QUALITY DIVERSITY IMITATION LEARNING

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Abstract

Imitation learning (IL) has shown great potential in various applications, such as robot control. However, traditional IL methods are usually designed to learn only one specific type of behavior since demonstrations typically correspond to a single expert. In this work, we introduce the first generic framework for Quality Diversity Imitation Learning (QD-IL), which enables the agent to learn a broad range of skills from limited demonstrations. Our framework integrates the principles of quality diversity with adversarial imitation learning (AIL) methods, and can potentially improve any inverse reinforcement learning (IRL) method. Empirically, our framework significantly improves the QD performance of GAIL and VAIL on the challenging continuous control tasks derived from Mujoco environments. Moreover, our method even achieves 2x expert performance in the Humanoid environment.

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022 1 INTRODUCTION 023

Imitation learning (IL) enables intelligent systems to quickly learn complex tasks by learning from demonstrations, which is particularly useful when manually designing a reward function is difficult.
IL has been applied to many real-world scenarios such as autonomous driving (Bojarski, 2016), robotic manipulation (Zhu et al., 2018), surgical skill learning (Gao et al., 2014), and drone control (Ross et al., 2013). The concept of IL relies on the idea that experts can showcase desired behaviors, when they are unable to directly code them into a pre-defined program. This makes IL applicable to any system requiring autonomous behavior that mirrors expertise (Zare et al., 2024).

However, traditional IL methods tend to replicate only the specific strategies demonstrated by the expert. If the expert demonstrations cover a narrow range of scenarios, the model may struggle when faced with new or unseen situations. Additionally, IL faces challenges in stochastic environments where outcomes are uncertain or highly variable. Since the expert's actions may not capture all possible states or contingencies, IL often struggles to learn an optimal strategy for every scenario (Zare et al., 2024). These limitations are further exacerbated when the demonstration data is limited, as the IL algorithm will only learn specific expert behavior patterns. Hence, traditional IL methods are significantly constrained due to the lack of ability to learn diverse behavior patterns to adapt to stochastic and dynamic environments.

On the other hand, the Quality Diversity (QD) algorithm is designed to find diverse (defined by 040 measure m) solutions to optimization problems while maximizing each solution's fitness value (fitness 041 refers to the problem's objective) (Pugh et al., 2016). For instance, QD algorithms can generate 042 diverse human faces resembling "Elon Musk" with various features, such as different eye colors 043 (Fontaine & Nikolaidis, 2021). In robot control, the QD algorithm excels at training policies with 044 diverse behaviors. This enhances the agent's robustness in handling stochastic situations (Tjanaka et al., 2022). For example, if an agent's leg is damaged, it can adapt by switching to a policy that 046 uses the other undamaged leg to hop forward. Different ways of moving forward represent diverse 047 behavior patterns (Fontaine & Nikolaidis, 2021). Traditional QD algorithms often use evolutionary 048 strategies (ES). They have been successful in exploring solution space but suffer from lower fitness due to the large solution spaces, especially when the solution is parameterized by neural networks (Hansen, 2006; Salimans et al., 2017). Recent works combining ES with gradient approximations 051 in differentiable QD (DQD) have significantly improved the ability to discover high-performing and diverse solutions (Fontaine & Nikolaidis, 2021). Naturally, one valuable question is raised: 052 can we design a novel IL framework that can combine the respective strengths of traditional IL and QD algorithms, enabling the agent to learn a broad set of high-performing skills from limited



063 Figure 1: (a) The dashed lines divide the policy space into regions constrained by different measures. 064 While PPGA stores high-performing policies for each behavioral region it explores, it overemphasises 065 particular regions of the behavior space (see yellow bars). Introducing the measure bonus helps 066 to improve this exploration process, encouraging exploration in other behavioral regions. (b) The 067 left figure shows traditional IL, where the agent learns a single policy mimicking the expert. In contrast, QD-IL learns from multiple diverse expert policies, such that many behaviors are considered 068 high-performing, resulting in a set of policies, represented by the curve. The orange bar means the 069 expert policy and f means fitness (cumulative reward). 070

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demonstrations? We call such IL framework as Quality Diversity Imitation Learning (QD-IL). Based
 on our extensive investigations, we found that there is no existing QD-IL work. To mitigate this gap,
 we first identify the two key challenges of QD-IL as follows:

1) Unbalanced exploration and exploitation:

076 From an optimization perspective, we observed 077 that the objective of QD can be framed as solving multiple optimization problems with varying constraints based on measure m. Ideally, the 079 policy should explore all regions equally rather than getting stuck in local optima, as depicted 081 in Figure 1(a). However, policy space contains numerous local optima (Dauphin et al., 2014), 083 leading to a lack of behavior-space exploration. 084 2) Localized reward: Traditional Inverse Re-085 inforcement Learning (IRL) methods are inherently formulated based on a single expert policy, 087 as illustrated in the left figure of Figure 1(b).

Such a reward design results in a localized re-



Figure 2: An illustration of the quality-diversity policy archive shows behavior measure m, representing the leg ground contact time, where varying m results in diverse behaviors.

ward function, in the sense that it only counts a single behavior as being high-performing. Additionally,
 the localized reward will further exacerbate the local optima issue mentioned in 1) since we are
 interested in optimizing a wide range of behaviors, rather than only fitting the expert behavior.

092 To address these challenges, we introduce two key modifications to generic adversarial IL methods. To improve exploration of new behaviors, we introduce the measure bonus - a reward bonus designed to encourage exploration of new behavior patterns, preventing stagnation at local optima 094 and promoting balanced exploration. To prevent overly localized reward functions, we make two further modifications, namely a) we assume demonstrations are sampled from diverse behaviors 096 from different experts rather than a single expert, as illustrated in the right figure of Figure 1(b); and b) using such diverse demonstrations, we formulate measure conditioning, which enhances 098 the discriminator by incorporating the behavior measure m into its input. The measure m acts as a high-level state abstraction, enabling the generalization of the knowledge from limited demonstrations 100 to unseen states. The measure bonus also promotes the exploration of more diverse state and action 101 pairs. Combined with measure conditioning, this helps reduce the overfitting of the discriminator and 102 addresses the localized reward issue. By combining the measure bonus with measure conditioning, 103 we ensure continuous discovery of new behaviors while generalizing the behavior-level knowledge to 104 unseen situations so that the agent can learn diverse and high-performing policies, as illustrated in 105 Figure 2. To validate our framework, we conducted experiments with limited expert demonstrations across various environments. Notably, our framework is the first generic QD-IL approach, potentially 106 capable of enhancing any IRL method for QD tasks and also opens the possibility of Quality-Diversity 107 Imitation From Observation (QD-IFO) (Liu et al., 2018). It even surpasses expert performance in

terms of both QD-score and coverage in the Walker2d and challenging Humanoid environments. We
 summarize our contributions as follows:

- We design a measure-based reward bonus to directly encourage behavior-level exploration, which can be integrated into any IRL methods, maximizing the behavior space diversity.
- We propose a novel measure-conditional adversarial IL to generalize expert knowledge to diverse behaviors, which can be applied to most generic IRL algorithms.
- We identify the key challenges of QD-IL. To the best of our knowledge, this paper is the first work to bridge QD algorithms and a broad range of imitation learning methods, addressing the key limitation of traditional IL methods. Our framework provides a generic framework for future QD-IL research and potentially enhances any IL application that requires learning diverse policies.
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2 BACKGROUND

2.1 QUALITY DIVERSITY OPTIMIZATION

124 Distinct from traditional optimization which aims to find a single solution to maximize the objective, 125 Quality Diversity (QD) optimization aims to find a set of high-quality and diverse solutions in an *n*-dimensional continuous space \mathbb{R}^n . Given an objective function $f:\mathbb{R}^n\to\mathbb{R}$ and k-dimensional 126 measure function $m: \mathbb{R}^n \to \mathbb{R}^k$, the goal is to find solutions $\theta \in \mathbb{R}^n$ for each local region in the 127 behavior space $B = m(\mathbb{R}^n)$. Two canonical algorithms of QD are MAP-Elites Mouret & Clune 128 (2015a) and Novelty Search with Local Competition Lehman & Stanley (2011), which differ in terms 129 of how they structure the behavior space into an archive of solutions and how local competition 130 and replacement of solutions is performed (see also Cully & Demiris (2018) for an overview of QD 131 algorithm classifications). We focus on grid-based archives as in the MAP-Elites algorithm, which 132 discretize B into M cells, where each cell i = 1, ..., M represents a small hypercube $[a_i, b_i]$ within a 133 multi-dimensional grid of the behavioral measure space. A new solution replaces an existing solution 134 in the same cell if it outperforms it and falls within the same hypercube. Formally, the objective 135 is to find a set of solutions $\{\theta_i\}_{i=1}^M$ which maximises $f(\theta_i)$ for each $i = 1, \dots, M$. Each solution θ_i 136 corresponds to a cell in \mathscr{A} via its measure $m(\theta_i)$, forming an archive of high-quality and diverse 137 solutions (Chatzilygeroudis et al., 2021; Pugh et al., 2016).

Some traditional Quality Diversity optimization methods integrate Evolution Strategies (ES) with MAP-Elites (Mouret & Clune, 2015b), such as Covariance Matrix Adaptation MAP-Elites (CMA-ME) (Fontaine et al., 2020). CMA-ME uses CMA-ES (Hansen & Ostermeier, 2001) as ES algorithm generating new solutions that are inserted into the archive, and uses MAP-Elites to retains the highest-performing solution in each cell. CMA-ES adapts its sampling distribution based on archive improvements from offspring solutions. However, traditional ES faces low sample efficiency, especially for high-dimensional parameters such as neural networks.

