002 003

004

Diversity By Design: Leveraging Distribution Matching for Offline Model-Based Optimization

Anonymous Authors¹

Abstract

The goal of offline model-based optimization (MBO) is to propose new designs that maximize a reward function given only an offline dataset. However, an important desiderata is to also propose a diverse set of final candidates that capture many optimal and near-optimal design configurations. We propose Diversity in Adversarial Model-based Optimization (DynAMO) as a novel method to introduce design diversity as an explicit objective into any MBO problem. Our key insight is to formulate diversity as a distribution matching problem where the distribution of generated designs captures the inherent diversity contained within the offline dataset. Extensive experiments spanning multiple scientific domains show that DynAMO can be used with common optimization methods to significantly improve the diversity of proposed designs while still discovering high-quality candidates.

1. Introduction

Discovering designs that optimize certain desirable properties is a ubiquitous task that spans a wide range of scientific and engineering domains. For example, we might seek to design a drug with the most potent therapeutic efficacy (Brown et al., 2019; Kong et al., 2023; Du et al., 2024); build a robot that is most capable of navigating complex environments (Ahn et al., 2020; Trabucco et al., 2021; Wang et al., 2023); or engineer a material with a certain desirable property (Stanev et al., 2018; Pogue et al., 2023; Gashmard et al., 2024; Ma et al., 2024). However, experimentally validating every proposed design can be expensive, time-intensive, or even impossible in many applications. These limitations can preclude the use of conventional 'online' optimization methods for such generative design tasks.

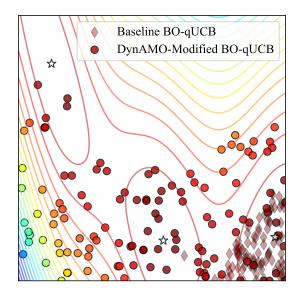


Figure 1. Overview of Diversity in Adversarial Model-based Optimization (DynAMO). Traditional model-based optimization (MBO) (Trabucco et al., 2021) techniques can generate highscoring designs, although often at the expense of the *diversity* of proposed designs. Ideally, the final set of candidates should be of high quality while capturing multiple 'modes of goodness' within the design space. For example, although there are 3 unique global maxima (stars) in the 2D Branin (Branin, 1972) optimization problem, traditional Bayesian optimization (BO-qUCB) proposes designs clustered around only a singla optima (diamonds). In contrast, we show how DynAMO can be used to modify the MBO objective to discover diverse *and* high-quality designs (circles).

An alternative approach is to instead discover design candidates in the *offline* setting, where we assume that no newly proposed designs can be experimentally evaluated during the course of the optimization process. Instead, we only have access to a static dataset of previously observed designs and their corresponding reward values. The objective then is to propose a (small) set of candidate designs to ultimately evaluate experimentally, with the hope that using the information available in the offline dataset will yield desirable designs in the real-world.

Multiple prior works have proposed a variety of offline optimization algorithms (Yu et al., 2021; Trabucco et al., 2021; Fu & Levine, 2021; Chen et al., 2022; Mashkaria et al., 2023;

¹Anonymous Institution, Anonymous City, Anonymous Region, Anonymous Country. Correspondence to: Anonymous Author <anon.email@domain.com>.

Preliminary work. Under review by the International Conference on Machine Learning (ICML). Do not distribute.

Krishnamoorthy et al., 2023; Nguyen et al., 2023; Kim et al., 2023). Using a static, offline dataset of previously evaluated 057 designs and their corresponding oracle scores, an offline 058 algorithm proposes a small set of final candidate designs 059 that are empirically evaluated using the expensive 'oracle' 060 function. Broadly, these algorithms can be divided into 061 two categories: model-based and model-free, where 'model' 062 refers to a predictive surrogate function trained on the of-063 fline dataset to approximate the hidden oracle function. We 064 specifically consider model-based optimization (MBO) 065 algorithms (Trabucco et al., 2021) here that explicitly opti-066 mize against the offline forward surrogate model to discover 067 designs that maximize the final oracle reward.

068 A secondary, often overlooked metric in offline MBO is can-069 didate diversity (Jain et al., 2022; Kim et al., 2023; Maus 070 et al., 2023): it is often ideal to include a diverse array of designs in the final samples proposed by an optimization procedure (Fig. 1). Different designs may achieve promising oracle rewards in different ways, and many real-world 074 optimization tasks seek to capture as many of these 'modes 075 of goodness' as possible (Mullis et al., 2019; Jain et al., 076 2022). Furthermore, there may be secondary optimization 077 objective(s) (e.g., manufacturing cost or drug toxicity) that 078 are better explored and evaluated in a diverse sample set. In 079 these settings, it may be more desirable to sample slightly suboptimal designs in addition to the most optimal design 081 to achieve a greater diversity of proposed candidates. 082

083 To this end, we introduce Diversity in Adversarial Model-084 based Optimization (DynAMO) as a novel approach to ex-085 plicitly control the trade-off between the reward-optimality 086 and diversity of a proposed batch of designs in offline MBO. 087 To motivate our contributions, we show how naïve opti-088 mization algorithms provably suffer from poor candidate 089 diversity. To overcome this limitation, we propose a mod-090 ified optimization objective in the offline setting that en-091 courages discovery of designs that encapsulate the diversity 092 of samples in the offline dataset-an approach inspired by 093 recent advancements in imitation learning and offline rein-094 forcement learning (Ho & Ermon, 2016; Kostrikov et al., 095 2020; Ke et al., 2021; Ma et al., 2022; Rafailov et al., 2023; Deka et al., 2023; Huang et al., 2024b). We then derive 096 097 DynAMO as a provably optimal solution to our modified 098 optimization objective. Finally, we empirically demonstrate 099 how DynAMO can be used with a wide variety of different 100 offline optimization methods to propose promising design candidates comparable to the state-of-the-art, while also achieving significantly better candidate diversity.

2. Background and Preliminaries

104

105

106 **Offline Model-Based Optimization.** In generative design 107 problems, we seek to learn a generative policy π^* over 108 a space of policies Π such that the distribution $q^{\pi^*}(x)$: 109 $\mathcal{X} \to [0,1]$ of designs generated by the policy maximizes an **oracle reward function** $r(x) : \mathcal{X} \to \mathbb{R}$

$$\pi^* = \operatorname*{arg\,max}_{\pi \in \Pi} \mathbb{E}_{x \sim q^{\pi}(x)}[r(x)] \tag{1}$$

over a design space \mathcal{X} . For example, x might be a candidate drug, and the reward r(x) the therapeutic efficacy of the drug. However, in many such problems the oracle reward function may be prohibitively expensive to evaluate; in the aforementioned example, we cannot administer arbitrary doses of potentially dangerous candidate molecules into patients to test their therapeutic efficacy. Similarly, experimentally evaluating designs in materials science discovery often necessitates many months of intensive laboratory work, and building candidate robots from scratch can be intractable. Instead, it is more common to have access to a static dataset of previously evaluated designs $\mathcal{D} = \{(x_i, y_i)\}_{i=1}^n$ where $y_i = r(x_i)$. Such settings where \mathcal{D} is readily available but r(x) is hidden are referred to as offline optimization.

To overcome the limitation that r(x) cannot be queried during the optimization process, one approach is to learn a forward surrogate approximation $r_{\theta}(x)$ of the true reward function r(x). Here, r_{θ} is parameterized by θ^* given by

$$\theta^* = \underset{\theta \in \Theta}{\operatorname{arg\,min}} \ \mathbb{E}_{(x_i, y_i) \sim \mathcal{D}} \left| \left| y_i - r_{\theta}(x_i) \right| \right|_2^2 \qquad (2)$$

In practice, such a surrogate model might be a neural network, a physics simulator, or other domain-specific model. In our work, we do not require any particular surrogate model architecture or training paradigm, and consider neural network implementations of r_{θ} for generalizability across different domains. Rather than solving (1), we can now instead consider the related optimization problem

$$\pi^* = \underset{\pi \in \Pi}{\operatorname{arg\,max}} \ \mathbb{E}_{x \sim q^{\pi}(x)}[r_{\theta}(x)] \tag{3}$$

with the hope that optimizing against $r_{\theta}(x)$ will learn a generative policy that also proposes optimal designs according to r(x), too. Such an approach is often referred to as offline **model-based optimization** (MBO) (Trabucco et al., 2021). Traditionally, an important limitation of offline MBO is the distribution shift between the forward surrogate r_{θ} and the oracle reward r: that is, r_{θ} may incorrectly overestimate the reward associated with proposed designs that are out-ofdistribution compared to D, which can often be exploited by traditional optimization algorithms (Trabucco et al., 2021; Yu et al., 2021; Fu & Levine, 2021; Yao et al., 2024).

Distribution Matching. Distribution matching is a technique leveraged in recent work on imitation learning and offline reinforcement learning (RL) (Kostrikov et al., 2020; Ke et al., 2021). The approach considers an experimental setup where RL agents cannot interact with the environment

and instead must learn from static, offline expert demonstra-111 tions sampled from an unknown state-action-reward distri-112 bution. The Kullback-Leibler (KL)- divergence (Matthews 113 et al., 2016) is commonly used to train an agent to minimize 114 the discrepancy between state-action visitations made by 115 the RL agent and the offline expert. Given a sufficiently 116 large and diverse dataset of expert demonstrations, we can 117 also think of the KL divergence as encouraging the agent to 118 match the diversity of the non-zero support of p(x). Distri-119 bution matching has been used in prior work to learn robotic 120 control policies (Ho & Ermon, 2016; Wang et al., 2020; 121 Kostrikov et al., 2020; Ke et al., 2021; Ma et al., 2022) and 122 align language models (Rafailov et al., 2023; Huang et al., 2024b; Chakraborty et al., 2024); here, we demonstrate 124 how distribution matching can also be leveraged in offline 125 generative design (a non-RL application) by matching the 126 distribution of designs learned by a generative policy with 127 the distribution of designs from the offline dataset.

128 Generative Adversarial Networks. Generative adversarial 129 networks (GANs) are a method popularized by Goodfellow 130 et al. (2014); Arjovsky et al. (2017); and others to train 131 a generative model. Such approaches train a generative 132 policy using adversarial supervision provided by a source 133 *critic* $c(x) : \mathcal{X} \to \mathbb{R}$. The source critic and generator are 134 trained in a zero-sum 'game' as the discriminator learns 135 to distinguish between generated and real designs, and the 136 generator simultaneously learns to generate designs that are 137 similar to real examples according to the source critic. One 138 particular GAN architecture introduced by Arjovsky et al. 139 (2017) is the Wasserstein GAN, which learns a source critic 140

$$c^*(x) = \underset{\substack{||c||_L \le 1}}{\arg \max} \left[\mathbb{E}_{x' \sim p(x)} c(x') - \mathbb{E}_{x \sim q(x)} c(x) \right] \quad (4)$$

where $||c||_L$ is the Lipschitz constant of the source critic, p(x) is a distribution over real designs (i.e., from an offline dataset D), and q(x) is a distribution over generated designs. Yao et al. (2024) previously showed how source critics as in (4) can be leveraged in offline generative design tasks to prevent out-of-distribution evaluation of the forward surrogate model $r_{\theta}(x)$; we leverage a similar approach in our work.

3. Distribution Matching for Generative Offline Optimization

3.1. Motivating Limitation of Naïve MBO

141

142

143

144

145

146

147

148

149

150

151

152

153 154

155

Prior work from Mullis et al. (2019); Jain et al. (2022);
Kim et al. (2023) have shown that an important challenge
in offline optimization as in (3) is that of reward hacking:
learned generative policies can exploit a small region of
the design space, resulting in a low diversity of proposed
designs. For example, consider the following lemma:

Lemma 3.1. (Diversity Collapse in Reward Optimization)
 Suppose that there exists a finite set of globally optimal

designs x_j^* such that $x_j^* := \arg \max_{x \in \mathcal{X}} r(x)$ and $r^* := r(x_j^*)$ is the optimal reward given a finite, non-uniform reward function r(x). Given any distribution q^{π} , we can decompose it into the form $q^{\pi}(x) = \sum_j w_j \delta(x - x_j^*) + \sum_j w_j' \mathbb{1}(x = x_j^*) + \tilde{q}(x)$, where $w_j \ge 0$ for all j, and $\tilde{q}(x) \ge 0$ and $\tilde{q}(x_j^*) = 0$ for all j. Then, $\tilde{q}(x)$ satisfies $\int dx \, \tilde{q}(x) = 0$.

The proof for Lemma 3.1 is included in Appendix A. Note that this result holds for both the oracle function r(x) and the forward surrogate $r_{\theta}(x)$. Intuitively, this lemma states that an optimal policy that maximizes (1) (resp., (3) in the offline setting) can only have measurable nonzero support at the global optimizers in the design space \mathcal{X} . However, many real-world reward functions do not have a large number of globally optimal designs (Trabucco et al., 2021), leading to a low diversity of generated designs seen in practice (Kim et al., 2023). Furthermore, there is no guarantee that the set of optimal x_j^* cover a large region of the design space; in practice, we might be interested in trading optimality of a subset of designs to achieve a greater diversity.

3.2. An Alternative MBO Problem Formulation

To reward generative policies in proposing diverse designs, we modify the original MBO objective in (3) according to

$$J(\pi) := \mathbb{E}_{x \sim q^{\pi}(x)}[r_{\theta}(x)] - \frac{\beta}{\tau} D_{\mathrm{KL}}(q^{\pi} || p_{\mathcal{D}}^{\tau}) \qquad (5)$$

where $D_{\text{KL}}(\cdot||\cdot)$ is the Kullback–Leibler divergence (KLdivergence) and $\tau, \beta \in \mathbb{R}_+$ are hyperparameters. In subsequent steps, we abbreviate the expectation value over probability distributions $\mathbb{E}_{x \sim q^{\pi}(x)}[\cdot]$ as $\mathbb{E}_{q^{\pi}}[\cdot]$ for brevity.

The temperature hyperparameter τ . Equation (5) implicitly introduces a hyperparameter $\tau \in \mathbb{R}_+$ to control the trade-off between diversity and optimality. Note that the KLdivergence in (5) is computed with respect to a distribution $p_{\mathcal{D}}^{\tau}(x)$ defined as the τ -weighted probability distribution:

Definition 3.2 (τ -Weighted Probability Distribution). Suppose that we are given a reward function $r(x) : \mathcal{X} \to \mathbb{R}$ over a space of possible designs \mathcal{X} , and access to an static, offline dataset \mathcal{D} of real designs. We define the τ -weighted probability distribution over \mathcal{X} (for $\tau \ge 0$) as

$$p^{\tau}(x) := \frac{\exp(\tau r(x))}{Z^{\tau}} \tag{6}$$

where the partition function $Z^{\tau} := \int_{\mathcal{X}} dx \exp(\tau r(x))$ is a normalizing constant. We use the dataset of prior observations $\mathcal{D} = \{(x_i, r(x_i))\}_{i=1}^n$ to empirically approximate $p^{\tau}(x)$, and refer to this approximation as $p_{\mathcal{D}}^{\tau}(x) \approx p^{\tau}(x)$. For $\tau \gg 1$, near-optimal designs that are associated with high reward scores are weighted more heavily in $p_{\mathcal{D}}^{\tau}$; conversely, $\tau = 0$ weights all designs equally to achieve the 165 greatest diversity in designs. The penalized objective in (5) 166 thereby encourages the learned policy to capture the diver-167 sity of designs in the τ -weighted distribution $p_{\mathcal{D}}^{\tau}(x)$. We

168 show empirical τ -weighted distributions in **Appendix D.7**. 169

170 **The KL-divergence strength hyperparameter** β . Sepa-171 rately, the hyperparameter $\beta \ge 0$ controls the relative im-172 portance of the distribution matching objective. As $\beta \to \infty$, 173 it becomes increasingly important for the generator to learn 174 a distribution of designs that match $p_{\mathcal{D}}^{\tau}(x)$; setting $\beta = 0$ 175 reduces $J(\pi)$ to the original MBO objective in (3).

3.3. Adversarial Source Critic as a Constraint

176

177

185 186

187

188

195

196

197

198

199

200

201

202

213

214 215

216 217

218

219

Separately, to address the problem of forward surrogate model overestimation of candidate design fitness according to $r_{\theta}(x)$, we constrain the optimization problem to ensure that expected source critic scores over $q^{\pi}(x)$ and $p_{\mathcal{D}}^{\tau}(x)$ differ by no more than a constant $W_0 \in \mathbb{R}_+$, similar to the approach to offline MBO used by Yao et al. (2024). That is,

$$\max_{\pi \in \Pi} \quad J(\pi) = \mathbb{E}_{q^{\pi}}[r_{\theta}(x)] - \frac{\beta}{\tau} D_{\mathrm{KL}}(q^{\pi}||p_{\mathcal{D}}^{\tau})$$

s.t.
$$\mathbb{E}_{p_{\mathcal{D}}^{\tau}}[c^{*}(x)] - \mathbb{E}_{q^{\pi}}[c^{*}(x)] \le W_{0}$$
 (7)

189 where the source critic $c^* : \mathcal{X} \to \mathbb{R}$ is a neural network as in 190 (4) that maximizes $\mathbb{E}_{p_{\mathcal{D}}^{\tau}}[c^*(x)] - \mathbb{E}_{q^{\pi}}[c^*(x)]$ subject to the 191 constraint $||c^*(x)||_L \leq 1$, where $||\cdot||_L$ is the Lipschitz norm. 192 Intuitively, this constraint prevents the evaluation of the 193 forward surrogate model $r_{\theta}(x)$ on wildly out-of-distribution 194 inputs encountered in the offline setting.

We are now interested in finding a generative policy π^* that solves this optimization problem in (7); in our work below, we demonstrate how this approach can yield a policy that generates high-scoring candidate designs that also better capture the diversity of possible designs in \mathcal{X} .

3.4. Constrained Optimization via Lagrangian Duality

203 Our problem in (7) is ostensibly challenging to solve: both 204 the objective $J(\pi)$ and the constraint imposed by the source 205 critic can be arbitrarily non-convex, making traditional con-206 strained optimization techniques intractable in solving the 207 optimization problem out-of-the-box. In this section, we de-208 rive an explicit solution to (7) to make the problem tractably 209 solvable using any standard optimization algorithm.

Recall from Lagrangian duality that solving (7) is equivalent to the min-max problem

$$\min_{\tau \in \Pi} \max_{\lambda \in \mathbb{R}_+} \mathcal{L}(\pi; \lambda) \tag{8}$$

where the Lagrangian $\mathcal{L}(\pi; \lambda) : \Pi \times \mathbb{R}_+ \to \mathbb{R}$ is given by

$$\mathcal{L}(\pi;\lambda) = -J(\pi) + \beta \lambda \left[\mathbb{E}_{p_{\mathcal{D}}^{\tau}}[c^*(x)] - \mathbb{E}_{q^{\pi}}[c^*(x)] - W_0 \right]$$
(9)

introducing $\lambda \in \mathbb{R}_+$ such that $\beta \lambda \in \mathbb{R}_+$ is the Lagrange multiplier associated with the constraint in (7). From weak duality, the *Lagrange dual problem* provides us with a tight lower bound on the primal problem in (7):

$$\max_{\lambda \in \mathbb{R}_+} \min_{\pi \in \Pi} \mathcal{L}(\pi; \lambda) := \max_{\lambda \in \mathbb{R}_+} g(\lambda) \le \min_{\pi \in \Pi} \max_{\lambda \in \mathbb{R}_+} \mathcal{L}(\pi; \lambda)$$
(10)

where $g(\lambda) := \min_{\pi \in \Pi} \mathcal{L}(\pi; \lambda)$ is the *Lagrange dual function*. In general, computing $g(\lambda)$ is challenging for an arbitrary offline optimization problem; in prior work, Trabucco et al. (2021) bypassed this dual problem entirely by treating λ as a hyperparameter tuned by hand (albeit for a different constraint); and Yao et al. (2024) approximated the dual function under certain assumptions about the input space by performing a grid search over possible λ values. In our approach, we look to rewrite the problem into an equivalent representation that admits a closed-form, computationally tractable expression for $g(\lambda)$.

Lemma 3.3 (Entropy-Divergence Formulation). *Define* $J(\pi)$ as in (5). An equivalent representation of $J(\pi)$ is

$$J(\pi) \simeq -\mathcal{H}(q^{\pi}(x)) - (1+\beta)D_{KL}(q^{\pi}(x)||p_{\mathcal{D}}^{\tau}(x)) \quad (11)$$

where $\mathcal{H}(\cdot)$ is the Shannon entropy. Maximizing (11) is equivalent to maximizing (5) in the sense that both objectives admit the same optimal policy.

The proof of this result is in **Appendix A**. To build intuition about how (11) is equivalent to (5), we can consider the behavior of the objective in the limit of $\tau \to +\infty$: the reference distribution $p_{\mathcal{D}}^{\tau}$ approaches the sum-of- δ -distributions formulation in **Lemma 3.1**. In this setting, the entropy and KL-divergence terms are equivalent, and the optimal policy π^* admits a distribution q^{π} with nonzero support only at the globally optimal designs in $p_{\mathcal{D}}^{\tau}$. Alternatively in the limit that $\tau \to 0$ and $\beta \to +\infty$, $p_{\mathcal{D}}^{\tau}$ approaches a uniform distribution and both (5) and (11) simplify to a state-matching objective according to the KL-divergence loss term, without any explicit optimization against the surrogate model $r_{\theta}(x)$.

The utility of **Lemma 3.3** is to enable us to write an exact formulation for the Lagrangian dual function $g(\lambda)$:

Lemma 3.4 (Explicit Dual Function of (7)). *Consider the primal problem*

$$\max_{\pi \in \Pi} \quad J(\pi) \simeq -\mathcal{H}(q^{\pi}) - (1+\beta)D_{KL}(q^{\pi}||p_{\mathcal{D}}^{\tau})$$

s.t.
$$\mathbb{E}_{p_{\mathcal{D}}^{\tau}}[c^*(x)] - \mathbb{E}_{q^{\pi}}[c^*(x)] \le W_0$$
 (12)

The Lagrangian dual function $g(\lambda)$ is bounded from below by the function $g_{\ell}(\lambda)$ given by

$$g_{\ell}(\lambda) := \beta \left[\lambda(\mathbb{E}_{p_{\mathcal{D}}^{\tau}}[c^*(x)] - W_0) - \mathbb{E}_{p_{\mathcal{D}}^{\tau}}e^{\lambda c^*(x) - 1} \right]$$
(13)

The proof of this result is included in **Appendix A**. Lemma 3.4 admits an explicit concave function $g_{\ell}(\lambda)$ such that

220 $g(\lambda) \ge g_{\ell}(\lambda)$ for all $\lambda \in \mathbb{R}_+$; because we are interested 221 in maximizing the dual function in leveraging Lagrangian 222 duality as in (10), it follows that maximizing $g_{\ell}(\lambda)$ bounds 223 the maxima over $g(\lambda)$ from below. In subsequent steps, we 224 therefore optimize over this explicit function $g_{\ell}(\lambda)$.

225 The utility of **Lemma 3.4** is in solving for the optimal 226 λ that maximizes the dual function lower bound in (13). 227 Prior work has explored approximating λ via a grid search 228 (Yao et al., 2024) or using iterative implicit solvers; these 229 methods cannot provide any formal guarantee in arriving 230 at a reasonable solution for λ . In contrast, maximizing 231 against $q_{\ell}(\lambda)$ is easy because the function is guaranteed to 232 be concave for any β , τ , W_0 and source critic $c^*(x)$. We can 233 therefore derive an *exact* solution for λ using any convex 234 optimization problem solver. We now have a method to 235 write an explicit expression for the Lagrangian $\mathcal{L}(\pi; \lambda)$ by 236 exactly specifying the optimal λ , and then leverage any 237 out-of-the-box policy optimization method to solve (7) via 238 solving the easier, ostensibly unconstrained problem in (8). 239

3.5. Overall Algorithm

240

241

263

264

242 To summarize, our work aims to solve two separate but 243 related problems in offline MBO in (3): traditional model-244 based optimization approaches can yield candidate designs 245 that are [1] of low diversity; and [2] not optimal due to 246 exploiting out-of-distribution errors of the forward surro-247 gate $r_{\theta}(x)$. We introduce a KL-divergence-based distribu-248 tion matching objective—with input hyperparameters τ and 249 β —to solve the diversity problem; and build off prior work 250 (Yao et al., 2024) to constrain the search space using source 251 critic feedback to solve the out-of-distribution evaluation 252 problem. We then show that there exists a provable, explicit 253 solution to our modified offline MBO problem (i.e., Lemma 254 **3.4** and (8)). In contrast with prior work imposing specific 255 constraints on the forward model (Trabucco et al., 2021; Yu 256 et al., 2021) or design space (Yao et al., 2024), or requiring 257 the use of model-free optimization methods (Krishnamoor-258 thy et al., 2023; Mashkaria et al., 2023), our approach only 259 modifies the MBO objective and is therefore both optimizer-260 and task- agnostic. We refer to our method as Diversity in 261 Adversarial Model-based Optimization (DynAMO). 262

4. Experimental Evaluation

265 Datasets and Offline Optimization Tasks. We evaluate Dy-266 nAMO on a set of six real-world offline MBO tasks spanning 267 multiple scientific domains and both discrete and continuous 268 search spaces. Five of the tasks are from Design-Bench, a 269 publicly available set of offline optimization benchmarking 270 tasks from Trabucco et al. (2022): (1) TFBind8 aims to max-271 imize the transcription factor binding efficiency of a short 272 DNA sequence (Barrera et al., 2016); (2) UTR the gene 273 expression from a 5' UTR DNA sequence (Sample et al., 274

Algorithm 1 (DynAMO). Diversity in Adversarial Modelbased Optimization

Inputs:

$$\begin{split} r_{\theta} : \mathcal{X} \to \mathbb{R} & -\text{pre-trained forward surrogate model} \\ c^* : \mathcal{X} \to \mathbb{R} & -\text{initialized source critic model} \\ \mathcal{D} &= \{(x'_j, r(x'_j))\}_{j=1}^n - \text{reference dataset} \\ \beta &\geq 0 - \text{KL regularization strength} \\ \tau &\geq 0 - \text{temperature} \\ b &\geq 1 - \text{batch size} \\ a^b : \mathcal{X} \times \mathbb{R} \to \mathcal{X}^b - \text{optimizer algorithm} \\ \eta_{\text{critic}} &> 0 - \text{source critic learning rate} \\ \eta_{\lambda} &> 0 - \lambda \text{ dual step size} \\ k &\geq 1 - \text{oracle evaluation budget} \\ \\ \text{Initialize sampled candidates } \mathcal{D}_{\text{gen}} = \emptyset \subset \mathcal{X} \times \mathbb{R} \\ \text{while } a^b \text{ has not converged } \mathbf{do} \end{split}$$

// Solve for the globally optimal λ using (13)

 $\begin{array}{l} \lambda \leftarrow \lambda_0 \quad (\lambda_0 = 1.0 \text{ in our experiments}) \\ \textbf{while } \lambda \text{ has not converged } \textbf{do} \\ \lambda \leftarrow \lambda + \eta_\lambda \frac{\partial g_\ell(\lambda)}{\partial \lambda} \\ \textbf{end while} \end{array}$

// Given previously sampled candidates \mathcal{D}_{gen} as input, // sample new candidates using the optimizer $\{x_i^{\text{new}}\}_{i=1}^b \leftarrow a^b(\mathcal{D}_{gen})$

// Re-train the source critic parameters θ_c

while δW has not converged do

$$\begin{split} \delta W &\leftarrow \vec{\nabla}_{\theta_c} \left[\mathbb{E}_{x' \sim \mathcal{D}}[c^*(x')] - \mathbb{E}_{x \sim \{x_i^{\mathsf{new}}\}_{i=1}^b}[c^*(x)] \right] \\ \theta_c &\leftarrow \min(\max(\theta_c + \eta_{\mathsf{critic}} \cdot \delta W, -0.01), 0.01) \\ \mathsf{end while} \end{split}$$

// Evaluate and cache the candidates according to (9) $\mathcal{D}_{gen} \leftarrow \mathcal{D}_{gen} \cup \{(x_i^{new}, -\mathcal{L}(x_i^{new}; \lambda))\}_{i=1}^b$ end while return top-k candidates from \mathcal{D}_{gen} according to their penalized MBO objective values

2019; Angermüeller et al., 2020); (3) ChEMBL the mean corpuscular hemoglobin concentration (MCHC) biological response of a molecule using an offline dataset collected from the ChEMBL assay CHEMBL3885882 (Gaulton et al., 2011); (4) **Superconductor** the critical temperature of a superconductor material specified by its chemical formula design (Hamidieh, 2018); and (5) D'Kitty the morphological structure of a quadrupedal robot (Ahn et al., 2020). Tasks (1) - (3) (i.e., TFBind8, UTR, and ChEMBL) are discrete optimization tasks, where tasks (4) and (5) (i.e., Superconductor and D'Kitty) are continuous optimization tasks. We also evaluate our method on the discrete (6) Molecule task described in Brown et al. (2019); Chen et al. (2021); Flam-Shepherd et al. (2022); Yao et al. (2024), where the goal is to design a maximally hydrophobic molecule. Additional implementation details are detailed in Appendix B.

275 **Experiment Implementation.** All our optimization tasks 276 include an offline, static dataset $\mathcal{D} = \{(x_i, r(x_i))\}_{i=1}^n$ of 277 previously observed designs and their corresponding objec-278 tive values. We first use \mathcal{D} to train a task-specific forward 279 surrogate model r_{θ} with parameters θ^* according to (2). We 280 parameterize each forward surrogate model $r_{\theta}(x)$ as a fully 281 connected neural network with two hidden layers of size 282 2048 and LeakyReLU activations, trained using an Adam 283 optimizer with a learning rate of $\eta = 0.0003$ for 100 epochs.

284 Importantly, optimization problems over discrete search 285 spaces are generally NP-hard and often involve heuristic-286 based solutions (Papalexopoulos et al., 2022; Xiong, 2022). 287 Instead, we use the standard approach of learning a vari-288 ational autoencoder (VAE) (Kingma & Welling, 2014) to 289 encode and decode discrete designs to and from a contin-290 uous latent space, and optimize over the continuous VAE 291 latent space instead—see Appendix B for additional details. 292

293 DynAMO also involves training and implementing a source 294 critic model $c^*(x)$ as in (4); we implement c^* as a fully con-295 nected neural network with two hidden layers each with size 296 512. We implement the constraint on the model's Lipschitz 297 norm by clamping the weights of the model such that the 298 ℓ_{∞} -norm of the parameters is no greater than 0.01 after each 299 optimization step, consistent with Arjovsky et al. (2017). 300 We train the critic using gradient descent with a learning 301 rate of $\eta = 0.01$ according to (4). Separately to solve for 302 the globally optimal λ using Lemma 3.4, we perform gra-303 dient ascent on λ until the algorithm converges. Finally, 304 we fix the KL-divergence weighting $\beta = 1.0$, temperature 305 hyperparameter $\tau = 1.0$, and constraint bound $W_0 = 0$ 306 for all experiments to avoid overfitting DynAMO to any 307 particular task or optimizer. All experiments were run for 308 10 random seeds on a single internal cluster with 8 NVIDIA 309 RTX A6000 GPUs. Of note, all DynAMO experiments were run using only a single GPU.

311 Baseline Methods. Our proposed work, DynAMO, specifi-312 cally looks to modify an offline MBO optimization problem 313 as in (3) where we assume access to a forward surrogate 314 model $r_{\theta}(x)$ to rank proposed design candidates and offer 315 potential information about the design space. We com-316 pare DynAMO against other objective modifying MBO 317 approaches: (1) Conservative Objective Models (COMs; 318 Trabucco et al. (2021)) penalizes the objective at a 'look-319 ahead' gradient-ascent iterate to prevent falsely promising 320 gradient ascent steps; (2) Robust Model Adaptation (RoMA; 321 Yu et al. (2021)) modifies the objective $r_{\theta}(x)$ to enforce 322 a local smoothness prior; (3) Retrieval-enhanced Offline 323 Model-Based Optimization (ROMO; Chen et al. (2023c)) 324 retrieves relevant samples from the offline dataset for more 325 trustworthy gradient updates; and (4) Generative Adversarial Model-Based Optimization (GAMBO; Yao et al. (2024)) 327 introduces a framework for initially leveraging source critic 328

329

feedback to regularize an MBO objective. We evaluate each of these MBO objective transformation methods alongside **DynAMO** and naïve, unmodified **Baseline** MBO using representative first-order methods (1) **Grad.** (Gradient Ascent) and (2) **Adam** (Adaptive Moment Estimation (Kingma & Ba, 2015)); evaluationary algorithms (3) **CMA-ES** (Covariance Matrix Adaptation Evolution Strategy (Hansen, 2016)) and (4) **CoSyNE** (Cooperative Synapse Neuroevolution (Gomez et al., 2008)); and Bayesian optimization with (5) Expected Improvement (**BO-qEI**) and (6) Upper Confidence Bound (**BO-qUCB**) acquisition functions.

Notably, the baseline methods COMs and RoMA impose specific constraints on the training process for the forward surrogate model $r_{\theta}(x)$, and/or also assume that the forward model can be updated during the sampling process (Yu et al., 2021; Trabucco et al., 2021). These constraints are not generally satisfied for any arbitrary offline MBO problem; for example, r_{θ} may be a non-differentiable black-box simulator with fixed parameters. In contrast, both our method (DynAMO) and baseline methods GAMBO and ROMO are compatible with this more general experimental setting; to ensure a fair experimental comparison, we evaluate both RoMA and COMs using a baseline forward surrogate (i.e., RoMA⁻, COMs⁻) and using a specialized forward surrogate model trained and updated according to the methods described by the respective authors (i.e., RoMA⁺, COMs⁺).

Evaluating the Diversity of Candidate Designs. To empirically evaluate the diversity of a final set of k = 128 candidate designs $\{x_i^F\}_{i=1}^k$ proposed by an offline MBO experiment, we report the **Pairwise Diversity** (PD) of a batch of k candidate designs, defined by Jain et al. (2022); Kim et al. (2023); and Maus et al. (2023) as

$$\operatorname{PD}(\{x_i^F\}_{i=1}^k) := \mathbb{E}_{x_i^F} \left[\mathbb{E}_{x_j^F \neq x_i^F} \left[d(x_i^F, x_j^F) \right] \right]$$
(14)

where $d(\cdot, \cdot)$ is the normalized Levenshtein edit distance (Haldar & Mukhopadhyay, 2011) (resp., Euclidean distance) for discrete (resp., continuous) tasks. We detail alternative definitions of diversity in **Appendix D.2**.

Evaluating the Quality of Candidate Designs. To ensure that diversity does not come at the expense of finding optimal design candidates, we report the **Best**@k oracle score obtained by evaluating k = 128 candidate designs $\{x_i^F\}_{i=1}^k$ proposed in an experiment. Consistent with prior work (Trabucco et al., 2021; Yao et al., 2024), we define

$$Best@k(\{x_i^F\}_{i=1}^k) := \max_{1 \le i \le k} r(x_i^F)$$
(15)

Crucially, the Best@k metric is computed with respect to the oracle function r(x) that was hidden during optimization; we only use r(x) in (15) to report the true reward associated with each candidate design.

Table 1. Quality and Diversity of Designs Under MBO Objective Transforms. We evaluate DynAMO against other MBO objectivemodifying methods using six different backbone optimizers. Each cell consists of 'Best@128 (Best)/Pairwise Diversity (PD)' Rank and Optimality Gap scores separated by a forward slash. Bolded (resp., Underlined) entries indicate the best (resp., second best) performing algorithm for a given optimizer (i.e., within each column). See Supplementary Table A1 for detailed results broken down by MBO task.

Best/PD	Rank ↓						Optimality Gap \uparrow					
	Grad.	Adam	CMA-ES	CoSyNE	BO-qEI	BO-qUCB	Grad.	Adam	CMA-ES	CoSyNE	BO-qEI	BO-qUCB
Baseline	5.0/5.5	4.5/6.0	3.7/3.8	5.3/4.5	5.8/5.2	3.7/3.0	6.8/-53.2	0.5/-52.4	14.4/9.5	-0.6/-52.1	18.7/47.1	19.4/43.5
COMs ⁻	7.3/6.5	6.0/5.3	5.7/5.2	5.7/5.7	4.3/4.0	4.5/4.5	-3.0/-53.5	-3.0/-52.4	7.6/-9.7	1.1/-51.6	19.2/51.4	19.0/45.5
COMs ⁺	2.5 /2.8	3.2/3.0	7.3/7.8	5.7/3.3	6.0/5.7	5.2/5.7	12.3/-6.9	8.1/-12.3	7.1/-38.2	3.5/-40.4	17.9/40.3	18.6/51.3
RoMA ⁻	6.7/5.7	4.5/6.3	3.7/3.5	5.3/4.5	2.7/3.3	3.8/3.0	-1.2/-53.3	0.5/-52.4	14.4/9.5	-0.6/-52.2	21.0 /48.4	19.2/43.6
RoMA ⁺	3.8/5.8	2.8 /5.2	5.0/4.8	2.8/5.0	5.2/6.3	4.7/6.5	9.2/-46.8	14.5 /-45.8	14.1/8.0	6.2/-52.0	18.3/32.9	18.5/39.9
ROMO	4.2/2.8	4.8/2.8	4.2/4.3	4.2/5.2	5.0/6.0	4.7/6.2	10.9/-12.7	6.4/-20.5	15.7/-3.1	3.1/-50.8	19.2/34.9	19.9/33.2
GAMBO	3.2/5.3	5.3/5.8	2.2 /4.3	3.7/6.3	2.2 /4.0	4.7/5.0	10.5/-52.1	<u>8.6</u> /-51.9	<u>16.7/16.8</u>	5.0/-53.6	<u>20.8</u> /30.0	<u>20.2</u> /30.3
)ynAMO	<u>2.8</u> /1.2	2.8/1.2	<u>3.3</u> /1.8	2.3/1.2	3.0/1.3	3.5/1.8	14.2/27.8	14.5/35.7	17.5/55.2	12.3/-20.7	20.7/ 74.2	20.5/59.4

Finally, we rank each method for a given optimizer and task and report the method's **Rank** averaged over the six tasks according to the Best@128 (15) and PD (14) metrics. We also report the **Optimality Gap** (Opt. Gap) (averaged over the six tasks), defined as as difference between the score achieved by an MBO optimization method and the score in the offline dataset, for both the Best@128 and PD metrics.

5. Results

Main Results. DynAMO consistently proposes the most diverse set of designs and achieves an Optimality Gap as high as 74.2 (DynAMO-BO-qUCB) and an average Rank as low as 1.2 compared to baseline methods (Table 1). We find that DynAMO offers the largest improvements in diversity for first-order methods, although also improves upon the evolutionary algorithms and Bayesian optimization methods evaluated. This makes sense, as both Grad. and Adam are only local optimizers that often end up exploring a much smaller region of the design space (without using DynAMO) compared to gradient-free methods. For example, DynAMO-Grad. (resp., DynAMO-CMA-ES; resp., DynAMO-BO-qEI) achieves a Pairwise Diversity Optimality Gap of 35.7 (resp., 55.2; resp., 74.2); in contrast, no other baseline method achieves a diversity score greater than -6.9 (resp., 16.8; resp., 51.4) within the same optimizer class.

These results do not come at the cost of the quality of designs; for example, for all 3 optimizers where DynAMO scores an average Rank of 1.2 (i.e., Grad., Adam, and CoSyNE backbone optimizers), DynAMO is also within the **top 2 methods** in proposing *high-quality* designs according to both Rank and Optimality Gap. In fact, DynAMO proposes the best designs for 5 out of the 6 backbone optimizers according to the Best@128 Optimality Gap. These results suggest that DynAMO can be used to improve both the quality *and* diversity of designs in a variety of experimental settings for both discrete and continuous search spaces.

Ablation Studies. DynAMO consists of two important

but separate algorithmic components: (1) a KL-divergencebased distribution matching objective; and (2) a constraint dependent on an adversarial source critic. We show both components are important for DynAMO to generate both diverse *and* high-quality designs (**Appendix E.2**). DynAMO also takes as input two important hyperparameters— β and τ —as introduced in (5). We empirically ablate the values of these hyperparameters in **Appendix E.3**. Additional results and discussion are included in **Appendix E**.

6. Related Work

Model-free offline optimization. In our work, we specifically look at model-based optimization methods that explicitly optimize against a forward surrogate model $r_{\theta}(x)$ that acts as a proxy for the hidden oracle function r(x). However, related work have also proposed offline optimization methods that do not require access to a model $r_{\theta}(x)$ and instead impose constraints on the backbone optimization method-we refer to such work as model-free offline optimization. For example, Mashkaria et al. (2023) frame generative design tasks as a 'next-sample' prediction problem and learn a transformer to roll out sample predictions; and Krishnamoorthy et al. (2023); Yun et al. (2024) learn a diffusion model to sample candidate designs conditioned on reward values. We compare DynAMO-enhanced MBO with these model-free optimization methods in Appendix D.5. Because DynAMO operates on MBO forward surrogate models $r_{\theta}(x)$, we cannot leverage DynAMO with these model-free methods. However, we compare them against DynAMO in Appendix D.5.

Active learning in optimization. In our work, we specifically consider the experimental setup of *one-shot*, *batched oracle evaluation*: that is, the final candidate designs that are scored by the oracle function at the end of optimization are *not* used to subsequently update the prior over the design space to better inform subsequent optimization steps. In contrast, a separate body of recent work has investigated generative design in the setting of *active learning* where there can
be multiple rounds of offline optimization to inform subsequent online acquisitions (Hernández-García et al., 2024; Li
et al., 2022b;a; Wu et al., 2023; Palizhati et al., 2022). For
example, Li et al. (2024) show how active learning can be
formulated as a multi-fidelity optimization problem.

Reinforcement learning. Prior work has explored how to formulate offline generative design tasks as reinforcement learning (RL) problems. Trabucco et al. (2022) used REINFORCE-style methods similar to Williams (1992) to learn a myopic sampling policy, although do not use RL for offline generative design. Angermueller et al. (2020); Korshunova et al. (2022); and Jang et al. (2022) leverage RL for offline optimization in the active learning setting described above, which is outside the scope of our work.

7. Discussion and Conclusion

401

402

439

403 We introduce DynAMO, a novel task- and optimizer- agnos-404 tic approach to MBO that improves the diversity of proposed 405 designs in offline optimization tasks. By framing diversity 406 as a distribution-matching problem, we show how DynAMO 407 can enable generative policies to sample both high-quality 408 and diverse sets of designs. Our experiments reveal that 409 DynAMO significantly improves the diversity of proposed 410 designs while also discovering high-quality candidates. 411

412 Limitations and Future Work. There are also important 413 limitations of our method. Firstly, we note that while Dy-414 nAMO can significantly improve the diversity of proposed 415 designs in offline MBO while preserving Best@128 per-416 formance, our method is not as competitive with existing 417 baselines according to the median score obtained by the 128 418 designs (Supp. Fig. A2, Appendix B). The suboptimal 419 performance of DvnAMO according to this Median@128 420 metric is unsurprising given that our primary motivation of 421 DynAMO is to obtain a diverse sample of designs while 422 simultaneously ensuring that a nonzero subset of them are 423 (near-) optimal. Furthermore, we empirically observe that 424 no method is state-of-the-art on both Best@128 and Me-425 dian@128 metrics. While it would be ideal for DynAMO 426 (or any method) to be state-of-the-art for all quality and 427 diversity metrics, we argue that obtaining a good Best@128 428 score is more important than a good Median@128 score, as 429 the the principle real-world goal of offline MBO is to find a 430 design that maximizes the oracle function.

431
432
432
433
434
434
435
435
436
437
438
438
438
439
430
430
430
431
431
432
433
434
435
435
436
437
438
438
438
439
430
430
431
431
431
431
431
432
433
434
435
435
436
437
438
437
438
438
438
439
430
430
431
431
431
431
432
431
432
433
434
435
435
436
437
438
437
438
438
438
437
438
438
438
439
439
430
430
431
431
431
432
431
432
432
433
434
435
435
436
437
438
437
438
438
438
439
439
430
430
431
431
431
432
432
432
432
433
434
434
435
435
436
437
438
437
438
438
438
438
438
438
431
431
432
432
432
434
435
435
435
436
437
438
436
437
438
438
438
438
438
438
438
438
438
438
438
438
438
438
438
438
438
438
438
438
438

such settings for future work.

Finally, our work focuses on evaluating DynAMO and baseline methods in a one-shot, batched oracle evaluation setting—future work might explore how to extend our method to the active learning setting. Separately, recent domainspecific foundation models (Lin et al., 2023; Ohana et al., 2024; Nguyen et al., 2024; Zeni et al., 2025) may also give rise to more sophisticated and accurate forward surrogate models $r_{\theta}(x)$ that can be leveraged with DynAMO and other MBO methods in future work.

Impact Statement. Offline generative methods such as DynAMO have significant potential to help design more effective drugs; engineer new materials with desirable properties; and solve other scientific tasks. However, like any real-world algorithm, these methods can also be misused to create potentially harmful or dangerous designs. Careful oversight by domain experts and researchers is essential to ensure our contributions are used for social good.

Code and Data Availability

All datasets used in our experiments are publicly available; offline datasets associated with Design-Bench tasks are made available by Trabucco et al. (2022). The offline dataset for the **Molecule** task is made available by Brown et al. (2019). Our custom code implementation for our experiments is made publicly available at github.com/michael-s-yao/DynAMO.

Acknowledgments

We thank Shuo Li at the University of Pennsylvania for their helpful comments and feedback on an earlier draft of this work. MSY is supported by NIH Award F30 MD020264. JCG is supported by NIH Award R01 EB031722. OB is supported by NSF Award CCF-1917852.

References

- Agarwal, S., Durugkar, I., Stone, P., and Zhang, A. f-Policy gradients: A general framework for goal conditioned RL using f-divergences. In *Proc NeurIPS*, pp. 12100–23, 2024. doi: 10.5555/3666122.3666652.
- Agrawal, R. and Horel, T. Optimal bounds between fdivergences and integral probability metrics. J Mach Learn Res, 22(128):1–59, 2021. doi: 10.48550/arXiv. 2006.05973.
- Ahn, M., Zhu, H., Hartikainen, K., Ponte, H., Gupta, A., Levine, S., and Kumar, V. Robel: Robotics benchmarks for learning with low-cost robots. In *Proc CoRL*, volume 100 of *Proceedings* of Machine Learning Research, pp. 1300–13. PMLR,

440 2020. URL https://proceedings.mlr.press/441 v100/ahn20a.html.

442

464

- Amos, B. On amortizing convex conjugates for optimal transport. In *Proc ICLR*, 2023. URL https: //openreview.net/forum?id=TQ5WUwS_4ai.
- Angermüeller, C., Belanger, D., Gane, A., Mariet, Z., Dohan, D., Murphy, K., Colwell, L., and Sculley, D.
 Population-based black-box optimization for biological sequence design. In *Proc ICML*, volume 119, pp. 324–34.
 PMLR, 2020. URL https://proceedings.mlr.
 press/v119/angermueller20a.html.
- Angermueller, C., Dohan, D., Belanger, D., Deshpande, R.,
 Murphy, K., and Colwell, L. Model-based reinforcement
 learning for biological sequence design. In *Proc ICLR*,
 2020. URL https://openreview.net/forum?
 id=HklxbgBKvr.
- 459 Arjovsky, M., Chintala, S., and Bottou, L. Wasser460 stein generative adversarial networks. In *Proc*461 *ICML*, volume 70, pp. 214–23. PMLR, 2017. URL
 462 https://proceedings.mlr.press/v70/
 463 arjovsky17a.html.
- Barrera, L. A., Vedenko, A., Kurland, J. V., Rogers, J. M., 465 Gisselbrecht, S. S., Rossin, E. J., Woodard, J., Mariani, L., 466 Kock, K. H., Inukai, S., Siggers, T., Shokri, L., Gordân, 467 R., Sahni, N., Cotsapas, C., Hao, T., Yi, S., Kellis, M., 468 Daly, M. J., Vidal, M., Hill, D. E., and Bulyk, M. L. 469 Survey of variation in human transcription factors reveals 470 prevalent DNA binding changes. Science, 351(6280): 471 1450-54, 2016. doi: 10.1126/science.aad2257. 472
- Benita, Y., Oosting, R. S., Lok, M. C., Wise, M. J., and Humphery-Smith, I. Regionalized GC content of template DNA as a predictor of PCR success. *Nucleic Acids Res*, 31(16):e99, 2003. doi: 10.1093/nar/gng101.
- 478
 479
 479
 479 in Python. *IEEE Access*, 8:89497–509, 2020. doi: 10. 1109/ACCESS.2020.2990567.
- 482 Borwein, J. and Lewis, A. *Convex analysis and non-*483 *linear optimization: Theory and examples.* Springer,
 484 2006. ISBN 978-0-387-29570-1. doi: 10.1007/
 485 978-0-387-31256-9.
- Boyd, S. and Vandenberghe, L. *Convex optimization*.
 Cambridge university press, 2004. doi: 10.1017/
 CBO978051180444.
- Branin, F. H. Widely convergent method for finding multiple solutions of simultaneous nonlinear equations. *IBM Journal of Research and Development*, 16(5):504–22, 1972. doi: 10.1147/rd.165.0504.

- Brown, N., Fiscato, M., Segler, M. H. S., and Vaucher, A. C. Guacamol: Benchmarking models for de novo molecular design. *J Chem Inf Model*, 59(3):1096–108, 2019. doi: 10.1021/acs.jcim.8b00839.
- Bubeck, S. Convex optimization: Algorithms and complexity. *Found Trends Mach Learn*, 8(3–4):231–357, 2015. doi: 10.1561/2200000050.
- Chakraborty, S., Qiu, J., Yuan, H., Koppel, A., Manocha, D., Huang, F., Bedi, A., and Wang, M. MaxMin-RLHF: Alignment with diverse human preferences. In *Proc ICML*, volume 235 of *Proceedings* of Machine Learning Research, pp. 6116–35. PMLR, 2024. URL https://proceedings.mlr.press/ v235/chakraborty24b.html.
- Chemingui, Y., Deshwal, A., Hoang, T. N., and Doppa, J. R. Offline model-based optimization via policy-guided gradient search. In *Proc AAAI*, pp. 11230–9, 2024. doi: 10.1609/aaai.v38i10.29001.
- Chen, C., Zhang, Y., Fu, J., Liu, X., and Coates, M. Bidirectional learning for offline infinite-width model-based optimization. In *Proc NeurIPS*, pp. 29454–67, 2022. doi: 10.5555/3600270.3602406.
- Chen, C., Beckham, C., Liu, Z., Liu, X. L., and Pal, C. Parallel-mentoring for offline model-based optimization. In *Proc NeurIPS*, pp. 76619–36, 2023a. doi: 10.5555/3666122.3669469.
- Chen, C., Zhang, Y., Liu, X., and Coates, M. Bidirectional learning for offline model-based biological sequence design. In *Proc ICML*, volume 202, pp. 5351–66. PMLR, 2023b. URL https://proceedings.mlr. press/v202/chen23ao.html.
- Chen, C. C., Beckham, C., Liu, Z., Liu, X., and Pal, C. Robust guided diffusion for offline black-box optimization. *Trans Mach Learn Res*, 2024. URL https: //openreview.net/forum?id=4JcqmEZ5zt.
- Chen, M., Zhao, H., Zhao, Y., Fan, H., Gao, H., Yu, Y., and Tian, Z. ROMO: Retrieval-enhanced offline model-based optimization. In *Proc Int Conf Dist Artif Intell*, pp. 1–9, 2023c. doi: 10.1145/3627676.3627685.
- Chen, Z., Min, M. R., Parthasarathy, S., and Ning, X. A deep generative model for molecule optimization via one fragment modification. *Nat Mach Intell*, 3:1040–9, 2021. doi: 10.1038/s42256-021-00410-2.
- Cortes, C., Mansour, Y., and Mohri, M. Learning bounds for importance weighting. In *Proc NeurIPS*, volume 23, pp. 442–50, 2010. doi: 10.5555/2997189.2997239.

- 495 Cuturi, M. Sinkhorn distances: Lightspeed computation of
 496 optimal transportation distances. In *Proc NeurIPS*, pp.
 497 2292–300, 2013. doi: 10.48550/arXiv.1306.0895.
 498
- Dao, M. C., Nguyen, P. L., Truong, T. N., and Hoang,
 T. N. Boosting offline optimizers with surrogate sensitivity. In *Proc ICML*, volume 235, pp. 10072–90. PMLR,
 2024. URL https://proceedings.mlr.press/

503 v235/dao24b.html.

- Deb, K., Sunda, J., Rao, U. B. N., and Chaudhuri, S. Reference point based multi-objective optimization using evolutionary algorithms. *Int J Comp Intell Res*, 2(3): 273–86, 2006.
- Deka, A., Liu, C., and Sycara, K. P. Arc Actor residual critic for adversarial imitation learning. In *Proc CoRL*, volume 205 of *Proc Mach Learn Res*, pp. 1446–56, 2023. URL https://proceedings.mlr.press/ v205/deka23a.html.
- 515 Du, Y., Jamasb, A. R., Guo, J., Fu, T., Harris, C.,
 516 Wang, Y., Duan, C., Liò, P., Schwaller, P., and Blun517 dell, T. L. Machine learning-aided generative molec518 ular design. *Nat Mach Intell*, 6:589–604, 2024. doi:
 519 10.1038/s42256-024-00843-5.
- Flam-Shepherd, D., Zhu, K., and Aspuru-Guzik, A. Language models can learn complex molecular distributions. *Nat Commun*, 13(3293), 2022. doi: 10.1038/ s41467-022-30839-x.

- Fu, J. and Levine, S. Offline model-based optimization via normalized maximum likelihood estimation. In *Proc ICLR*, 2021. URL https://openreview.net/ forum?id=FmMKS04e8JK.
- 530 Gardner, M. J., Hall, N., Fung, E., White, O., Berriman, 531 M., Hyman, R. W., Carlton, J. M., Pain, A., Nelson, 532 K. E., Bowman, S., Paulsen, I. T., James, K., Eisen, J. A., 533 Rutherford, K., Salzberg, S. L., Craig, A., Kyes, S., Chan, 534 M.-S., Nene, V., Shallom, S. J., Suh, B., Peterson, J., 535 Angiuoli, S., Pertea, M., Allen, J., Selengut, J., Haft, D., 536 Mather, M. W., Veidya, A. B., Martin, D. M. A., Fair-537 lamb, A. H., Fraunholz, M. J., Roos, D. S., Ralph, S. A., 538 McFadden, G. I., Cummings, L. M., Subramanian, G. M., 539 Mungall, C., Venter, J. C., Carucci, D. J., Hoffman, S. L., 540 Newbold, C., Davis, R. W., Fraser, C. M., and Barrell, 541 B. Genome sequence of the human malaria parasite Plas-542 modium falciparum. Nature, 419:498-511, 2002. doi: 543 10.1038/nature01097. 544
- Gashmard, H., Shakeripour, H., and Alaei, M. Predicting superconducting transition temperature through advanced machine learning and innovative feature engineering. *Sci Rep*, 14(3965), 2024. doi: 10.1038/s41598-024-54440-y.

- Gaulton, A., Bellis, L. J., Bento, A. P., Chambers, J., Davies, M., Hersey, A., Light, Y., McGlinchey, S., Michalovich, D., Al-Lazikani, B., and Overington, J. P. ChEMBL: A large-scale bioactivity database for drug discovery. *Nucleic Acids Research*, 40(D1):D1100–D1107, 2011. doi: 10.1093/nar/gkr777.
- Gomez, F., Schmidhuber, J., and Miikkulainen, R. Accelerated neural evolution through cooperatively coevolved synapses. J Mach Learn Res, 9(31):937– 65, 2008. URL http://jmlr.org/papers/v9/ gomez08a.html.
- Gómez-Bombarelli, R., Wei, J. N., Duvenaud, D., Hernández-Lobato, J. M., Sánchez-Lengeling, B., Sheberla, D., Aguilera-Iparraguirre, J., Hirzel, T. D., Adams, R. P., and Aspuru-Guzik, A. Automatic chemical design using a data-driven continuous representation of molecules. ACS Cent Sci, 4:268–76, 2018. doi: 10. 1021/acscentsci.7b00572.
- Gong, C., He, Q., Bai, Y., Yang, Z., Chen, X., Hou, X., Zhang, X., Liu, Y., and Fan, G. The f-Divergence reinforcement learning framework. *arXiv Preprint*, 2021. doi: 10.48550/arXiv.2109.11867.
- Gonzalez, J., Dai, Z., Hennig, P., and Lawrence, N. Batch Bayesian optimization via local penalization. In *Proc Int Conf AISTATS*, volume 51 of *Proc Mach Learn Res*, pp. 648–57. PMLR, 2016. URL https://proceedings.mlr.press/v51/ gonzalez16a.html.
- Gonzalez de Oliveira, R., Navet, N., and Henkel, A. Multiobjective optimization for safety-related available E/E architectures scoping highly automated driving vehicles. *ACM Transactions on Design Automation of Electronic Systems*, 28(41):1–37, 2023. doi: 10.1145/3582004.
- Goodfellow, I., Pouget-Abadie, J., Mirza, M., Xu, B., Warde-Farley, D., Ozair, S., Courville, A., and Bengio, Y. Generative adversarial nets. In *Proc NeurIPS*, volume 27, 2014. doi: 10.48550/arXiv.1406.2661.
- Grimmer, B., Shu, K., and Wang, A. L. Accelerated gradient descent via long steps. *arXiv Preprint*, 2023. doi: 10. 48550/arXiv.2309.09961.
- Haldar, R. and Mukhopadhyay, D. Levenshtein distance technique in dictionary lookup methods: An improved approach. *arXiv Preprint*, 2011. doi: 10.48550/arXiv. 1101.1232.
- Hamidieh, K. A data-driven statistical model for predicting the critical temperature of a superconductor. *Comp Mat Sci*, 154:346–54, 2018. doi: 10.1016/j.commatsci.2018. 07.052.

- Hansen, N. The CMA evolution strategy: A tutorial. *arXiv Preprint*, 2016. doi: 10.48550/arXiv.1604.00772.
- Hernández-García, A., Saxena, N., Jain, M., Liu, C.H., and Bengio, Y. Multi-fidelity active learning with
 GFlowNets. *Trans Mach Learn Res*, 2024. URL https:
 //openreview.net/forum?id=dLaazW9zuF.
- ⁵⁵⁷ Ho, J. and Ermon, S. Generative adversarial imitation
 ⁵⁵⁸ learning. In *Proc NeurIPS*, pp. 4572–80, 2016. doi: 10.5555/3157382.3157608.
- Hoang, M., Fadhel, A., Deshwal, A., Doppa, J., and Hoang,
 T. N. Learning surrogates for offline black-box optimization via gradient matching. In *Proc ICML*, pp. 18374–93,
 2024.
- Hoeffding, W. Probability inequalities for sums of bounded random variables. *J Am Stat Assoc*, 58(301):13–30, 1963. doi: 10.1080/01621459.1963.10500830.
- Huang, A., Zhan, W., Xie, T., Lee, J. D., Sun, W., Krishnamurthy, A., and Foster, D. J. Correcting the mythos
 of KL-regularization: Direct alignment without overoptimization via Chi-squared preference optimization. *arXiv Preprint*, 2024a. doi: 10.48550/arXiv.2407.13399.
- Huang, X., Li, S., Dobriban, E., Bastani, O., Hassani, H., and Ding, D. One-shot safety alignment for large language models via optimal dualization. In *Proc NeurIPS*, 2024b. doi: 10.48550/arXiv.2405.19544.
- Huo, Z., Liu, W., and Wang, Q. Multi objective optimization method for collision safety of networked vehicles based on improved particle optimization. *J Control and Decision*, 10:134–42, 2022. doi: 10.1080/23307706.2022.
 2080771.
- Jain, M., Bengio, E., Hernandez-Garcia, A., Rector-Brooks,
 J., Dossou, B. F. P., Ekbote, C. A., Fu, J., Zhang, T.,
 Kilgour, M., Zhang, D., Simine, L., Das, P., and Bengio,
 Y. Biological sequence design with GFlowNets. In *Proc ICML*, volume 162 of *Proc Mach Learn Res*, pp. 9786–
 801. PMLR, 2022. URL https://proceedings.
 mlr.press/v162/jain22a.html.
- Jang, S., Yoo, S., and Kang, N. Generative design by reinforcement learning: Enhancing the diversity of topology optimization designs. *Computer-Aided Design*, 146: 103225, 2022. doi: 10.1016/j.cad.2022.103225.
- Kamil, A. T., Saleh, H. M., and Hussain, I. A multi-swarm structure for particle swarm optimization: Solving the welded beam design problem. *J Phys: Conf Ser*, 1804: 012012, 2021. doi: 10.1088/1742-6596/1804/1/012012.
- Kantorovich, L. and Rubinstein, G. S. On a space of totally additive functions. *Vestnik Leningrad. Univ*, 13:52–9, 1958.

- Ke, L., Choudhury, S., Barnes, M., Sun, W., Lee, G., and Srinivasa, S. Imitation learning as f-divergence minimization. In *Algorithmic Foundations of Robotics XIV*, pp. 313–29, 2021. doi: 10.1007/978-3-030-66723-8_19.
- Kim, M., Berto, F., Ahn, S., and Park, J. Bootstrapped training of score-conditioned generator for offline design of biological sequences. In *Proc NeurIPS*, pp. 67643–61, 2023. doi: 10.5555/3666122.3669080.
- Kingma, D. P. and Ba, J. Adam: A method for stochastic optimization. In *Proc ICLR*, 2015. doi: 10.48550/arXiv. 1412.6980.
- Kingma, D. P. and Welling, M. Auto-encoding variational Bayes. In *Proc ICLR*, 2014. doi: 10.48550/arXiv.1312. 6114.
- Kong, D., Pang, B., Han, T., and Wu, Y. N. Molecule design by latent space energy-based modeling and gradual distribution shifting. In *Proc UAI*, volume 216 of *Proceedings of Machine Learning Research*, pp. 1109–20, 2023. URL https://proceedings.mlr.press/ v216/kong23a.html.
- Korshunova, M., Huang, N., Capuzzi, S., Radchenko, D. S., Savych, O., Moroz, Y. S., Wells, C. I., Willson, T. M., Tropsha, A., and Isayev, O. Generative and reinforcement learning approaches for the automated de novo design of bioactive compounds. *Commun Chem*, 5(129), 2022. doi: 10.1038/s42004-022-00733-0.
- Kostrikov, I., Nachum, O., and Tompson, J. Imitation learning via off-policy distribution matching. In *Proc ICLR*, 2020. URL https://openreview.net/forum? id=Hyg-JC4FDr.
- Krishnamoorthy, S., Mashkaria, S. M., and Grover, A. Diffusion models for black-box optimization. In *Proc ICML*, volume 202, pp. 17842–57, 2023. URL https://proceedings.mlr.press/ v202/krishnamoorthy23a.html.
- Kumar, A. and Levine, S. Model inversion networks for model-based optimization. In *Proc NeurIPS*, pp. 5126– 37, 2019. doi: 10.5555/3495724.3496155.
- Li, S., Phillips, J. M., Yu, X., Kirby, R. M., and Zhe, S. Batch multi-fidelity active learning with budget constraints. In *Proc NeurIPS*, pp. 995–1007, 2022a. doi: 10.5555/3600270.3600343.
- Li, S., Wang, Z., Kirby, R., and Zhe, S. Deep multi-fidelity active learning of high-dimensional outputs. In *Proc Int Conf Artif Intell Stats*, volume 151, pp. 1694–711. PMLR, 2022b. URL https://proceedings.mlr. press/v151/li22b.html.

- Li, S., Kirby, R. M., and Zhe, S. Batch multi-fidelity
 Bayesian optimization with deep auto-regressive networks. In *Proc NeurIPS*, pp. 25463–75, 2024. doi: 10.5555/3540261.3542211.
- Liao, X., Li, Q., Yang, X., Zhang, W., and Li, W. Multiobjective optimization for crash safety design of vehicles using stepwise regression model. *Structural and Multidisciplinary Optimization*, 35(6):561–9, 2008. doi: 10.1007/s00158-007-0163-x.
- Lin, Z., Akin, H., Rao, R., Hie, B., Zhu, Z., Lu, W., Smetanin, N., Verkuil, R., Kabeli, O., Shmueli, Y., dos Santos Costa, A., Fazel-Zarandi, M., Sercu, T., Candido, S., and Rives, A. Evolutionary-scale prediction of atomic-level protein structure with a language model. *Science*, 379(6637):1123–30, 2023. doi: 10.1126/science. ade2574.
- Ma, J., Cao, B., Dong, S., Tian, Y., Wang, M., Xiong, J.,
 and Sun, S. Mlmd: A programming-free AI platform
 to predict and design materials. *npj Comput Mater*, 10,
 2024. doi: 10.1038/s41524-024-01243-4.
- Ma, Y. J., Yan, J., Jayaraman, D., and Bastani, O. Offline
 goal-conditioned reinforcement learning via f-advantage
 regression. In *Proc NeurIPS*, pp. 310–23, 2022. doi:
 10.5555/3600270.3600293.

633

634

635

636

- Mashkaria, S. M., Krishnamoorthy, S., and Grover, A. Generative pretraining for black-box optimization. In *Proc ICML*, volume 202, pp. 24173–97, 2023. URL https://proceedings.mlr.press/ v202/mashkaria23a.html.
- Matthews, A. G., Hensman, J., Turner, R., and Ghahramani, Z. On sparse variational methods and the Kullback-Leibler divergence between stochastic processes. In *Proc Int Conf Artif Intell Stats*, volume 51, pp. 231–9. PMLR, 2016. URL https://proceedings.mlr.press/ v51/matthews16.html.
- Maus, N. T., Jones, H. T., Moore, J. S., Kusner, M. J., Bradshaw, J., and Gardner, J. R. Local latent space Bayesian
 optimization over structured inputs. In *Proc NeurIPS*,
 2022. doi: 10.48550/arXiv.2201.11872.
- Maus, N. T., Wu, K., Eriksson, D., and Gardner, J. R. Discovering many diverse solutions with Bayesian optimization. In *Proc Int Conf AI Stats*, volume 206, pp. 1779–98.
 PMLR, 2023. URL https://proceedings.mlr.press/v206/maus23a.html.
- Mullis, M. M., Ramo, I. M., Baker, B. J., and Reese, B. K.
 Diversity, ecology, and prevalence of antimicrobials in nature. *Front Microbiol*, 10, 2019. doi: 10.3389/fmicb. 2019.02518.

- Nachum, O. and Dai, B. Reinforcement learning via Fenchel-Rockafellar duality. *arXiv Preprint*, 2020. doi: 10.48550/arXiv.2001.01866.
- Nguyen, E., Poli, M., Durrant, M. G., Kang, B., Katrekar, D., Li, D. B., Bartie, L. J., Thomas, A. W., King, S. H., Brixi, G., Sullivan, J., Ng, M. Y., Lewis, A., Lou, A., Ermon, S., Baccus, S. A., Hernandez-Boussard, T., Ré, C., Hsu, P. D., and Hie, B. L. Sequence modeling and design from molecular to genome scale with Evo. *Science*, 386(6723): eado9336, 2024. doi: 10.1126/science.ado9336.
- Nguyen, T., Agrawal, S., and Grover, A. Expt: Synthetic pretraining for few-shot experimental design. In *Proc NeurIPS*, 2023. doi: 10.5555/3666122.3668109.
- Nishiyama, T. and Sason, I. On relations between the relative entropy and Chi-Squared-divergence, generalizations and applications. *Entropy*, 22(5), 2020. doi: 10.3390/e22050563.
- Ohana, R., McCabe, M., Meyer, L. T., Morel, R., Agocs, F. J., Beneitez, M., Berger, M., Burkhart, B., Dalziel, S. B., Fielding, D. B., Fortunato, D., Goldberg, J. A., Hirashima, K., Jiang, Y.-F., Kerswell, R., Maddu, S., Miller, J. M., Mukhopadhyay, P., Nixon, S. S., Shen, J., Watteaux, R., Régaldo-Saint Blancard, B., Rozet, F., Parker, L. H., Cranmer, M., and Ho, S. The Well: A large-scale collection of diverse physics simulations for machine learning. In *Proc NeurIPS*, 2024. URL https: //openreview.net/forum?id=00Sx577BT3.
- Palizhati, A., Torrisi, S. B., Aykol, M., Suram, S. K., Hummelshøj, J. S., and Montoya, J. H. Agents for sequential learning using multiple-fidelity data. *Sci Rep*, 12(4694), 2022. doi: 10.1038/s41598-022-08413-8.
- Papalexopoulos, T. P., Tjandraatmadja, C., Anderson, R., Vielma, J. P., and Belanger, D. Constrained discrete black-box optimization using mixed-integer programming. In *Proc ICML*, volume 162, pp. 17295–322. PMLR, 2022. URL https://proceedings.mlr.press/ v162/papalexopoulos22a.html.
- Pele, O. and Werman, M. Fast and robust Earth mover's distances. In *Proc ICCV*, pp. 460–7, 2009. doi: 10.1109/ ICCV.2009.5459199.
- Pogue, E. A., New, A., McElroy, K., Le, N. Q., Pekala, M. J., McCue, I., Gienger, E., Domenico, J., Hedrick, E., McQueen, T. M., Wilfong, B., Piatko, C. D., Ratto, C. R., Lennon, A., Chung, C., Montalbano, T., Bassen, G., and Stiles, C. D. Closed-loop superconducting materials discovery. *npj Comput Mater*, 9, 2023. doi: 10.1038/ s41524-023-01131-3.

- 660 Rafailov, R., Sharma, A., Mitchell, E., Ermon, S., Manning, 661 C. D., and Finn, C. Direct preference optimization: Your 662 language model is secretly a reward model. In Proc 663 NeurIPS, pp. 53728-41, 2023. doi: 10.5555/3666122. 664 3668460. 665 Ray, T. and Liew, K. M. A swarm metaphor for multiobjec-666 tive design optimization. Engineering Optimization, 34: 667 141-53, 2002. doi: 10.1080/03052150210915. 668 669 Sample, P. J., Wang, B., Reid, D. W., Presnyak, V., Mc-670 Fadyen, I. J., Morris, D. R., and Seelig, G. Human 5' 671 UTR design and variant effect prediction from a mas-672 sively parallel translation assay. Nat Biotechnol, 37:803-673 9, 2019. doi: 10.1038/s41587-019-0164-5. 674 675 Sobol, I. M. On the distribution of points in a cube and the 676 approximate evaluation of integrals. USSR Comp Math 677 Phys, 7(4):86-112, 1967. doi: 10.1016/0041-5553(67) 678 90144-9. 679 680 Stanev, V., Oses, C., Kusne, A. G., Rodriguez, E., Paglione, 681 J., Curtarolo, S., and Takeuchi, I. Machine learning mod-682 eling of superconducting critical temperature. npj Comput 683 Mater, 4, 2018. doi: 10.1038/s41524-018-0085-8. 684 685 Tan, R.-X., Xue, K., Lyu, S.-H., Shang, H., Wang, Y., Wang, 686 Y., Fu, S., and Qian, C. Offline model-based optimization 687 by learning to rank. arXiv Preprint, 2024. doi: 10.48550/ 688 arXiv.2410.11502. 689 690 Terjék, D. and González-Sánchez, D. Optimal trans-691 port with f-divergence regularization and generalized 692 Sinkhorn algorithm. 693 151 of Proc Mach Learn Res, pp. 5135-65. PMLR, 694 2022. URL https://proceedings.mlr.press/ 695 v151/terjek22a.html. 696 697 Todorov, E., Erez, T., and Tassa, Y. MuJoCo: A physics 698 engine for model-based control. In Proc Int Conf Intell 699 Rob Sys, pp. 5026-33, 2012. doi: 10.1109/IROS.2012. 700 6386109. 701 Trabucco, B., Kumar, A., Geng, X., and Levine, S. Conser-703 vative objective models for effective offline model-based 704 optimization. In Proc ICML, volume 139, pp. 10358-68. 705 PMLR, 2021. URL https://proceedings.mlr. 706 press/v139/trabucco21a.html. 708 Trabucco, B., Geng, X., Kumar, A., and Levine, S. Design-709
- Bench: Benchmarks for data-driven offline model-based 710 optimization. In Proc ICML, volume 162 of Proceed-711 ings of Machine Learning Research, pp. 21658-76, 712 2022. URL https://proceedings.mlr.press/ 713 v162/trabucco22a.html.

- Tripp, A., Daxberger, E., and Hernández-Lobato, J. M. Sample-efficient optimization in the latent space of deep generative models via weighted retraining. In Proc NeurIPS, pp. 11259-72, 2020. doi: 10.5555/3495724. 3496669.
- Tsybakov, A. B. Introduction to nonparametric estimation. Springer New York, NY, 2008. doi: 10.1007/b13794.
- Wang, C., Jian, Y., Yang, C., Liu, H., and Chen, Y. Beyond reverse KL: Generalizing direct preference optimization with diverse divergence constraints. In Proc ICLR, 2024. doi: 10.48550/arXiv.2309.16240.
- Wang, T.-H. J., Zheng, J., Ma, P., Du, Y., Kim, B., Spielberg, A., Tenenbaum, J., Gan, C., and Rus, D. DiffuseBot: Breeding soft robots with physics-augmented generative diffusion models. In Proc NeurIPS, volume 36, pp. 44398-423, 2023. doi: 10.5555/3666122.3668044.
- Wang, Y., He, H., and Tan, X. Truly proximal policy optimization. In Proc Conf Unc Artif Intell, volume 115, pp. 113-22. PMLR, 2020. URL https://proceedings.mlr.press/v115/ wang20b.html.
- Watanabe, K. and Isobe, N. Sinkhorn algorithm for sequentially composed optimal transports. arXiv Preprint, 2025. doi: 10.48550/arXiv.2412.03120.
- Wildman, S. A. and Crippen, G. M. Prediction of physicochemical parameters by atomic contributions. J Chem Info Comp Sci, 39(5):868-73, 1999. doi: 10.1021/ ci9903071.
- Williams, R. J. Simple statistical gradient-following algorithms for connectionist reinforcement learning. Mach Learn, 8(3-4):229-56, 1992. doi: 10.1007/BF00992696.
- Wilson, J. T., Moriconi, R., Hutter, F., and Disenroth, M. P. The reparameterization trick for acquisition functions. arXiv Preprint, 2017. doi: 10.48550/arXiv.1712.00424.
- Wu, D., Niu, R., Chinazzi, M., Ma, Y.-A., and Yu, R. Disentangled multi-fidelity deep Bayesian active learning. In Proc ICML, pp. 37624-34, 2023. doi: 10.5555/3618408. 3619975.
- Xiong, H. Dpcd: Discrete principal coordinate descent for binary variable problems. Proc AAAI Conf Artif Intell, 36 (9):10391-8, 2022. doi: 10.1609/aaai.v36i9.21281.
- Yakovchuk, P., Protozanova, E., and Frank-Kamenetskii, M. D. Base-stacking and base-pairing contributions into thermal stability of the DNA double helix. Nucleic Acids Res, 34:564-74, 2006. doi: 10.1093/nar/gkj454.

In Proc AISTATS, volume

- Yao, M. S., Zeng, Y., Bastani, H., Gardner, J. R., Gee,
 J. C., and Bastani, O. Generative adversarial model-based
 optimization via source critic regularization. In *Proc NeurIPS*, 2024. doi: 10.48550/arXiv.2402.06532.
- Yu, P., Zhang, D., He, H., Ma, X., Miao, R., Lu, Y., Zhang,
 Yu, P., Zhang, D., He, H., Ma, X., Miao, R., Lu, Y., Zhang,
 Y., Kong, D., Gao, R., Xie, J., Cheng, G., and Wu, Y. N.
 Latent energy-based odyssey: Black-box optimization via
 expanded exploration in the energy-based latent space. *arXiv Preprint*, 2024. doi: 10.48550/arXiv.2405.16730.
 - Yu, S., Ahn, S., Song, L., and Shin, J. Roma: Robust model adaptation for offline model-based optimization. In *Proc NeurIPS*, 2021. doi: 10.5555/3540261.3540614.
- Yuan, Y., Chen, C., Liu, Z., Neiswanger, W., and Liu, X.
 Importance-aware co-teaching for offline model-based optimization. In *Proc NeurIPS*, pp. 55718–33, 2023. doi: 10.5555/3666122.3668554.
- Yuan, Y., Zhang, Y., Chen, C., Wu, H., Li, Z., Li, J., Clark,
 J. J., and Liu, X. Design editing for offline model-based
 optimization. *arXiv Preprint*, 2024. doi: 10.48550/arXiv.
 2405.13964.
- Yun, T., Yun, S., Lee, J., and Park, J. Guided trajectory generation with diffusion models for offline model-based optimization. In *Proc NeurIPS*, 2024. URL https: //openreview.net/forum?id=ioKQzb8SMr.
- Zeni, C., Pinsler, R., Zügner, D., Fowler, A., Horton, M., Fu,
 X., Wang, Z., Shysheya, A., Crabbé, Ueda, S., Sordillo,
 R., Sun, L., Smith, J., Nguyen, B., Schulz, H., Lewis, S.,
 Huang, C.-W., Lu, Z., Zhou, Y., Yang, H., Hao, H., Li, J.,
 Yang, C., Li, W., Tomioka, R., and Xie, T. A generative
 model for inorganic materials design. *Nature*, 2025. doi:
 10.1038/s41586-025-08628-5.
- Zhang, G., Martens, J., and Grosse, R. Fast convergence of natural gradient descent for overparameterized neural networks. In *Proc NeurIPS*, pp. 8082–93, 2019. doi: 10.5555/3454287.3455013.
- Zhang, X.-C., Wu, C.-K., Yi, J.-C., Zeng, X.-X., Yang,
 C.-Q., Lu, A.-P., Hou, T.-J., and Cao, D.-S. Pushing
 the boundaries of molecular property prediction for drug
 discovery with multitask learning BERT enhanced by
 SMILES enumeration. *Research*, 2022:0004, 2022. doi:
 10.34133/research.0004.
- 762 Zhou, Z., Ji, Y., Li, W., Dutta, P., Davuluri, R. V., and
 763 Liu, H. DNABERT-2: Efficient foundation model and
 764 benchmark for multi-species genomes. In *Proc ICLR*,
 765 2024. URL https://openreview.net/forum?
 766 id=oMLQB4EZE1.
- 767

725

726

727

728

Table of Contents A. Proofs
Proof for Lemma 3.1: Diversity Collapse in Reward Optimization
Proof for Lemma 3.3: Entropy-Divergence Formulation
Remark A.1: Equivalence of Lemma 3.3 and Canonical State-Matching
Proof for Lemma 3.4: Explicit Dual Function of (7)
3. Additional Implementation Details
C. Additional Background and Preliminaries
C.1. <i>f</i> -Divergence and Fenchel Conjugates
C.2. Constrained Optimization via Lagrangian Duality
C.3. Wasserstein Distance and Optimal Transport
D. Additional Results
D.1. Additional Design Quality Results
D.2. Additional Design Diversity Results
D.3. Imposing Alternative f-Divergence Diversity Objectives via Mixed-Divergence Regularization
D.4. Theoretical Guarantees for DynAMO
D.5. Comparison with Offline Model-Free Optimization Methods
D.6. Empirical Computational Cost Analysis
D.7. τ -Weighted Distribution Visualization
D.8. Distribution Analysis of Quality and Diversity Results
D.9. Why Is Diversity Important?
E. Ablation Studies
E.1. Sampling Batch Size Ablation
E.2. Adversarial Critic Feedback and Distribution Matching Ablation
E.3. β and τ Hyperparameter Ablation
E.4. Oracle Evaluation Budget Ablation
E.5. Optimization Initialization Ablation

801 **A. Proofs** 802

800

808

822 823 824

Lemma 3.1. (Diversity Collapse in Reward Optimization) Suppose that there exists a finite set of globally optimal designs x_j^* such that $x_j^* := \arg \max_{x \in \mathcal{X}} r(x)$ and $r^* := r(x_j^*)$ is the optimal reward given a finite, non-uniform reward function r(x). Given any distribution q^{π} , we can decompose it into the form $q^{\pi}(x) = \sum_j w_j \delta(x - x_j^*) + \sum_j w'_j \mathbb{1}(x = x_j^*) + \tilde{q}(x)$, where $w_j \ge 0$ for all j, and $\tilde{q}(x) \ge 0$ and $\tilde{q}(x_j^*) = 0$ for all j. Then, $\tilde{q}(x)$ satisfies $\int dx \tilde{q}(x) = 0$.

