VReST: Enhancing Reasoning in Large Vision-Language Models through Tree Search and Self-Reward Mechanism

Anonymous ACL submission

Abstract

Large Vision-Language Models (LVLMs) have shown exceptional performance in multimodal tasks, but their effectiveness in complex visual reasoning is still constrained, especially when employing Chain-of-Thought prompting techniques. In this paper, we propose VReST, a novel training-free approach that enhances Reasoning in LVLMs through Monte Carlo Tree Search and Self-Reward mechanisms. VReST meticulously traverses the reasoning landscape by establishing a search tree, where each node encapsulates a reasoning step, and each path delineates a comprehensive reasoning sequence. Our innovative multimodal Self-Reward mechanism assesses the quality of reasoning steps by integrating the utility of sub-questions, answer correctness, and the relevance of vision-language clues, all without the need for additional models. VReST surpasses current prompting methods and secures stateof-the-art performance across three multimodal mathematical reasoning benchmarks. Furthermore, it substantiates the efficacy of test-time scaling laws in multimodal tasks, offering a promising direction for future research.

1 Introduction

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Chain-of-Thought (CoT) prompting (Wei et al., 2022; Kojima et al., 2022; Wang et al., 2023; Zhang et al., 2022) has been widely recognized as an effective technique for enhancing the performance of Large Language Models (LLMs) on complex reasoning tasks. Recently, OpenAI o1 (OpenAI, 2024) demonstrated the potential of generating ultra-long CoTs to achieve inference scaling laws.

Building on this progress, many studies (Zhang et al., 2023; Mitra et al., 2024; Shao et al., 2024; Zheng et al., 2023; Gao et al., 2024; Liu et al., 2024; Wu et al., 2024) have extended CoT prompting to Large Vision-Language Models (LVLMs), aiming to enhance their reasoning capabilities in multimodal tasks. While these methods show promise,



Figure 1: The difference between VReST and the previous multimodal CoT prompting methods. The methods in (a)(b)(c) obtain suboptimal solutions by a greedy algorithm, while VReST in (d) can fully explore the reasoning space to obtain the optimal solution.

they often generate limited intermediate reasoning steps and lack the ability to evaluate and refine the generated CoTs. Consequently, these approaches fail to fully unleash the reasoning potential of LVLMs, resulting in marginal improvements on challenging multimodal reasoning tasks (Zhang et al., 2025). As illustrated in Tables 1, 2, and 3, multimodal CoT reasoning underperforms direct question answering (Direct QA) on more complex visual mathematical tasks.

To improve LVLM reasoning, a potential solution is to construct large LVLM reasoning datasets (Chen et al., 2024; Xu et al., 2023; Shao et al., 2024) and train LVLMs (Cheng et al., 2024; Guo et al., 2024; Zhang et al., 2024a). However, this approach is expensive and difficult to scale. Thus, we focus on developing training-free methods to enhance the reasoning ability of LVLMs.

Recent studies have shown that LLM with Monte

Carlo Tree Search (MCTS) (Hao et al., 2023; Zhang et al., 2024b; Jiang et al., 2024; Long, 2023; Yao et al., 2024) can effectively expand the reasoning space in a training-free manner, improving CoT generation. Based on these findings, we extend the MCTS algorithm to LVLM. A key component of any tree search algorithm is the reward function, which guides the model's exploration within the vast space of possible reasoning traces (Feng et al., 2023). To ensure a fair comparison with baseline methods, we avoid introducing additional models. Hence, we propose a multimodal Self-Reward mechanism that incorporates visual knowledge with textual clues.

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To tackle the intricacies of complex vision tasks within LVLMs, we introduce VReST, a pioneering approach that Enhancing **Re**asoning in Large Vision-Language Models through Tree Search and Self-Reward mechanism. Figure 1 shows the difference between VReST and existing multimodal CoT methods. VReST employs MCTS to systematically navigate the reasoning space, where nodes symbolize individual reasoning steps, and paths constitute complete reasoning trajectories. By recursively identifying nodes with high confidence, VReST dynamically crafts reasoning steps and fosters diversity by modulating the temperature of LVLM generation, thus enriching the exploration of the reasoning space. Based on prior work (Hao et al., 2023), we present a multimodal Self-Reward mechanism that appraises the merit of reasoning steps. It considers sub-question utility, final answer correctness, and vision-language clues. Inspired by (Lightman et al., 2023), our mechanism assigns reward values to each node.

Finally, VReST expands, evaluates, and backpropagates reasoning traces in each iteration, thereby refining the search tree by updating node statistics. The optimal reasoning trace is selected based on the aggregate reward, with the final answer being extracted from the terminal node. Experiments show that VReST outperforms existing prompting methods on three visual reasoning datasets. Moreover, as shown in Section 4.7, the performance gain of our approach becomes more pronounced with increasing iterations of MCTS, surpassing other prompting methods, and demonstrating better multimodal test-time scaling. Our approach offers a promising direction for trainingfree methods to enhance LVLM reasoning.

Our main contributions are as follows:

• We introduce a training-free approach that

uses MCTS to enhance the depth and quality of reasoning in LVLMs. 114

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- We propose a Self-Reward mechanism incorporating visual information to evaluate reasoning traces.
- We achieve SOTA performance on three multimodal mathematical reasoning datasets, outperforming existing prompting methods.
- We demonstrate that VReST exhibits a better test-time scaling law in multimodal tasks.

2 Related Work

2.1 CoT for Large Vision-Language Models

Large Vision-Language Models (LVLMs) demonstrate remarkable abilities in integrating visual and linguistic information (Li et al., 2024; Peng et al., 2024), but face challenges in tasks requiring complex reasoning or multi-hop inferences (Lu et al., 2023; Wang et al., 2024a,c; Zhao et al., 2024; Chen et al., 2024). Extending the Chain of Thought (CoT) paradigm (Kojima et al., 2022; Zhang et al., 2022) to the multimodal domain offers a promising direction. While many approaches enhance the CoT reasoning abilities of LVLMs through extensive training (Xu et al., 2023; Shao et al., 2024; Cheng et al., 2024; Guo et al., 2024), optimizing reasoning traces provides a viable training-free alternative. Initial effort adopts a two-stage reasoning method (Zhang et al., 2023) where rationales precede the final answer to enable step-by-step inference. Subsequent advancements augment reasoning steps with precise visual details, such as scene graphs (Mitra et al., 2024) and related image regions (Shao et al., 2024). To better understand textual information, DDCoT (Zheng et al., 2023) decomposes questions into sub-questions, and utilize sub-answers to construct reasoning steps. Cantor (Gao et al., 2024) further improves this approach by framing LVLMs as multifaceted experts for multi-step reasoning.

However, these methods struggle with complex questions due to limited reasoning steps and lack of feedback to refine traces. VReST addresses these issues with a tree search for extended reasoning and reward evaluation for optimal solutions.

2.2 Tree-based Reasoning with LLMs

Tree-based reasoning methods enhance performance by increasing computational costs to explore diverse solution spaces (Jiang et al., 2024). Self-Consistency (Wang et al., 2022) improves accuracy



Figure 2: The framework of VReST. (a) Illustrates the MCTS rollout iteration process, including Selection, Expansion, Rewarding, and Backpropagation steps. (b) Depicts the generation of new reasoning steps using LVLM based on the constructed prompt. (c) Shows the Self-Rewarding mechanism for calculating the reward of new reasoning steps, considering both the usefulness of sub-questions and the correctness of the last answer. (d) Describes the Best-Trace strategy of the final reasoning trace selection.

by sampling multiple reasoning traces, while Tree 163 of Thoughts (ToT) (Long, 2023; Yao et al., 2024) 164 use heuristic methods to select optimal steps but of-165 ten converges to locally optimal solutions. Breadth-166 First Search(BFS) (Yao et al., 2024) identifies glob-167 ally optimal reasoning traces by exploring the en-168 tire space. Monte Carlo Tree Search (MCTS) (Hao et al., 2023; Zhang et al., 2024b) further integrates 170 rewarding and backpropagation mechanisms, quan-171 tifying each inference trace across multiple iterations to identify the globally optimal solution. De-173 spite their potential, tree-based reasoning methods 174 have rarely been applied to multimodal reasoning 175 tasks. Our framework incorporates visual informa-176 tion into reasoning steps and, to the best of our knowledge, is the first to employ MCTS for multi-178 modal CoT reasoning. 179

3 Method

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As shown in Figure 2, our approach combines Monte Carlo Tree Search (MCTS) with Large Vision-Language Model (LVLM) to generate stepby-step reasoning traces and evaluate them using a Self-Rewarding mechanism. Below, we detail the problem formulation (3.1), the MCTS framework with a Self-Reward mechanism (3.2), as well as the final reasoning trace selection method (3.3).

