MoLEx: Mixture of Layer Experts for Fine-tuning with Sparse Upcycling

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Paper under double-blind review

Abstract

Large-scale pre-training of deep models, followed by fine-tuning them to adapt to downstream tasks, is currently the cornerstone of natural language processing (NLP). The massive size of these models has led to remarkable success in many NLP tasks. However, a detriment is the expense required to retrain all the base model's parameters for the adaptation to each task or domain. Parameter Efficient Fine-Tuning (PEFT) provides a highly effective solution for this challenge by minimizing the number of parameters required to be trained while maintaining the quality of the model. In this paper, we study layers as extractors of different types of linguistic information that are valuable when used in conjunction with each other. We then propose the Mixture of Layer Experts (MoLEx), a novel sparse mixture of experts (SMoE) whose experts are layers in the pre-trained model. It performs a conditional computation of a mixture of layers during fine-tuning to provide the model with more structural knowledge about the data. By providing an avenue for information exchange between layers, MoLEx enables the model to make a more well-informed prediction for the downstream task, leading to better fine-tuning results with the same number of effective parameters. As experts can be processed in parallel, MoLEx introduces minimal additional computational overhead. We empirically corroborate the advantages of MoLEx when combined with popular PEFT baseline methods on a variety of downstream fine-tuning tasks, including the popular GLUE benchmark and End-to-End Challenge (E2E).

1 Introduction

Numerous natural language processing (NLP) applications depend on leveraging a large-scale, pre-trained language model for multiple downstream tasks (Liu, 2020; Zhu et al., 2020; Stickland et al., 2020; Zhang et al., 2020; Raffel et al., 2020a; Kale & Rastogi, 2020; Zhong et al., 2020; Liu & Lapata, 2019). This adaptation is typically achieved through fine-tuning, a process that involves updating all the parameters of the pre-trained model. Although fine-tuning large language models (LLMs) has driven impressive success across various NLP tasks (Devlin et al., 2018; Liu, 2019; Radford et al., 2019; Raffel et al., 2020b), a drawback is the high computational cost associated with retraining all of the base model's parameters for adaptation to each specific task or domain (Brown et al., 2020; Chowdhery et al., 2023). Parameter efficient fine-tuning (PEFT), such as Low-Rank Adaptation (LoRA) (Hu et al., 2021), offers an effective solution to this issue by reducing the number of parameters that need to be trained for task adaptation while still preserving the model's performance (Zaken et al., 2021; Rücklé et al., 2021; Xu et al., 2023; Pfeiffer et al., 2021; Lin et al., 2020; Houlsby et al., 2019; Li & Liang, 2021; Xu et al., 2023). Since scaling up language models has proven highly successful, extending this scalability to the fine-tuning process is a desirable goal. However, achieving scalable fine-tuning with parameter efficiency remains a challenging and unresolved problem.

Recently, Sparse Mixture of Experts (SMoE) has emerged as a promising approach to the efficient scaling of language models. By dividing the network into modular components and activating only a subset of experts for each input, SMoE retains constant computational costs while enhancing model complexity. This technique has enabled the development of billion-parameter models and has achieved notable success in diverse areas such as machine translation (Lepikhin et al., 2021), image classification (Riquelme et al., 2021), and speech recognition (Kumatani et al., 2021).

1.1 Sparse Mixture of Experts

An SMoE replaces a component in the layer of the model, for example, a feed-forward or convolutional layer, by a set of networks termed experts to perform a conditional computation. It consists of a router and E expert networks, u_i, $i = 1, 2, \ldots, E$. For each input token $\boldsymbol{x}_t \in \mathbb{R}^D$ at layer t, the SMoE's router computes the affinity scores between $\boldsymbol{x}_t$ and each expert as $g_i(\boldsymbol{x}_t)$, $i = 1, 2, \ldots, E$. In practice, we often choose the router $\boldsymbol{g}(\boldsymbol{x}_t) = [g_1(\boldsymbol{x}_t), g_2(\boldsymbol{x}_t), \ldots, g_E(\boldsymbol{x}_t)]^\top = \boldsymbol{W}\boldsymbol{x} + \boldsymbol{b}$, where $\boldsymbol{W} \in \mathbb{R}^{E\times D}$ and $\boldsymbol{b} \in \mathbb{R}^E$. Then, a sparse gating function TopK is applied to select only K experts with the greatest affinity scores. Here, we define the TopK function as:

$$\text{TopK}(g_i) := \begin{cases} g_i, & \text{if } g_i \text{ is in the } K \text{ largest elements of } g \\ -\infty, & \text{otherwise.} \end{cases} \tag{1}$$

The outputs from K expert networks chosen by the router are then linearly combined as

$$\boldsymbol{x}_{t+1} = \boldsymbol{x}_t + \sum_{i=1}^{E} \text{softmax}(\text{TopK}(g_i(\boldsymbol{x}_t))u_i(\boldsymbol{x}_t) = \boldsymbol{x}_t + u(\boldsymbol{x}_t), \tag{2}$$

where $\text{softmax}(g_i) := \exp(g_i)/\sum_{j=1}^{E}\exp(g_j)$. We often set $K = 2$, i.e., top-2 routing, as this configuration has been shown to provide the best trade-off between training efficiency and testing performance (Lepikhin et al., 2021; Du et al., 2022; Zhou et al., 2023).

Sparse Upcycling. Sparse upcycling (Komatsuzaki et al., 2022) is used to turn a dense pre-trained model into an SMoE model by replacing some multilayer perceptron layers (MLP) in the pre-trained model by SMoE layers. Each SMoE layer contains a fixed number of experts. Each expert is initialized as a copy of the original MLP.

1.2 Contribution

In this paper, we employ sparse upcycling (Komatsuzaki et al., 2022) to upgrade the model to an SMoE for parameter efficient fine-tuning, whose experts are layers in the pre-trained models, and we propose the novel Mixture of Layer Experts (MoLEx) upcycling method. MoLEx operates on every layer of the pre-trained model, implementing a conditional computation mechanism that aggregates multiple layers. Our contribution is three-fold.

1. We develop the Mixture of Layer Experts (MoLEx), a new layer-wise sparse upcycling method for the parameter-efficient fine-tuning of LLMs whose experts are layers in the pre-trained model.
2. We study MoLEx from an ensemble model perspective and theoretically prove that a linear MoLEx-upcycled model is more robust than the original dense model.
3. We empirically demonstrate the advantages of MoLEx in accuracy, robustness, and zero-shot transfer learning ability on various large-scale fine-tuning benchmarks, including GLUE (Wang et al., 2018) and the E2E NLG Challenge (Novikova et al., 2017b).

2 MoLEx: Mixture of Layer Experts

2.1 Backbone Architecture Setting

Our proposed method, MoLEx, is agnostic to the training objective, so it can be adapted to any type of backbone architecture. Without loss of generality and for the convenience of presenting our method, we focus on language modeling as our motivating use case. We first provide a setting for the backbone architecture. Given an input sequence $\boldsymbol{x} \in \mathcal{X}$, where $\mathcal{X} = \mathbb{R}^{N\times D_x}$, we consider the backbone architecture to be a deep model f that transforms the input data point $\boldsymbol{x}$ into its features $\boldsymbol{z}_T \in \mathcal{Z}$, where $\mathcal{Z} = \mathbb{R}^{N\times D_z}$, via a sequence of T processing layers $(u_0, u_1, \ldots, u_{T-1})$ as follows:

$$\boldsymbol{z}_0 = \boldsymbol{x};\ \boldsymbol{z}_{t+1} = \boldsymbol{z}_t + u_t(\boldsymbol{z}_t; \boldsymbol{\theta}_t),\ t = 0, \ldots, T-1. \tag{3}$$

where $\boldsymbol{\theta}_t$ is the learnable parameters of the processing layer t.

2.2 MoLEx Upcycling

Given the same setting as in Section 2.1, the MoLEx transform is applied on each layer t of the pre-trained model $f^{(0)}$ to turn $f^{(0)}$ into a sparsely upcycled model $\text{MoLEx}(f^{(0)})$ as follows:

$$\boldsymbol{z}_0 = \boldsymbol{x},\ \ v_t(\boldsymbol{z}_t) = \sum_{j=0}^{T-1} \text{softmax}(\text{TopK}(g_j(\boldsymbol{z}_t))u_j(\boldsymbol{z}_t; \boldsymbol{\theta}_j^{(0)}),\ t = 0, \ldots, T-1, \tag{4}$$

$$\boldsymbol{z}_{t+1} = \boldsymbol{z}_t + \alpha u_t(\boldsymbol{z}_t; \boldsymbol{\theta}_t^{(0)}) + (1-\alpha)v_t(\boldsymbol{z}_t),$$

