# Designing Draft Models for Speculative Decoding

### Anonymous ACL submission

#### Abstract

 Speculative Decoding is a widely used tech- nique to speed up inference for Large Lan- guage Models (LLMs) without sacrificing qual- ity. When performing inference, speculative decoding uses a smaller *draft* model to gener- ate speculative tokens and then uses the *target* LLM to verify those draft tokens. The speedup provided by speculative decoding heavily de- pends on the choice of the draft model. In this work, we perform a detailed study comprising over 350 experiments with LLAMA-65B and OPT-66B using speculative decoding and de- lineate the factors that affect the performance gain provided by speculative decoding. Our ex-**periments indicate that the performance of spec-** ulative decoding depends heavily on the latency of the draft model, and the draft model's capa- bility in language modeling does not correlate 019 strongly with its performance in speculative de- coding. Based on these insights we explore a new design space for draft models and design hardware-efficient draft models for speculative decoding. Our newly designed draft model for LLAMA-65B can provide 60% higher through- put than existing draft models and can general- ize further to the LLAMA-2 model family and supervised fine-tuned models.

## **028 1 Introduction**

 In recent years, Large Language Models (LLMs) have emerged as a cornerstone of modern compu- tational linguistics, offering unprecedented capa- bilities in generating and interpreting human lan- guage. As the demand for faster and more effi- cient language processing grows, understanding and optimizing the inference throughput of these models becomes increasingly crucial. Decoder- only LLMs [\(Brown et al.,](#page-8-0) [2020;](#page-8-0) [Touvron et al.,](#page-9-0) [2023a,](#page-9-0)[b\)](#page-9-1) use auto-regressive decoding to perform inference. Auto-regressive decoding is known to be hardware inefficient [\(Miao et al.,](#page-8-1) [2023;](#page-8-1) [Liu et al.,](#page-8-2)

[2023a\)](#page-8-2), leading to poor resource utilization and low **041** throughput during inference. **042**

Several methods [\(Yu et al.,](#page-9-2) [2022;](#page-9-2) [Wang et al.,](#page-9-3) 043 [2020;](#page-9-3) [Kwon et al.,](#page-8-3) [2023;](#page-8-3) [Dao et al.,](#page-8-4) [2023;](#page-8-4) [Hong](#page-8-5) **044** [et al.,](#page-8-5) [2023\)](#page-8-5) have been studied to optimize the serv- **045** ing of LLMs. One promising approach to improve **046** the throughput for serving LLMs without accuracy **047** [l](#page-9-5)oss is speculative decoding [\(Stern et al.,](#page-9-4) [2018;](#page-9-4) [Xia](#page-9-5) **048** [et al.,](#page-9-5) [2023a;](#page-9-5) [Leviathan et al.,](#page-8-6) [2023\)](#page-8-6). When us- **049** ing speculative decoding to serve an LLM (usually **050** 100s of billion parameters), a draft model (a signifi- **051** cantly smaller LLM) is used to generate speculative **052** tokens. The target LLM model then verifies the out- **053** put of the draft model and only outputs tokens that **054** match its output. In the case of speculative decod- **055** ing, the target LLM for inference acts as a *verifier* **056** for the draft model. By leveraging faster inference **057** of smaller draft models, speculative decoding turns **058** autoregressive decoding on the target LLM into a **059** more hardware-friendly batched operation (similar **060** to "prefill"), thereby increasing throughput while **061** preserving accuracy. 062

Given the promised benefits of speculative de- 063 coding, this paper first focuses on understanding **064** the key factors that dictate the throughput improve- **065** ments that can be obtained. We perform a com- **066** prehensive benchmarking study and profile spec- **067** ulative decoding to characterize bottlenecks. We **068** perform over 350 experiments, using LLMs like **069** LLAMA-65B, OPT-66B, and fine-tuned chat mod- **070** els such as Vicuna-33B [\(Chiang et al.,](#page-8-7) [2023\)](#page-8-7) as **071** target models and LLAMA and OPT families as **072** draft models, ranging from  $\approx$  5 $\times$  to 528 $\times$  fewer 073 parameters than the target models. Our findings **074** show that the key bottleneck in speculative decod- **075** ing is the draft model's latency, highlighting the **076** need to optimize draft model designs. **077**

Next, we find that existing draft models, which **078** are typically designed only for improving accuracy **079** in a given parameter budget, are sub-optimal for **080** maximizing the throughput with speculative decod- **081**

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Figure 1: This figure shows the speculative decoding process. In vanilla LLM inference, after the prompt is processed into KV caches (Prefill phase), LLM generates the output token by token in an autoregressive manner (Autoregressive generation phase). In speculative decoding, a draft model is first used to generate  $n$  candidate tokens at each step (Draft token generation phase). The LLM verifies the candidate tokens and accepts  $k (k \le n)$ tokens (LLM verification phase). Since LLM knows all n candidate tokens in advance, this step is identical to a prefill step of length n. In both cases, this process is repeated until either an end-of-sequence (EOS) token is generated or the maximum generation limit has been reached.

 ing. From our experiments, we first observe that the draft model latency is bottlenecked by model depth, and higher model depth leads to increased latency (Section [3.2\)](#page-4-0). Second, we also find that draft model accuracy on language modeling tasks does not correlate strongly with its performance in speculative decoding (Section [3.3\)](#page-4-1), *i.e.*, a draft model with higher accuracy on language modeling task can have similar TAR to a model with lower accuracy. Based on these two insights, we propose designing new draft models that trade increased depth for width (thus retaining the same parame- ter count) and show that our new draft models can boost inference throughput using speculative de- coding by over 60%. Finally, we show how pruning methods like Sheared-LLAMA [\(Xia et al.,](#page-9-6) [2023b\)](#page-9-6) can generate smaller draft models with favorable configurations.