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3.1 Problem Formulation

Given a question Q and an image I, our goal is to find the optimal reasoning trace \mathcal{P}^* that leads to the correct answer A. Each reasoning trace \mathcal{P} consists of an original question and a sequence of reasoning steps: $\{Q, S_1, S_2, ..., S_n\}$, where each step S_i contains a sub-question Q_i and its corresponding sub-answer A_i .

3.2 Monte Carlo Tree Search Framework

In Figure 2(a), we employ MCTS to explore the reasoning space systematically. Each node in the search tree represents a reasoning step S_i , and edges represent the transitions between steps. The rollout iteration in MCTS involves four steps: Selection, Expansion, Rewarding, and Backpropagation. These steps are iteratively performed K times to explore the reasoning space and refine the search

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tree. The experiments in section 4.7 show that VReST efficiently utilizes additional iterations to refine its reasoning traces, and exhibits a test-time scaling law on multimodal reasoning tasks.

3.2.1 Selection 210

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In Figure 2(a)(1), we select a path in the search tree. Starting from the root node (original question Q), we recursively select child nodes according to the Upper Confidence Bound applied to Trees (UCT) algorithm (Kocsis and Szepesvári, 2006), which selects a node v by balancing exploration and exploitation:

$$UCT(v) = R(v) + c\sqrt{\frac{\ln N(p(v))}{N(v)}}, \quad (1)$$

where R(v) is the reward value of node v, N(v)is the visit count, p(v) is the parent node, and c is the exploration constant. The child node with the highest UCT value is recursively selected until a leaf node is reached.

3.2.2 Expansion

We generate new reasoning steps for the selected path S_t using LVLM. As shown in Figure 2(b), the prompt for generation is constructed as:

$$\mathcal{P}_{t-1} = [Q, S_1, \dots, S_{t-1}].$$
 (2)

Based on the prompt \mathcal{P}_{t-1} , LVLMs are prompted to generate w distinct reasoning steps S_t by increasing the temperature parameter of LVLMs:

$$\{S_{t,j}|j=1,\ldots,w\} = \text{LVLM}(\mathcal{P}_{t-1},I), \quad (3)$$

where w is the width of the tree.

Subsequently, the initial reward value of each child node is obtained using the Self-Reward mechanism described in Section 3.2.3. Then, we select the child node with the highest reward:

$$S_{t,\text{selected}} = \arg\max_{j} R(S_{t,j}),$$
 (4)

where $R(S_{t,i})$ denotes the reward value for the *j*-th child node $S_{t,j}$. The selected node $S_{t,\text{selected}}$ becomes the current node in the reasoning trace, and the generation process continues to generate S_{t+1} according to Equations (2)(3)(4).

As shown in Figure 2(a)(2), this process continues iteratively until either a terminal node is reached or the maximum depth D_{max} of the tree is achieved. As shown in the prompt in Section G.1,

when the sub-question generated by LVLM contains the span "Now we can answer the question", the node is considered to be a terminal node. In the case that the terminal node is reached, we stop the generation process and backpropagate the reward values as described in Section 3.2.4.

3.2.3 Rewarding

We introduce a Self-Rewarding mechanism to calculate the reward value of the new reasoning step S_t using two criteria: (1) Usefulness of all the subquestions on the reasoning trace. (2) Correctness of the last answer on the reasoning trace.

First, as shown in Figure 2(c), we concatenate each reasoning step prior to S_t on the selected reasoning trace to construct the Rewarding prompt:

$$\mathcal{P}_t = [Q, S_1, \dots, S_t]. \tag{5}$$

Then, we calculate the usefulness of all the subquestions R_1 and the correctness of the last answer R_2 , respectively, and then calculate their geometric mean as the reward value R of reasoning step S_t :

$$R_1 = P(\text{"Yes"} | [\mathcal{P}_t, \mathcal{P}_Q], I),$$

$$R_2 = P(\text{"Yes"} | [\mathcal{P}_t, \mathcal{P}_A], I),$$

$$R = \sqrt{R_1 R_2},$$
(6)

where $P(\text{"Yes"}|\cdot)$ represents the probability that the first token generated by LVLM is "Yes". \mathcal{P}_Q is "Are questions Q_1, \ldots, Q_t useful?". \mathcal{P}_A is "Is the answer A_t correct?".

3.2.4 Backpropagation

As shown in Figure 2(a)(4), when a terminal node S_T is reached, the reward values of each node are backpropagated through all nodes in the selected path, where the T is the number of reasoning steps in the selected path. For each node S_t in the path, where $t = 1, \ldots, T$, we update its statistics by aggregating the rewards in all future steps of S_t :

$$R(S_t) = Avg(\{R(S_i)\}_{i=t}^T), N(S_t) = N(S_t) + 1.$$
(7)

3.3 Final Reasoning Trace Selection

After completing K MCTS iterations, we select the final reasoning trace \mathcal{P}^* based on the trace rewards. There are three ways for the reasoning trace selection.

Greedy Trace. Starting from root node Q, we select the reasoning trace \mathcal{P}^* by greedily choosing the node with the highest reward at each step.

Methods	FQA	GPS	MWP	TQA	VQA	ALG	ARI	GEO	LOG	NUM	SCI	STA	ALL
QA	60.59	48.56	60.75	56.96	50.28	49.11	52.69	46.03	16.22	34.03	59.84	67.44	55.70
CoT	63.57	40.87	56.99	62.03	48.04	45.91	50.42	42.68	18.92	40.28	59.02	70.43	54.60
CoT-Vote	70.63	48.08	69.89	63.92	56.98	51.60	60.34	50.63	10.81	<u>51.39</u>	60.66	79.07	62.30
Best-of-N	67.66	44.71	59.68	58.86	54.75	48.75	54.96	46.03	13.51	43.06	56.56	75.42	57.70
Cantor	63.57	48.08	62.90	61.39	56.42	50.89	55.81	49.37	21.62	45.83	60.66	70.43	58.60
ТоТ	66.54	53.37	63.44	61.39	54.19	54.80	55.24	<u>54.39</u>	13.51	43.75	57.38	74.09	60.20
VReST	68.03	56.73	<u>72.04</u>	67.09	<u>58.10</u>	59.43	<u>62.61</u>	58.16	29.73	50.69	<u>67.21</u>	75.75	<u>64.50</u>
VReST-Vote	<u>69.14</u>	<u>51.44</u>	75.81	<u>66.46</u>	64.25	<u>54.45</u>	67.42	53.56	<u>27.03</u>	60.42	68.03	<u>77.74</u>	65.40

Table 1: Accuracy (%) on the testmini set of MathVista, where bold indicates the best results, underlines indicate the second-best. Task types: FQA: figure question answering, GPS: geometry problem solving, MWP: math word problem, TQA: textbook question answering, VQA: visual question answering. Mathematical reasoning types: ALG: algebraic reasoning, ARI: arithmetic reasoning, GEO: geometry reasoning, LOG: logical reasoning, NUM: numeric commonsense, SCI: scientific reasoning, STA: statistical reasoning. ALL: overall accuracy.

