What Matters in Learning Facts in Language Models? Multifaceted Knowledge Probing with Diverse Multi-Prompt Datasets

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Abstract

Large language models (LLMs) face issues in handling factual knowledge, making it vital to evaluate their true ability to understand facts. In this study, we introduce knowledge probing frameworks, BELIEF(-ICL), to evaluate the knowledge understanding ability of decoder-based as well as encoder-based pretrained LMs (PLMs) from diverse perspectives. BELIEFs utilize a multi-prompt dataset to evaluate PLM's accuracy, consistency, and reliability in factual knowledge understanding. To enable a more reliable evaluation with BELIEFs, we semi-automatically create MyriadLAMA, which has massively diverse prompts. We validate the effectiveness of BELIEFs in correctly and comprehensively evaluating PLM's factual understanding ability via extensive evaluations with recent LLMs. We then investigate key factors in learning facts in LLMs, and reveal the limitation of the prompt-based knowledge probing. The dataset is anonymously publicized.¹

1 Introduction

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One of the strongest motivations for training a language model (LM) using a larger amount of text is to increase the LM's ability to manage factual knowledge in knowledge-intensive tasks (Kamalloo et al., 2023). However, even if LMs are trained on massive text, they suffer from hallucinations that generate incorrect knowledge-grounded sentences (Zhang et al., 2023). Considering that large language models (LLMs) are being widely applied to real-world tasks, it is vital to understand the true knowledge capacity of LLMs and what factors influence the knowledge learning during pre-training.

However, evaluating the LLM's knowledge capacity is still challenging. Although LAMA probing (Petroni et al., 2019) evaluates the knowledge contained in pre-trained LMs (PLMs), it provides only prediction accuracy. Some studies diversify the LAMA probing datasets to compute prediction consistency (robustness) (Elazar et al., 2021; Jiang et al., 2020), but those datasets have either low quality or low quantity issues (§ B). Moreover, since the LAMA probe assumes encoder-based PLMs with the masked LM objective to solve fill-in-the-blank tasks, directly applying it to recent decoder-based LLMs will underestimate their ability of knowledge understanding. Although recent studies leveraged QA-based datasets to probe LLMs' knowledge (Kalo and Fichtel, 2022; Mallen et al., 2023; Wiland et al., 2024; Maekawa et al., 2024) via prediction accuracy, they overlook other important aspects than accuracy such as robustness to diverse prompts and the reliability of predictions, which are important for real-world applications.

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In this study, we introduce BELIEF (§2) and its variant BELIEF-ICL (§3), the multifaceted factual knowledge probing frameworks for encoderand decoder-based PLMs. BELIEFs utilize diverse prompts for each fact to eliminate the specific influence of linguistic expression on the results. It enables us to evaluate PLMs' robustness and reliability by measuring accuracy fluctuations, consistency, and overconfidence in fact prediction. Since BELIEFs require a multi-prompt probing dataset with diverse prompts for each fact, we build a new probing dataset, MyriadLAMA, to enable a more accurate and comprehensive evaluation (§4).

We applied BELIEFs to various encoder- and decoder-based PLMs, including BERT (Devlin et al., 2019) and Llama2 (Touvron et al., 2023) (§5.1). Through extensive evaluations, we verify the effectiveness of BELIEFs in accurately uncovering PLMs' ability in factual understanding (§5). Moreover, by comparing different PLMs, we reveal insights into the factors affecting the acquisition of facts during pre-training (§6). Finally, we explore the upper limits of covered knowledge by different methods and reveal the limitations of prompt-based knowledge probing (§7).

¹https://anonymous.4open.science/r/belief-CC8A

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2 BELIEF Framework

We first present a multifaceted factual probing framework - BELIEF, specifically for encoderbased PLMs. Using a multi-prompt knowledge probing dataset, BELIEF evaluates the facts understanding ability of PLMs from accuracy, robustness and reliability (§2.2-2.4). Here, robustness measures PLMs' ability to maintain consistent accuracy and predictions when given different prompts in evaluation. Reliability reflects the extent to which we can trust the PLMs' predictions.

2.1 Preliminary

To accurately evaluate the facts in PLMs, BELIEF aggregates results from multiple prompts for each fact to mitigate biases from specific linguistic expressions. This requires a dataset with varied expressions for each fact, namely multi-prompt factual probing dataset.

We follow the setting of fill-in-the-blank datasets, where each fact is represented as a **knowledge triple** (subject, relation, object) (*e.g.*, (Tokyo, Capital, Japan)). To probe PLMs for a knowledge triple, we first create a **masked prompt** (hereafter, **prompt**) (*e.g.*, "Tokyo is the capital of [Y]") for it and then input it into PLMs to see if they correctly predict the object token. To create such prompts, we first need a template for the relation (hereafter, **relational template**, *e.g.*, [X] is the capital of [Y]). We then fill the template with target knowledge triples, replacing [X] with a subject expression and [Y] with a [MASK] token. A multi-prompt dataset offers diverse prompts for each fact by providing varied relational templates and entity expressions.

We denote the subject-relation pairs in dataset as T, the set of prompts for a given subject-relation pair $t \in T$ as P_t . If the output distribution corresponding to mask token of a prompt is $\mathcal{O} =$ $\{(w_j, o_j) | \sum_j o_j = 1\}$, the prediction result is defined as the token $\hat{w} = \operatorname{argmax}_{w_j, (w_j, o_j) \in \mathcal{O}} o_j$.

2.2 Accuracy and its fluctuations

To correctly evaluate the accuracy of PLMs, we ag-121 gregate predictions from diverse prompts. Specif-122 ically, we randomly select one prompt for each 123 subject-relation pair $t \in T$ to form a set of prompts 124 for all triples $P = \{p_1, ..., p_{|T|}\}$. By feeding these 125 prompts P to PLMs, we can calculate one accuracy 126 value based on their predictions. We repeat this 127 process to collect a set of accuracies, which we then use to calculate both average and fluctuation. 129

Average accuracy: In BELIEF, accuracy metrics include Acc@1, which measures the rate of prompts with the correct token predicted within the top-1 output probabilities. Then we repeat this process N times to obtain a set of accuracies, denoted as $V_{Acc@1}$, where $|V_{Acc@1}| = N$. The final average accuracy is calculated as the mean value of $V_{Acc@1}$. Fluctuation of accuracy: For $V_{Acc@1}$, we evaluate accuracy fluctuations using the range and standard deviation. The range is determined by the difference between the maximum and minimum accuracy values in $V_{Acc@1}$.

2.3 Consistency

For each subject-relation pair t, we assess the PLM's consistency in predicting the object across different prompts in P_t . Specifically, we compute the degree of match between the prediction result \hat{w}_t^i for a given prompt p_t^i and the prediction results \hat{w}_t^j for other prompts $p_t^j \in P_t$ (where $j \neq i$), across all subject-relation pairs in T:

$$\text{Consist} = \frac{1}{|T|} \sum_{t \in T} \frac{\sum_{i,j:i \neq j, i,j \leq |P_t|} \mathbb{1}[\hat{w}_i^t = \hat{w}_j^t]}{\frac{1}{2} |P_t| (|P_t| - 1)}$$
(1)

2.4 Reliability

The reliability of PLMs reflects the extent to which we can trust the predictions they provide. In our study, we measure PLMs' overconfidence level in making fact prediction, drawing from the expected error calibration metric (Desai and Durrett, 2020). Specially, we measure the difference between true prediction accuracy and models' confidence to their predicted tokens. For each prompt, we first acquire the maximum probability (hereafter, confidence) from the output distribution for the mask token. Subsequently, all of the prompts are arranged in descending order based on confidence and segmented into M bins $(P^{(1)}, P^{(2)}, ..., P^{(M)})$, with the same amount of data points in each bin. For each bin *i*, we compute the average accuracy $\overline{\operatorname{Acc}}{}^{(i)}$ and average confidence $\overline{o_{max}}^{(i)}$. In our work, we use M = 10 for all the experiments. Finally, the PLM's overconfidence in predicting the object is assessed by averaging differences between average confidence and accuracy across all bins:

$$\operatorname{Overconf} = \sum_{i=1}^{M} \frac{|P^{(i)}|}{M} (\overline{o_{max}}^{(i)} - \overline{\operatorname{Acc}}_{[1]}^{(i)})$$
(2)

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The closer the Overconf is to zero, the more aligned the model's confidence is with its accuracy, indicating reliable confidence. A negative Overconf value means the model is underconfident.

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3 BELIEF-ICL for Decoder-based LLMs

Recent LLMs are based on decoder-only Transformer architecture, and are trained to predict subsequent tokens in a sequence. This makes it challenging for them to directly predict [MASK] tokens in masked prompts, as they cannot utilize information following the [MASK] (*e.g.*, "[MASK] and Tokyo are twin cities"). To comprehensively evaluate LLMs and enable fair comparison between encoder- and decoder-based models, we extend BE-LIEF to LLMs by employing in-context learning (ICL), termed BELIEF-ICL.

3.1 In-context learning for fact probe

The in-context learning ability allows LLMs to perform complex tasks during inference using taskspecific prompts (Brown et al., 2020). When designing ICL for evaluating factual knowledge, it is essential to consider **task instructions** and **context examples** appended to the target prompts.

 Task instruction: We introduce the mask prediction (MP) instruction for prompting LLMs generating one word answer for the target masked prompt. The task instruction is formulated as "Predict the [MASK] in each sentence in one word.".

2) Context settings: We propose four types of contexts to assess the impact of examplar selection on factual knowledge probing, following the QA format outlined in InstructGPT (Ouyang et al., 2022). zero-shot: no context;

- **X-random:** sampling X facts from all relations as the few-shot learning examples;
- **X-relation:** sampling X facts from the same relation but with random templates;
- **X-template:** sampling X facts from the same relations and the same template.

In the few-shot learning settings, we ensure that the target fact is excluded in the examples. Refer to &E for examples of prompts.

3.2 Evaluation methods

216Since LLMs generate responses without a token217limit, matching the correct answer with the model's218output can be challenging. Variations in language219expressions, such as the presence or absence of ar-220ticles and singular or plural forms, complicate this

process. Additionally, the model may generate extra tokens not relevant to the [MASK] token, such as parts of the prompt. For example, for the prompt "John Lennon can play [MASK]," both "guitars" and "a guitar" should be considered correct.

To measure BELIEF metrics for LLMs, we need to compare two strings: the generated text and the correct target expression for Acc@1, and two generated texts for Consist and Overconf. Here, we first normalize the strings by tokenizing and lemmatizing them. For example, "a guitar" and "guitars" are normalized to "a, guitar" and "guitar." If a normalized string list is included in the other (partial matching), they are considered matched.

1) Accuracy and its fluctuations: Accuracy is calculated by comparing the string generated by the model using a greedy decoding strategy to the correct answers. Notably, the matching judgment is one-directional: it only checks if the correct answer is included in the generated string. One-directional matching is adopted to avoid incorrect judgments from the model generating unrelated words. We use the same N as in §2.2 for accuracy measurement.

