

# DIFFUSION POLICY POLICY OPTIMIZATION

Anonymous authors

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### ABSTRACT

We introduce *Diffusion Policy Policy Optimization*, **DPPO**, an algorithmic framework including best practices for fine-tuning diffusion-based policies (e.g. Diffusion Policy [\(Chi et al.,](#page-10-0) [2024b\)](#page-10-0)) in continuous control and robot learning tasks using the policy gradient (PG) method from reinforcement learning (RL). PG methods are ubiquitous in training RL policies with other policy parameterizations; nevertheless, they had been conjectured to be less efficient for diffusion-based policies. Surprisingly, we show that **DPPO** achieves the strongest overall performance and efficiency for fine-tuning in common benchmarks compared to other RL methods for diffusion-based policies and also compared to PG fine-tuning of other policy parameterizations. Through experimental investigation, we find that **DPPO** takes advantage of unique synergies between RL fine-tuning and the diffusion parameterization, leading to structured and on-manifold exploration, stable training, and strong policy robustness. We further demonstrate the strengths of **DPPO** in a range of realistic settings, including simulated robotic tasks with pixel observations, and via zero-shot deployment of simulation-trained policies on robot hardware in a long-horizon, multi-stage manipulation task. Website with videos: **[diffusionppoanon.github.io](https://diffusionppoanon.github.io)**. Code: **[anonymous.dppo](https://anonymous.4open.science/r/dppo-iclr-online-7B5B)**.

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# <span id="page-0-0"></span>1 INTRODUCTION

**031 032 033 034 035 036 037 038 039 040 041 042** Large-scale pre-training with additional fine-tuning has become a ubiquitous pipeline in the development of language and image foundation models [\(Brown et al.,](#page-10-1) [2020;](#page-10-1) [Radford et al.,](#page-13-0) [2021;](#page-13-0) [Ouyang et al.,](#page-13-1) [2022;](#page-13-1) [Ruiz et al.,](#page-13-2) [2023\)](#page-13-2). Though behavior cloning with expert data [\(Pomerleau,](#page-13-3) [1988\)](#page-13-3) is rapidly emerging as dominant paradigm for pre-training *robot policies* [\(Florence et al.,](#page-11-0) [2019;](#page-11-0) [2022;](#page-11-1) [Zhao et al.,](#page-15-0) [2023;](#page-15-0) [Lee et al.,](#page-12-0) [2024;](#page-12-0) [Fu et al.,](#page-11-2) [2024\)](#page-11-2), their performance can be suboptimal [\(Osa et al.,](#page-13-4) [2018\)](#page-13-4) due to expert data being suboptimal or expert data exhibiting limited coverage of possible environment conditions. As robot policies entail interaction with their environment, reinforcement learning (RL) [\(Sutton and Barto,](#page-14-0) [2018\)](#page-14-0) is a natural candidate for further optimizing their performance beyond the limits of demonstration data. However, RL fine-tuning can be nuanced for pre-trained policies parameterized as diffusion models [\(Ho et al.,](#page-11-3) [2020\)](#page-11-3), which have emerged as a leading parameterization for action policies [\(Chi et al.,](#page-10-0) [2024b;](#page-10-0) [Reuss et al.,](#page-13-5) [2023;](#page-13-5) [Pearce et al.,](#page-13-6) [2023\)](#page-13-6), due in large part to their high training stability and ability to represent complex distributions [\(Rombach et al.,](#page-13-7) [2022;](#page-13-7) [Poole et al.,](#page-13-8) [2022;](#page-13-8) [Kong et al.,](#page-12-1) [2020;](#page-12-1) [Ho et al.,](#page-11-4) [2022\)](#page-11-4).

**043 044 045 046** Contribution 1 *(***DPPO***)*. We introduce *Diffusion Policy Policy Optimization* (**DPPO**), a generic framework as well as a set of carefully chosen design decisions for fine-tuning a diffusion-based robot learning policy via popular policy gradient methods [\(Sutton et al.,](#page-14-1) [1999;](#page-14-1) [Schulman et al.,](#page-14-2) [2017\)](#page-14-2) in reinforcement learning.

**047 048 049 050 051 052 053** The literature has already studied improving/fine-tuning diffusion-based policies (*Diffusion Policy*) using RL [\(Psenka et al.,](#page-13-9) [2023;](#page-13-9) [Wang et al.,](#page-14-3) [2022;](#page-14-3) [Hansen-Estruch et al.,](#page-11-5) [2023\)](#page-11-5), and has applied policy gradient (PG) to fine-tuning non-interactive applications of diffusion models such as text-toimage generation [\(Black et al.,](#page-10-2) [2023;](#page-10-2) [Clark et al.,](#page-10-3) [2023;](#page-10-3) [Fan et al.,](#page-11-6) [2024\)](#page-11-6). Yet PG methods have been believed to be inefficient in training Diffusion Policy for continuous control tasks [\(Psenka](#page-13-9) [et al.,](#page-13-9) [2023;](#page-13-9) [Yang et al.,](#page-14-4) [2023\)](#page-14-4). On the contrary, we show that for a Diffusion Policy pre-trained from expert demonstrations, our methodology for *fine-tuning* via PG updates yields robust, highperforming policies with favorable training behavior.

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Figure 1: We introduce **DPPO**, *Diffusion Policy Policy Optimization*, that fine-tunes pre-trained Diffusion Policy using policy gradient. **DPPO** affords structured exploration and training stability during policy fine-tuning, and the fine-tuned policy exhibits strong robustness and generalization. **DPPO** improves policy performance across benchmarks, including ones with pixel observations and with long-horizon rollouts that have been very challenging to solve using previous RL methods.

**069 070 071 072 073 074 075** Contribution 2 *(Demonstration of* **DPPO***'s Performance).* We show that for *fine-tuning* a pretrained Diffusion Policy, **DPPO** yields consistent and marked improvements in training stability and often final policy performance in comparison to a range of alternatives, including those based on off-policy Q-learning [\(Wang et al.,](#page-14-3) [2022;](#page-14-3) [Hansen-Estruch et al.,](#page-11-5) [2023;](#page-11-5) [Yang et al.,](#page-14-4) [2023;](#page-14-4) [Psenka](#page-13-9) [et al.,](#page-13-9) [2023\)](#page-13-9) and weighted regression [\(Peng et al.,](#page-13-10) [2019;](#page-13-10) [Peters and Schaal,](#page-13-11) [2007;](#page-13-11) [Kang et al.,](#page-12-2) [2024\)](#page-12-2), other demo-augmented RL methods [\(Ball et al.,](#page-10-4) [2023;](#page-10-4) [Nakamoto et al.,](#page-12-3) [2024;](#page-12-3) [Hu et al.,](#page-11-7) [2023\)](#page-11-7), as well as common policy parameterizations such as Gaussian and Gaussian Mixture models.

**076 077 078 b**  $079$ The above finding might be surprising because PG methods do not appear to take advantage of the unique capabilities of diffusion sampling (e.g., guidance [Janner et al.](#page-12-4) [\(2022\)](#page-12-4); [Ajay et al.](#page-10-5) [\(2023\)](#page-10-5)). Through careful investigative experimentation, however, we find a unique synergy between RL fine-tuning and diffusion-based policies.

**080** reverse [0, 4, 1, 3] **082 083 084** Orange on blue, Contribution 3 *(Understanding the mechanism of* **DPPO***'s success).* We complement our results with numerous investigative experiments that provide insight into the mechanisms behind **DPPO**'s strong performance. Compared to other common policy parameterizations, we provide evidence that **DPPO** engages in *structured exploration* that takes better advantage of the "manifold" of training data, and finds policies that exhibit greater robustness to perturbation.

weblate **085 086 087 088** Through ablations, we further show that our design decisions overcome the speculated limitation of PG methods for fine-tuning Diffusion Policy. Finally, to justify the broad utility of **DPPO**, we verify its efficacy across both simulated and real environments, and in situations when either ground-truth states or pixels are given to the policy as input.

**089** Orange on red **090 091 092** Contribution 4 *(Tackling challenging robotic tasks and settings).* We show **DPPO** is effective in challenging robotic and control settings, including pixel observations and long-horizon manipulation tasks with sparse reward. We deploy a policy trained in simulation via **DPPO** on real hardware in zero-shot, which exhibits a remarkably small sim-to-real gap compared to the baseline.

**093 094 095 096 097 098 099 100** Potential impact beyond robotics. **DPPO** is a generic framework that can be potentially applied to fine-tuning diffusion-based models in sequential interactive settings beyond robotics. These include: extending diffusion-based text-to-image generation [\(Black et al.,](#page-10-2) [2023;](#page-10-2) [Clark et al.,](#page-10-3) [2023\)](#page-10-3) to a multiturn interactive setting with human feedback; drug design/discovery applications [\(Luo et al.,](#page-12-5) [2022;](#page-12-5) [Huang et al.,](#page-12-6) [2024\)](#page-12-6) with policy search on the molecular level in feedback with simulators (in the spirit of prior non-diffusion-based drug discovery with RL [\(Popova et al.,](#page-13-12) [2018\)](#page-13-12)); and the adaptation of diffusion-based language modeling [\(Sahoo et al.,](#page-13-13) [2024;](#page-13-13) [Lou et al.,](#page-12-7) [2024\)](#page-12-7) to interactive (e.g. with human feedback [\(Ouyang et al.,](#page-13-1) [2022\)](#page-13-1)), problem-solving and planning tasks.

- <span id="page-1-0"></span>2 RELATED WORK
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**103 104 105 106 107** Policy optimization and its application to robotics. Policy optimization methods update an explicit representation of an RL policy — typically parameterized by a neural network — by taking gradients through action likelihoods. Following the seminal policy gradient (PG) method [\(Williams,](#page-14-5) [1992;](#page-14-5) [Sutton et al.,](#page-14-1) [1999\)](#page-14-1), there have been a range of algorithms that further improve training stability and sample efficiency such as DDPG [\(Lillicrap et al.,](#page-12-8) [2015\)](#page-12-8) and PPO [\(Schulman et al.,](#page-14-6) [2015\)](#page-14-6). PG methods have been broadly effective in training robot policies [\(Andrychowicz et al.,](#page-10-6) [2020;](#page-10-6) [Hwangbo](#page-12-9)

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[Round-table](#page-12-9)

Figure 2: **DPPO** solves challenging long-horizon manipulation tasks from FURNITURE-BENCH [\(Heo et al.](#page-11-8) [\(2023\)](#page-11-8)), enabling robust sim-to-real transfer without using any real data [\(Section 5.4\)](#page-7-0).

**118 119 120 121 122 123 124 125** [et al.,](#page-12-9) [2019;](#page-12-9) [Kaufmann et al.,](#page-12-10) [2023;](#page-12-10) [Chen et al.,](#page-10-7) [2022b\)](#page-10-7), largely due to their training stability with high-dimensional continuous action spaces, as well as their favorable scaling with parallelized simulated environments. Given the challenges of from-scratch exploration in long-horizon tasks, PG has seen great success in fine-tuning a baseline policy trained from demonstrations [\(Rajeswaran et al.,](#page-13-14) [2017;](#page-13-14) [Torne et al.,](#page-14-7) [2024;](#page-14-7) [Peng et al.,](#page-13-15) [2021\)](#page-13-15). Our experiments find **DPPO** performing on-policy PG achieves stronger final performance in manipulation tasks, especially when the demonstrations are noisy, than off-policy Q-learning methods [\(Ball et al.,](#page-10-4) [2023;](#page-10-4) [Nakamoto et al.,](#page-12-3) [2024;](#page-12-3) [Hu et al.,](#page-11-7) [2023\)](#page-11-7). See [Appendix A.1](#page-17-0) for extended discussions on PG fine-tuning of robot policies and related methods.

**126 127 128 129 130 131 132 133 134 135 136 137 138** Learning and improving diffusion-based policies. Diffusion-based policies [\(Chi et al.,](#page-10-0) [2024b;](#page-10-0) [Reuss et al.,](#page-13-5) [2023;](#page-13-5) [Ankile et al.,](#page-10-8) [2024a;](#page-10-8) [Ze et al.;](#page-14-8) [Wang et al.,](#page-14-9) [2024;](#page-14-9) [Sridhar et al.,](#page-14-10) [2023;](#page-14-10) [Pearce](#page-13-6) [et al.,](#page-13-6) [2023\)](#page-13-6) have shown recent success in robotics and decision making applications. Most typically, these policies are trained from human demonstrations through a supervised objective, and enjoy both high training stability and strong performance in modeling complex and multi-modal trajectory distributions. As demonstration data are often limited and/or suboptimal, there have been many approaches proposed to improve the performance of diffusion-based policies. One popular approach has been to guide the diffusion denoising process using objectives such as reward signal or goal conditioning [\(Janner et al.,](#page-12-4) [2022;](#page-12-4) [Ajay et al.,](#page-10-5) [2023;](#page-10-5) [Liang et al.,](#page-12-11) [2023;](#page-12-11) [Venkatraman et al.,](#page-14-11) [2023;](#page-14-11) [Chen et al.,](#page-10-9) [2024\)](#page-10-9). More recent work has explored techniques including Q-learning and weighted regression, either from purely offline estimation [\(Chen et al.,](#page-10-10) [2022a;](#page-10-10) [Wang et al.,](#page-14-3) [2022;](#page-14-3) [Ding and](#page-11-9) [Jin,](#page-11-9) [2023\)](#page-11-9), and/or with online interaction [\(Kang et al.,](#page-12-2) [2024;](#page-12-2) [Hansen-Estruch et al.,](#page-11-5) [2023;](#page-11-5) [Psenka](#page-13-9) [et al.,](#page-13-9) [2023;](#page-13-9) [Yang et al.,](#page-14-4) [2023\)](#page-14-4). See [Appendix A.2](#page-17-1) for detailed descriptions of these methods.

**139 140 141 142 143 144 145 146** Policy gradient through diffusion models. RL techniques have been used to fine-tune diffusion models such as ones for text-to-image generation [\(Fan and Lee,](#page-11-10) [2023;](#page-11-10) [Fan et al.,](#page-11-6) [2024;](#page-11-6) [Black et al.,](#page-10-2) [2023;](#page-10-2) [Wallace et al.,](#page-14-12) [2023\)](#page-14-12). [Black et al.](#page-10-2) [\(2023\)](#page-10-2) treat the denoising process as an MDP and apply PPO updates. We build upon these earlier findings by embedding the denoising MDP into the environmental MDP of the dynamics in control tasks, forming a two-layer "Diffusion Policy MDP". Though [Psenka et al.](#page-13-9) [\(2023\)](#page-13-9) have already shown how PG can be taken through Diffusion Policy by propagating PG through both MDPs, they conjecture that it is likely to be ineffective due to large action variance caused by the increased effective horizon induced from the denoising steps. Our results contravene this supposition for diffusion-based policies in the fine-tuning setting.

