STOC-TOT: Stochastic Tree-of-Thought with Constrained Decoding for Complex Reasoning in Multi-Hop Question Answering

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Abstract

 Multi-hop question answering (MHQA) re- quires a model to retrieve and integrate informa- tion from multiple passages to answer a com- plex question. Recent systems leverage the power of large language models and integrate evidence retrieval with reasoning prompts (e.g., chain-of-thought reasoning) for the MHQA task. However, the complexities in the ques- tion types (bridge v.s. comparison questions) and the reasoning types (sequential v.s. par- allel reasonings) require more novel and fine- grained prompting methods to enhance the per- formance of MHQA under the zero-shot set-014 ting. In this paper, we propose STOC-TOT, a 015 stochastic tree-of-thought reasoning prompting method with constrained decoding for MHQA and conduct a detailed comparison with other reasoning prompts on different question types and reasoning types. Specifically, we construct a tree-like reasoning structure by prompting the model to break down the original question into smaller sub-questions to form different reason- ing paths. In addition, we prompt the model to provide a probability estimation for each rea- soning path at each reasoning step. At answer 026 time, we conduct constrained decoding on the model to generate more grounded answers and reduce hallucination. Experiments comparing STOC-TOT with on two MHQA datasets and five large language models showed that STOC- TOT outperforms other reasoning prompts by a significant margin.

033 1 Introduction

 Question answering (QA) is a fundamental task in natural language processing (NLP) that involves designing systems capable of understanding human language questions and providing accurate and rel- evant answers. With the recent advancement of large language models (LLMs) that demonstrated superior reasoning ability [\(Brown et al.,](#page-8-0) [2020\)](#page-8-0), re- searchers have been focusing more on complex QA tasks, such as multi-hop question answering

Figure 1: An example of the MHQA question. This question has two hops that require the model to reason about before answering the final question.

(MHQA). MHQA is more challenging as it requires **043** models to understand complicated questions, per- **044** form multiple reasoning steps, and gather evidence **045** across documents. Figure [1](#page-0-0) shows an example of a **046** two-hop MHQA question. To answer that question **047** in Figure [1,](#page-0-0) the QA model needs to first figure out **048** who is the actor that received the 2016 Academy 049 Honorary Award. Then based on the answer to the **050** previous question, the QA model needs to further **051** answer a second question about which movie the **052** actor co-starred with Chris Tucker. **053**

State-of-the-art methods for MHQA are fully- **054** supervised methods that often follow a retrieve- **055** and-read framework, including a passage retrieving **056** module that gathers relative evidence from docu- **057** ments and a reading comprehension module to rea- **058** son about the evidence [\(Zhu et al.,](#page-10-0) [2021;](#page-10-0) [Li et al.,](#page-8-1) **059** [2022\)](#page-8-1). Other methods include beam-search [\(Zhang](#page-10-1) **060** [et al.,](#page-10-1) [2023\)](#page-10-1) and label-smoothing [\(Yin et al.,](#page-10-2) [2023\)](#page-10-2). **061** However, these methods often require extensive **062** pre-training or fine-tuning and do not generalize **063** well to other datasets. 064

 Large language models (LLMs), on the other hand, show remarkable reasoning ability and rich knowledge of general-domain questions. Many LLMs can answer simple and straightforward ques- tions that do not require complex reasoning without any supervision involved but often fail to deal with complex questions requiring multiple reasoning steps. To tackle the problem, researchers have de- veloped many prompting techniques to improve LLM's reasoning ability, such as chain-of-thought (CoT) [\(Wei et al.,](#page-9-0) [2022\)](#page-9-0), self-consistency CoT (Sc-**CoT**) [\(Wang et al.,](#page-9-1) [2023\)](#page-9-1), and tree-of-thought (ToT) **prompting [\(Yao et al.,](#page-10-3) [2023a\)](#page-10-3).**