Proof. First, note that if $\int dx \, \tilde{q}(x) = 0$, we have

$$\mathbb{E}_{x \sim q^{\pi}(x)}[r(x)] = \int dx \, \sum_{j} w_{j} \delta(x - x_{j}^{*}) r(x) = \sum_{j} w_{j} \int dx \, \delta(x - x_{j}^{*}) r(x) = \sum_{j} w_{j} r^{*} = r^{*} \sum_{j} w_{j} = r^{*}, \quad (16)$$

813 which is optimal. Next, we prove that if $\int dx \, \tilde{q}(x) > 0$, then $\mathbb{E}_{x \sim q^{\pi}}[r(x)] < r^*$. To this end, we define

$$\mathcal{X}_1 := \{ x \in \mathcal{X} \mid 1 < r^* - r(x) \}, \quad \mathcal{X}_n := \left\{ x \in \mathcal{X} \mid \frac{1}{n} < r^* - r(x) \le \frac{1}{n-1} \right\} \subseteq \mathcal{X} \quad \forall n \ge 2$$
(17)

for each $n \in \mathbb{N}$. Note that all \mathcal{X}_n are disjoint by construction; also by construction, we have $\mathcal{X} \setminus \{x_j^*\} = \bigcup_{n=1}^{\infty} \mathcal{X}_n$. Furthermore, note that since $\tilde{q}(x) = 0$ for $x = x_j^*$ for some j, we have $0 < \int dx \, \tilde{q}(x) = \sum_{n=1}^{\infty} \int_{\mathcal{X}_n} dx \, \tilde{q}(x)$, so it must be that $\int_{\mathcal{X}_m} dx \, \tilde{q}(x) > 0$ for some m. As a consequence, we have

$$\int_{\mathcal{X}_m} dx \, \tilde{q}(x)(r^* - r(x)) \ge \frac{1}{m} \int_{\mathcal{X}_m} dx \, \tilde{q}(x) > 0.$$

825 Thus, the expected reward would be

$$\mathbb{E}_{x \sim q^{\pi}}[r(x)] = \int dx \, q^{\pi}(x) r(x)$$

$$= \int dx \left(\sum_{j} w_{j} \delta(x - x_{j}^{*}) + \sum_{j} w_{j}^{*} \mathbb{1}(x = x_{j}^{*}) \right) r(x) + \sum_{n=1}^{\infty} \int_{\mathcal{X}_{n}} dx \, \tilde{q}(x) r(x)$$

$$< \int dx \left(\sum_{j} w_{j} \delta(x - x_{j}^{*}) + \sum_{j} w_{j}^{*} \mathbb{1}(x = x_{j}^{*}) \right) r^{*} + \sum_{n=1}^{\infty} \int_{\mathcal{X}_{n}} dx \, \tilde{q}(x) r^{*}$$

$$= \int dx \, q^{\pi}(x) r^{*}$$

$$= r^{*}$$
(18)

so q^{π} is suboptimal. The claim follows.

Lemma 3.3. (Entropy-Divergence Formulation) Define $J(\pi)$ as in (5). An equivalent representation of $J(\pi)$ is

$$J(\pi) = -\mathcal{H}(q^{\pi}(x)) - (1+\beta)D_{\mathrm{KL}}(q^{\pi}(x)||p_{\mathcal{D}}^{\tau}(x))$$
(19)

where $\mathcal{H}(\cdot)$ is the Shannon entropy and $D_{KL}(\cdot || \cdot)$ is the KL divergence.

Proof. Firstly, note that

$$J(\pi) = \mathbb{E}_{q^{\pi}} [r_{\theta}(x)] - \frac{\beta}{\tau} D_{\mathrm{KL}}(q^{\pi} || p_{\mathcal{D}}^{\tau})$$

$$\simeq \tau \cdot \mathbb{E}_{q^{\pi}} \left[\log e^{r_{\theta}(x)} \right] - \beta D_{\mathrm{KL}}(q^{\pi} || p_{\mathcal{D}}^{\tau})$$

$$= \mathbb{E}_{q^{\pi}} \left[\log e^{\tau r_{\theta}(x)} \right] - \beta D_{\mathrm{KL}}(q^{\pi} || p_{\mathcal{D}}^{\tau})$$
(20)

where \simeq denotes an equivalent representation of the objective (i.e., scaling $J(\pi)$ by $\tau > 0$ does not change the optimal policy π^*). Further rewriting,

$$J(\pi) = \mathbb{E}_{q^{\pi}} \left[\log \frac{e^{\tau r_{\theta}(x)}}{Z^{\tau}} \right] + \mathbb{E}_{q^{\pi}} \log Z^{\tau} - \beta D_{\mathrm{KL}}(q^{\pi} || p_{\mathcal{D}}^{\tau}) \simeq \mathbb{E}_{q^{\pi}} \left[\log \frac{e^{\tau r_{\theta}(x)}}{Z^{\tau}} \right] - \beta D_{\mathrm{KL}}(q^{\pi} || p_{\mathcal{D}}^{\tau})$$
(21)

where we omit the constant $\mathbb{E}_{q^{\pi}} \log \mathcal{Z}_{\theta}^{\tau}$ because the expectation value argument is independent of the policy π . The remaining expectation value can be re-expressed via *importance weighting*:

$$J(\pi) = \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \left[\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \log \frac{e^{\tau r_{\theta}(x)}}{Z^{\tau}} \right] - \beta D_{\mathrm{KL}}(q^{\pi} || p_{\mathcal{D}}^{\tau})$$
(22)

Assuming that the surrogate $r_{\theta}(x)$ is well-trained on the offline dataset \mathcal{D} (i.e., $r(x) \approx r_{\theta}(x) \ \forall x \in \mathcal{D}$), we have

$$J(\pi) \approx \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \left[\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \log \frac{e^{\tau r(x)}}{Z^{\tau}} \right] - \beta D_{\mathrm{KL}}(q^{\pi} || p_{\mathcal{D}}^{\tau}) = \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \left[\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \log p_{\mathcal{D}}^{\tau} \right] - \beta D_{\mathrm{KL}}(q^{\pi} || p_{\mathcal{D}}^{\tau})$$
(23)

871 from **Definition 3.2**. Further rewriting, we have

$$J(\pi) = \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \left[\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \log \left(p_{\mathcal{D}}^{\tau} \cdot \frac{q^{\pi}}{q^{\pi}} \right) \right] - \beta D_{\mathrm{KL}}(q^{\pi} || p_{\mathcal{D}}^{\tau})$$
874

$$= \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \left[\frac{q^{\pi}}{n^{\tau}} \log \frac{p_{\mathcal{D}}^{\tau}}{q^{\pi}} \right] + \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \left[\frac{q^{\pi}}{n^{\tau}} \log q^{\pi} \right] - \beta D_{\mathrm{KL}}(q^{\pi} || p_{\mathcal{D}}^{\tau})$$
(24)

$$\begin{bmatrix} p_{\mathcal{D}} & q \end{bmatrix} \begin{bmatrix} p_{\mathcal{D}} \end{bmatrix}$$

$$= -\mathbb{E}_{p_{\mathcal{D}}^{\tau}} \left[\frac{q}{p_{\mathcal{D}}^{\tau}} \log \frac{q}{p_{\mathcal{D}}^{\tau}} \right] - \mathbb{E}_{q^{\pi}} \left[-\log q^{\pi} \right] - \beta D_{\mathrm{KL}}(q^{\pi} || p_{\mathcal{D}}^{\tau})$$
879

 $J(\pi) = -(1+\beta)\mathbb{E}_{p_{\mathcal{D}}^{\tau}} \left[\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \log \frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \right] - \mathbb{E}_{q^{\pi}} \left[-\log q^{\pi} \right]$

 $= -(1+\beta)\mathbb{E}_{p_{\mathcal{D}}^{\tau}}\left[f_{\mathrm{KL}}\left(\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}}\right)\right] - \mathbb{E}_{q^{\pi}}\left[f_{\ell}\left(q^{\pi}\right)\right]$

(25)

(26)

From the definition of KL-divergence,

up to a constant, where $f_{KL}(x) := x \log x$ and $f_{\ell}(x) := -\log x$ are convex functions, $\mathcal{H}(\cdot)$ is the Shannon entropy, and $D_{\rm KL}(\cdot || \cdot)$ is the KL divergence.

 $= -(1+\beta)D_{\mathrm{KL}}(q^{\pi}||p_{\mathcal{D}}^{\tau}) - \mathcal{H}(q^{\pi})$

Remark A.1 (Equivalence of Lemma 3.3 and Canonical State-Matching). Continuing from (25), one might notice that $J(\pi)$ can be equivalently rewritten as -π - ٦

$$\begin{split} J(\pi) &= -(1+\beta) \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \left[\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \log \frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \right] - \mathbb{E}_{q^{\pi}} \left[-\log q^{\pi} \right] \\ &= -(1+\beta) \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \left[\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \log \frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \right] - \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \left[-\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \log q^{\pi} \right] \\ &= -(1+\beta) \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \left[\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \log \frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \right] - (1+\beta) \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \left[\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \log(q^{\pi})^{-1/(1+\beta)} \right] \\ &= -(1+\beta) \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \left[\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \log \left(\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \cdot \frac{1}{(q^{\pi})^{1/(1+\beta)}} \right) \right] \end{split}$$

$$= -(1+\beta)\mathbb{E}_{q^{\pi}}\left[\log\frac{(q^{\pi})^{\beta/(1+\beta)}}{p_{\mathcal{D}}^{\tau}}\right]$$

Assume that there exists a probability distribution $\hat{p}_{\mathcal{D}}^{\tau}(x)$ such that $\hat{p}_{\mathcal{D}}^{\tau}(x) \propto (p_{\mathcal{D}}^{\tau}(x))^{(1+\beta)/\beta}$. Then

$$J(\pi) \simeq -(1+\beta)\mathbb{E}_{q^{\pi}}\left[\log\left(\frac{q^{\pi}}{\hat{p}_{\mathcal{D}}^{\tau}(x)}\right)^{\beta/(1+\beta)}\right] = -\beta\mathbb{E}_{\hat{p}_{\mathcal{D}}^{\tau}}\left[\frac{q^{\pi}}{\hat{p}_{\mathcal{D}}^{\tau}}\log\frac{q^{\pi}}{\hat{p}_{\mathcal{D}}^{\tau}(x)}\right] = -\beta D_{\mathrm{KL}}(q^{\pi}||\hat{p}_{\mathcal{D}}^{\tau})$$
(27)

In other words, the optimization objective considered in (5) and in Lemma 3.3 is equivalent to a pure state-matching objective $-\beta D_{\text{KL}}(q^{\pi}||\hat{p}_{\mathcal{D}})$ predicated on the existence of a 'rescaled' probability distribution $\hat{p}_{\mathcal{D}}(x)$ as defined above.

Lemma 3.4. (Explicit Dual Function of (7)) Consider the primal problem

$$\max_{\pi \in \Pi} \quad J(\pi) \simeq -\mathcal{H}(q^{\pi}) - (1+\beta)D_{\mathrm{KL}}(q^{\pi}||p_{\mathcal{D}}^{\tau})$$

s.t.
$$\mathbb{E}_{p_{\mathcal{D}}^{\tau}}[c^{*}(x)] - \mathbb{E}_{q^{\pi}}[c^{*}(x)] \leq W_{0}$$
 (28)

The Lagrangian dual function $g(\lambda)$ is bounded from below by the function $g_{\ell}(\lambda)$ given by

$$g_{\ell}(\lambda) := \beta \left[\lambda(\mathbb{E}_{p_{\mathcal{D}}^{\tau}} c^*(x) - W_0) - \mathbb{E}_{p_{\mathcal{D}}^{\tau}} e^{\lambda c^*(x) - 1} \right]$$
⁽²⁹⁾

Proof. Define $f_{\text{KL}}(u) := u \log u$. From (10), the dual function $g(\lambda) : \mathbb{R}_+ \to \mathbb{R}$ is given by

$$g(\lambda) := \min_{\pi \in \Pi} \left[(1+\beta) \mathbb{E}_{p_{\mathcal{D}}^{\tau}} f_{\mathsf{KL}} \left(\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \right) - \mathbb{E}_{q^{\pi}} \log (q^{\pi}) + \beta \lambda \left(\mathbb{E}_{p_{\mathcal{D}}^{\tau}} c^{*}(x) - \mathbb{E}_{q^{\pi}} c^{*}(x) - W_{0} \right) \right]$$

$$g(\lambda) := \min_{\pi \in \Pi} \left[(1+\beta) \mathbb{E}_{p_{\mathcal{D}}^{\tau}} f_{\mathsf{KL}} \left(\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \right) - \left(\mathbb{E}_{p_{\mathcal{D}}^{\tau}} f_{\mathsf{KL}} \left(\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \right) + \mathbb{E}_{q^{\pi}} \log p_{\mathcal{D}}^{\tau} \right) + \beta \lambda \left(\mathbb{E}_{p_{\mathcal{D}}^{\tau}} c^{*}(x) - \mathbb{E}_{q^{\pi}} c^{*}(x) - \mathbb{E}_{q^{\pi}} c^{*}(x) - W_{0} \right) \right]$$

$$g(\lambda) := \min_{\pi \in \Pi} \left[(1+\beta) \mathbb{E}_{p_{\mathcal{D}}^{\tau}} f_{\mathsf{KL}} \left(\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \right) - \left(\mathbb{E}_{p_{\mathcal{D}}^{\tau}} f_{\mathsf{KL}} \left(\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \right) + \mathbb{E}_{q^{\pi}} \log p_{\mathcal{D}}^{\tau} \right) + \beta \lambda \left(\mathbb{E}_{p_{\mathcal{D}}^{\tau}} c^{*}(x) - \mathbb{E}_{q^{\pi}} c^{*}(x) - \mathbb{E}_{q^{\pi}} c^{*}(x) - W_{0} \right) \right]$$

$$g(\lambda) := \min_{\pi \in \Pi} \left[(1+\beta) \mathbb{E}_{p_{\mathcal{D}}^{\tau}} f_{\mathsf{KL}} \left(\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \right) - \mathbb{E}_{q^{\pi}} \log p_{\mathcal{D}}^{\tau} + \beta \lambda \left(\mathbb{E}_{p_{\mathcal{D}}^{\tau}} c^{*}(x) - \mathbb{E}_{q^{\pi}} c^{*}(x) - W_{0} \right) \right]$$

$$g(\lambda) := \min_{\pi \in \Pi} \left[\beta \mathbb{E}_{p_{\mathcal{D}}^{\tau}} f_{\mathsf{KL}} \left(\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \right) - \mathbb{E}_{q^{\pi}} \log p_{\mathcal{D}}^{\tau} + \beta \lambda \left(\mathbb{E}_{p_{\mathcal{D}}^{\tau}} c^{*}(x) - \mathbb{E}_{q^{\pi}} c^{*}(x) - W_{0} \right) \right]$$

$$g(\lambda) := \min_{\pi \in \Pi} \left[\beta \mathbb{E}_{p_{\mathcal{D}^{\tau}} f_{\mathsf{KL}} \left(\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \right) - \mathbb{E}_{q^{\pi}} \log p_{\mathcal{D}}^{\tau} + \beta \lambda \left(\mathbb{E}_{p_{\mathcal{D}}^{\tau}} c^{*}(x) - \mathbb{E}_{q^{\pi}} c^{*}(x) - W_{0} \right) \right]$$

where we define $\beta \lambda \in \mathbb{R}_+$ as the Lagrangian multiplier associated with the constraint in (7). Rearranging terms,

932
933
934
$$g(\lambda) = \min_{\pi \in \Pi} \left[\beta \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \left[-\left(\lambda c^* \cdot \frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \right) + f_{\mathsf{KL}} \left(\frac{q^{\pi}}{p_{\mathcal{D}}} \right) \right] - \mathbb{E}_{q^{\pi}} \log p_{\mathcal{D}}^{\tau} + \beta \lambda \mathbb{E}_{p_{\mathcal{D}}^{\tau}} c^*(x) - \beta \lambda W_0 \right]$$
(31)

935 Because the sum of function minima is a lower bound on the minima of the sum of the functions themselves, we have

$$g(\lambda) \geq \beta \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \min_{\pi \in \Pi} \left[-\left(\lambda c^* \cdot \frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}}\right) + f_{\mathrm{KL}}\left(\frac{q^{\pi}}{p_{\mathcal{D}}}\right) \right] - \max_{\pi \in \Pi} \left[\mathbb{E}_{q^{\pi}} \log p_{\mathcal{D}}^{\tau}\right] + \min_{\pi \in \Pi} \left[\beta \lambda \mathbb{E}_{p_{\mathcal{D}}^{\tau}} c^*(x) - \beta \lambda W_0\right] \\ \sim \beta \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \min_{\pi \in \Pi} \left[-\left(\lambda c^* \cdot \frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}}\right) + f_{\mathrm{KL}}\left(\frac{q^{\pi}}{p_{\mathcal{D}}}\right) \right] + \beta \lambda \mathbb{E}_{p_{\mathcal{D}}^{\tau}} c^*(x) - \beta \lambda W_0$$

$$(32)$$

939 940 941

945

946 947 948

951 952 953

954

955

971 972 973

936 937 938

ignoring the term $\max_{\pi \in \Pi} [\mathbb{E}_{q^{\pi}} \log p_{\mathcal{D}}^{\tau}]$ that is constant with respect to λ . In general, simplifying (32) is challenging if not intractable. Instead, we note that minimizing over the set of admissible policies Π achieves an optimum that is lower bounded by minimizing over the superset

$$\begin{aligned} (\lambda) &\geq \beta \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \min_{z \in \mathbb{R}_{+}} \left[-\left(\lambda c^{*}(x) \cdot z\right) + f_{\mathrm{KL}}(z) \right] + \beta \lambda \mathbb{E}_{p_{\mathcal{D}}^{\tau}} c^{*}(x) - \beta \lambda W_{0} \\ &= \beta \left[-\mathbb{E}_{p_{\mathcal{D}}^{\tau}} f_{\mathrm{KL}}^{*}(\lambda c^{*}(x)) + \lambda (\mathbb{E}_{p_{\mathcal{D}}^{\tau}} c^{*}(x) - W_{0}) \right] \end{aligned}$$
(33)

where $f^{\star}(\cdot)$ is the Fenchel conjugate of a convex function $f(\cdot)$. The Fenchel conjugate of $f_{\text{KL}}(u) = u \log u$ is $f_{\text{KL}}^{\star}(v) = e^{v-1}$ following Borwein & Lewis (2006), and so

$$g(\lambda) \ge \beta \left[-\mathbb{E}_{p_{\mathcal{D}}^{\tau}} e^{\lambda c^*(x) - 1} + \lambda (\mathbb{E}_{p_{\mathcal{D}}^{\tau}} c^*(x) - W_0) \right]$$
(34)

Define the right hand side of this inequality as the function $g_{\ell}(\lambda)$ and the result is immediate.

956 957 **B. Additional Implementation Details**

g

958 **Oracle Functions for Optimization Tasks.** The task-specific oracle reward functions r(x) are developed by domain experts and assumed to exactly return the noiseless reward of all possible input designs in the search space \mathcal{X} . The oracle 959 960 functions associated wit tasks from the Design-Bench MBO evaluation suite are detailed by the original Design-Bench 961 authors in Trabucco et al. (2022); briefly, the TFBind8 (i.e., TFBind8-Exact-v0 in Design-Bench) task uses the oracle 962 function from Barrera et al. (2016); the UTR (UTR-ResNet-v0) task uses the oracle function from Angermüeller et al. 963 (2020); the ChEMBL (ChEMBL_MCHC_CHEMBL3885882_MorganFingerprint-RandomForest-v0) task uses 964 the oracle function from Trabucco et al. (2022); the Superconductor (Superconductor-RandomForest-v0) task 965 uses the oracle function from Hamidieh (2018); and the **D'Kitty** (DKittyMorphology-Exact-v0) task uses a MuJoCo 966 (Todorov et al., 2012) simulation environment and learned control policy from Trabucco et al. (2022) to evaluate input designs. The Molecule task uses the oracle function from Wildman & Crippen (1999). 967

Data Preprocessing. For all experiments, we follow Mashkaria et al. (2023) and normalize the objective values both in the offline dataset \mathcal{D} and in those reported in Section 5 according to:

$$y = \frac{\hat{y} - y_{\min}}{y_{\max} - y_{\min}} \tag{35}$$

where $\hat{y} = r(x)$ is the original unnormalized oracle value for an input design x, and y_{max} (resp., y_{min}) is the maximum (resp., minimum) value in the full offline dataset. A reported value of y > 1 means that an offline optimization experiment proposed a candidate design better than the best design in the offline dataset. Note that in many of the MBO tasks, the publicly available offline dataset \mathcal{D} is only a subset of the designs in the full offline dataset; it is therefore possible (and frequently the case) that $\max_{y \in \mathcal{D}} y < 1$ in our MBO tasks.

As introduced in the main text, we learn a VAE (Kingma & Welling, 2014) model to encode and decode designs for discrete optimization tasks to and from a continuous latent space, and perform our optimization experiments over the continuous VAE latent space. Following prior work (Maus et al., 2022; Tripp et al., 2020; Yao et al., 2024), we co-train a Transformer-based VAE autoencoder (consisting of an encoder $e_{\varphi} : \hat{X} \to X$ parameterized by φ^* and decoder $d_{\phi} : X : X \to \hat{X}$ parameterized by γ^*) with the surrogate model $r_{\theta} : X \to \mathbb{R}$ (parameterized by θ^*) according to

985
$$\theta^*, \varphi^*, \phi^* = \operatorname*{arg\,min}_{(\theta,\varphi,\phi)\in\Theta\times\Gamma\times\Phi} \mathbb{E}_{(x,r(x))\sim\mathcal{D}} \left[-\log d_\phi(x|e_\varphi(x)) + \beta D_{\mathrm{KL}}(\mathcal{N}(0,I)||e_\varphi(x)) + \alpha ||r_\theta(e_\varphi(x)) - r(x)||_2^2 \right]$$
(36)

where $\mathcal{N}(0, I)$ is the standard multivariate normal prior and $\alpha = 1$, $\beta = 10^{-4}$ are constant hyperparameters. We can then perform optimization against r_{θ} trained on the 256-dimensional continuous latent space of the VAE, and then decode the 990 candidate designs using $d_{\phi}(\cdot)$ to derive the corresponding discrete design following prior work from Maus et al. (2022); 991 Gómez-Bombarelli et al. (2018). We again use an Adam optimizer with a learning rate of $\eta = 3 \times 10^{-4}$ for both the VAE and the forward surrogate. In this way, the search space for our discrete tasks becomes the $\mathcal{X} \subseteq \mathbb{R}^d$ for d = 256, the 992 993 surrogate model is simply $r_{\theta} : \mathcal{X} \to \mathbb{R}$, and the reward function $r : \mathcal{X} \to \mathbb{R}$ is now 994 $r(x) := \mathbb{E}_{\hat{x} \sim d_{\pm}(\hat{x}|x)}[\hat{r}(\hat{x})]$ (37) 995 996 where $\hat{r} : \hat{\mathcal{X}} \to \mathbb{R}$ is the original expert oracle reward function over the discretized input space $\hat{\mathcal{X}}$, and r(x) is the 997 998 corresponding oracle reward function that accepts our continuous inputs from \mathcal{X} as input. Note that for the MBO tasks over 999 continuous search spaces (i.e., the **Superconductor** and **D'Kitty** tasks), we treat $\mathcal{X} = \mathcal{X}$ and fix both the encoder e_{φ} and 1000 decoder d_{ϕ} to be the identity functions, as no transformation to a separate continuous search space is necessary. 1001 **Optimization Experiments.** All baseline methods run evaluated using their official open-source implementations made 1002 publicly available by the respective authors. In DynAMO, we initialize all optimizers using the first b elements from a 1003 d-dimensional scrambled Sobol sequence (Sobol, 1967) using the official PyTorch quasi-random generator SobolEngine 1004 implementation, where b is the sampling batch size and d is the dimensionality of the search space. Note that the Sobol 1005 sequence only returns points with dimensions between 0 and 1; for each task, we therefore un-normalize the sampled Sobol 1006 points \tilde{x}_0 according to $x_0 = x_{\min} + (\tilde{x}_0 \cdot (x_{\max} - x_{\min}))$, where x_{\max}, x_{\min} are the maximum and minimum bounds on the 1007 search space for our experiments, respectively. We fix $x_{\min} = -4.0$ and $x_{\max} = +4.0$ for all d dimensions across all tasks. 1008 1009 In all experiments reported in Table 1, each optimizer continues to sample from the search space in batched acquisitions of b samples—we set b = 64 for all our experiments unless otherwise stated. After each acquisition, we score the sampled designs using the (penalized) forward surrogate model (i.e., the Lagrangian in (9) for DynAMO). If the maximum prediction 1012 from the recently sampled batch is not at least as optimal as the maximum prediction of the previously sampled designs, then 1013 we define the acquisition step as a *failure*; a sequence of 10 consecutive failures triggers a *restart* in the optimization process 1014 where the optimizer starts from the scratch beginning with sampling with the Sobol sequence to initialize the optimizer as 1015 described above. After 3 restarts are triggered, we consider the optimization process terminated, and all designs across all 1016 restarts are aggregated to choose the top k = 128 final candidate designs to be evaluated using the oracle reward function. Excluded Baselines. We exclude Boosting offline Optimizers with Surrogate Sensitivity (BOSS) from Dao et al. (2024) and 1018 Normalized maximum likelihood Estimation for Model-based Optimization (NEMO) from Fu & Levine (2021) from our 1019 experiments because they do not have open-source implementations. Excluded Optimization Tasks. In our experiments, we primarily evaluate DynAMO and baseline methods on optimization tasks from Design Bench, a suite of offline MBO tasks introduced by Trabucco et al. (2022). The following tasks from the original authors were excluded from our experiments: (1) Ant Morphology, excluded due to reproducibility issues 1024 as per GitHub Issues Link and OpenReview Discussion; (2) Hopper Controller, excluded due to errors in the original 1025 open-source implementation per GitHub Issues Link and prior work (Tan et al., 2024; Mashkaria et al., 2023); (3) NAS 1026 (Neural Architecture Search) on CIFAR10, excluded due to its prohibitively expensive computational cost for evaluating 1027 the oracle function as noted in prior work (Tan et al., 2024; Yu et al., 2021; Fu & Levine, 2021; Nguyen et al., 2023); and

(4) TFBind10, excluded due to its domain and experimental similarity with the TFBind8 task already included in our
evaluation suite. We augment our evaluation suite with the UTR task from Trabucco et al. (2022) and the Molecule task
from Yao et al. (2024); Brown et al. (2019) to provide a comprehensive experimental evaluation of DynAMO and baseline
methods across a wide variety of scientific domains.

C. Additional Background and Preliminaries

1035 C.1. *f*-Divergence and Fenchel Conjugates

1040 1041

Definition C.1 (*f*-Divergence). Suppose we are given two probability distributions P(x), Q(x) defined over a common support \mathcal{X} . For any continuous, convex function $f : \mathbb{R}_+ \to \mathbb{R}$ that is finite over \mathbb{R}_{++} , we define the *f*-divergence between P(x), Q(x) as

$$D_f(Q(x)||P(x)) := \mathbb{E}_{x \sim P(x)} \left[f\left(\frac{Q(x)}{P(x)}\right) \right]$$
(38)

We refer to f as the *generator* of $D_f(\cdot || \cdot)$. Two commonly used f-divergences are the Kullback-Leibler (KL)-Divergence (defined by the generator $f_{KL}(u) = u \log u$) and the χ^2 -Divergence (defined by the generator $f_{\chi^2}(u) = (u-1)^2/2$).

Definition C.2 (Fenchel Conjugate). The *Fenchel conjugate* (i.e., Legendre-Fenchel transform) of a function $f : \mathcal{U} \to \mathbb{R}$ is defined as

$$f^{\star}(v) := -\inf \{-\langle u, v \rangle + f(u) \mid u \in \mathcal{U}\}$$
(39)

where $\langle u, v \rangle$ is the inner product, and $f^* : \mathcal{V} \to \mathbb{R}$ is the Fenchel conjugate defined over the *dual space* \mathcal{V} of \mathcal{U} . Importantly, the Fenchel conjugate function is guaranteed to always be convex Borwein & Lewis (2006) regardless of the (non-)convexity of the original function f. This allows us to make important convergence guarantees in **Appendix D.4** in solving the Lagrangian dual problem in Algorithm 1. Fenchel conjugates are commonly used in optimization problems to rewrite difficult primal problems into more tractable dual formulations Ma et al. (2022); Borwein & Lewis (2006); Agrawal & Horel (2021)—we leverage a similar technique in our work in Algorithm 1.

Lemma C.3 (Fenchel Conjugate of the KL-Divergence Generator Function). Recall that the generator function of the *KL-divergence is* $f_{KL}(u) := u \log u$ for $u \in \mathbb{R}_{++}$. The Fenchel conjugate of this generator is $f_{KL}^{\star}(v) = e^{v-1}$.

Proof. The proof follows immediately from the definition of the Fenchel conjugate in (39).

$$f_{\mathsf{KL}}^{\star}(v) := \sup \left\{ uv - u \log u \mid u \in \mathbb{R}_{++} \right\}$$

$$\tag{40}$$

We differentiate the argument on the right hand side with respect to u to find the supremum given a particular $v \in \mathcal{V}$:

$$\frac{\partial}{\partial u} \left[uv - u \log u \right] \Big|_{u = u^*} = v - \log u^* - 1 = 0 \to u^* = e^{v-1}$$
(41)

It is easy to verify that u^* is a maxima. Plugging this result into (40),

$$f_{\rm KL}^{\star}(v) = u^* v - u^* \log u^* = v e^{v-1} - (v-1)e^{v-1} = e^{v-1} \tag{42}$$

Lemma C.4 (Fenchel Conjugate of the χ^2 -Divergence Generator Function). Recall that the generator function of the χ^2 -divergence is $f_{\chi^2}(u) := \frac{1}{2}(u-1)^2$ for $u \in \mathbb{R}_{++}$. The Fenchel conjugate of this generator is $f_{\chi^2}^{\star}(v) = \frac{v^2}{2} + v$.

Proof. The proof follows immediately from the definition of the Fenchel conjugate in (39).

$$f_{\chi^2}^{\star}(v) := \sup \left\{ uv - \frac{1}{2}(u-1)^2 \mid u \in \mathbb{R}_{++} \right\}$$
(43)

We differentiate the argument on the right hand side with respect to u to find the supremum given a particular $v \in \mathcal{V}$:

$$\frac{\partial}{\partial u} \left[uv - \frac{1}{2} (u-1)^2 \right] \Big|_{u=u^*} = v - u^* + 1 = 0 \to u^* = v + 1$$
(44)

It is easy to verify that u^* is a maxima. Plugging this result into (43),

$$f_{\chi^2}^{\star}(v) = u^*v - \frac{1}{2}(u^* - 1)^2 = (v + 1)v - \frac{1}{2}((v + 1) - 1)^2 = v^2 + v - \frac{1}{2}v^2 = \frac{v^2}{2} + v$$
(45)

Additional details and related technical discussion are offered by Borwein & Lewis (2006); Nachum & Dai (2020); Ma et al. (2022); Amos (2023); and Terjék & González-Sánchez (2022).

C.2. Constrained Optimization via Lagrangian Duality

In our problem formulation in (7) for DynAMO, we reformulate any naïve MBO problem as a separate constrained optimization problem, which is generally of the form

$$\begin{array}{ll} \text{minimize}_{x \in \mathcal{X}} & f(x) \\ \text{subject to} & f_i(x) \le 0 \quad \forall i \in \{1, \dots, m\} \end{array}$$
(46)

1100 given a set of m constraints. In general, satisfying any arbitrary set of (potentially nonlinear) constraints is challenging if not 1101 intractable, and it is often desirable instead to solve a related *unconstrained* optimization problem. One common mechanism 1102 to perform such a problem transformation is to define the *Lagrangian* of (46) as

$$\mathcal{L}(x;\lambda) = f(x) + \langle \lambda, \begin{bmatrix} f_1(x) & f_2(x) & \cdots & f_m(x) \end{bmatrix} \rangle$$
(47)

where $\vec{\lambda} \in \mathbb{R}^m_+$ and $\mathcal{L} : \mathcal{X} \times \mathbb{R}^m_+ \to \mathbb{R}$ is a real-valued function. It can be shown (Boyd & Vandenberghe, 2004) that the constrained optimization problem in (46) is equivalent to the unconstrained problem

$$\operatorname{minimize}_{x \in \mathcal{X}} \quad \operatorname{maximize}_{\vec{\lambda} \in \mathbb{R}^m} \mathcal{L}(x; \lambda) \tag{48}$$

¹¹¹⁰ in terms of the Lagrangian, where \succeq represents an element-wise inequality. The *dual problem* of (48) is constructed by ¹¹¹¹ reversing the order of the minimization and maximization problems:

$$\operatorname{maximize}_{\vec{\lambda} \in \mathbb{R}^m_{\perp}} \quad \operatorname{minimize}_{x \in \mathcal{X}} \mathcal{L}(x; \vec{\lambda}) = \operatorname{maximize}_{\vec{\lambda} \in \mathbb{R}^m_{\perp}} g(\vec{\lambda}) \tag{49}$$

where we implicitly define the *dual function* $g(\vec{\lambda}) := \min_{x \in \mathcal{X}} \mathcal{L}(x; \vec{\lambda})$. In general, it is guaranteed that the optimal solution to the dual problem in (49) is a lower bound for the optimal solution for the original problem in (46) from weak duality; if f(x) and $f_i(x)$ are convex and bounded from below such that Slater's condition applies, then strong duality guarantees that the optimal solutions to the dual and original problems are equal.

As an additional remark, we note that in our problem formulation in (7), Slater's condition is not satisfied as both the surrogate reward function $r_{\theta}(x)$ and adversarial source critic $c^*(x)$ may be arbitarily non-convex. However, we find empirically that the guarantee of weak duality is sufficient to make the approach of Lagrangian duality both tractable and effective in solving (7) to give us DynAMO.

1124 Furthermore, we also find that solving the dual optimization problem in (49) requires us to first solve for the dual function $q(\lambda)$ —this is a challenging task in general, and prior work has attempted to either approximate $q(\lambda)$ under specific 1125 assumptions on the search space \mathcal{X} (Yao et al., 2024) or forego solving for $q(\vec{\lambda})$ entirely by instead treating $\vec{\lambda}$ as a 1126 1127 hyperparameter to be manually tuned or set heuristically (Trabucco et al., 2021; Yu et al., 2021; Chen et al., 2023c). In our 1128 work, we show how penalizing the optimization objective via a KL-divergence term as in (7) is sufficient to yield an *exact* 1129 solution for the dual function $q(\lambda)$ (see Lemma 3.4). This is advantageous because it can be shown (Boyd & Vandenberghe, 1130 2004) that $g(\vec{\lambda})$ is convex; assuming that the gradient of $g(\vec{\lambda})$ has a bounded Lipschitz constant, we can therefore arrive in 1131 an ε -neighborhood around the optimal $\vec{\lambda}^*$ within $\mathcal{O}(1/\varepsilon)$ time (Bubeck, 2015; Grimmer et al., 2023; Zhang et al., 2019). 1132 We leverage this convergence guarantee to solve for $\vec{\lambda}^*$ naïvely via gradient ascent in DynAMO (see Algorithm 1). 1133

1134 1135 **C.3. Wasserstein Distance and Optimal Transport**

1104

1108

1109

1112 1113

1114

1142 1143

1153 1154

1136 In our motivating problem formulation in (7), we introduce a constrained optimization problem where the constraint is 1137 a function of a source critic $c^* : \mathcal{X} \to \mathbb{R}$ with a bounded Lipschitz norm. In this section, we show how this choice in 1138 adversarial source critic is connected to classical theory in optimal transport.

¹¹³⁹ ¹¹⁴⁰ In general, the *p*-Wasserstein distance $W_p(P(x)||Q(x))$ is a distance function between pairs of probability distributions ¹¹⁴¹ P(x) and Q(x). Given a metric space (M, d), we define the *p*-Wasserstein distance as

$$W_p(P(x)||Q(x)) = \inf_{\gamma \in \Gamma(P,Q)} \left(\mathbb{E}_{(x,x') \sim \gamma} d(x,x')^p \right)^{1/p}$$
(50)

1144 1145 for $p \ge 1$, and where $\Gamma(P,Q)$ is the set of all couplings between P(x), Q(x). Intuitively, one can think of the *p*-Wasserstein 1146 distance as representing the cost associated with the optimal (i.e., cost-minimizing) strategy of 'transporting' the 'mass' of 1147 one probability distribution to another.

For any two arbitrary multidimensional distributions, exactly computing the Wasserstein distance between them is computationally expensive (Pele & Werman, 2009; Watanabe & Isobe, 2025; Cuturi, 2013) and in many cases intractable in practice. Instead, a common technique used by Arjovsky et al. (2017) and others is to leverage the Kantorovich-Rubinstein duality theorem (Kantorovich & Rubinstein, 1958) to exactly rewrite (50) (specifically for the p = 1 Wasserstein distance) as

$$W_1(P(x)||Q(x)) = \sup_{||c||_L \le 1} \left[\mathbb{E}_{x \sim P(x)} c(x) - \mathbb{E}_{x \sim Q(x)} c(x) \right]$$
(51)

1155 where $||c||_L$ is the Lipschitz norm of a *source critic* function $c: \mathcal{X} \to \mathbb{R}$. Intuitively, we can think of the function c(x) as

1156 assigning of value of 'in-distribution-ness' relative to P(x): a larger value of c(x) (informally) means that the source critic 1157 predicts the input x to be more likely to have been drawn from P(x) as opposed to Q(x). In DynAMO, we follow Arjovsky 1158 et al. (2017); Yao et al. (2024); and others to constrain the MBO optimization problem by requiring that the estimated 1159 Wasserstein distance between the distribution of generated designs and τ -weighted distribution of designs from the offline 1160 dataset is less than a constant W_0 according to (51)—see Algorithm 1 for additional details.

1161

1172 1173

1195

1199 1200 1201

1207 1208 1209

¹¹⁶² **D. Additional Results**

1164 D.1. Additional Design Quality Results

We supplement the results shown in **Table 1** with the raw Best@128 oracle quality scores reported for each of the 6 tasks in our evaluation suite in **Supplementary Table A1**.

In Section 4, we define the Best@k score to evaluate the quality of observed designs according to a hidden oracle function used for evaluation of candidate fitness. Achieving a high Best@B = k score ensures that a desirable design is found. Consistent with prior work on batched optimization methods (Trabucco et al., 2021; Mashkaria et al., 2023; Krishnamoorthy et al., 2023), we are also interested in the Median@k score defined as

$$\operatorname{Median}@k(\{x_i^F\}_{i=1}^k) := \operatorname{median}_{1 \le i \le k} r(x_i^F)$$
(52)

1174 to evaluate whether a *batch* of candidate designs (as opposed to any singular design) is generally of high quality according 1175 to the oracle r(x). We report the Median@k score for k = 128 in Supplementary Table A2; in general, we find that 1176 DynAMO does not perform as well as other objective-modifying baseline methods according to this metric. However, we 1177 note that in many offline optimization applications, we are often not as interested in how the median design performs, but 1178 rather if we are able to discover optimal and near-optimal designs. For this reason, we chose to focus on the Best@128 1179 oracle scores in Table 1 to evaluate the quality of designs proposed by an optimizer in our main results. Nonetheless, 1180 future work may explore how to better tune DynAMO (e.g., the τ and β hyperparameters in Algorithm 1) to achieve more 1181 desirable Median@128 scores. 1182

1183 **D.2. Additional Design Diversity Results**

We supplement the results shown in **Table 1** with the raw Pairwise Diversity scores reported for each of the 6 tasks in our evaluation suite in **Supplementary Table A1**.

In Section 4, we describe the Pairwise Diversity metric previously used in prior work (Kim et al., 2023; Jain et al., 2022; Maus et al., 2023) to measure the diversity of samples obtained from a given offline optimization method. We can think of Pairwise Diversity as measuring the *between-candidate* diversity of candidates proposed by a generative algorithm. However, this is far from the only relevant definition of diversity; other possible metrics might measure the following:

1192
 1. *Candidate-Dataset Diversity*: How *novel* is a proposed candidate compared to the real designs previously observed in the offline dataset?

2. Aggregate Diversity: How well does the batch of candidate designs collectively cover the possible search space?

To evaluate (1), we follow prior work by Kim et al. (2023) and Jain et al. (2022) and evaluate the **Minimum Novelty (MN)** for a batch of k final proposed candidates with respect to the offline dataset \mathcal{D} , defined as

$$\mathbf{MN}(\{x_i^F\}_{i=1}^k; \mathcal{D}) := \mathbb{E}_{x_i^F} \left[\min_{x \in \mathcal{D}} d(x_i^F, x) \right]$$
(53)

where \mathcal{D} is the task-specific dataset of offline sample designs and x_i^F is the *i*th candidate design proposed by an optimization experiment. Following (14), we define the distance function $d(\cdot, \cdot)$ as the normalized Levenshtein edit distance (Haldar & Mukhopadhyay, 2011) (resp., Euclidean distance) for discrete (resp., continuous) tasks.

¹²⁰⁵ For (2), we report the L_1 Coverage (L1C) of the candidate designs, defined as

$$L1C(\{x_i^F\}_{i=1}^B) := \frac{1}{\dim(x)} \sum_{k=1}^{\dim(x)} \max_{i \neq j} |x_{ik}^F - x_{jk}^F|$$
(54)

1211 1212 1213

Table A1. Quality and Diversity of Designs Under MBO Objective Transforms (Full). We evaluate DynAMO against other MBO objective-modifying methods using six different backbone optimizers. Each cell consists of 'Best@128/Pairwise Diversity' oracle scores separated by a forward slash. Both metrics are reported mean $^{(95\% \text{ confidence interval})}$ across 10 random seeds, where higher is better. Dataset \mathcal{D} reports the maximum oracle score and mean pairwise diversity in the offline dataset. Bolded entries indicate overlapping 95% confidence 1214 intervals with the best performing algorithm (according to the mean) per optimizer. Bolded (resp., Underlined) Rank and Optimality Gap 1215 (Opt. Gap) metrics indicate the best (resp., second best) for a given backbone optimizer. 1216

