
Direct then Diffuse: Incremental Unsupervised Skill Discovery for State Covering and Goal Reaching

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Abstract

1 Learning meaningful behaviors in the absence of a task-specific reward function
2 is a challenging problem in reinforcement learning. A desirable unsupervised
3 objective is to learn a set of diverse skills that provide a thorough coverage of
4 the state space while being directed, i.e., reliably reaching distinct regions of the
5 environment. At test time, an agent could then leverage these skills to solve sparse
6 reward problems by performing efficient exploration and finding an effective goal-
7 directed policy with little-to-no additional learning. Unfortunately, it is challenging
8 to learn skills with such properties, as diffusing (e.g., stochastic policies performing
9 good coverage) skills are not reliable in targeting specific states, whereas directed
10 (e.g., goal-based policies) skills provide limited coverage. In this paper, inspired
11 by the mutual information framework, we propose a novel algorithm designed
12 to maximize coverage while ensuring a constraint on the directedness of each
13 skill. In particular, we design skills with a decoupled policy structure, with a first
14 part trained to be directed and a second diffusing part that ensures local coverage.
15 Furthermore, we leverage the directedness constraint to adaptively add or remove
16 skills as well as incrementally compose them along a tree that is grown to achieve a
17 thorough coverage of the environment. We illustrate how our learned skills enables
18 to efficiently solve sparse-reward downstream tasks in navigation and continuous
19 control environments, where it compares favorably with existing baselines.

20 1 Introduction

21 Deep reinforcement learning (RL) algorithms have been shown to effectively solve a wide variety of
22 complex problems [e.g., 23, 6, 31, 12, 2, 28]. However, they are often designed to solve one single
23 task at a time and they need to restart the learning process from scratch for any new problem, even
24 when it is defined on the very same environment (e.g., navigating to different locations in the same
25 apartment). Recently, unsupervised RL (URL) has been proposed as an approach to address this
26 limitation. In URL, the agent first interacts with the environment without any extrinsic reward signal.
27 Afterward, the agent leverages the experience accumulated during the unsupervised learning phase to
28 efficiently solve a variety of downstream tasks defined on the same environment.

29 In this paper, we consider the URL setting where the agent starts from an initial state s_0 and it resets
30 to it every time the policy terminates. We focus on sparse-reward downstream tasks, which require
31 effective exploration (i.e., via a thorough coverage of the state space) to find the goal as well as
32 learning a policy reliably reaching the goal (i.e., a directed policy).

33 We build on the insight that *mutual information* (MI) effectively formalizes the dual objective of
34 learning skills that both cover and navigate the environment efficiently [e.g., 11]. Specifically, given
35 the state variable S and some variables Z on which the skill policies are conditioned, MI is defined as

$$\mathcal{I}(S; Z) = \underbrace{\mathcal{H}(S)}_{\text{coverage}} - \underbrace{\mathcal{H}(S|Z)}_{\text{directedness}} = \mathcal{H}(Z) - \mathcal{H}(Z|S), \quad (1)$$

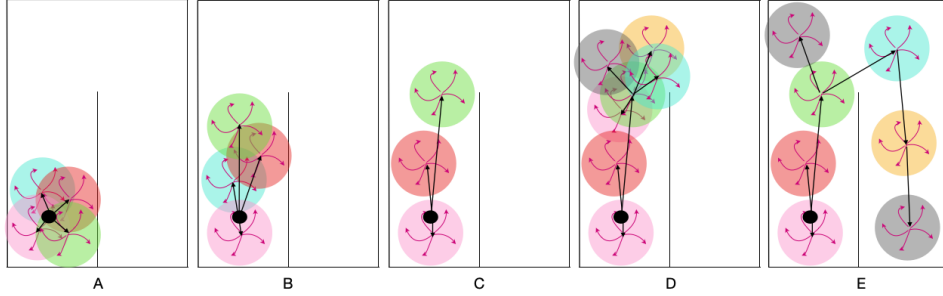


Figure 1: Overview of UPSIDE. The black dot corresponds to the initial state s_0 . (A) A set of random skills is initialized, each skill being composed of a *directed* part (illustrated as a black arrow) and a *diffusing* part (red arrows), which induces a local coverage (colored circles). (B) The policies associated to the directed part of each skill are then updated to maximize the discriminability of the states reached by their diffusing part (Sect. 3.1). (C) The least discriminable skills are iteratively removed while the policies of the remaining skills are re-optimized. This is executed until the discriminability of each skill satisfies a given constraint (see Sect. 3.2). In this example three skills are kept. (D) One of these learned skill is then used as basis to add new skills, which are then optimized following the same procedure. For the “red” and “purple” skills, UPSIDE is not able to find sub-skills of sufficient quality and thus they are not expanded any further. (E) At the end of the process, UPSIDE has created a tree of directed skills covering the state space (Sect. 3.3). These covering skills can then be used to solve downstream tasks. Moreover, the discriminator learned together with the skills can be used to select the skill to reach any specific goal region, where the directed parts get close to the goal, while the diffusing part provides the local coverage to attain the goal. The complete algorithm is detailed in Sect. 3.4 and Appendix.

36 where \mathcal{I} denotes the MI and \mathcal{H} is the entropy function. The first expression, known as the forward
 37 form of MI, explicitly balances the two sought-after properties of *coverage* — captured by the entropy
 38 over the state space $\mathcal{H}(S)$ — and *directedness*, i.e., the ability to reach specific states S depending
 39 on Z — captured by the negative conditional entropy $-\mathcal{H}(S|Z)$. The second expression of (1), often
 40 easier to optimize and referred to as the reverse form, stipulates that the skills should be sampled as
 41 diversely as possible while being discriminable.

42 Maximizing (1) has been shown to be a powerful approach for encouraging exploration in RL [16, 25]
 43 and for unsupervised skill discovery [e.g., 11, 9, 1, 30, 8]. Nonetheless, learning skills that maximize
 44 the MI is a challenging optimization problem. Several approximations have been proposed to simplify
 45 the problem at the cost of possibly deviating from the original objective of coverage and directedness
 46 (see Sect. 4 for a review of related work). In this paper, we propose UPSIDE (*UnsuPervised Skills*
 47 *that dIrect then DiffusE*) to learn skills that can be effectively used to solve goal-based downstream
 48 tasks. Our solution builds on the following components (see Fig. 1 for an illustration of UPSIDE):

- 49 • *Skill structure.* In order to balance coverage and directedness, we design skills composed of two
 50 parts: **1)** a *directed* part that is trained to reach a distinct region of the environment, and **2)** a
 51 *diffusing* part that covers the states around the region attained by the first part.
- 52 • *Optimization.* We further strengthen the coverage and directedness properties of the skills by
 53 turning the MI objective into a constrained optimization problem designed to maximize coverage
 54 under the constraint that *each* skill achieves a minimum level of discriminability. This in turn
 55 enables UPSIDE to adaptively add skills to improve coverage, when all the initial skills meet the
 56 constraint, or remove those that violate the constraint to guarantee that each skill is directed and
 57 reaches a distinct region of the environment.
- 58 • *Tree structure.* When the agent starts from a fixed initial state, the skills’ length is a crucial
 59 parameter, where short skills do not allow for proper coverage, and long skills are difficult to train.
 60 In UPSIDE we consider short skills to make the optimization easier, while composing them along a
 61 tree structure that ensures an adaptive and deep coverage of the environment.