Best Trace. As shown in Figure 2(d), we calculate the reward value for each trace in the tree:

$$R(\mathcal{P}) = Avg(\{R(S_t) | S_t \in \mathcal{P}, t = 1, \dots, T\}).$$
(8)

And then select the trace with the highest value:

$$\mathcal{P}^* = \arg\max_{\mathcal{P}} R(\mathcal{P}),\tag{9}$$

where $R(\mathcal{P})$ denotes the reward value for the trace \mathcal{P} . **Best-Trace** is written **VReST** in Tables 1, 2, 3.

Trace Vote. Similar to CoT-Vote, after calculating the reward of all the reasoning traces by Equation (8), we select the n with the highest reward value. **Trace-Vote** is written **VReST-Vote** in Tables 1, 2, 3.

For the Greedy Trace and Best Trace, the final answer A_T^* is extracted from the terminal node S_T^* of the selected trace \mathcal{P}^* . For the Trace Vote, the final answer A_T^* is obtained by extracting the majority of the answers from the *n* selected traces. In practice, we observe that the Best Trace and Trace Vote strategies usually yield the best results.

4 Experiments

4.1 Datasets

We evaluate our approach on three visual reasoning datasets: **MathVista** (Lu et al., 2023), **Math-Vision** (Wang et al., 2024a) and **CharXiv** (Wang et al., 2024c). All datasets are evaluated using answer accuracy. See Appendix B for more details on the datasets.

4.2 Models

The LVLM used in this paper is Qwen2-VL-7B-Instruct (Wang et al., 2024b). The LVLM is utilized in three components: (1) Generating reasoning steps during expansion. (2) Calculation of R_1 in Rewarding method. (3) Calculation of R_2 in Rewarding method. The temperature of LVLM is 0.7, the top_p is 0.95.

The text-only LLM used in this paper is Qwen2.5-7B-Instruct (Yang et al., 2024). The textonly LLM is utilized in two components: (1) Evaluating whether the final answers and golden answers are consistent. (2) Replacing LVLM in the VReST in ablation experiments in Section 4.6. The temperature of text-only LLM is 0.7, the top_p is 0.95.

4.3 Baselines

We compare VReST with six baselines: **Question Answering (QA), Chain of Thought (CoT)** (Kojima et al., 2022), **CoT-Vote** (Wang et al., 2022), **Best-of-N** (Lightman et al., 2023), **Cantor** (Gao et al., 2024), **Tree of Thought (ToT)** (Yao et al., 2024). We control the parameters of the baseline methods to be consistent with VREST, doing our best to maintain a fair comparison. See Appendix C for more details on baselines.

4.4 Implementation Details of VReST

For each MCTS iteration, we maintain a maximum depth of $D_{max} = 8$ steps and perform K = 10total iterations to ensure adequate exploration of the reasoning space. The exploration constant c = 1in the UCT formula is set to balance exploration and exploitation during the search process. The width of the tree is w = 5. In the **VReST-Vote**, the selected number of reasoning traces is n = K. The prompts are shown in Appendix G.

4.5 Main Results

MathVista. The results presented in Table 1 clearly highlight the superior performance of VReST and VReST-Vote across various mathematical and visual reasoning tasks on the testmini sub-

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Methods	ALG	AnaG	Ari	CombG	Comb	Cnt	DescG	GrphT	Log	Angle	Area	Len	SolG	Stat	Торо	TransG	ALL
QA	<u>15.79</u>	15.79	10.53	21.05	0.00	5.26	5.26	21.05	15.79	57.89	15.79	36.84	15.79	15.79	15.79	<u>26.32</u>	18.42
СоТ	<u>15.79</u>	10.53	15.79	10.53	15.79	10.53	26.32	15.79	15.79	10.53	0.00	10.53	15.79	26.32	21.05	10.53	14.47
CoT-Vote	0.00	26.32	21.05	15.79	42.11	26.32	5.26	26.32	15.79	21.05	<u>31.58</u>	10.53	21.05	<u>31.58</u>	31.58	21.05	21.71
Best-of-N	5.26	<u>31.58</u>	0.00	21.05	21.05	26.32	26.32	15.79	15.79	36.84	26.32	21.05	10.53	21.05	15.79	10.53	19.08
Cantor	5.26	21.05	10.53	15.79	15.79	10.53	0.00	10.53	21.05	15.79	10.53	0.00	5.26	15.79	5.26	15.79	11.18
ToT	21.05	26.32	15.79	21.05	21.05	15.79	15.79	15.79	5.26	31.58	36.84	21.05	15.79	42.11	10.53	10.53	20.39
VReST	21.05	<u>31.58</u>	21.05	21.05	15.79	10.53	10.53	42.11	42.11	15.79	36.84	10.53	26.32	<u>31.58</u>	52.63	36.84	<u>26.64</u>
VReST-Vote	10.53	42.11	<u>15.79</u>	31.58	<u>21.05</u>	<u>21.05</u>	36.84	<u>36.84</u>	<u>26.32</u>	<u>42.11</u>	26.32	<u>31.58</u>	15.79	<u>31.58</u>	<u>36.84</u>	<u>26.32</u>	28.29

Table 2: Accuracy scores (%) on the testmini subset of MATH-Vision. Alg: algebra, AnaG: analytic geometry, Ari: arithmetic, CombG: combinatorial geometry, Comb: combinatorics, Cnt: counting, DescG: descriptive geometry, GrphT: graph theory, Log: logic, Angle: metric geometry - angle, Area: metric geometry - area, Len: metric geometry-length, SolG: solid geometry, Stat: statistics, Topo: topology, TransG: transformation geometry.

357 set of MathVista. VReST achieves notable success, outperforming other methods in tasks such as MWP with 72.04%, SCI with 67.21%, and 359 STA with 75.75%. Additionally, the VReST-Vote method further elevates accuracy, particularly in 361 tasks such as MWP (75.81%), VQA (64.25%), and 362 NUM (60.42%), by aggregating multiple reasoning 363 traces through a voting mechanism. This reflects 365 VReST's robust ability to handle complex reasoning challenges that require logical, numerical, and scientific understanding. Its strength lies in the combination of MCTS for systematic exploration of reasoning traces and the Self-Reward mechanism, which dynamically evaluates reasoning steps based on sub-question utility, answer correctness and visual information. This allows VReST to refine its reasoning traces over time, enhancing 373 performance in a diverse set of tasks 374

MathVision. In Table 2, we evaluate various 375 methods on the testmini subset of the MATH-376 Vision dataset, which includes a range of mathematical and visual reasoning tasks. VReST achieves an overall accuracy of 26.64%, outperforming baseline and competitive methods, with notable results in GrphT (42.11%), Log (42.11%), and Topo 382 (52.63%), outperforming other methods such as QA, CoT, and ToT in these tasks, showcasing its ability to handle complex geometric reasoning. The VReST-Vote method further improves this to 28.29%, excelling in tasks like AnaG (42.11%), De-386 scG (36.84%), and Angle (42.11%). This demonstrates the effectiveness of the voting mechanism in aggregating diverse reasoning traces, leading to more reliable and accurate solutions. The integra-391 tion of MCTS and the Self-Reward mechanism in VReST allows it to effectively explore reasoning traces and dynamically adjust to improve performance, particularly in challenging areas like combinatorics and graph theory.

CharXiv. The results presented in Table 3 on the validation set of the CharXiv dataset clearly highlight the superiority of VReST and VReST-Vote across various domains, particularly in tasks involving complex visual reasoning and interpretation of charts and graphs. VReST achieves an overall accuracy of 33.10%, outperforming baseline methods, with notable results in Text in General (54.55%), Num in Chart (33.62%), and Mathematics (40.74%). VReST-Vote improves this to 38.10%, with strong performances in Text in General (61.62%), Num in Chart (39.22%), and Electrical Engineering and Systems Science (45.38%), demonstrating the effectiveness of the voting mechanism in aggregating diverse reasoning traces. The results indicate that VReST-Vote not only achieves superior performance in individual tasks but also significantly outperforms other methods across a wide range of subjects, highlighting its robustness in addressing the challenges of complex visual reasoning in the CharXiv dataset.