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# <span id="page-2-2"></span>3 PRELIMINARIES

**150 151 152 153 154 155 156 157 Markov Decision Process.** We consider a *Markov Decision Process* (MDP)<sup>[1](#page-2-0)</sup>  $M_{\text{Env}}$  :=  $(S, \mathcal{A}, P_0, P, R)$  with states  $s \in \mathcal{S}$ , actions  $a \in \mathcal{A}$ , initial state distribution  $P_0$ , transition probabilities P, and reward R. At each timestep t, the agent (e.g., robot) observes the state  $s_t \in S$ , takes an action  $a_t \sim \pi(a_t \mid s_t) \in A$ , transitions to the next state  $s_{t+1}$  according to  $s_{t+1} \sim P(s_{t+1} \mid s_t, a_t)$ while receiving the reward  $R(s_t, a_t)^2$  $R(s_t, a_t)^2$ . Fixing the MDP  $\mathcal{M}_{\text{Env}}$ , we let  $\mathbb{E}^{\pi}$  (resp.  $\mathbb{P}^{\pi}$ ) denote the expectation (resp. probability distribution) over trajectories  $(s_0, a_0, ..., s_T, a_T)$  with length  $T + 1$ , with initial state distribution  $s_0 \sim P_0$  and transition operator P. We aim to train a policy to optimize the cumulative reward, discounted by a function  $\gamma(\cdot)$ , such that the agent receives a cost  $\mathcal{J}(\pi_{\theta}) = \mathbb{E}^{\pi_{\theta},P_0}[\sum_{t\geq 0} \gamma(t) R(s_t,a_t)]$ 

**<sup>159</sup> 160 161** <sup>1</sup>More generally, we can view our environment as a Partially Observed Markov Decision Process (POMDP) where the agent's actions depend on observations  $o$  of the states  $s$  (e.g., action from pixels). Our implementation applies in this setting, but we omit additional observations from the formalism to avoid notional clutter.

<span id="page-2-1"></span><span id="page-2-0"></span><sup>&</sup>lt;sup>2</sup> For simplicity, we overload  $R(\cdot, \cdot)$  to denote both the random variable reward and its distribution.

**162 163 164 165 166 167 168 169 170** Policy optimization. The *policy gradient method* (e.g., REINFORCE [\(Williams,](#page-14-5) [1992\)](#page-14-5)) allows for improving policy performance by approximating the gradient of this objective w.r.t. the policy parameters:  $\nabla_{\theta} \mathcal{J}(\pi_{\theta}) = \mathbb{E}^{\pi_{\theta}, \vec{P}_0}[\sum_{t \geq 0} \nabla_{\theta} \log \pi_{\theta}(a_t|s_t) r_t(s_t, a_t)], r_t(s_t, a_t) :=$  $\sum_{\tau \geq t} \gamma(\tau) R(s_\tau, a_\tau)$  where  $r_t$  is the discounted cumulative future reward from time t (more generally,  $r_t$  can be replaced by a Q-function estimator [\(Sutton et al.,](#page-14-1) [1999\)](#page-14-1)),  $\gamma$  is the discount factor that depends on the time-step, and  $\nabla_{\theta} \log \pi_{\theta}(a_t|s_t)$  denotes the gradient of the logarithm of the *likelihood* of  $a_t \mid s_t$ . To reduce the variance of the gradient estimation, a state-value function  $\hat{V}^{\pi_{\theta}}(s_t)$  can be learned to approximate  $\mathbb{E}[r_t]$ . The estimated advantage function  $\hat{A}^{\pi_{\theta}}(s_t, a_t) :=$  $r_t(s_t, a_t) - \hat{V}^{\pi_\theta}(s_t)$  substitutes  $r_t(s_t, a_t)$ .

**171 172 173 174 175 176 177** Diffusion models. A denoising diffusion probabilistic model (DDPM) [\(Nichol and Dhariwal,](#page-13-16) [2021;](#page-13-16) [Ho et al.,](#page-11-3) [2020;](#page-11-3) [Sohl-Dickstein et al.,](#page-14-13) [2015\)](#page-14-13) represents a continuous-valued data distribution  $p(\cdot)$  =  $p(x^0)$  as the reverse denoising process of a forward noising process  $q(x^k|x^{k-1})$  that iteratively adds Gaussian noise to the data. The reverse process is parameterized by a neural network  $\varepsilon_{\theta}(x_k, k)$ , predicting the added noise  $\varepsilon$  that converts  $x_0$  to  $x_k$  [\(Ho et al.,](#page-11-3) [2020\)](#page-11-3). Sampling starts with a random sample  $x^K \sim \mathcal{N}(0, I)$  and iteratively generates the denoised sample:

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$$
x^{k-1} \sim p_{\theta}(x^{k-1}|x^k) := \mathcal{N}(x^{k-1}; \mu_k(x^k, \varepsilon_{\theta}(x^k, k)), \sigma_k^2 I). \tag{3.1}
$$

**179 180 181** Above,  $\mu_k(\cdot)$  is a fixed function, independent of  $\theta$ , that maps  $x^k$  and predicted  $\varepsilon_\theta$  to the next mean, and  $\sigma_k^2$  is a variance term that abides by a fixed schedule from  $k = 1, ..., K$ . We refer the reader to [Chan](#page-10-11) [\(2024\)](#page-10-11) for an in-depth survey.

**Diffusion models as policies.** *Diffusion Policy* (DP; see [Chi et al.](#page-10-0) [\(2024b\)](#page-10-0)) is a policy  $\pi_{\theta}$  parameterized by a DDPM which takes in s as a conditioning argument, and parameterizes  $p_{\theta}(a^{k-1} | a^k, s)$ as in  $(3.1)$ . DPs can be trained via behavior cloning by fitting the conditional noise prediction  $\varepsilon_{\theta}(a^k, s, k)$  to predict the added noise. Notice that unlike more standard policy parameterizations such as unimodal Gaussian policies, DPs do not maintain an explicit likelihood of  $p_{\theta}(a^0 \mid s)$ . In this work, we adopt the common practice of training DPs to predict an **action chunk** — a sequence of actions a few time steps (denoted  $T_a$ ) into the future — to promote temporal consistency. For fair comparison, our diffusion and non-diffusion baselines use the same chunk size. son and the contract of  $\overline{\phantom{0}}$ 

# <span id="page-3-2"></span><span id="page-3-1"></span>4 **DPPO**: DIFFUSION POLICY POLICY OPTIMIZATION



Figure 3: We treat the denoising process in Diffusion Policy as an MDP, and the whole environment episode can be considered as a chain of such MDPs. Now the entire chain ("Diffusion Policy MDP",  $M_{\text{DP}}$ ) involves a Gaussian likelihood at each (denoising) step and thus can be optimized with policy gradient. Blue circle denotes the state and red circle denotes the action in  $M_{\text{DP}}$ .

**206 207 208 209 210 211 212 213** As observed in [Black et al.](#page-10-2) [\(2023\)](#page-10-2) and [Psenka et al.](#page-13-9) [\(2023\)](#page-13-9), a denoising process can be represented as a multi-step MDP in which policy likelihood of each denoising step can be obtained directly. We extend this formalism by embedding the Diffusion MDP into the environmental MDP, obtaining a larger "Diffusion Policy MDP" denoted  $M_{\text{DP}}$ , visualized in [Fig. 3.](#page-3-1) Below, we use the notation δ to denote a Dirac distribution and ⊗ to denote a product distribution. Recall the environment MDP  $M_{\text{Env}} := (\mathcal{S}, \mathcal{A}, P_0, P, R)$  in [Section 3.](#page-2-2) The Diffusion MDP  $M_{\text{DP}}$  uses indices  $\bar{t}(t, k) =$  $tK + (K - k - 1)$  corresponding to  $(t, k)$ , which increases in t but (to keep the indexing conventions of diffusion) *decreases* lexicographically with  $K - 1 \ge k \ge 0$ . The states, actions and rewards are

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$$
\bar{s}_{\bar{t}(t,k)} = (s_t, a_t^{k+1}), \quad \bar{a}_{\bar{t}(t,k)} = a_t^k, \quad \bar{R}_{\bar{t}(t,k)}(\bar{s}_{\bar{t}(t,k)}, \bar{a}_{\bar{t}(t,k)}) = \begin{cases} 0 & k > 0 \\ R(s_t, a_t^0) & k = 0 \end{cases},
$$

**216 217 218 219** where the bar-action at  $\bar{t}(t, k)$  is the action  $a_t^k$  after one denoising step. Reward is only given at where the bat-action at  $t(t, \kappa)$  is the action  $a_t$  after one denoising step. Reward is only given at times corresponding to when  $a_t^0$  is taken. The initial state distribution is  $\bar{P}^0 = P_{0} \otimes \mathcal{N}(0, I)$ , corresponding to  $s_0 \sim P_0$  is the initial distribution from the environmental MDP and  $a_0^K \sim \mathcal{N}(0, \mathbf{I})$ independently. Finally, the transitions are

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$$
\bar{P}(\bar{s}_{\bar{t}+1} \mid \bar{s}_{\bar{t}}, \bar{a}_{\bar{t}}) = \begin{cases} (s_t, a_t^k) \sim \delta_{(s_t, a_t^k)} & \bar{t} = \bar{t}(t, k), k > 0\\ (s_{t+1}, a_{t+1}^K) \sim P(s_{t+1} \mid s_t, a_t^0) \otimes \mathcal{N}(0, \mathbf{I}) & \bar{t} = \bar{t}(t, k), k = 0 \end{cases}
$$

That is, the transition moves the denoised action  $a_t^k$  at step  $\bar{t}(t, k)$  *into the next state* when  $k > 0$ , or otherwise progresses the environment MDP dynamics with  $k = 0$ . The pure noise  $a_t^K$  is considered part of the *environment* when transitioning at  $k = 0$ . In light of [\(3.1\)](#page-3-0), the policy in  $M_{\text{DP}}$  is

$$
\bar{\pi}_{\theta}(\bar{a}_{\bar{t}(t,k)}) \mid \bar{s}_{\bar{t}(t,k)}) = \pi_{\theta}(a_{t}^{k} \mid a_{t}^{k+1}, s_{t}) = \mathcal{N}(a_{t}^{k}; \mu(a_{t}^{k+1}, \varepsilon_{\theta}(a_{t}^{k+1}, k+1, s_{t})), \sigma_{k+1}^{2}I). \tag{4.1}
$$

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Fortunately, [\(4.1\)](#page-4-0) is a *Gaussian likelihood*, which can be evaluated analytically and is amenable to the policy gradient updates (see also [Psenka et al.](#page-13-9) [\(2023\)](#page-13-9) for an alternative derivation):

$$
\nabla_{\theta}\bar{\mathcal{J}}(\bar{\pi}_{\theta}) = \mathbb{E}^{\bar{\pi}_{\theta}, \bar{P}, \bar{P}^{0}}[\sum_{\bar{t}\geq 0} \nabla_{\theta} \log \bar{\pi}_{\theta}(\bar{a}_{\bar{t}} \mid \bar{s}_{\bar{t}}) \bar{r}(\bar{s}_{\bar{t}}, \bar{a}_{\bar{t}})], \quad \bar{r}(\bar{s}_{\bar{t}}, \bar{a}_{\bar{t}}) := \sum_{\tau \geq \bar{t}} \gamma(\tau) \bar{R}(\bar{s}_{\tau}, \bar{a}_{\tau}). \quad (4.2)
$$

Evaluating the above involves sampling through the denoising process, which is the usual "forward pass" that samples actions in Diffusion Policy; as noted above, the inital state can be sampled from the enviroment via  $\bar{P}^0 = P_0 \otimes \mathcal{N}(0, \mathbf{I})$ , where  $P_0$  is from the environment MDP.

#### <span id="page-4-2"></span>4.1 INSTANTIATING **DPPO** WITH PROXIMAL POLICY OPTIMIZATION

We apply Proximal Policy Optimization (PPO) [\(Schulman et al.,](#page-14-2) [2017;](#page-14-2) [Engstrom et al.,](#page-11-11) [2019;](#page-11-11) [Huang](#page-11-12) [et al.,](#page-11-12) [2022;](#page-11-12) [Achiam,](#page-10-12) [2018\)](#page-10-12), a popular improvement of the vanilla policy gradient update.

Definition 4.1 (Generalized PPO, clipping variant). Consider a general MDP. Given an advantage estimator  $\hat{A}(s, a)$ , the PPO update [\(Schulman et al.,](#page-14-2) [2017\)](#page-14-2) is the sample approximation to

$$
\nabla_{\theta} \mathbb{E}^{(s_t, a_t) \sim \pi_{\theta_{\text{old}}}} \min \left( \hat{A}^{\pi_{\theta_{\text{old}}}}(s_t, a_t) \frac{\pi_{\theta}(a_t \mid s_t)}{\pi_{\theta_{\text{old}}}(a_t \mid s_t)}, \ \hat{A}^{\pi_{\theta_{\text{old}}}}(s_t, a_t) \operatorname{clip} \left( \frac{\pi_{\theta}(a_t \mid s_t)}{\pi_{\theta_{\text{old}}}(a_t \mid s_t)}, 1 - \varepsilon, 1 + \varepsilon \right) \right)
$$

where  $\varepsilon$ , the clipping ratio, controls the maximum magnitude of the policy updated.

**245 246 247 248** We instantiate PPO in our diffusion MDP with  $(s, a, t) \leftarrow (\bar{s}, \bar{a}, \bar{t})$ . Our advantage estimator respects the two-level nature of the MDP: let  $\gamma_{\text{ENV}} \in (0,1)$  be the environment discount and  $\gamma_{\text{DENOISE}} \in (0, 1)$  be the denoising discount. Consider the environment-discounted return:

$$
\bar{r}(\bar{s}_{\bar{t}}, \bar{a}_{\bar{t}}) := \sum_{t' \geq t} \gamma_{\text{env}}^t \bar{r}(\bar{s}_{\bar{t}(t',0)}, \bar{a}_{\bar{t}(t',0)}), \quad \bar{t} = \bar{t}(t,k),
$$

**251 252** since  $R(t) = 0$  at  $k > 0$ . This fact also obviates the need of estimating the value at  $k > 1$  and allows us to use the following denoising-discounted advantage estimator<sup>[3](#page-4-1)</sup>:

<span id="page-4-3"></span>
$$
\hat{A}^{\pi_{\theta_{\text{old}}}}(\bar{s}_{\bar{t}}, \bar{a}_{\bar{t}}) := \gamma^k_{\text{DENOISE}}\left(\bar{r}(\bar{s}_{\bar{t}}, \bar{a}_{\bar{t}}) - \hat{V}^{\bar{\pi}_{\theta_{\text{old}}}}(\bar{s}_{\bar{t}(t,0)})\right)
$$

**255 256 257 258 259** The denoising-discounting has the effect of downweighting the contribution of noisier steps (larger k) to the policy gradient (see study in [Appendix D.2\)](#page-20-0). Lastly, we choose the value estimator to *only depend* on the "s" component of  $\bar{s}$ :  $\hat{V}^{\bar{\pi}_{\theta_{old}}}(\bar{s}_{\bar{t}(t,0)}) := \tilde{V}^{\bar{\pi}_{\theta_{old}}}(s_t)$ , which we find leads to more efficient and stable training compared to also estimating the value of applying the denoised action  $a_t^{k=1}$  (part of  $\bar{s}_{\bar{t}(t,0)}$ ) as shown in [Appendix D.2.](#page-20-0)

**260 261 262 263 264 265 266 267 268** Best Practices for **DPPO**. We summarize a number of best practices for **DPPO**; precise details are given in [Appendix B.](#page-18-0) (1) We achieve substantial efficiency gains by fine-tuning the last few steps of the DDPM, whilst in many cases obtaining performance comparable to fine-tuning all steps. (2) For additional efficiency gains, one may fine-tune the Denoising Diffusion Implicit Model (DDIM) [\(Song et al.,](#page-14-14) [2020a\)](#page-14-14) instead. (3) We propose clipping the diffusion noise schedule at a larger-thanstandard noise level to encourage exploration and training stability. (4) **DPPO** can be implemented with either Perceptron (MLP) or UNet [\(Ronneberger et al.,](#page-13-17) [2015\)](#page-13-17) as the policy head; while the former is simpler and achieves comparable performance to the latter, the latter provides flexibility in action chunk length which is useful in more challenging tasks.

<span id="page-4-1"></span>**269** <sup>3</sup>In practice, we use Generalized Advantage Estimation (GAE, [Schulman et al.](#page-14-6) [\(2015\)](#page-14-6)) that better balances variance and bias in estimating the advantage. We present the simpler form here.

