

# KO-RAG : Knowledge Organization for Retrieval Augmented Large Language Models with Individual-then-Integrated Feedback

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## Abstract

Retrieval-augmented large language models have shown remarkable potential in knowledge-intensive tasks. However, their performance can be compromised by lengthy, noisy, or irrelevant retrieved information. Recent work focus on knowledge compression, but ignore the feedback from LLM or just incorporate with individual feedback. In this paper, we introduce **KO-RAG**, a knowledge organization method with an external knowledge organization model for retrieval augmented large language models, trained with individual-then-integrated feedback. KO-RAG learns to organize knowledge in a two-stage framework. In the individual feedback stage, our method ranks and filters knowledge by comparing each knowledge, which can measure the helpfulness of each knowledge individually. In the integrated feedback stage, our method organizes the knowledge integrally by utilizing LLM’s feedback on sampled knowledge permutations. Moreover, we design an empty knowledge placeholder to make KO-RAG organize knowledge dynamically. Evaluation on five open-domain question-answering datasets proves that the proposed method has significantly improves the LLMs’ performance, outperforming the baseline methods.

## 1 Introduction

Retrieval-augmented generation (RAG) enhances the large language models (LLMs) ability to provide up-to-date and contextually appropriate responses by incorporating relevant information from curated knowledge bases or the Internet (Nakano et al., 2021; Jiang et al., 2023d; Mallen et al., 2023; Shi et al., 2023). Despite their utility, retrieved texts can be noisy, redundant, and misleading due to imperfect retrievers and incomplete knowledge bases, potentially decreasing performance (Xu et al., 2023; Liu et al., 2024; Cuconasu et al., 2024). Recognizing this shortcoming, researchers have proposed various strategies to com-

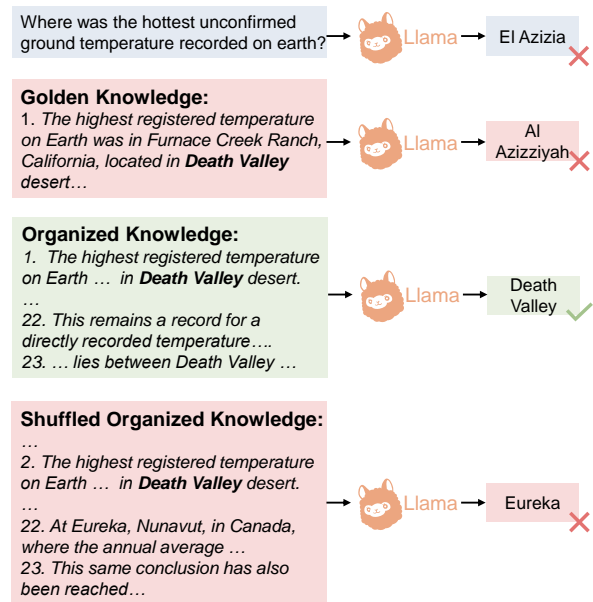


Figure 1: An example to show the necessary of knowledge organization. In the example, Llama’s responses are different to the same question under different knowledge contexts. **Golden Knowledge**: Selected both by human annotators and Llama feedback, which also contains the right answer of the given question, yet fails to elicit the correct answer. **Organized Knowledge**: Includes information not directly related to the question, but enables Llama to answer correctly. **Shuffled Organized Knowledge**: Randomly reordered version of the organized knowledge, leading to an incorrect prediction.

press retrieved knowledge, broadly categorized into two types. The first category is discriminator-based, which relies on a discriminator to judge whether tokens or sentences should be preserved (Jiang et al., 2023c; Li et al., 2023; Xu et al., 2023; Pan et al., 2024). The second method is reranker-based, which uses a scoring model to assign scores to sentences or paragraphs, then selects the top-k highest-scored ones (Glass et al., 2022; Liu, 2022; Huang and Huang, 2024).

Realizing the gap between pre-defined or heuristic based and LLM’s preference, recent research

has explored using LLM’s feedback to train discriminators or rerankers (Xu et al., 2023; Jiang et al., 2023b). However, these approaches typically operate at a individual level, which use LLM’s feedback to measure one retrieved document’s helpfulness, but not take all the knowledge context into consideration. While such method is straightforward to implement, but often leads to suboptimal results. As illustrated in Figure 1, the golden knowledge—both chosen by human annotators and the LLM itself<sup>1</sup>—may not always enable the LLM to generate the correct answer.<sup>2</sup> Our research demonstrates that organized knowledge, which includes information about "Death Valley" but is not directly helpful to answer the question, can actually help the LLM answer correctly. Moreover, we observed that shuffling this organized knowledge can mislead the LLM<sup>3</sup>. These observations underscore the critical role of LLM’s integrated feedback in knowledge content selection and arrangement.

Building on these insights, we introduce the concept of *knowledge organization*. We define this as the process of searching the optimal ordered subsequence of original knowledge that maximizes an LLM’s probability of answering correctly. Given that the precise mechanism by which LLMs integrate retrieved contextual knowledge with their parametric knowledge remains unclear, and that searching the optimal among all possible candidates is an NP-Hard problem, we propose **KO-RAG**, an external knowledge organization model with a two-stage training framework to investigate this problem. In the first stage, we rank knowledge based on individual LLM feedback, selecting those that demonstrably improve the LLM’s ability to answer correctly. The second stage involves calculating the LLM’s knowledge context preference using integrated feedback and optimizing the model through Direct Preference Optimization (DPO, Rafailov et al., 2024). To enable dynamic knowledge ranking, we introduce the concept of an empty knowledge placeholder, allowing for flexible sequence lengths and more nuanced organization strategies.

