
Weight-Space Geometry of Offline Reasoning Training

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Abstract

Offline reinforcement-learning losses (RFT, RIFT, DFT, Offline GRPO, DPO) are widely used to distill reasoning from large teachers into smaller students, and are typically compared on downstream accuracy alone. We ask whether they are mechanistically distinct or converge to a similar weight update. Training six methods (SFT, RFT, DFT, RIFT, Offline GRPO, DPO) on identical math rollouts from a single base model (Qwen3-4B) with attention-only LoRA, we analyze the resulting deltas via cosine similarity, principal-angle subspace analysis, linear mode connectivity, and CKA. We observe: (i) SFT, RFT, and RIFT have nearly colinear weight deltas (cosine ≥ 0.97 , top-1 principal angle $\sim 7^\circ$ median over 144 modules) and comparable GSM8K accuracy (87–88%, $n=1319$; pairwise McNemar $p \geq 0.15$); (ii) DFT diverges further in direction than any reward-weighted method despite using the same data; (iii) Offline GRPO adds a substantial component orthogonal to the SFT direction ($\sim 67\%$ globally, up to $\sim 86\%$ in late layers) while staying in the SFT loss basin; (iv) DPO sits in a near-orthogonal subspace, shows a mode-connectivity barrier, and collapses late-layer CKA to ~ 0.46 . DPO also reaches the highest accuracy in our protocol on both GSM8K (93.5%, McNemar $p < 10^{-9}$ vs. each other method) and AIME26 (30.0% vs. 3.3–10.0%); its training uses a $10\times$ smaller learning rate than the others (the standard convention), so the update-norm and accuracy gaps reflect loss-function and optimizer choices jointly, and a learning-rate-matched DPO comparison is left for future work.

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1. Introduction

Reasoning distillation has become a standard recipe for teaching small models to solve math and code tasks: a strong teacher generates rollouts, and a student is trained on them with one of a rapidly growing list of offline objectives. The past year alone introduced RIFT (Liu et al., 2026), Offline GRPO (KRAFTON AI, 2025), DFT (Wu et al., 2025), LUFFY (Yan et al., 2025), and DAPO (Yu et al., 2025), alongside an established preference-learning family — DPO (Rafailov et al., 2023), KTO (Ethayarajh et al., 2024), IPO (Azar et al., 2023), and NCA (Chen et al., 2024) — each accompanied by claims that its specific loss formulation is responsible for accuracy gains over plain SFT.

These methods are compared almost exclusively by benchmark accuracy. What they do to the model is unknown: do different losses produce weight updates that point in the same direction, or qualitatively different ones? The distinction matters for both practitioners (which loss is worth implementing?) and interpretability researchers (does “offline RL” name a single mechanism or a family?).

We present a controlled weight-space comparison of offline reasoning losses: identical rollouts, identical base model (Qwen3-4B-Instruct), shared LoRA initialization, six methods (DPO uses a smaller learning rate per its codebase convention, see §2). Following recent weight-space studies of fine-tuning (Arturi et al., 2025; Soligo et al., 2025; Zhong & Raghunathan, 2025; Ward et al., 2025), we analyze each method’s LoRA delta ΔW rather than its outputs.

Our contributions are: (1) reward-weighted losses (SFT, RFT, RIFT) converge on essentially the same direction in weight space (cosine ≥ 0.97) and produce GSM8K accuracies that are non-different by exact McNemar’s test ($p \geq 0.15$, $n=1319$); (2) DFT, despite being a one-line modification of SFT, produces a more distinctive update than any explicitly reward-weighted method; (3) Offline GRPO adds a quantifiable orthogonal component (globally 67%, rising to $\sim 80\%$ in late layers) while staying in the same loss basin as SFT/RIFT; (4) DPO sits in a near-orthogonal subspace with higher effective rank, a sharp linear-mode barrier, and reaches the highest pass@1 on both GSM8K and AIME26 in our protocol; we report this with the caveat that DPO uses a $10\times$ smaller learning rate, so the loss formulation

Table 1. Offline reasoning losses studied. “Neg.” = uses negative samples; “Rew.” = uses scalar reward; “Ref.” = needs a reference policy.

Method	Neg.	Rew.	Ref.	Key idea
SFT	–	–	–	MLE on all roll-outs
RFT	filter	impl.	–	MLE on positives
DFT	down-w.	–	–	$\mathcal{L} \cdot \text{sg}(\pi_\theta)$
RIFT	weight	yes	–	Reward-weighted MLE
Off. GRPO	yes	yes	yes	Group-relative adv.
DPO	paired	impl.	yes	Contrastive log-ratio

and optimizer setting cannot be cleanly separated here.