2) Consistency: We use bi-directional matching to evaluate the consistency (Consist) of generated sequences from two prompts.

3) Reliability: To calculate overconfidence, we need the model's confidence (probability) in its output. However, we cannot obtain this directly from the probability over generated tokens, as LLMs can produce diverse outputs that represent the same answer. To address this, we propose an approximate measurement. For each prompt, we generate 100 samples using multinomial sampling². We then measure the matching rate between the output generated from greedy decoding and the outputs from the 100 samples. This matching rate serves as the confidence value for the prompt³. The calculation of Overconf follows the same setting in §2.4. This method can approximate the BELIEF's Overconf calculation as BELIEF sampling answers from the output distribution. Note that, due to the high cost of generating 100 samples for each fact, we adopt a more efficient approach. We sample 10K prompts from 10K unique subject-relation pairs and only use these 10K prompts for answer sampling.

²Multinomial sampling selects a next token according to the probability, over the entire vocabulary given by the model.

³This method can approximate the overconfidence calculation in BELIEF of sampling answers from the output distribution. It makes the confidence calculated by BELIEF for encoder-based models comparable to that in BELIEF-ICL.

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4 MyriadLAMA Dataset

The fairness and accuracy of BELIEF evaluation depend on the diversity and quality of multiprompt factual probing datasets. However, existing datasets are either manually rewritten in small numbers (Elazar et al., 2021) or mined from texts (Jiang et al., 2020). The former is accurate but lacks diversity, providing an average of 7.3 prompts per fact with limited variation. For example, templates like "[X] works as [Y]" and "[X], who works as [Y]" are provided as different templates but very similar. Additionally, the number of templates is highly imbalanced, with 8 out of 46 relations having only one template, while P138⁴ has 20. The latter is diverse but includes templates that do not necessarily imply the relationship. For instance, for relation P937 $(\text{work location})^5$, the mined templates include "[X] to meet [Y].," which significantly deviates from the original meaning. To achieve a more accurate and fair evaluation, we introduce MyriadLAMA, a new multi-prompt factual probing dataset with improved diversity while retaining quality. Refer to § B for detailed qualitative and quantitative comparisons between MyriadLAMA and prior datasets.

4.1 Dataset construction

We build MyriadLAMA by semi-automatically extending the existing single-prompt probing dataset LAMA-UHN (Petroni et al., 2020). MyriadLAMA generates multiple prompts for each fact by providing multiple, equal relational templates for each relation and varying the linguistic expressions of subjects. Additionally, MyriadLAMA offers multiple expressions for each object to cover missed facts that are correctly predicted but in different tokens. For example, for the query "John Lennon was born in [MASK]", acceptable tokens could include "UK" and "Britain."⁶

Specifically, we define knowledge triples that neglect the diversity of surface expressions as **unique triples** and distinguish them from **derived triples**, which embody the diverse entity expressions and relational templates in each unique triple. The triple extension methods are described below.

Extending entities: The knowledge triples in

	LAMA-UHN	MyriadLAMA
Relational templates	41	4100
Unique triples	27,106	34,048
Derived triples	27,106	21,140,500
Subject-relation pairs	24,643	24,643
Prompts	24,643	6,492,800

Table 1: Statistics of LAMA-UHN and MyriadLAMA.

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LAMA-UHN constitute a subset of the Wikipedia knowledge base T-REx (Elsahar et al., 2018). T-REx selectively includes only certain objects for subject-relation pairs. MyriadLAMA extends the unique triples in LAMA-UHN by mining T-REx using subject-relation as key to include other available objects. For example, if LAMA-UHN contains only E_{guitar} for instruments that "John Lennon" can play, we can extend the unique triple to include E_{piano} . We also extend the entity expressions using aliases obtained from Wikidata.⁷

Paraphrasing relational templates: Myriad-LAMA creates a great variety of relational templates by a semi-automatic process. Firstly, we manually generate five distinct templates for each relation. They incorporate entailment expressions and diverse syntactic patterns like statements and question-answer formats to provide semantic and syntactic variations. Next, to enhance quantity and lexical diversity, we automatically paraphrase each manually created template 19 times using the GPT-4 API.⁸ Finally, all templates are filtered by human reviewers to remove low quality templates, yielding a total of 4100 templates covering 41 relations.

4.2 Dataset Statistics

We report the statistics of LAMA-UHN and MyriadLAMA, as shown in Table 1. As the result, the number of derived triples is increased from 27,106 in LAMA-UHN to 21,140,500, by combining various semi-automatically generated relational templates and the alias expressions for subject and object entities. As the prompts are generated from derived triples without considering the object expressions, the number of generated prompts are less than the number of derived triples, which is increased from 24,643 to 6,492,800.

Please refer to the appendix for details on dataset construction (§ A) and validity analysis of Myriad-LAMA (§ C). Examples of extended templates are provided in § A.3.

⁴https://www.wikidata.org/wiki/Property:P9138

⁵https://www.wikidata.org/wiki/Property:P937

⁶Note that, we follow the setting in LAMA-UHN to include triples where the object is a single token according to the BERT tokenizer. During evaluation, we consider the fact to be present, if the model's predicted token matches any of the correct tokens, regardless of which correct answer is predicted.

⁷https://www.wikidata.org/wiki/Wikidata:Data_access ⁸OpenAI: gpt-4-1106-preview

LLMs (#params)	Pre-training corpora	
LLIVIS (#params)	size source	_
BERT _{base} (110M) BERT _{large} (336M) BERT _{wwm} (336M)	3.3G 3.3G 3.3GEnglish Wikipedia and BookCorpus	
Llama2-7B (7B) Llama2-13B (13B) Llama2-70B (70B)	2.0T 2.0T 2.0T A collection of publicly available online data.	
Llama3-8B (8B) Llama3-70B (70B)	15T+ A collection of publicly 15T+ $available online data.$	
Phi3-mini (3.8B) Phi3-small (7B) Phi3-medium (14B)	3.3T 4.8T 4.8THigh-quality documents incl textbook-like generated text educational data and etc.	

Table 2: The PLMs for evaluation.

5 Effectiveness of BELIEFs

5.1 Experimental setups

We introduce the encoder- and decoder-based models used in experiments and evaluation settings. We evaluated three encoder-based models, BERT_{base}, BERT_{large}, and BERT_{wwm},⁹ and eight decoderbased models, Llama2-7B, -13B, -70B, Llama3-8B, -70B, Phi3-mini, -small, and -medium (Table 2). Refer to §F for more detailed model information.

We conduct a full-scale evaluation on LLMs with up to 8 billion parameters. Due to the computational cost of LLM inference, we use only five manually rewritten templates for the LLMs with more than 8B parameters, including Llama2-70B, Llama3-70B, and Phi3-medium.¹⁰ To calculate the average and fluctuation of accuracy (§2.2), we set a large sample number (N = 50,000) to provide stable and accurate accuracy measurement.

In the following sections, we analyze the evaluation results on various PLMs to deepen our understanding of how PLMs learn and represent factual knowledge. All evaluation results, including those for another family of encoder-based models, AL-BERT, are presented in Section §F.3.

5.2 Do BELIEFs provide additional insights?

BELIEF can offer evaluation from diverse perspectives rather than accuracy. As shown in Table 3 (Above), the evaluation result highlights accuracy fluctuations among the BERT variants. All

PLMs		Acc	Acc@1 \uparrow Fluctuation \downarrow		Consist ↑	Overconf	
PLN	15	LU	MyL	range	stdev	Consist	
BER						.1682	.2154
BER	[large	.2454	.1102	.1574	.0220	.1713	.2052
Θ BER	wwm	.2448	.1364	.1517	.0208	.1524	.1000
⊑ zero-						.0240	1119
🛱 4-ran	dom	.5050	.5205	.2033	.0273	.2156	0789
မှို 4-rela	tion	n/a ¹¹	.6871	.1236	.0156	.3659	0783
⊞ 4-tem	plate	.6490	.7268	.0220	.0026	.4015	0582

Table 3: Evaluation results of BERT variants (above) and Llama3-8B with BELIEF/-ICL (below). LU indicates LAMA-UHN evaluation results, and MyL represents the average Acc@1 on MyriadLAMA.

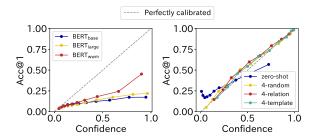


Figure 1: Calibration between confidence and Acc@1. (Left: Three BERT models types; **Right**: Llama3-8B with four different ICL settings.)

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BERT models show low consistency and tend to be overconfident in their predictions. Figure 1 (left) depicts the relationship between confidence and Acc@1 of the BERT models, indicating low accuracy even for prompts with confident outputs. Whereas $BERT_{wwm}$ performs better over most BE-LIEF metrics, $BERT_{large}$ outperforms $BERT_{wwm}$ on LAMA-UHN. This discrepancy arises from the limited prompts used in LAMA-UHN and the the single-faceted evaluation method. This highlights BELIEF's effectiveness in achieving a more accurate factual probing comparison between PLMs.

5.3 Does ICL adhere to instructions?

We then explore the effectiveness of different ICL settings in extracting facts from LLMs. We evaluate the instruction adherence of these settings from two aspects: predicting facts and generating oneword answers, which are crucial since the target objects in MyriadLAMA are primarily one-word entities. We assessed the fact prediction and oneword generation abilities of Llama2-7B, Llama3-8B, and Phi3-small using average Acc@1 and the rate of one-word generation. As shown in Table 4, only under few-shot settings, LLMs demonstrate

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 $^{^9}BERT_{\rm wwm}$ masks all tokens for a single word at the same time, while $BERT_{\rm base}$ and $BERT_{\rm large}$ masks a single token.

¹⁰The partial evaluation is sufficient to compare performance across different model sizes.

¹¹X-relation cannot be applied to single-prompt dataset.

ICL settings	Fact prediction (Average Acc@1)	one-word generation
	(Llama2-7B / Llam	a3-8B / Phi3-small)
zero-shot	.3385/.3427/.4258	.4802/.1572/.8883
4-random	.4816/.5205/.4889	.8058/.8147/.8913
4-relation	.6286/.6871/.6339	.9246/.9071/.9287
4-template	.6616/.7268/.6612	.9266/.9187/.9411

Table 4: Instruction following rates on Llama2-7B, Llama3-8B and Phi3- small.

a remarkable ability to understand instructions for 404 fact prediction and generating one-word answers, 405 indicating the effectiveness of prompting LLMs to 406 predict mask tokens through in-context learning 407 and the risk of evaluating LLMs under zero-shot 408 settings. Our evaluation with a QA-style ICL set-409 tings also confirm the same insight (see § D for 410 details). Moreover, using exemplars similar to the 411 target prompt in the few-shot context can achieve 412 improvement overall metrics (Table 3 Below), in-413 cluding the one-word generation rate (Table 4). 414

5.4 Can BELIEFs mitigate bias?

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We explore whether BELIEF can mitigate prompt bias in evaluations. To measure prompt bias quantitatively, we use content-free prompts, where the subject is replaced by meaningless tokens (Zhao et al., 2021; Xu et al., 2024), and collect the probabilities of candidate tokens in the output distributions over the mask token.¹² We measure the bias level of the prompt using the certainty of distributions over candidate tokens. Specifically, we define bias level as follows:

bias-level =
$$1 - \frac{\mathcal{H}}{\mathcal{H}_{max}}$$

where \mathcal{H} is the entropy, and \mathcal{H}_{max} is the maximum entropy for the uniform distribution with same size.