We conducted experiments across five knowledge-intensive tasks, including open-domain

<sup>1</sup>Given the knowledge and question, calculate the conditional probability that the LLM predict the correct answer.

<sup>2</sup>This phenomenon is known as context-parameter knowledge conflict (Tan et al., 2024; Xie et al., 2024) or extrinsic hallucinations (Huang et al., 2023; Ji et al., 2023).

<sup>3</sup>This finding is also corroborated by recent studies (Cucanasu et al., 2024; Liu et al., 2024)

question answering and long-form question answering. Our experimental results demonstrate that, given similar input knowledge length constraints, our method outperforms both discriminator-based and reranker-based baseline approaches. These findings suggest that our knowledge organization technique more effectively leverages available information, leading to improved performance on language understanding and generation tasks.

We conclude our contribution as follows:

- We propose KO-RAG, a two stage framework that enables model to organize knowledge via LLM’s individual and integrated feedback.
- We model knowledge organization in a unified process with proper distribution estimation by introducing empty knowledge placeholder.
- Experiments on various knowledge intensive tasks proved the efficiency of our proposed method.

## 2 Problem Formulation

In the basic RAG framework, we have a question  $Q$ , its corresponding answer  $A$ , and knowledge retrieved from a knowledge base  $K = \{k_1, k_2, \dots, k_n\}$ , where  $k_i$  denotes a knowledge sentence. We consider the knowledge organization process as a picking and ranking task, which can be viewed as finding a specific permutation of knowledge. Let  $O = \{O_1, O_2, \dots, O_m\}$ ,  $m = \sum_{i=0}^n \frac{n!}{(n-i)!} = \lfloor e * n! \rfloor$  represent all possible permutations of retrieved knowledge, where  $O_i$  denotes one partial permutation of  $\{1, 2, \dots, n\}$ ,  $e$  denotes the Euler number and  $\lfloor \cdot \rfloor$  denotes the floor function. The target  $O_{optimal}$  of our knowledge organization process can be defined as follows:

$$O_{optimal} := \max_{O_i \in O} P(A|Q, K_{O_i}) \quad (1)$$

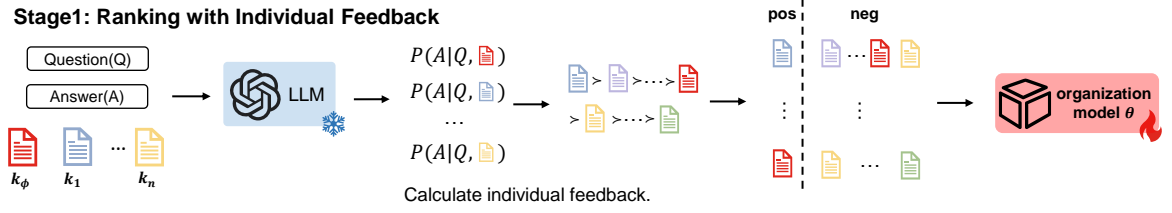
where  $K_{O_i}$  denotes the knowledge under the order  $O_i$ . This formulation seeks to find the permutation of knowledge that maximizes the probability of generating the correct answer  $A$  given the question  $Q$  and the organized knowledge  $K_{O_i}$ .

## 3 Method

The vast search space, with  $O(n!)$  possible candidates, renders exhaustive search computationally infeasible. To navigate these complexities, we employ a sophisticated, two-stage training methodol-

## Training of KO-RAG

- **Stage1: Ranking with Individual Feedback**



- **Stage2: Organization with Integrated feedback**

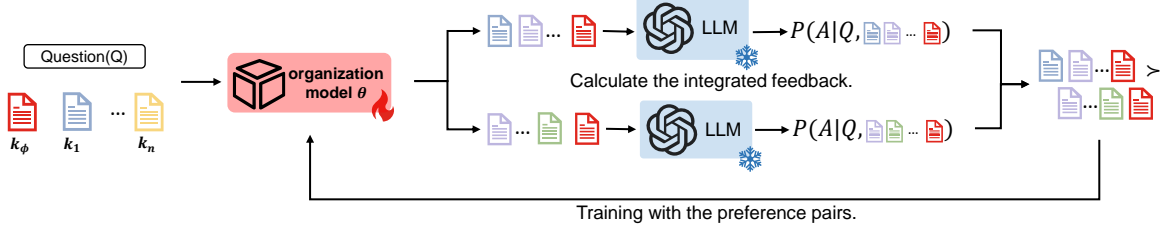


Figure 2: Overview of training process of the KO-RAG framework.  $k_i$  denotes the retrieved knowledge and the empty knowledge placeholder is denoted by  $k_\phi$ . In the stage 1, LLM provides feedback to rank each retrieved knowledge and the empty knowledge placeholder. In the stage 2, KO-RAG sample 2 different knowledge rank lists based on the scores predicted by KO-RAG, in which the empty knowledge placeholder serves as the end of list. KO-RAG is optimized with the integrated feedback of two knowledge lists and DPO.

ogy of knowledge organization. The overall procedure is illustrated in Figure 2, which includes Ranking with Individual Feedback (§3.1) and Organization with Integrated Feedback (§3.2).