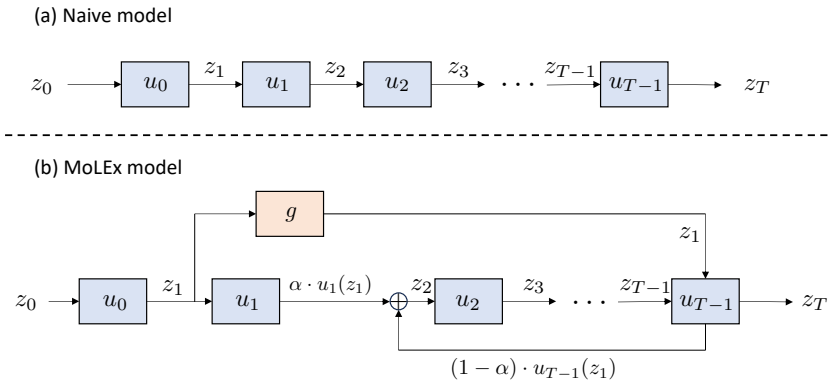

Figure 1: **(a)** A naive parameter efficient fine-tuning model with T layers, $u_0, u_1, \cdots, u_{T-1}$ and input z_0. z_t, for $t = 1, 2, \cdots, T$ are the outputs of each layer. **(b)** A MoLEx model transformed from a parameter efficient fine-tuning model with T layers, $u_0, u_1, \cdots, u_{T-1}$ and input z_0. z_t, for $t = 1, 2, \cdots, T$ are the outputs of each MoLEx layer. At each layer, the input to the layer is processed by a gate g to select the top-1 layer expert and the outputs of the layer and the selected layer are linearly combined and weighted by α and $1 - \alpha$ respectively. In the diagram, at layer u_1, layer u_{T-1} is chosen by the gate for mixing. Then, the outputs of layer u_1 and layer u_{T-1} are summed after multiplying them with α and $1 - \alpha$ respectively.

where, again, the sparse gating function TopK selects the top-K layers with highest affinity scores $g_j, j = 0, \ldots, T-1$, where K is set to 1 in our method, and $\text{softmax}(g_i) := \exp(g_i)/\sum_{j=0}^{T-1} \exp(g_j)$ is the softmax normalization operator as defined in Section 1.1. We follow the standard setting for SMoE in (Shazeer et al., 2017; Fedus et al., 2022) and choose the router $\boldsymbol{g}(\boldsymbol{z}_t) = [g_0(\boldsymbol{z}_t), g_1(\boldsymbol{z}_t), \ldots, g_{T-1}(\boldsymbol{z}_t)]^\top = \boldsymbol{W}\boldsymbol{z}_t + \boldsymbol{b}$, where $\boldsymbol{W} \in \mathbb{R}^{T \times D_z}$ and $\boldsymbol{b} \in \mathbb{R}^T$. Finally, α is a learnable parameter used to combine the original layer u_t with the chosen layer v_t from the SMoE, $t = 0, \ldots, T-1$. Compared to the original pre-trained model $f^{(0)}$, the MoLEx upcycling $\text{MoLEx}(f^{(0)})$ shares the layer parameters $\boldsymbol{\Theta} = \{\boldsymbol{\theta}_0, \boldsymbol{\theta}_1, \ldots, \boldsymbol{\theta}_{T-1}\}$ and only introduces additional parameters $\boldsymbol{W}$, $\boldsymbol{b}$, and α as a router and weight shared between all layers.

To clarify our method's implementation, we insert the relevant parameter efficient fine-tuning method into the pre-trained model to obtain each layer u_j. Then, we initialize a trainable gate, g, in the model to be shared across all layers. This gate determines the top-1 layer selected, v_t, to be mixed with u_j, $j = 0, 1, \ldots, T-1$. We provide a diagram in Figure 1 for visualization of MoLEx.

Despite its simple formulation, MoLEx offers an efficient and effective approach to sparse upcycling the models. Next, we will discuss the robustness property of MoLEx as an ensemble model.

2.3 MoLEx as an Ensemble Model

In this section, we consider the simple case when u_j is a linear layer to provide insights into the advantages of MoLEx. We start with deriving an ensemble perspective of MoLEx from the linearity of each u_j by unrolling $\boldsymbol{z}_t$ to obtain

$$\begin{aligned} u_j(\boldsymbol{z}_t) &= u_j(\boldsymbol{z}_{t-1} + \alpha u_{t-1}(\boldsymbol{z}_{t-1}) + (1-\alpha)u_{i_{t-1}}(\boldsymbol{z}_{t-1})) \\ &= u_j(\boldsymbol{z}_{t-1}) + \alpha u_j(u_{t-1}(\boldsymbol{z}_{t-1})) + (1-\alpha)u_j(u_{i_{t-1}}(\boldsymbol{z}_{t-1})). \end{aligned}$$

We denote i_t to be the layer index of the layer expert chosen by the gate at each layer t, i.e., to clarify, $u_{i_{t-1}} = v_{t-1}$ in Eqn. 4. Repeating this for each $j = 0, \cdots, T-1$, in Eqn. 5, we write $\boldsymbol{z}_{t+1}$ as a linear combination of compositions of u_j weighted by $c_{i_0, i_1, \cdots, i_t} \geq 0$, a constant that is non-zero if and only if the combination $u_{i_t} \circ u_{i_{t-1}} \circ \cdots \circ u_{i_0}$ was chosen by the gate. We can re-label each sequence of $i_0, i_1, \cdots, i_t$ to an integer $j \in \{1, 2, \cdots, 3^{t+1} - 1\}$ and each composition of $u_{i_t} \circ u_{i_{t-1}} \circ \cdots \circ u_{i_0}$ to f_j for $c_{i_0, i_1, \cdots, i_t} > 0$ as there are at most $3^{t+1} - 1$ combinations in t layers of MoLEx. Then, we will have

$$\begin{aligned} \boldsymbol{z}_{t+1} &= \boldsymbol{z}_t + \alpha u_t(\boldsymbol{z}_t) + (1-\alpha)u_{i_t}(\boldsymbol{z}_t) \qquad (5) \\ &= \boldsymbol{z}_0 + \sum_{T-1 \geq i_0, i_1, \cdots, i_t \geq 0} c_{i_0, i_1, \cdots, i_t} u_{i_t} \circ u_{i_{t-1}} \circ \cdots \circ u_{i_0}(\boldsymbol{x}) = \boldsymbol{x} + \sum_{j=1}^{3^{t+1}-1} c_j f_j \end{aligned}$$

With such an unrolling, we are able to view a linear MoLEx model as an ensemble of linear models. Next, we will show that MoLEx, as an ensemble, is more robust than a single base model in the ensemble. We begin with a formal definition of robustness.

Definition 1 (ϵ-Robustness). *Consider an input $\boldsymbol{x}$ and a classifier model, $f : \mathbb{R}^d \to [C]$, for a C-way classification task where $[C] = \{1, \cdots, C\}$. If for all $\tilde{\boldsymbol{x}}$ within a closed ball of radius $\epsilon > 0$ with center $\boldsymbol{x}$, i.e. $\tilde{\boldsymbol{x}} \in B(\boldsymbol{x}, \epsilon) = \{\boldsymbol{x} + \delta : \|\delta\|_2 \leq \epsilon\}$, $f(\tilde{\boldsymbol{x}}) = f(\boldsymbol{x})$, then we say f is ϵ-robust at $\boldsymbol{x}$. We say that f is more robust than g if and only if f is ϵ'-robust and g is ϵ-robust at x, with $\epsilon' > \epsilon$.*

Definition 2 (Linear MoLEx as an Ensemble Model). *From Eqn. 5, we can view a linear MoLEx model as a weighted ensemble of base functions, f_j, where each $f_j = u_{i_t} \circ u_{i_{t-1}} \circ \cdots \circ u_{i_0}$ is a composition of a certain permutation of the layers u_t, $t \in \{0, \cdots, T-1\}$. For simplicity, let $f_0 = Id$, the identity function, $c_0 = 1$ and $n_t = 3^{t+1} - 1$, so that we can write $\boldsymbol{z}_{t+1} = \sum_{j=0}^{n_t} c_j f_j$ as a MoLEx model with $t+1$ layers.*

We consider a set of fine-tuning sample data $\boldsymbol{X}$ drawn from some distribution χ with labels $\boldsymbol{Y}$. For the ease of understanding, we consider the output of the MoLEx model, $\boldsymbol{z}_{t+1}$, and a single base model with sequential layers, $f_{[0:t]} = u_t \circ u_{t-1} \circ \cdots u_0$, to be in the probability simplex, $\Delta^C = \{(x_1, x_2, \cdots, x_C) \in \mathbb{R}^C_{\geq 0} | \sum_{j=1}^{C} x_j = 1\}$ and refer to these as prediction models. A classifier model is then a prediction model composed with a classifier head $H(\boldsymbol{x}) = \arg\max_i x_i$ where x_i are the elements of the vector $\boldsymbol{x}$. Then, our classifier model is $F(\boldsymbol{x}) = H(f(\boldsymbol{x})) = \arg\max_{i \in [C]} f(\boldsymbol{x})_i$ where $f(\boldsymbol{x})_i$ is the i-th element in the output vector $f(\boldsymbol{x})$.

It is not difficult to see that for an input vector $\boldsymbol{x} \in \boldsymbol{X}$ with label y, and a perturbed $\tilde{\boldsymbol{x}} \in B(\boldsymbol{x}, \epsilon)$, for a classifier $F = H(f)$ to remain ϵ-robust at $\boldsymbol{x}$, we require that the prediction function satisfies

$$f(\tilde{\boldsymbol{x}})_y \geq f(\tilde{\boldsymbol{x}})_{y_i}, \forall y_i \neq y \tag{6}$$

where $f(\tilde{\boldsymbol{x}})_{y_i}$ is the y_i-th element of $f(\tilde{\boldsymbol{x}})$. Equivalently, we state this as a lemma below.