### **100** Our Contributions:

 • To the best of our knowledge, we are the first work to conduct comprehensive experiments on serving the open source LLAMA-65B and OPT-66B models utilizing speculative decod- ing, conducting more than 352 experiments to elucidate the factors one needs to consider while selecting and designing a draft model.

 • We show the need for a systematic redesign of draft models used for speculative decod- ing. We demonstrate that using accuracy on language modeling tasks to choose the draft model for speculative decoding can lead to suboptimal choices, and our experiments highlight that redesigning draft models can improve the throughput of speculative de- coding by up to 60%. Based on these in- sights, our pruned LLAMA-796M provides up to 60% higher throughput than ShearedLLAMA-1.3B while using only 0.8% of to- **119** kens (0.42B vs 50.42B) used to train Sheared- **120** LLAMA-1.3B. We also show that LLAMA- **121** 796M works well for other LLMs, such as **122** LLAMA-2 families of models and supervised **123** fine-tuned models (Vicuna-33B). **124**

• Finally, we also study how improvements in **125** models and hardware can further impact draft **126** model design for future generations of LLMs. **127** (Section [5.1\)](#page-6-0). **128**

# 2 Background and Related Work **<sup>129</sup>**

First, we provide a high-level overview of LLM **130** inference and the use of speculative decoding. **131**

### 2.1 Background **132**

A decoder-only LLM performs inference in two **133** phases: a prefill phase and an autoregressive- **134** decoding phase. In the prefill phase, the LLM is **135** initialized with a context or prompt, formulated as **136**  $C = \{c_1, c_2, ..., c_n\}$ , where C represents the input 137 context and *n* the length of the prefill. In the prefill 138 phase, the model processes the whole input context **139** in parallel and performs next-word prediction. Dur- **140** ing the autoregressive-decoding phase, the model **141** generates new text sequentially, one token at a time, **142** building upon the context provided in the prefill **143** phase. Due to its sequential nature, the autoregres- **144** sive decoding phase is widely known to be mem- **145** [o](#page-8-6)ry bandwidth bound on modern GPUs [\(Leviathan](#page-8-6) **146** [et al.,](#page-8-6) [2023\)](#page-8-6). **147**

To improve hardware utilization and throughput, **148** [Schuster et al.](#page-9-7) [\(2022\)](#page-9-7); [Chen et al.](#page-8-8) [\(2023\)](#page-8-8) proposed **149** *speculative decoding*, where a significantly smaller **150** *draft* model generates multiple tokens, and the *tar-* **151** *get* LLM performs verification on the generated **152** tokens in parallel. The verification is akin to *pre-* **153** *fill* stage in LLM inference. As long as more than 154

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(a) OPT Series on MMLU

(b) OPT Series on Hellaswag

Figure 2: This figure shows the throughput of different draft models from the OPT series. As model size increases, throughput decreases due to higher inference latency despite consistent increases in TAR.

 one token is accepted on average, speculative de- coding can potentially provide speedups. Figure [1](#page-1-0) shows how inference using speculative decoding differs from auto-regressive decoding. It is widely reported [\(Miao et al.,](#page-8-1) [2023;](#page-8-1) [Liu et al.,](#page-8-2) [2023a\)](#page-8-2) that the number of tokens accepted by the target model influences the speedup provided by speculative de-**162** coding.

 In this work, we conduct a comprehensive em- pirical study to identify the performance bottleneck of speculative decoding and identify strategies to design the best draft model for a given LLM.

### **167** 2.2 Related Work

 LLM Inference There has been significant amount of work on improving LLM serving includ- [i](#page-9-3)ng work in Orca [\(Yu et al.,](#page-9-2) [2022\)](#page-9-2), LightSeq [\(Wang](#page-9-3) [et al.,](#page-9-3) [2020\)](#page-9-3), DeepSpeed Inference [\(Aminabadi](#page-8-9) [et al.,](#page-8-9) [2022\)](#page-8-9), PagedAttention [\(Kwon et al.,](#page-8-3) [2023\)](#page-8-3), FlashDecoding [\(Dao et al.,](#page-8-4) [2023\)](#page-8-4) and FlashDecod- ing++ [\(Hong et al.,](#page-8-5) [2023\)](#page-8-5). These works seek to improve LLM inference by better utilization of hardware. There are lines of work that have looked at pruning LLMs based on input context to speed up inference [\(Liu et al.,](#page-8-10) [2023b\)](#page-8-10) or using shallower and wider neural networks for machine transla- tion [\(Kasai et al.,](#page-8-11) [2020\)](#page-8-11). However, in this work, we focus on speculative decoding [\(Leviathan et al.,](#page-8-6) [2023;](#page-8-6) [Chen et al.,](#page-8-8) [2023;](#page-8-8) [Santilli et al.,](#page-8-12) [2023\)](#page-8-12), which has been inspired by speculative execution in hard-ware [\(Hennessy and Patterson,](#page-8-13) [2011\)](#page-8-13).