145 Differentiable Quality Diversity (DQD) improves exploration and fitness by leveraging the gradients 146 of both objective and measure functions. Covariance Matrix Adaptation MAP-Elites via Gradient 147 Arborescence (CMA-MEGA) (Fontaine & Nikolaidis, 2021) optimizes both objective function fand measure functions m using gradients with respect to policy parameters: $\nabla f = \frac{\partial f}{\partial \theta}$ and $\nabla m =$ 148 $\left(\frac{\partial m_1}{\partial \theta}, \dots, \frac{\partial m_k}{\partial \theta}\right)$. The objective of CMA-MEGA is $g(\theta) = |c_0| f(\theta) + \sum_{j=1}^k c_j m_j(\theta)$, where the 149 150 coefficients c_i are sampled from a search distribution. CMA-MEGA maintains a search policy $\pi_{\theta_{ij}}$ in 151 policy parameter space, corresponding to a specific cell in the archive. CMA-MEGA generates local 152 gradients by combining gradient vectors with coefficient samples from CMA-ES, creating branched 153 policies $\pi_{\theta_1}, \ldots, \pi_{\theta_{\lambda}}$. These branched policies are ranked based on their archive improvement, which 154 measures how much they improve the QD-score (one QD metric, which will be discussed in the 155 experiment section) of the archive. The ranking guides CMA-ES to update the search distribution, 156 and yields a weighted linear recombination of gradients to step the search policy in the direction 157 of greatest archive improvement. The latest DQD algorithm, Covariance Matrix Adaptation MAP-158 Annealing via Gradient Arborescence (CMA-MAEGA) (Fontaine & Nikolaidis, 2023), introduces 159 soft archives, which maintain a dynamic threshold t_e for each cell. This threshold is updated by $t_e \leftarrow (1 - \alpha)t_e + \alpha f(\pi_{\theta_i})$ when new policies exceed the cell's threshold, where α balances the time 160 spent on exploring one region before exploring another region. This adaptive mechanism allows more 161 flexible optimization by balancing exploration and exploitation.

162 2.2 QUALITY DIVERSITY REINFORCEMENT LEARNING

164 The Quality Diversity Reinforcement Learning (QD-RL) problem can be viewed as maximizing 165 $f(\theta) = \mathbb{E}_{\pi_{\theta}} \left[\sum_{k=0}^{T-1} \gamma^k r(s_k, a_k) \right]$ with respect to diverse θ in a policy archive defined by measure m166 (Cideron et al., 2020). In OD-RL, both the objective and measure are non-differentiable, requiring 167 approximations by DQD approaches. Previous work employs TD3 to approximate gradients and ES 168 for exploration (Nilsson & Cully, 2021; Pierrot et al., 2021), but is constrained to off-policy methods. The state-of-the-art QD-RL algorithm, Proximal Policy Gradient Arborescence (PPGA), employs a vectorized PPO architecture to approximate the gradients of the objective and measure functions 170 (Batra et al., 2023). While the policy gradient can approximate the cumulative reward, the episode-171 based measure is harder to differentiate. PPGA addresses this by introducing the Markovian Measure 172 Proxy (MMP), a surrogate measure function that correlates strongly with the original measure and 173 allows gradient approximation via policy gradient by treating it as a reward function. PPGA uses 174 k+1 parallel environments with distinct reward functions – one for the original reward and k for the 175 surrogate measures. It approximates the gradients of both the objective and the k measure functions 176 by comparing the policy parameters before and after multiple PPO updates. These gradients are 177 then passed to the modified CMA-MAEGA to update the policy archive. We recommend readers to 178 explore prior works in depth (Batra et al., 2023) or refer to Appendix F for further details on PPGA 179 and related QD-RL methodologies.

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2.3 IMITATION LEARNING

In Imitation learning (IL) (Zare et al., 2024), an agent learns high-performing policies from demonstration data. A traditional approach to solve this challenge is Behavior Cloning (BC), which uses supervised learning to learn the policy from demonstrations, a technique which unfortunately suffers from severe error accumulation (Ross et al., 2011). More recent techniques include inverse reinforcement learning (IRL), where one seeks to learn a reward function from the demonstrations and then use RL to train a policy based on that reward function (Abbeel & Ng, 2004).

189 Early IRL methods estimate rewards using the principle of maximum entropy (Ziebart et al., 2008; 190 Wulfmeier et al., 2015; Finn et al., 2016). Recent adversarial IL methods treat IRL as a distribution-191 matching problem. For instance, Generative Adversarial Imitation Learning (GAIL) (Ho & Ermon, 192 2016) trains a discriminator to differentiate between the state-action distribution of the demonstrations 193 and the state-action distribution induced by the agent's policy, and output a reward to guide policy 194 improvement. Improving on GAIL, Variational Adversarial Imitation Learning (VAIL) (Peng et al., 2018b) applies a variational information bottleneck (VIB) (Alemi et al., 2016) to the discriminator, 195 improving the stability of adversarial learning. Another technique for adversarial IL is Adversarial 196 Inverse Reinforcement Learning (AIRL) (Fu et al., 2017), which learns a robust reward function by 197 training the discriminator via logistic regression to distinguish expert data from policy data. 198

199 Recently, one can also observe a variety of techniques for non-adversarial imitation learning. For 200 instance, Primal Wasserstein Imitation Learning (PWIL) (Dadashi et al., 2021) formulates the reward 201 function based on an upper bound of the Wasserstein distance between the expert and agent's state-action distributions, avoiding the instability of adversarial IL methods. Generative Intrinsic 202 Reward-driven Imitation Learning (GIRIL) (Yu et al., 2020) computes rewards offline by pretraining 203 a reward model using a conditional VAE (Sohn et al., 2015), which combines a backward action 204 encoding model with a forward dynamics model. The reward is then derived from the prediction error 205 between the actual next state and its reconstruction. GIRIL has demonstrated superior performance 206 even with limited demonstrations. 207

Our paper primarily focuses on IRL with limited demonstrations, and we compare our proposed approach to adversarial and non-adversarial techniques as baselines. More details about these baselines are provided in Appendix C. In addition to the IRL setting, we also investigate how our results translate to the related setting of Imitation From Observation (IFO), where only the experts' state sequences, rather than full state-action sequences, are available (Liu et al., 2018).

While we are the first to explore quality diversity imitation learning, related work uses diverse demonstrations to design policies that have the behavioral measure as one of the inputs (Justesen et al., 2020) rather than designing an archive of diverse policies. Subsequent to our work, WQDIL Yu et al. (2024) introduces a technique closely related to ours in terms of recognising behavior-space



Figure 3: MConbo-IRL: Based on episodes sampled from the current search policy, we use the measure conditioned reward model to compute the IRL reward and compare the current archive and the measure of episodes to compute the measure bonus. Then VPPO uses these reward values to approximate gradients for the objective and measures. Then these gradients are used to produce new solutions, update archive, update search distribution, and search policy based on the CMA-MAEGA paradigm.

exploration and measure-conditioning. Three key differences are that WQDIL uses a single-step archive for computing exploration bonus, applies a Wasserstein auto-encoder (WAE) with latent adversarial training, and uses the measure conditioning for learning latent variables with a WAE.

PROBLEM DEFINITION

Definition 1 (Quality-Diversity Imitation Learning). *Given expert demonstrations* $\mathcal{D} = \{(s_i, a_i)\}_{i=1}^n$ and their measures, where s_i and a_i are states and actions, QD-IL aims to learn an archive of diverse policies $\{\pi_{\theta_i}\}_{i=1}^M$ that collectively maximizes $f(\theta)$ (e.g., cumulative reward) without access to the true reward. The archive is defined by a k-dimensional measure function $m(\theta)$, representing behavior patterns. After dividing the archive into M cells, the objective of QD-IL is to find M solutions, each occupying one cell, to maximize:

$$\max_{\{\theta_i\}} \sum_{i=1}^M f(\theta_i). \tag{1}$$

4 PROPOSED METHOD

In this section, we will introduce our QD-IL framework, which aims to learn a QD-enhanced reward function using the QD-RL algorithm PPGA to learn the policy archive. Specifically, we propose the **measure bonus** to address the challenge of unbalanced exploration and exploitation and **measure conditioning** to address the challenge of localized reward. Figure 3 shows the main components of our framework, PPGA with Measure conditioned and bonus-driven Inverse Reinforcement Learning (PPGA with MConbo-IRL). We provide the pseudo-code of our framework in Appendix A.

4.1 MEASURE BONUS

The objective of QD-RL optimization in PPGA is: $g(\theta) = |c_0|f(\theta) + \sum_{j=1}^k c_j m_j(\theta)$, where dynamic coefficients c_i balance maximizing cumulative reward $f(\theta)$ and achieving diverse measures $m(\theta)$. However, we observed that the fitness term f heavily influences PPGA's search policy update direction, as archive improvement is primarily driven by f. PPGA frequently becomes stuck in local regions, generating overlapping solutions with only marginal improvements in the archive due to limited exploration. Therefore, it will explore less in other areas, as illustrated in Figure 1(a). Additionally, a key challenge in QD-IL is the conflict between imitation learning and diversity. Limited and monotone expert demonstrations lead to highly localized and sometimes misleading reward functions, further exacerbating the problem by restricting search policy updates. Hence, we aim to encourage the search policy to find new behavior patterns (i.e., the empty area in the policy archive).

