, such as evaluating on the real-world noisy dataset CC120K, which shares similar domains with mainstream pre-training datasets like CC4M and CC12M. Exploring the broad domain adaptability of OSA in real pre-training scenarios will be a valuable direction for future work.

#### **B.** Details of Implementation

**Dataset Details.** MSCOCO is widely used for noisy cross-modal matching, with each image accompanied by five descriptive captions. Following the setting of Huang et al. (2021), we utilize 113,287 images for training, 5,000 for validation, and 5,000 for testing. The Flickr30K dataset encompasses 31,783 image-text instances, each image paired with five textual annotations. Adhering to the NCR (Huang et al., 2021), we use 29,783 images for training and 1,000 images each for validation and testing. Regarding noise splits, following the NCR categorization, we conduct experiments at noise ratios of 0%, 20%, 40%, and 60%. CC120K is a real-world multimodal noisy dataset collected by Zhang et al. (2024) from the Internet, with about 3%-20% noise ratio. There are 118,851 image-text pairs for training, 1,000 for validation, and 1,000 for testing.

The Aircraft, Bird, and Car we used in the image classification task are three non-overlapping subsets of the WebFG-496 (Sun et al., 2021) dataset. WebFG-496 consists of 53,339 images, totaling 496 subcategories. This dataset is annotated using a webly supervised approach, which leverages resources from web search engines (*e.g.*, Google Image Search Engine, Bing Image Search Engine) to expand the annotated image dataset.

For the image retrieval task, we conduct experiments on the <u>CARS98N</u> dataset under PRISM's setting (Liu et al., 2021). We utilize 9,558 car-related images sourced from text-based searches on Pinterest as the training set, and employ the remaining 98 categories from CARS, unsearched on Pinterest, as a clean test set. The dataset's noise is inherently real-world, with its creators estimating a noise ratio of approximately 50%.

**Implementation Details.** To demonstrate the effectiveness of the OSA, we incorporate an estimator, built around the core of CLIP, and re-weighting operations based on the Estimator's outcomes into numerous downstream tasks. In the principal task of cross-modal image-text retrieval, we employ CLIP with ViT-B/32 as the baseline and target model by default. All experiments are conducted on a single RTX 3090 GPU using the AdamW optimizer. During both training phases, the model is trained for five epochs with a batch size of 256 and 500 warmup steps.

For the image classification task on the WebFG dataset, we align with the field's prevalent models for a fair comparison by employing the ResNet-50 model enhanced by CLIP for feature extraction and the CLIP image encoder as our estimator. Training and testing are executed on single RTX 3090 GPU, with an input image resolution of  $448 \times 448$ . The batch size and initial learning rate are specified as 64 and 1e-5, respectively. In the first phase, the estimator is trained with data modeled by a Gaussian Mixture Model (GMM), which considers the classification and matching losses of all training samples, with the GMM probability threshold of 0.95. The classification task leverages the CLIP protocol, where a fixed prompt ("This is a picture of") is prepended to category texts.

For the image retrieval task, we use CLIP ViT-B/32 as the baseline, with a batch size set to 128, an initial learning rate of 5e-6, and the number of epochs set to 10. Following the setup of the PRISM (Liu et al., 2021), we set the parameter for sampling positive examples by the random sampler of the dataloader to 4, and adjust the number of positive examples sampled per epoch to one-fourth of the original parameter according to the increase in batch size. In this task, we also adopt a two-stage training approach. The strictly clean in-domain training data for the first stage is obtained using a GMM model with a probability setting of 0.8.

#### C. Related work

#### C.1. Noise Mitigation in Cross-Modal Matching

The cross-modal matching task (Lee et al., 2018; Song & Soleymani, 2019; Li et al., 2019; 2022; Diao et al., 2021) serves as a fundamental component in multimodal learning. However, the inherent difference in information density between