 Speculative Decoding Several prior works have [s](#page-8-2)tudied ways to improve speculative decoding. [Liu](#page-8-2) [et al.](#page-8-2) [\(2023a\)](#page-8-2) seeks to continuously train the draft model on the output of the target model to improve the token acceptance rate. However, training on the same hardware during inference can be challenging, depending on the inference request rate and **191** hardware utilization. Predictive Pipeline Decod- **192** ing (PPD) [\(Yang et al.,](#page-9-8) [2023\)](#page-9-8) was one of the first **193** [m](#page-9-7)ethods to introduce the use of early exit [\(Schuster](#page-9-7) **194** [et al.,](#page-9-7) [2022\)](#page-9-7) from the target model to obtain draft **195** tokens. Similar to PPD, Draft&Verify [\(Zhang et al.,](#page-9-9) **196** [2023\)](#page-9-9) seeks to combine the use of early exit with **197** [s](#page-9-7)peculative decoding, where the early exit [\(Schus-](#page-9-7) **198** [ter et al.,](#page-9-7) [2022;](#page-9-7) [Bae et al.,](#page-8-14) [2023\)](#page-8-14) from the target **199** model acts as a draft token. A drawback of these **200** methods is that the maximum benefit in latency **201** is capped. For example, in speculative decoding, **202** we can use draft models that are orders of magni- **203** tude (e.g.,  $\approx 100x-1000x$ ) smaller than the target 204 model, while early exit methods usually exit af- **205** ter performing inference over at least a fourth of **206** the model [\(Schuster et al.,](#page-9-7) [2022\)](#page-9-7), thus, limiting **207** the gain in throughput. Other lines of work, such **208** as Medusa [\(Cai et al.,](#page-8-15) [2024\)](#page-8-15), propose fine-tuning **209** multiple generation heads within the LLM that do **210** not match the LLM output distribution exactly but **211** maintain the generation quality. **212** 

In this work, we aim to understand how the **213** choice of draft model affects the throughput pro- **214** vided by speculative decoding. We use insights **215** from benchmarking to design draft models that **216** maximize speculative decoding throughput. **217**

### 3 Understanding Speculative Decoding **<sup>218</sup>**

To study the effects of the choice of the draft model, **219** we first perform a detailed study on serving OPT- **220** 65B and LLAMA-65B (two popular LLMs) using **221** speculative decoding. **222** 

Setup. We implement speculative decoding in **223** the Microsoft Deepspeed library [\(Microsoft,](#page-8-16) [2023\)](#page-8-16). **224** We use the same setup as SpecInfer [\(Miao et al.,](#page-8-1) **225** [2023\)](#page-8-1), first using the draft model to generate draft **226**

<span id="page-3-0"></span>

Figure 3: Performance Breakdown of OPT speculative decoding, lookahead length is set to be optimal for each draft model found empirically.

<span id="page-3-1"></span>

(a) In this figure, we fix model parameters to 350M and vary the number of layers and attention heads. As the number of layers decreases from 24 to 4, the number of attention heads increases from 16 to 56 (Table [6](#page-10-0) in the Appendix).



(b) In this figure, we fix layer width and increase the number of layers. The number of parameters in the model increases from 79M to 350M.



(c) In this figure, we fix model depth and increase the number of attention heads in each layer. The number of parameters in the model increases from 350M to 1B.

Figure 4: This figure shows microbenchmarks on how model depth and width affect decoding latency.

 tokens and then using the target model to verify the output of the draft model. We set the batchsize to 1 and use greedy decoding. For all our exper- iments, we use 4 Nvidia 80GB A100 GPUs. We perform our experiment on the OPT and LLAMA

base models [\(Zhang et al.,](#page-9-10) [2022;](#page-9-10) [Touvron et al.,](#page-9-0) **232** [2023a\)](#page-9-0) on MMLU [\(Hendrycks et al.,](#page-8-17) [2020\)](#page-8-17), Hel- **233** laswag [\(Zellers et al.,](#page-9-11) [2019\)](#page-9-11), and Chatbot Arena **234** datasets [\(Zheng et al.,](#page-9-12) [2023\)](#page-9-12). For MMLU, we use **235** the standard 5-shot setup. The remaining datasets **236** were evaluated in a zero-shot setting. We use OPT- **237** 66B and LLAMA-65B as the target LLM for OPT **238** and LLAMA series and use OPT-125M, OPT- **239** 350M, OPT-1.3B, OPT-2.7B, and OPT-6.7B as **240** draft models for OPT series, and LLAMA-7B, and **241** LLAMA-13B as draft models for LLAMA series. **242**

Metrics. To quantify the performance of different **243** draft models when performing inference on a target **244** model, we measure throughput (tokens generated **245** per second) and TAR (Figure [2\)](#page-2-0). We note that the **246** primary goal of speculative decoding is to improve **247** throughput. **248**