-									
17	Grad.	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	$\mathbf{Rank}\downarrow$	Opt. Gap \uparrow
8	Dataset \mathcal{D}	43.9/65.9	59.4/57.3	60.5/60.0	88.9/36.7	40.0/66.0	88.4/85.7	_/	_/
9 -	Baseline	90.0 ^(4.3) /12.5 ^(8.0)	80.9 ^(12.1) /7.8 ^(8.8)	60.2 ^(8.9) /7.9 ^(7.8)	88.8 ^(4.0) /24.1 ^(13.3)	36 0 ^(6.8) /0 0 ^(0.0)	65.6 ^(14.5) /0.0 ^(0.0)	5.0/5.5	6.8/-53.2
)	COMs ⁻	$60.4^{(9.8)}/10.4^{(8.7)}$	$60.2^{(12.4)}/7.5^{(9.2)}$	$60.2^{(8.8)}/7.9^{(7.5)}$	88.4 ^(4.0) /24.8 ^(10.0)	$22.5^{(3.2)}/0.0^{(0.0)}$	$71.2^{(10.7)}/0.0^{(0.0)}$	7.3/6.5	-3.0/-53.5
	COMs ⁺	93.1 ^(3.4) / 66.6^(1.0)	67.0 ^(0.9) /57.4 ^(0.2)	64.6 ^(1.0) /81.6 ^(4.9)	97.1 ^(1.6) /3.8 ^(0.9)	41.2 ^(4.8) /99.5 ^(2.6)	91.8 ^(0.9) /21.1 ^(23.5)	2.5 /2.8	12.3/-6.9
	RoMA ⁻	62.0 ^(10.7) /12.3 ^(8.3)	60.9 ^(12.1) /7.9 ^(8.9)	60.2 ^(8.8) /7.7 ^(7.6)	88.8(4.0)/24.2(13.3)	36.0 ^(6.8) /0.0 ^(0.0)	65.6 ^(14.5) /0.0 ^(0.0)	6.7/5.7	-1.2/-53.3
	RoMA ⁺	66.5 ^(0.0) /20.3 ^(0.7)	77.8 ^(0.0) /3.8 ^(0.0)	63.3 ^(0.0) /6.2 ^(0.0)	84.5 ^(0.0) /1.8 ^(0.0)	49.0 ^(1.6) /54.1 ^(1.4)	95.2 ^(1.2) /4.9 ^(0.0)	3.8/5.8	9.2/-46.8
	ROMO	$98.1^{(0.7)}/62.1^{(0.8)}$	$66.8^{(1.0)}/57.1^{(0.1)}$	63.0 ^(0.8) /53.9 ^(0.6)	91.8 ^(0.9) /48.7 ^(0.1)	38.7 ^(2.5) /51.7 ^(3.2)	87.8 ^(0.9) /22.1 ^(5.5)	4.2/2.8	10.9/-12.7
	GAMBO	73.1 ^(12.8) /17.3 ^(12.8)	77.1 ^(9.6) /11.2 ^(10.3)	64.4 ^(1.5) /6.9 ^(7.7)	92.8^(8.0)/22.1^(10.5)	46.0 ^(6.8) /0.0 ^(0.0)	90.6 ^(14.5) /1.5 ^(3.2)	3.2/5.3	10.5/-52.1
_	DynAMO	90.3 ^(4.7) / 66.9^(6.9)	$86.2^{(0.0)}/68.2^{(1.8)}$	64.4 ^(2.5) /77.2 ^(2.2)	91.2 ^(0.0) / 93.0 ^(1.2)	44.2 ^(7.8) /129 ^(5.5)	89.8 ^(3.2) /104 ^(5.6)	<u>2.8</u> /1.2	14.2/27.8
	Adam	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	$\mathbf{Rank} \downarrow$	Opt. Gap ↑
_	Baseline	62.9 ^(13.0) /12.0 ^(12.3)	69.7 ^(10.5) /11.0 ^(12.1)	62.9 ^(1.9) /4.8 ^(3.8)	92.3 ^(8.9) /16.8 ^(12.4)	37.8 ^(6.3) /6.4 ^(14.5)	58.4(18.5)/6.2(14.0)	4.5/6.0	0.5/-52.4
	COMs ⁻	$62.9^{(13.0)}/13.6^{(12.2)}$	$65.1^{(11.0)}/11.0^{(10.6)}$	62.9 ^(1.9) /5.0 ^(3.8)	$92.4^{(1.0)}/21.2^{(18.2)}$	$22.5^{(3.2)}/0.0^{(0.0)}$	$57.3^{(19.5)}/6.3^{(14.3)}$	6.0/5.3	-3.0/-52.4
	COMs ⁺	95.6^(2.6)/44.2^(1.5)	67.1 ^(0.6) /57.4 ^(0.2)	64.6 ^(0.9) /81.5 ^(5.7)	95.3 ^(1.9) /3.7 ^(1.3)	39.6 ^(5.8) /79.3 ^(3.3)	67.1 ^(9.5) /31.8 ^(34.5)	3.2/3.0	8.1/-12.3
	RoMA ⁻	62.9(13.0)/12.3(12.4)	69.7(10.5)/10.9(12.0)	62.9 ^(1.9) /4.7 ^(3.8)	84.7 ^(0.0) /16.8 ^(12.4)	37.8 ^(6.3) /6.4 ^(14.5)	58.4(1.9)/6.2(14.0)	4.5/6.3	0.5/-52.4
	RoMA ⁺	96.5 ^(0.0) /21.3 ^(0.3)	77.8 ^(0.0) /3.8 ^(0.0)	63.3 ^(0.0) /5.9 ^(0.2)	92.3 ^(8.9) /1.8 ^(0.0)	49.8 ^(1.4) /49.4 ^(6.1)	95.7^(1.6)/14.8^(0.6)	2.8 /5.2	14.5 /-45.8
	ROMO	95.6 ^(0.0) /55.7 ^(0.3)	67.0 ^(0.2) /56.3 ^(0.1)	63.3 ^(0.0) /53.5 ^(0.1)	90.4 ^(0.0) /50.7 ^(0.0)	31.8 ^(3.1) /25.5 ^(20.3)	71.0 ^(0.6) /7.2 ^(3.9)	4.8/2.8	6.4/-20.5
	GAMBO	94.0 ^(2.2) /15.1 ^(11.2)	60.0 ^(12.6) /10.3 ^(11.5)	60.9 ^(8.7) /12.1 ^(11.3)	91.4 ^(6.3) /19.6 ^(15.2)	37.8 ^(6.3) /0.3 ^(0.8)	88.4 ^(13.8) /2.6 ^(3.9)	5.3/5.8	<u>8.6</u> /-51.9
_	DynAMO	$95.2^{(1.7)}/54.8^{(8.9)}$	86.2 ^(0.0) /72.3 ^(3.4)	$65.2^{(1.1)}/84.8^{(9.2)}$	91.2 ^(0.0) / 89.9^(5.3)	45.5 ^(5.7) /158 ^(37.3)	84.9 ^(12.0) /126 ^(5.7)	2.8/1.2	14.5/35.7
-	CMA-ES	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	$\mathbf{Rank}\downarrow$	Opt. Gap↑
	Baseline	87.6 ^(8.3) /47.2 ^(11.2)	86.2 ^(0.0) /44.6 ^(15.9)	66.1 ^(1.0) /93.5 ^(2.0)	106 ^(5.9) /66.2 ^(9.4)	49.0 ^(1.0) /12.8 ^(0.6)	72.2 ^(0.1) /164 ^(10.6)	3.7/3.8	14.4/9.5
	COMs ⁻	75.6 ^(10.2) /46.0 ^(17.6)	85.7 ^(1.3) /56.2 ^(15.8)	64.8 ^(1.0) /63.1 ^(23.0)	119 ^(3.3) /58.8 ^(24.2)	$18.8^{(7.9)}/22.0^{(7.9)}$	$62.9^{(2.1)}/67.2^{(8.0)}$	5.7/5.2	7.6/-9.7
	COMs ⁺	68.0 ^(6.0) /24.8 ^(11.3)	77.2 ^(9.7) /35.4 ^(16.5)	63.6 ^(0.5) /36.7 ^(9.0)	116 ^(5.6) /45.8 ^(16.1)	36.8 ^(3.5) /0.0 ^(0.0)	62.2 ^(15.5) /0.0 ^(0.0)	7.3/7.8	7.1/-38.2
	RoMA ⁻	87.6 ^(8.3) /46.7 ^(11.2)	86.2 ^(0.0) /44.8 ^(15.8)	66.1 ^(1.0) /93.5 ^(2.1)	106 ^(5.9) /66.2 ^(9.4)	49.0 ^(1.0) /12.8 ^(0.6)	72.2 ^(0.1) /164 ^(10.6)	3.7/3.5	14.4/9.5
	RoMA ⁺	85.9 ^(7.0) /53.1 ^(15.0)	79.8(3.7)/31.9(15.2)	64.6 ^(1.1) /60.5 ^(14.9)	118 ^(6.6) /63.7 ^(21.6)	44.6 ^(3.2) /98.2 ^(18.9)	72.2 ^(0.1) /112 ^(86.4)	5.0/4.8	14.1/8.0
	ROMO	88.3 ^(6.0) /57.5 ^(11.6)	86.2 ^(0.0) /40.2 ^(13.1)	64.5 ^(0.9) /66.5 ^(13.5)	113(6.0)/70.2(11.5)	45.7 ^(1.3) /97.7 ^(15.4)	77.3 ^(3.2) /20.9 ^(40.9)	4.2/4.3	15.7/-3.1
	GAMBO	90.4 ^(4.4) /39.6 ^(15.5)	86.2 ^(0.0) /53.4 ^(8.4)	66.2 ^(1.6) /84.8 ^(4.8)	121 ^(0.0) /61.3 ^(14.6)	$45.2^{(3.5)}/173^{(19.4)}$	72.2 ^(0.1) /59.9 ^(19.6)	2.2 /4.3	16.7/16.8
	DynAMO	89.8 ^(3.6) /73.6 ^(0.6)	85.7 ^(5.8) /73.1 ^(3.1)	$63.9^{(0.9)}/72.0^{(3.1)}$	$117^{(6.7)}/94.0^{(0.5)}$	50.6 ^(4.8) /97.8 ^(13.2)	78.5 ^(5.5) /292 ^(83.5)	3.3/1.8	17.5/55.2
-	<i>.</i>	07.0 775.0	05.7 /75.1	05.9 112.0	11/ /94.0	50.0 197.8	18.5 /292	<u>3.3</u> / 1.8	17.5/55.2
=	CoSyNE	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	<u>3.3</u> /1.8 Rank↓	Opt. Gap ↑
-	CoSyNE		UTR	ChEMBL	Molecule		D'Kitty	 Rank↓	Opt. Gap↑
-		TFBind8		ChEMBL 63.6 ^(0.4) /28.2 ^(11.3) 63.5 ^(0.4) /19.3 ^(14.1)		Superconductor 37.0 ^(4.1) /0.0 ^(0.0) 28.6 ^(5.5) /0.0 ^(0.0)	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0)		
_	CoSyNE Baseline	TFBind8 61.7 ^(10.0) / 5.6^(5.0)	UTR 57.3 ^(9.6) /12.7 ^(9.8) 73.2 ^(8.9) /8.7 ^(10.2) 56.2 ^(9.5) /26.5 ^(6.8)	ChEMBL 63.6 ^(0,4) /28.2 ^(11.3)	Molecule 94.8 ^(10.1) / 12.2^(7.3)	Superconductor 37.0^(4.1)/0.0^(0.0)	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0)	Rank↓ 5.3/4.5	Opt. Gap ↑ -0.6/-52.1
_	CoSyNE Baseline COMs ⁻	TFBind8 61.7 ^(10.0) / 5.6^(5.0) 70.1 ^(12.8) / 16.5^(8.5) 66.9 ^(5.1) / 15.4^(4.9) 61.7 ^(10.0) / 5.9^(5.2)	UTR 57.3 ^(9.6) /12.7 ^(9.8) 73.2 ^(8.9) /8.7 ^(10.2) 56.2 ^(9.5) /26.5 ^(6.8) 57.3 ^(9.6) /12.7 ^(9.9)	ChEMBL 63.6 ^(0,4) /28.2 ^(11.3) 63.5 ^(0,4) /19.3 ^(14.1) 63.3 ^(0,0) /18.5 ^(7.0) 63.6 ^(0,4) /27.7 ^(10.9)	Molecule 94.8 ^(10.1) /12.2 ^(7.3) 88.4 ^(11.7) /17.4 ^(4.1) 117 ^(3.6) /17.8 ^(8.1) 94.8 ^(10.1) /12.2 ^(7.3)	Superconductor 37.0 ^(4.1) /0.0 ^(0.0) 28.6 ^(5.5) /0.0 ^(0.0)	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 70.6^(1.1)/16.6^(9.0) 62.7 ^(1.3) /0.0 ^(0.0)	Rank↓ 5.3/4.5 5.7/5.7	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6
_	CoSyNE Baseline COMs ⁻ COMs ⁺	TFBind8 61.7 ^(10.0) /5.6 ^(5.0) 70.1 ^(12.8) /16.5 ^(8.5) 66.9 ^(5.1) /15.4 ^(4.9) 61.7 ^(10.0) /5.9 ^(5.2) 70.4 ^(7.2) /17.7 ^(5.5)	UTR 57.3 ^(9,6) /12.7 ^(9,8) 73.2 ^(8,9) /8.7 ^(10,2) 56.2 ^(9,5) /26.5 ^(6,8) 57.3 ^(9,6) /12.7 ^(9,9) 77.8 ^(4,4) /11.9 ^(4,0)	ChEMBL 63.6 ^(0,4) /28.2 ^(11,3) 63.5 ^(0,4) /19.3 ^(14,1) 63.3 ^(0,0) /18.5 ^(7,0) 63.6 ^(0,4) /27.7 ^(10,9) 64.4 ^(2,5) /19.8 ^(3,9)	Molecule 94.8 ^(10.1) /12.2 ^(7.3) 88.4 ^(11.7) /17.4 ^(4.1) 117 ^(3.6) /17.8 ^(8.1) 94.8 ^(10.1) /12.2 ^(7.3) 117 ^(6.5) /10.2 ^(4.4)	Superconductor 37.0 ^(4.1) /(0.0 ^(0.0)) 28.6 ^(5.5) /(0.0 ^(0.0)) 28.0 ^(7.8) /34.3 ^(13.5) 37.0 ^(4.1) /(0.0 ^(0.0)) 38.0 ^(8.1) /(0.0 ^(0.0))	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 70.6^(1.1) /16.6 ^(9.0) 62.7 ^(1.3) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0)	Rank↓ 5.3/4.5 5.7/5.7 5.7/ <u>3.3</u>	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/ <u>-40.4</u>
-	CoSyNE Baseline COMs ⁻ COMs ⁺ RoMA ⁻	TFBind8 61.7 ^(10.0) /5.6 ^(5.0) 70.1 ^(12.8) /16.5 ^(8.5) 66.9 ^(5.1) /15.4 ^(4.9) 61.7 ^(10.0) /5.9 ^(5.2) 70.4 ^(7.2) /17.7 ^(5.5) 79.7^(12.7)/15.7^(10.1)	UTR 57.3 ^(9,6) /12.7 ^(9,8) 73.2 ^(8,9) /8.7 ^(10,2) 56.2 ^(9,5) /26.5 ^(6,8) 57.3 ^(9,6) /12.7 ^(9,9) 77.8 ^(4,4) /1.9 ^(4,0) 62.0 ^(9,8) /5.8 ^(4,6)	ChEMBL 63.6 ^(0,4) /28.2 ^(11.3) 63.5 ^(0,4) /19.3 ^(14.1) 63.3 ^(0,0) /18.5 ^(7.0) 63.6 ^(0,4) /27.7 ^(10.9) 64.4 ^(2.5) /19.8 ^(3.9) 64.1 ^(0,6) /27.6 ^(12.4)	Molecule 94.8 ^(10.1) /12.2 ^(7.3) 88.4 ^(11.7) /17.4 ^(4.1) 117 ^(3.6) /17.8 ^(8.1) 94.8 ^(10.1) /12.2 ^(7.3) 117 ^(6.5) /10.2 ^(4.4) 90.8 ^(3.9) /17.3 ^(9.8)	Superconductor 37.0 ^(4.1) /(0.0 ^(0.0)) 28.6 ^(5.5) /(0.0 ^(0.0)) 28.0 ^(7.8) /34.3 ^(13.5) 37.0 ^(4.1) /(0.0 ^(0.0)) 38.0 ^(8.1) /(0.0 ^(0.0)) 30.6 ^(4.5) /(0.0 ^(0.0))	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 70.6^(1.1) /16.6 ^(9.0) 62.7 ^(1.3) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0) 72.1^(1.1) /0.1 ^(0.2)	Rank ↓ 5.3/4.5 5.7/5.7 5.7/ <u>3.3</u> 5.3/4.5	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/ <u>-40.4</u> -0.6/-52.2
-	CoSyNE Baseline COMs ⁻ COMs ⁺ RoMA ⁻ RoMA ⁺ ROMO GAMBO	TFBind8 61.7 ^(10.0) /5.6 ^(5.0) 70.1 ^(12.8) /16.5 ^(8.5) 66.9 ^(5.1) /15.4 ^(4.9) 61.7 ^(10.0) /5.9 ^(5.2) 70.4 ^(7.2) /17.7 ^(5.5) 79.7 ^(12.7) /15.7 ^(10.1) 79.8 ^(10.6) /5.2 ^(5.7)	UTR 57.3 ^(9,6) /12.7 ^(9,8) 73.2 ^(8,9) /8.7 ^(10,2) 56.2 ^(9,5) /26.5 ^(6,8) 57.3 ^(9,6) /12.7 ^(9,9) 77.8 ^(4,4) /11.9 ^(4,0) 62.0 ^(9,8) /5.8 ^(4,6) 68.0 ^(12,5) /9.1 ^(9,0)	ChEMBL 63.6 ^(0.4) /28.2 ^(11.3) 63.5 ^(0.4) /19.3 ^(14.1) 63.3 ^(0.0) /18.5 ^(7.0) 63.6 ^(0.4) /27.7 ^(10.9) 64.4 ^(2.5) /19.8 ^(3.9) 64.1 ^(0.6) /27.6 ^(12.4) 64.2 ^(0.9) /28.4 ^(15.7)	$\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$	$\begin{array}{c} \hline Superconductor\\ 37.0^{(4.1)}/(0.0^{(0.0)}\\ 28.6^{(5.5)}/(0.0^{(0.0)}\\ 28.0^{(7.8)}/34.3^{(13.5)}\\ 37.0^{(4.1)}/0.0^{(0.0)}\\ 38.0^{(8.1)}/(0.0^{(0.0)}\\ 30.6^{(4.5)}/(0.0^{(0.0)}\\ 37.0^{(4.1)}/(0.0^{(0.0)}) \end{array}$	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 70.6^(1.1)/16.6^(9.0) 62.7 ^(1.3) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0) 72.1^(1.1)/0.1^(0.2) 62.7 ^(1.3) /0.0 ^(0.0)	Rank ↓ 5.3/4.5 5.7/5.7 5.7/3.3 5.3/4.5 2.8/5.0 4.2/5.2 3.7/6.3	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/-40.4 -0.6/-52.2 6.2/-52.0 3.1/-50.8 5.0/-53.6
_	CoSyNE Baseline COMs ⁻ COMs ⁺ RoMA ⁻ RoMA ⁺ ROMO	TFBind8 61.7 ^(10.0) /5.6 ^(5.0) 70.1 ^(12.8) /16.5 ^(8.5) 66.9 ^(5.1) /15.4 ^(4.9) 61.7 ^(10.0) /5.9 ^(5.2) 70.4 ^(7.2) /17.7 ^(5.5) 79.7^(12.7)/15.7^(10.1)	UTR 57.3 ^(9,6) /12.7 ^(9,8) 73.2 ^(8,9) /8.7 ^(10,2) 56.2 ^(9,5) /26.5 ^(6,8) 57.3 ^(9,6) /12.7 ^(9,9) 77.8 ^(4,4) /1.9 ^(4,0) 62.0 ^(9,8) /5.8 ^(4,6)	ChEMBL 63.6 ^(0,4) /28.2 ^(11.3) 63.5 ^(0,4) /19.3 ^(14.1) 63.3 ^(0,0) /18.5 ^(7.0) 63.6 ^(0,4) /27.7 ^(10.9) 64.4 ^(2.5) /19.8 ^(3.9) 64.1 ^(0,6) /27.6 ^(12.4)	Molecule 94.8 ^(10.1) /12.2 ^(7.3) 88.4 ^(11.7) /17.4 ^(4.1) 117 ^(3.6) /17.8 ^(8.1) 94.8 ^(10.1) /12.2 ^(7.3) 117 ^(6.5) /10.2 ^(4.4) 90.8 ^(3.9) /17.3 ^(9.8)	Superconductor 37.0 ^(4.1) /0.0 ^(0.0) 28.6 ^(5.5) /0.0 ^(0.0) 28.0 ^(7.8) /34.3 ^(13.5) 37.0 ^(4.1) /0.0 ^(0.0) 38.0 ^(8.1) /0.0 ^(0.0) 30.6 ^(4.5) /0.0 ^(0.0)	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 70.6^(1.1) /16.6 ^(9.0) 62.7 ^(1.3) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0) 72.1^(1.1) /0.1 ^(0.2)	Rank \downarrow 5.3/4.5 5.7/5.7 5.7/ <u>3.3</u> 5.3/4.5 <u>2.8/5.0</u> 4.2/5.2	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/-40.4 -0.6/-52.2 6.2/-52.0 3.1/-50.8
=	CoSyNE Baseline COMs ⁻ COMs ⁺ RoMA ⁻ RoMA ⁺ ROMO GAMBO	TFBind8 61.7 ^(10.0) /5.6 ^(5.0) 70.1 ^(12.8) /16.5 ^(8.5) 66.9 ^(5.1) /15.4 ^(4.9) 61.7 ^(10.0) /5.9 ^(5.2) 70.4 ^(7.2) /17.7 ^(5.5) 79.7 ^(12.7) /15.7 ^(10.1) 79.8 ^(10.6) /5.2 ^(5.7)	UTR 57.3 ^(9,6) /12.7 ^(9,8) 73.2 ^(8,9) /8.7 ^(10,2) 56.2 ^(9,5) /26.5 ^(6,8) 57.3 ^(9,6) /12.7 ^(9,9) 77.8 ^(4,4) /11.9 ^(4,0) 62.0 ^(9,8) /5.8 ^(4,6) 68.0 ^(12,5) /9.1 ^(9,0)	ChEMBL 63.6 ^(0.4) /28.2 ^(11.3) 63.5 ^(0.4) /19.3 ^(14.1) 63.3 ^(0.0) /18.5 ^(7.0) 63.6 ^(0.4) /27.7 ^(10.9) 64.4 ^(2.5) /19.8 ^(3.9) 64.1 ^(0.6) /27.6 ^(12.4) 64.2 ^(0.9) /28.4 ^(15.7)	$\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$	$\begin{array}{c} \hline Superconductor\\ 37.0^{(4.1)}/(0.0^{(0.0)}\\ 28.6^{(5.5)}/(0.0^{(0.0)}\\ 28.0^{(7.8)}/34.3^{(13.5)}\\ 37.0^{(4.1)}/0.0^{(0.0)}\\ 38.0^{(8.1)}/(0.0^{(0.0)}\\ 30.6^{(4.5)}/(0.0^{(0.0)}\\ 37.0^{(4.1)}/(0.0^{(0.0)}) \end{array}$	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 70.6^(1.1)/16.6^(9.0) 62.7 ^(1.3) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0) 72.1^(1.1)/0.1^(0.2) 62.7 ^(1.3) /0.0 ^(0.0)	Rank ↓ 5.3/4.5 5.7/5.7 5.7/3.3 5.3/4.5 2.8/5.0 4.2/5.2 3.7/6.3	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/-40.4 -0.6/-52.2 6.2/-52.0 3.1/-50.8 5.0/-53.6
_	CoSyNE Baseline COMs ⁻ COMs ⁺ RoMA ⁻ RoMA ⁺ ROMO GAMBO DynAMO	$\begin{array}{c} \textbf{TFBind8} \\ \hline 61.7^{(10.0)}/5.6^{(5.0)} \\ 70.1^{(12.8)}/16.5^{(8.5)} \\ 66.9^{(5.1)}/15.4^{(4.9)} \\ 61.7^{(10.0)}/5.9^{(5.2)} \\ 70.4^{(7.2)}/17.7^{(5.5)} \\ \textbf{79}.7^{(12.7)}/15.7^{(10.1)} \\ \textbf{79.8}^{(10.6)}/5.2^{(5.7)} \\ \textbf{91.3}^{(4.4)}/18.1^{(13.0)} \end{array}$	UTR 57.3 ^(9,6) /12.7 ^(9,8) 73.2 ^(8,9) /8.7 ^(10,2) 56.2 ^(9,5) /26.5 ^(6,8) 57.3 ^(9,6) /12.7 ^(9,9) 77.8 ^(4,4) /11.9 ^(4,0) 62.0 ^(9,8) /5.8 ^(4,6) 68.0 ^(12,5) /9.1 ^(9,0) 77.2 ^(11,6) /20.3 ^(2,3)	$\begin{tabular}{ c c c c c } \hline ChEMBL \\\hline 63.6^{(0.4)}/28.2^{(11.3)} \\\hline 63.5^{(0.4)}/19.3^{(14.1)} \\\hline 63.3^{(0.0)}/18.5^{(7.0)} \\\hline 63.6^{(0.4)}/27.7^{(10.9)} \\\hline 64.4^{(2.5)}/19.8^{(3.9)} \\\hline 64.1^{(0.6)}/27.6^{(12.4)} \\\hline 64.2^{(0.9)}/28.4^{(15.7)} \\\hline 63.9^{(0.9)}/35.0^{(17.9)} \end{tabular}$	$\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$	$\begin{tabular}{ c c c c c c c } \hline Superconductor \\ \hline $37.0^{(4.1)}/0.0^{(0.0)}$\\ $28.6^{(5.5)}/0.0^{(0.0)}$\\ $28.0^{(7.8)}/34.3^{(13.5)}$\\ $37.0^{(4.1)}/0.0^{(0.0)}$\\ $36.0^{(4.1)}/0.0^{(0.0)}$\\ $30.6^{(4.5)}/0.0^{(0.0)}$\\ $37.0^{(4.1)}/0.0^{(0.0)}$\\ $40.6^{(8.6)}/74.4^{(46.3)}$\\ \hline Superconductor $53.1^{(3.3)}/190^{(0.8)}$\\ \hline \end{tabular}$	$\begin{array}{c} \textbf{D'Kitty} \\ \hline 62.7^{(1.3)}/0.0^{(0.0)} \\ \hline 63.8^{(1.6)}/0.0^{(0.0)} \\ \textbf{70.6}^{(1.1)}/16.6^{(9.0)} \\ \hline 62.7^{(1.3)}/0.0^{(0.0)} \\ \hline 50.7^{(1.5)}/0.0^{(0.0)} \\ \textbf{72.1}^{(1.1)}/0.1^{(0.2)} \\ \hline 62.7^{(1.3)}/0.0^{(0.0)} \\ \hline 67.5^{(1.4)}/\textbf{77.0}^{(35.9)} \end{array}$	Rank ↓ 5.3/4.5 5.7/5.7 5.7/5.7 5.7/5.7 5.3/4.5 2.8/5.0 4.2/5.2 3.7/6.3 2.3/1.2	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/-40.4 -0.6/-52.2 6.2/-52.0 3.1/-50.8 5.0/-53.6 12.3/-20.7
-	CoSyNE Baseline COMs ⁻ COMs ⁺ RoMA ⁺ ROMO GAMBO DynAMO BO-qEI	TFBind8 61.7 ^(10.0) /5.6 ^(5.0) 70.1 ^(12.8) /16.5 ^(8.5) 66.9 ^(5.1) /15.4 ^(4.9) 61.7 ^(10.0) /5.9 ^(5.2) 70.4 ^(7.2) /17.7 ^(5.5) 79.7 ^(12.7) /15.7 ^(10.1) 79.8 ^(10.6) /5.2 ^(5.7) 91.3 ^(4.4) /18.1 ^(13.0) TFBind8 87.3 ^(5.8) /73.7 ^(0.6) 93.2 ^(2.7) /73.7 ^(0.7)	UTR 57.3 ^(9,6) /12.7 ^(9,8) 73.2 ^(8,9) /8.7 ^(10,2) 56.2 ^(9,5) /26.5 ^(6,8) 57.3 ^(9,6) /12.7 ^(9,9) 77.8 ^(4,4) /11.9 ^(4,0) 62.0 ^(9,8) /5.8 ^(4,6) 68.0 ^(12,5) /9.1 ^(9,0) 77.2 ^(11,6) /20.3 ^(2,3) UTR 86.2 ^(0,0) /73.8 ^(0,5) 86.2 ^(0,0) /74.3 ^(0,5)	ChEMBL 63.6 ^(0,4) /28.2 ^(11,3) 63.5 ^(0,4) /19.3 ^(14,1) 63.3 ^(0,0) /18.5 ^(7,0) 63.6 ^(0,4) /27.7 ^(10,9) 64.4 ^(2,5) /19.8 ^(3,9) 64.1 ^(0,6) /27.6 ^(12,4) 64.2 ^(0,9) /28.4 ^(15,7) 63.9 ^(0,9) /35.0 ^(17,9) ChEMBL 65.4 ^(1,0) /99.3 ^(0,1) 66.4 ^(0,4) /99.3 ^(0,1)	Molecule 94.8 ^(10.1) /12.2 ^(7.3) 88.4 ^(11.7) /17.4 ^(4.1) 117 ^(3.6) /17.8 ^(8.1) 94.8 ^(10.1) /12.2 ^(7.3) 117 ^(6.5) /10.2 ^(4.4) 90.8 ^(3.9) /17.3 ^(9.8) 99.4 ^(15.0) /7.1 ^(8.0) 114 ^(7.0) /22.8 ^(11.9) Molecule 116 ^(3.1) /93.0 ^(0.5) 121 ^(0.0) /93.2 ^(0.4)	Superconductor 37.0 ^(4.1) /0.0 ^(0.0) 28.6 ^(5.5) /0.0 ^(0.0) 28.0 ^(7.8) /34.3 ^(13.5) 37.0 ^(4.1) /0.0 ^(0.0) 38.0 ^(8.1) /0.0 ^(0.0) 30.6 ^(4.5) /0.0 ^(0.0) 37.0 ^(4.1) /0.0 ^(0.0) 40.6 ^(8.6) /74.4 ^(46.3) Superconductor 53.1 ^(3.3) /190 ^(0.8) 43.2 ^(5.1) /192 ^(10.2)	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 70.6 ^(1.1) /16.6 ^(9.0) 62.7 ^(1.3) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0) 72.1 ^(1.1) /0.1 ^(0.2) 62.7 ^(1.3) /0.0 ^(0.0) 67.5 ^(1.4) /77.0 ^(35.9) D'Kitty 84.4 ^(0.9) /124 ^(7.4) 86.2 ^(0.9) /147 ^(8.9)	Rank↓ 5.3/4.5 5.7/5.7 5.7/5.7 5.3/4.5 2.8/5.0 4.2/5.2 3.7/6.3 2.3/1.2 Rank↓	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/-40.4 -0.6/-52.2 6.2/-52.0 3.1/-50.8 5.0/-53.6 12.3/-20.7 Opt. Gap ↑
	CoSyNE Baseline COMs ⁻ COMs ⁺ RoMA ⁺ ROMA [*] ROMO GAMBO DynAMO BO-qEI Baseline	TFBind8 61.7 ^(10.0) /5.6 ^(5.0) 70.1 ^(12.8) /16.5 ^(8.5) 66.9 ^(5.1) /15.4 ^(4.9) 61.7 ^(10.0) /5.9 ^(5.2) 70.4 ^(7.2) /17.7 ^(5.5) 79.7 ^(12.7) /15.7 ^(10.1) 79.8 ^(10.6) /5.2 ^(5.7) 91.3 ^(4.4) /18.1 ^(13.0) TFBind8 87.3 ^(5.8) /73.7 ^(0.6) 93.2 ^(2.7) /73.7 ^(0.7) 84.5 ^(5.5) /68.8 ^(0.8)	UTR 57.3 ^(9,6) /12.7 ^(9,8) 73.2 ^(8,9) /8.7 ^(10,2) 56.2 ^(9,5) /26.5 ^(6,8) 57.3 ^(9,6) /12.7 ^(9,9) 77.8 ^(4,4) /11.9 ^(4,0) 62.0 ^(9,8) /5.8 ^(4,6) 68.0 ^(12,5) /9.1 ^(9,0) 77.2 ^(11,6) /20.3 ^(2,3) UTR 86.2 ^(0,0) /73.8 ^(0,5) 86.2 ^(0,0) /74.3 ^(0,5) 85.6 ^(0,8) /71.8 ^(0,3)	ChEMBL 63.6 ^(0,4) /28.2 ^(11.3) 63.5 ^(0,4) /19.3 ^(14.1) 63.3 ^(0,0) /18.5 ^(7.0) 63.6 ^(0,4) /27.7 ^(10.9) 64.4 ^(2.5) /19.8 ^(3.9) 64.1 ^(0,6) /27.6 ^(12.4) 64.2 ^(0.9) /28.4 ^(15.7) 63.9 ^(0.9) /35.0 ^(17.9) ChEMBL 65.4 ^(1.0) /99.3 ^(0.1) 66.4 ^(0.4) /99.3 ^(0.1) 65.4 ^(1.0) /96.6 ^(0.9)	Molecule 94.8 ^(10.1) /12.2 ^(7.3) 88.4 ^(11.7) /17.4 ^(4.1) 117 ^(3.6) /17.8 ^(8.1) 94.8 ^(10.1) /12.2 ^(7.3) 117 ^(6.5) /10.2 ^(4.4) 90.8 ^(3.9) /17.3 ^(9.8) 99.4 ^(15.0) /7.1 ^(8.0) 114 ^(7.0) /22.8 ^(11.9) Molecule 116 ^(3.1) /93.0 ^(0.5) 121 ^(0.0) /9.3 ^(0.6)	$\begin{tabular}{ c c c c c } \hline Superconductor \\ \hline 37.0^{(4.1)}/0.0^{(0.0)} \\ 28.6^{(5.5)}/0.0^{(0.0)} \\ 28.0^{(7.8)}/34.3^{(13.5)} \\ 37.0^{(4.1)}/0.0^{(0.0)} \\ \hline 38.0^{(8.1)}/0.0^{(0.0)} \\ \hline 30.6^{(4.5)}/0.0^{(0.0)} \\ \hline 37.0^{(4.1)}/0.0^{(0.0)} \\ \hline 40.6^{(8.6)}/74.4^{(46.3)} \\ \hline \\ \hline Superconductor \\ \hline 53.1^{(3.3)}/190^{(0.8)} \\ \hline 43.2^{(5.1)}/192^{(10.2)} \\ \hline 47.3^{(4.1)}/206^{(1.2)} \\ \hline \end{tabular}$	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 70.6 ^(1.1) /16.6 ^(9.0) 62.7 ^(1.3) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0) 62.7 ^(1.3) /0.0 ^(0.0) 62.7 ^(1.3) /0.0 ^(0.0) 67.5 ^(1.4) /77.0 ^(35.9) D'Kitty 84.4 ^(0.9) /124 ^(7.4) 86.2 ^(0.9) /147 ^(8.9) 84.9 ^(1.1) /79.0 ^(2.8)	Rank ↓ 5.3/4.5 5.7/5.7 5.7/5.7 5.3/4.5 2.8/5.0 4.2/5.2 3.7/6.3 2.3/1.2 Rank ↓ 5.8/5.2	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/-40.4 -0.6/-52.2 6.2/-52.0 3.1/-50.8 5.0/-53.6 12.3/-20.7 Opt. Gap ↑ 18.7/47.1
	CoSyNE Baseline COMs ⁻ COMs ⁺ RoMA ⁻ ROMA ⁺ ROMO GAMBO DynAMO DynAMO BO-qEI Baseline COMs ⁻ COMs ⁺ ROMA ⁻	TFBind8 61.7 ^(10.0) /5.6 ^(5.0) 70.1 ^(12.8) /16.5 ^(8.5) 66.9 ^(5.1) /15.4 ^(4.9) 61.7 ^(10.0) /5.9 ^(5.2) 70.4 ^(7.2) /17.7 ^(5.5) 79.7 ^(12.7) /15.7 ^(10.1) 79.8 ^(10.6) /5.2 ^(5.7) 91.3 ^(4.4) /18.1 ^(13.0) TFBind8 87.3 ^(5.8) /73.7 ^(0.6) 93.2 ^(2.7) /73.7 ^(0.7) 84.5 ^(5.5) /68.8 ^(0.8) 95.2 ^(2.2) /74.1 ^(0.4)	UTR 57.3 ^(9.6) /12.7 ^(9.8) 73.2 ^(8.9) /8.7 ^(10.2) 56.2 ^(9.5) /26.5 ^(6.8) 57.3 ^(9.6) /12.7 ^(9.9) 77.8 ^(4.4) /11.9 ^(4.0) 62.0 ^(9.8) /5.8 ^(4.6) 68.0 ^(12.5) /9.1 ^(9.0) 77.2 ^(11.6) /20.3 ^(2.3) UTR 86.2 ^(0.0) /74.3 ^(0.5) 86.2 ^(0.0) /71.8 ^(0.5) 85.6 ^(0.8) /71.8 ^(0.3) 86.3 ^(0.1) /74.1 ^(0.3)	ChEMBL 63.6 ^(0,4) /28.2 ^(11.3) 63.5 ^(0,4) /19.3 ^(14.1) 63.3 ^(0,0) /18.5 ^(7.0) 63.6 ^(0,4) /27.7 ^(10.9) 64.4 ^(2.5) /19.8 ^(3.9) 64.1 ^(0,6) /27.6 ^(12.4) 64.2 ^(0.9) /28.4 ^(15.7) 63.9 ^(0.9) /35.0 ^(17.9) ChEMBL 65.4 ^(1.0) /99.3 ^(0.1) 66.4 ^(0.4) /99.3 ^(0.1) 65.1 ^(0.8) /96.6 ^(0.9) 65.4 ^(1.1) /99.3 ^(0.1)	Molecule 94.8 ^(10.1) /12.2 ^(7.3) 88.4 ^(11.7) /17.4 ^(4.1) 117 ^(3.6) /17.8 ^(8.1) 94.8 ^(10.1) /12.2 ^(7.3) 117 ^(6.5) /10.2 ^(4.4) 90.8 ^(3.9) /17.3 ^(9.8) 99.4 ^(15.0) /7.1 ^(8.0) 114 ^(7.0) /22.8 ^(11.9) Molecule 116 ^(3.1) /93.0 ^(0.5) 121 ^(0.0) /93.2 ^(0.4) 121 ^(0.0) /90.8 ^(0.8) 121 ^(0.0) /90.8 ^(0.8) 121 ^(0.0) /90.8 ^(0.8)	$\begin{tabular}{ c c c c c } \hline Superconductor \\ \hline 37.0^{(4.1)}/0.0^{(0.0)} \\ 28.6^{(5.5)}/0.0^{(0.0)} \\ 28.0^{(7.8)}/34.3^{(13.5)} \\ 37.0^{(4.1)}/0.0^{(0.0)} \\ \hline 38.0^{(8.1)}/0.0^{(0.0)} \\ \hline 30.6^{(4.5)}/0.0^{(0.0)} \\ \hline 37.0^{(4.1)}/0.0^{(0.0)} \\ \hline 40.6^{(8.6)}/74.4^{(46.3)} \\ \hline \\ \hline Superconductor \\ \hline 53.1^{(3.3)}/190^{(0.8)} \\ \hline 43.2^{(5.1)}/192^{(10.2)} \\ \hline 47.3^{(4.1)}/206^{(1.2)} \\ \hline 53.1^{(3.3)}/190^{(0.8)} \\ \hline \end{tabular}$	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 70.6 ^(1.1) /16.6 ^(9.0) 62.7 ^(1.3) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0) 72.1 ^(1.1) /0.1 ^(0.2) 62.7 ^(1.3) /0.0 ^(0.0) 67.5 ^(1.4) /77.0 ^(35.9) D'Kitty 84.4 ^(0.9) /124 ^(7.4) 86.2 ^(0.9) /147 ^(8.9) 84.9 ^(1.1) /79.0 ^(2.8) 85.8 ^(0.7) /131 ^(15.9)	Rank \downarrow 5.3/4.5 5.7/5.7 5.7/5.7 5.3/4.5 2.8/5.0 4.2/5.2 3.7/6.3 2.3/1.2 Rank \downarrow 5.8/5.2 4.3/4.0 6.0/5.7 2.7/3.3	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/-40.4 -0.6/-52.2 6.2/-52.0 3.1/-50.8 5.0/-53.6 12.3/-20.7 Opt. Gap ↑ 18.7/47.1 19.2/51.4 17.9/40.3 21.0/48.4
1	CoSyNE Baseline COMs ⁻ COMs ⁺ RoMA ⁻ RoMA ⁺ ROMO GAMBO DynAMO BO-qEI Baseline COMs ⁻ COMs ⁺ RoMA ⁻ RoMA ⁺	TFBind8 61.7 ^(10.0) /5.6 ^(5.0) 70.1 ^(12.8) /16.5 ^(8.5) 66.9 ^(5.1) /15.4 ^(4.9) 61.7 ^(10.0) /5.9 ^(5.2) 70.4 ^(7.2) /17.7 ^(5.5) 79.7 ^(12.7) /15.7 ^(10.1) 79.8 ^(10.6) /5.2 ^(5.7) 91.3 ^(4.4) /18.1 ^(13.0) TFBind8 87.3 ^(5.8) /73.7 ^(0.6) 93.2 ^(2.7) /73.7 ^(0.7) 84.5 ^(5.5) /68.8 ^(0.8) 95.2 ^(2.2) /74.1 ^(0.4) 82.9 ^(5.2) /67.5 ^(2.0)	UTR 57.3 ^(9,6) /12.7 ^(9,8) 73.2 ^(8,9) /8.7 ^(10,2) 56.2 ^(9,5) /26.5 ^(6,8) 57.3 ^(9,6) /12.7 ^(9,9) 77.8 ^(4,4) /11.9 ^(4,0) 62.0 ^(9,8) /5.8 ^(4,6) 68.0 ^(12,5) /9.1 ^(9,0) 77.2 ^(11,6) /20.3 ^(2,3) UTR 86.2 ^(0,0) /71.8 ^(0,5) 86.3 ^(0,1) /74.1 ^(0,3) 86.3 ^(0,1) /74.1 ^(0,3) 84.1 ^(1,0) /64.2 ^(1,0)	$\begin{tabular}{ c c c c c } \hline ChEMBL \\\hline 63.6^{(0.4)}/28.2^{(11.3)} \\\hline 63.5^{(0.4)}/19.3^{(14.1)} \\\hline 63.3^{(0.0)}/18.5^{(7.0)} \\\hline 63.6^{(0.4)}/27.7^{(10.9)} \\\hline 64.4^{(2.5)}/19.8^{(3.9)} \\\hline 64.4^{(2.5)}/19.8^{(3.9)} \\\hline 64.4^{(2.6)}/28.4^{(15.7)} \\\hline 63.9^{(0.9)}/28.4^{(15.7)} \\\hline 63.9^{(0.9)}/35.0^{(17.9)} \\\hline \hline ChEMBL \\\hline 65.4^{(1.0)}/99.3^{(0.1)} \\\hline 65.1^{(0.8)}/96.6^{(0.9)} \\\hline 65.4^{(1.1)}/99.3^{(0.1)} \\\hline 66.6^{(0.9)}/98.6^{(0.2)} \\\hline \end{tabular}$	$\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$	$\begin{tabular}{ c c c c c c c } \hline Superconductor \\ \hline 37.0^{(4.1)}/0.0^{(0.0)} \\ \hline 28.6^{(5.5)}/0.0^{(0.0)} \\ \hline 28.0^{(7.8)}/34.3^{(13.5)} \\ \hline 37.0^{(4.1)}/0.0^{(0.0)} \\ \hline 38.0^{(8.1)}/0.0^{(0.0)} \\ \hline 30.6^{(4.5)}/0.0^{(0.0)} \\ \hline 30.6^{(4.5)}/0.0^{(0.0)} \\ \hline 37.0^{(4.1)}/0.0^{(0.0)} \\ \hline 37.0^{(4.1)}/0.0^{(1.0)} \\ \hline 37.0^{(4.1)}/0.0$	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 62.7 ^(1.3) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0) 62.7 ^(1.3) /0.0 ^(0.0) 67.5 ^(1.4) /77.0 ^(35.9) D'Kitty 84.4 ^(0.9) /124 ^(7.4) 86.2 ^(0.9) /147 ^(8.9) 84.9 ^(1.1) /9.0 ^(2.8) 85.8 ^(0.7) /131 ^(15.9) 84.8 ^(1.3) /115 ^(15.3)	Rank \downarrow 5.3/4.5 5.7/5.7 5.7/5.7 5.3/4.5 2.8/5.0 4.2/5.2 3.7/6.3 2.3/1.2 Rank \downarrow 5.8/5.2 4.3/4.0 6.0/5.7	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/-40.4 -0.6/-52.2 6.2/-52.0 3.1/-50.8 5.0/-53.6 12.3/-20.7 Opt. Gap ↑ 18.7/47.1 19.2/51.4 17.9/40.3
	CoSyNE Baseline COMs ⁻ COMs ⁺ RoMA ⁺ ROMO GAMBO DynAMO BO-qEI Baseline COMs ⁺ RoMA ⁻ ROMA ⁺ ROMA ⁺	TFBind8 61.7 ^(10.0) /5.6 ^(5.0) 70.1 ^(12.8) /16.5 ^(8.5) 66.9 ^(5.1) /15.4 ^(4.9) 61.7 ^(10.0) /5.9 ^(5.2) 70.4 ^(7.2) /17.7 ^(5.5) 79.7 ^(12.7) /15.7 ^(10.1) 79.8 ^(10.6) /5.2 ^(5.7) 91.3 ^(4.4) /18.1 ^(13.0) TFBind8 87.3 ^(5.8) /73.7 ^(0.6) 93.2 ^(2.7) /73.7 ^(0.7) 84.5 ^(5.5) /68.8 ^(0.8) 95.2 ^(2.2) /74.1 ^(0.4) 82.9 ^(5.2) /67.5 ^(2.0) 93.8 ^(1.6) /73.8 ^(0.6)	UTR 57.3 ^(9,6) /12.7 ^(9,8) 73.2 ^(8,9) /8.7 ^(10,2) 56.2 ^(9,5) /26.5 ^(6,8) 57.3 ^(9,6) /12.7 ^(9,9) 77.8 ^(4,4) /11.9 ^(4,0) 62.0 ^(0,8) /5.8 ^(4,6) 68.0 ^(12,5) /9.1 ^(9,0) 77.2 ^(11,6) /20.3 ^(2,3) UTR 86.2 ^(0,0) /74.8 ^(0,5) 86.2 ^(0,0) /74.8 ^(0,5) 86.3 ^(0,1) /74.1 ^(0,3) 84.1 ^(1,0) /64.2 ^(1,0) 86.3 ^(0,1) /64.2 ^(1,0)	ChEMBL 63.6 ^(0,4) /28.2 ^(11,3) 63.5 ^(0,4) /19.3 ^(14,1) 63.3 ^(0,0) /18.5 ^(7,0) 63.6 ^(0,4) /27.7 ^(10,9) 64.1 ^(0,6) /27.5 ^(12,4) 64.1 ^(0,6) /27.6 ^(12,4) 64.1 ^(0,6) /98.4 ^(15,7) 63.9 ^(0,9) /35.0 ^(17,9) ChEMBL 65.4 ^(1,0) /99.3 ^(0,1) 66.4 ^(0,4) /99.3 ^(0,1) 65.4 ^(1,1) /99.3 ^(0,1) 66.4 ^(0,9) /88.6 ^(0,2) 63.9 ^(0,8) /94.8 ^(1,6)	$\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$	$\begin{tabular}{ c c c c c c c } \hline Superconductor \\ \hline 37.0^{(4.1)}/0.0^{(0.0)} \\ \hline 28.6^{(5.5)}/0.0^{(0.0)} \\ \hline 28.0^{(7.8)}/34.3^{(13.5)} \\ \hline 37.0^{(4.1)}/0.0^{(0.0)} \\ \hline 30.6^{(4.5)}/0.0^{(0.0)} \\ \hline 30.6^{(4.5)}/0.0^{(0.0)} \\ \hline 37.0^{(4.1)}/0.0^{(0.0)} \\ \hline 40.6^{(8.6)}/74.4^{(46.3)} \\ \hline \\ \hline Superconductor \\ \hline 53.1^{(3.3)}/190^{(0.8)} \\ \hline 43.2^{(5.1)}/192^{(10.2)} \\ \hline 53.1^{(3.3)}/190^{(0.8)} \\ \hline 50.9^{(2.1)}/196^{(0.5)} \\ \hline 48.5^{(3.7)}/196^{(2.7)} \end{tabular}$	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 70.6 ^(1.1) /16.6 ^(9.0) 62.7 ^(1.3) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0) 62.7 ^(1.3) /0.0 ^(0.0) 67.5 ^(1.4) /77.0 ^(35.9) D'Kitty 84.4 ^(0.9) /124 ^(7.4) 86.2 ^(0.9) /147 ^(8.9) 84.9 ^(1.1) /79.0 ^(2.8) 85.8 ^(0.7) /131 ^(15.9) 84.8 ^(1.3) /15 ^(5.5) 84.8 ^(1.5) /15 ^(5.2)	Rank \downarrow 5.3/4.5 5.7/5.7 5.7/5.7 5.3/4.5 5.3/4.5 5.3/4.5 5.3/4.5 2.3/5.7 3.3/4.5 2.8/5.0 4.2/5.2 3.7/6.3 2.3/1.2 Rank \downarrow 5.8/5.2 4.3/4.0 6.0/5.7 2.7/3.3 5.2/6.3 5.0/6.0	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/-40.4 -0.6/-52.2 6.2/-52.0 3.1/-50.8 5.0/-53.6 12.3/-20.7 Opt. Gap ↑ 18.7/47.1 19.2/51.4 17.9/40.3 21.0/48.4 18.3/32.9 19.2/34.9
1 - 22 3 5 5 5 7 7 7 7 8 7 7 7 7 7 7 7 7 7 7 7 7	CoSyNE Baseline COMs ⁻ COMs ⁺ RoMA ⁺ ROMO GAMBO DynAMO BO-qEI Baseline COMs ⁺ RoMA ⁻ RoMA ⁺ ROMA ⁺ ROMO GAMBO	TFBind8 61.7 ^(10.0) /5.6 ^(5.0) 70.1 ^(12.8) /16.5 ^(8.5) 66.9 ^(5.1) /15.4 ^(4.9) 61.7 ^(10.0) /5.9 ^(5.5) 70.4 ^(7.2) /17.7 ^(5.5) 79.7 ^(12.7) /15.7 ^(10.1) 79.8 ^(10.6) /5.2 ^(5.7) 91.3 ^(4.4) /18.1 ^(13.0) TFBind8 87.3 ^(5.8) /73.7 ^(0.6) 93.2 ^(2.7) /73.7 ^(0.7) 84.5 ^(5.5) /68.8 ^(0.8) 95.2 ^(2.2) /4.1 ^(0.4) 82.9 ^(5.2) /67.5 ^(2.0) 93.8 ^(1.6) /73.8 ^(0.6) 94.1 ^(1.9) /74.0 ^(0.6)	UTR 57.3 ^(9,6) /12.7 ^(9,8) 73.2 ^(8,9) /8.7 ^(10,2) 56.2 ^(9,5) /26.5 ^(6,8) 57.3 ^(9,6) /12.7 ^(9,9) 77.8 ^(4,4) /11.9 ^(4,0) 62.0 ^(0,8) /5.8 ^(4,6) 68.0 ^(12,5) /9.1 ^(9,0) 77.2 ^(11,6) /20.3 ^(2,3) UTR 86.2 ^(0,0) /74.8 ^(0,5) 86.2 ^(0,0) /74.8 ^(0,5) 86.3 ^(0,1) /74.1 ^(0,3) 84.1 ^(1,0) /64.2 ^(1,0) 86.3 ^(0,1) /64.2 ^(1,0) 86.3 ^(0,1) /64.2 ^(1,0) 86.3 ^(0,1) /64.2 ^(1,0) 86.3 ^(0,2) /74.3 ^(0,4)	ChEMBL 63.6 ^(0,4) /28.2 ^(11,3) 63.5 ^(0,4) /19.3 ^(14,1) 63.3 ^(0,0) /18.5 ^(7,0) 63.6 ^(0,4) /27.7 ^(10,9) 64.1 ^(2,5) /19.8 ^(3,9) 64.1 ^(2,6) /19.8 ^(1,5,7) 64.2 ^(0,9) /28.4 ^(15,7) 63.9 ^(0,9) /35.0 ^(17,9) ChEMBL 65.4 ^(1,0) /99.3 ^(0,1) 66.4 ^(0,4) /99.3 ^(0,1) 66.4 ^(0,9) /98.6 ^(0,2) 63.9 ^(0,8) /94.8 ^(1,6) 66.8 ^(0,7) /99.3 ^(0,1)	$\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$	$\begin{tabular}{ c c c c c c } \hline Superconductor \\ \hline 37.0^{(4.1)}/0.0^{(0.0)} \\ \hline 28.6^{(5.5)}/0.0^{(0.0)} \\ \hline 28.0^{(7.8)}/34.3^{(13.5)} \\ \hline 37.0^{(4.1)}/0.0^{(0.0)} \\ \hline 38.0^{(8.1)}/0.0^{(0.0)} \\ \hline 30.6^{(4.5)}/0.0^{(0.0)} \\ \hline 37.0^{(4.1)}/0.0^{(0.0)} \\ \hline 40.6^{(8.6)}/74.4^{(46.3)} \\ \hline \\ \hline Superconductor \\ \hline 53.1^{(3.3)}/190^{(0.8)} \\ \hline 43.2^{(5.1)}/192^{(10.2)} \\ \hline 47.3^{(4.1)}/206^{(1.2)} \\ \hline 53.1^{(3.3)}/190^{(0.5)} \\ \hline 48.5^{(3.7)}/196^{(2.7)} \\ \hline 50.8^{(3.3)}/193^{(1.2)} \\ \hline \end{tabular}$	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 70.6 ^(1.1) /16.6 ^(9.0) 62.7 ^(1.3) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0) 62.7 ^(1.3) /0.0 ^(0.0) 67.5 ^(1.4) /77.0 ^(35.9) D'Kitty 84.4 ^(0.9) /124 ^(7.4) 86.2 ^(0.9) /147 ^(8.9) 84.9 ^(1.1) /79.0 ^(2.8) 85.8 ^(0.7) /131 ^(15.5) 85.5 ^(1.7) /55.2 ^(36.3) 86.7 ^(1.1) /17.7 ^(3.5)	Rank \downarrow 5.3/4.5 5.7/5.7 5.7/5.7 5.3/4.5 2.3/5.7 5.3/4.5 5.3/4.5 5.3/4.5 5.3/4.5 5.3/4.5 2.8/5.0 4.2/5.2 3.7/6.3 2.3/1.2 Rank \downarrow 5.8/5.2 4.3/4.0 6.0/5.7 2.7/3.3 5.2/6.3 5.0/6.0 2.2/4.0	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/-40.4 -0.6/-52.2 6.2/-52.0 3.1/-50.8 5.0/-53.6 12.3/-20.7 Opt. Gap ↑ 18.7/47.1 19.2/51.4 17.9/40.3 21.0/48.4 18.3/32.9 19.2/34.9 20.8/30.0
$\begin{bmatrix} -\\ -\\ 2\\ 3\\ 3\\ 4\\ 5\\ 5\\ -\\ -\\ -\\ -\\ -\\ -\\ -\\ -\\ -\\ -\\ -\\ -\\ -\\$	CoSyNE Baseline COMs ⁻ COMs ⁺ RoMA ⁺ ROMO GAMBO DynAMO BO-qEI Baseline COMs ⁺ RoMA ⁻ ROMA ⁺ ROMA ⁺	TFBind8 61.7 ^(10.0) /5.6 ^(5.0) 70.1 ^(12.8) /16.5 ^(8.5) 66.9 ^(5.1) /15.4 ^(4.9) 61.7 ^(10.0) /5.9 ^(5.2) 70.4 ^(7.2) /17.7 ^(5.5) 79.7 ^(12.7) /15.7 ^(10.1) 79.8 ^(10.6) /5.2 ^(5.7) 91.3 ^(4.4) /18.1 ^(13.0) TFBind8 87.3 ^(5.8) /73.7 ^(0.6) 93.2 ^(2.7) /73.7 ^(0.7) 84.5 ^(5.5) /68.8 ^(0.8) 95.2 ^(2.2) /74.1 ^(0.4) 82.9 ^(5.2) /67.5 ^(2.0) 93.8 ^(1.6) /73.8 ^(0.6)	UTR 57.3 ^(9,6) /12.7 ^(9,8) 73.2 ^(8,9) /8.7 ^(10,2) 56.2 ^(9,5) /26.5 ^(6,8) 57.3 ^(9,6) /12.7 ^(9,9) 77.8 ^(4,4) /11.9 ^(4,0) 62.0 ^(0,8) /5.8 ^(4,6) 68.0 ^(12,5) /9.1 ^(9,0) 77.2 ^(11,6) /20.3 ^(2,3) UTR 86.2 ^(0,0) /74.8 ^(0,5) 86.2 ^(0,0) /74.8 ^(0,5) 86.3 ^(0,1) /74.1 ^(0,3) 84.1 ^(1,0) /64.2 ^(1,0) 86.3 ^(0,1) /64.2 ^(1,0)	ChEMBL 63.6 ^(0,4) /28.2 ^(11,3) 63.5 ^(0,4) /19.3 ^(14,1) 63.3 ^(0,0) /18.5 ^(7,0) 63.6 ^(0,4) /27.7 ^(10,9) 64.1 ^(0,6) /27.5 ^(12,4) 64.1 ^(0,6) /27.6 ^(12,4) 64.1 ^(0,6) /98.4 ^(15,7) 63.9 ^(0,9) /35.0 ^(17,9) ChEMBL 65.4 ^(1,0) /99.3 ^(0,1) 66.4 ^(0,4) /99.3 ^(0,1) 65.4 ^(1,1) /99.3 ^(0,1) 66.4 ^(0,9) /88.6 ^(0,2) 63.9 ^(0,8) /94.8 ^(1,6)	$\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$	$\begin{tabular}{ c c c c c c c } \hline Superconductor \\ \hline 37.0^{(4.1)}/0.0^{(0.0)} \\ \hline 28.6^{(5.5)}/0.0^{(0.0)} \\ \hline 28.0^{(7.8)}/34.3^{(13.5)} \\ \hline 37.0^{(4.1)}/0.0^{(0.0)} \\ \hline 30.6^{(4.5)}/0.0^{(0.0)} \\ \hline 30.6^{(4.5)}/0.0^{(0.0)} \\ \hline 37.0^{(4.1)}/0.0^{(0.0)} \\ \hline 40.6^{(8.6)}/74.4^{(46.3)} \\ \hline \\ \hline Superconductor \\ \hline 53.1^{(3.3)}/190^{(0.8)} \\ \hline 53.1^{(3.3)}/190^{(0.8)} \\ \hline 50.9^{(2.1)}/196^{(0.5)} \\ \hline 48.5^{(3.7)}/196^{(2.7)} \end{tabular}$	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 70.6 ^(1.1) /16.6 ^(9.0) 62.7 ^(1.3) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0) 62.7 ^(1.3) /0.0 ^(0.0) 67.5 ^(1.4) /77.0 ^(35.9) D'Kitty 84.4 ^(0.9) /124 ^(7.4) 86.2 ^(0.9) /147 ^(8.9) 84.9 ^(1.1) /79.0 ^(2.8) 85.8 ^(0.7) /131 ^(15.9) 84.8 ^(1.3) /15 ^(5.5) 84.8 ^(1.5) /15 ^(5.2)	Rank \downarrow 5.3/4.5 5.7/5.7 5.7/5.7 5.3/4.5 5.3/4.5 5.3/4.5 5.3/4.5 2.3/5.7 3.3/4.5 2.8/5.0 4.2/5.2 3.7/6.3 2.3/1.2 Rank \downarrow 5.8/5.2 4.3/4.0 6.0/5.7 2.7/3.3 5.2/6.3 5.0/6.0	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/-40.4 -0.6/-52.2 6.2/-52.0 3.1/-50.8 5.0/-53.6 12.3/-20.7 Opt. Gap ↑ 18.7/47.1 19.2/51.4 17.9/40.3 21.0/48.4 18.3/32.9 19.2/34.9
$\begin{bmatrix} - & - \\ - & 2 \\ 2 \\ 3 \\ 3 \\ 4 \\ 5 \\ 5 \\ 5 \\ - \\ - \\ 2 \\ 2 \\ 3 \\ 4 \\ 5 \\ 5 \\ - \\ 5 \\ 5 \\ - \\ - \\ 5 \\ 5 \\ - \\ -$	CoSyNE Baseline COMs ⁻ COMs ⁺ RoMA ⁺ ROMO GAMBO DynAMO BO-qEI Baseline COMs ⁺ RoMA ⁻ RoMA ⁺ ROMA ⁺ ROMO GAMBO	TFBind8 61.7 ^(10.0) /5.6 ^(5.0) 70.1 ^(12.8) /16.5 ^(8.5) 66.9 ^(5.1) /15.4 ^(4.9) 61.7 ^(10.0) /5.9 ^(5.2) 70.4 ^(7.2) /17.7 ^(5.5) 79.7 ^(12.7) /15.7 ^(10.1) 79.8 ^(10.6) /5.2 ^(5.7) 91.3 ^(4.4) /18.1 ^(13.0) TFBind8 87.3 ^(5.8) /73.7 ^(0.6) 93.2 ^(2.7) /73.7 ^(0.7) 84.5 ^(5.5) /68.8 ^(0.8) 95.2 ^(2.2) /74.1 ^(0.4) 82.9 ^(5.2) /67.5 ^(2.0) 93.8 ^(1.6) /73.8 ^(0.6) 94.1 ^(1.9) /74.0 ^(0.6) 91.9 ^(4.4) /74.8 ^(0.2)	UTR 57.3 ^(9,6) /12.7 ^(9,8) 73.2 ^(8,9) /8.7 ^(10,2) 56.2 ^(9,5) /26.5 ^(6,8) 57.3 ^(9,6) /12.7 ^(9,9) 77.8 ^(4,4) /11.9 ^(4,0) 62.0 ^(9,8) /5.8 ^(4,6) 68.0 ^{(12,5} /9.1 ^(9,0) 77.2 ^(11,6) /20.3 ^(2,3) UTR 86.2 ^(0,0) /74.3 ^(0,5) 86.3 ^(0,1) /74.3 ^(0,5) 85.6 ^(0,8) /71.8 ^(0,3) 86.3 ^(0,1) /74.3 ^(0,5) 86.3 ^(0,1) /74.3 ^(0,4) 86.3 ^(0,1) /68.7 ^(1,6) 86.3 ^(0,2) /74.3 ^(0,4) 86.2 ^(0,0) /74.6 ^(0,3) UTR	ChEMBL 63.6 ^(0,4) /28.2 ^(11,3) 63.5 ^(0,4) /19.3 ^(14,1) 63.3 ^(0,0) /18.5 ^(7,0) 63.6 ^(0,4) /27.7 ^(10,9) 64.1 ^(2,5) /19.8 ^(3,9) 64.1 ^(2,6) /19.8 ^(1,5,7) 64.1 ^(0,6) /27.6 ^(12,4) 64.1 ^(0,6) /98.4 ^(15,7) 63.9 ^(0,9) /35.0 ^(17,9) ChEMBL 65.4 ^(1,0) /99.3 ^(0,1) 66.4 ^(0,4) /99.3 ^(0,1) 66.4 ^(0,9) /98.6 ^(0,2) 63.9 ^(0,8) /94.8 ^(1,6) 66.8 ^(0,7) /99.3 ^(0,1)	$\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$	Superconductor 37.0 ^(4.1) /0.0 ^(0.0) 28.6 ^(5.5) /0.0 ^(0.0) 28.0 ^(7.8) /34.3 ^(13.5) 37.0 ^(4.1) /0.0 ^(0.0) 30.6 ^(4.5) /0.0 ^(0.0) 30.6 ^(4.5) /0.0 ^(0.0) 37.0 ^(4.1) /0.0 ^(0.0) 40.6 ^(8.6) /74.4 ^(46.3) Superconductor 53.1 ^(3.3) /190 ^(0.8) 43.2 ^(5.1) /192 ^(10.2) 47.3 ^(4.1) /206 ^(1.2) 53.1 ^(3.3) /190 ^(0.8) 50.9 ^(2.1) /196 ^(0.5) 48.5 ^(3.7) /196 ^(2.7) 50.8 ^(3.3) /193 ^(1.2) 53.5 ^(5.0) /198 ^(1.9) Superconductor	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 70.6 ^(1.1) /16.6 ^(9.0) 62.7 ^(1.3) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0) 62.7 ^(1.3) /0.0 ^(0.0) 67.5 ^(1.3) /77.0 ^(35.9) D'Kitty 84.4 ^(0.9) /124 ^(7.4) 86.2 ^(0.9) /147 ^(8.9) 84.9 ^(1.1) /79.0 ^(2.8) 85.8 ^(0.7) /131 ^(15.3) 85.5 ^(1.1) /75.2 ^(36.3) 86.7 ^(1.1) /17.7 ^(3.5) 85.5 ^(1.1) /277 ^(59.7) D'Kitty	Rank \downarrow 5.3/4.5 5.7/5.7 5.7/5.7 5.3/4.5 2.3/5.7 5.3/4.5 5.3/4.5 5.3/4.5 5.3/4.5 5.3/4.5 2.8/5.0 4.2/5.2 3.7/6.3 2.3/1.2 Rank \downarrow 5.8/5.2 4.3/4.0 6.0/5.7 2.7/3.3 5.2/6.3 5.0/6.0 2.2/4.0	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/-40.4 -0.6/-52.2 6.2/-52.0 3.1/-50.8 5.0/-53.6 12.3/-20.7 Opt. Gap ↑ 18.7/47.1 19.2/51.4 17.9/40.3 21.0/48.4 18.3/32.9 19.2/34.9 20.8/30.0
$ \begin{array}{c} - \\ - \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \\ - \\ 7 \\ - \\ 7 \\ - \\ 7 \\ - \\ 7 \\ - \\ $	CoSyNE Baseline COMs ⁻ COMs ⁺ RoMA ⁺ ROMA ⁺ ROMO GAMBO DynAMO BO-qEI Baseline COMs ⁺ RoMA ⁺ ROMA ⁺ ROMA ⁺ ROMA ⁺ ROMO GAMBO DynAMO	TFBind8 61.7 ^(10.0) /5.6 ^(5.0) 70.1 ^(12.8) /16.5 ^(8.5) 66.9 ^(5.1) /15.4 ^(4.9) 61.7 ^(10.0) /5.9 ^(5.2) 70.4 ^(7.2) /17.7 ^(5.5) 79.7 ^(12.7) /15.7 ^(10.1) 79.8 ^(10.6) /5.2 ^(5.7) 91.3 ^(4.4) /18.1 ^(13.0) TFBind8 87.3 ^(5.8) /73.7 ^(0.6) 93.2 ^(2.7) /73.7 ^(0.7) 84.5 ^(5.5) /68.8 ^(0.8) 95.2 ^(2.2) /74.1 ^(0.4) 82.9 ^(5.2) /67.5 ^(2.0) 93.8 ^(1.6) /73.8 ^(0.6) 94.1 ^(1.9) /74.0 ^(0.6) 91.9 ^(4.4) /74.8 ^(0.2) TFBind8 88.1 ^(5.3) /73.9 ^(0.5)	UTR 57.3 ^(9,6) /12.7 ^(9,8) 73.2 ^(8,9) /8.7 ^(10,2) 56.2 ^(9,5) /26.5 ^(6,8) 57.3 ^(9,6) /12.7 ^(9,9) 77.8 ^(4,4) /11.9 ^(4,0) 62.0 ^(9,8) /5.8 ^(4,6) 68.0 ^{(12,5} /9.1 ^(9,0) 77.2 ^(11,6) /20.3 ^(2,3) UTR 86.2 ^(0,0) /74.3 ^(0,5) 85.6 ^(0,8) /71.8 ^(0,3) 86.3 ^(0,1) /74.3 ^(0,5) 86.3 ^(0,1) /74.3 ^(0,4) 86.3 ^(0,1) /68.7 ^(1,6) 86.3 ^(0,2) /74.3 ^(0,4) 86.2 ^(0,0) /74.3 ^(0,4)	ChEMBL 63.6 ^(0,4) /28.2 ^(11.3) 63.5 ^(0,4) /19.3 ^(14.1) 63.3 ^(0,0) /18.5 ^(7.0) 63.6 ^(0,4) /27.7 ^(10.9) 64.1 ^(0,6) /27.6 ^(12.4) 64.2 ^(0,9) /28.4 ^(15.7) 63.9 ^(0,9) /28.4 ^(15.7) 63.9 ^(0,9) /35.0 ^(17.9) ChEMBL 65.4 ^(1.0) /99.3 ^(0.1) 66.6 ^(0.9) /98.6 ^(0.2) 63.9 ^(0.8) /94.8 ^(1.6) 66.8 ^(0.7) /99.3 ^(0.1) 66.6 ^(0.7) /99.3 ^(0.1) 67.0 ^(1.3) /99.4 ^(0.1) ChEMBL	$\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$	Superconductor 37.0 ^(4.1) /0.0 ^(0.0) 28.6 ^(5.5) /0.0 ^(0.0) 28.0 ^(7.8) /34.3 ^(13.5) 37.0 ^(4.1) /0.0 ^(0.0) 38.0 ^(8.1) /0.0 ^(0.0) 30.6 ^(4.5) /0.0 ^(0.0) 37.0 ^(4.1) /0.0 ^(0.0) 30.6 ^(4.5) /74.4 ^(46.3) Superconductor 53.1 ^(3.3) /190 ^(0.8) 43.2 ^(5.1) /192 ^(10.2) 47.3 ^(4.1) /206 ^(1.2) 53.1 ^(3.3) /190 ^(0.8) 50.9 ^(2.1) /196 ^(0.5) 48.5 ^(3.7) /196 ^(2.7) 50.8 ^(3.3) /193 ^(1.2) 53.5 ^(5.0) /198 ^(1.9) Superconductor 53.5 ^(5.0) /198 ^(1.9)	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 70.6 ^(1.1) /16.6 ^(9.0) 62.7 ^(1.3) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0) 62.7 ^(1.3) /0.0 ^(0.0) 67.5 ^(1.3) /0.0 ^(0.0) 67.5 ^(1.3) /0.0 ^(0.0) 67.5 ^(1.3) /0.0 ^(0.0) 84.4 ^(0.9) /124 ^(7.4) 86.2 ^(0.9) /147 ^(8.9) 84.9 ^(1.1) /79.0 ^(2.8) 85.8 ^(0.7) /131 ^(15.3) 85.5 ^(1.7) /55.2 ^(36.3) 86.7 ^(1.1) /17,7 ^(3.5) 85.5 ^(1.1) /277 ^(59.7) D'Kitty 84.5 ^(0.8) /94.1 ^(3.9)	Rank \downarrow 5.3/4.5 5.7/5.7 5.7/5.7 5.3/4.5 2.8/5.0 4.2/5.2 3.7/6.3 2.3/1.2 Rank \downarrow 5.8/5.2 4.3/4.0 6.0/5.7 2.7/3.3 5.2/6.3 5.0/6.0 2.2/4.0 3.0/1.3	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/-40.4 -0.6/-52.2 6.2/-52.0 3.1/-50.8 5.0/-53.6 12.3/-20.7 Opt. Gap ↑ 18.7/47.1 19.2/51.4 17.9/40.3 21.0/48.4 18.3/32.9 19.2/34.9 20.8/30.0 20.7/74.2
$\begin{bmatrix} - & - & - \\ - & - & - & - \\ - & - & - &$	CoSyNE Baseline COMs ⁻ COMs ⁺ RoMA ⁺ ROMA ⁺ ROMO GAMBO DynAMO BO-qEI Baseline COMs ⁻ COMs ⁺ ROMA ⁺ ROMA ⁺ ROMA ⁺ ROMO GAMBO DynAMO BO-qUCB	TFBind8 61.7 ^(10.0) /5.6 ^(5.0) 70.1 ^(12.8) /16.5 ^(8.5) 66.9 ^(5.1) /15.4 ^(4.9) 61.7 ^(10.0) /5.9 ^(5.2) 70.4 ^(7.2) /15.7 ^(10.1) 79.7 ^(12.7) /15.7 ^(10.1) 79.7 ^(12.7) /15.7 ^(10.1) 79.3 ^(10.6) /5.2 ^(5.7) 91.3 ^(4.4) /18.1 ^(13.0) TFBind8 87.3 ^(5.8) /73.7 ^(0.6) 93.2 ^(2.7) /73.7 ^(0.7) 84.5 ^(5.5) /68.8 ^(0.8) 95.2 ^(2.2) /74.1 ^(0.4) 82.9 ^(5.2) /67.5 ^(2.0) 93.8 ^(1.6) /73.8 ^(0.6) 94.1 ^(1.9) /74.0 ^(0.6) 91.9 ^(4.4) /74.8 ^(0.2) TFBind8 88.1 ^(5.3) /73.9 ^(0.5) 88.5 ^(6.4) /73.4 ^(0.6)	UTR 57.3 ^(9,6) /12.7 ^(9,8) 73.2 ^(8,9) /8.7 ^(10,2) 56.2 ^(9,5) /26.5 ^(6,8) 57.3 ^(9,6) /12.7 ^(9,9) 77.8 ^(4,4) /11.9 ^(4,0) 62.0 ^(9,8) /5.8 ^(4,6) 68.0 ^(12,5) /9.1 ^(9,0) 77.2 ^(11,6) /20.3 ^(2,3) UTR 86.2 ^(0,0) /73.8 ^(0,5) 86.3 ^(0,1) /74.3 ^(0,3) 86.3 ^(0,1) /68.7 ^(1,6) 86.3 ^(0,1) /68.7 ^(1,6) 86.3 ^(0,1) /68.7 ^(1,6) 86.3 ^(0,1) /74.3 ^(0,4) 86.2 ^(0,0) /74.3 ^(0,4) 86.2 ^(0,0) /74.3 ^(0,4) 86.2 ^(0,0) /74.3 ^(0,4) 86.2 ^(0,0) /74.2 ^(0,7)	ChEMBL 63.6 ^(0,4) /28.2 ^(11.3) 63.5 ^(0,4) /19.3 ^(14.1) 63.3 ^(0,0) /18.5 ^(7.0) 63.6 ^(0,4) /27.7 ^(10.9) 64.1 ^(0,6) /27.6 ^(12.4) 64.2 ^(0,9) /28.4 ^(15.7) 63.9 ^(0,9) /28.4 ^(15.7) 63.9 ^(0,9) /35.0 ^(17.9) ChEMBL 65.4 ^(1.0) /99.3 ^(0.1) 66.4 ^(0.4) /99.3 ^(0.1) 65.1 ^(0.8) /96.6 ^(0.9) 65.4 ^(1.1) /99.3 ^(0.1) 66.6 ^(0.9) /98.6 ^(0.2) 63.9 ^(0.8) /94.8 ^(1.6) 66.8 ^(0.7) /99.3 ^(0.1) 67.0 ^(1.3) /99.4 ^(0.1) ChEMBL ChEMBL	Molecule 94.8 ^(10.1) /12.2 ^(7.3) 88.4 ^(11.7) /17.4 ^(4.1) 117 ^(5.5) /17.8 ^(8.1) 94.8 ^(10.1) /12.2 ^(7.3) 117 ^(6.5) /10.2 ^(4.4) 90.8 ^(3.9) /17.3 ^(9.8) 99.4 ^(15.0) /7.1 ^(8.0) 114 ^(7.0) /22.8 ^(11.9) Molecule 116 ^(3.1) /93.0 ^(0.5) 121 ^(0.0) /93.2 ^(0.4) 121 ^(0.0) /93.5 ^(0.6) 121 ^(0.0) /93.5 ^(0.4) 121 ^(0.0) /93.3 ^(0.4) 121 ^(0.0) /93.3 ^(0.4) 121 ^(0.0) /93.3 ^(0.4) 121 ^(0.0) /93.3 ^(0.4)	$\begin{tabular}{ c c c c c c } \hline Superconductor \\ \hline 37.0^{(4.1)}/0.0^{(0.0)} \\ \hline 28.6^{(5.5)}/0.0^{(0.0)} \\ \hline 28.0^{(7.8)}/34.3^{(13.5)} \\ \hline 37.0^{(4.1)}/0.0^{(0.0)} \\ \hline 38.0^{(8.1)}/0.0^{(0.0)} \\ \hline 30.6^{(4.5)}/0.0^{(0.0)} \\ \hline 30.6^{(4.5)}/0.0^{(0.0)} \\ \hline 31.0^{(4.1)}/0.0^{(0.0)} \\ \hline 40.6^{(8.6)}/74.4^{(46.3)} \\ \hline Superconductor \\ \hline 53.1^{(3.3)}/190^{(0.8)} \\ \hline 43.2^{(5.1)}/192^{(10.2)} \\ \hline 43.3^{(5.1)}/190^{(0.8)} \\ \hline 50.9^{(2.1)}/196^{(0.5)} \\ \hline 48.5^{(3.7)}/196^{(2.7)} \\ \hline 50.8^{(3.3)}/193^{(1.2)} \\ \hline 53.5^{(5.0)}/198^{(1.5)} \\ \hline \\ \hline Superconductor \\ \hline 51.3^{(3.6)}/198^{(1.0)} \\ \hline 47.7^{(3.5)}/198^{(1.6)} \\ \hline \end{tabular}$	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 62.7 ^(1.3) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0) 62.7 ^(1.3) /0.0 ^(0.0) 67.5 ^(1.4) /77.0 ^(35.9) D'Kitty 84.9 ^(1.1) /9.0 ^(2.8) 85.8 ^(0.7) /131 ^(15.9) 85.8 ^(1.3) /15 ^(15.3) 85.5 ^(1.1) /55.2 ^(36.3) 86.7 ^(1.1) /17.7 ^(3.5) 85.5 ^(1.1) /277 ^(59.7) D'Kitty 84.5 ^(0.8) /94.1 ^(3.9) 85.4 ^(1.8) /107 ^(5.5)	Rank ↓ 5.3/4.5 5.7/5.7 5.7/5.7 5.3/4.5 2.8/5.0 4.2/5.2 3.7/6.3 2.3/1.2 Rank ↓ 5.8/5.2 4.3/4.0 6.0/5.7 2.7/3.3 5.0/6.0 2.2/4.0 3.0/1.3 Rank ↓	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/-40.4 -0.6/-52.2 6.2/-52.0 3.1/-50.8 5.0/-53.6 12.3/-20.7 Opt. Gap ↑ 18.7/47.1 19.2/51.4 17.9/40.3 21.0/48.4 18.3/32.9 19.2/34.9 20.8/30.0 20.7/74.2 Opt. Gap ↑
	CoSyNE Baseline COMs ⁻ COMs ⁺ RoMA ⁺ ROMA ⁺ ROMO GAMBO DynAMO BO-qEI Baseline COMs ⁺ ROMA ⁺ ROMA ⁺ ROMA BO-qUCB Baseline	TFBind8 61.7 ^(10.0) /5.6 ^(5.0) 70.1 ^(12.8) /16.5 ^(8.5) 66.9 ^(5.1) /15.4 ^(4.9) 61.7 ^(10.0) /5.9 ^(5.2) 70.4 ^(7.2) /17.7 ^(5.5) 79.7 ^(12.7) /15.7 ^(10.1) 79.8 ^(10.6) /5.2 ^(5.7) 91.3 ^(4.4) /18.1 ^(13.0) TFBind8 87.3 ^(5.8) /73.7 ^(0.6) 93.2 ^(2.7) /73.7 ^(0.6) 93.2 ^(2.7) /73.7 ^(0.6) 93.2 ^(2.7) /73.7 ^(0.6) 93.8 ^(1.6) /73.8 ^(0.6) 94.1 ^(1.9) /74.0 ^(0.6) 91.9 ^(4.4) /74.8 ^(0.2) TFBind8 88.1 ^(5.3) /73.9 ^(0.5) 88.5 ^(6.4) /73.4 ^(0.6) 89.1 ^(7.1) /6.0 ^(0.8)	UTR 57.3 ^(9,6) /12.7 ^(9,8) 73.2 ^(8,9) /8.7 ^(10,2) 56.2 ^(9,5) /26.5 ^(6,8) 57.3 ^(9,6) /12.7 ^(9,9) 77.8 ^(4,4) /11.9 ^(4,0) 62.0 ^(9,8) /5.8 ^(4,6) 68.0 ^(12,5) /9.1 ^(9,0) 77.2 ^(11,6) /20.3 ^(2,3) UTR 86.2 ^(0,0) /74.3 ^(0,5) 86.3 ^(0,1) /74.3 ^(0,5) 86.3 ^(0,1) /74.3 ^(0,5) 86.3 ^(0,1) /74.3 ^(0,4) 86.3 ^(0,1) /74.3 ^(0,4) 86.2 ^(0,0) /74.3 ^(0,4) 86.2 ^(0,0) /74.3 ^(0,4) 86.2 ^(0,0) /74.2 ^(0,7) 85.9 ^(0,4) /74.2 ^(0,5)	ChEMBL 63.6 ^(0,4) /28.2 ^(11,3) 63.5 ^(0,4) /28.2 ^(11,3) 63.5 ^(0,4) /28.2 ^(11,3) 63.6 ^(0,4) /27.7 ^(10,9) 64.4 ^(25,7) /9.8 ^(3,9) 64.4 ^(1,1) /9.9 ^(3,0,1) 65.4 ^(1,1) /9.9 ^(3,0,1) 65.1 ^(0,8) /9.6 ^(0,2) 63.9 ^(0,8) /9.8 ^(0,2) 63.9 ^(0,8) /9.8 ^(0,2) 63.9 ^(0,8) /9.8 ^(0,2) 63.9 ^(0,8) /9.8 ^(1,6) 66.8 ^(0,7) /9.9 ^(0,1) 66.4 ^(0,7) /9.9 ^(0,1) 66.6 ^(1,1) /9.2 ^(0,1) 65.6 ^(1,1) /9.7 ^(1,0)	$\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$	$\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 70.6 ^(1.1) /16.6 ^(9.0) 62.7 ^(1.3) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0) 67.5 ^(1.4) /77.0 ^(35.9) D'Kitty 84.9 ^(1.1) /79.0 ^(2.8) 84.9 ^(1.1) /79.0 ^(2.8) 85.8 ^(0.7) /131 ^(15.9) 84.8 ^(1.3) /115 ^(15.3) 85.5 ^(1.7) /55.2 ^(36.3) 86.7 ^(1.1) /17.7 ^(3.5) 85.5 ^(1.1) /277 ^(59.7) D'Kitty 84.5 ^(0.8) /94.1 ^(3.9) 85.4 ^(1.8) /107 ^(5.5) 84.7 ^(1.6) /89.2 ^(14.0)	Rank \downarrow 5.3/4.5 5.7/5.7 5.7/5.7 5.3/4.5 2.8/5.0 4.2/5.2 3.7/6.3 2.3/1.2 Rank \downarrow 5.8/5.2 4.3/4.0 6.0/5.7 2.7/3.3 5.2/6.3 5.0/6.0 2.2/4.0 3.0/1.3 Rank \downarrow 3.7/3.0	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/-40.4 -0.6/-52.2 6.2/-52.0 3.1/-50.8 5.0/-53.6 12.3/-20.7 Opt. Gap ↑ 18.7/47.1 19.2/51.4 17.9/40.3 21.0/48.4 18.3/32.9 19.2/34.9 20.8/30.0 20.7/74.2 Opt. Gap ↑ 19.4/43.5
= -	CoSyNE Baseline COMs ⁻ COMs ⁺ RoMA ⁺ ROMA ⁺ ROMO GAMBO DynAMO BO-qEI Baseline COMs ⁺ ROMA ⁺ ROMA ⁺ ROMA ⁺ ROMA ⁺ ROMA ⁺ ROMA BO-qUCB Baseline COMs ⁻	TFBind8 61.7 ^(10.0) /5.6 ^(5.0) 70.1 ^(12.8) /16.5 ^(8.5) 66.9 ^(5.1) /15.4 ^(4.9) 61.7 ^(10.0) /5.9 ^(5.2) 70.4 ^(7.2) /17.7 ^(5.5) 79.7 ^(12.7) /15.7 ^(10.1) 79.8 ^(10.6) /5.2 ^(5.7) 91.3 ^(4.4) /18.1 ^(13.0) TFBind8 87.3 ^(5.8) /73.7 ^(0.6) 93.2 ^(2.7) /73.7 ^(0.6) 93.2 ^(2.7) /73.7 ^(0.6) 93.2 ^(2.7) /73.7 ^(0.6) 93.8 ^(1.6) /73.7 ^(0.6) 93.8 ^(1.6) /73.8 ^(0.6) 94.1 ^(1.9) /74.0 ^(0.6) 94.1 ^(1.9) /74.0 ^(0.6) 94.1 ^(5.3) /73.9 ^(0.5) 88.5 ^(6.4) /73.4 ^(0.6) 89.1 ^(7.1) /69.0 ^(0.8) 86.9 ^(5.0) /73.9 ^(0.5)	UTR 57.3 ^(9,6) /12.7 ^(9,8) 73.2 ^(8,9) /8.7 ^(10,2) 56.2 ^(9,5) /26.5 ^(6,8) 57.3 ^(9,6) /12.7 ^(9,9) 77.8 ^(4,4) /11.9 ^(4,0) 62.0 ^(9,8) /5.8 ^(4,6) 68.0 ^(12,5) /9.1 ^(9,0) 77.2 ^(11,6) /20.3 ^(2,3) UTR 86.2 ^(0,0) /74.3 ^(0,5) 86.3 ^(0,1) /74.3 ^(0,5) 86.3 ^(0,1) /74.3 ^(0,5) 86.3 ^(0,1) /74.3 ^(0,5) 86.3 ^(0,1) /74.3 ^(0,4) 86.3 ^(0,1) /74.3 ^(0,4) 86.2 ^(0,0) /74.2 ^(0,7) 85.9 ^(0,4) /72.3 ^(0,5) 86.2 ^(0,1) /74.2 ^(0,5) 86.2 ^(0,1) /74.4 ^(0,4)	ChEMBL 63.6 ^(0,4) /28.2 ^(11,3) 63.5 ^(0,4) /19.3 ^(14,1) 63.3 ^(0,0) /18.5 ^(7,0) 63.6 ^(0,4) /27.7 ^(10,9) 64.4 ^(2,5) /19.8 ^(3,9) 64.4 ^(2,6) /27.6 ^(12,4) 64.2 ^(0,9) /28.4 ^(15,7) 63.9 ^(0,9) /35.0 ^(17,9) 65.4 ^(1,1) /99.3 ^(0,1) 66.4 ^(0,4) /99.3 ^(0,1) 66.4 ^(0,4) /99.3 ^(0,1) 66.4 ^(0,4) /99.3 ^(0,1) 66.6 ^(0,9) /98.6 ^(0,2) 63.9 ^(1,1) /99.3 ^(0,1) 66.6 ^(0,9) /98.6 ^(0,2) 63.9 ^(1,1) /99.3 ^(0,1) 66.6 ^(0,7) /99.3 ^(0,1) 66.8 ^(0,7) /99.3 ^(0,1) 67.0 ^(1,3) /99.4 ^(0,1) 66.6 ^(1,1) /99.2 ^(0,1) 65.6 ^(1,1) /97.1 ^(0,9) 66.4 ^(0,7) /99.4 ^(0,0)	$\begin{tabular}{ c c c c c c c c c c c c c c c c c c c$	Superconductor 37.0 ^(4.1) /0.0 ^(0.0) 28.6 ^(5.5) /0.0 ^(0.0) 28.0 ^(7.8) /34.3 ^(13.5) 37.0 ^(4.1) /0.0 ^(0.0) 38.0 ^(8.1) /0.0 ^(0.0) 30.6 ^(4.5) /0.0 ^(0.0) 37.0 ^(4.1) /0.0 ^(0.0) 40.6 ^(8.6) /74.4 ^(46.3) Superconductor 53.1 ^(3.3) /190 ^(0.8) 43.2 ^(5.1) /192 ^(10.2) 47.3 ^(4.1) /206 ^(1.2) 53.1 ^(3.3) /190 ^(0.3) 50.9 ^(2.1) /196 ^(0.5) 48.5 ^(3.7) /196 ^(2.7) 50.8 ^(3.3) /193 ^(1.2) 53.5 ^(5.0) /198 ^(1.5) 45.7 ^(3.5) /198 ^(1.6) 45.7 ^(3.7) /261 ^(5.0) 51.3 ^(3.6) /198 ^(1.6)	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 70.6 ^(1.1) /16.6 ^(9.0) 62.7 ^(1.3) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0) 62.7 ^(1.3) /0.0 ^(0.0) 67.5 ^(1.4) /77.0 ^(35.9) D'Kitty 84.4 ^(0.9) /124 ^(7.4) 86.2 ^(0.9) /147 ^(8.9) 84.9 ^(1.1) /79.0 ^(2.8) 85.8 ^(0.7) /131 ^(15.9) 84.8 ^(1.3) /15 ^(5.5) 85.5 ^(1.1) /55.2 ^(36.3) 86.7 ^(1.1) /17.7 ^(3.5) 85.5 ^(1.1) /277 ^(59.7) D'Kitty 84.5 ^(0.8) /94.1 ^(3.9) 84.7 ^(1.6) /99.2 ^(14.0) 84.5 ^(0.8) /94.1 ^(3.9)	Rank \downarrow 5.3/4.5 5.7/5.7 5.7/5.7 5.3/4.5 2.8/5.0 4.2/5.2 3.7/6.3 2.3/1.2 Rank \downarrow 5.8/5.2 4.3/4.0 6.0/5.7 2.7/3.3 5.2/6.3 5.0/6.0 3.0/1.3 Rank \downarrow 3.7/3.0 4.5/4.5	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/-40.4 -0.6/-52.2 6.2/-52.0 3.1/-50.8 5.0/-53.6 12.3/-20.7 Opt. Gap ↑ 18.7/47.1 19.2/51.4 17.9/40.3 21.0/48.4 18.3/32.9 19.2/34.9 20.8/30.0 20.7/74.2 Opt. Gap ↑ 19.4/43.5 19.0/45.5 18.6/51.3 19.2/43.6
	CoSyNE Baseline COMs ⁻ COMs ⁺ RoMA ⁺ ROMO GAMBO DynAMO BO-qEI Baseline COMs ⁺ ROMA ⁻ ROMA ⁺ ROMO GAMBO DynAMO BO-qUCB Baseline COMs ⁻ COMs ⁺ ROMA ⁻ ROMA ⁺ ROMA ⁻ ROMA ⁺ ROMA ⁺	TFBind8 61.7 ^(10.0) /5.6 ^(5.0) 70.1 ^(12.8) /16.5 ^(8.5) 66.9 ^(5.1) /15.4 ^(4.9) 61.7 ^(10.0) /5.9 ^(5.5) 79.7 ^(12.7) /17.7 ^(5.5) 79.7 ^(12.7) /15.7 ^(10.1) 79.8 ^(10.6) /5.2 ^(5.7) 91.3 ^(4.4) /18.1 ^(13.0) TFBind8 87.3 ^(5.8) /73.7 ^(0.6) 93.2 ^(2.7) /73.7 ^(0.6) 93.2 ^(1.6) /73.7 ^(0.6) 93.8 ^(1.6) /73.8 ^(0.6) 94.1 ^(1.9) /74.0 ^(0.6) 91.9 ^(4.4) /74.8 ^(0.2) TFBind8 88.1 ^(5.3) /73.9 ^(0.5) 88.5 ^(6.4) /73.4 ^(0.6) 89.1 ^(7.1) /69.0 ^(0.3) 86.9 ^(5.0) /73.9 ^(0.5) 84.6 ^(5.9) /68.2 ^(2.2)	UTR 57.3 ^(9,6) /12.7 ^(9,8) 73.2 ^(8,9) /8.7 ^(10,2) 56.2 ^(9,5) /26.5 ^(6,8) 57.3 ^(9,6) /12.7 ^(9,9) 77.8 ^(4,4) /11.9 ^(4,0) 62.0 ^(9,8) /5.8 ^(4,6) 68.0 ^(12,5) /9.1 ^(9,0) 77.2 ^(11,6) /20.3 ^(2,3) UTR 86.2 ^(0,0) /74.3 ^(0,5) 86.3 ^(0,1) /74.3 ^(0,5) 86.3 ^(0,1) /74.3 ^(0,5) 86.3 ^(0,1) /74.3 ^(0,5) 86.3 ^(0,1) /74.3 ^(0,4) 86.3 ^(0,1) /68.7 ^(1,6) 86.3 ^(0,2) /74.3 ^(0,4) 86.2 ^(0,0) /74.3 ^(0,4) 86.2 ^(0,1) /74.3 ^(0,4) 86.2 ⁽¹⁾ /74.3 ^(0,4) 86.2 ⁽¹⁾ /74.3 ^(0,4) 86.2 ⁽¹⁾ /74.3 ⁽¹⁾ /74.3 ⁽¹⁾ 86.3 ⁽¹⁾ /74.3 ⁽¹⁾ /74.3 ⁽¹⁾ /74.3 ⁽¹⁾ 87.3 ⁽¹⁾ /74.3 ⁽¹⁾ /74.	ChEMBL 63.6 ^(0,4) /28.2 ^(11,3) 63.5 ^(0,4) /19.3 ^(14,1) 63.3 ^(0,0) /18.5 ^(7,0) 63.6 ^(0,4) /27.7 ⁽¹⁰⁾ 64.4 ^(2,5) /19.8 ^(3,9) 64.1 ^(0,6) /27.6 ^(12,4) 64.2 ^(0,9) /28.4 ^(15,7) 63.9 ^(0,9) /35.0 ^(17,9) ChEMBL 65.4 ^(1,0) /99.3 ^(0,1) 66.4 ^(0,4) /99.3 ^(0,1) 66.4 ^(0,9) /98.6 ^(0,2) 63.9 ^(0,8) /94.8 ^(1,6) 66.8 ^(0,7) /99.3 ^(0,1) 66.6 ^(0,7) /99.3 ^(0,1) 67.0 ^(1,3) /99.4 ^(0,1) 65.6 ^(1,1) /99.2 ^(0,1) 65.6 ^(1,1) /99.2 ^(0,1) 65.6 ^(1,1) /97.1 ^(0,9) 66.4 ^(0,7) /99.4 ^(0,1) 65.6 ^(1,1) /97.1 ^(0,9) 66.4 ^(0,7) /99.4 ^(0,0) 66.9 ^(1,0) /98.3 ^(0,3)	Molecule 94.8 ^(10.1) /12.2 ^(7.3) 88.4 ^(11.7) /17.4 ^(4.1) 117 ^(3.6) /17.8 ^(8.1) 94.8 ^(10.1) /12.2 ^(7.3) 117 ^(6.5) /10.2 ^(4.4) 90.8 ^(3.9) /17.3 ^(9.8) 99.4 ^(15.0) /7.1 ^(8.0) 114 ^(7.0) /22.8 ^(11.9) 114 ^(7.0) /22.8 ^(11.9) 114 ^(7.0) /93.2 ^(0.4) 121 ^(0.0) /93.2 ^(0.4) 121 ^(0.0) /93.5 ^(0.6) 121 ^(0.0) /93.5 ^(0.4) 121 ^(0.0) /93.5 ^(0.4) 121 ^(0.0) /93.3 ^(0.4)	Superconductor 37.0 ^(4.1) /0.0 ^(0.0) 28.6 ^(5.5) /0.0 ^(0.0) 28.0 ^(7.8) /34.3 ^(13.5) 37.0 ^(4.1) /0.0 ^(0.0) 30.6 ^(4.5) /0.0 ^(0.0) 30.6 ^(4.5) /0.0 ^(0.0) 37.0 ^(4.1) /0.0 ^(0.0) 40.6 ^(8.6) /74.4 ^(46.3) Superconductor 53.1 ^(3.3) /190 ^(0.8) 43.2 ^(5.1) /192 ^(10.2) 47.3 ^(4.1) /206 ^(1.2) 53.1 ^(3.3) /190 ^(0.8) 43.2 ^(5.1) /192 ^(10.2) 47.3 ^(4.1) /206 ^(1.2) 50.9 ^(2.1) /196 ^(0.5) 48.5 ^(3.7) /196 ^(2.7) 50.8 ^(3.3) /193 ^(1.2) 53.5 ^(5.0) /198 ^(1.5) Superconductor 51.3 ^(3.6) /198 ^(10.3) 45.7 ^(3.7) /261 ^(60.0) 51.3 ^(3.6) /198 ^(10.3) 52.1 ^(3.2) /194 ^(0.8)	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 70.6 ^(1.1) /16.6 ^(9.0) 62.7 ^(1.3) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0) 62.7 ^(1.3) /0.0 ^(0.0) 67.5 ^(1.4) /77.0 ^(35.9) D'Kitty 84.4 ^(0.9) /124 ^(7.4) 86.2 ^(0.9) /147 ^(8.9) 84.9 ^(1.1) /79.0 ^(2.8) 85.8 ^(0.7) /131 ^(15.9) 84.8 ^(1.3) /15 ^(15.3) 85.5 ^(1.7) /55.2 ^(36.3) 86.7 ^(1.1) /17.7 ^(3.5) 85.5 ^(1.1) /277 ^(59.7) D'Kitty 84.5 ^(0.8) /94.1 ^(3.9) 84.5 ^(0.8) /94.1 ^(3.9) 84.5 ^(0.8) /94.1 ^(3.9) 84.5 ^(0.8) /94.1 ^(3.9) 84.5 ^(0.8) /94.1 ^(3.9) 82.9 ^(1.2) /109 ^(8.3)	Rank \downarrow 5.3/4.5 5.7/5.7 5.7/5.7 5.7/5.7 5.3/4.5 5.7/5.7 5.3/4.5 5.3/4.5 5.3/4.5 2.8/5.0 4.2/5.2 3.7/6.3 2.3/1.2 Rank \downarrow 5.8/5.2 4.3/4.0 6.0/5.7 2.7/3.3 5.2/6.3 5.0/6.0 2.2/4.0 3.0/1.3 Rank \downarrow 3.7/3.0 4.5/4.5 5.2/5.7 3.8/3.0 4.7/6.5	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/-40.4 -0.6/-52.2 6.2/-52.0 3.1/-50.8 5.0/-53.6 12.3/-20.7 Opt. Gap ↑ 18.7/47.1 19.2/51.4 17.9/40.3 21.0/48.4 18.3/32.9 19.2/34.9 20.8/30.0 20.7/74.2 Opt. Gap ↑ 19.4/43.5 19.0/45.5 18.6/51.3 19.2/34.6 18.5/39.9
	CoSyNE Baseline COMs ⁻ COMs ⁺ RoMA ⁺ ROMO GAMBO DynAMO BO-qEI Baseline COMs ⁺ ROMA ⁺ ROMA ⁺ ROMO GAMBO DynAMO BO-qUCB Baseline COMs ⁻ ROMA ⁺ ROMO BO-qUCB	TFBind8 61.7 ^(10.0) /5.6 ^(5.0) 70.1 ^(12.8) /16.5 ^(8.5) 66.9 ^(5.1) /15.4 ^(4.9) 61.7 ^(10.0) /5.9 ^(5.2) 70.4 ^(7.2) /17.7 ^(5.5) 79.7 ^(12.7) /15.7 ^(10.1) 79.8 ^(10.6) /5.2 ^(5.7) 91.3 ^(4.4) /18.1 ^(13.0) TFBind8 87.3 ^(5.8) /73.7 ^(0.6) 93.2 ^(2.7) /73.8 ^(0.6) 94.1 ^(1.9) /74.0 ^(0.6) 94.1 ^(1.9) /74.0 ^(0.6) 94.1 ^(1.9) /74.0 ^(0.6) 94.1 ^(1.9) /73.9 ^(0.5) 88.5 ^(6.4) /73.9 ^(0.5) 84.6 ^(5.9) /68.2 ^(2.2) 95.2 ^(2.5) /74.0 ^(0.5)	UTR 57.3 ^(9,6) /12.7 ^(9,8) 73.2 ^(8,9) /8.7 ^(10,2) 56.2 ^(9,5) /26.5 ^(6,8) 57.3 ^(9,6) /12.7 ^(9,9) 77.8 ^(4,4) /11.9 ^(4,0) 62.0 ^(9,5) /9.1 ^(9,0) 77.2 ^(11,6) /20.3 ^(2,3) T7.2 ^(11,6) /20.3 ^(2,3) 86.2 ^(0,0) /74.8 ^(0,5) 86.2 ^(0,0) /74.8 ^(0,5) 86.3 ^(0,1) /74.1 ^(0,3) 84.1 ^(1,0) /64.2 ^(1,0) 86.3 ^(0,1) /64.7 ^(1,6) 86.3 ^(0,1) /74.3 ^(0,4) 86.2 ^(0,0) /74.3 ^(0,4) 86.2 ^(0,0) /74.3 ^(0,4) 86.2 ^(0,1) /74.	ChEMBL 63.6 ^(0,4) /28.2 ^(11,3) 63.5 ^(0,4) /19.3 ^(14,1) 63.3 ^(0,0) /18.5 ^(7,0) 63.6 ^(0,4) /27.7 ^(10,9) 64.1 ^(0,6) /27.6 ^(12,4) 64.1 ^(0,6) /27.6 ^(12,4) 64.2 ^(0,0) /28.4 ^(15,7) 63.9 ^(0,9) /35.0 ^(17,9) ChEMBL 65.4 ^(1,0) /99.3 ^(0,1) 66.4 ^(0,4) /99.3 ^(0,1) 66.4 ^(0,4) /99.3 ^(0,1) 66.6 ^(0,9) /98.6 ^(0,2) 63.9 ^(0,8) /94.8 ^(1,6) 66.8 ^(0,7) /99.3 ^(0,1) 66.4 ^(0,7) /99.4 ^(0,1) 66.4 ^(0,7) /99.4 ^(0,1) 66.4 ^(0,7) /99.4 ^(0,1) 66.4 ^(0,7) /99.4 ^(0,1) 66.9 ^(1,0) /98.3 ^(0,3) 64.7 ^(1,0) /94.9 ^(1,3)	Molecule 94.8 ^(10.1) /12.2 ^(7.3) 88.4 ^(11.7) /17.4 ^(4.1) 117 ^(3.6) /17.8 ^(8.1) 94.8 ^(10.1) /12.2 ^(7.3) 117 ^(6.5) /10.2 ^(4.4) 90.8 ^(13.0) /17.3 ^(9.8) 99.4 ^(15.0) /7.1 ^(8.0) 114 ^(7.0) /22.8 ^(11.9) 114 ^(7.0) /22.8 ^(11.9) 116 ^(3.1) /93.2 ^(0.4) 121 ^(0.0) /93.5 ^(0.6) 121 ^(0.0) /93.5 ^(0.6) 121 ^(0.0) /93.5 ^(0.4) 121 ^(0.0) /93.5 ^(0.4) 121 ^(0.0) /93.5 ^(0.4) 121 ^(0.0) /93.3 ^(0.4) 121 ^(0.2) /78.3 ^(4.5) 121 ^(0.2) /78.3 ^(4.5) 121 ^(0.2) /78.3 ^(4.5)	Superconductor 37.0 ^(4.1) /0.0 ^(0.0) 28.6 ^(5.5) /0.0 ^(0.0) 28.0 ^(7.8) /34.3 ^(13.5) 37.0 ^(4.1) /0.0 ^(0.0) 30.6 ^(4.5) /0.0 ^(0.0) 37.0 ^(4.1) /0.0 ^(0.0) 40.6 ^(8.6) /74.4 ^(46.3) Superconductor 53.1 ^(3.3) /190 ^(0.8) 43.2 ^(5.1) /192 ^(10.2) 47.3 ^(4.1) /206 ^(1.2) 50.9 ^(2.1) /196 ^(0.5) 48.5 ^(3.7) /196 ^(2.7) 50.8 ^(3.3) /193 ^(1.2) 53.5 ^(5.0) /198 ^(1.0) 51.3 ^(3.6) /198 ^(1.6) 47.7 ^(3.5) /198 ^(1.6) 45.7 ^(3.7) /198 ^(1.6) 45.7 ^(3.7) /198 ^(1.6) 51.3 ^(3.6) /194 ^(0.8) 50.2 ^(4.7) /197 ^(1.3)	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 70.6 ^(1.1) /16.6 ^(9.0) 62.7 ^(1.3) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0) 72.1 ^(1.1) /0.1 ^(0.2) 62.7 ^(1.3) /0.0 ^(0.0) 67.5 ^(1.4) /77.0 ^(35.9) 7.5 ^(1.4) /77.0 ^(35.9) 84.4 ^(0.9) /124 ^(7.4) 86.2 ^(0.9) /147 ^(8.9) 84.9 ^(1.1) /79.0 ^(2.8) 85.8 ^(0.7) /131 ^(15.9) 84.8 ^(1.3) /115 ^(15.3) 85.5 ^(1.1) /55.2 ^(36.3) 86.7 ^(1.1) /17.7 ^(3.5) 85.5 ^(1.1) /277 ^(55.7) 7.1 ^(1.6) /89.2 ^(14.0) 84.5 ^(0.8) /94.1 ^(3.9) 85.5 ^(1.1) /107 ^(6.5) 84.7 ^(1.6) /89.2 ^(14.0) 85.5 ^(1.1) /107 ^(6.3) 85.5 ^(1.1) /109 ^(6.3)	Rank \downarrow 5.3/4.5 5.7/5.7 5.7/5.7 5.7/5.7 5.7/5.7 5.7/5.7 5.7/5.7 5.7/5.7 5.7/5.7 5.7/5.7 5.7/5.7 5.7/5.7 5.7/5.7 5.7/5.7 5.3/4.5 2.3/7/6.3 2.3/7/6.3 2.3/1.2 Rank \downarrow 5.8/5.2 4.3/4.0 6.0/5.7 2.7/3.3 5.2/6.3 5.0/6.0 2.2/4.0 3.0/1.3 Rank \downarrow 3.7/3.0 4.5/4.5 5.2/5.7 3.8/3.0 4.7/6.5 4.7/6.5	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/-40.4 -0.6/-52.2 6.2/-52.0 3.1/-50.8 5.0/-53.6 12.3/-20.7 Opt. Gap ↑ 18.7/47.1 19.2/51.4 17.9/40.3 21.0/48.4 18.3/32.9 19.2/34.9 20.8/30.0 20.7/74.2 Opt. Gap ↑ 19.4/43.5 19.0/45.5 18.6/51.3 19.2/43.6 18.5/39.9 19.9/33.2
1	CoSyNE Baseline COMs ⁻ COMs ⁺ RoMA ⁺ ROMO GAMBO DynAMO BO-qEI Baseline COMs ⁻ ROMA ⁺ ROMA ⁺ ROMO GAMBO DynAMO BO-qUCB Baseline COMs ⁺ ROMA ⁻ ROMA ⁻ ROMA ⁻ ROMA ⁻	TFBind8 61.7 ^(10.0) /5.6 ^(5.0) 70.1 ^(12.8) /16.5 ^(8.5) 66.9 ^(5.1) /15.4 ^(4.9) 61.7 ^(10.0) /5.9 ^(5.2) 79.7 ^(12.7) /15.7 ^(10.1) 79.8 ^(10.6) /5.2 ^(5.7) 91.3 ^(4.4) /18.1 ^(13.0) TFBind8 87.3 ^(5.8) /73.7 ^(0.6) 93.2 ^(2.7) /73.8 ^(0.6) 93.8 ^(1.6) /73.8 ^(0.6) 94.1 ^(1.9) /74.0 ^(0.6) 91.9 ^(4.4) /74.8 ^(0.2) TFBind8 88.5 ^(6.4) /73.4 ^(0.6) 89.1 ^(7.1) /69.0 ^(0.5) 84.6 ^(5.5) /73.9 ^(0.5) 84.6 ^(5.5) /73.9 ^(0.5) 84.6 ^(5.5) /74.0 ^(0.5) 95.4 ^(1.6) /74.0 ^(0.5)	UTR 57.3 ^(9,6) /12.7 ^(9,8) 73.2 ^(8,9) /8.7 ^(10,2) 56.2 ^(9,5) /26.5 ^(6,8) 57.3 ^(9,6) /12.7 ^(9,9) 77.8 ^(4,4) /11.9 ^(4,0) 62.0 ^(9,8) /5.8 ^(4,6) 68.0 ^(12,5) /9.1 ^(9,0) 77.2 ^(11,6) /20.3 ^(2,3) UTR 86.2 ^(0,0) /74.8 ^(0,5) 86.2 ^(0,0) /74.3 ^(0,5) 86.3 ^(0,1) /74.1 ^(0,3) 84.1 ^(1,0) /64.2 ^(1,0) 86.3 ^(0,1) /74.3 ^(0,4) 86.2 ^(0,0) /74.3 ^(0,4) 86.2 ^(0,1) /74.3 ^(0,2) 86.2 ^(0,1) /74.3 ^(0,2) 86.2 ^(0,1) /74.3 ^(0,2) 86.2 ^(0,1) /74.3 ^(0,2) 86.2 ^(0,1) /74.3 ^(0,2)	ChEMBL 63.6 ^(0,4) /28.2 ^(11,3) 63.5 ^(0,4) /19.3 ^(14,1) 63.3 ^(0,0) /18.5 ^(7,0) 63.6 ^(0,4) /27.7 ^(10,9) 64.1 ^(0,6) /27.6 ^(12,4) 64.1 ^(0,6) /27.6 ^(12,4) 64.2 ^(0,0) /28.4 ^(15,7) 63.9 ^(0,9) /35.0 ^(17,9) ChEMBL 65.4 ^(1,0) /99.3 ^(0,1) 66.4 ^(0,4) /99.3 ^(0,1) 66.4 ^(0,4) /99.3 ^(0,1) 66.6 ^(0,9) /98.6 ^(0,2) 63.9 ^(0,8) /94.8 ^(1,6) 66.8 ^(0,7) /99.3 ^(0,1) 66.4 ^(0,7) /99.4 ^(0,1) 66.4 ^(0,7) /99.4 ^(0,1) 66.4 ^(0,7) /99.4 ^(0,1) 66.4 ^(0,7) /99.4 ^(0,1) 66.4 ^(1,0) /98.3 ^(0,3) 64.7 ^(1,0) /94.9 ^(1,3) 66.3 ^(1,1) /99.3 ^(0,1)	Molecule 94.8 ^(10.1) /12.2 ^(7.3) 88.4 ^(11.7) /17.4 ^(4.1) 117 ^(3.6) /17.8 ^(8.1) 94.8 ^(10.1) /12.2 ^(7.3) 117 ^(6.5) /10.2 ^(4.4) 90.8 ^(13.9) /17.3 ^(9.8) 99.4 ^(15.0) /7.1 ^(8.0) 114 ^(7.0) /22.8 ^(11.9) 114 ^(7.0) /22.8 ^(11.9) 114 ^(7.0) /93.2 ^(0.4) 121 ^(0.0) /93.5 ^(0.6) 121 ^(0.0) /93.5 ^(0.6) 121 ^(0.0) /93.5 ^(0.4) 121 ^(0.0) /93.5 ^(0.4) 121 ^(0.0) /93.3 ^(0.4) 121 ^(0.2) /78.3 ^(4.5) 121 ^(0.2) /78.3 ^(4.5) 121 ^(0.2) /78.3 ^(4.5) 121 ^(0.2) /78.3 ^(4.5) 121 ^(0.1) /92.4 ^(1.0) 121 ^(1.3) /93.4 ^(0.4)	Superconductor 37.0 ^(4.1) /0.0 ^(0.0) 28.6 ^(5.5) /0.0 ^(0.0) 28.0 ^(7.8) /34.3 ^(13.5) 37.0 ^(4.1) /0.0 ^(0.0) 30.6 ^(4.5) /0.0 ^(0.0) 37.0 ^(4.1) /0.0 ^(0.0) 40.6 ^(8.6) /74.4 ^(46.3) Superconductor 53.1 ^(3.3) /190 ^(0.8) 43.2 ^(5.1) /192 ^(10.2) 47.3 ^(4.1) /206 ^(1.2) 53.1 ^(3.3) /190 ^(0.8) 43.2 ^(5.1) /192 ^(10.2) 47.3 ^(4.1) /206 ^(1.2) 50.9 ^(2.1) /196 ^(0.5) 48.5 ^(3.7) /196 ^(2.7) 50.8 ^(3.3) /193 ^(1.2) 53.5 ^(5.0) /198 ^(1.0) 51.3 ^(3.6) /198 ^(1.0) 47.7 ^(3.5) /198 ^(1.0) 51.3 ^(3.6) /198 ^(1.0) 51.2 ^(3.6) /194 ^(0.8) 50.2 ^(4.7) /197 ^(1.3) 50.2 ^(2.8) /199 ^(9.3)	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 70.6 ^(1.1) /16.6 ^(9.0) 62.7 ^(1.3) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0) 62.7 ^(1.3) /0.0 ^(0.0) 67.5 ^(1.4) /77.0 ^(35.9) 72.1 ^(1.1) /0.1 ^(0.2) 67.5 ^(1.4) /77.0 ^(35.9) 72.1 ^(1.1) /0.1 ^(0.2) 84.9 ^(1.1) /77.0 ^(35.9) 84.9 ^(1.1) /79.0 ^(2.8) 85.8 ^(0.7) /131 ^(15.9) 84.8 ^(1.3) /115 ^(15.3) 85.5 ^(1.1) /27.5 ^(36.3) 86.7 ^(1.1) /17.7 ^(3.5) 85.5 ^(1.1) /17.7 ^(3.5) 85.5 ^(1.1) /277 ^(55.7) 7 ^(1.6) /89.2 ^(14.0) 84.5 ^(0.8) /94.1 ^(3.9) 82.9 ^(1.2) /109 ^(8.3) 85.5 ^(1.1) /107 ^(5.5) 81.7 ^(1.6) /89.2 ^(14.0) 84.5 ^(1.6) /109 ^(8.3) 85.5 ^(1.1) /107 ^(5.5) 83.6 ^(1.0) /22.0 ^(2.1)	Rank \downarrow 5.3/4.5 5.7/5.7 5.7/5.7 5.7/5.7 5.3/4.5 2.8/5.0 4.2/5.2 3.7/6.3 2.3/1.2 Rank \downarrow 5.8/5.2 4.3/4.0 6.0/5.7 2.7/3.3 5.2/6.3 5.0/6.0 2.2/4.0 3.0/1.3 Rank \downarrow 3.7/3.0 4.5/4.5 5.2/5.7 3.8/3.0 4.7/6.5 4.7/6.5 4.7/6.5 4.7/6.5	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/-40.4 -0.6/-52.2 6.2/-52.0 3.1/-50.8 5.0/-53.6 12.3/-20.7 Opt. Gap ↑ 18.7/47.1 19.2/51.4 17.9/40.3 21.0/48.4 18.3/32.9 19.2/34.9 20.8/30.0 20.7/74.2 Opt. Gap ↑ 19.4/43.5 19.0/45.5 18.6/51.3 19.2/43.6 18.5/39.9 19.9/33.2 20.2/30.3
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	CoSyNE Baseline COMs ⁻ COMs ⁺ RoMA ⁺ ROMO GAMBO DynAMO BO-qEI Baseline COMs ⁺ ROMA ⁺ ROMA ⁺ ROMO GAMBO DynAMO BO-qUCB Baseline COMs ⁻ ROMA ⁺ ROMO BO-qUCB	TFBind8 61.7 ^(10.0) /5.6 ^(5.0) 70.1 ^(12.8) /16.5 ^(8.5) 66.9 ^(5.1) /15.4 ^(4.9) 61.7 ^(10.0) /5.9 ^(5.2) 70.4 ^(7.2) /17.7 ^(5.5) 79.7 ^(12.7) /15.7 ^(10.1) 79.8 ^(10.6) /5.2 ^(5.7) 91.3 ^(4.4) /18.1 ^(13.0) TFBind8 87.3 ^(5.8) /73.7 ^(0.6) 93.2 ^(2.7) /73.8 ^(0.6) 94.1 ^(1.9) /74.0 ^(0.6) 94.1 ^(1.9) /74.0 ^(0.6) 94.1 ^(1.9) /74.0 ^(0.6) 94.1 ^(1.9) /73.9 ^(0.5) 88.5 ^(6.4) /73.9 ^(0.5) 84.6 ^(5.9) /68.2 ^(2.2) 95.2 ^(2.5) /74.0 ^(0.5)	UTR 57.3 ^(9,6) /12.7 ^(9,8) 73.2 ^(8,9) /8.7 ^(10,2) 56.2 ^(9,5) /26.5 ^(6,8) 57.3 ^(9,6) /12.7 ^(9,9) 77.8 ^(4,4) /11.9 ^(4,0) 62.0 ^(9,5) /9.1 ^(9,0) 77.2 ^(11,6) /20.3 ^(2,3) T7.2 ^(11,6) /20.3 ^(2,3) 86.2 ^(0,0) /74.8 ^(0,5) 86.2 ^(0,0) /74.8 ^(0,5) 86.3 ^(0,1) /74.1 ^(0,3) 84.1 ^(1,0) /64.2 ^(1,0) 86.3 ^(0,1) /64.7 ^(1,6) 86.3 ^(0,1) /74.3 ^(0,4) 86.2 ^(0,0) /74.3 ^(0,4) 86.2 ^(0,0) /74.3 ^(0,4) 86.2 ^(0,1) /74.	ChEMBL 63.6 ^(0,4) /28.2 ^(11,3) 63.5 ^(0,4) /19.3 ^(14,1) 63.3 ^(0,0) /18.5 ^(7,0) 63.6 ^(0,4) /27.7 ^(10,9) 64.1 ^(0,6) /27.6 ^(12,4) 64.1 ^(0,6) /27.6 ^(12,4) 64.2 ^(0,0) /28.4 ^(15,7) 63.9 ^(0,9) /35.0 ^(17,9) ChEMBL 65.4 ^(1,0) /99.3 ^(0,1) 66.4 ^(0,4) /99.3 ^(0,1) 66.4 ^(0,4) /99.3 ^(0,1) 66.6 ^(0,9) /98.6 ^(0,2) 63.9 ^(0,8) /94.8 ^(1,6) 66.8 ^(0,7) /99.3 ^(0,1) 66.4 ^(0,7) /99.4 ^(0,1) 66.4 ^(0,7) /99.4 ^(0,1) 66.4 ^(0,7) /99.4 ^(0,1) 66.4 ^(0,7) /99.4 ^(0,1) 66.9 ^(1,0) /98.3 ^(0,3) 64.7 ^(1,0) /94.9 ^(1,3)	Molecule 94.8 ^(10.1) /12.2 ^(7.3) 88.4 ^(11.7) /17.4 ^(4.1) 117 ^(3.6) /17.8 ^(8.1) 94.8 ^(10.1) /12.2 ^(7.3) 117 ^(6.5) /10.2 ^(4.4) 90.8 ^(13.0) /17.3 ^(9.8) 99.4 ^(15.0) /7.1 ^(8.0) 114 ^(7.0) /22.8 ^(11.9) 114 ^(7.0) /22.8 ^(11.9) 116 ^(3.1) /93.2 ^(0.4) 121 ^(0.0) /93.5 ^(0.6) 121 ^(0.0) /93.5 ^(0.6) 121 ^(0.0) /93.5 ^(0.4) 121 ^(0.0) /93.5 ^(0.4) 121 ^(0.0) /93.5 ^(0.4) 121 ^(0.0) /93.3 ^(0.4) 121 ^(0.2) /78.3 ^(4.5) 121 ^(0.2) /78.3 ^(4.5) 121 ^(0.2) /78.3 ^(4.5)	Superconductor 37.0 ^(4.1) /0.0 ^(0.0) 28.6 ^(5.5) /0.0 ^(0.0) 28.0 ^(7.8) /34.3 ^(13.5) 37.0 ^(4.1) /0.0 ^(0.0) 30.6 ^(4.5) /0.0 ^(0.0) 37.0 ^(4.1) /0.0 ^(0.0) 40.6 ^(8.6) /74.4 ^(46.3) Superconductor 53.1 ^(3.3) /190 ^(0.8) 43.2 ^(5.1) /192 ^(10.2) 47.3 ^(4.1) /206 ^(1.2) 50.9 ^(2.1) /196 ^(0.5) 48.5 ^(3.7) /196 ^(2.7) 50.8 ^(3.3) /193 ^(1.2) 53.5 ^(5.0) /198 ^(1.0) 51.3 ^(3.6) /198 ^(1.6) 47.7 ^(3.5) /198 ^(1.6) 45.7 ^(3.7) /198 ^(1.6) 45.7 ^(3.7) /198 ^(1.6) 51.3 ^(3.6) /194 ^(0.8) 50.2 ^(4.7) /197 ^(1.3)	D'Kitty 62.7 ^(1.3) /0.0 ^(0.0) 63.8 ^(1.6) /0.0 ^(0.0) 70.6 ^(1.1) /16.6 ^(9.0) 62.7 ^(1.3) /0.0 ^(0.0) 50.7 ^(1.5) /0.0 ^(0.0) 72.1 ^(1.1) /0.1 ^(0.2) 62.7 ^(1.3) /0.0 ^(0.0) 67.5 ^(1.4) /77.0 ^(35.9) 7.5 ^(1.4) /77.0 ^(35.9) 84.4 ^(0.9) /124 ^(7.4) 86.2 ^(0.9) /147 ^(8.9) 84.9 ^(1.1) /79.0 ^(2.8) 85.8 ^(0.7) /131 ^(15.9) 84.8 ^(1.3) /115 ^(15.3) 85.5 ^(1.1) /55.2 ^(36.3) 86.7 ^(1.1) /17.7 ^(3.5) 85.5 ^(1.1) /277 ^(55.7) 84.5 ^(1.1) /17.7 ^(3.5) 85.5 ^(1.1) /277 ^(55.7) 84.5 ^(1.6) /94.1 ^(3.9) 85.9 ^(1.1) /107 ^(5.5) 84.7 ^(1.6) /89.2 ^(14.0) 84.5 ^(0.8) /94.1 ^(3.9) 85.5 ^(1.1) /109 ^(6.3) 85.5 ^(1.1) /109 ^(6.3)	Rank \downarrow 5.3/4.5 5.7/5.7 5.7/5.7 5.7/5.7 5.7/5.7 5.7/5.7 5.7/5.7 5.7/5.7 5.7/5.7 5.7/5.7 5.7/5.7 5.7/5.7 5.7/5.7 5.7/6.3 2.3/1.2 Rank \downarrow 5.8/5.2 4.3/4.0 6.0/5.7 2.7/3.3 5.2/6.3 5.0/6.0 2.2/4.0 3.0/1.3 Rank \downarrow 3.7/3.0 4.5/4.5 5.2/5.7 3.8/3.0 4.7/6.5 4.7/6.5	Opt. Gap ↑ -0.6/-52.1 1.1/-51.6 3.5/-40.4 -0.6/-52.2 6.2/-52.0 3.1/-50.8 5.0/-53.6 12.3/-20.7 Opt. Gap ↑ 18.7/47.1 19.2/51.4 17.9/40.3 21.0/48.4 18.3/32.9 19.2/34.9 20.8/30.0 20.7/74.2 Opt. Gap ↑ 19.4/43.5 19.0/45.5 18.6/51.3 19.2/43.6 18.5/39.9 19.9/33.2

Table A2. Additional Model-Based Optimization Quality Results. Each cell is the Median@128 oracle score (i.e., the median oracle score achieved by 128 sampled design candidates), reported as mean^(95% confidence interval) across 10 random seeds, where higher is better.
 Bolded entries indicate overlapping 95% confidence intervals with the best performing algorithm (according to the mean) per optimizer.
 Bolded (resp., <u>Underlined</u>) Rank and Optimality Gap metrics indicate the best (resp., second best) for a given backbone optimizer.