### 3.1 Ranking with Individual Feedback

**Training procedure** Following the definition in Section 2, we can seek an order  $O_{id} = \{o_1, o_2, \dots, o_n\}$ , such that  $\forall i > j P(A|Q, k_{o_i}) > P(A|Q, k_{o_j})$ , which relies on LLM’s individual feedback. To remove unhelpful knowledge, we introduce an empty knowledge placeholder  $\phi$ , where  $P(A|Q, \phi) = P(A|Q)$ . This allows comparison of each knowledge sentence’s utility against a baseline of no additional knowledge. Hence we obtain a knowledge rank based on the individual feedback  $O_{id} = \{o_1, o_2, \dots, o_{n+1}\}$  and  $k_{o_m} = k_\phi$ . Then we consider all knowledge rank higher than the empty knowledge placeholder (including the empty knowledge placeholder) as positive examples. For each positive knowledge sentence  $K_{o_i}$ , we sample  $T$  lower-ranked knowledge sentences as negative samples and construct the training dataset  $D$  with  $Q$  and  $O_{id}$  as follows.

$$D = \{(Q, o_p, o_{n_1}, \dots, o_{n_T}) | o_p, o_{n_i} \in Q_{id} \& o_p > o_{n_i}\} \quad (2)$$

based on the corresponding query  $Q$  and the knowledge  $k_{o_i}$ , the score model  $\mathcal{F}$  will predict the score  $s_{o_i} := \mathcal{F}(Q, k_{o_i})$ . The training loss which is InfoNCE loss (Oord et al., 2018), is defined as fol-

lows:

$$L = \sum_{(Q, o_p, o_{n_1}, \dots, o_{n_T}) \in D} \frac{\exp(s_{o_p}/\tau)}{\exp(s_{o_p}/\tau) + \sum_{j=1}^T \exp(s_{o_{n_j}}/\tau)} \quad (3)$$

Where  $\tau$  is a temperature parameter controlling the sharpness of the probability distribution.

**Score Model** Following recent approaches in the field (Chen et al., 2024; Pan et al., 2024), we employ an encoder architecture as our score model. Given an input query  $Q$  and a knowledge sentence  $k_i$ , the model calculates a helpfulness score  $s_i$  as follows:

$$s_i = Enc(Emb(Q \circ k_i)) \quad (4)$$

where  $Enc$  represents the encoder function,  $Emb()$  denotes the embedding output and  $\circ$  denotes string concatenation.

### Virtual Tokens for Empty Knowledge Placeholder

The empty sequence presents a significant challenge in the training process due to its format contrasts with normal "question-knowledge" pairs, as it lacks any knowledge text. To address this issue, we draw inspiration from Prefix-Tuning techniques (Li and Liang, 2021), and introduce additional virtual tokens to represent the empty knowledge placeholder. These virtual tokens serve as a proxy for the absent content, providing a more

consistent input structure across all cases. The calculation process of empty knowledge placeholder  $K_\phi$  is defined as follows:

$$s_\phi = Enc(V \oplus Emb(Q)) \quad (5)$$

where  $V := [V_0, V_1, \dots, V_{m-1}] \in \mathbb{R}^{m \times d}$  represents  $m$  randomly initialized virtual tokens, each with dimension  $d$ ,  $\oplus$  denotes vector concatenation and  $Emb()$  denotes the embedding output.

### 3.2 Organization with Integrated Feedback

**Training procedure** We begin by defining a preference relationship between knowledge orders. Given a question  $Q$ , its corresponding answer  $A$ , and two predicted knowledge orders  $O_i$  and  $O_j$ , we define the preference as follows

$$O_i \succ O_j \text{ if } P(A|Q, K_{O_i}) > P(A|Q, K_{O_j}) \quad (6)$$

in which  $K_{O_i}$  denotes the knowledge under the order  $O_i$ .

Based on this preference relationship, we can construct a training dataset  $D := (Q, O_w, O_l) | O_w, O_l \in O, O_w \succ O_l$ , where  $O_w$  is the preferred (winning) order and  $O_l$  is the less preferred (losing) order for a given question. Rather than pre-building the entire training dataset, we adopt an online reinforcement learning paradigm.

We employ DPO to train our model using feedback from LLM’s feedback. Let  $P_{ref}$  and  $P_\theta$  denote the probability distributions estimated by the reference model and the model being trained, respectively. Given a preferred order  $O_w$  and a less preferred order  $O_l$ , the DPO loss function is defined as:

$$L_{DPO} = -\log \sigma(\beta \log \frac{P_\theta(O_w) \cdot P_{ref}(O_l)}{P_{ref}(O_w) \cdot P_\theta(O_l)}) \quad (7)$$

where  $\sigma(\cdot)$  is the sigmoid function and  $\beta$  is a constrained hyper-parameter.

To enhance training stability and maintain high confidence in preferred orders, we introduce an additional Maximum Likelihood Estimation (MLE) loss for the preferred order  $O_w$ :

$$L_{MLE} = -\log P_\theta(O_w) \quad (8)$$

this MLE loss encourages the model to assign high probabilities to preferred orders. We combine the DPO and MLE losses to form our final loss function:

$$L = L_{DPO} + \lambda L_{MLE} \quad (9)$$

where  $\lambda$  is a hyper-parameter that balances the contribution of the MLE loss relative to the DPO loss.