### <span id="page-3-2"></span>3.1 Bottlenecks in Speculative Decoding **249**

To understand the throughput of LLMs, we first **250** plot a latency breakdown of speculative decoding **251** in Figure [3.](#page-3-0) We show the latency breakdown be- **252** tween the draft token generation phase and the tar- **253** get model verification phase for serving OPT-66B **254** model when using various variants of OPT as the **255** draft model. A similar figure for LLAMA models **256** (Figure [9\)](#page-10-1) can be found in the Appendix. **257**

In Figure [3,](#page-3-0) the time taken by the draft model **258** for token generation increases with an increase in **259** model sizes, going from 6.23 ms for OPT-125M to **260** 18.56 ms for OPT-6.7B. However, even the small- **261** est draft model, OPT-125M, still takes significant **262** time in a speculative decoding iteration to perform **263** draft model autoregressive decoding. Though the **264** target LLM has a higher latency in each decoding **265** iteration, it only has to perform one prefill oper- **266** ation on the entire candidate token sequence. In **267** contrast, the draft model has to perform multi-step **268** autoregressive decoding sequentially, creating a **269** bottleneck. This highlights why draft model la- **270** tency is one of the key bottlenecks in speculative **271** decoding performance. We note that while Figure [3](#page-3-0) **272** uses lookahead values from 6 to 8, depending on **273** the draft model, even if we scale lookahead length **274** to hundreds of tokens, the target model verifica- **275** tion time stays constant. The draft model latency **276** remains the bottleneck due to the difference in effi- **277** ciency between prefill and auto-regressive decod- **278** ing. Next, we investigate how we can reduce draft **279** model latency.

<span id="page-4-2"></span>

(a) Model accuracy vs TAR for OPT models

(b) Model accuracy vs TAR for LLAMA models

<span id="page-4-0"></span>Figure 5: This figure shows the task accuracy versus TAR for OPT and LLAMA models on Hellaswag. The accuracy numbers are obtained from OpenLLM Leaderboard [\(HuggingFace,](#page-8-18) [2023\)](#page-8-18).

#### **281** 3.2 Understanding Draft Model Latency

 When studying the breakdown in latencies for spec- ulative decoding in the previous section, we ob- served something intriguing in Figure [3.](#page-3-0) We see that OPT-350M has a similar draft-model latency as OPT-1.3B, a model almost four times its size. This indicates that OPT-350M is inefficient, and we can design better models.

 We perform three microbenchmarks to validate our hypothesis and analyze decoding throughput: First, we fix the total model parameters at 350M and see how changing layer width and depth would affect decoding latency. Then, we fix either the layer width or depth to be the same as in OPT- 350M and modify the other to see how latency scales with wider layers or shallower models.

 Figure [4](#page-3-1) shows the results of these three bench- marks. In the first benchmark (Figure [4a\)](#page-3-1), we vary the number of attention heads, feed-forward di- mension, and layers in a model to keep the model parameters at around 350M. The detailed configu- ration for each model can be found in Table [6](#page-10-0) in the Appendix. The plot shows that the autoregres- sive decoding latency is linear in terms of layer depth despite each model having roughly the same parameter count.

 The same is true for the second benchmark (Fig- ure [4b\)](#page-3-1). The original OPT-350M model has 24 layers. As we reduce the number of layers while keeping all other configurations the same, the au- toregressive decoding latency decreases linearly. On the other hand, the third benchmark (Figure [4c\)](#page-3-1) shows that as we scale the number of attention heads up from the original OPT-350's 16 heads to 36 heads, the decoding latency stays almost con-stant even if layer width has doubled.

 These experiments indicate more latency- efficient model architectures with the same param- eter budget exist. Changing the number of layers and attention heads not only changes the throughput but also affects the quality of predictions made **321** by the model. We will next study how changes in **322** model depth and width affect model accuracy and **323** TAR and the correlation between them. **324**

# <span id="page-4-1"></span>3.3 Understanding Draft Model TAR **325**

In prior work [\(Leviathan et al.,](#page-8-6) [2023\)](#page-8-6), speculative **326** decoding throughput is modeled by  $\frac{1-\alpha^{\gamma+1}}{(1-\alpha)(\gamma c+1)}$ , 327 where  $\frac{1-\alpha^{\gamma+1}}{1-\alpha}$  $\frac{-\alpha^{7}}{1-\alpha}$  represents the improvement factor 328 (expected number of tokens matched in each itera- **329** tion) and  $\gamma c + 1$  represents the combined latency of  $\beta$ 330 draft and target models. Therefore, tokens matched **331** per iteration (also known as TAR) have a linear **332** effect on speculative decoding throughput. **333**

In this section, we perform experiments to un- **334** derstand the correlation between the accuracy of **335** a model on popular NLP tasks and its TAR. We **336** plot the accuracy of a model against the TAR it **337** achieves in Figure [5.](#page-4-2) Surprisingly, we find that **338** TAR has little correlation to the model's accuracy **339** on a task. We believe this lack of correlation is due **340** to the majority of tokens in a sentence not being **341** content words, which do not affect the accuracy of **342** the model on a specific task. **343** 

For example, if a user asks a model: *What is* **344** *the capital of Uruguay?* An LLM may correctly **345** answer: *The capital of Uruguay is Montevideo.* **346** But a draft model, without retaining this much  $347$ knowledge, may respond incorrectly: *The capital* **348** *of Uruguay is Paris.* For model accuracy evalua- **349** tion, this would be a failure. However, this would **350** be a good set of candidate tokens in speculative **351** decoding, as the first five words are generated cor- **352** rectly. Therefore, as shown in Figure [5,](#page-4-2) TAR in- **353** creases sub-linearly with an increase in model size, **354** irrespective of its accuracy on the task. Results **355** on more datasets can be found in the Appendix **356** (Figure [10\)](#page-11-0). **357**

Combining insights from these experiments, **358** we observe that current draft models are not de- **359** signed to maximize speculative decoding through- **360**

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**361** put. Next, we will show how to design new draft **362** models that outperform existing models.