these modalities leads to high annotation costs and inconsistent annotation quality, rendering cross-modal tasks particularly vulnerable to label noise. Some approaches explicitly identify and correct noisy samples through cross-prediction between concurrently trained dual models (Huang et al., 2021; Yang et al., 2023a; Liang et al., 2022b), while others (Zhang et al., 2024; Qin et al., 2022) implicitly estimate the probability of sample noise, reducing its training impact by adjusting the loss function. NCR (Huang et al., 2021) employs the memorization capacity of its counterpart model for simple clean samples to rectify the output results. BiCro (Yang et al., 2023a) utilizes the consistency of similarity score distributions from a Siamese model ensemble on noisy data, alongside anchors modeled on the loss distribution via a Beta-Mixture-Model (BMM), to filter out noisy samples. NPC (Zhang et al., 2024), deviating from the dual-model training schemes, introduces a two-stage single-model training approach that reduces training overhead by replacing two backward passes with one forward and one backward pass. Specifically, the first stage estimates the impact of potentially noisy samples on model performance by constructing a high-quality clean sample bank; the second stage then utilizes these estimates to reweight the loss function. However, current methods for distinguishing clean from noisy samples rely on numerous hyperparameters that are closely linked to dataset size and model capacity. This dependency not only limits their adaptability to various downstream tasks but also makes them challenging to deploy in real-world applications.

#### C.2. Noise Mitigation in Image Classification

Image classification is vulnerable to training data noise, due to varied noise types and strong model memorization. Noise in datasets manifests in two primary forms: synthetic alterations and those arising from real-world scenarios. The former typically involves shuffling the labels of a subset of the data or retaining the labels while introducing corresponding category images from external datasets. The latter entails substituting images for a random selection of data points with those sourced from image search engines. Existing approaches are categorized based on their operational focus: loss correction (Yi & Wu, 2019; Zhang & Sabuncu, 2018a; Menon et al., 2015; Natarajan et al., 2013; Patrini et al., 2017; Xia et al., 2019; Ghosh et al., 2017; Wang et al., 2019a;b; Xu et al., 2019; Zhang & Sabuncu, 2018b) and sample selection (Sun et al., 2022; Albert et al., 2023; Yao et al., 2021; Li et al., 2020; Albert et al., 2022). Loss correction methods typically incorporate a regularization term into the loss function, implicitly reweighting clean and noisy samples within the loss. Sample selection strategies, in contrast, explicitly differentiate between clean and noisy samples, applying distinct processing to each category during loss computation. Representative for the loss correction category, (Zhang & Sabuncu, 2018a) aims to generalize ordinary Cross-Entropy loss and MAE loss by setting the loss threshold to iid and ood noisy samples. DivideMix (Li et al., 2020) concurrently trains two networks, each utilizing the data partitioning from the other network to distinguish between clean and noisy samples based on loss values, thereby mitigating the influence of confirmation bias inherent within each network. PNP (Sun et al., 2022) framework employs a unified predictive network to estimate the in-distribution (iid), out-of-distribution (ood), and clean probabilities for a given sample. Co-training trained on a sample that has a lower loss, and with the different predictions by its siamese network.

#### C.3. Noise Mitigation in Image Retrieval.

Although image retrieval tasks focus on pairwise relationships, the noise predominantly originates from image categorization errors. Analogous to image classification tasks, this can be bifurcated into in-domain (Wang & Tan, 2018) and open-set noise (Liu et al., 2021). In terms of task configuration, noise retrieval typically operates at the category level, treating images within the same category as positive instances. PRISM (Liu et al., 2021) tries to find noisy image samples by finding the outliers score in the whole similarity matrix from the same category. The generalization ability of the image feature is ensured by a broader query bank restored multi-view of it. TITAN (Yang et al., 2023b) utilizes prototypes to be representative of the anchor of the clean and noisy samples and then generates synthetic samples by a combination of prototypes for substitution of noisy samples. T-SINT (Ibrahimi et al., 2022b) utilizes more negative samples by the interaction between noisy samples and negative samples that belong to another category.

#### **D. Proofs**

#### D.1. Proof of High-dimensional Orthogonality

Suppose  $u,v \in \mathbb{R}^d$  are any two random vectors. The cosine similarity  $\cos(u,v) \sim \mathcal{N}(0,d^{-1})$ . The probability that  $\cos(u,v)$  is within a specific range [-a,a] is denoted as:

$$P(-a \le \cos(u, v) \le a) = \Phi\left(\frac{a}{\varsigma}\right) - \Phi\left(\frac{-a}{\varsigma}\right),\tag{7}$$

where  $\Phi$  represents the CDF of the standard normal distribution, and  $\varsigma = \frac{1}{\sqrt{d}}$  is the standard deviation of the cosine similarity. When d=1024 and a=0.1, there are

$$\varsigma = \frac{1}{\sqrt{1024}} = \frac{1}{32},\tag{8}$$

and

$$P(-0.1 \le \cos(u, v) \le 0.1) = \Phi\left(\frac{0.1}{1/32}\right) - \Phi\left(\frac{-0.1}{1/32}\right) \approx 0.9986. \tag{9}$$

#### D.2. Proof of Theorem 1

In the Section. 2.2, we propose that Theorem 1 about the relative relationship of pairs in the original entire space, will not change after transmitting to the narrow cone space of the trained model, and there is always a boundary r concentrated on most random vectors.