#### <span id="page-5-1"></span>**270** 5 PERFORMANCE EVALUATION OF **DPPO**

**271**

**272 273 274 275 276 277** We study the performance of **DPPO** in popular RL and robotics benchmarking environments. Tables of all baselines and takeaways are given in [Appendix C.](#page-19-0) While our evaluations focus primarily on fine-tuning, we also present training-from-scratch results in [Appendix D.](#page-20-1) Wall-clock times are reported and discussed in [Appendix E;](#page-24-0) they are roughly comparable ( often faster) than other diffusion-based RL baselines, though can be up to  $2\times$  slower than other policy parameterizations. Full choices of training hyperparameters and additional training details are presented in [Appendix F.](#page-26-0)

**278 279 280 281** Environments: OpenAI Gym. We first consider three population OpenAI GYM locomotion benchmarks [\(Brockman et al.,](#page-10-13) [2016\)](#page-10-13) : {Hopper-v2, Walker2D-v2, HalfCheetah-v2}. All policies are pre-trained with the full medium-level datasets from D4RL [\(Fu et al.,](#page-11-13) [2020\)](#page-11-13) with state input and action chunk size  $T_a = 4$ . We use the original **dense** reward setup in fine-tuning.

**282 283 284 285 286 287 288** Environments: Robomimic. Next we consider four simulated robot manipulation tasks from the ROBOMIMIC benchmark [\(Mandlekar et al.,](#page-12-12) [2021\)](#page-12-12), {Lift, Can, Square, Transport}, ordered in increasing difficulty. These are more representative of real-world robotic tasks, and Square and Transport [\(Fig. 4\)](#page-5-0) are considered very challenging for RL training. Both **state** and **pixel** policy input are considered. State-based and pixel-based policies are pre-trained with Multi-Human demonstrations provided by ROBOMIMIC. We consider  $T_a = 4$  for Can, Lift, and Square, and  $T_a = 8$  for Transport. They are then fine-tuned with **sparse** reward upon task completion.

**289 290 291 292 293 294 295 296 Environments: Furniture-Bench & real furniture assembly.** Finally, we demonstrate solving longer-horizon, multi-stage robot manipulation tasks from the FURNITURE-BENCH [\(Heo et al.,](#page-11-8)  $2023$ ) benchmark. We consider three simulated furniture assembly tasks,  $\{\text{One-leg, Lamp},\}$ Round-table}, shown in [Fig. 4](#page-5-0) and described in detail in [Appendix F.8.](#page-30-0) We consider two levels of randomness over initial state distribution, Low and Med, defined by the benchmark. All policies are pre-trained with 50 human demonstrations collected in simulation and  $T_a = 8$ . They are then fine-tuned with sparse (indicator of task stage completion) reward. We also evaluate the zero-shot sim-to-real performance with One-leg.

<span id="page-5-0"></span>

Figure 4: Long-horizon robot manipulations tasks including (left) the bimanual Transport from ROBOMIMIC and (right) FURNITURE-BENCH tasks (full rollouts visualized in [Fig. 22\)](#page-31-0).

<span id="page-5-2"></span>5.1 COMPARISON TO DIFFUSION-BASED RL ALGORITHMS

We compare **DPPO** to an extensive list of RL methods for fine-tuning diffusion models. **DRWR** and **DAWR** are *our own, novel* baselines based on reward-weighted regression [\(Peters and Schaal,](#page-13-11) [2007\)](#page-13-11) and advantage-weighted regression [\(Peng et al.,](#page-13-10) [2019\)](#page-13-10). The remaining methods, **DIPO** [\(Yang et al.,](#page-14-4) [2023\)](#page-14-4), **IDQL** [\(Hansen-Estruch et al.,](#page-11-5) [2023\)](#page-11-5), **DQL** [\(Wang et al.,](#page-14-3) [2022\)](#page-14-3), and **QSM** [\(Psenka et al.,](#page-13-9) [2023\)](#page-13-9), are existing in the literature. We evaluate on the three OpenAI GYM tasks and the four ROBOMIMIC tasks with **state** input; see [Appendix F.3](#page-27-0) for further baseline and training details.

**312 313 314 315 316 317 318 319** Overall, **DPPO** performs consistently, exhibits great training stability, and enjoys strong fine-tuning performance across tasks. In the GYM tasks [\(Figure 5,](#page-6-0) top row), **IDQL** and **DAWR** exhibit competitive performance, while the other methods perform worse and train less stably. **DPPO** is the strongest performer in the ROBOMIMIC tasks [\(Figure 5,](#page-6-0) bottom row), especially in the challenging Transport tasks. Surprisingly, **DRWR** is a strong baseline in {Lift, Can, Square} but underperforms in Transport, while all other baselines fare worse still. We postulate that the other baselines, using off-policy updates, suffers from training instability in sparse-reward ROBOMIMIC tasks given continuous action space plus large action chunk sizes (see furtuer studies in [Appendix D.2\)](#page-20-0).

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<span id="page-5-3"></span>5.2 COMPARISON TO OTHER DEMO-AUGMENTED RL ALGORITHMS

**323** We compare **DPPO** with recently proposed RL methods for training robot policies (not necessarily diffusion-based) leveraging offline data, including **RLPD** [\(Ball et al.,](#page-10-4) [2023\)](#page-10-4), **Cal-QL** [\(Nakamoto](#page-12-3)

<span id="page-6-0"></span>

Figure 5: Comparing to other diffusion-based RL algorithms. Top row: GYM tasks [\(Brockman](#page-10-13) [et al.,](#page-10-13) [2016\)](#page-10-13) averaged over five seeds. Bottow row: ROBOMIMIC tasks [\(Mandlekar et al.,](#page-12-12) [2021\)](#page-12-12), averaged over three seeds, with state observation. We opt to not show the erratic **QSM** error bar in Hopper-v2. **DPPO** curves are slightly thicker for better visibility.

[et al.,](#page-12-3) [2024\)](#page-12-3), and **IBRL** [\(Hu et al.,](#page-11-7) [2023\)](#page-11-7). These methods add expert data in the replay buffer and performs off-policy updates (**IBRL** and **Cal-QL** also do pre-training), which significantly improves efficiency v.s. **DPPO** in HalfCheetah-v2. However, in sparse-reward manipulation tasks including Can and Square, **DPPO** achieves much better final performance than all three methods; **RLPD** and **Cal-QL** fail to learn at all and **IBRL** saturates at lower success levels. See [Appendix D.1,](#page-20-2) containing [Fig. 12,](#page-20-3) for further discussion.

### <span id="page-6-2"></span>5.3 COMPARISON TO OTHER POLICY PARAMETERIZATIONS

 We compare **DPPO** with popular RL policy parameterizations: unimodal Gaussian with diagonal covariance [\(Sutton et al.,](#page-14-1) [1999\)](#page-14-1) and Gaussian Mixture Model (GMM, [Bishop and Nasrabadi](#page-10-14) [\(2006\)](#page-10-14)), using either MLPs or Transformers [\(Vaswani et al.,](#page-14-15) [2017\)](#page-14-15), and also fine-tuned with the PPO objective. We compare these to **DPPO**-MLP and **DPPO**-UNet, which use either MLP or UNet as the network backbone. We evaluate on the four tasks from ROBOMIMIC (Lift, Can, Square, Transport) with both state and pixel input. With state input, **DPPO** pre-trains with 20 denoising steps and then fine-tunes the last 10. With pixel input, **DPPO** pre-trains with 100 denoising steps and then fine-tunes 5 DDIM steps.

<span id="page-6-1"></span>

Figure 6: Comparing to other policy parameterizations in the more challenging Square and Transport tasks from ROBOMIMIC, with **state** (left) or **pixel** (right) observation. Results are averaged over three seeds.

 [Fig. 6](#page-6-1) display results for the more challenging Square and Transport — we defer the results in Lift and Can to [Fig. 20.](#page-23-0) With state input, **DPPO** outperforms Gaussian and GMM policies, with faster convergence to  $\sim$ 100% success rate in Lift and Can, and greater final performance on Square and the challenging  $Transport$ , where it reaches  $> 90\%$ . UNet and MLP variants perform similarly, with the latter training somewhat more rapidly. With **pixel** inputs, we use a Vision-Transformer-based (ViT) image encoder introduced in [Hu et al.](#page-11-7) [\(2023\)](#page-11-7) and an MLP head

**378 379 380 381 382 383** and compare the resulting variants **DPPO**-ViT-MLP and Gaussian-ViT-MLP (we omit GMM due to poor performance in state-based training). While the two are comparable on Lift and Can, **DPPO** trains more quickly and to higher accuracy on Square, and *drastically outperforms* on Transport, whereas Gaussian does not improve from its  $0\%$  pre-trained success rate. To our knowledge, **DPPO** is *the first RL algorithm* to solve **Transport** from either state or pixel input to high (>50%) success rates.

<span id="page-7-0"></span>

<span id="page-7-1"></span>

**400 401** Figure 7: (Top) DPPO vs. Gaussian-MLP baseline in simulated FURNITURE-BENCH tasks. Results are averaged over three seeds. (Bottom) Sim-to-real transfer results in  $One-Leg$ .

**403 404 405 406 407 408 409** Here we evaluate **DPPO** on the long-horizon manipulation tasks from FURNITURE-BENCH [\(Heo](#page-11-8) [et al.,](#page-11-8) [2023\)](#page-11-8). We compare **DPPO** to Gaussian-MLP, the overall most effective baseline from [Sec](#page-6-2)[tion 5.3.](#page-6-2) [Fig. 7](#page-7-1) (top row) shows the evaluation success rate over fine-tuning iterations. **DPPO** exhibits strong training stability and improves policy performance in all six settings. Gaussian-MLP collapses to zero success rate in all three tasks with Med randomness (except for one seed in Lamp) and Round-table with Low randomness. Note that we are only using 50 human demonstrations for pre-training; we expect **DPPO** can leverage additional human data (better state space coverage) to further improve in Med, which is corroborated by ablation studies in [Appendix D.3.](#page-22-0)

**410 411 412 413 414 415 416 417 418 419 420 421 422** Sim-to-real transfer. We evaluate **DPPO** and Gaussian policies trained in the simulated One-leg task on physical hardware zero-shot (i.e., no real data fine-tuning / co-training) over 20 trials. Please see additional simulation training and hardware details in [Appendix F.8.](#page-30-0) [Fig. 7](#page-7-1) (bottom row) shows simulated and hardware success rates after pre-training and fine-tuning. Notably, **DPPO** improves the real-world performance to 80% (16 out of 20 trials). Though the Gaussian policy achieves a high success rate in simulation after fine-tuning (88%), it fails entirely on hardware (0%). Supplemental video suggests it exhibits volatile and jittery behavior. For stronger comparison, we also fine-tune the Gaussian policy with an auxiliary behavior-cloning loss [\(Torne et al.,](#page-14-7) [2024\)](#page-14-7) such that the fine-tuned policy is encouraged to stay close to the base policy. However, this limits finetuning and only leads to a 53% success rate in simulation and 50% in reality. *Qualitatively*, we find fine-tuned policies to be more robust and exhibit more corrective behaviors than pre-trained-only policies, especially during the insertion stage of the task; such behaviors are visualized in [Fig. 2](#page-2-3) and [Fig. 23](#page-33-0) shows representative rollouts on hardware.

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### <span id="page-7-2"></span>5.5 SUMMARY OF ABLATION FINDINGS

**425 426 427 428 429 430 431** Our ablation studies (c.f. [Appendix D.2\)](#page-20-0) find that: (1) for challenging tasks, using a value estimator which depends on environment state but is *independent of denoised action* is crucial for performance; we conjecture that this is related to the high stochasticity of Diffusion Policy; (2) there is a sweet spot for clipping the denoising noise level for **DPPO** exploration, trading off between too little exploration and too much action noise; (3) **DPPO** is resilient to fine-tuning fewer-than- $K$  denoising steps, yielding improved runtime and comparable performance; (4) **DPPO** yields improvements over Gaussian-MLP baselines for varying levels of expert demonstration data, and achieves comparable final performance and sample efficiency when training from scratch in GYM environments.

#### **432** 6 UNDERSTANDING THE PERFORMANCE OF **DPPO**

**433 434 435**

<span id="page-8-2"></span>We study the factors contributing to **DPPO**'s improvements in performance over the popular Gaussian and GMM methods introduced in [Section 5.3.](#page-6-2) We use the Avoid environment from D3IL benchmark [\(Jia et al.,](#page-12-13) [2024\)](#page-12-13), where a robot arm needs to reach the other side of the table while avoiding an array of obstacles [\(Fig. 8,](#page-8-0) top-left). The action space is the 2D target location of the end-effector. D3IL provides expert demonstrations that covers different possible paths to the goal line — we consider three subsets of the demonstrations, M1, M2, and M3 in [Fig. 8,](#page-8-0) each with two distinct modes; with only two modes in each setting, Gaussian (with exploration noise)<sup>[4](#page-8-1)</sup> and GMM can fit the expert data distribution reasonably well, allowing fair comparisons in fine-tuning.

We pre-train MLP-based Diffusion, Gaussian, and GMM policies ( $T_a = 4$  unless noted) with the demonstrations. For fine-tuning, we assign (sparse) reward when the robot reaches the goal line from the topmost mode. Gaussian and GMM policies are also fine-tuned with the PPO objective.

<span id="page-8-0"></span>

Figure 8: (Left) We use the Avoid environment from [Jia et al.](#page-12-13) [\(2024\)](#page-12-13) to visualize the **DPPO**'s exploration tendencies. The task is to reach the green goal line from the topmost mode. (Right) Structured exploration. We show sampled trajectories at the *first iteration of fine-tuning* for DPPO, Gaussian, and GMM after pre-training on three sets of expert demonstrations, M1, M2, and M3.

**Benefit 1: Structured, on-manifold exploration.** [Fig. 8](#page-8-0) (right) shows the sampled trajectories (with exploration noise) from **DPPO**, Gaussian, and GMM during the first iteration of fine-tuning. **DPPO** explores in wide coverage around the expert data manifold, whereas Gaussian generates less structured exploration noise (especially in M2) and GMM exhibits narrower coverage. Moreover, the combination of diffusion parameterization with the denoising of *action chunks* means that policy stochasticity in **DPPO** is structured in both action dimension and time horizon.

**469 470 471 472 473 474 475 476 Benefit 2: Training stability from multi-step denoising process.** In [Fig. 9](#page-9-0) (left), we run finetuning after pre-training with M2 and *attempt to de-stabilize fine-tuning* by gradually adding noise to the action during the fine-tuning process (see [Appendix F.9](#page-34-0) for details). We find that Gaussian and GMM's performance both collapse, while with **DPPO**, the performance is robust to the noise if at least four denoising steps are used. This property also allows **DPPO** to apply significant noise to the sampled actions, simulating an imperfect low-level controller to facilitate sim-to-real transfer in [Section 5.4.](#page-7-0) In [Fig. 9](#page-9-0) (right), we also find **DPPO** enjoys greater training stability when fine-tuning long action chunks, e.g., up to  $T_a = 16$ , while Gaussian and GMM can fail to improve at all.

**477 478 479 480** [Fig. 10](#page-9-1) visualizes how **DPPO** affects the multi-step denoising process. Over fine-tuning iterations, the action distribution gradually converges through the denoising steps — the iterative refinement is largely preserved, as opposed to, e.g., "collapsing" to the optimal actions at the first fine-tuned denoising step or the final one. We postulate this contributes to the training stability of **DPPO**.