-									
	Grad.	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	$\mathbf{Rank}\downarrow$	Opt. Gap ↑
	Dataset \mathcal{D}	33.7	42.8	50.9	87.6	6.7	77.8	_/	_/
	Baseline	58.1 ^(6.1)	58.6(13.1)	59.3 ^(8.6)	85.3 ^(7.7)	36.0 ^(6.7)	65.1 ^(14.4)	4.3	10.5
	COMs ⁻	53.0 ^(8.5)	58 3 ^(13.2)	59.1 ^(8.6)	84.0 ^(7.2)	22 5(3.2)	71.0 ^(10.7)	5.8	8.1
	COMs ⁺	43 9 ^(0.0)	59 0 ^(0.5)	63 3 ^(0.0)	93 2 ^(7.7)	$21.3^{(5.6)}$	89.9 ^(1.0)	4.0	11.8
	RoMA ⁻	51.1 ^(6.1)	58 6 ^(13.1)	59 1 ^(8.6)	85.3 ^(7.7)	36 0 ^(6.7)	65.1 ^(14.4)	5.0	9.3
	RoMA ⁺	48.2 ^(4.3)	77.4 ^(0.0)	63.3 ^(0.0)	$84.5^{(0.0)}$	38.2 ^(0.8)	88.5 ^(0.1)	3.2	<u>16.8</u>
	ROMO	58.7 ^(3.3)	37 7 ^(0.3)	$27.4^{(1.2)}$	$61.8^{(2.6)}$	$2.7 0^{(0.6)}$	46.0 ^(11.7)	6.5	-6.8
	GAMBO	63.8 ^(13.7)	75.3 ^(9.9)	60.1 ^(3.3)	91.6 ^(11.2)	46.0 ^(6.7)	90.1 ^(14.4)	1.8	21.2
	DynAMO	47.0 ^(2.8)	69.8 ^(6.0)	61.9 ^(2.2)	85.9 ^(0.4)	23.4 ^(8.5)	68.7 ^(12.1)	4.5	9.5
	Adam	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	$\mathbf{Rank}\downarrow$	Opt. Gap ↑
	Baseline	54.7 ^(8.8)	60.4(12.7)	59.2 ^(8.6)	87.9 ^(10.0)	37.4(6.2)	56.8(19.8)	3.3	9.5
	COMs ⁻	54.8 ^(8.8)	59 5 ^(12.7)	59 2 ^(8.6)	90.8 ^(10.4)	$22.5^{(3.2)}$	57 1 ^(19.6)	4.0	7.4
	COMs ⁺	48.0 ^(1.7)	59 1 ^(0.5)	63.3 ^(0.0)	89.3 ^(10.4)	$233^{(3.7)}$	56 4 ^(13.3)	4.8	6.6
	RoMA ⁻	54.7 ^(8.8)	$60.4^{(12.7)}$	59.2 ^(8.6)	87.9 ^(10.0)	37.4 ^(6.2)	$56.8^{(19.8)}$	3.3	9.5
	RoMA ⁺	50.1 ^(4.3)	77.4 ^(0.0)	63.3 ^(0.0)	84.7 ^(0.0)	34.9 ^(1.8)	$63.7^{(6.2)}$	3.3	12.4
	ROMO	54.0 ^(0.0)	36.8 ^(0.1)	63.3 ^(0.0)	$50.5^{(0.3)}$	26.1 ^(0.5)	$30.9^{(0.0)}$	5.7	-6.3
	GAMBO	49.5 ^(8.9)	55.7 ^(12.7)	57.7 ^(9.1)	84.3 ^(9.6)	37.4(6.2)	87.8 ^(4.3)	5.0	12.1
	DynAMO	47.7 ^(3.0)	69.0 ^(5.2)	62.4 ^(1.9)	86.4 ^(0.6)	23.0 ^(6.0)	65.6 ^(14.1)	4.7	9.1
	CMA-ES	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	$\mathbf{Rank}\downarrow$	Opt. Gap ↑
	Baseline	50.7 ^(2.7)	71.7(10.4)	63.3 ^(0.0)	83.9(1.0)	37.9 ^(0.7)	59.3 ^(10.9)	3.2	11.2
	COMs ⁻	$45.0^{(2.2)}$	68.0 ^(8.6)	60.5 ^(3.0)	80 Q ^(10.8)	$18.8^{(7.9)}$	59.8 ^(9.9)	5.3	7.1
	COMs ⁺	44 3 ^(3.6)	$62.0^{(8.8)}$	59.7 ^(4.3)	91.6 ^(9.3)	$29.0^{(5.9)}$	61.2 ^(15.0)	5.0	8.0
	RoMA ⁻	50.7 ^(2.7)	71.7 ^(10.4)	63.3 ^(0.0)	$83.9^{(1.0)}$	37.9 ^(0.7)	59.3 ^(10.9)	3.2	11.2
	RoMA ⁺	47.4 ^(4.2)	58.0 ^(7.0)	59.9 ^(4.4)	91.6 ^(10.0)	31.6 ^(5.0)	60.4 ^(7.7)	4.5	8.2
	ROMO	48.9 ^(3.1)	74.0 ^(9.2)	60.0 ^(3.4)	$84.5^{(1.7)}$	22.8 ^(1.6)	61.6 ^(15.3)	3.5	8.7
	GAMBO	$44.2^{(0.8)}$	72.7 ^(3.8)	62.7 ^(1.1)	$86.1^{(0.5)}$	21.4 ^(2.0)	54 9 ^(9.6)	5.5	7.1
	DynAMO	45.3(2.4)	65.8 ^(8.9)	59.3 ^(3.8)	99.0 ^(12.1)	22.5 ^(5.1)	60.6 ^(15.0)	4.8	8.8
	CoSyNE	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	Rank↓	Opt. Gap ↑
	Baseline	55.3 ^(8.0)	53.6 ^(10.2)	60.8 ^(3.2)	87.4(16.6)	36.6 ^(4.4)	59.3 ^(14.5)	4.3	8.9
	COMs ⁻	51.7 ^(10.6)	70.9 ^(9.2)	62.8 ^(0.7)	83 1 ^(8.3)	28.3 ^(5.4)	58 Q ^(17.3)	5.3	9.3
	COMs ⁺	53 9 ^(2,4)	$41 \ 1^{(1.1)}$	63.3 ^(0.0)	107 ^(3.8)	$23.4^{(7.9)}$	$61.2^{(15.6)}$	4.2	8.4
	RoMA ⁻	55.3 ^(8.0)	53.6 ^(10.2)	60.8 ^(3.2)	$87 4^{(16.6)}$	36.6 ^(4.4)	59.3 ^(14.5)	4.3	8.9
	RoMA ⁺	60.2 ^(7.1)	67.7 ^(8.7)	60.2 ^(4.5)	103(11.2)	37.8 ^(8.1)	48.9 ^(13.9)	3.5	13.1
		re (12.0)	= (11.3)	62.1 ^(1.4)	88.4 ^(5.2)	a a (15)	70.7 ^(10.7)		
	ROMO	69.1 ^(12.9)	58.5(11.3)	62.1	88.4	29.9(4.3)	/0./	3.2	13.2
	GAMBO	69.1 ^(12.9) 59.5 ^(12.0)	58.5 ^(11.3) 63.5 ^(11.2)	55.4 ^(9.6)	$84.2^{(17.2)}$	29.9 ^(4.5) 36.6 ^(4.4)	59.3 ^(14.5)	3.2 4.5	13.2 9.8
		69.1 ^(12.9) 59.5 ^(12.0) 53.8 ^(11.0)	58.5 ^(11.3) 63.5 ^(11.2) 63.4 ^(11.5)		88.4 ^(17.2) 84.2 ^(17.2) 99.0^(12.1)	36.6 ^(4.4)	59.3 ^(14.5)		
	GAMBO DynAMO	59.5 ^(12.0) 53.8 ^(11.0)	63.5 ^(11.2) 63.4 ^(11.5)	55.4 ^(9.6) 59.3 ^(3.8)	84.2 ^(17.2) 99.0^(12.1)	36.6 ^(4.4) 20.5 ^(5.8)	59.3 ^(14.5) 60.6 ^(15.0)	4.5 5.3	9.8 9.5
	GAMBO DynAMO BO-qEI	59.5 ^(12.0) 53.8 ^(11.0) TFBind8	63.5 ^(11.2) 63.4 ^(11.5) UTR	55.4^(9.6) 59.3 ^(3.8) ChEMBL	84.2 ^(17.2) 99.0 ^(12.1) Molecule	36.6 ^(4.4) 20.5 ^(5.8) Superconductor	59.3 ^(14.5) 60.6 ^(15.0) D'Kitty	4.5 5.3 Rank ↓	9.8 9.5 Opt. Gap ↑
-	GAMBO DynAMO BO-qEI Baseline	59.5 ^(12.0) 53.8 ^(11.0) TFBind8 48.5 ^(1.5) 50 9 ^(1.9)	63.5 ^(11.2) 63.4 ^(11.5) UTR 59.9 ^(2.0)	55.4 ^(9,6) 59.3 ^(3,8) ChEMBL 63.3 ^(0,0) 63.3 ^(0,0)	84.2 ^(17.2) 99.0 ^(12.1) Molecule	36.6 ^(4.4) 20.5 ^(5.8) Superconductor 28.7 ^(1.8) 19 4 ^(1.1)	59.3 ^(14.5) 60.6 ^(15.0) D'Kitty 72.4 ^(1.8) 78 1 ^(1.1)	4.5 5.3 Rank ↓ 4.3	9.8 9.5 Opt. Gap ↑ 10.0
	GAMBO DynAMO BO-qEI Baseline COMs ⁻	59.5 ^(12.0) 53.8 ^(11.0) TFBind8 48.5 ^(1.5) 50 9 ^(1.9)	63.5 ^(11.2) 63.4 ^(11.5) UTR 59.9 ^(2.0) 59.6 ^(1.6)	55.4 ^(9,6) 59.3 ^(3,8) ChEMBL 63.3 ^(0,0) 63.3 ^(0,0)	84.2 ^(17.2) 99.0 ^(12.1) Molecule 86.7 ^(0.6) 86.6 ^(0.6)	36.6 ^(4.4) 20.5 ^(5.8) Superconductor 28.7 ^(1.8) 19 4 ^(1.1)	59.3 ^(14.5) 60.6 ^(15.0) D'Kitty 72.4 ^(1.8) 78 1 ^(1.1)	4.5 5.3 Rank ↓ 4.3 4.7	9.8 9.5 Opt. Gap ↑ 10.0 9.7
-	GAMBO DynAMO BO-qEI Baseline COMs ⁻ COMs ⁺	59.5 ^(12.0) 53.8 ^(11.0) TFBind8 48.5 ^(1.5) 50.9 ^(1.9) 43.6 ^(0.0)	63.5 ^(11.2) 63.4 ^(11.5) UTR 59.9 ^(2.0) 59.6 ^(1.6) 66.0 ^(1.6)	55.4 ^(9.6) 59.3 ^(3.8) ChEMBL 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0)	84.2 ^(17.2) 99.0 ^(12.1) Molecule 86.7 ^(0.6) 86.6 ^(0.6) 87.5 ^(0.6)	36.6⁽⁴⁴⁾ 20.5 ^(5.8) Superconductor 28.7^(1.8) 19.4 ^(1.1) 20.6 ^(0.9)	59.3 ^(14.5) 60.6 ^(15.0) D'Kitty 72.4 ^(1.8) 78.1 ^(1.1) 66.3 ^(2.2)	4.5 5.3 Rank↓ 4.3 4.7 4.5	9.8 9.5 Opt. Gap ↑ 10.0 9.7 8.0
-	GAMBO DynAMO BO-qEI Baseline COMs ⁻ COMs ⁺ RoMA ⁻	59.5 ^(12.0) 53.8 ^(11.0) TFBind8 48.5 ^(1.5) 50.9 ^(1.9) 43.6 ^(0.0) 50.0 ^(1.6)	63.5 ^(11.2) 63.4 ^(11.5) UTR 59.9 ^(2.0) 59.6 ^(1.6) 66.0 ^(1.6) 60.0 ^(2.1)	55.4 ^(9.6) 59.3 ^(3.8) ChEMBL 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0)	84.2 ^(17.2) 99.0 ^(12.1) Molecule 86.7 ^(0.6) 86.6 ^(0.6) 87.5 ^(0.6) 87.5 ^(0.6) 86.4 ^(0.5)	36.6 ^(4.4) 20.5 ^(5.8) Superconductor 28.7 ^(1.8) 19.4 ^(1.1) 20.6 ^(0.9) 28.7 ^(1.8)	59.3 ^(14.5) 60.6 ^(15.0) D'Kitty 72.4 ^(1.8) 78.1 ^(1.1) 66.3 ^(2.2) 78.5 ^(1.2)	4.5 5.3 Rank ↓ 4.3 4.7 4.5 3.5	9.8 9.5 Opt. Gap ↑ 10.0 9.7 8.0 11.2
-	GAMBO DynAMO BO-qEI Baseline COMs ⁻ COMs ⁺ RoMA ⁻ RoMA ⁺	59.5 ^(12.0) 53.8 ^(11.0) TFBind8 48.5 ^(1.5) 50.9 ^(1.9) 43.6 ^(0.0) 50.0 ^(1.6) 52.5^(0.0)	63.5 ^(11.2) 63.4 ^(11.5) UTR 59.9 ^(2.0) 59.6 ^(1.6) 66.0 ^(1.6) 60.0 ^(2.1) 61.0 ^(1.1)	55.4 ^(9.6) 59.3 ^(3.8) ChEMBL 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0)	84.2 ^(17.2) 99.0 ^(12.1) Molecule 86.7 ^(0.6) 86.6 ^(0.6) 87.5 ^(0.6) 86.4 ^(0.5) 93.3 ^(5.7)	36.6 ^(4.4) 20.5 ^(5.8) Superconductor 28.7 ^(1.8) 19.4 ^(1.1) 20.6 ^(0.9) 28.7 ^(1.8) 26.4 ^(1.1)	59.3 ^(14.5) 60.6 ^(15.0) D'Kitty 72.4 ^(1.8) 78.1 ^(1.1) 66.3 ^(2.2) 78.5 ^(1.2) 74.3 ^(1.3)	4.5 5.3 Rank ↓ 4.3 4.7 4.5 3.5 2.7	9.8 9.5 Opt. Gap ↑ 10.0 9.7 8.0 11.2 11.9
-	GAMBO DynAMO BO-qEI Baseline COMs ⁻ COMs ⁺ ROMA ⁻ ROMA ⁺	59.5 ^(12.0) 53.8 ^(11.0) TFBind8 48.5 ^(1.5) 50.9 ^(1.9) 43.6 ^(0.0) 50.0 ^(1.6) 52.5 ^(0.0) 49.9 ^(2.2)	63.5 ^(11.2) 63.4 ^(11.5) UTR 59.9 ^(2.0) 59.6 ^(1.6) 66.0 ^(1.6) 60.0 ^(2.1) 61.0 ^(1.1) 59.0 ^(1.4)	55.4 ^(9.6) 59.3 ^(3.8) ChEMBL 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0)	84.2 ^(17.2) 99.0 ^(12.1) Molecule 86.7 ^(0.6) 86.6 ^(0.6) 87.5 ^(0.6) 86.4 ^(0.5) 93.3 ^(5.7) 86.8 ^(0.6)	36.6 ⁽⁴⁴⁾ 20.5 ^(5.8) Superconductor 28.7 ^(1.8) 19.4 ^(1.1) 20.6 ^(0.9) 28.7 ^(1.8) 26.4 ^(1.1) 24.4 ^(0.8)	59.3 ^(14.5) 60.6 ^(15.0) D'Kitty 72.4 ^(1.8) 78.1 ^(1.1) 66.3 ^(2.2) 78.5 ^(1.2) 74.3 ^(1.3) 73.8 ^(2.0)	4.5 5.3 Rank ↓ 4.3 4.7 4.5 3.5 2.7 4.7	9.8 9.5 Opt. Gap ↑ 10.0 9.7 8.0 11.2 11.9 9.6
-	GAMBO DynAMO BO-qEI Baseline COMs ⁺ RoMA ⁻ RoMA ⁺ ROMO GAMBO	59.5 ^(12.0) 53.8 ^(11.0) TFBind8 48.5 ^(1.5) 50.9 ^(1.9) 43.6 ^(0.0) 50.0 ^(1.6) 52.5^(0.0) 49.9 ^(2.2) 46.4 ^(1.8)	63.5 ^(11.2) 63.4 ^(11.5) UTR 59.9 ^(2.0) 59.6 ^(1.6) 66.0 ^(1.6) 60.0 ^(2.1) 61.0 ^(1.1) 59.0 ^(1.4) 63.4 ^(3.3)	55,4 ^(9,6) 59,3 ^(3,3) ChEMBL 63,3 ^(0,0) 63,3 ^(0,0) 63,3 ^(0,0) 63,3 ^(0,0) 63,3 ^(0,0) 63,3 ^(0,0) 63,3 ^(0,0)	84.2 ^(17,2) 99.0 ^(12,1) Molecule 86.7 ^(0,6) 86.6 ^(0,6) 87.5 ^(0,6) 86.4 ^(0,5) 93.3 ^(5,7) 86.8 ^(0,6) 86.3 ^(0,5)	36.6 ⁽⁴⁴⁾ 20.5 ^(5.8) Superconductor 28.7 ^(1.8) 19.4 ^(1.1) 20.6 ^(0.9) 28.7 ^(1.8) 26.4 ^(1.1) 24.6 ^(0.8) 28.9 ^(1.1)	59.3 ^(14.5) 60.6 ^(15.0) D'Kitty 72.4 ^(1.8) 78.1 ^(1.1) 66.3 ^(2.2) 78.5 ^(1.2) 74.3 ^(1.3) 73.8 ^(2.0) 79.1 ^(0.7)	4.5 5.3 Rank ↓ 4.3 4.7 4.5 3.5 2.7 4.7 3.5	9.8 9.5 Opt. Gap ↑ 10.0 9.7 8.0 11.2 11.9 9.6 11.3
-	GAMBO DynAMO BO-qEI Baseline COMs ⁻ COMs ⁺ RoMA ⁻ RoMA ⁺ ROMO GAMBO DynAMO	59.5 ^(12.0) 53.8 ^(11.0) TFBind8 48.5 ^(1.5) 50.9 ^(1.9) 43.6 ^(0.0) 50.0 ^(1.6) 52.5 ^(0.0) 49.9 ^(2.2) 46.4 ^(1.8) 51.5 ^(0.9)	63.5 ^(11.2) 63.4 ^(11.5) UTR 59.9 ^(2.0) 59.6 ^(1.6) 66.0 ^(1.6) 60.0 ^(2.1) 61.0 ^(1.1) 59.0 ^(1.4) 63.4 ^(3.3) 65.6 ^(3.1)	55,4 ^(9,6) 59,3 ^(3,3) ChEMBL 63,3 ^(0,0) 63,3 ^(0,0) 63,3 ^(0,0) 63,3 ^(0,0) 63,3 ^(0,0) 63,3 ^(0,0) 63,3 ^(0,0) 63,3 ^(0,0)	84.2 ^(17,2) 99.0 ^(12,1) Molecule 86.7 ^(0,6) 86.6 ^(0,6) 87.5 ^(0,6) 86.4 ^(0,5) 93.3 ^(5,7) 86.8 ^(0,6) 86.3 ^(0,5) 86.7 ^(0,6)	36.6 ⁽⁴⁴⁾ 20.5 ^(5.8) Superconductor 28.7 ^(1.8) 19.4 ^(1.1) 20.6 ^(0.9) 28.7 ^(1.8) 26.4 ^(1.1) 24.6 ^(0.8) 28.9 ^(1.1) 23.5 ^(2.4)	59.3 ^(14.5) 60.6 ^(15.0) D'Kitty 72.4 ^(1.8) 78.1 ^(1.1) 66.3 ^(2.2) 78.5 ^(1.2) 74.3 ^(1.3) 73.8 ^(2.0) 79.1 ^(0.7) 77.0 ^(0.7)	4.5 5.3 Rank ↓ 4.3 4.7 4.5 3.5 2.7 4.7 3.5 <u>3.3</u>	9.8 9.5 Opt. Gap ↑ 10.0 9.7 8.0 11.2 11.9 9.6 11.3 11.3
-	GAMBO DynAMO Bo-qEI Baseline COMs ⁻ COMs ⁺ ROMA ⁺ ROMA ⁺ ROMO GAMBO DynAMO BO-qUCB	59.5 ^(12.0) 53.8 ^(11.0) TFBind8 48.5 ^(1.5) 50.9 ^(1.9) 43.6 ^(0.0) 50.0 ^(1.6) 52.5 ^(0.0) 49.9 ^(2.2) 46.4 ^(1.8) 51.5 ^(0.9) TFBind8	63.5 ^(11.2) 63.4 ^(11.5) UTR 59.9 ^(2.0) 59.6 ^(1.6) 66.0 ^(1.6) 60.0 ^(2.1) 61.0 ^(1.1) 59.0 ^(1.4) 63.4 ^(3.3) 65.6 ^(3.1) UTR	55.4 ^(9,6) 59.3 ^(3,3) ChEMBL 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0)	84.2 ^(17,2) 99.0 ^(12,1) Molecule 86.7 ^(0,6) 86.6 ^(0,6) 87.5 ^(0,6) 86.4 ^(0,5) 93.3 ^(5,7) 86.8 ^(0,6) 86.3 ^(0,6) 86.7 ^(0,6) 86.7 ^(0,6)	36.6^(4.4) 20.5 ^(5.8) Superconductor 28.7^(1.8) 19.4 ^(1.1) 20.6 ^(0.9) 28.7^(1.8) 26.4 ^(1.1) 24.6 ^(0.8) 28.9^(1.1) 23.5 ^(2.4) Superconductor	59.3 ^(14.5) 60.6 ^(15.0) D'Kitty 72.4 ^(1.8) 78.1 ^(1.1) 66.3 ^(2.2) 78.5 ^(1.2) 74.3 ^(1.3) 73.8 ^(2.0) 79.1 ^(0.7) 77.0 ^(0.7) D'Kitty	4.5 5.3 Rank ↓ 4.3 4.7 4.5 3.5 2.7 4.7 3.5 <u>3.3</u> Rank ↓	9.8 9.5 Opt. Gap ↑ 10.0 9.7 8.0 11.2 11.9 9.6 11.3 <u>11.3</u> <u>11.3</u> Opt. Gap ↑
-	GAMBO DynAMO Bo-qEI Baseline COMs ⁻ COMs ⁺ RoMA ⁺ RoMA ⁺ ROMA GAMBO GAMBO DynAMO BO-qUCB Baseline	59.5 ^(12.0) 53.8 ^(11.0) TFBind8 48.5 ^(1.5) 50.9 ^(1.9) 43.6 ^(0.0) 50.0 ^(1.6) 52.5 ^(0.0) 49.9 ^(2.2) 46.4 ^(1.8) 51.5 ^(0.9) TFBind8 50.3 ^(1.8)	63.5 ^(11,2) 63.4 ^(11,5) UTR 59.9 ^(2,0) 59.6 ^(1,6) 66.0 ^(1,6) 60.0 ^(2,1) 61.0 ^(1,1) 59.0 ^(1,4) 63.4 ^(3,3) 65.6 ^(3,1) UTR 62.1 ^(3,4)	55.4 ^(9,6) 59.3 ^(3,3) ChEMBL 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0)	84.2 ^(17,2) 99.0 ^(12,1) Molecule 86.7 ^(0,6) 87.5 ^(0,6) 87.5 ^(0,6) 87.5 ^(0,6) 86.4 ^(0,5) 93.3 ^(5,7) 86.8 ^(0,6) 86.3 ^(0,5) 86.7 ^(0,6) Molecule 86.6 ^(0,6)	36.6 ^(4.4) 20.5 ^(5.8) Superconductor 28.7 ^(1.8) 19.4 ^(1.1) 20.6 ^(0.9) 28.7 ^(1.8) 26.4 ^(1.1) 24.6 ^(0.8) 28.9 ^(1.1) 23.5 ^(2.4) Superconductor 31.7 ^(1.2)	59.3 ^(14.5) 60.6 ^(15.0) D'Kitty 72.4 ^(1.8) 78.1 ^(1.1) 66.3 ^(2.2) 78.5 ^(1.2) 74.3 ^(1.3) 73.8 ^(2.0) 79.1 ^(0.7) 77.0 ^(0.7) D'Kitty 74.4 ^(0.6)	4.5 5.3 Rank ↓ 4.3 4.7 4.5 3.5 2.7 4.7 3.5 <u>3.3</u> Rank ↓ 2.7	9.8 9.5 Opt. Gap ↑ 10.0 9.7 8.0 11.2 11.9 9.6 <u>11.3</u> <u>11.3</u> <u>11.3</u> <u>11.3</u> <u>11.3</u>
-	GAMBO DynAMO Bo-qEI Baseline COMs ⁻ COMs ⁺ RoMA ⁺ ROMA ⁺ ROMO GAMBO DynAMO BO-qUCB Baseline COMs ⁻	59.5 ^(12.0) 53.8 ^(11.0) TFBind8 48.5 ^(1.5) 50.9 ^(1.9) 43.6 ^(0.0) 50.0 ^(1.6) 52.5 ^(0.0) 49.9 ^(2.2) 46.4 ^(1.8) 51.5 ^(0.9) TFBind8 50.3 ^(1.8) 51.1 ^(1.0)	63.5 ^(11,2) 63.4 ^(11,5) UTR 59.9 ^(2,0) 59.6 ^(1,6) 66.0 ^(1,6) 60.0 ^(2,1) 61.0 ^(1,1) 59.0 ^(1,4) 63.4 ^(3,3) 65.6 ^(3,1) UTR 62.1 ^(3,4) 61.0 ^(2,9)	55.4 ^(9,6) 59.3 ^(3,3) ChEMBL 63.3 ^(0,0) 63.3 ^(0,0)	84.2 ^(17,2) 99.0 ^(12,1) Molecule 86.7 ^(0,6) 86.6 ^(0,6) 87.5 ^(0,6) 86.4 ^(0,5) 93.3 ^(5,7) 86.8 ^(0,6) 86.3 ^(0,5) 86.7 ^(0,6) 86.3 ^(0,7)	36.6 ^(4.4) 20.5 ^(5.8) Superconductor 28.7 ^(1.8) 19.4 ^(1.1) 20.6 ^(0.9) 28.7 ^(1.8) 26.4 ^(1.1) 24.6 ^(0.8) 28.9 ^(1.1) 23.5 ^(2.4) Superconductor 31.7 ^(1.2) 19.8 ^(1.3)	59.3 ^(14.5) 60.6 ^(15.0) D'Kitty 72.4 ^(1.8) 78.1 ^(1.1) 66.3 ^(2.2) 78.5 ^(1.2) 74.3 ^(1.3) 73.8 ^(2.0) 79.1 ^(0.7) 77.0 ^(0.7) D'Kitty 74.4 ^(0.6) 74.2 ^(1.3)	$\begin{array}{c} 4.5 \\ 5.3 \end{array}$ Rank \downarrow 4.3 \\ 4.7 \\ 4.5 \\ 3.5 \\ 2.7 \\ 4.7 \\ 3.5 \\ 3.3 \end{array} Rank \downarrow 2.7 4.5	9.8 9.5 Opt. Gap ↑ 10.0 9.7 8.0 11.2 11.9 9.6 <u>11.3</u> <u>11.3</u> <u>11.3</u> <u>11.3</u> <u>11.3</u> <u>11.5</u> 9.4
-	GAMBO DynAMO Bo-qEI Baseline COMs ⁻ COMs ⁺ RoMA ⁻ RoMA ⁺ ROMO GAMBO DynAMO BO-qUCB Baseline COMs ⁻ COMs ⁺	59.5 ^(12.0) 53.8 ^(11.0) TFBind8 48.5 ^(1.5) 50.9 ^(1.9) 43.6 ^(0.0) 52.5 ^(0.0) 52.5 ^(0.0) 49.9 ^(2.2) 46.4 ^(1.8) 51.5 ^(0.9) TFBind8 50.3 ^(1.8) 51.1 ^(1.0) 43.6 ^(0.0)	63.5 ^(11,2) 63.4 ^(11,5) UTR 59.9 ^(2,0) 59.6 ^(1,6) 66.0 ^(1,6) 60.0 ^(2,1) 61.0 ^(1,1) 59.0 ^(1,4) 63.4 ^(3,3) 65.6 ^(3,1) UTR 62.1 ^(3,4) 61.0 ^(2,9) 65.6 ^(1,4)	55,4 ^{9,6)} 59,3 ^(3,3) ChEMBL 63,3 ^(0,0) 63,3 ^(0,0) 63,3 ^(0,0) 63,3 ^(0,0) 63,3 ^(0,0) 63,3 ^(0,0) 63,3 ^(0,0) 63,3 ^(0,0) 63,3 ^(0,0) 63,3 ^(0,0)	84.2 ^(17,2) 99.0 ^(12,1) Molecule 86.7 ^(0,6) 86.6 ^(0,6) 86.4 ^(0,5) 93.3 ^(5,7) 86.8 ^(0,6) 86.3 ^(0,5) 86.7 ^(0,6) 86.3 ^(0,5) 86.3 ^(0,7) 87.5 ^(0,9)	$\begin{array}{c} \textbf{36.6}^{(\textbf{4.4})} \\ 20.5^{(5.8)} \\ \hline \textbf{Superconductor} \\ \textbf{28.7}^{(\textbf{1.8})} \\ 19.4^{(1.1)} \\ 20.6^{(0.9)} \\ \textbf{28.7}^{(\textbf{1.8})} \\ 26.4^{(1.1)} \\ 24.6^{(0.8)} \\ \textbf{28.9}^{(\textbf{1.1})} \\ 23.5^{(2.4)} \\ \hline \textbf{Superconductor} \\ \textbf{31.7}^{(\textbf{1.2})} \\ 19.8^{(1.3)} \\ 20.1^{(1.0)} \\ \end{array}$	59.3 ^(14.5) 60.6 ^(15.0) D'Kitty 72.4 ^(1.8) 78.1 ^(1.1) 66.3 ^(2.2) 78.5 ^(1.2) 74.3 ^(1.3) 73.8 ^(2.0) 79.1 ^(0.7) 77.0 ^(0.7) D'Kitty 74.4 ^(0.6) 74.2 ^(1.3) 54.2 ^(11.9)	4.5 5.3 Rank ↓ 4.3 4.7 4.5 3.5 2.7 4.7 3.5 <u>3.3</u> Rank ↓ 2.7 4.5 4.5 4.5	9.8 9.5 Opt. Gap ↑ 10.0 9.7 8.0 11.2 11.9 9.6 11.3 <u>11.3</u> <u>11.3</u> Opt. Gap ↑ 11.5 9.4 5.8
-	GAMBO DynAMO BO-qEI Baseline COMs ⁺ ROMA ⁻ ROMA ⁺ ROMA ⁺ ROMO GAMBO DynAMO BO-qUCB Baseline COMs ⁺ COMs ⁺ ROMA ⁻	59.5 ^(12.0) 53.8 ^(11.0) TFBind8 48.5 ^(1.5) 50.9 ^(1.9) 43.6 ^(0.0) 50.0 ^(1.6) 52.5 ^(0.0) 49.9 ^(2.2) 46.4 ^(1.8) 51.5 ^(0.9) TFBind8 50.3 ^(1.8) 51.1 ^(1.0) 43.6 ^(0.0) 50.0 ^(1.7)	63.5 ^(11,2) 63.4 ^(11,5) UTR 59.9 ^(2,0) 59.6 ^(1,6) 66.0 ^(1,6) 60.0 ^(2,1) 61.0 ^(1,1) 59.0 ^(1,4) 63.4 ^(3,3) 65.6 ^(3,1) UTR 62.1 ^(3,4) 65.6 ^(1,4) 62.1 ^(3,4)	55,4 ^(9,6) 59,3 ^(3,3) ChEMBL 63,3 ^(0,0) 63,3 ^(0,0)	84.2 ^(17,2) 99.0 ^(12,1) Molecule 86.7 ^(0,6) 86.6 ^(0,6) 86.4 ^(0,5) 93.3 ^(5,7) 86.8 ^(0,6) 86.3 ^(0,5) 86.7 ^(0,6) Molecule 86.6 ^(0,6) 86.3 ^(0,7) 87.5 ^(0,9) 86.7 ^(0,6)	36.6 ^(4.4) 20.5 ^(5.8) Superconductor 28.7 ^(1.8) 19.4 ^(1.1) 20.6 ^(0.9) 28.7 ^(1.8) 26.4 ^(1.1) 24.6 ^(0.8) 28.9 ^(1.1) 23.5 ^(2.4) Superconductor 31.7 ^(1.2) 19.8 ^(1.3) 20.1 ^(1.0) 31.7 ^(1.2)	59.3 ^(14.5) 60.6 ^(15.0) D'Kitty 72.4 ^(1.8) 78.1 ^(1.1) 66.3 ^(2.2) 78.5 ^(1.2) 74.3 ^(1.3) 73.8 ^(2.0) 79.1 ^(0.7) 77.0 ^(0.7) D'Kitty 74.4 ^(0.6) 74.2 ^(1.5) 54.2 ^(1.9) 74.4 ^(0.6)	4.5 5.3 Rank ↓ 4.3 4.7 4.5 3.5 2.7 4.7 3.5 <u>3.3</u> Rank ↓ 2.7 4.5 4.5 4.5 2.7	9.8 9.5 Opt. Gap ↑ 10.0 9.7 8.0 11.2 11.9 9.6 <u>11.3</u> <u>11.3</u> Opt. Gap ↑ 11.5 9.4 5.8 <u>11.4</u>
-	GAMBO DynAMO BO-qEI Baseline COMs ⁺ RoMA ⁻ RoMA ⁻ ROMA ⁺ ROMO GAMBO DynAMO BO-qUCB Baseline COMs ⁺ ROMA ⁻ ROMA ⁺	59.5 ^(12.0) 53.8 ^(11.0) TFBind8 48.5 ^(1.5) 50.9 ^(1.9) 43.6 ^(0.0) 50.0 ^(1.6) 52.5 ^(0.0) 49.9 ^(2.2) 46.4 ^(1.8) 51.5 ^(0.9) TFBind8 50.3 ^(1.8) 51.1 ^(1.0) 43.6 ^(0.0) 50.0 ^(1.7) 52.5 ^(0.0)	63.5 ^(11,2) 63.4 ^(11,5) UTR 59.9 ^(2,0) 59.6 ^(1,6) 60.0 ^(2,1) 61.0 ^(1,1) 63.4 ^(3,3) 65.6 ^(3,1) UTR 62.1 ^(3,4) 61.0 ^(2,9) 65.6 ^(1,4) 62.1 ^(3,4) 60.8 ^(0,9)	55,4 ^(9,6) 59,3 ^(3,3) ChEMBL 63,3 ^(0,0) 63,3 ^(0,0)	84.2 ^(17,2) 99.0 ^(12,1) Molecule 86.7 ^(0,6) 86.6 ^(0,6) 87.5 ^(0,6) 86.3 ^(0,5) 86.3 ^(0,5) 86.3 ^(0,5) 86.3 ^(0,5) 86.7 ^(0,6) Molecule 86.6 ^(0,6) 86.3 ^(0,7) 87.5 ^(0,9) 86.7 ^(0,6) 91.4 ^(5,6)	36.6 ⁽⁴⁴⁾ 20.5 ^(5.8) Superconductor 28.7 ^(1.8) 19.4 ^(1.1) 20.6 ^(0.9) 28.7 ^(1.8) 26.4 ^(1.1) 24.6 ^(0.8) 28.9 ^(1.1) 23.5 ^(2.4) Superconductor 31.7 ^(1.2) 19.8 ^(1.3) 20.1 ^(1.0) 31.7 ^(1.2) 29.5 ^(1.4)	59.3 ^(14.5) 60.6 ^(15.0) D'Kitty 72.4 ^(1.8) 78.1 ^(1.1) 66.3 ^(2.2) 78.5 ^(1.2) 74.3 ^(1.3) 73.8 ^(2.0) 79.1 ^(0.7) 79.1 ^(0.7) 71.0 ^(0.7) D'Kitty 74.4 ^(0.6) 54.2 ^(11.9) 74.4 ^(0.6) 65.8 ^(0.3)	$\begin{array}{c} 4.5\\ 5.3\\ \hline \textbf{Rank} \downarrow \\ 4.3\\ 4.7\\ 4.5\\ 3.5\\ \textbf{2.7}\\ 4.7\\ 3.5\\ \underline{3.3}\\ \hline \textbf{Rank} \downarrow \\ \hline \textbf{2.7}\\ 4.5\\ 4.5\\ \textbf{2.7}\\ 4.5\\ \textbf{2.7}\\ \underline{3.2}\\ \end{array}$	9.8 9.5 Opt. Gap ↑ 10.0 9.7 8.0 11.2 11.9 9.6 11.3 <u>11.3</u> Opt. Gap ↑ 11.5 9.4 5.8 11.4 10.6
= -	GAMBO DynAMO Bo-qEI Baseline COMs ⁺ RoMA ⁺ ROMA ⁺ ROMO GAMBO DynAMO BO-qUCB Baseline COMs ⁺ ROMA ⁺ ROMA ⁺ ROMA ⁺	59.5 ^(12.0) 53.8 ^(11.0) TFBind8 48.5 ^(1.5) 50.9 ^(1.9) 43.6 ^(0.0) 50.0 ^(1.6) 52.5 ^(0.0) 49.9 ^(2.2) 46.4 ^(1.8) 51.5 ^(0.9) TFBind8 50.3 ^(1.8) 51.1 ^(1.0) 43.6 ^(0.0) 50.0 ^(1.7) 52.5 ^(0.0) 49.8 ^(2.0)	63.5 ^(11,2) 63.4 ^(11,5) UTR 59.9 ^(2,0) 59.6 ^(1,6) 60.0 ^(2,1) 61.0 ^(1,1) 63.4 ^(3,3) 65.6 ^(3,1) UTR 62.1 ^(3,4) 61.0 ^(2,9) 65.6 ^(1,4) 62.1 ^(3,4) 60.8 ^(0,9) 58.2 ^(0,2)	55,4 ^(9,6) 59,3 ^(3,3) ChEMBL 63,3 ^(0,0) 63,3 ^(0,0)	84.2 ^(17,2) 99.0 ^(12,1) Molecule 86.7 ^(0,6) 86.6 ^(0,6) 87.5 ^(0,6) 86.3 ^(0,5) 86.3 ^(0,5) 86.3 ^(0,5) 86.3 ^(0,7) 86.3 ^(0,5) 86.3 ⁽⁰	36.6 ⁽⁴⁴⁾ 20.5 ^(5,8) Superconductor 28.7 ^(1,8) 19.4 ^(1,1) 20.6 ^(0,9) 28.7 ^(1,8) 26.4 ^(1,1) 24.6 ^(0,8) 28.9 ^(1,1) 23.5 ^(2,4) Superconductor 31.7 ^(1,2) 19.8 ^(1,3) 20.1 ^(1,0) 31.7 ^(1,2) 29.5 ^(1,4) 24.3 ^(0,7)	59.3 ^(14.5) 60.6 ^(15.0) D'Kitty 72.4 ^(1.8) 78.1 ^(1.1) 66.3 ^(2.2) 78.5 ^(1.2) 74.3 ^(1.3) 73.8 ^(2.0) 79.1 ^(0.7) 77.0 ^(0.7) D'Kitty 74.4 ^(0.6) 74.2 ^(1.3) 54.2 ^(1.9) 74.2 ^(1.9) 75.0 ^(1.7)	$\begin{array}{c} 4.5 \\ 5.3 \\ \hline \textbf{Rank} \downarrow \\ 4.3 \\ 4.7 \\ 4.5 \\ 3.5 \\ \textbf{2.7} \\ 4.7 \\ 3.5 \\ \textbf{3.5} \\ \textbf{3.3} \\ \hline \textbf{Rank} \downarrow \\ \textbf{2.7} \\ 4.5 \\ 4.5 \\ \textbf{4.5} \\ \textbf{2.7} \\ \textbf{3.2} \\ \textbf{3.8} \\ \hline \end{array}$	9.8 9.5 Opt. Gap \uparrow 10.0 9.7 8.0 11.2 11.9 9.6 11.3 <u>11.3</u> Opt. Gap \uparrow 11.5 9.4 5.8 11.4 10.6 9.6
-	GAMBO bynAMO Bo-qEI Baseline COMs ⁺ RoMA ⁻ RoMA ⁻ ROMA ⁺ ROMO GAMBO DynAMO Bo-qUCB Baseline COMs ⁺ COMs ⁺ ROMA ⁺	59.5 ^(12.0) 53.8 ^(11.0) TFBind8 48.5 ^(1.5) 50.9 ^(1.9) 43.6 ^(0.0) 50.0 ^(1.6) 52.5 ^(0.0) 49.9 ^(2.2) 46.4 ^(1.8) 51.5 ^(0.9) TFBind8 50.3 ^(1.8) 51.1 ^(1.0) 43.6 ^(0.0) 50.0 ^(1.7) 52.5 ^(0.0)	63.5 ^(11,2) 63.4 ^(11,5) UTR 59.9 ^(2,0) 59.6 ^(1,6) 60.0 ^(2,1) 61.0 ^(1,1) 63.4 ^(3,3) 65.6 ^(3,1) UTR 62.1 ^(3,4) 61.0 ^(2,9) 65.6 ^(1,4) 62.1 ^(3,4) 60.8 ^(0,9)	55,4 ^(9,6) 59,3 ^(3,3) ChEMBL 63,3 ^(0,0) 63,3 ^(0,0)	84.2 ^(17,2) 99.0 ^(12,1) Molecule 86.7 ^(0,6) 86.6 ^(0,6) 87.5 ^(0,6) 86.3 ^(0,5) 86.3 ^(0,5) 86.3 ^(0,5) 86.3 ^(0,5) 86.7 ^(0,6) Molecule 86.6 ^(0,6) 86.3 ^(0,7) 87.5 ^(0,9) 86.7 ^(0,6) 91.4 ^(5,6)	36.6 ⁽⁴⁴⁾ 20.5 ^(5.8) Superconductor 28.7 ^(1.8) 19.4 ^(1.1) 20.6 ^(0.9) 28.7 ^(1.8) 26.4 ^(1.1) 24.6 ^(0.8) 28.9 ^(1.1) 23.5 ^(2.4) Superconductor 31.7 ^(1.2) 19.8 ^(1.3) 20.1 ^(1.0) 31.7 ^(1.2) 29.5 ^(1.4)	59.3 ^(14.5) 60.6 ^(15.0) D'Kitty 72.4 ^(1.8) 78.1 ^(1.1) 66.3 ^(2.2) 78.5 ^(1.2) 74.3 ^(1.3) 73.8 ^(2.0) 79.1 ^(0.7) 79.1 ^(0.7) 71.0 ^(0.7) D'Kitty 74.4 ^(0.6) 54.2 ^(11.9) 74.4 ^(0.6) 65.8 ^(0.3)	$\begin{array}{c} 4.5\\ 5.3\\ \hline \textbf{Rank} \downarrow \\ 4.3\\ 4.7\\ 4.5\\ 3.5\\ \textbf{2.7}\\ 4.7\\ 3.5\\ \underline{3.3}\\ \hline \textbf{Rank} \downarrow \\ \hline \textbf{2.7}\\ 4.5\\ 4.5\\ \textbf{2.7}\\ 4.5\\ \textbf{2.7}\\ \underline{3.2}\\ \end{array}$	9.8 9.5 Opt. Gap ↑ 10.0 9.7 8.0 11.2 11.9 9.6 11.3 <u>11.3</u> Opt. Gap ↑ 11.5 9.4 5.8 11.4 10.6

where dim(x) is the number of design dimensions and x_{ik}^F is the *k*th dimension of design x_i^F . Note that the L1C metric is only defined for designs sampled from a continuous search space; to compute the L1C metric for discrete optimization tasks, we use task-specific foundation models to embed discrete designs into a continuous latent space. For DNA design tasks (i.e., **TFBind8** and **UTR**), we use the DNABERT-2 foundation model with 117M parameters (zhihan1996/DNABERT-2-117M) from Zhou et al. (2024) to embed candidate DNA sequences into a continuous latent space. Similarly for molecule design tasks (i.e., **ChEMBL** and **Molecule**), we use the ChemBERT model (jonghyunlee/ChemBERT_ChEMBL_pretrained) from Zhang et al. (2022) to embed candidate molecules into a continuous latent space.

We report MN and L1C metric scores in **Supplementary Table A3**. We find that compared with other MBO objectivemodifying methods, DynAMO achieves the best Rank and Optimality Gap for 3 of the 6 optimizers evaluated (Grad., Adam, and BO-qEI). For the remaining 3 optimizers evaluated, DynAMO is within the top 2 evaluated methods in terms of both average Rank and Optimality Gap for the L1C (L_1 coverage) metric. Altogether, our results support that DynAMO is competitive according to the MN and L1C diversity metrics in addition to the Pairwise Diversity metric reported in **Table 1**.

1334 What is the best notion of diversity? In our work, we focus on the Pairwise Diversity metric in our main results (Table 1335 1)—however, this does not mean that this metric is the best for all applications. Rather, our focus on the Pairwise Diversity metric is determined by our problem motivation. Compared with the minimum novelty and L_1 coverage diversity metrics, 1336 the definition of pairwise diversity best captures the notion of diversity that we are interested in-that is, capturing many possible 'modes of goodness' in optimizing the oracle reward function. We note that these modes of goodness may not 1338 necessarily be significantly 'novel' according to our task-specific distance metric, and so we treated the Minimum Novelty 1340 metric as only a secondary diversity objective for evaluating DynAMO. (Indeed, because DynAMO encourages a generative 1341 policy to match a distribution of designs constructed from the offline dataset, DynAMO may not increase the minimum 1342 novelty of designs compared to those proposed by the comparable baseline optimizer.) Similarly, we find that the L_1 1343 Coverage metric is more sensitive to outlier designs when compared to the Pairwise Diversity, and therefore also treat it as a 1344 secondary diversity evaluation metric for our experiments in **Supplementary Table A3**. Future work might explore other 1345 methods that focus on improving not only the Pairwise Diversity metric, but also other diversity metric(s), too. 1346

1347 D.3. Imposing Alternative *f*-Divergence Diversity Objectives via Mixed-Divergence Regularization

The MBO problem formulation proposed in (7) introduces a weighted KL-divergence regularization of the original MBO
optimization objective. However, alternative distribution matching objectives have been used in prior work (Agarwal et al., 2024; Gong et al., 2021; Ma et al., 2022), and one might hypothesize that we can similarly generalize (7) as

1352 1353

1355

1356

1374

$$\max_{\pi \in \Pi} \quad J_f(\pi) = \mathbb{E}_{q^{\pi}}[r_{\theta}(x)] - \frac{\beta}{\tau} D_f(q^{\pi} || p_{\mathcal{D}}^{\tau})$$

s.t.
$$\mathbb{E}_{x \sim p_{\mathcal{D}}^{\tau}(x)}[c^*(x)] - \mathbb{E}_{x \sim q^{\pi}(x)}[c^*(x)] \le W_0$$
 (55)

to any arbitrary *f*-divergence metric $D_f(\cdot||\cdot)$ that measures the difference between two probability distributions Q, P over a space Ω defined by $D_f(Q||P) := \int_{\Omega} dP f\left(\frac{dQ}{dP}\right)$ for a convex univariate *generator* function *f*. For example in our main text, we specialize to the KL-divergence where $f_{\text{KL}}(u) := u \log u$ traditionally used in the imitation learning literature.

However, we found that such a naïve approach does *not* generalize well to alternative *f*-divergences: recall that a core contribution of our work was the ability to reformulate the optimization objective as a weighted sum over distribution entropy and divergence (i.e., **Lemma 3.3**) in order to admit an explicit, closed form solution for the dual function in **Lemma 3.4**. Such an approach is intractable using standard algebraic techniques. This is not ideal, as a number of prior works have proposed that alternative divergences—such as the χ^2 -divergence defined by the generator $f_{\chi^2}(u) = (u-1)^2/2$ —can better penalize out-of-distribution surrogate behavior and better quantify model uncertainty when compared to the KL-divergence (Tsybakov, 2008; Nishiyama & Sason, 2020; Ma et al., 2022; Wang et al., 2024).

In this section, we show how to overcome this limitation and demonstrate how our theoretical and empirical results generalize to alternative *f*-divergence objectives for enforcing distribution matching in the sampling policy. Firstly, we look to recent work by Huang et al. (2024a) and others describing 'mixed *f*-regularization' defined by a mixed generator function $f_{\gamma}(u) := \gamma f(u) + u \log u$ for some weighting scalar $\gamma \in [1, +\infty)$, which admits a 'mixed *f*-divergence' given by

$$D_f(Q||P;\gamma) := \gamma D_f(Q||P) + D_{\mathrm{KL}}(Q||P)$$
(56)

Table A3. Additional Model-Based Optimization Diversity Results. Each cell is a value mn/llc; where mn is the Minimum Novelty 1378 and llc the L_1 Coverage. Both metrics are reported mean^(95% confidence interval) across 10 random seeds, where higher is better. Bolded 1379 entries indicate overlapping 95% confidence intervals with the best performing algorithm (according to the mean) per optimizer. Bolded 1380 (resp., <u>Underlined</u>) Rank and Optimality Gap (Opt. Gap) metrics indicate the best (resp., second best) for a given backbone optimizer.

