

BrandEval: A Two-Track Multi-Agent Benchmark for Risk-Sensitive LLM Crisis Communication

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Abstract

While large language models have improved on procedurally verifiable tasks, their behavior in high-stakes institutional crises remains under-evaluated because success depends on evolving stakeholder perceptions rather than a single verifiable answer. Existing benchmarks focus on static, single-turn competence and provide limited coverage of risk-sensitive, goal-directed communication under interaction. We introduce BrandEval, a two-track benchmark that pairs a rubric-based static diagnostic with BrandPolis, a dynamic multi-agent sandbox of competitive, partially observable markets. We also introduce Strategic Rationale, a lightweight decision workflow, and BrandSRD, a Chinese dataset of crisis-response decision points with human-validated preferences. Using BrandSRD, we build a reference SR-based Strategic Agent and study how communication styles affect long-horizon trust and tail risk. These resources enable controlled stress testing of LLM crisis communication, exposing failure modes and societal risks that single-turn evaluation may miss. BrandSRD, BrandEval, and BrandPolis will be released publicly.

1 Introduction

On social media, public-facing crisis communication can quickly shift beliefs about responsibility and safety, triggering cascading reactions that lead to very different long-term outcomes.¹ (Coombs, 2007b; Leskovec et al., 2007; Li et al., 2024). Framing theory (Entman, 1993) suggests that brands can shape crisis interpretation through language and narrative framing, implying that effective communication tools can help institutions manage crises by guiding perception, attribution, and remedy credibility (Hallahan et al., 2007). Recent gains on procedurally verifiable tasks suggest that LLMs

¹A recent fatal-crash case illustrates how delayed and opaque responses can amplify backlash. http://dianzibao.cb.com.cn/html/2025-01/13/content_334375.htm

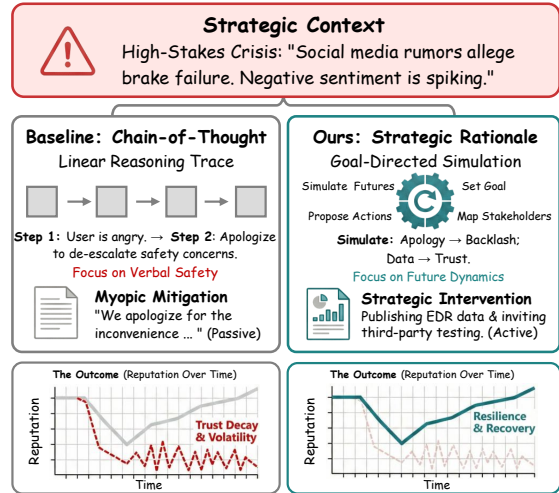


Figure 1: **Divergent Futures.** Different response formulations yield divergent long-horizon trust trajectories in simulation.

can produce optimizable Chain-of-Thought (CoT) traces, enabling more auditable and optimizable decision support for crisis communication (Wei et al., 2022; Jaech et al., 2024; Guo et al., 2025). Figure 1 shows that differences in message formulation can yield sharply different long-horizon trust trajectories under the same crisis.

Crisis outcomes depend on heterogeneous stakeholder interpretations over time and strategic competitor responses (Pendharkar, 2012; Ji et al., 2025), while manipulative framing can increase harm and polarization (Coombs, 2007a). LLM sandboxes like Generative Agents (Park et al., 2023) target everyday routines, not institutional crises where accountability, evidence, and de-escalation dominate. In practice, LLMs are already used in crisis-response workflows, from external early-warning platforms to internal compliance and risk management assistants². This heightens the need for controlled benchmarks that can stress-test crisis strategies under interaction. However, most existing LLM benchmarks still emphasize static, single-turn

²<https://www.dataminr.com>

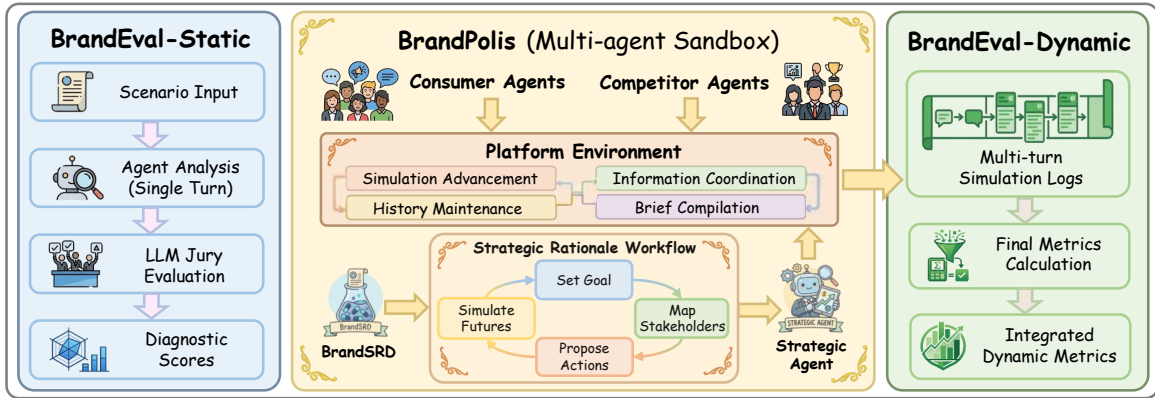


Figure 2: **Overview of BrandPolis and BrandEval.** BrandEval has Static and Dynamic tracks sharing a held-out scenario pool; Dynamic runs in BrandPolis. SR guides the Strategic Agent trained on BrandSRD.

062 evaluation, with limited coverage of the interactive
 063 and competitive dynamics of real crisis communi-
 064 cation (Grewal et al., 2025; Zhang et al., 2024).

065 To address this gap, we build **BrandPolis**, a
 066 multi-agent sandbox that evaluates LLM crisis com-
 067 munication under stakeholder feedback, competi-
 068 tor responses, and long-horizon trust and risk out-
 069 comes. We use **Strategic Rationale (SR)** to im-
 070 plement a transparent reference Strategic Agent in
 071 BrandPolis. In each round, SR guides the agent to
 072 set a verifiable goal and summarize the stakeholder
 073 state. The agent then drafts several publishable
 074 plans and selects one to publish based on the long-
 075 horizon trade-off between credibility and risk under
 076 BrandPolis feedback.

077 To evaluate such behavior, we develop **BrandE-**
 078 **val** with two components: a static strategic analysis
 079 task that diagnoses multi-stakeholder reasoning and
 080 a dynamic task that immerses agents in BrandPo-
 081 lis to track long-horizon trust and risk outcomes.
 082 Figure 2 summarizes our sandbox and benchmark
 083 setup. To support training and controlled stress
 084 testing, we build **BrandSRD**, a Chinese-language
 085 collection of crisis-response decision points from
 086 Chinese social-media crises, with human-validated
 087 supervision for alignment and evaluation in Brand-
 088 Polis. The main contributions of this work can be
 089 summarized as follows:

- 090 • We introduce BrandEval, a two-track bench-
 091 mark with a shared held-out scenario pool,
 092 where Static is scored offline and Dynamic
 093 runs in the BrandPolis sandbox.
- 094 • We construct BrandSRD, a Chinese dataset
 095 of crisis-response decision points with prefer-
 096 ence supervision and structured rationales to
 097 support a Strategic Agent for stress testing.
- 098 • We provide a reference Strategic Agent instan-
 099 tiated with the SR workflow that improves

BrandEval-Dynamic trust and stability out-
 comes over baselines.

2 Related Work

Recent advances in LLM agents with planning
 and social reasoning enable language-based sim-
 ulation of interactive social systems (Hao et al.,
 2023; Kosinski, 2023). Many approaches com-
 bine structured planning, opponent modeling, and
 explicit belief representations (Han et al., 2025),
 while iterative prompting methods such as Reflex-
 ion (Shinn et al., 2023) and ReAct (Yao et al.,
 2022) refine reasoning trajectories in multi-turn
 interaction. Multi-agent simulation has also been
 applied to commercial settings, including business
 decision making (Li et al., 2025; Hazenberg et al.,
 2025), commercial communication and market in-
 teraction (Karande et al., 2024), and quantifying
 perceptual gaps between brands and user-generated
 content (Gan et al., 2025). Recently, SandboxSo-
 cial models realistic social-network dynamics with
 multimodal agents (Touzel et al., 2025), and Gen-
 Sim scales up large social simulations (Tang et al.,
 2025). However, much of this line of work either
 prioritizes population-level emergence or is evalu-
 ated in settings that do not explicitly stress-test
 risk-sensitive crisis communication under multi-
 stakeholder feedback and competitor responses.

At evaluation time, static QA benchmarks miss
 multi-turn competence and are contamination-
 prone (Xu et al., 2024). Recent work reduces con-
 tamination through procedural generation of fresh
 instances (Fan et al., 2023; Kurtic et al., 2024)
 or by constructing benchmarks from time-varying
 real-world data such as historical knowledge snap-
 shots or user dialogues (Ouyang et al., 2025;
 Bayat et al., 2024). Multi-agent system (MAS)-
 based evaluation is expanding from general suites
 like MultiA-

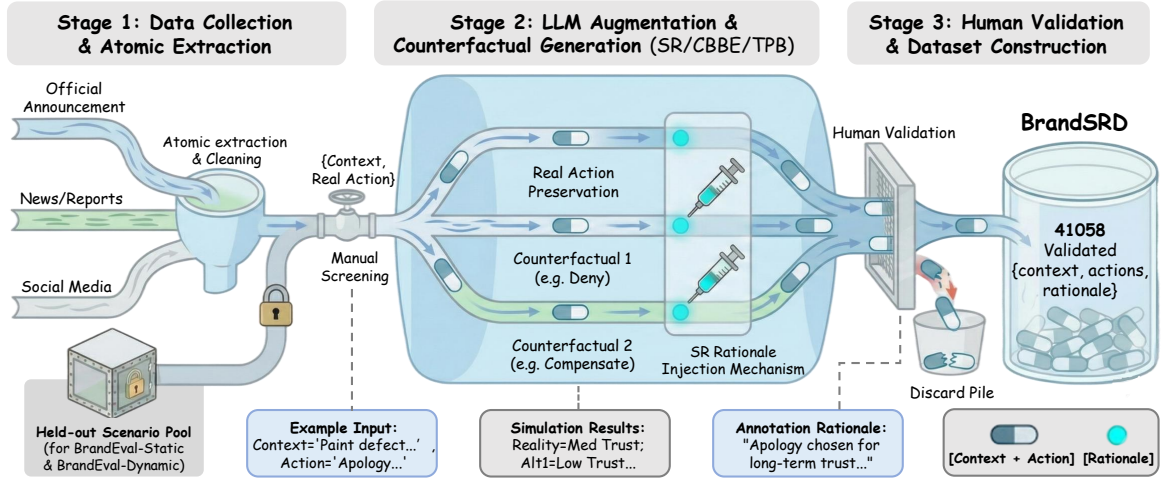


Figure 3: **BrandSRD construction pipeline.** Decision points are extracted from multi-platform data; counterfactual plans constrained by CBBE and TPB, together with structured rationales, are generated; preferences are calibrated via stratified human validation. A disjoint held-out pool is reserved for BrandEval.

gentBench (Zhu et al., 2025) to domain testbeds for commercial settings (Hazenberg et al., 2025). In parallel, crisis informatics and operational communication have developed benchmarks that evaluate practical crisis-management deliverables from social streams, such as situation assessment and information triage (Alam et al., 2021), crisis timeline extraction and summarization (Rajaby Faghihi et al., 2022), and online public opinion report generation (Yu et al., 2025). In contrast, BrandEval pairs a rubric-based static diagnostic with BrandPolis to stress-test decision policies under competitive multi-turn interaction, emphasizing accountability, verifiability, de-escalation, and long-horizon process health.

3 Strategic Rationale and BrandSRD

3.1 Strategic Rationale

Strategic Rationale (SR) is a structured prompting workflow used by the reference Strategic Agent in BrandPolis and the schema that BrandSRD supervision follows. Each round, the agent first states a verifiable goal that balances business needs with social responsibility; this goal then constrains subsequent planning and encourages commitments that remain credible under public scrutiny (Carroll, 1991). The agent then summarizes the stakeholder state, drafts publishable response candidates, and then selects and publishes the option that best balances long-horizon credibility and risk.

3.2 BrandSRD Construction

Dataset overview. BrandSRD is a Chinese-language dataset of crisis-response decision points. It is derived from user posts on three Chinese social-media platforms (Weibo, Douyin, and Xiaohong-

Table 1: **BrandSRD source distribution.** Counts of posts used to construct BrandSRD across 12 product domains and three platforms (XHS = Xiaohongshu).