**Distribution estimation of  $P(O)$**  We first introduce the distribution estimation of the permutation. Given a query  $q$  and a set of retrieved knowledge  $K = \{k_1, k_2, \dots, k_n\}$ , the score model  $M$  will calculate the scores of each text  $S = \{s_i | s_i = M(q, k_i)\}$ . According to the Plackett-Luce model, we can define the probability of a full ranking order  $O_f = \{o_{f_1}, o_{f_2}, \dots, o_{f_n}\}$  as follows:

$$P(O_f|x) = \prod_{i=1}^n P(o_{f_i} | o_{<f_i}, x) \quad (10)$$

$$= \prod_{i=1}^n \frac{\exp(s_{f_i})}{\sum_{j=i}^n \exp(s_{f_j})}$$

extending this concept, we propose a method to calculate the probability of a partial ranking order  $O_p = \{o_{p_1}, o_{p_2}, \dots, o_{p_m}\}$ , where  $m \leq n$  and  $k_{o_{p_m}} = \phi$ :

$$P(O_p|x) = \prod_{i=1}^m P(o_{p_i} | o_{<p_i}, x) \quad (11)$$

$$= \prod_{i=1}^m \frac{\exp(s_{p_i})}{\sum_{p_j \notin \{o_{<p_i}\}} \exp(s_{p_j})}$$

for a detailed proof, please refer to Appendix A. This formulation allows us to treat the passage scoring process as a sequential decision-making problem, opening the possibility of optimizing it using reinforcement learning techniques.

### 3.3 Inference Stage

During inference, we employ a greedy method to select and order the knowledge. Given a query  $q$  and a set of retrieved knowledge passages  $K = \{k_1, k_2, \dots, k_n\}$ , our scoring model  $M$  calculates a score for each passage, producing a set of scores  $S = \{s_i | s_i = M(q, k_i)\}$ . We then construct the predicted order  $O = \{o_1, o_2, \dots, o_m\}$  such that:  $\forall i > j, s_{o_i} > s_{o_j}$  and  $k_{o_m} = \phi$  (the empty knowledge placeholder).

## 4 Experiment setup

**Datasets** To evaluate the effectiveness of our proposed method, we conduct experiments on several knowledge intensive datasets. Specifically, we conduct experiments on three open domain question answering datasets: Natural Questions (NQ, Kwiatkowski et al. 2019), AmbigNQ (Min et al., 2020), PopQA<sup>4</sup> (Mallen et al., 2023) and two long-

<sup>4</sup>Since there is no official train-test split of PopQA, we use top-13000 as the train set and 1267 as test set.

Dataset	Train	Test	Avg token
NQ	87372	2837	3168
AmbigNQ	19363	5749	3177
PopQA	13000	1267	3237
ASQA	4353	948	3169
ELI5	272633	1507	3021

Table 1: Statistical information of datasets. We report the number of question-answer pairs in train dataset and test dataset in "Train" and "Test". We also introduce the average number of tokens of retrieved knowledge in "Avg token", which includes train set and test set.

form question answering datasets: ASQA (Stelmakh et al., 2022), ELI5 (Fan et al., 2019). The statistical information is listed in Table 1

**Baselines** In this paper, we consider the following three categories baselines:

- Naive baselines: **Zero-shot**, without any context knowledge. **RAG**, we use top-50% knowledge scored by the retriever.
- Discriminator-based baselines for RAG: **Selective-Context (SC)** (Li et al., 2023), **LongLLMLingua (LLingua)** (Jiang et al., 2023b), **LLMLingua2(Lingua-2)** (Pan et al., 2024). For discriminator-based baselines, we control the compression rate to 50%, which means deleting 50% of retrieved knowledge in token-level.
- Reranker-based baselines for RAG: **BM25** (Robertson et al., 1995), **RankT5 (T5)** (Zhuang et al., 2023), **BGE-reranker (BGE)** (Chen et al., 2024). For reranker-based baselines, we use reranker to do a sentence-level rerank and pick top 50%.

**Implementation Detail** In experiment, we use Llama2-13B-chat (Touvron et al., 2023) as the base model to provide feedback and as a answer generator in RAG framework. We also test our method based on Llama-2-7B-chat (Touvron et al., 2023) and Mistral-7B-Instruct (Jiang et al., 2023a). For knowledge retrieval, we use contriever (Izacard et al., 2021) as a knowledge retriever, and the 2019/08/01 Wikipedia dump pre-processed by Petroni et al. (2021) as a knowledge base. For each question, we retrieve top-20 chunks as retrieved knowledge. The model architecture is XLM-roberta-large (Conneau et al., 2020). Hyperparameter and more details are listed in Appendix B. Prompts we use are listed in Appendix D.

**Metric** For open-domain question answering, we use fuzzy **Exact Match(EM)** to measure whether generated answers contains the golden answers. And for long-form question answering, we use precision-based metric **BLEU-1(B-1, Papineni et al. 2002)** to calculate the similarity between generated answers and golden answers. Besides reporting the performance, we also report **average knowledge token(#token)**<sup>5</sup> of each method.

## 5 Results and Discussion

### 5.1 Main result

The experimental results are presented in Table 2. Our proposed method outperforms all baseline methods across nearly all datasets with the shortest average context length, with the exception of ELI5. In ELI5, our proposed method achieve the best performance with a comparable average context length with discriminator-based and reranker-based knowledge compression method.

### Comparison with Discriminator-based Methods

Selective-context and LLMLingua2, designed for universal context compression rather than specifically for RAG, demonstrate relatively lower performance. LongLLMLingua, which is tailored for RAG and utilizes Llama2-7B for knowledge compression, exhibits strong performance but still falls short of our proposed method.

### Comparison with Reranker-based Method

Model-based reranker methods show impressive performance on open-domain question answering tasks but appear less effective for long-form question answering. N-gram based methods like BM25 perform poorly on open-domain question answering and long-form question answering scenarios. In terms of overall performance across diverse tasks, our proposed method consistently outperforms these approaches.