We measure bias in both single- and multiprompt evaluations. We use average bias-level over all relational templates to represent prompt bias existing during the single-prompt evaluation. Then, we simulate the prompt sampling for accuracy calculation in multi-prompt evaluation by averaging output distributions over templates of the same relation. We then use the bias-level of this average distribution to quantify bias in multi-prompt evaluation. In experiments with BERT models, we observe consistent improvement with multi-prompt

PLMs	Average Acc@1↑	Fluctu	ation↓	Consist^	Overconf
1 12/015	Acc@1	range	stdev	Consist	Overcom
Llama2-7B	.6699	.0257	.0034	.4174	0933
Llama2-13B	.7080	.0235	.0031	.4326	0662
Llama2-70B	.7784	.0190	.0024	.4449	0690
Llama3-8B	.7316	.0194	.0025	.4060	1119
Llama3-70B	.8211	.0139	.0017	.4636	0812
Phi3-mini	.6106	.0314	.0039	.3686	.0911
Phi3-small	.6668	.0306	.0039	.3667	.1221
Phi3-medium	.7100	.0207	.0025	.4009	.0317

 Table 5: BELIEF-ICL evaluation on LLMs with the

 4-template setting using manually-rewritten templates.

evaluation. For example, $BERT_{wwm}$ has average bias-level of 0.304 for single- and 0.217 for multiprompt evaluations. Taking P31:instance-of¹³ as an example, the average probability of "science" over all templates is 8.30%, but it rises to 52.79% for template: "[Y] contains [X] as one of its elements." 429

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6 Differentiating PLMs in Fact Probing

In this section, we compare the performance of different PLMs and explore the factors that impact factual knowledge learning during pre-training.

6.1 Factors affecting the acquisition of facts

1) **Pre-training strategy** From Table 3, we can observe that $BERT_{wwm}$ outperforms $BERT_{large}$ in terms of all metrics, while $BERT_{wwm}$ differs from $BERT_{large}$ only in the masking strategy during pretraining. The superiority of $BERT_{wwm}$ likely stems from its challenging pre-training paradigm, which requires recalling whole words without sub-token information, enhancing word-level contextual understanding. This underscores the importance of pre-training strategy in knowledge acquisition.

2) Model size: Then, we compare models with difference sizes as shown in Table 5.¹⁴ We find that larger LLMs consistently achieve higher accuracy in predicting facts. Combining with the improvement from BERT_{base} to BERT_{large} from Table 3, the importance of model size in fact acquisition during pre-training is confirmed. Moreover, larger models also demonstrate better robustness in handling diverse prompts and shows better reliability.

3) Pre-training corpora: Table 5 shows that Llama3-8B outperforms the larger Llama2-13B

¹²Specifically, we adopt a similar setting to (Zhao et al., 2021), by ensembling the distribution over prompts with three content-free tokens: "N/A," an empty string, and "?".

¹³https://www.wikidata.org/wiki/Property:P31

¹⁴Owing to the high computational cost of inference on large LLMs like Llama2-70B, we select only five manually rewritten templates with 4-template ICL setting for evaluation.

PLMs Acc@1		Fluctuation		Consist Overconf		1-word
		range		00110100	0,0,000	gen.
Llama2-7B	.3384	.2602	.0299	.1269	0731	.4752
Llama3-8B					1119	.1572
Phi3-mini	.3498	.2374	.0292	.1465	.1758	.8641

Table 6: BELIEF-ICL evaluation with zero-shot setting.

in fact probing. This is likely due to Llama3's pre-training corpus being seven times larger than Llama2. Additionally, Llama3-70B surpasses Llama2-70B, confirming the importance of pre-training data volume for fact acquisition.

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In the zero-shot evaluation using the entire MyriadLAMA, as shown in Table 6, Phi3-mini outperforms Llama2-7B and Llama3-8B in knowledge retrieval and fidelity to instructions (one-word generation rate). Given that Phi3-mini has about half the model size of Llama2-7B and Llama3-8B (3.8B), and model size typically enhances knowledge retrieval, this result is notable. This superior performance can be attributed to the high-quality, textbook-like material used for pre-training the Phi3 models, highlighting the significant impact of high-quality training data.

6.2 Factors affecting the reliability

Table 3 shows a significant difference in Overconf between BERT models and Llama3-8B, with BERT models being overconfident and Llama3-8B being underconfident. In this section, we explore the reasons for these differences and investigate additional factors affecting reliability beyond model size.

1) The number of output tokens: One main difference in Overconf calculation between encoderand decoder-based PLMs is that the decoder-based PLMs will generate multiple tokens. Thus, we investigate the effect of output token count on Overconf values. We divide the MyriadLAMA prompt set into groups based on the number of tokens generated. For each group, we calculate the probability of the entire token sequence and compute Overconf for token counts from 1 to 5.¹⁵

The Overconf values for each group of 1 to 5 output tokens on Llama3-8B (4-template) are -0.1030, -0.0906, -0.0297, -0.0546, and 0.0573, showing models become more overconfident with more output tokens. This trend is consistent across models.

2) The writing style of training data: As shown

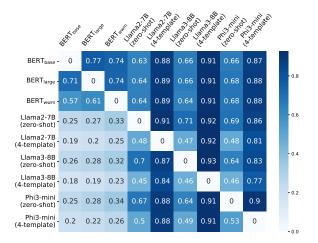


Figure 2: The knowledge sharing rate between models and ICL settings. Each cell indicates the rate of facts correctly predicted by the top-listed model relative to those captured by the left-listed model.

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in Table 5, the Phi3 and BERT models, which were pre-trained on textbook-like text such as Wikipedia, exhibit significant overconfidence in their predictions. In contrast, the Llama2 and Llama3 models, which use general online data, show better calibration between accuracy and confidence (Figure 1 **Right**). This is probably because the Phi3 and BERT models are trained to predict textbook-like text with more expressions directly describing factual knowledge (e.g., definition sentences). This highlights the significant impact of the pre-training corpora's writing style on PLM reliability.

6.3 How do PLMs perceive facts differently?

Finally, we measure the differences in fact coverage among models. We first collect the correctly predicted facts for each template, defining these as the model's covered facts. Given the covered facts of two models, we measure the knowledge sharing rates using an asymmetric metric. This metric calculates the proportion of shared facts relative to each model's total covered facts.

The results are shown in Figure 2. The average sharing rate among BERT models is 69.07%, while for Llama2-7B, Llama3-8B, and Phi3-mini in the zero-shot ICL setting, it is 67.58%. In comparison, the average sharing rate between encoder- and decoder-based PLMs reduced to 47.10%. Additionally, knowledge sharing rates in both zero-shot and 4-template settings indicate that incorporating context examples improves the knowledge elicited by the models. However, about 10% of knowledge can still only be elicited in the zero-shot setting.

¹⁵The prompts generated within five tokens cover 98.78% of Llama3-8B's generations with the 4-template ICL setting.

PLMs	Average	Maximum	Oracle
BERT _{wwm}	.1364	.4501	.6636
Llama2-7B (zero-shot)	.3385	.6577	.8153
Llama3-8B (zero-shot)	.3427	.7099	.8756
Phi3-small (zero-shot)	.4258	.6828	.8642
Llama2-7B (4-template)	.6616	.7197	.8133
Llama3-8B (4-template)	.7268	.7731	.8628
Phi3-small (4-template)	.6612	.7181	.8346

Table 7: Average: mean accuracy using all templates; Maximum: accuracy with the best template for each relation; Oracle: accuracy when the best template is selected for each factual knowledge.

7 Limitation of prompt-based probing

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Finally, we examine the limitation of prompt-based knowledge probing by using our massively diverse dataset. First, we gauge the average knowledge coverage rate by using the average Acc@1 (average). Next, for each relation, we calculate the maximum Acc@1 using the template that yields the highest accuracy,¹⁶ and use this value to estimate the upper limit of prompt-based knowledge probing (maximum). Finally, we approximate the upper limit of facts contained in LLMs, by considering a fact as existing if at least one prompt of this fact can produce the correct answer (oracle).

Table 7 shows three knowledge coverage rates on small-scale LLMs. For BERT_{wwm} and LLMs with zero-shot settings, we observe nearly a 30% increase between average and maximum accuracy, emphasizing the importance of selecting suitable templates for specific relationships and the potential gains from prompt engineering. This gap can be reduced to 5% by using few-shot settings. However, the gap between **maximum** and **oracle** accuracy mostly remains. This indicates that different facts prefer different templates, suggesting no versatile template works for all facts. Combining different templates reveals the true upper limits of PLMs in factual understanding and underscores the importance of using diverse prompts for knowledge retrieval instead of optimizing a single prompt. Refer to §F.4 for results on more models.

8 Related work

The LAMA probe was first proposed to evaluate the utility of PLMs as knowledge bases via solving the fill-in-the-blank task (Petroni et al., 2019). Several researchers extend the LAMA probe to evaluate PLMs' ability to understand facts from diverse linguistic aspects, such as the effect of negation/mispriming (Kassner and Schütze, 2020), distractors (Pandia and Ettinger, 2021), multilingual understanding (Keleg and Magdy, 2023; Zhao et al., 2024) and models' consistency facing prompts with minor nuances (Fierro and Søgaard, 2022; Elazar et al., 2021). However, these studies lack the inspection of PLMs' reliability in knowledge prediction, which is vital in deploying LLMs to realworld tasks. Moreover, solving the fill-in-the-blank task by LLMs with the causal LM objective can underestimate their knowledge understanding ability. 567

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Recently, QA-based datasets have been developed to evaluate the knowledge recall ability of decoder-only LMs. Kalo and Fichtel (2022) created a high-quality QA prompt set, which is further extended by Wiland et al. (2024) to evaluate both causal and masked LMs. Mallen et al. (2023) and (Maekawa et al., 2024) developed QA datasets to see the impact of knowledge popularity and retrieval augmentation. Since the writing style of these datasets is limited to questions, we cannot perform reliable robustness evaluation.