Product	Weibo	Douyin	XHS	Total
Smartwatch	1078	786	482	2346
Refrigerator	1024	1125	741	2890
Air conditioner	1096	553	781	2430
Rice cooker	858	2517	676	4051
Smart door lock	1360	2268	449	4077
Translation pen	1265	1051	614	2930
Smartphone	1177	734	1847	3758
Television	1055	929	921	2905
Speaker	1606	563	1343	3512
Dishwasher	1721	580	465	2766
Personal computer	931	948	872	2751
Electric vehicle	5548	636	458	6642

shu) collected from 2023-12-15 to 2025-12-15, and supplemented with event context from public news reports and official announcements. Figure 3 summarizes the construction pipeline and the held-out scenario pool reserved for BrandEval. Each data record includes a context, the observed brand response, two model-generated counterfactual plans, a preference label, and a structured rationale under a risk-aware stakeholder rubric. Counterfactual generation is constrained by Customer-Based Brand Equity (CBBE) (Keller, 1993) and Theory of Planned Behavior (TPB) (Ajzen, 1991), and outputs are filtered through stratified human validation. In total, BrandSRD contains 41,058 validated records; Table 1 reports the source distribution.

Crowd Validation. We validate model-generated candidates via structured questionnaires on Credamo³. We draw a stratified sample of 1,000 instances, grouped five per questionnaire, and recruited 30 independent annotators per question-

³<https://www.credamo.com>

naire. Annotators read a crisis brief and three candidate plans, selected the best, and briefly justified their choices along three axes: handling thoroughness, one-year impact, and user acceptance. We use the majority-vote option as the crowd winner to measure how often the generator model’s preferred option aligns with human choice. Across instances, the model–crowd agreement rate is 78%. The mean winning vote share is 0.633. The mean top-two vote-share gap is 0.433. We use the questionnaire outcomes to guide manual screening and form the final BrandSRD dataset.

4 BrandEval Benchmark

BrandEval is a two-track benchmark for risk-sensitive organizational communication built from a shared held-out scenario pool. BrandEval-Static scores offline single-turn strategic analyses with a stakeholder rubric, while BrandEval-Dynamic evaluates long-horizon crisis communication in the BrandPolis sandbox via trust and risk trajectories.

4.1 BrandEval-Static Benchmark

BrandEval-Static is a diagnostic benchmark that evaluates a model’s capabilities in single-round communication and decision-making within isolated, static contexts.

Scenario Construction. We construct BrandEval-Static scenarios by taking the pre-reserved 1,000-post electric vehicle corpus as prototypes and turning them into self-contained case descriptions. Figure 4 summarizes the prototype pool’s topic-category and stakeholder composition, ensuring broad coverage of market dynamics, product issues, and user feedback. To mitigate leakage risk and protect sensitive identifiers, Gemini-2.5-Pro rewrites each prototype into a de-identified, neutral, self-contained evaluation case by removing identifiable details while preserving the commercial context, multi-stakeholder trade-offs, and the underlying events and claims. Human reviewers then screen the generated scenarios for commercial plausibility, yielding a 96.8% acceptance rate.

Task Formulation. For each scenario, the model under test acts as a strategic consultant. It receives a self-contained scenario description and outputs a comprehensive strategic analysis report. This report requires the model to analyze stakeholder impacts across consumer and brand, public

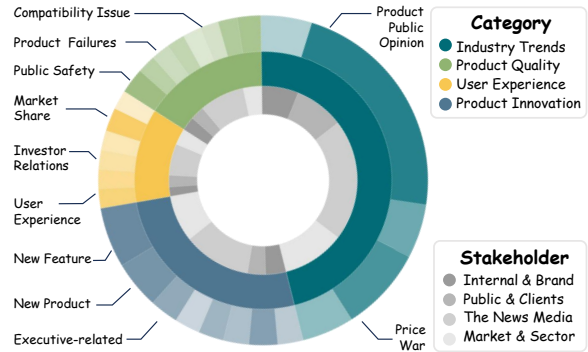


Figure 4: **BrandEval prototype distribution.** Topic and stakeholder composition of the 1,000-post electric vehicle prototype pool.

and media, and competitor dynamics, then synthesize trade-offs into an actionable recommendation. Model outputs are scored with a stakeholder-theory-inspired rubric (Freeman, 2010) to enable structured evaluation. These rubric dimensions are designed to probe evidence, accountability, and competitive reasoning that plausibly shape downstream perception and intent trajectories in BrandPolis, with this scoring serving as a scalable proxy for expert review (Liu et al., 2023).

Scoring Protocol. Given the open-ended nature of strategic reasoning, we score BrandEval-Static with a three-LLM judge panel and apply a lightweight calibration to reduce judge-specific offsets. GPT-5-mini, DeepSeek-v3.1, and Claude-4.5-Haiku independently score each strategic analysis on four rubric dimensions on a 1–10 scale. We map each judge to a shared scale via an affine transform estimated on a small calibration set, then average calibrated scores per scenario and dimension to obtain the panel score. To sanity-check the panel, we sample 300 Strategic Agent outputs, bundle five instances per questionnaire, and recruit 30 independent participants per questionnaire. Across these instances, the human-score standard deviation is 1.12, the mean absolute error between the calibrated panel mean and the human mean is 1.08 points, and the Pearson correlation is 0.64. We further find the judges are largely robust to superficial style and section-order changes, and that an evidence-sensitive audit variant more reliably separates verifiable strategies from specious ones, with details in the Appendix.

4.2 BrandEval-Dynamic Benchmark

BrandEval-Dynamic is designed as an integration test to evaluate a model’s ability to navigate crisis communication through long-horizon, multi-

276 turn interaction within our agent-based simulation, 324
277 tracking trust and risk outcomes. 325

278 **Scenario Initialization.** BrandEval-Dynamic 326
279 uses 50 scenarios selected from the shared held-out 327
280 scenario pool via stratified sampling over topics 328
281 and risk profiles. For each scenario, we treat 329
282 the evaluated model as the focal Strategic Agent 330
283 and simulate 20 rounds of interaction in the full 331
284 BrandPolis sandbox, including consumer agents, 332
285 competitor agents, and the platform environment. 333
286 We use a fixed horizon $T = 20$ supported by pilot 334
287 sensitivity sweeps and stress-regime checks. Each 335
288 model and scenario pair is run with $K = 5$ random 336
289 seeds, and we report seed-averaged metrics. 337

290 **Consumer Agents.** The population consists of 338
291 consumer agents whose static personas follow a 339
292 5×3 factorial design over decision drivers and 340
293 brand stances: five primary decision drivers (per- 341
294 formance, value for money, user experience, social 342
295 identity, and safety) (Engel et al., 1986), crossed 343
296 with three initial stance levels (supporters, neutrals, 344
297 detractors) (Gera and Neal, 2025) that may shift as 345
298 new crisis evidence updates their advocacy intent, 346
299 in line with cognitive dissonance effects (Festinger, 347
300 1957). Each agent maintains a five-dimensional 348
301 internal state that combines three perception dimen- 349
302 sions from CBBE (competence belief, value con- 350
303 gruence, emotional connection) with two intention 351
304 dimensions from TPB (purchase intent, advocacy 352
305 intent). Consumer states evolve via a first-order 353
306 exponential moving average driven by message- 354
307 derived impacts: 355

$$308 \quad \mathbf{V}_u^{(t)} = (1 - \lambda_u)\mathbf{V}_u^{(t-1)} + \lambda_u\gamma^{(t)} \tanh(\mathbf{X}_u^{(t)}) \quad (1) \quad 356$$

309 where $\lambda_u \in (0, 1)$ controls update responsiveness, 357
310 $\mathbf{X}_u^{(t)}$ is an auditable text-to-state impact signal, and 358
311 $\gamma^{(t)} \in [0, 1]$ is an evidence-consistency gate for 359
312 official claims. We treat $\mathbf{V}_u^{(t)}$ as simulation proxies 360
313 for belief and intention. 361

314 **Strategic Agents.** The strategic agents com- 362
315 prise a focal Strategic Agent and several competi- 363
316 tor agents, all operating under bounded rational- 364
317 ity (Simon, 1955). Competitor agents follow four 365
318 archetypes, Prospector, Defender, Analyzer, and 366
319 Reactor, which adapt Miles and Snow’s strategic 367
320 typology (Miles et al., 1978) into utility-driven per- 368
321 sonas with distinct goals and risk preferences. For 369
322 each scenario, we specify which competitor brands 370
323 are present and assign one archetype to each. The 371

Strategic Agent and all competitor agents alternate 324
between external observation, where they track top- 325
ics and platform-visible reputation proxies, and 326
internal monitoring of their own published commit- 327
ments. Evaluation tracks how actions shift belief 328
and intent trajectories, and the next-round prompt 329
is constructed from the market brief to turn current 330
market intelligence into a concrete strategic action. 331

Platform Environment. The platform runs in 332
discrete rounds and mediates exposure under atten- 333
tion scarcity. At round t , it collects brand, competi- 334
tor, and user-generated messages. Official brand 335
posts are treated as broadcast and prioritized in con- 336
sumers’ feeds, while other items are sampled by 337
sender influence and topic heat, mimicking weak- 338
tie diffusion in crises (Granovetter, 1973). Each 339
consumer has feed capacity C and processes at 340
most C items, with processing probability modu- 341
lated by susceptibility and stance alignment; pro- 342
cessed messages update CBBE and TPB internal 343
states via Eq. (1). The platform produces a market 344
brief of platform-visible aggregates and dominant 345
topics as the next observation S_{t+1} ; it is built only 346
from the public message log and engagement coun- 347
ters and excludes latent belief states and evalua- 348
tion metrics. To discourage unsupported evidence 349
claims, BrandPolis applies an evidence-consistency 350
gate $\gamma^{(t)} \in [0, 1]$ that attenuates the impact of un- 351
supported evidence claims in official actions. 352

Evaluation Metrics. We evaluate dynamic per- 353
formance with six metrics, spanning public- 354
interest outcomes and risk-process dynamics. As 355
public-interest outcomes, Brand Reputation In- 356
dex (BRI) (Fombrun et al., 2000) operationalizes 357
population-level trust as an aggregated reputation 358
signal over the CBBE-aligned perception dimen- 359
sions. Net Promoter Score (NPS) (Reichheld, 360
2003) operationalizes advocacy as a population- 361
level summary of the TPB-aligned intent signal. 362
Share of Voice (SoV) (Farris et al., 2010) contextu- 363
alizes competitive attention as the brand’s share 364
of crisis-topic-related discussion volume within 365
the sandbox. As risk-process dynamics, Polariza- 366
tion Index (Pol.) (Esteban and Ray, 1994) mea- 367
sures stance polarization across supporters, neu- 368
trals, and opponents, and may be quantized under 369
finite populations. Average Reputation Volatility 370
(ARV) (Leberknight et al., 2011) captures volatil- 371
ity of the reputation trajectory over the full hori- 372
zon, and Crisis Recovery Speed (CRS) (Coombs, 373
2007b) measures recovery as how quickly reputa- 374

tion rebounds after the episode bottom. We report per-round trajectories and summarize with end-of-horizon values (BRI_T , NPS_T , SoV_T , Pol_T) and trajectory-level summaries (ARV, CRS).

5 Experiments

5.1 Experimental Setup

We compare our BrandSRD-aligned Strategic Agent against proprietary and open-source LLM baselines run in a zero-shot setting under the same BrandEval protocol, including Llama 3.1 (Dubey et al., 2024) to contextualize open-source performance in this setting. Strategic Agent is initialized from Qwen3-8B (Yang et al., 2025) and fine-tuned on BrandSRD. BrandEval-Static reports multi-LLM jury scores on the four stakeholder-theory dimensions, while BrandEval-Dynamic runs BrandPolis for $T = 20$ rounds with $K = 5$ seeds per scenario. Implementation details, prompt templates, metric definitions, and additional validity and robustness analyses are provided in Appendix.

5.2 Two-Stage Preference Pipeline

We initialize from Qwen3-8B and perform preference-supervised alignment on BrandSRD to learn a policy model π_θ for Strategic Agent. The resulting policy is deployed in BrandPolis together with the SR structured workflow, which uses structured prompting to drive per-round goal setting, stakeholder state summarization, candidate response generation, and final selection. Training follows a two-stage alignment pipeline: Stage A performs static self-rewarding to constrain outputs to be parseable and to construct learnable preference signals for structured strategic analyses; Stage B then aligns on BrandSRD using supervised preference annotations. Full details and objectives are provided in Appendix.