### 5.2 The Effectiveness of Integrated Feedback

To assess the impact of integrated feedback from LLMs, we conducted a comparative analysis of our system’s performance before and after the integrated feedback stage. The results are presented in Table 3. Our findings demonstrate that the incorporation of integrated feedback leads to further performance improvements across all the datasets.

<sup>5</sup>In this paper, all the token refers to the text tokenized by Llama2 tokenizer.

	NQ		AmbigNQ		PopQA		ASQA		ELI5	
	EM	#token	EM	#token	EM	#token	B-1	#token	B-1	#token
<i>Naive</i>										
Zero-shot	43.32	0	32.75	0	11.13	0	<u>11.39</u>	0	13.93	0
RAG	45.51	<u>1576</u>	36.49	<u>1588</u>	36.54	<u>1613</u>	10.40	<u>1585</u>	14.22	<b>1511</b>
<i>Discriminator-based baselines for RAG</i>										
SC (Li et al., 2023)	43.57	1890	33.55	1897	34.65	1987	10.33	1893	<u>14.25</u>	1795
LLingua (Jiang et al., 2023b)	<u>47.83</u>	1714	<u>39.73</u>	1729	<u>39.07</u>	1758	10.82	1722	14.22	1659
Lingua2(Pan et al., 2024)	46.00	1788	35.43	1808	35.44	1829	10.98	1803	14.14	1696
<i>Reranker-based baselines for RAG</i>										
BM25 (Robertson et al., 1995)	43.56	1838	36.26	1861	34.65	1823	9.83	1841	13.88	1769
T5 (Zhuang et al., 2023)	46.67	1757	37.85	1725	37.17	1716	10.42	1756	14.03	<u>1578</u>
BGE (Chen et al., 2024)	47.76	1787	37.82	1837	36.54	1863	10.38	1841	14.22	1692
KO-RAG	<b>50.58</b>	<b>1350</b>	<b>42.29</b>	<b>1366</b>	<b>42.46</b>	<b>614</b>	<b>11.96</b>	<b>1206</b>	<b>14.74</b>	1773

Table 2: Performance comparison on knowledge-intensive tasks. This table presents the evaluation results across various knowledge-intensive tasks. The **bold** values indicate the best performance for each metric, while underlined values represent the second-best performance. For context length, **bold** figures denote the shortest number of tokens, and underlined figures indicate the second shortest. Note that the Zero-shot method is excluded from this token count comparison due to its unique nature

Dataset	w/o. IF	w. IF	baseline
NQ	47.87	50.58	47.83
AmbigNQ	38.20	42.29	39.73
PopQA	40.81	42.46	39.07
ASQA	10.25	11.96	11.39
ELI5	13.76	14.74	14.25

Table 3: Impact of integrated feedback(IF) on model performance. "w/o. IF" denotes the performance without integrated feedback and "w. IF" denotes the performance after organization with integrated feedback. "baseline" denotes the best performance of baseline method.

Notably, even in the absence of the integrated feedback stage, our proposed method outperforms the baseline approach on several datasets, including NQ and PopQA. This underscores the effectiveness of our initial knowledge reorganization stage. The dual benefits observed—improvements from both the initial knowledge reorganization and the subsequent integrated feedback stage—suggest that our two-stage approach offers a powerful framework for enhancing LLM performance.

### 5.3 Fine-grained Performance Analysis

While knowledge organization and compression can lead to overall performance improvements, they may also cause changes at the individual sample level. To analyze this, we categorize questions into four groups based on their pre- and post-reorganization performance: *PP* (correct before

and after), *NP* (incorrect before, correct after), *PN* (correct before, incorrect after), and *NN* (incorrect before and after). We then introduce a fine-grained efficiency score  $S$ , defined as:

$$S = \frac{|NP|}{|PN|} \quad (12)$$

where  $|NP|$  and  $|PN|$  denotes the sample number of NP and PN group. A higher  $S$  value indicates that when the model potentially distorts one sample (PN), it can rectify a larger number of samples (NP), thus demonstrating higher efficiency. We calculate this efficiency score across three datasets: NQ, AmbigNQ, PopQA. Our experimental results, which are listed in table 4 that demonstrate our proposed method consistently maintains higher efficiency scores across all datasets compared to baseline approaches. This suggests that our knowledge reorganization technique not only enhances overall accuracy but also achieves this improvement more efficiently, with a better trade-off between correcting previously incorrect answers and maintaining correct ones.

### 5.4 Generalize to Different LLMs

Our method is trained using feedback from a specific LLM. A natural question arises: can this method generalize to different models? To address this, we evaluated our approach on three open-domain question answering datasets using two distinct models: Llama2-7B (Touvron et al.,

	NQ	AmbigNQ	PopQA	Avg
SC	0.81	0.69	0.79	0.74
LLingua	<u>1.30</u>	<u>1.57</u>	<u>1.51</u>	<u>1.47</u>
Lingua2	1.05	0.87	0.85	0.93
BM25	0.82	0.97	0.75	0.89
T5	1.14	1.20	1.10	1.17
BGE	1.27	1.19	1.00	1.20
KO-RAG	<b>1.65</b>	<b>2.02</b>	<b>2.07</b>	<b>1.89</b>

Table 4: The efficiency score of different method across different datasets. We **bold** the highest stable score and underline the score highest score.

2023) and Mistral-7B (Jiang et al., 2023a). We present a summary of our findings in Table 6 for Llama2-7B-chat and Table 5 for Mistral-7B<sup>6</sup>. The results demonstrate that our method consistently outperforms all baseline approaches across both models, indicating strong generalization capabilities. Interestingly, we observed that the performance gap between our method and the baselines narrows when applied to Mistral-7B, compared to its performance with Llama2 series models. This suggests that the different LLMs may have similar knowledge preference, thus enabling our method generalize to these LLMs.