# **<sup>363</sup>** 4 Draft Model Design for Speculative **<sup>364</sup>** Decoding

 The above results indicate that to improve the throughput of speculative decoding, it is necessary to improve the latency of draft models, *i.e.*, can we design a model that provides a similar TAR at a lower inference cost? In the next section, we study the possibility of such a design based on the above insights.

# **372** 4.1 Draft Model Design

 In section [3.1,](#page-3-2) we show that model depth bottle- necks draft model latency, while in section [3.3,](#page-4-1) we show that a draft model's performance in specula- tive decoding is largely irrelevant to its accuracy on language modeling. These two insights prompted us to test if we can build a wider and shallower network and study how it affects latency and TAR.

 Method: We leverage recent advances in struc- tured LLM pruning, Sheared-LLAMA [\(Xia et al.,](#page-9-6) [2023b\)](#page-9-6), which provides a framework to prune larger models to a specified smaller configuration. Sheared-LLAMA [\(Xia et al.,](#page-9-6) [2023b\)](#page-9-6) learns layers, attention heads, and neurons to mask from the large model to prune it into the specified small model. The flexibility enables us to prune LLAMA-7B into desirable model configurations. In our exper- iments, we prune our models from LLAMA-7B using 0.4B tokens sampled from the RedPajama Dataset [\(Computer,](#page-8-19) [2023\)](#page-8-19) (the same as in Sheared- LLAMA [\(Xia et al.,](#page-9-6) [2023b\)](#page-9-6)), but skipped the ex- pensive fine-tuning step on 50B more tokens (and hence the name NoFT). We find that this is suffi-cient to achieve a significantly higher throughput.

 Deep vs Wide Model Comparison: Our goal is to start with LLAMA-7B and produce a wider version of Sheared-LLAMA-1.3B while keeping the number of parameters the same as in Sheared- LLAMA-1.3B. We choose Sheared-LLAMA-1.3B since it achieves the highest throughput in our benchmark among existing models (Blue dots in Figure [6\)](#page-6-1). We use two configurations: the first con- figuration was provided by the Sheared-LLAMA authors (NoFT-1.3B), and we designed the second configuration (NoFT-Wide-1.3B) to optimize for better speculative decoding throughput. Table [1](#page-5-0) shows the detailed configuration of the two models. We slash the number of layers by half, from 24 to 12, and keep the total parameter count roughly the same by increasing the intermediate size from 5504

<span id="page-5-0"></span>Table 1: This table shows the model configuration of the two pruned models. Here l represents the number of layers, h represents the number of attention heads,  $d_{\text{inter}}$  represents intermediate size, and  $d_{\text{model}}$  represents model dimension.

Model		h	$d_{\text{inter}}$	$d_{\text{model}}$
$NoFT-1.3B$			24 16 5504	- 2048
NoFT-Wide-1.3B			12 20 9280	2560
NoFT-Wide-796M	5.		32 11008	-4096
NoFT-Wide-543M	$\mathcal{R}$		32 11008 4096	
NoFT-Wide-290M 1 32 11008 4096				

to 9280, the number of attention heads from 16 to **412** 20, and the corresponding model dimension from **413** 2048 to 2560. **414**

Figure [6a,](#page-6-1) [6b,](#page-6-1) and [8b](#page-10-2) show that we can achieve 415 up to 30% higher speculative decoding throughput **416** using only 0.8% of tokens used to train Sheared- **417** LLAMA-1.3B. **418**

Table [2](#page-6-2) also shows the latency and TAR of the **419** two sheared models on MMLU. The deep variant **420** (NoFT-1.3B) can achieve 3% higher TAR, but the **421** wide variant (NoFT-Wide-1.3B) reduces draft la-  $422$ tency by 49%, improving overall throughput by **423** 41%. We found results are very similar for other **424** datasets, such as Chatbot Arena (Figure [8b](#page-10-2) in the **425** Appendix) and Hellaswag (Figure [6b\)](#page-6-1). This exper- **426** iment shows a need to rethink the model design **427** space for speculative decoding, where we should **428** specifically design models for higher throughput. **429**

Draft model scaling: To understand the limita- **430** tion of draft model depth-width tradeoff in spec- **431** ulative decoding, we created three configurations, **432** NoFT-Wide-796M, 543M, and 290M, that use the **433** same number of attention heads, intermediate size,  $434$ and model dimension as LLAMA-7B, but reduce **435** the number of layers to 5, 3, and 1, respectively. **436** This is the widest configuration possible using the **437** Sheared-LLAMA pruning scheme. 438