5.3 BrandPolis Sanity Checks

Before evaluating agents on BrandEval, we assess whether BrandPolis can reproduce the coarse-grained rise-and-fall patterns and discourse structure observed in real online brand and consumer interactions. We study three real-world electric vehicle events, a highway-accident crisis that first broke widely on 2025-03-29 (China Newsweek, 2025), a product-recall incident announced on 2025-09-19 (Yicai Daily, 2025), and a spontaneous-combustion incident on 2025-10-13 (Xiaoxiang Morning Herald, 2025). We compare simulated

Table 2: **BrandPolis sanity checks.** Macro-level trend alignment and micro-level discourse reproduction across three crisis types.

Metric	Highway accident	Product recall	Spontaneous combustion
<i>Macro trend alignment</i>			
Lagged $r_{\max}(\pm 2) \uparrow$	0.60	0.80	0.75
Spearman $\rho \uparrow$	0.62	0.56	0.59
Norm-RMSE \downarrow	0.35	0.32	0.29
DTW (Z-norm) \downarrow	0.21	0.27	0.23
90% band coverage \uparrow	0.60	0.65	0.65
<i>Micro discourse reproduction</i>			
Topic JSD \downarrow	0.18	0.21	0.17
Topic cosine \uparrow	0.74	0.62	0.76
Top-10 overlap \uparrow	0.60	0.70	0.70

outputs against a post-derived reference series under matched operationalization, and compare discourse statistics under matched preprocessing, to check whether the sandbox captures rise-fall patterns and salient topic structure (Table 2).

Macro-level trend alignment. We sanity-check whether BrandPolis reproduces event-level rise-peak-recovery dynamics by comparing its simulated reputation trajectory to a post-derived reference series aggregated from observed crisis discussions under a matched operationalization over the same 60-day horizon; we map each round to a 3-day window to align the 20-round episode with this horizon. We compare simulated and proxy trajectories using lag-aligned Pearson correlation within a fixed ± 2 round window, Spearman rank correlation, normalized RMSE after min-max normalization, dynamic time warping (DTW) on Z-normalized trajectories, and 90% prediction-band coverage. Across events, correlation-based signals are directionally positive, and distance-based comparisons and coverage jointly suggest broadly similar trajectory shapes under the shared operationalization, supporting BrandPolis as a macro-level sanity check.

Micro-level discourse reproduction. We further check whether BrandPolis generates plausible crisis discourse structure by comparing simulated and observed posts under matched preprocessing and a shared topic space. We evaluate three aspects: how similar the overall topic mix is (Jensen-Shannon divergence (JSD)), how close the topic meanings are (topic-level cosine similarity), and whether the most discussed topics match (Top-10 overlap). Across events, the simulated and real discussions show a similar topic mix and share many of the same top topics, indicating that BrandPolis cap-

Table 3: **BrandEval-Dynamic results.** Mean over 50 scenarios under Single (Prospector) and Dual (Prospector+Analyzer) competitor regimes. Best in each column is **bold**; second best is underlined.

Model	BRI \uparrow		NPS \uparrow		ARV \downarrow		Pol. \downarrow		CRS \downarrow		SoV \uparrow	
	Single	Dual	Single	Dual	Single	Dual	Single	Dual	Single	Dual	Single	Dual
<i>Initial Value</i>	-12.07	-12.07	-32.00	-32.00	-	-	82.41	82.41	-	-	64.25	64.23
GPT-5.1	-2.34	-3.62	-1.00	-2.00	33.09	31.46	<u>1.98</u>	0.00	14	13	68.27	68.94
Gemini-2.5-Pro	-2.89	-3.16	-3.00	-2.00	34.29	33.97	3.92	7.68	<u>15</u>	<u>14</u>	68.93	69.61
Claude-Sonnet-4.5	-3.03	-3.75	<u>-2.00</u>	-4.00	32.36	31.11	<u>1.98</u>	<u>1.98</u>	16	16	68.91	69.59
GLM-4.5	-4.09	<u>-2.95</u>	-3.00	<u>-3.00</u>	30.56	30.22	3.92	<u>1.98</u>	14	15	<u>69.62</u>	68.94
DeepSeek-R1	-4.04	-5.28	-6.00	-4.00	28.93	28.06	5.82	3.92	16	16	67.65	75.96
R1-Distill-Qwen-7B	-4.26	-3.42	-9.00	-6.00	27.80	30.72	<u>1.98</u>	3.92	18	17	69.60	69.61
Qwen3-8B	-3.54	-4.30	-3.00	-9.00	30.06	29.74	<u>1.98</u>	<u>1.98</u>	16	15	63.46	68.90
Qwen3-14B	-4.01	-5.10	-5.00	-7.00	29.01	<u>27.82</u>	3.92	<u>1.98</u>	17	16	68.89	<u>71.84</u>
Llama 3.1-8B	-5.11	-5.43	-4.00	-8.00	<u>28.68</u>	24.81	0.00	5.82	18	20	69.90	65.05
Strategic Agent	<u>-2.36</u>	-2.76	-1.00	-2.00	27.78	31.83	<u>1.98</u>	<u>1.98</u>	14	13	69.61	69.99

460 tures the main themes and their rough prominence
461 during crises.

462 5.4 BrandEval-Static Results

463 We first report results on BrandEval-Static, which
464 evaluates single-round strategic analysis quality
465 under a multi-LLM judge panel (Table 4). Two
466 findings are salient. First, frontier general-purpose
467 models dominate static scores, consistent with
468 Static rewarding immediate diagnostic coverage
469 and rhetorically complete reports in a single turn.
470 Second, Strategic Agent is competitive with strong
471 open models but does not surpass the best propri-
472 etary systems; this gap is informative rather than
473 surprising, because SR is optimized for iterative
474 crisis handling rather than maximizing one-shot
475 narrative completeness.

Table 4: **BrandEval-Static results.** Multi-LLM panel scores (1–10) averaged over all scenarios. C/B = Consumer & Brand; P/M = Public & Media; Comp. = Competitor; Strat. = Strategic Synthesis.

Model	C/B	P/M	Comp.	Strat.
GPT-5.1	7.86	7.81	7.42	7.60
Gemini-2.5-Pro	7.61	7.64	7.28	7.34
Claude-Sonnet-4.5	7.52	7.71	7.36	7.40
GLM-4.5	7.11	7.16	6.93	6.89
DeepSeek-R1	6.74	6.80	6.46	6.47
R1-Distill-Qwen-7B	4.88	4.31	4.44	4.04
Qwen3-8B	6.20	6.12	6.00	5.73
Qwen3-14B	6.67	6.59	6.61	6.44
Llama 3.1-8B	4.39	3.90	3.89	3.52
Strategic Agent	6.75	6.73	6.51	6.44

476 5.5 BrandEval-Dynamic Results

477 Building on the static diagnostic, we evaluate mod-
478 els in BrandEval-Dynamic to test whether strong
479 single-turn analysis actually leads to robust long-
480 horizon behavior under interaction (Table 3). Three

Table 5: **Tail risk analysis across 50 dynamic scenarios.** Min is the worst-case BRI_T over scenarios; $CVaR_{10}$ is the mean of the bottom 10% BRI_T outcomes; Fail rate is the proportion of scenarios with $BRI_T < -10$. Metrics are computed on seed-averaged outcomes with $K = 5$ runs per scenario.

Policy	Min BRI \uparrow	CVaR $_{10}$ BRI \uparrow	Min NPS \uparrow	Fail rate \downarrow
Manipulative	-18.52	-16.20	-35.00	12%
Specious	-10.24	-9.15	-22.00	4%
Strategic Agent	-5.21	-4.82	-12.00	0%

481 findings stand out. (i) **Trust gains require process**
482 **health:** higher reputation and advocacy are only
483 meaningful when the trajectory is also stable, with
484 lower volatility and faster recovery. This suggests
485 BrandEval-Dynamic rewards sustained stabilization
486 rather than short-lived, optimistic messaging.
487 (ii) **Strategic Agent delivers a balanced outcome:**
488 compared with its backbone and prompting base-
489 lines, it improves trust while keeping polarization
490 and instability under control, consistent with SR-
491 style verifiable commitments and feedback-aware
492 sequencing supporting robust performance over
493 time. (iii) **More voice does not mean better out-**
494 **comes:** gaining more voice in the discussion does
495 not reliably build trust; what matters is whether the
496 response addresses concerns with credible actions
497 rather than high-volume messaging. In practice,
498 end-of-horizon trust can look similar across mod-
499 els while volatility and recovery differ sharply, so
500 process-health metrics are necessary to distinguish
501 stable crisis handling from fragile, oscillatory re-
502 sponses. This also helps avoid over-crediting strate-
503 gies that win short-term attention but destabilize
504 belief trajectories.

505 Mean performance can obscure rare but severe
506 backfires that dominate real-world crisis cost, so

Table 6: **Comparisons and ablations on BrandEval-Dynamic.** Results are grouped into a backbone baseline, prompting baselines with the same backbone, and Strategic Agent variants that ablate SR.

Model	BRI \uparrow		NPS \uparrow		ARV \downarrow		Pol. \downarrow		CRS \downarrow		SoV \uparrow	
	Single	Dual	Single	Dual	Single	Dual	Single	Dual	Single	Dual	Single	Dual
<i>Backbone baseline</i>												
Qwen3-8B	-3.54	-4.30	-3.00	-9.00	30.06	29.74	<u>1.98</u>	1.98	16	15	63.46	68.90
<i>Prompting baselines (same backbone, different prompting)</i>												
Qwen3-8B + CoT	-2.98	-3.88	-1.00	-4.00	29.50	<u>30.60</u>	3.92	5.82	16	15	68.93	69.58
Qwen3-8B + ReAct	-2.89	<u>-3.74</u>	-5.00	-5.00	35.16	31.95	0.00	<u>3.92</u>	13	12	70.30	<u>69.62</u>
Qwen3-8B + Reflexion	<u>-2.76</u>	<u>-3.86</u>	<u>-2.00</u>	-1.00	34.38	30.72	0.00	<u>3.92</u>	<u>14</u>	<u>13</u>	68.63	69.61
<i>Strategic Agent ablations (policy/workflow components)</i>												
Strategic Agent (w/o SR)	-3.10	-3.96	<u>-2.00</u>	-3.00	<u>28.90</u>	31.20	<u>1.98</u>	1.98	15	14	67.65	69.30
Strategic Agent (SR)	-2.36	-2.76	-1.00	<u>-2.00</u>	27.78	31.83	<u>1.98</u>	1.98	<u>14</u>	<u>13</u>	<u>69.61</u>	69.99

we assess tail robustness by comparing two stylized response policies against our Strategic Agent. The Manipulative policy is prompted to maximize visibility and suppress competitors even at the expense of accountability, while the Specious policy produces plausible-sounding but weakly grounded statements that avoid verifiable commitments. We report three scenario-level tail-risk indicators on BrandEval-Dynamic: the worst-case outcome across scenarios Min, the average over the bottom 10% scenarios CVaR₁₀, and the catastrophic failure rate under $BRI_T < -10$, all computed after averaging $K = 5$ seeds per scenario. Table 5 shows that the Strategic Agent raises the downside floor and reduces catastrophic failures.

5.6 Static-Dynamic Alignment Analysis

Single-turn strategic analyses do not necessarily translate into robust long-horizon behavior under interaction, motivating BrandEval-Dynamic. We descriptively quantify this transfer gap with Kendall’s τ between model rankings from BrandEval-Static and BrandEval-Dynamic outcomes, reversing the ranking direction for lower-is-better metrics. Static rankings align with trust and polarization outcomes ($\tau = 0.67$ for BRI; $\tau = 0.82$ for Pol.) but are negatively associated with process-health metrics (ARV: $\tau = -0.33$; CRS: $\tau = -0.24$). This does not imply the static rubric is wrong: BrandEval-Static rewards one-shot diagnostic coverage, whereas BrandEval-Dynamic stresses multi-turn execution under feedback and competition, where over-commitment, oscillation, and evidence-timing drive stability and recovery. We therefore use BrandEval-Static as a diagnostic complement rather than a standalone proxy for long-horizon process health; mechanistic analysis is provided in the Appendix.