To prove this Theorem, we first introduce a useful lemma of monotonicity of cosine similarity proposed by Liang et al. (2022a), indicating that the cosine similarity between two vectors increases with a high probability after one feedforward computation consisting of a linear transformation and ReLU computation.

**Lemma D.1.** Suppose  $u, v \in \mathbb{R}^{d_{in}}$  are any two fixed vectors such that ||u|| = r ||v|| for some r > 0,  $\mathbf{W} \in \mathbb{R}^{d_{out} \times d_{in}}$  is a random weight matrix where each element  $\mathbf{W}_{k,l} \sim \mathcal{N}(0, d_{out}^{-1})$  for  $k \in [d_{out}]$ ,  $l \in [d_{in}]$ , and  $\mathbf{b} \in \mathbb{R}^{d_{out}}$  is a random bias vector such that  $\mathbf{b}_k \sim \mathcal{N}(0, d_{out}^{-1})$  for  $k \in [d_{out}]$ . If  $\cos(u, v) < (\frac{1}{2}(r + \frac{1}{r}))^{-1}$ , then the following holds with probability at least  $1 - O(1/d_{out})$ .

$$\cos(\sigma(\mathbf{W}u + \mathbf{b}), \sigma(\mathbf{W}v + \mathbf{b})) > \cos(u, v). \tag{10}$$

Proof of Theorem. 2.1. Let  $\mathbb{R}^{d_{in}}$  be the original space before being transmitted in a neural network. Suppose  $u,v\in\mathbb{R}^{d_{in}}$  are any two random vectors with  $\cos(u,v)\approx 0$ .  $u_c,v_c\in\mathbb{R}^{d_{in}}$  is a pair of clean vectors with  $\cos(u_c,v_c)>0$ , while  $u_n,v_n\in\mathbb{R}^{d_{in}}$  is a noisy pair with  $\cos(u_n,v_n)<0$ . Given a Neural Network  $F(x)=f_t(f_{t-1}(\dots f_2(f_1(x))))\in\mathbb{R}^{d_{out}}$  with t layers.  $f_i(x)=\sigma_i(\mathbf{W}_ix+\mathbf{b}_i)$  denotes  $i^{th}$  layer, where  $\sigma(\cdot)$  indicates activation function.  $\mathbf{W}_i\in\mathbb{R}^{d_{out}^i\times d_{in}^i}$  is a random weight matrix where each element  $\mathbf{W}_i^{k,l}\sim\mathcal{N}(0,1/d_{out}^i)$  for  $k\in[d_{out}^i]$ ,  $l\in[d_{in}^i]$ , and  $\mathbf{b}_i\in\mathbb{R}^{d_{out}^i}$  is a random bias vector such that  $\mathbf{b}_i^k\sim\mathcal{N}(0,1/d_{out}^i)$  for  $k\in[d_{out}^i]$ . We would like to prove that there are always be a boundary  $\beta$ , satisfying:

$$\cos(F(u_n), F(v_n)) < \cos(F(u), F(v)) \approx \beta < \cos(F(u_c), F(v_c)), \tag{11}$$

which is equivalent to proving.

$$\cos(f_i(u_n), f_i(v_n)) < \cos(f_i(u), f_i(v)) \approx \beta_i < \cos(f_i(u_c), f_i(v_c)), \tag{12}$$

where  $\beta_i$  is the boundary of  $i^{th}$  layer.