2. Setup

Data. All methods share one set of rollouts: DeepScaleR prompts ($\sim 40k$ verified math (Agentica, 2025)), teacher DeepSeek-V4-Flash, $K=4$ CoT completions/prompt, binary `math-verify` reward. Reference-policy methods use π_{base} . DPO consumes $\sim 1.8K$ (chosen, rejected) pairs vs. $\sim 75K$ rows for the rest. Identical rollouts is the central control.

Methods. Table 1 summarizes the six losses. With $\ell_i = -\log \pi_\theta(y_i | x)$ shorthand for the per-sequence NLL: SFT = $\sum_i \ell_i$ on all i ; RFT (Yuan et al., 2023) = $\sum_{i:r_i=1} \ell_i$ on positives only; DFT (Wu et al., 2025) = $\sum_t \text{sg}(\pi_\theta(y_t | y_{<t}, x)) \ell_t^{\text{tok}}$ down-weights confident tokens; RIFT (Liu et al., 2026) = $\sum_i (1 - r_i \lambda) \ell_i$ is a linear-in-reward surrogate that admits negatives; Offline GRPO (KRAFTON AI, 2025; Shao et al., 2024) = $\sum_i \hat{A}_i \ell_i$ with $\hat{A}_i = r_i - \bar{r}_g + b$; DPO (Rafailov et al., 2023) = $-\log \sigma\left(\beta \left[\log \frac{\pi_\theta(y_w)}{\pi_{\text{ref}}(y_w)} - \log \frac{\pi_\theta(y_l)}{\pi_{\text{ref}}(y_l)}\right]\right)$ on (chosen y_w , rejected y_l) pairs.

Training. Qwen3-4B-Instruct-2507, LoRA on attention projections (`q, k, v, o_proj`; rank 32, $\alpha=64$, dropout 0; 144 modules over 36 layers). Effective batch 32, cosine schedule, 5% warmup, wd 0.01, grad-clip 1.0, seed 42, bf16. Peak LR 5×10^{-6} for all but DPO (5×10^{-7} , codebase convention; higher diverges). DPO: sigmoid loss, $\beta=0.1$; Offline GRPO: additive bias 0.1 on the centered advantage, no probability weighting, no explicit KL. 1,500 steps; we report step 1,000 uniformly.

Analysis. Let $\Delta W^{(m)} = B^{(m)} A^{(m)}$ be the stacked LoRA delta of method m . We measure: (i) global/per-layer cosine $\langle \Delta W^{(m)}, \Delta W^{(m')} \rangle / \|\Delta W^{(m)}\| \|\Delta W^{(m')}\|$; (ii) per-layer SVD (effective rank, principal angles between top- k subspaces); (iii) linear mode connectivity (Frankle et al., 2020): masked-answer CE on GSM8K along $\alpha \Delta W^{(m)} + (1-\alpha) \Delta W^{(m')}$; (iv) CKA (Kornblith et al., 2019) of

merged-model hidden states.

3. Results

3.1. Downstream accuracy

Figure 3 (appendix) reports greedy pass@1 on full GSM8K ($n=1319$) and AIME26 ($n=30$). SFT/RFT/DFT/RIFT/Offline GRPO sit at 87.3–88.2% on GSM8K, pairwise non-different by exact McNemar ($p \geq 0.15$); DPO reaches 93.5% ($p < 10^{-9}$). On AIME26 the ordering repeats but $n=30$ is underpowered (SFT–DPO $p=0.07$). DPO trains at a $10\times$ smaller LR with $\sim 40\times$ fewer rows, so we treat the gap as suggestive. Llama-3.2-3B replicates the geometry and the 5–7 point DPO accuracy edge.

On-policy RL preserves accuracy; SFT-style loses it.

Re-measuring greedy pass@1 for the on-policy methods (Table 2, our adapters, same protocol) shows their reward-orthogonal updates (§3.4) do *not* cost accuracy: Online GRPO/DAPO and DPO all stay at the base instruct model’s 93–94% on GSM8K, whereas SFT and Offline GRPO drop to $\sim 87\%$ (below base). Online GRPO is best on AIME26 (20.0%).