Lemma 1 (Robustness condition for classifier model). *Consider a prediction function f, classifier head H, data point $(\boldsymbol{x}, y) \in (\boldsymbol{X}, \boldsymbol{Y})$ and a perturbed point $\tilde{\boldsymbol{x}} \in B(\boldsymbol{x}, \epsilon)$. If $F(\boldsymbol{x}) = H(f(\boldsymbol{x})) = y$, then F is ϵ-Robust at $\boldsymbol{x}$ if and only if*

$$\forall y_i \in [C], y_i \neq y, \min_{\tilde{\boldsymbol{x}} \in B(\boldsymbol{x}, \epsilon)} f(\tilde{\boldsymbol{x}})_y - f(\tilde{\boldsymbol{x}})_{y_i} \geq 0 \tag{7}$$

We are now ready to state our result regarding the improved robustness of linear ensembles and we defer all proofs to the appendix in section A.

Theorem 1 (Linear ensembles are more robust). *Consider a data point $(\boldsymbol{x}, y) \in (\boldsymbol{X}, \boldsymbol{Y})$, $\epsilon > 0$, and M linear base models, $f_j(\boldsymbol{x}) = \boldsymbol{W}_j^\top \boldsymbol{x}$ such that $\forall y_i$ and $\boldsymbol{W}_j$,*

1. $\frac{1}{\epsilon}(\boldsymbol{e}_y - \boldsymbol{e}_{y_i})^\top f_j(\boldsymbol{x}) \geq \|\boldsymbol{W}_j(\boldsymbol{e}_y - \boldsymbol{e}_{y_i})\|_2$
2. $\boldsymbol{W}_j(\boldsymbol{e}_y - \boldsymbol{e}_{y_i})$ *are not colinear,*

where e_y is the standard basis vector with 1 at the y-th position and 0 everywhere else. An ensemble classifier model, with a classification head H, $F_M = H(\sum_{j=0}^{M-1} c_j f_j)$ is ϵ'-robust at $\boldsymbol{x}$ with $\epsilon' > \epsilon$.

Corollary 1 (Sufficient conditions for ϵ-robustness). *Consider a data point $(\boldsymbol{x}, y) \in (\boldsymbol{X}, \boldsymbol{Y})$, if a classifier model $F = H(f)$ with prediction function, $f(\boldsymbol{x}) = \boldsymbol{W}^\top \boldsymbol{x}$ satisfies*

$$\frac{1}{\epsilon}(\boldsymbol{e}_y - \boldsymbol{e}_{y_i})^\top f(\boldsymbol{x}) \geq \|\boldsymbol{W}(\boldsymbol{e}_y - \boldsymbol{e}_{y_i})\|_2,$$

then F is ϵ-robust at $\boldsymbol{x}$.

Corollary 2 (Linear MoLEx is more robust than sequential model). *If the base models of MoLEx $f_j = u_{i_t} \circ u_{i_{t-1}} \circ \ldots \circ u_{i_0}$ satisfies assumptions 1 and 2 in Theorem 1 above, then $\boldsymbol{z}_{t+1} = \sum_{j=0}^{n_t} c_j f_j$ is more robust than $f_{[0:t]}$.*

Consequently, we have established the robustness of a linear MoLEx model under perturbations within a closed ϵ-ball.

3 Experimental Results

In this section, we empirically validate the fine-tuning performance of MoLEx on the Natural Language Understanding (NLU) task, GLUE (Wang et al., 2018), the Natural Language Generation (NLG) benchmark, the End-to-End (E2E) dataset (Novikova et al., 2017a), and in a zero-shot evaluation on several GLUE tasks. Across all tasks and models, we apply MoLEx to LoRA on various models, including RoBERTa-base, RoBERTa-large (Liu, 2019), and GPT-2 (medium) (Radford

Table 1: RoBERTa-base (RoB_{base}) and RoBERTa-large (RoB_{large}) fine-tuned on the popular GLUE benchmark. MoLEx (bold and shaded in gray) is our proposed method in combination with LoRA. Hence, we use LoRA as our baseline for comparison. For all tasks, we report accuracy except for Matthew's correlation for CoLA, Pearson correlation for STS-B, the overall (matched and mismatched) accuracy for MNLI.

Model & Method	# Trainable Parameters	MNLI	SST-2	MRPC	CoLA	QNLI	QQP	RTE	STS-B	Avg.
RoB_{base} (LoRA)	0.3M	$87.5_{\pm.2}$	$95.0_{\pm.1}$	$88.7_{\pm.3}$	$62.8_{\pm1.0}$	$93.2_{\pm.2}$	$90.8_{\pm.0}$	$76.9_{\pm1.1}$	$90.8_{\pm.2}$	85.7
RoB_{base} (MoLEx)	0.309M	**$87.7_{\pm.2}$**	**$95.4_{\pm.2}$**	**$89.8_{\pm.2}$**	**$64.8_{\pm.5}$**	$93.2_{\pm.2}$	**$91.0_{\pm.0}$**	**$77.3_{\pm1.3}$**	**$91.0_{\pm.2}$**	**86.3**
RoB_{large} (LoRA)	0.8M	$90.7_{\pm.1}$	$96.3_{\pm.2}$	$90.9_{\pm.4}$	$67.8_{\pm1.7}$	$94.8_{\pm.3}$	$91.5_{\pm.1}$	$86.5_{\pm.9}$	$91.9_{\pm.1}$	88.8
RoB_{large} (MoLEx)	0.809M	**$90.9_{\pm.1}$**	**$96.4_{\pm.2}$**	**$91.4_{\pm.7}$**	**$68.2_{\pm.2}$**	$94.8_{\pm.0}$	**$91.6_{\pm.1}$**	**$87.1_{\pm.9}$**	**$92.0_{\pm.2}$**	**89.1**

Table 2: GPT2 medium (M) fine-tuned on the standard E2E NLG Challenge benchmark. We reproduce the LoRA baseline and compare it to our proposed method MoLEx (bold and shaded in gray) using the usual BLEU, NIST, MET, ROUGE-L and CIDEr metrics, where higher numbers indicate better performance.

Model & Method	# Trainable Parameters	E2E NLG Challenge				
		BLEU	NIST	MET	ROUGE-L	CIDEr
GPT-2 M (LoRA)	0.35M	$70.0_{\pm.5}$	$8.77_{\pm.05}$	**$46.8_{\pm.2}$**	$71.6_{\pm.3}$	$2.52_{\pm.01}$
GPT-2 M (MoLEx)	0.359M	**$70.7_{\pm.4}$**	**$8.87_{\pm.03}$**	$46.5_{\pm.09}$	**$71.8_{\pm.1}$**	$2.52_{\pm.01}$

et al., 2019). We use LoRA as our baseline for comparison. While MoLEx is compatible with any other fine-tuning method, we choose LoRA as it is one of the most popular light-weight adapters. Details on these tasks, models, metrics and implementations can be found in Appendix B. We also include Tables 9 and 10 in Appendix E.1 for a comprehensive comparison of our method and LoRA with results from prior works of other adaptation methods for reference. Our results are averaged over 5 runs with different seeds and conducted on a server with 8 A100 GPUs.

3.1 Natual Language Understanding

Using a pre-trained RoBERTa-base and RoBERTa-large model, we fine-tune the models for all tasks in **GLUE** using LoRA and MoLEx for comparison and report our results in Table 1. Across all metrics, higher numbers indicate better performance. We observe that across almost all tasks, MoLEx outperforms the baseline LoRA on both RoBERTa-base and RoBERTa-large, demonstrating the effectiveness and scalability of our method. A key advantage of MoLEx is its enhancement of model performance without any changes to the existing method or any increase in effective parameter count. Instead, it introduces a structural modification to the model's architecture, enabling the model to extract more information from the data, thereby leading to improved results.

3.2 Natual Language Generation

To further illustrate the versatility of our method on different language tasks, we evaluate MoLEx on the standard **E2E NLG Challenge** dataset introduced by (Novikova et al., 2017b) for training end-to-end, data-driven NLG systems. We fine-tune GPT-2 medium on E2E, following the set up of Li & Liang (2021), and report our results in Table 2. For all metrics, higher is better.

Compared with the baseline LoRA method, MoLEx outperforms significantly on 3 metrics with a remarkable increase on BLEU by 0.7. We further note that the standard deviations for MoLEx is generally lower than LoRA. This aligns with our analysis of MoLEx as an ensemble model, which is expected to have lower variance (Ganaie et al., 2022; Gupta et al., 2022), and improves the reliability of the model in language generation.

3.3 Zero-shot transfer learning

We assess the ability of LoRA and MoLEx to transfer knowledge across relatively similar tasks in a zero-shot transfer learning setup on GLUE using RoBERTa-base. In Table 3, we present an evaluation of MoLEx in comparison with the baseline LoRA method when fine-tuned on one task and evaluated on another without any additional training.