We first consider the cosine similarity between u and v as:

$$\cos(u, v) = \frac{u \cdot v}{\|u\| \|v\|}.$$
(13)

After a linear transformation of  $i^{th}$  layer, the cosine similarity of  $\cos(\mathbf{W}_i u + \mathbf{b}_i, \mathbf{W}_i v + \mathbf{b}_i)$  denotes:

$$\cos(\mathbf{W}_i u + \mathbf{b}_i, \mathbf{W}_i v + \mathbf{b}_i) = \frac{(\mathbf{W}_i u + \mathbf{b}_i) \cdot (\mathbf{W}_i v + \mathbf{b}_i)}{\|\mathbf{W}_i u + \mathbf{b}_i\| \|\mathbf{W}_i v + \mathbf{b}_i\|}.$$
(14)

Since  $\mathbf{b}_i$  has a mean of zero and is independent from  $\mathbf{W}_i u$  and  $\mathbf{W}_i v$ , the expectation of  $\mathbf{b}_i$  and  $(\mathbf{W}_i u + \mathbf{b}_i) \cdot \mathbf{W}_i v + \mathbf{b}_i)$  can be signified as:

$$\mathbb{E}\left[\mathbf{b}_{i}\right] = 0,\tag{15}$$

$$\mathbb{E}\left[\left(\mathbf{W}_{i}u + \mathbf{b}_{i}\right) \cdot \left(\mathbf{W}_{i}v + \mathbf{b}_{i}\right)\right] = \mathbb{E}\left[\left(\mathbf{W}_{i}u \cdot \mathbf{W}_{i}v\right)\right] = \sum_{i=1}^{n} \sum_{i=1}^{n} \frac{1}{d_{out}^{i}} u_{k} v_{k} = \frac{1}{d_{out}^{i}} (u \cdot v). \tag{16}$$

715 Additionally, we have

$$\|\mathbf{W}_i u + \mathbf{b}_i\|^2 = \mathbf{W}_i u \cdot \mathbf{W}_i u + 2\mathbf{W}_i u \cdot \mathbf{b}_i + \mathbf{b}_i \cdot \mathbf{b}_i. \tag{17}$$

Due to  $\mathbb{b}^k \sim \mathcal{N}(0, 1/d_{out}^i)$ , as  $d_o^i ut$  increases, the term of  $2\mathbf{W}_i u \cdot \mathbf{b}_i$  and  $\mathbf{b}_i \cdot \mathbf{b}_i$  become negligible, which implies

$$\|\mathbf{W}_i u + \mathbf{b}_i\|^2 \approx \mathbf{W}_i u \cdot \mathbf{W}_i u = \sum_{i=1}^n (\mathbf{W}_i u)^2.$$
(18)

Therefore, the expectation of  $\|\mathbf{W}_i u + \mathbf{b}_i\|^2$  is approximate to

$$\mathbb{E}\left[\|\mathbf{W}_{i}u\|^{2}\right] = \sum_{k=1}^{n} u_{k}^{2} \frac{1}{d_{out}^{i}} = \frac{\|u\|}{d_{out}^{i}},\tag{19}$$

and

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$$\cos(\mathbf{W}_{i}u + \mathbf{b}_{i}, \mathbf{W}_{i}v + \mathbf{b}_{i}) \approx \frac{\mathbb{E}[\mathbf{W}_{i}u \cdot \mathbf{W}_{i}v]}{\sqrt{\mathbb{E}[\|\mathbf{W}_{i}u + \mathbf{b}_{i}\|^{2}]\mathbb{E}[\|\mathbf{W}_{i}v + \mathbf{b}_{i}\|^{2}]}}$$

$$= \frac{\frac{1}{d_{out}^{i}}(u \cdot v)}{\sqrt{\frac{1}{d_{out}^{i}}\|u\|^{2} \cdot \frac{1}{d_{out}^{i}}\|v\|^{2}}}$$

$$= \cos(u, v). \tag{20}$$

Based on Eq. 20, with  $\cos(u_n, v_n) < \cos(u, v) \approx 0 < \cos(u_c, v_c)$ , there are

$$\cos(\mathbf{W}_i u_n + \mathbf{b}_i, \mathbf{W}_i v_n \mathbf{b}_i) < \cos(\mathbf{W}_i u + \mathbf{b}_i, \mathbf{W}_i v + \mathbf{b}_i) < \cos(\mathbf{W}_i u_c + \mathbf{b}_i, \mathbf{W}_i v_c + \mathbf{b}_i). \tag{21}$$

Since the activation function  $\sigma$  is a monotonically increasing function, it follows

$$\cos(f_i(u_n), f_i(v_n)) < \cos(f_i(u), f_i(v)) < \cos(f_i(u_c), f_i(v_c)). \tag{22}$$

Due to Lemma. D.1,  $\cos(f_i(u), f_i(v))$  will be increase with the transmitting layers, and  $\cos(f_i(u), f_i(v))$  will always be a  $\beta_i > 0$ , to satisfy:

$$\cos(f_i(u_n), f_i(v_n)) < \cos(f_i(u), f_i(v)) \approx \beta_i < \cos(f_i(u_c), f_i(v_c)). \tag{23}$$