 CoT has been shown effective across tasks re- quiring extensive, step-by-step reasoning, such as math calculation and reading comprehension. How- ever, there could be various possible reasoning paths for many complex multi-hop questions, and CoT models cannot "turn back" when they have made a mistake along their reasoning paths. Sc- CoT further improves on CoT by proposing differ- ent chains of thought, thus expanding the reasoning space. However, there is no local reasoning expan- sion within each chain, and the "majority voting" strategy often fails in open-domain tasks where the output space is unlimited. ToT, designed to main- tain different reasoning paths along its reasoning process, is more suitable for dealing with complex question types. However, the intermediate reason- ing steps in NLP generation tasks are much less constrained and require more than a simple rule- based evaluation. The complexities in the question types (bridge v.s. comparison questions in Table [1\)](#page-5-0), as well as the reasoning types (sequential v.s. parallel reasonings in Table [2\)](#page-5-1), require more novel and fine-grained prompting methods to enhance the reasoning ability of LLMs.

 To tackle the challenges and design a more reli- able reasoning method for open-domain NLP tasks, we propose STOC-TOT, a stochastic ToT-based framework that instructs the model to generate dif- ferent reasoning paths from the same question and assign probability scores to reasoning paths to ef- fectively avoid reasoning dead-ends. To the best of our knowledge, our work is the first to adapt the tree-of-thought reasoning prompting to natural lan- guage tasks that require complex reasoning, such as MHQA. We provide an example overview of our framework in Figure [2.](#page-2-0) Specifically, we con- struct a tree-like reasoning structure by prompting the model to break down the original question into

smaller sub-questions to form different reasoning 116 paths. We evaluate the validity of each reason- **117** ing path on three levels of aspects and arrive at a **118** model-given probability score. At answer time, we **119** innovatively propose to use constrained decoding **120** in the answering process to reduce hallucination by **121** forcing the model to generate grounded answers **122** from evidence and letting models give concise and **123** exact answers. Ultimately, we arrive at the best **124** answer by choosing the path with the highest ag- **125** gregated probability score. Experiments on two **126** benchmarking MHQA datasets demonstrate that **127** STOC-TOT significantly improves the reasoning **128** ability of LLMs in complex reasoning scenarios, **129** especially with GPT-4, improving Exact Match ac- **130** curacy by 7%, and F1 score by 7.8 points on the **131** HotpotQA dataset over the original tree-of-thought **132** prompting. Our contributions are as follows: **133**

- We propose STOC-TOT, which constructs a **134** stochastic reasoning tree in complex reasoning **135** scenarios. We introduce stochastic estimations **136** on different reasoning paths, which helps the **137** model have a more reliable reasoning process **138** than previous reasoning prompting methods. **139**
- We innovatively propose to use constrained de- **140** coding in the answering process. This step re- **141** duces model hallucination by forcing the model **142** to generate grounded answers from evidence and **143** letting models give concise and exact answers. **144**
- We evaluate the effectiveness of STOC-TOT by **145** conducting experiments on two MHQA datasets. **146** We observe substantial improvements over other **147** reasoning prompting methods, with STOC-TOT **148** surpassing all other selected reasoning prompting **149** baselines on 5 tested models. **150**

2 Related Work **¹⁵¹**

Multi-Hop Question Answering Multi-hop **152** Question Answering (MHQA) is a challenging **153** task requiring models to reason over different ev- **154** idence across documents to answer a complex **155** multi-hop question. Many high-quality MHQA **156** datasets have been developed, including HotpotQA **157** [\(Yang et al.,](#page-10-4) [2018\)](#page-10-4), WikiHop [\(Welbl et al.,](#page-10-5) [2018\)](#page-10-5), **158** MuSiQue [\(Trivedi et al.,](#page-9-2) [2022\)](#page-9-2), and others. Among **159** these, HotpotQA is the task's most representative **160** and widely used dataset. Previous state-of-the-art **161** MHQA models often follow a two-stage pipeline: **162** a retriever that extracts evidence from the docu- **163** ments, and a reader that reasons about the evidence 164

Figure 2: Overview of our framework, with the example in Figure 1. The top-right Corner shows the overall structure of the constructed tree, with each node's label on the left. Darker green in the nodes means a higher evaluated probability of the reasoning path. The original Question is colored in blue. We chose the first round of our tree-building process as an example in the purple block.

 to arrive at an answer [\(Zhu et al.,](#page-10-0) [2021;](#page-10-0) [Li et al.,](#page-8-1) [2022\)](#page-8-1). Other methods include beam-search [\(Zhang](#page-10-1) [et al.,](#page-10-1) [2023\)](#page-10-1) and label-smoothing [\(Yin et al.,](#page-10-2) [2023\)](#page-10-2). Some LLM-based frameworks [\(Yao et al.,](#page-10-6) [2023b;](#page-10-6) [Gou et al.,](#page-8-2) [2024\)](#page-8-2) were also evaluated on the task of MHQA, but their performance fell short compared with supervised methods.