Method	GSM8K	AIME26
Base instruct	94.0	16.7
SFT / Offline GRPO	87.6 / 87.3	6.7 / 6.7
DPO	94.2	13.3
Online GRPO	93.7	20.0
Online DAPO	93.3	16.7

Table 2. Greedy pass@1 (%) for our consistently-trained adapters; GSM8K $n=1319$, AIME26 $n=30$. SFT-direction methods sit below the base model; reward-orthogonal methods match or beat it.

3.2. Weight-space convergence

Figure 1 shows the cosine similarity matrix between global LoRA deltas. Three regimes are visible. *First*, SFT, RFT, and RIFT form a tight cluster: the SFT–RFT, SFT–RIFT, and RFT–RIFT cosines are 0.977, 0.967, 0.969. Filtering negatives (RFT) and reward-weighting them (RIFT) does not measurably change the direction of the update relative to plain SFT on the union; it only adjusts the step size, with $\|\Delta W\|_F$ ranging from 2.82 (RFT) to 3.04 (RIFT). *Second*, DFT, which differs from SFT by a single multiplicative factor on the loss, sits at cosine 0.572 to SFT and 0.536 to RIFT — a larger directional change than any explicitly reward-weighted method. *Third*, DPO is orthogonal to everything: cosine to SFT, RFT, and RIFT all fall in [0.057, 0.065]. Offline GRPO occupies an intermediate position (cosine ≈ 0.74 to the SFT cluster).

The per-layer view (Figure 4) decomposes this further. SFT/RFT/RIFT pairs are essentially flat above 0.95 at every

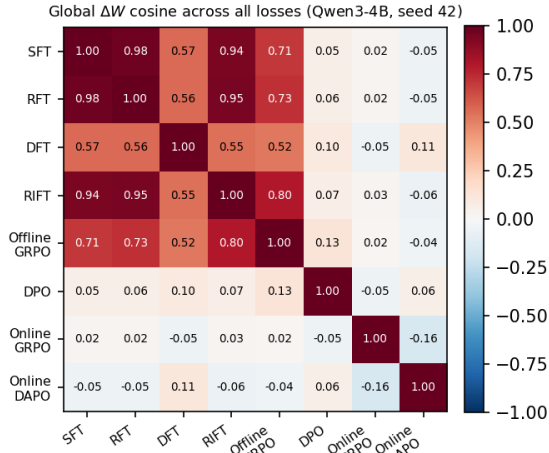


Figure 1. Global ΔW cosine across all eight losses (Qwen3-4B, seed 42; all adapters trained in one consistent space). Reward-weighted SFT/RFT/RIFT cluster (0.94–0.98); DFT intermediate (~ 0.55); *Offline* GRPO at 0.71–0.80 to the cluster; DPO near-orthogonal (≤ 0.13). The two *on-policy* methods, *Online* GRPO and *Online* DAPO, are each near-orthogonal to every offline loss and to each other (-0.16); orthogonal-fraction off SFT is 0.69 (offline GRPO) vs. 0.998/0.995 (online GRPO/DAPO). On-policy sampling, not the group-relative loss, drives the departure from SFT.

layer. SFT–GRPO drops gradually with depth. SFT–DFT is bimodal — close to 1 at certain bottleneck layers and well below 0.5 at others. SFT–DPO hovers near zero throughout. The visible drop on layers 34–36 across all pairs reflects the small-norm tail of LoRA updates in the last decoder block; we treat this as a LoRA artifact rather than a finding.

3.3. Subspace analysis

Per-layer SVD lets us go beyond a single direction and ask whether two methods adapt the same low-dimensional subspace. We report principal angles between the top-10 left singular vectors of each $\Delta W^{(m)}$ at the same module. Smaller angles mean shared subspace.

Aggregating across all 144 attention modules (top-10 left singular vectors per module), median top-1 principal angles are 6.7° (SFT–RFT), 8.2° (SFT–RIFT), 18.5° (SFT–Offline GRPO), 26.7° (SFT–DFT), and 54.6° (SFT–DPO); the median worst (top-10) angles are 36° , 40° , 76° , 85° , 90° in the same order. SFT–DPO IQR for the worst angle is $[89.6^\circ, 89.8^\circ]$: essentially every module is orthogonal at every singular index. The reward-weighted cluster shares the top of its subspace with SFT to within $\sim 10^\circ$; GRPO and DFT partially overlap; DPO does not.