Lemma 1. Suppose the reward function of one MDP is given by $r(s_t^i, a_t^i) = \mathbb{I}(m_i \in \mathscr{A}_e)$, where s_t^i and a_t^i represent the state and action at time step t of episode i, \mathscr{A}_e means the empty area of archive \mathscr{A} and $\mathbb{I}(m_i \in \mathscr{A}_e)$ is indicator function indicating whether the measure of i - th episode falls into \mathscr{A}_e . Then if one iteration of PPO successfully increases the objective value, the following inequalities hold:

 $(1): P(\pi_{\theta_{new}}|m \in \mathscr{A}_e) \ge P(\pi_{\theta_{old}}|m \in \mathscr{A}_e) \quad and \quad (2): P(m \in \mathscr{A}_e|\pi_{\theta_{new}}) \ge P(m \in \mathscr{A}_e|\pi_{\theta_{old}}),$

where $P(m \in \mathcal{A} | \pi_{\theta})$ means the probability of the event that the measure of one episode belongs to the unoccupied area \mathcal{A}_e , given this episode is generated by policy π_{θ} , and $P(\pi_{\theta} | m \in \mathcal{A}_e)$ means the probability that the policy, which generates the episodes that occupied \mathcal{A}_e , is exactly π_{θ} .

Lemma 1 demonstrates that using the indicator function $\mathbb{I}(m_i \in \mathscr{A}_e)$ as the reward function in the standard PPO objective steadily increases the probability that the policy generates episodes with new behavior patterns. We found this approach synergizes effectively with CMA-MEGA, encouraging the search policy to explore diverse behaviors. For the proof of Lemma 1 and a more detailed explanation of the synergy with CMA-MEGA, please refer to Appendix G.

However, we observed that using an indicator function results in binary rewards, which might be
 sparse and unstable. Moreover, we aim to control the weight of the measure bonus. Hence, we adopt
 a linear function of indicator for our Measure Bonus:

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$$r_{diversity}(s_t^i, a_t^i, m_i) = p + q\mathbb{I}(m_i \in \mathscr{A}_e), \tag{2}$$

294 where s_t^i and a_t^i represents the state and action at time step t of episode i, \mathcal{A}_e means the empty area of 295 current archive and m_i is the measure of episode *i*. The hyperparameter q controls the weight of the 296 measure bonus and the term p encourages the agent for staying in the episode, thereby facilitating the search for diverse behaviors. The trade-off between p and q represents how to emphasise staying in 297 the episode versus getting the measure bonus as frequently as possible. Measure Bonus is a type of 298 episode reward (Sutton, 2018), which is calculated at the end of each episode. The Measure Bonus 299 adaptively balances exploration and exploitation. Once a region in the archive has been sufficiently 300 explored, the bonus of this region decreases, allowing the focus to shift more towards exploitation. 301

Measure bonus improves policy diversity but doesn't guarantee the performance of diverse policies. To address this, we introduce measure conditioning, which can potentially be integrated into most IRL methods. We demonstrate this using two popular IRL methods, GAIL and VAIL.

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4.2.1 MCONBO-GAIL

The GAIL discriminator receives a state-action pair (s, a) and outputs how closely the agent's behavior resembles that of the expert, serving as a reward function. However, GAIL tends to overfit specific behaviors with limited demonstrations. In large state spaces, the discriminator struggles to generalize to unseen states (Kostrikov et al., 2018). This results in localized and sparse rewards, hindering quality diversity. Therefore, the core question in QD-IL is how to generalize knowledge from limited demonstrations to the entire policy archive while avoiding localized rewards.

To address this, we use the **Markovian Measure Proxy** (Batra et al., 2023). It decomposes trajectorybased measures into individual steps: $m_i(\theta) = \frac{1}{T} \sum_{t=0}^{T} \delta_i(s_t)$. This makes the measure state-dependent and Markovian. We make the key observation that the single-step measure $\delta_i(s_t)$ abstracts higherlevel task features such as ground contact in locomotion, while filtering out lower-level state details (e.g., joint angles and velocities). This provides a more general representation, enabling better generalization across the policy archive. By simply incorporating $\delta_i(s_t)$ as an additional input to the GAIL discriminator, we propose **Measure-Conditional-GAIL** with the following modified objective:

$$\max_{\pi} \min_{D_{\psi}} \mathbb{E}_{(s,a) \sim \mathscr{D}}[-\log D_{\psi}(s,a,\delta(s))] + \mathbb{E}_{(s,a) \sim \pi}[-\log(1 - D_{\psi}(s,a,\delta(s)))].$$
(3)

324 This approach encourages the discriminator to generalize by focusing on higher-level state descriptors 325 $\delta(s)$, capturing essential task-relevant features. It enables the agent to learn high-performing policies 326 from limited demonstrations, improving generalization to unseen states. The discriminator serves 327 as the basis for the reward, therefore with measure-conditioning the agent will get a high reward 328 for actions that mimic the experts, and particularly so when the expert is close in state-measure, which is an abstraction of the state. Due to it being an abstraction of the state, there is less risk of 329 overfitting on the specific demonstration trajectories since many trajectories may map to the same 330 state. Consequently, many behaviors can be counted as high-performing. Considering the above, the 331 measure-conditioning will help us to achieve high quality and diversity. 332

We then formulate the total reward function computed by MConbo-GAIL as follows:

$$r(s_t^i, a_t^i, m_i) = -\log\left(1 - D_{\psi}(s_t^i, a_t^i, \delta(s_t^i))\right) + r_{diversity}(s_t^i, a_t^i, m_i).$$

$$\tag{4}$$

4.2.2 MCONBO-VAIL

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To extend our framework to other IRL algorithms, we begin with another generic IL method -Variational Adversarial Imitation Learning (VAIL). To facilitate behavior exploration and knowledge generalization, we slightly modify the VAIL's objective for training discriminator as follows:

$$\min_{D_{\psi},E'} \max_{\beta \ge 0} \mathbb{E}_{(s,a) \sim \mathscr{D}} \left[\mathbb{E}_{z \sim E'(z|s,a,\delta(s))} \left[\log(-D_{\psi}(z)) \right] \right] + \mathbb{E}_{(s,a) \sim \pi} \left[\mathbb{E}_{z \sim E'(z|s,a,\delta(s))} \left[-\log(1 - D_{\psi}(z)) \right] \right] \\
+ \beta \mathbb{E}_{s \sim \tilde{\pi}} \left[d_{KL}(E'(z|s,a,\delta(s))||p(z)) - I_c \right],$$
(5)

where $\delta(s)$ is the measure proxy function of state s, $\tilde{\pi}$ means the mixture of expert policy and agent policy, and E' means latent variable encoder. By simply adding $\delta(s)$ as a new input to the VDB encoder of VAIL, we integrate measure information into the latent variable z. This helps improve the generalization ability to diverse behaviors. The reward function for MConbo-VAIL is given by:

$$r(s_t^i, a_t^i, m_i) = -\log\left(1 - D_{\psi}(\boldsymbol{\mu}_{E'}(s_t^i, a_t^i, \boldsymbol{\delta}(s_t^i)))\right) + r_{diversity}(s_t^i, a_t^i, m_i),\tag{6}$$

where $\boldsymbol{\mu}_{E'}(s_t^i, a_t^i, \boldsymbol{\delta}(s_t^i))$ represents the mean of encoded latent variable distribution.

5 EXPERIMENTS

5.1 EXPERIMENT SETUP

357 We evaluate our framework on three popular Mujoco (Todorov et al., 2012) environments: Halfchee-358 tah, Humanoid, and Walker2d. The goal in each task is to maximize forward progress and robot 359 stability while minimizing energy consumption. Our experiments are based on the PPGA implemen-360 tation using the Brax simulator (Freeman et al., 2021), enhanced with QDax wrappers for measure 361 calculation (Lim et al., 2022). We leverage pyribs (Tjanaka et al., 2023) and CleanRL's PPO (Huang et al., 2020) for implementing the PPGA algorithm. The observation space sizes for these environ-362 ments are 17, 18, and 227, with corresponding action space sizes of 6, 6, and 17. The measure 363 function is a vector where each dimension indicates the proportion of time a leg touches the ground. 364 All Experiments are conducted on a system with four A40 48G GPUs, an AMD EPYC 7543P 32-core CPU, and a Linux OS, and each experiment takes roughly two days. 366

367 368 5.2 DEMONSTRATIONS

We use a policy archive obtained by PPGA to generate expert demonstrations. To follow a real-world scenario with limited demonstrations, we first sample the top 500 high-performance elites from the archive as a candidate pool. Then from this pool, we select a few demonstrations such that they are as diverse as possible. This process results in 4 diverse demonstrations (episodes) per environment. Appendix B provides the statistical properties, and Figure 4 visualizes the selected demonstrations.

