# **SOA: Strategic Operator Adaptation for Accelerating Joint In-Context Prompt Optimization**

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#### **Abstract**

Strategic prompt-tuning in Large Language Models (LLMs) presents a formidable challenge that requires substantial resources and expert human input. Prior research has treated the tuning of prompt instructions and few-shot examples as distinct and separate problems, resulting in sub-optimal performance. This work overcomes this limitation by introducing a joint prompt-tuning approach that optimizes both the instruction and examples simultaneously. However, formulating such an optimization in the discrete and high-dimensional space of natural language poses significant challenges in terms of convergence and computational efficiency. To address these challenges, we propose, SOA, a novel Strategic Operator Adaptation framework, designed to accelerate the optimization process by strategically employing a variety of operators to traverse the prompt space effectively for both zero-shot and few-shot scenarios. SOA features a quad-phased design that fully exploits the potential of each phase, alternating between global traversal and local optimization to strike a balance between exploration and exploitation in this complex space. By adaptively selecting the best operators for traversal and actively pruning less desirable candidates, SOA is able to identify the best combination of instructions and examples while minimizing inference costs. We have conducted a comprehensive evaluation across 35 benchmark tasks, and the results show that SOA significantly outperforms state-of-the-art baseline methods by a large margin, achieving an average task performance improvement of **35.47**% while significantly reducing computational costs by **58.67**% in the BIG-Bench-Hard tasks. [1](#page-0-0)

#### **1 Introduction**

Large Language Models (LLMs) have exhibited extraordinary performance across various domains and tasks [\(Bubeck et al., 2023;](#page-10-0) [Yang et al., 2023b\)](#page-12-0), largely owing to their remarkable ability of in-context learning (ICL). Prompt engineering seeks to craft effective prompts that unleash the complete capabilities of LLMs. It is becoming an increasingly popular option for quickly adapting LLMs for downstream tasks due to its compatibility with black-box APIs (e.g., GPT-4 [\(OpenAI, 2023\)](#page-12-1) and PaLM 2 [\(Chowdhery et al.,](#page-11-0) [2022\)](#page-11-0)), and its cost-effectiveness compared to the conventional fine-tuning paradigm. The two most typical prompting strategies are *zero-shot prompting* which contains a task instruction and a query question, and *few-shot prompting* which includes additional illustrative examples. A good prompt design can substantially improve LLM's performance [\(Zhu et al., 2023\)](#page-13-0); however, manual prompt tuning and selection is a heavily *time-consuming* process that requires significant human effort and expert knowledge.

Automating prompt tuning is a non-trivial optimization task that involves discrete variables and complex high-dimensional spaces [\(Zhou et al., 2023\)](#page-13-1). Existing studies treat the tuning of prompt instruction and in-context examples as separate tasks: one line of research [\(Pryzant et al., 2023;](#page-12-2) [Chen et al., 2023;](#page-11-1) [Yang et al.,](#page-12-3) [2023a;](#page-12-3) [Guo et al., 2023\)](#page-11-2) takes the zero-shot prompting approach [\(Kojima et al., 2022\)](#page-11-3) to focus on *tuning a short instruction* that comprises one or few sentences; while the other line of work [\(Liu et al., 2021;](#page-11-4) [Lu](#page-11-5) [et al., 2021;](#page-11-5) [2022;](#page-11-6) [Zhang et al., 2022b;](#page-13-2) [An et al., 2023\)](#page-10-1) emphasizes more the importance of few-shot examples [\(Brown et al., 2020\)](#page-10-2) and seeks to *selecting the best set of examples* from a pre-defined dataset given a *fixed*

<span id="page-0-0"></span><sup>&</sup>lt;sup>1</sup>The source code and datasets are ready to be publicly available for research purposes.

instruction. Although such treatment reduces the problem complexity, it overlooks the significance of the interplay between instruction and in-context examples, resulting in *sub-optimal* performance [\(Hsieh et al.,](#page-11-7) [2023\)](#page-11-7).

In this work, we tackle two important challenges of past prompt-tuning strategies: (i) how to design an automatic pipeline that effectively traverses the high-dimensional joint space of instructions and examples, steering clear of local minima and ensuring continuous performance enhancement? (ii) what strategies can be employed to accelerate joint prompt tuning, enabling fast convergence with a reasonable level of computational cost?

We first introduce a joint prompt-tuning problem that simultaneously optimizes the prompt instruction and examples as a whole. As illustrated in Figure [1,](#page-1-0) our formulation does not impose any restrictions or assumptions on the style (zero-shot or few-shot) of the prompt, thereby unlocking the full potential of prompt traversal in contrast to previous instructiononly optimization methods [\(Zhou et al., 2023;](#page-13-1) [Pryzant et al., 2023;](#page-12-2) [Chen et al., 2023;](#page-11-1) [Guo](#page-11-2) [et al., 2023;](#page-11-2) [Fernando et al., 2023\)](#page-11-8), Notably,

<span id="page-1-0"></span>

Figure 1: An illustrative example of the joint prompt-tuning of instruction and examples, which shows better performance than instruction-only optimization.

our formulation not only enables innovative instruction exploration but is also capable of producing novel examples to enhance the generalizability of LLMs. Consequently, our optimal prompt is highly adaptive and flexible to any style from a simple zero-shot instruction-only prompt to an elaborative few-shot prompt with detailed examples, depending on the specific task at hand.

We then propose a novel Strategic Operator Adaptation (SOA) framework aimed at accelerating joint prompt optimization in high-dimensional spaces while minimizing inference costs. SOA introduces a quad-phased design that fully excavates all potentials of each phase and alternates between global traversal and local optimization, striking an optimal balance between exploration and exploitation within the challenging high-dimensional space. This is accomplished by thoroughly analyzing a suite of LLM operators to pinpoint their unique strengths and features. By adaptively choosing the best operators for traversal and actively pruning undesired candidates, SOA can achieve optimal performance while accelerating convergence speed. Additionally, we integrate two innovative designs to enhance the performance and efficiency of SOA. Firstly, we introduce a task-aware similarity metric based on performance-based vectors and hamming distance, proving more effective than traditional lexical similarity metrics. Secondly, we implement adaptive phase stop criteria that ensure maximum performance improvement with the current operator before transitioning to the next, optimizing the overall framework efficiency.

We conduct an extensive evaluation on a total number of 35 benchmark tasks and empirically show that SOA demonstrates substantial improvements compared to state-of-the-art (SOTA) methods, including *APE* [\(Zhou](#page-13-1) [et al., 2023\)](#page-13-1), *APO* [\(Pryzant et al., 2023\)](#page-12-2), *OPRO* [\(Yang et al., 2023a\)](#page-12-3), *PromptBreeder* [\(Fernando et al., 2023\)](#page-11-8), *EvoPrompt* [\(Guo et al., 2023\)](#page-11-2), and *AELP* [\(Hsieh et al., 2023\)](#page-11-7), and these advancements are achieved with the lowest computational cost among all baselines. For harder tasks like BBH, SOA introduces an average of **35.47%** task accuracy improvement while reducing **58.67%** of inference costs compared to SOTA methods.

# **2 Problem Description**

Considering the task  $\mathcal T$  specified by a dataset  $\mathcal D = (\mathcal Q, \mathcal A)$  of input/output pairs, the LLM  $\mathcal L$  produces the corresponding output A via prompting with the concatenation of prompt P and a given input Q, i.e.,  $[\mathcal{P};\mathcal{Q}]$ .



Global Optima & Local Optima <sup>o</sup> In-Context Prompt

Figure 2: SOA framework aims at surfacing the globally optimal in-context prompt (instruction and example combination) by iteratively traversing the high-dimensional discrete space from a pool of candidates and pruning unpromising candidates along the process. SOA realizes strategic traversal by introducing a dual exploration-exploitation strategy, i.e., "global exploration"  $\rightarrow$  "local exploitation"  $\rightarrow$  "global exploration"  $\rightarrow$ "local exploitation" where operators are applied strategically during phases and transitions between phases are determined adaptively at run time. SOA achieves strategic pruning by employing a greedy-based strategy looking at the candidate's performance.

The objective of prompt optimization is to design the best natural language prompt  $\mathcal{P}^*$  that maximizes the performance of  $\mathcal L$  on  $\mathcal T$ .