The effective rank, averaged over all 144 modules, is ~ 16 for SFT, RFT, DFT, and RIFT, 14.8 for Offline GRPO, and 24.5 for DPO. DPO writes into a higher-dimensional subspace, but, given its $13\times$ smaller Frobenius norm, with

much smaller singular values; together with the orthogonality to SFT, this suggests DPO learns a different decomposition of the same projection matrices rather than a low-rank refinement of SFT.

To quantify how much of Offline GRPO’s update is genuinely new direction, we project ΔW^{GRPO} onto the SFT direction at every adapted module and report $\|\Delta W^{\text{GRPO}} - \Pi_{\text{sft}} \Delta W^{\text{GRPO}}\|_F / \|\Delta W^{\text{GRPO}}\|_F$. Globally this is 0.67; per layer it grows from ~ 0.55 in middle blocks to 0.79–0.86 in the final five blocks — the same layers where CKA diverges (Section 3.6).

Top-1 singular directions. The rank-1 approximation $\Delta W \approx \sigma_1 u_1 v_1^\top$ isolates the single most important output direction u_1 each loss writes into. Mean $|\langle u_1^m, u_1^{m'} \rangle|$ over 144 modules is 0.97–0.98 within SFT/RFT/RIFT, 0.78–0.80 to Offline GRPO, 0.64–0.67 to DFT, and 0.11 to DPO. Right singular vectors v_1 (input directions) converge much more tightly: 0.99–1.00 for non-DPO pairs, 0.94 for DFT, 0.66–0.70 for DPO. All methods (except DPO) read from nearly the same input subspace; they differ in how they transform it.

3.4. Seed and learning-rate sensitivity

The colinearity above is at a *single* seed, conflating loss agreement with shared-init agreement. We disentangle by training each loss at two seeds (42, 123) and three LRs (5×10^{-7} , \dots , 5×10^{-5}); $\Delta W = (\alpha/r)BA$ is gauge-invariant, so its cosine is genuine.

Seed rotates ΔW more than the loss — but only on the input side. At a fixed seed SFT–RFT are colinear (cosine 0.996, angle 3.7°), yet the *same loss at two seeds* has cosine only 0.07 (5×10^{-7})–0.36 (5×10^{-5}). Cause: LoRA’s random A init — across seeds the top-1 *output* direction u_1 still agrees at 0.99 while the *input* direction v_1 agrees at 0.07 (median top-8 angle 26° vs. 76° for unrelated runs). Functionally the seeds are the *same* solution: interpolating their deltas shows no barrier (midpoint $+0.004$). So the cross-method colinearity is partly shared-init, but convergence onto a common output subspace is seed-robust (Figure 2).

Learning rate changes direction, not just magnitude. A $10\times$ LR step rotates ΔW (cosine ≈ 0.55) and grows its norm only $\sim 3\times$ — not a pure rescaling, which sharpens the caveat on the $10\times$ -smaller-LR DPO comparison.

Online GRPO is far more orthogonal than offline GRPO. We also train *online* GRPO under the same LoRA recipe (on-policy rollouts, group-relative advantage, `math.verify` reward; 600 steps, 8 generations/prompt, lr 5×10^{-6} , seed 42) — the comparison the original protocol could not produce. The resulting update is almost entirely orthogonal to the SFT/RFT cluster: cosine 0.025 to SFT and 0.024 to

RFT, with an orthogonal fraction of 0.998 off the SFT direction (Figure 1), versus 0.67 for *offline* GRPO (§3.2). Its Frobenius norm is $\sim 10\times$ smaller than SFT’s at the same LR (0.30 vs. 2.84), echoing the small-norm regime of DPO. On-policy sampling thus moves the update off the shared SFT subspace far more than the offline group-relative loss does, indicating that the SFT/offline-RL directional convergence is partly a consequence of training on the *same fixed rollouts*: replacing them with on-policy samples largely breaks it.

3.5. Linear mode connectivity

We linearly interpolate LoRA deltas, merge into the base, and measure the per-token cross-entropy of the gold `\boxed{answer}` continuation right after the prompt on GSM8K. The metric is length-sensitive: DPO produces longer, structured CoTs (median 5100 vs 1100 chars on correct AIME26; verification steps in 9/9 correct DPO solutions vs 0/3 SFT), inflating per-token NLL of the bare boxed answer. Offline GRPO \rightarrow RIFT improves monotonically (4.93 \rightarrow 2.25) and SFT \rightarrow Offline GRPO worsens monotonically (2.06 \rightarrow 4.93): one basin. RIFT \rightarrow DPO shows a sharp non-monotonic barrier above $\alpha=0.5$ (3.82 \rightarrow 7.06 \rightarrow 8.64): even discounting length, linear interpolation destroys the solution.