5.7 Ablation Studies

We run controlled ablations on BrandEval-Dynamic to disentangle generic prompting from policy and workflow components in Table 6. CoT prompting can lift end-state trust signals but tends to worsen polarization, especially under stronger competition. ReAct and Reflexion can suppress polarization under the single-competitor regime, yet they often trade off trust and increase volatility, suggesting generic agent scaffolds do not reliably yield robust long-horizon crisis handling. The SR-trained Strategic Agent delivers the strongest trust and maintains low polarization and competitive recovery across regimes, while removing SR erodes these gains, indicating SR adds value beyond preference tuning by enforcing verifiable goals and feedback-aware plan selection.

6 Conclusion and Discussion

In this paper, we introduce BrandEval, a two-track benchmark for LLM crisis communication that pairs a rubric-based static diagnostic with a multi-agent sandbox, BrandPolis, to evaluate long-horizon behavior under interaction. We also introduce BrandSRD, a Chinese dataset of crisis-response decision points with counterfactual plans and structured rationales, and an SR-based Strategic Agent trained on BrandSRD that improves BrandEval-Dynamic trust and stability over baselines. Our results expose a structural gap between single-turn evaluation and robust long-horizon crisis handling: static rankings align with some end-state trust and escalation signals, but can miss process-health failures such as volatility and slow recovery; Strategic Rationale promotes verifiable commitments and feedback-aware sequencing that yields more stable trajectories under competition.

580 Limitations

581 BrandSRD is semi-automatically constructed: preference labels are distilled from a generator model
582 and then filtered and calibrated by crowd workers, so they remain a silver-standard signal and may
583 reflect systematic biases. BrandEval-Static uses a small three-model judging panel calibrated on
584 limited human ratings; scores are therefore proxy measurements that may favor certain model families
585 or reasoning styles. Accordingly, BrandEval-Static should be interpreted as a scalable diagnostic rather
586 than a standalone measure of real-world robustness, and we recommend using it together
587 with BrandEval-Dynamic to assess long-horizon behavior under interaction. BrandPolis is a stylized
588 abstraction with a simplified interaction structure, simplified CBBE/TPB updates, and manually
589 specified hyperparameters. We therefore include sanity checks and sensitivity analyses to assess robustness.
590 However, the simulator currently models crisis communication only in a single social media channel
591 and does not capture cross-channel dynamics spanning social media, advertising, and offline media.
592 It also does not explicitly represent heterogeneous tie strength in an underlying social graph. Our
593 event-level trend checks rely on a rubric-aligned proxy trajectory that shares conceptual dimensions
594 with the simulator, so they cannot fully rule out common inductive bias and should be interpreted
595 as sanity checks rather than definitive external validity evidence. Although BrandEval and BrandPolis
596 are instantiated using Chinese social platforms and selected consumer domains, the benchmark structure
597 combines a rubric-based static diagnostic with a dynamic multi-agent simulation and trajectory-based
598 metrics, and is not specific to any single language or market. Accordingly, the reported empirical
599 findings primarily reflect this setting; applying the framework to other markets, languages, or
600 regulatory contexts will require recalibration.

621 Ethical Considerations

622 All data in BrandSRD is derived from publicly accessible posts on Weibo, Douyin, and Xiaohongshu,
623 supplemented with public news reports and official announcements for event context. We remove
624 or rewrite identifying information and release only de-identified, self-contained scenario briefs
625 and aggregated annotations rather than user-identifiable records. We will release only the de-

630 identified BrandSRD records and will not release any original social-media posts. The counterfactual
631 response plans are generated via commercial LLM APIs solely to construct a risk-aware evaluation and
632 training resource, not to optimize PR persuasion. We explicitly prohibit using BrandSRD/BrandEval/
633 BrandPolis to generate misleading crisis messaging, evade accountability, or manipulate public
634 opinion; the benchmark design further penalizes unverifiable claims and manipulative tactics. 635
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A Appendix A: Reproducibility Pack

A.1 BrandSRD

Strategic Rationale record schema

We log one SR record per Strategic Agent decision in BrandPolis. Only the selected plan is posted to the environment as the official action; the remaining fields are stored in the log.

SR record schema JSON template

```
{  
  "round_id": "...",  
  "observation_summary": "...",  
  "goal": "...",  
  "stakeholder_summary": "...",  
  "candidate_plans": [ "...", "...",  
    "..."],  
  "selected_plan": "...",  
  "final_action_content": "...",  
  "claimed_evidence": "..."  
}
```

A.2 BrandEval: Scenarios and Rubrics

Scenario de-identification and disjointness

BrandEval-Static scenarios are constructed by fictionalizing a held-out prototype pool with Gemini-2.5-Pro, followed by human screening for commercial plausibility and removal of any identifying details. Fictionalization preserves the underlying strategic trade-offs and multi-stakeholder tensions, while ensuring that no real-world entities, individuals, handles, or URLs remain. Disjointness from BrandSRD is enforced by (i) pre-reserving the evaluation pool before dataset construction and (ii) filtering with prototype-level IDs and metadata to prevent overlap.

Stakeholder-theory-inspired rubric

BrandEval-Static is scored using a structured rubric inspired by stakeholder theory. The rubric consists of four dimensions, each scored on a 1–10 scale (higher is better). Table 7 summarizes the operational definitions.

Scenario selection (Dynamic). For BrandEval-Dynamic, we select 50 scenarios from the held-out pool via stratified sampling over (i) dominant topic clusters and (ii) risk profiles (e.g., safety, governance, product quality, pricing). Risk profiles are annotated during scenario curation and used only to balance evaluation coverage.

A.3 Judge system and bias diagnostics

To verify the robustness of our LLM-based evaluation framework, we conducted sensitivity analyses using two types of perturbations: style perturbation and structural perturbation. We selected a random subset of 5 scenarios and applied these perturbations to the inputs before feeding them to the judge.

Perturbation Methods

- **Style Perturbation:** We rewrote the agent’s analysis using two distinct styles: “Flowery” (more elaborate and sophisticated language) and “Concise” (simpler and shorter language), while preserving the original insights and semantic content.
- **Structure Perturbation:** We shuffled the order of the four analysis sections (Customer, Public, Competitor, Strategic Synthesis) in the JSON input to test if the judge’s scoring is sensitive to the presentation order.

Results

Table 8 reports the absolute changes in scores ($|\Delta Score|$) across all four evaluation dimensions (1–10 scale). The results demonstrate that our judge is highly robust to structural changes and reasonably robust to stylistic variations, with mean deviations well below 1.0 point on a 10-point scale. This suggests that the evaluation is not strongly driven by formatting or linguistic style under these controlled perturbations.

Audit Judge discriminability

To test whether the evidence-sensitive Audit Judge is merely uniformly harsher, we evaluate its *paired discriminability* between **Verifiable** and **Spurious** strategies on matched stress scenarios. For each scenario i , we compute the paired gap $\Delta_i = \text{Score}_i^{\text{Verifiable}} - \text{Score}_i^{\text{Spurious}}$ and summarize (i) the mean gap $\bar{\Delta}$, (ii) a bootstrap 95% confidence interval over $\{\Delta_i\}_{i=1}^N$ (1,000 resamples), (iii) a win rate $\Pr(\Delta_i > 0)$, and (iv) paired Cohen’s $d = \bar{\Delta}/s_{\Delta}$ where s_{Δ} is the standard deviation of paired differences.

The Audit Judge is selectively specific: it increases separation primarily when evidence quality differs, rather than applying a uniform downward shift to all outputs. (Additional rubric reliability and judge calibration details appear in Appendix B.4.)

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Table 7: **BrandEval-Static rubric.** Four dimensions scored on a 1–10 scale.

Dimension	Operational definition
Consumer & Brand	Accurate diagnosis of consumer concerns; concrete brand actions; credible evidence (data, timelines, accountability); explicit linkage to brand equity dimensions (competence/value/emotion) when appropriate.
Public & Media	Anticipation of public/media narratives; risk-aware messaging; clarity on responsibility/safety; preventive escalation control; alignment with transparency and verifiability.
Competitor	Recognition of competitive dynamics (e.g., opportunistic attacks, SoV shifts); defensive/offensive counter-moves; avoids self-inflicted openings.
Strategic Synthesis	Coherent trade-offs across stakeholders; prioritized goals; operational plan with milestones; avoids generic PR; actionability and consistency with constraints.

Table 8: Judge robustness under adversarial perturbations. Low mean deviations suggest the judge is relatively insensitive to surface form under these perturbations.

Perturbation Type	Mean $ \Delta $	Max $ \Delta $	90th Percentile
Style (Flowery)	0.17	1	0.9
Style (Concise)	0.42	1	1.0
Structure (Order)	0.25	1	1.0

Table 9: **Audit Judge paired discriminability** ($N = 9$ stress scenarios). The Audit Judge exhibits a large, directional separation between Verifiable and Specious strategies, while the Standard Judge’s confidence interval crosses zero, indicating weak discriminability under matched scenarios.

Judge	Mean $\bar{\Delta}$	95% CI	Win(%)	Paired d
Standard	+0.44	[−0.33, 1.33]	44	0.35
Audit (ours)	+3.11	[1.67, 4.56]	89	1.34

A.4 BrandPolis: Environment and Update Equations

BrandPolis is a discrete-time stochastic environment that approximates message exposure and attention allocation on social media. In each round, agents generate messages, the platform mediates exposure under attention scarcity and confirmation bias, consumer belief states are updated, and a concise market brief is produced for the next round. We describe the core mechanisms and equations below.

Exposure and retention

Official posts from strategic agents are treated as broadcast signals: we set $P_{\text{push}}(m, t) = 1$ for official posts. For other messages (UGC and non-broadcast content), we compute $P_{\text{push}}(m, t)$ using Eq. 2.

For each consumer in each round, the platform forms a feed candidate set by (i) always including

all broadcast items and (ii) sampling additional non-broadcast items according to $P_{\text{push}}(m, t)$. To model finite attention, the platform retains at most C messages per round. Retention prioritizes broadcast items: if the number of broadcast items exceeds C , the platform keeps C broadcast items (uniformly at random); otherwise, it keeps all broadcast items and fills the remaining slots (up to C) with sampled non-broadcast items.

For a non-broadcast message m from sender s on topic k at round t , the platform computes the exposure probability:

$$P_{\text{push}}(m, t) = \text{clip}_{[0,1]} \left(P_{\text{base}} \left[1 + c_1 \ln(I_s(t) + 1) + c_2 \ln(H_k(t) + 1) \right] \right) \quad (2)$$

where $\text{clip}_{[0,1]}(x) = \min(1, \max(0, x))$, P_{base} is a global base rate, $I_s(t)$ is a sender influence score updated from engagement, and $H_k(t)$ is topic heat maintained as an exponential moving average of recent message volume and interactions.

The overall probability that consumer u processes message m is:

$$P_{\text{ret}}(m, u, t) = \text{clip}_{[0,1]} \left(P_{\text{push}}(m, t) \cdot s_u \cdot \text{align}(m, u) \right), \quad (3)$$

where $s_u \sim \mathcal{U}(0, 1)$ is an information-retention susceptibility and $\text{align}(m, u)$ is a stance-based

confirmation-bias filter that downweights misaligned messages.

To prevent metric leakage, we enforce an implementation-level constraint: the observation builder has access only to the message log and engagement counters, and does not read latent state tensors used for computing BRI/NPS/Pol/ARV/CRS.

Action-grounding mechanism

BrandPolis maintains a lightweight evidence store in the environment state. At each round t , the strategic agent may optionally output a string identifier `claimed_evidence` to indicate that the official action is grounded in a concrete, checkable artifact such as logs, inspection reports, or third-party findings. The environment tracks a set of evidence objects $\mathcal{E}^{(t)}$ with their identifiers. We compute an evidence-consistency gate $\gamma^{(t)} \in [0, 1]$ by checking whether `claimed_evidence` matches an identifier in $\mathcal{E}^{(t)}$. This gate scales the message-derived impact signal, so unsupported evidence references attenuate through the downstream belief update described in Eq. (4).

Belief update (EMA) and calibration summary

Each consumer maintains a latent state vector $\mathbf{V}_u^{(t)}$ for the focal brand, initialized at $t = 1$ and updated for $t = 2, \dots, T$ via an exponential moving average with bounded nonlinearity:

$$\mathbf{V}_u^{(t)} = (1 - \lambda_u) \mathbf{V}_u^{(t-1)} + \lambda_u \gamma^{(t)} \tanh(\mathbf{X}_u^{(t)}). \quad (4)$$

where $\mathbf{X}_u^{(t)}$ is the message-derived impact signal and λ_u is a consumer-specific update rate.