Typically, an ideal prompt  $P$  consists of *instruction*, denoted by  $I$  and *examples* denoted by  $E$  as in-context learning (ICL) demonstrations. Our goal of joint prompt optimization is to search for the optimal prompt  $\mathcal{P}_{(\mathcal{I},\mathcal{E})}^*$  given  $\mathcal{L}$  that maximizes the performance towards a performance metric function  $\mathcal{F}$  (e.g., accuracy). This can be formally defined as the following optimization problem:

<span id="page-2-0"></span>
$$
\mathcal{P}_{(\mathcal{I},\mathcal{E})}^* = \underset{\mathcal{P}_{(\mathcal{I},\mathcal{E})} \in \mathcal{X}}{\arg \max} \mathbb{E}_{(\mathcal{Q},\mathcal{A})} \left[ \mathcal{F}(\mathcal{P}_{(\mathcal{I},\mathcal{E})};\mathcal{Q},\mathcal{A}) \mid \mathcal{L} \right],
$$
\n(1)

where  $\mathcal X$  denotes the sample space for a natural language prompt, a discrete and intractable space of arbitrarily large dimension, which makes the optimization problem in Eq. [1](#page-2-0) extremely difficult.

#### **3 Proposed Methodology: Strategic Operator Adaptation (SOA)**

We propose a novel framework, SOA, that leverages a variety of operators to traverse the prompt space for both zero-shot and few-shot to surface the best instruction and examples combination. By adaptively choosing the best operators for traversal and actively pruning undesired candidates, SOA can achieve optimal performance while accelerating convergence speed.

SOA adaptively switches between two distinct traversal strategies to balance speed and performance: (1) *Exploration*, where a specific subset of operators are leveraged for a *global* search to broadly explore the entire solution space and prevent entrapment in locally optimal solutions; (2) *Exploitation*, which involves the use of another set of operators for local search to expedite convergence and improve efficiency. Instead of blindly using a fixed set of operators following a pre-defined sequence, or randomly selecting operators, SOA aims to organize multiple operators adaptively and strategically. The application of the optimal operator at the right time, combined with active greedy-based pruning, ultimately leads to accelerated performance in both task accuracy and convergence speed.

#### **3.1 Operator Elaboration**

Following the insight of leveraging global search and local search, we introduce five operators that can be categorized as global operators and local operators. The three *global* operators are:

- **Lamarckian Operator** is a reverse-engineering operator O*<sup>L</sup>* that passes input-output pairs to an LLM agent and asks the agent to "reverse-engineer" the instruction.
- **Estimation of Distribution Operator (EDA)** is a function operator  $\mathcal{O}_E$  that takes in a group of candidates and inquires an LLM agent to output a new candidate by studying the input group. If the input group is chosen by prioritizing distinctiveness, we call it  $EDA + Index (EDA+I)$ .
- **Crossover Operator (CR)** is a function operator  $\mathcal{O}_C$  that takes two parents and asks an LLM agent to generate a new candidate mixing the traits of both parents. If the parents are chosen by prioritizing distinctiveness between them, we call it Crossover  $+$  Distinct  $(CR + D)$ .

The two *local* operators are:

- **Feedback Operator** is a function operator  $\mathcal{O}_F$  that utilizes two LLM agents.  $\mathcal{O}_F$  first passes in inputoutput pairs of tasks where an existing candidate makes mistakes to an "Examiner" agent, whose task is to examine the places of mistakes and provide remediation strategies. It then uses an "Improver" agent that takes the remediation strategies and applies them to the existing candidate to generate a new candidate.
- **Semantic Operator** is a function operator  $\mathcal{O}_S$  that takes in an existing candidate, and modifies the candidate lexically while preserving its semantic meaning.

To better harness the power of these operators, we compare them along the following five features that are critical to our exploration-exploitation strategy in terms of performance and efficiency:

- **Add or remove examples?** This examines whether an operator can add or remove few-shot examples, to traverse the entire prompt space of both zero-shot and few-shot.
- **Probability of improvement.** This evaluates the probability (successful rate) of an operator that brings performance improvement (gain) after iterations. The higher, the better.
- **Convergence speed.** This metric evaluates how fast (in terms of iterations) an operator needs to traverse to the current candidate's local minimum solution.
- **Two or more parents?** This indicates whether an operator needs two or more parents, which has the potential to combine traits from diverse ancestor lines, enhancing global exploration capability.
- **Inference cost per operation.** This is the number of inference calls needed to perform a specific operator acted by an LLM agent.

<span id="page-3-0"></span>Table 1: Elaborated feature analysis of operators. The number of black dots (•) represents a relative comparison among operators in terms of performance gain, convergence, and computational cost.



We conducted a series of experiments (ran each operator 100 times based on 4 different initialization settings) to assess the performance of each operator regarding the five features, aiming at obtaining a comprehensive understanding of the inherent strengths and weaknesses of each operator. This allows us to select effective operators to find optimal solutions in an accelerated manner. As shown in Table [1,](#page-3-0) we observe that the Lamarckian operator is a crucial operator that introduces diverse samples, enabling the addition of examples for global initialization. The feedback operator leads to faster convergence (four •) for exploitation and facilitates the addition or removal of examples but it requires two API/inference calls (two  $\bullet$ ), higher than the other operators (one •). EDA and Crossover operators share similar characteristics that indicate a higher probability of improvement (four  $\bullet$ ) than the semantic operator (three  $\bullet$ ) and feedback operator (two  $\bullet$ ) in exploring the global space. For a more in-depth discussion on operators, please refer to Appendix [C.1](#page-16-0) and [C.2.](#page-20-0)

### **3.2 SOA Framework**

#### **3.2.1 Phase 0: Global Initialization**

Our objective is to create diverse candidates as the initial pool to explore the vast joint space of instruction and example. We provide two types of initialization based on the availability of data (*input/output pair*) and human expert knowledge (*prompt example*).

- **Reverse Engineer from input/output pairs.** Given a set of input/output pairs *S* =  $\{(Q_1, A_1), ..., (Q_m, A_m)\}\$ from the training set  $\mathcal{D}_{\text{train}}$  for the task  $\mathcal{T}$ , we define an LLM agent to apply Lamarckian Operator O*<sup>L</sup>* to *reverse engineer* the prompt from provided demonstrating pairs.
- **Human expert prompt example.** This way allows humans to jump-start the tuning process by incorporating prior knowledge. We also perform the semantic operator  $\mathcal{O}_S$  to enhance the diversity of the initial pool.

#### **3.2.2 Phase 1: Local Feedback Operation**

While an initial phase (Phase 0) may result in a diverse pool, each candidate could still be distant from its local optimal solution. We want to arrive at the local optimal to exhaust the potential of the candidates. To address this, we employ the Feedback Operator  $\mathcal{O}_F$  to expedite each candidate's convergence towards their local minimums, leveraging the "gradient" information. This involves the introduction of an LLM *Examiner*, which scrutinizes instances where the current candidate falls short, and subsequently offers improvement guidance. Such information is taken as the feedback gradient and is further utilized by an LLM *Improver*, to generate new candidates by local exploitation. These new candidates contain global information inherited from the previous phase and can thus be regarded as better initialization for the next optimization phase.

#### **3.2.3 Phase 2: Global Evolution Operation**

Phase 1 provides a more refined set of candidates, while some of them might be stuck in local optima. To address this issue, we prioritize exploration rather than exploitation in Phase 2, which helps to escape from these restricted localities by conducting a global search. We leverage LLM agents that are inspired by genetic evolution, specifically EDA (EDA-I) operators  $\mathcal{O}_E$  and CR (CR-D) operators  $\mathcal{O}_C$  to facilitate the increased interaction of genetic information among candidates on a larger global scale. Rather than employing cosine similarity as distance metrics, we adopt the Hamming distance (see more discussions in Section [3.3\)](#page-4-0) for calculating similarity on performance-based vectors such that Phase 2 can promote greater diversity during iteration.

#### **3.2.4 Phase 3: Local Semantic Operation**

Upon completing Phase 2's exploration, Phase 3 employs local exploitation to hasten the "last mile" of convergence. As the concluding phase of SOA, the performance of the pool is notably optimized at this stage relative to earlier phases. Consequently, the Semantic operator  $\mathcal{O}_S$  is selected to expedite more cost-effective exploitation of the candidates. Finally, we identify the best candidate as our ultimate optimal prompt and assess its performance on the testing dataset  $\mathcal{D}_{\text{test}}$ . The workflow of SOA framework is shown in Algorithm [1.](#page-5-0)

#### <span id="page-4-0"></span>**3.3 SOA Design Schemes**

Within the SOA framework, we propose two novel design schemes to improve performance and efficiency.