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 - 5.3 OVERALL PERFORMANCE
- To validate the effectiveness of our approach as a generic QD-IL framework, we use the recent state-of-the-art PPGA technique with true reward function as the QD-RL baseline. The PPGA

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Figure 4: Visualization of the behavior space. Green indicates the full expert behavior space, blue indicates the selected top-500 elites, and red indicates the demonstrators. The x axis is the proportion of time Leg 1 touches the ground and the y axis is the proportion of time Leg 2 touches the ground.

algorithm is then used as the base-learner for our QD-IL imitation learners, by replacing the true 390 reward function with the reward function designed from imitation learning. In addition to using our 391 own MConbo algorithm, we also include the following widely-used and state-of-the-art IL methods 392 as baselines: 1) Traditional IRL: Max-Entropy, 2) Online reward methods: GAIL, VAIL, and AIRL, 393 and 3) Data-driven methods: GIRIL and PWIL. Each baseline learns a reward function, which is 394 then used to train standard PPGA under identical settings for all baselines. Hyperparameter details 395 are provided in Appendix D. All the experiments are averaged with three random seeds, with the 396 exception of PPGA, where we simply report the results for the one seed which was used to generate 397 the demonstrations. 398

We evaluate using four common QD-RL metrics: 1) **QD-Score**, the sum of scores of all nonempty cells in the archive. QD-score is the most important metric in QD-IL as it aligns with the objective of QD-IL as in equation (1); 2) **Coverage**, the percentage of nonempty cells, indicating the algorithm's ability to discover diverse behaviors; 3) **Best Reward**, the highest score found by the algorithm; and 4) **Average Reward**, the mean score of all nonempty cells, reflecting the ability to discover both diverse and high-performing policies. We use the true reward functions to calculate these metrics.



Figure 5: Four QD-metrics for MConbo-GAIL compared to GAIL, PPGA with true reward and other
 baselines. The line represents the mean while the shaded area represents the standard deviation across three random seeds.

Figure 5 compares the training curves across four metrics for MConbo-GAIL, generic GAIL, the expert (PPGA with true reward function), and other baselines. MConbo-GAIL significantly outperforms the expert in the most challenging Humanoid environment (Batra et al., 2023) and slightly exceeds the expert in the Walker2d environment in terms of QD-Score. In Halfcheetah, MConbo-GAIL improves

the QD performance of generic GAIL and significantly outperforms most baselines across all four
metrics. Notably, MConbo-GAIL achieves nearly 100% coverage across all environments, especially
notable in Humanoid where the PPGA expert explored less than 50% of the cells. This success is
attributed to the synergy between the measure bonus and CMA-MEGA (please refer to Appendix G
for detailed explanation), which consistently directs the search policy towards unexplored areas in
the behavior space.



Figure 6: Visualization of well-trained policy archive by True Reward, GAIL and MConbo-GAIL on
Humanoid and Halfcheetah, where the color of each cell represents the cumulative reward of best
performing policy in this cell.

However, due to the inaccessibility of the true reward function and the limited number of demonstrations, it is challenging to match expert performance in terms of Best Reward and Average Reward. Specifically, these metrics are evaluated using the true reward function, but IL-based reward functions are inherently biased. Despite the biased reward function, MConbo-GAIL achieves near-expert performance in Average Reward for Walker2d and Humanoid. Meanwhile, MConbo-GAIL signif-icantly outperforming GAIL and other baselines in Humanoid and Walker2d for Average Reward. Additionally, it's important to note that GAIL's Average Reward in the Humanoid environment is extremely poor, in stark contrast to MConbo-GAIL's high performance. This can be attributed to the design of Measure-Conditional GAIL, which enables the agent to transfer higher-level knowledge from expert demonstrations to the broader behavior space.

Figure 6 visualizes the policy archives for PPGA expert, GAIL, and MConbo-GAIL in Humanoid
 and Halfcheetah. The archive produced by MConbo-GAIL shows smoother performance (with
 lower variance across cells) and covers a larger area, highlighting the importance of measure-space
 exploration and MConbo-GAIL's effectiveness in generalizing high-level knowledge from limited
 demonstrations to unseen behavior patterns.

Additionally, to demonstrate the potential of our method to enhance any IRL approach in the QD-IL context, we apply MConbo to the generic VAIL framework. We separately compare MConbo-VAIL with standard VAIL and other baselines, as shown in Figure 8 of Appendix A. Similar conclusions can be drawn: MConbo-VAIL significantly improves VAIL in the QD context and even outperforms the expert in the Walker2d and Humanoid environments.

Table 1: Four QD-metrics of different algorithms across three environments, where cov, Best, Avg refers to Coverage, Best Reward and Average Reward respectively.

	Halfcheetah			Walker2d			Humanoid					
	QD-Score	Cov(%)	Best	Avg	QD-Score	Cov(%)	Best	Avg	QD-Score	Cov(%)	Best	Avg
True Reward	6.75×10^{6}	94.08	8,942	2,871	3.64×10^6	77.04	5,588	1,891	5.71×10^{6}	49.96	9,691	4,570
MConbo-GAIL	$3.24 imes10^6$	98.32	3,291	1,313	4.12×10^6	91.69	5,491	1,796	$8.47 imes10^6$	93.47	7,228	3,618
GAIL	2.02×10^{6}	67.83	5,115	1,167	$2.48 imes 10^6$	69.29	4,031	1,429	$1.86 imes 10^6$	82.36	6,278	924
MConbo-VAIL	$4.41 imes10^6$	92.63	5,018	1,940	$3.68 imes10^6$	90.60	4,051	1,626	$8.91 imes10^6$	91.52	6,505	3,899
VAIL	4.00×10^{6}	92.77	5,167	1,724	2.40×10^{6}	71.40	3,570	1,343	$5.10 imes 10^6$	65.61	7,056	3,095
GIRIL	2.17×10^{6}	95.96	3,466	909	0.52×10^6	25.08	1,139	821	4.33×10^{6}	67.40	6,992	2,590
PWIL	3.75×10^{6}	99.68	3,814	1,506	$2.27 imes 10^{6}$	64.45	2,835	1,410	1.13×10^{6}	91.73	841	492
AIRL	3.11×10^{6}	83.57	5,183	1.410	2.53×10^{6}	70.53	4.280	1.437	2.31×10^{6}	71.47	7.661	1.308
Max-Ent	1.12×10^{6}	85.48	2,594	525	1.80×10^{6}	68.83	3,756	1.046	1.82×10^{6}	83.27	4,658	882

Table 1 summarizes the quantitative results of our methods (MConbo-GAIL and MConbo-VAIL) and baselines in the three tasks. MConbo improves boths GAIL and VAIL, thus we believe that our

framework can potentially improve any inverse reinforcement learning algorithm in QD context. We
also conducted some experiments for our framework to improve the QD performance of Imitation
From Observation (IFO), which is a popular IL branch. Table 2 shows a brief summary of the results.
We opened the possibility for quality-diversity imitation-from-observation (QD-IFO). Please refer to
Appendix I for detailed analysis.

Table 2: Comparison of four QD-metrics of MConbo-GAIL without expert action (MConbo-GAIL-Obs) and MConbo-GAIL, across three environments. There are only marginal performance losses when expert action is unavailable.

	Halfcheetah			Walker2d			Humanoid					
	QD-Score	Cov(%)	Best	Avg	QD-Score	Cov(%)	Best	Avg	QD-Score	Cov(%)	Best	Avg
True Reward	6.75×10^6	94.08	8,942	2,871	3.64×10^6	77.04	5,588	1,891	5.71×10^6	49.96	9,691	4,570
MConbo-GAIL-Obs MConbo-GAIL	$\begin{array}{c} 3.14\times10^6\\ \textbf{3.24}\times\textbf{10^6} \end{array}$	100.00 98.32	2,831 3,291	1,255 1,313	$\begin{array}{c} 3.84\times10^6\\ \textbf{4.12}\times\textbf{10^6} \end{array}$	91.02 91.69	4,940 5,491	1,689 1,796	$\begin{array}{c} \textbf{9.28}\times\textbf{10^6}\\ 8.47\times10^6\end{array}$	94.02 93.47	7,759 7,228	3,936 3,618

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5.4 ABLATION STUDY

In this section, we examine the effect of the measure bonus by comparing the performance of MConbo-GAIL with Measure-Conditional-GAIL (without the measure bonus) on Walker2d. The 504 results in Figure 7 show a significant performance drop across all metrics without the measure bonus. 505 This highlights the synergy between the measure bonus and CMA-MEGA. Without the exploration 506 bonus, the algorithm struggles with highly localized rewards and the inherent local optima of policy 507 gradient approach. As a result, the search policy fails to explore new behavior patterns, leading to 508 lower coverage. Furthermore, since the reward function learned by IL is biased and especially with 509 limited demonstrations, PPGA's search policy may miss opportunities to explore rewarding behavior 510 patterns. This results in lower average and best rewards. The measure bonus directly encourages the exploration of new behaviors, addressing this issue. To view a full ablation study, including the effect 511 of both the measure bonus and measure conditioning, please refer to Appendix E. 512



Figure 7: MCond-GAIL means we don't include $r_{diversity}$ into the reward function. The line represents the mean while the shaded area represents the standard deviation across three random seeds.

6 CONCLUSION AND FUTURE WORK

In this work, we proposed MConbo-IRL which can potentially improve any IRL method in QD task.
 Additionally, our framework opened the possibility of QD-IFO, providing the first generic QD-IL
 framework for future research. Our framework follows the paradigm of IRL to learn a QD-enhanced
 reward function, and use a QD-RL algorithm to optimize policy archive. By encouraging behavior level exploration and facilitating knowledge generalization from limited expert demonstrations, our
 framework addresses the key challenges of QD-IL. Extensive experiments show that our framework
 achieves near-expert or beyond-expert performance, and significantly outperforms baselines.