9 Conclusions

This paper presents multi-faceted factual probing frameworks, BELIEF and BELIEF-ICL, for encoder-based PLMs and decoder-based LLMs, respectively. Leveraging a multi-prompt dataset, BE-LIEFs provides various evaluation metrics, including accuracy, consistency, and reliability, enabling a thorough assessment of PLMs' comprehension of factual knowledge. To make BELIEF more reliable, we build a new multi-prompt dataset for knowledge probing, MyriadLAMA, featuring diverse prompts for each fact. We conducted extensive experiments of multiple encoder-based PLMs and recent LLMs. Based on the evaluation results, we verify the effectiveness of BELIEF in accurately and comprehensively probing knowledge by revealing differences between PLMs and demonstrating its ability to mitigate bias. Additionally, we identify key factors affecting the correctness and reliability of PLMs' answers in factual probing, such as model size, pretraining strategy and corpora. Finally, by probing facts in different ways, we find that PLMs hold more knowledge than what is revealed by using the optimal template, highlighting the limitations of prompt-based factual probing.

¹⁶We select the prompt with the best subject expression among prompts for each fact.

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Limitations

MyriadLAMA contains an extensive amount of

prompts, which leads to high evaluation costs. In

the future, we aim to extract a diverse yet robust

subset from MyriadLAMA to enable a more effi-

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A Construction of MyriadLAMA

In this appendix, we explain the detailed procedure for generating the derived triples from unique triples in MyriadLAMA. As discussed in §4, this study first extends the unique triples contained in LAMA-UHN (Petroni et al., 2020) by searching new objects from T-REx (Elazar et al., 2021). Next, for the obtained unique triples, we generate derived triples by combining concrete linguistic expressions associated with entities ("subjects" and objects) and diversify relational templates using both manual labor and LLMs. We describe the detailed procedure as following.

A.1 The extension of entities

Extension of unique triples from T-REx LAMA-UHN is a refined subset derived from the LAMA dataset, which LAMA originates from T-REx (Elsahar et al., 2018). T-REx is a largescale knowledge base containing 11 million realworld knowledge triples, aligned with 3.09 million Wikipedia abstracts, designed to create largescale alignments between Wikipedia abstracts and Wikidata triples. To achieve this alignment, T-REx employed three distinct aligners—NoSub, AllEnt, and SPO-each offering varying levels of accuracy (0.98, 0.96, and 0.88, respectively) as measured on a test set. Despite the high alignment accuracy of all three aligners, LAMA-UHN selects only the triples aligned by NoSub, the aligner with the highest accuracy. While this choice ensures the high correctness of triples within LAMA, it potentially compromises the ability to fairly assess a PLM's capability in understanding facts, as it may overlook valid answers during evaluation. To address this limitation, we expand the MyriadLAMA dataset by incorporating triples aligned by all three aligners-NoSub, AllEnt, and SPO-found in T-REx, based on the subject-relation pairs present in LAMA-UHN. As the result, we increase the number of unique triples from 27,106 to 34,048 as shown in Table 1.

Extension of entities using aliases Next, we utilize aliases of entities obtained from Wikidata to acquire diverse linguistic expressions (and their

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paraphrases) for the "subjects" and objects. Specifically, we used the Wikidata identifiers of entities¹⁷ and the Wikidata API¹⁸ to retrieve the (English) alias expressions of entities. By combining the aliases of "subjects" and objects with the relation templates mentioned later, we generate numerous new derived triples. If N "subjects" and M objects are given for an unique triple, the number of derived triples according to this unique triple generated from a single relational template is $N \times M$.

A.2 Diversification of relation templates

We use a two-step procedure to create new relational templates, to enhance ensure both the quality and quantity. Initially, we manually rewrite relational templates, ensuring that every relation has five templates. Then, we employ the generative LLM (GPT4) to automatically paraphrase 19 additional templates. In total, we produce 100 templates for each relation.

Step 1: Manually rewriting relational templates. The manual rewriting of the relational templates is performed by the first author of this paper. We create new templates by describing the relationship between subject and object from different perspectives rather than creating templates with absolutely the same meaning with original template. Utilizing the resource provided by Wikidata¹⁹, we not only paraphrase existing templates to generate new ones with diverse lexicons but also devise entailment expressions to encompass various semantic expressions that convey the same relations. These newly created templates are guaranteed to uphold relational equivalence, following the relationship between the subject and object. Taking P20 ([X] died in [Y].)²⁰ as an example, we create new templates by either changing the sentence pattern or adding type information of object (e.g, [X] resided in [Y] until death). Furthermore, we also create templates without directly using the keywords of the relation (dead/death) but in a entailment way (e.g., [X] spent the last years of life in [Y].) Moreover, we devise a question-answer style template for each relation to enhance syntactic diversity. In this template, the question incorporates the subject

> ¹⁷https://www.wikidata.org/wiki/Wikidata: Identifiers

> ¹⁸https://www.wikidata.org/wiki/Special: EntityData/<entity_identifier>.json

¹⁹https://www.wikidata.org/wiki/Property: <relation_identifier> and relation information, while the answer corresponds to the object.

Note that, during the paraphrase, we observe that some templates in LAMA-UHN only partially express the original meaning of relations defined in Wikidata. These are inappropriate for specific knowledge triples. For example, P136 describes the creative work's genre or an artist's field of work²¹, which the type of work includes music, film, literature, etc. However, the original templates of P136 in LAMA-UHN is "[X] plays [Y] music.," which cannot correctly retrieve information on work other than music. For this kinds of template, we abandon the original templates and newly create five templates.

Step 2: Paraphrasing templates using GPT-4 Based on the original relation templates and the relation templates rewritten manually, we further paraphras these relation templates automatically using the GPT4-API (gpt-4-1106-preview²²) provided by OpenAPI. The instruction for paraphrasing used for GPT-4 generation is:

You are a professional tool that can paraphrase sentences into natural sentences that can correctly represent the relationship between [X] and [Y], without repetition. Make the paraphrase as diverse as possible using simple words. Please paraphrase the given sentence 19 times.

When the duplicated sentence is generated, we remove the duplication and regenerate new templates with the same instruction, until 19 different templates is generated. Furthermore, we observe that GPT-4 occasionally generates relation templates that are semantically inappropriate for specific relationships due to incorrect category information of entities. Consequently, in such instances, we refine the instructions to include the category information of the entities, ensuring accurate representation of the relationship between the subjects and the objects. For example, when paraphrasing the relational template "[X] used to work in [Y]."²³, we additionally add explicit guidance regarding the expected format and semantics of the relation templates to the above instruction, as following.

²⁰https://www.wikidata.org/wiki/Property:P20

²¹https://www.wikidata.org/wiki/Property:P136 ²²https://platform.openai.com/docs/models/

gpt-4-and-gpt-4-turbo

²³https://www.wikidata.org/wiki/Property:P937

24	Be aware that [Y] is the geographic loca-
25	tion but NOT company or organization,
26	where persons or organizations were ac-
27	tively participating in employment, busi-
28	ness or other work.

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As a result, we can obtain the following paraphrased relational templates for "[X] used to work in [Y].":

- "[X] was formerly employed in [Y]."
- "[X] once worked at [Y]."
- "[Y] was the place where [X] used to be engaged in work."

A.3 Example of extended relational templates in MyriadLAMA

We display part of the created templates in MyriadLAMA. We randomly select two manually rewritten templates and three auto-generated templates of these two templates. We show the sampled templates for all the relations in Tables 19, 20, 21, 22, 23 and 24.

B The Advangage of MyriadLAMA

Given that our study seeks to mitigate the influence of individual prompt bias in evaluations, the availability of a wide range of prompts characterized in both quantity and diversity is crucial. The diversity ensures that different prompts can capture different aspects of the true knowledge distribution. On the other side, the quality or correctness of prompts ensure the evaluation can accurately reflect the true ability of understanding facts.

In this section, we provide a quantitative analysis of the quality and diversity of multi-prompt factual knowledge probing datasets. The comparison results demonstrate the superiority of MyriadLAMA over previous datasets, enabling more accurate and comprehensive evaluations. We conduct comparison between MyriadLAMA and other multi-prompts probing datasets, LPAQA (Jiang et al., 2020) and PARAREL (Elazar et al., 2021), from the perspective of quantity and diversity.

B.1 Diversity comparison

We measure the diversity of multi-prompt factual knowledge probing datasets from both **quantity** and **linguistic diversity**.

Specifically, we calculate the average number of prompts for each subject-relation pair as the

Dataset	Ouantity [↑]	Diversity [↑]			
Dataset	Quantity	Lexicon	Syntax	Semantic	
PARAREL	7.30	.4860	.1489	11.03	
LPAQA	53.27	.5449	.1713	13.55	
MyriadLAMA	263.47	.6652	.2138	12.69	

Table 8: Comparison between multi-prompts datasets.

quantity measure. MyriadLAMA introduces diversity into prompts by using various subject expressions and relational templates. On average, MyriadLAMA provides 2.47 expressions for each subject. In addition, we measure the **linguistic diversity** of relational templates from three aspects, as shown below:

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- **Lexicon:** We utilize the Jaccard distance of words in templates to gauge lexicon diversity.
- **Syntax:** We adopt the syntax distance measure proposed in (Oya, 2020), which calculates the distance between dependency trees.
- Semantics: We quantify semantic diversity by calculating the L2 distance of sentence embeddings given by $BERT_{large}$.

The results are shown in Table 8. MyriadLAMA demonstrates superior quantity and diversity compared to existing multi-prompt factual probing datasets. Although LPAQA exhibits greater semantic diversity, this is mainly due to its use of distant supervision to discover new templates. This method often results in problematic templates that inadequately describe the relationships between subjects and objects. For example, for relation P937²⁴ ("[X] used to work in [Y]."), LPAQA includes templates like "[X] to meet [Y]," which significantly deviate from the original semantic meaning. We analyze and compare template quality in the next section.

B.2 Quality comparison

In this section, we evaluate the quality of relational templates created MyriadLAMA in correctly expressing the relation between the subject and object. We manually evaluate the quality templates created in each dataset through a strict quality evaluation framework. Specifically, we evaluate each template based on its fluency and its ability to correctly express the semantic relationship between subjects

²⁴https://www.wikidata.org/wiki/Property:P937

and objects. Given the complex and specific con-1008 straints defined by Wikidata relations, creating per-1009 fect templates that satisfy all subjects and objects 1010 for a given relation is challenging. 1011

and relation

Semantic relationship between template

[**Template** \subseteq **Relation**]: If the subject and object

fit the template, it is correct for the relation, but

the relation's knowledge range is broader than the

template can cover. We denote such templates as

[**Template** \subseteq **Relation**]. Using the templates in

LAMA-UHN, which are often considered golden

templates as examples, relation P136²⁵ uses the

template "[X] plays [Y] music." to describe cre-

ative work genres or an artist's field. However,

P136 encompasses film, literature, and other arts,

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not just music.

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[**Relation** ⊆ **Template**]: In contrast, If the subjectobject pair is true for the relation, it is also true for the template, meaning the template's knowledge range is broader than the relation. For example, LAMA-UHN creates the template "[X] died in [Y]." for $P20^{26}$. While this template can be used to infer a person's place of death, "[Y]" could also be the year "[X]" passed away.