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4.6 Ablation Results

The importance of visual information. To illustrate the importance of visual information, we conducted ablation experiments shown in Figure 3a. As described in Section 4.2, the LVLM is utilized in three components. We performed ablation experiments by replacing LVLM with text-only LLM in each component separately. The study evaluates different configurations of visual and text-only components across three datasets: Math-Vista, MathVision, and CharXiv. The configuration where all components (reasoning generation, R1, and R2 reward computation) use LVLM achieves the highest performance across all datasets. When visual components are partially replaced with textonly components, the performance drops significantly. The ablation study clearly demonstrates that

Methods	Text in Chart	Text in General	Num in Chart	Num in General	CS	EC	EESS	MATH	PHY	QB	QF	STA	ALL
QA	31.82	38.38	28.45	22.27	33.33	30.43	31.93	29.63	35.43	25.40	21.55	27.43	29.50
СоТ	29.09	40.40	26.72	18.78	21.43	27.54	32.77	29.63	26.77	23.81	23.28	<u>33.63</u>	27.30
CoT-Vote	32.95	45.45	28.88	22.71	26.98	28.99	33.61	30.37	39.37	29.37	25.86	32.74	30.90
Best-of-N	34.09	48.48	28.02	24.02	33.33	30.43	30.25	35.56	<u>38.58</u>	31.75	24.14	29.20	31.80
Cantor	27.73	43.43	30.60	23.58	26.19	27.54	27.73	31.11	37.01	24.60	30.17	27.43	29.00
ТоТ	34.09	45.45	33.62	20.96	30.95	26.81	36.97	31.85	35.43	29.37	26.72	39.82	32.10
VReST	33.64	<u>54.55</u>	33.62	22.27	30.95	<u>31.16</u>	<u>41.18</u>	40.74	33.86	26.98	<u>30.17</u>	29.20	<u>33.10</u>
VReST-Vote	37.95	61.62	39.22	27.07	37.30	38.41	45.38	43.70	<u>38.58</u>	31.75	36.21	32.74	38.10

Table 3: Accuracy scores (%) on the Validation set of CharXiv. CS: Computer Science, EC: Economics, EESS: Electrical Engineering and Systems Science, MATH: Mathematics, PHY: Physics, QB: Quantitative Biology, QF: Quantitative Finance, STA: Statistics.



Figure 3: (a) Ablation results of different configurations of visual and text-only components. (V, V, V) represents using LVLM for all components (reasoning generation, R1, and R2 rewarding), while T denotes using text-only LLM. (b) Ablation results from different reward methods. w/o R1 and w/o R2 denote R1 or R2 is omitted, respectively. w/o PRM indicates that the Process Reward Model is no longer employed.

visual information is indispensable for LVLM to solve complex visual reasoning tasks. Our method, VReST, leverages Large Vision-Language Models (LVLM) to integrate visual and textual information seamlessly, enabling the generation of accurate and reliable reasoning traces. Specifically, the Self-Rewarding mechanism in VReST relies on both visual and textual information to evaluate reasoning traces effectively. Without visual input, the model loses the ability to make informed decisions, especially in tasks that involve interpreting visual elements such as charts, graphs, and geometric figures. This is particularly evident in datasets like MathVision and CharXiv, where visual reasoning plays a central role.

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449 The importance of reward method. To demonstrate the effectiveness of our Self-Rewarding 450 mechanism, we conducted ablation experiments 451 as shown in Figure 3b. Specifically, w/o R1 and 452 w/o R2 denote the scenarios where R1 or R2 is 453 454 omitted during the calculation of the reward value, respectively. w/o PRM indicates that the Process 455 Reward Model is no longer employed; instead, only 456 the reward value of the terminal node is computed, 457 while the reward value of non-terminal nodes is 458

uniformly set to 0.5. In this case, the reward of nonterminal nodes is updated solely through the backpropagation mechanism. The ablation study clearly demonstrates that the Self-Rewarding mechanism in VReST-Vote is indispensable for achieving high accuracy in complex reasoning tasks. The R1 reward ensures that each reasoning step is evaluated and guided toward correctness, while the R2 reward evaluates the final answer to ensure the overall trace is accurate. The Process Reward Method (PRM) plays a crucial role in assigning intermediate rewards to non-terminal nodes, guiding the reasoning process effectively. Omitting any of these components leads to a significant performance drop, highlighting the importance of a comprehensive reward mechanism.

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The importance of selection method. We analyze the results of different selection methods for final trace evaluation, as presented in Table 4. As described in Section 3.3, there are three methods for the selection of the final trace and evaluation of the final answer: Greedy-Trace, Best-Trace, and Trace-Vote. The study evaluates three methods across three datasets: MathVista, Math-Vision, and CharXiv. The results of the ablation



Figure 4: The impact of the number of samples or iterations. It shows that our VReST exhibits a better test-time scaling law than other SOTA methods in multimodal reasoning tasks.

Methods	MathVista	MathVision	CharXiv
Trace-Vote	65.40	28.29	38.10
Best-Trace	64.50	26.64	33.10
Greedy-Trace	60.00	23.03	31.30

Table 4: Results of different selection methods.

484 study on selection methods demonstrate that the Trace-Vote method is the most effective for final 485 trace evaluation. By leveraging a voting mecha-486 nism to aggregate multiple high-reward reasoning 487 traces, Trace-Vote achieves superior performance across all datasets. It effectively mitigates the risk 489 of selecting a suboptimal trace by considering a 490 broader range of potential solutions. In contrast, 491 the Greedy-Trace method relies on a single trace se-492 lection strategy, suffering from a significant perfor-493 mance drop. This indicates that a greedy approach 494 may not fully capture the complexity of the reason-495 ing process, especially in tasks that require deep vi-496 sual and logical reasoning. The Best-Trace method, 497 while performing better than Greedy-Trace, is still 498 outperformed by Trace-Vote. This suggests that 499 selecting the single best trace, although effective, 500 does not fully exploit the potential of multiple high-501 reward traces. The voting mechanism in Trace-Vote 502 provides a more robust and reliable way to deter-503 mine the final answer, especially in complex tasks that involve multiple reasoning steps.

4.7 Multimodal Test-Time Scaling Law

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507To investigate the impact of different methods508on the number of samples or iterations, we con-509ducted hyperparameter experiments as shown in510Figure 4 by controlling the number of samples511in each method. The study evaluates the perfor-512mance of CoT-Vote, Best-of-N, ToT, and VReST-

Vote across three datasets: MathVista, MathVision, and CharXiv. The x-axis of Figure 4 corresponds to different hyperparameters across various baseline methods. Specifically, in CoT-Vote, the x-axis represents the number of votes n. In Best-of-N, the x-axis denotes the number of sampled reasoning traces n. In ToT, the x-axis represents the width of the tree w. In VReST-Vote, the x-axis corresponds to the number of iterations for MCTS K. 513

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It can be observed that VReST-Vote consistently outperforms the baselines across all numbers of samples or iterations. The superior performance of VReST-Vote can be attributed to its Monte Carlo Tree Search (MCTS) algorithm, which efficiently explores the search space and converges to optimal solutions with relatively fewer iterations. Moreover, VReST-Vote shows a more significant performance improvement than the baselines as the number of iterations increases, indicating that it efficiently utilizes additional iterations to refine its reasoning traces. This proves that our method exhibits a better test-time scaling law on multimodal reasoning tasks.

5 Conclusion

In this paper, we presented VReST, a novel trainingfree approach that enhances reasoning capabilities in Large Vision-Language Models through Monte Carlo Tree Search and Self-Reward mechanism. Through extensive experiments on three challenging multimodal mathematical reasoning datasets, VReST significantly outperformed existing prompting methods and achieved state-of-the-art performance. Furthermore, we validate test-time scaling laws' applicability to multimodal tasks, offering a promising direction to improving LVLM performance for future research.

549 Limitations

Although our results already outperform baselines
overall, our work still suffers from the following
limitations.