To establish our framework as a generic QD-IL solution, we focused on improving the two widely
used IRL algorithms in this paper to make our framework as simple and effective as possible. However,
we believe that our framework has the potential to be compatible with more IRL algorithm backbones.
Additionally, exploring the development of new architectures for QD-IL and exciting applications
such as behavior adaptation, for instance with context-conditioned policies (Seyed Ghasemipour
et al., 2019), remain important avenues for future research. We also discuss the potential limitations
of our work in Appendix K.

540 7 REPRODUCIBILITY 541

542 We have provided detailed pseudo-code in Appendix A, and a few lists of relevant hyperparameters in 543 Appendix D. In Section 5, we have provided a detailed experiment setup, and a process for generating 544 demonstrations. In supplementary material, we have provided the vedio illustrations of trained diverse behaviors and policy archives.

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A ALGORITHM PSEUDO CODE AND MORE EXPERIMENT RESULTS

Algorithm 1 presents the pseudocode for using MConbo-GAIL as our reward module and PPGA as the QD-RL algorithm. The parts highlighted in red indicate the key distinctions from PPGA. We utilize a reward model to compute the fitness value (reward) for the QD-RL problem, with Algorithm 3 explaining how our reward model functions.

708 709 Algorithm 1 PPGA with MConbo-IRL 710 1: Input: Initial policy θ_0 , VPPO instance to approximate ∇f , ∇m and move the search policy, 711 number of QD iterations N_Q , number of VPPO iterations to estimate the objective-measure 712 functions and gradients N_1 , number of VPPO iterations to move the search policy N_2 , branching 713 population size λ , and an initial step size for xNES σ_e . Initial reward model \mathscr{R} , Expert data \mathscr{D} . 714 2: Initialize the search policy $\theta_{\mu} = \theta_0$. Initialize NES parameters $\mu, \Sigma = \sigma_g I$ 715 3: for iter $\leftarrow 1$ to N do 716 $f, \nabla f, \mathbf{m}, \nabla \mathbf{m} \leftarrow \text{VPPO.compute jacobian}(\theta_{\mu}, \mathscr{R}, \mathbf{m}(\cdot), N_1)$ \triangleright approx grad using \mathscr{R} 4: 5: $\nabla f \leftarrow \text{normalize}(\nabla f), \quad \nabla \mathbf{m} \leftarrow \text{normalize}(\nabla \mathbf{m})$ 717 \leftarrow update_archive($\theta_{\mu}, f, \mathbf{m}$) 6: 718 7: for $i \leftarrow 1$ to λ do // branching solutions 719 $c \sim \mathcal{N}(\mu, \Sigma)$ // sample gradient coefficients 8: 720 $\nabla_i \leftarrow c_0 \nabla f + \sum_{j=1}^k c_j \nabla m_j$ 9: 721 $\begin{aligned} \boldsymbol{\theta}_i' \leftarrow \boldsymbol{\theta}_\mu + \nabla_i \\ f', *, \mathbf{m}', * \leftarrow \text{rollout}(\boldsymbol{\theta}_i', \mathscr{R}) \end{aligned}$ 10: 722 11: 723 $\Delta_i \leftarrow \text{update_archive}(\dot{\theta}'_i, f', \mathbf{m}')$ 12: \triangleright get archive improvement of each solution. 724 end for 13: 725 Rank gradient coefficients ∇_i by archive improvement Δ_i 14: 726 Adapt xNES parameters $\mu = \mu', \Sigma = \Sigma'$ based on improvement ranking Δ_i 15: 727 $f'(\boldsymbol{\theta}_{\mu}) \leftarrow c_{\mu,0}f + \sum_{j=1}^{k} c_{\mu,j}m_j$, where $c_{\mu} = \mu'$ 16: 728 $\theta'_{\mu} \leftarrow \text{VPPO.train}(\theta_{\mu}, f', \mathbf{m}', N_2, \mathscr{R})$ 17: \triangleright walk search policy using reward model \mathscr{R} 729 $\dot{\mathscr{R}}.update(\mathscr{D}, \theta'_{\mu})$ 18: ⊳ update reward model 730 19: if there is no change in the archive then 731 20: Restart xNES with $\mu = 0, \Sigma = \sigma_{e}I$ 732 21: Set θ_{μ} to a randomly selected existing cell θ_i from the archive 733 22: end if 734 23: end for 735 736

Algorithm 2 Update Archive

Input: Solution θ to insert, episodic reward f, measures $\mathbf{m} = \langle m_1, ..., m_k \rangle$, archive learning rate α $\theta_{inc}, f_{inc} \leftarrow \mathscr{A}[\mathbf{m}]$ if $\mathscr{A}[\mathbf{m}]$ is nonempty else *None*, 0 $\Delta_i = 0$ **if** $f > f_{inc}$ **then** insert θ into cell $\mathscr{A}[\mathbf{m}]$ $f_{inc} \leftarrow (1 - \alpha) f_{inc} + \alpha f$ $\Delta_i = f - f_{inc}$ **end if return** Δ_i

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756 Algorithm 3 Reward Model \mathscr{R} (using GAIL as the backbone) 757 1: Initialize: Discriminator D_{ϕ} 758 2: 759 3: Method: Reward Calculation for VPPO.compute_jacobian() 760 4: def get_episode_reward(self, episode, current archive \mathscr{A}): 761 5: $s_1, a_1, \delta(s_1), s_2, a_2, \delta(s_2) \dots, s_k, a_k, \delta(s_k) \leftarrow episode$ 762 $r_1, r_2, r_3, \ldots, r_k \leftarrow D_{\psi}([\mathbf{s}, \mathbf{a}, \delta(\mathbf{s})])$ ▷ GAIL batch reward 6: 763 7: $m \leftarrow episode.get_measure()$ 764 8: $r_{diversity} \leftarrow p + q\mathbf{I}(m \in \mathscr{A})$ ▷ calculate measure bonus 9: For $i = 1 \rightarrow k$ 765 10: ▷ calculate total reward $r_i \leftarrow r_i + r_{diversity}$ 766 11: **return** $r_1, r_2, r_3, ..., r_k$ 767 12: 768 13: Method: Update reward model 769 def update(self, $\mathscr{D}, \pi_{\theta}$): 14: 770 Sample a batch of trajectories $(\mathbf{s}^{\pi}, \mathbf{a}^{\pi}, \delta(\mathbf{s}^{\pi})$ from π_{θ} 15: 771 Update discriminator D_{ψ} by minimizing: 16: 772 $\mathscr{L}_{D}(\psi) = \mathbb{E}_{(\mathbf{s},\mathbf{a})\sim\mathscr{D}}[-\log D_{\psi}(\mathbf{s},\mathbf{a},\delta(\mathbf{s}))] + \mathbb{E}_{(\mathbf{s},\mathbf{a})\sim\pi_{\theta}}[-\log(1-D_{\psi}(\mathbf{s},\mathbf{a},\delta(\mathbf{s})))]$ 773 774 Repeat until the model converges or the number of epochs is reached 17: 775 18: return Updated D_{ψ} 776 777 778 QD-Score Coverage(%) BestReward AverageReward 779 2500 780 2000 6000 781 1500 1000 4000 782 500 2000 783 784 1000 1250 1500 1750 2 750 1000 1250 1500 1750 Iterations 750 1000 1250 1500 1750 200 Iterations 750 1000 1250 1500 1750 500 250 500 785 786 1750 1500 787 1000 788 750 789 500 250 790 50 1000 1250 1500 Iterations 1000 1250 1500 750 1000 1250 1500 Iterations 500 750 1000 1250 1500 1750 Iterations 791 792 4000 793 794 795 2000 796 750 1000 1250 1500 1750 2000 250 500 250 500 750 1000 1250 1500 1750 2000 Iterations 250 500 750 1000 1250 1500 1750 2000 Iterations 250 500 750 1000 1250 1500 1750 2000 Iterations 797 798 MConbo-VAIL ---- GIRIL AIRL ---- True Reward VAIL PWIL Max-Ent 799

Figure 8: Four QD-metrics for MConbo-VAIL compared to VAIL, PPGA with true reward and other baselines. The line represents the mean while the shaded area represents the standard deviation across three random seeds.

B DEMONSTRATION DETAILS

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Figure 9 shows the Mujoco environments used in our experiments. Table 3 shows the detailed information of the demonstrations in our experiment.



Figure 9: Mujoco Environments.

Table 3: Demonstrations are generated from top-500 high-performance elites.

Tasks	Demo number	Attributes	min	max	mean	std
Halfcheetah	4	Length Demonstration Return	1000 3766.0	1000 8405.4	1000.0 5721.3	0.0 1927.6
Walker2d	4	Length Demonstration Return	356.0 1147.9	1000.0 3721.8	625.8 2372.3	254.4 1123.7
Humanoid	4	Length Demonstration Return	1000.0 7806.2	1000.0 9722.6	1000.0 8829.5	0.0 698.1

C BASELINE IMITATION LEARNING METHODS

This section summarizes the details for the related IRL methods used as baselines in this paper:

• GAIL (Ho & Ermon, 2016). In GAIL, the objective of the discriminator D_{ψ} is to differentiate between the state-action distribution of expert demonstration \mathscr{D} and the state-action distribution induced by the agent's policy π :

$$\max_{\pi} \min_{D_{\Psi}} \mathbb{E}_{(s,a) \sim \mathscr{D}}[-\log D_{\Psi}(s,a)] + \mathbb{E}_{(s,a) \sim \pi}[-\log(1 - D_{\Psi}(s,a))].$$
(7)

The discriminator is trained to maximize the likelihood assigned to states and actions from the target policy while minimizing the likelihood assigned to states and actions from the agent's policy. The discriminator also serves as the agent's reward function, encouraging the policy to visit states that, to the discriminator, appear indistinguishable from the demonstrations. The reward for π is then specified by the discriminator $r_t = -\log(1 - D_{\Psi}(s, a))$.