$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	Grad	l. TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	Rank↓	Opt. Gap ↑
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Dataset 7	0.0/0.42	0.0/0.31	0.0/1.42	0.0/0.68	0.0/6.26	0.0/0.58	_/	_/
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	Baselin	e 21.2^(3.0)/0 16 ^(0.1)	51.7^(2.9)/0 20 ^(0.13)	97.4 ^(3.9) /0 21 ^(0.10)	79.5 ^(19.7) /0 42 ^(0.18)	95 0 ^(0.7) /0 00 ^(0.00)	$102^{(6.1)}/0.00^{(0.00)}$	3 3/6 3	74 5/-1 44
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $		$-22.1^{(2.7)}/0.14^{(0.11)}$		97.4 ^(3.9) /0.24 ^(0.11)	89.0 ^(7.7) /0.40 ^(0.10)				
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	COMs	+ 10.9 ^(0.3) /0.49 ^(0.02)	31.7 ^(0.8) /0.31 ^(0.00)	52.4 ^(11.0) /1.11 ^(0.16)	13.7 ^(1.1) /0.61 ^(0.09)	99.6 ^(0.3) /0.37 ^(0.11)	$100^{(0.0)}/0.80^{(0.76)}$	6.2/2.7	51.4/-1.00
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	RoMA						102 ^(6.1) /0.00 ^(0.00)	<u>2.8</u> /5.8	74.5/-1.44
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $,				
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$									
		(1.1) (0.0.0)							
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	DynAM) 21.1 ⁽¹¹⁾ /0.36 ⁽⁰⁰⁾ /	52.2(10)/0.52(000)	98.6 ⁽¹²⁾ /1.46 ⁽⁰¹⁰⁾	85.8(10)/2.49(000)	95.0 ^(6,1) / 6.4 7 ⁽¹¹²⁴⁾	10/(0./)/5.85(100)	2.2/1.3	76.7/1.25
$ \begin{array}{c} \mbox{COMS} & {\bf 23} {\bf 31}^{240}, {\bf 13}^{0100} & {\bf 51} {\bf 64}^{260}, {\bf 02}^{0101} & {\bf 55}^{25}, {\bf 30}, {\bf 24}^{0100} & {\bf 75}, {\bf 30}^{220}, {\bf 100}^{0100}, {\bf 50}^{0110} & {\bf 90}^{010}, {\bf 03}^{0200} & {\bf 03}^{010}, {\bf 03}^{0000} & {\bf 33}, {\bf 06}, {\bf 8}^{-1}, {\bf 27}, {\bf 45}, {\bf 13}^{-1}, {\bf 100}^{000}, {\bf 10}, {\bf 08}^{0000} & {\bf 10}^{0000}, {\bf 00}^{011}, {\bf 03}^{0000} & {\bf 33}, {\bf 06}, {\bf 8}^{-1}, {\bf 27}, {\bf 100}^{-1}, {\bf 100}^{0000} & {\bf 10}^{0000}, {\bf 00}^{011}, {\bf 03}^{0000} & {\bf 33}, {\bf 06}, {\bf 7}^{-1}, {\bf 57}, {\bf 64}, {\bf 91}, {\bf 91}$	Adaı			ChEMBL	Molecule	•	D'Kitty	$\mathbf{Rank} \downarrow$	Opt. Gap↑
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	Baselin		51.1 ^(3.5) /0.22 ^(0.09)			2	100 /0121	3.5/5.8	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$							101 /0100		
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $							///////////////////////////////////////		
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$									
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $									
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$									
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$		(1.0) (0.05)							
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$									
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$			-			=	•	•	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$									
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	com								
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$									
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$									
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$									
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$				95.0 ^(1.5) /2.17 ^(0.06)	72.5 ^(23.6) /1.83 ^(0.15)	85.6 ^(3.0) / 3.37^(0.49)	41.5 ^(2.0) /3.12 ^(0.40)		
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	DynAM	D 12.9 ^(0.8) / 0.40^(0.03)	48.0 ^(1.6) /0.56 ^(0.01)	$96.7^{(3.5)} / 1.82^{(0.72)}$	$81.8^{(13.4)}/2.54^{(0.05)}$	94.5 ^(0.7) / 4.75^(2.16)	$112^{(7.8)}/3.29^{(1.56)}$	4.0/2.2	74.3/0.62
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	CoSyN	E TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	Rank	Opt. Gap ↑
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$								v	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	Baselin	e 24.5 ^(3.5) /0.10 ^(0.07)	49.7 ^(3.1) /0.22 ^(0.10)	98.5 ^(1.6) /0.39 ^(0.20)	86.6 ^(12.7) /0.27 ^(0.13)	93.2 ^(1.0) /0.10 ^(0.00)	•	•	74.1/-1.41
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$		- 15.4 ^(4.9) /0.23 ^(0.09)				93.8^(0.6)/0.07^(0.01)	91.9 ^(2.0) /0.10 ^(0.00) 101 ^(6.3) /0.06 ^(0.00)	<u>3.2</u> /5.3	
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	COMS	$ \begin{array}{r} - & 15.4^{(4.9)} / 0.23^{(0.09)} \\ + & 12.8^{(0.6)} / 0.24^{(0.04)} \end{array} $	$\frac{44.9^{(3.5)}/0.20^{(0.13)}}{42.7^{(1.4)}/\textbf{0.32^{(0.03)}}}$	90.0^(15.2)/ 0.38 ^(0.27) 34.1 ^(14.4) / 1.31^(0.22)	$\frac{86.2^{(7.7)}/0.39^{(0.29)}}{50.0^{(1.9)}/1.39^{(0.24)}}$	93.8 ^(0.6) /0.07 ^(0.01) 87.8 ^(3.1) / 1.29 ^(0.37)	91.9 ^(2.0) /0.10 ^(0.00) 101 ^(6.3) /0.06 ^(0.00) 30.8 ^(5.7) /0.25 ^(0.09)	<u>3.2</u> /5.3 5.0/5.8	71.9/-1.39
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	COMs COMs RoMA	$ \begin{array}{r} - & 15.4^{(4.9)} / 0.23^{(0.09)} \\ + & 12.8^{(0.6)} / 0.24^{(0.04)} \\ - & 24.6^{(3.5)} / 0.10^{(0.07)} \end{array} $	44.9 ^(3.5) /0.20 ^(0.13) 42.7 ^(1.4) / 0.32^(0.03) 49.7^(3.0) /0.22 ^(0.11)	$\begin{array}{l} \textbf{90.0}^{(15.2)} / 0.38^{(0.27)} \\ 34.1^{(14.4)} / \textbf{1.31}^{(0.22)} \\ \textbf{98.6}^{(1.5)} / 0.40^{(0.20)} \end{array}$	86.2 ^(7.7) /0.39 ^(0.29) 50.0 ^(1.9) / 1.39^(0.24) 86.6^(12.7)/0.27^(0.12)	93.8^(0.6)/0.07^(0.01) 87.8 ^(3.1) / 1.29^(0.37) 93.2^(1.0)/0.10^(0.00)	$\begin{array}{c} 91.9^{(2.0)}/0.10^{(0.00)}\\ 101^{(6.3)}/0.06^{(0.00)}\\ 30.8^{(5.7)}/0.25^{(0.09)}\\ 91.9^{(2.0)}/0.10^{(0.00)} \end{array}$	<u>3.2</u> /5.3 5.0/5.8 7.5/ 1.5 2.5 /5.2	71.9/-1.39 43.0/ -0.81 <u>74.1</u> /-1.41
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	COMs COMs RoMA RoMA	$ \begin{array}{r} ^{-} & 15.4^{(4.9)} / 0.23^{(0.09)} \\ ^{+} & 12.8^{(0.6)} / 0.24^{(0.04)} \\ ^{-} & 24.6^{(3.5)} / 0.10^{(0.07)} \\ ^{+} & 17.1^{(3.3)} / 0.22^{(0.05)} \end{array} $	$\begin{array}{l} 44.9^{(3.5)}/0.20^{(0.13)}\\ 42.7^{(1.4)}/\textbf{0.32^{(0.03)}}\\ \textbf{49.7^{(3.0)}}/0.22^{(0.11)}\\ \textbf{49.3^{(3.0)}}/\textbf{0.42^{(0.09)}} \end{array}$	$\begin{array}{l} \textbf{90.0}^{(15.2)} / 0.38^{(0.27)} \\ \textbf{34.1}^{(14.4)} / \textbf{1.31}^{(0.22)} \\ \textbf{98.6}^{(1.5)} / 0.40^{(0.20)} \\ \textbf{99.5}^{(0.9)} / 0.53^{(0.13)} \end{array}$	86.2 ^(7.7) /0.39 ^(0.29) 50.0 ^(1.9) / 1.39^(0.24) 86.6^(12.7) /0.27 ^(0.12) 89.6^(3.4) /0.55 ^(0.22)	93.8 ^(0.6) /0.07 ^(0.01) 87.8 ^(3.1) / 1.29^(0.37) 93.2 ^(1.0) /0.10 ^(0.00) 93.2 ^(1.6) /0.10 ^(0.00)	$\begin{array}{c} 91.9^{(2.0)}/0.10^{(0.00)}\\ 101^{(6.3)}/0.06^{(0.00)}\\ 30.8^{(5.7)}/0.25^{(0.09)}\\ 91.9^{(2.0)}/0.10^{(0.00)}\\ 65.5^{(25.2)}/0.05^{(0.03)} \end{array}$	<u>3.2</u> /5.3 5.0/5.8 7.5/ 1.5 2.5 /5.2 4.0/3.7	71.9/-1.39 43.0/ -0.81 <u>74.1</u> /-1.41 69.0/-1.30
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	COMs COMs RoMA RoMA ROM	$\begin{array}{rcrr} & 15.4^{(4.9)} / 0.23^{(0.09)} \\ & 12.8^{(0.6)} / 0.24^{(0.04)} \\ & 24.6^{(3.5)} / 0.10^{(0.07)} \\ & 17.1^{(3.3)} / 0.22^{(0.05)} \\ & 22.9^{(6.3)} / 0.18^{(0.09)} \end{array}$	44.9 ^(3.5) /0.20 ^(0.13) 42.7 ^(1.4) / 0.32^(0.03) 49.7 ^(3.0) /0.22 ^(0.11) 49.3 ^(3.0) /0.42 ^(0.09) 48.9 ^(1.5) /0.25 ^(0.10)	90.0 ^(15.2) /0.38 ^(0.27) 34.1 ^(14.4) / 1.31^(0.22) 98.6 ^(1.5) /0.40 ^(0.20) 99.5 ^(0.9) /0.53 ^(0.13) 75.8 ^(6.1) / 1.20^(0.21)	86.2 ^(7,7) /0.39 ^(0.29) 50.0 ^(1.9) / 1.39^(0.24) 86.6 ^(12,7) /0.27 ^(0.12) 89.6 ^(3,4) /0.55 ^(0.22) 92.2 ^(3,3) /0.39 ^(0.12)	93.8 ^(0.6) /0.07 ^(0.01) 87.8 ^(3.1) / 1.29 ^(0.37) 93.2 ^(1.0) /0.10 ^(0.00) 93.2 ^(1.6) /0.10 ^(0.00) 84.6 ^(4.4) /0.09 ^(0.00)	$\begin{array}{c} 91.9^{(2.0)}/0.10^{(0.00)}\\ 101^{(6.3)}/0.06^{(0.00)}\\ 30.8^{(5.7)}/0.25^{(0.09)}\\ 91.9^{(2.0)}/0.10^{(0.00)}\\ 65.5^{(25.2)}/0.05^{(0.03)}\\ 31.8^{(5.6)}/0.06^{(0.10)} \end{array}$	<u>3.2/5.3</u> 5.0/5.8 7.5/ 1.5 2.5 /5.2 4.0/3.7 5.0/4.5	71.9/-1.39 43.0/ -0.81 74.1/-1.41 69.0/-1.30 59.4/-1.25
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	COMs COMs RoMA RoMA ROM0 GAMB0	$\begin{array}{rcrr} & 15.4^{(4.9)}/0.23^{(0.09)} \\ & 12.8^{(0.6)}/0.24^{(0.04)} \\ & - & 24.6^{(3.5)}/0.10^{(0.07)} \\ & + & 17.1^{(3.3)}/0.22^{(0.05)} \\ & 0 & 22.9^{(6.3)}/0.18^{(0.09)} \\ & 0 & 22.8^{(2.3)}/0.12^{(0.08)} \end{array}$	44.9 ^(3.5) /0.20 ^(0.13) 42.7 ^(1.4) /0.32 ^(0.03) 49.7 ^(3.0) /0.22 ^(0.11) 49.3 ^(3.0) /0.42 ^(0.09) 48.9 ^(1.5) /0.25 ^(0.10) 50.8 ^(1.5) /0.22 ^(0.15)	$\begin{array}{l} \textbf{90.0}^{(15.2)} / 0.38^{(0.27)} \\ \textbf{34.1}^{(14.4)} / \textbf{1.31}^{(0.22)} \\ \textbf{98.6}^{(1.5)} / 0.40^{(0.20)} \\ \textbf{99.5}^{(0.9)} / 0.53^{(0.13)} \\ \textbf{75.8}^{(6.1)} / \textbf{1.20}^{(0.21)} \\ \textbf{90.8}^{(14.2)} / 0.53^{(0.18)} \end{array}$	86.2 ^(7,7) /0.39 ^(0.29) 50.0 ^(1.9) / 1.39^(0.24) 86.6^(12.7)/0.27^(0.12) 89.6^(3.4)/0.55^(0.22) 92.2^(3.3)/0.39^(0.12) 91.9^(3.4)/0.14^(0.13)	93.8 ^(0.6) /0.07 ^(0.01) 87.8 ^(3.1) / 1.29^(0.37) 93.2^(1.0) /0.10 ^(0.00) 93.2^(1.6) /0.10 ^(0.00) 84.6 ^(4.4) /0.09 ^(0.00) 86.0 ^(3.3) /0.10 ^(0.00)	$\begin{array}{c} 91.9^{(2.0)}/0.10^{(0.00)}\\ 101^{(6.3)}/0.06^{(0.00)}\\ 30.8^{(5.7)}/0.25^{(0.09)}\\ 91.9^{(2.0)}/0.10^{(0.00)}\\ 65.5^{(25.2)}/0.05^{(0.03)}\\ 31.8^{(5.6)}/0.06^{(0.10)}\\ 29.6^{(3.6)}/0.02^{(0.00)}\\ \end{array}$	3.2/5.3 5.0/5.8 7.5/1.5 2.5/5.2 4.0/3.7 5.0/4.5 4.5/6.3	71.9/-1.39 43.0/ -0.81 74.1/-1.41 69.0/-1.30 59.4/-1.25 62.0/-1.42
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	COMs COMs RoMA RoMA ROMG GAMB DynAM	$\begin{array}{rcrr} & 15.4^{(4.9)}/0.23^{(0.09)} \\ & & 12.8^{(0.6)}/0.24^{(0.04)} \\ & & & 24.6^{(3.5)}/0.10^{(0.07)} \\ & & & 17.1^{(3.3)}/0.22^{(0.05)} \\ & & & 22.9^{(6.3)}/0.18^{(0.09)} \\ & & & & 22.8^{(2.8)}/0.12^{(0.08)} \\ & & & & & \\ & & & & & & \\ & & & & & $	$\begin{array}{c} 44.9^{(3.5)}/0.20^{(0.13)}\\ 42.7^{(1.4)}/0.32^{(0.03)}\\ 49.7^{(3.0)}/0.22^{(0.11)}\\ 49.3^{(3.0)}/0.42^{(0.09)}\\ 48.9^{(1.5)}/0.25^{(0.15)}\\ 50.8^{(1.5)}/0.22^{(0.15)}\\ 48.4^{(2.3)}/0.18^{(0.09)} \end{array}$	$\begin{array}{l} \textbf{90.0}^{(15.2)} / 0.38^{(0.27)} \\ 34.1^{(14.4)} / \textbf{1.31}^{(0.22)} \\ \textbf{98.6}^{(15)} / 0.40^{(0.20)} \\ \textbf{99.5}^{(0.9)} / 0.53^{(0.13)} \\ 75.8^{(6.1)} / \textbf{1.20}^{(0.21)} \\ \textbf{90.8}^{(14.2)} / 0.53^{(0.18)} \\ \textbf{96.7}^{(3.5)} / 0.64^{(0.42)} \end{array}$	$\begin{array}{l} \textbf{86.2}^{(7.7)} / 0.39^{(0.29)} \\ 50.0^{(1.9)} / \textbf{1.39}^{(0.24)} \\ \textbf{86.6}^{(12.7)} / 0.27^{(0.12)} \\ \textbf{89.6}^{(3.4)} / 0.55^{(0.22)} \\ \textbf{92.2}^{(3.3)} / 0.39^{(0.12)} \\ \textbf{91.9}^{(3.4)} / 0.14^{(0.13)} \\ \textbf{80.2}^{(12.9)} / 0.43^{(0.34)} \end{array}$	$\begin{array}{l} \textbf{93.8}^{(0.6)}/(0.07^{(0.01)}\\ 87.8^{(3.1)}/\textbf{1.29}^{(0.37)}\\ \textbf{93.2}^{(1.0)}/(0.10^{(0.00)}\\ \textbf{93.2}^{(1.6)}/(0.10^{(0.00)}\\ 84.6^{(4.4)}/(0.09^{(0.00)}\\ 86.0^{(3.3)}/(0.10^{(0.00)}\\ \textbf{94.5}^{(0.7)}/\textbf{1.85}^{(0.22)}\\ \end{array}$	$\begin{array}{c} 91.9^{(2.0)}/0.10^{(0.00)}\\ \textbf{101}^{(6.3)}/0.06^{(0.00)}\\ 30.8^{(5.7)}/0.25^{(0.09)}\\ 91.9^{(2.0)}/0.10^{(0.00)}\\ 65.5^{(25.2)}/0.05^{(0.03)}\\ 31.8^{(5.6)}/0.06^{(0.10)}\\ 29.6^{(3.6)}/0.02^{(0.00)}\\ \textbf{112}^{(7.8)}/0.94^{(0.17)}\\ \end{array}$	3.2/5.3 5.0/5.8 7.5/1.5 2.5/5.2 4.0/3.7 5.0/4.5 4.5/6.3 4.0/ <u>3.3</u>	71.9/-1.39 43.0/- 0.81 74.1/-1.41 69.0/-1.30 59.4/-1.25 62.0/-1.42 75.0/ <u>-0.90</u>
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	COMS COMS RoMA RoMA GAMB DynAM BO-qE	- 15.4 ^(4.9) /0.23 ^(0.09) + 12.8 ^(0.6) /0.24 ^(0.04) - 24.6 ^(3.5) /0.10 ^(0.07) + 17.1 ^(3.3) /0.22 ^(0.05) 0 22.9 ^(6.3) /0.18 ^(0.09) 0 22.8 ^(2.8) /0.12 ^(0.08) 0 17.8 ^(5.5) /0.21 ^(0.11) I TFBind8	44.9 ^(3.5) /0.20 ^(0.13) 42.7 ^(1.4) / 0.32^(0.03) 49.7 ^(3.0) /0.22 ^(0.11) 49.3 ^(3.0) /0.42 ^(0.09) 48.9 ^(1.5) /0.25 ^(0.10) 50.8 ^(1.5) /0.22 ^(0.15) 48.4 ^(2.3) /0.18 ^(0.09) UTR	90.0 ^(15.2) /0.38 ^(0.27) 34.1 ^(14.4) /1.31 ^(0.22) 98.6 ^(1.5) /0.40 ^(0.20) 99.5 ^(0.9) /0.53 ^(0.13) 75.8 ^(6.1) /1.20 ^(0.21) 90.8 ^(14.2) /0.53 ^(0.18) 96.7 ^(3.5) /0.64 ^(0.42)	86.2 ^(7,7) /0.39 ^(0,29) 50.0 ^(1,9) /1.39 ^(0,24) 86.6 ^(12,7) /0.27 ^(0,12) 89.6 ^(3,4) /0.55 ^(0,22) 92.2 ^(3,3) /0.39 ^(0,12) 91.9 ^(3,4) /0.14 ^(0,13) 80.2 ^(12,9) /0.43 ^(0,34)	93.8 ^(0.6) /0.07 ^(0.01) 87.8 ^(3.1) /1.29 ^(0.37) 93.2 ^(1.0) /0.10 ^(0.00) 93.2 ^(1.6) /0.10 ^(0.00) 84.6 ^(4.4) /0.09 ^(0.00) 86.0 ^(3.3) /0.10 ^(0.00) 94.5 ^(0.7) /1.85 ^(0.22) Superconductor	91.9 ^(2.0) /0.10 ^(0.00) 101 ^(6.3) /0.06 ^(0.00) 30.8 ^(5.7) /0.25 ^(0.09) 91.9 ^(2.0) /0.10 ^(0.00) 65.5 ^(25.2) /0.05 ^(0.03) 31.8 ^(5.6) /0.06 ^(0.10) 29.6 ^(3.6) /0.02 ^(0.00) 112 ^(7.8) /0.94 ^(0.17) D'Kitty	3.2/5.3 5.0/5.8 7.5/1.5 2.5/5.2 4.0/3.7 5.0/4.5 4.5/6.3 4.0/ <u>3.3</u> Rank↓	71.9/-1.39 43.0/-0.81 74.1/-1.41 69.0/-1.30 59.4/-1.25 62.0/-1.42 75.0/-0.90
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	COMS COMS RoMA ROMA GAMB DynAMO BO-qE Baselin	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{r} 44.9^{(3.5)}/0.20^{(0.13)}\\ 42.7^{(1.4)}/0.32^{(0.03)}\\ 49.7^{(3.0)}/0.22^{(0.11)}\\ 49.3^{(3.0)}/0.42^{(0.09)}\\ 48.9^{(1.5)}/0.25^{(0.10)}\\ 50.8^{(1.5)}/0.22^{(0.15)}\\ 48.4^{(2.3)}/0.18^{(0.09)}\\ \hline UTR\\ 51.5^{(0.3)}/0.55^{(0.01)}\\ \end{array}$	90.0 ^(15.2) /0.38 ^(0.27) 34.1 ^(14.4) /1.31 ^(0.22) 98.6 ^(1.5) /0.40 ^(0.20) 99.5 ^(0.9) /0.53 ^(0.13) 75.8 ^(6.1) /1.20 ^(0.21) 90.8 ^(14.2) /0.53 ^(0.18) 96.7 ^(3.5) /0.64 ^(0.42) ChEMBL 97.6 ^(0.3) /2.37 ^(0.03)	86.2 ^(7,7) /0.39 ^(0,29) 50.0 ^(1,9) /1.39 ^(0,24) 86.6 ^(12,7) /0.27 ^(0,12) 89.6 ^(3,4) /0.55 ^(0,22) 92.2 ^(3,3) /0.39 ^(0,12) 91.9 ^(3,4) /0.14 ^(0,13) 80.2 ^(12,9) /0.43 ^(0,34) Molecule 85.4 ^(1,5) /2.11 ^(0,15)	93.8 ^(0.6) /0.07 ^(0.01) 87.8 ^(3.1) /1.29 ^(0.37) 93.2 ^(1.0) /0.10 ^(0.00) 93.2 ^(1.6) /0.10 ^(0.00) 84.6 ^(4.4) /0.09 ^(0.00) 86.0 ^(3.3) /0.10 ^(0.00) 94.5 ^(0.7) /1.85 ^(0.22) Superconductor 94.6 ^(0.1) /7.84 ^(0.01)	$\begin{array}{c} 91.9^{(2.0)}/0.10^{(0.00)}\\ 101^{(6.3)}/0.06^{(0.00)}\\ 30.8^{(5.7)}/0.25^{(0.09)}\\ 91.9^{(2.0)}/0.10^{(0.00)}\\ 65.5^{(25.2)}/0.05^{(0.03)}\\ 31.8^{(5.6)}/0.06^{(0.10)}\\ 29.6^{(3.6)}/0.02^{(0.00)}\\ 112^{(7.8)}/0.94^{(0.17)}\\ \hline D'Kitty\\ 106^{(2.9)}/6.61^{(0.33)}\\ \end{array}$	3.2/5.3 5.0/5.8 7.5/1.5 2.5/5.2 4.0/3.7 5.0/4.5 4.5/6.3 4.0/ <u>3.3</u> Rank↓ 3.3/5.0	71.9/-1.39 43.0/-0.81 74.1/-1.41 69.0/-1.30 59.4/-1.25 62.0/-1.42 75.0/-0.90 Opt. Gap ↑ 76.2/1.70
$ \begin{array}{c c c c c c c c c c c c c c c c c c c $	COMS COMS RoMA ROMA GAMBG DynAMG BO-qE Baselin COMS	$\begin{array}{rcrr} & 15.4^{(4.9)}/0.23^{(0.09)} \\ & 12.8^{(0.6)}/0.24^{(0.04)} \\ & - & 24.6^{(3.5)}/0.10^{(0.07)} \\ & 17.1^{(3.3)}/0.22^{(0.05)} \\ & 22.9^{(6.3)}/0.18^{(0.09)} \\ & 22.8^{(2.8)}/0.12^{(0.08)} \\ & 0 & 17.8^{(5.5)}/0.21^{(0.11)} \\ \hline \\ \hline & \\ \hline \hline & \\ \hline \hline & \\ \hline \hline & \\ \hline \hline & \hline \hline \\ \hline & \hline \hline \\ \hline \hline \\ \hline \hline \\ \hline \hline \\ \hline \hline \hline \\ \hline \hline \hline \hline \\ \hline \hline \hline \\ \hline \hline \hline \hline \\ \hline \hline \hline \hline \hline \\ \hline \hline \hline \hline \hline \hline \\ \hline \hline$	$\begin{array}{c} 44.9^{(3.5)}/0.20^{(0.13)}\\ 42.7^{(1.4)}/0.32^{(0.03)}\\ 49.7^{(3.0)}/0.22^{(0.11)}\\ 49.3^{(3.0)}/0.42^{(0.09)}\\ 48.9^{(1.5)}/0.25^{(0.10)}\\ 50.8^{(1.5)}/0.22^{(0.15)}\\ 48.4^{(2.3)}/0.18^{(0.09)}\\ \hline \\ \hline \\ UTR\\ 51.5^{(0.3)}/0.55^{(0.01)}\\ 51.8^{(0.2)}/0.56^{(0.01)}\\ \hline \end{array}$	90.0 ^(15.2) /0.38 ^(0.27) 34.1 ^(14.4) /1.31 ^(0.22) 98.6 ^(1.5) /0.40 ^(0.20) 99.5 ^(0.9) /0.53 ^(0.13) 75.8 ^(6.1) /1.20 ^(0.21) 90.8 ^(14.2) /0.53 ^(0.18) 96.7 ^(3.5) /0.64 ^(0.42) ChEMBL 97.6 ^(0.3) /2.37 ^(0.03) 97.3 ^(0.5) /2.44 ^(0.05)	86.2 ^(7,7) /0.39 ^(0,29) 50.0 ^(1.9) /1.39 ^(0,24) 86.6 ^(12,7) /0.27 ^(0,12) 89.6 ^(3.4) /0.55 ^(0,22) 92.2 ^(3.3) /0.39 ^(0,12) 91.9 ^(3.4) /0.14 ^(0,13) 80.2 ^(12,9) /0.43 ^(0,34) Molecule 85.4 ^(1.5) /2.11 ^(0,15) 85.2 ^(0.5) /2.55 ^(0.02)	93.8 ^(0.6) /0.07 ^(0.01) 87.8 ^(3.1) /1.29 ^(0.37) 93.2 ^(1.0) /0.10 ^(0.00) 93.2 ^(1.0) /0.10 ^(0.00) 84.6 ^(4.4) /0.09 ^(0.00) 86.0 ^(3.3) /0.10 ^(0.00) 94.5 ^(0.7) /1.85 ^(0.22) Superconductor 94.6 ^(0.1) /7.84 ^(0.01) 92.5 ^(1.2) /7.61 ^(0.24)	$\begin{array}{c} 91.9^{(2.0)}/0.10^{(0.00)}\\ 101^{(6.3)}/0.06^{(0.00)}\\ 30.8^{(5.7)}/0.25^{(0.09)}\\ 91.9^{(2.0)}/0.10^{(0.00)}\\ 65.5^{(25.2)}/0.05^{(0.03)}\\ 31.8^{(5.6)}/0.06^{(0.10)}\\ 29.6^{(3.6)}/0.02^{(0.00)}\\ 112^{(7.8)}/0.94^{(0.17)}\\ \hline D'Kitty\\ 106^{(2.9)}/6.61^{(0.33)}\\ 105^{(1.6)}/7.19^{(0.22)}\\ \end{array}$	$\frac{3.2/5.3}{5.0/5.8}$ 7.5/1.5 2.5/5.2 4.0/3.7 5.0/4.5 4.5/6.3 4.0/ <u>3.3</u> Rank \downarrow 3.3/5.0 4.0/ <u>3.0</u>	71.9/-1.39 43.0/-0.81 74.1/-1.41 69.0/-1.30 59.4/-1.25 62.0/-1.42 75.0/-0.90 Opt. Gap ↑ 75.6/1.85
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	COMS COMS RoMA ROMA GAMB DynAMA BO-qE Baselin COMS COMS	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{c} 44.9^{(3.5)}/0.20^{(0.13)}\\ 42.7^{(1.4)}/0.32^{(0.03)}\\ 49.7^{(3.0)}/0.22^{(0.11)}\\ 49.3^{(3.0)}/0.42^{(0.09)}\\ 48.9^{(1.5)}/0.25^{(0.10)}\\ 50.8^{(1.5)}/0.22^{(0.15)}\\ 48.4^{(2.3)}/0.18^{(0.09)}\\ \hline \\ \hline \\ \hline \\ \hline \\ 51.5^{(0.3)}/0.55^{(0.01)}\\ 51.8^{(0.2)}/0.55^{(0.01)}\\ 43.2^{(0.2)}/0.57^{(0.01)}\\ \end{array}$	90.0 ^(15.2) /0.38 ^(0.27) 34.1 ^(14.4) /1.31 ^(0.22) 98.6 ^(1.5) /0.40 ^(0.20) 99.5 ^(0.0) /0.53 ^(0.13) 75.8 ^(6.1) /1.20 ^(0.21) 90.8 ^(14.2) /0.53 ^(0.18) 96.7 ^(3.5) /0.64 ^(0.42) ChEMBL 97.6 ^(0.3) /2.37 ^(0.03) 97.3 ^(0.5) /2.44 ^(0.05) 83.3 ^(2.1) /2.50 ^(0.05)	$\begin{array}{c} \textbf{86.2}^{(7.7)} / 0.39^{(0.29)} \\ 50.0^{(1.9)} / \textbf{1.39}^{(0.24)} \\ \textbf{86.6}^{(12.7)} / 0.27^{(0.12)} \\ \textbf{89.6}^{(3.4)} / 0.55^{(0.22)} \\ \textbf{92.2}^{(3.3)} / 0.39^{(0.12)} \\ \textbf{91.9}^{(3.4)} / 0.14^{(0.13)} \\ \textbf{80.2}^{(12.9)} / 0.43^{(0.34)} \\ \hline \\ \hline \\ \hline \\ \textbf{Molecule} \\ \hline \\ \textbf{85.4}^{(1.5)} / \textbf{2.11}^{(0.15)} \\ \textbf{85.2}^{(0.5)} / \textbf{2.55}^{(0.02)} \\ \textbf{79.4}^{(1.3)} / \textbf{2.41}^{(0.07)} \\ \end{array}$	$\begin{array}{l} \textbf{93.8}^{(0.6)}/(0.07^{(0.01)}\\ 87.8^{(3.1)}/1.29^{(0.37)}\\ \textbf{93.2}^{(1.0)}/(0.10^{(0.00)}\\ \textbf{93.2}^{(1.6)}/(0.10^{(0.00)}\\ \textbf{84.6}^{(4.4)}/(0.09^{(0.00)}\\ \textbf{86.0}^{(3.3)}/(0.10^{(0.00)}\\ \textbf{94.5}^{(0.7)}/1.85^{(0.22)}\\ \hline \textbf{Superconductor}\\ \textbf{94.6}^{(0.1)}/7.84^{(0.01)}\\ \textbf{92.5}^{(1.2)}/7.61^{(0.24)}\\ \textbf{85.5}^{(0.4)}/7.50^{(0.01)}\\ \end{array}$	$\begin{array}{c} 91.9^{(2.0)}/0.10^{(0.00)}\\ 101^{(6.3)}/0.06^{(0.00)}\\ 30.8^{(5.7)}/0.25^{(0.09)}\\ 91.9^{(2.0)}/0.10^{(0.00)}\\ 65.5^{(25.2)}/0.05^{(0.03)}\\ 31.8^{(5.6)}/0.06^{(0.10)}\\ 29.6^{(3.6)}/0.02^{(0.00)}\\ 112^{(7.8)}/0.94^{(0.17)}\\ \hline D'Kitty\\ 106^{(2.9)}/6.61^{(0.33)}\\ 105^{(1.6)}/7.19^{(0.22)}\\ 35.5^{(1.2)}/1.66^{(0.01)}\\ \end{array}$	$\begin{array}{c} 3.2/5.3\\ 5.0/5.8\\ 7.5/1.5\\ 2.5/5.2\\ 4.0/3.7\\ 5.0/4.5\\ 4.5/6.3\\ 4.0/3.3\\ \hline \mathbf{Rank} \downarrow\\ 3.3/5.0\\ 4.0/3.0\\ 7.5/3.8\\ \end{array}$	71.9/-1.39 43.0/-0.81 74.1/-1.41 69.0/-1.30 59.4/-1.25 62.0/-1.42 75.0/-0.90 Opt. Gap ↑ 76.2/1.70 75.6/1.85 56.6/0.90
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	COMS COMS RoMA ROMA GAMB DynAMA BO-qE Baselin COMS COMS RoMA	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{c} 44.9^{(3.5)}/0.20^{(0.13)}\\ 42.7^{(1.4)}/0.32^{(0.03)}\\ 49.7^{(3.0)}/0.22^{(0.11)}\\ 49.3^{(3.0)}/0.42^{(0.09)}\\ 48.9^{(1.5)}/0.25^{(0.10)}\\ 50.8^{(1.5)}/0.22^{(0.15)}\\ 48.4^{(2.3)}/0.18^{(0.09)}\\ \hline \\ \hline \\ \hline \\ \hline \\ \hline \\ \hline \\ 51.5^{(0.3)}/0.55^{(0.01)}\\ 51.8^{(0.2)}/0.55^{(0.01)}\\ 51.8^{(0.2)}/0.55^{(0.01)}\\ 51.8^{(0.2)}/0.55^{(0.01)}\\ 51.7^{(0.3)}/0.55^{(0.02)}\\ \hline \end{array}$	90.0 ^(15.2) /0.38 ^(0.27) 34.1 ^(14.4) /1.31 ^(0.22) 98.6 ^(1.5) /0.40 ^(0.20) 99.5 ^(0.9) /0.53 ^(0.13) 75.8 ^(6.1) /1.20 ^(0.21) 90.8 ^(14.2) /0.53 ^(0.18) 96.7 ^(3.5) /0.64 ^(0.42) ChEMBL 97.6 ^(0.3) /2.37 ^(0.03) 97.3 ^(0.5) /2.44 ^(0.05) 83.3 ^(2.1) /2.50 ^(0.05) 97.7 ^(0.5) /2.41 ^(0.04)	$\begin{array}{c} \textbf{86.2}^{(7.7)} / 0.39^{(0.29)} \\ 50.0^{(1.9)} / \textbf{1.39}^{(0.24)} \\ \textbf{86.6}^{(12.7)} / 0.27^{(0.12)} \\ \textbf{89.6}^{(3.4)} / 0.55^{(0.22)} \\ \textbf{92.2}^{(3.3)} / 0.39^{(0.12)} \\ \textbf{91.9}^{(3.4)} / 0.14^{(0.13)} \\ \textbf{80.2}^{(12.9)} / 0.43^{(0.34)} \\ \hline \\ \hline \\ \hline \\ \textbf{Molecule} \\ \hline \\ \textbf{85.4}^{(1.5)} / \textbf{2.11}^{(0.15)} \\ \textbf{85.2}^{(0.5)} / \textbf{2.55}^{(0.02)} \\ \textbf{79.4}^{(1.3)} / \textbf{2.41}^{(0.07)} \\ \textbf{85.9}^{(1.1)} / 0.52^{(0.02)} \\ \end{array}$	93.8 ^(0.6) /0.07 ^(0.01) 87.8 ^(3.1) /1.29 ^(0.37) 93.2 ^(1.6) /0.10 ^(0.00) 93.2 ^(1.6) /0.10 ^(0.00) 84.6 ^(4.4) /0.09 ^(0.00) 86.0 ^(3.3) /0.10 ^(0.00) 94.5 ^(0.7) /1.85 ^(0.22) Superconductor 94.6 ^(0.1) /7.84 ^(0.01) 92.5 ^(1.2) /7.61 ^(0.24) 85.5 ^(0.4) /7.50 ^(0.01) 94.6 ^(0.1) /7.84 ^(0.01)	91.9 ^(2.0) /0.10 ^(0.00) 101 ^(6.3) /0.06 ^(0.00) 30.8 ^(5.7) /0.25 ^(0.09) 91.9 ^(2.0) /0.10 ^(0.00) 65.5 ^(25.2) /0.05 ^(0.03) 31.8 ^(5.6) /0.06 ^(0.10) 29.6 ^(3.6) /0.02 ^(0.00) 112 ^(7.8) /0.94 ^(0.17) D'Kitty 106 ^(2.9) /6.61 ^(0.33) 105 ^(1.6) /7.19 ^(0.22) 35.5 ^(1.2) /1.66 ^(0.01) 105 ^(3.5) /6.45 ^(0.66)	$\begin{array}{c} 3.2/5.3\\ 5.0/5.8\\ 7.5/1.5\\ 2.5/5.2\\ 4.0/3.7\\ 5.0/4.5\\ 4.5/6.3\\ 4.0/3.3\\ \hline \mathbf{Rank}\downarrow\\ \hline 3.3/5.0\\ 4.0/\underline{3.0}\\ 7.5/3.8\\ \underline{3.2}/5.2\\ \end{array}$	$\overline{71.9/-1.39}$ 43.0/-0.81 74.1/-1.41 69.0/-1.30 59.4/-1.25 62.0/-1.42 75.0/-0.90 Opt. Gap \uparrow $\overline{76.2/1.70}$ 75.6/1.85 56.6/0.90 76.1/1.42
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	COMS COMS RoMA ROMA GAMBO DynAMO Baselin COMS COMS RoMA RoMA	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{c} 44.9^{(3.5)}/0.20^{(0.13)}\\ 42.7^{(1.4)}/0.32^{(0.03)}\\ 49.7^{(3.0)}/0.22^{(0.11)}\\ 49.3^{(3.0)}/0.42^{(0.09)}\\ 48.9^{(1.5)}/0.25^{(0.10)}\\ 50.8^{(1.5)}/0.22^{(0.15)}\\ 48.4^{(2.3)}/0.18^{(0.09)}\\ \hline \\ \hline \\ \hline \\ \hline \\ \hline \\ \hline \\ 51.5^{(0.3)}/0.55^{(0.01)}\\ 51.8^{(0.2)}/0.55^{(0.01)}\\ 51.7^{(0.3)}/0.55^{(0.02)}\\ 45.0^{(0.2)}/0.56^{(0.01)}\\ \hline \end{array}$	90.0 ^(15.2) /0.38 ^(0.27) 34.1 ^(14.4) /1.31 ^(0.22) 98.6 ^(1.5) /0.40 ^(0.20) 99.5 ^(0.9) /0.53 ^(0.13) 75.8 ^(6.1) /1.20 ^(0.21) 90.8 ^(14.2) /0.53 ^(0.18) 96.7 ^(3.5) /0.64 ^(0.42) ChEMBL 97.6 ^(0.3) /2.37 ^(0.03) 97.3 ^(0.5) /2.44 ^(0.05) 83.3 ⁽²¹⁾ /2.50 ^(0.05) 97.7 ^(0.5) /2.41 ^(0.04) 98.5 ^(0.4) /1.86 ^(0.05)	$\begin{array}{c} \textbf{86.2}^{(7.7)} / 0.39^{(0.29)} \\ 50.0^{(1.9)} / \textbf{1.39}^{(0.24)} \\ \textbf{86.6}^{(12.7)} / 0.27^{(0.12)} \\ \textbf{89.6}^{(3.4)} / 0.55^{(0.22)} \\ \textbf{92.2}^{(3.3)} / 0.39^{(0.12)} \\ \textbf{91.9}^{(3.4)} / 0.14^{(0.13)} \\ \textbf{80.2}^{(12.9)} / 0.43^{(0.34)} \\ \hline \\ \hline \\ \hline \\ \hline \\ \textbf{Molecule} \\ \hline \\ \textbf{85.4}^{(1.5)} / \textbf{2.11}^{(0.15)} \\ \textbf{85.2}^{(0.5)} / \textbf{2.55}^{(0.02)} \\ \textbf{79.4}^{(1.3)} / \textbf{2.41}^{(0.07)} \\ \textbf{85.9}^{(1.1)} / 0.52^{(0.02)} \\ \textbf{88.2}^{(0.6)} / 1.99^{(0.06)} \\ \hline \end{array}$	93.8 ^(0.6) /0.07 ^(0.01) 87.8 ^(3.1) /1.29 ^(0.37) 93.2 ^(1.6) /0.10 ^(0.00) 93.2 ^(1.6) /0.10 ^(0.00) 84.6 ^(4.4) /0.09 ^(0.00) 86.0 ^(3.3) /0.10 ^(0.00) 94.5 ^(0.7) /1.85 ^(0.22) Superconductor 94.6 ^(0.1) /7.84 ^(0.01) 92.5 ^(1.2) /7.61 ^(0.24) 85.5 ^(0.4) /7.50 ^(0.01) 94.3 ^(0.1) /7.84 ^(0.01)	$\begin{array}{c} 91.9^{(2.0)}/0.10^{(0.00)}\\ 101^{(6.3)}/0.06^{(0.00)}\\ 30.8^{(5.7)}/0.25^{(0.09)}\\ 91.9^{(2.0)}/0.10^{(0.00)}\\ 65.5^{(25.2)}/0.05^{(0.03)}\\ 31.8^{(5.6)}/0.06^{(0.10)}\\ 29.6^{(3.6)}/0.02^{(0.00)}\\ 112^{(7.8)}/0.94^{(0.17)}\\ \hline D'Kitty\\ 106^{(2.9)}/6.61^{(0.33)}\\ 105^{(1.6)}/7.19^{(0.22)}\\ 35.5^{(1.2)}/1.66^{(0.01)}\\ 105^{(3.5)}/6.45^{(0.66)}\\ 116^{(2.5)}/7.09^{(0.49)}\\ \end{array}$	$\begin{array}{r} 3.2/5.3\\ 5.0/5.8\\ 7.5/1.5\\ 2.5/5.2\\ 4.0/3.7\\ 5.0/4.5\\ 4.5/6.3\\ 4.0/\underline{3.3}\\ \hline \textbf{Rank}\downarrow\\ 3.3/5.0\\ 4.0/\underline{3.0}\\ 7.5/3.8\\ \underline{3.2/5.2}\\ 3.7/5.0\\ \end{array}$	$\overline{71.9/-1.39}$ $43.0/-0.81$ $74.1/-1.41$ $69.0/-1.30$ $59.4/-1.25$ $62.0/-1.42$ $75.0/-0.90$ $Opt. Gap \uparrow$ $\overline{76.2/1.70}$ $75.6/1.85$ $56.6/0.90$ $76.1/1.42$ $76.0/1.67$
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	COMS COMS RoMA ROMA GAMBI DynAMO BO-qE Baselin COMS COMS RoMA ROMA	$\begin{array}{rcrr} & 15.4^{(4.9)}/0.23^{(0.09)} \\ & 12.8^{(0.6)}/0.24^{(0.04)} \\ & - 24.6^{(3.5)}/0.10^{(0.07)} \\ & 17.1^{(3.3)}/0.22^{(0.05)} \\ & 0 & 22.9^{(6.3)}/0.12^{(0.08)} \\ & 0 & 22.8^{(2.3)}/0.12^{(0.08)} \\ & 0 & 22.8^{(2.3)}/0.21^{(0.11)} \\ \hline \mbox{I} & TFBind8 \\ e & 21.8^{(0.5)}/0.41^{(0.02)} \\ & - 21.9^{(0.5)}/0.41^{(0.03)} \\ & 12.7^{(0.4)}/0.44^{(0.01)} \\ & 13.6^{(0.3)}/0.31^{(0.02)} \\ & - 15.6^{(0.4)}/0.39^{(0.02)} \\ \end{array}$	$\begin{array}{c} 44.9^{(3.5)}/0.20^{(0.13)}\\ 42.7^{(1.4)}/0.32^{(0.03)}\\ 49.7^{(3.0)}/0.22^{(0.11)}\\ 49.3^{(3.0)}/0.42^{(0.00)}\\ 48.9^{(1.5)}/0.22^{(0.15)}\\ 48.4^{(2.3)}/0.18^{(0.09)}\\ \hline \\ \hline$	90.0 ^(15.2) /0.38 ^(0.27) 34.1 ^(14.4) /1.31 ^(0.22) 98.6 ^(1.5) /0.40 ^(0.20) 99.5 ^(0.9) /0.53 ^(0.13) 75.8 ^(6.1) /1.20 ^(0.21) 90.8 ^(14.2) /0.53 ^(0.18) 96.7 ^(3.5) /0.64 ^(0.42) 75.8 ^(6.1) /2.37 ^(0.03) 97.3 ^(0.5) /2.44 ^(0.05) 83.3 ^(2.1) /2.50 ^(0.05) 87.7 ^(1.3) /2.50 ^(0.03) 87.7 ^(1.3) /2.50 ^(0.03) 87.7 ^(1.3) /2.50 ^(0.03) 87.7 ^(1.3) /2.50 ^(0.03) 87.7 ^(1.3) /2.50 ^(0.03) 87.8 ^(0.3) /2.38 ^(0.10)	86.2 ^(7,7) /0.39 ^(0,29) 50.0 ^(1,9) /1.39 ^(0,24) 86.6 ^(12,7) /0.27 ^(0,12) 89.6 ^(3,4) /0.55 ^(0,22) 92.2 ^(3,3) /0.39 ^(0,12) 91.9 ^(3,4) /0.14 ^(0,13) 80.2 ^(12,9) /0.43 ^(0,34) Molecule 85.4 ^(1,5) /2.11 ^(0,15) 85.2 ^(0,5) /2.55 ^(0,02) 79.4 ^(1,3) /2.41 ^(0,07) 85.9 ^(1,1) /0.52 ^(0,02) 88.2 ^(0,6) /1.99 ^(0,06) 87.9 ^(1,0) /2.48 ^(0,05)	93.8 ^(0.6) /0.07 ^(0.01) 87.8 ^(3.1) /1.29 ^(0.37) 93.2 ^(1.6) /0.10 ^(0.00) 93.2 ^(1.6) /0.10 ^(0.00) 84.6 ^(4.4) /0.09 ^(0.00) 86.0 ^(3.3) /0.10 ^(0.00) 94.5 ^(0.7) /1.85 ^(0.22) Superconductor 94.6 ^(0.1) /7.84 ^(0.01) 92.5 ^(1.2) /7.61 ^(0.24) 85.5 ^(0.4) /7.50 ^(0.01) 94.6 ^(0.1) /7.84 ^(0.01) 94.3 ^(0.1) /7.8 ^(0.01) 94.3 ^(0.1) /7.8 ^(0.01) 86.6 ^(2.2) /7.51 ^(0.09)	$\begin{array}{c} 91.9^{(2.0)}/0.10^{(0.00)}\\ 101^{(6.3)}/0.06^{(0.00)}\\ 30.8^{(5.7)}/0.25^{(0.09)}\\ 91.9^{(2.0)}/0.10^{(0.00)}\\ 65.5^{(25.2)}/0.05^{(0.03)}\\ 31.8^{(5.6)}/0.06^{(0.00)}\\ 12^{(6.3)}/0.02^{(0.00)}\\ 112^{(7.8)}/0.94^{(0.17)}\\ \hline D'Kitty\\ 106^{(2.9)}/6.61^{(0.33)}\\ 105^{(1.6)}/7.19^{(0.22)}\\ 35.5^{(1.2)}/1.66^{(0.01)}\\ 105^{(3.5)}/6.45^{(0.66)}\\ 116^{(2.5)}/7.09^{(0.49)}\\ 30.8^{(2.5)}/2.14^{(1.34)}\\ \end{array}$	$\begin{array}{r} 3.2/5.3\\ 5.0/5.8\\ 7.5/1.5\\ 2.5/5.2\\ 4.0/3.7\\ 5.0/4.5\\ 4.5/6.3\\ 4.0/\underline{3.3}\\ \hline \textbf{Rank} \downarrow \\ 3.3/5.0\\ 4.0/\underline{3.0}\\ 7.5/3.8\\ \underline{3.2/5.2}\\ 3.7/5.0\\ 5.5/5.3\\ \end{array}$	$\overline{71.9}/-1.39$ $43.0/-0.81$ $74.1/-1.41$ $69.0/-1.30$ $59.4/-1.25$ $62.0/-1.42$ $75.0/-0.90$ $\overline{0pt. Gap \uparrow}$ $\overline{76.2}/1.70$ $75.6/1.85$ $56.6/0.90$ $76.1/1.42$ $76.0/1.67$ $59.3/0.98$
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$	COMS COMS RoMA ROMA GAMB DynAM BO-qF Baselin COMS COMS RoMA ROMA ROMA	$\begin{array}{rcrr} & 15.4^{(4.9)}/0.23^{(0.09)} \\ & 12.8^{(0.6)}/0.24^{(0.04)} \\ & - 24.6^{(3.5)}/0.10^{(0.07)} \\ & 17.1^{(3.3)}/0.22^{(0.05)} \\ & 0 & 22.9^{(6.3)}/0.18^{(0.09)} \\ & 0 & 22.8^{(2.3)}/0.12^{(0.08)} \\ & 0 & 22.8^{(2.3)}/0.12^{(0.08)} \\ & 17.8^{(5.5)}/0.21^{(0.11)} \\ \hline \\ $	$\begin{array}{c} 44.9^{(3.5)}/0.20^{(0.13)}\\ 42.7^{(1.4)}/0.32^{(0.03)}\\ 49.7^{(3.0)}/0.22^{(0.11)}\\ 49.3^{(3.0)}/0.42^{(0.00)}\\ 48.9^{(1.5)}/0.22^{(0.15)}\\ 48.4^{(2.3)}/0.18^{(0.09)}\\ \hline \\ \hline$	90.0 ^(15.2) /0.38 ^(0.27) 34.1 ^(14.4) /1.31 ^(0.22) 98.6 ^(1.5) /0.40 ^(0.20) 99.5 ^(0.9) /0.53 ^(0.13) 75.8 ^(6.1) /1.20 ^(0.21) 90.8 ^(14.2) /0.53 ^(0.18) 96.7 ^(3.5) /0.64 ^(0.42) 75.8 ^(6.1) /2.37 ^(0.03) 97.3 ^(0.5) /2.44 ^(0.05) 83.3 ^(2.1) /2.50 ^(0.05) 87.7 ^(1.3) /2.50 ^(0.03) 87.7 ^(1.3) /2.50 ^(0.03) 87.7 ^(1.3) /2.50 ^(0.03) 87.7 ^(1.3) /2.50 ^(0.03) 87.7 ^(1.3) /2.50 ^(0.03) 87.8 ^(0.3) /2.38 ^(0.10)	86.2 ^(7,7) /0.39 ^(0,29) 50.0 ^(1,9) /1.39 ^(0,24) 86.6 ^(12,7) /0.27 ^(0,12) 89.6 ^(3,4) /0.55 ^(0,22) 92.2 ^(3,3) /0.39 ^(0,12) 91.9 ^(3,4) /0.14 ^(0,13) 80.2 ^(12,9) /0.43 ^(0,34) Molecule 85.4 ^(1,5) /2.11 ^(0,15) 85.2 ^(0,5) /2.55 ^(0,02) 79.4 ^(1,3) /2.41 ^(0,07) 85.9 ^(1,1) /0.52 ^(0,02) 88.2 ^(0,6) /1.99 ^(0,06) 87.9 ^(1,0) /2.48 ^(0,05) 84.9 ^(0,9) /2.53 ^(0,05)	93.8 ^(0.6) /0.07 ^(0.01) 87.8 ^(3.1) /1.29 ^(0.37) 93.2 ^(1.6) /0.10 ^(0.00) 93.2 ^(1.6) /0.10 ^(0.00) 84.6 ^(4.4) /0.09 ^(0.00) 86.0 ^(3.3) /0.10 ^(0.00) 94.5 ^(0.7) /1.85 ^(0.22) Superconductor 94.6 ^(0.1) /7.184 ^(0.01) 92.5 ^(1.2) /7.61 ^(0.24) 85.5 ^(0.4) /7.51 ^(0.01) 94.3 ^(0.1) /7.84 ^(0.01) 94.3 ^(0.1) /7.84 ^(0.01) 94.3 ^(0.1) /7.84 ^(0.01) 95.5 ^(1.2) /7.51 ^(0.09) 85.1 ^(0.4) /7.45 ^(0.01)	$\begin{array}{c} 91.9^{(2.0)} 0.10^{(0.00)}\\ 101^{(6.3)} / 0.06^{(0.00)}\\ 30.8^{(5.7)} / 0.25^{(0.09)}\\ 91.9^{(2.0)} / 0.10^{(0.00)}\\ 65.5^{(25.2)} / 0.05^{(0.03)}\\ 31.8^{(5.6)} / 0.06^{(0.00)}\\ 12^{(6.6)} / 0.02^{(0.00)}\\ 112^{(7.8)} / 0.94^{(0.17)}\\ \hline D'Kitty\\ 106^{(2.9)} / 6.61^{(0.33)}\\ 105^{(1.6)} / 7.19^{(0.22)}\\ 35.5^{(1.2)} / 1.66^{(0.01)}\\ 105^{(2.5)} / 7.09^{(0.49)}\\ 30.8^{(2.5)} / 2.14^{(1.34)}\\ 14.3^{(1.5)} / 1.29^{(0.08)}\\ \end{array}$	$\begin{array}{c} 3.2/5.3\\ 5.0/5.8\\ 7.5/1.5\\ 2.5/2.2\\ 4.0/3.7\\ 5.0/4.5\\ 4.5/6.3\\ 4.0/\underline{3.3}\\ \hline \mathbf{Rank}\downarrow\\ 3.3/5.0\\ 4.0/\underline{3.0}\\ 7.5/3.8\\ \underline{3.2/5.2}\\ 3.7/5.0\\ 5.5/5.3\\ 5.7/6.3\\ \end{array}$	$\overline{71.9}/-1.39$ $43.0/-0.81$ $74.1/-1.41$ $69.0/-1.30$ $59.4/-1.25$ $62.0/-1.42$ $75.0/-0.90$ $\overline{Opt. Gap} \uparrow$ $\overline{76.2}/1.70$ $75.6/1.85$ $56.6/0.90$ $76.1/1.42$ $76.0/1.67$ $59.3/0.98$ $58.2/0.82$
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	COMS COMS RoMA ROMA GAMB DynAMA BO-qE Baselin COMS RoMA ROMA GAMB DynAMA	$\begin{array}{rcrr} & 15.4^{(4.9)}/0.23^{(0.09)} \\ & 12.8^{(0.6)}/0.24^{(0.04)} \\ & - 24.6^{(3.5)}/0.10^{(0.07)} \\ & 17.1^{(3.3)}/0.22^{(0.05)} \\ & 0 & 22.9^{(6.3)}/0.18^{(0.09)} \\ & 0 & 22.8^{(2.8)}/0.12^{(0.08)} \\ & 0 & 17.8^{(5.5)}/0.21^{(0.11)} \\ \hline \\ $	$\begin{array}{r} 44.9^{(3.5)}/0.20^{(0.13)}\\ 42.7^{(1.4)}/0.32^{(0.03)}\\ 49.7^{(3.0)}/0.22^{(0.11)}\\ 49.3^{(3.0)}/0.42^{(0.09)}\\ 48.9^{(1.5)}/0.25^{(0.10)}\\ 50.8^{(1.5)}/0.22^{(0.15)}\\ 48.4^{(2.3)}/0.18^{(0.09)}\\ \hline \\ \hline \\ \hline \\ \hline \\ \hline \\ \hline \\ \hline \\ \\ \hline \\ \\ \hline \\ \hline \\ \hline \\ \\ \hline \\ \hline \\ \\ \hline \\ \hline \\ \hline \\ \hline \\ \\ \hline \\ \\ \hline \hline \\ \hline \hline \\ \hline \hline \\ \hline \\ \hline \\ \hline \\ \hline \hline \\ \hline \hline \\ \hline \\ \hline \hline \\ \hline \\ \hline \hline \hline \hline \\ \hline \hline \hline \\ \hline \hline \hline \hline \hline \\ \hline \\ \hline \hline$	$\begin{array}{c} \textbf{90.0}^{(15.2)} / 0.38^{(0.27)} \\ 34.1^{(14.4)} / \textbf{1.31}^{(0.22)} \\ \textbf{98.6}^{(1.5)} / 0.40^{(0.20)} \\ \textbf{99.5}^{(0.9)} / 0.53^{(0.13)} \\ 75.8^{(6.1)} / \textbf{1.20}^{(0.21)} \\ \textbf{90.8}^{(14.2)} / 0.53^{(0.18)} \\ \textbf{96.7}^{(3.5)} / 0.64^{(0.42)} \\ \hline \\ $	$\begin{array}{c} \textbf{86.2}^{(7.7)} (0.39^{(0.29)} \\ 50.0^{(1.9)} / \textbf{1.39}^{(0.24)} \\ \textbf{86.6}^{(12.7)} / 0.27^{(0.12)} \\ \textbf{89.6}^{(3.4)} / 0.55^{(0.22)} \\ \textbf{92.2}^{(3.3)} / (0.39^{(0.12)} \\ \textbf{91.9}^{(3.4)} / 0.14^{(0.13)} \\ \textbf{80.2}^{(12.9)} / 0.43^{(0.34)} \\ \hline \\ \hline \\ \hline \\ \textbf{Molecule} \\ \textbf{85.4}^{(1.5)} / \textbf{2.11}^{(0.15)} \\ \textbf{85.2}^{(0.5)} / \textbf{2.55}^{(0.02)} \\ \textbf{79.4}^{(1.3)} / \textbf{2.41}^{(0.07)} \\ \textbf{85.9}^{(1.1)} / 0.52^{(0.02)} \\ \textbf{88.2}^{(0.6)} / 1.90^{(0.06)} \\ \textbf{87.9}^{(1.0)} / \textbf{2.53}^{(0.05)} \\ \textbf{85.2}^{(0.9)} / \textbf{2.53}^{(0.06)} \\ \textbf{85.2}^{(0.9)} / \textbf{2.54}^{(0.03)} \\ \end{array}$	93.8 ^(0.6) /0.07 ^(0.01) 87.8 ^(3.1) /1.29 ^(0.37) 93.2 ^(1.0) /0.10 ^(0.00) 93.2 ^(1.0) /0.10 ^(0.00) 84.6 ^(4.4) /0.09 ^(0.00) 86.0 ^(3.3) /0.10 ^(0.00) 94.5 ^(0.7) /1.85 ^(0.22) Superconductor 94.6 ^(0.1) /7.84 ^(0.01) 92.5 ^(1.2) /7.61 ^(0.24) 85.5 ^(0.4) /7.50 ^(0.01) 94.6 ^(0.1) /7.84 ^(0.01) 94.6 ^(0.1) /7.87 ^(0.01) 85.1 ^(0.4) /7.51 ^(0.00) 85.1 ^(0.4) /7.45 ^(0.01)	$\begin{array}{c} 91.9^{(2.0)}/0.10^{(0.00)}\\ 101^{(6.3)}/0.06^{(0.00)}\\ 30.8^{(5.7)}/0.25^{(0.09)}\\ 91.9^{(2.0)}/0.10^{(0.00)}\\ 65.5^{(25.2)}/0.05^{(0.03)}\\ 31.8^{(5.6)}/0.06^{(0.10)}\\ 29.6^{(3.6)}/0.02^{(0.00)}\\ 112^{(7.8)}/0.94^{(0.17)}\\ \hline D'Kitty\\ 106^{(2.9)}/6.61^{(0.33)}\\ 105^{(1.6)}/7.19^{(0.22)}\\ 35.5^{(1.2)}/1.66^{(0.01)}\\ 105^{(3.5)}/6.45^{(0.66)}\\ 116^{(2.5)}/7.09^{(0.49)}\\ 30.8^{(25.4)}/2.14^{(1.34)}\\ 14.3^{(1.5)}/1.29^{(0.08)}\\ 126^{(14.6)}/7.92^{(0.04)}\\ \end{array}$	$\frac{3.2}{5.0}, \frac{5.2}{5.0}, \frac{5.0}{5.8}, \frac{5.0}{5.2}, \frac{5.0}{5.2}, \frac{4.0}{3.7}, \frac{5.0}{5.0}, \frac{4.5}{5.0}, \frac{4.5}{5.0}, \frac{4.5}{5.0}, \frac{4.0}{3.3}, \frac{3.0}{5.0}, \frac{3.2}{5.5}, \frac{5.5}{5.3}, \frac{5.7}{5.3}, \frac{5.0}{5.7}, \frac{3.0}{2.2}, \frac{2.0}{5.5}, \frac{3.0}{2.2}, \frac{2.0}{5.5}, \frac{3.0}{2.2}, \frac{2.0}{5.5}, \frac{3.0}{2.2}, \frac{2.0}{5.5}, \frac{3.0}{2.2}, \frac{2.0}{5.5}, 2$	71.9/-1.39 43.0/-0.81 74.1/-1.41 69.0/-1.30 59.4/-1.25 62.0/-1.42 75.0/-0.90 Opt. Gap ↑ 76.2/1.70 75.6/1.85 56.6/0.90 76.1/1.42 76.0/1.67 59.3/0.98 58.2/0.82 79.4/2.02
$ \begin{array}{c} \text{COMs}^{+} & 12.6^{(0.3)} / 0.44^{(0.02)} \\ \text{RoMa}^{-} & \textbf{21.6}^{(0.3)} / 0.39^{(0.03)} \\ \text{RoMA}^{+} & 13.9^{(0.3)} / 0.31^{(0.02)} \\ \text{ROMO} & 16.0^{(0.4)} / 0.40^{(0.02)} \\ \text{GAMBO} & \textbf{21.9}^{(0.4)} / 0.40^{(0.01)} \\ \text{GAMBO} & \textbf{21.9}^{(0.4)} / 0.40^{(0.01)} \\ \end{array} \\ \begin{array}{c} 43.5^{(0.3)} / 0.57^{(0.01)} \\ \textbf{34.0}^{(2.3)} / 2.55^{(0.01)} \\ \textbf{35.6}^{(0.3)} / 2.55^{(0.01)} \\ \textbf{35.6}^{(0.3)} / 1.55^{(0.01)} \\ \textbf{35.7}^{(1.2)} / 2.51^{(0.06)} \\ \textbf{35.6}^{(1.2)} / 2.51^{(0.06)} \\ \textbf{35.6}^{(1.0)} / 2.52^{(0.04)} \\ \textbf{36.6}^{(1.0)} / 2.52^{(0.04$	COMS COMS RoMA ROMA GAMB DynAM BO-qE Baselin COMS COMS RoMA ROMA ROMA BO-qUC	$\begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	44.9 ^(3.5) /0.20 ^(0.13) 42.7 ^(1.4) / 0.32 ^(0.03) 49.7 ^(3.0) /0.22 ^(0.11) 49.3 ^(3.0) /0.42 ^(0.09) 48.9 ^(1.5) /0.22 ^(0.15) 48.4 ^(2.3) /0.18 ^(0.09) UTR 51.5 ^(0.3) /0.55 ^(0.01) 51.8 ^(0.2) /0.56 ^(0.01) 43.2 ^(0.2) /0.57 ^(0.01) 51.7 ^(0.3) /0.55 ^(0.01) 51.7 ^(0.3) /0.55 ^(0.01) 51.8 ^(0.2) /0.55 ^(0.01) 51.8 ^(0.2) /0.55 ^(0.01) 51.9 ^(0.2) /0.56 ^(0.01) 51.9 ^(0.2) /0.56 ^(0.01) 51.9 ^(0.2) /0.56 ^(0.01)	90.0 ^(15.2) /0.38 ^(0.27) 34.1 ^(14.4) /1.31 ^(0.22) 98.6 ^(1.5) /0.40 ^(0.20) 99.5 ^(0.9) /0.53 ^(0.13) 75.8 ^(6.1) /1.20 ^(0.21) 90.8 ^(14.2) /0.53 ^(0.18) 96.7 ^(3.5) /0.64 ^(0.42) ChEMBL 97.6 ^(0.3) /2.37 ^(0.03) 97.3 ^(0.5) /2.44 ^(0.05) 83.3 ^(2.1) /2.50 ^(0.05) 97.7 ^(0.5) /2.41 ^(0.04) 98.5 ^(0.4) /1.86 ^(0.05) 87.7 ^(1.3) /2.50 ^(0.03) 97.8 ^(0.3) /2.38 ^(0.10) 97.4 ^(0.3) /2.47 ^(0.03)	86.2 ^(7,7) /0.39 ^(0,29) 50.0 ^(1.9) /1.39 ^(0,24) 86.6 ^(12,7) /0.27 ^(0,12) 89.6 ^(3,4) /0.55 ^(0,22) 92.2 ^(3,3) /0.39 ^(0,12) 91.9 ^(3,4) /0.14 ^(0,13) 80.2 ^(12,9) /0.43 ^(0,34) Molecule 85.4 ^(1.5) /2.11 ^(0,15) 85.2 ^(0,5) /2.55 ^(0,02) 79.4 ^(1,3) /2.41 ^(0,07) 85.9 ^(1,1) /0.52 ^(0,02) 88.2 ^(0,6) /1.99 ^(0,06) 87.9 ^(1,0) /2.48 ^(0,05) 85.2 ^(0,9) /2.53 ^(0,05) 85.2 ^(0,9) /2.54 ^(0,03)	93.8 ^(0.6) /0.07 ^(0.01) 87.8 ^(3.1) /1.29 ^(0.37) 93.2 ^(1.6) /0.10 ^(0.00) 93.2 ^(1.6) /0.10 ^(0.00) 84.6 ^(4.4) /0.09 ^(0.00) 86.0 ^(3.3) /0.10 ^(0.00) 94.5 ^(0.7) /1.85 ^(0.22) Superconductor 94.6 ^(0.1) /7.84 ^(0.01) 92.5 ^(1.2) /7.61 ^(0.24) 85.5 ^(0.4) /7.50 ^(0.01) 94.6 ^(0.1) /7.84 ^(0.01) 94.6 ^(0.1) /7.87 ^(0.01) 85.1 ^(0.4) /7.87 ^(0.01) 94.8 ^(0.1) /7.87 ^(0.01) 94.8 ^(0.1) /7.87 ^(0.01)	$\begin{array}{c} 91.9^{(2.0)}/0.10^{(0.00)}\\ 101^{(6.3)}/0.06^{(0.00)}\\ 30.8^{(5.7)}/0.25^{(0.09)}\\ 91.9^{(2.0)}/0.10^{(0.00)}\\ 65.5^{(25.2)}/0.05^{(0.03)}\\ 31.8^{(5.6)}/0.06^{(0.10)}\\ 29.6^{(3.6)}/0.02^{(0.00)}\\ 112^{(7.8)}/0.94^{(0.17)}\\ \hline D'Kitty\\ 106^{(2.9)}/6.61^{(0.33)}\\ 105^{(1.6)}/7.19^{(0.22)}\\ 35.5^{(1.2)}/1.66^{(0.01)}\\ 105^{(3.5)}/6.45^{(0.66)}\\ 116^{(2.5)}/7.09^{(0.49)}\\ 30.8^{(25.4)}/2.14^{(1.34)}\\ 14.3^{(1.5)}/1.29^{(0.08)}\\ 126^{(14.6)}/7.92^{(0.04)}\\ \hline D'Kitty\\ \hline \end{array}$	3.2/5.3 5.0/5.8 7.5/1.5 2.5/5.2 4.0/3.7 5.0/4.5 4.5/6.3 4.0/3.3 Rank↓ 3.3/5.0 4.0/ <u>3.0</u> 7.5/3.8 <u>3.2/5.2</u> 3.7/5.0 5.5/5.3 5.7/6.3 3.0/2.2 Rank↓	71.9/-1.39 43.0/-0.81 74.1/-1.41 69.0/-1.30 59.4/-1.25 62.0/-1.42 75.0/-0.90 Opt. Gap ↑ 76.2/1.70 75.6/1.85 56.6/0.90 76.1/1.42 76.0/1.67 59.3/0.98 58.2/0.82 79.4/2.02
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	COMS COMS RoMA ROMA GAMBG DynAMG BO-qE Baselin COMS RoMA ROMA ROMA BO-qUC Baselin	$\begin{array}{rcrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$	$\begin{array}{r} 44.9^{(3.5)}/0.20^{(0.13)}\\ 42.7^{(1.4)}/0.32^{(0.03)}\\ 49.7^{(3.0)}/0.22^{(0.11)}\\ 49.3^{(3.0)}/0.42^{(0.09)}\\ 48.9^{(1.5)}/0.25^{(0.10)}\\ 50.8^{(1.5)}/0.22^{(0.15)}\\ 48.4^{(2.3)}/0.18^{(0.09)}\\ \hline \\ \hline$	90.0 ^(15.2) /0.38 ^(0.27) 34.1 ^(14.4) /1.31 ^(0.22) 98.6 ^(1.5) /0.40 ^(0.20) 99.5 ^(0.9) /0.53 ^(0.13) 75.8 ^(6.1) /1.20 ^(0.21) 90.8 ^(14.2) /0.53 ^(0.18) 96.7 ^(3.5) /0.64 ^(0.42) ChEMBL 97.6 ^(0.3) /2.37 ^(0.03) 97.3 ^(0.5) /2.41 ^(0.04) 98.5 ^(0.4) /1.86 ^(0.05) 87.7 ^(1.3) /2.50 ^(0.03) 97.8 ^(0.3) /2.38 ^(0.10) 97.8 ^(0.3) /2.38 ^(0.10) 97.4 ^(0.4) /2.47 ^(0.03) 97.9 ^(0.4) /2.40 ^(0.05)	86.2 ^(7,7) /0.39 ^(0,29) 50.0 ^(1.9) /1.39 ^(0,24) 86.6 ^(12,7) /0.27 ^(0,12) 89.6 ^(3,4) /0.55 ^(0,22) 92.2 ^(3,3) /0.39 ^(0,12) 91.9 ^(3,4) /0.14 ^(0,13) 80.2 ^(12,9) /0.43 ^(0,34) Molecule 85.4 ^(1.5) /2.11 ^(0,15) 85.2 ^(0,5) /2.55 ^(0,02) 79.4 ^(1,3) /2.41 ^(0,07) 85.9 ^(1,1) /0.52 ^(0,02) 88.2 ^(0,6) /1.99 ^(0,06) 87.9 ^(1,0) /2.48 ^(0,05) 84.9 ^(0,9) /2.53 ^(0,05) 85.2 ^(0,9) /2.54 ^(0,03) 85.2 ^(0,9) /2.54 ^(0,07)	93.8 ^(0.6) /0.07 ^(0.01) 87.8 ^(3.1) /1.29 ^(0.37) 93.2 ^(1.0) /0.10 ^(0.00) 93.2 ^(1.0) /0.10 ^(0.00) 84.6 ^(4.4) /0.09 ^(0.00) 86.0 ^(3.3) /0.10 ^(0.00) 94.5 ^(0.7) /1.85 ^(0.22) Superconductor 94.6 ^(0.1) /7.84 ^(0.01) 92.5 ^(1.2) /7.61 ^(0.24) 85.5 ^(0.4) /7.50 ^(0.01) 94.6 ^(0.1) /7.87 ^(0.01) 94.6 ^(0.1) /7.87 ^(0.01) 94.6 ^(0.1) /7.87 ^(0.01) 94.6 ^(0.1) /7.87 ^(0.01) 94.8 ^(0.1) /7.87 ^(0.01) 94.8 ^(0.1) /7.87 ^(0.01) 94.8 ^(0.1) /7.87 ^(0.01)	$\begin{array}{r} 91.9^{(2.0)}/0.10^{(0.00)}\\ 101^{(6.3)}/0.06^{(0.00)}\\ 30.8^{(5.7)}/0.25^{(0.09)}\\ 91.9^{(2.0)}/0.10^{(0.00)}\\ 65.5^{(25.2)}/0.05^{(0.03)}\\ 31.8^{(5.6)}/0.02^{(0.00)}\\ 112^{(7.8)}/0.94^{(0.17)}\\ \hline D'Kitty\\ 106^{(2.9)}/6.61^{(0.33)}\\ 105^{(1.6)}/7.19^{(0.22)}\\ 35.5^{(1.2)}/1.66^{(0.01)}\\ 105^{(3.3)}/6.45^{(0.66)}\\ 116^{(2.5)}/7.09^{(0.49)}\\ 30.8^{(25.4)}/2.14^{(1.34)}\\ 14.3^{(1.5)}/1.29^{(0.08)}\\ 126^{(14.6)}/7.92^{(0.04)}\\ 126^{(14.6)}/7.92^{(0.04)}\\ \hline D'Kitty\\ 98.8^{(1.1)}/6.64^{(0.09)}\\ \end{array}$	$\begin{array}{r} 3.2/5.3\\ 5.0/5.8\\ 7.5/1.5\\ 2.5/5.2\\ 4.0/3.7\\ 5.0/4.5\\ 4.5/6.3\\ 4.0/3.3\\ \hline \textbf{Rank}\downarrow\\ 3.3/5.0\\ 4.0/3.0\\ 7.5/3.8\\ \underline{3.2}/5.2\\ 3.7/5.0\\ 5.5/5.3\\ 5.7/6.3\\ 3.0/2.2\\ \hline \textbf{Rank}\downarrow\\ \underline{3.5}/4.7\\ \end{array}$	71.9/-1.39 43.0/-0.81 74.1/-1.41 69.0/-1.30 59.4/-1.25 62.0/-1.42 75.0/-0.90 Opt. Gap ↑ 76.2/1.70 75.6/1.85 56.6/0.90 76.1/1.42 76.0/1.67 59.3/0.98 58.2/0.82 79.4/2.02 Opt. Gap ↑ 74.8/1.77
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	COMS COMS RoMA ROMA GAMBG DynAMG BO-qE Baselin COMS RoMA ROMA GAMBG DynAMG BO-qUC Baselin COMS	$\begin{array}{rcrr} & 15.4^{(4.9)}/0.23^{(0.09)} \\ & 12.8^{(0.6)}/0.24^{(0.04)} \\ & - 24.6^{(3.5)}/0.10^{(0.07)} \\ & 17.1^{(3.7)}/0.22^{(0.05)} \\ & 0 & 22.9^{(6.3)}/0.18^{(0.09)} \\ & 0 & 22.8^{(2.8)}/0.12^{(0.08)} \\ & 17.8^{(5.5)}/0.21^{(0.11)} \\ \hline \\ $	$\begin{array}{r} 44.9^{(3.5)}/0.20^{(0.13)}\\ 42.7^{(1.4)}/0.32^{(0.03)}\\ 49.7^{(3.0)}/0.22^{(0.11)}\\ 49.3^{(3.0)}/0.42^{(0.09)}\\ 48.9^{(1.5)}/0.22^{(0.10)}\\ 50.8^{(1.5)}/0.22^{(0.15)}\\ 48.4^{(2.3)}/0.18^{(0.09)}\\ \hline \\ \hline \\ \hline \\ \hline \\ \hline \\ 51.5^{(0.3)}/0.55^{(0.01)}\\ 51.8^{(0.2)}/0.56^{(0.01)}\\ 51.7^{(0.3)}/0.55^{(0.02)}\\ 45.0^{(0.2)}/0.56^{(0.01)}\\ 51.8^{(0.2)}/0.55^{(0.01)}\\ 51.9^{(0.2)}/0.56^{(0.01)}\\ 51.9^{(0.2)}/0.56^{(0.01)}\\ 51.7^{(0.2)}/0.56^{(0.01)}\\ 51.9^{(0.2)}/0.56^{(0.01)}\\ 51.7^{(0.2)}/0.56^{(0.01)}\\ 51.7^{(0.2)}/0.54^{(0.01)}\\ 51.7^{(0.2)}/0.54^{(0.01)}\\ 51.7^{(0.2)}/0.54^{(0.01)}\\ 51.7^{(0.2)}/0.56^{(0.01)}\\ 51.7^{(0.2)}/0.56^{(0.01)}\\ 51.7^{(0.2)}/0.56^{(0.01)}\\ 51.7^{(0.2)}/0.56^{(0.01)}\\ \hline \\ \hline$	$\begin{array}{r} \textbf{90.0}^{(15.2)} / 0.38^{(0.27)} \\ 34.1^{(14.4)} / \textbf{1.31}^{(0.22)} \\ \textbf{98.6}^{(1.5)} / 0.40^{(0.20)} \\ \textbf{99.5}^{(0.9)} / 0.53^{(0.13)} \\ 75.8^{(6.1)} / 1.20^{(0.21)} \\ \textbf{90.8}^{(14.2)} / 0.53^{(0.18)} \\ \textbf{96.7}^{(35)} / 0.64^{(0.42)} \\ \hline \textbf{ChEMBL} \\ \textbf{97.6}^{(0.3)} / 2.37^{(0.3)} \\ \textbf{97.3}^{(0.5)} / 2.44^{(0.05)} \\ \textbf{83.3}^{(2.1)} / 2.50^{(0.05)} \\ \textbf{87.7}^{(1.3)} / 2.50^{(0.03)} \\ \textbf{97.8}^{(0.3)} / 2.38^{(0.10)} \\ \textbf{97.8}^{(0.3)} / 2.38^{(0.10)} \\ \textbf{97.4}^{(0.4)} / 2.47^{(0.05)} \\ \textbf{97.4}^{(0.4)} / 2.40^{(0.05)} \\ \textbf{97.4}^{(0.4)} / 2.4$	86.2 ^(7,7) /0.39 ^(0,29) 50.0 ^(1.9) /1.39 ^(0,24) 86.6 ^(12,7) /0.27 ^(0,12) 89.6 ^(3,4) /0.55 ^(0,22) 92.2 ^(3,3) /0.39 ^(0,12) 91.9 ^(3,4) /0.14 ^(0,13) 80.2 ^(12,9) /0.43 ^(0,34) Molecule 85.4 ^(1.5) /2.11 ^(0,15) 85.2 ^(0,5) /2.55 ^(0,02) 79.4 ^(1,3) /2.41 ^(0,07) 85.9 ^(1.1) /0.52 ^(0,02) 88.2 ^(0,6) /1.99 ^(0,06) 87.9 ^(1.0) /2.48 ^(0,05) 84.9 ^(0,9) /2.53 ^(0,05) 85.2 ^(0,9) /2.54 ^(0,03) 85.2 ^(0,9) /2.54 ^(0,03) 85.2 ^(1.1) /2.52 ^(0,07) 85.4 ^(1.4) /2.49 ^(0,04)	$\begin{array}{r} {93.8^{(0.6)}/(0.07^{(0.01)}}\\ {87.8^{(3.1)}/1.29^{(0.37)}}\\ {93.2^{(1.0)}/(0.10^{(0.00)}}\\ {93.2^{(1.0)}/(0.10^{(0.00)})}\\ {84.6^{(4.4)}/(0.09^{(0.00)})}\\ {86.0^{(3.3)}/(0.10^{(0.00)})}\\ {94.5^{(0.7)}/1.85^{(0.22)}}\\ \hline \\ {\textbf{Superconductor}}\\ {94.6^{(0.1)}/7.84^{(0.01)}}\\ {92.5^{(1.2)}/7.61^{(0.24)}}\\ {85.5^{(0.4)}/7.50^{(0.01)}}\\ {94.6^{(0.1)}/7.87^{(0.01)}}\\ {94.6^{(0.1)}/7.87^{(0.01)}}\\ {94.6^{(0.1)}/7.87^{(0.01)}}\\ {95.1^{(0.4)}/7.45^{(0.01)}}\\ {94.8^{(0.1)}/7.87^{(0.01)}}\\ {93.8^{(0.6)}/7.78^{(0.04)}}\\ {92.9^{(1.1)}/7.57^{(0.09)}}\\ \hline \end{array}$	$\begin{array}{r} 91.9^{(2.0)}/0.10^{(0.00)}\\ 101^{(6.3)}/0.06^{(0.00)}\\ 30.8^{(5.7)}/0.25^{(0.09)}\\ 91.9^{(2.0)}/0.10^{(0.00)}\\ 65.5^{(25.2)}/0.05^{(0.03)}\\ 31.8^{(5.6)}/0.06^{(0.10)}\\ 29.6^{(3.6)}/0.02^{(0.00)}\\ 112^{(7.8)}/0.94^{(0.17)}\\ \hline D'Kitty\\ 106^{(2.9)}/6.61^{(0.33)}\\ 105^{(1.6)}/7.19^{(0.22)}\\ 35.5^{(1.2)}/1.66^{(0.01)}\\ 105^{(3.5)}/6.45^{(0.66)}\\ 116^{(2.5)}/7.09^{(0.49)}\\ 30.8^{(25.4)}/2.14^{(1.34)}\\ 14.3^{(1.5)}/1.29^{(0.08)}\\ 126^{(14.6)}/7.92^{(0.04)}\\ \hline D'Kitty\\ 98.8^{(1.1)}/6.64^{(0.09)}\\ 99.2^{(1.6)}/6.84^{(0.11)}\\ \end{array}$	$\begin{array}{r} 3.2/5.3\\ 5.0/5.8\\ 7.5/1.5\\ 2.5/5.2\\ 4.0/3.7\\ 5.0/4.5\\ 4.5/6.3\\ 4.0/3.3\\ \hline \textbf{Rank}\downarrow\\ \hline 3.3/5.0\\ 4.0/\underline{3.0}\\ 7.5/3.8\\ \underline{3.2/5.2}\\ 3.7/5.0\\ 5.5/5.3\\ 5.7/6.3\\ \hline \textbf{3.0/2.2}\\ \hline \textbf{Rank}\downarrow\\ \hline \underline{3.5/4.7}\\ \overline{3.8/3.7}\\ \hline \end{array}$	71.9/-1.39 43.0/-0.81 74.1/-1.41 69.0/-1.30 59.4/-1.25 62.0/-1.42 75.0/-0.90 Opt. Gap ↑ 76.2/1.70 75.6/1.85 56.6/0.90 76.1/1.42 76.0/1.67 59.3/0.98 58.2/0.82 79.4/2.02 Opt. Gap ↑ 74.8/1.77 74.8/1.77 74.8/1.77
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	COMS COMS RoMA ROMA GAMBI DynAMO BO-qE Baselin COMS RoMA ROMA ROMA GAMBI DynAMO BO-qUC Baselin COMS	$\begin{array}{rcrr} & 15.4^{(4.9)}/0.23^{(0.09)} \\ & 12.8^{(0.6)}/0.24^{(0.04)} \\ & - 24.6^{(3.5)}/0.10^{(0.07)} \\ & 17.1^{(3.3)}/0.18^{(0.09)} \\ & 0 & 22.9^{(6.3)}/0.18^{(0.09)} \\ & 0 & 22.8^{(2.8)}/0.12^{(0.08)} \\ & 0 & 22.8^{(2.8)}/0.12^{(0.08)} \\ & 17.8^{(5.5)}/0.21^{(0.01)} \\ \hline \\ & \mathbf{I} & \mathbf{TFBind8} \\ e & 21.8^{(0.5)}/0.41^{(0.02)} \\ & 12.7^{(0.4)}/0.44^{(0.01)} \\ & 12.7^{(0.4)}/0.44^{(0.01)} \\ & + 12.7^{(0.4)}/0.44^{(0.02)} \\ & 13.6^{(0.3)}/0.31^{(0.02)} \\ & 0 & 15.6^{(0.4)}/0.39^{(0.02)} \\ & 0 & 15.4^{(0.3)}/0.40^{(0.03)} \\ & \mathbf{O} & 21.6^{(0.3)}/0.40^{(0.02)} \\ \hline \\ & \mathbf{B} & \mathbf{TFBind8} \\ e & 21.6^{(0.3)}/0.40^{(0.02)} \\ & - 21.7^{(0.3)}/0.40^{(0.02)} \\ & + 12.6^{(0.3)}/0.44^{(0.02)} \\ \end{array}$	$\begin{array}{r} 44.9^{(3.5)}/0.20^{(0.13)}\\ 42.7^{(1.4)}/0.32^{(0.03)}\\ 49.7^{(3.0)}/0.22^{(0.11)}\\ 49.3^{(3.0)}/0.42^{(0.09)}\\ 48.9^{(1.5)}/0.25^{(0.10)}\\ 50.8^{(1.5)}/0.25^{(0.10)}\\ 51.5^{(0.2)}/0.18^{(0.09)}\\ \hline \\ \hline$	90.0 ^(15.2) /0.38 ^(0.27) 34.1 ^(14.4) /1.31 ^(0.22) 98.6 ^(1.5) /0.40 ^(0.20) 99.5 ^(0.9) /0.53 ^(0.13) 75.8 ^(6.1) /1.20 ^(0.21) 90.8 ^(14.2) /0.53 ^(0.18) 96.7 ^(3.5) /0.64 ^(0.42) 75.8 ^(0.3) /2.37 ^(0.03) 97.3 ^(0.5) /2.44 ^(0.05) 83.3 ^(2.1) /2.50 ^(0.05) 97.7 ^(0.5) /2.41 ^(0.04) 98.5 ^(0.4) /1.86 ^(0.05) 87.7 ^(1.3) /2.50 ^(0.03) 97.8 ^(0.3) /2.38 ^(0.10) 97.4 ^(0.4) /2.47 ^(0.05) 97.4 ^(0.4) /2.40 ^(0.05) 97.4 ^(0.4) /2.40 ^(0.05) 84.0 ^(2.3) /2.52 ^(0.05)	86.2 ^(7,7) /0.39 ^(0,29) 50.0 ^(1,9) /1.39 ^(0,24) 86.6 ^(12,7) /0.27 ^(0,12) 89.6 ^(3,4) /0.55 ^(0,22) 92.2 ^(3,3) /0.39 ^(0,12) 91.9 ^(3,4) /0.14 ^(0,13) 80.2 ^(12,9) /0.43 ^(0,34) Molecule 85.4 ^(1,5) /2.11 ^(0,15) 85.2 ^(0,5) /2.55 ^(0,02) 79.4 ^(1,3) /2.41 ^(0,07) 85.9 ^(1,1) /0.52 ^(0,02) 88.2 ^(0,6) /1.99 ^(0,06) 87.9 ^(1,0) /2.48 ^(0,05) 84.9 ^(0,9) /2.53 ^(0,05) 85.2 ^(0,9) /2.54 ^(0,07) 85.4 ^(1,4) /2.49 ^(0,04) 79.2 ^(1,4) /2.49 ^(0,04) 79.2 ^(1,4) /2.38 ^(0,08)	93.8 ^(0.6) /0.07 ^(0.01) 87.8 ^(3.1) /1.29 ^(0.37) 93.2 ^(1.6) /0.10 ^(0.00) 93.2 ^(1.6) /0.10 ^(0.00) 84.6 ^(4.4) /0.09 ^(0.00) 86.0 ^(3.3) /0.10 ^(0.00) 94.5 ^(0.7) /1.85 ^(0.22) 94.6 ^(0.1) /7.84 ^(0.01) 92.5 ^(1.2) /7.61 ^(0.24) 85.5 ^(0.4) /7.50 ^(0.01) 94.3 ^(0.1) /7.87 ^(0.01) 94.3 ^(0.1) /7.87 ^(0.01) 86.6 ^(2.2) /7.51 ^(0.09) 85.1 ^(0.4) /7.87 ^(0.01) 94.8 ^(0.1) /7.87 ^(0.01) 94.8 ^(0.1) /7.87 ^(0.01) 94.8 ^(0.1) /7.87 ^(0.01) 93.8 ^(0.6) /7.78 ^(0.04) 92.9 ^(1.1) /7.51 ^(0.02)	$\begin{array}{c} 91.9^{(2.0)}/0.10^{(0.00)}\\ 101^{(6.3)}/0.06^{(0.00)}\\ 30.8^{(5.7)}/0.25^{(0.09)}\\ 91.9^{(2.0)}/0.10^{(0.00)}\\ 65.5^{(25.2)}/0.05^{(0.03)}\\ 31.8^{(5.6)}/0.06^{(0.10)}\\ 29.6^{(3.6)}/0.02^{(0.00)}\\ 112^{(7.8)}/0.94^{(0.17)}\\ \hline D'Kitty\\ 106^{(2.9)}/6.61^{(0.33)}\\ 105^{(1.6)}/7.19^{(0.22)}\\ 35.5^{(1.2)}/1.66^{(0.01)}\\ 105^{(3.5)}/6.45^{(0.66)}\\ 116^{(2.5)}/7.09^{(0.49)}\\ 30.8^{(25.4)}/2.14^{(1.34)}\\ 14.3^{(1.5)}/1.29^{(0.08)}\\ 126^{(14.6)}/7.92^{(0.04)}\\ \hline D'Kitty\\ 98.8^{(1.1)}/6.64^{(0.09)}\\ 99.2^{(1.6)}/6.84^{(0.11)}\\ 39.4^{(6.0)}/1.66^{(0.01)}\\ \end{array}$	$\frac{3.2}{5.0}$ $\frac{3.2}{5.3}$ $5.0/5.8$ $7.5/1.5$ $2.5/5.2$ $4.0/3.7$ $5.0/4.5$ $4.5/6.3$ $4.0/\underline{3.3}$ Rank \downarrow $3.3/5.0$ $4.0/\underline{3.0}$ $7.5/3.8$ $3.2/5.2$ $3.7/5.0$ $5.5/5.3$ $5.7/6.3$ $3.0/2.2$ Rank \downarrow $\frac{3.5}{4.7}$ $3.8/3.7$ $7.5/\underline{3.7}$	71.9/-1.39 43.0/-0.81 74.1/-1.41 69.0/-1.30 59.4/-1.25 62.0/-1.42 75.0/_0.90 Opt. Gap ↑ 76.2/1.70 75.6/1.85 56.6/0.90 76.1/1.42 76.0/1.67 59.3/0.98 58.2/0.82 79.4/2.02 Opt. Gap ↑ 74.8/1.77 74.8/1.77 74.8/1.77 74.8/1.70 57.2/0.90
GAMBO 21.9 ^(0,4) /0.40 ^(0,01) 51.7 ^(0,3) / 0.56 ^(0,01) 97.5 ^(0,4) /2.39 ^(0,05) 85.2 ^(1,0) / 2.52 ^(0,04) 81.9 ^(1,9) /7.37 ^(0,09) 25.9 ^(1,4) /1.34 ^(0,04) 4.7/6.0 60.7/0.82	COMS COMS RoMA ROMA GAMB DynAM BO-qF Baselin COMS COMS RoMA BO-qUC Baselin COMS GAMB DynAM	$\begin{array}{rcrr} & 15.4^{(4.9)}/0.23^{(0.09)} \\ & 12.8^{(0.6)}/0.24^{(0.04)} \\ & - 24.6^{(3.5)}/0.10^{(0.07)} \\ & 17.1^{(3.3)}/0.22^{(0.05)} \\ & 0 & 22.9^{(6.3)}/0.12^{(0.08)} \\ & 0 & 22.8^{(2.3)}/0.12^{(0.08)} \\ & 0 & 17.8^{(5.5)}/0.21^{(0.11)} \\ \hline & \mathbf{I} & \mathbf{TFBind8} \\ e & 21.8^{(0.5)}/0.41^{(0.02)} \\ & - 21.9^{(0.5)}/0.41^{(0.03)} \\ & - 21.9^{(0.5)}/0.41^{(0.03)} \\ & - 21.6^{(0.3)}/0.40^{(0.03)} \\ & + 13.6^{(0.3)}/0.31^{(0.02)} \\ & 0 & 15.4^{(0.3)}/0.40^{(0.03)} \\ & 0 & 21.0^{(0.5)}/0.42^{(0.01)} \\ \hline & \mathbf{B} & \mathbf{TFBind8} \\ e & 21.6^{(0.3)}/0.40^{(0.02)} \\ & - 21.7^{(0.3)}/0.40^{(0.02)} \\ & - 21.6^{(0.3)}/0.40^{(0.02)} \\ & - 21.6^{(0.3)}/0.40^{(0.02)} \\ & - 21.6^{(0.3)}/0.40^{(0.02)} \\ & - 21.6^{(0.3)}/0.40^{(0.02)} \\ & - 21.6^{(0.3)}/0.39^{(0.03)} \\ \end{array}$	$\begin{array}{r} 44.9^{(3.5)}/0.20^{(0.13)}\\ 42.7^{(1.4)}/0.32^{(0.03)}\\ 49.7^{(3.0)}/0.22^{(0.11)}\\ 49.3^{(3.0)}/0.42^{(0.09)}\\ 48.9^{(1.5)}/0.25^{(0.10)}\\ 50.8^{(1.5)}/0.25^{(0.10)}\\ 51.5^{(0.3)}/0.55^{(0.21)}\\ 51.5^{(0.3)}/0.55^{(0.01)}\\ 51.8^{(0.2)}/0.56^{(0.01)}\\ 43.2^{(0.2)}/0.56^{(0.01)}\\ 43.2^{(0.2)}/0.55^{(0.01)}\\ 51.8^{(0.2)}/0.55^{(0.01)}\\ 51.8^{(0.2)}/0.55^{(0.01)}\\ 51.9^{(0.2)}/0.55^{(0.01)}\\ 51.9^{(0.2)}/0.55^{(0.01)}\\ 51.7^{(0.2)}/0.55^{(0.01)}\\ 51.7^{(0.2)}/0.55^{(0.01)}\\ 51.7^{(0.2)}/0.55^{(0.01)}\\ 51.6^{(0.3)}/0.57^{(0.01)}\\ 51.6^{(0.3)}/0.55^{(0.01)}\\ 51.6^{(0.3)}/0.55^{(0.01)}\\ \end{array}$	90.0 ^(15.2) /0.38 ^(0.27) 34.1 ^(14.4) /1.31 ^(0.22) 98.6 ^(1.5) /0.40 ^(0.20) 99.5 ^(0.9) /0.53 ^(0.13) 75.8 ^(6.1) /1.20 ^(0.21) 90.8 ^(14.2) /0.53 ^(0.18) 96.7 ^(3.5) /0.64 ^(0.42) ChEMBL 97.6 ^(0.3) /2.37 ^(0.03) 97.3 ^(0.5) /2.44 ^(0.05) 83.3 ^(2.1) /2.50 ^(0.05) 87.7 ^(1.3) /2.50 ^(0.03) 87.7 ^(1.3) /2.50 ^(0.03) 87.7 ^(1.3) /2.50 ^(0.03) 97.8 ^(0.3) /2.38 ^(0.10) 97.4 ^(0.4) /2.47 ^(0.05) 97.8 ^(0.4) /2.37 ^(0.05) 98.8 ^(0.3) /1.85 ^(0.2)	86.2 ^(7,7) /0.39 ^(0,29) 50.0 ^(1,9) /1.39 ^(0,24) 86.6 ^(12,7) /0.27 ^(0,12) 89.6 ^(3,4) /0.55 ^(0,22) 92.2 ^(3,3) /0.39 ^(0,12) 91.9 ^(3,4) /0.14 ^(0,13) 80.2 ^(12,9) /0.43 ^(0,34) Molecule 85.4 ^(1,5) /2.11 ^(0,15) 85.2 ^(0,5) /2.55 ^(0,02) 79.4 ^(1,3) /2.41 ^(0,07) 88.2 ^(0,6) /1.99 ^(0,06) 87.9 ^(1,0) /2.48 ^(0,05) 84.9 ^(0,9) /2.53 ^(0,05) 85.2 ^(0,9) /2.54 ^(0,03) Molecule 85.3 ^(1,1) /2.52 ^(0,07) 85.4 ^(1,4) /2.49 ^(0,04) 79.2 ^(1,4) /2.48 ^(0,08) 85.5 ^(1,1) /2.54 ^(0,07)	93.8 ^(0.6) /0.07 ^(0.01) 87.8 ^(3.1) /1.29 ^(0.37) 93.2 ^(1.6) /0.10 ^(0.00) 93.2 ^(1.6) /0.10 ^(0.00) 84.6 ^(4.4) /0.09 ^(0.00) 86.0 ^(3.3) /0.10 ^(0.00) 94.5 ^(0.7) /1.85 ^(0.22) 94.6 ^(0.1) /7.185 ^(0.22) 94.6 ^(0.1) /7.185 ^(0.22) 94.6 ^(0.1) /7.185 ^(0.01) 94.6 ^(0.1) /7.84 ^(0.01) 94.3 ^(0.1) /7.84 ^(0.01) 94.3 ^(0.1) /7.84 ^(0.01) 94.3 ^(0.1) /7.84 ^(0.01) 94.3 ^(0.1) /7.87 ^(0.01) 94.8 ^(0.1) /7.87 ^(0.01) 94.8 ^(0.1) /7.87 ^(0.01) 93.8 ^(0.6) /7.78 ^(0.04) 92.9 ^(1.1) /7.75 ^(0.02) 93.8 ^(0.6) /7.78 ^(0.04)	$\begin{array}{c} 91.9^{(2.0)}/0.10^{(0.00)}\\ 101^{(6.3)}/0.06^{(0.00)}\\ 30.8^{(5.7)}/0.25^{(0.09)}\\ 91.9^{(2.0)}/0.10^{(0.00)}\\ 65.5^{(25.2)}/0.05^{(0.03)}\\ 31.8^{(5.6)}/0.06^{(0.01)}\\ 29.6^{(3.6)}/0.02^{(0.00)}\\ 112^{(7.8)}/0.94^{(0.17)}\\ \hline D'Kitty\\ 106^{(2.9)}/6.61^{(0.33)}\\ 105^{(1.6)}/7.19^{(0.22)}\\ 35.5^{(1.2)}/1.66^{(0.01)}\\ 105^{(3.5)}/6.45^{(0.66)}\\ 116^{(2.5)}/7.09^{(0.49)}\\ 30.8^{(2.5)}/2.14^{(1.34)}\\ 14.3^{(1.5)}/1.29^{(0.08)}\\ 126^{(14.6)}/7.92^{(0.04)}\\ \hline D'Kitty\\ 98.8^{(1.1)}/6.64^{(0.09)}\\ 99.2^{(1.6)}/6.64^{(0.09)}\\ 98.8^{(1.1)}/6.64^{(0.09)}\\ 98.8^{(1.1)}/6.64^{(0.09)}\\ 112^{(2.5)}/7.23^{(0.16)}\\ \hline \end{array}$	$\frac{3.2}{5.3}$ $5.0/5.8$ $7.5/1.5$ $2.5/5.2$ $4.0/3.7$ $5.0/4.5$ $4.5/6.3$ $4.0/\underline{3.3}$ Rank \downarrow $3.3/5.0$ $4.0/\underline{3.0}$ $7.5/3.8$ $3.2/5.2$ $3.7/5.0$ $5.5/5.3$ $5.7/6.3$ $3.0/2.2$ Rank \downarrow $\frac{3.5/4.7}{3.8/\underline{3.7}}$ $7.5/3.7$ $3.5/4.8$	71.9/-1.39 43.0/-0.81 74.1/-1.41 69.0/-1.30 59.4/-1.25 62.0/-1.42 75.0/-0.90 Opt. Gap ↑ 76.2/1.70 75.6/1.85 56.6/0.90 76.1/1.42 76.0/1.67 59.3/0.98 58.2/0.82 79.4/2.02 Opt. Gap ↑ 74.8/1.77 74.7/1.80 57.2/0.90 74.9/1.77
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	COMS COMS RoMA ROMA GAMB DynAM BO-qE Baselin COMS COMS RoMA ROMA BO-qUC Baselin COMS COMS COMS COMS COMS COMS COMS	$\begin{array}{rcrr} & 15.4^{(4.9)}/0.23^{(0.09)} \\ & 12.8^{(0.6)}/0.24^{(0.04)} \\ & 12.8^{(0.6)}/0.24^{(0.04)} \\ & 12.8^{(0.5)}/0.12^{(0.07)} \\ & 17.1^{(3.3)}/0.22^{(0.05)} \\ & 0 & 22.9^{(6.3)}/0.12^{(0.08)} \\ & 0 & 22.8^{(2.3)}/0.12^{(0.08)} \\ & 0 & 22.8^{(2.3)}/0.12^{(0.08)} \\ & 0 & 17.8^{(5.5)}/0.21^{(0.11)} \\ \hline {\bf I} & {\bf TFBind8} \\ e & 21.8^{(0.5)}/0.41^{(0.02)} \\ & - & 21.9^{(0.5)}/0.41^{(0.02)} \\ & - & 21.9^{(0.5)}/0.41^{(0.02)} \\ & - & 21.9^{(0.5)}/0.41^{(0.02)} \\ & + & 12.7^{(0.4)}/0.44^{(0.01)} \\ & + & 12.7^{(0.4)}/0.44^{(0.01)} \\ & - & 21.6^{(0.3)}/0.40^{(0.02)} \\ & 0 & 15.6^{(0.4)}/0.39^{(0.02)} \\ & 0 & 15.6^{(0.4)}/0.42^{(0.01)} \\ \hline {\bf B} & {\bf TFBind8} \\ e & 21.6^{(0.3)}/0.44^{(0.02)} \\ & - & 21.6^{(0.3)}/0.44^{(0.02)} \\ & - & 21.6^{(0.3)}/0.39^{(0.03)} \\ & - & 21.6^{(0.3)$	$\begin{array}{r} 44.9^{(3.5)}/0.20^{(0.13)}\\ 42.7^{(1.4)}/0.32^{(0.03)}\\ 49.7^{(3.0)}/0.22^{(0.11)}\\ 49.3^{(3.0)}/0.42^{(0.09)}\\ 48.9^{(1.5)}/0.25^{(0.10)}\\ 50.8^{(1.5)}/0.22^{(0.15)}\\ 48.4^{(2.3)}/0.18^{(0.09)}\\ \hline \\ \hline \\ \hline \\ S1.5^{(0.3)}/0.55^{(0.01)}\\ 51.8^{(0.2)}/0.56^{(0.01)}\\ 43.2^{(0.2)}/0.55^{(0.01)}\\ 51.8^{(0.2)}/0.55^{(0.01)}\\ 51.8^{(0.2)}/0.55^{(0.01)}\\ 51.9^{(0.2)}/0.55^{(0.01)}\\ 51.9^{(0.2)}/0.55^{(0.01)}\\ 51.9^{(0.2)}/0.55^{(0.01)}\\ 51.9^{(0.2)}/0.55^{(0.01)}\\ 51.7^{(0.2)}/0.56^{(0.01)}\\ 51.7^{(0.2)}/0.55^{(0.01)}\\ 51.7^{(0.2)}/0.56^{(0.01)}\\ 51.7^{(0.2)}/0.56^{(0.01)}\\ 51.6^{(0.3)}/0.55^{(0.01)}\\ 45.1^{(0.5)}/0.56^{(0.01)}\\ 47.7^{(0.2)}/0.55^{(0.01)}\\ 47.7^{(0.2)}/0.55^{(0.01)}\\ \end{array}$	90.0 ^(15.2) /0.38 ^(0.27) 34.1 ^(14.4) /1.31 ^(0.22) 98.6 ^(1.5) /0.40 ^(0.20) 99.5 ^(0.9) /0.53 ^(0.13) 75.8 ^(6.1) /1.20 ^(0.21) 90.8 ^(14.2) /0.53 ^(0.18) 96.7 ^(3.5) /0.64 ^(0.42) ChEMBL 97.6 ^(0.3) /2.37 ^(0.03) 97.3 ^(0.5) /2.44 ^(0.05) 83.3 ^(2.1) /2.50 ^(0.05) 97.7 ^(0.5) /2.41 ^(0.04) 98.5 ^(0.4) /1.26 ^(0.05) 97.4 ^(0.4) /2.47 ^(0.03) 97.4 ^(0.4) /2.47 ^(0.05) 97.4 ^(0.4) /2.47 ^(0.05) 97.4 ^(0.4) /2.40 ^(0.05) 97.4 ^(0.4) /2.40 ^(0.05) 97.8 ^(0.4) /2.37 ^(0.05) 97.8 ^(0.4) /2.37 ^(0.05) 98.8 ^(0.4) /1.85 ^(0.02) 88.1 ^(1.2) /2.51 ^(0.06)	$\begin{array}{r} 86.2^{(7.7)}/0.39^{(0.29)}\\ 50.0^{(1.9)}/1.39^{(0.29)}\\ 50.0^{(1.9)}/1.39^{(0.24)}\\ 86.6^{(12.7)}/0.27^{(0.12)}\\ 89.6^{(3.4)}/0.55^{(0.22)}\\ 92.2^{(3.3)}/0.39^{(0.12)}\\ 91.9^{(3.4)}/0.14^{(0.13)}\\ 80.2^{(12.9)}/0.43^{(0.34)}\\ \hline \\ \hline$	93.8 ^(0.6) /0.07 ^(0.01) 87.8 ^(3.1) /1.29 ^(0.37) 93.2 ^(1.6) /0.10 ^(0.00) 93.2 ^(1.6) /0.10 ^(0.00) 93.2 ^(1.6) /0.10 ^(0.00) 94.6 ^(0.1) /7.84 ^(0.01) 94.5 ^(0.7) /1.85 ^(0.22) Superconductor 94.6 ^(0.1) /7.84 ^(0.01) 92.5 ^(1.2) /7.61 ^(0.24) 85.5 ^(0.4) /7.54 ^(0.01) 94.3 ^(0.1) /7.84 ^(0.01) 94.3 ^(0.1) /7.87 ^(0.01) 95.1 ^(0.4) /7.45 ^(0.01) 94.8 ^(0.1) /7.87 ^(0.01) 93.8 ^(0.6) /7.78 ^(0.04) 92.9 ^(1.1) /7.78 ^(0.04) 93.8 ^(0.6) /7.8 ^(0.04)	$\begin{array}{c} 91.9^{(2.0)}/0.10^{(0.00)}\\ 101^{(6.3)}/0.06^{(0.00)}\\ 30.8^{(5.7)}/0.25^{(0.09)}\\ 91.9^{(2.0)}/0.10^{(0.00)}\\ 65.5^{(25.2)}/0.05^{(0.03)}\\ 31.8^{(5.6)}/0.06^{(0.10)}\\ 29.6^{(3.6)}/0.02^{(0.00)}\\ 112^{(7.8)}/0.94^{(0.17)}\\ \hline D'Kitty\\ 106^{(2.9)}/6.61^{(0.33)}\\ 105^{(1.6)}/7.19^{(0.22)}\\ 35.5^{(1.2)}/1.66^{(0.01)}\\ 105^{(3.5)}/6.45^{(0.66)}\\ 116^{(2.5)}/7.09^{(0.49)}\\ 30.8^{(25.4)}/2.14^{(1.34)}\\ 14.3^{(1.5)}/1.29^{(0.08)}\\ 126^{(14.6)}/7.92^{(0.04)}\\ \hline D'Kitty\\ 98.8^{(1.1)}/6.64^{(0.09)}\\ 99.2^{(1.6)}/6.84^{(0.11)}\\ 39.8^{(1.1)}/6.64^{(0.09)}\\ 112^{(2.5)}/7.23^{(0.16)}\\ 20.9^{(2.4)}/1.60^{(0.03)}\\ \end{array}$	$\begin{array}{r} 3.2/5.3\\ 5.0/5.8\\ 7.5/1.5\\ 2.5/5.2\\ 4.0/3.7\\ 5.0/4.5\\ 4.5/6.3\\ 4.0/3.3\\ \hline \textbf{Rank}\downarrow\\ 3.3/5.0\\ 4.0/3.0\\ 7.5/3.8\\ \hline 3.2/5.2\\ 3.7/5.0\\ 5.5/5.3\\ \hline 3.0/2.2\\ \hline \textbf{Rank}\downarrow\\ \hline 3.5/4.7\\ 3.8/3.7\\ 7.5/3.7\\ \hline 3.5/4.8\\ \hline 3.3/5.2\\ \hline \end{array}$	71.9/-1.39 43.0/-0.81 74.1/-1.41 69.0/-1.30 59.4/-1.25 62.0/-1.42 75.0/_0.90 Opt. Gap ↑ 76.2/1.70 75.6/1.85 56.6/0.90 76.1/1.42 76.0/1.67 59.3/0.98 58.2/0.82 79.4/2.02 Opt. Gap ↑ 74.8/1.77 74.8/1.77 74.9/1.80 57.2/0.90 74.9/1.77 75.4/1.69
	COMS COMS RoMA ROMA GAMBG DynAMG BO-qE Baselin COMS GAMBG DynAMG BO-qUC Baselin COMS GAMBG COMS RoMA ROMA ROMA ROMA	$\begin{array}{rcrr} & 15.4^{(4.9)}/0.23^{(0.09)} \\ & 12.8^{(0.6)}/0.24^{(0.04)} \\ & 12.8^{(0.6)}/0.24^{(0.04)} \\ & 12.8^{(0.5)}/0.24^{(0.05)} \\ & 22.9^{(6.3)}/0.18^{(0.09)} \\ & 22.8^{(2.8)}/0.12^{(0.08)} \\ & 0 & 22.8^{(2.8)}/0.12^{(0.08)} \\ & 0 & 17.8^{(5.5)}/0.21^{(0.11)} \\ \hline {I & TFBind8} \\ e & 21.8^{(0.5)}/0.41^{(0.02)} \\ & 21.9^{(0.5)}/0.41^{(0.02)} \\ & 21.6^{(0.3)}/0.44^{(0.01)} \\ & 13.6^{(0.3)}/0.40^{(0.03)} \\ & 13.6^{(0.3)}/0.40^{(0.03)} \\ & 0 & 15.4^{(0.3)}/0.40^{(0.02)} \\ & 21.6^{(0.3)}/0.42^{(0.01)} \\ \hline {B & TFBind8} \\ e & 21.6^{(0.3)}/0.40^{(0.02)} \\ & 12.6^{(0.3)}/0.40^{(0.02)} \\ & 12.6^{(0.3)}/0.40^{(0.02)} \\ & 12.6^{(0.3)}/0.31^{(0.02)} \\ & 12.6^{(0.3)}/0.31^{(0.02)} \\ & 12.6^{(0.3)}/0.31^{(0.02)} \\ & 21.9^{(0.3)}/0.31^{(0.02)} \\ & 21.9^{(0.3)}/0.31^{(0.02)} \\ & 21.9^{(0.3)}/0.31^{(0.02)} \\ & 21.9^{(0.3)}/0.31^{(0.02)} \\ & 21.9^{(0.3)}/0.31^{(0.02)} \\ & 21.9^{(0.4)}/0.40^{(0.01)} \\ \end{array}$	$\begin{array}{r} 44.9^{(3.5)}/0.20^{(0.13)}\\ 42.7^{(1.4)}/0.32^{(0.03)}\\ 49.7^{(3.0)}/0.22^{(0.11)}\\ 49.3^{(3.0)}/0.42^{(0.09)}\\ 48.9^{(1.5)}/0.25^{(0.10)}\\ 50.8^{(1.5)}/0.22^{(0.15)}\\ 48.4^{(2.3)}/0.18^{(0.09)}\\ \hline \\ \hline$	90.0 ^(15.2) /0.38 ^(0.27) 34.1 ^(14.4) /1.31 ^(0.22) 98.6 ^(1.5) /0.40 ^(0.20) 99.5 ^(0.9) /0.53 ^(0.13) 75.8 ^(6.1) /1.20 ^(0.21) 90.8 ^(14.2) /0.53 ^(0.18) 96.7 ^(3.5) /0.64 ^(0.42) ChEMBL 97.6 ^(0.3) /2.37 ^(0.03) 97.3 ^(0.5) /2.44 ^(0.05) 83.3 ^(2.1) /2.50 ^(0.05) 97.7 ^(0.5) /2.41 ^(0.04) 98.5 ^(0.4) /1.86 ^(0.05) 87.7 ^(1.3) /2.50 ^(0.03) 97.8 ^(0.3) /2.38 ^(0.10) 97.8 ^(0.3) /2.38 ^(0.10) 97.4 ^(0.4) /2.47 ^(0.05) 97.4 ^(0.4) /2.47 ^(0.05) 97.4 ^(0.4) /2.40 ^(0.05) 97.8 ^(0.3) /2.52 ^(0.05) 97.8 ^(0.3) /2.52 ^(0.05) 97.8 ^(0.3) /2.51 ^(0.06) 97.5 ^(0.4) /2.39 ^(0.05)	$\begin{array}{r} 86.2^{(7.7)}/0.39^{(0.29)}\\ 50.0^{(1.9)}/1.39^{(0.24)}\\ 86.6^{(12.7)}/0.27^{(0.12)}\\ 89.6^{(3.4)}/0.55^{(0.22)}\\ 92.2^{(3.3)}/0.39^{(0.12)}\\ 91.9^{(3.4)}/0.14^{(0.13)}\\ 80.2^{(12.9)}/0.43^{(0.54)}\\ \hline \\ \hline$	93.8 ^(0.6) /0.07 ^(0.01) 87.8 ^(3.1) /1.29 ^(0.37) 93.2 ^(1.6) /0.10 ^(0.00) 93.2 ^(1.6) /0.10 ^(0.00) 93.2 ^(1.6) /0.10 ^(0.00) 94.6 ^(0.1) /1.85 ^(0.22) Superconductor 94.6 ^(0.1) /7.84 ^(0.01) 92.5 ^(1.2) /7.61 ^(0.24) 85.5 ^(0.4) /7.50 ^(0.01) 94.6 ^(0.1) /7.84 ^(0.01) 94.6 ^(0.1) /7.87 ^(0.01) 94.6 ^(0.1) /7.87 ^(0.01) 95.1 ^(0.4) /7.45 ^(0.01) 94.8 ^(0.1) /7.87 ^(0.01) 94.8 ^(0.1) /7.87 ^(0.01) 94.8 ^(0.1) /7.87 ^(0.01) 93.8 ^(0.6) /7.78 ^(0.04) 92.9 ^(1.1) /7.78 ^(0.04) 93.8 ^(0.6) /7.78 ^(0.04) 93.8 ^(0.6) /7.78 ^(0.04) 94.1 ^(0.1) /7.86 ^(0.01) 94.1 ^(0.1) /7.86 ^(0.01)	$\begin{array}{c} 91.9^{(2.0)}/0.10^{(0.00)}\\ 101^{(6.3)}/0.06^{(0.00)}\\ 30.8^{(5.7)}/0.25^{(0.09)}\\ 91.9^{(2.0)}/0.10^{(0.00)}\\ 65.5^{(25.2)}/0.05^{(0.03)}\\ 31.8^{(5.6)}/0.06^{(0.10)}\\ 29.6^{(3.6)}/0.02^{(0.00)}\\ 112^{(7.8)}/0.94^{(0.17)}\\ \hline D'Kitty\\ 106^{(2.9)}/6.61^{(0.33)}\\ 105^{(1.6)}/7.19^{(0.22)}\\ 35.5^{(1.2)}/1.66^{(0.01)}\\ 105^{(3.5)}/6.45^{(0.66)}\\ 116^{(2.5)}/7.09^{(0.49)}\\ 30.8^{(25.4)}/2.14^{(1.34)}\\ 14.3^{(1.5)}/1.29^{(0.08)}\\ 126^{(14.6)}/7.92^{(0.04)}\\ \hline D'Kitty\\ 98.8^{(1.1)}/6.64^{(0.09)}\\ 99.2^{(1.6)}/6.84^{(0.11)}\\ 39.4^{(6.0)}/1.66^{(0.03)}\\ 20.9^{(2.4)}/1.60^{(0.03)}\\ 25.9^{(1.4)}/1.34^{(0.04)}\\ \end{array}$	$\begin{array}{r} 3.2/5.3\\ 5.0/5.8\\ 7.5/1.5\\ 2.5/5.2\\ 4.0/3.7\\ 5.0/4.5\\ 4.5/6.3\\ 4.0/3.3\\ \hline \textbf{Rank} \downarrow\\ 3.3/5.0\\ 4.0/3.0\\ 7.5/3.8\\ 3.2/5.2\\ 3.7/5.0\\ 5.5/5.3\\ 3.0/2.2\\ \hline \textbf{Rank} \downarrow\\ \hline 3.5/4.7\\ 3.8/3.7\\ 7.5/3.7\\ 3.5/4.8\\ 3.3/5.2\\ 5.7/5.3\\ \hline \textbf{S.7/5.3}\\ \hline $	$\overline{71.9/-1.39}$ $43.0/-0.81$ $74.1/-1.41$ $69.0/-1.30$ $59.4/-1.25$ $62.0/-1.42$ $75.0/-0.90$ Opt. Gap \uparrow $76.2/1.70$ $75.6/1.85$ $56.6/0.90$ $76.1/1.42$ $76.0/1.67$ $59.3/0.98$ $58.2/0.82$ $79.4/2.02$ Opt. Gap \uparrow $74.8/1.77$ $74.7/1.80$ $57.2/0.90$ $74.9/1.77$ $75.4/1.69$ $58.2/0.89$
	COMS COMS RoMA ROMA GAMB DynAM BO-qE Baselin COMS COMS RoMA ROMA BO-qUC Baselin COMS COMS COMS COMS COMS COMS RoMA	$\begin{array}{rcrr} & 15.4^{(4.9)}/0.23^{(0.09)} \\ & 12.8^{(0.6)}/0.24^{(0.04)} \\ & 12.8^{(0.6)}/0.24^{(0.04)} \\ & 12.8^{(0.5)}/0.24^{(0.07)} \\ & 17.1^{(3.3)}/0.22^{(0.05)} \\ & 0 & 22.9^{(6.3)}/0.18^{(0.09)} \\ & 0 & 22.8^{(2.3)}/0.12^{(0.08)} \\ & 0 & 22.8^{(2.3)}/0.12^{(0.08)} \\ & 0 & 22.8^{(2.3)}/0.21^{(0.11)} \\ \hline {\bf I} & {\bf TFBind8} \\ e & 21.8^{(0.5)}/0.41^{(0.02)} \\ & - & 21.9^{(0.5)}/0.41^{(0.02)} \\ & - & 21.9^{(0.5)}/0.41^{(0.02)} \\ & + & 12.7^{(0.4)}/0.44^{(0.01)} \\ & + & 13.6^{(0.3)}/0.40^{(0.03)} \\ & - & 21.6^{(0.3)}/0.40^{(0.03)} \\ & 0 & 15.6^{(0.4)}/0.39^{(0.02)} \\ & 0 & 15.6^{(0.4)}/0.49^{(0.02)} \\ & 0 & 21.6^{(0.3)}/0.40^{(0.02)} \\ & - & 21.6^{(0.3)}/0.40^{(0.02)} \\ & - & 21.6^{(0.3)}/0.40^{(0.02)} \\ & + & 13.9^{(0.3)}/0.31^{(0.02)} \\ & 0 & 16.0^{(0.4)}/0.40^{(0.01)} \\ \end{array}$	$\begin{array}{r} 44.9^{(3.5)}/0.20^{(0.13)}\\ 42.7^{(1.4)}/0.32^{(0.03)}\\ 49.7^{(3.0)}/0.22^{(0.11)}\\ 49.3^{(3.0)}/0.42^{(0.09)}\\ 48.9^{(1.5)}/0.25^{(0.10)}\\ 50.8^{(1.5)}/0.22^{(0.15)}\\ 48.4^{(2.3)}/0.18^{(0.09)}\\ \hline \\ \hline$	90.0 ^(15.2) /0.38 ^(0.27) 34.1 ^(14.4) /1.31 ^(0.22) 98.6 ^(1.5) /0.40 ^(0.20) 99.5 ^(0.9) /0.53 ^(0.13) 75.8 ^(6.1) /1.20 ^(0.21) 90.8 ^(14.2) /0.53 ^(0.18) 96.7 ^(3.5) /0.64 ^(0.42) ChEMBL 97.6 ^(0.3) /2.37 ^(0.03) 97.3 ^(0.5) /2.44 ^(0.05) 83.3 ^(2.1) /2.50 ^(0.05) 97.7 ^(0.5) /2.41 ^(0.04) 98.5 ^(0.4) /1.86 ^(0.05) 87.7 ^(1.3) /2.50 ^(0.03) 97.8 ^(0.3) /2.38 ^(0.10) 97.8 ^(0.3) /2.38 ^(0.10) 97.4 ^(0.4) /2.47 ^(0.05) 97.4 ^(0.4) /2.47 ^(0.05) 97.4 ^(0.4) /2.40 ^(0.05) 97.8 ^(0.3) /2.52 ^(0.05) 97.8 ^(0.3) /2.52 ^(0.05) 97.8 ^(0.3) /2.51 ^(0.06) 97.5 ^(0.4) /2.39 ^(0.05)	$\begin{array}{r} 86.2^{(7.7)}/0.39^{(0.29)}\\ 50.0^{(1.9)}/1.39^{(0.24)}\\ 86.6^{(12.7)}/0.27^{(0.12)}\\ 89.6^{(3.4)}/0.55^{(0.22)}\\ 92.2^{(3.3)}/0.39^{(0.12)}\\ 91.9^{(3.4)}/0.14^{(0.13)}\\ 80.2^{(12.9)}/0.43^{(0.54)}\\ \hline \\ \hline$	93.8 ^(0.6) /0.07 ^(0.01) 87.8 ^(3.1) /1.29 ^(0.37) 93.2 ^(1.6) /0.10 ^(0.00) 93.2 ^(1.6) /0.10 ^(0.00) 93.2 ^(1.6) /0.10 ^(0.00) 94.6 ^(0.1) /1.85 ^(0.22) Superconductor 94.6 ^(0.1) /7.84 ^(0.01) 92.5 ^(1.2) /7.61 ^(0.24) 85.5 ^(0.4) /7.50 ^(0.01) 94.6 ^(0.1) /7.84 ^(0.01) 94.6 ^(0.1) /7.87 ^(0.01) 94.6 ^(0.1) /7.87 ^(0.01) 95.1 ^(0.4) /7.45 ^(0.01) 94.8 ^(0.1) /7.87 ^(0.01) 94.8 ^(0.1) /7.87 ^(0.01) 94.8 ^(0.1) /7.87 ^(0.01) 93.8 ^(0.6) /7.78 ^(0.04) 92.9 ^(1.1) /7.78 ^(0.04) 93.8 ^(0.6) /7.78 ^(0.04) 93.8 ^(0.6) /7.78 ^(0.04) 94.1 ^(0.1) /7.86 ^(0.01) 94.1 ^(0.1) /7.86 ^(0.01)	$\begin{array}{c} 91.9^{(2.0)}/0.10^{(0.00)}\\ 101^{(6.3)}/0.06^{(0.00)}\\ 30.8^{(5.7)}/0.25^{(0.09)}\\ 91.9^{(2.0)}/0.10^{(0.00)}\\ 65.5^{(25.2)}/0.05^{(0.03)}\\ 31.8^{(5.6)}/0.06^{(0.10)}\\ 29.6^{(3.6)}/0.02^{(0.00)}\\ 112^{(7.8)}/0.94^{(0.17)}\\ \hline D'Kitty\\ 106^{(2.9)}/6.61^{(0.33)}\\ 105^{(1.6)}/7.19^{(0.22)}\\ 35.5^{(1.2)}/1.66^{(0.01)}\\ 105^{(3.5)}/6.45^{(0.66)}\\ 116^{(2.5)}/7.09^{(0.49)}\\ 30.8^{(25.4)}/2.14^{(1.34)}\\ 14.3^{(1.5)}/1.29^{(0.08)}\\ 126^{(14.6)}/7.92^{(0.04)}\\ \hline D'Kitty\\ 98.8^{(1.1)}/6.64^{(0.09)}\\ 99.2^{(1.6)}/6.84^{(0.11)}\\ 39.4^{(6.0)}/1.66^{(0.03)}\\ 20.9^{(2.4)}/1.60^{(0.03)}\\ 25.9^{(1.4)}/1.34^{(0.04)}\\ \end{array}$	$\begin{array}{r} 3.2/5.3\\ 5.0/5.8\\ 7.5/1.5\\ 2.5/5.2\\ 4.0/3.7\\ 5.0/4.5\\ 4.5/6.3\\ 4.0/3.3\\ \hline \textbf{Rank} \downarrow\\ 3.3/5.0\\ 4.0/3.0\\ 7.5/3.8\\ \underline{3.2/5.2}\\ 3.7/5.0\\ 5.5/5.3\\ 5.7/6.3\\ \underline{3.0/2.2}\\ \hline \textbf{Rank} \downarrow\\ \underline{3.5/4.7}\\ \underline{3.5/4.7}\\ 3.8/\underline{3.7}\\ 7.5/3.7\\ \underline{3.5/4.8}\\ \mathbf{3.3/5.2}\\ 5.7/5.3\\ 4.7/6.0\\ \hline \end{array}$	$\overline{71.9}/-1.39$ $43.0/-0.81$ $74.1/-1.41$ $69.0/-1.30$ $59.4/-1.25$ $62.0/-1.42$ $75.0/-0.90$ Opt. Gap \uparrow $76.2/1.70$ $75.6/1.85$ $56.6/0.90$ $76.1/1.42$ $76.0/1.67$ $59.3/0.98$ $58.2/0.82$ $79.4/2.02$ Opt. Gap \uparrow $74.8/1.77$ $74.7/1.80$ $57.2/0.90$ $74.9/1.77$ $75.4/1.69$ $58.2/0.89$ $60.7/0.82$
	COMS COMS RoMA ROMA GAMBG DynAMG BO-qE Baselin COMS GAMBG DynAMG BO-qUC Baselin COMS GAMBG COMS RoMA ROMA ROMA ROMA	$\begin{array}{rcrr} & 15.4^{(4.9)}/0.23^{(0.09)} \\ & 12.8^{(0.6)}/0.24^{(0.04)} \\ & 12.8^{(0.6)}/0.24^{(0.04)} \\ & 12.8^{(0.5)}/0.24^{(0.07)} \\ & 17.1^{(3.3)}/0.22^{(0.05)} \\ & 0 & 22.9^{(6.3)}/0.18^{(0.09)} \\ & 0 & 22.8^{(2.3)}/0.12^{(0.08)} \\ & 0 & 22.8^{(2.3)}/0.12^{(0.08)} \\ & 0 & 22.8^{(2.3)}/0.21^{(0.11)} \\ \hline {\bf I} & {\bf TFBind8} \\ e & 21.8^{(0.5)}/0.41^{(0.02)} \\ & - & 21.9^{(0.5)}/0.41^{(0.02)} \\ & - & 21.9^{(0.5)}/0.41^{(0.02)} \\ & + & 12.7^{(0.4)}/0.44^{(0.01)} \\ & + & 13.6^{(0.3)}/0.40^{(0.03)} \\ & - & 21.6^{(0.3)}/0.40^{(0.03)} \\ & 0 & 15.6^{(0.4)}/0.39^{(0.02)} \\ & 0 & 15.6^{(0.4)}/0.49^{(0.02)} \\ & 0 & 21.6^{(0.3)}/0.40^{(0.02)} \\ & - & 21.6^{(0.3)}/0.40^{(0.02)} \\ & - & 21.6^{(0.3)}/0.40^{(0.02)} \\ & + & 13.9^{(0.3)}/0.31^{(0.02)} \\ & 0 & 16.0^{(0.4)}/0.40^{(0.01)} \\ \end{array}$	$\begin{array}{r} 44.9^{(3.5)}/0.20^{(0.13)}\\ 42.7^{(1.4)}/0.32^{(0.03)}\\ 49.7^{(3.0)}/0.22^{(0.11)}\\ 49.3^{(3.0)}/0.42^{(0.09)}\\ 48.9^{(1.5)}/0.25^{(0.10)}\\ 50.8^{(1.5)}/0.22^{(0.15)}\\ 48.4^{(2.3)}/0.18^{(0.09)}\\ \hline \\ \hline$	90.0 ^(15.2) /0.38 ^(0.27) 34.1 ^(14.4) /1.31 ^(0.22) 98.6 ^(1.5) /0.40 ^(0.20) 99.5 ^(0.9) /0.53 ^(0.13) 75.8 ^(6.1) /1.20 ^(0.21) 90.8 ^(14.2) /0.53 ^(0.18) 96.7 ^(3.5) /0.64 ^(0.42) ChEMBL 97.6 ^(0.3) /2.37 ^(0.03) 97.3 ^(0.5) /2.44 ^(0.05) 83.3 ^(2.1) /2.50 ^(0.05) 97.7 ^(0.5) /2.41 ^(0.04) 98.5 ^(0.4) /1.86 ^(0.05) 87.7 ^(1.3) /2.50 ^(0.03) 97.8 ^(0.3) /2.38 ^(0.10) 97.8 ^(0.3) /2.38 ^(0.10) 97.4 ^(0.4) /2.47 ^(0.05) 97.4 ^(0.4) /2.47 ^(0.05) 97.4 ^(0.4) /2.40 ^(0.05) 97.8 ^(0.3) /2.52 ^(0.05) 97.8 ^(0.3) /2.52 ^(0.05) 97.8 ^(0.3) /2.51 ^(0.06) 97.5 ^(0.4) /2.39 ^(0.05)	$\begin{array}{r} 86.2^{(7.7)}/0.39^{(0.29)}\\ 50.0^{(1.9)}/1.39^{(0.24)}\\ 86.6^{(12.7)}/0.27^{(0.12)}\\ 89.6^{(3.4)}/0.55^{(0.22)}\\ 92.2^{(3.3)}/0.39^{(0.12)}\\ 91.9^{(3.4)}/0.14^{(0.13)}\\ 80.2^{(12.9)}/0.43^{(0.54)}\\ \hline \\ \hline$	93.8 ^(0.6) /0.07 ^(0.01) 87.8 ^(3.1) /1.29 ^(0.37) 93.2 ^(1.0) /0.10 ^(0.00) 93.2 ^(1.0) /0.10 ^(0.00) 93.2 ^(1.0) /0.10 ^(0.00) 94.6 ^(0.1) /7.185 ^(0.22) Superconductor 94.6 ^(0.1) /7.84 ^(0.01) 92.5 ^(1.2) /7.61 ^(0.24) 85.5 ^(0.4) /7.50 ^(0.01) 94.6 ^(0.1) /7.84 ^(0.01) 94.6 ^(0.1) /7.87 ^(0.01) 94.6 ^(0.1) /7.87 ^(0.01) 95.1 ^(0.4) /7.45 ^(0.01) 94.8 ^(0.1) /7.87 ^(0.01) 94.1 ^(0.1) /7.8 ^(0.01) 94.1 ^(0.1) /7.86 ^(0.01) 94.1 ^(0.1) /7.86 ^(0.01) 94.1 ^(0.1) /7.86 ^(0.01)	$\begin{array}{c} 91.9^{(2.0)}/0.10^{(0.00)}\\ 101^{(6.3)}/0.06^{(0.00)}\\ 30.8^{(5.7)}/0.25^{(0.09)}\\ 91.9^{(2.0)}/0.10^{(0.00)}\\ 65.5^{(25.2)}/0.05^{(0.03)}\\ 31.8^{(5.6)}/0.06^{(0.10)}\\ 29.6^{(3.6)}/0.02^{(0.00)}\\ 112^{(7.8)}/0.94^{(0.17)}\\ \hline D'Kitty\\ 106^{(2.9)}/6.61^{(0.33)}\\ 105^{(1.6)}/7.19^{(0.22)}\\ 35.5^{(1.2)}/1.66^{(0.01)}\\ 105^{(3.5)}/6.45^{(0.66)}\\ 116^{(2.5)}/7.09^{(0.49)}\\ 30.8^{(25.4)}/2.14^{(1.34)}\\ 14.3^{(1.5)}/1.29^{(0.08)}\\ 126^{(14.6)}/7.92^{(0.04)}\\ \hline D'Kitty\\ 98.8^{(1.1)}/6.64^{(0.09)}\\ 99.2^{(1.6)}/6.84^{(0.11)}\\ 39.4^{(6.0)}/1.66^{(0.03)}\\ 20.9^{(2.4)}/1.60^{(0.03)}\\ 25.9^{(1.4)}/1.34^{(0.04)}\\ \end{array}$	$\begin{array}{r} 3.2/5.3\\ 5.0/5.8\\ 7.5/1.5\\ 2.5/5.2\\ 4.0/3.7\\ 5.0/4.5\\ 4.5/6.3\\ 4.0/3.3\\ \hline \textbf{Rank} \downarrow\\ 3.3/5.0\\ 4.0/3.0\\ 7.5/3.8\\ \underline{3.2/5.2}\\ 3.7/5.0\\ 5.5/5.3\\ 5.7/6.3\\ \underline{3.0/2.2}\\ \hline \textbf{Rank} \downarrow\\ \underline{3.5/4.7}\\ \underline{3.5/4.7}\\ 3.8/\underline{3.7}\\ 7.5/3.7\\ \underline{3.5/4.8}\\ \mathbf{3.3/5.2}\\ 5.7/5.3\\ 4.7/6.0\\ \hline \end{array}$	$\overline{71.9}/-1.39$ $43.0/-0.81$ $74.1/-1.41$ $69.0/-1.30$ $59.4/-1.25$ $62.0/-1.42$ $75.0/-0.90$ Opt. Gap \uparrow $76.2/1.70$ $75.6/1.85$ $56.6/0.90$ $76.1/1.42$ $76.0/1.67$ $59.3/0.98$ $58.2/0.82$ $79.4/2.02$ Opt. Gap \uparrow $74.8/1.77$ $74.7/1.80$ $57.2/0.90$ $74.9/1.77$ $75.4/1.69$ $58.2/0.89$ $60.7/0.82$