[Relation ∩ **Template** > **0]:** Additionally, some templates do not fit neatly into either [Relation \subseteq **Template**] or [**Template** \subseteq **Relation**] but can still correctly describe the relationship for some subjectobject pairs. For example, PARAREL, which paraphrases templates by human effort, uses "[X] is a follower of [Y]." to describe relation $P140^{27}$ (religion or worldview). This template is appropriate for individuals but not for organizations, and it does not fully capture the relation's scope. Therefore, it does not fit [**Relation** \subseteq **Template**]. Additionally, when "[X]" is a person, "[Y]" can be either a religious figure, leader, or the religion itself, which does not satisfy [**Template** \subseteq **Relation**]. However, many subject-relation pairs can still be correctly captured by this template. We use [Relation \cap **Template > 0**] to denote them.

[Irrelevant]: We consider templates that do not correctly convey the relationship between subject and object as [Irrelevant]. For example, LPAQA mined many irrelevant templates from the corpus

Template-aware facts Relation-defined facts Template \subseteq Relation Relation ⊆ Template Fully matching

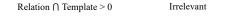


Figure 3: The relationship between the factual knowledge that can be covered by relation and template.

without careful checking, resulting in low-quality templates, such as "[X] arrived in [Y]" for P937. [Fully matching]: Finally, we use [Fully matching] to denote templates that can accurately capture all the subject-object pairs fitting in the relation.

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We demonstrate the five types of semantic relationships between template and relation in Figure 3 using the Venn diagram.

B.2.2 Template quality evaluation metrics

To accurately capture the fluency and the ability of created templates to correctly express the relationship between subjects and objects, we use the following metrics to score template quality. Each item is scored as either 1 or 0 based on whether the template meets the requirement.

1) Fluency: Is the template a natural sentence or noun phrase²⁸? Set 1 if the templates are natural; Otherwise 0.

2) [Relation \subseteq Template]: If the template can satisfy the definition of [Template \subseteq Relation], then 1; Otherwise 0.

3) [Template \subseteq Relation]: If the template can satisfy the definition of [Template \subseteq Relation], then 1; Otherwise 0.

4) [**Relation** \cap **Template** > 0]: If the template can satisfy the definition of [Relation \cap Template > **0**], then 1; Otherwise 0.

If either [**Relation** \subseteq **Template**] or [**Template**] \subseteq **Relation**] is 1, then [**Relation** \cap **Template** > 0] must also be 1. If [**Relation** \subseteq **Template**], [**Template** \subseteq **Relation**], and [**Relation** \cap **Template** > 0] are all 0, the template can is classified as [Irrelevant]. If all three metrics are 1, the template is classified as [Fully Matching].

²⁵https://www.wikidata.org/wiki/Property:P1303

²⁶https://www.wikidata.org/wiki/Property:P20 ²⁷https://www.wikidata.org/wiki/Property:P140

²⁸We take the noun phrase into consideration as LPAQA created lots of noun phrase templates, such as "[X], who works as [Y]." for relation P106 (https://www.wikidata. org/wiki/Property:P106)

Specifically, as what PLMs see is the prompt with subject, we will consider the existence of subject when scoring the template. For example, $P413^{29}$ describe the position or specialism of a player on a team. While the template "[X] plays in the position of [Y]." can be too general, as it could also describe a player's position in an orchestra, specifying "[X]" in the prompt reduces ambiguity, making it an accurate [**Fully Matching**] template to describe the relation.

B.2.3 Evaluation result and analysis

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The comparison includes the 4 dataset: LAMA-UHN, PARAREL, LPAQA and MyriadLAMA. Considering the amount of all the templates in the three models (6654 templates in total), we randomly sample 200 templates for multi-prompt probing datasets and use all 41 templates in LAMA-UHN for evaluation. To ensure objectivity, we anonymize the source of each template and mix them together for annotator (the first author). We publicize the annotation results here³⁰. The evaluation result is shown in Table 9.

From the Table 9, We observe that our semi-automatically generated relational templates achieve quality comparable to manually created datasets like LAMA-UHN and PARAREL, while being 100 times larger than LAMA-UHN and 13.7 times larger than LPAQA. MyriadLAMA significantly outperforms LPAQA in template quality due to our two-stage template creation method.

Furthermore, Figure 4 shows the score distributions for 200 templates across the three multiprompt datasets. It reveals that LPAQA has many low-score templates, with 0 being the most common score. Compared to PARAREL, Myriad-LAMA has slightly more templates with a score of 3 but slightly fewer with a score of 4, resulting in slightly lower overall quality.

C Ablation Analysis of MyriadLAMA

In this section, we conduct ablation analysis MyriadLAMA to understand the validity of diversification on entities and templates.

C.1 Validity of extended entity expressions

We evaluate the validity of the extended entity expressions in MyriadLAMA by checking if these extensions cover facts that PLMs can capture but are

Figure 4: Quality score distributions over multi-prompt factual probing datasets.

missed in LAMA-UHN due to strict entity expression limitations. We conduct this analysis on BERT models, focusing on facts with extended subject and object expressions. MyriadLAMA contains 13,123 facts with extended subjects and 23,195 facts with extended objects. We measure the rate at which extended subjects/objects achieve higher ranks than the original expressions in the token distribution output. 1134

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The results, shown in the Table 10 below, indicate that around 50% of extended subjects and 20% of extended objects achieve higher ranks than the original entities. This suggests that many facts are missed in LAMA-UHN and other singleexpression factual knowledge probing datasets.

C.2 Validity of paraphrased templates

In this section, we evaluate the validity of the rela-1150 tion templates in MyriadLAMA. We investigate the 1151 accuracy of each template and compare the accura-1152 cies between templates in LAMA-UHN, manually 1153 rewritten templates and auto-generate templates. 1154 Specifically, for each relation, we evaluate the ac-1155 curacy (Acc@1) of all relation templates separately, 1156 and then calculate the minimum, and maximum ac-1157 curacies among all templates for each relation. We 1158 then measure the dataset-level minimum/maximum 1159 accuracy by micro-averaging the template set with 1160 the minimum/maximum template accuracies (41 1161 templates in each set). Finally, all of the template-1162 specific accuracies are then micro-averaged to com-1163 pute the average Acc@1. As indicated in Table 11, 1164 while the quality of MyriadLAMA's prompts sig-1165 nificantly varies, the high-quality prompts are no-1166 tably superior to those of LAMA-UHN. Although 1167 the average accuracy of MyriadLAMA is lower 1168 than that of LAMA-UHN, it is considered that this 1169

²⁹https://www.wikidata.org/wiki/Property:P413 ³⁰https://anonymous.4open.science/r/ belief-CC8A

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Dataset	Fluency	$\textbf{Template} \subseteq \textbf{Relation}$	$\textbf{Relation} \subseteq \textbf{Template}$	Relation \cap Template > 0	Total Average
LAMA-UHN	1	.732	.976	1	3.707
PARAREL	0.99	.790	.905	.985	3.670
LPAQA	0.57	.220	.345	.405	1.540
MyriadLAMA	1	.770	.830	.985	3.585

Table 9: The average quality metrics across templates from various factual probing datasets. LAMA-UHN has 41 templates, all of which were used for evaluation. For the other three multi-prompt probing datasets, we sampled 200 templates for comparison.

PLMs	Subject	Object
$BERT_{base}$.5355	.2107
$BERT_{large}$.5358	.2116
$BERT_{wwm}$.5272	.1853

Table 10: Rate of prompts where the extend entities gain higher probability than the original entity.

PLMs		MyriadLAMA		
r Livis	LAMA-UHN	Min	Max	Mean
BERT _{base}	.2403	.0000	.3534	.1103
$BERT_{large}$.2454	.0007	.3728	.1185
BERTwwm	.2448	.0015	.3695	.1453

Table 11: Acc@1 of MyriadLAMA and LAMA-UHN

is because MyriadLAMA uses relation templates that have been semi-automatically created, whereas LAMA-UHN uses carefully selected entities and templates.

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C.3 What matters to robustness? Diverse subject vs. templates

Next, we aim to investigate the factors contributing to varying performance and inconsistent predictions of prompts. MyriadLAMA creates diverse prompts for each fact by combining different subject expressions and templates. To gauge their impact on robustness, we examine both the consistency (Consist) and the accuracy range (min/max) across various expressions of subjects or relations, assessed individually. To achieve this, the complete set of prompts was partitioned into multiple subsets, with each subset containing only one expression for each unique subjects or relations. The Acc@1 of the prompts obtained in this manner is then evaluated using different variants of BERT.

The results in Table 12 indicate that while the accuracy range (min/max) and consistency (Consist) caused by aliases of subjects is less pronounced compared to diverse expressions of relational templates, its effect on factual knowledge evaluation remains significant. These findings highlight the

PLMs	Con	nsist↑	Acc@1 range (min/max)		
	Subject	Relation	Subject	Relation	
$\text{BERT}_{\text{base}}$.5745	.1504	.0673/.1441	.0000/.3534	
$BERT_{large}$.5497	.1548	.0714/.1554	.0007/.3728	
BERT_{wwm}	.5005	.1057	.0831/.1884	.0015/.3695	

Table 12: Diversity evaluation of subjects and relation templates

vulnerability of factual knowledge evaluation based on single prompts and underscore the significance of harnessing the diversity of prompts within MyriadLAMA for robust assessments. 1196

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C.4 Manually rewritten vs. auto-generated templates

Upon comparing relational templates generated through manual rewriting and GPT-4 autogeneration, we find that auto-generated templates exhibit comparable quality (accuracy) to manually rewritten templates; they also demonstrate less diversity in acquiring different predictions, aligning with our expectations.

To assess the validity of LLM-generated templates for knowledge probing, we rank the accuracies (Acc@1) of manually created templates against those generated by LLMs. Specifically, for each relation, we rank the 5 manual templates among all 100 templates and calculate the average rank across all manually created templates for all relations. Table 13 shows the average Acc@1 ranks of manual templates among 100 templates on BERT_{base}, BERT_{large}, BERT_{wwm}. They are 47.40, 45.64, and 44.80, respectively. These values closely approximate the average rank of 50, indicating that auto-generated templates can achieve nearly the same accuracy as manually created templates.

Furthermore, we quantify the diversity discrepancy between manually written and auto-generated templates. We categorize the auto-generated templates, including the original ones, as one group, resulting in five groups for each relation, each

PLMs	Average rank of	Consist		
1 1//15	manual prompts based on Acc@1	Inner-group	Inter-group	
$BERT_{base}$	47.40	.2904	.1065	
$BERT_{large}$	45.64	.2884	.1125	
BERT_{wwm}	44.80	.2387	.0630	

Table 13: Comparison between prompts generated through manual labor and LLM.

comprising 20 templates. Subsequently, we evaluate the similarity between templates within the same group and across different groups using the consistency measure (Consist), as presented in Table 13. The consistency among prompts within the same group (inner-group) is notably high, whereas prompts from different groups (inter-group) exhibit less diversity in predictions. This underscores the significance of manual phrase rewriting, which can yield more diverse prompts and facilitate a more comprehensive evaluation.