#### <span id="page-5-0"></span>**Algorithm 1** SOA for Accelerating Joint In-Context Prompt Optimization

- 1: **requirements**: size of pool *n*, a dev set  $\mathcal{D}_{dev}$ , score function  $\mathcal{F}$  on the base LLM  $\mathcal{L}$ , phase improvement *t* and threshold  $t^*$  and minimum run time for phases  $\mathcal{K}_i$ , designed operators  $\mathcal{O}_L$ ,  $\mathcal{O}_F$ ,  $\mathcal{O}_E$ ,  $\mathcal{O}_C$  and  $\mathcal{O}_S$
- 2: **initialization**: generate diverse initial prompts  $\mathcal{P}^0 = \{p_1^0, ..., p_n^0\}$  by  $\mathcal{O}_l$  with input/output pairs or  $\mathcal{O}_s$  with existing prompt, and evaluate initial scores  $S^0 \leftarrow \{s_i^0 = \mathcal{F}(p_i^0) \}$  $//$  Phase 0 3: **while**  $t < t^*$  or  $k \leq \mathcal{K}_1$  do or  $k \leq \mathcal{K}_1$  **do** // Phase 1
- 4: *Local Feedback Operation:* generate new prompts by feedback operator,  $\mathcal{P}_t \leftarrow \mathcal{O}_f(\mathcal{P}^0)$ , evaluate  $\mathcal{S}_t \leftarrow$  $\mathcal{F}(\mathcal{P}^0, \mathcal{D}_{\text{dev}})$ , and update the pool  $\mathcal{P}^1 \leftarrow {\{\mathcal{P}_t, \mathcal{P}^0\}}$ , and score set  $\mathcal{S}^1 \leftarrow {\{\mathcal{S}_t, \mathcal{S}^0\}}$