**481 482 483 484 485** Benefit 3: Robust and generalizable fine-tuned policy. **DPPO** also generates final policies robust to perturbations in dynamics and the initial state distribution. In [Fig. 11,](#page-9-2) we again add noise to the actions sampled from the fine-tuned policy (no noise applied during training) and find that **DPPO** policy exhibits strong robustness to the noise compared to the Gaussian policy. **DPPO** policy

<span id="page-8-1"></span><sup>&</sup>lt;sup>4</sup>Without noise, Gaussian policy is fully deterministic and cannot capture the two modes.

<span id="page-9-0"></span>

Figure 9: **Training stability.** Fine-tuning performance (averaged over five seeds, standard deviation not shown) after pre-training with M2. (Left) Noise is injected into the applied actions after a few training iterations. (Right) The action chunk size  $T_a$  is varied.

<span id="page-9-1"></span>

Figure 10: Preserving the iterative refinement. The 2D actions from 50 trajectories at the branching point *through fine-tuning* iterations after pre-training with M2. For **DPPO**, we also visualize the action distribution through the final denoising steps at each fine-tuning iteration.

also converges to the (near-)optimal path from a larger distribution of initial states. This finding echoes theoretical guarantees that Diffusion Policy, capable of representing complex multi-modal data distribution, can effectively deconvolve noise from noisy states [\(Block et al.,](#page-10-15) [2024\)](#page-10-15), a property used in [Chen et al.](#page-10-9) [\(2024\)](#page-10-9) to stabilize long-horizon video generation.

<span id="page-9-2"></span>**517 518**

reverse [4, 1, 3, 0]



**DPPO** 

Gaussian

**520**

**521 522** [1, 3, 0, 4] shift\_left

**523** swap [0, 1, 4, 3]



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# <span id="page-9-3"></span>7 CONCLUSION AND FUTURE WORK

**Final trajectories** 

**530 531 532 533 534 535 536 537 538 539** We believe **DPPO** will become an important component in the pre-training-plus-fine-tuning pipeline for training general-purpose real-world robotic policies. To this end, we hope in future work to further showcase the promise of **DPPO** for simulation-to-real transfer [\(Chen et al.,](#page-10-16) [2023;](#page-10-16) [Liang](#page-12-14) [et al.,](#page-12-14) [2020;](#page-12-14) [Ren et al.,](#page-13-18) [2023;](#page-13-18) [Chi et al.,](#page-10-17) [2024a\)](#page-10-17) in which we fine-tune a vision-based policy that has been pre-trained on a variety of diverse tasks. We expect this pre-training to provide a large and diverse expert data manifold, of which, as we have shown in [Section 6,](#page-8-2) **DPPO** is well-suited to take advantage for better exploration during fine-tuning. We are also excited to understand how **DPPO** can fit together with other decision-making tools such as model-based planning [\(Janner et al.,](#page-12-4) [2022;](#page-12-4) [Ding et al.,](#page-11-14) [2024\)](#page-11-14) and decision-making aided by video prediction [\(Chen et al.,](#page-10-9) [2024\)](#page-10-9); these tools may help address the main limitation of **DPPO** — its lower sample efficiency than off-policy methods — and unlocking performing practical RL in physical hardware.

Figure 11: Policy robustness *after fine-tuning*. Green dot / box indicates the initial state region.

w/ action perturbation

w/ OOD initialization



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# <span id="page-17-2"></span><span id="page-17-0"></span>A EXTENDED RELATED WORK

A.1 RL TRAINING OF ROBOT POLICIES WITH OFFLINE DATA

**933 934** Here, we discuss related work in training robot policies using RL augmented with offline data to help RL better explore online in sparse reward settings.

**935 936 937 938 939 940 941 942 943 944 945 946** One simple form is to use offline data to pre-train the policy, typically using behavior cloning, and then fine-tune the policy online. This is the approach that **DPPO** takes. Often, a regularization loss is applied to constrain the fine-tuned policy to stay close to the base policy, leading to natural fine-tuned behavior and often better learning [\(Rajeswaran et al.,](#page-13-14) [2017;](#page-13-14) [Zhu et al.,](#page-15-1) [2019;](#page-15-1) [Torne et al.,](#page-14-7) [2024\)](#page-14-7). **DPPO** does not apply regularization at fine-tuning as we find the on-manifold exploration helps **DPPO** maintain natural behavior after fine-tuning [Section 5.4.](#page-7-0) Another popular approach is to learn a *residual* policy with RL on top of the frozen base policy [\(Alakuijala et al.,](#page-10-18) [2021;](#page-10-18) [Haldar](#page-11-15) [et al.,](#page-11-15) [2023\)](#page-11-15). A closer work to ours is [Ankile et al.](#page-10-19) [\(2024b\)](#page-10-19), which trains a one-step residual nondiffusion policy with on-policy RL on top of a pre-trained chunked diffusion policy. This approach has the benefit of being fully closed-loop but lacks the structured on-manifold exploration of **DPPO**. Another hybrid approach is from [Hu et al.](#page-11-7) [\(2023\)](#page-11-7), which uses pre-trained and fine-tuned policies to sample online experiences.

**947 948 949 950 951 952 953 954 955** Another popular line of work, instead of training a base policy using offline data, directly adds the data in the replay buffer for online, off-policy learning in a single stage [\(Hester et al.,](#page-11-16) [2018;](#page-11-16) [Vecerik et al.,](#page-14-16) [2017;](#page-14-16) [Nair et al.,](#page-12-15) [2020\)](#page-12-15). One recent approach from [Ball et al.](#page-10-4) [\(2023\)](#page-10-4), **RLPD**, further improves sample efficiency from previous off-policy methods incorporating, e.g., critic ensembling. [Luo et al.](#page-12-16) [\(2024\)](#page-12-16) demonstrates **RLPD** solving real-world manipulation tasks (although generally less challenging than ones solved by **DPPO**). Other approaches including **Cal-QL** build on offline RL to learn from offline data and then switch to online RL [\(Nakamoto et al.,](#page-12-3) [2024;](#page-12-3) [Hansen-Estruch](#page-11-5) [et al.,](#page-11-5) [2023\)](#page-11-5). **IBRL** from [Hu et al.](#page-11-7) [\(2023\)](#page-11-7) pre-trains the base policy and samples offline data in fine-tuning.

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### <span id="page-17-1"></span>A.2 DIFFUSION-BASED RL METHODS

**958 959 960 961** This section discusses related methods that directly train or improve diffusion-based policies with RL methods. The baselines to which we compare in [Section 5.1](#page-5-2) are discussed below as well, and are highlighted in their corresponding colors. We also refer the readers to [Zhu et al.](#page-15-2) [\(2023\)](#page-15-2) for an extensive survey on diffusion models for RL.

**962 963 964 965 966 967 968 969 970 971** Most previous works have focused on the **offline** setting with a static dataset. One line of work focuses on state trajectory planning and *guiding* the denoising sampling process such that the sampled actions satisfy some desired objectives. [Janner et al.](#page-12-4) [\(2022\)](#page-12-4) applies classifier guidance that generates trajectories with higher predicted rewards. [Ajay et al.](#page-10-5) [\(2023\)](#page-10-5) introduces classifier-free guidance that avoids learning the value of noisy states. There is another line of work that uses diffusion models as an action policy (instead of state planner) and generally applies Q-learning. **DQL** [\(Wang et al.,](#page-14-3) [2022\)](#page-14-3) introduces Diffusion Q-Learning that learns a state-action critic for the final denoised actions and backpropagates the gradient from the critic through the entire Diffusion Policy (actor) denoising chain, akin to the usual Q-learning. **IDQL** [\(Hansen-Estruch et al.,](#page-11-5) [2023\)](#page-11-5), or Implicit Diffusion Q-learning, proposes learning the critic to select the actions at inference time for either training or evaluation while fitting the actor to all sampled actions. [Kang et al.](#page-12-2) [\(2024\)](#page-12-2) instead proposes using

**972 973 974 975** the critic to re-weight the sampled actions for updating the actor itself, similar to weighted regression baselines **DAWR** and **DRWR** introduced in our work. [Goo and Niekum](#page-11-17) [\(2022\)](#page-11-17) similarly extracts the policy in the spirit of AWR [\(Peng et al.,](#page-13-10) [2019\)](#page-13-10). [Chen et al.](#page-10-10) [\(2022a\)](#page-10-10) trains the critic using value iteration instead based on samples from the actor.

**976 977 978 979 980 981 982 983 984** We note that methods like **DQL** and **IDQL** can also be applied in the **online** setting. A small amount of work also focuses entirely on the online setting. **DIPO** [\(Yang et al.,](#page-14-4) [2023\)](#page-14-4) differs from **DQL** and related work in that it uses the critic to update the sampled actions ("action gradient") instead of the actor — the actor is then fitted with updated actions from the replay buffer. **QSM**, or Q-Score Matching [\(Psenka et al.,](#page-13-9) [2023\)](#page-13-9), suggests that optimizing the likelihood of the entire chain of denoised actions can be inefficient (contrary to our findings in the fine-tuning setting) and instead proposes learning the optimal policy by iteratively aligning the gradient of the actor (i.e., score) with the action gradient of the critic. [Rigter et al.](#page-13-19) [\(2023\)](#page-13-19) proposes learning a diffusion dynamic model to generate synthetic trajectories for online training of a non-diffusion RL policy.

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# <span id="page-18-0"></span>B BEST PRACTICES FOR **DPPO**

**Fine-tune only the last few denoising steps.** Diffusion Policy often uses up to  $K = 100$  denoising steps with DDPM to better capture the complex data distribution of expert demonstrations. With **DPPO**, we can choose to fine-tune only a subset of the denoising steps instead, e.g., the last  $K'$ steps. In [Section 4.1](#page-4-3) and [Section 6](#page-8-2) we find this speeds up **DPPO** training and reduces GPU memory usage without sacrificing the asymptotic performance. Instead of fine-tuning the pre-trained model weights  $\theta$ , we make a copy  $\theta_{FT}$  —  $\theta$  is frozen and used for the early denoising steps, while  $\theta_{FT}$  is used for the last K′ steps and updated with **DPPO**.

**Fine-tune DDIM.** Instead of fine-tuning all  $K$  or the last few steps of the DDPM, one can also apply Denoising Diffusion Implicit Model (DDIM) [\(Song et al.,](#page-14-14) [2020a\)](#page-14-14) during fine-tuning, which greatly reduces the number of sampling steps  $K^{\text{DDIM}} \ll K$ , e.g., as few as 5 steps, and thus potentially improves **DPPO** efficiency as fewer steps are fine-tuned.

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<span id="page-18-1"></span> $x^{k-1} \sim p_{\theta}^{\text{DDIM}}(x^{k-1}|x^k) := \mathcal{N}(x^{k-1}; \mu^{\text{DDIM}}(x^k, \varepsilon_{\theta}(x^k, k)), \eta \sigma_k^2 \mathbf{I}), \quad k = K^{\text{DDIM}}, ..., 0.$  (B.1)

**1003 1004 1005 1006 1007 1008** Although DDIM is typically used as a deterministic sampler by setting  $\eta = 0$  in [\(B.1\)](#page-18-1), we can use  $\eta > 0$  for fine-tuning that provides exploration noise and avoids calculating Gaussian likelihood with a Dirac distribution. In practice, we set  $\eta = 1$  for training (equivalent to applying DDPM [Song et al.](#page-14-14) [\(2020a\)](#page-14-14)) and then  $\eta = 0$  for evaluation. *We reserve DDIM sampling for our pixel-based experiments and long-horizon furniture assembly tasks, where the efficiency improvements are much desired.*

**1010 1011 1012 1013 1014 1015 1016 Diffusion noise scheduling.** We use the cosine schedule for  $\sigma_k$  introduced in [Nichol and Dhariwal](#page-13-16) [\(2021\)](#page-13-16), which was originally annealed to a small value on the order of  $1E-4$  at  $k = 0$ . In **DPPO**, the value of  $\sigma_k$  also translates to the exploration noise that is crucial to training efficiency. Empirically, we find that clipping  $\sigma_k$  to a higher minimum value (denoted  $\sigma_{min}^{exp}$ , e.g.,  $0.01 - 0.1$ ) when sampling actions helps exploration (see sensitivity analysis in [Appendix D.2\)](#page-20-0). Additionally we clip  $\sigma_k$  to be at least 0.1 (denoted  $\sigma_{\min}^{\text{prob}}$ ) when evaluating the Gaussian likelihood  $\log \bar{\pi}_{\theta}(\bar{a}_{\bar{t}}|\bar{s}_{\bar{t}})$ , which improves training stability by avoiding large magnitude.

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**1018 1019 1020 1021 1022 1023** Network architecture. We study both Multi-layer Perceptron (MLP) and UNet [\(Ronneberger](#page-13-17) [et al.,](#page-13-17) [2015\)](#page-13-17) as the policy heads in Diffusion Policy. An MLP offers simpler setup and we find it generally fine-tunes more stably with **DPPO**. Moreover, since the UNet applies convolution to the denoised action, we can pre-train and fine-tune with different action chunk size  $T_a$  (the number of environment timesteps that the policy predicts future actions with), e.g., 16 and 8. We find that **DPPO** benefits from pre-training with larger  $T_a$  (better prediction) and fine-tuning with smaller  $T_a$ (more amenable to policy gradient)<sup>[5](#page-18-2)</sup>.

<span id="page-18-2"></span><sup>&</sup>lt;sup>5</sup>With fully-connected layers in MLP, empirically we find that using different chunk sizes for pre-training and fine-tuning with MLP leads to training instability.

# <span id="page-19-0"></span>C SUMMARY OF ALL BASELINES



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# Comparison to Other Diffusion RL Methods



## Comparison to Other Demonstration-Augmented RL Methods



## Comparison to Other Policy Parameterization/Architecture



#### <span id="page-20-1"></span>**1080 1081** D ADDITIONAL EXPERIMENTAL RESULTS

#### <span id="page-20-2"></span>**1082 1083** D.1 COMPARING TO OTHER DEMO-AUGMENTED RL METHODS

**1084 1085 1086 1087 1088 1089 1090 1091 1092** In [Section 5.2](#page-5-3) we discuss that **DPPO** leads to superior final performance in manipulation tasks compared to other RL methods leveraging offline data, including **RLPD** [\(Ball et al.,](#page-10-4) [2023\)](#page-10-4), **Cal-QL** [\(Nakamoto et al.,](#page-12-3) [2024\)](#page-12-3), and **IBRL** [\(Hu et al.,](#page-11-7) [2023\)](#page-11-7). The full results are shown in [Fig. 12](#page-20-3) below. We use action chunk size  $T_a = 1$  following the setup from these methods (DPPO may benefit from longer chunk size, albeit). The three baselines all achieve high reward in HalfCheetah-v2 with much higher sample efficiency thanks to performing off-policy updates. However, in sparsereward ROBOMIMIC tasks including Can and Square, **DPPO** outperforms all three significantly and achieves ∼100% final success rates. **RLPD** and **Cal-QL** fail to achieve any success (0%) during evaluation, while **IBRL** saturates at lower success levels.

**1093 1094 1095 1096 1097** Our results with **RLPD** in Can and Square corroborates those from [Hu et al.](#page-11-7) [\(2023\)](#page-11-7). **IBRL** is shown to achieve high success rates ( $> 90\%$ ) in both tasks in [Hu et al.](#page-11-7) [\(2023\)](#page-11-7); we hypothesize here it underperforms possibly due to (1) the noisier expert data (Multi-Human dataset from ROBOMIMIC) affects gradient update with mixed batches of online and offline data, and (2) our setup not using any history observation unlike [Hu et al.](#page-11-7) [\(2023\)](#page-11-7) stacking three observations.

**1098 1099 1100 1101** Lastly, we note that although **DPPO** uses more environment steps, it runs significantly faster than the baselines as it leverages sampling from highly parallelized environments (40 in HalfCheetah-v2) and 50 in Can and Square), while off-policy methods may fail to fully leverage such parallelized setup as the policy is updated less often and the performance may be affected.