62 We study how our learned skill structure enables to both perform efficient exploration and learn
 63 effective goal-reaching policies in a variety of navigation and continuous control environments
 64 (including MuJoCo’s *reacher*) and we compare its performance to relevant baselines.

65 2 Setting

66 We consider the URL setting where the agent interacts with a Markov decision process (MDP) M
 67 with state space \mathcal{S} , action space \mathcal{A} , dynamics $p(s'|s, a)$, and **no reward**. The agent starts each

68 episode from a designated initial state $s_0 \in \mathcal{S}$. Upon termination of the chosen policy, the agent is
 69 then reset to s_0 . This setting is particularly challenging from an exploration point of view since the
 70 agent cannot rely on the initial distribution to cover the state space.

71 We recall the MI-based unsupervised skill discovery approach [see e.g., 11]. Denote by Z some
 72 (latent) variables on which the skills of length T are conditioned. There are three optimization
 73 variables: (i) the support of the skills denoted by $|Z|$ (we consider it to be discrete so $|Z|$ is the
 74 number of skills), (ii) the policy $\pi(z)$ associated to skill z , and (iii) the sampling rule ρ (i.e., $\rho(z)$
 75 is the probability of sampling skill z at the beginning of the episode). Let the variable S_T be the
 76 random (final) state induced by sampling a skill z from ρ and executing the associated policy $\pi(z)$
 77 from s_0 for an episode. We denote by $p_{\pi(z)}(s_T)$ the distribution over (final) states induced by
 78 executing the policy of skill z , by $p(z|s_T)$ the probability of z being the skill to induce state s_T , and
 79 let $\bar{p}(s_T) = \sum_{z \in Z} \rho(z) p_{\pi(z)}(s_T)$. Then maximizing the MI between Z and S_T can be written as

$$\begin{aligned} \max_{|Z|, \rho, \pi} \mathcal{I}(S_T; Z) &= \mathcal{H}(S_T) - \mathcal{H}(S_T|Z) = - \sum_{s_T} \bar{p}(s_T) \log \bar{p}(s_T) + \sum_{z \in Z} \rho(z) \mathbb{E}_{s_T} [\log p_{\pi(z)}(s_T)] \\ &= \mathcal{H}(Z) - \mathcal{H}(Z|S_T) = - \sum_{z \in Z} \rho(z) \log \rho(z) + \sum_{z \in Z} \rho(z) \mathbb{E}_{s_T} [\log p(z|s_T)], \quad (1) \end{aligned}$$

80 where in the expectations $s_T \sim p_{\pi(z)}(s_T)$. As discussed in Sect. 1, learning the optimal $|Z|$, ρ , and π
 81 is a challenging problem [see e.g., 11, 9, 8].

82 3 Algorithm Structure

83 UPSIDE is based on three main components: **a**) the skill learning corresponding to stage *A* and *B* of
 84 Fig. 1 and described in Sect. 3.1, **b**) a constrained optimization problem used to optimize the number
 85 of skills (stage *C* and Sect. 3.2) and **c**) a tree-building procedure (stage *D* and Sect. 3.3). Together,
 86 these components allow UPSIDE to discover skills that combine coverage and directedness.

87 3.1 Skill Structure and Optimization

88 As shown in e.g., [9, 30, 37], the level of stochasticity of each skill (e.g., induced via a regularization
 89 on the entropy over the actions) plays a key role in trading off coverage and directedness. In fact,
 90 while randomness promotes broader coverage, it may compromise the directedness of the skills.
 91 In fact, a highly stochastic skill tends to induce a distribution $p_{\pi(z)}(s_T)$ over final states with high
 92 entropy (thus decreasing $-\mathcal{H}(S_T|Z)$), which prevents the skill to be reusable in solving sparse-reward
 93 downstream tasks where the objective is to reliably reach a specific goal state of the environment.
 94 Determining *how much* stochasticity to inject to adequately balance both objectives and optimize (1)
 95 is a difficult problem.¹

96 We propose to design skills with a *decoupled policy structure*:

- A *directed* part (of length T) with low stochasticity and trained to reach a specific region of the environment. It is responsible for increasing the $-\mathcal{H}(S|Z)$ term in (1).
- A *diffusing* part (of length H) with high stochasticity to promote local coverage of the states around the region reached by the directed part. It is responsible for increasing the $\mathcal{H}(S)$ term in (1).

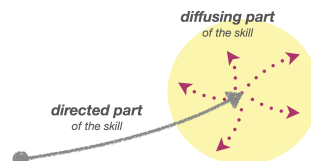


Figure 2: Directed and diffusing parts of the skill.

98 Similar to prior work [e.g., 11, 9], the policy associated to the directed part of skill z is trained to max-
 99 imize an intrinsic reward $r_z(s) \approx p(z|s)$,² where $p(z|s)$ measures the “discriminability” of the skill z
 100 given the state s . More formally, $\pi(z)$ maximizes the cumulative reward $\mathbb{E}_{\pi(z)} [\sum_{t=T+1}^{T+H} r_z(s_t)]$
 101 over the states traversed by the policy during the diffusing part. In practice, we also add a small
 102 entropy regularization $\mathcal{H}(\pi(\cdot|z, s_t))$ to the directed policy in order to ensure a minimum level of
 103 exploration and make the learning more robust. For the diffusing part, we rely on a simple random
 104 walk policy (i.e., a stochastic policy with uniform distribution over actions).

¹In RL, stochasticity is injected at “train time” to boost *exploration* or improve *robustness*, while the policy executed at “test time” is deterministic. Here we refer to stochasticity introduced to better optimize (1).

²Although [11, 9] employ rewards in the log domain, we find that using a reward that is a non-linear transformation into $[0, 1]$ works better in practice, as also observed in [33, 5]. Furthermore, in practice we replace $p(z|s)$ by the predictions of a learned discriminator $q_\phi(z|s)$ as explained in Sect. 3.4.