Self-Reward Mechanism To ensure a fair com-553 parison with baseline methods, we designed the 554 self-reward mechanism to use the LVLM itself 555 for reward scoring, without introducing additional 556 models. This approach aligns with the training-557 free nature of our method, enabling quick deployment without the need for training a separate reward model. However, this mechanism heavily 560 relies on the LVLM's own judgments to evaluate the quality of reasoning traces. As a result, there is a risk that model biases or errors could propagate through the reward process, potentially affecting 564 the accuracy and reliability of the reasoning pro-565 cess. Future work could involve training an addi-566 tional reward model to assist the LVLM's reasoning 567 process, helping to mitigate potential biases and improve the accuracy of the reward signal. 569

570 **Computational Cost** The MCTS approach re-571 lies on multiple iterations and extensive tree explo-572 ration, resulting in significant computational over-573 head compared to current prompting methods. This 574 increased cost may limit the scalability of VReST 575 for large-scale applications. In future work, we 576 aim to address this by incorporating pruning strate-577 gies or early stopping techniques within the tree 578 search process, which could help reduce the com-579 putational burden while maintaining performance.

Model Dependency Currently, we have only 580 evaluated the effectiveness of VReST on the 581 Qwen2-VL-7B-Instruct model. Although this 582 model demonstrates the benefits of our approach, the effectiveness of VReST may vary across different LVLMs, especially models with different 585 architectures, scales, or training regimens. In fu-586 ture work, further experimentation on a wider range 587 of LVLMs will be essential to determine the gener-588 alizability of our approach.

590Dataset DependencyOur experiments primarily591focus on a limited set of visual reasoning datasets.592While VReST shows promising results on these593datasets, its performance on other datasets with594different characteristics, such as those involving595diverse types of reasoning or tasks outside visual596reasoning, remains unexplored. Expanding our597evaluation to a broader set of datasets will help as-

sess the robustness and versatility of VReST across different multimodal tasks.

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A Discussion

In this section, we will address the following Discussion Questions (**DQ**) to elucidate our contributions more clearly.

DQ1: Why do we not need any additional baselines?

See Appendix C, where we list all the baselines used to compare with our proposed method. However, we did not compare with other methods using MCTS.

At present, many MCTS-based methods require training the LLM itself or a reward model, such as ReST-MCTS* (Zhang et al., 2024a) and LLaMA-Berry (Zhang et al., 2024b), among others. Our work, as an initial endeavor to introduce MCTS into multimodal reasoning tasks, primarily focuses on training-free methods. To ensure a fair comparison, we have opted not to incorporate additional reward models, thereby maintaining the comparability of our experiments with baseline methods.

Consequently, under the training-free setting, we have taken into account as many methods as possible, and we believe that the current baselines are sufficiently comprehensive.

DQ2: Why the datasets we have chosen are sufficient to demonstrate the effectiveness of VReST?

See Appendix B, where we list all the datasets used in this paper. While our primary evaluation focuses on mathematical reasoning, the datasets we selected (MathVista, MathVision, and CharXiv) actually cover a broad spectrum of multimodal reasoning tasks. For example:

MathVista includes various task types like figure question answering (FQA), geometry problem solving (GPS), and visual question answering (VQA).

CharXiv contains diverse chart understanding tasks involving both descriptive and complex reasoning questions.

MathVision covers 16 distinct mathematical disciplines including topology, graph theory, and geometric reasoning.

Therefore, these three datasets can largely prove the effectiveness of our method.

B Datasets

We evaluate our approach on three visual reasoning datasets. The details are given below:

MathVista (Lu et al., 2023) is a comprehensive benchmark dataset designed to evaluate the mathematical reasoning capabilities of foundation models in visual contexts. It consists of 6,141 examples derived from 28 existing multimodal datasets and 3 newly created datasets: IQTest, FunctionQA, and PaperQA. These datasets address the need for evaluating logical reasoning on puzzle test figures, algebraic reasoning over functional plots, and scientific reasoning with academic paper figures, respectively. In this paper, we used Mathvista testmini, which includes 1000 samples.

MathVision (Wang et al., 2024a) is a meticulously curated collection of 3,040 high-quality mathematical problems with visual contexts, sourced from real math competitions such as Math Kangaroo, AMC, and AIME. Spanning 16 distinct mathematical disciplines and graded across 5 levels of difficulty, it provides a comprehensive benchmark for evaluating the multimodal mathematical reasoning capabilities of large multimodal models (LMMs). The dataset emphasizes both visual perception and mathematical reasoning, covering topics like algebra, topology, and graph theory, and includes both multiple-choice and free-form questions. In this paper, we used MathVision testmini, which includes 304 samples.

CharXiv (Wang et al., 2024c) is a comprehensive evaluation suite designed to rigorously assess the chart understanding capabilities of Multimodal Large Language Models. Comprising 2,323 natural, diverse, and challenging charts sourced from arXiv scientific papers, CharXiv addresses the limitations of existing datasets that often rely on oversimplified, homogeneous charts and templatebased questions, leading to an over-optimistic assessment of model performance. The dataset includes two types of questions: descriptive questions that focus on extracting basic chart elements and reasoning questions that require synthesizing complex visual and numerical information across charts. To better evaluate the model's ability to solve complex problems, we use all reasoning questions from the validation set of CharXiv, which includes 1,000 samples.

C Baselines

We compare VReST with six baseline methods. We control the parameters of the baseline method to be consistent with VREST, doing our best to maintain a fair comparison.

Question Answering (QA). It is a straightforward prompting method where the model is given

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steps.

in Appendix G.1.

CoT-Vote is n = 10.

simpler sub-questions and solve them sequentially. In this paper, we implement zero-shot CoT by ex-

plicitly asking the model to decompose the original

question into sub-questions. To ensure a fair com-

parison, for the generation of sub-questions and

answers in CoT, we use the same prompt as shown

CoT-Vote (Wang et al., 2022). It extends the

CoT approach by generating multiple reasoning

chains and selecting the most frequent answer from

among them. This method is also known as Self-

Consistency. In this paper, the number of votes in

native to CoT-Vote, where the reasoning trace with the highest reward value is selected from multiple

reasoning traces as the final answer. We calculate

the reward value for the last step of each reason-

ing trace in CoT-Vote using the rewarding method

described in Section 3.2.3, and then select the one

with the highest value. In this paper, the number of

a decision maker to break down the question into different parts, which are then assigned to different

experts (also LVLMs) for processing, and finally

the results of each expert are summarized to obtain

produce the same method as in ToT's paper. When

generating each reasoning step, we sample mul-

tiple different child nodes, and then calculate the

reward value of each child node through the re-

warding method in Section 3.2.3. The node with

the highest value is then iteratively selected in a

greedy decoding-like manner until a terminating

node is generated. To ensure a fair comparison, for

the generation of sub-questions and answers in ToT,

we use the same prompt as shown in Appendix G.1.

The width of the tree in ToT is w = 10, and the

Tree of Thought (ToT) (Yao et al., 2024). We re-

Cantor (Gao et al., 2024). It uses an LVLM as

reasoning traces in Best-of-N is n = 10.

Best-of-N (Lightman et al., 2023). It is an alter-

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D Algorithm

the final answer.

Algorithm 1 below presents the algorithm used in our VReST framework. 917

maximum depth in ToT is $D_{max} = 8$.

a question and image and expected to generate a Methods **MathVista MathVision** CharXiv direct answer without any intermediate reasoning QA 1.44 2.46 1.84 CoT 7.28 10.57 9.04 CoT-Vote 15.32 24.18 19.36 Chain of Thought (CoT) (Kojima et al., 2022). Best-of-N 18.56 28.50 21.07 It is a prompting technique that guides the model Cantor 21.46 36.39 32.67 to break down complex questions into a series of ToT 34.39 45.89 39.29

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VReST

Table 5: The average time (in seconds) for the different methods to complete a sample.