After transmitting each layer, Eq. 23 are always satisfied. When transmitting a neural network with t layers, we have

$$\cos(F(u_n), F(v_n)) < \cos(F(u), F(v)) \approx \beta < \cos(F(u_c), F(v_c)). \tag{24}$$

#### D.3. Proof of Orthogonality Validity in Cone Space

Although we have demonstrated in Appendix. D.1 that in the original high-dimensional space, the cosine similarity between two randomly selected vectors—each dimension following a Gaussian distribution—typically converges near the orthogonal boundary, this property may not necessarily extend to the subspace of the shared embedding space maintained by the trained models. Specifically, for real image-text pairs, the subspace may deviate from the orthogonal characteristics observed in the original space. Thus, it is essential to investigate whether the orthogonality property holds within the cone space for the image-text subdomain post-training.

To explore this, we first analyze the distribution of several dimensions of image and text features from the CC120K dataset, as illustrated in Figure. 3. The results reveal that all vector dimensions, including trained parameters, exhibit a Gaussian distribution with near-zero means. This phenomenon arises from the convergence properties in two-layer networks that adhere to the central limit theorem (Sirignano & Spiliopoulos, 2020), which, through the application of mean-field analysis, has been extended to neural network architectures (Lu et al., 2020). Consequently, the model parameters exhibit an overall Gaussian distribution, leading to Gaussian features. If the dimensions of the trained embedding space follow Gaussian distributions, the process of selecting random vectors within this space would be analogous to that of the original space, thereby preserving the orthogonality property. Here, we present the following theorem: The output features of large-scale models tend to Gaussian distribution. The detailed theorem and proof are provided below.

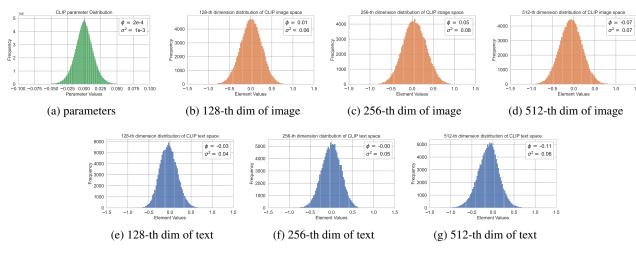


Figure 3: The illustrations of several distributions on CC120K. (a) The parameter distribution. (b-d) The distribution of image features for the 128th, 256th, and 512th dimensions. (e-g) The distribution of text features for the 128th, 256th, and 512th dimensions.

**Theorem D.2** (Output features tends to Gaussian). Given a Neural Network  $F(x) = \{f_t(f_{t-1}(\dots f_2(f_1(x))))\} \in \mathbb{R}^{d_{out}}$  with t layers.  $f_l(x) = \phi_l(\mathbf{W}_l x + \mathbf{b}_l)$  denotes the  $l^{th}$  layer, where  $\phi(\cdot)$  indicates the activation function, and the final layer  $f_t(x) = \mathbf{W}_t x + \mathbf{b}_t$  is a fully-connected layer without an activation function for common space projection. Let  $x^k \in \mathbb{R}^{d_{in}^k}$  be the sample feature that will be transmitted into the  $k^{th}$  layer, where  $x^1$  denotes the original feature with an unknown distribution  $x^1 \sim (\mu_x, \sigma_x^2)$ .  $\mathbf{W}_k \in \mathbb{R}^{d_{out}^k \times d_{in}^k}$  is a random weight matrix where each element  $w_{ij}^k \sim \mathcal{N}(0, \sigma_w^2)$  for  $i \in [d_{out}^k]$ ,  $j \in [d_{in}^k]$ , and  $\mathbf{b}_k \in \mathbb{R}^{d_{out}^k}$  is a bias vector such that  $b_i^k \sim \mathcal{N}(0, \sigma_w^2)$  for  $i \in [d_{out}^k]$ . In such a neural network, linear layers lead features x gradually to a Gaussian distribution from any initial distribution, and as  $|d_{in}|$  is sufficiently large,  $F(x) \sim \mathcal{N}(0, \sigma^2)$ .