D QA-Style ICL and its Evaluation

D.1 QA-style instruction

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Beside the mask-prediction-style (MP-style) ICL task, we also defined and evaluate a questionanswer-style (QA-style) ICL task utilizing the QA-style relational templates available in MyriadLAMA. This is available because MyriadLAMA provides 20 QA-style templates for each relation, offering not only syntactical diversity but also suitability for the autoregressive generation process in LLMs. Each QA-style prompt adheres to a format where the subject and relation construct the question, and the object corresponds to the answer, such as "Who developed [X]? [Y]." For the QA prompt, we employ the few-shot prompt comprising X random QA pairs, following the format outlined in InstructGPT (Ouyang et al., 2022). Given that all objects in MyriadLAMA are intended to be matched with single words, we append the instruction "Answer each question in one word." to ensure compatibility.

Given the limited number of templates (20 for each relation) in the QA-style, the evaluation of QA-style prompts represents only one-fifth of the full prompts in MyriadLAMA.

D.2 Evaluation

We measure the ability of QA-style prompts in adhering to instructions and compare it to MP-style prompts. To ensure a fair comparison between QA-

ICL settings		rediction c@1)	One-word generation	
	QA	MP	QA	MP
zero-shot	.4534	.5066	.5285	.4802
4-random	.5429	.5591	.7996	.8058
4-relation	.6582	.6649	.9187	.9246
4-template	.6687	.6765	.9216	.9266

Table 14: Instruction following rate on Llama2-7B.

and MP-style ICL, we conduct evaluations using shared templates in both settings on Llama2-7B, with 20 QA-style templates for each relation.

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We evaluate the abilities of fact prediction and one-word generation individually on Llama2-7B using average Acc@1 and rate of the one-word generation. As demonstrated in Table 4, Llama2-7B exhibits a remarkable capability to comprehend instructions for answering questions and generating one-word answers. We observe that QA-style instructions perform better under the zero-shot setting, likely due to decoder-based PLMs' ability to autoregressively generate text. However, this gap diminishes with the use of few-shot examples. This suggests that while MP-style prompts may slightly underestimate the knowledge in LLMs in zero-shot settings, MP-style ICL settings can demonstrate comparable or even superior performance in factual knowledge prediction compared to QA-style ICL prompts.

E Examples of **BELEIF-ICL** Prompts

In this section, we provide example prompts for the four patterns introduced in §3: zero-shot, Xrandom, X-relation, and X-template. We focus on examples where X equals 4, which is the primary setting used in our work.

E.1 zero-shot

Predict the [MASK] in each sentence in	129
one word.	129
Q: [MASK] consists of LAUPT.	129
A:	129

E.2 4-random

Predict the [MASK] in each sentence in 1300 one word. 1301 Q: [MASK] is the administrative center 1302 of Jiangsu. 1303 A: Nanjing. 1304 Plata Q: Mar del and [MASK] are

sister cities that have been developing

	to weth an
1307	together.
1308	A: Havana.
1309	Q: Malawi has established diplomatic
1310	ties with [MASK].
1311	A: Australia.
1312	Q: Which country is House of
1313	Representatives located? [MASK].
1314	A: Libya.
1315	Q: [MASK] consists of LAUPT.
1316	A:
1317	E.3 4-relation
1318	Predict the [MASK] in each sentence in
1319	one word.
1320	Q: What is the overarching group for
1321	Panzer Division Kempf? [MASK].
1322	A: Wehrmacht.
1323	Q: To whom does Mount Bulusan relate?
1324	[MASK].
1325	A: Luzon.
1326	Q: Who is responsible for Army National
1327	Guard? [MASK].
1328	A: National Guard.
1329	Q: What group is pharmacy a part of?
1330	[MASK].
1331	A: biology.
1332	Q: [MASK] consists of environmental
1333	factors.
1334	A:
1335	E.4 4-template
1336	Predict the [MASK] in each sentence in
1337	one word.
1338	Q: [MASK] consists of Panzer Division
1339	Kempf.
1340	A: Wehrmacht.
1341	Q: [MASK] consists of Mount Bulusan.
1342	A: Luzon.
1343	Q: [MASK] consists of Army National Guard.
1344	A: National Guard.
1345	Q: [MASK] consists of pharmacy.
1346	A: biology.
1347	Q: [MASK] consists of environmental
1348	factors.
1349	A:

F Experimental details

1351In this section, we list the detailed information of1352PLMs used in our study, including 3 encoder-based1353models and 8 decoder-based LLMs.

F.1 Model cards	1354
Here are the links from Hugging Face to load each model:	1355 1356
<pre>BERT_{base}: https://huggingface.co/</pre>	1357
bert-base-uncased	1358
<pre>BERT_{large}: https://huggingface.co/</pre>	1359
bert-large-uncased	1360
<pre>BERT_{wwm}: https://huggingface.co/</pre>	1361
bert-large-uncased-whole-word-masking	1362
ALBERT _{base} : https://huggingface.co/	1363
albert/albert-base-v2	1364
ALBERT _{large} : https://huggingface.co/	1365
tftransformers/albert-xxlarge-v2	1366
<pre>Llama2-7B: https://huggingface.co/ meta-llama/Llama-2-7B</pre>	1367 1368
<pre>Llama2-13B: https://huggingface.co/</pre>	1369
meta-llama/Llama-2-13B	1370
<pre>Llama2-70B: https://huggingface.co/</pre>	1371
meta-llama/Llama-2-70B	1372
Llama3-8B: https://huggingface.co/	1373
meta-llama/Meta-Llama-3-8B	1374
Llama3-70B: https://huggingface.co/	1375
meta-llama/Meta-Llama-3-70B	1376
<pre>Phi3-mini: https://huggingface.co/ microsoft/Phi-3-mini-4k-instruct</pre>	1377 1378
<pre>Phi3-small: https://huggingface.co/ microsoft/Phi-3-small-8k-instruct</pre>	1379 1380
<pre>Phi3-medium: https://huggingface.co/ microsoft/Phi-3-medium-4k-instruct</pre>	1381 1382

F.2 Model differences

We outline the differences between PLMs in their pre-training details in Table 15, including the type of Transformer architecture, model size, and the size and resources of the pre-training corpora. 1383

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F.3 Evaluation results on all PLMs based on BELIEFs

We present all evaluation results and their computational costs in this section. In Table 16,1390putational costs in this section. In Table 16,1391we report the full-scale experiments using all1392the prompts provided by MyriadLAMA. This includes PLMs with 8B parameters or fewer, such as1394

LLMs	Architecture	Model size		Pre-training corpora
			Size	Resource
$BERT_{\rm base}$	Encoder-based	110M	3.3G)
$\text{BERT}_{\rm large}$	Encoder-based	336M	3.3G	Two datasets:
$\text{BERT}_{\rm wwm}$	Encoder-based	336M	3.3G	BookCorpus, a dataset consisting of 11,038 unpublished books and
$ALBERT_{\rm base}$	Encoder-based*	11.8M	3.3G	English Wikipedia (excluding lists, tables and headers).
$ALBERT_{\rm large}$	Encoder-based*	223M	3.3G	
Llama2-7B	Decoder-based	7B	2.0T	A collection of publicly available online data
Llama2-13B	Decoder-based	13B	2.0T	(excluding sites containing a lot of personal information.
Llama2-70B	Decoder-based	70B	2.0T	The knowledge sources for factual knowledge are upsampled).
Llama3-8B	Decoder-based	8B	15T+	A collection of publicly available online data
Llama3-70B	Decoder-based	70B	15T+	$\int (\text{details unknown, the code is 4 times that of Llama2}).$
Phi3-mini	Decoder-based	3.8B	3.3T	
Phi3-small	Decoder-based	7B	4.8T	High-quality materials including educational data and code, (textbook-like generated text, high-quality chats.
Phi3-medium	Decoder-based	14B	4.8T	
+ LL DEDT				

*ALBERT use parameter compression techniques, including parameter sharing between token embeddings and transformer layers.

Table 15: The pre-training information of various PLMs used in this study

BERT_{base}, BERT_{large}, BERT_{wwm}, ALBERT_{base}, ALBERT_{large}, Llama2-7B, Llama3-8B, Phi3-mini (3.8B), and Phi3-small (7B). For decoder-based models, we conduct experiments on 4 types of ICL settings.

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For PLMs with more than 8B parameters, we 1400 report the evaluation results using partial prompts 1401 from MyriadLAMA, specifically using manually-1402 rewritten templates (5 per relation), which account 1403 for 1/20 of the prompts compared to the full-scale 1404 experiments. Meanwhile, we run these models on 1405 only two ICL settings: zero-shot and 4-template. 1406 1407 To ensure fair comparison with models having 8B parameters or fewer, we apply the same settings 1408 to all other decoder-based LLMs. The result is 1409 shown in Table 17. We also list the approximate 1410 runtime for each experiments in these two tables. 1411 The experiments are all run on the NVIDIA RTX 1412 6000 Ada. For experiments using model less than 1413 or equal to 8B parameters, we use single GPU to 1414 measure the consumption time. We use 2 GPUs for 1415 Llama2-13B and Phi3-small and 4 GPUs for 70B 1416 models. 1417

1418Furthermore, we display the calibration level1419between accuracy and confidence for a straightfor-1420ward inspection on Overconf metrics. We show1421the calibration figures of models with full-scale ex-1422periments in Figure 5 and experiments with partial1423prompts in Figure 6.

F.4 Knowledge coverage rate on all PLMs 1424

We present the average, maximum, and upper limit1425knowledge coverage rates, as introduced in §7, for1426all PLMs evaluated using all templates. The results1427are shown in Figure 18.1428

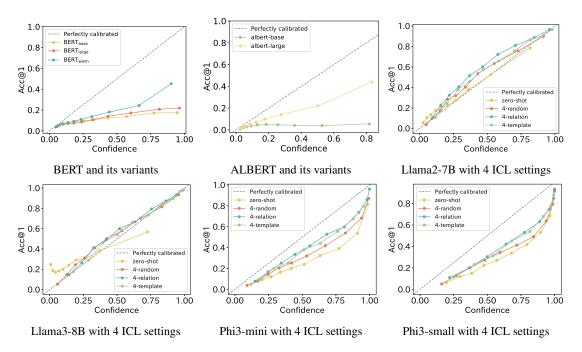


Figure 5: The calibration between accuracy and confidence of PLMs' prediction with full-scale experiments.