105 Intuitively, the diffusing part defines a cluster of states that is used as a goal for the directed part.
 106 This allows us to “ground” the latent variable representations of the skills Z to specific regions of
 107 the environment (i.e., the clusters). As a result, maximizing the MI over such skills can be seen as
 108 learning a set of “cluster-conditioned”, and thus directed, policies.

109 3.2 Skill Support and Sampling Rule

110 The MI objective (1) crucially depends on the number of skills ($|Z|$) and the distribution $\rho(z)$.
 111 Unfortunately, it is been shown [e.g., 8] that solving (1) is particularly challenging. In order to
 112 simplify the optimization and the associated learning problem, we modify (1) in two ways.

113 First, coherently with the skill optimization detailed in Sect. 3.1, the random variable S in the
 114 conditional entropy is any state reached during the diffusing part of the skill and not just the terminal
 115 state. More formally, we denote by S_{diff} the random variable and its distribution for a specific skill z
 116 is $p_{\pi(z)}(s_{\text{diff}}) = 1/H \sum_{t=T+1}^{T+H} p_{\pi(z)}(s_t)$, i.e., the distribution over states obtained by averaging the
 117 distributions at any of the steps in the diffusing part. Similarly, $p(z|s_{\text{diff}})$ now denotes the probability
 118 of z being the skill to traverse s_{diff} during its diffusing part. As a result, training the skills to maximize
 119 MI naturally leads the diffusing parts to “push” the directed parts away so as to reach diverse regions
 120 of the environment. The combination of “global” coverage of the directed parts and “local” coverage
 121 of the diffusing part ensures that the whole environment is properly visited with $|Z| \ll S$ skills.³

122 Second, we introduce an alternative problem that simplifies the optimization while preserving the
 123 coverage and directedness properties of MI. This is achieved by introducing a stronger requirement
 124 on the discriminability. While the conditional entropy term $-\mathcal{H}(Z|S)$ in (1) promotes the discrim-
 125 inability of skills *on average*, we argue that a more suitable objective is to *constrain* each skill to
 126 achieve a *minimum* level of discriminability. First, we move from the average to the minimum over
 127 skills by lower bounding the conditional entropy as

$$-\mathcal{H}(Z|S_{\text{diff}}) = \sum_{z \in Z} \rho(z) \mathbb{E}_{s_{\text{diff}}} [\log p(z|s_{\text{diff}})] \geq \min_{z \in Z} \mathbb{E}_{s_{\text{diff}}} [\log p(z|s_{\text{diff}})], \quad (2)$$

128 which leads to the following optimization (assuming π is fixed for convenience)

$$\max_{|Z|=N, \rho} \left\{ \mathcal{H}(Z) + \min_{z \in [N]} \mathbb{E}_{s_{\text{diff}}} [\log p(z|s_{\text{diff}})] \right\}, \quad (3)$$

129 where with an abuse of notation we use $z \in [N]$ to denote all skills in a set Z with cardinality N .
 130 Since (3) is a lower bound to MI, it tends to promote the same type of covering and directed skills.
 131 Furthermore, (2) no longer depends on the distribution over skills and the entropy term $\mathcal{H}(Z)$ is
 132 maximized by setting ρ to the uniform distribution over N skills (i.e., $\max_{\rho} \mathcal{H}(Z) = \log(N)$), thus
 133 simplifying the optimization, which now only depends on N .

134 While optimizing (3) promotes a cardinality N such that all skills have good discriminability, a more
 135 convenient formulation is to explicitly set a minimum level of discriminability for all skills through
 136 the following constrained optimization problem:

$$\max_{N \geq 1} \log(N) \quad \text{s.t.} \quad \min_{z \in [N]} \mathbb{E}_{s_{\text{diff}}} [\log p(z|s_{\text{diff}})] \geq \log \eta. \quad (4)$$

137 where η is a parameter that defines the discriminability threshold. A skill z is said to be η -consolidated
 138 if it satisfies the constraint. Crucially, let $P_N := \min_{z \in [N]} \mathbb{E}_{s_{\text{diff}}} [\log p(z|s_{\text{diff}})]$, then the sequence
 139 $(P_N)_{N \geq 1}$ is non-increasing with $P_1 = 0$ (i.e., the more skills the harder it is to meet the constraint).
 140 As a result, (4) can be optimized following a simple greedy strategy incrementally adding skills until
 141 the constraint is violated. The optimal N thus defines the *effective number* of η -consolidated skills and
 142 it corresponds to the largest number of skills that is guaranteed to display sufficient discriminability.
 143 Alternatively, we can interpret (4) as finding the largest number of clusters (i.e., the region reached
 144 by the directed part of a skill and covered by its associated diffusing part) with a minimum level of
 145 inter-cluster distance. This effect is qualitatively illustrated in Fig. 1, where the states attained by the
 146 directed part of the skills attain different regions that are locally covered by their diffusing parts.

³Notice that (1) is maximized by setting $|Z| = |S|$ (since $\max_Y \mathcal{I}(X, Y) = \mathcal{I}(X, X) = \mathcal{H}(X)$), i.e., where each skill is a goal-conditioned policy reaching a different state. This implies having as many policies as states, which makes the learning particularly challenging as the complexity of the environment increases.

Algorithm 1: UPSIDE

Initialize: Discriminability threshold $\eta \in (0, 1)$, branching factor $N_0 \geq 1$, patience K
Initialize: Tree \mathcal{T} initialized as a root node indexed by 0, queue of parent nodes $\mathcal{W} = \{0\}$.
while $\mathcal{W} \neq \emptyset$ **do** // tree expansion
1 Dequeue a node/skill $w \in \mathcal{W}$ and expand \mathcal{T} at w by adding a set $\mathcal{C}(w)$ of N_0 nodes/skills
2 Create random policies $\pi_z, \forall z \in \mathcal{C}(w)$
3 Initialize discriminator q_ϕ with $|\mathcal{T}|$ classes
4 **Continue** = true; **Saturated** = false
5 **while** **Continue** **do**
6 **for** K iterations **do**
7 Sample a skill z from \mathcal{T} at random
8 Extract the sequence of nodes $z_{(1)}, \dots, z$ in \mathcal{T} leading to z
9 Execute the composed (directed part) policy $(\pi_{z_{(1)}}, \dots, \pi_z)$ followed by the diffusing part
10 Add states observed during the diffusion part to state buffer \mathcal{B}_z
11 Update discriminator q_ϕ with SGD on \mathcal{B}_z to predict label z
12 **if** $z \in \mathcal{C}(w)$ **then** // Update only new policies, other policies kept fixed
13 | Update policy π_z using SAC to optimize the discriminator reward as in Sect. 3.1.
14 Compute the skill-discriminability $d(z) = \hat{q}_\phi^{(B)}(z) = \frac{1}{|\mathcal{B}_z|} \sum_{s \in \mathcal{B}_z} q_\phi(z|s)$ for all $z \in \mathcal{C}(w)$
15 **if** $\min_{z \in \mathcal{C}(w)} d(z) < \eta$ **then** // Node removal
16 | Remove the node/skill $z = \arg \min_{z \in \mathcal{C}(w)} d(z)$ from $\mathcal{C}(w)$ and \mathcal{T}
17 | Set **Saturate** = true
18 **else if not Saturated then**
19 | Add one new node/skill to $\mathcal{C}(w)$ and \mathcal{T}
20 **else**
21 | Set **Continue** = false
22 Enqueue in \mathcal{W} the consolidated nodes $\mathcal{C}(w)$