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5: while t < t^* or k \le K_2 do \hspace{1cm} // Phase 2
```
- 6: *Global Evolution Operation:* select input prompts from the current pool,  $\{p_{r_1},...,p_{r_k}\} \in \mathcal{P}^1$ , generate a new prompt by performing EDA operators  $p_t \leftarrow \mathcal{O}_e(p_{r_1},...,p_{r_k})$  or crossover operators  $p_t \leftarrow \mathcal{O}_c(p_{r_1},...,p_{r_k})$ , evaluate on  $\mathcal{D}_{\text{dev}}$ ,  $s_t \leftarrow \mathcal{F}(p_t, \mathcal{D}_{\text{dev}})$ , and update  $\mathcal{P}^2 \leftarrow {\{\mathcal{P}^1, p_t\}}$  and  $\mathcal{S}^2 \leftarrow {\{\mathcal{S}^1, s_t\}}$ 7: while  $t < t^*$  or  $k \le K_3$  do  $\hspace{1cm}$  // Phase 3
- 
- 8: *Local Semantic Operation:* generate new prompts by the semantic operator  $\mathcal{P}_t^* \leftarrow \mathcal{O}_s(\mathcal{P}^2)$ , evaluate  $\mathcal{S}_t^* \leftarrow \mathcal{F}(\mathcal{P}^2, \mathcal{D}_{\text{dev}})$ , and update  $\mathcal{P}^3 \leftarrow {\{\mathcal{P}_t^*, \mathcal{P}^2\}}$ , and  $\mathcal{S}^3 \leftarrow {\{\mathcal{S}_t^*, \mathcal{S}^2\}}$
- 9: **return** the optimal prompt  $p^*$ , from the final pool  $\mathcal{P}^3$ :  $p^* \leftarrow \arg \max_{p \in \mathcal{P}^3} \mathcal{F}(p, \mathcal{D}_{\text{dev}})$

*Design 1: Performance vector with Hamming distance.* Operators like EDA and Crossover function optimally when parents exhibit distinct attributes. In terms of evaluating similarity scores, we adhere to the principle that similarity should be gauged based on the performance of the prompts rather than their linguistic or semantic similarities. Inspired by this intuition, we propose to construct candidate vectors based on individual performance on the evaluation dataset, named "performance vectors". To exemplify, in an evaluation dataset comprising five elements, a candidate answering the first three queries correctly and the final two incorrectly would feature a vector representation of [1*,* 1*,* 1*,* 0*,* 0].

Rather than calculating the cosine similarity of embedding space, we propose to compute candidate similarity scores by *Hamming distance*, which calculates the distance between two vectors of equal length by examining the number of positions at which the corresponding symbols are different. This way ensures that one candidate is more likely to be paired with a candidate that does not contain the same mistakes, and thereby generates a diverse pool with a more diverse set of genetic information.

*Design 2: Adaptive Phase Stop Criteria.* To ensure that each operation phase is fully conducted before we transition to the next, the decision to move to the next phase is made adaptively based on two primary criteria.

- **Performance Gain.** If no performance gain manifests after implementing the operators in a particular phase, it's indicative that the candidate has been thoroughly optimized by the operators. Consequently, we transition to the next phase.
- **Operator-specific Tolerance.** As operators inherently vary, for more localized operators, e.g., the feedback operator, which has high improvement probabilities, if no performance gain is perceived, it indicates applying the operator for another iteration will unlikely bring additional benefits. However, global operators might have low initial improvement probabilities but are capable of accessing broader branches worth exploring. Therefore, we should be more patient by assigning greater *tolerance*, which will run them at least for a pre-defined time even without immediate performance improvement. More details about the stop criteria can be found in Appendix [C.2.](#page-20-0)

## **4 Experiments**

#### **4.1 Experimental Setup**

**Tasks and Datasets.** We curate 35 benchmark tasks from three domains for thorough experiments: 8 Big Bench Hard (**BBH**) [\(Suzgun et al., 2022a\)](#page-12-4); 3 NLP detection tasks, including **Ethos** [\(Mollas et al., 2021\)](#page-12-5), **Liar** [\(Wang, 2017\)](#page-12-6), and **Sarcasm** [\(Farha & Magdy, 2020\)](#page-11-9); 24 instruction induction tasks [\(Honovich et al.,](#page-11-10) [2022\)](#page-11-10). The task and dataset details are in Appendix [E.](#page-26-0)

<span id="page-6-0"></span>

Figure 3: Iteration history of score values with different operators during optimization. The local and global operators are strategically and adaptively selected by each iteration.

**Baselines.** We evaluate SOA against a variety of LLM-based approaches that have achieved state-of-the-art performance in prompt optimization:

- **APE** [\(Zhou et al., 2023\)](#page-13-1) and **APO** [\(Pryzant et al., 2023\)](#page-12-2): APE utilizes an iterative Monte Carlo Search strategy that emphasizes *exploration*, while APO emphasizes *exploitation*, which harnesses incorrect instances as feedback gradient to refine the original prompt.
- **OPRO** [\(Yang et al., 2023a\)](#page-12-3): OPRO leverages LLM as optimizers to generate better instruction via meta-prompt, solution-score pairs, and task descriptions.
- **PromptBreeder** [\(Fernando et al., 2023\)](#page-11-8), **EvoPrompt** [\(Guo et al., 2023\)](#page-11-2) and **AELP** [\(Hsieh et al.,](#page-11-7) [2023\)](#page-11-7): these methods connect LLMs with evolution algorithms (EAs) to tackle prompt optimization tasks. Specifically, EvoPrompt implements EAs using genetic algorithm [\(Holland, 1992\)](#page-11-11) and differential evolution [\(Storn & Price, 1997\)](#page-12-7), while PromptBreeder introduces multiple operators inspired by thinking styles. AELP focuses on long prompt optimization by mutating on a sentence level with a history-guided search.

**Implementation Details.** We utilized GPT-3.5 to develop LLM agents capable of performing various operators. We set up training, development, and testing datasets, select the prompt with the highest score on the dev set, and report its score on the testing set. We compared the performance of multiple LLM agent models, including PaLM 2, Claude 2, Llama2/3, and Mistral models. More details are provided in Appendix [E.](#page-26-0)

#### **4.2 Main Results**

**BBH Tasks.** Following the practice of AELP [\(Hsieh et al., 2023\)](#page-11-7), we conduct 8 BBH tasks to evaluate the performance of SOA holistically. We consider two initialization schemes SOA-pair and SOA-example and report the final best prompt results in Table [2.](#page-7-0) SOA demonstrates substantial improvements compared to state-of-the-art methods, achieving an average improvement of over AELP (**60.4**%↑), EvoPromopt (**21.7**%↑), and OPRO (**24.3**%↑). In terms of computational cost, SOA consumes **40%** of AELP, **80%** of EvoPrompt, **4%** of OPRO. Fig. [3](#page-6-0) depicts the iterative history of prompt evolution, emphasizing the score variations for the best candidate, worst candidate, and the pool's average across iterations. It has been observed that the Feedback operator yields a performance boost within a single iteration and rarely introduces continual improvements. Global operators such as EDA and Crossover aid in escaping local minima and offering additional performance leaps (refer to Hyperbaton). This observation aligns with our initial operator analysis. The success of SOA lies in the organic organization of these operators, effectively harnessing their advantages to optimize performance and accelerate convergence.

**Detection Tasks.** To present a more extensive comparison, we adopted the configuration outlined in APO [\(Pryzant et al., 2023\)](#page-12-2) and conducted a comparative analysis against it across three tasks. It should be noted that data for the fourth task mentioned in the original paper is unavailable. As shown in Table [3,](#page-7-1) SOA exhibits marginally superior performance to APO in relatively simple tasks such as Ethos (by 1%) and Sarcasm (by 4.7%). However, for more complex tasks such as Liar, SOA demonstrates a significant improvement of

<span id="page-7-0"></span>

Method	Causal Judgement	Dis -ambiguation	Dyck Languages	Formal Fallacies	Hyperbaton	Logical Five	Color Reasoning	Salient Translation
<b>OPRO</b>	71.94	71.53	36.73	49.51	75.92	50.00	65.55	43.88
EvoPrompt	67.24	53.70	47.96	50.81	74.79	61.40	60.90	47.58
AELP	77.77	64.79	10.67	58.25	53.74	73.49	68.14	41.43
$SOA-pair$	72.13	72.37	8.060	58.87	86.02	48.19	60.52	49.19
SOA-example	89.09	68.47	46.77	58.65	87.51	86.29	80.64	47.59
Over AELP	14.5% ↑	11.7% ↑	338.3% ↑	$1.1\%$ $\uparrow$	62.8% $\uparrow$	17.4% $\uparrow$	$18.3\%$ ↑	18.7% ↑
Over EvoPrompt	32.5% $\uparrow$	34.8% $\uparrow$	$-2.5\%$	15.9% $\uparrow$	17.0% $\uparrow$	40.5% $\uparrow$	$32.4\%$ <sup><math>\dagger</math></sup>	$3.4\%$ <sup>↑</sup>
Over OPRO	$23.8\%$ ↑	$1.2\%$ ↑	$27.3\%$ ↑	18.9% $\uparrow$	15.3% $\uparrow$	$72.6\%$ ↑	$23.0\%$ ↑	$12.1\%$ ↑

Table 2: Testing performance of the optimal prompt on 8 representative tasks from BBH.

27.5% compared to APO. Moreover, we have also provided results for SOA using GPT-4, which demonstrated performance comparable to those of SOA employing GPT-3.5.

**Instruction Induction Tasks.** To compare SOA-generated prompts with manually added few-shot examples, we evaluated the optimized prompt from SOA against the best prompts from APE-fewshot [\(Zhou et al., 2023\)](#page-13-1) and PromptBreeder-fewshot [\(Fernando et al., 2023\)](#page-11-8) on APE's 24 instruction induction tasks. The results show that SOA outperforms APE in 17 out of 24 tasks and PromptBreeder in 18 out of 24 tasks. The Appendix [F.1](#page-27-0) provides complete experimental results. Fig. [4](#page-7-2) shows that

<span id="page-7-1"></span>Table 3: Testing performance on three detect tasks used by APO.



few-shot methods do not always outperform zero-shot methods, highlighting the need for a joint in-context prompt search. Moreover, we observed that the prompts generated by SOA are easier to interpret and align better with the task description. Appendix [F.2](#page-28-0) provides more detail on prompt quality.