	NQ	AmbigNQ	PopQA
Zero-shot	46.21	37.35	31.41
RAG	50.26	39.73	40.41
SC	47.30	35.76	36.70
LLingua	<u>52.73</u>	<u>43.19</u>	<u>43.09</u>
Lingua2	51.00	38.28	40.02
BM25	48.82	38.41	36.54
T5	51.64	40.27	40.25
BGE	<u>52.73</u>	40.86	40.57
KO-RAG	<b>54.04</b>	<b>43.50</b>	<b>45.54</b>

Table 5: Performance on open-domain question answering tasks, which is based on Mistral-7b. The **bold** and underline values indicate the best and the second-best performance for each metric, respectively.

## 5.5 Model Context Preference Estimation

In this section, we address two critical questions: "Is our trained model an effective estimator of LLM's context preferences?" and "Does reinforcement learning improve the model's ability to estimate LLM preferences?". To investigate these issues, we compare the agreement and Cohen's kappa (Cohen, 1960) between KO-RAG and LLMs. Specifically, we reuse the LLMs' preference de-

<sup>6</sup>We use the Mistral-7B-instruct-v0.2 version

	NQ	AmbigNQ	PopQA
Zero-shot	41.28	30.27	28.97
RAG	43.11	34.27	36.23
SC	40.01	31.41	30.54
LLingua	<u>44.70</u>	<u>36.88</u>	<u>37.02</u>
Lingua2	43.29	33.74	32.99
BM25	40.82	32.63	32.83
T5	42.47	34.61	35.44
BGE	43.18	34.04	35.28
KO-RAG	<b>47.44</b>	<b>40.22</b>	<b>43.49</b>

Table 6: Performance on open-domain question answering tasks, which is based on Llama2-7b. The **bold** and underline values indicate the best and the second-best performance for each metric, respectively.

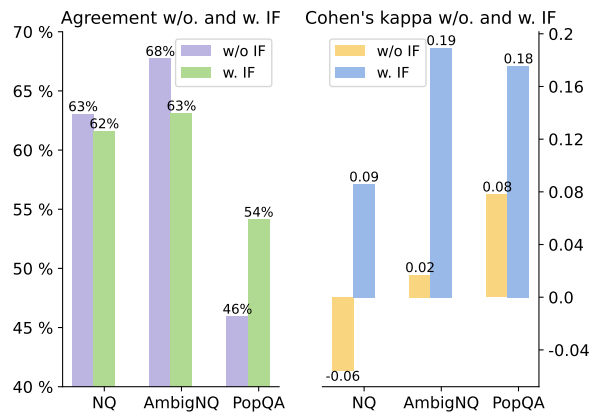


Figure 3: Agreement rate and Cohen's kappa between KO-RAG and LLM preferences w/o. and w. integrated feedback (IF) across NQ, AmbigNQ, and PopQA datasets

defined in equation 6 and KO-RAG's preference defined in equation 11. Figure 3 illustrates our findings. Interestingly, while reinforcement learning does not significantly improve the raw agreement rate, it does enhance the Cohen's kappa score. This suggests that the reinforcement learning process refines the model's ability to capture more nuanced aspects of LLM preferences, beyond simple binary agreement. However, it is important to note that both the agreement rate and Cohen's kappa remain below satisfactory levels. This indicates that while our approach shows promise, there is still considerable room for improvement in accurately modeling LLM context preferences.

## 5.6 Case Study

Table 7 illustrates examples comparing model performance using contexts processed by KO-RAG versus silver knowledge contexts (The optimization target in Stage 1, refer to Chapter 3.1). Consider

the question, "Who plays the science officer on Star Trek: Discovery who is also a chief engineer?" When the initially retrieved knowledge lacks the correct answer, the silver context fails to guide the LLM towards an accurate response. In contrast, KO-RAG demonstrates its effectiveness by successfully leveraging the LLM's inherent parameter knowledge that "Paul Stamets is played by actor Anthony Rapp." By effectively filtering and reorganizing this information, KO-RAG enables the LLM to provide the correct answer: Anthony Rapp.

---

**Question:**

Who plays the science officer on Star Trek discovery who is a chief engineer?

---

**Standard answer:**

"Anthony Rapp", "Anthony Deane Rapp"

---

**Silver context:**

- 1: Yelchin died in a car accident on June 19, 2016,
- 2: ... specifically from Captain **Christopher Pike**, ...

**LLM's prediction:**

The character who plays the science officer and chief engineer on Star Trek: Discovery is Captain **Christopher Pike**, portrayed by Anson Mount.

---

**KO-RAG context:**

- 1: Yelchin died in a car accident on June 19, 2016,
2. Science Officers Saru and **Stamets**, respectively.
3. After the first season concluded with the ...
- ...
6. ... the relationship between Culber and **Stamets** would continue to be explored.

**LLM's prediction:**

The character who plays the science officer and chief engineer on Star Trek: Discovery is **Paul Stamets**, played by actor Anthony Rapp.

---

Table 7: Case comparison between silver context and KO-RAG processed context On AmbigNQ dataset. Entities that appear in both the context and the LLM's prediction are highlighted in red.