147 3.3 Composing Skills in a Tree Structure

148 The MI optimization problem as well as our constrained variant (4) depend on the initial state s_0
149 and on the length of each skill. Although these quantities are usually predefined and only appear
150 implicitly in the equations, they have a crucial impact on the obtained behavior. In fact, resetting after
151 each skill execution unavoidably restricts the coverage to a radius of at most $T + H$ steps around s_0 .
152 This may suggest to set T and H to a large value. However, increasing the horizon makes the training
153 of the skills more challenging, as learning π would require solving a difficult RL problem itself.

154 Instead, we propose to “extend” the length of the skills through composition. Indeed, the decoupled
155 skill structure and the constraint in (4) entail that the directed part of each of the η -consolidated skills
156 reliably reach a specific (and distinct) region of the environment and it is thus re-usable and amenable
157 to composition. We propose to chain the directed part of the skills in order to reach further and further
158 parts of the state space. Specifically, we build a growing tree, where the root is the initial state s_0 , the
159 edges represent the directed part of the skills, and the nodes represent the diffusing part of skills. As
160 such, whenever a skill z is selected, the directed part of all the policies associated to its predecessor
161 skills in the tree are executed first (see Fig. 1 for an illustration of the tree structure).

162 As a result, the agent naturally builds a curriculum on the episode lengths, which grow as the sequence
163 $(iT + H)_{i \geq 1}$. As such, it does not require prior knowledge on an adequate horizon of the downstream
164 goal-based task.⁴ Here this knowledge is replaced by T and H which are more environment-agnostic
165 and task-agnostic quantities, as their choice rather has an impact on the size and shape of the learned
166 tree (e.g., the smaller T and H the bigger the tree).

167 3.4 The UPSIDE Algorithm

168 We are now ready to introduce UPSIDE, which provides a specific implementation of the components
169 described before (see Fig. 1 for a qualitative illustration and Algorithm 1 for the detailed pseudo-code).

170 We perform standard approximations to make the constraint in (4) easier to estimate. We approximate
171 the unknown posterior $p(z|s)$ with a learned discriminator $q_\phi(z|s)$ with parameters ϕ . We also

⁴See e.g., the discussion in [26] on the “importance of properly choosing the training horizon in accordance with the downstream-task horizon the policy will eventually face.”

172 remove the logarithm from the constraint to have an estimation range of $[0, 1]$ and thus lower
 173 variance². Finally, we replace the expectation over s with an empirical estimate $\widehat{q}_\phi^{(B)}(z)$ averaging the
 174 value of the discriminator evaluated on the last B states observed while executing the diffusing part
 175 of z . Integrating these approximations in (4) leads to

$$\max_{N \geq 1, \pi} N \quad \text{s.t.} \quad \min_{z \in [N]} \widehat{q}_\phi^{(B)}(z) \geq \eta. \quad (5)$$

176 As discussed in Sect. 3.2, this problem can be conveniently optimized using a greedy strategy. We
 177 then integrate the optimization of (5) into an adaptive tree expansion strategy: **(Generating new**
 178 **skills)** Given a tree structure as described in Sect. 3.3, we expand the tree at a leaf w by adding N_0
 179 new nodes/skills following a breadth-first-search approach (lines 1, 2). Then **(Skill Learning)** the
 180 new skills are optimized by: **i)** sampling random skills in the tree to update the discriminator (lines
 181 7-11), and **ii)** by updating the policies to optimize the discriminability reward (Sect. 3.1) computed
 182 using the discriminator (lines 13). To speed-up convergence, we only update the policies that have be
 183 added to the tree structure, keeping all the previous policies fixed (line 12). Note that in the update of
 184 the discriminator we leverage the states observed in previous phases of the algorithm by maintaining
 185 a (small) replay buffer of states for each skill. **(Node Consolidation)** After a *patience* period (line 6),
 186 if all skills are η -consolidated, we tentatively add more skills to the leaf w (line 18). On the other
 187 hand, if any skill does not meet the discriminability threshold, we remove it and consolidate the
 188 remaining skills into the tree (lines 16, 17) and we repeat the process.

189 **Model selection.** A core aspect of any RL algorithm is *model selection*, i.e., finding the best
 190 configuration of hyperparameters. In URL with no prior knowledge of the downstream task(s), it
 191 is non-trivial to devise an adequate criterion for model selection and this aspect is rarely addressed,
 192 despite being crucial in practice. For instance, while the coverage of the state space may be a
 193 good proxy for the performance of a URL algorithm [see e.g., 8], it may be difficult to measure in
 194 continuous problems. Interestingly, our optimization problem directly provides a single, task-agnostic
 195 and environment-agnostic criterion for model selection, which is the number N of η -consolidated
 196 skills discovered by the agent. Indeed in all of our experiments we simply select the model (i.e., set
 197 of hyperparameters) that maximizes N . This is a significant advantage w.r.t. existing methods, such
 198 as VIC and DIAYN, for which no principled approach to model selection is provided.

199 4 Related work

200 Unsupervised Reinforcement Learning methods can be broadly decomposed according to the way
 201 they summarize the experience accumulated during the unsupervised phase into reusable knowledge
 202 to solve downstream tasks. This includes both off-policy model-free [e.g., 27] and model-based
 203 [e.g., 29] methods that seek to populate a representative replay buffer and build accurate value or
 204 model estimates, that are used to solve a given downstream task in a zero- or few-shot manner.
 205 The accumulated experience during train time can also be compressed into a low-dimensional
 206 representation for value functions as well as policies and to improve exploration [e.g., 36]. An
 207 alternative line of work focuses on the discovery of a set of skills in an unsupervised manner. Our
 208 approach falls in this category, on which we now focus our related work review.