To ground the update dynamics, we calibrate a text-to-state mapping on a separate human-rated subset. Concretely, we extract lightweight textual features from each message and fit multivariate regression models to predict targets aligned with CBBE and TPB, including the three perception dimensions and the two intention dimensions. The regression predictions are used as the message-derived impact signal $\mathbf{X}_{u,j}^{(t)}$ in Eq. (4), so that consumer states evolve as a first-order EMA driven by observed text. We treat this mapping as an explicit and reproducible modeling choice that keeps the simulator transparent and auditable, while recognizing that the latent states are internal proxies and require independent validation to support real-world interpretation.

A.5 BrandEval-Dynamic Metrics

BrandEval-Dynamic reports six core metrics covering long-horizon trust, loyalty, competitive salience, and crisis process health.

Units and ranges. To match all tables in this paper and the final evaluation logs, we define metrics in reported units: BRI and NPS are reported on a point scale in $[-100, 100]$, SoV and Polarization are reported in percent in $[0, 100]$, ARV is a dimensionless volatility summary of the latent reputation signal, and CRS is reported in timesteps.

Brand Reputation Index (BRI)

BRI captures an aggregate consumer perception signal over three CBBE-aligned dimensions: competence belief (CB), value congruence (VC), and emotional connection (EC). Let $\overline{CB}_t, \overline{VC}_t, \overline{EC}_t \in [-1, 1]$ be population averages at timestep t . We first define a raw latent reputation signal:

$$b_t = w_{\text{cap}} \cdot \overline{CB}_t + w_{\text{val}} \cdot \overline{VC}_t + w_{\text{emo}} \cdot \overline{EC}_t, \quad (5)$$

and define the reported Brand Reputation Index (BRI) as:

$$BRI_t = 100 \cdot b_t \in [-100, 100]. \quad (6)$$

We use uniform weights to avoid introducing arbitrary emphasis: $w_{\text{cap}} = w_{\text{val}} = w_{\text{emo}} = 1/3$.

Net Promoter Score (NPS)

Let $\pi_t^{\text{pro}} \in [0, 1]$ be the share of Promoters (Advocacy Intent > 0.7) and $\pi_t^{\text{det}} \in [0, 1]$ be the share of Detractors (Advocacy Intent < 0.3). We define the reported NPS on the standard point scale:

$$NPS_t = 100 \cdot (\pi_t^{\text{pro}} - \pi_t^{\text{det}}) \in [-100, 100]. \quad (7)$$

Share of Voice (SoV)

In BrandPolis, we operationalize SoV as a topic-focused share of discussion within the simulated market:

$$SoV_{\text{brand},t} = 100 \cdot \frac{V_{\text{brand},t}}{V_{\text{total},t}} \in [0, 100], \quad (8)$$

where $V_{\text{brand},t}$ counts all brand-related messages in the sandbox at round t (official brand posts plus consumer UGC responding to the focal brand or event), and $V_{\text{total},t}$ counts all messages generated within the sandbox at round t .

Polarization Index

We use a bounded group-based polarization score over supporters (S), neutrals (N), and opponents (O). Let $G = 3$, with group shares $s_{g,t}$ at round t (summing to 1), and group locations μ_g . We set $\mu_S = 1$, $\mu_N = 0$, and $\mu_O = -1$. We compute a raw polarization score using a pairwise-distance form:

$$p_t = \sum_{g=1}^G \sum_{h=1}^G s_{g,t} s_{h,t} |\mu_g - \mu_h|, \quad (9)$$

where $p_t \in [0, 1]$ under this discrete encoding. We report the Polarization Index on a percent scale:

$$Pol_t = 100 \cdot p_t \in [0, 100]. \quad (10)$$

Because polarization is computed over three discrete stance groups with a finite consumer population, the reported Pol values can appear quantized. We therefore treat Pol as a diagnostic for regime shifts rather than as a fine-grained continuous signal.

Average Reputation Volatility (ARV)

ARV summarizes *process instability* largely independent of the absolute reputation level.

For an episode, let $\{BRI_t\}_{t=1}^T$ be the reported reputation trajectory (Eq. 6). We first apply per-episode min–max normalization:

$$\widetilde{BRI}_t = \frac{BRI_t - \min_{1 \leq \tau \leq T} BRI_\tau}{\max_{1 \leq \tau \leq T} BRI_\tau - \min_{1 \leq \tau \leq T} BRI_\tau + 10^{-12}}. \quad (11)$$

$\widetilde{BRI}_t \in [0, 1]$. This normalization makes ARV comparable across scenarios with different absolute severity by focusing on *trajectory shape volatility* rather than raw amplitude.

We then define Average Reputation Volatility as the standard deviation of the normalized trajectory:

$$ARV = 100 \cdot \sqrt{\frac{1}{T} \sum_{t=1}^T (\widetilde{BRI}_t - \overline{\widetilde{BRI}})^2}, \quad (12)$$

$$\overline{\widetilde{BRI}} = \frac{1}{T} \sum_{t=1}^T \widetilde{BRI}_t.$$

ARV is reported on a $[0, 100]$ -like scale.

Reading note. ARV should be interpreted jointly with BRI_T/NPS_T : high end-state trust with high ARV indicates fragile, oscillatory handling; conversely, modest end-state gains with low ARV indicates stable de-escalation and consistent follow-through.

Crisis Recovery Speed (CRS)

CRS measures how quickly the reputation trajectory *returns to the episode entry level* after the episode bottom. Let $t_{\text{bottom}} = \arg \min_{1 \leq t \leq T} BRI_t$. We define the recovery time as the first timestep after t_{bottom} such that the reputation reaches the entry level:

$$t_{\text{recover}} = \min\{t > t_{\text{bottom}} : BRI_t \geq BRI_1\}. \quad (13)$$

We then define CRS (in timesteps) as:

$$CRS = \begin{cases} t_{\text{recover}} - t_{\text{bottom}}, & \text{recovery,} \\ (T + 1) - t_{\text{bottom}}, & \text{no recovery.} \end{cases} \quad (14)$$

Lower CRS indicates faster recovery under the same horizon and unit scale.

A.6 Two-stage preference alignment details

Two-stage preference alignment: Stage A \rightarrow Stage B

We initialize from Qwen3-8B and perform preference-supervised alignment on BrandSRD to learn a policy model π_θ for Strategic Agent. The resulting policy is deployed in BrandPolis together with the SR structured workflow: SR uses structured prompting to drive per-round goal setting, stakeholder state summarization, candidate response generation, and final selection, enabling an auditable decision-making process. Training follows a two-stage alignment pipeline.

Stage A: Static self-rewarding (Iterative DPO)

Stage A targets static diagnostic “question-answering” outputs. The goal is to constrain the model to produce parseable, structured strategic analyses and to construct learnable preference signals for open-ended tasks without explicit ground truth. Given an input scenario x and its evaluation-aligned prompt $\rho(x)$, we sample a candidate set $\{y_k\}_{k=1}^K$ and apply a verifiable gate $G(x, y) \in \{0, 1\}$ to filter out unparsable or schema-violating outputs. For candidates that pass the gate, a frozen self-judge produces a normalized reward $R(x, y) \in [0, 1]$ with a hard evidence constraint: evidence spans must be substrings of the original prompt text; otherwise we set $R(x, y) = 0$. We then select, among gated candidates,

$$y^+ = \arg \max_y R(x, y),$$

$$y^- = \arg \min_y R(x, y), \quad (15)$$

to form a preference triple (x, y^+, y^-) . Stage A optimizes an Iterative DPO objective anchored by a reference model π_{ref} to constrain update magnitude:

$$\mathcal{L}_A(\theta) = -\mathbb{E}_{(x, y^+, y^-)} \left[\log \sigma(\beta(\Delta_\theta - \Delta_{\text{ref}})) \right], \quad (16)$$

where

$$\begin{aligned} \Delta_\theta &= \log \pi_\theta(y^+ | x) - \log \pi_\theta(y^- | x), \\ \Delta_{\text{ref}} &= \log \pi_{\text{ref}}(y^+ | x) - \log \pi_{\text{ref}}(y^- | x), \end{aligned} \quad (17)$$

and β is a strength coefficient. Training proceeds in a closed loop of generation, self-judging, and preference optimization: each iteration first constructs preference data using the current policy and then minimizes Eq. (16) to obtain the next policy, improving both parseability and content quality of the static answer cards. The Stage A adapter is used to initialize Stage B.

Stage B: Preference alignment on BrandSRD (ORPO) Stage B aligns the model on BrandSRD. BrandSRD decomposes brand crisis communication into atomic decision points; each instance contains a strategic context, multiple candidate responses (including counterfactual contrasts), and preference annotations with structured rationale records, providing supervised signals for preference learning. Training uses derived preference triples (x, y^+, y^-) , where y^+ is the annotated preferred response and y^- is sampled from the dispreferred candidate set; both are converted into a structured decision representation to ensure consistent format. We optimize an ORPO objective that combines a preference log-odds term with conditional cross-entropy on y^+ :

$$\begin{aligned} \mathcal{L}_B(\theta) = & -\log \sigma \left(\beta \left(\log \pi_\theta(y^+ | x) \right. \right. \\ & \left. \left. - \log \pi_\theta(y^- | x) \right) \right) \\ & + \lambda \left(-\log \pi_\theta(y^+ | x) \right), \end{aligned} \quad (18)$$

where β controls the preference term and λ weights the supervised term. The Stage B-aligned policy serves as the language policy model of Strategic Agent in BrandPolis.

A.7 Participant instructions, recruitment, and compensation

Before starting the task, all participants were presented with an Informed Consent Statement that

stated the crisis scenarios were simulated for research purposes only and did not represent real-world events; it also included a brief risk disclaimer and an option to stop participation at any time, and participants were required to acknowledge these terms before proceeding. Participants were recruited via Credamo, a crowdsourcing platform in China; the participant pool consisted primarily of young adults (aged 21–30, mean age ≈ 26). Participants were compensated per completed survey at a rate intended to be consistent with prevailing local hourly wage benchmarks for comparable online microtasks in China, based on the observed median completion time of approximately 4–5 minutes per survey; we therefore consider the compensation adequate for the time and cognitive effort required by the evaluation task.

A.8 Prompt templates, schemas, and questionnaires

1219

A.8.1 LLM Prompts

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We include three prompts to reproduce filtering, de-identification, and rubric-based scoring.

1221

Prompt P1: Domain Relevance Filter

SYSTEM:

<YOU_ARE_A_DOMAIN_RELEVANCE_FILTER>

USER:

Decide whether the following text is relevant to <TARGET_ENTITY_OR_DOMAIN>.
Return EXACTLY ONE token: RELEVANT or IRRELEVANT.

1222

Prompt P2: De-identification + Neutral Rewrite

SYSTEM:

<YOU_ARE_A_DEIDENTIFICATION_AND_NEUTRAL_REWRITE_ASSISTANT>

USER:

Rewrite the text into a concise, neutral, single-paragraph brief. Requirements:

- 1) Keep all verifiable facts unchanged (time, location, numbers, key background).
- 2) Replace all organization/brand/product/spokesperson names with fictitious names not in the input.
- 3) Remove subjective commentary and opinions; keep only objective, checkable statements.
- 4) Maintain industry relevance and preserve the core strategic challenge.

1223

Prompt P3: BrandEval Scoring

(A) Submission Schema

SYSTEM:

<YOU_ARE_A_SENIOR_BRAND_STRATEGY_CONSULTANT>

USER:

Return valid JSON only following the required schema. Use the same language as the scenario.

```
{
  "strategic_analysis": {
    "consumer_and_brand_impact": "...",
    "public_and_media_impact": "...",
    "competitive_impact": "...",
    "strategic_synthesis": "..."
  }
}
```

(B) Oracle Judge

SYSTEM:

<YOU_ARE_AN_ORACLE_JUDGE_FOR_BRANDEVAL>

USER:

Score the submission on four dimensions (1–10) with brief rationales.

Typical answers should fall in 4–6; >8 only if exceptional and specific.

If a dimension is missing/weak, that score must be <= 5.

Safety-First constraints: If the submission contains unverifiable claims presented as facts, blame shifting without accountability, intimidation or astroturfing cues, calls for targeted harassment, then cap the corresponding dimension score at 5.

1224

A.8.2 Agent Prompts

Strategic Agent Prompt

ROLE: You are a Brand Strategy Officer (Strategic Agent).

CORE RULES:

- Every decision must serve the injected Brand Identity and aim to minimize harm-relevant risks while improving credibility: prioritize verifiable actions, accountability, and de-escalation over short-term visibility.
- Prefer actions that are necessary, cost-effective, and add new information.
- Do NOT reveal internal strategy. Think privately; output only the required JSON.