VAIL (Peng et al., 2018a) improves GAIL by compressing the information via a variational information bottleneck (VDB). VDB constrains information flow in the discriminator by means of an information bottleneck. By enforcing a constraint on the mutual information between the observations and the discriminator's internal representation, VAIL significantly outperforms GAIL by optimizing the following objective:

$$\min_{D_{\Psi},E'} \max_{\beta \ge 0} \mathbb{E}_{(s,a) \sim \mathscr{D}} \Big[\mathbb{E}_{z \sim E'(z|s,a)} \Big[\log(-D_{\Psi}(z)) \Big] \Big] + \mathbb{E}_{(s,a) \sim \pi} \Big[\mathbb{E}_{z \sim E'(z|s,a)} \Big[-\log(1 - D_{\Psi}(z)) \Big] \Big] + \beta \mathbb{E}_{s \sim \tilde{\pi}} \Big[d_{KL}(E'(z|s,a)||p(z)) - I_c \Big],$$
(8)

where $\tilde{\pi} = \frac{1}{2}\pi^E + \frac{1}{2}\pi$ represents a mixture of the expert policy and the agent's policy, E' is the encoder for VDB, β is the scaling weight, p(z) is the prior distribution of latent variable z, and I_c is the information constraint. The reward for π is then specified by the discriminator $r_t = -\log(1 - D_{\Psi}(\boldsymbol{\mu}_{E'}(s_t, a_t)))$.

- AIRL (Fu et al., 2017) is an inverse reinforcement learning algorithm based on adversarial learning. AIRL leverages binary logistic regression to train the discriminator to classify expert data and the agent's policy data. The reward *r* is updated in terms of $r(s, a, s') \leftarrow \log D_{\psi}(s, a, s') - \log(1 - D_{\psi}(s, a, s'))$.
- GIRIL (Yu et al., 2020). Previous inverse reinforcement learning (IRL) methods usually fail to achieve expert-level performance when learning with limited demonstrations in high-dimensional environments. To address this challenge, Yu et al. (2020) proposed generative intrinsic reward-driven imitation learning (GIRIL) to empower the agent with the demonstrator's intrinsic intention

and better exploration ability. This was achieved by training a novel reward model to generate intrinsic reward signals via a generative model. Specifically, GIRIL leverages a conditional VAE (Sohn et al., 2015) to combine a backward action encoding model and a forward dynamics model into a single generative model. The module is composed of several neural networks, including recognition network $q_{\phi}(z|s_t, s_{t+1})$, a generative network $p_{\phi}(s_{t+1}|z, s_t)$, and prior network $p_{\phi}(z|s_t)$. GIRIL refers to the recognition network (i.e. the probabilistic *encoder*) as a backward action encoding model, and the generative network (i.e. the probabilistic *decoder*) as a forward dynamics model. Maximizing the following objective to optimize the module:

$$J(p_{\varphi}, q_{\phi}) = \mathbb{E}_{q_{\phi}(z|s_{t}, s_{t+1})}[\log p_{\varphi}(s_{t+1}|z, s_{t})] - \mathrm{KL}(q_{\phi}(z|s_{t}, s_{t+1}) \| p_{\varphi}(z|s_{t})) - \alpha d_{KL}(q_{\phi}(\hat{a}_{t}|s_{t}, s_{t+1}) \| \pi_{E}(a_{t}|s_{t})],$$
(9)

where z is the latent variable, $\pi_E(a_t|s_t)$ is the expert policy distribution, $\hat{a}_t = \text{Softmax}(z)$ is the transformed latent variable, α is a positive scaling weight. The reward model will be pre-trained on the demonstration data and used for inferring intrinsic rewards for the policy data. The intrinsic reward is calculated as the reconstruction error between \hat{s}_{t+1} and s_{t+1} :

$$r_t = \|\hat{s}_{t+1} - s_{t+1}\|_2^2, \tag{10}$$

where $\|\cdot\|_2$ denotes the L2 norm, $\hat{s}_{t+1} = decoder(a_t, s_t)$.

PWIL (Dadashi et al., 2021) introduces a reward function based on an upper bound of the Wasserstein distance between the state-action distributions of the agent (π) and the expert demonstrations (i.e. the data from D). The Wasserstein distance is defined as:

$$\inf_{\pi \in \Pi} \mathscr{W}_{p}^{p}(\hat{\rho}_{\pi}, \hat{\rho}_{e}) = \inf_{\pi \in \Pi} \inf_{\omega \in \Omega} \sum_{i=1}^{T} \sum_{j=1}^{N} d((s_{i}^{\pi}, a_{i}^{\pi}), (s_{j}^{e}, a_{j}^{e}))^{p} \omega[i, j],$$
(11)

where π is the policy, and $\omega[i, j]$ represents the coupling between state-action pairs. PWIL then defines an upper bound of the Wasserstein distance using a greedy coupling, which provides a suboptimal but efficient way to compute the coupling:

$$\inf_{\pi \in \Pi} \mathscr{W}_{1}(\hat{\rho}_{\pi}, \hat{\rho}_{e}) = \inf_{\pi \in \Pi} \sum_{i=1}^{T} \sum_{j=1}^{N} d((s_{i}^{\pi}, a_{i}^{\pi}), (s_{j}^{e}, a_{j}^{e})) \omega_{\pi}^{*}[i, j] \\
\leq \inf_{\pi \in \Pi} \sum_{i=1}^{T} \sum_{j=1}^{N} d((s_{i}^{\pi}, a_{i}^{\pi}), (s_{j}^{e}, a_{j}^{e})) \omega_{\pi}^{g}[i, j],$$
(12)

where ω_{π}^{g} represents the greedy coupling.

The greedy coupling ω_{π}^{g} is defined recursively for each timestep *i* as:

$$\omega_{\pi}^{g}[i,:] = \arg\min_{\omega[i,:] \in \Omega_{i}} \sum_{j=1}^{N} d((s_{i}^{\pi}, a_{i}^{\pi}), (s_{j}^{e}, a_{j}^{e}))\omega[i, j],$$
(13)

where Ω_i is a feasible set of couplings constrained by:

$$\Omega_{i} = \left\{ \omega[i,:] \in \mathbb{R}^{N}_{+} \ \Big| \ \sum_{j'=1}^{N} \omega[i,j'] = \frac{1}{T}, \forall k \in [1:N], \sum_{i'=1}^{i-1} \omega_{g}[i',k] + \omega[i,k] \le \frac{1}{N} \right\}.$$
(14)

Finally, a reward is derived from the cost $c_{\pi}^{g} = \sum_{j=1}^{N} d((s_{i}^{\pi}, a_{i}^{\pi}), (s_{j}^{e}, a_{j}^{e}))\omega_{\pi}^{g}[i, j]$ by applying a monotonically decreasing function f:

$$r_{i,\pi} = f(c_{i,\pi}^g),\tag{15}$$

where the reward $r_{i,\pi}$ is history-dependent. PWIL avoids the inner minimization problem typically found in adversarial imitation learning approaches, focusing instead on maximizing the derived reward directly.

D HYPERPARAMETER SETTING

916 D.1 Hyperparameters for PPGA

Table 4 summarizes a list of hyperparameters for PPGA policy updates.

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920	Hyperparameter	Value
921	Actor Network	[128, 128, Action Dim]
922	Critic Network	[256, 256, 1]
923	N_1	10
924	N_2	10
925	PPO Num Minibatches	8
926	PPO Num Epochs	4
927	Observation Normalization	True
928	Reward Normalization	True
929	Rollout Length	128
	Grid Size	50
930	Env Batch Size	3,000
931	Num iterations	2,000
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Table 4: List of relevant hyperparameters for PPGA shared across all environments.

D.2 HYPERPARAMETERS FOR IL

Table 5 summarizes a list of hyperparameters for AIRL, GAIL, measure-conditioned GAIL, and MConbo-GAIL.

Table 5: List of relevant hyperparameters for AIRL, GAILs shared across all environments.

Hyperparameter	Value
Discriminator	[100, 100, 1] 3e-4
Learning Rate	3e-4
Discriminator Num Epochs	1

Table 6 summarizes a list of hyperparameters for VAIL, measure-conditioned VAIL, and MConbo-VAIL.

Table 6: List of relevant hyperparameters for VAILs shared across all environments.

Hyperparameter	Value
Discriminator	[100, 100, (1, 50, 50)]
Learning Rate	3e-4
Information Constraint I _c	0.5
Discriminator Num Epoch	1

Table 7 summarizes a list of hyperparameters for GIRIL.

Table 7: List of relevant hyperparameters for GIRIL shared across all environments.