209 Skill discovery based on MI maximization was first proposed in VIC [11], where only the final
 210 states of each trajectory are considered in the reverse form of (1) and where both the skills and
 211 their sampling rules are simultaneously learned (with a fixed support $|Z|$, i.e., a fixed number of
 212 skills). DIAYN [9] fixes the sampling rule to be uniform, and weighs the skills with an action-entropy
 213 coefficient (i.e., it additionally minimizes the MI between actions and skills given the state), so as
 214 to push the skills away from each other and enhance coverage. DADS [30] learns skills that are not
 215 only diverse but also predictable by learned dynamics models, by using a generative model over
 216 observations (rather than over skills) and optimizing a forward form of MI, namely $\mathcal{I}(s'; z|s)$ between
 217 the next state s' and current skill z (with continuous latent) conditioned on the current state s . EDL [8]
 218 shows that existing skill discovery approaches can provide insufficient coverage, and instead proposes
 219 to rely on a fixed distribution over states $p(s)$ which is either provided by an oracle or learned. In
 220 SMM [19], the MI formalism is used to learn a policy for which the state marginal distribution matches
 221 a given target state distribution (e.g., uniform), which can be seen as a more scalable way of tackling
 222 the problem of maximum entropy over the state space [15], and as a way to encourage skills to go
 223 through unknown state regions. Other MI-based skill discovery methods include [10, 14, 24, 5, 34],
 224 as well as [35, 20] which investigate skill discovery in non-episodic settings.

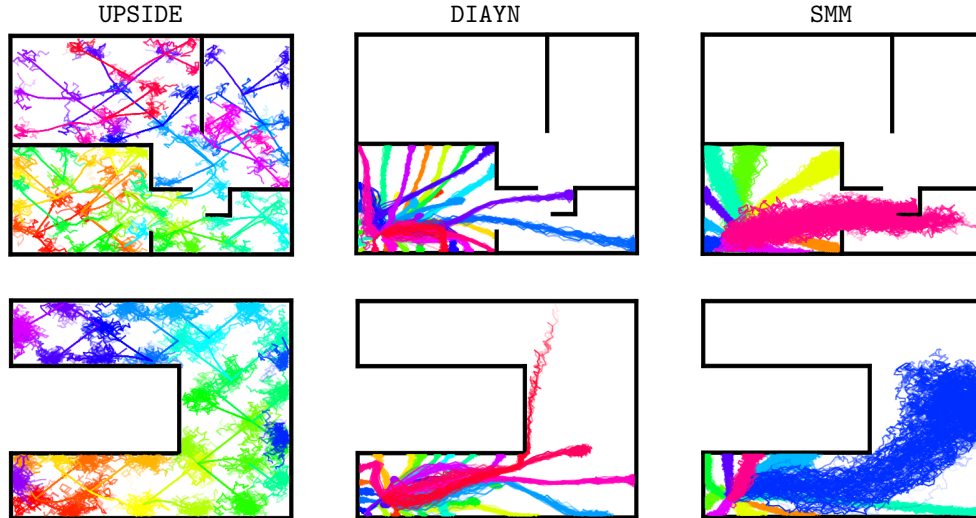


Figure 3: UPSIDE, DIAYN-curriculum and SMM-10 skills learned in a bottleneck maze (*Top*) and a U-maze (*Bottom*). For both DIAYN and SMM we report the stochastic execution of the learned skills and for UPSIDE we report the deterministic directed parts (that are composed) followed by the (stochastic) diffusing part, which is the same protocol used to evaluate coverage.

225 Our approach shares a similar motivation to prior MI-based works of targeting skills that are both
 226 directed and state-covering. In particular, the decoupled structure introduced in Sect. 3.1 can be seen
 227 as a more suitable way to achieve the objective of improving the coverage of VIC as done in DIAYN
 228 and SMM, without compromising the directedness of the skills.

229 While most skill discovery approaches consider a fixed number of skills, a curriculum with increasing
 230 number of skills is studied in [1, 3]. Our discriminability constraint is what enables skills to be
 231 composed along a tree structure, which allows increases or decreases the support of available skills
 232 depending on the region of the state space.

233 Recently, [37] proposed a hierarchical RL method that discovers abstract and task-agnostic skills
 234 while jointly learning a higher-level policy which is trained to maximize environment reward. Our
 235 approach builds on a similar promise of composing skills instead of resetting to s_0 after each execution,
 236 yet we articulate the composition differently, by exploiting the direct-then-diffuse structure to ground
 237 learned skills to the state space instead of being abstract.

238 In addition, approaches such as DISCERN [33] and Skew-Fit [27] learn a goal-conditioned policy in
 239 an unsupervised way with an MI objective. As explained in [8, Sect. 5], this can be interpreted as a
 240 skill discovery approach with latent $Z = S$, i.e., where each goal state can define a different skill.
 241 Conditioning on either goal states or abstract latent skills forms two extremes of the spectrum of
 242 unsupervised RL. We target an intermediate approach, seeking to benefit from the groundedness of
 243 the latent skill Z and the states S (and thus amenability to composition) of goal-conditioned RL, and
 244 from the reduced search space and sampling ease of skill-based RL.

245 An alternative approach to skill discovery builds on “spectral” properties of the dynamics of the
 246 environment. This includes eigenoptions [21, 22] and covering options [17, 18], as well as the
 247 algorithm of [4] that builds a discrete graph representation which learns and composes spectral skills.

248 5 Experiments

249 In this section, we investigate the following questions: **i)** Can the adaptive tree structure of UPSIDE in-
 250 crementally cover an unknown environment while preserving directedness of the skills? **ii)** Following
 251 the unsupervised phase, how can UPSIDE be leveraged to solve goal-based downstream tasks?

252 We report results on: **a)** Navigation problems in continuous mazes, where actions represent the desired
 253 shift in x and y coordinates; **b)** A difficult instance of CartPole, where the cart starts with zero speed
 254 and the pole is oriented downside; **c)** The Reacher [32] problem using the MuJoCo implementation
 255 in Gym [7]. In all environments, the per-dimension action space is in $[-1; +1]$.

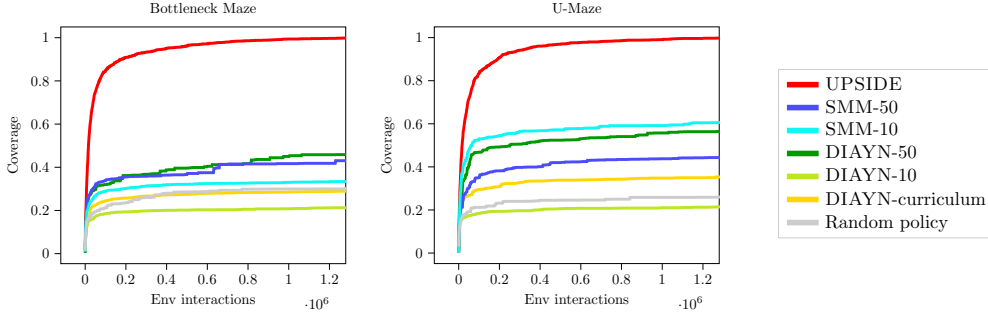


Figure 4: Normalized coverage in U-maze and bottleneck.