1430 for probability distributions Q, P.¹ Given a mixed f-divergence, we can define a modified MBO objective as in (5):

$$J_{f}(\pi;\gamma) := \mathbb{E}_{q^{\pi}}[r_{\theta}(x)] - \frac{\beta}{\tau} D_{f}(q^{\pi}||p_{\mathcal{D}}^{\tau};\gamma) = \mathbb{E}_{q^{\pi}}[r_{\theta}(x)] - \frac{\beta}{\tau} D_{\mathrm{KL}}(q^{\pi}||p_{\mathcal{D}}^{\tau}) - \frac{\beta\gamma}{\tau} D_{f}(q^{\pi}||p_{\mathcal{D}}^{\tau})$$

$$= J(\pi) - \frac{\beta\gamma}{\tau} D_{f}(q^{\pi}||p_{\mathcal{D}}^{\tau})$$
(57)

where r_{θ} is again the forward surrogate model, $J(\pi)$ is as in (5), $p_{\mathcal{D}}^{\tau}(x)$ is the τ -weighted probability distribution as in **Definition 3.2**, and $q^{\pi}(x)$ is the sampled distribution over designs admitted by the realized sampling policy π . Given this expression for the modified MBO objective, it is easy to rewrite $J_f(\pi; \gamma)$ similar to **Lemma 3.3** in the main text:

Lemma D.1 (Generalized Entropy-Divergence Formulation for Mixed *f*-Divergence). Define $J_f(\pi; \gamma)$ as in (57). An 1441 equivalent representation of $J_f(\pi; \gamma)$ is

$$J_f(\pi) \simeq -\mathcal{H}(q^{\pi}(x)) - (1+\beta)D_{KL}(q^{\pi}(x)||p_{\mathcal{D}}^{\tau}(x)) - \beta\gamma D_f(q^{\pi}(x)||p_{\mathcal{D}}^{\tau}(x))$$
(58)

where $\mathcal{H}(\cdot)$ as the Shannon entropy and $D_f(\cdot||\cdot)$ as the f-divergence.

Proof. The proof is trivial using **Lemma 3.3**: 1449

$$J_{f}(\pi) := \mathbb{E}_{q^{\pi}}[r_{\theta}(x)] - \frac{\beta}{\tau} D_{f}(q^{\pi} || p_{\mathcal{D}}^{\tau}; \pi) = J(\pi) - \frac{\beta \gamma}{\tau} D_{f}(q^{\pi} || p_{\mathcal{D}}^{\tau})$$

$$\simeq \tau \cdot J(\pi) - \beta \gamma D_{f}(q^{\pi} || p_{\mathcal{D}}^{\tau})$$

$$\simeq -\mathcal{H}(q^{\pi}) - (1 + \beta) D_{\mathrm{KL}}(q^{\pi} || p_{\mathcal{D}}^{\tau}) - \beta \gamma D_{f}(q^{\pi} || p_{\mathcal{D}}^{\tau})$$
(59)

¹⁴⁵⁵₁₄₅₆ up to a constant independent of the policy π .

We now consider its derivative optimization problem constrained by source critic feedback analogous to (7):

$$\max_{\pi \in \Pi} \quad J_f(\pi; \gamma) = \mathbb{E}_{q^{\pi}}[r_{\theta}(x)] - \frac{\beta}{\tau} D_f(q^{\pi} || p_{\mathcal{D}}^{\tau}; \gamma)$$

s.t.
$$\mathbb{E}_{x \sim p_{\mathcal{D}}^{\tau}(x)} c^*(x) - \mathbb{E}_{x \sim q^{\pi}(x)} c^*(x) \le W_0$$
 (60)

where $c^*(x)$ is again an adversarial source critic and W_0 is some nonnegative constant. We can show that (60) admits an explicit dual function which can be used to tractably solve this optimization problem.

1467 Lemma D.2 (Explicit Dual Function of (60)). Consider the primal problem

$$\max_{\pi \in \Pi} \quad J_f(\pi; \gamma) = \mathbb{E}_{q^{\pi}}[r_{\theta}(x)] - \frac{\beta}{\tau} D_f(q^{\pi} || p_{\mathcal{D}}^{\tau}; \gamma)$$

$$s.t. \quad \mathbb{E}_{x \sim p_{\mathcal{D}}^{\tau}(x)}[c^*(x)] - \mathbb{E}_{x \sim q^{\pi}(x)}[c^*(x)] \le W_0$$
(61)

1474 for some convex function f where $0 \notin dom(f)$. The Lagrangian dual function $g(\lambda)$ is bounded from below by the function 1474 $g_{\ell}(\lambda)$ given by

$$g_{\ell}(\lambda) := \beta \left[(1+\gamma)\lambda(\mathbb{E}_{p_{\mathcal{D}}^{\tau}}[c^{*}(x)] - W_{0}) - \mathbb{E}_{p_{\mathcal{D}}^{\tau}}e^{\lambda c^{*}(x) - 1} - \gamma \mathbb{E}_{p_{\mathcal{D}}^{\tau}}f^{*}(\lambda c^{*}(x)) \right]$$
(62)

1478 where $f^{\star}(\cdot)$ is the Fenchel conjugate of f.

1481 Proof. Recall that the generator function of the mixed f-divergence penalty is given by $f_{\gamma}(u) = \gamma f(u) + u \log u$ for some 1482 weighting scalar $\gamma \in [1, +\infty)$. Define $f_{\text{KL}}(u) := u \log u$. From (10), the dual function $g(\lambda) : \mathbb{R}_+ \to \mathbb{R}$ of the primal

¹⁴⁸³ ¹It is trivial to verify both that $f_{\gamma}(u)$ is convex and that $0 \notin \text{dom}(f_{\gamma})$ given a function f(u) that also satisfies both of these conditions.

1485 problem is given by

1486

1492

1499 1500

1503 1504

1525

1526

1534 1535 1536

$$\begin{aligned} & I_{1487} \\ I_{488} \\ I_{488} \\ I_{489} \\ I_{490} \end{aligned} = \min_{\pi \in \Pi} \left[(1+\beta) \mathbb{E}_{p_{\mathcal{D}}^{\tau}} f_{\mathsf{KL}} \left(\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \right) + \beta \gamma \mathbb{E}_{p_{\mathcal{D}}^{\tau}} f \left(\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \right) - \mathbb{E}_{q^{\pi}} \log (q^{\pi}) + \beta (1+\gamma) \lambda \left(\mathbb{E}_{p_{\mathcal{D}}^{\tau}} c^{*}(x) - \mathbb{E}_{q^{\pi}} c^{*}(x) - W_{0} \right) \right] \\ & = \min_{\pi \in \Pi} \left[(1+\beta) \mathbb{E}_{p_{\mathcal{D}}^{\tau}} f_{\mathsf{KL}} \left(\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \right) + \beta \gamma \mathbb{E}_{p_{\mathcal{D}}^{\tau}} f \left(\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \right) - \left(\mathbb{E}_{p_{\mathcal{D}}^{\tau}} f_{\mathsf{KL}} \left(\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \right) + \mathbb{E}_{q^{\pi}} \log p_{\mathcal{D}}^{\tau} \right) \right]
\end{aligned}$$

$$+ \beta (1+\gamma) \lambda \left(\mathbb{E}_{p_{\mathcal{D}}^{\tau}} c^*(x) - \mathbb{E}_{q^{\pi}} c^*(x) - W_0 \right)$$

$$\lim_{\pi \in \Pi} \left[\beta \mathbb{E}_{p_{\mathcal{D}}^{\tau}} f_{\mathsf{KL}} \left(\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \right) + \beta \gamma \mathbb{E}_{p_{\mathcal{D}}^{\tau}} f \left(\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}} \right) - \mathbb{E}_{q^{\pi}} \log p_{\mathcal{D}}^{\tau} + \beta (1+\gamma) \lambda \left(\mathbb{E}_{p_{\mathcal{D}}^{\tau}} c^{*}(x) - \mathbb{E}_{q^{\pi}} c^{*}(x) - W_{0} \right) \right]$$
(63)

where we define $\beta(1 + \gamma)\lambda \in \mathbb{R}_+$ as the Lagrangian multiplier associated with the constraint in (60) (recall that \mathbb{R}_+ is closed under multiplication). We rearrange terms to rewrite $g(\lambda)$ as

$$g(\lambda) = \min_{\pi \in \Pi} \left[\beta \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \left[-\left(\lambda c^{*}(x) \cdot \frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}}\right) + f_{\mathsf{KL}}\left(\frac{q^{\pi}}{p_{\mathcal{D}}}\right) \right] + \beta \gamma \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \left[-\left(\lambda c^{*}(x) \cdot \frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}}\right) + f\left(\frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}}\right) \right] - \mathbb{E}_{q^{\pi}} \log p_{\mathcal{D}}^{\tau} + \beta (1+\gamma) \lambda \mathbb{E}_{p_{\mathcal{D}}^{\tau}} c^{*}(x) - \beta (1+\gamma) \lambda W_{0} \right]$$

$$(64)$$

 $\frac{1505}{1506}$ The sum of function minima is a lower bound on the minima of the sum:

$$g(\lambda) \geq \beta \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \min_{\pi \in \Pi} \left[-\left(\lambda c^{*}(x) \cdot \frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}}\right) + f_{\mathrm{KL}}\left(\frac{q^{\pi}}{p_{\mathcal{D}}}\right) \right] + \beta \gamma \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \min_{\pi \in \Pi} \left[-\left(\lambda c^{*}(x) \cdot \frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}}\right) + f\left(\frac{q^{\pi}}{p_{\mathcal{D}}}\right) \right] - \max_{\pi \in \Pi} \mathbb{E}_{q^{\pi}} \log p_{\mathcal{D}}^{\tau} + \min_{\pi \in \Pi} \left[\beta (1+\gamma) \lambda \mathbb{E}_{p_{\mathcal{D}}^{\tau}} c^{*}(x) - \beta (1+\gamma) \lambda W_{0} \right] \sim \beta \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \min_{\pi \in \Pi} \left[-\left(\lambda c^{*}(x) \cdot \frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}}\right) + f_{\mathrm{KL}}\left(\frac{q^{\pi}}{p_{\mathcal{D}}}\right) \right] + \beta \gamma \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \min_{\pi \in \Pi} \left[-\left(\lambda c^{*}(x) \cdot \frac{q^{\pi}}{p_{\mathcal{D}}^{\tau}}\right) + f\left(\frac{q^{\pi}}{p_{\mathcal{D}}}\right) \right] + \beta (1+\gamma) \lambda \mathbb{E}_{p_{\mathcal{D}}^{\tau}} c^{*}(x) - \beta (1+\gamma) \lambda W_{0}$$

$$(65)$$

ignoring the term $\max_{\pi \in \Pi} [\mathbb{E}_{q^{\pi}} \log p_{\mathcal{D}}^{\tau}]$ that is constant with respect to λ . We then perform the same tactic of minimizing over the superset $\mathbb{R}_+ \supseteq \{z \mid \exists \pi \in \Pi \text{ s.t. } q^{\pi}(x)/p_{\mathcal{D}}^{\tau}(x) = z\}$ as in **Appendix A**:

where $f^{\star}(\cdot)$ is the Fenchel conjugate of a convex function $f(\cdot)$. The Fenchel conjugate of $f_{\text{KL}}(u) = u \log u$ is $f_{\text{KL}}^{\star}(v) = e^{v-1}$ (Borwein & Lewis, 2006), so

$$g(\lambda) \ge \beta \left[-\mathbb{E}_{p_{\mathcal{D}}^{\tau}} e^{\lambda c^*(x) - 1} - \gamma \mathbb{E}_{p_{\mathcal{D}}^{\tau}} f^*(\lambda c^*(x)) + (1 + \gamma)\lambda(\mathbb{E}_{p_{\mathcal{D}}^{\tau}} c^*(x) - W_0) \right]$$
(67)

¹⁵²⁷ Define the right hand side of this inequality as the function $g_{\ell}(\lambda)$ and the result is immediate.

1529 **Corollary D.3** (Explicit Dual Function of (60) Using Mixed χ^2 -Divergence). As an example, we can consider the mixed 1530 χ^2 -divergence defined by $D_{\chi^2}(Q||P; \gamma) = \gamma D_{\chi^2}(Q||P) + D_{KL}(Q||P)$ as used in Huang et al. (2024a). The χ^2 -divergence 1531 generator function is $f_{\chi^2}(u) = (u-1)^2/2$, and its Fenchel conjugate is $f_{\chi^2}^*(v) = v + (v^2/2)$ from Lemma C.4. Directly 1532 applying Lemma D.2, our lower bound on the our dual function is

$$g(\lambda) \ge g_{\ell}(\lambda) := \beta \left[-\mathbb{E}_{p_{\mathcal{D}}^{\tau}} e^{\lambda c^*(x) - 1} - \gamma \mathbb{E}_{p_{\mathcal{D}}^{\tau}} \left(\frac{1}{2} (\lambda c^*(x))^2 + \lambda c^*(x) \right) + (1 + \gamma) \lambda (\mathbb{E}_{p_{\mathcal{D}}^{\tau}} c^*(x) - W_0) \right]$$
(68)

To experimentally evaluate the utility of distribution matching using a mixed χ^2 -KL-Divergence, we substitute the $D_{\text{KL}}(\cdot || \cdot)$ divergence with the mixed χ^2 -Divergence $D_{f_{\chi^2}}(\cdot || \cdot; \gamma)$ (setting $\gamma = 1.0$ for experimental evaluation) and its associated *1540* dual function bound from (68) into Algorithm 1. Practically, we find that this only requires updating the dual function per*1541* Corollary D.3 and the Lagrangian of (60) given by

$$\mathcal{L}(x;\lambda) = -\mathbb{E}_{q^{\pi}}[r_{\theta}(x)] + \frac{\beta}{\tau} \left[\gamma D_{f}(q^{\pi}||p_{\mathcal{D}}^{\tau}) + D_{\mathrm{KL}}(q^{\pi}||p_{\mathcal{D}}^{\tau})\right] + \beta(1+\gamma)\lambda \left[\mathbb{E}_{p_{\mathcal{D}}^{\tau}}c^{*}(x) - \mathbb{E}_{q^{\pi}}c^{*}(x) - W_{0}\right]$$
(69)

1544 1545 in **Algorithm 1**.

1542 1543

1560 1561

1574

1592

1594

1546 **Experimental Results.** We compare DynAMO implemented with a mixed χ^2 divergence penalty (with $\gamma = 1.0$) against our 1547 original DynAMO implementation (i.e., $\gamma = 0$) in **Supplementary Tables A4-A5**. Empirically, we find that using the mixed 1548 χ^2 -divergence penalty offers limited utility compared with KL-divergence alone: the latter is non-inferior to the former 1549 according to both the Rank and Optimality Gap metrics for all 6 optimizers assessed according to the Best@128 oracle score. Furthermore, DynAMO outperforms DynAMO with mixed χ^2 -divergence according to the Rank and Optimality Gap 1550 metrics for 5 out of the 6 optimizers assessed according to the Pairwise Diversity metric. Based on our qualitative analysis, we hypothesize that the over-conservatism often attributed to χ^2 -divergence-based penalties in related literature (Ma et al., 2022; Huang et al., 2024a; Wang et al., 2024) may adversely affect the generative policy's ability to sufficiently explore the 1554 design space when compared to using KL-divergence-base distribution matching alone. Further work is needed to tune the relative mixing parameter γ and/or explore how other alternative f-divergence metrics may be used with DynAMO.

D.4. Theoretical Guarantees for DynAMO

1559 In this section, we seek to place an upper bound on the difference between true diversity-penalized objective

$$J^{\star}(\pi) := \mathbb{E}_{x \sim q^{\pi}(x)}[r(x)] - \frac{\beta}{\tau} D_{\mathrm{KL}}(q^{\pi}(x)||p^{\tau}(x))$$
(70)

realized by the final generative policy $\hat{\pi} \in \Pi$ learned by DynAMO (denoted as π^* in the main text), and the true diversitypenalized objective realized by the true optimal policy $\pi^* := \arg \max_{\pi \in \Pi} J^*(\pi)$. Note that this objective $J^*(\pi)$ is *not* equivalent to the offline MBO objective $J(\pi)$ introduced in (5); importantly, the objective $J(\pi)$ is a function of the *true*, hidden oracle reward r(x) as opposed to the forward surrogate model $r_{\theta}(x)$. Furthermore, the KL-divergence penalty is computed with respect to the *true* τ -weighted probability distribution $p^{\tau}(x)$, as opposed to its empirical estimate computed from the offline dataset \mathcal{D} as in **Definition 3.2**. In principle, (70) captures the true trade-off between diversity and quality of designs that we hope to achieve by the theoretically optimal zero-regret generative policy π^* that maximizes (70) over Π .

Our main result is in **Theorem D.9** below, although we first step through the relevant assumptions and intermediate results necessary to arrive at our bound on (70). Firstly, we assume the following:

1572 Assumption D.4 (Surrogate Model Error Bound). There exists a finite $\varepsilon_0^2 \in \mathbb{R}_+$ such that

$$\mathbb{E}_{x \sim p^{\tau}(x)} [r(x) - r_{\theta}(x)]^2 \le \varepsilon_0^2 / 4 \tag{71}$$

¹⁵⁷⁵ for any choice in $\tau \ge 0$, where $p^{\tau}(x)$ is the true τ -weighted probability distribution over \mathcal{X} .

Assumption D.5 (Policy Realizability). Both the true optimal sampling policy π^* according to (70) and optimal sampling policy $\hat{\pi}$ according to (7) are contained in the (finite) policy class Π .

Assumption D.6 (Bounded Importance Weights). Define the *importance weight* w(x) as the ratio between probability distributions $q^{\pi}(x)$ and p(x). There exists a finite $M \in \mathbb{R}_+$ such that for all possible permutations of $\pi \in \{\hat{\pi}, \pi^*\}$ and $p(x) \in \{p^{\tau}(x), p_{\mathcal{D}}^{\tau}(x)\}$, we have $w(x) := q^{\pi}(x)/p(x) \leq M$ for all $x \in \mathcal{X}$.

Remark. This assumption is mild assuming that (1) \mathcal{D} is large enough such that $p_{\mathcal{D}}^{\tau}(x) \approx p^{\tau}(x)$; and (2) the policy π has been learned with sufficiently large β according to **Algorithm 1** or a similar distribution matching objective, such that the distribution of designs learned by the generative policy $q^{\hat{\pi}}(x)$ well-approximates the expert distribution $p_{\mathcal{D}}^{\tau}(x)$. Because the optimal policy π^* should also well-approximate $p^{\tau}(x)$ (and therefore $p_{\mathcal{D}}^{\tau}(x)$ by assumption), the assumption that such a finite *M* exists is reasonable.

¹⁵⁸⁸ Under these assumptions, we first place a bound on the error of the forward surrogate model over the distribution of ¹⁵⁸⁹ generated designs from the optimal policies according to both the offline objective $J(\pi)$ and true objective $J^*(\pi)$:

1590 **Lemma D.7** (Bounded Prediction Error). Assume there exists an $M \in \mathbb{R}_+$ finite satisfying Assumption D.6. Then with 1591 probability at least $1 - \delta$ we have (for any $\delta > 0$ and for both $\pi = \pi^*$ and $\pi = \hat{\pi}$)

$$\mathbb{E}_{x \sim q^{\pi}(x)} |r(x) - r_{\theta}(x)| \le \frac{\varepsilon_0}{2} + M \sqrt{\frac{2\log(2|\Pi|/\delta)}{n}}$$
(72)

1596

1597

1598

Table A4. Quality of Design Candidates Using Mixed χ^2 -Divergence DynAMO. Using Corollary D.3 and (60), we show that it is possible to extend DynAMO to leverage a *mixed* χ^2 -*divergence* that equally weights both χ^2 -divergence and KL-divergence to penalize the original MBO objective. We evaluate this specialized implementation of DynAMO against baseline DynAMO and vanilla optimization methods, and report the Best@128 (resp.., Median@128) oracle score achieved by the 128 evaluated designs in the top (resp., bottom) table. Metrics are reported mean^{(95%} confidence interval) across 10 random seeds, where higher is better. Bolded entries indicate average scores with an overlapping 95% confidence interval to the best performing method. Bolded (resp., <u>Underlined</u>) Rank and Optimality Gap (Opt. Gap) metrics indicate the best (resp., second best) for a given backbone optimizer.

5	Best@128	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	Rank ↓	Opt. Gap
7	Dataset \mathcal{D}	43.9	59.4	60.5	88.9	40.0	88.4		_
	Grad.	90.0 ^(4.3)	80.9 ^(12.1)	60.2 ^(8.9)	88.8(4.0)	36.0 ^(6.8)	65.6(14.5)	2.8	6.8
	DynAMO-Grad.	90.3 ^(4.7)	86.2 ^(0.0)	64.4 ^(2.5)	$91.2^{(0.0)}$	44.2 ^(7.8)	89.8 ^(3.2)	1.2	14.2
	Mixed χ^2 DynAMO-Grad.	59.3 ^(8.3)	86.2 ^(0.0)	64.4 ^(2.6)	120 ^(1.4)	42.0 ^(5.6)	83.6 ^(1.4)	2.0	12.5
	Adam	62.9(13.0)	69.7 ^(10.5)	62.9 ^(1.9)	92.3 ^(8.9)	37.8 ^(6.3)	58.4 ^(18.5)	2.7	0.5
	DynAMO-Adam	95.2 ^(1.7)	86.2 ^(0.0)	65.2 ^(1.1)	91.2 ^(0.0)	45.5 ^(5.7)	84.9 ^(12.0)	1.3	14.5
	Mixed χ^2 DynAMO-Adam	59.3 ^(8.3)	86.2(0.0)	64.4 ^(2.6)	120 ^(1.4)	42.0 ^(5.6)	83.6 ^(1.4)	<u>2.0</u>	12.5
	BO-qEI	87.3 ^(5.8)	86.2 ^(0.0)	65.4 ^(1.0)	116 ^(3.1)	53.1 ^(3.3)	84.4 ^(0.9)	2.8	18.7
	DynAMO-BO-qEI	91.9 ^(4.4)	86.2 ^(0.0)	67.0 ^(1.3)	$121^{(0.0)}$	53.5 ^(5.0)	85.5 ^(1.1)	1.5	20.7
	Mixed χ^2 DynAMO-BO-qEI	92.2 ^(4.1)	86.3 ^(0.1)	66.8 ^(1.2)	123 ^(3.0)	51.7 ^(4.4)	85.1 ^(1.5)	1.7	20.7
	BO-qUCB	88.1 ^(5.3)	86.2 ^(0.1)	66.4 ^(0.7)	121 ^(1.3)	51.3 ^(3.6)	84.5 ^(0.8)	2.2	19.4
	DynAMO-BO-qUCB	95.1 ^(1.9)	86.2 ^(0.0)	66.7 ^(1.5)	$121^{(0.0)}$	48.1 ^(4.0)	86.9 ^(4.5)	1.7	20.5
	Mixed χ^2 DynAMO-BO-qUCB	85.7 ^(5.4)	86.3 ^(0.2)	66.3 ^(0.9)	$121^{(0.0)}$	51.5 ^(4.3)	83.8 ^(1.1)	2.0	19.0
	CMA-ES	87.6 ^(8.3)	86.2 ^(0.0)	66.1 ^(1.0)	106 ^(5.9)	49.0 ^(1.0)	72.2 ^(0.1)	2.0	14.4
	DynAMO-CMA-ES	89.8 ^(3.6)	85.7 ^(5.8)	63.9 ^(0.9)	117 ^(6.7)	50.6 ^(4.8)	78.5 ^(5.5)	1.7	17.5
	Mixed χ^2 DynAMO-CMA-ES	84.2 ^(10.7)	84.5 ^(2.6)	65.1 ^(1.3)	113 ^(4.8)	45.0 ^(4.9)	81.8 ^(4.0)	2.3	15.4
	CoSyNE	61.7(10.0)	57.3 ^(9.6)	63.6 ^(0.4)	94.8 ^(10.1)	37.0 ^(4.1)	62.7 ^(1.3)	2.8	-0.6
	DynAMO-CoSyNE	91.3 ^(4.4)	77.2 ^(11.6)	63.9 ^(0.9)	114 ^(7.0)	40.6 ^(8.6)	$67.5^{(1.4)}$	1.5	12.3
	Mixed χ^2 DynAMO-CoSyNE	94.3 ^(2.3)	78.3 ^(8.3)	63.1 ^(2.2)	100 ^(10.9)	37.4 ^(9.7)	82.3 ^(4.1)	1.7	12.4
	Median@128	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty		Opt. Gap
	Dataset D	33.7	42.8	50.9	87.6	6.7	77.8		Opt. Gap
								_	
	Grad.	58.1 ^(6.1)	58.6 ^(13.1)	59.3 ^(8.6)	85.3 ^(7.7)	36.0 ^(6.7)	65.1 ^(14.4)	<u>2.0</u>	10.5
	DynAMO-Grad.	$47.0^{(2.8)}$	69.8 ^(6.0)	61.9 ^(2.2)	85.9 ^(0.4)	$23.4^{(8.5)}$	68.7 ^(12.1)	1.5	<u>9.5</u>
	Mixed χ^2 DynAMO-Grad.	45.2 ^(6.9)	66.9 ^(5.2)	58.3 ^(6.5)	86.6 ^(2.1)	20.6 ^(1.4)	64.4 ^(8.3)	2.5	7.1
	Adam			-0.0(86)					0.5
		54.7 ^(8.8)	60.4 ^(12.7)	59.2 ^(8.6)	87.9 ^(10.0)	37.4 ^(6.2)	56.8 ^(19.8)	<u>1.8</u>	9.5
	DynAMO-Adam	47.7 ^(3.0)	69.0 ^(5.2)	62.4 ^(1.9)	86.4 ^(0.6)	23.0(6.0)	65.6 ^(14.1)	1.7	<u>9.1</u>
		$47.7^{(3.0)} 45.2^{(6.9)}$	69.0 ^(5.2) 66.9 ^(5.2)	$\begin{array}{c} 62.4^{(1.9)} \\ 58.3^{(6.5)} \end{array}$	86.4 ^(0.6) 86.6 ^(2.1)	$23.0^{(6.0)} \\ 20.6^{(1.4)}$	$65.6^{(14.1)} \\ 64.4^{(8.3)}$		
	DynAMO-Adam	47.7 ^(3.0) 45.2 ^(6.9) 48.5 ^(1.5)	69.0 ^(5.2) 66.9 ^(5.2) 59.9 ^(2.0)	62.4 ^(1.9) 58.3 ^(6.5)	86.4 ^(0.6) 86.6 ^(2.1) 86.7 ^(0.6)	23.0 ^(6.0) 20.6 ^(1.4) 28.7 ^(1.8)	65.6 ^(14.1) 64.4 ^(8.3) 72 4 ^(1.8)	1.7	<u>9.1</u>
	DynAMO-Adam Mixed χ^2 DynAMO-Adam BO-qEI DynAMO-BO-qEI	47.7 ^(3.0) 45.2 ^(6.9) 48.5 ^(1.5) 51.5 ^(0.9)	69.0 ^(5.2) 66.9 ^(5.2) 59.9 ^(2.0) 65.6 ^(3.1)	62.4 ^(1.9) 58.3 ^(6.5) 63.3 ^(0.0) 63.3 ^(0.0)	86.4 ^(0.6) 86.6 ^(2.1) 86.7 ^(0.6) 86.7 ^(0.6)	23.0 ^(6.0) 20.6 ^(1.4) 28.7 ^(1.8) 23.5 ^(2.4)	65.6 ^(14.1) 64.4 ^(8.3) 72.4 ^(1.8) 77.0 ^(0.7)	1.7 2.5	<u>9.1</u> 7.1
	$\begin{array}{c} {\rm DynAMO-Adam} \\ \\ {\rm Mixed} \ \chi^2 \ {\rm DynAMO-Adam} \\ \\ \\ {\rm BO-qEI} \end{array}$	47.7 ^(3.0) 45.2 ^(6.9) 48.5 ^(1.5)	69.0 ^(5.2) 66.9 ^(5.2) 59.9 ^(2.0) 65.6 ^(3.1) 66.1 ^(3.0)	$\begin{array}{c} 62.4^{(1.9)} \\ 58.3^{(6.5)} \end{array}$	86.4 ^(0.6) 86.6 ^(2.1)	23.0 ^(6.0) 20.6 ^(1.4) 28.7 ^(1.8)	65.6 ^(14.1) 64.4 ^(8.3) 72 4 ^(1.8)	1.7 2.5 <u>1.8</u>	9.1 7.1 10.0
	DynAMO-Adam Mixed χ^2 DynAMO-Adam BO-qEI DynAMO-BO-qEI	47.7 ^(3.0) 45.2 ^(6.9) 48.5 ^(1.5) 51.5 ^(0.9)	69.0 ^(5.2) 66.9 ^(5.2) 59.9 ^(2.0) 65.6 ^(3.1) 66.1 ^(3.0) 62.1 ^(3.4)	62.4 ^(1.9) 58.3 ^(6.5) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0)	$\begin{array}{r} 86.4^{(0.6)}\\ 86.6^{(2.1)}\\ \\ 86.7^{(0.6)}\\ 86.7^{(0.6)}\\ \\ 86.4^{(0.6)}\\ \\ \end{array}$	23.0 ^(6.0) 20.6 ^(1.4) 28.7 ^(1.8) 23.5 ^(2.4) 27.7 ^(3.5) 31.7 ^(1.2)	65.6 ^(14.1) 64.4 ^(8.3) 72.4 ^(1.8) 77.0 ^(0.7) 73.9 ^(2.8) 74.4 ^(0.6)	1.7 2.5 <u>1.8</u> 1.7	9.1 7.1 10.0 11.3
	$\begin{array}{c} {\rm DynAMO-Adam} \\ {\rm Mixed}\; \chi^2 \; {\rm DynAMO-Adam} \\ \\ {\rm BO-qEI} \\ {\rm DynAMO-BO-qEI} \\ \\ {\rm Mixed}\; \chi^2 \; {\rm DynAMO-BO-qEI} \\ \\ \\ {\rm BO-qUCB} \end{array}$	47.7 ^(3.0) 45.2 ^(6.9) 48.5 ^(1.5) 51.5 ^(0.9) 44.8 ^(1.4) 50.3 ^(1.8) 48.8 ^(1.8)	69.0 ^(5.2) 66.9 ^(5.2) 59.9 ^(2.0) 65.6 ^(3.1) 66.1 ^(3.0) 62.1 ^(3.4) 65.9 ^(3.7)	62.4 ^(1.9) 58.3 ^(6.5) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0)	$\begin{array}{r} 86.4^{(0.6)}\\ 86.6^{(2.1)}\\ \hline 86.7^{(0.6)}\\ 86.7^{(0.6)}\\ 86.4^{(0.6)}\\ \hline 86.6^{(0.6)}\\ 86.5^{(0.5)}\\ \end{array}$	23.0 ^(6.0) 20.6 ^(1.4) 28.7 ^(1.8) 23.5 ^(2.4) 27.7 ^(3.5) 31.7 ^(1.2)	65.6 ^(14.1) 64.4 ^(8.3) 72.4 ^(1.8) 77.0 ^(0.7) 73.9 ^(2.8) 74.4 ^(0.6) 50.4 ^(14.6)	1.7 2.5 <u>1.8</u> 1.7 2.3 1.5	9.1 7.1 10.0 11.3 10.4
	$\begin{array}{c} {\rm DynAMO-Adam} \\ {\rm Mixed}\; \chi^2 \; {\rm DynAMO-Adam} \\ {\rm BO-qEI} \\ {\rm DynAMO-BO-qEI} \\ {\rm Mixed}\; \chi^2 \; {\rm DynAMO-BO-qEI} \end{array}$	47.7 ^(3.0) 45.2 ^(6.9) 48.5 ^(1.5) 51.5 ^(0.9) 44.8 ^(1.4) 50.3 ^(1.8)	69.0 ^(5.2) 66.9 ^(5.2) 59.9 ^(2.0) 65.6 ^(3.1) 66.1 ^(3.0) 62.1 ^(3.4)	62.4 ^(1.9) 58.3 ^(6.5) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0)	$\frac{86.4^{(0.6)}}{86.6^{(2.1)}}$ $\frac{86.7^{(0.6)}}{86.7^{(0.6)}}$ $86.4^{(0.6)}$	23.0 ^(6.0) 20.6 ^(1.4) 28.7 ^(1.8) 23.5 ^(2.4) 27.7 ^(3.5)	65.6 ^(14.1) 64.4 ^(8.3) 72.4 ^(1.8) 77.0 ^(0.7) 73.9 ^(2.8)	1.7 2.5 1.8 1.7 2.3	9.1 7.1 10.0 11.3 10.4 11.5
	$\begin{array}{c} {\rm DynAMO-Adam} \\ {\rm Mixed}\; \chi^2 \; {\rm DynAMO-Adam} \\ \\ {\rm BO-qEI} \\ {\rm DynAMO-BO-qEI} \\ \\ {\rm Mixed}\; \chi^2 \; {\rm DynAMO-BO-qEI} \\ \\ \\ {\rm BO-qUCB} \\ \\ {\rm DynAMO-BO-qUCB} \end{array}$	47.7 ^(3.0) 45.2 ^(6.9) 48.5 ^(1.5) 51.5 ^(0.9) 44.8 ^(1.4) 50.3 ^(1.8) 48.8 ^(1.8) 44.0 ^(0.7)	69.0 ^(5.2) 66.9 ^(5.2) 59.9 ^(2.0) 65.6 ^(3.1) 66.1 ^(3.0) 62.1 ^(3.4) 65.9 ^(3.7)	62.4 ^(1.9) 58.3 ^(6.5) 63.3 ^(0.0)	$\begin{array}{c} 86.4^{(0.6)}\\ 86.6^{(2.1)}\\ \hline \\ 86.7^{(0.6)}\\ 86.7^{(0.6)}\\ \hline \\ 86.4^{(0.6)}\\ \hline \\ 86.6^{(0.6)}\\ \hline \\ 86.5^{(0.5)}\\ \hline \\ 86.5^{(0.6)}\\ \hline \end{array}$	$\begin{array}{r} 23.0^{(6.0)}\\ 20.6^{(1.4)}\\ \hline 28.7^{(1.8)}\\ 23.5^{(2.4)}\\ \hline 27.7^{(3.5)}\\ \hline 31.7^{(1.2)}\\ 22.7^{(2.0)}\\ 20.9^{(1.3)}\\ \end{array}$	65.6 ^(14.1) 64.4 ^(8.3) 72.4 ^(1.8) 77.0 ^(0.7) 73.9 ^(2.8) 74.4 ^(0.6) 50.4 ^(14.6) 74.5 ^(2.0) 59.3 ^(10.9)	1.7 2.5 1.8 1.7 2.3 1.5 2.0	9.1 7.1 10.0 11.3 10.4 11.5 6.3 9.6
	$\begin{array}{c} {\rm DynAMO-Adam} \\ {\rm Mixed} \ \chi^2 \ {\rm DynAMO-Adam} \\ {\rm BO-qEI} \\ {\rm DynAMO-BO-qEI} \\ {\rm Mixed} \ \chi^2 \ {\rm DynAMO-BO-qEI} \\ {\rm BO-qUCB} \\ {\rm DynAMO-BO-qUCB} \\ {\rm Mixed} \ \chi^2 \ {\rm DynAMO-BO-qUCB} \\ {\rm Mixe$	47.7 ^(3.0) 45.2 ^(6.9) 48.5 ^(1.5) 51.5 ^(0.9) 44.8 ^(1.4) 50.3 ^(1.8) 48.8 ^(1.8)	69.0 ^(5.2) 66.9 ^(5.2) 59.9 ^(2.0) 65.6 ^(3.1) 66.1 ^(3.0) 62.1 ^(3.4) 65.9 ^(3.7) 68.2 ^(3.0)	62.4 ^(1.9) 58.3 ^(6.5) 63.3 ^(0.0)	$\begin{array}{r} 86.4^{(0.6)}\\ 86.6^{(2.1)}\\ \hline 86.7^{(0.6)}\\ 86.7^{(0.6)}\\ 86.4^{(0.6)}\\ \hline 86.6^{(0.6)}\\ 86.5^{(0.5)}\\ \end{array}$	23.0 ^(6.0) 20.6 ^(1.4) 23.5 ^(2.4) 27.7 ^(3.5) 31.7 ^(1.2) 22.7 ^(2.0) 20.9 ^(1.3) 37.9 ^(0.7)	65.6 ^(14.1) 64.4 ^(8.3) 72.4 ^(1.8) 77.0 ^(0.7) 73.9 ^(2.8) 74.4 ^(0.6) 50.4 ^(14.6) 74.5 ^(2.0) 59.3 ^(10.9) 60.6 ^(15.0)	1.7 2.5 1.8 1.7 2.3 1.5 2.0 1.5	9.1 7.1 10.0 11.3 10.4 11.5 6.3 9.6 11.2
	$\begin{array}{c} {\rm DynAMO-Adam} \\ {\rm Mixed} \ \chi^2 \ {\rm DynAMO-Adam} \\ {\rm BO-qEI} \\ {\rm DynAMO-BO-qEI} \\ {\rm Mixed} \ \chi^2 \ {\rm DynAMO-BO-qEI} \\ {\rm BO-qUCB} \\ {\rm DynAMO-BO-qUCB} \\ {\rm Mixed} \ \chi^2 \ {\rm DynAMO-BO-qUCB} \\ {\rm Mixed} \ \chi^2 \ {\rm DynAMO-BO-qUCB} \\ {\rm Mixed} \ \chi^2 \ {\rm DynAMO-BO-qUCB} \end{array}$	47.7 ^(3.0) 45.2 ^(6.9) 48.5 ^(1.5) 51.5 ^(0.9) 44.8 ^(1.4) 50.3 ^(1.8) 48.8 ^(1.8) 44.0 ^(0.7) 50.7 ^(2.7)	69.0 ^(5.2) 66.9 ^(5.2) 59.9 ^(2.0) 65.6 ^(3.1) 66.1 ^(3.0) 62.1 ^(3.4) 65.9 ^(3.7) 68.2 ^(3.0) 71.7 ^(10.4)	$\begin{array}{c} 62.4^{(1.9)} \\ \overline{58.3}^{(6.5)} \\ \hline 63.3^{(0.0)} \\ 63.3^{(0.0)} \\ \overline{63.3}^{(0.0)} \\ \hline 63.3^{(0.0)} \\ 63.3^{(0.0)} \\ \overline{63.3}^{(0.0)} \\ \hline \end{array}$	86.4 ^(0.6) 86.6 ^(2.1) 86.7 ^(0.6) 86.7 ^(0.6) 86.4 ^(0.6) 86.5 ^(0.6) 86.5 ^(0.6) 86.5 ^(0.6) 83.9 ^(1.0)	$\begin{array}{r} 23.0^{(6.0)}\\ 20.6^{(1.4)}\\ \hline 28.7^{(1.8)}\\ 23.5^{(2.4)}\\ \hline 27.7^{(3.5)}\\ \hline 31.7^{(1.2)}\\ 22.7^{(2.0)}\\ 20.9^{(1.3)}\\ \end{array}$	65.6 ^(14.1) 64.4 ^(8.3) 72.4 ^(1.8) 77.0 ^(0.7) 73.9 ^(2.8) 74.4 ^(0.6) 50.4 ^(14.6) 74.5 ^(2.0)	1.7 2.5 1.8 1.7 2.3 1.5 2.0	9.1 7.1 10.0 11.3 10.4 11.5 6.3 9.6
	$\begin{array}{c} {\rm DynAMO-Adam} \\ {\rm Mixed}\; \chi^2\; {\rm DynAMO-Adam} \\ {\rm BO-qEI} \\ {\rm DynAMO-BO-qEI} \\ {\rm Mixed}\; \chi^2\; {\rm DynAMO-BO-qEI} \\ {\rm BO-qUCB} \\ {\rm DynAMO-BO-qUCB} \\ {\rm Mixed}\; \chi^2\; {\rm DynAMO-BO-qUCB} \\ {\rm Mixed}\; \chi^2\; {\rm DynAMO-BO-qUCB} \\ {\rm CMA-ES} \\ {\rm DynAMO-CMA-ES} \\ {\rm Mixed}\; \chi^2\; {\rm DynAMO-CMA-ES} \\ {\rm Mixed}\; \chi^2\; {\rm DynAMO-CMA-ES} \\ \end{array}$	47.7 ^(3.0) 45.2 ^(6.9) 48.5 ^(1.5) 51.5 ^(0.9) 44.8 ^(1.4) 50.3 ^(1.8) 48.8 ^(1.8) 44.0 ^(0.7) 50.7 ^(2.7) 45.3 ^(2.4) 48.5 ^(3.0) 55.3 ^(8.0)	69.0 ^(5.2) 66.9 ^(5.2) 59.9 ^(2.0) 65.6 ^(3.1) 66.1 ^(3.0) 62.1 ^(3.4) 65.9 ^(3.7) 68.2 ^(3.0) 71.7 ^(10.4) 65.8 ^(8.9) 70.0 ^(6.5) 53.6 ^(10.2)	62.4 ^(1.9) 58.3 ^(6.5) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 59.3 ^(3.8) 63.2 ^(0.3)	86.4 ^(0.6) 86.6 ^(2.1) 86.7 ^(0.6) 86.4 ^(0.6) 86.4 ^(0.6) 86.5 ^(0.6) 86.5 ^(0.6) 83.9 ^(1.0) 99.0 ^(12.1) 87.0 ^(2.0)	23.0 ^(6.0) 20.6 ^(1.4) 28.7 ^(1.8) 23.5 ^(2.4) 27.7 ^(3.5) 31.7 ^(1.2) 22.7 ^(2.0) 20.9 ^(1.3) 37.9 ^(0.7) 22.5 ^(5.1) 19.4 ^(3.8)	65.6 ^(14.1) 64.4 ^(8.3) 72.4 ^(1.8) 77.0 ^(0.7) 73.9 ^(2.8) 74.4 ^(0.6) 50.4 ^(14.6) 74.5 ^(2.0) 59.3 ^(10.9) 60.6 ^(15.0) 43.7 ^(14.6)	1.7 2.5 1.8 1.7 2.3 1.5 2.0 2.0 2.0 2.2 2.3	$\begin{array}{r} \underline{9.1} \\ 7.1 \\ 10.0 \\ 11.3 \\ \underline{10.4} \\ 11.5 \\ 6.3 \\ 9.6 \\ 11.2 \\ \underline{8.8} \\ 5.4 \\ \end{array}$
	$\begin{array}{c} {\rm DynAMO-Adam} \\ {\rm Mixed} \ \chi^2 \ {\rm DynAMO-Adam} \\ {\rm BO-qEI} \\ {\rm DynAMO-BO-qEI} \\ {\rm Mixed} \ \chi^2 \ {\rm DynAMO-BO-qEI} \\ {\rm BO-qUCB} \\ {\rm DynAMO-BO-qUCB} \\ {\rm Mixed} \ \chi^2 \ {\rm DynAMO-BO-qUCB} \\ {\rm Solution} \\ {\rm Solution} \\ {\rm Solution} \\ {\rm Mixed} \ \chi^2 \ {\rm DynAMO-BO-qUCB} \\ {\rm Solution} \\ {\rm Solution} \\ {\rm Mixed} \ \chi^2 \ {\rm DynAMO-BO-qUCB} \\ {\rm Solution} \\ {\rm S$	$\begin{array}{r} {\color{red} 47.7^{(3.0)} \\ {\color{red} 45.2^{(6.9)} } \\ \\ {\color{red} 48.5^{(1.5)} \\ {\color{red} 51.5^{(0.9)} \\ {\color{red} 44.8^{(1.4)} } \\ \\ {\color{red} 50.3^{(1.8)} \\ {\color{red} 48.8^{(1.8)} \\ {\color{red} 44.0^{(0.7)} } \\ \\ \\ {\color{red} 50.7^{(2.7)} \\ {\color{red} 45.3^{(2.4)} } } \end{array}}$	69.0 ^(5.2) 66.9 ^(5.2) 59.9 ^(2.0) 65.6 ^(3.1) 66.1 ^(3.0) 62.1 ^(3.4) 65.9 ^(3.7) 68.2 ^(3.0) 71.7 ^(10.4) 65.8 ^(8.9)	62.4 ^(1,9) 58.3 ^(6,5) 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0) 63.3 ^(0,0) 59.3 ^(3,8)	86.4 ^(0.6) 86.6 ^(2.1) 86.7 ^(0.6) 86.7 ^(0.6) 86.4 ^(0.6) 86.6 ^(0.6) 86.5 ^(0.5) 86.5 ^(0.6) 83.9 ^(1.0) 99.0 ^(12.1)	23.0 ^(6.0) 20.6 ^(1.4) 23.5 ^(2.4) 27.7 ^(3.5) 31.7 ^(1.2) 22.7 ^(2.0) 20.9 ^(1.3) 37.9 ^(0.7) 22.5 ^(5.1)	65.6 ^(14.1) 64.4 ^(8.3) 72.4 ^(1.8) 77.0 ^(0.7) 73.9 ^(2.8) 74.4 ^(0.6) 50.4 ^(14.6) 74.5 ^(2.0) 59.3 ^(10.9) 60.6 ^(15.0)	1.7 2.5 1.8 1.7 2.3 1.5 2.0 2.0 1.5 2.2	9.1 7.1 10.0 11.3 10.4 11.5 6.3 9.6 11.2 8.8

1647

1648

1650 1651 Table A5. Diversity of Design Candidates Using Mixed χ^2 -Divergence DynAMO. Using Corollary D.3 and (60), we show that it is 1651 possible to extend DynAMO to leverage a *mixed* χ^2 -*divergence* that equally weights both χ^2 -divergence and KL-divergence to penalize 1652 the original MBO objective. We evaluate this specialized implementation of DynAMO against baseline DynAMO and vanilla optimization 1654 methods, and report the pairwise diversity (resp., minimum novelty and L_1 coverage) oracle score achieved by the 128 evaluated designs 1655 in the top (resp., middle and bottom) table. Metrics are reported mean^(95% confidence interval) across 10 random seeds, where higher is better. 1656 Bolded entries indicate average scores with an overlapping 95% confidence interval to the best performing method. Bolded (resp., 1656 Underlined) Rank and Optimality Gap (Opt. Gap) metrics indicate the best (resp., second best) for a given backbone optimizer.

Pairwise Diversity@128	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	Rank ↓	Opt. Gap ↑	-
Dataset D	65.9	57.3	60.0	36.7	66.0	85.7		օրե օգր	-
	12.5 ^(8.0)	7.8 ^(8.8)	7.9 ^(7.8)	24.1(13.3)	0.0 ^(0.0)	0.0 ^(0.0)	3.0	-53.2	
Grad. DynAMO-Grad.	66.9 ^(6.9)	68.2 ^(10.8)	77.2 ^(21.5)	93.0 ^(1.2)	129(55.3)	104(56.1)	5.0 1.3	-33.2 27.8	
Mixed χ^2 DynAMO-Grad.	16.8(12.6)	72.6 ^(1.1)	47.0 ^(31.1)	91.0 ^(1.6)	182 ^(45.9)	74.2(3.0)	<u>1.7</u>	18.7	
Adam	12.0(12.3)	11.0(12.1)	4.8(3.8)	16.8(12.4)	6.4(14.5)	6.2(14.0)	3.0	-52.4	
DynAMO-Adam	54.8 ^(8.9)	$72.3^{(3.4)}$	84.8 ^(9.2)	89.9 ^(5.3)	158 ^(37.3)	126 ^(57.3)	<u>1.7</u>	35.7	
Mixed χ^2 DynAMO-Adam	16.8(12.6)	72.6 ^(1.1)	99.2 ^(0.7)	91.0 ^(1.6)	182 ^(45.9)	74.2(3.0)	1.3	27.4	
BO-qEI DynAMO-BO-qEI	73.7 ^(0.6) 74.8 ^(0.2)	73.8 ^(0.5) 74.6 ^(0.3)	99.3 ^(0.1) 99.4 ^(0.1)	93.0 ^(0.5) 93.5 ^(0.4)	190 ^(0.8) 198 ^(1.9)	124 ^(7.4) 277 ^(59.7)	2.5 1.3	47.1 74.2	
Mixed χ^2 DynAMO-BO-qEI	7 4.6 73.6 ^(0.7)	74.0 ^(0.5)	99.4 ^(0.0)	93.9 ^(0.4)	167 ^(41.5)	29.1 ^(7.7)	<u>1.3</u> <u>2.2</u>	27.5	
BO-qUCB	73.9 ^(0.5)	74.3(0.4)	99.4 ^(0.1)	93.6 ^(0.5)	198 ^(10.3)	94.1 ^(3.9)	2.2	43.5	
DynAMO-BO-qUCB	74.3 ^(0.5)	74.4 ^(0.6)	99.3 ^(0.1)	93.5 ^(0.6)	211 ^(22.8)	175(44.7)	1.7	59.4	
Mixed χ^2 DynAMO-BO-qUCB	73.4 ^(0.7)	74.3 ^(0.4)	99.5 ^(0.1)	93.7 ^(0.5)	177 ^(25.2)	28.1(7.3)	<u>2.2</u>	29.0	
CMA-ES	47.2(11.2)	44.6 ^(15.9)	93.5 ^(2.0)	66.2 ^(9.4)	12.8 ^(0.6)	164 ^(10.6)	2.5	9.5	
DynAMO-CMA-ES Mixed χ^2 DynAMO-CMA-ES	73.6 ^(0.6) 52.9 ^(20.8)	73.1 ^(3.1) 51.5 ^(22.1)	72.0 ^(3.1) 67.7 ^(24.7)	94.0 ^(0.5) 69.7 ^(12.4)	97.8 ^(13.2) 154 ⁽¹⁰⁷⁾	292 ^(83.5) 86.9 ^(72.9)	1.3	55.2	
	5.6 ^(5.0)		28.2(11.3)	12.2 ^(7.3)			2.2	18.6	
CoSyNE DynAMO-CoSyNE	18.1 ^(13.0)	12.7 ^(9.8) 20.3 ^(2.3)	35.0 ^(17.9)	22.8 ^(11.9)	0.0 ^(0.0) 74.4 ^(46.3)	0.0 ^(0.0) 77.0 ^(35.9)	3.0 <u>1.7</u>	-52.1 -20.7	
Mixed χ^2 DynAMO-CoSyNE	22.4 ^(8.1)	34.1 ^(20.1)	34.1 ^(20.1)	23.0 ^(17.4)	104 ^(77.9)	49.4 ^(25.6)	$\frac{1.7}{1.3}$	-17.5	
Minimum Novelty@128	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	Rank↓	Opt. Gap ↑	
Dataset D	0.0	0.0	0.0	0.0	0.0	0.0		_	
Grad.	21.2(3.0)	51.7 ^(2.9)	97.4 ^(3.9)	79.5 ^(19.7)	95.0 ^(0.7)	102(6.1)	2.3	74.5	
DynAMO-Grad.	21.1 ^(1.1)	52.2 ^(1.3)	98.6 ^(1.5)	85.8 ^(1.0)	95.0 ^(0.4)	107 ^(6.7)	1.3	76.7	
Mixed χ^2 DynAMO-Grad.	14.6 ^(2.8)	51.9 ^(0.4)	99.2 ^(0.7)	85.2 ^(2.1)	85.2 ^(1.6)	34.0(1.1)	<u>2.3</u>	61.7	
Adam	$23.7^{(2.8)}$	51.1 ^(3.5)	95.5 ^(5.3)	79.3 ^(21.2)	94.8 ^(0.7)	103 ^(6,3)	2.0	74.5	
DynAMO-Adam Mixed χ^2 DynAMO-Adam	14.7 ^(1.9) 20.4 ^(3.3)	46.2 ^(0.5) 51.9^(0.4)	98.7 ^(1.2) 87.3 ^(57.9)	85.9 ^(1.8) 85.2 ^(2.1)	94.9^(0.4) 85.2 ^(1.6)	108 ^(7.2) 34.0 ^(1.1)	1.7 2.3	74.7 60.7	
BO-qEI	20.4	51.5 ^(0.3)	97.6 ^(0.3)	85.4 ^(1.5)	94.6 ^(0.1)	106 ^(2.9)	1.8	76.2	
DynAMO-BO-qEI	$21.0^{(0.5)}$	51.5 51.9 ^(0.2)	97.4 ^(0.4)	85.2 ^(0.9)	94.8 ^(0.1)	126 ^(14.6)	<u>1.0</u>	<u>70.2</u> 79.4	
Mixed χ^2 DynAMO-BO-qEI	14.6(0.5)	51.9 ^(0.4)	97.4 ^(0.5)	85.5 ^(1.3)	80.8 ^(3.7)	16.6(4.5)	2.2	57.8	
BO-qUCB	21.6 ^(0.3)	51.7(0.2)	97.9 ^(0.4)	85.3(1.1)	93.8 ^(0.6)	98.8 ^(1.1)	1.8	74.8	
DynAMO-BO-qUCB	21.4 ^(0.5)	51.7 ^(0.2)	97.1 ^(0.5) 97.4 ^(0.4)	85.3 ^(1.1)	94.7 ^(0.2)	109^(4.5) 14.9 ^(3.3)	2.0	76.6	
Mixed χ^2 DynAMO-BO-qUCB	19.8 ^(0.3)	52.0 ^(0.1)		85.6(1.3)	79.8 ^(3.5)		2.2	58.2	
CMA-ES DynAMO-CMA-ES	$16.5^{(2.1)}$ $12.9^{(0.8)}$	$47.8^{(1.0)}$ $48.0^{(1.6)}$	96.5 ^(0.7) 96.7 ^(3.5)	73.0 ^(18.0) 81.8 ^(13.4)	100^(0.0) 94.5 ^(0.7)	100 ^(0.0) 112 ^(7.8)	2.3 2.0	<u>72.3</u> 74.3	
Mixed χ^2 DynAMO-CMA-ES	23.0 ^(1.6)	51.8 ^(0.4)	98.0 ^(0.9)	83.8 ^(9.9)	87.1 ^(2.1)	48.6 ^(16.8)	$\frac{2.0}{1.7}$	65.4	
CoSyNE	24.5(3.5)	49.7 ^(3.1)	98.5 ^(1.6)	86 6(12.7)	93.2 ^(1.0)	91.9(2.0)	1.7	74.1	
DynAMO-CoSyNE	17.8 ^(5.5)	48.4 ^(2.3)	96.7 ^(3.5)	80.2 ^(12.9)	94.5 ^(0.7)	112 ^(7.8)	2.3	75.0	
Mixed χ^2 DynAMO-CoSyNE	23.5 ^(3.7)	52.5 ^(2.0)	99.9 ^(0.1)	80.6 ^(21.5)	83.9(2.6)	30.3(4.2)	<u>2.0</u>	61.8	
L ₁ Coverage@128	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	$\mathbf{Rank} \downarrow$	Opt. Gap ↑	
Dataset D	0.42	0.31	1.42	0.68	6.26	0.58	_		
Grad.	$0.16^{(0.10)}$	0.20 ^(0.13)	0.21 ^(0.10)	$0.42^{(0.18)}$	$0.00^{(0.00)}$	$0.00^{(0.00)}$	3.0	-1.44	
DynAMO-Grad. Mixed χ^2 DynAMO-Grad.	0.36^(0.04) 0.16 ^(0.09)	$\begin{array}{c} 0.52^{(0.06)} \\ 0.54^{(0.02)} \end{array}$	1.46 ^(0.38) 0.87 ^(0.58)	2.49^(0.06) 2.20 ^(0.10)	6.47 ^(1.24) 6.67 ^(1.68)	5.85 ^(1.35) 1.61 ^(0.03)	1.3 1.7	1.25 0.40	
		0.54(0.09)	0.23 ^(0.15)	0.48 ^(0.31)	0.27 ^(0.55)	0.24 ^(0.49)	_	0.40	
Adam DynAMO-Adam	0.11 ^(0.06) 0.33 ^(0.05)	0 55(0.03)	1 44(0.39)	2 40(0.16)	7.06 ^(0.73)	6 91 ^(0.71)	3.0 1.0	-1.35 1.50	
Mixed χ^2 DynAMO-Adam	0.16 ^(0.09)	0.55 ^(0.02)	0.47 ^(0.31)	2.40 ^(0.10)	6.67 ^(1.68)	1.61 ^(0.03)	<u>2.0</u>	<u>0.33</u>	
BO-qEI	0 41(0.02)	0.55 ^(0.01)	2.37 ^(0.03)	2 11 ^(0.15)	7.84 ^(0.01)	6.61 ^(0.33)	2.3	1.70	
DynAMO-BO-qEI	0 42(0.01)	$0.56^{(0.01)}$	$2.47^{(0.03)}$	$2.54^{(0.03)}$	7.87 ^(0.01)	7.92 ^(0.04)	1.2	2.02	
Mixed χ^2 DynAMO-BO-qEI	0.39(0.02)	0.55 ^(0.01)	2.39 ^(0.04)	2.56 ^(0.02)	6.11 ^(0.64)	1.36 ^(0.12)	2.5	0.62	
BO-qUCB	0.40 ^(0.02)	$0.54^{(0.01)}$	$2.40^{(0.05)}$	$2.52^{(0.07)}$	$7.78^{(0.04)}$	$6.64^{(0.09)}$	2.5	<u>1.77</u>	
DynAMO-BO-qUCB Mixed χ^2 DynAMO-BO-qUCB	$\begin{array}{c} 0.40^{(0.02)} \\ 0.39^{(0.02)} \end{array}$	$\begin{array}{c} 0.55^{(0.01)} \\ 0.56^{(0.01)} \end{array}$	2.47 ^(0.07) 2.41 ^(0.05)	2.54 ^(0.05) 2.53 ^(0.06)	7.88^(0.03) 5.96 ^(0.78)	7.80^(0.23) 1.38 ^(0.11)	1.2	2.00 0.59	
	0.39(0.05)	0.48 ^(0.04)	2.41	1.82 ^(0.12)	3.26 ^(1.42)	3.77 ^(1.36)	2.3		
CMA-ES	0 40 ^(0.03)	$0.56^{(0.01)}$	$1.82^{(0.72)}$	$2.54^{(0.05)}$	3.26 ^(1.42) 4.75 ^(2.16)	3.29(1.56)	2.3 1.7	0.36 0.62	
DvnAMO-CMA-FS				1.07(0.19)	5.58 ^(1.68)	4.03 ^(3.01)		0.71	
DynAMO-CMA-ES Mixed χ^2 DynAMO-CMA-ES	0.30 ^(0.09)	0.52(0.05)	1.56 ^(0.68)	1.97(0.17)	5.50	4.05	2.0	0.71	
	0.30 ^(0.09)	0 22(0.10)	0 39(0.20)	1.97 ^(0.19) 0.27 ^(0.13)	0.10 ^(0.00)	0.10 ^(0.00)			
Mixed χ ² DynAMO-CMA-ES CoSyNE DynAMO-CoSyNE	0.30 ^(0.09) 0.10 ^(0.07) 0.21 ^(0.11)	0.22 ^(0.10) 0.18 ^(0.09)	0.39 ^(0.20) 0.64 ^(0.42)	0.27 ^(0.13) 0.43 ^(0.34)	0.10 ^(0.00) 1.85 ^(0.22)	0.10 ^(0.00) 0.94 ^(0.17)	2.8 <u>2.0</u>	-1.41 -0.90	
Mixed χ ² DynAMO-CMA-ES CoSyNE	0.30 ^(0.09)	0 22(0.10)	0 39(0.20)	0.27(0.13)	0.10 ^(0.00)	0.10 ^(0.00)	2.8	-1.41	

1705 where $n := |\mathcal{D}|$ is the number of datums in the offline dataset \mathcal{D} . 1706 *Proof.* Under Assumption D.4, Jensen's inequality gives us $\mathbb{E}_{x \sim p^{\tau}(x)} |r(x) - r_{\theta}(x)| \le \sqrt{\mathbb{E}_{x \sim p^{\tau}(x)} [r(x) - r_{\theta}(x)]^2} \le \sqrt{\frac{\varepsilon_0^2}{4}} =: \frac{\varepsilon_0}{2}$ 1709 (73)1710 1711 Furthermore, Assumption D.6 and Cortes et al. (2010) yield 1712 1713 $\left|\mathbb{E}_{x \sim p^{\tau}(x)} \left| r(x) - r_{\theta}(x) \right| - \mathbb{E}_{x \sim q^{\pi}(x)} \left| r(x) - r_{\theta}(x) \right|\right|$ 1714 $= \left| \mathbb{E}_{x \sim p^{\tau}(x)} \left| r(x) - r_{\theta}(x) \right| - \mathbb{E}_{x \sim p^{\tau}_{\mathcal{D}}(x)} \left[\frac{q^{\pi}(x)}{p^{\tau}_{\mathcal{D}}(x)} \left| r(x) - r_{\theta}(x) \right| \right] \right|$ (74)1716 $\leq M \sqrt{\frac{2\log(2|\Pi|/\delta)}{2\log(2|\Pi|/\delta)}}$ 1718 1719 1720 with probability at least $1 - \delta$. In the offline setting (as in our work) and assuming that the forward surrogate model $r_{\theta}(x)$ has been well-trained according to (2) or a similar learning paradigm (e.g., see Trabucco et al. (2021); Yu et al. (2021)), we can reasonably assume that $\varepsilon_0^2 \leq \mathbb{E}_{x \sim q^{\pi}(x)} [r(x) - r_{\theta}(x)]^2$. We therefore have an upper bound on the prediction error of the forward surrogate model over the distribution $q^{\pi}(x)$ over generated designs: 1723 1724 $\mathbb{E}_{x \sim q^{\pi}(x)} |r(x) - r_{\theta}(x)| \leq \mathbb{E}_{x \sim p^{\tau}(x)} |r(x) - r_{\theta}(x)| + M \sqrt{\frac{2\log(2|\Pi|/\delta)}{n}} \leq \frac{\varepsilon_0}{2} + M \sqrt{\frac{2\log(2|\Pi|/\delta)}{n}}$ 1725 (75)1726 1727 with probability at least $1 - \delta$. 1728 1729 Under Assumption D.6, we can also place an upper bound on the true and realized KL-divergence penalties: 1730 **Lemma D.8** (Bounded KL-Divergence). Assume there exists an $M \in \mathbb{R}_+$ finite satisfying Assumption D.6. Then with 1731 probability at least $1 - \delta$ we have (for any $\delta > 0$ and for both $\pi = \pi^*$ and $\pi = \hat{\pi}$) 1732 1733 $|D_{\kappa I}(q^{\pi}(x))||p^{\tau}(x)) - D_{\kappa I}(q^{\pi}(x))||p_{\mathcal{D}}^{\tau}(x))| \le M_{\Lambda} \sqrt{\log(|\Pi|/\delta)}$ (76)1734 1735 *Proof.* According to the definition of M and the definition of the KL-divergence from Definition C.1, 1736 1737 $D_{\mathrm{KL}}(q^{\pi}(x)||p^{\tau}(x)) = \mathbb{E}_{x \sim p^{\tau}(x)} \left[\frac{q^{\pi}(x)}{n^{\tau}(x)} \log \left(\frac{q^{\pi}(x)}{n^{\tau}(x)} \right) \right] \le M \log M$ (77)1738 1739 From Hoeffding's inequality (Hoeffding, 1963), 1740 1741 $\mathbb{P}\left(|D_{\mathsf{KL}}(q^{\pi}(x)||p^{\tau}(x)) - D_{\mathsf{KL}}(q^{\pi}(x)||p_{\mathcal{D}}^{\tau}(x))| \ge \varepsilon\right) \le |\Pi| \cdot \exp\left(-\frac{2\varepsilon^2}{M\log M}\right)$ 1742 (78)1743 1744 for any $\varepsilon > 0$. We can choose to define $\varepsilon := \sqrt{(M \log M) \cdot \log(|\Pi|/\delta)/2}$ such that 1745 1746 $|D_{\mathrm{KL}}(q^{\pi}(x)||p^{\tau}(x)) - D_{\mathrm{KL}}(q^{\pi}(x)||p_{\mathcal{D}}^{\tau}(x))| \leq \frac{\sqrt{(M\log M) \cdot \log(|\Pi|/\delta)}}{\sqrt{2}} \leq \frac{M\sqrt{\log(|\Pi|/\delta)}}{\sqrt{2}} \leq M\sqrt{\log(|\Pi|/\delta)}$ (79) 1747 1748 1749 with probability at least $1 - \delta$. 1750 1751 We are now ready to prove our main result: 1752 **Theorem D.9** (Bounded Diversity-Penalized Objective $J^*(\pi)$). Assume that there exists an $M \in \mathbb{R}_+$ finite satisfying 1753 Assumption D.6. Then with probability at least $1 - \delta$, we have (for any $\delta > 0$) 1754 1755 $J^{\star}(\pi^{\star}) - J^{\star}(\hat{\pi}) \le \varepsilon_0 + 2M\left(\frac{2}{\sqrt{n}} + \frac{\beta}{\tau}\right) \sqrt{\log\left(\frac{8|\Pi|}{\delta}\right)}$ 1756 (80)1757

where $n := |\mathcal{D}|$ is the size of the offline dataset \mathcal{D} .