<span id="page-7-2"></span>

Figure 4: Test accuracy of SOA on the instruction induction tasks.

#### **4.3 Analysis**

**Applicability of SOA framework.** To study the general applicability of SOA framework, we conduct end-to-end optimization tasks on a variety of models covering both open-source LLMs and closed-source LLMs (API calls). As shown in Table [4,](#page-8-0) three end-to-end runs are implemented per task with the average performance and standard deviation reported. All experiments are initialized with SOA-pair method. We observed that GPT-4 performs the best in all tasks, followed by Llama3-70B. Claude 2 is comparable to GPT-3.5. For open-source LLM models, Mistral-7B and Llama3-8B are comparable to each other, both outperforming Llama2-7B by a large margin.

**Effect of Examples.** To compare with more latest work like OPRO and Evoprompt and better understand whether the performance gain introduced by SOA is largely caused by adding few-shot examples, we conduct

<span id="page-8-0"></span>

Method	Dis-ambiguation	Formal Fallacies	Hyperbaton	Salient Translation
$GPT-3.5$	$69.99_{(2.95)}$	$58.49_{(0.33)}$	$84.35_{(1.83)}$	$48.39_{(0.66)}$
$GPT-4$	$79.34_{(3.33)}$	$75.91_{(0.53)}$	$90.58_{(1.39)}$	$70.45_{(0.99)}$
PaLM 2	$71.49_{(0.37)}$	$58.33_{(1.53)}$	$79.45_{(0.98)}$	$49.07_{(3.25)}$
Claude 2	$72.95_{(2.26)}$	$49.46_{(1.52)}$	$83.32_{(1.01)}$	$61.82_{(0.38)}$
Mistral-7B	$65.89_{(0.76)}$	$53.23_{(1.74)}$	$78.76_{(1.36)}$	$43.84_{(1.00)}$
$Llama2-7B$	$42.74_{(4.61)}$	$56.72_{(1.37)}$	$53.23_{(2.37)}$	$21.23_{(1.01)}$
$Llama3-8B$	$62.63_{(3.85)}$	$71.50_{(4.85)}$	$57.52_{(4.28)}$	$37.09_{(2.86)}$
$Llama3-70B$	$74.73_{(2.01)}$	$70.93_{(2.25)}$	$82.26_{(0.66)}$	$62.90_{(1.97)}$

Table 4: SOA performance with different LLM models

an experiment by randomly adding two few-shot examples to OPRO and EvoPrompt. Our results, as shown in Table [5,](#page-8-1) indicated that OPRO exhibited a performance gain on only one out of four tasks while EvoPrompt showed improvement in two out of four tasks. This suggests the need for caution as performance degrades if optimized instructions do not align with naive few-shot selection.

Looking at the best prompt generated by SOA in Appendix G, we noted that 4 out of 8 of the optimal prompts for tasks in Table 2 did not contain any few-shot examples. This observation suggests that SOA's ability to arrive at the most effective prompt does not depend on whether or not there are few-shot examples available. SOA truly optimizes the prompt based on the specific task at hand.

<span id="page-8-1"></span>

Method	Dis-ambiguation	Formal Fallacies	Hyperbaton	Salient Translation
<b>OPRO</b>	71.53	49.51	75.92	43.88
OPRO-few-shot	66.93	52.41	62.90	37.39
EvoPrompt	53.70	50.81	74.79	47.58
EvoPrompt-few-shot	57.43	43.54	79.83	31.45
AELP	64.70	58.25	53.74	41.43
SOA-pair	72.37	58.87	86.02	48.19
SOA-example	68.47	58.65	87.51	47.59

Table 5: Effect of few-shot (fs) examples on 4 BBH tasks.

**Effect of Hamming Distance.** We examine the impact of hamming distance with the performancebased vectors in comparison to cosine distance and lexical embedding for similarity calculation. The study encompasses both approaches carried out in 4 iterations using the same initial pool. Table [6](#page-8-2) displays the outcomes on four BBH tasks. The results indicate that the hamming distance with performance-based vectors outperforms the cosine distance with lexical embedding, showing higher average and maximum scores, particularly for Disambiguation  $(+5.2)$  and Hyperbaton  $(+4.6)$  tasks.

Table 6: Effect of performance vector with hamming distance compared to cosine similarity.

<span id="page-8-2"></span>

Method	Causal Judgement		Disambiguation		Hyperbaton		Salient Translation	
	Average score	High score	Average score	High score	Average score	High score	Average score	High score
Cosine distance	$64.70_{(2,31)}$	$67.86_{(2.47)}$	$58.96_{(1.47)}$	$63.30_{(0.00)}$	$74.70_{(1.60)}$	$85.7_{(0.00)}$	$49.56_{(1.07)}$	$58.80_{(0.00)}$
Hamming distance	$65.74_{(2.87)}$	$69.60_{(2.97)}$	64.11 $_{(1,28)}$	66.94 $_{(2.88)}$	$79.30_{(4.48)}$	$86.78_{(2.15)}$	$50.33_{(2.32)}$	$58.80_{(0.00)}$

**Initialization Strategy.** The SOA can accommodate two types of inputs: *input/output pair* (SOA-pair) and *prompt example* (SOA-example), each bringing its own benefits. When using the *input/output pair* approach, the initialization occurs solely based on LLM's proposal, resulting in greater diversity in the initial pool. On the other hand, *prompt example* empowers users to introduce prior knowledge without leaning on LLM interpretation, and consequently, it performs better in more complex tasks such as Dyck Languages, Logical Five, and Color Reasoning, as illustrated in Table [2.](#page-7-0)

<span id="page-9-0"></span>

Figure 5: Variation of prompt length during SOA optimization. The prompt can be varied from zero-shot to few-shot, and few-shot to zero-shot. The operators are adaptively selected in each iteration.

**Effect of Operators on Prompt Length.** SOA aims to explore the entirety of the prompt space, spanning both zero-shot and few-shot scenarios. Understanding the variation in prompt length and the impact of the operator on this fluctuation is crucial. Fig. [5](#page-9-0) provides a visual representation of the average prompt token length throughout the iterations. Interestingly, the length can either increase, decrease, or oscillate, which aligns with the "unfettered" expectations of global search. Specifically, we observed the initialization phase had a significant impact on prompt length. This observation is in agreement with our analysis of the Lamarckian and Feedback operators, which hold the power to both add and remove examples.

**Synthetic Few-shot Examples.** We observe that in certain cases SOA would generate novel synthetic few-shot examples instead of selecting from existing ones. To verify their veracity, we conduct a manual evaluation of the accuracy of the few-shot examples generated by SOA on a total of 24 instruction deduction tasks. We find that 90 out of the 92 examples evaluated (97.8%) are accurate. Among them, 24 out of the 92 (24.09%) are aligned with samples present in the training set. There are two cases where the synthetic example is inaccurate: the sentiment of *"A non-mystery mystery"* is identified as *"neutral"* where the ground truth is *"negative"*, and *"Little more than a well-mounted history lesson"* is identified as *"neutral"* where the ground truth is *"negative"*.

<span id="page-9-1"></span>

Figure 6: Comparison of computational cost on a total number of evaluations (x-axis) and iterations (y-axis).

**Computational Cost.** We monitor the computational cost of SOA based on two criteria: the number of model API calls consumed by evaluation and operator application, and the number of iterations. As shown in Fig. [6,](#page-9-1) SOA is the most cost-effective method that significantly reduces multiple orders of magnitude compared to evolution strategies, such as PromptBreeder. SOA also performs competitively in terms of iterations compared to the gradient descent approach, such as APO.

#### **5 Related Work**

In-context prompting is an efficient approach for communicating LLMs but the performance is strongly affected by the design of the prompt in specifized tasks. Prompt Tuning to find the optimal prompt has thus obtained broader attention. One research direction is the continuous prompt approaches that traverse the embedding space of input tokens to generate better prompts [\(Li & Liang, 2021;](#page-11-12) [Zhang et al., 2021;](#page-12-8) [Sun](#page-12-9) [et al., 2022b;](#page-12-9)[a;](#page-12-10) [Chen et al., 2023\)](#page-11-1). However, the optimized "soft" prompts from this paradigm often fall short of interpretability and are inaccessible for blackbox APIs. Discrete prompt approaches [\(Diao et al., 2022;](#page-11-13) [Prasad et al., 2022\)](#page-12-11), operating discrete tokens directly, offer an interactive interface to humans with better interpretability and show promising performance in various NLP tasks. Various methods have been proposed via gradient-based search [\(Shin et al., 2020\)](#page-12-12), reinforcement learning [\(Zhang et al., 2022a;](#page-13-3) [Deng et al., 2022;](#page-11-14) [Sun et al., 2023\)](#page-12-13) and ensemble methods [\(Hou et al., 2023;](#page-11-15) [Pitis et al., 2023\)](#page-12-14) while these methods encounter concerns in terms of scalability, reliability and efficiency [\(Wang et al., 2023\)](#page-12-15).

Recent advancements rely on iterative sampling, scoring, and selection of exceptionally promising prompts, generating diverse possibilities for prompt optimization [\(Fernando et al., 2023;](#page-11-8) [Guo et al., 2023;](#page-11-2) [Hsieh et al.,](#page-11-7) [2023\)](#page-11-7), which proposed leveraging LLMs to implement evolution strategies in prompt searches. [Yang et al.](#page-12-3) [\(2023a\)](#page-12-3) demonstrates the capability of LLM as optimizers in prompt design. [Pryzant et al.](#page-12-2) [\(2023\)](#page-12-2) and [Zhou et al.](#page-13-1) [\(2023\)](#page-13-1) utilize natural language feedback to refine prompt instructions. However, these prompt evolution/refinement strategies largely focus on prompt instructions, typically short sentences. Our research reformulates the problem by permitting unrestrained tuning of a jointly in-context prompt, incorporating both instructions and examples, and offering more avenues for improvement, yet it also poses new challenges in navigating the high-dimensional combined space, while retaining high efficiency. While previous search and sampling algorithms have been investigated, such as Monte Carlo search [\(Zhou et al., 2023\)](#page-13-1), Gibbs sampling [\(Xu et al., 2023\)](#page-12-16), Beam search [\(Pryzant et al., 2023\)](#page-12-2), or Evolution Algorithm [\(Fernando et al.,](#page-11-8) [2023\)](#page-11-8), we introduce a novel dual exploration-exploitation strategy that leverages the in-depth traits of each operator, utilizing an intuitive blend of global-local search, conducive to enhancing interactive dynamics during optimization.