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Ε Time efficiency analysis

Table 5 shows the average time (in seconds) for the different methods to complete a sample. Note that VReST and VReST-Vote only differ in the Final Reasoning Trace Selection stage, so both take the same time to complete a sample.

While VReST does require more computation than standard CoT approaches, we believe the performance gains justify the additional cost.

\mathbf{F} **More Experimental Results**

As shown in Tables 6, 7, 8, we also provide experimental results on the smaller model Qwen2.5-VL-3B-Instruct. Experimental results show that our method is still effective on smaller scale models.

G **Prompt Templates**

To ensure a fair comparison, for the generation of reasoning steps in VReST, CoT, CoT-Vote, and ToT, we use the same prompts as in the previous work (Hao et al., 2023), as shown in Appendix G.1. For the prompts in Appendix G.1, G.2, and G.3, the samples in the prompts are only used to guide the LVLM in generating content in the expected format, and no multimodal samples are included in the prompts. Therefore, we consider the method in this paper to be a zero-shot prompting technique. For all methods in this paper, we use the prompt template in Appendix G.4 to judge whether the final answer is correct or not.

G.1 Reasoning Step Generation

As shown in the Prompt Template of Reasoning 947 Step Generation, we input k-1 sub-questions and 948 corresponding answers and let LVLM continue to 949 generate the k-th sub-question and corresponding 950 answer. Model-generated content is annotated in 951 blue. 952 Algorithm 1 VReST

Require: Question Q, Image I, Max iterations K, Max depth D_{max} , Tree width w **Ensure:** Final reasoning trace \mathcal{P}^* and answer A^* 1: function VREST (Q, I, K, D_{max}, w) Initialize search tree \mathcal{T} with root node Q2: 3: for k = 1 to K do ▷ UCT-based selection 4: $\mathcal{P}_{\text{selected}} \leftarrow \text{SELECTION}(\mathcal{T})$ $\mathcal{P}_{\text{expanded}} \leftarrow \text{EXPANSION}(\mathcal{P}_{\text{selected}}, w, D_{\text{max}})$ 5: $R \leftarrow \text{SELFREWARDING}(\mathcal{P}_{\text{expanded}}, I)$ 6: BACKPROPAGATION ($\mathcal{P}_{expanded}, R$) 7: end for 8: 9: $\mathcal{P}^* \leftarrow \text{FINALTRACESELECTION}(\mathcal{T})$ return \mathcal{P}^*, A^* 10: 11: end function 12: **function** SELFREWARDING(\mathcal{P} , I) $\mathcal{P}_t \leftarrow [Q, S_1, \dots, S_t]$ 13: $R_1 \leftarrow P(\text{"Yes"}|[\mathcal{P}_t, \mathcal{P}_Q], I)$ > Question usefulness 14: $R_2 \leftarrow P(\text{"Yes"}|[\mathcal{P}_t, \mathcal{P}_A], I)$ 15: ▷ Answer correctness 16: return $\sqrt{R_1R_2}$ 17: end function function EXPANSION(\mathcal{P}, w, D_{max}) 18: $\mathcal{P}_{current} \leftarrow \mathcal{P}$ 19: while not terminal and $|\mathcal{P}_{current}| < D_{max}$ do 20: $\{S_{t,j}\}_{j=1}^w \leftarrow \text{LVLM}(\mathcal{P}_{\text{current}}, I)$ 21: $R_j \leftarrow \text{SELFREWARDING}([S_{t,j}], I) \text{ for } j = 1, \dots, w$ 22: $S_{t,\text{selected}} \leftarrow \arg \max_j R_j$ 23: 24: $\mathcal{P}_{\text{current}} \leftarrow \mathcal{P}_{\text{current}} \cup \{S_{t, \text{selected}}\}$ end while 25: return $\mathcal{P}_{current}$ 26: 27: end function function FINALTRACeSelection(\mathcal{T}) 28: 29: for each trace \mathcal{P} in \mathcal{T} do $R(\mathcal{P}) \leftarrow \operatorname{AVG}(\{R(S_t) | S_t \in \mathcal{P}\})$ 30: end for 31: $\mathcal{P}^* \leftarrow \arg \max_{\mathcal{P}} R(\mathcal{P})$ 32: ▷ Best Trace strategy $A^* \leftarrow$ extract answer from terminal node of \mathcal{P}^* 33: return \mathcal{P}^*, A^* 34: 35: end function

(a)	 + 11 7 2 6 17 13 8 10 Question: Every box shows the result of the addition of the numbers on the very left and on the very top (for example: 6+2=8). Which number is written behind the question mark? Ground Truth Answer: 15 											
Сот	Sub- Q_1 : What is the pattern being applied in ea Sub- A_1 : The numbers in the boxes following this are 17 (6+11), 8 (7+2), 21 (13+8), and ? (unknow answer is that the pattern is adding the bottom le top right numbers.	ch box? pattern m). The ft and $\mathbf{Sub-Q_2}$: Which numbers from the pattern are relevant for solving the problem? $\mathbf{Sub-A_2}$: The relevant numbers for solving the unknown box are 10 and 13. The answer is 10 and 13.										
тот	Sub- Q_1 : What is the rule for filling the boxes?Sub- A_1 : The number in each box is the sum of the number from the top row and the number from the left column. The answer is: Box = Top Number + Left Number.	Sub- Q_2 : Are the known boxes operations correct?Sub- Q_3 : What is the value of the number written behind the question mark?Sub- A_2 : Let's verify: $6 + 11 = 17, 6 + 7 =$ $13, 6 + 2 = 8$. All of them are correct. The answer is' verified '.Sub- A_3 : The number above the question mark should be 4, because $6+4=10$. So $4+7=11$. The final answer is 11.										
VReST	Sub- Q_1 : What is the rule for filling the boxes?Sub- A_1 : The number in each box is the sum of the number from the top row and the number from the left column. The answer is:Box = Top Number + Left Number.	Sub- Q_2 : What is the missing number in the left column?Sub- Q_3 : What number is in the missing box?Sub- A_2 : From the bottom-right box, we know ?+2=10, so ?=10-2=8. The answer is: The missing number is 8.Sub- A_3 : Using the rule 8+7=15, the missing box contains 15. The answer is: 15.										

(b)	Question: How many diffe Ground Truth Answer: 6	Question: How many different digits can you find in this picture? Ground Truth Answer: 6											
Сот	Sub-Q_1: What digits are visible in the drawing? Sub-A_1: The digits visible in the drawing are 0, 5, and 3. The answer is 0, 5, and 3.	Sub-Q ₂ : How ma present in the dra Sub-A ₂ : The unit 3, which gives us answer is 3.	any unique digits are awing? que digits are 0, 5, and s 3 unique digits. The	Sub-Q ₃ : Now we can answer the questio How many different digits can you find in this picture? Sub-A ₃ : There are 3 different digits in the picture. The final answer is 3.									
тот	Sub- Q_1 : What components of the drawing represent digits?Sub- A_1 : The digits in the drawing appear in various parts, including the face (0 and 5) and the feet (3). The answer is 0, 5, and 3.	Sub-Q ₂ : Are then the drawing? Sub-A ₂ : Yes, the eyes, but it is stil unique digit. The	re any repeated digits in e digit 0 is repeated in the I counted as a single e answer is yes.	Sub-Q ₃ : How many unique digits are present in total? Sub-A ₃ : After removing duplicates, the digits are 0, 5, and 3, which gives us 3 unique digits. The answer is 3.									
VReST	$Sub-Q_1$: What digits can be identified in the drawing? $Sub-Q_2$: Are the digits on the drawing? $Sub-A_1$: The digits visible in the drawing are 0, 5, 3, and 2. The answer is 0, 5, 3, and 2. $Sub-A_2$: Yes, b there are also answer is: The	ere any other awing? esides 0, 5, 3, 2, 8 and 9. The digits are 8 and 9.	Sub- Q_3 : How many unic digits are present in tota Sub- A_3 : The unique digi 5, 3, 2, 8 and 9. which m unique digits. The answ	que l? its are 0, nakes 6 rer is 6.	Sub-Q4: Now we can answer the question: How many different digits can you find in this picture? Sub-A4: There are 6 different digits. The final answer is 6.								