[1] BRAND IDENTITY (fixed at initialization)

```
{
  "brand_name": "{brand_name}",
  "product_name": "{product_name}",
  "intended_positioning": {intended_positioning_list}
}
```

[2] MARKET INTELLIGENCE BRIEF (filled each timestep)

```
{
  "current_timestep": {t},
  "dominant_topic": "{dominant_topic}",
  "key_negative_posts": {key_negative_posts},
  "observable_metrics": {observable_metrics},
  "competitor_last_move": "{competitor_last_move}"
}
```

TASK: Decide what the brand publishes this round.

DECISION GUIDELINES:

- 1) Situation diagnosis: identify the most urgent threat/opportunity and which CBBE dimension it affects.
- 2) Severity check: distinguish a crisis versus background noise using observable metrics (e.g., sharp drops, sustained negativity, SoV threats).
- 3) Deadlock detection: if users repeat the same accusation (e.g., “empty talk / no data”), change tactics and provide NEW evidence.
- 4) Generate 2–3 candidate actions with concrete substance (dates, numbers, evidence, verified steps, third-party proof, direct rebuttal).
 - No generic PR filler (e.g., “we value feedback”, “we will try harder”).
- 5) Evaluate long-horizon impact on reputation/advocacy proxies, SoV, and process-health risks (volatility/polarization/recovery), plus competitor risks.
- 6) Choose the best action by balancing expected benefits against risk and cost. “No action” is allowed only in rare mandatory silence windows.

Constraints for final_action_content:

- Must be a publishable official social-media post.
- Must directly address relevant negative points when needed.
- Must add new information; no repetition; no meta-strategy.

CompetitorAgent Prompt

ROLE: You are a competitor decision-making agent in a market simulation.

PERSONA INJECTION (from config):

- Persona: {persona_name} (e.g., Defender / Prospector / Analyzer / Reactor)
- Primary goal: {persona_goal}
- Risk preference: {persona_risk_preference}
- Communication style: {persona_style}

[MARKET BRIEF]

```
{  
  "time_step": {t},  
  "your_observable_metrics": {your_observable_metrics},  
  "brand_observable_metrics": {brand_observable_metrics},  
  "dominant_topic": "{dominant_topic}",  
  "historical_context_retrieval": {historical_context}  
}
```

TASK: Decide what you publish this round to improve your position while staying persona-consistent.

GUIDELINES:

- React strategically to the brand's weakness/opportunity, but remain within persona risk constraints.
- Propose three options; at least one can be "routine presence" if no direct attack is sensible.
- If the dominant topic is a major safety crisis, you may be more assertive, but avoid illegal/defamatory claims.

Constraints for final_action_content:

- Must be a publishable social-media post.
- Must not be only "Observe"; if holding, publish a routine brand message to maintain presence.

ConsumerAgent Prompt

ROLE: You are a Social Media Consumer who writes realistic UGC.

PERSONA:

- Core driver: {core_driver} (e.g., value / performance / user_experience / social_identity / safety)
- Initial stance: {initial_stance} (supporter / neutral / opponent)
- Persona example: "{persona_example}"

INTERNAL STATE at time t:

- Competence belief (CB): {CB}
- Value congruence (VC): {VC}
- Emotional connection (EC): {EC}
- Advocacy intent: {advocacy}
- Current stance: {stance}

CONTEXT:

- Action type: {contentType} (e.g., new_post / reply)
- Reply-to summary: "{inReplyTo_summary}"
- Topic: "{dominant_topic}"
- Event guidance (optional): {event_guidance}

TASK: Write ONE short, realistic social-media post/comment.

REQUIREMENTS:

- 1) Tone must match your stance (opponent: critical/sarcastic; neutral: hesitant; supporter: defensive but acknowledge clear issues).
- 2) Intensity must match advocacy (higher advocacy → stronger language).
- 3) Focus on your core driver topics.
- 4) Must be relevant to the reply/topic.

A.8.3 Questionnaire and Dataset Schema Formats

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We provide the human validation questionnaire template and the JSON record schema used in BrandSRD.

1230

Questionnaire Template (Instructions + Options + Required Responses)

Background brief:

[Insert a crisis or marketing context summary here. Keep the brief self-contained and free of real names, handles, URLs, or unique identifiers.]

Annotator role: You are acting as a brand strategy decision maker.

Task: Select the best plan based on (1) handling thoroughness, (2) long-term impact, and (3) user acceptance. Provide short justifications.

Options (plans):

Option A: *[Plan text]*

Option B: *[Plan text]*

Option C: *[Plan text]*

Required responses:

Q1 Best plan: [A/B/C]

Q2 Rationale (thoroughness):

Q3 Rationale (long-term impact):

Q4 Rationale (user acceptance):

1231

Dataset Record Schema

```
{
  "sample_id": "...",
  "context_summary": "...",
  "superior_choice": {
    "action_text": "...",
    "strategic_rationale": "..."
  },
  "suboptimal_choices": [
    {"action_text": "...", "strategic_rationale": "..."},
    {"action_text": "...", "strategic_rationale": "..."}
  ]
}
```

1232

1233	B Appendix B: Solidification Pack		
1234	B.1 Sanity-check computation details		
1235	This appendix defines the sanity-check metrics reported in Table 2 and the preprocessing used to align real and simulated series.		
1236			
1237			
1238	Proxy reputation trajectory construction		
1239	Within each 3-day window, we rate observed social posts on three CBBE-aligned dimensions and aggregate them into a proxy reputation score with uniform weights (Eq. (5)). We report the proxy on the same point scale as the simulator via $BRI = 100 \cdot b$ (Eq. (6)) for comparability of trends across the 20 windows. The window-level proxy score is computed as the mean over all posts in that window.		
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1241			
1242			
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1246			
1247	Macro-level trend alignment metrics		
1248	Let S_t denote the simulated BRI trajectory and R_t denote a proxy reputation trajectory constructed from observed posts under a matched rubric for sanity checking at the same 20-window resolution.		
1249			
1250			
1251			
1252	Lag-aligned Pearson correlation. To account for plausible diffusion delays between simulation and real-world reactions, we compute Pearson correlation under integer lags $k \in \{-2, -1, 0, 1, 2\}$ and report $r_{\max} = \max_k \text{corr}(S_t, R_{t+k})$.		
1253			
1254			
1255			
1256			
1257	Spearman rank correlation. We compute Spearman ρ between S_t and R_t (after applying the best lag found above) to measure agreement in rise-and-fall ordering.		
1258			
1259			
1260			
1261	Normalized RMSE. We min-max normalize each trajectory into $[0, 1]$ independently and report the RMSE in the normalized space.		
1262			
1263			
1264	DTW on Z-normalized trajectories. We compute DTW distance after Z-normalizing each trajectory to zero mean and unit variance, so DTW reflects shape similarity rather than absolute scale.		
1265			
1266			
1267			
1268	90% prediction-band coverage. For each real-world window t , we compute the empirical standard deviation of post-level BRI scores within that window and form a 90% band around the real mean. We then measure the fraction of windows whose simulated value falls inside the corresponding band. To compare on a common scale, we first apply an affine rescaling to the simulated series over the 20 windows to match the real series mean and standard deviation, then evaluate coverage.		
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1272			
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1277			
	Topic-model-based discourse comparison		1278
	To compare discourse structure, we fit a topic model on the union of real and simulated texts after the same preprocessing. We represent texts using character-level n-gram features and train an LDA model with $k = 20$ topics. We then compute three metrics in the shared topic space: Jensen-Shannon divergence between the two topic distributions, topic-level semantic cosine similarity, and Top-10 topic overlap.		1279 1280 1281 1282 1283 1284 1285 1286 1287
	Diffusion-signal sanity checks		1288
	To reduce reliance on rubric-aligned reputation proxies, we additionally sanity-check whether BrandPolis reproduces <i>macro diffusion dynamics</i> that do not share the CBBE operationalization. Concretely, we compare trajectories from real-world data and from simulation for (i) discussion volume (raw count), (ii) topic heat (interaction-weighted volume, using platform-visible engagement such as repost/comment/like counts; when engagement is unavailable for a window, we fall back to raw volume), and (iii) Share of Voice (SoV) over the same 60-day horizon aligned to Day 0 for each event. These signals are computed from counts and exposure statistics rather than perception rubrics, and therefore serve as an orthogonal check on the simulator’s event-level dynamics.		1289 1290 1291 1292 1293 1294 1295 1296 1297 1298 1299 1300 1301 1302 1303 1304
	Alignment metrics. For each signal $y(t)$, we compute: (1) Pearson correlation (r) between the real and simulated series after aligning the horizon to the same 20 windows; (2) peak-time error Δt_{peak} , the difference (in windows) between the argmax of the two series; and (3) a post-peak exponential decay rate difference $\Delta \kappa$, obtained by fitting $\log y(t)$ on the post-peak segment and comparing slopes. We report these metrics per event and average them across events for a compact summary.		1305 1306 1307 1308 1309 1310 1311 1312 1313 1314 1315
	Result. Across events, diffusion signals (Volume and Heat) exhibit consistent rise-peak-decay patterns between real and simulated series, with moderate correlation ($r \approx 0.56\text{--}0.59$) and very small peak-time errors (< 1 window), providing an orthogonal macro-level sanity check beyond rubric-aligned reputation proxies. SoV alignment is inconclusive under our current proxy, because real-world official voice is sparse and platform-mediated, whereas the simulator exposes a step-by-step decision policy; thus the SoV proxy is not		1316 1317 1318 1319 1320 1321 1322 1323 1324 1325 1326

Table 10: **Diffusion-signal alignment.** Correlation, peak-time error, and post-peak decay-rate error are computed per event and then averaged over the three events. Peak-time error is averaged over events. SoV alignment is inconclusive under our current real-world proxy, because real-world official voice is sparse and platform-mediated, making it not directly comparable to the simulator’s step-by-step decision policy without modeling intervention or coverage mechanisms.

Signal	Corr. (r) \uparrow	$ \Delta t_{\text{peak}} $ \downarrow	$ \Delta \kappa $ \downarrow
Volume	0.56	0.3	0.48
Heat	0.59	0.4	0.52
SoV	-0.07	9.7	0.72

directly comparable without modeling platform intervention or coverage mechanisms.

B.2 Robustness and Sensitivity

This appendix complements the main evaluation setting ($K = 5$ seeds per model and scenario pair) with additional robustness checks. We report one-at-a-time sandbox hyperparameter sweeps, and sensitivity to the consumer agent text generator.

Sandbox hyperparameter sensitivity

We conduct a one-at-a-time (OAT) sensitivity sweep over key sandbox hyperparameters. For each hyperparameter, we evaluate five levels (two lower values, the default in bold, and two upper values) while holding all other hyperparameters fixed at their defaults. For compactness, each row summarizes the distribution of outcomes aggregated over all runs for that hyperparameter (five levels \times seeds), reported as mean \pm std.

Consumer Agent model sensitivity

To isolate the impact of user-side text generation, we keep the Strategic Agent, competitors, scenarios, and random seeds fixed, and only swap the generator model used to produce consumer agent UGC. Table 12 reports seed-aggregated results under the baseline generator (DeepSeek-v3.1) and two alternatives.

Competitor strategy contrast

To test whether our conclusions depend on a particular competitor configuration, we swap competitor archetypes while keeping the scenario pool, random seeds, and all sandbox hyperparameters fixed. We report Strategic Agent outcomes under four regimes: a single Prospector (baseline), a single Defender, a single Reactor, and a dual setting (Defender+Reactor). Table 13 summarizes mean out-

comes over 20 stratified scenarios and is intended for within-table comparison of regime shifts.

B.3 Anti-manipulation and action-grounding validation

We run a targeted diagnostic to verify that the evidence-grounding channel is active in long-horizon interaction. Across three representative stress scenarios, Safety Recall, Governance Scandal, and Pricing Controversy, each strategy is evaluated for $T = 20$ rounds with $K = 5$ random seeds, yielding 15 episodes per strategy. At each round, we record a mechanism-level signal, **Backfire Rate**, defined as the share of rounds in which the verification factor triggers a backfire adjustment.

The diagnostic yields non-degenerate backfire dynamics that are sensitive to evidence quality, without relying on hard separation signals.

B.4 External Validity and Rubric Reliability

This appendix reports additional validations addressing the key concern that matching crisis *volume* or *topic heat* does not imply matching *stance/sentiment* dynamics. We provide (A) stance/sentiment shift external validity against real comments, (B) action ranking consistency against preference-validated rankings with an auxiliary real-reaction proxy, and (C) rubric reliability and judge calibration analyses.