# **6 Conclusion and Discussion**

In this work, we propose a joint prompt-tuning framework that enables the combined optimization of prompt instruction and examples for LLMs. Benefiting from the global-local phased strategy and the adaptive selection of operators, SOA achieves state-of-the-art performance over a wide range of benchmark tasks while significantly reducing the computational cost. Despite having such achievements, SOA still needs thousands of inference calls in several iterations, which might be insufficient for supporting large-scale applications. Future work could explore better online strategies to further improve efficiency, and also investigate multi-objective prompt tuning beyond single accuracy or performance metric, such as safety, security, and robustness.

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# **A Appendix**

# **B Operator Definition**

Operators are used to generate new candidates. Seven types of operators, broadly categorized into five classes are used by SOA. The idea is to provide a diverse set of operators so that a broad cognitive space of linguistics is covered.

### **B.1 Lamarckian Operator**

The Lamarckian operator follows the principles proposed in APE and Prompt Breeder [\(Zhou et al., 2023;](#page-13-1) [Fernando et al., 2023\)](#page-11-8). Given a set of input-output pairs for the task, an LLM agent is used to reverse-engineer the prompt from the provided demonstrating pairs. This type of operator allows a diverse set of prompt candidates to be generated with no prior knowledge of the task. Any prompt candidate will have to be induced from the demonstrating pairs. The prompt used by the LLM agent is in Table [11.](#page-23-0)

(Lamarckian Operator) Given a set of input/output pairs  $(Q, \mathcal{A}) = [(Q_1, A_1), ..., (Q_m, A_m)]$  and a base LLM L, the Lamarckian operator is to reverse engineer the instruction  $\mathcal{O}_L$  so that  $\mathcal{O}_L(Q_i) = A_i, i = 1, ..., m$ .

### **B.2 Feedback Operator**

Inspired by the concept of *Gradient Descent* in machine learning model training, we introduce an LLM agent that works as an examiner which examines the cases where the current task prompt fails and provides improvement guidance. Such guidance will be treated as *gradient* and be used by another LLM Agent as an improver to generate a new candidate. Though similar to what is proposed in APO [\(Pryzant et al.,](#page-12-2) [2023\)](#page-12-2), instead of only using gradient descent repeatedly, which has a higher probability of arriving at a local minimum, we take advantage of its fast converge rate to local minimum and combine it with other operators to target global minimum. When applying the Feedback operator, it will be applied to every candidate in the current pool. The prompt can be found in Table [12](#page-23-1) - [13.](#page-24-0)

(Feedback Operator) The Feedback operator generates a new prompt  $p'$  based on the existing prompt  $p \in \mathcal{P}$ , and where  $p$  made mistakes for a task. The feedback operator  $\mathcal{O}_F$  first looks at the cases where the current  $p$ failed to generate a list of advice  $G$ , and then asks LLM  $\mathcal L$  to apply such advice  $G$  to existing prompt  $p$  for generating the new prompt *p* ′ .

#### **B.3 Estimation of Distribution Operator**

The next class of operators takes a set of parents as input to generate a modified candidate.

**Estimation of Distribution Operator (EDA)**: Following the principles proposed by [\(Hauschild & Pelikan,](#page-11-16) [2011\)](#page-11-16) and work in [\(Fernando et al., 2023\)](#page-11-8), we use a LLM agent that is fed with a subset of the current pool to generate new candidate. To ensure the diversity and quality of the subset, we first rank the candidates in the current pool by their performance in descending order. Then starting from the first item in the ordered candidates, we only add the candidate to the subset if it does not have a similarity score over a threshold with any other candidate that is already in the subset. This way candidates with higher performance are more prone to be added to the subset and the diversity of the subset is achieved. More details on how similarity is calculated can be found in section [3.3.](#page-4-0) The subset will be randomized before feeding into the LLM agent so the candidate's performance does not dictate its order. The prompt can be found in Table [14.](#page-24-1)

**EDA and Index Operator**: This is a variant of the EDA operator above. Based on the observations that LLM is more prone to use examples that appear late in the in-context learning [\(Liu et al., 2023;](#page-11-17) [Fernando et al., 2023\)](#page-11-8), after generating the subset following procedures of EDA, the subset is ordered by their performance in *ascending order*. To further balance exploitation and exploration and avoid being too biased over the candidate with the highest performance [\(Fernando et al., 2023\)](#page-11-8), we instructed LLM that the candidates are ranked by their performance in *descending order* so that the low performance candidates are taken into consideration. The prompt can be found in Table [15.](#page-24-2)

(Estimation of Distribution Operator - EDA) EDA generates a new candidate based on a list of parents. It is a function operator  $\mathcal{O}_E$  that performs  $\mathcal{O}_E(\mathcal{P}, \mathcal{L}) = p'$ . Given a list of prompts  $\mathcal{P} = [p_1, ..., p_m]$  and an LLM  $\mathcal{L}$ , EDA provides a new prompt  $p'$ . Items in  $\mathcal{P}$  satisfy the restriction that  $d(p_i, p_j) < t$ , where *d* is a function that calculates similarity, and  $t$  is a predefined threshold. If the items in  $\mathcal P$  are ordered based on certain criteria, we call it  $EDA + Index (EDA+I).$ 

### **B.4 Crossover Operator**

This class of operators takes two parents as input to generate a crossover candidate. The prompt can be found in Table [16.](#page-25-0)

**Crossover Operator(CR)**: Following the concept of crossover in the evolution algorithm, we introduce an LLM agent to function as a crossover operator that takes two parents and generates a crossover candidate. It takes the best two candidates in the current pool, namely the top two candidates with the highest performance, and performs linguistic crossover.

**Crossover with Diversity Operator(CR+D)**: This is a variance of the Crossover Operator. To provoke exploration, we follow a similar process in EDA where diversity in parents is considered. Thus it takes the best candidate and the most distinct individual to it as two parents for crossover operation. The distinctness between two candidates is measured by a similarity score. More details on how the similarity score is calculated can be found in section [3.3.](#page-4-0)

(Crossover Operator - CR) Crossover generates a new candidate based on two parents. It is a function operator  $\mathcal{O}_C$  that performs  $\mathcal{O}_C(p_1, p_2, \mathcal{L}) = p'$  where  $p_1, p_2$  are two prompts selected from a prompt pool  $\mathcal P$  where  $\mathcal{P} = [p_1, \ldots, p_m], p'$  is the generated prompt that hold features from both  $p_1$  and  $p_2$ . If  $p_2 = \arg\min_{p \in \mathcal{P}} d(p_1, p_i)$ is applied for choosing  $p_2$ , we call it Crossover + Distinct  $(CR + D)$ .

### **B.5 Semantic Operator**

This class of operators takes a candidate and uses an LLM agent to compose a new candidate that shares its semantic meaning. When applying the Semantic operator, it will be applied to every candidate in the current pool. The prompt can be found in Table [17.](#page-25-1)

(Semantic Operator) The Semantic operator is a function operator  $\mathcal{O}_S$  that performs  $\mathcal{O}_S(p,\mathcal{L}) = p'$  where p is the generated prompt that shares the same semantic meaning as *p*.

# **C Operator Analysis**

### <span id="page-16-0"></span>**C.1 Few-Shot Additional / Removal Analysis**

The ability to add and remove few-shot examples is crucial in dictating whether it is possible to traverse the full in-context prompt space. Thus we conduct the few-shot addition/ removal analysis to gauge each operator's capabilities. Below are examples of how operators add or remove few-shot examples.

Table 7: Lamarckian Operator Add Few-shot Example



Table 8: Feedback Operator Add Few-shot Example: In this operation, few-shot examples are added based on the feedback. Individual feedback and their corresponding changes are colorcoded.



Table 9: Feedback Operator Remove Few-shot Example: In this operation, few-shot examples are removed based on the feedback. Individual feedback and their corresponding changes are colorcoded.



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Table 10: Semantic Operator Remove Few-shot Example

### <span id="page-20-0"></span>**C.2 Operator Feature Analysis**

To study the features of each operator we conduct a preliminary experiment where we study four operators: EDA Operator, Crossover, Feedback Operator, and Semantic Operator.