## 6 Related Work

**Retrieval Augmentation Generation** Retrieval augmented generation, which uses retrieved knowledge as generation context, significantly improves the accuracy, credibility and interpretability of generated texts (Gao et al., 2023; Ren et al., 2023; Wang et al., 2023b; Louis et al., 2024). One mainstream method is training retriever and LLMs end-to-end (Guu et al., 2020; Wang et al., 2024a; Nakano et al., 2021; Asai et al., 2023; Borgeaud et al., 2022; Wang et al., 2023a). Another method freezes the LLMs and uses retrieved knowledge as additional context with various strategies including

retrieval query refinement, structured knowledge indexing, and iterative retrieval mechanisms (Ma et al., 2023; Jiang et al., 2023d; Wang et al., 2024b). Nonetheless, the inclusion of retrieved data can introduce new challenges, as it often yields noisy or redundant information that might distract the LLMs from pertinent content (Yoran et al., 2023; Liu et al., 2024).

**Knowledge Compression For RAG** Knowledge compression could remove the irrelevant contexts and reduce the input context length, thus improving the model's performance and decrease the cost of inference. One effective method is reranker-based, which use a reranker model to modeling the relevance between retrieved knowledge and question, then remove the less relevant knowledge to improve performance and reduce context length (Glass et al., 2022; Izacard et al., 2023; Wang et al., 2023c; Xu et al., 2023; Huang and Huang, 2024). Another main method is discriminator based, which relies on a discriminator to determine which part should be deleted, including sentence-level self-information calculated by a small language model (Li et al., 2023; Jiang et al., 2023c), token-level discriminator (Pan et al., 2024) or combine token-level discriminator and reranker (Jiang et al., 2023b). But these method ignores LLM's feedback or just utilize LLM's feedback in a individual level with greedy search. Recently, there are several studies to tackle this problem with a Seq2Seq model (Yang et al., 2023; Jin et al., 2024; Zhu et al., 2024). While these methods are easily trained with LLM's feedback, they have different drawbacks inherited from Seq2Seq architecture, such as generation hallucinations, limited input context and could not inference in parallel. Since these method have different drawbacks and model architectures, we do not consider them as baselines.

## 7 Conclusion

We introduce KO-RAG, an advanced knowledge organization model to enhance RAG system. Our method is accomplished with two-stage training framework, utilizing LLM's individual and integrated feedback respectively. Our comprehensive experiments across diverse open-domain and long-form question answering datasets demonstrate the efficacy of our method. Through in-depth analysis, we elucidate the benefits of the integrated feedback, and highlight our method's fine-grained efficiency and its ability to generalize across various LLMs.



## 528 Limitation

529 We conclude the limitation of our method as fol-  
530 lows: First, we test our method in various open  
531 domain question answering datasets and long form  
532 question answering datasets, but the questions in  
533 these datasets are not complex. For complex ques-  
534 tions, which need LLM to perform multi-step rea-  
535 soning and iterative retrieval, whether our method  
536 still works remains to be examined. Secondly, our  
537 method relies on training with LLM’s feedback,  
538 thus making it more time costing and GPU cost-  
539 ing than the heuristic method such as Selective-  
540 Context (Li et al., 2023) and LLMLingua (Jiang  
541 et al., 2023c).

## 542 Acknowledgements

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	<b>A Detail Proof of the Extend Plackett-Luce Model</b>	832
		833
	Given retrieved knowledge $K = \{k_1, k_2, \dots, k_n\}$ and responding scores $S = \{s_1, s_2, \dots, s_n\}$ , according to Plackett-Luce model, the probability distribution of a full rank $O_i = \{o_1, o_2, \dots, o_n\}$ defined is as follows:	834
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Then, considering the empty knowledge as a special case, we have a knowledge  $K = \{k_0, k_1, k_2, \dots, k_n\}$ ,  $k_0 = \phi$  and its responding scores  $S = \{s_0, s_1, s_2, \dots, s_n\}$ . For a partial rank  $E_i = \{e_0, e_1, \dots, e_m\}$  that satisfying  $m \leq n + 1$  and  $k_{e_m} = \phi$ , its probability distribution is

$$P(E_i) = \prod_{i=0}^m \frac{\exp(s_{e_i})}{\sum_{j \notin \{o < e_i\}} \exp(s_j)} \quad (14)$$

To approve this, we consider the remaining knowledge set  $R = \{k_i | i = 1, 2, \dots, n \text{ and } k_i \notin E_i\}$ , the remaining scores set  $S_R = \{s_i | k_i \in R\}$  and  $R$ 's all possible permutation  $O_R = \{O_{R_i}\}$ . The partial rank  $E_i$  and one permutation of  $O_{R_i} \in O_R$  make up a full rank of  $O_i \in O$ . Noting that two different permutation of  $K$ , which share the same partial rank  $E_i$ , shows no difference to LLM, the probability of  $E_i$  should be the sum of probability of permutation  $O_i \in O$  which starts with  $E_i$ . In other words, we have :

$$\begin{aligned} P(E_i) &= \sum_{O_{R_i} \in O_R} P(E_i \oplus O_{R_i}) \\ &= \sum_{O_{R_i} \in O_R} \prod_{i=0}^m \frac{\exp(s_{e_i})}{\sum_{j=i}^m \exp(s_{e_j}) + \sum_{j=1}^{n-m+1} \exp(s_{r_j})} \\ &\quad \prod_{j=1}^{n-m+1} \frac{\exp(s_{r_i})}{\sum_{j=i}^{n-m+1} \exp(s_{r_j})} \\ &= \prod_{i=0}^m \frac{\exp(s_{e_i})}{\sum_{j=i}^m \exp(s_{e_j}) + \sum_{j=1}^{n-m+1} \exp(s_{r_j})} \\ &\quad \sum_{O_{R_i} \in O_R} \prod_{j=1}^{n-m+1} \frac{\exp(s_{r_i})}{\sum_{j=i}^{n-m+1} \exp(s_{r_j})} \end{aligned} \quad (15)$$

in which  $\oplus$  means concatenation of two sequence.