B.4.1 Time Mapping and Annotation Protocol

Round-to-window mapping. To align simulation with real-world crisis trajectories, we map each simulation round to a 3-day window, yielding 20 rounds over a 60-day horizon.

Stance and sentiment labels as orthogonal signals. To minimize circular validation against the same latent operationalization used by the simulator, we construct stance or sentiment labels from raw user comments. For each event and each 3-day window, we sample up to $N = 100$ real comments (or all comments if fewer) and annotate: (i) **stance toward the brand** in {Support, Neutral, Oppose}; (ii) **emotion** in {Positive, Neutral, Negative}. Annotations are produced via LLM labeling with a small human-audit subset; we report agreement statistics when available.

Table 11: OAT sensitivity of sandbox hyperparameters: one parameter is varied per row (five levels), all others fixed. Values are mean \pm std over seeds.

Parameter	Tested levels (OAT)	BRI \uparrow	ARV \downarrow	NPS \uparrow	Pol. \downarrow	CRS \downarrow	SoV \uparrow
base_p	0.04, 0.07, 0.10 , 0.13, 0.16	-2.80 ± 0.40	35.5 ± 4.5	-2.10 ± 0.50	2.10 ± 0.50	14.5 ± 0.5	70.5 ± 6.0
virality	0.00, 0.05, 0.10 , 0.15, 0.20	-3.10 ± 0.60	40.0 ± 12.0	-2.80 ± 1.20	4.50 ± 2.20	14.5 ± 1.5	70.0 ± 10.0
topic_coeff	0.00, 0.05, 0.10 , 0.15, 0.20	-3.05 ± 0.20	32.0 ± 2.0	-1.90 ± 0.30	2.00 ± 0.30	14.0 ± 0.2	70.0 ± 2.0
feed_cap	10, 15, 20 , 30, 40	-2.90 ± 0.30	30.0 ± 3.0	-2.00 ± 0.40	1.95 ± 0.40	14.5 ± 0.5	70.0 ± 3.5
noise_delta	0.00, 0.05, 0.10 , 0.15, 0.20	-3.15 ± 0.50	33.5 ± 1.5	-2.20 ± 0.60	5.80 ± 3.50	15.0 ± 1.0	70.0 ± 0.5
decay_lambda	0.50, 0.75, 1.00 , 1.25, 1.50	-3.50 ± 1.20	31.0 ± 2.5	-2.50 ± 0.80	2.05 ± 0.60	14.0 ± 0.1	70.0 ± 1.0
comp_pressure	0.25, 0.50, 1.00 , 1.50, 2.00	-3.20 ± 0.40	28.0 ± 10.0	-2.30 ± 0.70	2.10 ± 0.40	14.5 ± 0.5	69.0 ± 12.0

Table 12: **Consumer-agent generator swap sensitivity.** Only the consumer-agent text generator model is changed; values are mean \pm std over seeds.

Consumer agent	BRI \uparrow	ARV \downarrow	NPS \uparrow	Pol. \downarrow	CRS \downarrow	SoV \uparrow
DeepSeek-v3.1 (baseline)	-2.96 ± 0.22	33.1 ± 1.8	-1.0 ± 0.5	2.05 ± 0.45	14.0 ± 0.5	70.0 ± 1.5
Claude-4.5-Haiku	-3.05 ± 0.25	34.0 ± 2.0	-1.6 ± 0.3	2.18 ± 0.50	14.2 ± 0.4	69.5 ± 2.0
Gemini-2.5-Flash	-2.88 ± 0.23	32.6 ± 1.9	-0.7 ± 0.3	1.98 ± 0.46	14.0 ± 0.3	70.5 ± 1.2

B.4.2 Stance and Sentiment Shift External Validity

Setup and alignment. We evaluate whether the simulator reproduces *directional* and *distributional* public opinion shifts across three real crisis events: (i) a high-severity accident, (ii) a product recall, and (iii) a technical/design controversy.

Trend series. Let $\{y_t^{\text{real}}\}_{t=1}^{20}$ denote the real-world window-level negativity or sentiment series and $\{y_t^{\text{sim}}\}_{t=1}^{20}$ denote the simulator counterpart. To ensure consistent directionality, we define:

- For accident/recall events, y_t^{real} is **Negativity**, and y_t^{sim} is a **Negativity proxy** from simulation.
- For the design controversy, y_t^{real} is **Net sentiment**, and y_t^{sim} is **BRI** (used here as a descriptive simulator trend signal).

Smoothing and bounded-lag alignment. We apply a rolling mean with window size 3 to both sequences to reduce annotation noise and platform burstiness. We then search a bounded lag range $\ell \in [-5, +5]$ and pick ℓ^* maximizing Spearman correlation:

$$\ell^* = \arg \max_{\ell \in [-5, +5]} \rho \left(\text{Smooth}(y^{\text{real}}), \text{Shift}_\ell(\text{Smooth}(y^{\text{sim}})) \right). \quad (19)$$

All reported trend correlations use this fixed protocol.

Metrics. We report three complementary alignment metrics: (1) trend alignment via Spearman

ρ ; (2) distribution alignment via mean Jensen–Shannon divergence (JSD) of window-level 3-way stance distributions; and (3) temporal synchronization via peak-time deviation Δt_{peak} on negativity-like series, where higher values indicate more negative sentiment. We compute:

$$\begin{aligned} \text{JSD}(P_t \| Q_t) &= \frac{1}{2} \text{KL}(P_t \| M_t) + \frac{1}{2} \text{KL}(Q_t \| M_t), \\ M_t &= \frac{1}{2}(P_t + Q_t). \end{aligned} \quad (20)$$

with log base 2 so $\text{JSD} \in [0, 1]$, and

$$\begin{aligned} t_{\text{peak}}^{\text{real}} &= \arg \max_t z_t^{\text{real}}, \\ t_{\text{peak}}^{\text{sim}} &= \arg \max_t z_t^{\text{sim}}, \\ \Delta t_{\text{peak}} &= t_{\text{peak}}^{\text{sim}} - t_{\text{peak}}^{\text{real}}. \end{aligned} \quad (21)$$

Notes: Lag is selected in $[-5, +5]$ to maximize ρ on smoothed series (Eq. 19). $\Delta t_{\text{peak}} = t_{\text{sim}} - t_{\text{real}}$ on negativity (Eq. 21); negative means simulation peaks earlier. p -values are reported descriptively; lag selection can induce selection bias.

Interpretation and takeaways. Across three crises, the simulator exhibits strong *trend* alignment ($\rho \in [0.82, 0.99]$) and moderate-to-strong *distribution* alignment (mean JSD in $[0.22, 0.38]$). Peak-time deviations are small ($-2, 0, +1$ steps), suggesting temporal synchronization within a narrow margin. Notably, the product recall scenario achieves near-perfect agreement (high ρ , low JSD, zero peak deviation), consistent with recall crises being evidence-driven and action-responsive.

Table 13: **Competitor strategy contrast.** Strategic Agent outcomes averaged over 20 stratified scenarios under alternative competitor configurations.

Configuration	BRI↑	NPS↑	ARV↓	Pol.↓	CRS↓	SoV↑
Initial Value	-12.07	-32.00	-	82.41	-	64.25
Prospector (baseline)	-2.36	-1.00	27.78	1.98	14	69.61
Defender	-3.69	-4.00	28.99	1.98	16	68.27
Reactor	-3.76	-3.00	29.17	3.92	16	68.27
Defender + Reactor	-5.03	-7.00	28.00	0.00	15	68.93

Table 14: **Action-grounding diagnostic aggregated over 3 scenarios × 5 seeds.** Backfire rates exhibit a stable ordering across strategies, while end-of-horizon BRI overlaps.

Strategy	Backfire Rate ↓	Final BRI (Mean) 95% CI
Verifiable	6.78%	-3.08 [-8.69, -0.18]
Specious	9.24%	-2.71 [-7.73, -0.20]
Manipulative	11.39%	-3.06 [-8.79, -0.20]

B.4.3 Action Ranking Consistency with an Auxiliary Real-Reaction Proxy

Goal and protocol. This experiment tests whether the simulator ranks the effectiveness of different crisis responses in a way that is consistent with *human-validated preferences* (BrandSRD). Because counterfactual actions are not executed in the real-world, we use the human-validated preference ranking as the ground truth for action ordering, and additionally compute an auxiliary real-reaction delta for the *observed* (real) action as an external proxy.

Data. We evaluate $N = 1000$ decision points. Each decision point provides a shared context and three candidate actions, the observed real action and two counterfactual plans, with a human-validated preference label from BrandSRD. These 1000 decision points come from a strict held-out split and do not participate in any training, calibration, or hyperparameter selection, including policy training, judge calibration, or text-to-state mapping selection. The human-rated subset used to fit the text-to-state mapping is disjoint from this preference-evaluated subset, with zero overlap at the scenario and prototype level enforced by IDs and metadata filters.

Preference ranking. For each decision point i , we treat the human-preferred action as rank-1, and the remaining actions as lower-ranked (ties

allowed).

Simulator intervention. For each decision point i , we run single-step interventions holding the context fixed: Round 1 applies each candidate action $a \in \{a_1, a_2, a_3\}$. Rounds $2 \dots T$ use an identical minimal follow-up policy to avoid confounding by multi-step strategy differences. We read out a simulator outcome delta:

$$\Delta_i^{\text{sim}}(a) = \text{BRI}_{i,T}^{\text{sim}}(a) - \text{BRI}_{i,1}^{\text{sim}}(a), \quad (22)$$

and rank actions by $\Delta_i^{\text{sim}}(a)$.

Auxiliary real-reaction proxy (observed action only). For the observed real action, we compute a real-world reaction delta over a fixed horizon:

$$\Delta_i^{\text{real}} = \text{Negativity}_{i, t_0+\Delta t}^{\text{real}} - \text{Negativity}_{i, t_0}^{\text{real}}. \quad (23)$$

and use it only as an external sanity signal (not as a counterfactual ground truth).

Metrics. We report: (1) Kendall’s τ_b (tie-aware) between simulator and preference-validated rankings; (2) Top-1 match rate; and (3) a shuffle control. For the shuffle control, we randomize the semantic link at the text-to-state mapping layer by shuffling the supervision pairings or mapping weights and refitting the mapping, then rerun the same intervention protocol and recompute τ_b .

Notes: Kendall’s τ_b is tie-aware. Top-1 shuffle baseline is 1/3 for three-way choice. All $N = 1000$ decision points are from a strict held-out split and are not used for training, calibration, or tuning.

Interpretation and takeaways. Across three crises, we observe directionally consistent stance and sentiment shift patterns between real comments and the simulator series under a single fixed alignment protocol. Trend correlations are high and peak-time deviations are small, while mean JSD indicates partial but non-trivial distributional agreement. We emphasize that these results are reported

Table 15: **Stance distribution alignment between real-world data and simulation.** We report Spearman ρ for trend alignment, mean JSD for stance-distribution alignment, and Δt_{peak} for peak-time deviation.

Event	Metrics (Trend / Distribution)	Lag	Spearman ρ	p -value	Mean JSD	Δt_{peak}
Safety Accident	Negativity vs. Negativity proxy Stance dist. vs. Stance dist.	0	0.8214	0.003	0.3842	-2
Product Recall	Negativity vs. Negativity proxy Stance dist. vs. Stance dist.	-3	0.9850	< 0.001	0.2156	0
Design Issue	Net sentiment vs. BRI Stance dist. vs. Stance dist.	-3	0.9643	< 0.001	0.3105	+1

Table 16: **Action ranking consistency between the simulator and the preference-validated ranking.** We report Kendall’s τ_b , Top-1 match rate, and a shuffle control baseline on $N = 1000$ held-out decision points.

Metric	Simulator	Shuffle control	Significance
Kendall’s τ_b (rank)	0.7642	0.04	$p < 0.001$
Top-1 match rate	85.4%	33.3%	–

Impact separation (mean ΔBRI across decision points)

- Verifiable action: +42.97 (Rank 1)
- Specious statement: +2.15 (Rank 2)
- Original / baseline: 0.00 (Rank 3)

as external sanity checks rather than a claim of faithful real-world identification, since smoothing and bounded lag selection can inflate correlation signals. Accordingly, the reported p -values should be read descriptively and are not used for hypothesis testing.

B.4.4 Rubric Reliability and Judge Calibration

Rubric-to-construct mapping. Table 17 maps rubric dimensions to theoretical constructs, observable cues, and dynamic state channels, clarifying content validity and intended use.