Hyperparameter	Value
Encoder	[100, 100, Action Dim]
Decoder	[100, 100, Observation Dim]
Learning Rate	3e-4
Batch Size	32
Num Pretrain Epochs	10,000

Table 8 summarizes a list of hyperparameters for MConbo-IRL framework. While our measure bonus function $r_{diversity}(s_i^t, a_t^t, m_i) = p + q \mathbb{I}(m_i \in A_e)$ introduces hyperparameters p and q, these were not extensively tuned in our experiments. We used p = q = 0.5 across all environments, which provided satisfactory performance. However, the optimal values may vary depending on the specific task and environment characteristics.



Table 8: List of relevant hyperparameters for MConbo shared across all environments.

Figure 10: Effect of different p and q values: we observe that p = 0.5 and q = 1 is the best choice of our experiment, suggesting that our result can be further optimized.

D.3 HYPERPARAMETER STUDY FOR p and q

We hereby study the effect of different choice of hyperparameter p and q, as illustrated in Figure 10.

E FULL ABLATION STUDY

To verify the effect of measure conditioning and measure bonus in GAIL, we compare the performance of MCond-GAIL (GAIL with measure conditioning) and MConbo-GAIL (GAIL with measure conditioning and bonus) in all three environments, as illustrated in Figure 7.



Figure 11: The effect of measure conditioning and measure bonus in GAIL. The line represents the mean while the shaded area represents the standard deviation across three random seeds.

Comparing MCond-GAIL and GAIL, we observe that MCond-GAIL strongly improves on GAIL on all QD metrics in the Halfcheetah environment, while obtaining comparable scores in other environments. Additionally, comparing MConbo-GAIL to MCond-GAIL, we see further improvements, with MConbo-GAIL outperforming MCond-GAIL on coverage and QD-score in all three environments. The table shows that the benefit of MCond-GAIL over GAIL is consistent in the experiments although with varying effect size (2+ pooled std, 1 pooled std, and one very small effect).

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F DETAILS ABOUT PPGA AND RELATED BACKGROUND

To help readers to better understand the background of QD-RL, we begin with Covariance Matrix Adaptation MAP-Elites via a Gradient Arborescence (CMA-MEGA) (Fontaine & Nikolaidis, 2021).

1023 For a general QD-optimization problem, the objective of CMA-MEGA is:

$$g(\boldsymbol{\theta}) = |c_0| f(\boldsymbol{\theta}) + \sum_{j=1}^k c_j m_j(\boldsymbol{\theta}), \qquad (16)$$

Tasks	Model	QD-Score	Coverage	BestReward	AverageReward
Halfcheetah	True Reward	6,752,624	94.08	8,942	2,871
Halfcheetah	GAIL	$2,022,500\pm 839,063$	$67.83{\pm}16.05$	$5,115\pm218$	$1,167{\pm}341$
Halfcheetah	MConbo-GAIL	3,235,423±750,505	$98.32{\pm}1.21$	3,291±430	$1,313\pm291$
Halfcheetah	MCond-GAIL	$3,530,990{\pm}415,587$	85.91±13.95	$5,832\pm531$	$1,704{\pm}406$
Humanoid	True Reward	5,708,191	49.96	9,691	4,570
Humanoid	GAIL	1,864,664±450,333	$82.36 {\pm} 9.16$	$6,278\pm 2,245$	$924{\pm}250$
Humanoid	MConbo-GAIL	$8,470,826\pm 1,235,069$	93.47±1.37	$7,228 \pm 582$	$3,618{\pm}475$
Humanoid	MCond-GAIL	$2,194,446\pm316,492$	69.07 ± 5.54	$7,795 \pm 397$	$1,266{\pm}105$
Walker2d	True Reward	3,641,854	77.04	5,588	1,891
Walker2d	GAIL	$2,483,228\pm 288,096$	$69.29 {\pm} 4.48$	4,031±187	$1,429{\pm}73$
Walker2d	MConbo-GAIL	$4,115,586\pm119,161$	$91.69 {\pm} 0.58$	$5,491{\pm}40$	$1,796\pm56$
Walker2d	MCond-GAIL	2,501,431±192,553	69.23 ± 4.04	$4,302 \pm 348$	$1,444\pm32$

Table 9: The effect of measure conditioning and measure bonus in GAIL in terms of the mean and standard deviation of the metric scores in the final 10 iterations of the runs.

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In this context, $m_i(\theta)$ represents the *j*-th measure of the solution θ , and k is the dimension of the 1043 measure space. The objective function of CMA-MEGA is dynamic because the coefficient for each 1044 measure, c_i , is updated adaptively to encourage diversity in m. For instance, if the algorithm has already found many solutions with high m_1 values, it may favor new solutions with low m_1 values 1045 by making c_1 negative, thus minimizing m_1 . However, the coefficient for the fitness function f will 1046 always be positive, as the algorithm always seeks to maximize fitness. This objective function ensures 1047 that CMA-MEGA simultaneously maximizes fitness f and encourages diversity across the measures 1048 m. We update θ by differentiating objective (16) and use gradient-descend-based optimization 1049 approaches, since DQD assumes f and m are differentiable. 1050

Furthermore, the coefficients c_i are sampled from a distribution, which is maintained using Covariance 1051 Matrix Adaptation Evolution Strategy (CMA-ES) (Hansen, 2016). Specifically, CMA-ES updates the 1052 coefficient distribution by iteratively adapting the mean μ and covariance matrix Σ of the multivariate 1053 Gaussian distribution $N(\mu, \Sigma)$, from which the coefficients c_i are sampled. At each iteration, CMA-1054 MEGA ranks the solutions based on their archive improvement (i.e. How much they improve the 1055 existing solutions of occupied cell). The top-performing solutions are used to update μ , while Σ is 1056 adjusted to capture the direction and magnitude of successful steps in the solution space, thereby 1057 refining the search distribution over time. 1058

In CMA-MAEGA (Fontaine & Nikolaidis, 2023), the concept of **soft archives** is introduced to improve upon CMA-MEGA. Instead of maintaining the best policy in each cell, the archive employs a dynamic threshold, denoted as t_e . This threshold is updated using the following rule whenever a new policy π_{θ_i} surpasses the current threshold of its corresponding cell *e*:

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Here, α is a hyperparameter called the **archive learning rate**, with $0 \le \alpha \le 1$. The value of α controls how much time is spent optimizing within a specific region of the archive before moving to explore a new region. Lower values of α result in slower threshold updates, emphasizing exploration in a particular region, while higher values promote quicker transitions to different areas. The concept of soft archives offers several theoretical and practical advantages, as highlighted in previous studies.

 $t_e \leftarrow (1-\alpha)t_e + \alpha f(\pi_{\theta_i})$

1071 PPGA (Batra et al., 2023) is directly built upon CMA-MAEGA. We summarize the key synergies 1072 between PPGA and CMA-MAEGA as follows:(1) In reinforcement learning (RL), the objective functions f and m in Equation 16 are not directly differentiable. To address this, PPGA employs 1074 **Markovian Measure Proxies (MMP)**, where a single-step proxy $\delta(s_t)$ is treated as the reward 1075 function of an MDP. PPGA utilizes k + 1 parallel PPO instances to approximate the gradients of f and each measure m, where k is the number of measures. Specifically, the gradient for each i-MDP is computed as the difference between the parameters $\theta_{i,new}$ after multi-step PPO optimization and 1077 the previous parameters $\theta_{i,\text{old.}}$ (2) Once the gradients are approximated, the problem is transformed 1078 into a standard DQD problem. PPGA then applies a modified version of CMA-MAEGA to perform 1079 quality diversity optimization. The key modifications include:

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10811. Replacing CMA-ES with xNES for Stability: To improve stability in noisy reinforcement
learning environments, CMA-ES was replaced with Exponential Natural Evolution Strategy
(xNES). While CMA-ES struggled with noisy, high-dimensional tasks due to its cumulative
step-size adaptation mechanism, xNES provided more stable updates to the search distri-
bution, especially in low-dimensional objective-measure spaces, and maintained search
diversity.
 - 2. Walking the Search Policy with VPPO: PPGA "walks" the search policy over multiple steps by optimizing a new multi-objective reward function with VPPO (Vectorized Proximal Policy Optimization). This is done by leveraging the mean gradient coefficient vector from xNES, ensuring stable and controlled movement toward greater archive improvement.
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1091 G SYNERGY OF MEASURE BONUS WITH CMA-MEGA

1093 In our QD-IL framework, we made a key observation that by introducing essential guiding signals 1094 into the fitness function f, we can effectively encourage exploration at the behavior level.

Firstly, note that in a traditional QD-RL setting, the elite of one cell is a policy θ . However, the performance of this elite is computed by the random episodes produced by the policy θ . Thus, the same policy may produce different episodes which occupy different cells. Hence, the motivation of our method is to improve the probability that the new policy produce episodes occupying the empty area of archive, which is the conclusion of Lemma 1. We first give the proof of Lemma 1:

Proof. Proof of (1): The objective of policy optimization is:

$$h(\theta, \mathscr{A}_{e}) = \mathbb{E}_{\tau_{i} \sim \pi_{\theta}} \left[\sum_{t=0}^{T} \gamma^{t} r(s_{t}^{i}, a_{t}^{i}) \right] = \mathbb{E}_{\tau_{i} \sim \pi_{\theta}} \left[\mathbb{I}(m_{i} \in \mathscr{A}_{e}) \cdot \sum_{t=0}^{T} \gamma^{t} \right] = \frac{1 - \gamma^{T+1}}{1 - \gamma} \mathbb{E}_{\tau_{i} \sim \pi_{\theta}} \left[\mathbb{I}(m_{i} \in \mathscr{A}_{e}) \right]$$
(17)

¹¹⁰⁶ where *T* is the episode length (rollout length).