<span id="page-20-3"></span>

**1115** Figure 12: Comparing to other demo-augmented RL methods. Results are averaged over five seeds in HalfCheetah-v2 and three seeds in Can and Square.

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### <span id="page-20-0"></span>D.2 ABLATION STUDIES ON DESIGN DECISIONS IN **DPPO**

**1119 1120 1121 1. Choice of advantage estimator.** In [Section 4.1](#page-4-3) we demonstrate how to efficiently estimate the advantage used in PPO updates by learning  $\tilde{V}(s_t)$  that only depends on the environment state; the advantage used in **DPPO** is formally

 $\hat{A} = \gamma_{\text{\tiny DENOISE}}^k(\bar{r}(\bar{s}_{\bar{t}},\bar{a}_{\bar{t}}) - \tilde{V}(s_t)).$ 

**1124 1125 1126 1127 1128** We now compare this choice with learning the value of the full state  $\bar{s}_{\bar{t}(t,0)}$  that includes environment state  $s_t$  and denoised action  $a_t^{k=1}$ . We additionally compare with the state-action Q-function estimator used in [Psenka et al.](#page-13-9)  $(2023)^6$  $(2023)^6$  $(2023)^6$ ,  $\tilde{Q}(s_t, a_t^{k=0})$ , that does not directly use the rollout reward  $\bar{r}$ in the advantage.

**1129 1130 1131** [Fig. 13](#page-21-0) shows the fine-tuning results in  $Hopper-v2$  and  $HalfChecketh-v2$  from GYM, and Can and Square from ROBOMIMIC. On the simpler  $Hopper-v2$ , we observe that the two baselines, both estimating the value of some action, achieves higher reward during fine-tuning than

<span id="page-20-4"></span>**<sup>1132</sup> 1133** <sup>6</sup>[Psenka et al.](#page-13-9) [\(2023\)](#page-13-9) applies off-policy training with double Q-learning (according to its open-source implementation) and policy gradient over the denoising steps. Note that this is a baseline in [Psenka et al.](#page-13-9) [\(2023\)](#page-13-9) that is conjectured to be inefficient. We follow the same except for applying on-policy PPO updates.

 **DPPO**'s choice. However, in the more challenging tasks, the environment-state-only advantage used in **DPPO** consistently leads to the most improved performance. We believe estimating the accurate value of applying a continuous and high-dimensional action can be challenging, and this is exacerbated by the high stochasticity of diffusion-based policies and the action chunk size. The results here corroborate the findings in [Section 5.1](#page-5-2) that off-policy Q-learning methods can perform well in  $Hopper-v2$  and  $Walker2D-v2$ , but exhibit training instability in manipulation tasks from ROBOMIMIC.

<span id="page-21-0"></span>

 Figure 13: Choice of advantage estimator. Results are averaged over five seeds in  $Hopper-v2$ and HalfCheetah-v2 and three seeds in Can and Square.

 **Denoising discount factor.** We further examine how  $\gamma_{\text{DENOISE}}$  in the **DPPO** advantage estimator affects fine-tuning. Using a smaller value (i.e., more discount) has the effect of downweighting the contribution of earlier denoising steps in the policy gradient. [Fig. 14](#page-21-1) shows the fine-tuning results in the same four tasks with varying  $\gamma_{\text{DENOISE}} \in [0.5, 0.8, 0.9, 1]$ . We find in Hopper-v2 and HalfCheetah-v2  $\gamma_{\text{DENOISE}} = 0.8$  leads to better efficiency while smaller  $\gamma_{\text{DENOISE}} = 0.5$  slows training. The value does not affect training noticeably in Can. In Square the smaller  $\gamma_{\text{DENOISE}} =$ .5 works slightly better. Overall in manipulation tasks, **DPPO** training seems relatively robust to this choice.

<span id="page-21-1"></span>

 Figure 14: Choice of denoising discount factor. Results are averaged over five seeds in Hopper-v2 and HalfCheetah-v2 and three seeds in Can and Square.

 2. Choice of diffusion noise schedule. As introduced in [Section 4.1,](#page-4-3) we find it helpful to clip the diffusion noise  $\sigma_k$  to a higher minimum value  $\sigma_{min}^{exp}$  to ensure sufficient exploration. In [Figure 15,](#page-22-1) we perform analysis on varying  $\sigma_{\min}^{\exp} \in \{.001, .01, .1, .2\}$  (keeping  $\sigma_{\min}^{\text{prob}} = .1$  to evaluate likelihoods). Although in Can the choice of  $\sigma_{min}^{exp}$  does not affect the fine-tuning performance, in Square a higher  $\sigma_{min}^{exp} = 0.1$  is required to prevent the policy from collapsing. We conjecture that this is due to limited exploration causing policy over-optimizing the collected samples that exhibit limited stateaction coverage. We also visualize the trajectories at the beginning of fine-tuning in Avoid task from D3IL. With higher  $\sigma_{min}^{exp}$ , the trajectories still remain near the two modes of the pre-training data but exhibit a higher coverage in the state space — we believe this additional coverage leads to better exploration. Anecdotally, we find terminating the denoising process early can also provide exploration noise and lead to comparable results, but it requires a more involved implementation around the denoising MDP.

 3. Choice of the number of fine-tuned denoising steps. We examine how the number of finetuned denoising steps in **DPPO**, K′ , affects the fine-tune performance and wall-clock time in [Fig. 16.](#page-22-2) We show the curves of individual runs (three for each  $K<sup>7</sup>$ ) instead of the average as their wall-clock times (X-axis) are not perfectly aligned. Generally, fine-tuning too few denoising steps (e.g., 3) can lead to subpar asymptotic performance and slower convergence especially in Can. Fine-tuning 10 steps leads to the overall best efficiency. Similar results are also shown in [Fig. 19](#page-23-3) with Avoid task. Lastly, we note that the GPU memory usage scales linearly with  $K'$ .

<span id="page-22-1"></span>

 Figure 15: Choice of minimum diffusion noise. Results are averaged over three seeds. Note in Left, with higher minimum noise level, the sampled trajectories exhibit wider coverage at the two modes but still maintain the overall structure.

 We note that the findings here mostly correlate with those from varying the denoising discount factor,  $\gamma_{\text{DENOISE}}$ . Discounting the earlier denoising steps in the policy gradient can be considered as a soft version of hard limiting the number of fine-tuned denoising steps. Depending on the amount of fine-tuning needed from the pre-trained action distribution, one can flexibly adjust  $\gamma_{\text{DENOISE}}$  and  $K'$  to achieve the best efficiency.

<span id="page-22-2"></span>

Figure 16: Choice of number of fine-tuned denoising steps,  $K'$ . Individual runs are shown. The curves are smoothed using a Savitzky–Golay filter.

### <span id="page-22-0"></span>D.3 EFFECT OF EXPERT DATA

 We investigate the effect of the amount of pre-training expert data on fine-tuning performance. In [Fig. 17](#page-22-3) we compare **DPPO** and Gaussian in Hopper-v2, Square, and One-leg task from FUR-NITURE-BENCH, using varying numbers of expert data (episodes) denoted in the figure. Overall, we find **DPPO** can better leverage the pre-training data and fine-tune to high success rates. Notably, **DPPO** obtains non-trivial performance (60% success rate) on One-leg from only 10 episode of demonstrations.

<span id="page-22-3"></span>

 Figure 17: Varying the number of expert demonstrations. The numbers in the legends indicates the number of episodes used in pre-training.

 Training from scratch. In [Fig. 18](#page-23-4) we compare **DPPO** (10 denoising steps) and Gaussian *trained from scratch* (no pre-training on expert data) in the three OpenAI GYM tasks. As using larger action chunk sizes  $T_a$  leads to poor from-scratch training shown in [Fig. 17,](#page-22-3) we focus on single-action chunks  $T_a = 1$  as is typical in RL benchmarking. Though we find Gaussian trains faster than **DPPO** (expected since **DPPO** solves an MDP with longer effective horizon), **DPPO** still attains reasonable final performance. However, due to the multi-step (10) denoising sampling, **DPPO** takes about  $6 \times$ wall-clock time compared to Gaussian. We hope that future work will explore how to design the

<span id="page-23-4"></span>

 training curriculum of denoising steps for the best balance of training performance and wall-clock efficiency.



Gaussian-MLP,  $T_a = 1$ 

### <span id="page-23-1"></span>D.4 COMPARING TO OTHER POLICY PARAMETERIZATIONS IN AVOID

DPPO-MLP,  $T_a=1$ 

 

 [Figure 19](#page-23-3) depicts the performance of various parameterizations of **DPPO** (with differing numbers of fine-tuned denoising steps,  $K'$ ) to Gaussian and GMM baselines. We study the Avoid task from D3IL, after pre-training with the data from M1, M2, M3 as described in [Section 6.](#page-8-2) We find that, for  $K' \in \{15, 20\}$ , **DPPO** attains the highest performance of all methods and trains the quickest in terms of environment steps; on M1, M2, it appears to attain the greatest terminal performance as well.  $K' = 10$  appears slightly better than, but roughly comparable to, the Gaussian baseline, with GMM and  $K' < 10$  performing less strongly.

<span id="page-23-3"></span>

 Figure 19: Fine-tuning performance (averaged over five seeds, standard deviation not shown) after pre-training with M1, M2, and M3 in **Avoid task from D3IL. DPPO**  $(K = 20)$ , Gaussian, and GMM policies are compared. We also sweep the number of fine-tuned denoising steps K′ in **DPPO**.

### <span id="page-23-2"></span>D.5 COMPARING TO OTHER POLICY PARAMETERIZATIONS IN THE EASIER TASKS FROM ROBOMIMIC

 [Figure 20](#page-23-0) compares the performance of **DPPO** to Gaussian and GMM baslines, across a variety of architectures, and with **state** and **pixel** inputs, in  $L$ ift and Can environments in the ROBOMIMIC suite. Compared to the Square and Transport (results shown in [Section 5\)](#page-5-1), these environments are considered to be "easier", and this is reflected in the greater performance of **DPPO** and Gaussian baselines (GMM still exhibits subpar performance). Nonetheless, **DPPO** still achieves similar or even better sample efficiency compared to Gaussian baseline.

<span id="page-23-0"></span>

Figure 20: **Comparing to other policy parameterizations** in the easier Lift and Can tasks from ROBOMIMIC, with state (left) or pixel (right) observation. Results are averaged over three seeds.

#### <span id="page-24-1"></span>**1296 1297** D.6 COMPARING TO POLICY GRADIENT USING EXACT LIKELIHOOD OF DIFFUSION POLICY

**1298 1299 1300 1301 1302 1303 1304** Here we experiment another novel method (which, to our knowledge, has not been explicitly studied in any previous work) for performing policy gradient with diffusion-based policies. Although diffusion model does not directly model the action likelihood,  $p_{\theta}(a_0|s)$ , there have been ways to *estimate* the value, e.g., by solving the probability flow ODE that implements DDPM [\(Song et al.,](#page-14-17) [2020b\)](#page-14-17). We refer the readers to Appendix. D in [Song et al.](#page-14-17) [\(2020b\)](#page-14-17) for a comprehensive exposition. We follow the official open-source code from Song et al.<sup>[7](#page-24-2)</sup>, and implement policy gradient (single-level MDP) that uses the exact action likelihood  $\pi_{\theta}(a_t|s_t)$ .

**1305 1306 1307 1308 1309 1310 1311** [Fig. 21](#page-24-3) shows the comparison between **DPPO** and diffusion policy gradient using exact likelihood estimate. Exact policy gradient improves the base policy in  $Hopper-v2$  but does not outperform **DPPO**. It also requires more runtime and GPU memory as it backpropagates through the ODE. In the more challenging Can its success rate drops to zero. Moreover, policy gradient with exact likelihood does not offer the flexibility of fine-tuning fewer-than-K denoising steps or discounting the early denoising steps that **DPPO** offers, which have shown in [Appendix D.2](#page-20-0) to often improve fine-tuning efficiency.

<span id="page-24-3"></span>

Figure 21: Comparing to diffusion policy gradient with exact action likelihood. Results are averaged over five seeds in  $Hopper-v2$  and  $HalfChecketh-v2$ , and three seeds in Can.

**1323 1324**

# <span id="page-24-0"></span>E REPORTING OF WALL-CLOCK TIMES

**1325 1326**

**1327 1328 1329 1330 1331 1332 1333 1334** Comparing to other diffusion-based RL algorithms [Section 5.1.](#page-5-2) [Table 1](#page-24-4) and [Table 2](#page-25-0) shows the the wall-clock time used in each OpenAI GYM task and ROBOMIMIC task. In GYM tasks, on average **DPPO** trains 41%, 37%, and 12% faster than **DAWR**, **DIPO**, and **DQL**, respectively, which all require a significant amount of gradient updates per sample to train stably. **QSM**, **DRWR**, and **IDQL** trains 43%, 33%, and 7% faster than **DPPO**, respectively. ROBOMIMIC tasks are more expensive to simulate, especially with Transport task, and thus the wall-clock difference is smaller among the different methods. All methods use comparable time except for **DIPO** that uses slightly more on average.

<span id="page-24-4"></span>

**1345 1346 1347 1348** Table 1: Wall-clock time in seconds for a single training iteration in OpenAI GYM tasks when comparing diffusion-based RL algorithms. Each iteration involves 500 environment timesteps in each of the 40 parallelized environments running on 40 CPU threads and a NVIDIA RTX 2080 GPU (20000 steps total).

<span id="page-24-2"></span><sup>7</sup> [https://github.com/yang-song/score\\_sde\\_pytorch](https://github.com/yang-song/score_sde_pytorch)

<span id="page-25-0"></span>

| Method      | Task |      |        |           |
|-------------|------|------|--------|-----------|
|             | Lift | Can  | Square | Transport |
| <b>DRWR</b> | 32.5 | 39.5 | 59.8   | 346.1     |
| <b>DAWR</b> | 38.6 | 46.0 | 70.5   | 354.3     |
| <b>DIPO</b> | 43.9 | 51.6 | 73.3   | 359.7     |
| <b>IDQL</b> | 33.8 | 41.7 | 63.7   | 349.9     |
| <b>DOL</b>  | 36.9 | 44.4 | 68.5   | 353.5     |
| <b>OSM</b>  | 31.8 | 44.5 | 68.7   | 322.5     |
| <b>DPPO</b> | 35.2 | 42.0 | 65.6   | 350.3     |

**1359 1360 1361 1362 1363** Table 2: Wall-clock time in seconds for a single training iteration in ROBOMIMIC tasks with state input when comparing diffusion-based RL algorithms. Each iteration involves 4 episodes (1200 environment timesteps for Lift and Can, 1600 for Square, and 3200 for Transport) from each of the 50 parallelized environments running on 50 CPU threads and a NVIDIA L40 GPU (60000, 80000, 160000 steps).