256 We compare to different baselines. DIAYN- K , where K is a fixed number of skills, is the original
 257 algorithm proposed in [9]. DIAYN-Curriculum is a variant where the number of skills is automatically
 258 tuned following the same procedure as in UPSIDE ensuring a good discriminability. We also compare
 259 to SMM [19], which is similar to DIAYN, but it includes an exploration bonus encouraging the policies
 260 to visit rarely encountered states. In our implementation, the exploration bonus is obtained by
 261 maintaining a multinomial distribution over “buckets of states” obtained by discretization, resulting
 262 in an computation-efficient and stable implementation that is more stable than the original VAE-based
 263 method. UPSIDE and all baselines are implemented with Soft-Actor Critic (SAC) [13].

264 **Unsupervised Phase.** We run all methods until convergence. We then do model selection according
 265 to the criterion of either the final number of skills for UPSIDE and DIAYN-curriculum and the final
 266 average discriminability for DIAYN- K and SMM. To compute the coverage, we perform rollouts by
 267 first sampling a skill uniformly at random and executing its associated policy until termination. We
 268 discretize states into buckets (50 interval per dimension for mazes and 10 for control environments)
 269 and report the proportion of buckets reached by each method as a function of the total number of
 270 steps executed in the environment over multiple rollouts. Since only a small portion of the discretized
 271 states can be reached, we normalize the coverage such that the best method obtains 1.

272 We consider two topologies of mazes with size (height and width) 50 such that exploration is non-
 273 trivial (i.e., a random policy is only able to cover a small part of the state space): a U-shaped maze
 274 and a Bottleneck maze (which is a harder version of the one in [8, Fig. 1] which is only of size 10
 275 for the same action space). In Fig. 3 we show that UPSIDE succeeds in covering the near-entirety
 276 of the state space by creating a tree of directed skills. Moreover, UPSIDE created directed skills
 277 with a low entropy, while the two baselines tend to create skills that are more stochastic. This is
 278 particularly evident for SMM, due to the state-entropy exploration bonus, that while it encourages
 279 broader coverage makes skills less directed.

280 In Fig. 4 we report the coverage on the Bottleneck maze and U-Maze. For UPSIDE, executing a
 281 skill corresponds to executing the directed part of all the “parent” skills in the tree and concluding
 282 with the diffusion part of the skill. SMM achieves better coverage than DIAYN thanks to the increased
 283 level of stochasticity (diffusion) of its skills. UPSIDE outperforms both by reaching regions of the
 284 environment that are not be achieved by other methods. Here, we plot UPSIDE with $T = 10$ and
 285 $H = 10$, but we found UPSIDE to be robust to these parameters as shown in the supplementary.

286 Results are similar in the CartPole problem (see Fig. 5) where UPSIDE (with $T = 20$ and $H = 20$)
 287 obtains better coverage than baselines. On the other hand, in Reacher (see Fig. 5), DIAYN-50
 288 outperforms UPSIDE in terms of coverage. This can be explained by the fact that, in this environment,
 289 highly stochastic skills provide a good coverage. Nonetheless, this comes at the cost of very low
 290 discriminability (rightmost plot), which suggests DIAYN-50 skills have poor directedness. On the
 291 other hand, UPSIDE (and DIAYN-curriculum) achieves much larger discriminability by removing
 292 redundant skills and favoring more directed policies.

293 **Downstream Tasks.** Following the unsupervised phase, UPSIDE has learned a tree of skills. We
 294 now investigate how these skills are used to tackle a downstream task. In that setting, we propose to
 295 use skill-based approaches (i.e UPSIDE, DIAYN and SMM) in the following way: a) (exploration) first
 296 we sample rollouts over the different skills. b) We then select the best skill based on the maximum
 297 cumulative reward collected and c) we fine-tune this skill to maximize the reward. We report results
 298 on mazes (additional results are provided in the supplementary). We consider a sparse positive reward

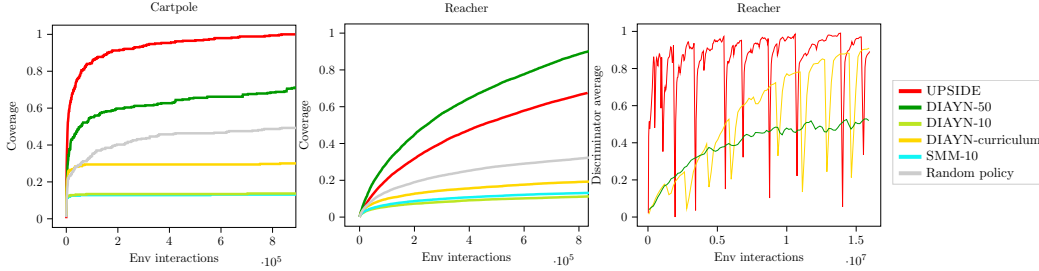
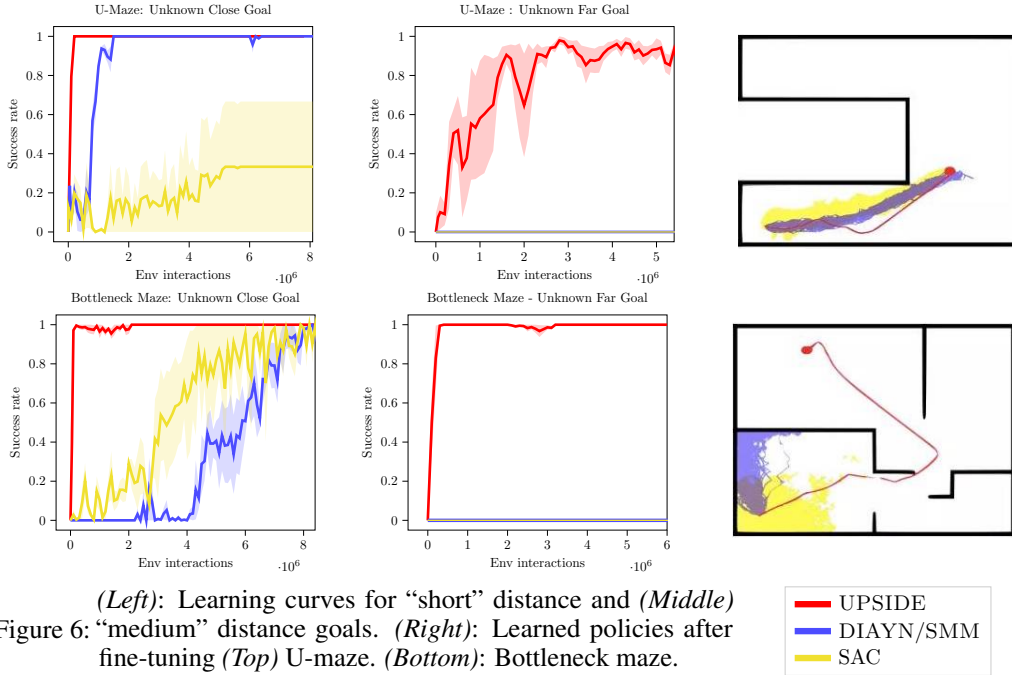


Figure 5: Normalized coverage in Cartpole (*Left*) and Reacher (*Middle*). (*Right*) Average discriminability of the skills during training in Reacher.