3.6. Representational similarity

CKA on hidden states (Figure 6, 100 GSM8K prompts) confirms the weight-space picture. SFT–RIFT CKA stays above 0.99 at every layer; SFT/RIFT–Offline GRPO drop to ~ 0.85 in the final layer (GRPO reshapes output-facing layers); Offline GRPO–DPO and DFT–DPO start near 0.93 and collapse to ~ 0.45 from layer 25 onward. A logit-lens probe gives a complementary null — mean prediction depth is 35.3–36.0 out of 36 for every method — but this is partly forced by attention-only LoRA leaving MLPs frozen, so it should not be read as a finding about the losses.

4. Discussion

Reward-weighted MLE is SFT, plus DFT is the surprise. SFT, RFT, and RIFT differ only in how they handle negative samples (drop, weight, or include uniformly), yet the resulting LoRA deltas have cosine ≥ 0.97 , principal angles $< 25^\circ$, and indistinguishable per-layer CKA, and they sit within 1 percentage point of each other on full GSM8K. The Frobenius norms differ by up to 7%. If RIFT outperforms SFT at the same step count, our results suggest the explanation lies in magnitude (effective step size in the SFT direction), not direction — a longer or higher-lr SFT run should close the gap. DFT, by contrast, has cosine ~ 0.55 to SFT/RIFT despite using *less* information than they do (no reward, no filtering): self-weighting by $sg(\pi_\theta)$ reweights *which* examples drive the update in a way explicit reward

does not, yet leaves the loss basin unchanged.

Offline GRPO shifts direction but stays in basin; online GRPO does not. Among offline rewards, only Offline GRPO substantially shifts direction from SFT (cosine 0.73; orthogonal-fraction 0.67, ~ 0.8 late; angles up to 59°), yet barrier-free interpolations keep it in the SFT/RIFT basin. *Online* GRPO goes much further — orthogonal fraction 0.998 (Figure 1) — so the SFT/offline-RL convergence is partly an artifact of shared fixed rollouts, which on-policy sampling breaks.

DPO sits apart, geometrically and on accuracy. DPO occupies a near-orthogonal subspace (74° – 89°), a higher-rank update with much smaller Frobenius norm, a sharp linear-mode barrier, and late-layer CKA ~ 0.45 ; it also reaches the highest pass@1 on GSM8K (93.5%) and AIME26 (30.0%). It trains at a $10\times$ smaller LR, so its norm/accuracy gaps are entangled with the optimizer — correlation worth a LR-matched follow-up, not a causal claim. Extending the weight-space view to the wider contrastive family (IPO, KTO, SimPO, Cal-DPO) is left open.

Limitations. Single domain and checkpoint; attention-only LoRA; greedy-only on small AIME26 ($n=30$). DPO uses $10\times$ smaller LR and $\sim 40\times$ fewer rows, so its norm/accuracy gaps are entangled with the optimizer. *Online* GRPO is reported at lr 5×10^{-6} , seed 42 (§3.4); the remaining LR/seed cells, a matched accuracy comparison, and calibrated DPO variants (KTO, IPO, SimPO) are left to a fuller sweep. Code, adapters, and analysis scripts are released.

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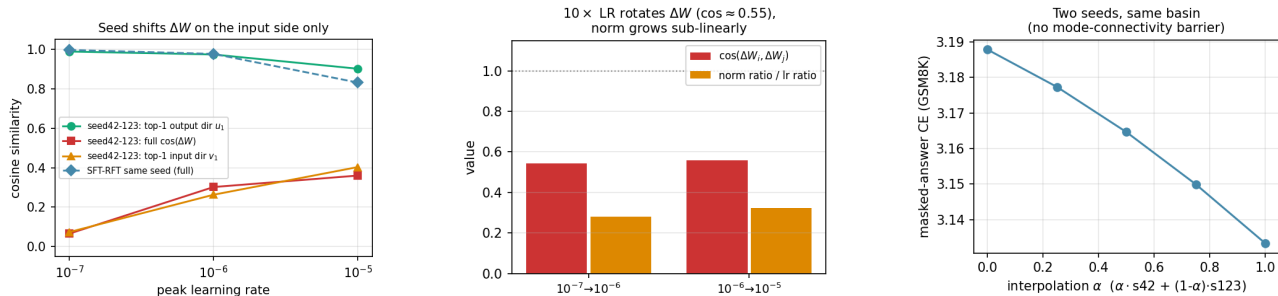