Table 3 suggests that MoLEx can generalize better to new data distributions compared to LoRA as across all evaluations, mixing layers consistently leads to significant improvements in zero-shot performance on new tasks. These results illustrate the ability of MoLEx to improve the model's transferability between different classification tasks, further validating our approach.

Table 3: Zero-shot evaluation of RoBERTa-base on several GLUE tasks, QNLI, RTE, MRPC, and QQP when fine-tuned with LoRA and our MoLEx (bold and shaded in gray) on different tasks.

Fine-tune on	**Evaluate on**							
	QNLI		RTE		MRPC		QQP	
	LoRA	**MoLEx**	LoRA	**MoLEx**	LoRA	**MoLEx**	LoRA	**MoLEx**
QNLI			$56.7_{\pm 1.1}$	$\mathbf{59.9}_{\pm \mathbf{1.3}}$	-	-	$63.2_{\pm .0}$	$\mathbf{65.7}_{\pm \mathbf{.0}}$
RTE	$56.1_{\pm .2}$	$\mathbf{58.5}_{\pm .2}$			-	-	-	-
MRPC	-	-	-	-			$65.7_{\pm .0}$	$\mathbf{67.9}_{\pm \mathbf{.0}}$
QQP	$50.5_{\pm .2}$	$\mathbf{56.2}_{\pm .2}$	-	-	$67.2_{\pm .4}$	$\mathbf{69.9}_{\pm \mathbf{.7}}$		

4 Empirical Analysis

We conduct additional experiments on robustness, efficiency, and an ablation study. Further, in Appendix C, we provide results on additional probing tasks for a linguistic analysis of the model.

4.1 Robustness

Though the models used in our experiments are non-linear, we expect that the theoretical robustness properties still hold and can be extended to practical situations. To verify this, we perform a simple experiment using MoLEx and LoRA in a RoBERTa-base model trained on 2 GLUE tasks as described in Section 3 and present the results in Table 4. For the tasks presented, we add random noise into the input data for evaluation and find that MoLEx is indeed more robust than the baseline LoRA model as it achieves a higher accuracy.

Table 4: Robustness (in accuracy) of RoBERTa-base on GLUE tasks, QNLI, and SST2 when fine-tuned with LoRA and MoLEx. Random noise is added to the input during evaluation to assess their robustness to ℓ_2-perturbations.

Method	QNLI (with added noise)	SST-2 (with added noise)
LoRA	$63.1_{\pm .2}$	$69.3_{\pm .1}$
MoLEx	$\mathbf{64.0}_{\pm \mathbf{.2}}$	$\mathbf{70.9}_{\pm \mathbf{.2}}$

4.2 Efficiency Analysis & Ablation Study

We provide a detailed efficiency analysis in Appendix E.4. There is only a marginal increase in computation time due to the additional gating function. Also, in Table 8, Appendix D, we conduct 3 GLUE tasks, CoLA, QQP, and SST-2 when using Top1 and Top2 routing. We observe that Top1 yields better results. Thus, we uses a Top1 routing for MoLEx.

5 Related Work

Parameter-Efficient Fine-Tuning (PEFT). The simplest solution of PEFT is to only update a small subset of weights (partial fine-tuning) (Li & Liang, 2021). Other methods that fine-tune a selected subset of parameters include BiTFiT (Zaken et al., 2021) and its extension using Neural Architecture Search (Lawton et al., 2023). A separate approach is to introduce extra trainable parameters into the model for adaptation. These include soft prompt-based tuning (Hambardzumyan et al., 2021; Lester et al., 2021; Liu et al., 2023; Zhang et al., 2023) and prefix-tuning (Li & Liang, 2021). Qi et al. (2022) suggests only training the gain and bias term of the LayerNorm in the model. In addition, adapter tuning (Houlsby et al., 2019) involves inserting adapter layers into a transformer layer. More efficient methods have also been proposed by (Lin et al., 2020; Pfeiffer et al., 2021) to reduce the number of adapter layers and by (Rücklé et al., 2021) to drop adapter layers.

6 Concluding Remarks

In this paper, we introduce a Mixture of Layer Experts (MoLEx), a novel approach that leverages layers as experts to facilitate the exchange of linguistic information and improve a model's fine-tuning and transfer knowledge ability. Orthogonal to current PEFT methods, we do not add in or modify any internal components in the model. Instead, we propose a structural change to the architecture of the model that can be effortlessly integrated with any PEFT method while maintaining the same number of effective parameters. We theoretically justify the robustness of MoLEx in a simplified model and provide empirical evidence for it. Our experiments demonstrate that MoLEx significantly improves performance across a range of downstream tasks, including the GLUE benchmark and the E2E Challenge, while incurring minimal additional computational overhead and scales well with model size. Additionally, its distinctive architectural design enables us to deepen our understanding of a model's internal natural language processing. A limitation of our work is that our robustness guarantee is only for deep linear models. Extending this result to the case of deep nonlinear models, as well as exploring layer mixing across different models, is an interesting direction to pursue. We leave these exciting research ideas as future work.

Reproducibility Statement. Source code for our experiments are provided in the supplementary material. We provide the full details of our experimental setup – including datasets, model specification, train regime, and evaluation protocol – for all experiments Section 3 and Appendix B. All datasets are publicly available.

Ethics Statement. Given the nature of the work, we do not foresee any negative societal and ethical impacts of our work.

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Supplement to "MoLEx: Mixture of Layer Experts for Finetuning with Sparse Upcycling"

Table of Contents

A Proofs

A.1 Proof of Theorem 1

We restate the theorem below for convenience.

Theorem 1 (Linear ensembles are more robust than base models)**.** *For a data point* $(\boldsymbol{x}, y) \in (\boldsymbol{X}, \boldsymbol{Y})$*, and* M *linear base models,* $f_j(\boldsymbol{x}) = \boldsymbol{W}_j^\top \boldsymbol{x}$ *such that* $\forall y_i$ *and* $\boldsymbol{W}_j$*,*

1. $\frac{1}{\epsilon}(\boldsymbol{e}_y - \boldsymbol{e}_{y_i})^\top f_j(\boldsymbol{x}) \geq \|\boldsymbol{W}_j(\boldsymbol{e}_y - \boldsymbol{e}_{y_i})\|_2$
2. $\boldsymbol{W}_j(\boldsymbol{e}_y - \boldsymbol{e}_{y_i})$ *are not colinear,*

an ensemble classifier model, with a classification head H*,* $F_M = H(\sum_{j=0}^{M-1} c_j f_j)$ *is* ϵ'*-robust at* $\boldsymbol{x}$ *with* $\epsilon' > \epsilon$*.*

Proof. For a linear ensemble classifier, F_M to be robust, from Lemma 1, we require that $\forall y_i \in [C], y_i \neq y, \min_{\tilde{\boldsymbol{x}} \in B(\boldsymbol{x}, \epsilon)} \sum_{j=0}^{M-1} c_j (f_j(\tilde{\boldsymbol{x}})_y - f_j(\tilde{\boldsymbol{x}})_{y_i}) \geq 0$. Expanding this, with $\boldsymbol{e}_y$ being the

standard basis vector with 1 in the y-th position,

$$\begin{aligned}
&\min_{\tilde{\boldsymbol{x}} \in B(\boldsymbol{x}, \epsilon)} \sum_{j=0}^{M-1} c_j (f_j(\tilde{\boldsymbol{x}})_y - f_j(\tilde{\boldsymbol{x}})_{y_i}) \\
&= \min_{\tilde{\boldsymbol{x}} \in B(\boldsymbol{x}, \epsilon)} \sum_{j=0}^{M-1} c_j (\boldsymbol{e}_y - \boldsymbol{e}_{y_i})^\top f_j(\tilde{\boldsymbol{x}}) \\
&= \min_{\tilde{\boldsymbol{x}} \in B(\boldsymbol{x}, \epsilon)} \sum_{j=0}^{M-1} c_j (\boldsymbol{e}_y - \boldsymbol{e}_{y_i})^\top (\boldsymbol{W}_j^\top \boldsymbol{x} + \boldsymbol{W}_j^\top (\tilde{\boldsymbol{x}} - \boldsymbol{x})) \\
&= \sum_{j=0}^{M-1} c_j (\boldsymbol{e}_y - \boldsymbol{e}_{y_i})^\top f_j(\boldsymbol{x}) + \min_{\tilde{\boldsymbol{x}} \in B(\boldsymbol{x}, \epsilon)} (\boldsymbol{e}_y - \boldsymbol{e}_{y_i})^\top (\sum_{j=0}^{M-1} c_j \boldsymbol{W}_j^\top)(\tilde{\boldsymbol{x}} - \boldsymbol{x}) \\
&= \sum_{j=0}^{M-1} c_j (\boldsymbol{e}_y - \boldsymbol{e}_{y_i})^\top f_j(\boldsymbol{x}) + \min_{\tilde{\boldsymbol{x}} \in B(\boldsymbol{x}, \epsilon)} (\bar{\boldsymbol{W}} (\boldsymbol{e}_y - \boldsymbol{e}_{y_i}))^\top (\tilde{\boldsymbol{x}} - \boldsymbol{x}) \\
&\geq \sum_{j=0}^{M-1} c_j (\boldsymbol{e}_y - \boldsymbol{e}_{y_i})^\top f_j(\boldsymbol{x}) - \epsilon \|\bar{\boldsymbol{W}} (\boldsymbol{e}_y - \boldsymbol{e}_{y_i})\|_2
\end{aligned}$$