Proof. Firstly, we combine Lemmas D.7 and D.8 using the triangle inequality to bound the difference between the true reward $J^*(\hat{\pi})$ and the offline reward $J(\hat{\pi})$, where $\hat{\pi} \in \Pi$ maximizes $J(\pi)$ as defined in (5).

$$\begin{aligned}
I^{1763}_{1764} & J(\hat{\pi}) - J^{\star}(\hat{\pi}) \coloneqq \left(\mathbb{E}_{x \sim q^{\hat{\pi}}(x)}[r_{\theta}(x)] - \frac{\beta}{\tau} D_{\mathrm{KL}}(q^{\hat{\pi}}(x)||p_{\mathcal{D}}^{\tau}) \right) - \left(\mathbb{E}_{x \sim q^{\hat{\pi}}(x)}[r(x)] - \frac{\beta}{\tau} D_{\mathrm{KL}}(q^{\hat{\pi}}(x)||p^{\tau}(x)) \right) \\
\\
I^{1765}_{1766} & \leq \mathbb{E}_{x \sim q^{\hat{\pi}}(x)} |r(x) - r_{\theta}(x)| + \frac{\beta}{\tau} \left| D_{\mathrm{KL}}(q^{\hat{\pi}}(x)||p^{\tau}(x)) - D_{\mathrm{KL}}(q^{\hat{\pi}}(x)||p^{\tau}(x)) \right| \\\\
I^{1767}_{1768} & \leq \left(\frac{\varepsilon_{0}}{2} + M \sqrt{\frac{2 \log(8|\Pi|/\delta)}{n}} \right) + M \cdot \frac{\beta}{\tau} \sqrt{\log(4|\Pi|/\delta)} \\\\
I^{1770}_{1771} & \leq \frac{\varepsilon_{0}}{2} + M \left(\frac{2}{\sqrt{n}} + \frac{\beta}{\tau} \right) \sqrt{\log\left(\frac{8|\Pi|}{\delta}\right)}
\end{aligned}$$
(81)

> with probability $1 - (\delta/2)$. Because $\hat{\pi} := \operatorname{argmax}_{\pi \in \Pi} J(\pi)$, we must have $J(\pi^*) \leq J(\hat{\pi})$. Substituting this into the left hand side of (81) gives

$$J(\pi^{\star}) - J^{\star}(\hat{\pi}) \le \frac{\varepsilon_0}{2} + M\left(\frac{2}{\sqrt{n}} + \frac{\beta}{\tau}\right) \sqrt{\log\left(\frac{8|\Pi|}{\delta}\right)}$$
(82)

Separately, we have (with probability $1 - (\delta/2)$)

$$\begin{array}{ll}
\begin{array}{ll}
\begin{array}{ll}
1780\\
1781\\
1782\\
1782\\
1782\\
1783\\
1784\\
1785\\
1786\\
1787\\
1788\\
1789\\
1789
\end{array}
\qquad J^{\star}(\pi^{\star}) - J(\pi^{\star}) := \left(\mathbb{E}_{x \sim q^{\pi^{\star}}(x)}[r(x)] - \frac{\beta}{\tau} D_{\mathrm{KL}}(q^{\pi^{\star}}(x)||p^{\tau}(x)) \right) - \left(\mathbb{E}_{x \sim q^{\pi^{\star}}}[r_{\theta}(x)] - \frac{\beta}{\tau} D_{\mathrm{KL}}(q^{\pi^{\star}}(x)||p^{\tau}_{\mathcal{D}}(x)) \right) \\
\leq \mathbb{E}_{x \sim q^{\pi^{\star}}(x)} |r(x) - r_{\theta}(x)| + \frac{\beta}{\tau} \left| D_{\mathrm{KL}}(q^{\pi^{\star}}(x)||p^{\tau}(x)) - D_{\mathrm{KL}}(q^{\pi^{\star}}(x)||p^{\tau}_{\mathcal{D}}(x)) \right| \\
\leq \left(\frac{\varepsilon_{0}}{2} + M \sqrt{\frac{2\log(8|\Pi|/\delta)}{n}} \right) + M \cdot \frac{\beta}{\tau} \sqrt{\log(|4\Pi|/\delta)} \\
\leq \frac{\varepsilon_{0}}{2} + M \left(\frac{2}{\sqrt{n}} + \frac{\beta}{\tau} \right) \sqrt{\log\left(\frac{8|\Pi|}{\delta}\right)}
\end{array}$$

$$(83)$$

following the derivation in (81) except for π^* (as opposed to $\hat{\pi}$) that maximizes $J^*(\pi)$ (as opposed to $J(\pi)$). Summing (82) and (83) gives

$$J^{\star}(\pi^{\star}) - J^{\star}(\hat{\pi}) \le \varepsilon_0 + 2M\left(\frac{2}{\sqrt{n}} + \frac{\beta}{\tau}\right) \sqrt{\log\left(\frac{8|\Pi|}{\delta}\right)}$$
(84)

with probability $1 - \delta$.

Note that we only prove **Theorem D.9** in the unconstrained optimization setting; in principle, a tighter bound could exist in the adversarially constrained formulation introduced in (7), as a bound on the 1-Wasserstein distance between $q^{\hat{\pi}}(x)$ and $p_{\mathcal{D}}^{\tau}(x)$ will almost surely place a favorably *tighter* bound on the forward surrogate model prediction error than Lemma D.7.

D.5. Comparison with Offline Model-Free Optimization Methods

In our main experimental results reported in Section 5, we focus on comparing DynAMO against other model-based optimization (MBO) methods—that is, optimization methods that explicitly (1) learn a proxy forward surrogate model $r_{\theta}(x)$ for the oracle reward function from the offline dataset; and (2) optimize against $r_{\theta}(x)$ and rank final candidate designs according to a scoring metric involving r_{θ} . Alternatively, recent work have also proposed methods that instead do *not* learn a forward surrogate model $r_{\theta}(x)$; we refer to such methods as *model-free* algorithms.

Survey of Existing Model-Free and Additional Model-Based Methods. Mashkaria et al. (2023) introduce BONET (i.e., Black-box Optimization Networks), which learns an auto-regressive model on synthetically constructed optimization trajectories that simulate runs of implicit black-box optimization experiments. The auto-regressive model is trained to learn a rollout of monotonic transitions from low- to high- scoring design candidates using the offline dataset. Nguyen et al. (2023) propose ExPT (i.e., Experiment Pretrained Transformers) as a task-agnostic method of pre-training a transformer

1815 foundation model to learn an inverse modeling of designs from input reward scores and associated contexts. **DDOM** (i.e., 1816 Denoising Diffusion Optimization Models) learns a generative diffusion model conditioned on the oracle reward values in 1817 the offline dataset (Krishnamoorthy et al., 2023). Similarly, GTG (i.e., Guided Trajectory Generation) trains a diffusion 1818 model to learn from synthetically constructed optimization trajectories conditioned on final scores. MINs (i.e., Model 1819 Inversion Networks) from Kumar & Levine (2019) learn and optimize against an inverse mapping from reward scores to candidate designs.² Tri-Mentoring and ICT (i.e., Importance-aware Co-Teaching) co-learn an ensemble of multiple 1820 1821 surrogate models (Chen et al., 2023a; Yuan et al., 2023). Separately, PGS (i.e., Policy-Guided Search) from Chemingui et al. 1822 (2024) learns a policy to optimize against a surrogate model (although only limit their method to first-order optimization 1823 algorithms), and Match-Opt from Hoang et al. (2024) proposes a black-box gradient matching algorithm to learn better 1824 forward surrogate mdoels. Finally, RGD (i.e., Robust-Guided Diffusion) uses a forward surrogate model to guide the 1825 generative sampling process from a diffusion model (Chen et al., 2024). Other model-free optimization methods have been 1826 proposed specifically for the biological sequence design problems (Kim et al., 2023; Chen et al., 2023b; Jain et al., 2022); 1827 we exclude these from our analysis and instead focus on task-agnostic optimization algorithms. We also exclude Design 1828 Editing for offline Model-based Optimization (DEMO) from Yuan et al. (2024), Noise-intensified Telescoping density-Ratio Estimation (NTRE) from Yu et al. (2024), and Ranking Models (RaM) from Tan et al. (2024) from our analysis since there 1829 1830 are no presently available open-source implementations. 1831

Experimental Results. We compare representative implementations of DynAMO (i.e., DynAMO with Gradient Ascent 1832 (DynAMO-Grad.), Bayesian optimization with Upper Confidence Bound acquisition function (DynAMO-BO-qUCB), 1833 and Covariance Matrix Adaptation Evolution Strategy (DynAMO-CMA-ES)) against other model-based optimization 1834 methods using the respective backbone optimizer described by the original authors (i.e., RoMA from Yu et al. (2021) using 1835 Adam Ascent, COMs from Trabucco et al. (2021) using Gradient Ascent, ROMO from Chen et al. (2023c) using Gradient 1836 Ascent, GAMBO from Yao et al. (2024) using BO-qEI) against model-free optimization methods in Supplementary 1837 **Tables A6-A8.** We find that DynAMO-augmented optimizers can be competitive in proposing high-quality designs—in 1838 particular, DynAMO-BO-qUCB achieves both the second best Rank and Optimality Gap across all six tasks according 1839 to the Best@128 oracle score metric. However, the improvement in *diversity* of designs using DynAMO is significant: 1840 DynAMO-BO-qUCB achieves the best Rank and Optimality gap according to both the Pairwise Diversity and L_1 Coverage 1841 metrics, and DynAMO-Grad. achieves the best Rank and Optimality gap according to the Minimum Novelty metric. 1842 Furthermore, DynAMO-BO-qUCB attains the best mean Pairwise Diversity score compared to the model-free optimization 1843 methods evaluated in 5 out of the 6 tasks assessed. Altogether, our results suggest that DynAMO is a promising technique to 1844 propose a diverse set of high-quality designs compared with existing state-of-the-art offline optimization methods. 1845

18461847D.6. Empirical Computational Cost Analysis

1848 To evaluate the empirical cost associated with running DynAMO, we report both the runtime and maximum GPU utilization of 1849 optimization methods both with and without DynAMO augmentation in **Supplementary Table A9**. Briefly, all experimental 1850 results reported in Supplementary Table A9 were conducted on one internal cluster with 8 NVIDIA RTX A6000 GPUs, 1851 and one 24-core Intel Xeon CPU-however, only a single GPU was made available for each program instance reported in 1852 our experiments. Across all six optimization methods evaluated, DynAMO increases the runtime (resp., maximum GPU 1853 usage) of the optimization method (averaged over all six tasks) by a mean of 181.7% (resp. 1.9%). While our experiments 1854 reveal that DynAMO is indeed associated with additional computational costs, they also show that DynAMO is empirically 1855 tractable to run even using a single GPU. Furthermore, we note that as discussed by Yao et al. (2024) and others, the primary 1856 real-world application of offline optimization solvers is in generative design tasks where the true oracle reward function is 1857 prohibitively expensive or inaccessible. In these settings, we argue that it is often worth leveraging additional compute to 1858 use DynAMO (or other offline optimization methods) to generate the best results possible before final oracle evaluation. 1859

¹⁸⁶⁰ D.7. τ -Weighted Distribution Visualization

In **Definition 3.2**, we define the τ -weighted probability distribution to serve as the reference distribution for a generative policy to learn from in (7). This reference probability distribution is important and should ideally capture the diversity of *high-quality* designs contained in the offline dataset. To investigate if this is indeed the case, we plot the empirical τ -weighted distributions for each of the six offline optimization tasks in our experimental evaluation suite using $\tau = 1.0$,

¹⁸⁶⁶ ²One might argue that MINs (Kumar & Levine, 2019) are also a form of model-based optimization, as the method involves learning a surrogate function $f_{\theta}^{-1} : \mathbb{R} \to \mathcal{X}$. However, the method proposes a design *x* given an input score value, and therefore does not make available an output proxy score by which to rank candidate designs. We therefore include MINs as a *model-free* optimization algorithm.

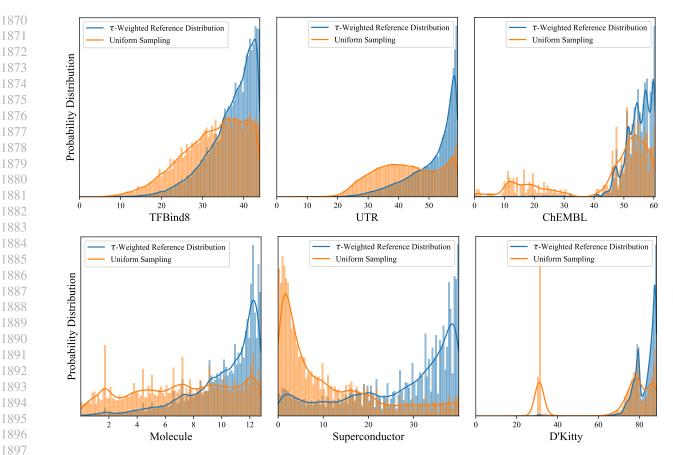


Figure A1. Sample τ -Weighted Probability Distributions. We plot ($\tau = 1.0$)-weighted distributions $p_{\mathcal{D}}^{\tau}(y)$ (blue) versus the original 1898 distribution of oracle scores y in the public offline dataset \mathcal{D} (orange) for the 6 offline optimization tasks in our experimental evaluation 1899 suite: (1) TFBind8 (top left); (2) UTR (top middle); (3) ChEMBL (top right); (4) Molecule (bottom left); (5) Superconductor (bottom 1900 middle); and (6) D'Kitty (bottom right). DynAMO penalizes a model-based optimization objective to encourage sampling policies to match the *diversity* of (high-scoring) designs in the τ -weighted distribution. The x-axis represents the normalized oracle scores. 1902

which is the value of the temperature hyperparameter used in our experiments in Table 1. The resulting plots are shown in 1905 Figure A1; in general, we can see that our τ -weighted reference distributions weight optimal and near-optimal designs more 1906 heavily (i.e., a distribution with negative skew), while still capturing a variety of different possible designs. 1907

D.8. Distribution Analysis of Quality and Diversity Results 1909

1901

1903 1904

1908

1910 In our experimental results in the main text and in the Appendices, we primarily focus on reporting summative statistics: for 1911 example, the Best@128 oracle score and the average Pairwise Diversity metric over the final batch of k = 128 samples. In 1912 this section, we isolate a single representative experimental run and plot the distribution of scores achieved by all k = 1281913 designs from a single experimental run to better interrogate the robustness and empirical properties of DynAMO. 1914

In Supplementary Figure A2, we first plot the distributions of the oracle reward score $r(x_i^F)$ and minimum novelty score 1915 $\min_{x' \in D} d(x_i^F, x')$ achieved by each of the k = 128 designs in the set $\{x_i^F\}_{i=1}^k$ proposed by the CMA-ES optimizer with 1916 and without DynAMO augmentation in a single experimental run. (Recall that \mathcal{D} is the static, offline dataset of reference 1917 designs and $d(\cdot, \cdot)$ is the normalized Levenshtein distance metric for this task.) We see that in general, DynAMO not only 1918 enables the optimizer to discover more optimal designs with higher probability, but also yields a wider-tailed distribution of 1919 oracle scores compared to the baseline method. Separately, we see that DynAMO augmentation decreases both the median and mode Minimum Novelty score compared to the baseline method, in agreement with our discussion in Appendix D.2. 1921

In the bottom row of Supplementary Figure A2, we visualize a heat map of pairwise diversity scores; that is, the color of pixel (i, j) is correlated with the distance $d(x_i^F, x_j^F)$ for any $1 \le i, j \le k$ pair of generated designs proposed by the

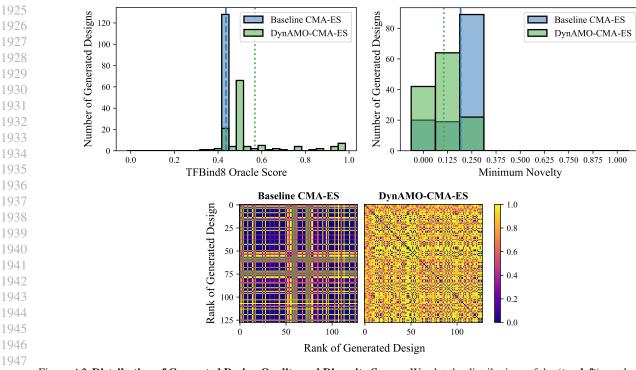


Figure A2. Distribution of Generated Design Quality and Diversity Scores. We plot the distributions of the (top left) oracle score; (top right) minimum novelty; and (bottom) pairwise diversity of the k = 128 proposed designs from a single representative experimental run using the CMA-ES backbone optimizers with and without DynAMO on the TFBind8 task. Dashed blue (resp., dotted green) lines in the top panels represent the mean score achieved by the Baseline CMA-ES (resp., DynAMO-CMA-ES) method from the experimental run.

optimization method. Even a cursory visual inspection reveals that DynAMO augmentation of the backbone CMA-ES
 optimizer significance improves the pairwise diversity of candidate designs when compared to the baseline method.

1956 1957 **D.9. Why Is Diversity Important?**

1952

1968

Our principle motivation for obtaining a diverse sample of designs in offline MBO is to enable downstream **secondary exploration** of other objectives that we might care about in real-world applications. For example, given a batch of proposed candidates drugs that were optimized for maximal therapeutic efficacy in treating a disease, we might then try to quantify each candidate's manufacturing cost, difficulty of synthesize, profile of potential side effects, and other objectives. In this setting, obtaining highly similar designs from offline MBO may result in strong therapeutic efficacy, but also *equally* unacceptable values of other secondary objectives.

To validate this motivating claim that diversity is important to obtain a wide range of secondary objective values, we compare the range and variance of secondary objective values within a batch of proposed candidate designs. We consider the following 3 offline MBO tasks:

1969 1. Vehicle Safety is continuous, 5-dimensional optimization problem from Liao et al. (2008) to find an optimal set of 1970 car dimensions that minimize the total Mass of the vehicle. The problem initially stems from the multi-objective 1971 optimization literature (Blank & Deb, 2020; Liao et al., 2008; Huo et al., 2022; Gonzalez de Oliveira et al., 2023), where the secondary goals are to (1) minimize the worst-case Acceleration-induced biomechanical damage of the car occupants in the event of a collision; and (2) minimize the worst-case toe board **Intrusion** of the vehicle in the event of 1974 an 'offset-frontal crash.' We treat the Mass as the offline MBO optimization objective and Acceleration and Intrusion 1975 as the downstream secondary objectives. We negate all objective values prior to max-min normalization as described in Appendix B to frame this as a *maximization* problem in accordance with the setup in Table 1. An offline dataset of n = 800 designs was synthetically constructed, and we used the oracle function from Liao et al. (2008) to compute all 3 objective values. 1979

Diversity By Design: Leveraging Distribution Matching for Offline Model-Based Optimization

- 2. Welded Beam is a continuous, 4-dimensional optimization problem from Ray & Liew (2002) to find an optimal set of dimensions for a welded steel beam that minimizes the total manufacturing Cost. Similar to the Vehicle task, this problem was initially proposed in the multi-objective optimization literature (Blank & Deb, 2020; Liao et al., 2008; Kamil et al., 2021; Deb et al., 2006) where the secondary goal is to (1) minimize the end Deflection of the beam.³ Again, we negate all objective values prior to max-min normalization as described in Appendix B to frame this as a maximization problem. An offline dataset of n = 800 designs was synthetically constructed, and we used the oracle function from Ray & Liew (2002) to compute both objective values.
- 3. UTR is a discrete, 50-dimensional optimization problem from Angermüeller et al. (2020) and Sample et al. (2019) with the goal of finding an optimal 50-bp DNA sequence that maximizes the gene expression from a 5' UTR DNA sequence. This is an offline MBO problem from the Design-Bench benchmarking suite (Trabucco et al., 2022) that we use to evaluate offline MBO algorithms in our main experimental results in **Table 1** and elsewhere. However, a secondary objective is to minimize the GC Content of the resulting DNA sequence, which is correlated with the difficulty of cloning and sequencing the DNA sequence using standard DNA amplification and analysis methods in the laboratory setting (Benita et al., 2003; Yakovchuk et al., 2006; Gardner et al., 2002). To evaluate this secondary objective, we use the same experimental setting as for the initial UTR experiments described in Appendix B and evaluate the GC Content of the k = 128 proposed designs as the secondary objective according to Benita et al. (2003).

We used the standard deviation of secondary objective values achieved by a proposed set of designs to quantify the range of secondary objective values, and the pairwise diversity metric (PD@128) to quantify the diversity of designs. We evaluated both baseline and DynAMO-enhanced optimization methods on the three tasks above (**Supplementary Table A10**). Our results consistently demonstrate that a greater diversity score of the final proposed designs (i.e., higher PD@128 score) is correlated with a greater range of captured secondary objective values. As a result, a diverse set of designs (such as those proposed by DynAMO-enhanced optimization methods) can better enable downstream evaluation of the trade-offs between different objectives for a given design.

³The original problem from Ray & Liew (2002) was proposed as a constrained optimization problem with 5 sets of constraints on the maximum considered shear stress, bending stress, buckling load, and other material testing parameters. To simplify our experimental setting, we consider the *unconstrained* version of the optimization problem here.

Table A6. Comparison of Design Quality Against Model-Free Optimization Methods. We evaluate DynAMO and other model-based optimization methods against model-free optimization methods. We report the maximum (resp., median) oracle score achieved out of 128 evaluated designs in the top (resp., bottom) table. Metrics are reported mean^(95% confidence interval) across 10 random seeds, where higher is better. $\max(\mathcal{D})$ reports the top oracle score in the offline dataset. All metrics are multiplied by 100 for easier legibility. **Bolded** entries indicate average scores with an overlapping 95% confidence interval to the best performing method. Bolded (resp., Underlined) Rank and Optimality Gap (Opt. Gap) metrics indicate the best (resp., second best) for a given backbone optimizer.

Best@128	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	Rank ↓	Opt. 0
Dataset \mathcal{D}	43.9	59.4	60.5	88.9	40.0	88.4	_	_
Grad.	90.0 ^(4.3)	80.9(12.1)	60.2 ^(8.9)	88.8 ^(4.0)	36.0 ^(6.8)	65.6 ^(14.5)	16.0	6.
BO-qUCB	88.1 ^(5.3)	$86.2^{(0.1)}$	$66.4^{(0.7)}$	121 ^(1.3)	51.3 ^(3.6)	$84.5^{(0.8)}$	7.3	19.
CMA-ES	87.6 ^(8.3)	86.2 ^(0.0)	66.1 ^(1.0)	106 ^(5.9)	49.0 ^(1.0)	72.2 ^(0.1)	10.2	14.
BONET	$95.5^{(0.0)}$	92.9 ^(0.1)	63.3 ^(0.0)	97.3 ^(0.0)	$39.0^{(0.7)}$	93.7 ^(0.2)	8.0	16
DDOM	93.0 ^(3.6)	85.3 ^(0.5)	63.5 ^(0.4)	87.9(0.6)	44.7 ^(2.2)	63.0(12.1)	13.0	9.
ExPT	89.3 ^(5.7)	84.2 ^(2.4)	63.3 ^(0.0)	93.0 ^(0.8)	48.5(11.0)	82.3 ^(2.3)	12.0	13
MINs	89.0 ^(3.4)	68.3 ^(0.6)	63.9 ^(0.9)	93.1 ^(0.7)	45.8 ^(2.1)	91.5 ^(1.1)	11.2	11
GTG	92.1 ^(0.0)	$70.2^{(0.0)}$	63.3 ^(0.0)	85.0 ^(0.0)	52.5 ^(0.0)	96.4 ^(0.0)	9.7	13
Tri-Mentoring	82.4 ^(0.0)	66.6 ^(0.0)	68.4 ^(0.0)	88.9 ^(0.0)	50.9 ^(1.1)	94.0 ^(0.0)	10.2	11
ICT	93.3 ^(3.4)	$66.6^{(0.0)}$	68.4 ^(0.0)	88.9 ^(0.0)	48.9 ^(1.4)	95.5 ^(1.1)	9.0	13
PGS	79.6 ^(7.5)	$67.1^{(0.8)}$	68.4 ^(0.0)	88.9 ^(0.0)	54.8 ^(0.8)	$72.3^{(0.0)}$	11.3	8.
Match-Opt	90.9 ^(3.4)	$68.4^{(0.8)}$	63.3 ^(0.1)	87.8 ^(0.6)	35.2 ^(2.3)	72.3 $72.2^{(0.1)}$	15.5	6.
RGD	90.9 ^(4.2)	$68.7^{(0.6)}$	63.4 ^(0.2)	$90.2^{(0.3)}$	43.0 ^(2.7)	88.5 ^(1.1)	13.3	10
COMs	93.1 ^(3.4)	$67.0^{(0.9)}$	63.4 ^(1.0)	$90.2^{(1.6)}$ $97.1^{(1.6)}$	$43.0^{(4.8)}$ $41.2^{(4.8)}$	88.3 91.8 ^(0.9)	13.2	10
RoMA	95.1 ^(0.0)	77.8 ^(0.0)	$63.3^{(0.0)}$	97.1 84.7 ^(0.0)	$41.2^{(1.4)}$ $49.8^{(1.4)}$	91.8 ^(1.6)	9.7	12
	96.5 ^(0.7) 98.1 ^(0.7)	$66.8^{(1.0)}$	63.0 ^(0.8)	$91.8^{(0.9)}$	49.8 38.7 ^(2.5)	95.7 ^(0.9) 87.8 ^(0.9)		
ROMO	98.1 ^(1.9) 94.1 ^(1.9)	86.3 ^(0.2)	63.0 ^(0.7) 66.8 ^(0.7)	91.8 ^(0.0) 121 ^(0.0)	50.8 ^(3.3)		12.7	10
GAMBO						86.7 ^(1.1)	4.8	20
DynAMO-Grad.	90.3 ^(4.7)	86.2(0.0)	64.4 ^(2.5)	91.2(0.0)	44.2(7.8)	89.8 ^(3.2)	9.5	14
DynAMO-BO-qUCB	95.1 ^(1.9)	86.2(0.0)	66.7 ^(1.5)	121 ^(0.0)	48.1 ^(4.0)	86.9 ^(4.5)	<u>6.3</u>	<u>20</u>
DynAMO-CMA-ES	89.8 ^(3.6)	85.7 ^(5.8)	63.9 ^(0.9)	117 ^(6.7)	50.6 ^(4.8)	78.5 ^(5.5)	9.3	17
Median@128	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	Rank ↓	Opt.
Dataset $\mathcal D$	33.7	42.8	50.9	87.6	6.7	77.8		
								- 10
Grad.	58.1 ^(6.1)	58.6(13.1)	59.3 ^(8.6)	85.3 ^(7.7)	36.0 ^(6.7)	65.1(14.4)		
Grad. BO-qUCB	58.1 ^(6.1) 50.3 ^(1.8)	$58.6^{(13.1)} \\ 62.1^{(3.4)}$	59.3 ^(8.6) 63.3 ^(0.0)	85.3 ^(7.7) 86.6 ^(0.6)	36.0 ^(6.7) 31.7 ^(1.2)	$\begin{array}{c} 65.1^{(14.4)} \\ 74.4^{(0.6)} \end{array}$	6.8	11
Grad. BO-qUCB CMA-ES	58.1 ^(6.1) 50.3 ^(1.8) 50.7 ^(2.7)	58.6 ^(13.1) 62.1 ^(3.4) 71.7 ^(10.4)	59.3 ^(8.6) 63.3 ^(0.0) 63.3 ^(0.0)	85.3 ^(7.7) 86.6 ^(0.6) 83.9 ^(1.0)	36.0 ^(6.7) 31.7 ^(1.2) 37.9 ^(0.7)	$\begin{array}{c} 65.1^{(14.4)} \\ 74.4^{(0.6)} \\ 59.3^{(10.9)} \end{array}$	6.8 7.2	11 11
Grad. BO-qUCB CMA-ES BONET	58.1 ^(6.1) 50.3 ^(1.8) 50.7 ^(2.7) 53.1 ^(0.0)	$58.6^{(13.1)}$ $62.1^{(3.4)}$ $71.7^{(10.4)}$ $46.5^{(0.6)}$	59.3 ^(8.6) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0)	85.3 ^(7.7) 86.6 ^(0.6) 83.9 ^(1.0) 91.2 ^(0.1)	36.0 ^(6.7) 31.7 ^(1.2) 37.9 ^(0.7) 37.9 ^(0.0)	65.1 ^(14.4) 74.4 ^(0.6) 59.3 ^(10.9) 92.1^(0.0)	6.8 7.2 5.2	11 11 <u>14</u>
Grad. BO-qUCB CMA-ES BONET DDOM	58.1 ^(6.1) 50.3 ^(1.8) 50.7 ^(2.7) 53.1 ^(0.0) 55.9^(0.7)	$58.6^{(13.1)}$ $62.1^{(3.4)}$ $71.7^{(10.4)}$ $46.5^{(0.6)}$ $57.6^{(0.8)}$	59.3 ^(8.6) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0)	85.3 ^(7.7) 86.6 ^(0.6) 83.9 ^(1.0) 91.2 ^(0.1) 83.4 ^(0.1)	36.0 ^(6.7) 31.7 ^(1.2) 37.9 ^(0.7) 37.9 ^(0.0) 21.9 ^(1.7)	65.1 ^(14.4) 74.4 ^(0.6) 59.3 ^(10.9) 92.1^(0.0) 57.6 ^(13.2)	6.8 7.2 5.2 12.2	11 11 <u>14</u> 6
Grad. BO-qUCB CMA-ES BONET DDOM ExPT	58.1 ^(6.1) 50.3 ^(1.8) 50.7 ^(2.7) 53.1 ^(0.0) 55.9^(0.7) 44.7 ^(6.8)	$58.6^{(13.1)}$ $62.1^{(3.4)}$ $71.7^{(10.4)}$ $46.5^{(0.6)}$ $57.6^{(0.8)}$ $57.0^{(4.8)}$	$59.3^{(8.6)}$ $63.3^{(0.0)}$ $63.3^{(0.0)}$ $63.3^{(0.0)}$ $63.3^{(0.0)}$ $63.3^{(0.0)}$	85.3 ^(7,7) 86.6 ^(0,6) 83.9 ^(1,0) 91.2 ^(0,1) 83.4 ^(0,1) 89.8 ^(3,3)	36.0 ^(6.7) 31.7 ^(1.2) 37.9 ^(0.7) 37.9 ^(0.0) 21.9 ^(1.7) 34.1 ^(12.3)	$\begin{array}{c} 65.1^{(14.4)} \\ 74.4^{(0.6)} \\ 59.3^{(10.9)} \\ \textbf{92.1}^{(\textbf{0.0)}} \\ 57.6^{(13.2)} \\ 67.8^{(14.1)} \end{array}$	6.8 7.2 5.2 12.2 9.3	11 11 <u>14</u> 6. 9.
Grad. BO-qUCB CMA-ES BONET DDOM ExPT MINs	58.1 ^(6.1) 50.3 ^(1.8) 50.7 ^(2.7) 53.1 ^(0.0) 55.9^(0.7) 44.7 ^(6.8) 41.3 ^(1.2)	$58.6^{(13.1)}$ $62.1^{(3.4)}$ $71.7^{(10.4)}$ $46.5^{(0.6)}$ $57.6^{(0.8)}$ $57.0^{(4.8)}$ $58.0^{(0.5)}$	59.3(8.6) $63.3(0.0) 63.3(0.0) 63.3(0.0) 63.3(0.0) 63.3(0.0) 63.3(0.0)63.3(0.0)$	85.3 ^(7.7) 86.6 ^(0.6) 83.9 ^(1.0) 91.2 ^(0.1) 83.4 ^(0.1) 89.8 ^(3.3) 88.3 ^(0.3)	36.0 ^(6.7) 31.7 ^(1.2) 37.9 ^(0.7) 37.9 ^(0.0) 21.9 ^(1.7) 34.1 ^(12.3) 32.3 ^(1.6)	$\begin{array}{c} 65.1^{(14.4)} \\ 74.4^{(0.6)} \\ 59.3^{(10.9)} \\ \textbf{92.1}^{(0.0)} \\ 57.6^{(13.2)} \\ 67.8^{(14.1)} \\ 68.9^{(15.9)} \end{array}$	6.8 7.2 5.2 12.2 9.3 9.7	11 11 <u>14</u> 6. 9. 8.
Grad. BO-qUCB CMA-ES BONET DDOM ExPT MINs GTG	58.1(6.1) 50.3(1.8) 50.7(2.7) 53.1(0.0) 55.9(0.7) 44.7(6.8) 41.3(1.2) 43.4(0.3)	$58.6^{(13.1)}$ $62.1^{(3.4)}$ $71.7^{(10.4)}$ $46.5^{(0.6)}$ $57.6^{(0.8)}$ $57.0^{(4.8)}$ $58.0^{(0.5)}$ $64.2^{(0.0)}$	59.3(8.6) 63.3(0.0) 63.3(0.0) 63.3(0.0) 63.3(0.0) 63.3(0.0) 63.3(0.0) 63.3(0.0) 63.3(0.0)	85.3 ^(7.7) 86.6 ^(0.6) 83.9 ^(1.0) 91.2 ^(0.1) 83.4 ^(0.1) 89.8 ^(3.3) 88.3 ^(0.3) 83.1 ^(0.0)	36.0 ^(6.7) 31.7 ^(1.2) 37.9 ^(0.7) 37.9 ^(0.0) 21.9 ^(1.7) 34.1 ^(12.3) 32.3 ^(1.6) 28.0 ^(0.0)	$\begin{array}{c} 65.1^{(14.4)} \\ 74.4^{(0.6)} \\ 59.3^{(10.9)} \\ \textbf{92.1}^{(\textbf{0.0})} \\ 57.6^{(13.2)} \\ 67.8^{(14.1)} \\ 68.9^{(15.9)} \\ \textbf{90.6}^{(0.0)} \end{array}$	6.8 7.2 5.2 12.2 9.3 9.7 9.3	11 11 <u>14</u> 6. 9. 8. 12
Grad. BO-qUCB CMA-ES BONET DDOM ExPT MINs GTG Tri-Mentoring	$\begin{array}{c} \textbf{58.1}^{\textbf{(6.1)}}\\ \textbf{50.3}^{(1.8)}\\ \textbf{50.7}^{(2.7)}\\ \textbf{53.1}^{(0.0)}\\ \textbf{55.9}^{\textbf{(0.7)}}\\ \textbf{44.7}^{(6.8)}\\ \textbf{41.3}^{(1.2)}\\ \textbf{43.4}^{(0.3)}\\ \textbf{46.1}^{(0.0)} \end{array}$	$58.6^{(13.1)}$ $62.1^{(3.4)}$ $71.7^{(10.4)}$ $46.5^{(0.6)}$ $57.6^{(0.8)}$ $57.0^{(4.8)}$ $58.0^{(0.5)}$ $64.2^{(0.0)}$ $61.1^{(0.0)}$	$59.3^{(8.6)}$ $63.3^{(0.0)}$ $63.3^{(0.0)}$ $63.3^{(0.0)}$ $63.3^{(0.0)}$ $63.3^{(0.0)}$ $63.3^{(0.0)}$ $63.3^{(0.0)}$ $63.3^{(0.0)}$ $63.3^{(0.0)}$	85.3 ^(7.7) 86.6 ^(0.6) 83.9 ^(1.0) 91.2 ^(0.1) 83.4 ^(0.1) 89.8 ^(3.3) 88.3 ^(0.3) 83.1 ^(0.0) 88.9 ^(0.0)	36.0 ^(6.7) 31.7 ^(1.2) 37.9 ^(0.7) 37.9 ^(0.0) 21.9 ^(1.7) 34.1 ^(12.3) 32.3 ^(1.6) 28.0 ^(0.0) 34.2 ^(1.2)	$\begin{array}{c} 65.1^{(14.4)}\\ 74.4^{(0.6)}\\ 59.3^{(10.9)}\\ \textbf{92.1}^{(0.0)}\\ \textbf{57.6}^{(13.2)}\\ 67.8^{(14.1)}\\ 68.9^{(15.9)}\\ \textbf{90.6}^{(0.0)}\\ 88.4^{(0.0)} \end{array}$	6.8 7.2 5.2 12.2 9.3 9.7 9.3 <u>6.5</u>	111 111 <u>144</u> 6. 9. 8. 12 13
Grad. BO-qUCB CMA-ES BONET DDOM ExPT MINs GTG Tri-Mentoring ICT	$\begin{array}{c} \textbf{58.1}^{\textbf{(6.1)}}\\ 50.3^{(1.8)}\\ 50.7^{(2.7)}\\ \textbf{53.1}^{(0.0)}\\ \textbf{55.9}^{\textbf{(0.7)}}\\ 44.7^{(6.8)}\\ 41.3^{(1.2)}\\ 43.4^{(0.3)}\\ 46.1^{(0.0)}\\ \textbf{59.5}^{\textbf{(3.0)}} \end{array}$	$58.6^{(13.1)}$ $62.1^{(3.4)}$ $71.7^{(10.4)}$ $46.5^{(0.6)}$ $57.6^{(0.8)}$ $57.0^{(4.8)}$ $58.0^{(0.5)}$ $64.2^{(0.0)}$ $61.1^{(0.0)}$	$\begin{array}{c} {\color{black}{59.3^{(8.6)}}}\\ {\color{black}{63.3^{(0.0)}}}\\ {\color{black}{63.3^{(0.0)}}}\\ {\color{black}{63.3^{(0.0)}}}\\ {\color{black}{63.3^{(0.0)}}}\\ {\color{black}{63.3^{(0.0)}}}\\ {\color{black}{63.3^{(0.0)}}}\\ {\color{black}{63.3^{(0.0)}}}\\ {\color{black}{57.1^{(0.0)}}}\end{array}$	85.3 ^(7.7) 86.6 ^(0.6) 83.9 ^(1.0) 91.2 ^(0.1) 83.4 ^(0.1) 89.8 ^(3.3) 88.3 ^(0.3) 83.1 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0)	36.0 ^(6.7) 31.7 ^(1.2) 37.9 ^(0.7) 37.9 ^(0.0) 21.9 ^(1.7) 34.1 ^(12.3) 32.3 ^(1.6) 28.0 ^(0.0) 34.2 ^(1.2) 37.0 ^(1.2)	$\begin{array}{c} 65.1^{(14.4)}\\ 74.4^{(0.6)}\\ 59.3^{(10.9)}\\ \textbf{92.1}^{(0.0)}\\ \textbf{57.6}^{(13.2)}\\ 67.8^{(14.1)}\\ 68.9^{(15.9)}\\ \textbf{90.6}^{(0.0)}\\ 88.4^{(0.0)}\\ 88.4^{(0.1)}\\ \end{array}$	6.8 7.2 5.2 12.2 9.3 9.7 9.3 <u>6.5</u> 7.0	111 11 <u>14</u> 6. 9. 8. 12 13 15
Grad. BO-qUCB CMA-ES BONET DDOM ExPT MINs GTG Tri-Mentoring ICT PGS	$\begin{array}{c} \textbf{58.1}^{\textbf{(6.1)}}\\ 50.3^{(1.8)}\\ 50.7^{(2.7)}\\ \textbf{53.1}^{(0.0)}\\ \textbf{55.9}^{\textbf{(0.7)}}\\ 44.7^{(6.8)}\\ 41.3^{(1.2)}\\ 43.4^{(0.3)}\\ 46.1^{(0.0)}\\ \textbf{59.5}^{\textbf{(3.0)}}\\ 40.7^{(2.6)} \end{array}$	$58.6^{(13.1)}$ $62.1^{(3.4)}$ $71.7^{(10.4)}$ $46.5^{(0.6)}$ $57.6^{(0.8)}$ $57.0^{(4.8)}$ $58.0^{(0.5)}$ $64.2^{(0.0)}$ $61.1^{(0.0)}$ $61.1^{(0.0)}$ $60.3^{(0.7)}$	59.3 ^(8.6) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 57.1 ^(0.0) 58.4 ^(0.0)	85.3 ^(7.7) 86.6 ^(0.6) 83.9 ^(1.0) 91.2 ^(0.1) 83.4 ^(0.1) 89.8 ^(3.3) 88.3 ^(0.3) 83.1 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0)	36.0 ^(6.7) 31.7 ^(1.2) 37.9 ^(0.7) 37.9 ^(0.0) 21.9 ^(1.7) 34.1 ^(12.3) 32.3 ^(1.6) 28.0 ^(0.0) 34.2 ^(1.2) 37.0 ^(1.2) 28.2 ^(0.5)	$\begin{array}{c} 65.1^{(14.4)}\\ 74.4^{(0.6)}\\ 59.3^{(10.9)}\\ \textbf{92.10.00}\\ 57.6^{(13.2)}\\ 67.8^{(14.1)}\\ 68.9^{(15.9)}\\ 90.6^{(0.0)}\\ 88.4^{(0.0)}\\ 88.4^{(0.1)}\\ 70.9^{(0.7)} \end{array}$	6.8 7.2 5.2 12.2 9.3 9.7 9.3 <u>6.5</u> 7.0 12.3	111 111 14 6 9 8 12 13 15 8
Grad. BO-qUCB CMA-ES BONET DDOM ExPT MINs GTG Tri-Mentoring ICT PGS Match-Opt	$\begin{array}{c} \textbf{58.1}^{\textbf{(6.1)}}\\ \textbf{50.3}^{(1.8)}\\ \textbf{50.7}^{(2.7)}\\ \textbf{53.1}^{(0.0)}\\ \textbf{55.9}^{\textbf{(0.7)}}\\ \textbf{44.7}^{(6.8)}\\ \textbf{41.3}^{(1.2)}\\ \textbf{43.4}^{(0.3)}\\ \textbf{46.1}^{(0.0)}\\ \textbf{59.5}^{\textbf{(3.0)}}\\ \textbf{40.7}^{(2.6)}\\ \textbf{40.7}^{(1.2)} \end{array}$	$58.6^{(13.1)}$ $62.1^{(3.4)}$ $71.7^{(10.4)}$ $46.5^{(0.6)}$ $57.6^{(0.8)}$ $57.0^{(4.8)}$ $58.0^{(0.5)}$ $64.2^{(0.0)}$ $61.1^{(0.0)}$ $61.1^{(0.0)}$ $60.3^{(0.7)}$ $57.9^{(0.5)}$	59.3 ^(8.6) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 57.1 ^(0.0) 58.4 ^(0.0) 63.3 ^(0.0)	85.3 ^(7.7) 86.6 ^(0.6) 83.9 ^(1.0) 91.2 ^(0.1) 83.4 ^(0.1) 89.8 ^(3.3) 88.3 ^(0.3) 83.1 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 83.9 ^(0.1)	36.0 ^(6.7) 31.7 ^(1.2) 37.9 ^(0.7) 37.9 ^(0.0) 21.9 ^(1.7) 34.1 ^(12.3) 32.3 ^(1.6) 28.0 ^(0.0) 34.2 ^(1.2) 37.0 ^(1.2) 28.2 ^(0.5) 14.5 ^(0.9)	$\begin{array}{c} 65.1^{(14.4)}\\ 74.4^{(0.6)}\\ 59.3^{(10.9)}\\ \textbf{92.1}^{(0.0)}\\ \textbf{57.6}^{(13.2)}\\ 67.8^{(14.1)}\\ 68.9^{(15.9)}\\ \textbf{90.6}^{(0.0)}\\ 88.4^{(0.0)}\\ 88.4^{(0.1)}\\ 70.9^{(0.7)}\\ 60.5^{(9.0)} \end{array}$	6.8 7.2 5.2 12.2 9.3 9.7 9.3 <u>6.5</u> 7.0 12.3 15.0	111 111 144 6. 9. 8. 122 133 155 8. 8. 3.
Grad. BO-qUCB CMA-ES BONET DDOM ExPT MINs GTG Tri-Mentoring ICT PGS Match-Opt RGD	$\begin{array}{c} \textbf{58.1}^{\textbf{(6.1)}}\\ \textbf{50.3}^{(1.8)}\\ \textbf{50.7}^{(2.7)}\\ \textbf{53.1}^{(0.0)}\\ \textbf{55.9}^{\textbf{(0.7)}}\\ \textbf{44.7}^{(6.8)}\\ \textbf{41.3}^{(1.2)}\\ \textbf{43.4}^{(0.3)}\\ \textbf{46.1}^{(0.0)}\\ \textbf{59.5}^{\textbf{(3.0)}}\\ \textbf{40.7}^{(2.6)}\\ \textbf{40.7}^{(1.2)}\\ \textbf{41.1}^{(1.3)} \end{array}$	$58.6^{(13.1)} \\62.1^{(3.4)} \\71.7^{(10.4)} \\46.5^{(0.6)} \\57.6^{(0.8)} \\57.0^{(4.8)} \\58.0^{(0.5)} \\64.2^{(0.0)} \\61.1^{(0.0)} \\61.1^{(0.0)} \\60.3^{(0.7)} \\57.9^{(0.5)} \\57.4^{(0.9)} \\$	59.3 ^(8.6) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 57.1 ^(0.0) 58.4 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0)	85.3 ^(7.7) 86.6 ^(0.6) 83.9 ^(1.0) 91.2 ^(0.1) 83.4 ^(0.1) 89.8 ^(3.3) 88.3 ^(0.3) 83.1 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 83.2 ^(0.1) 86.4 ^(0.1)	$\begin{array}{c} \textbf{36.0}^{(6.7)} \\ \textbf{31.7}^{(1.2)} \\ \textbf{37.9}^{(0.7)} \\ \textbf{37.9}^{(0.0)} \\ \textbf{21.9}^{(1.7)} \\ \textbf{34.1}^{(12.3)} \\ \textbf{32.3}^{(1.6)} \\ \textbf{28.0}^{(0.0)} \\ \textbf{34.2}^{(1.2)} \\ \textbf{37.0}^{(1.2)} \\ \textbf{28.2}^{(0.5)} \\ \textbf{14.5}^{(0.9)} \\ \textbf{20.7}^{(0.6)} \end{array}$	$\begin{array}{c} 65.1^{(14.4)}\\ 74.4^{(0.6)}\\ 59.3^{(10.9)}\\ \textbf{92.1}^{(0.0)}\\ 57.6^{(13.2)}\\ 67.8^{(14.1)}\\ 68.9^{(15.9)}\\ 90.6^{(0.0)}\\ 88.4^{(0.0)}\\ 88.4^{(0.0)}\\ 88.4^{(0.1)}\\ 70.9^{(0.7)}\\ 60.5^{(9.0)}\\ 70.9^{(1.8)}\\ \end{array}$	6.8 7.2 5.2 12.2 9.3 9.7 9.3 <u>6.5</u> 7.0 12.3 15.0 12.3	111 114 6. 9. 8. 12 133 15 8. 3. 6.
Grad. BO-qUCB CMA-ES BONET DDOM ExPT MINs GTG Tri-Mentoring ICT PGS Match-Opt RGD COMs	$\begin{array}{c} \textbf{58.1}^{\textbf{(6.1)}}\\ \textbf{50.3}^{(1.8)}\\ \textbf{50.7}^{(2.7)}\\ \textbf{53.1}^{(0.0)}\\ \textbf{55.9}^{\textbf{(0.7)}}\\ \textbf{44.7}^{(6.8)}\\ \textbf{41.3}^{(1.2)}\\ \textbf{43.4}^{(0.3)}\\ \textbf{46.1}^{(0.0)}\\ \textbf{59.5}^{\textbf{(3.0)}}\\ \textbf{40.7}^{(2.6)}\\ \textbf{40.7}^{(1.2)}\\ \textbf{41.1}^{(1.3)}\\ \textbf{43.9}^{(0.0)} \end{array}$	$58.6^{(13.1)} \\62.1^{(3.4)} \\71.7^{(10.4)} \\46.5^{(0.6)} \\57.6^{(0.8)} \\57.0^{(4.8)} \\58.0^{(0.5)} \\64.2^{(0.0)} \\61.1^{(0.0)} \\61.1^{(0.0)} \\61.1^{(0.0)} \\57.9^{(0.5)} \\57.4^{(0.9)} \\59.0^{(0.5)} \\59.0^{(0.5)} \\$	59.3 ^(8.6) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 57.1 ^(0.0) 58.4 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0)	85.3 ^(7.7) 86.6 ^(0.6) 83.9 ^(1.0) 91.2 ^(0.1) 83.4 ^(0.1) 89.8 ^(3.3) 83.3 ^(0.3) 83.3 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 83.2 ^(0.1) 86.4 ^(0.1) 93.2 ^(7.7)	$\begin{array}{c} \textbf{36.0}^{(6.7)} \\ \textbf{31.7}^{(1.2)} \\ \textbf{37.9}^{(0.7)} \\ \textbf{37.9}^{(0.0)} \\ \textbf{21.9}^{(1.7)} \\ \textbf{34.1}^{(12.3)} \\ \textbf{32.3}^{(1.6)} \\ \textbf{28.0}^{(0.0)} \\ \textbf{34.2}^{(1.2)} \\ \textbf{37.0}^{(1.2)} \\ \textbf{28.2}^{(0.5)} \\ \textbf{14.5}^{(0.9)} \\ \textbf{20.7}^{(0.6)} \\ \textbf{21.3}^{(5.6)} \end{array}$	$\begin{array}{c} 65.1^{(14.4)}\\ 74.4^{(0.6)}\\ 59.3^{(10.9)}\\ \textbf{92.1}^{(0.0)}\\ \textbf{57.6}^{(13.2)}\\ 67.8^{(14.1)}\\ 68.9^{(15.9)}\\ \textbf{90.6}^{(0.0)}\\ 88.4^{(0.0)}\\ 88.4^{(0.1)}\\ 70.9^{(0.7)}\\ 60.5^{(9.0)}\\ 70.9^{(1.8)}\\ \textbf{89.9}^{(1.0)}\\ \end{array}$	6.8 7.2 5.2 12.2 9.3 9.7 9.3 <u>6.5</u> 7.0 12.3 15.0 12.3 8.5	111 111 144 6. 9. 8. 122 133 155 8.8 3. 6. 11
Grad. BO-qUCB CMA-ES BONET DDOM ExPT MINs GTG Tri-Mentoring ICT PGS Match-Opt RGD COMs RoMA	$\begin{array}{c} \textbf{58.1}^{(\textbf{6.1})} \\ 50.3^{(1.8)} \\ 50.7^{(2.7)} \\ \textbf{53.1}^{(0.0)} \\ \textbf{55.9}^{(\textbf{0.7)}} \\ 44.7^{(6.8)} \\ 41.3^{(1.2)} \\ 43.4^{(0.3)} \\ 46.1^{(0.0)} \\ \textbf{59.5}^{(\textbf{3.0)}} \\ 40.7^{(2.6)} \\ 40.7^{(1.2)} \\ 41.1^{(1.3)} \\ 43.9^{(0.0)} \\ \textbf{50.1}^{(4.3)} \end{array}$	$\begin{array}{c} 58.6^{(13.1)}\\ 62.1^{(3.4)}\\ 71.7^{(10.4)}\\ 46.5^{(0.6)}\\ 57.6^{(0.8)}\\ 57.0^{(4.8)}\\ 58.0^{(0.5)}\\ 64.2^{(0.0)}\\ 61.1^{(0.0)}\\ 61.1^{(0.0)}\\ 60.3^{(0.7)}\\ 57.9^{(0.5)}\\ 57.4^{(0.9)}\\ 59.0^{(0.5)}\\ 77.4^{(0.0)}\\ \end{array}$	59.3 ^(8.6) 63.3 ^(0.0) 63.3 ^(0.0)	85.3 ^(7.7) 86.6 ^(0.6) 83.9 ^(1.0) 91.2 ^(0.1) 83.4 ^(0.1) 89.8 ^(3.3) 83.3 ^(0.3) 83.1 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 83.2 ^(0.1) 86.4 ^(0.1) 93.2 ^(7.7) 84.7 ^(0.0)	$\begin{array}{c} \textbf{36.0}^{(6.7)} \\ \textbf{31.7}^{(1.2)} \\ \textbf{37.9}^{(0.7)} \\ \textbf{37.9}^{(0.0)} \\ \textbf{21.9}^{(1.7)} \\ \textbf{34.1}^{(12.3)} \\ \textbf{32.3}^{(1.6)} \\ \textbf{28.0}^{(0.0)} \\ \textbf{34.2}^{(1.2)} \\ \textbf{37.0}^{(1.2)} \\ \textbf{28.2}^{(0.5)} \\ \textbf{14.5}^{(0.9)} \\ \textbf{20.7}^{(0.6)} \\ \textbf{21.3}^{(5.6)} \\ \textbf{34.9}^{(1.8)} \end{array}$	$\begin{array}{c} 65.1^{(14.4)}\\ 74.4^{(0.6)}\\ 59.3^{(10.9)}\\ \textbf{92.1}^{(0.0)}\\ 57.6^{(13.2)}\\ 67.8^{(14.1)}\\ 68.9^{(15.9)}\\ 90.6^{(0.0)}\\ 88.4^{(0.0)}\\ 88.4^{(0.1)}\\ 70.9^{(0.7)}\\ 60.5^{(9.0)}\\ 70.9^{(1.8)}\\ 89.9^{(1.0)}\\ 63.7^{(6.2)} \end{array}$	6.8 7.2 5.2 12.2 9.3 9.7 9.3 <u>6.5</u> 7.0 12.3 15.0 12.3 8.5 7.3	111 111 14 6. 9. 8. 12 133 15 8. 3. 6. 111
Grad. BO-qUCB CMA-ES BONET DDOM ExPT MINs GTG Tri-Mentoring ICT PGS Match-Opt RGD COMs RoMA ROMO	$\begin{array}{c} \textbf{58.1}^{\textbf{(6.1)}}\\ \textbf{50.3}^{(1.8)}\\ \textbf{50.7}^{(2.7)}\\ \textbf{53.1}^{(0.0)}\\ \textbf{55.9}^{\textbf{(0.7)}}\\ \textbf{41.3}^{(1.2)}\\ \textbf{43.4}^{(0.3)}\\ \textbf{46.1}^{(0.0)}\\ \textbf{59.5}^{\textbf{(3.0)}}\\ \textbf{40.7}^{(2.6)}\\ \textbf{40.7}^{(1.2)}\\ \textbf{41.1}^{(1.3)}\\ \textbf{43.9}^{(0.0)}\\ \textbf{50.1}^{(4.3)}\\ \textbf{58.7}^{\textbf{(3.3)}} \end{array}$	$\begin{array}{c} 58.6^{(13.1)}\\ 62.1^{(3.4)}\\ 71.7^{(10.4)}\\ 46.5^{(0.6)}\\ 57.6^{(0.8)}\\ 57.0^{(4.8)}\\ 58.0^{(0.5)}\\ 64.2^{(0.0)}\\ 61.1^{(0.0)}\\ 61.1^{(0.0)}\\ 61.1^{(0.0)}\\ 60.3^{(0.7)}\\ 57.9^{(0.5)}\\ 57.4^{(0.9)}\\ 59.0^{(0.5)}\\ 77.4^{(0.0)}\\ 37.7^{(0.3)} \end{array}$	59.3 ^(8.6) 63.3 ^(0.0) 63.3 ^(0.0) 6	85.3 ^(7.7) 86.6 ^(0.6) 83.9 ^(1.0) 91.2 ^(0.1) 83.4 ^(0.1) 89.8 ^(3.3) 88.3 ^(0.3) 83.1 ^(0.0) 88.9 ^(0.0) 83.2 ^(7.7) 84.7 ^(0.0) 61.8 ^(2.6)	$\begin{array}{c} \textbf{36.0}^{(6.7)} \\ \textbf{31.7}^{(1.2)} \\ \textbf{37.9}^{(0.7)} \\ \textbf{37.9}^{(0.0)} \\ \textbf{21.9}^{(1.7)} \\ \textbf{34.1}^{(12.3)} \\ \textbf{32.3}^{(1.6)} \\ \textbf{28.0}^{(0.0)} \\ \textbf{34.2}^{(1.2)} \\ \textbf{37.0}^{(1.2)} \\ \textbf{28.2}^{(0.5)} \\ \textbf{14.5}^{(0.9)} \\ \textbf{20.7}^{(0.6)} \\ \textbf{21.3}^{(5.6)} \\ \textbf{34.9}^{(1.8)} \\ \textbf{27.0}^{(0.6)} \end{array}$	$\begin{array}{c} 65.1^{(14.4)}\\ 74.4^{(0.6)}\\ 59.3^{(10.9)}\\ \textbf{92.1}^{(0.0)}\\ 57.6^{(13.2)}\\ 67.8^{(14.1)}\\ 68.9^{(15.9)}\\ 90.6^{(0.0)}\\ 88.4^{(0.0)}\\ 88.4^{(0.1)}\\ 70.9^{(0.7)}\\ 60.5^{(9.0)}\\ 70.9^{(1.8)}\\ 89.9^{(1.0)}\\ 63.7^{(6.2)}\\ 46.0^{(11.7)}\\ \end{array}$	$\begin{array}{c} 6.8 \\ 7.2 \\ \textbf{5.2} \\ 12.2 \\ 9.3 \\ 9.7 \\ 9.3 \\ \underline{6.5} \\ 7.0 \\ 12.3 \\ 15.0 \\ 12.3 \\ 8.5 \\ 7.3 \\ 15.8 \end{array}$	111 111 14 6. 9. 8. 12 133 15 8. 3. 6. 111 12 -6
Grad. BO-qUCB CMA-ES BONET DDOM ExPT MINs GTG Tri-Mentoring ICT PGS Match-Opt RGD COMs RoMA	$\begin{array}{c} \textbf{58.1}^{\textbf{(6.1)}} \\ \textbf{50.3}^{(1.8)} \\ \textbf{50.7}^{(2.7)} \\ \textbf{53.1}^{(0.0)} \\ \textbf{55.9}^{\textbf{(0.7)}} \\ \textbf{44.7}^{(6.8)} \\ \textbf{41.3}^{(1.2)} \\ \textbf{43.4}^{(0.3)} \\ \textbf{46.1}^{(0.0)} \\ \textbf{59.5}^{\textbf{(3.0)}} \\ \textbf{40.7}^{(2.6)} \\ \textbf{40.7}^{(1.2)} \\ \textbf{41.1}^{(1.3)} \\ \textbf{43.9}^{(0.0)} \\ \textbf{50.1}^{(\textbf{4.3)}} \\ \textbf{58.7}^{\textbf{(3.3)}} \\ \textbf{46.4}^{(1.8)} \end{array}$	$\begin{array}{c} 58.6^{(13.1)}\\ 62.1^{(3.4)}\\ 71.7^{(10.4)}\\ 46.5^{(0.6)}\\ 57.6^{(0.8)}\\ 57.0^{(4.8)}\\ 58.0^{(0.5)}\\ 64.2^{(0.0)}\\ 61.1^{(0.0)}\\ 61.1^{(0.0)}\\ 60.3^{(0.7)}\\ 57.9^{(0.5)}\\ 57.4^{(0.9)}\\ 59.0^{(0.5)}\\ 77.4^{(0.0)}\\ \end{array}$	$\begin{array}{c} {\bf 59.3}^{(8.6)}\\ {\bf 63.3}^{(0.0)}\\ {\bf 57.1}^{(0.0)}\\ {\bf 58.4}^{(0.0)}\\ {\bf 63.3}^{(0.0)}\\ {\bf 63$	85.3 ^(7.7) 86.6 ^(0.6) 83.9 ^(1.0) 91.2 ^(0.1) 83.4 ^(0.1) 89.8 ^(3.3) 88.3 ^(0.3) 83.1 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 83.2 ^(0.1) 86.4 ^(0.1) 93.2 ^(7.7) 84.7 ^(0.0) 61.8 ^(2.6) 86.3 ^(0.5)	$\begin{array}{c} \textbf{36.0}^{(6.7)} \\ \textbf{31.7}^{(1.2)} \\ \textbf{37.9}^{(0.7)} \\ \textbf{37.9}^{(0.0)} \\ \textbf{21.9}^{(1.7)} \\ \textbf{34.1}^{(12.3)} \\ \textbf{32.3}^{(1.6)} \\ \textbf{28.0}^{(0.0)} \\ \textbf{34.2}^{(1.2)} \\ \textbf{37.0}^{(1.2)} \\ \textbf{28.2}^{(0.5)} \\ \textbf{14.5}^{(0.9)} \\ \textbf{20.7}^{(0.6)} \\ \textbf{21.3}^{(5.6)} \\ \textbf{34.9}^{(1.8)} \end{array}$	$\begin{array}{c} 65.1^{(14.4)}\\ 74.4^{(0.6)}\\ 59.3^{(10.9)}\\ \textbf{92.1}^{(0.0)}\\ \textbf{57.6}^{(13.2)}\\ 67.8^{(14.1)}\\ 68.9^{(15.9)}\\ \textbf{90.6}^{(0.0)}\\ 88.4^{(0.0)}\\ 88.4^{(0.0)}\\ 88.4^{(0.1)}\\ 70.9^{(0.7)}\\ 60.5^{(9.0)}\\ 70.9^{(1.8)}\\ \textbf{89.9}^{(1.0)}\\ 63.7^{(6.2)}\\ 46.0^{(11.7)}\\ \textbf{79.1}^{(0.7)}\\ \end{array}$	6.8 7.2 5.2 12.2 9.3 9.7 9.3 <u>6.5</u> 7.0 12.3 15.0 12.3 8.5 7.3	111 111 14 6. 9. 8. 12 133 15 8. 3. 6. 111 12 -6
Grad. BO-qUCB CMA-ES BONET DDOM ExPT MINs GTG Tri-Mentoring ICT PGS Match-Opt RGD COMs RoMA ROMO	$\begin{array}{c} \textbf{58.1}^{(\textbf{6.1})} \\ 50.3^{(1.8)} \\ 50.7^{(2.7)} \\ \textbf{53.1}^{(0.0)} \\ \textbf{55.9}^{(\textbf{0.7)}} \\ 44.7^{(6.8)} \\ 41.3^{(1.2)} \\ 43.4^{(0.3)} \\ 46.1^{(0.0)} \\ \textbf{59.5}^{(\textbf{3.0)}} \\ 40.7^{(2.6)} \\ 40.7^{(1.2)} \\ 41.1^{(1.3)} \\ 43.9^{(0.0)} \\ 50.1^{(4.3)} \\ \textbf{58.7}^{(\textbf{3.3)}} \\ 46.4^{(1.8)} \\ 47.0^{(2.8)} \end{array}$	$58.6^{(13.1)}$ $62.1^{(3.4)}$ $71.7^{(10.4)}$ $46.5^{(0.6)}$ $57.6^{(0.8)}$ $57.0^{(4.8)}$ $58.0^{(0.5)}$ $64.2^{(0.0)}$ $61.1^{(0.0)}$ $61.1^{(0.0)}$ $61.3^{(0.7)}$ $57.9^{(0.5)}$ $57.4^{(0.9)}$ $59.0^{(0.5)}$ $77.4^{(0.0)}$ $37.7^{(0.3)}$ $63.4^{(3.3)}$ $69.8^{(6.0)}$	59.3 ^(8.6) 63.3 ^(0.0) 63.3 ^(0.0) 6	85.3 ^(7.7) 86.6 ^(0.6) 83.9 ^(1.0) 91.2 ^(0.1) 83.4 ^(0.1) 89.8 ^(3.3) 83.1 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 83.2 ^(0.1) 86.4 ^(0.1) 93.2 ^(7.7) 84.7 ^(0.0) 61.8 ^(2.6) 86.3 ^(0.5) 85.9 ^(0.4)	$\begin{array}{c} \textbf{36.0}^{(6.7)} \\ \textbf{31.7}^{(1.2)} \\ \textbf{37.9}^{(0.0)} \\ \textbf{21.9}^{(1.7)} \\ \textbf{34.1}^{(12.3)} \\ \textbf{32.3}^{(1.6)} \\ \textbf{28.0}^{(0.0)} \\ \textbf{34.2}^{(1.2)} \\ \textbf{37.0}^{(1.2)} \\ \textbf{28.2}^{(0.5)} \\ \textbf{14.5}^{(0.9)} \\ \textbf{20.7}^{(0.6)} \\ \textbf{21.3}^{(5.6)} \\ \textbf{34.9}^{(1.8)} \\ \textbf{27.0}^{(0.6)} \\ \textbf{28.9}^{(1.1)} \\ \textbf{23.4}^{(8.5)} \end{array}$	$\begin{array}{c} 65.1^{(14.4)}\\ 74.4^{(0.6)}\\ 59.3^{(10.9)}\\ \textbf{92.1}^{(0.0)}\\ \textbf{57.6}^{(13.2)}\\ 67.8^{(14.1)}\\ 68.9^{(15.9)}\\ \textbf{90.6}^{(0.0)}\\ 88.4^{(0.0)}\\ 88.4^{(0.0)}\\ 88.4^{(0.1)}\\ 70.9^{(0.7)}\\ 60.5^{(9.0)}\\ 70.9^{(1.8)}\\ \textbf{89.9}^{(1.0)}\\ 63.7^{(6.2)}\\ 46.0^{(11.7)}\\ \textbf{79.1}^{(0.7)}\\ \textbf{68.7}^{(12.1)}\\ \end{array}$	$\begin{array}{c} 6.8 \\ 7.2 \\ \textbf{5.2} \\ 12.2 \\ 9.3 \\ 9.7 \\ 9.3 \\ \underline{6.5} \\ 7.0 \\ 12.3 \\ 15.0 \\ 12.3 \\ 8.5 \\ 7.3 \\ 15.8 \end{array}$	111 111 146 6 9 9 8 12 13 15 8 8 3 6 6 111 12 -6 11
Grad. BO-qUCB CMA-ES BONET DDOM ExPT MINs GTG Tri-Mentoring ICT PGS Match-Opt RGD COMs RoMA ROMO GAMBO	$\begin{array}{c} \textbf{58.1}^{\textbf{(6.1)}} \\ \textbf{50.3}^{(1.8)} \\ \textbf{50.7}^{(2.7)} \\ \textbf{53.1}^{(0.0)} \\ \textbf{55.9}^{\textbf{(0.7)}} \\ \textbf{44.7}^{(6.8)} \\ \textbf{41.3}^{(1.2)} \\ \textbf{43.4}^{(0.3)} \\ \textbf{46.1}^{(0.0)} \\ \textbf{59.5}^{\textbf{(3.0)}} \\ \textbf{40.7}^{(2.6)} \\ \textbf{40.7}^{(1.2)} \\ \textbf{41.1}^{(1.3)} \\ \textbf{43.9}^{(0.0)} \\ \textbf{50.1}^{(\textbf{4.3)}} \\ \textbf{58.7}^{\textbf{(3.3)}} \\ \textbf{46.4}^{(1.8)} \end{array}$	$58.6^{(13.1)} \\62.1^{(3.4)} \\71.7^{(10.4)} \\46.5^{(0.6)} \\57.6^{(0.8)} \\57.0^{(4.8)} \\58.0^{(0.5)} \\64.2^{(0.0)} \\61.1^{(0.0)} \\61.1^{(0.0)} \\61.3^{(0.7)} \\57.9^{(0.5)} \\57.4^{(0.9)} \\59.0^{(0.5)} \\77.4^{(0.0)} \\37.7^{(0.3)} \\63.4^{(3.3)} \\$	$\begin{array}{c} {\bf 59.3}^{(8.6)}\\ {\bf 63.3}^{(0.0)}\\ {\bf 57.1}^{(0.0)}\\ {\bf 58.4}^{(0.0)}\\ {\bf 63.3}^{(0.0)}\\ {\bf 63$	85.3 ^(7.7) 86.6 ^(0.6) 83.9 ^(1.0) 91.2 ^(0.1) 83.4 ^(0.1) 89.8 ^(3.3) 88.3 ^(0.3) 83.1 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 88.9 ^(0.0) 83.2 ^(0.1) 86.4 ^(0.1) 93.2 ^(7.7) 84.7 ^(0.0) 61.8 ^(2.6) 86.3 ^(0.5)	$\begin{array}{c} \textbf{36.0}^{(6.7)} \\ \textbf{31.7}^{(1.2)} \\ \textbf{37.9}^{(0.0)} \\ \textbf{21.9}^{(1.7)} \\ \textbf{34.1}^{(12.3)} \\ \textbf{32.3}^{(1.6)} \\ \textbf{28.0}^{(0.0)} \\ \textbf{34.2}^{(1.2)} \\ \textbf{37.0}^{(1.2)} \\ \textbf{28.2}^{(0.5)} \\ \textbf{14.5}^{(0.9)} \\ \textbf{20.7}^{(0.6)} \\ \textbf{21.3}^{(5.6)} \\ \textbf{34.9}^{(1.8)} \\ \textbf{27.0}^{(0.6)} \\ \textbf{28.9}^{(1.1)} \end{array}$	$\begin{array}{c} 65.1^{(14.4)}\\ 74.4^{(0.6)}\\ 59.3^{(10.9)}\\ \textbf{92.1}^{(0.0)}\\ \textbf{57.6}^{(13.2)}\\ 67.8^{(14.1)}\\ 68.9^{(15.9)}\\ \textbf{90.6}^{(0.0)}\\ 88.4^{(0.0)}\\ 88.4^{(0.0)}\\ 88.4^{(0.1)}\\ 70.9^{(0.7)}\\ 60.5^{(9.0)}\\ 70.9^{(1.8)}\\ \textbf{89.9}^{(1.0)}\\ 63.7^{(6.2)}\\ 46.0^{(11.7)}\\ \textbf{79.1}^{(0.7)}\\ \end{array}$	$\begin{array}{c} 6.8 \\ 7.2 \\ \textbf{5.2} \\ 12.2 \\ 9.3 \\ 9.7 \\ 9.3 \\ \underline{6.5} \\ 7.0 \\ 12.3 \\ 15.0 \\ 12.3 \\ 8.5 \\ 7.3 \\ 15.8 \\ 7.8 \end{array}$	

Table A7. Comparison of Design Diversity Against Model-Free Optimization Methods. We evaluate DynAMO and other model-based optimization methods against model-free optimization methods. We report the pairwise diversity (resp., minimum novelty) oracle score achieved by the 128 evaluated designs in the top (resp., bottom) table. Metrics are reported mean^(95% confidence interval) across 10 random seeds, where higher is better. All metrics are multiplied by 100 for easier legibility. Bolded entries indicate average scores with an overlapping 95% confidence interval to the best performing method. Bolded (resp., Underlined) Rank and Optimality Gap (Opt. Gap) metrics indicate the best (resp., second best) for a given backbone optimizer.