Figure 2. **Seed and learning-rate sensitivity (SFT, Qwen3-4B).** *Left:* across two seeds the output direction u_1 stays aligned (~ 0.99) while the input direction v_1 and full cosine are low at small LR and rise with LR; dashed shows SFT-RFT at a fixed seed. *Middle:* a $10 \times$ LR step rotates ΔW (cosine ≈ 0.55) and grows its norm sub-linearly — LR is not a pure rescaling. *Right:* interpolating the two seeds’ deltas shows no loss barrier — different weights, same basin.

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A. Supplementary figures

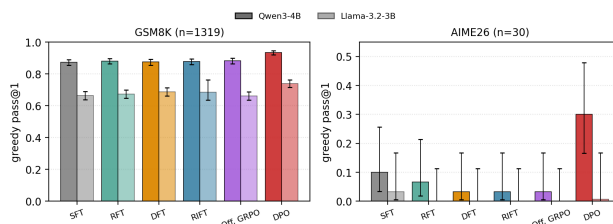


Figure 3. Greedy pass@1 with Wilson 95% CI bars on GSM8K ($n=1319$) and AIME26 ($n=30$). Dark bars: Qwen3-4B-Instruct. Light bars: Llama-3.2-3B-Instruct. On both architectures, DPO sits noticeably above the SFT/RFT/DFT/RIFT/Offline GRPO cluster on GSM8K (Qwen3: McNemar $p < 10^{-9}$ vs. each other method); Llama-3.2-3B AIME26 floors near zero at this model scale.

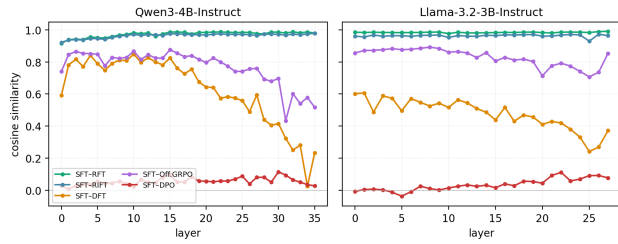


Figure 4. Per-layer cosine similarity of LoRA deltas to SFT, on Qwen3-4B (left, 36 layers) and Llama-3.2-3B (right, 28 layers). SFT/RFT/RIFT track each other across all layers; Offline GRPO, DFT, and especially DPO diverge in deeper layers, with the same qualitative pattern on both architectures.

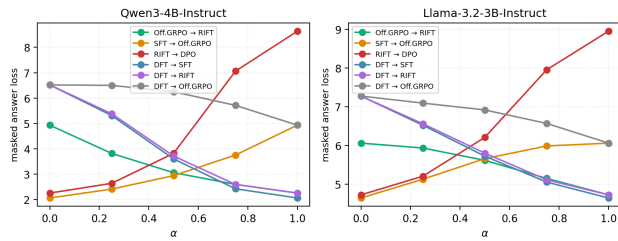


Figure 5. Linear mode connectivity (masked-answer CE on GSM8K) on Qwen3-4B (left) and Llama-3.2-3B (right). Same picture: SFT/Off.GRPO/RIFT/DFT pairs are barrier-free; RIFT \rightarrow DPO shows a sharp barrier above $\alpha=0.5$ on both architectures (DPO endpoint loss 8.64 Qwen3, 8.96 Llama32).

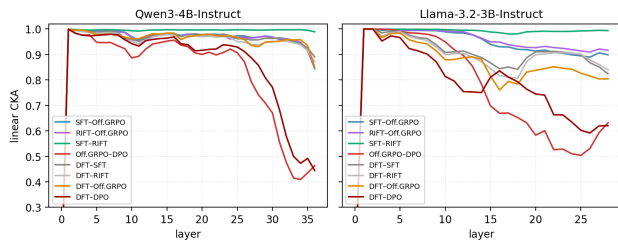


Figure 6. Linear CKA of hidden states across all blocks for selected method pairs on 100 GSM8K prompts: Qwen3-4B (left, 36 blocks), Llama-3.2-3B (right, 28 blocks). On both architectures: SFT/RIFT indistinguishable (> 0.99), Off.GRPO diverges in output-facing layers, and DPO collapses in the final third (Qwen3 ~ 0.45 , Llama32 ~ 0.62).