where the last inequality holds by the Cauchy-Schwartz inequality and we denote $\bar{\boldsymbol{W}}^\top := (\sum_{j=0}^{M-1} c_j f_j) = \sum_{j=0}^{M-1} c_j \boldsymbol{W}_j^\top$ to represent our ensemble function. Hence, if the following holds,

$$\sum_{j=0}^{M-1} c_j (\boldsymbol{e}_y - \boldsymbol{e}_{y_i})^\top f_j(\boldsymbol{x}) - \epsilon \|\bar{\boldsymbol{W}} (\boldsymbol{e}_y - \boldsymbol{e}_{y_i})\|_2 \geq 0 \iff \frac{1}{\epsilon} \sum_{j=0}^{M-1} c_j (\boldsymbol{e}_y - \boldsymbol{e}_{y_i})^\top f_j(\boldsymbol{x}) \geq \|\bar{\boldsymbol{W}} (\boldsymbol{e}_y - \boldsymbol{e}_{y_i})\|_2,$$

then F_M is robust. Since, in our assumption 2, $\forall y_i$ and $\boldsymbol{W}_j$, $\boldsymbol{W}_j(\boldsymbol{e}_y - \boldsymbol{e}_{y_i})$ are not colinear, from triangle inequality and assumption 1, we have

$$\begin{aligned}
\|\bar{\boldsymbol{W}} (\boldsymbol{e}_y - \boldsymbol{e}_{y_i})\|_2 = \| \sum_{j=0}^{M-1} c_j \boldsymbol{W}_j (\boldsymbol{e}_y - \boldsymbol{e}_{y_i})\|_2 &< \sum_{j=0}^{M-1} c_j \|\boldsymbol{W}_j (\boldsymbol{e}_y - \boldsymbol{e}_{y_i})\|_2 \\
&\leq \frac{1}{\epsilon} \sum_{j=0}^{M-1} c_j (\boldsymbol{e}_y - \boldsymbol{e}_{y_i})^\top f_j(\boldsymbol{x})
\end{aligned}$$

As the inequality holds strictly, we can always find an $\epsilon' > \epsilon$ such that the inequality still holds. Hence, F_M is ϵ'-robust. □

A.2 Proof of Corollary 1

We restate the corollary below for convenience.

Corollary 1 (Sufficient conditions for ϵ-robustness)**.** *For a data point $(\boldsymbol{x}, y) \in (\boldsymbol{X}, \boldsymbol{Y})$, if a classifier model $F = H(f)$ with prediction function, $f(\boldsymbol{x}) = \boldsymbol{W}^\top \boldsymbol{x}$ satisfies $\frac{1}{\epsilon}(\boldsymbol{e}_y - \boldsymbol{e}_{y_i})^\top f(\boldsymbol{x}) \geq \|\boldsymbol{W}(\boldsymbol{e}_y - \boldsymbol{e}_{y_i})\|_2$, then F is ϵ-robust at $\boldsymbol{x}$.*

Proof. This result follows directly from the proof of Theorem 1, with $M = 1$. □

A.3 Proof of Corollary 2

We restate the corollary below for convenience.

Corollary 2 (Linear MoLEx is more robust than sequential model)**.** *If the base models of MoLEx $f_j = u_{i_t} \circ u_{i_{t-1}} \circ \ldots \circ u_{i_0}$ satisfies assumptions 1 and 2 in Theorem 1 above, then $\boldsymbol{z}_{t+1} = \sum_{j=0}^{n_t} c_j f_j$ is more robust than $f_{[0:t]}$.*

Proof. In each layer t of MoLEx, as one layer expert is always fixed to be the original pre-trained layer u_t, the sequential model, $f_{[0:t]}$ will always be one of the base models. Then, by Corollary 1 and assumption 1, $f_{[0:t]}$ is ϵ-robust. The rest of the corollary follows as a consequence of Theorem 1 as $\boldsymbol{z}_{t+1}$ will be ϵ'-robust with $\epsilon' > \epsilon$. □

B Additional Experimental Details

B.1 Natural Language Understanding: GLUE

Tasks: CoLA (Warstadt et al., 2019) consists of sequences of words taken from books and journal articles on linguistic theory with labels to determine if they are grammatically acceptable or not. SST-2 (Socher et al., 2013) comprises of movie reviews and the task is to predict their sentiments as positive or negative. MRPC (Dolan & Brockett, 2005) is a corpus of pairs of sentences pulled from online news sources and annotated by humans whether they are semantically equivalent. The QQP[1] dataset was collated from the community question-answering website Quora. It contains question pairs and simlar to MRPC, the goal is to determine if they are labelled to be semantically equivalent. STS-B (Cer et al., 2017) is another sentence pair similarity task extracted from news headlines, video and image captions, and natural language inference data. However, it differs from the previous tasks in not using binary labels and instead each examples is accompanied by a similarity score from 1 to 5. MNLI (Williams et al., 2018) uses pairs of premise and hypothesis sentences that have been collected from ten different sources, including transcribed speech, fiction, and government reports. The objective is to predict whether the premise entails the hypothesis (entailment), contradicts the hypothesis (contradiction), or neither (neutral). QNLI (Rajpurkar et al., 2018) is a task to determine if the context sentence in a question-sentence pair contains the answer to the question. The sentences were taken from paragraphs in Wikipedia and the questions were annotated by humans. Lastly, we have RTE (Dagan et al., 2006; Bar-Haim et al., 2006; Giampiccolo et al., 2007; Bentivogli et al., 2009), a compilation of datasets from a series of annual textual entailment challenges. Similar to MNLI, the objective is to determine if the sentence pairs contain an entailment or not. The classes for contradiction and neutral as in MNLI are collapsed into a single non-entailment class.

Metrics: All tasks in GLUE are classification tasks, except for STS-B which is a regression task. Therefore, the metric reported for STS-B is the Pearson correlation coefficient as is standard practise. We report the overall accuracy for MNLI which includes both matched and mismatched data. These correspond to evaluations on pairs of sentences within the same domain or cross-domain respectively. On CoLA, we use the Matthews correlation coefficient (Matthews, 1975) for evaluation due to the unbalanced binary classification data. This metric ranges from -1 to 1, with 0 indicating random guessing. For all other tasks, we present their accuracy for evaluation. Across all metrics, a higher number reflects stronger performance.

Model: We use the pre-trained RoBERTa-base and RoBERTa-large model (Liu, 2019) from the HuggingFace Transformers library (Wolf et al., 2020) for evaluation on the GLUE task. RoBERTa is an optimized version of the original pre-training recipe proposed in BERT (Devlin et al., 2018). RoBERTa-base has 125M parameters with 12 layers, 12 attention heads and 768 hidden dimensions while RoBERTa-large has 355M parameters with 24 layers, 16 attention heads and 1024 hidden dimensions.

Implementation details: We follow the same fine-tuning set up as in the original LoRA (Hu et al., 2021) paper for all GLUE experiments using the their publicly available code `https://github.com/microsoft/LoRA`. We use the same setting for fine-tuning on the pre-trained model and from an MNLI checkpoint. For each task, we also optimize the hyperparameters of the gate used in deciding the layer experts to be used for mixing. These settings can be found in Table 5 and for all gates, we use the same optimizer, AdamW (Loshchilov, 2017), as the LoRA parameters with a learning rate of 0.1 and weight decay of 0.01. We report the mean and standard deviation over 5 random seeds for all results and the result for each run is taken from the best epoch.

While we employ batch routing in the mixture of layers, each token will have a different choice of layer to be routed to as every token is processed by the gate. In deciding the overall batch's decision, we use 2 different aggregates. The first is a majority-takes-all scheme where we route the batch to the layer which majority of tokens have chosen. The second is to use the maximum over the mean probability vector of all the tokens choices. These are referred to as Mode and Mean respectively under Batch Agg in the table. For gate types with suffix "Sig" we use a sigmoid activation before taking TopK values and the default is a softmax activation. For almost all gates, if they do not have an "Indv Gate", this means that we use the same gate for all layers to decide the mixing layers. On RTE and STS-B, we use individual gates, which means that each layer has its own linear gating function and mixing weights instead of sharing one between all the layers. For all tasks, if the mixing weights are fixed, we use $\alpha = 0.95$ as defined in Eqn. 4.

Table 5: Hyperparameter settings for LoRA and MoLEx on each GLUE task when fine-tuning RoBERTa-base and RoBERTa-large.