(c)	Question: Every box shows the result of the addition of the numbers on the very left and on the very top (for example: \$6+2=8\$). Which number is written behind the question mark? Ground Truth Answer: 6											
Сот	Sub-Q ₁ : What does the second Sub-A ₁ : The sum of three circ each circle represents 4. The a	line tell us? les is 12, so answer is 4.	Sub-Q ₂ : What is th Sub-A ₂ : 4+Star+H Star+Heart=11. Th	he first line equation? leart=15, so he answer is 11.	Su W Su co Th	Ib-Q_3: Now we can answer the question: hat number does the star represent? Ib-A_3: By solving the equation, we can nclude that the star represents 7 . In final answer is 7.						
тот	Sub- Q_1 : What equation can we the rows?Sub- A_1 : Circle + Star + Heart = Circle + Star = 12, Star + 2 × H answer is the three equations at	write based on 15, 2 × eart = 16.The bove.	Sub-Q ₂ : What is the and Heart? Sub-A ₂ : From the Circle + Star = 12, Circle = 3, we find	he value of the Circle second equation: 2 × and substituting I Heart = Circle + 3 = 6	Su Su int so	Ib-Q_3: What is the value of the Star? Ib-A_3: Substitute Circle = 3 and Heart = 6 o the first equation: Circle + Star + Heart 15, which becomes: 3 + Star + 6 = 15, Star = 6.The answer is 6.						
VReST	Sub- Q_1 : What does the second line tell us? Sub- A_1 : The sum of three circles is 12, so each circle represents 4. The answer is 4.	Sub- Q_2 : What from row 1 usin Sub- A_2 : Since s + h = 15, the The answer is	can we determine ag the circle value? circle=4, and 4 + refore $s + h = 11$. 11 Sub-Q_3: What can we determine from row 3? Sub-A_3: Since $s + h + h$ 16, and we know $s + h$ 11			Sub- Q_4 : Now we can answer the question: What number does the star represent? Sub- A_4 : Since s + h = 11 and h = 5, then s = 6. Therefore, the star represents 6. The answer is 6.						

Figure 5: Case study comparing the reasoning results of CoT, ToT, and VReST frameworks. (a) involves determining the missing value in a grid based on the summation rule. (b) involves identifying all unique digits in a drawing based on visual patterns. (c) involves determining the missing value in a grid based on algebraic equations.

Methods	FQA	GPS	MWP	TQA	VQA	ALG	ARI	GEO	LOG	NUM	SCI	STA	ALL
QA	66.91	64.42	58.60	53.16	51.40	56.23	52.12	61.92	21.62	39.58	62.30	71.10	59.90
СоТ	65.43	63.46	56.99	51.90	50.84	55.52	50.99	60.67	18.92	39.58	60.66	69.44	58.70
CoT-Vote	69.89	67.79	65.05	58.86	55.31	60.50	57.51	65.27	29.73	43.75	68.85	74.42	64.20
Best-of-N	69.52	66.35	60.75	55.06	53.07	58.01	54.39	65.27	29.73	41.67	64.75	72.43	62.00
Cantor	69.14	68.75	61.29	58.86	54.19	61.21	55.24	66.53	24.32	43.75	66.39	73.75	63.30
ToT	69.14	70.19	67.74	60.13	57.54	63.35	58.64	67.36	24.32	47.22	68.03	74.42	65.60
VReST	74.35	71.15	67.20	58.86	55.31	64.41	59.21	67.78	37.84	45.14	66.39	77.08	66.50
VReST-Vote	72.12	72.12	67.20	63.92	58.10	65.48	60.34	69.04	40.54	48.61	72.13	74.75	67.40

Table 6: Accuracy scores (%) on the testmini subset of MathVista on the Qwen2.5-VL-3B-Instruct.

Methods	ALG	AnaG	Ari	CombG	Comb	Cnt	DescG	GrphT	Log	Angle	Area	Len	SolG	Stat	Торо	TransG	ALL
QA	26.32	10.53	21.05	26.32	5.26	10.53	31.58	10.53	26.32	42.11	15.79	26.32	15.79	21.05	10.53	26.32	20.39
CoT	26.32	10.53	15.79	26.32	0.00	5.26	26.32	10.53	26.32	31.58	10.53	21.05	15.79	15.79	5.26	26.32	17.11
CoT-Vote	26.32	15.79	26.32	31.58	10.53	10.53	31.58	10.53	26.32	57.89	15.79	26.32	15.79	26.32	10.53	26.32	23.03
Best-of-N	31.58	10.53	21.05	26.32	5.26	10.53	36.84	10.53	26.32	42.11	15.79	26.32	15.79	26.32	10.53	26.32	21.38
Cantor	21.05	5.26	21.05	15.79	5.26	10.53	26.32	5.26	15.79	31.58	15.79	15.79	5.26	10.53	10.53	26.32	15.13
ToT	31.58	21.05	26.32	26.32	10.53	10.53	31.58	26.32	26.32	42.11	21.05	26.32	15.79	26.32	10.53	26.32	23.68
VReST	42.11	15.79	21.05	31.58	15.79	15.79	31.58	26.32	31.58	57.89	15.79	31.58	31.58	26.32	15.79	36.84	27.96
VReST-Vote	31.58	15.79	31.58	31.58	15.79	31.58	47.37	26.32	26.32	57.89	26.32	36.84	26.32	31.58	15.79	26.32	29.93

Table 7: Accuracy scores (%) on the testmini subset of MATH-Vision on the Qwen2.5-VL-3B-Instruct.

G.2 R1 Rewarding

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As shown in the Prompt Template of Calculating Usefulness of All the Sub-questions, we feed the current sub-questions and the latest sub-question into LVLM and let it judge whether the new subquestion is useful or not. Model-generated content is annotated in blue.

G.3 R2 Rewarding

As shown in the Prompt Template of Calculating Correctness of the last Answer, we feed all the current sub-questions and their corresponding answers into LVLM and let it judge whether the last answer is correct or not. Model-generated content is annotated in blue.

G.4 Answer Evaluation

As shown in the Prompt Template for answer evaluation, we feed the predicted answer together with the ground truth into the text-only LLM and let it judge whether the predicted answer is correct or not.

H Case Study

Figure 5 evaluates the capability of VReST in solving a series of multimodal reasoning problems involving numerical and visual patterns. The tasks
test the ability of reasoning frameworks to interpret
relationships, verify intermediate steps, and derive
accurate conclusions across diverse scenarios.

To address these problems, we compare three frameworks: CoT, ToT, and our proposed VReST. In Case 1, which involves summing corresponding values from a grid to determine a missing number, CoT incorrectly calculates 10+13=23, failing to verify intermediate results like 6+11=17. ToT improves by adopting a tree structure but still misjudges node selection, concluding an incorrect answer of 11. In contrast, VReST uses MCTS to explore alternatives systematically, accurately deriving 8+7=15 as the solution.

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In Case 2, which requires identifying unique digits in a drawing, CoT lists visible digits as 0,5,3 but overlooks others like 2,8,9, resulting in an incomplete answer of 3. ToT detects additional digits but fails to verify their uniqueness, producing an erroneous total of 6. VReST, leveraging visual clues such as digits on the face and feet, systematically identifies all unique digits 0,5,3,2,8,9, arriving at the correct answer of 6.

In Case 3, which involves solving a grid of algebraic equations, CoT's linear reasoning misses critical steps, leading to an incorrect answer of 7. ToT applies tree-based reasoning but inadequately propagates constraints, yielding 11 as the result. VReST, however, integrates equations like 4+7+?=11 and verifies intermediate solutions, correctly determining the missing value as 6.