**1367 1368 1369 1370 1371 1372 1373 1374 1375** Comparing to other policy parameterizations and architecture [Section 5.3](#page-6-2) and [Section 5.4.](#page-7-0) [Table 3](#page-25-1) and [Table 4](#page-25-2) shows the wall-clock time used in fine-tuning in each ROBOMIMIC task with state or pixel input, respectively. Gaussian and GMM use similar times and Transformer is slightly more expensive than MLP. On average with state input, **DPPO**-MLP trains 24%, 21%, 24%, and 22% slower than baselines due to the more expensive diffusion sampling. **DPPO**-UNet requires more time with the extensive use of convolutional and normalization layers and trains on average 49% slower than **DPPO**-MLP. On average with pixel input, **DPPO**-ViT-MLP trains 14% slower than Gaussian-ViT-MLP — the difference is smaller than the state input case as the rendering in simulation can be expensive. [Table 5](#page-26-3) shows the wall-clock time used in FURNITURE-BENCH tasks. **DPPO**-UNet trains 20% slower than Gaussian-MLP on average.

| Method                 | Task |      |        |           |  |
|------------------------|------|------|--------|-----------|--|
|                        | Lift | Can  | Square | Transport |  |
| Gaussian-MLP           | 27.7 | 35.7 | 56.2   | 255.6     |  |
| Gaussian-Transformer   | 29.8 | 37.1 | 57.8   | 266.1     |  |
| <b>GMM-MLP</b>         | 28.0 | 36.2 | 55.2   | 254.5     |  |
| <b>GMM-Transformer</b> | 29.5 | 37.4 | 58.1   | 260.2     |  |
| DPPO-MLP               | 35.6 | 43.3 | 65.0   | 350.5     |  |
| <b>DPPO-UNet</b>       | 83.6 | 92.7 | 130.4  | 431.1     |  |

**1388 1389 1390** Table 3: Wall-clock time in seconds for a single training iteration in ROBOMIMIC tasks with state input when comparing policy parameterizations. Each iteration involves 4 episodes (1200) environment timesteps for Lift and Can, 1600 for Square, and 3200 for Transport) from each of the 50 parallelized environments running on 50 CPU threads and a NVIDIA L40 GPU (60000, 80000, 160000 steps).

<span id="page-25-2"></span>

**1401 1402 1403** Table 4: Wall-clock time in seconds for a single training iteration in ROBOMIMIC tasks with pixel input when comparing policy parameterizations. Each iteration involves 4 episodes (1200 environment timesteps for Lift and Can, 1600 for Square, and 3200 for Transport) from each of the 50 parallelized environments running on 50 CPU threads and a NVIDIA L40 GPU (60000, 80000, 160000 steps).

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<span id="page-25-1"></span>**1376 1377**

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**1409 1410 1411 1412 1413** Table 5: Wall-clock time in seconds for a single training iteration in FURNITURE-BENCH tasks when comparing policy parameterizations. Each iteration involves 1 episodes (700 environment timesteps for One-leg, and 1000 for Lamp and Round-table) from each of the 1000 parallelized environments running on a NVIDIA L40 GPU (700000, 1000000, 1000000 steps).

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- <span id="page-26-0"></span>F ADDITIONAL EXPERIMENTAL DETAILS
- **1417 1418**
- <span id="page-26-1"></span>F.1 DETAILS OF POLICY ARCHITECTURES USED IN ALL EXPERIMENTS

**1419 1420 1421 1422 1423 1424 1425** MLP. For most of the experiments, we use a Multi-layer Perceptron (MLP) with two-layer residual connection as the policy head. For diffusion-based policies, we also use a small MLP encoder for the state input and another small MLP with sinusoidal positional encoding for the denoising timestep input. Their output features are then concatenated before being fed into the MLP head. Diffusion Policy, proposed by [Chi et al.](#page-10-0) [\(2024b\)](#page-10-0), does not use MLP as the diffusion architecture, but we find it delivers comparable (or even better) pre-training performance compared to UNet.

**1426**

**1427 1428 1429 1430 Transformer.** For comparing to other policy parameterizations in [Section 5.3,](#page-6-2) we also consider Transformer as the policy architecture for the Gaussian and GMM baselines. We consider decoder only. No dropout is used. A learned positional embedding for the action chunk is the sequence into the decoder.

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**1433 1434 1435 1436 1437** UNet. For comparing to other policy parameterizations in [Section 5.3,](#page-6-2) we also consider UNet [\(Ronneberger et al.,](#page-13-17) [2015\)](#page-13-17) as a possible architecture for DP. We follow the implementation from [Chi et al.](#page-10-0) [\(2024b\)](#page-10-0) that uses sinusoidal positional encoding for the denoising timestep input, except for using a larger MLP encoder for the observation input in each convolutional block. We find this modification helpful in more challenging tasks.

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**1439 1440 1441 1442 1443** ViT. For pixel-based experiments in [Section 5.3](#page-6-2) we use Vision-Transformer(ViT)-based image encoder introduced by [Hu et al.](#page-11-7) [\(2023\)](#page-11-7) before an MLP head. Proprioception input is appended to each channel of the image patches. We also follow [\(Hu et al.,](#page-11-7) [2023\)](#page-11-7) and use a learned spatial embedding for the ViT output to greatly reduce the number of features, which are then fed into the downstream MLP head.

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- <span id="page-26-2"></span>**1446 1447** F.2 ADDITIONAL DETAILS OF GYM TASKS AND TRAINING IN S[ECTION](#page-5-2) 5.1

**1448 1449 1450 1451 Pre-training.** The observations and actions are normalized to [0, 1] using min/max statistics from the pre-training dataset. For all three tasks the policy is trained for 3000 epochs with batch size 128, learning rate of 1e-3 decayed to 1e-4 with a cosine schedule, and weight decay of 1e-6. Exponential Moving Average (EMA) is applied with a decay rate of 0.995.

- **1452**
- **1453**

**1454 1455 1456 1457** Fine-tuning. All methods from [Section 5.1](#page-5-2) use the same pre-trained policy. Fine-tuning is done using online experiences sampled from 40 parallelized MuJoCo environments [\(Todorov et al.,](#page-14-18) [2012\)](#page-14-18). Reward curves shown in [Fig. 5](#page-6-0) are evaluated by running fine-tuned policies with  $\sigma_{min}^{exp} = 0.001$  (i.e., without extra noise) for 40 episodes. Each episode terminates if the default conditions are met or the episode reaches 1000 timesteps. Detailed hyperparameters are listed in [Table 7](#page-35-1) and [Table 8.](#page-35-2)

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**1473 1474 1475 1476 1477** Table 6: Comparison of the different tasks considered. "Obs dim - State": dimension of the state observation input. "Obs dim - State": dimension of the pixel observation input. "Act dim - State": dimension of the action space. T: maximum number of steps in an episode. "Sparse reward ?": whether sparse reward is used in training instead of dense reward.

<span id="page-27-0"></span>**1478 1479** F.3 DESCRIPTIONS OF DIFFUSION-BASED RL ALGORITHM BASELINES IN S[ECTION](#page-5-2) 5.1

**1480 1481 1482 DRWR:** This is a **customized** reward-weighted regression (RWR) algorithm [Peters and Schaal](#page-13-11) [\(2007\)](#page-13-11) that fine-tunes a pre-trained DP with a supervised objective with higher weights on actions that lead to higher reward-to-go  $r$ .

**1483 1484 1485 1486** The reward is scaled with  $\beta$  and the exponentiated weight is clipped at  $w_{\text{max}}$ . The policy is updated with experiences collected with the current policy (no buffer for data from previous iteration) and a replay ratio of  $N_{\theta}$ . No critic is learned.

$$
\mathcal{L}_{\theta} = \mathbb{E}^{\bar{\pi}_{\theta}, \varepsilon_{t}} \left[ \min(e^{\beta r_{t}}, w_{\max}) \|\varepsilon_{t} - \varepsilon_{\theta}(a_{t}^{0}, s_{t}, k)\|^{2} \right].
$$

**1489 1490 1491 1492 1493 DAWR:** This is a **customized** advantage-weighted regression (AWR) algorithm [Peng et al.](#page-13-10) [\(2019\)](#page-13-10) that builds on **DRWR** but uses TD-bootstrapped [Sutton and Barto](#page-14-0) [\(2018\)](#page-14-0) advantage estimation instead of the higher-variance reward-to-go for better training stability and efficiency. **DAWR** (and **DRWR**) can be seen as approximately optimizing [\(4.2\)](#page-4-4) with a Kullback–Leibler (KL) divergence constraint on the policy [Peng et al.](#page-13-10) [\(2019\)](#page-13-10); [Black et al.](#page-10-2) [\(2023\)](#page-10-2).

**1494 1495 1496 1497** The advantage is scaled with  $\beta$  and the exponentiated weight is clipped at  $w_{\text{max}}$ . Unlike **DRWR**, we follow [\(Peng et al.,](#page-13-10) [2019\)](#page-13-10) and trains the actor in an off-policy manner: recent experiences are saved in a replay buffer  $D$ , and the actor is updated with a replay ratio of  $N_{\theta}$ .

 $\mathcal{L}_{\theta} = \mathbb{E}^{\mathcal{D},\varepsilon_t} \big[ \min(e^{\beta \hat{A}_{\phi}(s_t, a^0_t)}, w_{\max}) \|\varepsilon_t - \varepsilon_{\theta}(a^0_t, s_t, k)\|^2 \big].$ 

**1499 1500 1501** The critic is updated less frequently (we find diffusion models need many gradient updates to fit the actions) with a replay ratio of  $N_{\phi}$ .

$$
\mathcal{L}_{\phi} = \mathbb{E}^{\mathcal{D}} \big[ \| \hat{A}_{\phi}(s_t, a_t^0) - A(s_t, a_t^0) \|^2 \big],
$$

**1504** where A is calculated using TD( $\lambda$ ), with  $\lambda$  as  $\lambda_{\text{DAWR}}$  and the discount factor  $\gamma_{\text{ENV}}$ .

**1506 1507 1508 DIPO** [\(Yang et al.,](#page-14-4) [2023\)](#page-14-4): This baseline applies "action gradient" that uses a learned state-action Q function to update the actions saved in the replay buffer, and then has DP fitting on them without weighting.

**1509 1510** Similar to **DAWR**, recent experiences are saved in a replay buffer D. The actions ( $k = 0$ ) in the buffer are updated for  $M_{\text{DIPO}}$  iterations with learning rate  $\alpha_{\text{DIPO}}$ .

$$
a_t^{m+1,k=0} = a_t^{m,k=0} + \alpha_{\text{DIFO}} \nabla_{\phi} \hat{Q}_{\phi}(s_t, a_t^{m,k=0}), \ m = 0, \dots, M_{\text{DIFO}} - 1.
$$

**1512 1513** The actor is then updated with a replay ratio of  $N_{\theta}$ .

$$
\frac{1514}{1515}
$$

 $\mathcal{L}_{\theta} = \mathbb{E}^{\mathcal{D}} \big[ \| \varepsilon_t - \varepsilon_{\theta} ( a_t^{M_{\text{DIPO}},k=0}, s_t, k) \|^2 \big].$ 

**1516 1517** The critic is trained to minimize the Bellman residual with a replay ratio of  $N_{\phi}$ . Double Q-learning is also applied.

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**IDQL** [\(Hansen-Estruch et al.,](#page-11-5) [2023\)](#page-11-5): This baseline learns a state-action Q function and state V

 $\mathcal{L}_{\phi} = \mathbb{E}^{\mathcal{D}} \big[ \| (R_t + \gamma_{\text{ENV}} \hat{Q}_{\phi}(s_{t+1}, \bar{\pi}_{\theta}(a_{t+1}^{k=0} | s_{t+1})) - \hat{Q}_{\phi}(s_t, a_t^{m=0, k=0}) \|^2 \big]$ 

**1521 1522** function to choose among the sampled actions from DP. DP fits on new samples without weighting.

**1523 1524** Again recent experiences are saved in a replay buffer  $D$ . The state value function is updated to match the expected Q value with an expectile loss, with a replay ratio of  $N_{\psi}$ .

$$
\mathcal{L}_{\psi} = \mathbb{E}^{\mathcal{D}} \big[ |\tau_{\text{IDQL}} - \mathbb{1}(\hat{Q}_{\phi}(s_t, a_t^0) < \hat{V}_{\psi}^2(s_t))| \big].
$$

**1527** The value function is used to update the Q function with a replay ratio of  $N_{\phi}$ .

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 $\mathcal{L}_{\phi} = \mathbb{E}^{\mathcal{D}} \big[ \|(R_t + \gamma_{\text{env}} \hat{V}_{\psi}(s_{t+1}) - \hat{Q}_{\phi}(s_t, a_t^0) \|^2 \big].$ 

**1530 1531** The actor fits all sampled experiences without weighting, with a replay ratio of  $N_{\theta}$ .

 $\mathcal{L}_{\theta} = \mathbb{E}^{\mathcal{D}} \big[ \| \varepsilon_t - \varepsilon_{\theta} (a_t^0, s_t, k) \|^2 \big].$ 

**1533 1534 1535 1536** At inference time,  $M_{\text{IDOL}}$  actions are sampled from the actor. For training, Boltzmann exploration is applied based on the difference between Q value of the sampled actions and and the V value at the current state. For evaluation, the greedy action under  $Q$  is chosen.

**1537 1538 1539 DQL** [\(Wang et al.,](#page-14-3) [2022\)](#page-14-3): This baseline learns a state-action Q function and backpropagates the gradient from the critic through the entire actor (with multiple denoising steps), akin to the usual Q-learning.

**1540 1541 1542** Again recent experiences are saved in a replay buffer  $D$ . The actor is then updated using both a supervised loss and the value loss with a replay ratio of  $N_{\theta}$ .

$$
\mathcal{L}_{\theta} = \mathbb{E}^{\mathcal{D}} \big[ \| \varepsilon_t - \varepsilon_{\theta}(a_t^0, s_t, k) \|^2 - \alpha_{\text{DQL}} \hat{Q}_{\phi}(s_t, \bar{\pi}_{\theta}(a_t^0 | s_t)) \big],
$$

**1545 1546** where  $\alpha_{\text{DOI}}$  is a weighting coefficient. The critic is trained to minimize the Bellman residual with a replay ratio of  $N_{\phi}$ . Double Q-learning is also applied.

$$
\mathcal{L}_{\phi} = \mathbb{E}^{\mathcal{D}}\!\left[\|(R_t + \gamma_{\text{env}}\hat{Q}_{\phi}(s_{t+1}, \bar{\pi}_{\theta}(a_{t+1}^0|s_{t+1})) - \hat{Q}_{\phi}(s_t, a_t^0)\|^2\right]
$$

**1549 1550 QSM** [\(Psenka et al.,](#page-13-9) [2023\)](#page-13-9): This baselines learns a state-action Q function, and then updates the actor by aligning the score of the diffusion actor with the gradient of the Q function.

**1552 1553** Again recent experiences are saved in a replay buffer  $D$ . The critic is trained to minimize the Bellman residual with a replay ratio of  $N_{\phi}$ . Double Q-learning is also applied.

$$
\mathcal{L}_{\phi} = \mathbb{E}^{\mathcal{D}} \big[ \| (R_t + \gamma_{\text{env}} \hat{Q}_{\phi}(s_{t+1}, \bar{\pi}_{\theta}(a_{t+1}^0 | s_{t+1})) - \hat{Q}_{\phi}(s_t, a_t^0) \|^2 \big].
$$

**1556 1557** The actor is updated as follows with a replay ratio of  $N_{\theta}$ .

$$
\mathcal{L}_{\theta} = \mathbb{E}^{\mathcal{D}} \big[ ||\alpha_{\text{QSM}} \nabla_a \hat{Q}_{\phi}(s_t, a_t) - (-\varepsilon_{\theta}(a_t^0, s_t, k))||^2 \big],
$$

**1560 1561** where  $\alpha_{\rm OSM}$  scales the gradient. The negative sign before  $\varepsilon_{\theta}$  is from taking the gradient of the mean  $\mu$  in the denoising process.

<span id="page-28-0"></span>**1562**

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#### **1563** F.4 DESCRIPTIONS OF RL FINE-TUNING ALGORITHM BASELINES IN S[ECTION](#page-5-3) 5.2

**1565** In this subsection, we detail the baselines **RLPD**, **Cal-QL**, and **IBRL**. All policies  $\pi_{\theta}$  are parameterized as unimodal Gaussian with an action chunk size of 1.