 Reasoning Prompting of LLMs Various prompt [e](#page-9-0)ngineering methods have been developed [\(Wei](#page-9-0) [et al.,](#page-9-0) [2022;](#page-9-0) [Wang et al.,](#page-9-1) [2023;](#page-9-1) [Yao et al.,](#page-10-3) [2023a;](#page-10-3) [Besta et al.,](#page-8-3) [2024;](#page-8-3) [Sel et al.,](#page-9-3) [2024;](#page-9-3) [Chen et al.,](#page-8-4) [2023\)](#page-8-4), aiming to improve large language models' reasoning ability across various tasks and domains. Chain-of-thought (CoT) prompting [\(Wei et al.,](#page-9-0) [2022\)](#page-9-0) prompts the large language models (LLMs) to divide their reasoning process into smaller steps when solving a question, forming a chain of thoughts. Chain-of-thought self-consistency prompting [\(Wang et al.,](#page-9-1) [2023\)](#page-9-1) improves on the CoT method by proposing different reasoning chains and ensembles on the final result. Tree-of-thought (ToT) prompting method [\(Yao et al.,](#page-10-3) [2023a\)](#page-10-3) ac- tively maintains a tree of thoughts, where each thought is a coherent language sequence that serves as an intermediate step toward problem-solving. Graph-of-thought [\(Besta et al.,](#page-8-3) [2024\)](#page-8-3) further im-proves ToT by constructing a Directed Graph instead of a tree. LLMs can loop over a thought to **192** refine it and aggregate thoughts or chains. **193**

Constrained Decoding Constrained decoding is **194** the technique that asks the models to generate out- **195** puts following a given set of rules. The most **196** common way of conducting constrained generation **197** uses beam search [\(Och and Ney,](#page-8-5) [2004\)](#page-8-5) in decoding **198** time. Before the LLM era, works on constrained **199** decoding focused on task-specific sequence-to- **200** sequence models that span across many fields, such **201** as machine translation [\(Hokamp and Liu,](#page-8-6) [2017;](#page-8-6) **202** [Post and Vilar,](#page-9-4) [2018\)](#page-9-4), named entity recognition **203** [\(Lester et al.,](#page-8-7) [2020\)](#page-8-7), and dialogue generation [\(Bal-](#page-8-8) **204** [akrishnan et al.,](#page-8-8) [2019\)](#page-8-8). Recently, Microsoft intro- **205** duced Guidance^{[1](#page-2-1)}, which allows users of various 206 large language models to control their outputs given **207** a human-defined vocabulary or rules. **208**

3 Method **²⁰⁹**

3.1 Task Formation **210**

Given a multi-hop question Q and background cor- **211** pus of evidence P, the goal of our framework is **212** to output the answer A to question Q, drawing its **213** reasoning with the support of multiple evidence **214** passages p_1, p_2, \ldots retrieved from corpus P. $\qquad \qquad$ 215

¹ https://github.com/guidance-ai/guidance

216 3.2 STOC-TOT Framework

 For each of the questions Q, multiple reasoning lines and, thus, multiple ways of breaking down the question could exist. However, not every reasoning line would lead us to the right answer, and they take us to dead ends. To avoid such reasoning dead-ends, we build a stochastic reasoning tree to represent the possible reasoning lines and the probability of each reasoning line taking us to the right answer. We achieve this by proposing a self- interactive framework that automatically builds the reasoning tree given a multi-hop question. Figure [2](#page-2-0) shows our framework with an example question.