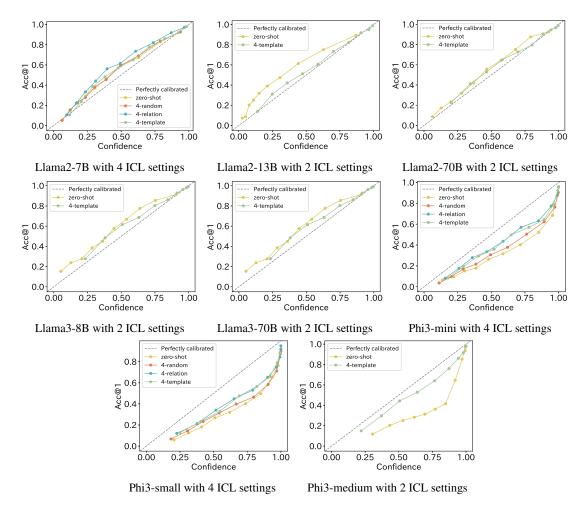


Figure 6: The calibration between accuracy and confidence of PLMs' prediction with partial-scale experiments (using manually rewritten templates only).

PLN	Ле	Average	Fluctu	ation↓	Consist^	Overconf	one-word 🔶	Runtime
	15	Acc@1	Range	Stdev	Consist	Overcom	Generation Rate	Kuntinie
	$BERT_{base}$.1095	.1534	.0217	.1682	.2154	N/A	6.3h
BERT	$BERT_{\mathrm{large}}$.1102	.1574	.0220	.1713	.2052	N/A] – 41
	BERT_{wwm}	.1364	.1517	.0208	.1524	.1000	N/A	}7.4h
ALBERT	$ALBERT_{\rm base}$.0362	.0668	.0131	.1333	.1647	N/A	6.1h
ALDENI	$ALBERT_{\rm large}$.0974	.1110	.0148	.0821	.0553	N/A	15.2h
	zero-shot	.3385	.2602	.0299	.1269	1119	.4752	46.4h
Llama2-7B	4-random	.4816	.2250	.0270	.2312	0894	.8247	
Liailia2-7D	4-relation	.6286	.1221	.0150	.3753	1335	.9060	47.8h
	4-template	.6616	.0294	.0036	.4163	0933	.9299	J
	zero-shot	.3427	.2864	.0350	.0240	1329	.1572	44.9h
Llama3-8B	4-random	.5205	.2033	.0273	.2156	0796	.8147)
Liama5-0D	4-relation	.6871	.1236	.0156	.3659	0783	.9071	82.1h
	4-template	.7268	.0220	.0026	.4015	0582	.9187	J
	zero-shot	.3498	.2374	.0292	.1465	.1752	.8641	30.7h
$\mathbf{D}\mathbf{h}_{i2}$ mini $(2.9\mathbf{D})$	4-random	.4193	.2324	.0269	.1649	.1189	.8184)
Phi3-mini (3.8B)	4-relation	.5686	.1440	.0164	.2818	.0755	.8769	32.9h
	4-template	.6067	.0510	.0048	.3612	.0887	.8808	
	zero-shot	.4258	.2437	.0292	.1782	.2171	.8883	82.4h
	4-random	.4889	.2170	.0276	.2070	.1670	.8913	
Phi3-small (7B)	4-relation	.6339	.1012	.0129	.3361	.1252	.9287	148h
	4-template	.6612	.0360	.0043	.3626	.1279	.9411	J

Table 16: Evaluation results and approximate experiment runtime on all MyriadLAMA data. Comparison of LLMs with 8B parameters or less, including BERT and its variants, across four ICL settings.

PLMs		Average	Fluctu	Fluctuation ↓		Overconf	one-word 🔒	Runtime
		Acc@1	Range	Stedv	Consist↑	Overcom	Generation Rate	Kuntine
	Phi3-mini (3.8B)	.4248	.1880	.0247	.2066	.1609	.8596	1.54h
	Phi3-small (7B)	.4881	.1900	.0244	.2284	.1985	.8996	4.12h
	Llama2-7B	.4311	.2014	.0249	.1932	0922	.5558	2.32h
zaza shat	Llama3-8B	.4224	.2820	.0353	.1269	1438	.1786	2.45h
zero-shot	Llama2-13B	.4785	.2131	.0260	.1437	1673	.3185	4.84h
	Phi3-medium (14B)	.5173	.2123	.0277	.6167	.2316	.7759	4.85h
	Llama2-70B	.5675	.2126	.0280	.0359	0988	.6239	28.97h
	Llama3-70B	.5974	.2137	.0278	.2290	1438	.7790	32.55h
	Phi3-mini (3.8B)	.6106	.0314	.0039	.3686	.0911	.9051	1.65h
	Phi3-small (7B)	.6668	.0306	.0039	.3666	.1222	.9413	7.40h
	Llama2-7B	.6699	.0257	.0034	.4174	0933	.9299	2.39h
1 tommlata	Llama3-8B	.7316	.0194	.0025	.4060	1119	.9190	4.10h
4-template	Llama2-13B	.7080	.0235	.0031	.4326	0662	.9190	4.23h
	Phi3-medium (14B)	.7304	.0207	.0025	.4009	.0317	.9350	3.88h
	Llama2-70B	.7784	.0190	.0024	.4448	0690	.9256	21.99h
	Llama3-70B	.8211	.0139	.0017	.4636	0812	.9378	43.10h

Table 17: Evaluation results and approximate experiment runtime on partial MyriadLAMA data. Comparison of all LLMs (8 models) using zero-shot and 4-template ICL settings with manually rewritten templates.

P	PLMs		Maximum	Upper Limit
	$BERT_{base}$.1095	.4248	.6209
BERT	$\text{BERT}_{\text{large}}$.1102	.4451	.6556
	BERTwwm	.1364	.4501	.6636
ALBERT	$ALBERT_{\mathrm{base}}$.0362	.2175	.3405
ALDENI	$ALBERT_{\rm large}$.0974	.3746	.5979
	zero-shot	.3385	.6577	.8153
Llama2-7B	4-random	.4816	.7026	.8587
Liaiiia2-7D	4-relation	.6286	.7179	.8475
	4-template	.6616	.7197	.8133
	zero-shot	.3427	.7099	.8756
Llama3-8B	4-random	.5205	.7339	.8867
Liama5-0D	4-relation	.6871	.7733	.8934
	4-template	.7268	.7731	.8628
	zero-shot	.3498	.6346	.8381
Phi3-mini	4-random	.4193	.6506	.8423
F1113-111111	4-relation	.5686	.6791	.8436
	4-template	.6067	.6754	.8114
	zero-shot	.4258	.6828	.8642
Phi3-small	4-random	.4889	.7037	.8695
i mo-small	4-relation	.6339	.7172	.8507
	4-template	.6612	.7181	.8346

Table 18: Knowledge coverage rate on models with full-scale experiments. **Average**: mean accuracy using all templates; **Maximum**: accuracy with the best template for each relation; **Upper Limit**: accuracy when the best template is selected for each knowledge relation.

Relation IDs	Manual rewriting templates	GPT-4 paraphrased templates
		[X] took their first steps of life in [Y].
	[X] started their life in [Y].	[X] activated their life's beginning in [Y].
		[X] initiated their journey of life within [Y].
		The origin of [X] took place in [Y].
P19	The birth of [X] occurred in [Y].	The inception of [X] was within [Y].
		It was in [Y] that [X] first made its appearance
		In [Y], [X] spent the end of their life.
	[X] spent the last years of life in [Y].	[X]'s final era was in [Y].
	[X] spent the last years of file in [1].	In [Y], [X]'s life came to a close.
D2 0	[X] is the last place or [X] lived out it death	[X] inhabited [Y] up until death.
P20	[Y] is the last place where [X] lived until death.	[Y] was the end-of-life dwelling for [X].
		[Y] served as the last dwelling for [X]
		before they died. What is the general class that [X] is
		a part of as a subclass? [Y].
	Of which class is [X] a subclass? [Y].	What larger class encompasses [X] as
		a subclass? [Y].
		Into which class is [X] categorized as
P279		a subclass? [Y].
		[X] is intrinsically a [Y].
	[X] is also necessarily a [Y].	[X] is fundamentally a [Y].
		[X] is by definition a [Y].
	[Y] is spoken as an official language by people in [X].	[Y] is the authorized language for formal
		use in [X].
		The official language spoken by individuals
		in [X] is [Y].
		[X] endorses [Y] as the language for state-related communication.
P37		In [X], the standard language for dialogue
	Officially, the people living in [X]	among the populace is [Y].
	use the language [Y] for communication.	Residents of [X] typically converse in [Y].
		The official medium of verbal exchange
		in [X] is the [Y] language.
		[X] was selected for the [Y] position.
	[X] was given the [Y] job.	[X] was named the new [Y].
		The [Y] duties have been allocated to [X].
		[X] has risen to fame with their [Y]
P413		playing abilities.
	[X] is a famous [Y] player.	[X] is well-known for playing [Y].
		[X] is notable for their expertise in [Y].
		[Y] was the origin of the broadcast for [X].
	[X] premiered on the network [Y].	[X] was initially broadcasted by [Y].
		The debut broadcast of [X] was on [Y].
		[X] was originally brought to the public by [Y
P449	[Y] is the first air channel of [X].	[X] first hit the airwaves courtesy of [Y].
1 ++ 7	[1] is the first an enamer of [A].	• • • •
		[X] first reached listeners and viewers via [Y] [X] and [Y] are countries that are in
		close proximity.
	[X] and [Y] are neighboring countries.	[Y] lies in the vicinity of [X].
		[Y] and [X] are countries that share a boundar
P47	Version of threads [V] (1.5V)	[X] acts as a gateway to [Y].
-	You can go through [X] to reach [Y].	To reach [Y], one can travel through [X].
		Traveling over [X] can bring you to [Y].