Proof of Theorem. D.2. For the  $k^{th}$  layer  $(k \in [t])$ , we first calculate the expectation and variance of the linear combination  $\sum_{j=1}^{d_{in}^k} w_{ij}^k x_j^k$ . For the expectation, since  $w_{ij}^k$  and  $x_j^k$  are independent and  $\mathbf{w}_{ij}^k \sim \mathcal{N}(0, \frac{1}{d_{out}^k})$ , we have:

$$\mathbb{E}\left[\sum_{j=1}^{d_{in}^k} w_{ij}^k x_j^k\right] = \sum_{j=1}^{d_{in}^k} \mathbb{E}[w_{ij}^k] \mathbb{E}[x_j^k] = \sum_{j=1}^{d_{in}^k} (0 \times \mathbb{E}[x_j^k]) = 0.$$
 (25)

For variance, since  $w_{ij}^k$  and  $x_j^k$  are independent, we have:

$$\operatorname{Var}\left(\sum_{j=1}^{d_{in}^{k}} w_{ij}^{k} x_{j}^{k}\right) = \sum_{j=1}^{d_{in}^{k}} \operatorname{Var}(w_{ij}^{k} x_{j}^{k}) = \sum_{j=1}^{d_{in}^{k}} \mathbb{E}\left[(w_{ij}^{k})^{2}(x_{j}^{k})^{2}\right]$$

$$= \sum_{j=1}^{d_{in}^{k}} \mathbb{E}\left[(w_{ij}^{k})^{2}\right] \mathbb{E}\left[(x_{j}^{k})^{2}\right]$$

$$= \sum_{j=1}^{d_{in}^{k}} \sigma_{w^{k}}^{2} \left(\operatorname{Var}(x_{j}^{k}) + (\mathbb{E}[x_{j}^{k}])^{2}\right)$$

$$= \sum_{j=1}^{d_{in}^{k}} \sigma_{w^{k}}^{2} \left(\sigma_{x^{k}}^{2} + \mu_{x^{k}}^{2}\right) = d_{in}^{k} \sigma_{w^{k}}^{2} \left(\sigma_{x^{k}}^{2} + \mu_{x^{k}}^{2}\right).$$
(26)

Since  $w_{ij}^k$  are independently distributed Gaussian random variables, and  $x_j^k$  has a known mean and variance, the sum of

 $w_{ij}^k x_j^k$  can apply to a generalized Central Limit Theorem. We have

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$$\frac{\sum_{j=1}^{d_{in}^k} w_{ij}^k x_j^k - \mathbb{E}\left[\sum_{j=1}^{d_{in}^k} w_{ij}^k x_j^k\right]}{\sqrt{\operatorname{Var}\left(\sum_{j=1}^{d_{in}^k} w_{ij}^k x_j^k\right)}} \xrightarrow{d} \mathcal{N}(0,1),$$

which is equivalent to 

$$\frac{\sum_{j=1}^{d_{in}^k} w_{ij}^k x_j^k - 0}{\sqrt{d_{in}^k \sigma_{-k}^2 \left(\sigma_{-k}^2 + \mu_{-k}^2\right)}} \xrightarrow{d} \mathcal{N}(0,1). \tag{28}$$

(27)

Therefore,

$$\sum_{j=1}^{d_{in}^k} w_{ij}^k x_j^k \xrightarrow{d} \mathcal{N}(0, d_{in}^k \sigma_{w^k}^2 (\sigma_{x^k}^2 + \mu_{x^k}^2)). \tag{29}$$

Due to  $b^k \sim \mathcal{N}(0, \sigma_b^2)$ , we finally get

$$\sum_{i=1}^{d_{in}^k} w_{ij}^k x_j^k + b_i^k \xrightarrow{d} \mathcal{N}\left(0, d_{in}^k \sigma_{w^k}^2 (\sigma_{x^k}^2 + \mu_{x^k}^2) + \sigma_b^2\right). \tag{30}$$

Although activation functions truncate the Gaussian distribution after each linear layer, the samples still gradually approach a Gaussian distribution from the initial unknown distribution as they pass through the layers. Furthermore, because there is a fully connected layer (layer) without an activation function before mapping to the final common space, the final feature distribution will approximate a Gaussian distribution, as follows:

$$F(x) \sim \mathcal{N}(0, d_{in}^t \sigma_{w^t}^2 (\sigma_{x^t}^2 + \mu_{x^t}^2) + \sigma_b^2).$$
 (31)

#### E. SDM Visualization

We visualize some representative samples from our synthetic domain originating from COCO by using SDM. The results are shown in Figure. 4. We generate two styles of image based on the MSCOCO caption, and then use pre-trained multimodal models to calculate cosine similarity with the SDM-generated image and original caption.