Figure [6](#page-6-1) shows that the NoFT-Wide-796M 439 model provides another 20% improvement in **440** throughput over NoFT-Wide-1.3B and demon- **441** strates up to 60% throughput improvement over the **442** existing Sheared-LLAMA-1.3B model. Though **443** the smaller NoFT-Wide-543M provides up to  $40\%$  444 throughput improvements over Sheared-LLAMA- **445** 1.3B, it has a lower throughput than NoFT-Wide- **446** 796M. **447**

Results in figure [6](#page-6-1) show that reducing the layer **448** count to less than 5 layers would cause the model's **449** alignment capability to reduce dramatically. In **450** addition, as we reduce models to 5 layers, target **451** model latency takes more than 80% of the time **452**

<span id="page-6-1"></span>

(a) LLAMA Series on MMLU

(b) LLAMA Series on Hellaswag

Figure 6: This figure shows the throughput scaling of different draft models from the LLAMA series on MMLU and Hellaswag. Asterisks represent models that are pruned but not fine-tuned. The red asterisks represent model configurations that we designed.

<span id="page-6-2"></span>Table 2: This table shows the speculative decoding throughput and the latencies to generate 8 tokens using the two pruned draft models.

ation when we use different target models. The draft	
model we use is NoFT-Wide-796M.	

Target Model MMLU Hellaswag Chatbot Arena

LLAMA-65B 2.66 2.74 2.61<br>LLAMA-2.70B 2.55 2.68 2.64

 $LLAMA-2$  70 $B$ 

<span id="page-6-3"></span>Table 3: This table shows the tokens accepted per iter-



 in a decoding cycle. Therefore, further reducing the latency would only provide a marginal gain in overall decoding latency since the target model latency remains constant. In this case, the drop in TAR significantly outweighs the latency gain, causing decoding throughput to decrease.

#### **459** 4.2 Ablation Studies

**460** In this section, we study if using a different or **461** supervised fine-tuned target model would affect **462** our draft model's performance.

 Varying the target model: Prior experiments are performed with LLAMA-65B as the target model. As newer generations of models roll out, we would like to see if our conclusion holds on newer generations of models. In this ablation study, we evaluate our best NoFT-Wide-796M model against LLAMA-2-70B model. Table [3](#page-6-3) shows that though our NoFT-Wide-796M is distilled from LLAMA- 7B, it can achieve a similar token acceptance rate when the target model is from LLAMA-2 family. We believe the similarity in performance is due to similar training datasets. This shows that our dis- tilled model can be applied to future families of models based on similar training recipes with little to no changes.

 Supervised fine-tuned models: Prior exper- iments are performed on base models to study the scaling of draft models. In practice, super- vised fine-tuned models are adopted for their better instruction-following capabilities. In this section,

<span id="page-6-4"></span>Table 4: This table shows the throughput of speculative decoding (tokens/s) with Vicuna 33B as the target model.

Draft Model			MMLU Hellaswag Chatbot Arena
Tiny-LLAMA-1.1B	20.78	18.25	18.73
NoFT-Wide-796M	29.87	26.55	25.61

we compare our best NoFT-Wide-796M model to **483** Tiny-LLAMA-1.1B with Vicuna 33B as the target **484** model. Note that our NoFT-Wide-796M is pruned **485** from the base version of LLAMA-7B without fine- **486** tuning. Table [4](#page-6-4) shows that NoFT-Wide-796M out- **487** performs Tiny-LLAMA-1.1B in all cases by up to **488** 45%. While Tiny-LLAMA-1.1B has a TAR 35% **489** and 32% higher than NoFT-Wide-796M on MMLU **490** and Hellaswag, respectively, its latency is 4x higher **491** due to having 22 layers in the model compared **492** to NoFT-Wide-796M with merely 5 layers. This **493** ablation study also demonstrates how speculative **494** decoding is bottlenecked by draft model depth and **495** that a draft model obtained from the non-fine-tuned **496** base model, when appropriately designed, can still **497** provide significant speedup over draft models fine- **498** tuned for chatbot purposes. **499**

### 5 Discussion **<sup>500</sup>**

Next, we discuss how our insights can change if  $501$ the models or the underlying hardware change. **502**

### <span id="page-6-0"></span>5.1 Future Draft Model Design **503**

To study how compute and performance changes **504** can lead to different choices of draft models, we use **505** a performance model. The original speculative de- **506**

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**511**

<span id="page-7-1"></span>Table 5: This table shows the latency reduction needed for larger draft models to achieve parity throughput with OPT-125M on MMLU.

Model		Latency (ms) Parity Latency	Reduction $(\%)$
125M	43.7	43.7	
350M	79.8	50.6	36.6
1.3B	87.1	58.7	32.6
2.7 <sub>B</sub>	114.3	49.8	56.4
6.7B	139.5	68.2	51.1

**coding [\(Leviathan et al.,](#page-8-6) [2023\)](#page-8-6) model**  $\frac{1-\alpha^{\gamma+1}}{(1-\alpha)(\gamma c+1)}$  can be simplified to the following to remove the unnecessary assumption of mutual independence between generated tokens in a sequence:

$$
Tput = \begin{cases} \frac{TAR}{(t_{target}^d + t_{draff}^d)} & \text{if } TAR > 1, \\ \frac{1}{(t_{target}^d + t_{draff}^d)} & \text{if } TAR \le 1. \end{cases}
$$

 In the Appendix (Figure [12\)](#page-11-1), we show that this sim- plified formula almost perfectly captures the real **Speculative decoding throughput. Here,**  $t^d$  **repre-** sents the latency to generate d tokens autoregres- sively. In this section, with the aid of the perfor- mance model, we provide quantitative answers to several questions: First, we study the improvement in TAR a larger draft model needs to be provided to compensate for the additional inference cost. Next, we study how much improvement in latency is re-quired to change the choice of the draft model.