We notice that  $\frac{\exp(s_{r_i})}{\sum_{j=i}^{n-m+1} \exp(s_{r_j})}$  is the probability of  $O_{R_i}$  under the set  $R$ , which simplify the equation as

$$\begin{aligned} P(E_i) &= \prod_{i=0}^m \frac{\exp(s_{e_i})}{\sum_{j=i}^m \exp(s_{e_j}) + \sum_{j=1}^{n-m+1} \exp(s_{r_j})} \\ &\quad \sum_{O_{R_i} \in O_R} P(O_{R_i}) \\ &= \prod_{i=0}^m \frac{\exp(s_{e_i})}{\sum_{j=i}^m \exp(s_{e_j}) + \sum_{j=1}^{n-m+1} \exp(s_{r_j})} \\ &= \prod_{i=0}^m \frac{\exp(s_{e_i})}{\sum_{j \notin \{o < e_i\}} \exp(s_j)} \end{aligned} \quad (16)$$

## B Implementation Details

### B.1 Datasets

**Natural Question (NQ)** is a corpus of real questions issued to the Google search engine. We use

the data processed by KILT.

**AmbigNQ** collects questions from NQ and rewrite the questions to solve the ambiguity. We use the official released data.

**PopQA** collects knowledge triples from Wikidata and convert the knowledge triple to a question-answer pair with templates. We use the official released data and use the top-13000 as the train set, remaining 1267 as the test set.

**ASQA** is a dataset of high-quality long-form answers to 6,316 ambiguous factoid questions. We use the official released data.

**ELI5** collects question-answer pair from a subreddit from Reddit, named as Explain Like I'm Five(ELI5). We use the data processed by KILT.

### B.2 Hyper parameter

In stage 1, we search the learning rate in  $\{2e-4, 1e-4, 5e-5, 1e-5\}$ , and the learning rate for NQ is  $2e-4$ , AmbigNQ is  $1e-4$ , PopQA is  $5e-5$ , ASQA is  $1e-5$  and eli5 is  $1e-5$ . We set the number of batch size as 8 and the number of negative samples as 31. we set the gradient accumulation steps as 2. We set the number of virtual token in equation 5 as 50.

In stage 2, we set the learning rate as  $1e-6$ , the  $\beta$  is 0.2 and the  $\lambda$  in equation 9 as 0.1. We set the batch size as 4 and the gradient accumulation steps as 4.

### B.3 Additional Details

In data preparation stage, we split the retrieved knowledge chunks into sentences by open-source tools<sup>7</sup> and drop the sentences which is incomplete and too short (less than 5 words). In training stage, we use Adam (Kingma and Ba, 2014) as the optimizer. In inference stage, we use the vllm (Kwon et al., 2023) to accelerate text generation. In text generation process, we use the greedy decoding. All the process, including data preparation, model training and model inference is accomplished on a 8\*A800 GPU server.

## C Case study

The full content of the case 7 is listed in table 8.

## D Prompts For Data Preparation and Inference

In data preparation, training (stage 2) and inference, we use the same prompts. When the input knowledge is none, we use the following prompt:

<sup>7</sup><https://github.com/mediacloud/sentence-splitter>

	"Answer the subsequent question. \n\n Question: [Q] \n\n Answer: ". When the input knowledge is not none, we use the following prompt:Given the following passage, answer the subsequent question.\n\n Passages: [P] \n\n Question: [Q] \n\n Answer: . The "[P]" represents the input knowledge and "[Q]" indicates the input question.	920 921
<hr/> <p><b>Question:</b> Who plays the science officer on Star Trek discovery who is a chief engineer?</p> <hr/>		922 923
<p><b>Standard answer:</b> "Anthony Rapp", "Anthony Deane Rapp"</p> <hr/>		924 925 926
<p><b>Silver context:</b> 1: Yelchin died in a car accident on June 19, 2016, 2: After the first season concluded with the "Discovery" receiving a distress call from the USS "Enterprise", specifically from Captain <b>Christopher Pike</b>, Harberts expressed interest in exploring that character; Anson Mount was</p> <p><b>LLM's prediction:</b> The character who plays the science officer and chief engineer on Star Trek: Discovery is Captain <b>Christopher Pike</b>, portrayed by Anson Mount.</p> <hr/>		
<p><b>KO-RAG context:</b> 1: Yelchin died in a car accident on June 19, 2016, 2. Science Officers Saru and <b>Stamets</b>, respectively. 3. After the first season concluded with the "Discovery" receiving a distress call from the USS "Enterprise", specifically from Captain Christopher Pike, Harberts expressed interest in exploring that character; Anson Mount was 4: Scotty joins Kirk and Pavel Chekov (Walter Koenig) 5: Scotty joins Kirk's crew aboard the USS "Enterprise"-A at the end of "" (1986). 6. However, the executive producers of the series, Cruz, and GLAAD immediately released a statement saying "death is not always final in the "Star Trek" universe" and that the relationship between Culber and <b>Stamets</b> would continue to be explored.</p> <p><b>LLM's prediction:</b> Based on the passage, the character who plays the science officer and chief engineer on Star Trek: Discovery is <b>Paul Stamets</b>, played by actor Anthony Rapp.</p> <hr/>		

Table 8: Case study