 In our reasoning process, we first prompt the model to propose different possible sub-questions to solve at each reasoning step. Each sub-question corresponds to one possible reasoning path and is presented as a node in the tree. We then ask the model to answer the generated sub-questions. To prevent hallucination and make the model more fo- cused on the given question and evidence, we build a vocabulary bank using words from the evidence list and the original question and instruct the model to do constrained decoding from the vocabulary bank when generating its answers. After answering every sub-question generated from the same ques- tion in the previous reasoning level, we prompt the model to evaluate each reasoning path and es- timate how likely the reasoning path would lead us to the right answer. This probability estimation would be assigned to the corresponding node in the tree. After the reasoning process finishes, each rea- soning path would have an aggregated probability calculated from nodes along the path.

 Formally, given a question Q, we instruct the 251 model to generate sub-questions $q_1, q_2, ..., q_n$, and build a tree structure with the original question Q **as the root node and each question** q_i as subsequent nodes. The tree would expand as each sub-question q_i has its sub-question q_j , and the reasoning paths are thus represented as branches in the tree struc- ture. From the original question Q and the evi-258 dence list $E = e_1, e_2, ..., e_n$, we build a vocabulary **bank** $V = [w_1, w_2, ..., w_n], w_i \in Q, w_j \in E$. We then prompt the model to generate their answer $a_1, a_2, ..., a_n$ using only $w_i \in V$. We describe the details of our framework below.

 Example-Based Sub-Question Generation Our framework starts with the sub-question gener- ation module, which generates sub-questions $q_1, q_2, ..., q_n$ using the question Q_g from the previous reasoning level. The sub-questions are gen- **267** erated based on both the model's reasoning abil- **268** ity and the model's semantic understanding of the **269** question Q_q . An example is given in Figure [2,](#page-2-0) 270 where the sub-questions from nodes 2 and 3 were **271** generated using the question from node 1. How- **272** ever, we cannot guarantee that each sub-question **273** asked is a good sub-question, and sometimes, the **274** generated sub-question merely repeats the previous **275** question. We introduce the paraphrase detection **276** module and pass on the generated sub-questions to **277** reduce redundancy and improve question quality. **278**

Paraphrase Detection Answering repetitive **279** questions often leads to low-quality answers and **280** time-consuming steps. Following the sub-question **281** generation module, we introduce the paraphrase de- **282** tection module to reduce redundancy and improve **283** question quality. In this module, we prompt the **284** model and ask it to distinguish informative ques- **285** tions from questions that merely repeat what is **286** already stated at the previous reasoning level. If a **287** sub-question is a paraphrase, we instruct the model **288** to stop generating sub-questions from the current **289** question. In other words, we prune the low-quality **290** sub-branch of the tree that could otherwise be gen- **291** erated. By pruning these branches, we effectively **292** improve the efficiency of our framework. **293**

Evidence Retrieval and Answering We then **294** move on to answering the question after our para- **295** phrase detection module. Our evidence retrieval **296** and answering module focuses on retrieving ev- **297** idence and generating answers to the given sub- **298** question. We also pass in the full evidence list pro- **299** vided and prompt the model to give out an answer **300** to the given sub-question. The evidence retrieval **301** and answering module selects relative evidence **302** from an evidence pool for each sub-question and **303** uses words only from the vocabulary bank to gen- **304** erate its final answer. We will discuss details of **305** constrained decoding in Section [3.3.](#page-4-0) The generated **306** sub-answer and the answered sub-question are then **307** passed on to the sub-question generation module **308** at the next level to continue the reasoning process. **309**

Validity Estimation Not each sub-question **310** asked is a good sub-question, and not each rea- **311** soning path is reasonable. After every sub-question **312** q_i generated from the same question Q_q has been 313 answered, we prompt the model to provide a proba- **314** bility estimation p_i for each (q_i, a_i) pair. This prob-
315 ability is the model's evaluation of going down the **316** **317** correct reasoning path. Specifically, this probabil-**318** ity is obtained by prompting the model to consider **319** the following three aspects:

- **320** Question Level: Is the question semantically
- **321** clear and answerable?
- **322** Reasoning Level: Is the reasoning line coherent
- **323** when considering previous levels?
- **324** Answer Level: Does the evidence fully support **325** the answer to the question?