 Improvement in TAR needed to switch to a larger draft model model. In Figure [2,](#page-2-0) we ob- served that with existing datasets and models, we are better off with the smallest model as the draft model, *e.g.*, OPT-125M, than choosing a larger model. However, there is a possibility that the TAR difference will become greater for new datasets. In Figure [7,](#page-7-0) we plot the improvement in TAR (extra TAR), which larger models in the OPT model fam- ily should provide to match the throughput of the smallest model (OPT-125M) for MMLU. We find that if a 1.3B model can achieve a TAR advantage greater than 2 over OPT-125M for a new workload, we would choose the 1.3B model instead. Further- more, given that the maximum TAR is capped at 8 in our scenario due to the length of draft token generation, it becomes unfeasible for OPT-2.7B and OPT-6.7B to surpass OPT-125M in perfor- mance. This is because the improvement needed in TAR for OPT-6.7B to match the throughput of OPT-125M would exceed this maximum limit. Improvement in latency for switching to higher TAR model. As hardware evolves, latency scal-ing patterns may change with more computing

<span id="page-7-0"></span>



Figure 7: This figure shows the extra TAR needed for each model to achieve parity throughout with OPT-125M on MMLU.

power and memory bandwidth. Therefore, conclu- **547** sions drawn on specific hardware (*e.g.*, A100) may **548** not hold for newer or older hardware (*e.g.*, H100 **549** or V100). To account for changing hardware, we **550** study how much draft model latency improvement **551** is needed to achieve throughput parity. To demon- **552** strate this, we first compute the latency reduction **553** needed for different members in OPT family to **554** reach the same throughput as the smallest draft **555** model in Table [5.](#page-7-1) We find that up to 56% of latency **556** reduction is needed to achieve the same through- **557** put. For instance, for OPT-1.3B to achieve parity **558** throughput with OPT-125M, its latency needs to be **559** reduced by 32.9%. This reinforces our finding that **560** latency reduction provided by the smaller models **561** has significantly more benefit than the extra TAR **562** provided by a larger draft model. **563**

## 6 Conclusion **<sup>564</sup>**

In this work, we conduct a large-scale experimen- **565** tal study to understand how we can optimize the **566** throughput of speculative decoding. Using our ex- **567** periments, we outline the various factors that affect **568** speculative decoding throughput. We observe that **569** draft model accuracy on language modeling does **570** not correlate strongly with its performance in spec- **571** ulative decoding. Further, we find that draft model **572** latency is bottlenecked by model depth, and higher **573** model depth increases latency. Based on these two **574** insights, we propose new draft models pruned to **575** align with the target model while trading model **576** depth for width. Our proposed draft model can **577** increase throughput by up to 60% over existing **578** models. We find that the pruned models can be **579** used for supervised fine-tuned target models with- **580** out modification and discuss how future models **581** may impact draft model selection. **582**

# **<sup>583</sup>** 7 Limitations

**584** Our work aims to improve the inference efficiency

**585** of LLMs by designing better draft models for spec-**586** ulative decoding. Since speculative decoding pre-

- **587** serves the output from the LLM, our work will not
- **588** amplify existing biases in LLMs. However, limit-
- **589** ing and reducing such biases are out of the scope of **590** this work. Furthermore, since we are making LLM
- **591** generation more efficient, we believe our work will
- **592** not have a significant negative environmental im-
- **593** pact.

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# A More Experiment Results **<sup>755</sup>**

In this section, we show more experimental analy- **756** sis of speculative decoding. In Figure [8,](#page-10-2) we plot the **757** throughput of OPT and LLAMA models against **758** its TAR on Chatbot Arena. This figure shows that **759** as model size increases, throughput generally de- **760** creases due to significantly higher inference latency **761** despite consistent increases in TAR. **762** 

In Figure [9,](#page-10-1) we plot the throughput of OPT and **763** LLAMA models against its TAR on Chatbot Arena. **764** This figure shows that draft latency occupies a large **765** chunk of time in a speculative decoding iteration, **766** opening up new avenues for designing draft models **767** optimal for speculative decoding. **768**

In Figure [10,](#page-11-0) we plot the task accuracy versus **769** TAR for OPT and LLAMA models on MMLU. **770** The accuracy numbers are obtained from Open- **771** LLM Leaderboard [\(HuggingFace,](#page-8-18) [2023\)](#page-8-18). This fig- **772** ure shows that task accuracy is irrelevant to TAR. **773**