## **Sketch Style**



A kitchen counter with dirty dishes near sink.



A couple of young men playing a game of frisbee.



A wooden kitchen table with three wooden chairs.

## **Cartoon Style**



A woman in a young girl inside of the cabin.



Miscellaneous kitchen utensils on a wooden shelf.



Skier standing for picture on a gentle slope.

Figure 4: Examples of generated SDM dataset. The first row is in sketch style, while the second row is in cartoon style.

## F. Additional Experimental Results

#### F.1. Exploration of Different Scoring Function

In Section 3.3.1, we introduce a scoring function designed to handle overlaps effectively and re-weight samples based on their cosine similarity. This section explores several scoring functions, including the Linear, Cosine, and High-degree functions. The functions are presented individually as follows:

Linear Function.

$$w(x,y,\beta) = \begin{cases} 0 & ,\tilde{s}_{x,y} \le 0\\ \tilde{s}_{x,y} & ,otherwise \end{cases}$$
 (32)

**Cosine Function.** 

$$w(x, y, \beta) = \begin{cases} 0 & , \tilde{s}_{x,y} \le 0\\ \frac{\cos(\pi(\tilde{s}_{x,y} - 1)) + 1}{2} & , otherwise \end{cases}$$

$$(33)$$

**High-degree Function.** 

$$w(x, y, \beta) = \begin{cases} 0 & , \tilde{s}_{x,y} \le 0 \\ -(\tilde{s}_{x,y})^2 (\tilde{s}_{x,y} - 1) & , otherwise \end{cases}$$
(34)

The results presented in Table. 6 indicate that the High-Degree Function outperforms the others across all evaluation metrics.

This superior performance can be attributed to the rapid gradient changes near the decision boundary, which align better with the tendency of orthogonal boundaries. As a result, we adopt the High-Degree Function as our scoring function.

Table 6: Comparison of different scoring function.

				MS-CC	OCO 1K			MS-COCO 5K					
Noise ratio	Method		i2t			t2i			i2t			t2i	
		R@1	R@5	R@10	R@1	R@5	R@10	R@1	R@5	R@10	R@1	R@5	R@10
	Linear Function	80.4	96.2	98.6	67.8	91.6	96.4	64.0	85.5	91.9	47.9	74.6	83.8
50%	Cosine Function	80.8	96.3	98.5	67.7	91.6	96.3	64.4	86.2	92.3	48.0	74.9	83.9
	High-Degree Function	81.4	96.5	98.6	68.4	92.0	96.6	64.7	86.8	92.4	48.6	75.9	84.6

Table 7: Comparison on noisy Flickr30K.

Method	Noise ratio		i2t			t2i		Noise ratio		i2t			t2i	
Michiou	INDISC TALIO	R@1	R@5	R@10	R@1	R@5	R@10	INOISE TALLO	R@1	R@5	R@10	R@1	R@5	R@10
NCR		77.3	94.0	97.5	59.6	84.4	89.9		73.5	93.2	96.6	56.9	82.4	88.5
DECL		79.8	94.9	97.4	59.5	83.9	89.5		77.5	93.8	97.0	56.1	81.8	88.5
BiCro	007	81.7	95.3	98.4	61.6	85.6	90.8	200	78.1	94.4	97.5	60.4	84.4	89.9
NPC	0%	87.9	98.1	99.4	75.0	93.7	97.2	20%	87.3	97.5	98.8	72.9	92.1	95.8
CLIP		86.2	97.6	99.2	72.9	92.3	96.0		82.3	95.5	98.3	66.0	88.5	93.5
+OSA		88.6	97.7	99.3	75.6	93.6	96.8		88.9	97.7	99.1	75.6	93.3	96.9
NCR		68.1	89.6	94.8	51.4	78.4	84.8		13.9	37.7	50.5	11.0	30.1	41.4
DECL		72.7	92.3	95.4	53.4	79.4	86.4		65.2	88.4	94.0	46.8	74.0	82.2
BiCro	4007	74.6	92.7	96.2	55.5	81.1	87.4	6007	67.6	90.8	94.4	51.2	77.6	84.7
NPC	40%	85.6	97.5	98.4	71.3	91.3	95.3	60%	83.0	95.9	98.6	68.1	89.6	94.2
CLIP		76.2	93.3	96.5	59.4	85.0	90.9		66.3	87.3	93.0	52.1	78.8	87.4
+OSA		87.3	97.6	99.3	74.2	93.1	96.7		87.2	98.1	99.6	74.4	92.9	96.4