326 As shown in Figure [2,](#page-2-0) we conduct validity estima-**327** tion for sub-questions and sub-answers in nodes 2 **328** and 3 since the sub-questions were generated from

329 the same question in node 1. **330** At the leaf node of our tree, we would have a

331 final question q_f **. along with a final answer A to**

 the original question Q, and also an aggregated 333 probability $p_{final} = \prod_i p_i$, with each p_i being the probability of the nodes along the reasoning path. We assign p_{final} to the leaf node, representing the

336 aggregated probability of answer A being the cor-**337** rect answer to Q.

338 3.3 Constrained Decoding

 One challenge for generative LLMs in the task of question answering is hallucination. LLMs often fail to pay attention to the golden evidence and hallucinate their own reference even when large amounts of evidence exist. To alleviate the problem of LLM halluscination during evidence selection and answer generation, we innovatively propose to use constrained decoding in the answering process to reduce hallucination by forcing the model to generate grounded answers from evidence and let models give concise and exact answers. As shown in Figure [2,](#page-2-0) we conduct constrained decoding by asking the model to generate words from the vo- cabulary bank, consisting of words taken only from the original question and the evidence list provided. More formally, we construct a vocabulary bank $V = w_1, w_2, ..., w_i$ from all words in the provided evidence sentences. We conduct a simple filtering by removing common English stop words. We then instruct the model's evidence retrieval and answer- ing module to construct its answers using words only from the given vocabulary V .

361 Code-based Constrained Decoding For open-**362** source LLMs (e.g., Llama), we build our logit pro-**363** cessor at the decoding time. Specifically, for every word $w_i \notin V$, we manually set the score to nega- 364 tive infinity to prevent the model from generating **365** them. Thus, every answer generated will only use **366** words from the evidence list.

Prompt-based Constrained Decoding For **368** closed-source LLMs (e.g., GPT models), since we **369** do not have access to their decoding function, we **370** had to instruct the GPT models using prompts to **371** do constrained decoding. We provide our prompt **372** template used in Appendix [A.](#page-11-0) **373**

4 Experimental Setup **³⁷⁴**

Dataset We compare STOC-TOT with baseline **375** methods on the HotpotQA dataset [\(Yang et al.,](#page-10-4) **376** [2018\)](#page-10-4) and the MuSiQue dataset [\(Trivedi et al.,](#page-9-2) **377** [2022\)](#page-9-2), both of which are widely used MHQA **378** datasets across state-of-the-art MHQA baselines. **379** The experiments are conducted under the distrac- **380** tor setting, where we provide the model with an **381** evidence pool containing both golden and irrele- **382** vant evidence. The model needs to find the golden **383** evidence to answer the question correctly. We ran- **384** domly selected 200 examples from each dataset as **385** our evaluation set. **386**

Baselines We included three baselines: **387**

- Vanilla Prompting with no examples provided. **388** We only provide the model with questions and **389** evidence and instruct it to output the answer. **390**
- Chain-of-Thought (CoT) prompting [\(Wei et al.,](#page-9-0) **391** [2022\)](#page-9-0) with a standard input-output (IO) prompt. **392** We design the prompt with one in-context exam- **393** ple, which presents the whole reasoning chain, **394** including all intermediate steps. **395**
- Tree-of-Thought prompting [\(Yao et al.,](#page-10-3) [2023a\)](#page-10-3) **396** with slight modifications to adapt to the MHQA 397 task. We largely followed the original framework **398** and used majority voting on the reasoning lines **399** to decide the final answer. **400**

We recognize that there are LLM-based retrieval 401 augmented generation frameworks [\(Yao et al.,](#page-10-6) **402** [2023b;](#page-10-6) [Gou et al.,](#page-8-2) [2024\)](#page-8-2) that were also evaluated **403** on HotpotQA. However, we excluded them from **404** our baselines as they used outside knowledge bases, **405** which are under a different testing scenario. 406

4.1 Implementation 407

We experiment with the baselines and our model **408** utilizing five LLMs: GPT-3.5-turbo [\(Brown et al.,](#page-8-0) **409**

Prompting Method	GPT3.5		GPT4		LLaMa2(13B)		LLaMa2(70B)		LLaMa3(8B)	
	EM	F1	EM	F1	EM	F1	EM	F1	EM	F1
Zero-Shot Vanilla	34.0	45.0	51.0	65.0	25.5	36.5	30.5	41.0	27.5	40.7
Chain-of-Thought	35.5	47.3	52.0	66.8	30.5	42.5	33.5	45.0	32.5	44.6
Tree-of-Thought	36.5	49.5	55.0	68.5	29.5	41.3	35.5	47.3	30.5	37.5
STOC-TOT	45.5	56.2	62.0	76.3	31.0	43.0	43.0	56.3	33.0	44.5
w/o constrained decoding	40.5	53.5	59.5	73.0	31.0	43.0	40.5	53.5	32.0	44.3

Table 1: Performance comparison of STOC-TOT and baseline methods on the HotpotQA dataset.