Method	Dataset	MNLI	SST-2	MRPC	CoLA	QNLI	QQP	RTE	STS-B
	Optimizer	AdamW							
	Warmup Ratio	0.06							
	LR Schedule	Linear							
RoBERTa-base LoRA	Batch Size	16	16	16	32	32	16	32	16
	# Epochs	30	60	30	80	25	25	80	40
	Learning Rate	5E-04	5E-04	4E-04	4E-04	4E-04	5E-04	5E-04	4E-04
	LoRA Config.	$r_q = r_v = 8$							
	LoRA α	8							
	Max Seq. Len.	512							
RoBERTa-base MoLEx gate	Gate Type	Cos-Sig	Cos	Linear	Linear	Cos	Cos-Sig	Linear	Linear
	Projection Dim	416	128	-	-	96	384	-	-
	Indv Gate	×	×	×	×	×	×	✓	✓
	Batch Agg	Mode	Mode	Mode	Mode	Mean	Mode	Mean	Mean
	Mixing Weights	Learn	Learn	Learn	Fix	Learn	Learn	Fix	Fix
	Load Balance	0.005	0.01	0.0	0.01	0.001	0.001	0.001	0.006
RoBERTa-large LoRA	Batch Size	4	4	4	4	4	4	8	8
	# Epochs	10	10	20	20	10	20	20	30
	Learning Rate	3E-04	4E-04	3E-04	2E-04	2E-04	3E-04	4E-04	2E-04
	LoRA Config.	$r_q = r_v = 8$							
	LoRA α	16							
	Max Seq. Len.	128	128	512	128	512	512	512	512
RoBERTa-large MoLEx gate	Gate Type	Cos	Cos	Linear	Linear	Cos	Cos-Sig	Linear	Linear
	Projection Dim	416	64	-	-	256	384	-	-
	Indv Gate	×	×	✓	×	×	×	✓	✓
	Batch Agg	Mode	Mode	Mode	Mode	Mean	Mode	Mode	Mode
	Mixing Weights	Fix	Fix	Fix	Fix	Fix	Learn	Fix	Fix
	Load Balance	0.0001	0.0	0.0001	0.01	0.001	0.001	0.0	0.0

B.2 Natural Language Generation: E2E

Dataset: The E2E NLG dataset approximately consists of more than 50,000 examples from the restaurant domain and there is a 76.5-8.5-15 split of the dataset into a training, validation and test set respectively. The E2E dataset is commonly used for the evaluation of data-to-text tasks and brings new challenges such as open vocabulary, complex syntactic structures and diverse discourse phenomena. Every data input consists of a meaning representation (MR) that includes a sequence of attribute-value pairs and a corresponding target, a natural language (NL) reference text.

Metrics: We report the same metrics as in (Novikova et al., 2017b), namely BLEU (Papineni et al., 2002), NIST (Doddington, 2002), METEOR (Lavie & Agarwal, 2007), ROUGE-L (Lin, 2004) and CIDEr (Vedantam et al., 2015). BLEU is a method to evaluate the quality of automated machine translations that scales the geometric mean of the precision scores of the n-grams in a generated text by an exponential brevity penalty factor. Similarly, NIST is based on BLEU with some slight changes. NIST uses weighted precision scores of the n-grams determined by how informative each of them are, instead of an equal weighting as in BLEU, and loosens the brevity penalty for small variations. METEOR evaluates the quality of the generated text at a segment level. It constructs a word alignment between strings and scores them using a parameterized harmonic mean of their unigram precision and recall. ROGUE-L is a metric that naturally captures sentence level structures by only awarding scores to in-sequence co-occurrences in the predicted and reference text. Lastly, CIDEr is a measure for how well the generated text matches the consensus of a set of reference image descriptors. It scores the frequency of n-grams in the generated text that occurs in the reference sentences and discounts n-grams that appear commonly across all images in the dataset.

Model: We use the pre-trained GPT-2 medium (Radford et al., 2019) from the HuggingFace Transformers library (Wolf et al., 2020) for evaluation on the E2E dataset. GPT-2 medium contains 355M parameters with 24 layers, 16 attention heads and 1,024 hidden dimensions.

Table 6: Hyperparameter settings for LoRA and MoLEx on the E2E NLG task when fine-tuning GPT-2 medium (M).

	Dataset	E2E
	Training	
GPT-2 M LoRA	Optimizer	AdamW
	Weight Decay	0.01
	Dropout Prob	0.1
	Batch Size	8
	# Epoch	5
	Warmup Steps	500
	Learning Rate Schedule	Linear
	Label Smooth	0.1
	Learning Rate	0.0002
	Adaptation	$r_q = r_v = 4$
	LoRA α	32
GPT-2 M MoLEx gate	Gate Type	Linear
	Layers with MoLEx	0 to 11 (inclusive)
	Indv Gate	$\times$
	Batch Agg	Mode
	Mixing Weights	Fixed
	Load Balance	0.01
	Inference	
	Beam Size	10
	Length Penalty	0.9
	No Repeat Ngram Size	4

Implementation details: We follow the same fine-tuning setup as in Li & Liang (2021) and LoRA (Hu et al., 2021) using their publicly available code `https://github.com/microsoft/LoRA`. We also optimize the hyperparameters of the gate used in deciding the layer experts to be used for mixing. These settings can be found in Table 6 and we use the same optimizer, AdamW (Loshchilov, 2017), as the LoRA parameters with a learning rate of 0.1 and weight decay of 0.01. We report the mean and standard deviation over 5 random seeds for all results and the result for each run is taken from the best epoch.

While we employ batch routing in MoLEx, each token will have a different choice of layer to be routed to as every token is processed by the gate. In deciding the overall batch's decision for GPT-2, we use a majority-takes-all scheme where we route the batch to the layer which majority of tokens have chosen (Mode). We use a linear gating function with a softmax activation and only implement MoLEx in the first 12 layers of the model. The mixing weights are fixed and we use a value of $\alpha = 0.95$ as defined in Eqn. 4. All layers share the same gate for routing.

C Additional Empirical Analysis Details

C.1 Probing Tasks

Language models, such as RoBERTa (Liu, 2019), attain impressive results on a multitude of NLP tasks that range in complexity, even with fine-tuning on a small subset of parameters (Zaken et al., 2021; Rücklé et al., 2021; Xu et al., 2023; Pfeiffer et al., 2021; Lin et al., 2020; Houlsby et al., 2019; Li & Liang, 2021). This suggests that the pre-trained base model already captures important linguistic properties of sentences that are capitalized upon during training on different tasks. At this junction, MoLEx with its unique feature of layer mixing can be leveraged to shed light on how the linguistic properties captured in the pre-trained base model can be combined for different downstream finetuning tasks. By piecing together the type of information mixed in each layer of MoLEx, we enhance our understanding of the language processing occurring in a RoBERTa model during fine-tuning and improve the interpretability of neural networks in NLP (Belinkov & Glass, 2019).

Table 7: Probing task performance (accuracy of a simple MLP classifier) for each layer of RoBERTa-base. Bolded numbers are the top 2 values within each task.

Layer	SentLen (Surface)	WC (Surface)	TreeD (Syntactic)	TopConst (Syntactic)	BShift (Syntactic)	Tense (Semantic)	SubjNum (Semantic)	ObjNum (Semantic)	SOMO (Semantic)	CoordInv (Semantic)
0	**91.48**	**4.10**	**32.00**	48.93	50.00	82.27	77.56	73.81	49.87	57.47
1	**87.99**	0.61	29.75	35.10	54.32	79.74	74.05	71.83	49.87	50.00
2	87.03	0.33	29.06	29.32	64.99	82.06	78.51	73.49	49.88	50.00
3	85.78	0.16	29.30	29.26	73.29	82.29	76.14	74.69	50.07	50.00
4	85.32	2.40	31.06	54.12	77.95	84.37	77.33	73.67	59.21	57.69
5	84.15	1.97	**31.83**	57.57	81.82	85.35	80.80	78.53	62.74	60.05
6	82.17	2.91	31.81	**59.90**	82.41	85.61	81.22	**81.48**	63.67	61.97
7	79.75	0.68	28.99	48.44	82.34	84.79	80.28	80.26	**64.94**	57.88
8	80.49	1.09	30.73	52.24	**83.56**	**86.81**	**81.65**	**80.92**	**65.00**	65.07
9	77.75	1.06	29.83	49.96	83.10	86.19	81.63	79.14	64.52	**66.28**
10	66.65	1.15	26.97	43.68	82.59	85.25	80.91	75.95	61.78	61.92
11	73.69	**18.25**	30.56	**60.26**	**85.25**	**87.55**	**82.92**	79.51	63.52	**66.62**

Probing (or diagonostic) tasks (Adi et al., 2016; Hupkes et al., 2018; Conneau et al., 2018) aid us in the discovery of linguistic features potentially encoded in a deep learning model. Specifically, in the hidden representations of the input in each layer. In order to understand these representations using a probe, an auxiliary classification task is set up where the representations are used as features to predict certain linguistic properties of interest. The better the performance of the classifier, the more likely that the layer's hidden embedding encodes for that particular property. Using the 10 probing tasks developed by (Conneau et al., 2018) and inspired by (Jawahar et al., 2019), who had done a similar analysis on BERT, we evaluate each layer of RoBERTa and present the results in Table 7.

In each tasks's dataset, there are 100K training sentences and 10K-sentence validation and test sets. All sets are equally balance among the target classes. These datasets were constructed by (Conneau et al., 2018) from the Toronto Book Corpus (Zhu, 2015; Paperno et al., 2016).