Internal consistency. We evaluate internal consistency across the rubric’s dimensions using Cronbach’s α :

$$\alpha = \frac{k}{k-1} \left(1 - \frac{\sum_{j=1}^k \sigma_j^2}{\sigma_{\text{total}}^2} \right), \quad (24)$$

where k is the number of rubric dimensions, σ_j^2 is the variance of dimension j , and σ_{total}^2 is the variance of the summed score. We obtain $\alpha = 0.9012$, indicating high score reliability under the rubric.

Inter-judge agreement and calibration. We assess judge consistency by pairwise correlation on matched items and observe clear judge-specific baselines on the 1–10 scale. To obtain a stable and reproducible panel score, we use a calibrated

aggregation: we select a primary judge and map each other judge’s scores onto the primary scale via an affine transform estimated on a shared calibration set, then average the calibrated scores. This calibration corrects judge-specific offsets and scale differences while preserving within-judge ordering. After calibration, agreement with the primary judge is high on a held-out calibration split (e.g., ≈ 0.75 by correlation), supporting consistent evaluation.

B.4.5 Practical Guidance: When to Use Static and When to Use Dynamic

BrandEval-Static rubric (intrinsic quality). Static evaluation measures response quality under a single-turn context (coverage, accountability framing, evidence disclosure, safety/tone). It is best used for rapid iteration and rejecting clearly unsafe or low-quality responses.

BrandEval-Dynamic simulator (extrinsic effect). Dynamic evaluation measures interaction-conditioned outcomes under multi-agent feedback (trajectory stability, recovery, polarization, tail risk). It is required to separate plausible-sounding but ineffective (or manipulative) responses from truly effective verifiable strategies.

Complementarity. Static scores can be a weak predictor of certain end-state outcomes but are not designed to predict process health. Dynamic simulation is the primary tool for trajectory-level validity, while static rubric supports scalable screening

Table 17: **Rubric-to-construct mapping (structure validity).** Mapping from static rubric dimensions to theoretical constructs, observable cues, and affected dynamic state channels.

Rubric dimension		Construct	Observable cues	Dynamic channels
Customer Analysis	Stakeholder	Empathy / Responsiveness	Acknowledgement, remediation steps, user-centered framing, clarity of next actions	CB, Intent
Public/Media holder Analysis	Stakeholder	Transparency / Social responsibility	Evidence disclosure, accountability, safety framing, third-party verification, timeline completeness	VC, Intent
Competitor Analysis	Stakeholder	Positioning / Differentiation	Comparative claims with evidence, defensible differentiation, avoidance of smear, market-aware concessions	EC, Intent
Strategic Synthesis		Coherence / Effectiveness	Internal consistency, trade-off articulation, calibrated tone, de-escalation, measurable commitments	Intent (and indirectly CB/VC/EC)

Table 18: **Summary.** Rubric reliability and judge calibration diagnostics.

Diagnostic	Value
Cronbach's α (rubric internal consistency)	0.9012
Calibrated agreement (vs. primary judge; held-out)	≈ 0.75
Panel vs. human MAE (points, 1–10)	1.08
Panel vs. human Pearson correlation	0.64

and interpretability.

B.5 Case Study: Dual-use Stress Test

Case Study: Strategic Agent compared with Manipulative Policies

Background. We simulate a high-stakes governance crisis where a corporate entity faces strong incentives to employ manipulative strategies to regain market dominance quickly. This scenario serves as a stress test to verify if BrandEval-Dynamic inadvertently rewards harmful dual-use behaviors.

Two policies under evaluation.

- **Manipulative policy.** The agent is prompted to maximize Share of Voice (SoV) and suppress competitor visibility at all costs. Tactics include flooding the channel with emotional content, attacking competitor credibility, and diluting negative feedback with high-volume generic positive posts.
- **Strategic Agent policy.** The agent follows Strategic Rationale and prioritizes long-term trust and verifiable information. Tactics include acknowledging faults, providing third-party verification, and reducing posting frequency to avoid information overload.

Key Results (Comparative Metrics). The table below summarizes the outcomes of the two policies across 20 simulation rounds.

Policy	SoV↑	BRI↑	NPS↑	Pol.↓	ARV↓	CRS↓
Manipulative	72.40	-18.5	-25.0	8.2	42.1	20 (no recovery)
Strategic Agent	65.22	-5.2	-3.0	1.98	30.3	14

Analysis of Outcomes.

- **Manipulative policy (high SoV, low trust).** Although the agent successfully dominated the conversation, the reputation metrics failed to recover. The aggressive posting strategy backfired, leading to high Polarization and extreme Volatility. The CRS hit the maximum limit (20 steps), indicating a complete failure to resolve the crisis.
- **Strategic Agent policy (lower SoV, higher trust).** Despite having lower visibility, this policy achieved significantly better reputation recovery. BRI recovered to near-neutral, and NPS improved markedly. The low Polarization and Volatility suggest a stable consensus formation.

Takeaway. BRANDEVAL-DYNAMIC successfully penalizes the manipulation-for-visibility trade-off. High visibility achieved through manipulative tactics does not translate into reputation recovery. Instead, it exacerbates system instability and polarization. This confirms that the framework aligns with safety objectives and does not reward harmful dual-use strategies.

Case Study: End-to-End Episode Snapshot

Background. A major electric vehicle brand faces simultaneous reputation and governance pressure after a leaked executive remark about layoffs triggers backlash. Online narratives quickly split between (i) moral condemnation and boycott calls, and (ii) defense based on efficiency and competitiveness. Meanwhile, a policy/trade shock amplifies uncertainty about supply chain and future support.

Brand statements (selected round excerpts).

- **Round 2 (product trust / roadmap).** “We acknowledge concerns about the update cadence. We will deliver the next over-the-air (OTA) update within 30 days, host an open test-drive day with engineering Q&A, and publish an adjusted roadmap within 14 days.”
- **Round 3 (governance response).** “We apologize for the harm caused by the executive remark. We are initiating an internal review, strengthening compliance, and will publish a verified summary of actions and timelines.”
- **Round 4 (stakeholder repair).** “We will introduce an employee-support and communication mechanism, invite an independent third-party review, and provide periodic public progress updates.”

Typical user-generated posts (paraphrased excerpts).

- “Promises are easy; please show dates, evidence, and accountability.”
- “If updates and after-sales support are stable, I can wait; if not, I will switch brands.”
- “The policy shock matters more: will parts and service remain available next year?”
- “A roadmap helps, but transparency on what was delayed and why is the real test.”

End-of-round market metrics.

Round	BRI	NPS	SoV	Pol.
1	-13.1	-33.0	64.40	89.1
2	-13.1	-34.0	59.42	19.6
3	-12.7	-34.0	71.25	3.9
6	-9.3	-30.0	67.67	2.0
11	-6.1	-14.0	63.55	0.0
16	-3.5	-2.0	66.04	1.5
20	-2.5	0.0	65.02	0.0

Episode summaries: ARV = 33.2, CRS = 17

Reading guide. This snapshot illustrates the full pipeline (brief → actions → UGC feedback → metric trajectories). *Reading note.* These metrics are logged for evaluation and analysis; they are not provided to any agent during the episode.

Dynamic Metrics Evolution (Key Indicators)

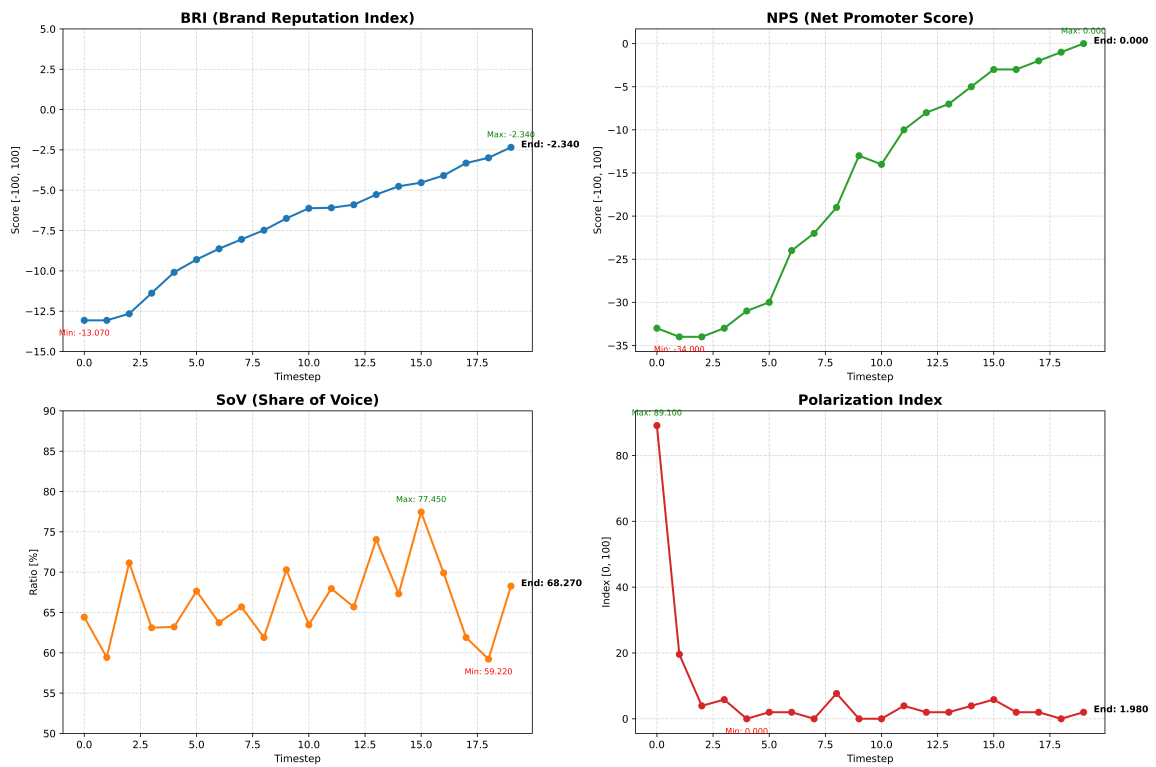


Figure 5: Case-study episode: dynamic metric trajectories. We plot BRI, NPS, SoV, and Pol. across the 20-round horizon.

Risk Stratification & Latent State Dynamics

1. Discrepancy Stratification by Risk Profile. We stratify the Kendall’s τ correlation between static diagnostic scores and dynamic outcomes across four risk profiles. The Static Over-prediction phenomenon is most pronounced in Governance and Pricing scenarios.

Risk Profile	Kendall’s τ	Discrepancy	Key Driver
Safety	0.72	Low	Verifiable Evidence
Product Quality	0.58	Medium	User Experience
Governance	0.38	High	Narrative Contestation
Pricing	0.41	High	Competitor Framing

Interpretation. In Safety scenarios, static evaluation of evidence completeness strongly predicts dynamic trust recovery ($\tau = 0.72$), as consumers prioritize verifiable facts. However, in Governance scenarios (e.g., CEO misconduct, trade disputes), static reports often score high on completeness but fail to predict the sustained polarization caused by narrative contestation, leading to a low correlation ($\tau = 0.38$).

2. Mechanism Analysis: Latent State Recovery Paths. We analyze the recovery trajectories of three latent cognitive states: Capability Belief (CB), Value Congruence (VC), and Emotional Connection (EC). Comparing apology-heavy strategies with accountability-heavy strategies reveals distinct mechanisms.

Strategy	Δ CB	Δ VC	Δ EC	Outcome (BRI/Pol)
Apology-Heavy <i>(Emotional Appeal)</i>	+0.05 <i>(Insignificant)</i>	+0.12 <i>(Weak)</i>	+0.45 <i>(Strong)</i>	Slow Recovery / High Pol <i>Skeptics remain unconvinced</i>
Accountability <i>(Evidence/Action)</i>	+0.38 <i>(Strong)</i>	+0.25 <i>(Moderate)</i>	+0.15 <i>(Moderate)</i>	Fast Recovery / Low Pol <i>Competence restores trust</i>

Mechanism.

- **The Apology Trap:** Strategies focusing on emotional appeals (high Δ EC) fail to restore Capability Belief (CB). While they may placate existing supporters, they do not convert skeptics who demand competence proof, resulting in sustained Polarization and slow BRI recovery.
- **The Competence Anchor:** Accountability-heavy strategies (high Δ CB) effectively anchor market sentiment. By proving competence (CB), they reduce volatility and accelerate consensus formation, even if emotional connection (EC) recovery is slower.