299 when reaching a particular defined goal.⁵ We consider goals at different distances from the initial
 300 state s_0 , the further, the harder. Fig. 6 shows the learning curves obtained when fine-tuning the best
 301 skill for the different models and compare to a classical SAC algorithm where a single policy is
 302 learned from scratch. DIAYN/SMM means we use the best state-covering policies between DIAYN and
 303 SMM. For the “close” goal setting, both UPSIDE and DIAYN/SMM are able to learn to reach this goal
 304 efficiently while SAC solves the task only for some of the training runs. Note that we do not show
 305 DIAYN performance since it is lower than the SMM one. For the “far” goal setting, only UPSIDE learns
 306 to reach this goal. Obtained trajectories are illustrated in Fig. 6.



(*Left*): Learning curves for “short” distance and (*Middle*) “medium” distance goals. (*Right*): Learned policies after fine-tuning (*Top*) U-maze. (*Bottom*): Bottleneck maze.

307 6 Conclusion

308 We introduced UPSIDE, a novel algorithm for unsupervised skill discovery designed to trade off
 309 between coverage and directedness and develop a tree of skills that can be used to both perform
 310 efficient exploration of the environment and learn effective goal-directed policies. Natural venues for
 311 future investigation are: **1)** The diffusing part of each skill could be explicitly trained to maximize
 312 local coverage; **2)** UPSIDE assumes a good representation of the state is provided as input, it would
 313 be interesting to pair UPSIDE with effective representation learning techniques to tackle problems
 314 with high-dimensional input (e.g., image-based RL); **3)** While UPSIDE is grounded on the solid
 315 principle of MI maximization, a more thorough theoretical investigation is needed to explicitly link
 316 the optimization problem and its approximations to the downstream performance.

⁵Notice that if the goal was known, the learned discriminator could be directly used to identify the most promising skill to fine-tune.

317 **References**

- 318 [1] J. Achiam, H. Edwards, D. Amodei, and P. Abbeel. Variational option discovery algorithms.
319 *arXiv preprint arXiv:1807.10299*, 2018.
- 320 [2] M. Andrychowicz, D. Crow, A. Ray, J. Schneider, R. Fong, P. Welinder, B. McGrew, J. Tobin,
321 P. Abbeel, and W. Zaremba. Hindsight experience replay. In *NIPS*, 2017.
- 322 [3] A. Aubret, L. Matignon, and S. Hassas. Elsim: End-to-end learning of reusable skills through
323 intrinsic motivation. *arXiv preprint arXiv:2006.12903*, 2020.
- 324 [4] A. Bagaria, J. Crowley, J. W. N. Lim, and G. Konidaris. Skill discovery for exploration and
325 planning using deep skill graphs. 2021.
- 326 [5] K. Baumli, D. Warde-Farley, S. Hansen, and V. Mnih. Relative variational intrinsic control.
327 *arXiv preprint arXiv:2012.07827*, 2020.
- 328 [6] M. G. Bellemare, Y. Naddaf, J. Veness, and M. Bowling. The arcade learning environment: An
329 evaluation platform for general agents. *Journal of Artificial Intelligence Research*, 47:253–279,
330 2013.
- 331 [7] G. Brockman, V. Cheung, L. Pettersson, J. Schneider, J. Schulman, J. Tang, and W. Zaremba.
332 Openai gym, 2016.
- 333 [8] V. Campos, A. Trott, C. Xiong, R. Socher, X. Giro-i Nieto, and J. Torres. Explore, discover and
334 learn: Unsupervised discovery of state-covering skills. In *International Conference on Machine*
335 *Learning*, 2020.
- 336 [9] B. Eysenbach, A. Gupta, J. Ibarz, and S. Levine. Diversity is all you need: Learning skills
337 without a reward function. In *International Conference on Learning Representations*, 2019.
- 338 [10] C. Florensa, Y. Duan, and P. Abbeel. Stochastic neural networks for hierarchical reinforcement
339 learning. *arXiv preprint arXiv:1704.03012*, 2017.
- 340 [11] K. Gregor, D. J. Rezende, and D. Wierstra. Variational intrinsic control. *arXiv preprint*
341 *arXiv:1611.07507*, 2016.
- 342 [12] S. Gu, E. Holly, T. Lillicrap, and S. Levine. Deep reinforcement learning for robotic manipula-
343 tion with asynchronous off-policy updates. In *2017 IEEE international conference on robotics*
344 *and automation (ICRA)*, pages 3389–3396. IEEE, 2017.
- 345 [13] T. Haarnoja, A. Zhou, P. Abbeel, and S. Levine. Soft actor-critic: Off-policy maximum entropy
346 deep reinforcement learning with a stochastic actor. *CoRR*, abs/1801.01290, 2018.
- 347 [14] S. Hansen, W. Dabney, A. Barreto, D. Warde-Farley, T. Van de Wiele, and V. Mnih. Fast task
348 inference with variational intrinsic successor features. In *International Conference on Learning*
349 *Representations*, 2019.
- 350 [15] E. Hazan, S. Kakade, K. Singh, and A. Van Soest. Provably efficient maximum entropy
351 exploration. In *International Conference on Machine Learning*, pages 2681–2691, 2019.
- 352 [16] R. Houthoofd, X. Chen, Y. Duan, J. Schulman, F. De Turck, and P. Abbeel. Vime: variational
353 information maximizing exploration. In *Proceedings of the 30th International Conference on*
354 *Neural Information Processing Systems*, pages 1117–1125, 2016.
- 355 [17] Y. Jinnai, J. W. Park, D. Abel, and G. Konidaris. Discovering options for exploration by
356 minimizing cover time. In *International Conference on Machine Learning*, pages 3130–3139.
357 PMLR, 2019.
- 358 [18] Y. Jinnai, J. W. Park, M. C. Machado, and G. Konidaris. Exploration in reinforcement learning
359 with deep covering options. In *International Conference on Learning Representations*, 2020.
- 360 [19] L. Lee, B. Eysenbach, E. Parisotto, E. Xing, S. Levine, and R. Salakhutdinov. Efficient
361 exploration via state marginal matching. *arXiv preprint arXiv:1906.05274*, 2019.