**1566 1567 1568 RLPD** [\(Ball et al.,](#page-10-4) [2023\)](#page-10-4): This baseline is based on Soft Actor Critic (SAC, [Haarnoja et al.](#page-11-18) [\(2018\)](#page-11-18)) — it learns an entropy-regularized state-action Q function, and then updates the actor by maximizing the Q function w.r.t. the action.

**1569 1570 1571 1572 1573** A replay buffer  $D$  is initialized with offline data, and online samples are added to  $D$ . Each gradient update uses a batch of mixed 50/50 offline and online data. An ensemble of  $N_{\text{critic}}$  critics is used, and at each gradient step two critics are randomly chosen. The critics are trained to minimize the Bellman residual with replay ratio  $N_{\phi}$ :

$$
\mathcal{L}_{\phi} = \mathbb{E}^{\mathcal{D}} \big[ || (R_t + \gamma_{\text{env}} \hat{Q}_{\phi'}(s_{t+1}, \pi_{\theta}(a_{t+1}|s_{t+1})) - \hat{Q}_{\phi}(s_t, a_t) ||^2 \big].
$$

**1575 1576** The target critic parameter  $\phi'$  is updated with delay. The actor minimizes the following loss with a replay ratio of 1:

$$
\mathcal{L}_{\theta} = \mathbb{E}^{\mathcal{D}} \big[ -\hat{Q}_{\phi}(s_t, a_t) + \alpha_{\text{ent}} \log \pi_{\theta}(a_t|s_t) \big],
$$

**1578 1579** where  $\alpha_{\text{ent}}$  is the entropy coefficient (automatically tuned as in SAC starting at 1).

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**1580 1581 1582 1583 Cal-QL** [\(Nakamoto et al.,](#page-12-3) [2024\)](#page-12-3): This baseline trains the policy  $\mu$  and the action-value function  $Q^{\mu}$  in an offline phase and then an online phase. During offline phase only offline data is sampled for gradient update, while during online phase mixed 50/50 offline and online data are sampled. The critic is trained to minimize the following loss (Bellman residual and calibrated Q-learning):

$$
\mathcal{L}_{\phi} = \mathbb{E}^{\mathcal{D}} \left[ \| (R_t + \gamma_{\text{ENV}} \hat{Q}_{\phi'}(s_{t+1}, \pi_{\theta}(a_{t+1}|s_{t+1}))) - \hat{Q}_{\phi}(s_t, a_t) \|^2 \right] + \beta_{\text{cq}} (\mathbb{E}^{\mathcal{D}} \left[ \max(Q_{\phi}(s_t, a_t), V(s_t)) \right] - \mathbb{E}^{\mathcal{D}} \left[ Q_{\phi}(s_t, a_t) \right]),
$$

**1587 1588 1589** where  $\beta_{\text{cal}}$  is a weighting coefficient between Bellman residual and calibration Q-learning and  $V(s_t)$ is estimated using Monte-Carlo returns. The target critic parameter  $\phi'$  is updated with delay. The actor minimizes the following loss:

$$
\mathcal{L}_{\theta} = \mathbb{E}^{\mathcal{D}} \big[ -\hat{Q}_{\phi}(s_t, a_t) + \alpha_{\text{ent}} \log \pi_{\theta}(a_t|s_t) \big],
$$

**1592** where  $\alpha_{\text{ent}}$  is the entropy coefficient (automatically tuned as in SAC starting at 1).

**1594 1595 1596 1597 IBRL** [\(Hu et al.,](#page-11-7) [2023\)](#page-11-7): This baseline first pre-trains a policy  $\mu_{\psi}$  using behavior cloning, and for fine-tuning it trains a RL policy  $\pi_{\theta}$  initialized as  $\mu_{\psi}$ . During fine-tuning recent experiences are saved in a replay buffer  $D$ . An ensemble of  $N_{\text{critic}}$  critics is used, and at each gradient step two critics are randomly chosen. The critics are trained to minimize the Bellman residual with replay ratio  $N_{\phi}$ :

$$
\mathcal{L}_{\phi} = \mathbb{E}^{\mathcal{D}} \big[ \| (R_t + \gamma_{\text{env}} \max_{a' \in \{a^{IL}, a^{RL}\}} \hat{Q}_{\phi'}(s_{t+1}, a') - \hat{Q}_{\phi}(s_t, a_t) \|^2 \big]
$$

**1600 1601** where  $a^{IL} = \mu_{\psi}(s_{t+1})$  (no noise) and  $a^{RL} \sim \pi_{\theta'}(s_{t+1})$ , and  $\pi_{\theta'}$  is the target actor. The target critic parameter  $\phi'$  is updated with delay. The actor minimizes the following loss with a replay ratio of 1:

$$
\mathcal{L}_{\theta} = -\mathbb{E}^{\mathcal{D}} \big[ \hat{Q}_{\phi}(s_t, a_t) \big].
$$

**1603 1604** The target actor parameter  $\theta'$  is also updated with delay.

#### **1606** F.5 ADDITIONAL DETAILS OF **DPPO** IMPLEMENTATION IN ALL TASKS

**1607 1608 1609 1610 1611** Similar to all baselines in [Appendix F.3,](#page-27-0) we denote  $N_{\theta}$  and  $N_{\phi}$  the replay ratio for the actor (Diffusion Policy) and the critic (state value function) in **DPPO**; in practice we always set  $N_{\theta} = N_{\phi}$ in **DPPO**, with the combined loss  $\mathcal{L} = \mathcal{L}_{\theta} + \mathcal{L}_{\phi}$ . Similar to usual PPO implementations [\(Huang](#page-11-12) [et al.,](#page-11-12) [2022\)](#page-11-12), the batch updates in an iteration terminate when the KL divergence between  $\pi_{\theta}$  and  $\pi_{\theta_{old}}$  reaches 1.

**1612 1613 1614 1615 1616 1617 1618 1619** We also find the PPO clipping ratio,  $\varepsilon$ , can affect the training stability significantly in **DPPO** (as well as in Gaussian and GMM policies) especially in sparse-reward manipulation tasks. In practice we find that, a good indicator of the amount of clipping leading to optimal training efficiency, is to aim for a clipping fraction (fraction of individual samples being clipped in a batch) of 10% to 20%. For each method in different tasks, we vary  $\varepsilon$  in  $\{.1, .01, .001\}$  and choose the highest value that satisfies the clipping fraction target. Empirically we also find that, using a higher  $\varepsilon$  for earlier denoising steps in **DPPO** further improves training stability in manipulation tasks. Denote  $\varepsilon_k$  the clipping value at denoising step k, and in practice we set  $\varepsilon_{k=(K-1)} = 0.1\varepsilon_{k=0}$ , and it follows an exponential schedule among intermediate k.

#### <span id="page-30-1"></span>**1620 1621** F.6 ADDITIONAL DETAILS OF ROBOMIMIC TASKS AND TRAINING IN S[ECTION](#page-6-2) 5.3

**1622 1623 1624 1625 1626** Tasks. We consider four tasks from the ROBOMIMIC benchmark [\(Mandlekar et al.,](#page-12-12) [2021\)](#page-12-12): (1) Lift: lifting a cube from the table,  $(2)$  Can: picking up a Coke can and placing it at a target bin, (3) Square: picking up a square nut and place it on a rod, and (4) Transport: two robot arms removing a bin cover, picking and placing a cube, and then transferring a hammer from one container to another one.

**1627 1628 1629 1630 1631 1632 1633 1634 Pre-training.** ROBOMIMIC provides the Multi-Human (MH) dataset with noisy human demonstrations for each task, which we use to pre-train the policies. The observations and actions are normalized to [0, 1] using min/max statistics from the pre-training dataset. No history observation (pixel, proprioception, or ground-truth object states) is used. All policies are trained with batch size 128, learning rate 1e-4 decayed to 1e-5 with a cosine schedule, and weight decay 1e-6. Diffusionbased policies are trained with 8000 epochs, while Gaussian and GMM policies are trained with 5000 epochs — we find diffusion models require more gradient updates to fit the data well.

- **1635 1636 1637 1638 1639** Fine-tuning. Diffusion-based, Gaussian, and GMM pre-trained policies are then fine-tuned using online experiences sampled from 50 parallelized MuJoCo environments [\(Todorov et al.,](#page-14-18) [2012\)](#page-14-18). Success rate curves shown in [Fig. 5,](#page-6-0) [Fig. 6,](#page-6-1) and [Fig. 20](#page-23-0) are evaluated by running fine-tuned policies with  $\sigma_{\min}^{\text{exp}} = 0.001$  (i.e., without extra noise) for 50 episodes. Episodes terminates only when they reach maximum episode lengths (shown in [Table 6\)](#page-27-1). Detailed hyperparameters are listed in [Table 10.](#page-36-0)
- **1640 1641 1642 1643 1644 Pixel training.** We use the wrist camera view in Lift and Can, the third-person camera view in Square, and the two robot shoulder camera views in Transport. Random-shift data augmentation is applied to the camera images during both pre-training and fine-tuning. Gradient accumulation is used in fine-tuning so that the same batch size (as in state-input training) can fit on the GPU. Detailed hyperparameters are listed in [Table 11.](#page-37-0)
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# <span id="page-30-2"></span>F.7 DESCRIPTIONS OF POLICY PARAMETERIZATION BASELINES IN S[ECTION](#page-6-2) 5.3

**1648 1649 1650 1651 1652 1653 1654 1655 1656 1657** Gaussian. We consider unimodal Gaussian with diagonal covariance, the most commonly used policy parameterization in RL. The standard deviation for each action dimension,  $\sigma_{\text{Gau}}$ , is fixed during pre-training; we also tried to learn  $\sigma_{\text{Gau}}$  from the dataset but we find the training very unstable. During fine-tuning  $\sigma_{\text{Gau}}$  is learned starting from the same fixed value and also clipped between 0.01 and 0.2. Additionally we clip the sampled action to be within 3 standard deviation from the mean. As discusses in [Appendix F.5,](#page-29-0) we choose the PPO clipping ratio  $\varepsilon$  based on the empirical clipping fraction in each task. This setup is also used in the FURNITURE-BENCH experiments. We note that we spend significant amount of efforts tuning the Gaussian baseline, and our results with it are some of the best known ones in RL training for long-horizon manipulation tasks (exceeding our initial expectations), e.g., reaching  $\sim$ 100% success rate in Lamp with Low randomness.

**1658 1659 1660 1661** GMM. We also consider Gaussian Mixture Model as the policy parameterization. We denote  $M_{\text{GMM}}$  the number of mixtures. The standard deviation for each action dimension in each mixture,  $\sigma$ <sub>GMM</sub>, is also fixed during pre-training. Again during fine-tuning  $\sigma$ <sub>GMM</sub> is learned starting from the same fixed value and also clipped between 0.01 and 0.2.

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**1663** F.8 ADDITIONAL DETAILS OF FURNITURE-BENCH TASKS AND TRAINING IN S[ECTION](#page-7-0) 5.4

**1665 1666 1667 1668 1669** Tasks. We consider three tasks from the FURNITURE-BENCH benchmark [\(Heo et al.,](#page-11-8) [2023\)](#page-11-8): (1) One-leg: assemble one leg of a table by placing the tabletop in the fixture corner, grasping and inserting the table leg, and screwing in the leg, (2) Lamp: place the lamp base in the fixture corner, grasp, insert, and screw in the light bulb, and finally place the lamp shade, (3) Round-table: place a round tabletop in the fixture corner, insert and screw in the table leg, and then insert and screw in the table base. See [Fig. 22](#page-31-0) for the visualized rollouts in simulation.

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**1672 1673** Pre-training. The pre-training dataset is collected in the simulated environments using a Space-Mouse<sup>[8](#page-30-3)</sup>, a 6 DoF input device. The simulator runs at 10Hz. At every timestep, we read off the state

<span id="page-30-3"></span><sup>8</sup> <https://3dconnexion.com/us/product/spacemouse-wireless/>

**1674 1675 1676 1677 1678 1679 1680 1681** of the SpaceMouse as  $\delta \mathbf{a} = [\Delta x, \Delta y, \Delta z, \Delta \text{roll}, \Delta \text{pitch}, \Delta \text{yaw}]$ , which is converted to a quaternion before passed to the environment step and stored as the action alongside the current observation in the trajectory. If  $|\Delta a_i| < \varepsilon$  ∀*i* for some small  $\varepsilon = 0.05$  defining the threshold for a no-op, we do not record any action nor pass it to the environment. Discarding no-ops is important for allowing the policies to learn from demonstrations effectively. When the desired number of demonstrations has been collected (typically 50), we process the actions to convert the delta actions stored from the SpaceMouse into absolute pose actions by applying the delta action to the current EE pose at each timestep.

**1682 1683 1684 1685 1686 1687 1688** The observations and actions are normalized to  $[-1, 1]$  using min/max statistics from the pre-training dataset. No history observation (proprioception or ground-truth object states) is used, i.e., only the current observation is passed to the policy. All policies are trained with batch size 256, learning rate 1e-4 decayed to 1e-5 with a cosine schedule, and weight decay 1e-6. Diffusion-based policies are trained with 8000 epochs, while Gaussian policies are trained with 3000 epochs. Gaussian policies can easily overfit the pre-trained dataset, while diffusion-based policies are more resilient. Gaussian policies also require a very large MLP ( $\sim$ 10 million parameters) to fit the data well.

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**1690 1691 1692 1693 1694 1695 1696** Fine-tuning. Diffusion-based and Gaussian pre-trained policies are then fine-tuned using online experiences sampled from 1000 parallelized IsaacGym environments [Makoviychuk et al.](#page-12-17) [\(2021\)](#page-12-17). Success rate curves shown in [Fig. 7](#page-7-1) are evaluated by running fine-tuned policies with  $\sigma_{min}^{exp} = 0.001$ (i.e., without extra noise) for 1000 episodes. Episodes terminate only when they reach maximum episode length (shown in [Table 6\)](#page-27-1). Detailed hyperparameters are listed in [Table 12.](#page-37-1) We find a smaller amount of exploration noise (we set  $\sigma_{min}^{exp}$  and  $\sigma_{Gau}$  to be 0.04) is necessary for the pre-trained policy achieving nonzero success rates at the beginning of fine-tuning.

<span id="page-31-0"></span>

Figure 22: Representative rollouts from simulated FURNITURE-BENCH tasks.

**1712 1713 1714 1715 1716 1717 1718 Robust sim-to-real transfer in zero-shot** policies output a sequence of desired end-effector poses in the robot base frame to control the robot. calculate the desired end-effector velocity as the difference between the desired and current poses divided by the delta time  $dt = 1/10$ . We then convert this to desired joint velocities using the Hardware setup - robot control. The physical robot used is a Franka Emika Panda arm. The These poses are converted into joint position targets through differential inverse kinematics. We Jacobian and compute the desired joint positions with a first-order integration over the current joint positions and desired velocity. The resulting joint position targets are passed to a low-level joint impedance controller provided by Polymetis [\(Lin et al.,](#page-12-18) [2021\)](#page-12-18), running at 1kHz.

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**1721 1722 1723 1724 1725 1726 1727** Hardware setup - state estimation. To deploy state-based policies on real hardware, we utilize AprilTags [\(Wang and Olson,](#page-14-19) [2016\)](#page-14-19) for part pose estimation. The FURNITURE-BENCH [\(Heo et al.,](#page-11-8) [2023\)](#page-11-8) task suite provides AprilTags for each part and code for estimating part poses from tag detections. The process involves several steps: (1) detecting tags in the camera frame, (2) mapping tag detections to the robot frame for policy compatibility, (3) utilizing known offsets between tags and object centers in the simulator, and (4) calibrating the camera pose using an AprilTag at a known position relative to the robot base. Despite general accuracy, detections can be noisy, especially during movement or partial occlusion, which the One-leg task features. Since the task requires high precision, we find the following to help make the estimation reliable enough:

**1728 1729 1730 1731 1732 1733 1734 1735 1736** • Camera coverage: We find detection quality sensitive to distance and angle between the camera and tag. This issue is likely due to the RealSense D435 camera having mediocre image quality and clarity and the relatively small tags. To remedy this, we opt to use 4 cameras roughly evenly spread out around the scene to ensure that at least one camera has a solid view of a tag on all the parts (i.e., as close as possible with a straight-on view). To find the best camera positions, we start with having a camera in each of the cardinal directions around the scene. Then, we adjust the pose of each to get it as close as possible to the objects while still covering the necessary workspace and capturing the base tag for calibration. Moving the robot arm around the scene to avoid the worst occlusion is also helpful.