Required TAR to match throughput. We can **775** also use our analytical model to predict the TAR **776** necessary for different models to achieve a tar-  $\frac{777}{2}$ get throughput. This can be useful in scenar- **778** ios where developers deploy speculative decoding- **779** based LLMs and must meet a throughput goal. In **780** Figure [11,](#page-11-2) we plot the TAR needed by existing  $\frac{781}{20}$ models to achieve a specific throughput. The fig- **782** ure shows that the TAR gap between draft mod- **783** els at each given throughput is much larger than **784** we observed in Figure [2.](#page-2-0) When the throughput 785 requirement is high, a large draft model, such as **786** OPT-6.7B, can't achieve the desired throughput. **787** This will allow model designers to quickly judge **788** which draft and target model pair allows them to **789** meet throughput requirements. **790** 

## **B** OPT-350M Configurations **791**

Table [6](#page-10-0) shows the detailed model configurations **792** of the OPT-350M variants we created. The goal is **793**

<span id="page-10-2"></span>

(a) Throughput scaling with increasing TAR in OPT series on Chatbot Arena





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<span id="page-10-1"></span>

Figure 9: Performance Breakdown of LLAMA speculative decoding, lookahead length is set to be optimal lookahead length found empirically.

<span id="page-10-0"></span>Table 6: This table shows model configuration of various OPT-350M models we created. The goal is to explore the tradeoff between model depth and width while keeping the total parameter count constant.

	Num Layers Attn. Heads Hidden size FFN Dim		
24	16	1024	4096
20	20	1280	3448
16	22	1408	4096
12	28	1792	3448
	36	2304	3448
	56	3584	3448

**794** to keep the total parameter count close to that of **795** OPT-350M while adjusting model width and depth.

# **<sup>796</sup>** C Simplifying Analytical model

 [T](#page-8-6)he original speculative decoding paper [\(Leviathan](#page-8-6) [et al.,](#page-8-6) [2023\)](#page-8-6) proposed an analytical model  $\frac{1-\alpha^{\gamma+1}}{(1-\alpha)(\gamma c+1)}$  to describe the speedup achieved by <sup>799</sup>  $\frac{(1-\alpha)(\gamma c+1)}{(1-\alpha)(\gamma c+1)}$  to describe the speedup active decoding  $\alpha$  denotes the ex- pected token acceptance rate (in percentage) and  $\gamma$  denotes the lookahead length. However, this model is inaccurate since it assumes that the tokens generated in a sentence are mutually independent.

Table 7: This table shows the latency of each autoregressive generation step of the draft model.

Model	Latency (ms)
<b>OPT-125M</b>	6.23
<b>OPT-350M</b>	11.74
$OPT-1.3B$	12.64
$OPT-2.7B$	16.35
$OPT-6.7B$	18.56

We simplify this cost model and use our updated **805** analytical model in our experiments. **806**

Assuming a setup similar to prior **807** work [\(Leviathan et al.,](#page-8-6) [2023;](#page-8-6) [Chen et al.,](#page-8-8) **808** [2023;](#page-8-8) [Miao et al.,](#page-8-1) [2023\)](#page-8-1) where speculative **809** execution of the draft model and target model **810** verification phases happen sequentially, the **811** performance of speculative decoding can be **812** decomposed into the following factors, **813**

$$
Tput = \begin{cases} \frac{TAR}{(t_{target}^d + t_{draff}^d)} & \text{if } TAR > 1, \\ \frac{1}{(t_{target}^d + t_{draff}^d)} & \text{if } TAR \le 1. \end{cases}
$$

Considering a case where, in each iteration,  $d$  815 tokens are generated by the draft model,  $t_{draff}^d$  de- 816 picts the time draft models take to generate  $\overrightarrow{d}$  draft  $817$ tokens, while  $t_{target}^d$  is the time taken by the target  $818$ model for verifying those d draft tokens. TAR is 819 used to denote the average number of tokens that **820** were matched across a query or a dataset. **821**

Verifying Analytical Model In Figure [12,](#page-11-1) we **822** compare the throughput predicted by our model **823** with throughput measured on real hardware for 824 two model families: LLAMA (7B and 13B) and **825**

**814**

<span id="page-11-0"></span>

(a) Model accuracy vs. TAR for OPT models on MMLU (b) Model accuracy vs TAR for LLAMA models on and Hellaswag MMLU and Hellaswag

Figure 10: This figure shows the task accuracy versus TAR for OPT and LLAMA models on MMLU. The accuracy numbers are obtained from OpenLLM Leaderboard [\(HuggingFace,](#page-8-18) [2023\)](#page-8-18).

<span id="page-11-2"></span>

Figure 11: This figure shows the required TAR to achieve a given throughput.

**826** OPT (125M, 350M, 1.3B, 2.7B, and 6.7B) to serve **827** LLAMA-65B and OPT-66B on MMLU.

 We run these experiments on 4 Nvidia 80GB A100 GPUs for 100 iterations on the real server, and the error bars in Figure [12](#page-11-1) represent the stan- dard deviation of the measurement. For the per-832 formance model, we collect  $t_{draff}^d$  and  $t_{target}^d$  on a real cluster with a single iteration. For TAR, we collect the average token acceptance rate from the MMLU dataset. The maximum deviation we ob- served between our proposed analytical model and 837 the results obtained is 3.5%. The close correspon- dence between our performance model and real measurements shows that our performance model accurately predicts the throughput of speculative decoding.

<span id="page-11-1"></span>

Figure 12: This figure shows that our performance model correctly captures the real performance of speculative decoding. We use LLAMA-65B and OPT-66B as the target model for each model family, respectively.