Table 2: Performance comparison of STOC-TOT and baseline methods on the MusiQue dataset.

Prompting Method	GPT3.5			GPT4	LLaMa2(13B)		LLaMa3(8B)	
	EM	F1	EM	F1	EM	F1	EM	F1
Zero-Shot Vanilla	17.0	28.8	31.5	41.2	9.5	16.0	12.0	19.2
Chain-of-Thought	18.0	29.7	32.5	44.2	11.0	17.5	12.5	21.6
Tree-of-Thought	20.5	32.0	35.0	47.3	11.0	17.2	12.0	20.6
STOC-TOT	26.5	38.0	42.0	55.3	11.5	18.0	14.5	22.0
w/o constrained decoding	24.0	35.5	38.5	51.0	11.5	18.0	14.0	22.0

 [2020\)](#page-8-0) and GPT-4[\(OpenAI et al.,](#page-8-9) [2024\)](#page-8-9) from Ope- nAI, LLaMa 2-13B [\(Touvron et al.,](#page-9-5) [2023\)](#page-9-5), LLaMa 2-70B, and LLaMa 3-8B from MetaAI. Due to the lengthy running time, LLaMa 2-70B was not tested on the MusiQue dataset. For all models, We set 415 the temperature to 0.5 , top_k to 1.0, and maximum number of iterations to 5.

417 4.2 Evaluation Metric

 Following the metrics in [\(Yang et al.,](#page-10-4) [2018\)](#page-10-4), we use Exact Match and F1 score as two evaluation metric. For an answer a given by our framework, the Exact Match score equals 1 if the answer span matches the golden answer exactly and 0 otherwise. The F1 metric measures the average overlap between the prediction and ground truth answers.

⁴²⁵ 5 Results

426 5.1 Overall Results

 We compare STOC-TOT with LLM baselines on the HotpotQA dataset and the MusiQue dataset and present our results in Tables [1](#page-5-0) and [2.](#page-5-1) The backbone LLMs in our experiments include GPT3.5, GPT4, Llama2-13B, Llama2-70B, and Llama3-8B. Due to time constraints, we only tested with Llama2- 70B on the HotpotQA dataset. On the HotpotQA dataset, STOC-TOT attains an on-average increase in performance of over 6 % compared with vanilla prompting on GPT models, and the improvement goes up to 11% when we further implement STOC- TOT with constrained decoding. On the more chal-lenging MusiQue dataset, we still see an increase

in performance of STOC-TOT compared with the **440** other baselines, most notably on GPT4, where we **441** observe an 11.5% EM improvement (from 31.50 to **442** 42.0). **443**

Comparison with Tree-of-Thought STOC-TOT **444** surpasses the original Tree-of-Thought prompting **445** by 7% with the GPT4 model on both tested datasets. **446** For LLMs with inferior reasoning ability, such as **447** LLaMa2-8B, we still observe a performance im- **448** provement, even on the harder MusiQue dataset. **449** These results suggest that STOC-TOT is more ef- **450** fective at forming and selecting reliable reasoning **451** paths under complex reasoning scenarios. **452**

Constrained Decoding Even though the LLM's **453** reasoning ability can be improved by reasoning **454** prompting, such techniques have little help in pre- **455** venting hallucination. However, STOC-TOT im- **456** plements constrained decoding, which makes the **457** model much more grounded to evidence when an- **458** swering the question, effectively addressing hallu- **459** cination issues and improving the overall perfor- **460** mance of our framework. 461

5.2 Ablation Study **462**

Sensitivity to Demonstration Question Type **463** We study the effect on STOC-TOT performance 464 when different types of demonstration questions 465 are provided in the prompt template. The Hot- **466** PotOA dataset specified two types of questions. 467 The "Bridge" question contains a "bridge entity" **468** that connects the question and the final answer. In **469**

Table 3: Performance of STOC-TOT with different prompt types on the HotpotQA dataset in terms of EM score. "Com" represents comparison questions, and "Bri" represents bridge questions.