- **1737 1738 1739 1740** • Lighting: Even with better camera coverage and placement, detection quality depends on having crisp images. We find proper lighting helpful to improve image quality. In particular, the scene should be well and evenly lit around the scene without causing reflections in either the tag or table.
- **1741 1742 1743 1744 1745 1746** • Filtering: Bad detections can sometimes cause the resulting pose estimate to deviate significantly from the true pose, i.e., jumping several centimeters from one frame to the next. This usually only happens on isolated frames, and thus before "accepting" a given detection, we check if the new position and orientation are within 5 cm and 20 degrees of the previously accepted pose. In addition, we apply low-pass filtering on the detection using a simple exponential average (with  $\alpha = 0.25$ ) to smooth out the high-frequency noise.
- **1747 1748 1749 1750 1751 1752** • Averaging: The objects have multiple tags that can be detected from multiple cameras. After performing the filtering step, we average all pose estimates for the same object across different tags and cameras, which also helps smooth out noise. This alone, however, does not fully cancel the case when a single detection has a large jump, as this can severely skew the average, still necessitating a filtering step. Having multiple cameras benefits this step, too, as it provides more detections to average over.
- **1753 1754 1755 1756 1757 1758 1759** • Caching part pose in hand: A particularly difficult phase of the task to achieve good detections is when the robot transports the table leg from the initial position to the tabletop for insertion. The main problems are that the movement can blur the images, and the grasping can cause occlusions. Therefore, we found it helpful to assume that once the part was grasped by the robot, it would not move in the grasp until the gripper opened. With this, we can "cache" the pose of the part relative to the end-effector once the object is fully grasped and use this instead of relying on detections during the movement.
- **1760 1761 1762 1763 1764 1765 1766** • Normalization pitfalls and clipping: We generally use min-max normalization of the state observations to ensure observations are in  $[-1, 1]$ . The tabletop part moves very little in the z-direction demonstration data, meaning the resulting normalization limits (the minimum and maximum value of the data) can be very close,  $x_{\text{max}} - x_{\text{min}} \approx 0$ . With these tight limits, the noise in the real-world detection can be amplified greatly as  $x_{\text{norm}} = \frac{x - x_{\text{min}}}{x_{\text{max}} - x_{\text{min}}}$ . Therefore, ensure that normalization ranges are reasonable. As an extra safeguard, clipping the data to  $[-1, 1]$  can also help.
- **1767 1768 1769 1770** • Only estimate necessary states: Despite the One-leg task having 5 parts, only 2 are manipulated. Only estimating the pose of those parts can eliminate a lot of noise. In particular, the pose of the 3 legs that are not used and the obstacle (the U-shaped fixture) can be set to an arbitrary value from the dataset.
	- Visualization for debugging: We use the visualization tool MeshCat $^9$  $^9$  extensively for debugging of state estimation. The tool allows for easy visualizations of poses of all relevant objects in the scene, like the robot end-effector and parts, which makes sanity-checking the implementation far easier than looking at raw numbers.
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**1776 1777 1778 1779 1780** Hardware evaluation. We perform 20 trials for each method. We adopt a single-blind model selection process: at the beginning of each trial, we first randomize the initial state. Then, we randomly select a method and roll it out, but the experimenter does not observe which model is used. We record the success and failure of each trial and then aggregate statistics for each model after all trials are completed.

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<span id="page-32-0"></span><sup>9</sup><https://github.com/meshcat-dev/meshcat>

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**1810 1811 1812 1813** Figure 23: Qualitative comparison of pre-trained vs. fine-tuned **DPPO** policies in real evaluation. (A) Successful rollout with the pre-trained policy. (B) Failed rollout with the pre-trained policy due to imprecise insertion. (C) Successful rollout with the fine-tuned policy. (D) Successful rollout with the fine-tuned policy that requires corrective behavior.

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**1816 1817 1818 1819 1820 1821 1822 1823 Domain randomization for sim-to-real transfer.** To facilitate the sim-to-real transfer, we apply additional domain randomization to the simulation training. We record the range of observation noises in hardware without any robot motion and then apply the same amount of noise to state observations in simulation. We find the state estimation in hardware particularly sensitive to the object heights. Also, we apply random noise (zero mean with 0.03 standard deviation) to the sampled action from **DPPO** to simulate the imperfect low-level controller; we find adding such noise to the Gaussian policy leads to zero task success rate while **DPPO** is robust to it (also see discussion in [Section 6\)](#page-8-2).

**1825 1826 1827 1828** BC regularization loss used for Gaussian baseline. Since the fine-tuned Gaussian policy exhibits very jittery behavior and leads to zero success rate in real evaluation, we further experiment with adding a behavior cloning (BC) regularization loss in fine-tuning with the Gaussian baseline. The combined loss follows

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$$
\mathcal{L}_{\theta, +BC} = \mathcal{L}_{\theta} - \alpha_{BC} \mathbb{E}^{\pi_{\theta_{old}}} \left[ \sum_{k=0}^{K-1} \log \pi_{\theta_{pre\text{-trained}}}(a_t^k | a_t^{k+1}, s_t) \right],
$$

**1833 1834 1835** where  $\pi_{\theta_{pre-trained}}$  is the frozen BC-only policy. The extra term encourages the newly sampled actions from the fine-tuned policy to remain high-likelihood under the BC-only policy. We set  $\alpha_{BC} = 0.1$ . However, although this regularization reduces the sim-to-real gap, it also significantly limits finetuning, leading to the fine-tuning policy saturating at 53% success rate shown in [Fig. 7.](#page-7-1)

#### <span id="page-34-0"></span> F.9 ADDITIONAL DETAILS OF AVOID TASK FROM D3IL AND TRAINING IN S[ECTION](#page-8-2) 6

 Pre-training. We split the original dataset from D3IL based on the three settings, M1, M2, and M3; in each setting, observations and actions are normalized to  $[0, 1]$  using min/max statistics. All policies are trained with batch size 16 (due to the small dataset size), learning rate 1e-4 decayed to 1e-5 with a cosine schedule, and weight decay 1e-6. Diffusion-based policies are trained with about 15000 epochs, while Gaussian and GMM policies are trained with about 10000 epochs; we manually examine the trajectories from different pre-trained checkpoints and pick ones that visually match the expert data the best.

 Fine-tuning. Diffusion-based, Gaussian, and GMM pre-trained policies are then fine-tuned using online experiences sampled from 50 parallelized MuJoCo environments [\(Todorov et al.,](#page-14-18) [2012\)](#page-14-18). Reward curves shown in [Fig. 9](#page-9-0) and [Fig. 19](#page-23-3) are evaluated by running fine-tuned policies with the same amount of exploration noise used in training for 50 episodes; we choose to use the training (instead of evaluation) setup since Gaussian policies exhibit multi-modality only with training noise. Episodes terminate only when they reach 100 steps.

 Added action noise during fine-tuning. In [Fig. 9](#page-9-0) left, we demonstrate that **DPPO** exhibits stronger training stability when noise is added to the sampled actions during fine-tuning. The noise starts at the 5th iteration. It is sampled from a uniform distribution with the lower limit ramping up to 0.1 and the upper limit ramping up to 0.2 linearly in 5 iterations. The limits are kept the same from the 10th iteration to the end of fine-tuning.

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### <span id="page-35-1"></span><span id="page-35-0"></span>F.10 LISTED TRAINING HYPERPARAMETERS

|             |   | Task(s)         |                 |                    |                        |  |
|-------------|---|-----------------|-----------------|--------------------|------------------------|--|
| Method      | Parameter                               | <b>GYM</b>      | Lift, Can       | Square             | Transport              |  |
|             | $\gamma_{\text{\tiny{ENV}}}$            | 0.99            | 0.999           | 0.999              | 0.999                  |  |
|             | $\sigma_{\min}^{\exp}$                  | 0.1             | 0.1             | 0.1                | 0.08                   |  |
|             |   |                 |                 | 0.1                |                        |  |
| Common      | $T_a$                                   | $\overline{4}$  | 4               | 4                  | 8                      |  |
|             | $\boldsymbol{K}$<br>Actor learning rate | $1e-4$          | $1e-5$          | 20<br>$1e-5$       | 1e-5 (decayed to 1e-6) |  |
|             | Critic learning rate (if applies)       |                 |                 | $1e-3$             |                        |  |
|             | Actor MLP dims                          | [512, 512, 512] | [512, 512, 512] | [1024, 1024, 1024] | [1024, 1024, 1024]     |  |
|             | Critic MLP dims (if applies)            |                 |                 | [256, 256, 256]    |                        |  |
|             | $\beta$                                 |                 |                 | 10                 |                        |  |
| <b>DRWR</b> | $w_{\max}$                              | 100             |                 |                    |                        |  |
|             | $N_{\theta}$                            | 16              |                 |                    |                        |  |
|             | Batch size                              |                 |                 | 1000               |                        |  |
|             | $\beta$                                 |                 |                 | 10                 |                        |  |
|             | $w_{\text{max}}$                        | 100             |                 |                    |                        |  |
| <b>DAWR</b> | $\lambda_{\text{DAWR}}$<br>$N_{\theta}$ |                 |                 | 0.95<br>64         |                        |  |
|             | $N_{\phi}$                              | 16              | $\overline{4}$  | 4                  | 4                      |  |
|             | <b>Buffer</b> size                      | 200000          | 150000          | 150000             | 150000                 |  |
|             | Batch size                              |                 |                 | 256                |                        |  |
|             | $\alpha_{\rm DIPO}$                     |                 |                 | $1e-4$             |                        |  |
|             | $M_{\text{DIPO}}$                       |                 |                 | 10                 |                        |  |
| <b>DIPO</b> | $N_{\theta}$                            |                 | 64              |                    |                        |  |
|             | <b>Buffer</b> size<br>Batch size        | 400000<br>5000  |                 |                    |                        |  |
|             |   |                 |                 |                    |                        |  |
|             | $M_{\text{IDOL}}$<br>$N_{\theta}$       | 20              | 10              | 10<br>16           | 10                     |  |
| <b>IDQL</b> | $N_{\phi}$                              |                 |                 | 16                 |                        |  |
|             | <b>Buffer</b> size                      | 200000          | 150000          | 150000             | 150000                 |  |
|             | <b>Batch</b> size                       | 256             | 512             | 512                | 512                    |  |
|             | $\alpha_{\rm DQL}$                      |                 |                 | 1                  |                        |  |
|             | $N_{\theta}$                            |                 |                 | 64                 |                        |  |
| <b>DQL</b>  | $N_{\phi}$                              |                 |                 | 64                 |                        |  |
|             | Buffer eize                             |                 |                 | 400000             |                        |  |
|             | <b>Batch</b> size                       |                 |                 | 5000               |                        |  |

Table 7: Fine-tuning hyperparameters for OpenAI GYM and ROBOMIMIC tasks when comparing diffusion-based RL methods. We list hyperparameters shared by all methods first, and then method-specific ones.

<span id="page-35-2"></span>

|                 |                         | $Task(s)$ (cont'd) |           |        |           |
|-----------------|-------------------------|--------------------|-----------|--------|-----------|
| Method (cont'd) | Parameter (cont'd)      | <b>GYM</b>         | Lift, Can | Square | Transport |
|                 | $\alpha$ <sub>QSM</sub> |                    |           | 50     |           |
|                 | $N_{\theta}$            |                    |           | 32     |           |
| <b>QSM</b>      | $N_{\phi}$              | 32                 |           |        |           |
|                 | <b>Buffer</b> size      | 200000             | 150000    | 150000 | 150000    |
|                 | Batch size              |                    |           | 5000   |           |
|                 | $\gamma_{\rm DENOISE}$  |                    |           | 0.99   |           |
|                 | GAE $\lambda$           |                    |           | 0.95   |           |
|                 | $N_{\theta}$            | 5                  | 10        | 10     | 8         |
| <b>DPPO</b>     | $N_{\phi}$              | 5                  | 10        | 10     | 8         |
|                 | $\varepsilon$           | 0.01               |           |        |           |
|                 | Batch size              | 5000               | 7500      | 10000  | 10000     |
|                 | K'                      | 10                 |           |        |           |

Table 8: Continuation of Table [7.](#page-35-1)



**1964 1965 1966 1967** Table 9: Fine-tuning hyperparameters for HalfCheetah-v2, Can, and Square when comparing demo-augmented RL methods. We list hyperparameters shared by all methods first, and then method-specific ones.

<span id="page-36-0"></span>

**1994 1995 1996 1997** Table 10: Fine-tuning hyperparameters for ROBOMIMIC tasks with state input when comparing policy parameterizations. We list hyperparameters shared by all methods first, and then methodspecific ones. Since the different policy parameterizations use different neural network architecture, we list the total model size here instead of the details such as MLP dimensions.

<span id="page-37-0"></span>

**2015 2016 2017 2018** Table 11: Fine-tuning hyperparameters for ROBOMIMIC tasks with pixel input when comparing policy parameterizations. We list hyperparameters shared by all methods first, and then methodspecific ones. Since the different policy parameterizations use different neural network architecture, we list the total model size here instead of the details such as MLP dimensions.

<span id="page-37-1"></span>

|                  |  | Task                   |        |             |  |  |
|------------------|--|------------------------|--------|-------------|--|--|
| Method           | Parameter                                | One-leg                | Lamp   | Round-table |  |  |
|                  | $\gamma_{\rm{ENV}}$                      | 0.999                  |        |             |  |  |
|                  | $T_a$                                    |                        | 8      |             |  |  |
|                  | Actor learning rate                      | 1e-5 (decayed to 1e-6) |        |             |  |  |
|                  | Critic learning rate                     | $1e-3$                 |        |             |  |  |
| Common           | GAE $\lambda$                            | 0.95                   |        |             |  |  |
|                  | $N_{\theta}$                             | 5                      |        |             |  |  |
|                  | $N_{\phi}$                               | 5                      |        |             |  |  |
|                  | $\varepsilon$                            | 0.001                  |        |             |  |  |
|                  | <b>Batch</b> size                        | 8800                   |        |             |  |  |
|                  | Model size                               | 10.64M                 | 10.62M | 10.62M      |  |  |
| Gaussian-MLP     | $\sigma_{\text{Gau}}$                    |                        | 0.04   |             |  |  |
| <b>DPPO-UNet</b> | Model size                               | 6.86M                  | 6.81M  | 6.81M       |  |  |
|                  | $\gamma_{\rm DENOISE}$                   | 0.9                    |        |             |  |  |
|                  | $\sigma^{\rm exp}$<br>min                |                        | 0.04   |             |  |  |
|                  | $\sigma_{\min}^{\overline{\text{prob}}}$ |                        | 0.1    |             |  |  |
|                  | K  | 100                    |        |             |  |  |
|                  | K'                                       | 5(DDIM)                |        |             |  |  |

Table 12: Fine-tuning hyperparameters for FURNITURE-BENCH tasks when comparing policy parameterizations. We list hyperparameters shared by all methods first, and then method-specific ones.

**2044 2045 2046**

**2047 2048**

**2049 2050**