**Initialization:** As the initialized points have a tremendous impact on optimization problems. We randomly use four different seeds to create four initial pools for four different tasks: Causal Judgement, Salient Translation Error Detection, Disambiguation QA, and Hyperbaton. The idea is to provide various initialization points so that the performance of operators can be averaged to rule out the influence of initialization.

**Operator Applications:** For each initialization, we apply the following procedure for all four operators.

- For one round, starting with the initial pool, we consecutively apply the operator 5 times. This is to study the value of applying the operator consecutively.
	- **–** For EDA and CrossOver, as they require multiple parents, we keep a pool size of 5 for each iteration after applying the operator. Performance gain is defined as whether the average performance of the pool is improved.
	- **–** For Feedback Operator and Semantic Operator, as they only need one parent, we apply them to a random candidate from the initial pool and use the new candidate as the base for the next round. Performance gain is defined as whether the new candidate has a higher performance than its parent.
- To reduce the impact of randomness, we run this process 5 rounds for each operator.

<span id="page-20-1"></span>Thus for each operator, it will be run a total of 4 tasks  $*$  5 rounds  $*$  5 application = 100 times.



Figure 7: Operator Improvement Count

**Analysis:** There are two aspects we are particularly interested in. The first is **what the likelihood of performance gain when applying an operator is** (Probability of Improvement), and the second is **how fast each operator can continuously bring improvement** (Convergence Speed).

- **Probability Of Improvement**: Figure [7](#page-20-1) shows the number of times performance is improved by each operator. Crossover and EDA Operator introduces improvements in more steps with Semantic Operator ranking third. Feedback Operator introduces the least number of improvements. This result helps populate the *Prob* column in table [1.](#page-3-0)
- **Convergence Speed**: Figure [8](#page-21-0) shows that for each operator, as they are applied in 5 consecutive steps, the number of times improvement is introduced for each step. Figure [9](#page-22-0) shows the average percentage of performance gain operators brought in each step.
- **–** For EDA Operator and Crossover, each 5 step has a similar number of contributions for performance gains as shown in figure [8.](#page-21-0) From figure [9](#page-22-0) we can also observe the first step brings the most improvement and the first 4 steps bring a similar improvement ratio.
- **–** For Feedback Operator and Semantic Operator, the first step has a significantly higher chance of introducing improvement as shown in figure [8.](#page-21-0) This is especially true for Feedback Operator where step 1 accounts for over 34% of the total improvement counts. As for the improvement ratio, the first step for both Feedback Operator and Semantic Operator introduces significantly more improvements than the rest of the steps shown in figure [9.](#page-22-0)

Based on the tests, we learned that the value gained for applying Feedback Operator and Semantic Operator is significantly reduced after the 1st application. We interpret it as **Feedback Operator and Semantic Operator can jump to the local minimum pretty fast**, namely in 1 step, thus leading to less possibility of improvement for steps 2 - 5. Whereas for EDA Operator and Crossover, as they are merging genetic information between candidates, the likelihood of improvement is relatively randomized. So even if the first round of applying them renders no improvement, there is still a chance of performance gain in the following run. In other words, **we should be more patient with EDA Operator and Crossover**. Thus the operator tolerance (described in section [3.3-](#page-4-0)design 2) for EDA and Crossover is set to 4 and for Feedback Operator and Semantic Operator is 1. These learnings help populate the *Speed* column in table [1.](#page-3-0)

<span id="page-21-0"></span>

Figure 8: Operator Improvement Pattern: EDA Operator and Crossover have similar improvement counts for each step whereas for Feedback Operator and Semantic Operator, the first step introduced significantly more times of improvement compared to the others.

<span id="page-22-0"></span>

Figure 9: Improvement Ratio: On the left, for EDA and Crossover, we observe an almost equal improvement ratio for the first four steps. Improvement Ratio is defined as the relative percentage of improvement in the average performance for the entire pool. On the right, for Feedback and Semantic Operator, we observe the first round contributes significantly more improvement compared to the others. As Feedback and Semantic Operators take one input candidate, Improvement Ratio is defined as the relative performance improvement percentage for the candidate after applying the operator.

# **D Operator Prompts**

**Operator Implementation:** The state-of-art frameworks such as APO, EVOPROMPT, and AELP have already implemented operators such as feedback operator, crossover operator, and semantic operator with LLM. However, these implementations inflict restrictions on LLM with prompts. For example, in APO when implementing the feedback operator, the prompt specifically identified the use case to be zero-shot. [\(Pryzant](#page-12-2) [et al., 2023\)](#page-12-2) In EVOPROMPT-DE, when applying crossover operators, the focus is to only change the parts that two parents differentiate from each other. [\(Guo et al., 2023\)](#page-11-2) In AELP, when applying semantic operators, it is restricted to a sentence level, not the whole prompt. [\(Hsieh et al., 2023\)](#page-11-7). In SOA, we pay special attention not to apply any restrictions in our operator prompt, realizing the full potential of LLMs.

Table 11: Lamarckian Operator Prompt

<span id="page-23-0"></span>I gave a friend an instruction and some input. The friend read the instruction and wrote an output for every one of the inputs. Here are the input-output pairs:

## Example  $\#$ # {*input output pairs*}

The instruction was:

<span id="page-23-1"></span>Table 12: Gradient Descent Generation Prompt: Unlike APO which is also using gradient descent, we are NOT adding restrictions such as *"zero-shot classifier prompt."*, nor providing any differentiation between *instructions* and *examples*. Instead, we specifically ask LLM to output multiple feedback in one go. Also as are **passing in the existing prompt as a whole**, thus feedback should be on the paragraph/prompt level instead of the sentence/instruction level. We highlight the design that helps us achieve this below.

> You are a quick improver. Given an existing prompt and a series of cases where it made mistakes. Look through each case carefully and identify what is causing the mistakes. Based on these observations, output ways to improve the prompts based on the mistakes.

 $\#\#\$  Existing Prompt  $\#\#$ {*existing prompt*}

 $\#\#\text{ Cases where it gets wrong:}\#\#$ {*wrong cases*}

ways to improve the existing prompt based on observations of the mistakes in the cases above are:

<span id="page-24-0"></span>Table 13: Gradient Descent Application Prompt: Following the principle of optimizing prompt as a whole, our operator prompts take input and output on the entire prompt level

You are a quick improver. Given an existing prompt and feedback on how it should improve. Create an improved version based on the feedback.

 $#$ # Existing Prompt  $#$ # {*existing prompt*}

 $\# \#$  Feedback $\# \#$ {*feedback*}

 $##$  Improved Prompt $##$ 

#### Table 14: EDA Prompt

<span id="page-24-1"></span>You are a mutator. Given a series of prompts, your task is to generate another prompt with the same semantic meaning and intentions.

 $\#\#\text{ Existing Prompts }\#\#$ {*existing prompt*}

The newly mutated prompt is:

<span id="page-24-2"></span>Table 15: EDA+Index Prompt: The difference between EDA + Index and EDA is that EDA + Index takes advantage of the in-context learning technique and informs the order of the passed-in prompts

> You are a mutator. Given a series of prompts, your task is to generate another prompt with the same semantic meaning and intentions. The series of prompts are ranked by their quality from best to worst.

 $\#\#\text{ Existing Prompts }\#\#$ {*existing prompt*}

The newly mutated prompt is:

#### Table 16: Cross Over Prompt

<span id="page-25-0"></span>You are a mutator who is familiar with the concept of cross-over in genetic algorithm, namely combining the genetic information of two parents to generate new offspring. Given two parent prompts, you will perform a cross-over to generate an offspring prompt that covers the same semantic meaning as both parents.

#### $#$  Example

Parent prompt 1: Now you are a categorizer, your mission is to ascertain the sentiment of the provided text, either favorable or unfavorable

Parent prompt 2: Assign a sentiment label to the given sentence from ['negative', 'positive'] and return only the label without any other text.

Offspring prompt: Your mission is to ascertain the sentiment of the provided text and assign a sentiment label from ['negative', 'positive'].

 $\#\#\$  Given  $\#\#$ Parent prompt 1: {*prompt 1* } Parent prompt 2: {*prompt 2* } Offspring prompt:

<span id="page-25-1"></span>Table 17: Semantic Operator Prompt: To provoke LLM's creativity, we do not restrict to the **semantic** level but expand that to *intentions*, allowing LLM to not **stick to a sentence-by-sentence modification**.

> You are a mutator. Given a prompt, your task is to generate another prompt with the same semantic meaning and intentions.

 $#$  Example:

current prompt: Your mission is to ascertain the sentiment of the provided text and assign a sentiment label from ['negative', 'positive'].

mutated prompt: Determine the sentiment of the given sentence and assign a label from ['negative', 'positive'].

Given: current prompt: {*existing prompt*} mutated prompt::