Table 4: Question Type Examples. On the left side, the bridging entity is highlighted in red, and the final question is highlighted in orange. On the right side, entities that are being compared are highlighted in blue.

Table 5: Reasoning Type Examples. On the left side, the entity in red needs to be found before solving the question in orange. On the right side, questions with parallel reasoning contain parts (highlighted in blue) that can be solved in arbitrary order.

Sting?

What distinction is held by the former NBA player who was a member of the Charlotte Hornets during their 1992-93 season and was head coach for the WNBA team Charlotte

 contrast, the "Comparison" question requires the model to compare two entities of the same type. Of the 200 questions in our evaluation set, 34 are com- parison questions, and 166 are bridge questions. Examples of bridge and comparison questions are in Table [4.](#page-6-0)

 We examined STOC-TOT performance under the two different question types, each with a differ- ent prompt template: one containing only a com- parison question as an example and the other con- taining only a bridge question as an example. We provide the content of our templates in Appendix [A.](#page-11-0) Results are shown in Table [3.](#page-6-1) We observe that the difference in prompt templates influences the per- formance of our framework under different ques- tion types by a small margin. The comparison ques- tions are generally easier to solve, and STOC-TOT performs better on comparison questions than on bridge questions. STOC-TOT will handle compari- son questions better if the prompt template contains comparison questions and vice versa.

 Question and Reasoning Types We examine STOC-TOT, Tree-of-Thought prompting, and Chain-of-Thought prompting by comparing their performance under different question-type settings. Detailed results are shown in Figure [3\(](#page-7-0)a). STOC- TOT performs better at both Bridge Questions and Sequential Questions, suggesting that STOC-TOT can avoid reasoning dead-ends and is better at forming intermediate reasoning lines. **499**

We also conduct an in-depth analysis of the rea- 500 soning types in the existing MHQA datasets by 501 randomly selecting 100 questions from our testing **502** set. The questions are roughly divided into two cat- **503** egories: 1) tree-like parallel reasoning and 2) chain- **504** like sequential reasoning. Questions with parallel **505** reasoning contain two or more reasoning paths that **506** can be solved arbitrarily. Questions with sequential **507** reasoning follow a strict reasoning chain, and all **508** the sub-questions must be solved to form the cor- **509** rect reasoning process. All comparison questions **510** are parallel reasoning, but some bridge questions **511** contain parallel reasoning. Examples of sequential **512** and parallel reasoning questions are in Table [5.](#page-6-2) Out **513** of the selected 100 questions, 59 questions were **514** Sequential and 41 questions were Parallel. Results **515** are shown in Figure [3\(](#page-7-0)b). STOC-TOT performs bet- **516** ter on both reasoning types, especially on questions **517** containing parallel reasoning. This suggests that **518** STOC-TOT's stochastic way of forming the tree is **519** very effective when solving questions containing **520** multiple reasoning paths. 521

Performance and Hops As the number of hops 522 increases in a question, the reasoning line gets **523** more complex and varied. Figure [4](#page-7-1) shows the **524** performances of different prompting techniques **525** on questions in the MusiQue dataset with differ- **526**

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Figure 3: Performace comparison of Chain-of-Thought, Tree-of-Thought, and STOC-TOT on questions of different question types (Left) and reasoning types (Right). Experiments were done on the HotpotQA dataset.

Figure 4: Performance comparison of CoT, ToT, and STOC-TOT on different number of hops in the question. Experiments done in the MusiQue dataset.

Figure 5: Ratio of different categories in error cases, on the HotpotQA dataset.

 ent numbers of hops. STOC-TOT performs best in all categories, demonstrating our framework's superior ability to deal with complex reasoning sce- narios. This ablation study was conducted only on GPT4, as other models performed poorly on 3-hop and 4-hop scenarios, regardless of the reasoning prompting technique used.