Surface Information: SentLen is a task to predict the length of a sentence, which is considered to be the number of words in the sentence. It is converted into a 6-way classification task by grouping sentence lengths into 6 equal-width bins. WC is a classification task with 1000 classes. Each class is a word and each input is a sentence that contains one and only one of the words within those classes. The task is to predict which word is contained within the input sentence.

Syntactic Information: BShift is a binary classification task where half the dataset has sentences intact and another half has sentences with 2 random adjacent words inverted. The goal is to predict if the sentence has a legal word order or if it has been inverted. TreeD assesses whether the hierarchical structure of sentences can be inferred from the hidden layer's embedding. The task is to determine the depth of the longest path from root to any leaf in the sentence, with possible depths ranging from 5 to 12. Hence, resulting in a 8-way classification task. TopConst is a 20-class task where 19 classes represent the most frequent top constituent sequence and the last class is for all the others. The classifier has to identify which sequence of top constituents immediately follow the input sentence node, which is illustrative of the latent syntactic structures captured by each layer's representation.

Semantic Information: The goal of the Tense task is to identify the tense of the main-clause verb in the input sentence. For the SubjNum and ObjNum tasks, both focus on the number of the subject and respectively, direct object, of the main clause. In the SOMO dataset, sentences are modified through the replacement of a random noun or verb with another in a challenging way. The bigrams containing these noun or verb replacements will have a comparable corpus frequency with the original, making the task all the more difficult. The last task, the CoordInv dataset comprises of sentences with pairs of coordinate clauses, of which some orders have been inverted. The classifier is meant to identify if the sentences are intact or inverted as a binary classification task.

C.2 Implementation Details

We use the SentEval toolkit (Conneau & Kiela, 2018), available publicly at `https://github.com/facebookresearch/SentEval`, and the same set up as (Jawahar et al., 2019) for our probe analysis. We send each of the datasets in the 10 probing tasks through the pre-trained RoBERTA-base model that we use for fine-tuning and extract the feature representations from each layer. Next, we train classifiers, that are simple MLPs with a sigmoid activation, on these features as input. We use the recommended hyperparameter search space of $\{50, 100, 200\}$ hidden units and

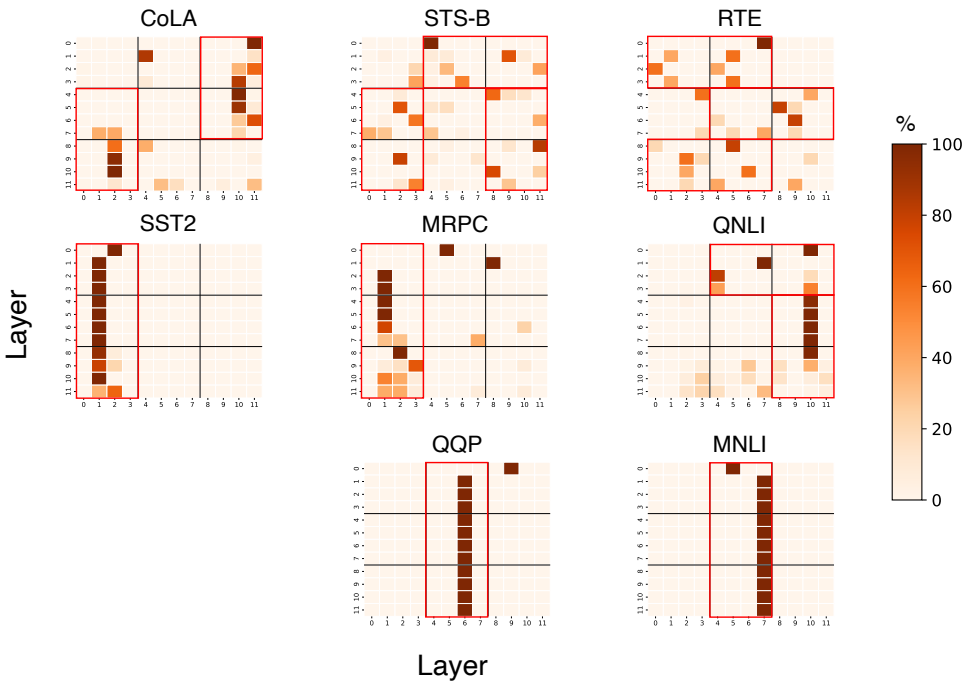

Figure 2: Plots of heat maps to visualize the percentage of time each layer expert is chosen at every layer of MoLEx when fine-tuning RoBERTa-base on all GLUE tasks. As one expert is fixed to be the original layer, the x-axis corresponds to the sequential layer while the y-axis corresponds to the layer experts. The darker a square is, the more often that layer is chosen by the gate during inference. For example, when fine-tuning on CoLA, layer 9 mixes with layer 2, 100% of the time. The grids are partitioned into thirds along the x-axis and y-axis for easy visualization of early, middle and later layers.

$\{0.0, 0.1, 0.2\}$ dropout for each task and an additional logistic regression model for the word content (WC) task as it contains 1,000 classes. We report the best classifier's results in Table 7.

C.3 Full results of Section 4

We present the full results of the different layer experts being mixed at inference time for all GLUE tasks when fine-tuning RoBERTa-base with MoLEx in Figure 2. Interestingly, for QQP and MNLI, there is a heavy emphasis on the middle layers. As the middle layers encode for syntactic information, MNLI as an inference task does require that structural information to understand the logical implications of the input. However, as QQP is a semantic similarity classification task, it is not obvious why it would require more syntactic information. Indeed, if we look at MRPC, a similar task on sentences instead of questions, it mainly chooses the earlier layers for surface level information which does make sense for sentence similarity. The main distinction between the 2 tasks is that the inputs are either questions or sentences. A plausible explanation is that questions require more syntactic information to be understood, resulting in our findings.

C.4 Linguistic Properties Captured by RoBERTa

In this section we will discuss the linguistic properties captured by RoBERTa as revealed through our probe analysis. We observe in Table 7 that across almost all probes, layer 11 does particularly well, suggesting that the last layer of the model encodes a considerable amount of general linguistic information. This is the main contrast to the probe analysis performed on BERT in (Jawahar et al., 2019) and could be an unintended consequence of the optimized training recipe in RoBERTa, highlighting how various training protocols can influence the learning outcomes of a model. It is also worth noting that all probes on RoBERTa, except for WC, performs roughly on the same scale as BERT while WC is much poorer in comparison, even with logistic regression. This could suggest that this surface level information is not relevant to the NLP in the model.

The remainder of the analysis corroborates with the probe analysis on BERT whereby the early layers contain superficial information, the middle layers, syntactic information and later layers, seman-

Table 8: Comparison of RoBERTa-base on GLUE tasks, CoLA, QQP and SST-2 when fine-tuned with MoLEx using Top-1 and Top-2 routing. We report accuracy for all tasks in the table below.

Method	CoLA	QQP	SST-2
MoLEx (Top1)	**64.8** $\pm.5$	**91.0** $\pm.0$	**95.4** $\pm.2$
MoLEx (Top2)	63.7 $\pm.4$	90.7 $\pm.0$	95.0 $\pm.3$

tic. This further aligns with the intuition that more complex structures within the data are revealed deeper in the model as it undergoes more processing as discussed in Section 2.2.

D Ablation Study

Table 8 compares results on 3 GLUE tasks, CoLA, QQP, and SST-2 when using Top1 and Top2 routing. We observe that Top1 yields more improvement. Thus, we use a Top1 routing for our MoLEx models.

E Additional Experimental Results and Efficency Analysis

E.1 Tables of comparison for NLU and NGL tasks with other adaptation methods

In this section, we present a comprehensive table of our results from Section 3 to compare LoRA and MoLEx with results from prior works of other adaptation methods for reference. We include results from a previous work that kept all layers except the last 2 frozen on GPT-2 (FT^{Top2}) (Li & Liang, 2021). Other methods that fine-tune a selected subset of parameters include BiTFiT (Zaken et al., 2021), where only the bias vectors are updated. Another method is prefix-layer tuning (PreLayer) that learns new activations after every Transformer layer. Qi et al. (2022) suggests only training the gain and bias term of the LayerNorm in the model. In addition, adapter tuning (Houlsby et al., 2019) involves inserting adapter layers into a transformer layer. This design is denoted as $\text{Adapter}^{\text{H}}$ in Table 10. More efficient methods have also been proposed by (Lin et al., 2020; Pfeiffer et al., 2021) to reduce the number of adapter layers ($\text{Adapter}^{\text{L}}$) and by (Rücklé et al., 2021) to drop adapter layers ($\text{Adapter}^{\text{D}}$).

E.2 Full parameter fine-tuning for RoBERTa

We conduct additional experiments for RoBERTa-base using full parameter fine-tuning on the GLUE benchmark. We present the results in Table 11 below. Our MoLEx model consistently outperforms the full parameter fine-tuning across all tasks. These findings further confirm MoLEx's adaptability to different models and training methods.