# <span id="page-26-0"></span>**E Details of Experiments**

#### **E.1 Baselines**

- **APE** [\(Zhou et al., 2023\)](#page-13-1) uses LLM agent for instruction induction tasks. It proposes forward mode generation and reverse mode generation and uses log probability to generate and evaluate candidates.
- **APO** [\(Pryzant et al., 2023\)](#page-12-2) uses feedback provided by LLM as gradients to approach prompt optimization. It uses beam search to find the best candidate.
- **PromptBreeder** [\(Fernando et al., 2023\)](#page-11-8) uses the evolution algorithm to tackle prompt optimization tasks and utilizes thinking styles, and mutation prompts to surface the best task prompt.
- **AELP** [\(Hsieh et al., 2023\)](#page-11-7) uses existing prompts [\(Suzgun et al., 2022b\)](#page-12-17) to target long prompt optimization and improves them by mutating on a sentence level with history-guided search.
- **EVOPROMPT** [\(Guo et al., 2023\)](#page-11-2) uses crossover mutation and semantic mutation with an evolution algorithm to find the best prompt.
- **OPRO** [\(Yang et al., 2023a\)](#page-12-3) uses meta prompt, solution-score pairs, and task descriptions to generate candidates.

#### **E.2 Benchmark tasks**

- **24 Instruction Induction Tasks**: These 24 instruction tasks [\(Honovich et al., 2022\)](#page-11-10) span many facets of language understanding, from simple phrase structure to similarity and causality identification. Both training and testing data are provided for these tasks and we create our training and evaluation data set from the available training data and use the provided testing data set as is. Depending on the task, we use up to 50 training data and up to 50 evaluation data. We use *input/output pair* format for these tasks.
- **Ethos**: Ethos [\(Mollas et al., 2021\)](#page-12-5) is an online English hate speech detection data set with 997 online comments and hate speech labels. We select 50 for training, 50 for evaluation, and 150 for testing. We use *prompt example* format for this data set following the practice of APO [\(Pryzant et al., 2023\)](#page-12-2).
- **Liar**: Liar [\(Wang, 2017\)](#page-12-6) is an English fake news detection data set with 4000 statements, context, and lie labels. We select 50 for training, 50 for evaluation, and 150 for testing. We use *prompt example* format for this data set following the practice of APO [\(Pryzant et al., 2023\)](#page-12-2).
- **Sarcasm**: Sarcasm [\(Farha & Magdy, 2020\)](#page-11-9) is an Arabic sarcasm detection data set with 10,000 online comments and sarcasm labels. We select 50 for training, 50 for evaluation, and 150 for testing. We use *prompt example* format for this data set following the practice of APO [\(Pryzant et al., 2023\)](#page-12-2).
- **BBH**: BBH [\(Aarohi & bench authors, 2023\)](#page-10-3) is a collaborative benchmark that aims to quantitatively measure the capabilities and limitations of language models. We followed the same practice in the AELP paper with the same tasks and randomly selected 50 for training, 50 for evaluation, and 125 for test. [\(Hsieh](#page-11-7) [et al., 2023\)](#page-11-7)

#### **E.3 SOA Setting**

- **Pool Size**: In the experiments, for *phase 0: Global initialization* we set the pool size to be 15. For the rest phases, we set the pool to be 5.
- **Operator Tolerance**: Based on operator analysis in section [C.2,](#page-20-0) the tolerance for Feedback Operator and Semantic Operator is set to 1. The tolerance for EDA Operator and Crossover is set to 4. Thus the minimum number of times operators will be applied in *phase 2: global evolution operation* is 8.
- **Model Configuration**: For operators, we set the temperature to 0.5 to tap into LLM's creativity. For evaluations, we set the temperature to 0.
- **Performance Gain in Stop Criteria**: To improve efficiency, when evaluating performance gain to decide whether we should move to the next phase, we are only looking at the best candidate in the current pool.
- **Candidate Selection**: To improve efficiency, after getting new candidates, we combine them with the current pool and use a greedy algorithm to select the top performer to be the new pool.

# **F Additional Experiment Results**

#### <span id="page-27-0"></span>**F.1 24 Instruction Induction Tasks**

Table [18](#page-27-1) shows the comparison between APE, PromptBreeder, and SOA evaluated by the best prompt on 24 instruction induction tasks. SOA outperforms 21/24 tasks over APE zero shot, 17 / 24 tasks over APE few shot and 18 / 24 tasks on Prompt Breeder. SOA generated few-shot prompts for 20 / 24 tasks and zero-shot examples for 4 / 24 tasks. For the full set of generated prompts please refer to table [26.](#page-44-0)

<span id="page-27-1"></span>

<b>Task</b>	<b>APE</b> $(zero-$ shot)	$few-$ <b>APE</b> shot)	PromptBreeder (few-shot)	$SOA-3.5$	$SOA-4$	
Antonyms	0.83	0.86	0.87	0.89	0.91	
Cause Effect	0.84	$\mathbf{1}$	$\mathbf{1}$	0.96	$\mathbf{1}$	
Common Concept	0.27	0.32	$\Omega$	0.23	0.28	
Diff	$\mathbf{1}$	$\mathbf{1}$	$\,1\,$	$\mathbf{1}$	$\mathbf{1}$	
First Word Letter	$\mathbf{1}$	$\mathbf{1}$	$\mathbf{1}$	$\mathbf{1}$	$\mathbf{1}$	
<b>Informal</b> Formal	0.65	0.70	0.07	0.6	0.67	
Large Ani- mal	$0.97\,$	0.97	0.97	0.96	0.94	
Letters List	0.99	$\mathbf{1}$	0.99	$\mathbf{1}$	$\mathbf{1}$	
<b>Taxonomy</b> Animal	0.66	0.79	$\mathbf{1}$	0.96	$\mathbf{1}$	
Negation	0.83	0.9	0.9	0.94	0.88	
Num Verb	$\mathbf{1}$	$\mathbf{1}$	$\mathbf{1}$	$\mathbf{1}$	$\mathbf{1}$	
<b>Active Pas-</b> sive	$\mathbf{1}$	$\mathbf{1}$	$\mathbf{1}$	$\mathbf{1}$	$\mathbf{1}$	
Singular Plural	$1\,$	$\mathbf{1}$	$\mathbf{1}$	$\mathbf{1}$	$\mathbf{1}$	
Rhymes	$\mathbf{1}$	0.61	$\mathbf{1}$	$\mathbf{1}$	$\mathbf{1}$	
Second Word Let- ter	0.87	0.69	$0.95\,$	$\mathbf{1}$	$\mathbf{1}$	
Sentence Similarity	0.36	0.43	0.56	0.38	$0.55\,$	
Continuation of Table 18						

Table 18: 24 Instruction Induction Task in APE



# <span id="page-28-0"></span>**F.2 Generated Prompt Comparison**

We notice that the **prompts generated by SOA are easier to understand by humans.** Below is a comparison between prompts generated for task Rhymes. The task description is: *"Write a word that rhymes with the input word."*

The prompt generated by APE and Instruct Zero does not fit the task. The prompt generated by Prompt Breeder is not easy to understand how it relates to rhyme. The prompt generated by SOA is easy to understand with few shot examples added.



<span id="page-28-1"></span>



Continuation of Table [19](#page-28-1)



# **G Few-shot Add/ Removal Examples**

Below are cases listing examples where few-shot examples are added or removed with SOA.

#### **G.1 Zero-shot to Few-shot**





### **G.2 Zero-shot to Zero-shot**

#### Table 21: Zero-shot to Zero-shot



### <span id="page-31-0"></span>**G.3 Few-shot to Zero-shot**

Table 22: Few-shot to Zero-shot





Table 23: Few-shot to Few-shot

<span id="page-32-0"></span>



Continuation of Table [23](#page-32-0)



# **H Generated Prompts**

In this section, we list the prompts generated by SOA with the best performance for each task. All prompts are generated by gpt-3.5. We observe a mix of few-shot prompts and zero-shot prompts for different tasks. This indicates both LLM's ability to perform in-context prompt optimization and SOA's ability to traverse the whole problem space to find optimal solutions.

<span id="page-35-0"></span>We also notice that the few-shot examples in the final prompts are largely generated by LLM instead of copied from example instruction or training sets. Thus it serves as further proof of LLM's capability of in-context prompt optimization and SOA's credibility in this problem space.

#### Table 24: BBH Prompts







Continuation of Table [24](#page-35-0)







Continuation of Table [24](#page-35-0)





Does the provided text contain hate speech? Return a boolean value of True or False.					
Analyze the context and other information provided to determine the truthfulness of the statement. To do so, consider the following guidelines:					
Identify key sources of information, such as reputable news outlets or gov- ernment reports, and consider the credibility of the sources. Look for corroborating evidence and consider any potential biases or conflicts of interest.					
2. Conduct additional research or seek out expert opinions when necessary to determine the truthfulness of a statement. Use resources or links to relevant information provided, and consider consulting with subject matter experts or fact-checking organizations.					
3. Note that the determination of truthfulness may not always be possible based on the information provided, and that additional research or analysis may be required. Use your best judgment and be transparent about any uncertainties or limitations in your analysis.					
Consider specific examples or scenarios to help you apply the prompt in different contexts. For instance, you might analyze a political statement, a scientific claim, or a news article. Be aware of common pitfalls or errors, such as relying on unreliable sources or failing to consider alternative explanations.					
Output Format: Assign 0 for true and 1 for false. Note that this determina- tion is based on the information provided and may not be definitive.					
Determine if the input contains any language that could be considered derogatory or discriminatory towards a particular group based on their race, ethnicity, gender, sexual orientation, religion, or any other protected characteristic. If such language is found, output True. If not, output False. The prompt should be trained on a diverse dataset to improve its accuracy and reduce errors.					

Table 25: APO Prompts

### Table 26: APE Prompts

<span id="page-44-0"></span>







Continued next page for Table [26](#page-44-0)















Continued next page for Table [26](#page-44-0)