Results on CC120K. To further verify the reliability of OSA in real scenarios, we conduct evaluations on a large-scale real-world noisy dataset, CC120K, with 3%-20% noise ratio. The results in Table. 8 indicate that OSA outperforms the current state-of-the-art method NPC, even in larger-scale real-world domains. This demonstrates the feasibility and generality of OSA even in practical training scenarios.

Table 8: Comparison on real-world noisy dataset CC120K.

		i2t		t2i			
Method	R@1	R@5	R@10	R@1	R@5	R@10	
NPC							
CLIP	68.8	87.0	92.9	67.8	86.4	90.9	
+OSA	73.1	92.2	95.7	73.9	91.2	94.7	

Table 9: The results of other methods employing OSA on MSCOCO 1K.

			i2t			t2i	
Noise Ratio	Method	R@1	R@5	R@10	R@1	R@5	R@10
0%	NPC	82.2	96.5	98.7	68.3	92.0	98.7
070	+OSA	82.4	96.4	98.6	68.5	91.8	98.7
20%	NPC	79.9	95.9	98.4	66.3	90.5	98.4
20%	+OSA	81.2	96.0	98.6	66.9	91.2	98.6
50%	NPC	78.2	94.4	97.7	63.1	89.0	97.7
30%	+OSA	79.3	95.6	98.2	66.8	90.8	98.2

Table 10: Ablation study of estimator type on noisy MS-COCO.

				MS-CC	CO 11	Κ				MS-CC	CO 5I	K	
Noise ratio	Estimator		i2t			t2i			i2t			t2i	
		R@1	R@5	R@10	R@1	R@5	R@10	R@1	R@5	R@10	R@1	R@5	R@10
	None	80.1	95.7	98.2	67.1	91.4	96.6	62.9	84.9	91.6	46.5	73.8	82.9
0%	CLIP (w/o DA)	82.6	96.7	98.7	68.5	92.1	96.7	66.2	87.0	93.3	48.6	75.7	84.8
0%	ALIGN (w/o DA)	81.9	96.7	98.7	68.9	92.2	96.9	64.8	86.6	92.7	49.0	75.9	84.7
	CLIP (w DA)	82.2	96.5	98.7	68.8	92.1	96.7	65.6	86.8	92.9	49.1	76.2	84.8
	None	76.0	94.3	97.5	63.4	89.0	94.8	55.3	79.1	86.9	41.0	68.8	79.3
2007	CLIP (w/o DA)	81.8	96.1	98.7	68.2	91.9	96.5	64.8	86.6	92.3	48.3	75.4	84.1
20%	ALIGN (w/o DA)	81.2	96.0	98.6	67.7	91.5	96.4	64.8	86.2	92.3	47.8	74.9	83.9
	CLIP (w DA)	81.6	96.2	98.5	68.9	92.0	96.6	65.8	86.4	92.5	48.7	76.1	84.5
	None	73.9	93.0	97.2	60.1	87.3	94.0	54.1	78.5	86.6	39.7	67.2	77.5
<b>5</b> 007	CLIP (w/o DA)	79.6	95.6	98.4	65.9	90.8	95.9	62.4	84.8	90.8	45.7	73.1	82.5
50%	ALIGN (w/o DA)	80.4	95.6	98.3	66.0	90.5	95.8	62.0	84.9	91.8	45.7	73.2	82.5
	CLIP (w DA)	81.4	96.5	98.6	68.4	92.0	96.6	64.7	86.8	92.4	48.6	75.9	84.6

Table 11: Mean Noise Rank Comparison between OSA and NPC.

Noise Ratio	Method	Mean Noise Rank↑	<b>Optimal Rank</b>	Noise Number	Sample Number
20%	NPC	1641.3	1815.5	370	2,000
20%	OSA	1809.1	1815.5	370	2,000
50%	NPC	1456.2	1524.0	953	2,000
30%	OSA	1520.7	1524.0	953	2,000

Table 12: Overhead Comparison.

Model	Time	Extra Cost
CLIP	97 min	0 min
NPC	323 min	226 min
OSA	118 min	21 min