E.3 Fine-tuning Llama-3.2-1B using LoRA

We conduct additional experiments to fine-tune Llama-3.2-1B on the Alpaca dataset using LoRA. We use the publicly available repository `https://github.com/meta-llama/llama3` for our experiments and employ MoLEx to fine-tune the model in comparison with LoRA. As shown in Table 12, on this task with Llama-3.2-1B, MoLEx achieves better train and validation PPL than LoRA, demonstrating the effectiveness of MoLEx in large language models.

Further, we evaluate each model on the standard MMLU (Hendrycks et al., 2020), AGIEval English (Zhong et al., 2024), Hellaswag (Zellers et al., 2019), and ARC-Challenge dataset Clark et al. (2018) and report their results in Table 13. Consistent with our results on Alpaca, MoLEx improves over the naive LoRA model, confirming its advantage.

E.4 Detailed Efficiency Analysis on Llama-3.2-1B

While more resources are required during inference in MoLEx as compared to the naive PEFT model, these can be accelerated during inference time through parallization. In this section, we include a more detailed efficiency analysis when implementing MoLEx in Llama-3.2-1B and using LoRA for fine-tuning on the Alpaca dataset.

As computational efficiency refers to the amount of time required for a given step in a calculation, we maintain that MoLEx is as efficient as the original method used without MoLEx. While MoLEx almost doubles the overall computational load (flops), there is only a minimal increase in inference time due to parallelization of the forward computations through two layers. We present our analysis in the Table 14 for a more detailed comparison with naive PEFT models.

Table 9: RoBERTa-base (RoB_{base}) and RoBERTa-large (RoB_{large}) fine-tuned on the popular GLUE benchmark with different adaptations methods. MoLEx (bold and shaded in gray) is our proposed method in combination with LoRA. Hence, we use LoRA as our baseline and only reproduce results for LoRA in the table. An * indicates numbers published in previous work. For all tasks, we report accuracy except for Matthew's correlation for CoLA, Pearson correlation for STS-B, the overall (matched and mismatched) accuracy for MNLI. The average stated for models fine-tuned from the best MNLI checkpoint is the average of all tasks with results for MRPC, RTE and STS-B from the pre-trained RoBERTa checkpoint replaced by those from the MNLI checkpoint. Across almost all tasks, MoLEx surpasses the baseline LoRA on both both RoBERTa-base and RoBERTa-large, establishing its effectiveness and scalability.

Model & Method	# Trainable Parameters	MNLI	SST-2	MRPC	CoLA	QNLI	QQP	RTE	STS-B	Avg.
Results published in prior works for reference										
RoB_{base} (FT)*	125.0M	87.6	94.8	90.2	63.6	92.8	91.9	78.7	91.2	86.4
RoB_{base} (BitFit)*	0.1M	84.7	93.7	92.7	62.0	91.8	84.0	81.5	90.8	85.2
RoB_{base} ($Adpt^D$)*	0.3M	$87.1_{\pm.0}$	$94.2_{\pm.1}$	$88.5_{\pm1.1}$	$60.8_{\pm.4}$	$93.1_{\pm0.1}$	$90.2_{\pm.0}$	$71.5_{\pm2.7}$	$89.7_{\pm.3}$	84.4
RoB_{base} ($Adpt^D$)*	0.9M	$87.3_{\pm.1}$	$94.7_{\pm.3}$	$88.4_{\pm.1}$	$62.6_{\pm.9}$	$93.0_{\pm.6}$	$90.6_{\pm.0}$	$75.9_{\pm2.2}$	$90.3_{\pm.1}$	85.4
Reproduced result from pre-trained RoBERTa checkpoint										
RoB_{base} (LoRA)	0.3M	$87.5_{\pm.2}$	95.0 $_{\pm.1}$	88.7 $_{\pm.3}$	$62.8_{\pm1.0}$	$93.2_{\pm.2}$	90.8 $_{\pm.0}$	$76.9_{\pm1.1}$	$90.8_{\pm.2}$	85.7
RoB_{base} (MoLEx)	0.309M	**$87.7_{\pm.2}$**	**95.4** $_{\pm.2}$	**$89.8_{\pm.2}$**	**$64.8_{\pm.5}$**	$93.2_{\pm.2}$	**$91.0_{\pm.0}$**	**$77.3_{\pm1.3}$**	**$91.0_{\pm.2}$**	**86.3**
RoB_{large} (LoRA)	0.8M	90.7 $_{\pm.1}$	$96.3_{\pm.2}$	$90.9_{\pm.4}$	$67.8_{\pm1.7}$	$94.8_{\pm.3}$	$91.5_{\pm.1}$	$86.5_{\pm.9}$	$91.9_{\pm.1}$	88.8
RoB_{large} (MoLEx)	0.8M	**90.9** $_{\pm.1}$	**$96.4_{\pm.2}$**	**$91.4_{\pm.7}$**	**$68.2_{\pm.2}$**	$94.8_{\pm.0}$	**$91.6_{\pm.1}$**	**$87.1_{\pm.9}$**	**$92.0_{\pm.2}$**	**89.1**
Reproduced result from fine-tuned MNLI checkpoint										
RoB_{base} (LoRA)	0.3M	-	-	89.7 $_{\pm.6}$	-	-	-	86.8 $_{\pm.2}$	91.3 $_{\pm.1}$	87.1
RoB_{base} (MoLEx)	0.3M	-	-	**91.1** $_{\pm.6}$	-	-	-	86.8 $_{\pm.2}$	91.3 $_{\pm.0}$	87.6

Table 10: GPT2 medium (M) fine-tuned on the standard E2E NLG Challenge benchmark. We reproduce the LoRA baseline and compare it to our proposed method MoLEx (bold and shaded in gray) using the usual BLEU, NIST, MET, ROUGE-L and CIDEr metrics, where higher numbers indicate better performance. An * indicates numbers published in previous work and we include them in the table for reference. MoLEx significantly outperforms the baseline LoRA on 3 metrics with lower standard deviations, verifying its advantage.

Model & Method	# Trainable Parameters	E2E NLG Challenge				
		BLEU	NIST	MET	ROUGE-L	CIDEr
Results published in prior works for reference						
GPT-2 M (FT)*	354.92M	68.2	8.62	46.2	71.0	2.47
GPT-2 M ($Adapter^L$)*	0.37M	66.3	8.41	45.0	69.8	2.40
GPT-2 M ($Adapter^L$)*	11.09M	68.9	8.71	46.1	71.3	2.47
GPT-2 M ($Adapter^H$)*	11.09M	$67.3_{\pm.6}$	$8.50_{\pm.07}$	$46.0_{\pm.2}$	$70.7_{\pm.2}$	$2.44_{\pm.01}$
GPT-2 M (FT^{Top2})*	25.19M	68.1	8.59	46.0	70.8	2.41
GPT-2 M (PreLayer)*	0.35M	69.7	8.81	46.1	71.4	2.49
Results reproduced for comparison						
GPT-2 M (LoRA)	0.35M	70.0 $_{\pm.5}$	$8.77_{\pm.05}$	**46.8** $_{\pm.2}$	$71.6_{\pm.3}$	$2.52_{\pm.01}$
GPT-2 M (MoLEx)	0.359M	**70.7** $_{\pm.4}$	**$8.87_{\pm.03}$**	$46.5_{\pm.09}$	**$71.8_{\pm.1}$**	$2.52_{\pm.01}$

Table 11: RoBERTa-base with full parameter fine-tuning and with MoLEx when fine-tuned on the GLUE benchmark. We report accuracy for all tasks except for, Pearson correlation for STS-B, Matthew's correlation for CoLA and the overall (matched and mismatched) accuracy for MNLI. A higher value reflects a better performance of the model.

Method	RTE	MRPC	STS-B	CoLA	MNLI	QNLI	SST-2	QQP	Ave.
RoBERTa (full parameter)	80.1	88.7	90.9	62.6	87.7	92.9	95.0	91.8	86.2
RoBERTa (MoLEx)	**80.9**	**89.5**	**91.1**	**63.3**	**87.8**	**93.1**	**95.1**	91.8	**86.6**

Table 12: Train and validation perplexity (PPL) when fine-tuning Llama-3.2-1B on Alpaca using LoRA and LoRA + MoLEx. Lower PPL is indicative of better performance.

Method	Train PPL (↓)	Validation PPL (↓)
LoRA	4.18	4.11
MoLEx	**4.05**	**4.02**

Table 13: Accuracy when evaluating Llama-3.2-1B on MMLU, AGIEval English, Hellaswag, and ARC-Challenge using LoRA and LoRA + MoLEx. A higher value is indicative of better performance.

Method	MMLU	AGIEval English	Hellaswag	ARC-Challenge
LoRA	30.42	19.16	47.14	36.69
MoLEx	**31.51**	**19.81**	**48.23**	**37.80**

Table 14: Efficiency analysis of Llama-3.2-1B fine-tuned using LoRA during inference on the Alpaca dataset with and without MoLEx implemented.

Method	Total Parameters	Trainable Parameters	Trainable Parameters (%)	Memory (MB)	Flop/ Sample	Sec/ Sample	Flop/ Sec	Min/ Epoch
LoRA	1,236,666,368	851,968	0.0689	10,442	12.329 T	0.506	24.366 T	4:59
MoLEx	1,236,699,152	884,752	0.0715	10,442	22.511 T	0.557	40.415 T	6:00