We demonstrate a bad case from Figure 6 where, despite the final output from VReST being incorrect, the root cause of the error lies in the in-

Methods	Text in Chart	Text in General	Num in Chart	Num in General	CS	EC	EESS	MATH	PHY	QB	QF	STA	ALL
QA	30.45	47.47	31.90	21.83	30.95	32.61	27.73	31.11	34.65	30.95	27.59	27.43	30.50
CoT	28.18	44.44	29.31	20.96	28.57	29.71	25.21	28.89	33.86	27.78	26.72	25.66	28.40
CoT-Vote	31.82	49.49	33.19	24.02	33.33	34.06	30.25	31.85	36.22	32.54	27.59	30.09	32.10
Best-of-N	32.73	48.48	34.05	25.33	31.75	34.06	29.41	34.07	35.43	33.33	33.62	30.97	32.90
Cantor	28.18	44.44	31.47	21.40	29.37	31.88	26.05	30.37	33.07	28.57	25.00	26.55	29.00
ТоТ	33.41	47.47	37.93	24.45	33.33	36.23	30.25	34.81	37.01	33.33	31.03	33.63	33.80
VReST	34.32	51.52	36.21	26.20	33.33	36.96	35.29	36.30	36.22	33.33	31.03	33.63	34.60
VReST-Vote	34.32	52.53	35.78	31.00	34.92	39.86	36.97	34.07	40.16	35.71	30.17	32.74	35.70

Table 8: Accuracy scores (%) on the Validation set of CharXiv on the Qwen2.5-VL-3B-Instruct.

<imagel>:</imagel>	Sub- Q_1 : What was the original shape of the paper?Sub- A_1 : The original shape of the paper was a square. The answer is a square.
<image2>: A B C B C C C C C C C C C C C C C C C C</image2>	Sub- Q_2 : How many pieces is the square cut into?Sub- A_2 : The square is cut into three pieces. The answer is three pieces.
Question: A square piece of paper has been	Sub-Q ₃ : What are the two visible pieces shown in the image? Sub-A ₃ : The two visible pieces shown in the image are a small square and a more complex angular shape. The answer is a small square and a complex angular shape.
Ground Truth Answer: A	Sub- Q_4 : Now we can answer the question: What is the third piece? Sub- A_4 : The third piece is the shape that completes the square, and based on the analysis of the pieces, the answer is the shape that fits with the given cut. The third
	piece is likely option C from the provided choices. The final answer is option C.

Figure 6: Bad case of VReST frameworks.

sufficient granularity of problem decomposition. While VReST is capable of breaking down the 1012 1013 problem into sub-questions, and each individual sub-question does not provide incorrect answers, 1014 the decomposition itself does not significantly con-1015 tribute to the final answer. Moreover, the difficulty 1016 of the problem plays a critical role in this failure. 1017 The question belongs to the Level 5 category in the 1018 dataset, which is notably challenging and requires a more sophisticated and nuanced breakdown. In 1020 this case, the lack of depth in the decomposition did not equip the LVLM with the necessary insights 1022 to overcome the complexity of the task. 1023

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Compared to CoT and ToT, VReST demonstrates superior performance by leveraging multimodal fusion and systematic exploration. CoT struggles with intermediate verification, while ToT lacks effective feedback and global judgment. VReST addresses these shortcomings by incorporating MCTS, effectively integrating visual and textual information, and quantifying the reliability of reasoning traces. Across all cases, VReST not only achieves correct answers but also ensures interpretability and robustness, highlighting its effectiveness in solving complex vision-language reasoning tasks.

D.1 Prompt Template of Reasoning Step Generation

Instruction

Given a question, please decompose it into sub-questions. For each sub-question, please answer it in a complete sentence, ending with "The answer is". When the original question is answerable, please start the sub-question with "Now we can answer the question:".

Output Example:

Question: Four years ago, Kody was only half as old as Mohamed. If Mohamed is currently twice as 30 years old, how old is Kody?

Sub-question 1: How old is Mohamed? Answer 1: He is currently 30 * 2 = 60 years old. The answer is 60.

Sub-question 2: How old was Mohamed four years ago? Answer 2: Four years ago, he must have been 60 - 4 = 56 years old. The answer is 56.

Sub-question 3: How old is Kody four years ago? Answer 3: Four years ago, Kody was half as old as Mohamed. So Kody was 56 / 2 = 28 years old. The answer is 28.

Sub-question 4: How old is Kody now? Answer 4: Kody is 28 + 4 = 32 years old. The answer is 32.

Sub–question 5: Now we can answer the question: How old is Kody? Answer 5: Kody is currently 32 years old. The final answer is 32.

Test example:

Question: [question]

Sub-question 1: [sub-question 1] Answer 1: [answer 1]

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Sub-question k-1: [sub-question k-1] Answer k-1: [answer k-1]

Answer:

Sub-question k: [sub-question k] Answer k: [answer k]

D.2 Prompt Template of Calculating Usefulness of All the Sub-questions. (R1 Rewarding)

Instruction

Given a question and some sub-questions, determine whether the last sub-question is useful to answer the question. Output 'Yes' or 'No', and a reason.

Output Example:

Question: Four years ago, Kody was only half as old as Mohamed. If Mohamed is currently twice as 30 years old, how old is Kody?

Sub–question 1: How old is Mohamed?

Sub-question 2: How old was Mohamed four years ago?

New Sub-question 3: How old was Kody four years ago?

Is the new question useful? Yes. We need the answer to calculate how old is Kody now.

Question: Traci and Harris are baking cakes together. Traci has brought flour from her own house and Harris has 400g of flour in his house. Each cake needs 100g of flour and Traci and Harris have created 9 cakes each. How much flour, in grams, did Traci bring from her own house?

New Sub-question 1: How many cakes did Traci bring from her own house? Is the new question useful? No. The new question is not related to the original question.

Question: A quantity surveyor is figuring out the construction costs for a couple that wishes to build a house. The costs are as follows: land costs \$50 per square meter, bricks cost \$100 per 1000 bricks and roof tiles cost \$10 per roof tile. If the house they wish to build requires 2000 square meters, 10000 bricks, and 500 roof tiles, how much construction costs are required for this project?

Sub-question 1: How much does the land cost?

Sub-question 2: How much do the bricks cost?

New Sub-question 3: How much do the roof tiles cost?

Is the new question useful? Yes. We need the answer to calculate the total construction costs.

Question: Wallace's water heater is twice the size of Catherine's water heater. If the capacity of Wallace's water heater is 40 gallons and it's 3/4 full, calculate the total number of gallons of water they both have if Catherine's water heater is also full with water to 3/4 of its capacity.

Sub-question 1: How much water is in Wallace's water heater?

New Sub–question 2: How much water do they have in total?

Is the new question useful? No. It is too hard to answer the new question based on the current information.

Test example:

Question: [question]
Sub-question 1: [sub-question 1]
Sub-question 2: [sub-question 2]

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New Sub-question k: [sub-question k] Is the new question useful?

Answer:

Yes/No. [reason]

D.3 Prompt Template of Calculating Correctness of the Last Answer. (R2 Rewarding)

Instruction

Given a question and some sub-questions and answers, determine whether the last answer of the last sub-question is correct. Output 'Yes' or 'No'.

Test example:

Question: [question]
Sub-question 1: [sub-question 1]
Answer 1: [answer 1]
Sub-question 2: [sub-question 2]
Answer 2: [answer 2]

Sub-question k: [sub-question k] Answer k: [answer k] Is the answer correct?

Answer:

Yes/No.

D.4 Prompt Template for answer evaluation

Instruction

You will be given a **Question**, the **Ground Truth Answer**, and a **Predicted Answer**. Your task is to compare the **Ground Truth Answer** with the **Predicted Answer** and determine whether the **Predicted Answer** is correct. It's acceptable to have different grammar or form. If the **Predicted Answer** is correct, you should say "Yes". If the ** Predicted Answer** is incorrect, you should say "No".

Test example:

Question: [question]
Ground Truth Answer: [ground_truth]
Predicted Answer: [model_response]
Is the **Predicted Answer** correct?

Answer:

Yes/No.