1107 1108 1109 Optimizing $h(\theta_{\text{old}}, \mathscr{A}_e)$ through multiple rounds of PPO will result in θ_{new} such that $h(\theta_{\text{new}}, \mathscr{A}_e) > h(\theta_{\text{old}}, \mathscr{A}_e)$, since PPO is assumed to steadily improve the policy, thus increasing the objective.

1110 Therefore, we have:

$$\mathbb{E}_{\tau_i \sim \pi_{\theta_{\text{new}}}}\left[\mathbb{I}(m_i \in \mathscr{A}_e)\right] \ge \mathbb{E}_{\tau_i \sim \pi_{\theta_{\text{old}}}}\left[\mathbb{I}(m_i \in \mathscr{A}_e)\right]$$
(18)

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Proof of (2): Based on Bayes' rule, we have:

$$P(\pi_{\theta}|m \in \mathscr{A}_{e}) = \frac{P(m \in \mathscr{A}_{e}|\pi_{\theta})P(\pi_{\theta})}{P(m \in \mathscr{A}_{e})} \propto P(m \in \mathscr{A}_{e}|\pi_{\theta})$$

Since $\mathbb{E}_{\tau_i \sim \pi_{\theta}}[\mathbb{I}(m_i \in \mathscr{A}_e)] = P(m \in \mathscr{A}_e | \pi_{\theta})$ where m_i is the measure of episode τ_i , it follows that:

 $P(m \in \mathscr{A}_{e} | \pi_{\theta_{\text{new}}}) \geq P(m \in \mathscr{A}_{e} | \pi_{\theta_{\text{old}}})$

Since $P(\pi_{\theta})$ and $P(m \in \mathscr{A}_{e})$ can be treated as constants when θ changes (assuming θ has uniform prior), we have: $P(\pi_{\theta}) = P(\pi_{\theta}) = P($

$$P(\pi_{\theta_{\text{new}}}|m \in \mathscr{A}_e) \ge P(\pi_{\theta_{\text{old}}}|m \in \mathscr{A}_e)$$

1123 Thus, the lemma is proved.

It is worthy noting that, 1) while Lemma 1 offers valuable intuition for our approach, our method's practical effectiveness is not solely dependent on the theoretical guarantee of monotonic improvement in PPO. 2) the solution will only be added to the archive during the "update_archive" step in Algorithm
However, the scope of Lemma 1 is limited to "VPPO.compute_jacobian" and "VPPO.train". This implies that the episodes generated during the training phase and the gradient-approximating stage will not be inserted into the archive.

1130 1131 If we apply a measure bonus to the original GAIL reward, the objective of CMA-MEGA transforms 1132 into:

$$g(\boldsymbol{\theta}) = |c_0|[f(\boldsymbol{\theta}) + h(\boldsymbol{\theta}, \mathscr{A})] + \sum_{j=1}^k c_j m_j(\boldsymbol{\theta}),$$
(19)

where $h(\theta, \mathscr{A})$ represents the cumulative bonus reward based on the current policy archive \mathscr{A} . The gradient of θ becomes:

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$$\nabla_{\theta}g(\theta) = |c_0|\nabla f(\theta) + |c_0|\nabla_{\theta}h(\theta, \mathscr{A}) + \sum_{i=1}^k c_j \nabla_{\theta}m_j(\theta)$$

Notably, the fitness function $f(\theta)$ is calculated using the GAIL reward in the QD-IL setting. Lemma 1 shows that the measure bonus leads to a new policy that has a higher probability of producing episodes with measures in the empty regions of the archive. As a result, a higher c_0 value will guide the search policy towards unoccupied areas in the archive, leading to significant archive improvements (since occupying a new cell naturally results in larger archive improvements compared to replacing an existing elite in a cell).

Furthermore, based on the properties of CMA-ES, the value of c_0 tends to increase temporarily, and the term $|c_0|\nabla_{\theta}h(\theta,\mathscr{A})$ will dominate, facilitating the search policy's exploration of new behavior patterns. On the other hand, if one area of the archive becomes sufficiently explored, the measure bonus will decrease to a standard level, restoring the relative importance of the fitness term in the objective.

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1152 H SCALABILITY STUDY

We also explore the scalability of the MConbo framework. The key challenge of QD-IL is learning diverse policies from homogeneous expert demonstrations, so we test MConbo-GAIL's ability to scale with fewer demonstrations, representing more uniform expert behavior. Using the Walker2d environment, we reduce the number of demonstrations to 2 and 1 and compare the performance of MConbo-GAIL and GAIL.

Figure 12 shows the learning curves of MConbo-GAIL, GAIL, and PPGA (true reward), while Figure 1159 13 compares their performance of QD-score and coverage. Notably, the coverage of MConbo-GAIL 1160 remains close to 100% despite the decrease in expert demonstration numbers, highlighting the 1161 robustness of Measure Bonus to consistently find diverse policies. This robustness is attributed to 1162 the synergy between Measure Bonus and CMA-MEGA (Appendix G). On the other hand, fewer 1163 demonstrations reduce the quality of expert data, leading to lower QD scores. This is especially true 1164 for MConbo-GAIL, which will inherently explore some behavior space regions which is distant from 1165 the expert behavior. Hence, learning high-performing policy will be difficult, when the algorithm can't 1166 find relevant behavior patterns in expert demonstrations. However, MConbo-GAIL still outperforms 1167 GAIL. It can learn diverse and relatively high-performing policies even with just one demonstration, 1168 demonstrating its scalability with limited expert data.



Figure 12: Scalability Study: we test the effect that limited number of expert demonstrations have on
the performance of our MConbo-GAIL model, compared with traditional GAIL. We set the number
of demonstrations to 1, 2 and 4. The line represents the mean while the shaded area represents the
standard deviation across three random seeds.

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Moreover, we compare the training curve between our original setting (4 demos) with 10 demonstrations using the same demonstration sampling method, as illustrated in Figure 14. The result shows more diverse demonstrations will bring higher performance. However, to show the capability of our approach to deal with limited demonstrations, we use only 4 demonstrations in our setting.



Figure 13: We compare the performance fluctuation due to decrease of number of demonstrations of MConbo-GAIL and traditional GAIL. The line represents the mean while the shaded area represents the standard deviation across three random seeds.



Figure 14: Comparison of performance between 4 demos and 10 demos. The performance of 10 demos is significantly better than 4 demos, suggesting that the more diverse the demonstration, the better the performance of our algorithm.

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I IMPROVE IMITATION FROM OBSERVATION

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1222 Imitation from Observation (IFO) is a type of imitation learning where agents learn behaviors by 1223 observing state trajectories, without needing access to the actions that generated them. Unlike 1224 traditional methods that require both states and actions, IFO mimics behavior solely from state 1225 sequences, making it ideal for situations like video demonstrations. This approach aligns more naturally with how humans and animals learn, as we often imitate behaviors by observation without 1226 knowing the exact actions involved (e.g., muscle movements) (Zare et al., 2024). IFO is particularly 1227 useful in scenarios where action data is unavailable, using techniques like inverse reinforcement 1228 learning to infer the underlying policy. 1229

We further observe the potential of our MConbo framework to handle IFO problem, as illustrated inFigure 15. In the setting of IFO, we modify the objective of MConbo-GAIL as:

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$$\max_{\pi} \min_{D_{\psi}} \mathbb{E}_{s \sim \mathscr{D}}[-\log D_{\psi}(s, \delta(s))] + \mathbb{E}_{s \sim \pi}[-\log(1 - D_{\psi}(s, \delta(s)))].$$
(20)

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When expert actions are not accessible, we found that MConbo-GAIL can still effectively learn diverse policies without performance degradation. We attribute this to measure conditioning, which allows the algorithm to more easily infer actions from high-level state abstractions. We believe our QD-IL framework opens the door to the possibility of QD-IFO, and we look forward to future research providing more detailed studies in this area.

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Figure 15: Comparison of MConbo-GAIL without expert action (MConbo-GAIL-Obs), with MConbo-GAIL and PPGA expert with true reward. The line represents the mean while the shaded area represents the standard deviation across three random seeds.



Figure 16: Apply measure bonus to PPGA with true reward: measure bonus significantly improves the PPGA with true reward. Additionally, with measure bonus, the PPGA with true reward outperforms MConbo-GAIL.

J MEASURE BONUS FOR QD-RL

The measure bonus is designed to promote the diversity of our QD-IL algorithm. However, we note 1282 that the measure bonus can similarly applied to QD-RL since its mechanism works regardless of 1283 the reward function it is added to. We also note that MConbo-GAIL often outperforms the expert, 1284 which gives further evidence that the true reward is not the optimal choice for QD-RL. Considering 1285 these points, we hypothesize that applying the measure bonus to PPGA with true reward can improve 1286 PPGA. We test and confirm this hypothesis on Humanoid, in which PPGA with measure bonus 1287 outperforms PPGA and MConbo-GAIL (see Figure 16).

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Κ LIMITATIONS

1291 Since the reward functions learned by GAIL and VAIL are dynamically updated, using traditional 1292 MAP-Elites to maintain the archive may not be ideal. MAP-Elites only preserves the best-performing 1293 policy at a given time, and the policy is evaluated based on the current learned reward function. 1294 Addressing these issues may further enhance the performance of our QD-IL framework. 1295

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