 Error Analysis We conduct a detailed analysis of the errors made by our framework on GPT3 and GPT4, and present our results in Figure [5.](#page-7-2) We cate-gorize the errors into four types: (1) No Answer: our framework did not come up with an answer **538** for the question due to not finishing the reasoning **539** process; (2) Intermediate Answer: our framework **540** came up with an answer for one of the intermediate **541** hops instead of for the final question; (3) Wrong **542** Answer: our framework came up with an answer **543** that is neither the final answer nor one of the inter- **544** mediate answers; (4) Semantically Correct: our **545** framework came up with the right answer, but did **546** not have an exact match with the final answer. Ap- **547** pendix [B](#page-11-1) shows examples of each error category. **548** Large amounts of error cases were correct answers **549** with extra wording or hallucination errors, signal- 550 ing potential improvements over our constrained **551** decoding scheme. Reasoning process errors, in- **552** cluding no answer and intermediate answer, make **553** up only 25% of the total error cases. This result **554** shows that our framework is capable of building a **555** robust reasoning process for complex questions. **556**

6 Conclusion **⁵⁵⁷**

This paper proposes STOC-TOT, a stochastic **558** tree-of-thought reasoning framework with con- **559** strained generation for multi-hop question answer- **560** ing. STOC-TOT is specialized in dealing with **561** complex reasoning scenarios in natural language **562** tasks. Experiments on two benchmark datasets **563** show that our framework outperforms previous rea- **564** soning prompting techniques with multiple Large **565** Language Models. Detailed analysis shows that our **566** framework is capable of building a robust reasoning **567** process given different types of questions. Further **568** research can aim to enhance the reliability of our **569** framework by proposing better validity evaluation **570** schemes and more effective methods for improving 571 groundedness and preventing hallucination. **572**

⁵⁷³ Limitations

 Our framework relies on initiating multiple model instances and requires multiple prompts per round. The repetitive callings impose heavy time costs for our framework, even after implementing our para- phrase module. Another limitation comes from how we generated sub-questions. Currently, we di- rectly prompt the model to generate sub-questions. A more complex standard can be used to increase the quality of the sub-questions generated. Also, more extensive experiments should be provided, including experimenting on other different datasets and case studies.

⁵⁸⁶ Ethics Statement

 This research adhered to the ethical standards and best practices outlined in the ACL Code of Ethics. Language Models can sometimes produce illogi- cal or inaccurate reasoning paths, so their outputs should be cautiously used. The outputs are only examined to understand how a model arrives at its answers and investigate why it makes certain errors. All experiments used publicly available datasets from previously published works and did not involve ethical or privacy issues.

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A Prompt Templates

 Sub Question Generation Template The prompt template containing one comparison question and one bridge question is given below:

 prompt: Break a question into high-quality sub- questions that are easier to answer. Here are two examples as guidelines:

 "Question: Are Tokyo and Busan in the same coun- try? Thought 1: I could either find which country Tokyo is located in, or which country Busan is located in. Sub Question 1-1: Which country is Tokyo located in? Sub Question 1-2: Which coun-try is Busan located in?"

 "Question: Tokyo is located in the country that has what colors present on its national flag? Thought 1: I need to first find out which country Tokyo is located in. Sub Question 1-1: Which country is Tokyo located in?"

 Only give out your thought process and current- level sub-questions. Do not give out answers to your questions. Question: *Given Question*. Thought 1:

 Prompt-based Constrained Generation Tem-**plate** The prompt template at answering time is given below:

 prompt: Given a question and a list of evidence that may of help, give your answer directly, using words only from the vocabulary bank, without any explanations.

 Question: *Given Question*. Evidence as reference: *Given Evidence*. Vocabulary Bank: *Given Vocabu-lary*. Answer:

B Examples of the Error Cases

880 •Type-2: Intermediate Answer

Question:

 Where does the hotel and casino located in which Bill Cosby's third album was recorded? *Answer* given by STOC-TOT on GPT4: Las Vegas. *Golden Answer*: Las Vegas Strip in Paradise.

890 •**Type-3: Wrong Answer**

Question:

 Aside from the Apple Remote, what other device can control the program Apple Remote was originally designed to interact with?

•Type-4: Semantically Correct **902**

Question: **904**