Relation IDs	Manual rewriting templates	GPT-4 paraphrased templates
	Who or what is [X] named after? [Y].	Who is the namesake behind [X]? [Y]. What is the etymology behind [X]'s name? [Y]. Who or what was [X] called after? [Y].
P138	[X] is named after [Y].	[X] takes its name from [Y].[Y] is the inspiration behind the name of [X].[X] holds the name given in tribute to [Y].
	[X] is created in language [Y].	[X] was composed in the [Y] language.[X] unfolds in the language known as [Y].[X] is expressed through the language of [Y].
P364 P463	[X] was written in the [Y] language.	The words of [X] are in the [Y] language. The composition of [X] is in the [Y] language. [X] was created using the [Y] language.
	[X] served for [Y].	[X] took part in [Y].[X] collaborated with [Y].[X] held a position at [Y].
	Which group or organization does [X] belong to? [Y].	[X] is part of what organization? [Y].[X] is a member of which entity? [Y].Can you tell me which entity [X] is a member of? [Y].
	Which field does [X] work in? [Y].	In what industry is [X] employed? [Y]. [X] holds a position in which field? [Y]. [X] is a professional in what sector? [Y].
P101	[X] is influential in the domain of [Y].	The domain of [Y] feels the considerable impact of [X]. [X] plays a pivotal role in the sphere of [Y]. [X] has a profound effect on [Y].
DIAC	[X] is famous for achievements as a [Y].	 [X] is well-known for their accomplishments in the [Y] role. [X] is well-known for their successful career as a [Y]. [X] is a celebrated [Y] with a long list of achievements.
P106	[X] is a [Y] by profession.	[X] has built a career as a [Y].[X] is employed as a [Y].[X] carries out the role of a [Y].
	[Y] is a member of [X].	[X] contains [Y] as part of its composition.[Y] holds a place in [X].[Y] is a piece of [X].
P527	[Y] belongs to [X].	[Y] is held by [X].[X] has [Y] under its ownership.[Y] is one of the items owned by [X].
Р530	[Y] is one of the countries [X] has diplomatic relations with.	 [Y] is a member of the group of countries with which [X] conducts diplomacy. [X] has a formal diplomatic relationship with [Y], as it does with several other countries. [Y] is recognized by [X] as a diplomatic
	[X] has established diplomatic ties with [Y].	 partner among other nations. [X] has initiated formal diplomatic relations with [Y]. [X] and [Y] have begun a diplomatic relationshi [X] and [Y] have set up official diplomatic links

Table 20: Examples of templates in MyriadLAMA - part 2

Relation IDs	Manual rewriting templates	GPT-4 paraphrased templates	
	[X] is a product of [Y]'s manufacturing.	The entity [Y] crafts and produces [X]. The item [X] is fabricated by [Y]. [X] is brought to life by [Y]'s manufacturing capabilities.	
P176	Which company produced [X]? [Y].	Can you tell me who made [X]? [Y]. Which producer can be linked to [X]? [Y]. What is the producing company of [X]? [Y].	
	[X] is a person from country [Y].	[X] is a resident of [Y].[X] bears the nationality of [Y].[X] is a product of [Y].	
P27	The nationality of [X] is [Y].	[X] is a native of [Y].[X] is identified as a national from [Y].[Y] is the country of origin for [X].	
P407	[X] is in language [Y].	The language of [X] is [Y]. The primary linguistic expression of [X] is in [Y]. [X] is articulated through the [Y] language.	
	[X] is a work in the [Y] language.	The [Y] language is the linguistic fabric of [X].[X] has been produced using the [Y] language.[X] is an example of literature in the[Y] language.	
P30	On what continent is [X] located? [Y].	 What's the name of the continent that [X] calls home? [Y]. What continental landmass does [X] occupy? [Y]. [X] lies on which of the Earth's continents? [Y]. 	
	[X] is a part of the continent [Y].	 [X] is a section of the continental land of [Y]. [X] is geographically positioned as part of continent [Y]. [X] is an integral piece of the continent [Y]. 	
P178	[X] was originally created by [Y].	The foundation of [X] was laid by [Y]. The concept of [X] was conceived by [Y]. [X] first came into existence thanks to [Y].	
	[X] is developed by [Y].	[Y] has developed [X].[Y] is the developer behind [X].[Y] stands as the creator of [X].	
P1376	[X] is the capital of [Y].	[Y]'s governmental seat is in [X].[X] is recognized as the official capital of [Y].The leading city and capital of [Y] is [X].	
	[X] is the administrative center of [Y].	 [Y]'s administrative leadership is situated in [X]. [Y]'s administrative affairs are managed from [X] [X] is where [Y]'s administrative management is anchored. 	
	[Y] is the place where [X] is located.	[X] resides in [Y].[X] can be found at the location of [Y].[X] is anchored in [Y].	
P131	[X] is located in [Y].	[Y] is where [X] is established.[Y] contains [X].[Y] houses [X].	

Table 21: Examples of templates in MyriadLAMA - part 3

Relation IDs	Manual rewriting templates	GPT-4 paraphrased templates
		[X] communicates in what vernacular? [Y].
	What language does [X] use? [Y].	What tongue does [X] utilize? [Y].
		What is the primary language for [X]? [Y].
		The tongue of [X] is the language [Y].
P1412	[Y] is the language that is used by [X].	[X] uses [Y] as its mode of speech.
		[Y] is the language that enables communication for [X].
		[Y] is the employer of [X].
	[X] is employed by [Y].	[X] has a job at [Y].
		[Y] is the source of employment for [X].
		Who does [X] report to in their job? [Y].
P108	Who does [X] work for? [Y].	For whom is [X] currently working? [Y].
		Who holds [X] on their team? [Y].
		In terms of genre, how would you classify
	What is the same of [V]2 [V]	[X]? [Y].
	What is the genre of [X]? [Y].	What category of genre does [X] belong to? [Y].
		In what genre category would you place [X]? [Y].
P136	[X] is the representative of the [Y] style.	[X] personifies the [Y] style in its purest form.
		[X] is the epitome of the [Y] approach.
		[X] is the archetype of the [Y] tradition.
	Which country is [X] located? [Y].	Can you identify the country where [X]
		is situated? [Y].
		Could you specify the country of [X]'s location? [Y].
		[X] can be located in what country? [Y].
P17		[X] can be located in what country? [1]. [Y] is the nation that houses [X].
11,	[Y] is the country in which [X] is located.	[Y] encompasses the region where [X] can be found
	[1] is the country in which [A] is located.	[Y] is the setting for the location of [X].
		What position does [X] occupy? [Y].
	What position does [X] hold? [Y].	What is the employment status of [X]? [Y].
		What is the position title for [X]? [Y].[X] has been designated the official role of [Y].
P39	[X] was sworn in as [Y].	
F 39		[X] pledged their commitment to the role of [Y].
		[X] was confirmed in the role of [Y].
	W71 · 1 · 1 1 ·	Which label has [X] on its roster? [Y].
	Which music label represents [X]? [Y].	Who is [X]'s music label? [Y].
		With whom is [X] signed for music production? [Y]
D2(4		The music label acting on behalf of [X] is [Y].
P264	[X] is represented by music label [Y].	[Y] is the music label that has signed [X].
		[X] has music label [Y] as its representative.
		What's the location of [X]? [Y].
	Where is [X] located? [Y].	Where can [X] be found? [Y].
		Where should I look for [X]? [Y].
		[X] is positioned in [Y].
P276	[X] is located in [Y].	[X] occupies a space in [Y].
		[Y] contains [X].

Table 22: Examples of templates in MyriadLAMA - part 4

Relation IDs	Manual rewriting templates	GPT-4 paraphrased templates
	[Y] is the place where [X] worked.	[X] had their employment based in [Y].[X] found their employment setting in [Y].[X] conducted their professional activities in [Y].
P937	[X] had work activity in [Y].	[X] took part in business tasks in [Y].[X] was employed within the confines of [Y].[X] was operational in the workforce at [Y].
P140	Which religion is [X] affiliated with? [Y].	What religious belief does [X] adhere to? [Y]. Which spiritual path is embraced by [X]? [Y]. What is the creed of [X]? [Y].
	[X] is affiliated with the [Y] religion.	[X] is part of the [Y] religious denomination.[X] is associated with the [Y] spiritual tradition.
	[X] is a [Y] player.	 [X] adheres to the [Y] religion. [X] specializes in the [Y]. [X] is a seasoned [Y] player. [X] is a [Y] specialist.
P1303	[X] plays [Y].	 [X] expresses their musicianship through [Y]. [X] has chosen [Y] as their musical companion. [X] is a musician who specializes in [Y].
	Who owns [X]? [Y].	Whose property is [X] considered to be? [Y]. Who is the legal holder of [X]? [Y]. Who has the ownership rights to [X]? [Y].
P127	[X] is owned by [Y].	[Y] is the proprietor of [X].[Y] holds the title to [X].[Y] possesses [X].
	[X] grew up speaking [Y] as their first language.	[X]'s formative years were shaped by speaking [Y][X] started their life speaking [Y].[X]'s childhood language was [Y].
P103	[Y] is the mother tongue of [X].	 [X] has [Y] as their original tongue. [X] was nurtured in an environment where [Y] is spoken. [X] has [Y] as the language of their upbringing.
	The city of [X] is twinned with [Y].	 [Y] has [Y] as the language of their upornight. [Y] and [X] have entered into a twinning arrangement. [X] is in a twinning relationship with [Y]. A twinning link has been established between [X] and [Y].
P190	[X] and [Y] are sister cities that have been developing together.	[X] and [Y] have been sister cities on a shared developmental journey. The cities of [X] and [Y] have jointly progressed as sister municipalities. [X] and [Y] have been in lockstep as sister cities in their development.
	[X] applies to the jurisdiction in [Y].	The jurisdiction of [Y] encompasses [X]. [X] is answerable to the legal system in [Y]. [Y] exercises legal control over [X].
P1001	The region of [Y] uses [X] as a legal term.	 [X] is a term with legal standing in [Y]. The legal system of [Y] includes [X] as an official term. [X] is employed as a juridical term in [Y].

Table 23: Examples of templates in MyriadLAMA - part 5

Relation IDs	Manual rewriting templates	GPT-4 paraphrased templates
		[X] represents a [Y].
	[X] is a [Y].	[X] is an example of a [Y].
		[X] is termed a [Y].
		[X] is a particular instance that reflects [Y].
P31	Speaking of [Y], [X] is an example of it.	[X] is a variant that falls within the
		scope of [Y].
		[Y] can be demonstrated through [X].
		[X] was first found in the land of [Y].
	[X] originates from the country of [Y].	The inception of [X] is linked to the country [Y].
		The origin of [X] can be traced back to [Y].
		[X] has its roots in [Y].
P495	[X] first appeared in [Y].	[X] was first crafted in [Y].
		The origin of [X] is attributed to [Y].
		[X]'s functioning is reliant on the main
	The operation of [X] depends on the headquarters in [Y].	office in [Y].
		The base in [Y] is essential for [X] to function.
		The primary operations of [X] are contingent upon the base in [Y].
P159	The headquarters of [X] is in [Y].	[Y] is home to the central office of [X].
		The top office of [X] is positioned in [Y].
		The nerve center for [X]'s operations
		is based in [Y].
	[Y] is the administrative center of [X].	The nerve center for [X]'s administration
		is found in [Y].
		[X]'s administrative governance is centralized in [Y].
		[X] is administratively governed by [Y].
P36		[Y] functions as [X]'s political hub.
	[Y] represents the capital city for [X].	[X] uses [Y] as its head city.
		[X]'s administrative center is [Y].
		[Y] served as the starting point for [X]'s career.
	[X] started their career in [Y].	[X] began earning their stripes in the
		field of [Y].
		[X] commenced their employment journey with [Y].
P740	The formation location of [X] is [Y].	The assembly point for [X] is [Y].
1,10		[Y] is recognized as the setting for
		[X]'s formation.
		[Y] is where [X] originates.
		Who owns [X]? [Y].
	Which entity does [X] belong to? [Y].	What is the overarching group for [X]? [Y].
		What organization encompasses [X]? [Y].
2011		[X] is what [Y] is primarily made of.
P361	[Y] consists of [X].	[Y] incorporates [X] within it.
		[Y] is structured with [X].

Table 24: Exa	mples of tem	plates in M	IyriadLAMA -	part 6
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