- 362 [20] K. Lu, A. Grover, P. Abbeel, and I. Mordatch. Reset-free lifelong learning with skill-space
363 planning. *arXiv preprint arXiv:2012.03548*, 2020.
- 364 [21] M. C. Machado, M. G. Bellemare, and M. Bowling. A laplacian framework for option discovery
365 in reinforcement learning. In *International Conference on Machine Learning*, pages 2295–2304.
366 PMLR, 2017.
- 367 [22] M. C. Machado, C. Rosenbaum, X. Guo, M. Liu, G. Tesauro, and M. Campbell. Eigenoption
368 discovery through the deep successor representation. In *International Conference on Learning
369 Representations*, 2018.
- 370 [23] V. Mnih, K. Kavukcuoglu, D. Silver, A. A. Rusu, J. Veness, M. G. Bellemare, A. Graves,
371 M. Riedmiller, A. K. Fidjeland, G. Ostrovski, et al. Human-level control through deep rein-
372 forcement learning. *nature*, 518(7540):529–533, 2015.
- 373 [24] N. Modhe, P. Chattopadhyay, M. Sharma, A. Das, D. Parikh, D. Batra, and R. Vedantam.
374 Ir-vic: Unsupervised discovery of sub-goals for transfer in rl. In *Proceedings of the Twenty-
375 Ninth International Joint Conference on Artificial Intelligence, IJCAI-20*. International Joint
376 Conferences on Artificial Intelligence Organization, 2020.
- 377 [25] S. Mohamed and D. J. Rezende. Variational information maximisation for intrinsically motivated
378 reinforcement learning. In *Advances in neural information processing systems*, pages 2125–
379 2133, 2015.
- 380 [26] M. Mutti, L. Pratissoli, and M. Restelli. A policy gradient method for task-agnostic exploration.
381 *arXiv preprint arXiv:2007.04640*, 2020.
- 382 [27] V. H. Pong, M. Dalal, S. Lin, A. Nair, S. Bahl, and S. Levine. Skew-fit: State-covering
383 self-supervised reinforcement learning. In *International Conference on Machine Learning*,
384 2020.
- 385 [28] J. Schulman, F. Wolski, P. Dhariwal, A. Radford, and O. Klimov. Proximal policy optimization
386 algorithms. *arXiv preprint arXiv:1707.06347*, 2017.
- 387 [29] R. Sekar, O. Rybkin, K. Daniilidis, P. Abbeel, D. Hafner, and D. Pathak. Planning to explore
388 via self-supervised world models. In *International Conference on Machine Learning*, pages
389 8583–8592. PMLR, 2020.
- 390 [30] A. Sharma, S. Gu, S. Levine, V. Kumar, and K. Hausman. Dynamics-aware unsupervised
391 discovery of skills. In *International Conference on Learning Representations*, 2020.
- 392 [31] D. Silver, J. Schrittwieser, K. Simonyan, I. Antonoglou, A. Huang, A. Guez, T. Hubert, L. Baker,
393 M. Lai, A. Bolton, et al. Mastering the game of go without human knowledge. *nature*,
394 550(7676):354–359, 2017.
- 395 [32] E. Todorov, T. Erez, and Y. Tassa. Mujoco: A physics engine for model-based control. In *2012
396 IEEE/RSJ International Conference on Intelligent Robots and Systems*, pages 50pou26–5033,
397 2012.
- 398 [33] D. Warde-Farley, T. Van de Wiele, T. Kulkarni, C. Ionescu, S. Hansen, and V. Mnih. Unsuper-
399 vised control through non-parametric discriminative rewards. In *International Conference on
400 Learning Representations*, 2019.
- 401 [34] K. Xie, H. Bharadhwaj, D. Hafner, A. Garg, and F. Shkurti. Skill transfer via partially amortized
402 hierarchical planning. In *International Conference on Learning Representations*, 2021.
- 403 [35] K. Xu, S. Verma, C. Finn, and S. Levine. Continual learning of control primitives: Skill
404 discovery via reset-games. *arXiv preprint arXiv:2011.05286*, 2020.
- 405 [36] D. Yarats, R. Fergus, A. Lazaric, and L. Pinto. Reinforcement learning with prototypical
406 representations. *arXiv preprint arXiv:2102.11271*, 2021.
- 407 [37] J. Zhang, H. Yu, and W. Xu. Hierarchical reinforcement learning by discovering intrinsic
408 options. In *International Conference on Learning Representations*, 2021.

409 **Checklist**

- 410 1. For all authors...
- 411 (a) Do the main claims made in the abstract and introduction accurately reflect the paper's
412 contributions and scope? [Yes]
- 413 (b) Did you describe the limitations of your work? [Yes] We discuss the limitations and
414 directions of further investigation in the conclusion.
- 415 (c) Did you discuss any potential negative societal impacts of your work? [N/A] We do
416 not foresee any obvious negative societal impacts from our work, which focuses on the
417 fundamentals of reinforcement learning and proposes a new algorithm for unsupervised
418 skill discovery.
- 419 (d) Have you read the ethics review guidelines and ensured that your paper conforms to
420 them? [Yes]
- 421 2. If you are including theoretical results...
- 422 (a) Did you state the full set of assumptions of all theoretical results? [N/A]
- 423 (b) Did you include complete proofs of all theoretical results? [N/A]
- 424 3. If you ran experiments...
- 425 (a) Did you include the code, data, and instructions needed to reproduce the main exper-
426 imental results (either in the supplemental material or as a URL)? [No] We plan to
427 release our code upon acceptance of this work.
- 428 (b) Did you specify all the training details (e.g., data splits, hyperparameters, how they
429 were chosen)? [Yes] See Appendix.
- 430 (c) Did you report error bars (e.g., with respect to the random seed after running experi-
431 ments multiple times)? [Yes] Yes when possible.
- 432 (d) Did you include the total amount of compute and the type of resources used (e.g., type
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- 434 4. If you are using existing assets (e.g., code, data, models) or curating/releasing new assets...
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440 using/curating? [N/A]
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442 information or offensive content? [N/A]
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- 444 (a) Did you include the full text of instructions given to participants and screenshots, if
445 applicable? [N/A]
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447 Board (IRB) approvals, if applicable? [N/A]
- 448 (c) Did you include the estimated hourly wage paid to participants and the total amount
449 spent on participant compensation? [N/A]

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