Pairwise Diversity@128	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	Rank ↓	Opt. Gap
Dataset \mathcal{D}	65.9	57.3	60.0	36.7	66.0	85.7	_	
Grad.	12.5(8.0)	7.8 ^(8.8)	7.9 ^(7.8)	24.1(13.3)	$0.0^{(0.0)}$	$0.0^{(0.0)}$	18.7	-53.2
BO-qUCB	73.9 ^(0.5)	74.3 ^(0.4)	99.4 ^(0.1)	93.6 ^(0.5)	198 ^(10.3)	94.1 ^(3.9)	3.8	43.5
CMA-ES	47.2 ^(11.2)	44.6 ^(15.9)	93.5 ^(2.0)	$66.2^{(9.4)}$	$12.8^{(0.6)}$	$164^{(10.6)}$	10.8	9.5
BONET	46.7 ^(2.5)	$24.6^{(0.4)}$	$14.9^{(1.6)}$	5.5 ^(0.2)	$0.2^{(0.0)}$	$0.1^{(0.0)}$	17.3	-46.6
DDOM	51.3 ^(1.0)	$47.1^{(0.3)}$	$21.9^{(3.6)}$	97.2 ^(0.0)	$1.9^{(0.1)}$	50.7 ^(13.1)	12.5	-16.9
ExPT	$15.3^{(5.6)}$	$16.5^{(1.6)}$	$21.3^{(1.8)}$	5.3 ^(0.7)	8 1 ^(2.3)	$0.2^{(0.0)}$	17.5	-50.8
MINs	$67.0^{(0.3)}$	56.8 ^(0.4)	53.5 ^(3.1)	34.1 ^(2.6)	84.6 ^(21.1)	$4.3^{(0.3)}$	11.8	-11.9
GTG	$60.9^{(0.0)}$	$44.6^{(0.0)}$	$2.8^{(0.0)}$	$0.9^{(0.0)}$	$114.8^{(0.1)}$	$2.7^{(0.0)}$	15.0	-24.2
Tri-Mentoring	58.5 ^(0.0)	57.6 ^(0.0)	85.5 ^(0.0)	39.9 ^(0.0)	47.7 ^(0.0)	62.5 ^(0.0)	10.5	-24.2
ICT	$44.8^{(6.0)}$	57.5 ^(0.0)	89.9 ^(1.8)	70.3 ^(8.6)	78.9 ^(3.7)	$164^{(0.8)}$	9.3	22.3
	44.8 $65.8^{(1.6)}$	$57.3^{(0.3)}$	$63.2^{(0.0)}$	39.9 ^(0.0)	36.7 ^(0.6)	$164^{(0.7)}$		8.9
PGS	65.1 ^(0.4)	57.4 ^(0.1)	99.8 ^(0.0)	97.2 ^(0.0)	10.9 ^(0.4)	$202^{(0.5)}$	10.5	
Match-Opt	$65.1^{(0.2)}$	55.9(02)	99.8 ^(0.0) 99.8 ^(0.0)	97.2 ^(0.0) 97.3 ^(0.0)	88.4 ^(3.8)	202 ^(0.7) 76.2 ^(0.7)	7.5	26.6
RGD	$67.1^{(0.2)}$	$58.4^{(0.2)}$			$88.4^{(3.3)}$	76.2(0.7)	5.0	19.3
COMs	66.6 ^(1.0)	57.4 ^(0.2)	81.6 ^(4.9)	3.8 ^(0.9)	99.5 ^(25.8)	$21.1^{(23.5)}$	10.7	-6.9
RoMA	21.3(0.3)	3.8 ^(0.0)	5.9 ^(0.2)	$1.8^{(0.0)}$	49.4 ^(6.1)	$14.8^{(0.6)}$	17.2	-45.8
ROMO	$62.1^{(0.8)}$	$57.1^{(0.1)}$	53.9 ^(0.6)	48.7 ^(0.1)	51.7(31.7)	$22.1^{(5.5)}$	11.5	-12.7
GAMBO	74.0 ^(0.6)	74.3 ^(0.4)	99.3 ^(0.1)	93.3 ^(0.4)	193 ^(1.2)	17.7 ^(3.5)	5.5	30.0
DynAMO-Grad.	66.9(6.9)	68.2 ^(10.8)	77.2(21.5)	93.0 ^(1.2)	129(55.3)	104(56.1)	6.8	27.8
DynAMO-BO-qUCB	74.3 ^(0.5)	74.4 ^(0.6)	99.3 ^(0.1)	93.5 ^(0.6)	211 ^(22.8)	175 ^(44.7)	2.8	59.4
DynAMO-CMA-ES	73.6 ^(0.6)	73.1 ^(3.1)	72.0 ^(3.1)	94.0 ^(0.5)	97.8 ^(13.2)	292 ^(83.5)	5.2	<u>55.2</u>
Minimum Novelty@128	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	Rank ↓	Opt. Ga
Dataset \mathcal{D}	0.0	0.0	0.0	0.0	0.0	0.0		
Grad.	21.2(3.0)	51.7 ^(2.9)	97.4 ^(3.9)	79.5(19.7)	95 ^(0.7)	102.2(6.1)	5.8	74.5
BO-qUCB	21.2 $21.6^{(0.3)}$	51.7 ^(0.2)	97.9 ^(0.4)	85.3 ^(1.1)	93.8 ^(0.6)	98.8 ^(1.1)	6.0	74.8
CMA-ES	$16.5^{(2.1)}$	$47.8^{(1.0)}$	97.9 96.5 ^(0.7)	73.0 ^(18.0)	100 ^(0.0)	$100^{(0.0)}$	0.0 7.8	74.8
	10.5	47.0	90.5		100	100	1.0	
DONET	$0.4 c^{(1.3)}$	200(0.1)	$A1 2^{(0.3)}$	10 2(0.1)	1 2(0.0)	1 1 (0.0)	147	21.2
BONET	94.6 ^(1.3)	$38.8^{(0.1)}$	$41.2^{(0.3)}$	$10.3^{(0.1)}$	$1.3^{(0.0)}$	$1.1^{(0.0)}$	14.7	31.2
DDOM	$11.1^{(0.4)}$	$38.6^{(0.1)}$	96.5 ^(0.9)	$94.2^{(0.1)}$	98.0 ^(0.1)	$100^{(0.0)}$	9.3	73.1
DDOM ExPT	$11.1^{(0.4)} \\ 11.1^{(1.6)}$	$38.6^{(0.1)}$ $39.0^{(0.7)}$	96.5 ^(0.9) 54.2 ^(2.0)	94.2 ^(0.1) 15.6 ^(1.2)	98.0 ^(0.1) 69.8 ^(6.8)	$100^{(0.0)}$ 3.5 ^(0.9)	9.3 15.2	73.1 32.2
DDOM ExPT MINs	$11.1^{(0.4)} \\ 11.1^{(1.6)} \\ 12.2^{(0.4)}$	38.6 ^(0.1) 39.0 ^(0.7) 38.3 ^(0.2)	$96.5^{(0.9)} \\ 54.2^{(2.0)} \\ 48.7^{(2.9)}$	$94.2^{(0.1)} \\ 15.6^{(1.2)} \\ 22.1^{(1.7)}$	$98.0^{(0.1)} \\ 69.8^{(6.8)} \\ 6.1^{(1.1)}$	$100^{(0.0)} \\ 3.5^{(0.9)} \\ 0.6^{(0.1)}$	9.3 15.2 16.5	73.1 32.2 21.3
DDOM ExPT MINs GTG	$11.1^{(0.4)} \\ 11.1^{(1.6)} \\ 12.2^{(0.4)} \\ 13.8^{(0.0)}$	$38.6^{(0.1)} 39.0^{(0.7)} 38.3^{(0.2)} 37.8^{(0.0)}$	96.5 ^(0.9) 54.2 ^(2.0) 48.7 ^(2.9) 99.3^(0.0)	94.2 ^(0.1) 15.6 ^(1.2) 22.1 ^(1.7) 99.4^(0.0)	$98.0^{(0.1)} \\ 69.8^{(6.8)} \\ 6.1^{(1.1)} \\ 67.7^{(0.0)}$	$100^{(0.0)} \\ 3.5^{(0.9)} \\ 0.6^{(0.1)} \\ 0.2^{(0.0)}$	9.3 15.2 16.5 10.5	73.1 32.2 21.3 53.0
DDOM ExPT MINs GTG Tri-Mentoring	$11.1^{(0.4)} \\ 11.1^{(1.6)} \\ 12.2^{(0.4)} \\ 13.8^{(0.0)} \\ 13.9^{(0.0)}$	$38.6^{(0.1)} 39.0^{(0.7)} 38.3^{(0.2)} 37.8^{(0.0)} 31.8^{(0.0)}$	96.5 ^(0.9) 54.2 ^(2.0) 48.7 ^(2.9) 99.3^(0.0) 74.7 ^(0.0)	$94.2^{(0.1)}$ $15.6^{(1.2)}$ $22.1^{(1.7)}$ $99.4^{(0.0)}$ $75.5^{(0.0)}$	$98.0^{(0.1)} \\ 69.8^{(6.8)} \\ 6.1^{(1.1)} \\ 67.7^{(0.0)} \\ 44.0^{(0.0)}$	$100^{(0.0)} \\ 3.5^{(0.9)} \\ 0.6^{(0.1)} \\ 0.2^{(0.0)} \\ 64.3^{(0.0)}$	9.3 15.2 16.5 10.5 14.3	73.1 32.2 21.3 53.0 50.7
DDOM ExPT MINs GTG Tri-Mentoring ICT	$11.1^{(0.4)} \\ 11.1^{(1.6)} \\ 12.2^{(0.4)} \\ 13.8^{(0.0)} \\ 13.9^{(0.0)} \\ 19.3^{(1.2)}$	$38.6^{(0.1)} 39.0^{(0.7)} 38.3^{(0.2)} 37.8^{(0.0)} 31.8^{(0.0)} 31.7^{(0.1)}$	$96.5^{(0.9)} \\ 54.2^{(2.0)} \\ 48.7^{(2.9)} \\ 99.3^{(0.0)} \\ 74.7^{(0.0)} \\ 70.8^{(0.4)}$	94.2 ^(0.1) 15.6 ^(1.2) 22.1 ^(1.7) 99.4^(0.0) 75.5 ^(0.0) 75.6 ^(0.0)	$98.0^{(0.1)}$ $69.8^{(6.8)}$ $6.1^{(1.1)}$ $67.7^{(0.0)}$ $44.0^{(0.0)}$ $46.2^{(0.4)}$	$100^{(0.0)} \\ 3.5^{(0.9)} \\ 0.6^{(0.1)} \\ 0.2^{(0.0)} \\ 64.3^{(0.0)} \\ 66.2^{(0.7)}$	9.3 15.2 16.5 10.5 14.3 13.2	73.1 32.2 21.3 53.0 50.7 51.6
DDOM ExPT MINs GTG Tri-Mentoring ICT PGS	$11.1^{(0.4)} \\ 11.1^{(1.6)} \\ 12.2^{(0.4)} \\ 13.8^{(0.0)} \\ 13.9^{(0.0)} \\ 19.3^{(1.2)} \\ 11.5^{(0.4)} $	$\begin{array}{c} 38.6^{(0.1)}\\ 39.0^{(0.7)}\\ 38.3^{(0.2)}\\ 37.8^{(0.0)}\\ 31.8^{(0.0)}\\ 31.7^{(0.1)}\\ 33.1^{(1.8)} \end{array}$	$96.5^{(0.9)}$ $54.2^{(2.0)}$ $48.7^{(2.9)}$ $99.3^{(0.0)}$ $74.7^{(0.0)}$ $70.8^{(0.4)}$ $16.0^{(0.0)}$	94.2 ^(0.1) 15.6 ^(1.2) 22.1 ^(1.7) 99.4^(0.0) 75.5 ^(0.0) 75.6 ^(0.0) 15.8 ^(0.0)	$98.0^{(0.1)} \\ 69.8^{(6.8)} \\ 6.1^{(1.1)} \\ 67.7^{(0.0)} \\ 44.0^{(0.0)} \\ 46.2^{(0.4)} \\ 45.0^{(0.2)} \\ \end{cases}$	$100^{(0.0)} \\ 3.5^{(0.9)} \\ 0.6^{(0.1)} \\ 0.2^{(0.0)} \\ 64.3^{(0.0)} \\ 66.2^{(0.7)} \\ 74.8^{(1.1)}$	9.3 15.2 16.5 10.5 14.3 13.2 16.3	73.1 32.2 21.3 53.0 50.7 51.6 32.7
DDOM ExPT MINs GTG Tri-Mentoring ICT PGS Match-Opt	$11.1^{(0.4)} \\ 11.1^{(1.6)} \\ 12.2^{(0.4)} \\ 13.8^{(0.0)} \\ 13.9^{(0.0)} \\ 19.3^{(1.2)} \\ 11.5^{(0.4)} \\ 12.1^{(0.5)} $	$\begin{array}{c} 38.6^{(0.1)}\\ 39.0^{(0.7)}\\ 38.3^{(0.2)}\\ 37.8^{(0.0)}\\ 31.8^{(0.0)}\\ 31.7^{(0.1)}\\ 33.1^{(1.8)}\\ 40.0^{(0.1)} \end{array}$	$96.5^{(0.9)}$ $54.2^{(2.0)}$ $48.7^{(2.9)}$ $99.3^{(0.0)}$ $74.7^{(0.0)}$ $70.8^{(0.4)}$ $16.0^{(0.0)}$ $98.5^{(0.1)}$	94.2 ^(0.1) 15.6 ^(1.2) 22.1 ^(1.7) 99.4^(0.0) 75.5 ^(0.0) 75.6 ^(0.0) 15.8 ^(0.0) 94.9 ^(0.1)	$98.0^{(0.1)} \\ 69.8^{(6.8)} \\ 6.1^{(1.1)} \\ 67.7^{(0.0)} \\ 44.0^{(0.0)} \\ 46.2^{(0.4)} \\ 45.0^{(0.2)} \\ 91.9^{(0.1)} \\ \end{cases}$	$100^{(0.0)} \\ 3.5^{(0.9)} \\ 0.6^{(0.1)} \\ 0.2^{(0.0)} \\ 64.3^{(0.0)} \\ 66.2^{(0.7)} \\ 74.8^{(1.1)} \\ 85.8^{(2.6)} \\ \end{cases}$	9.3 15.2 16.5 10.5 14.3 13.2 16.3 8.7	73.1 32.2 21.3 53.0 50.7 51.6 32.7 70.5
DDOM ExPT MINs GTG Tri-Mentoring ICT PGS Match-Opt RGD	$11.1^{(0.4)}$ $11.1^{(1.6)}$ $12.2^{(0.4)}$ $13.8^{(0.0)}$ $13.9^{(0.0)}$ $19.3^{(1.2)}$ $11.5^{(0.4)}$ $12.1^{(0.5)}$ $12.3^{(0.5)}$	$\begin{array}{c} 38.6^{(0.1)}\\ 39.0^{(0.7)}\\ 38.3^{(0.2)}\\ 37.8^{(0.0)}\\ 31.8^{(0.0)}\\ 31.7^{(0.1)}\\ 33.1^{(1.8)}\\ 40.0^{(0.1)}\\ 39.0^{(0.2)} \end{array}$	$96.5^{(0.9)}$ $54.2^{(2.0)}$ $48.7^{(2.9)}$ $99.3^{(0.0)}$ $74.7^{(0.0)}$ $70.8^{(0.4)}$ $16.0^{(0.0)}$ $98.5^{(0.1)}$	$94.2^{(0.1)}$ $15.6^{(1.2)}$ $22.1^{(1.7)}$ $99.4^{(0.0)}$ $75.5^{(0.0)}$ $75.6^{(0.0)}$ $15.8^{(0.0)}$ $94.9^{(0.1)}$ $94.2^{(0.1)}$	$98.0^{(0.1)} \\ 69.8^{(6.8)} \\ 6.1^{(1.1)} \\ 67.7^{(0.0)} \\ 44.0^{(0.0)} \\ 46.2^{(0.4)} \\ 45.0^{(0.2)} \\ 91.9^{(0.1)} \\ 90.4^{(0.3)} \\ \end{cases}$	$100^{(0.0)} \\ 3.5^{(0.9)} \\ 0.6^{(0.1)} \\ 0.2^{(0.0)} \\ 64.3^{(0.0)} \\ 66.2^{(0.7)} \\ 74.8^{(1.1)} \\ 85.8^{(2.6)} \\ 90.5^{(2.3)} \\ \end{cases}$	9.3 15.2 16.5 10.5 14.3 13.2 16.3 8.7 8.5	73.1 32.2 21.3 53.0 50.7 51.6 32.7 70.5 70.9
DDOM ExPT MINs GTG Tri-Mentoring ICT PGS Match-Opt RGD COMs	$11.1^{(0.4)}$ $11.1^{(1.6)}$ $12.2^{(0.4)}$ $13.8^{(0.0)}$ $13.9^{(0.0)}$ $19.3^{(1.2)}$ $11.5^{(0.4)}$ $12.1^{(0.5)}$ $12.3^{(0.5)}$ $10.9^{(0.3)}$	$\begin{array}{c} 38.6^{(0.1)}\\ 39.0^{(0.7)}\\ 38.3^{(0.2)}\\ 37.8^{(0.0)}\\ 31.8^{(0.0)}\\ 31.7^{(0.1)}\\ 33.1^{(1.8)}\\ 40.0^{(0.1)}\\ 39.0^{(0.2)}\\ 31.7^{(0.8)} \end{array}$	$96.5^{(0.9)} \\ 54.2^{(2.0)} \\ 48.7^{(2.9)} \\ 99.3^{(0.0)} \\ 74.7^{(0.0)} \\ 70.8^{(0.4)} \\ 16.0^{(0.0)} \\ 98.5^{(0.1)} \\ 98.6^{(0.1)} \\ 52.4^{(11.0)}$	$\begin{array}{c} 94.2^{(0.1)}\\ 15.6^{(1.2)}\\ 22.1^{(1.7)}\\ \textbf{99.4^{(0.0)}}\\ 75.5^{(0.0)}\\ 75.6^{(0.0)}\\ 15.8^{(0.0)}\\ 94.9^{(0.1)}\\ 94.2^{(0.1)}\\ 13.7^{(1.1)} \end{array}$	$98.0^{(0.1)} \\ 69.8^{(6.8)} \\ 6.1^{(1.1)} \\ 67.7^{(0.0)} \\ 44.0^{(0.0)} \\ 46.2^{(0.4)} \\ 45.0^{(0.2)} \\ 91.9^{(0.1)} \\ 90.4^{(0.3)} \\ 99.6^{(0.3)} \\ \end{cases}$	$\begin{array}{c} 100^{(0.0)}\\ 3.5^{(0.9)}\\ 0.6^{(0.1)}\\ 0.2^{(0.0)}\\ 64.3^{(0.0)}\\ 66.2^{(0.7)}\\ 74.8^{(1.1)}\\ 85.8^{(2.6)}\\ 90.5^{(2.3)}\\ 100^{(0.0)} \end{array}$	9.3 15.2 16.5 10.5 14.3 13.2 16.3 8.7 8.5 14.0	73.1 32.2 21.3 53.0 50.7 51.6 32.7 70.5 70.9 51.4
DDOM ExPT MINs GTG Tri-Mentoring ICT PGS Match-Opt RGD	$11.1^{(0.4)}$ $11.1^{(1.6)}$ $12.2^{(0.4)}$ $13.8^{(0.0)}$ $13.9^{(0.0)}$ $19.3^{(1.2)}$ $11.5^{(0.4)}$ $12.1^{(0.5)}$ $12.3^{(0.5)}$ $10.9^{(0.3)}$ $18.3^{(0.5)}$	$\begin{array}{c} 38.6^{(0.1)}\\ 39.0^{(0.7)}\\ 38.3^{(0.2)}\\ 37.8^{(0.0)}\\ 31.8^{(0.0)}\\ 31.7^{(0.1)}\\ 33.1^{(1.8)}\\ 40.0^{(0.1)}\\ 39.0^{(0.2)}\\ 31.7^{(0.8)}\\ 40.1^{(0.2)} \end{array}$	$96.5^{(0.9)} \\ 54.2^{(2.0)} \\ 48.7^{(2.9)} \\ 99.3^{(0.0)} \\ 74.7^{(0.0)} \\ 70.8^{(0.4)} \\ 16.0^{(0.0)} \\ 98.5^{(0.1)} \\ 98.6^{(0.1)} \\ 52.4^{(11.0)} \\ 18.9^{(0.2)} \\ \end{cases}$	$\begin{array}{c} 94.2^{(0.1)}\\ 15.6^{(1.2)}\\ 22.1^{(1.7)}\\ \textbf{99.4^{(0.0)}}\\ 75.5^{(0.0)}\\ 75.6^{(0.0)}\\ 15.8^{(0.0)}\\ 94.9^{(0.1)}\\ 94.2^{(0.1)}\\ 13.7^{(1.1)}\\ 95.3^{(0.0)} \end{array}$	$98.0^{(0.1)} \\ 69.8^{(6.8)} \\ 6.1^{(1.1)} \\ 67.7^{(0.0)} \\ 44.0^{(0.0)} \\ 46.2^{(0.4)} \\ 45.0^{(0.2)} \\ 91.9^{(0.1)} \\ 90.4^{(0.3)} \\ 99.6^{(0.3)} \\ 47.6^{(2.4)} \\$	$\begin{array}{c} 100^{(0.0)}\\ 3.5^{(0.9)}\\ 0.6^{(0.1)}\\ 0.2^{(0.0)}\\ 64.3^{(0.0)}\\ 66.2^{(0.7)}\\ 74.8^{(1.1)}\\ 85.8^{(2.6)}\\ 90.5^{(2.3)}\\ 100^{(0.0)}\\ 5.1^{(0.2)} \end{array}$	9.3 15.2 16.5 10.5 14.3 13.2 16.3 8.7 8.5 14.0 11.0	73.1 32.2 21.3 53.0 50.7 51.6 32.7 70.5 70.9 51.4 37.6
DDOM ExPT MINs GTG Tri-Mentoring ICT PGS Match-Opt RGD COMs	$11.1^{(0.4)}$ $11.1^{(1.6)}$ $12.2^{(0.4)}$ $13.8^{(0.0)}$ $13.9^{(0.0)}$ $19.3^{(1.2)}$ $11.5^{(0.4)}$ $12.1^{(0.5)}$ $12.3^{(0.5)}$ $10.9^{(0.3)}$ $18.3^{(0.5)}$ $16.1^{(0.5)}$	$\begin{array}{c} 38.6^{(0.1)}\\ 39.0^{(0.7)}\\ 38.3^{(0.2)}\\ 37.8^{(0.0)}\\ 31.8^{(0.0)}\\ 31.7^{(0.1)}\\ 33.1^{(1.8)}\\ 40.0^{(0.1)}\\ 39.0^{(0.2)}\\ 31.7^{(0.8)}\\ 40.1^{(0.2)}\\ 32.9^{(0.1)} \end{array}$	$96.5^{(0.9)} \\ 54.2^{(2.0)} \\ 48.7^{(2.9)} \\ 99.3^{(0.0)} \\ 74.7^{(0.0)} \\ 70.8^{(0.4)} \\ 16.0^{(0.0)} \\ 98.5^{(0.1)} \\ 98.6^{(0.1)} \\ 52.4^{(11.0)} \\ 18.9^{(0.2)} \\ 5.0^{(0.7)} \\ \end{cases}$	$\begin{array}{c} 94.2^{(0.1)}\\ 15.6^{(1.2)}\\ 22.1^{(1.7)}\\ \textbf{99.4^{(0.0)}}\\ 75.5^{(0.0)}\\ 75.6^{(0.0)}\\ 15.8^{(0.0)}\\ 94.9^{(0.1)}\\ 94.2^{(0.1)}\\ 13.7^{(1.1)}\\ 95.3^{(0.0)}\\ 23.1^{(0.0)} \end{array}$	$\begin{array}{c} 98.0^{(0.1)} \\ 69.8^{(6.8)} \\ 6.1^{(1.1)} \\ 67.7^{(0.0)} \\ 44.0^{(0.0)} \\ 46.2^{(0.4)} \\ 45.0^{(0.2)} \\ 91.9^{(0.1)} \\ 90.4^{(0.3)} \\ 99.6^{(0.3)} \\ 47.6^{(2.4)} \\ 78.5^{(0.5)} \end{array}$	$\begin{array}{c} 100^{(0.0)}\\ 3.5^{(0.9)}\\ 0.6^{(0.1)}\\ 0.2^{(0.0)}\\ 64.3^{(0.0)}\\ 66.2^{(0.7)}\\ 74.8^{(1.1)}\\ 85.8^{(2.6)}\\ 90.5^{(2.3)}\\ 100^{(0.0)}\\ 5.1^{(0.2)}\\ 153.3^{(0.4)} \end{array}$	9.3 15.2 16.5 10.5 14.3 13.2 16.3 8.7 8.5 14.0	73.1 32.2 21.3 53.0 50.7 51.6 32.7 70.5 70.9 51.4
DDOM ExPT MINs GTG Tri-Mentoring ICT PGS Match-Opt RGD COMs RoMA	$11.1^{(0.4)} \\ 11.1^{(1.6)} \\ 12.2^{(0.4)} \\ 13.8^{(0.0)} \\ 13.9^{(0.0)} \\ 19.3^{(1.2)} \\ 11.5^{(0.4)} \\ 12.1^{(0.5)} \\ 12.3^{(0.5)} \\ 10.9^{(0.3)} \\ 18.3^{(0.5)} \\ 16.1^{(0.5)} \\ 15.4^{(0.3)} \\ 15.4^{(0.3)} \\ 10.0000000000000000000000000000000000$	$\begin{array}{c} 38.6^{(0.1)}\\ 39.0^{(0.7)}\\ 38.3^{(0.2)}\\ 37.8^{(0.0)}\\ 31.8^{(0.0)}\\ 31.7^{(0.1)}\\ 33.1^{(1.8)}\\ 40.0^{(0.1)}\\ 39.0^{(0.2)}\\ 31.7^{(0.8)}\\ 40.1^{(0.2)} \end{array}$	$\begin{array}{c} 96.5^{(0.9)} \\ 54.2^{(2.0)} \\ 48.7^{(2.9)} \\ \textbf{99.3}^{(0.0)} \\ 74.7^{(0.0)} \\ 70.8^{(0.4)} \\ 16.0^{(0.0)} \\ 98.5^{(0.1)} \\ 98.6^{(0.1)} \\ 52.4^{(11.0)} \\ 18.9^{(0.2)} \\ 5.0^{(0.7)} \\ \textbf{97.8}^{(0.3)} \end{array}$	$\begin{array}{c} 94.2^{(0.1)}\\ 15.6^{(1.2)}\\ 22.1^{(1.7)}\\ \textbf{99.4^{(0.0)}}\\ 75.5^{(0.0)}\\ 75.6^{(0.0)}\\ 15.8^{(0.0)}\\ 94.9^{(0.1)}\\ 94.2^{(0.1)}\\ 13.7^{(1.1)}\\ 95.3^{(0.0)}\\ 23.1^{(0.0)}\\ 84.9^{(0.9)}\\ \end{array}$	$98.0^{(0.1)} \\ 69.8^{(6.8)} \\ 6.1^{(1.1)} \\ 67.7^{(0.0)} \\ 44.0^{(0.0)} \\ 46.2^{(0.4)} \\ 45.0^{(0.2)} \\ 91.9^{(0.1)} \\ 90.4^{(0.3)} \\ 99.6^{(0.3)} \\ 47.6^{(2.4)} \\$	$\begin{array}{c} 100^{(0.0)}\\ 3.5^{(0.9)}\\ 0.6^{(0.1)}\\ 0.2^{(0.0)}\\ 64.3^{(0.0)}\\ 66.2^{(0.7)}\\ 74.8^{(1.1)}\\ 85.8^{(2.6)}\\ 90.5^{(2.3)}\\ 100^{(0.0)}\\ 5.1^{(0.2)} \end{array}$	9.3 15.2 16.5 10.5 14.3 13.2 16.3 8.7 8.5 14.0 11.0	73.1 32.2 21.3 53.0 50.7 51.6 32.7 70.5 70.9 51.4 37.6
DDOM ExPT MINs GTG Tri-Mentoring ICT PGS Match-Opt RGD COMs RoMA ROMO	$\begin{array}{c} 11.1^{(0.4)}\\ 11.1^{(1.6)}\\ 12.2^{(0.4)}\\ 13.8^{(0.0)}\\ 13.9^{(0.0)}\\ 19.3^{(1.2)}\\ 11.5^{(0.4)}\\ 12.1^{(0.5)}\\ 12.3^{(0.5)}\\ 10.9^{(0.3)}\\ 18.3^{(0.5)}\\ 16.1^{(0.5)}\\ 15.4^{(0.3)}\\ \end{array}$	$\begin{array}{r} 38.6^{(0.1)}\\ 39.0^{(0.7)}\\ 38.3^{(0.2)}\\ 37.8^{(0.0)}\\ 31.8^{(0.0)}\\ 31.7^{(0.1)}\\ 33.1^{(1.8)}\\ 40.0^{(0.1)}\\ 39.0^{(0.2)}\\ 31.7^{(0.8)}\\ 40.1^{(0.2)}\\ 32.9^{(0.1)}\\ 51.8^{(0.2)}\\ \end{array}$	96.5 ^(0.9) 54.2 ^(2.0) 48.7 ^(2.9) 99.3^(0.0) 74.7 ^(0.0) 70.8 ^(0.4) 16.0 ^(0.0) 98.5 ^(0.1) 98.6 ^(0.1) 52.4 ^(11.0) 18.9 ^(0.2) 5.0 ^(0.7) 97.8 ^(0.3) 98.6^(1.5)	94.2 ^(0.1) 15.6 ^(1.2) 22.1 ^(1.7) 99.4^(0.0) 75.5 ^(0.0) 75.6 ^(0.0) 15.8 ^(0.0) 94.9 ^(0.1) 94.2 ^(0.1) 13.7 ^(1.1) 95.3 ^(0.0) 23.1 ^(0.0) 84.9 ^(0.9)	$\begin{array}{c} 98.0^{(0.1)} \\ 69.8^{(6.8)} \\ 6.1^{(1.1)} \\ 67.7^{(0.0)} \\ 44.0^{(0.0)} \\ 46.2^{(0.4)} \\ 45.0^{(0.2)} \\ 91.9^{(0.1)} \\ 90.4^{(0.3)} \\ 99.6^{(0.3)} \\ 47.6^{(2.4)} \\ 78.5^{(0.5)} \\ 85.1^{(0.4)} \\ \hline \end{array}$	$\begin{array}{c} 100^{(0.0)}\\ 3.5^{(0.9)}\\ 0.6^{(0.1)}\\ 0.2^{(0.0)}\\ 64.3^{(0.0)}\\ 66.2^{(0.7)}\\ 74.8^{(1.1)}\\ 85.8^{(2.6)}\\ 90.5^{(2.3)}\\ 100^{(0.0)}\\ 5.1^{(0.2)}\\ 153.3^{(0.4)} \end{array}$	9.3 15.2 16.5 10.5 14.3 13.2 16.3 8.7 8.5 14.0 11.0 12.3	73.1 32.2 21.3 53.0 50.7 51.6 32.7 70.5 70.9 51.4 37.6 51.5
DDOM ExPT MINs GTG Tri-Mentoring ICT PGS Match-Opt RGD COMs RoMA ROMO GAMBO	$11.1^{(0.4)} \\ 11.1^{(1.6)} \\ 12.2^{(0.4)} \\ 13.8^{(0.0)} \\ 13.9^{(0.0)} \\ 19.3^{(1.2)} \\ 11.5^{(0.4)} \\ 12.1^{(0.5)} \\ 12.3^{(0.5)} \\ 10.9^{(0.3)} \\ 18.3^{(0.5)} \\ 16.1^{(0.5)} \\ 15.4^{(0.3)} \\ 15.4^{(0.3)} \\ 10.0000000000000000000000000000000000$	$\begin{array}{c} 38.6^{(0.1)}\\ 39.0^{(0.7)}\\ 38.3^{(0.2)}\\ 37.8^{(0.0)}\\ 31.8^{(0.0)}\\ 31.7^{(0.1)}\\ 33.1^{(1.8)}\\ 40.0^{(0.1)}\\ 39.0^{(0.2)}\\ 31.7^{(0.8)}\\ 40.1^{(0.2)}\\ 32.9^{(0.1)}\\ 51.8^{(0.2)} \end{array}$	$96.5^{(0.9)} \\ 54.2^{(2.0)} \\ 48.7^{(2.9)} \\ 99.3^{(0.0)} \\ 74.7^{(0.0)} \\ 70.8^{(0.4)} \\ 16.0^{(0.0)} \\ 98.5^{(0.1)} \\ 98.6^{(0.1)} \\ 52.4^{(11.0)} \\ 18.9^{(0.2)} \\ 5.0^{(0.7)} \\ \end{cases}$	$\begin{array}{c} 94.2^{(0.1)}\\ 15.6^{(1.2)}\\ 22.1^{(1.7)}\\ \textbf{99.4^{(0.0)}}\\ 75.5^{(0.0)}\\ 75.6^{(0.0)}\\ 15.8^{(0.0)}\\ 94.9^{(0.1)}\\ 94.2^{(0.1)}\\ 13.7^{(1.1)}\\ 95.3^{(0.0)}\\ 23.1^{(0.0)} \end{array}$	$\begin{array}{c} 98.0^{(0.1)} \\ 69.8^{(6.8)} \\ 6.1^{(1.1)} \\ 67.7^{(0.0)} \\ 44.0^{(0.0)} \\ 46.2^{(0.4)} \\ 45.0^{(0.2)} \\ 91.9^{(0.1)} \\ 90.4^{(0.3)} \\ 99.6^{(0.3)} \\ 47.6^{(2.4)} \\ 78.5^{(0.5)} \\ 85.1^{(0.4)} \end{array}$	$\begin{array}{c} 100^{(0.0)}\\ 3.5^{(0.9)}\\ 0.6^{(0.1)}\\ 0.2^{(0.0)}\\ 64.3^{(0.0)}\\ 66.2^{(0.7)}\\ 74.8^{(1.1)}\\ 85.8^{(2.6)}\\ 90.5^{(2.3)}\\ 100^{(0.0)}\\ 5.1^{(0.2)}\\ \textbf{153.3^{(0.4)}}\\ 14.3^{(1.5)} \end{array}$	9.3 15.2 16.5 10.5 14.3 13.2 16.3 8.7 8.5 14.0 11.0 12.3 8.8	73.1 32.2 21.3 53.0 50.7 51.6 32.7 70.5 70.9 51.4 37.6 51.5 58.2

Table A8. **Comparison of Design Diversity Against Model-Free Optimization Methods (cont.).** We evaluate DynAMO and other 2160 model-based optimization methods against model-free optimization methods. We report the L_1 coverage score achieved by the 128 2161 evaluated designs. Metrics are reported mean^(95% confidence interval) across 10 random seeds, where higher is better. All metrics are multiplied 2162 by 100 for easier legibility. **Bolded** entries indicate average scores with an overlapping 95% confidence interval to the best performing 2163 method. **Bolded** (resp., <u>Underlined</u>) Rank and Optimality Gap (Opt. Gap) metrics indicate the best (resp., second best) for a given 2164 backbone optimizer.

L_1 Coverage@128	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	$\mathbf{Rank}\downarrow$	Opt. Gap \uparrow
Dataset \mathcal{D}	0.42	0.31	1.42	0.68	6.26	0.58	_	_
Grad.	0.16 ^(0.10)	0.20 ^(0.13)	0.21(0.10)	0.42 ^(0.18)	$0.00^{(0.00)}$	$0.00^{(0.00)}$	19.5	-1.44
BO-qUCB	$0.40^{(0.02)}$	$0.54^{(0.01)}$	2.40 ^(0.05)	$2.52^{(0.07)}$	$7.79^{(0.04)}$	$6.64^{(0.09)}$	4.3	<u>1.77</u>
CMA-ES	0.33(0.05)	$0.48^{(0.04)}$	$2.18^{(0.04)}$	$1.82^{(0.12)}$	3.26 ^(1.42)	3.78(1.36)	$\frac{4.3}{8.5}$	0.36
BONET	$0.11^{(0.00)}$	$0.22^{(0.00)}$	$0.72^{(0.02)}$	$0.54^{(0.00)}$	0.03 ^(0.00)	$0.07^{(0.00)}$	17.8	-1.33
DDOM	0.43 ^(0.01)	$0.29^{(0.00)}$	$0.68^{(0.05)}$	$0.85^{(0.02)}$	9.24 ^(0.23)	$0.66^{(0.11)}$	10.8	0.41
ExPT	$0.22^{(0.05)}$	0.25 ^(0.01)	$0.60^{(0.03)}$	$0.29^{(0.03)}$	$0.45^{(0.01)}$	$0.10^{(0.00)}$	18.0	-1.29
MINs	0.43 ^(0.02)	0.30 ^(0.01)	$1.32^{(0.03)}$	$0.70^{(0.03)}$	0.86 ^(0.13)	$0.43^{(0.01)}$	11.0	-0.94
GTG	$0.42^{(0.00)}$	$0.30^{(0.00)}$	1.61 ^(0.00)	1.96 ^(0.00)	$8.77^{(0.00)}$	0.31 ^(0.00)	8.7	0.62
Tri-Mentoring	0.48 ^(0.00)	$0.30^{(0.00)}$	$1.08^{(0.00)}$	0.53 ^(0.00)	$1.94^{(0.00)}$	3.79 ^(0.00)	10.8	-0.26
ICT	$0.34^{(0.02)}$	$0.30^{(0.00)}$	$0.90^{(0.02)}$	$0.80^{(0.05)}$	$0.56^{(0.01)}$	3.73(0.02)	12.8	-0.51
PGS	$0.45^{(0.04)}$	$0.30^{(0.01)}$	$1.40^{(0.00)}$	$0.60^{(0.00)}$	$1.92^{(0.00)}$	$3.66^{(0.04)}$	10.0	-0.22
Match-Opt	$0.41^{(0.01)}$	$0.32^{(0.01)}$	$0.69^{(0.01)}$	$0.86^{(0.02)}$	5.26 ^(0.02)	$5.22^{(0.07)}$	8.7	0.52
RGD	$0.42^{(0.01)}$	$0.33^{(0.00)}$	0.69 ^(0.01)	$0.86^{(0.02)}$	4.08 ^(0.13)	4.90 ^(0.07)	9.0	0.27
COMs	0.49 ^(0.02)	0.31 ^(0.00)	$1.11^{(0.16)}$	0.61 ^(0.09)	0.37 ^(0.11)	$0.81^{(0.76)}$	11.0	-1.00
RoMA	$0.28^{(0.00)}$	$0.46^{(0.01)}$	$0.41^{(0.02)}$	$0.42^{(0.01)}$	1.87 ^(0.06)	$0.79^{(0.01)}$	14.8	-0.91
ROMO	0.33(0.02)	0.30 ^(0.00)	1.31 ^(0.02)	0.62 ^(0.02)	0.34 ^(0.16)	6.13 ^(2.81)	11.8	-0.11
GAMBO	$0.40^{(0.03)}$	0.55 ^(0.01)	$2.38^{(0.10)}$	$2.53^{(0.05)}$	7.45 ^(0.01)	$1.29^{(0.08)}$	6.3	0.82
DynAMO-Grad.	0.36 ^(0.04)	0.53 ^(0.06)	1.46 ^(0.38)	2.50 ^(0.06)	6.47 ^(1.24)	5.85 ^(1.35)	6.7	1.25
DynAMO-BO-qUCB	$0.40^{(0.03)}$	0.55 ^(0.01)	$2.47^{(0.07)}$	$2.54^{(0.04)}$	$7.88^{(0.03)}$	7.80 ^(0.23)	2.8	2.00
DynAMO-CMA-ES	$0.40^{(0.03)}$	0.56 ^(0.01)	1.82 ^(0.72)	2.54 ^(0.05)	4.75 ^(2.16)	$3.29^{(1.56)}$	6.3	0.62

212	Table A9. Computational Requirements of DynAMO. To evaluate the computational cost of augmenting an MBO problem with
)12	DynAMO, we compare both the total runtime and maximum GPU utilization of vanilla optimizers with that of their DynAMO equivalents
11	on six MBO problems. Runtime is reported mean ^(95% confidence interval) in seconds across 10 random seeds. Maximum GPU utilization is
214	reported for a single experimental run. The average metric across all six tasks is reported in the final column.

Runtime (seconds)	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	Average \downarrow
Grad.	58.1(24.6)	240.0(11.1)	104.7(8.3)	458.7(28.2)	24.7 ^(3.7)	10357(2044)	1874
DynAMO-Grad.	517.0(68.7)	2686 ^(868.3)	297.0(100.0)	$1091^{(243.1)}$	917.5 ^(554.4)	13302 ⁽⁴³⁰¹⁾	3135
Adam	26.1 ^(0.5)	249.2(17.5)	75.3(13.2)	748.2(34.6)	24.4 ^(2.6)	8797 ⁽¹³³³⁾	1653
DynAMO-Adam	646.7 ^(185.6)	$616.6^{(106.1)}$	709.6 ^(410.3)	953.7 ^(140.9)	6941 ⁽²⁰⁵⁾	24444 ⁽²⁴⁶⁶⁾	5719
BO-qEI	182.4 ^(51.6)	339.6(61.7)	494.3(34.2)	1548 ^(56.4)	567.8(119.3)	3196(158.4)	838.0
DynAMO-BO-qEI	449.9(111.0)	952.8 ^(140.6)	494.4 ^(161.8)	1307 ^(232.1)	$1122^{(150.0)}$	5973 ⁽¹²⁴⁵⁾	1717
BO-qUCB	186.9(36.4)	414.4(73.7)	289.8(80.0)	589.8 ^(50.2)	524.9 ^(232.5)	8424(1336)	1738
DynAMO-BO-qUCB	408.4 ^(66.3)	1531 ^(146.6)	932.3 ^(323.1)	1525 ^(357.1)	2100 ⁽¹⁵⁴⁷⁾	11648 ⁽⁵⁰⁹¹⁾	3024
CMA-ES	109.4(66.0)	130.0(3.2)	66.0 ^(1.4)	604.1(12.4)	20.0 ^(0.3)	14027(2651)	2493
DynAMO-CMA-ES	10744 ⁽⁷⁹⁰⁴⁾	9551 ⁽²⁷¹⁷⁾	751.3 ^(381.0)	8088 ⁽¹⁵³³⁾	4796 ⁽⁴⁴⁵⁾	13727 ⁽⁵⁸⁷⁰⁾	7943
CoSyNE	133.9 ^(81.3)	187.0 ^(1.7)	110.3(2.6)	716.8(30.0)	25.8 ^(0.5)	9876.8 ^(735.3)	1842
DynAMO-CoSyNE	8823 ⁽³³⁷⁰⁾	11388 ⁽²³⁷⁵⁾	$1374^{(584.6)}$	$8002^{(1802)}$	6261 ⁽³²⁰²⁾	17147 ⁽³⁸⁵⁶⁾	8832
	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	Average ↓
Max GPU Utilization (MB) Grad.	TFBind8 307.9	786.8	503.9	1920	133.6	D'Kitty 131.7	630.7
Max GPU Utilization (MB)	TFBind8	-	-			D'Kitty	0 .
Max GPU Utilization (MB) Grad. DynAMO-Grad. Adam	TFBind8 307.9 374.1 307.9	786.8 994.8 786.8	503.9 503.9 503.9	1920 1920 1920	133.6 208.3 133.6	D'Kitty 131.7 160.1 131.7	630.7 693.6 630.7
Max GPU Utilization (MB) Grad. DynAMO-Grad.	TFBind8 307.9 374.1	786.8 994.8	503.9 503.9	1920 1920	133.6 208.3	D'Kitty 131.7 160.1	630.7 693.6
Max GPU Utilization (MB) Grad. DynAMO-Grad. Adam DynAMO-Adam BO-qEI	TFBind8 307.9 374.1 307.9 374.4 307.9	786.8 994.8 786.8 995.0 786.8	503.9 503.9 503.9 503.9 503.9 519.1	1920 1920 1920 1920 1920 1920	133.6 208.3 133.6 208.4 372.6	D'Kitty 131.7 160.1 131.7 160.1 544.1	630.7 693.6 630.7 693.7 741.8
Max GPU Utilization (MB) Grad. DynAMO-Grad. Adam DynAMO-Adam BO-qEI DynAMO-BO-qEI	TFBind8 307.9 374.1 307.9 374.4 307.9 371.4	786.8 994.8 786.8 995.0 786.8 789.0	503.9 503.9 503.9 503.9 503.9 519.1 503.9	1920 1920 1920 1920 1920 1920 1920 1920	133.6 208.3 133.6 208.4 372.6 479.4	D'Kitty 131.7 160.1 131.7 160.1 544.1 445.2	630.7 693.6 630.7 693.7 741.8 751.6
Max GPU Utilization (MB) Grad. DynAMO-Grad. Adam DynAMO-Adam BO-qEI DynAMO-BO-qEI BO-qUCB	TFBind8 307.9 374.1 307.9 374.4 307.9 371.4 597.3	786.8 994.8 786.8 995.0 786.8 789.0 786.8	503.9 503.9 503.9 503.9 503.9 519.1 503.9 642.3	1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920	133.6 208.3 133.6 208.4 372.6 479.4 712.4	D'Kitty 131.7 160.1 131.7 160.1 544.1 445.2 879.5	630.7 693.6 630.7 693.7 741.8 751.6 923.1
Max GPU Utilization (MB) Grad. DynAMO-Grad. Adam DynAMO-Adam BO-qEI DynAMO-BO-qEI BO-qUCB DynAMO-BO-qUCB	TFBind8 307.9 374.1 307.9 374.4 307.9 371.4 597.3 516.2	786.8 994.8 786.8 995.0 786.8 789.0 786.8 786.8 786.8	503.9 503.9 503.9 503.9 503.9 503.9 503.9 642.3 646.9	1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920	133.6 208.3 133.6 208.4 372.6 479.4 712.4 712.4 718.0	D'Kitty 131.7 160.1 131.7 160.1 544.1 445.2 879.5 406.1	630.7 693.6 630.7 693.7 741.8 751.6 923.1 832.4
Max GPU Utilization (MB) Grad. DynAMO-Grad. Adam DynAMO-Adam BO-qEI DynAMO-BO-qEI BO-qUCB DynAMO-BO-qUCB DynAMO-BO-qUCB	TFBind8 307.9 374.1 307.9 374.4 307.9 371.4 597.3 516.2 307.9	786.8 994.8 786.8 995.0 786.8 789.0 786.8 786.8 786.8 786.8	503.9 503.9 503.9 503.9 503.9 503.9 503.9 642.3 646.9 503.9	1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920	133.6 208.3 133.6 208.4 372.6 479.4 712.4 712.4 718.0 133.6	D'Kitty 131.7 160.1 131.7 160.1 544.1 445.2 879.5 406.1 131.7	630.7 693.6 630.7 693.7 741.8 751.6 923.1 832.4 630.7
Max GPU Utilization (MB) Grad. DynAMO-Grad. Adam DynAMO-Adam BO-qEI DynAMO-BO-qEI BO-qUCB DynAMO-BO-qUCB CMA-ES DynAMO-CMA-ES	TFBind8 307.9 374.1 307.9 374.4 307.9 371.4 597.3 516.2 307.9 307.9	786.8 994.8 786.8 995.0 786.8 789.0 786.8 786.8 786.8 786.8 786.8 786.8 786.8 786.8	503.9 503.9 503.9 503.9 503.9 503.9 503.9 642.3 646.9 503.9 503.9	1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920	133.6 208.3 133.6 208.4 372.6 479.4 712.4 712.4 718.0 133.6 133.6	D'Kitty 131.7 160.1 131.7 160.1 544.1 445.2 879.5 406.1 131.7 131.7	630.7 693.6 630.7 693.7 741.8 751.6 923.1 832.4 630.7 630.7
Max GPU Utilization (MB) Grad. DynAMO-Grad. Adam DynAMO-Adam BO-qEI DynAMO-BO-qEI BO-qUCB DynAMO-BO-qUCB DynAMO-BO-qUCB	TFBind8 307.9 374.1 307.9 374.4 307.9 371.4 597.3 516.2 307.9	786.8 994.8 786.8 995.0 786.8 789.0 786.8 786.8 786.8 786.8	503.9 503.9 503.9 503.9 503.9 503.9 503.9 642.3 646.9 503.9	1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920 1920	133.6 208.3 133.6 208.4 372.6 479.4 712.4 712.4 718.0 133.6	D'Kitty 131.7 160.1 131.7 160.1 544.1 445.2 879.5 406.1 131.7	630.7 693.6 630.7 693.7 741.8 751.6 923.1 832.4 630.7

Table A10. **Pairwise Diversity as a Predictor for Downstream Secondary Exploration.** We evaluate the pairwise diversity achieved by 128 proposed designs (**PD@128**); and also the variance of the distribution of oracle secondary objective values of those same 128 proposed designs. Note that the secondary objectives are *not* explicitly optimized against in the offline MBO setting. Metrics are reported mean^(95% confidence interval) across 10 random seeds, where higher is better (i.e., more diverse designs and better capture of the range of secondary objective values). All metrics are multiplied by 100 for easier legibility.

		Vehicle Safety		Welde	d Beam	τ	TR
Method	PD@128	Acceleration	Intrusion	PD@128	Deflection	PD@128	GC Content
Grad. DynAMO-Grad.	$\begin{array}{c} 0.0^{(0.0)} \\ 2.5^{(0.2)} \end{array}$	$0.1^{(0.0)} \\ 12.6^{(0.5)}$	$\frac{0.0^{(0.0)}}{10.7^{(0.9)}}$	0.0 ^(0.0) 19.6 ^(33.3)	$\begin{array}{c} 0.1^{(0.3)} \\ 31.7^{(9.3)} \end{array}$	$7.8^{(8.8)} \\ 68.2^{(10.8)}$	$\begin{array}{c} 0.7^{(0.7)} \\ 3.4^{(0.7)} \end{array}$
Adam DynAMO-Adam	$0.0^{(0.0)}$ $2.2^{(0.1)}$	$0.1^{(0.1)} \\ 12.6^{(0.6)}$	$\begin{array}{c} 0.1^{(0.1)} \\ 10.3^{(1.0)} \end{array}$	$\frac{0.0^{(0.0)}}{11.1^{(3.5)}}$	$\frac{1.5^{(1.6)}}{49.5^{(21.3)}}$	$\frac{11.0^{(12.1)}}{72.3^{(3.4)}}$	$4.0^{(5.9)} \\ 14.0^{(3.1)}$
CMA-ES DynAMO-CMA-ES	$\frac{0.0^{(0.0)}}{8.6^{(6.0)}}$	$0.5^{(0.2)} \\ 28.5^{(10.8)}$	$\begin{array}{c} 0.4^{(0.2)} \\ 30.8^{(20.0)} \end{array}$	$\begin{array}{c} 0.1^{(0.1)} \\ 43.9^{(6.0)} \end{array}$	$\begin{array}{c} 0.0^{(0.0)} \\ 19.8^{(18.8)} \end{array}$	$\frac{44.6^{(15.9)}}{73.1^{(3.1)}}$	36.5 ^(8.3) 42.0 ^(2.3)
CoSyNE DynAMO-CoSyNE	$\begin{array}{c} 0.0^{(0.0)} \\ 1.9^{(2.7)} \end{array}$	$\begin{array}{c} 0.6^{(0.1)} \\ 4.0^{(4.2)} \end{array}$	$0.5^{(0.1)} \\ 2.2^{(2.6)}$	$\begin{array}{c} 0.1^{(0.0)} \\ 55.1^{(65.3)} \end{array}$	$\frac{16.8^{(6.5)}}{65.8^{(13.2)}}$	$\frac{12.7^{(9.8)}}{20.3^{(2.3)}}$	$\frac{1.6^{(2.5)}}{1.0^{(1.3)}}$
BO-qEI DynAMO-BO-qEI	$\frac{1.3^{(0.1)}}{2.4^{(0.1)}}$	$7.5^{(0.4)} \\ 13.3^{(0.2)}$	$7.2^{(0.4)} \\ 10.5^{(0.2)}$	$\frac{46.3^{(2.0)}}{78.1^{(18.0)}}$	8.0 ^(0.3) 26.6 ^(2.1)	$73.8^{(0.5)} \\ 74.6^{(0.3)}$	$44.8^{(0.8)} \\ 45.7^{(0.6)}$
BO-qUCB DynAMO-BO-qUCB	$\frac{1.2^{(0.1)}}{2.8^{(0.1)}}$	$5.7^{(0.4)} \\ 12.3^{(0.2)}$	$\begin{array}{c} 6.1^{(0.4)} \\ 10.9^{(0.1)} \end{array}$	$46.5^{(7.5)} \\ 63.9^{(4.2)}$	$7.8^{(0.2)} \\ 29.0^{(1.9)}$	$74.3^{(0.2)} \\ 74.4^{(0.6)}$	$45.3^{(0.4)} 45.2^{(0.5)}$

E. Ablation Experiments

E.1. Sampling Batch Size Ablation

Recall from (7) that a key component of our DynAMO algorithm is the estimation of the empirical KL-divergence between the τ -weighted probability distribution of real designs from the offline dataset and the distribution of sampled designs from the generative policy. The latter distribution of generated designs is fundamentally dependent on our sampling batch size b in Algorithm 1—the larger the batch size per sampling step, the better our empirical estimate of the KL divergence between our two distributions. However, as the batch size increases, there also exists a greater likelihood of significant regret in the sampling policy when compared to the optimal sequential policy (Gonzalez et al., 2016; Wilson et al., 2017). To better evaluate the impact of the sampling batch size parameter b DynAMO, we experimentally evaluate sampling batch size values logarithmically ranging between $2 \le b \le 512$. We use a BO-qEI sampling policy with the DynAMO-modified objective on the TFBind8 optimization task, and evaluate both the Best@128 oracle score and Pairwise Diversity of the 128 final proposed design candidates across 10 random seeds.

Our ablation experiment results are shown in Figure A3. We find that the Best@128 design quality scores do not vary significantly as a function of the batch sizes that were evaluated; however, there exists an optimal batch size (b = 64 in our experiments) that maximizes the diversity of designs according to the pairwise diversity metric.

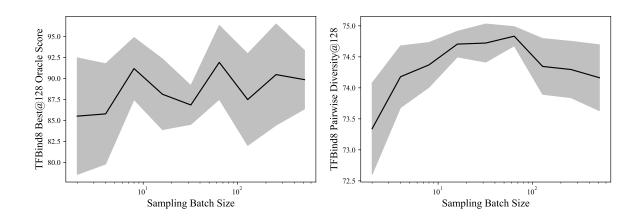


Figure A3. Sampling Batch Size Ablation. We vary the sampling batch size b in Algorithm 1 between 2 and 512, and report both the (left) Best@128 Oracle Score and (right) Pairwise Diversity score for 128 final designs proposed by a DynAMO-BO-qEI policy on the TFBind8 optimization task. We plot the mean \pm 95% confidence interval over 10 random seeds.

E.2. Adversarial Critic Feedback and Distribution Matching Ablation

Recall that instead of solving the original MBO optimization problem in (3), DynAMO leverages weak Lagrangian duality to solve the constrained optimization problem in (7)—copied below for convenience:

$$\max_{\pi \in \Pi} \quad J(\pi) = \mathbb{E}_{q^{\pi}}[r_{\theta}(x)] - \frac{\beta}{\tau} D_{\mathrm{KL}}(q^{\pi} || p_{\mathcal{D}}^{\tau})$$

s.t.
$$\mathbb{E}_{x \sim p_{\mathcal{D}}^{\tau}(x)} c^{*}(x) - \mathbb{E}_{x \sim q^{\pi}(x)} c^{*}(x) \leq W_{0}$$
 (85)

We can think of this problem formulation as as the fusion of two separable components: (1) Adversarial feedback via a source-critic model $c^*(x)$ to prevent out-of-distribution evaluation of $r_{\theta}(x)$; and (2) Diversity (via KL-divergence-based distribution matching with a diverse reference distribution $p_{\mathcal{D}}^{\tau}$) in Model-based Optimization. These two components together form the foundation of DynAMO presented in Algorithm 1. To better understand how each of these two components affects the performance of DynAMO-augmented optimizers, we can separate these two components and study them individually.

AMO is our ablation method that solves the related optimization problem

$$\max_{\pi \in \Pi} \quad \mathbb{E}_{q^{\pi}}[r_{\theta}(x)]$$

s.t.
$$\mathbb{E}_{x \sim p_{\mathcal{D}}^{\tau}(x)} c^{*}(x) - \mathbb{E}_{x \sim q^{\pi}(x)} c^{*}(x) \leq W_{0}$$
(86)

instead of (85). Note that AMO solves the same constrained optimization problem as DynAMO in the setting where $\beta = 0$. We note that our derivation of the Lagrange dual function of (7) in **Appendix A** is invalid when $\beta = 0$, and so we cannot **Dyn**MO is our separate ablation method that solves the related (unconstrained) optimization problem

2371 2372

2388

$$\max_{\pi \in \Pi} \quad J(\pi) = \mathbb{E}_{q^{\pi}}[r_{\theta}(x)] - \frac{\beta}{\tau} D_{\mathrm{KL}}(q^{\pi} || p_{\mathcal{D}}^{\tau})$$
(87)

instead of (85). To implement DynMO empirically, we modify **Algorithm 1** by ignoring the subroutine to solve for the globally optimal Lagrange multiplier λ using (13), and instead fixing $\lambda = 0$ for the entire optimization process to effectively remove any contributions from the adversarial source critic $c^*(x)$. All other implementation details were kept constant.

We compare DynAMO with AMO and DynMO in Supplementary Tables A11-A13. Firstly, we note that DynAMO and 2377 AMO are competitive in proposing the high-quality designs according to the Best@128 oracle scores, alternating between 2378 having the highest and second best Rank and Optimality Gaps across all six tasks when compared with DynMO and the 2379 baseline optimizer for all optimizers evaluated. This makes sense, as the purpose of the adversarial source critic-dependent 2380 constraint in (85) and (86) is to minimize out-of-distribution evaluation of $r_{\theta}(x)$ during optimization—as a result, the 2381 forward surrogate model $r_{\theta}(x)$ can provide a better estimate of the quality of sampled designs, leading to higher quality 2382 designs according to the true oracle function r(x). Separately, we find that DynMO and DynAMO also perform similarly 2383 in terms of the all 3 diversity metrics evaluated. However, we find that DynMO (resp., AMO) struggles on proposing 2384 high-quality (resp., diverse) sets of final designs. These experimental results collectively allow us to conclude that both 2385 the adversarial source critic supervision and KL-divergence-based distribution matching are important for DynAMO 2386 to propose both high-quality and diverse sets of designs. 2387

2389 E.3. β and τ Hyperparameter Ablation

2390 Fundamentally, DynAMO relies on two important hyperparameters that define the constrained optimization problem in 2391 (7): (1) the β hyperparameter dictates the relative weighting of the KL-divergence penalty relative to the original MBO 2392 objective; and (2) the τ temperature hyperparameter describes the distribution of reference designs weighted according 2393 to their oracle scores in the offline dataset. To better interrogate how these hyperparameters impact the performance of 2394 DynAMO-augmented MBO optimizers, we (independently) ablate the values of both β and τ logarithmically between 2395 $0.01 < \beta, \tau < 100$. Similar to our experiments in Appendix E.1, we use a BO-qEI sampling policy with the DynAMO-2396 modified objective on the TFBind8 optimization task, and evaluate both the Best@128 oracle score and Pairwise Diversity 2397 of the 128 final proposed design candidates across 10 random seeds. 2398

Our experimental results for our β ablation study are shown in **Supplementary Figure A4**. Firstly, as the strength of the 2399 KL-divergence term β increases, the diversity of proposed designs (according to the Pairwise Diversity metric) increases 2400 roughly proportional to the logarithm of β (Supplementary Fig. A4). This is expected: as the distribution matching 2401 objective becomes more important relative to the $r_{\theta}(x)$ forward surrogate model, the generative policy is rewarded for 2402 finding an increasingly diverse set of designs that matches the τ -weighted reference distribution. Similarly, we found that 2403 for sufficiently large values of β (i.e., $\beta > 0.03$ in our particular experimental setting), the quality of designs (according 2404 to the Best@128 oracle score) decreases due to the inherent trade-off between design quality (according to $r_{\theta}(x)$) and 2405 diversity (according to the KL-divergence in (7)). Interestingly, for small values of β (i.e., $\beta < 0.03$) the quality of designs 2406 actually *increases* with β . This is because in this regime, naïvely optimizing against primarily $r_{\theta}(x)$ leads to the policy 2407 exploiting suboptimal regions of the design space—penalizing the optimization objective with a 'small amount of' the 2408 diversity objective helps the policy explore new regions of the design space that can contain more optimal designs according 2409 to the hidden oracle objective r(x). 2410

2411 Separately, the experimental results for our τ ablation study are shown in **Supplementary Figure A5**. (Note that in these 2412 experiments, we fix $\beta = \tau$ so that the ratio β/τ in Algorithm 1 remains constant.) As the value of τ increases, the diversity 2413 of designs captured by the reference τ -weighted probability distribution decreases and approaches a (potential mixture of) 2414 Dirac delta functions with non-zero support at the optimal designs in the offline dataset. As a result, distribution matching 2415 via the KL-divergence objective no longer encourages the generative policy to find a diverse sample of designs, as the 2416 reference distribution is no longer diverse itself for $\tau \gg 1$. Similar to our β ablation study, we find that there is a unique 2417 exploration-exploitation trade-off phenomenon according to the Best@128 oracle score as a function of τ : in our particular 2418 experimental setting, we find that for $\tau \leq 1$, the Best@128 oracle score (modestly) increases, while for $\tau \geq 1$, the score 2419

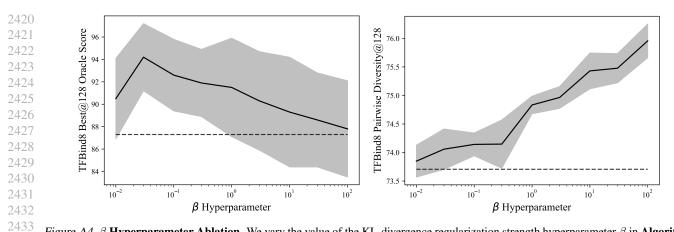


Figure A4. β Hyperparameter Ablation. We vary the value of the KL-divergence regularization strength hyperparameter β in Algorithm 1 between 0.01 and 100, and report both the (left) Best@128 Oracle Score and (right) Pairwise Diversity score for 128 final design candidates proposed by a DynAMO-BO-qEI policy on the TFBind8 optimization task. We plot the mean \pm 95% confidence interval over 10 random seeds in both plots. The dotted horizontal line corresponds to the $\beta = 0$ experimental mean score, which could not be plotted as a point on the logarithmic *x*-axis.

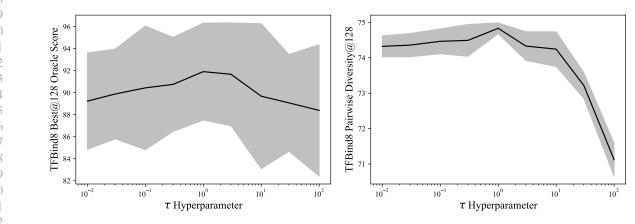


Figure A5. τ **Temperature Hyperparameter Ablation.** We vary the value of the temperature hyperparameter τ in **Algorithm 1** between 0.01 and 100, and report both the (left) Best@128 Oracle Score and (right) Pairwise Diversity score for 128 final designs proposed by a DynAMO-BO-qEI policy on the TFBind8 optimization task. We plot the mean \pm 95% confidence interval over 10 random seeds.

decreases. For $\tau \approx 1$, we find that the generative policy is encouraged to match a sample of high-quality samples that is simultaneously *diverse* enough for the generative policy to explore new regions of the design space.

E.4. Oracle Evaluation Budget Ablation

Recall that in our experiments, we evaluate DynAMO and baseline methods using an oracle evaluation budget of k = 128samples consistent with prior work (Mashkaria et al., 2023; Yu et al., 2021; Trabucco et al., 2021; Chen et al., 2023c; Yao et al., 2024). More specifically, this means that any offline optimization method proposes exactly k design candidates that are evaluated by the hidden oracle function r(x) as the final step for experimental evaluation. In **Table 1**, we reported both the Best@k and Pairwise Diversity@k metrics, where Best@k represents the maximum oracle score achieved by the k final design candidates; and Pairwise Diversity@k represents the pairwise diversity averaged over the k candidates.

However, in different experimental settings we might have a different evaluation budget available—larger values of k are more costly but enable us to evaluate more designs that are potentially promising, whereas smaller, more practical budgets may preclude the evaluation of optimal designs according to r(x). In this section, we evaluate the performance of DynAMO as a function of the allowed evaluation budget $16 \le k \le 1024$. We compare DynAMO-augmented optimizers against the corresponding vanilla backbone optimization method on the TFBind8 task, and plot the mean and 95% confidence interval Best@k and Pairwise Diversity@k metrics as a function of k in **Supplementary Figure A6**. As expected, the Best@k oracle score is monotonically non-decreasing as a function of k for all DynAMO-enhanced and baseline optimizers (**Supplementary Fig. A6**). We also find that in the limit of $k \gg 1$, the DynAMO optimizers are able to propose best designs that are more optimal than the designs by their baseline counterparts for first-order, evolutionary, and Bayesian optimization algorithms. Furthermore, DynAMO achieves a mean Best@k score non-inferior to that of the baseline method for all $k \ge 128$ across all the optimization methods evaluated on the TFBind8 task.

2480 Separately, we find that the Pairwise Diversity of the k designs proposed by DynAMO-augmented first-order optimizers (i.e., 2481 **DynAMO-Grad.** and **DynAMO-Adam**) increases as a function of k. This makes sense, as first-order methods generally 2482 produce optimization trajectories that are simple curves in the design space as a function of the acquisition step. As a 2483 result, increasing k can be informally thought of as increasing the fraction of the trajectory curve connecting the initial 2484 and final samples during the acquisition process. In contrast, we find that the Pairwise Diversity decreases after a certain 2485 optimizer-dependent threshold k for evolutionary and Bayesian optimization-based backbone optimizers. This is because as 2486 both classes of optimization methods do not necessarily sample repeatedly from any given region of the input space; as a 2487 result, the pairwise diversity between any two sampled points may decrease as more of the design space has been explored 2488 as a function of k. Finally, we found that leveraging DynAMO improves the Pairwise Diversity of designs compared to the 2489 baseline objective for almost all optimizers and values of k assessed, as expected. 2490

Altogether, these results suggest that DynAMO helps optimization methods discover both high-quality and diverse sets of designs across a wide range of oracle evaluation budgets.

2494 E.5. Optimization Initialization Ablation

2495 In Algorithm 1, we initialize DynAMO by sampling the initial batch of b = 64 designs according to a pseudo-random 2496 Sobol sequence as described in **Appendix B**. This initial batch of designs is used as the 'starting point' in our first-order 2497 optimization experiments. However, most first-order offline MBO algorithms reported in prior work (Trabucco et al., 2021; 2498 Yu et al., 2021) do not follow this same initialization schema. Instead, they perform a top-k initialization strategy where the 2499 top k = b designs in the dataset with the highest associated reward score constitute the initial batch of designs. First-order 2500 optimization is then performed on these initial top-k designs. However, it is possible that for many MBO problems, these 2501 top-k initial designs constitute only a small 'area' of the overall search space, resulting in a lower diversity of final designs 2502 when compared to Sobol sequence initialization. 2503

To interrogate whether the gains in diversity of designs obtained with DynAMO are due to our Sobol sequence-based initialization strategy, we evaluated baseline Gradient Ascent, COMs, RoMA, ROMO, GAMBO with Gradient Ascent, and DynAMO with Gradient Ascent using both Sobol sequence-based and top-*k*-based initialization strategies. All algorithms were initialized using k = b = 64 samples and used Gradient Ascent as the backbone optimizer (except for RoMA from Yu et al. (2021), which used Adam Ascent in line with the original method proposed by the authors).

Our results are shown in **Supplementary Table A14**. Empirically, we found that the relative performance of Sobol sequence-initialized and Top-k-initialized optimizer largely depends on the specific algorithm; for example, COMs and RoMA strongly benefit from using Top-k initialization in obtaining high-quality designs. This makes sense, as the original authors for both methods use Top-k initialization for all their experiments. In contrast, the quality of designs proposed by GAMBO and DynAMO is better with Sobol sequence initialization.

2515 While DynAMO using Sobol sequence initialization does indeed outperform the Top-k-initialized counterpart across all 2516 tasks, both initialization strategies consistently propose batches of designs with competitive pairwise diversity scores 2517 when compared to other first-order optimization algorithms. This suggests that DynAMO is able to provide a significant 2518 advantage in proposing diverse designs that extend beyond the choice of initialization strategy alone. Separately for the 2519 other first-order optimization methods assessed, there is no clear advantage in obtaining diverse designs when using Sobol 2520 sequence initialization according to the pairwise diversity metric across all tasks. In summary, these results suggest that 2521 DynAMO is able to propose both high-quality and diverse sets of designs with performance exceeding what is possible with 2522 a switching to a Sobol sequence initialization alone. 2523

2523

- 2524 2525
- 2525
- 2520
- 2528
- 2529

Table A11. Quality of Design Candidates in Ablation of Adversarial Critic Feedback (AMO) and Diversity in (DynMO) Modelbased Optimization. We evaluate our method (1) with the KL-divergence penalized-MBO objective as in (11) only (DynMO); (2)
with the adversarial source critic-dependent constraint as introduced by Yao et al. (2024) only (AMO); and (3) with both algorithmic components as in DynAMO described in Algorithm 1. We report the Best@128 (resp., Median@128) oracle score achieved by the 128
evaluated designs in the top (resp., bottom) table. Metrics are reported mean^(95% confidence interval) across 10 random seeds, where higher is
better. Bolded entries indicate average scores with an overlapping 95% confidence interval to the best performing method. Bolded (resp., 2536
Underlined) Rank and Optimality Gap (Opt. Gap) metrics indicate the best (resp., second best) for a given backbone optimizer.

Best@128	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	Rank ↓	Opt. Gap↑
Dataset \mathcal{D}	43.9	59.4	60.5	88.9	40.0	88.4	_	_
Grad.	90.0 ^(4.3)	80.9 ^(12.1)	60.2 ^(8.9)	88.8 ^(4.0)	36.0 ^(6.8)	65.6 ^(14.5)	3.2	6.8
<u>A</u> MO-Grad.	73.1 ^(12.8)	77.1 ^(9.6)	64.4 ^(1.5)	92.8 ^(8.0)	46.0 ^(6.8)	90.6 ^(14.5)	1.8	<u>10.5</u>
DynMO-Grad.	61.3 ^(9.7)	63.6 ^(11.6)	59.8 ^(8.6)	89.3 ^(5.6)	36.3(6.9)	70.4 ^(12.0)	3.5	0.0
Dyn <u>A</u> MO-Grad.	90.3 ^(4.7)	86.2 ^(0.0)	64.4 ^(2.5)	91.2 ^(0.0)	44.2 ^(7.8)	89.8 ^(3.2)	1.5	14.2
Adam	62.9(13.0)	69.7 ^(10.5)	62.9 ^(1.9)	92.3 ^(8.9)	37.8 ^(6.3)	58.4 ^(18.5)	2.8	0.5
<u>A</u> MO-Adam	94.0 ^(2.2)	60.0(12.6)	60.9 ^(8.7)	91.4 ^(6.3)	37.8 ^(6.3)	88.4 ^(13.8)	2.8	<u>8.6</u>
DynMO-Adam	66.6 ^(12.9)	68.7 ^(10.1)	63.7 ^(0.4)	92.0 ^(8.3)	38.6 ^(5.7)	66.5 ^(14.6)	<u>2.5</u>	2.5
Dyn <u>A</u> MO-Adam	95.2 ^(1.7)	86.2 ^(0.0)	65.2 ^(1.1)	91.2 ^(0.0)	45.5 ^(5.7)	84.9 ^(12.0)	1.7	14.5
BO-qEI	87.3 ^(5.8)	86.2 ^(0.0)	65.4 ^(1.0)	117 ^(3.1)	53.1 ^(3.3)	84.4(0.9)	3.5	18.7
<u>A</u> MO-BO-qEI	94.1 ^(1.9)	86.3 ^(0.2)	66.8 ^(0.7)	$121^{(0.0)}$	50.8 ^(3.3)	86.7 ^(1.1)	1.5	20.8
DynMO-BO-qEI	93.2 ^(3.3)	86.2 ^(0.0)	66.0 ^(0.8)	121 ^(0.0)	49.6 ^(2.6)	85.9 ^(1.0)	2.7	20.2
Dyn <u>A</u> MO-BO-qEI	91.9 ^(4.4)	86.2 ^(0.0)	67.0 ^(1.3)	121 ^(0.0)	53.5 ^(5.0)	85.5 ^(1.1)	<u>1.8</u>	<u>20.7</u>
BO-qUCB	88.1(5.3)	86.2 ^(0.1)	66.4 ^(0.7)	121 ^(1.3)	51.3 ^(3.6)	84.5 ^(0.8)	2.2	19.4
AMO-BO-qUCB	95.4 ^(1.6)	86.2 ^(0.0)	66.3 ^(1.1)	121 ^(1.3)	50.2 ^(2.8)	83.6 ^(1.0)	<u>2.7</u>	20.2
DynMO-BO-qUCB	93.6 ^(3.0)	86.2 ^(0.1)	66.0 ^(0.9)	121 ^(0.0)	49.9 ^(3.0)	83.9 ^(1.1)	2.7	20.0
Dyn <u>A</u> MO-BO-qUCB	95.1 ^(1.9)	86.2 ^(0.0)	66.7 ^(1.5)	$121^{(0.0)}$	48.1 ^(4.0)	86.9 ^(4.5)	2.2	20.5
Baseline-CMA-ES	87.6 ^(8.3)	86.2 ^(0.0)	66.1 ^(1.0)	106(5.9)	49.0 ^(1.0)	72.2 ^(0.1)	2.8	14.4
AMO-CMA-ES	90.4 ^(4.4)	86.2 ^(0.0)	66.2 ^(1.6)	$121^{(0.0)}$	45.2 ^(3.5)	72.2 ^(0.1)	1.8	16.7
DynMO-CMA-ES	85.2 ^(10.1)	86.2 ^(0.0)	65.0 ^(0.6)	104 ^(7.8)	51.6 ^(2.0)	83.6 ^(3.1)	2.7	15.8
Dyn <u>A</u> MO-CMA-ES	89.8 ^(3.6)	85.7 ^(5.8)	63.9 ^(0.9)	117 ^(6.7)	50.6 ^(4.8)	78.5 ^(5.5)	2.7	17.5
CoSyNE	61.7(10.0)	57.3 ^(9.6)	63.6 ^(0.4)	94.8(10.1)	37.0 ^(4.1)	62.7 ^(13.1)	3.5	-0.6
	(10.6)	68.0 ^(12.5)	64.2 ^(0.9)	99.4 ^(15.0)	37.0 ^(4.1)	62.7 ^(13.1)	2.2	5.0
AMO-CoSvNE	79.8 ^(10.0)	00.0						
<u>A</u> MO-CoSyNE Dyn MO-CoSyNE	79.8 ^(10.6) 63.6 ^(10.1)	59.3 ^(10.8)	63.9 ^(1.6)	90.1 ^(12.7)	37.0 ^(4.1)	62.7 ^(13.1)	3.0	-0.7
	79.8 ^(10.0) 63.6 ^(10.1) 91.3 ^(4.4)	59.3 ^(10.8) 77.2 ^(11.6)	63.9 ^(1.6) 63.9 ^(0.9)	90.1 ^(12.7) 114 ^(7.0)	37.0 ^(4.1) 40.6 ^(8.6)	62.7 ^(13.1) 67.5 ^(14.1)		-0.7 12.3
DynMO-CoSyNE	63.6 ^(10.1)	59.3 ^(10.8)	63.9 ^(1.6)	90.1 ^(12.7)	37.0 ^(4.1)	62.7 ^(13.1)	3.0	
DynMO-CoSyNE Dyn <u>A</u> MO-CoSyNE	63.6 ^(10.1) 91.3 ^(4.4)	59.3 ^(10.8) 77.2 ^(11.6)	63.9 ^(1.6) 63.9 ^(0.9)	90.1 ^(12.7) 114 ^(7.0)	37.0 ^(4.1) 40.6 ^(8.6)	62.7 ^(13.1) 67.5 ^(14.1)	3.0 1.2	12.3
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7	62.7 ^(13.1) 67.5 ^(14.1) D'Kitty 77.8	3.0 1.2 Rank↓	12.3 Opt. Gap 1
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad.	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1)	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8 58.6 ^(13.1)	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6)	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7) 91.6 ^(11.2)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7)	62.7 ^(13.1) 67.5 ^(14.1) D'Kitty 77.8 65.1 ^(14.4) 90.1 ^(14.4)	3.0 1.2 Rank↓ 	12.3 Opt. Gap
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad. AMO-Grad.	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1) 63.8 ^(13.7) 50.5 ^(6.5)	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8 58.6 ^(13.1) 75.3 ^(9.9) 58.6 ^(13.1)	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3) 59.7 ^(8.7)	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7) 91.6 ^(11.2) 85.1 ^(8.1)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7	62.7 ^(13.1) 67.5 ^(14.1) D'Kitty 77.8 65.1 ^(14.4) 90.1 ^(14.4) 70.0 ^(12.0)	3.0 1.2 Rank↓	12.3 Opt. Gap 1
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad.	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1)	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8 58.6 ^(13.1) 75.3 ^(9.9)	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3)	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7) 46.0 ^(6.7)	62.7 ^(13.1) 67.5 ^(14.1) D'Kitty 77.8 65.1 ^(14.4)	3.0 1.2 Rank ↓ — 3.2 1.2	12.3 Opt. Gap 1
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad. AMO-Grad. DynMO-Grad.	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1) 63.8 ^(13.7) 50.5 ^(6.5) 47.0 ^(2.8) 54.7 ^(8.8)	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8 58.6 ^(13.1) 75.3 ^(9.9) 58.6 ^(13.1) 69.8 ^(6.0) 69.4 ^(12.7)	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3) 59.7 ^(8.7) 61.9 ^(2.2) 59.2 ^(8.6)	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7) 91.6 ^(11.2) 85.1 ^(8.1)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7) 46.0 ^(6.7) 36.3 ^(6.9) 23.4 ^(8.5) 37.4 ^(6.2)	62.7 ^(13.1) 67.5 ^(14.1) D'Kitty 77.8 65.1 ^(14.4) 90.1 ^(14.4) 70.0 ^(12.0) 68.7 ^(12.1) 56.8 ^(19.8)	3.0 1.2 Rank ↓ 3.2 1.2 3.0 <u>2.7</u>	12.3 Opt. Gap 1
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad.	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1) 63.8 ^(13.7) 50.5 ^(6.5) 47.0 ^(2.8) 54.7 ^(8.8) 49.5 ^(8.9)	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8 58.6 ^(13.1) 75.3 ^(9.9) 58.6 ^(13.1) 69.8 ^(6.0) 60.4 ^(12.7) 55.7 ^(12.7)	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3) 59.7 ^(8.7) 61.9 ^(2.2) 59.2 ^(8.6)	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7) 91.6 ^(11.2) 85.1 ^(8.1) 85.9 ^(0.4) 87.9 ^(10.0) 84.3 ^(9.6)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7) 46.0 ^(6.7) 36.3 ^(6.9) 23.4 ^(8.5) 37.4 ^(6.2) 37.4 ^(6.2)	62.7 ^(13.1) 67.5 ^(14.1) D'Kitty 77.8 65.1 ^(14.4) 90.1 ^(14.4) 70.0 ^(12.0) 68.7 ^(12.1) 56.8 ^(19.8)	3.0 1.2 Rank ↓ - 3.2 1.2 3.0	12.3 Opt. Gap
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. DynAMO-Grad. Adam	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1) 63.8 ^(13.7) 50.5 ^(6.5) 47.0 ^(2.8) 54.7 ^(8.8) 49.5 ^(8.9) 54.0 ^(9.9)	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8 58.6 ^(13.1) 75.3 ^(9.9) 58.6 ^(13.1) 69.8 ^(6.0) 60.4 ^(12.7) 55.7 ^(12.7)	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3) 59.7 ^(8.7) 61.9 ^(2.2)	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7) 91.6 ^(11.2) 85.1 ^(8.1) 85.9 ^(0.4) 87.9 ^(10.0) 84.3 ^(9.6) 85.9 ^(10.8)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7) 46.0 ^(6.7) 36.3 ^(6.9) 23.4 ^(8.5)	62.7 ^(13.1) 67.5 ^(14.1) D'Kitty 77.8 65.1 ^(14.4) 90.1 ^(14.4) 70.0 ^(12.0) 68.7 ^(12.1)	3.0 1.2 Rank ↓ 3.2 1.2 3.0 2.7 2.3	12.3 Opt. Gap 1
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. Adam AMO-Adam	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1) 63.8 ^(13.7) 50.5 ^(6.5) 47.0 ^(2.8) 54.7 ^(8.8) 49.5 ^(8.9)	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8 58.6 ^(13.1) 75.3 ^(9.9) 58.6 ^(13.1) 69.8 ^(6.0) 69.4 ^(12.7)	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3) 59.7 ^(8.7) 61.9 ^(2.2) 59.2 ^(8.6) 57.7 ^(9.1)	90.1 ^(12.7) 114 ^(7.0) 87.6 85.3 ^(7.7) 91.6 ^(11.2) 85.1 ^(8.1) 85.9 ^(0.4) 87.9 ^(10.0)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7) 46.0 ^(6.7) 36.3 ^(6.9) 23.4 ^(8.5) 37.4 ^(6.2) 37.4 ^(6.2)	62.7 ^(13.1) 67.5 ^(14.1) D'Kitty 77.8 65.1 ^(14.4) 90.1 ^(14.4) 70.0 ^(12.0) 68.7 ^(12.1) 56.8 ^(19.8) 87.8 ^(4.3)	$3.0 \\ 1.2 \\ \hline \\ Rank \downarrow \\ \hline \\ 3.2 \\ 1.2 \\ 3.0 \\ 2.7 \\ \hline \\ 2.3 \\ 3.0 \\ \hline \\ 3.0 \\ \hline \\ 2.3 \\ 3.0 \\ \hline \\ \hline \\ \end{array}$	12.3 Opt. Gap ↑
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. Adam AMO-Adam DynMO-Adam DynAMO-Adam	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1) 63.8 ^(13.7) 50.5 ^(6.5) 47.0 ^(2.8) 54.7 ^(8.8) 49.5 ^(8.9) 54.0 ^(9.9) 47.7 ^(3.0)	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8 58.6 ^(13.1) 75.3 ^(9.9) 58.6 ^(13.1) 69.8 ^(6.0) 60.4 ^(12.7) 55.7 ^(12.7) 60.5 ^(12.6)	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3) 59.7 ^(8.7) 61.9 ^(2.2) 59.2 ^(8.6) 57.7 ^(9.1) 59.3 ^(8.6)	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7) 91.6 ^(11.2) 85.1 ^(8.1) 85.9 ^(0.4) 87.9 ^(10.0) 84.3 ^(9.6) 85.9 ^(10.8) 86.4 ^(0.6)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7) 46.0 ^(6.7) 36.3 ^(6.9) 23.4 ^(8.5) 37.4 ^(6.2) 37.4 ^(6.2) 37.4 ^(6.2) 37.7 ^(6.4) 23.0 ^(6.0) 28.7 ^(1.8)	62.7 ^(13.1) 67.5 ^(14.1) D'Kitty 77.8 65.1 ^(14.4) 90.1 ^(14.4) 70.0 ^(12.0) 68.7 ^(12.1) 56.8 ^(19.8) 87.8 ^(4.3) 63.6 ^(15.6)	$3.0 \\ 1.2 \\ \hline Rank \downarrow \\ \hline \\ 3.2 \\ 1.2 \\ 3.0 \\ 2.7 \\ \hline \\ 2.3 \\ 3.0 \\ 2.2 \\ 2.3 \\ \hline \\ 2.3 \\ 2.3 \\ \hline \\ 2.3 \\ 2.3 \\ \hline \\ 2.3 \\ 2.3 \\ \hline \\ 2.3 \\ 2.3 \\ 2.3 \\ \hline \\ 2.3$	12.3 Opt. Gap
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. Adam AMO-Adam DynMO-Adam	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1) 63.8 ^(13.7) 50.5 ^(6.5) 47.0 ^(2.8) 54.7 ^(8.8) 49.5 ^(8.9) 54.0 ^(9.9) 47.7 ^(3.0) 48.5 ^(1.5)	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8 58.6 ^(13.1) 75.3 ^(9.9) 58.6 ^(13.1) 69.8 ^(6.0) 60.4 ^(12.7) 55.7 ^(12.7) 60.5 ^(12.6) 69.0 ^(5.2) 59.9 ^(2.0) 63.4 ^(3.3)	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3) 59.7 ^(8.7) 61.9 ^(2.2) 59.2 ^(8.6) 57.7 ^(9.1) 59.3 ^(8.6) 62.4 ^(1.9) 63.3 ^(0.0) 63.3 ^(0.0)	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7) 91.6 ^(11.2) 85.1 ^(8.1) 85.9 ^(0.4) 87.9 ^(10.0) 84.3 ^(9.6) 85.9 ^(10.8) 86.4 ^(0.6) 86.7 ^(0.6) 86.3 ^(0.5)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7) 46.0 ^(6.7) 36.3 ^(6.9) 23.4 ^(8.5) 37.4 ^(6.2) 37.4 ^(6.2) 37.4 ^(6.2) 37.7 ^(6.4) 23.0 ^(6.0) 28.7 ^(1.8)	62.7 ^(13.1) 67.5 ^(14.1) D'Kitty 77.8 65.1 ^(14.4) 90.1 ^(14.4) 70.0 ^(12.0) 68.7 ^(12.1) 68.7 ^(12.1) 56.8 ^(19.8) 87.8 ^(4.3) 63.6 ^(15.6) 65.6 ^(14.1) 72.4 ^(1.8) 79.1 ^(0.7)	$3.0 \\ 1.2 \\ \hline Rank \downarrow \\ \hline \\ 3.2 \\ 1.2 \\ 3.0 \\ 2.7 \\ \hline \\ 2.3 \\ 3.0 \\ 2.2 \\ 2.3 \\ 2.5 \\ \hline \end{cases}$	12.3 Opt. Gap ~
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. Adam AMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1) 63.8 ^(13.7) 50.5 ^(6.5) 47.0 ^(2.8) 54.7 ^(8.8) 49.5 ^(8.9) 54.0 ^(9.9) 47.7 ^(3.0) 48.5 ^(1.5) 46.4 ^(1.8) 50.5 ^(1.5)	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8 58.6 ^(13.1) 75.3 ^(9.9) 58.6 ^(13.1) 69.8 ^(6.0) 60.4 ^(12.7) 55.7 ^(12.7) 60.5 ^(12.6) 69.0 ^(5.2) 59.9 ^(2.0) 63.4 ^(3.3)	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3) 59.7 ^(8.7) 61.9 ^(2.2) 59.2 ^(8.6) 57.7 ^(9.1) 59.3 ^(8.6) 62.4 ^(1.9) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0)	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7) 91.6 ^(11.2) 85.1 ^(8.1) 85.9 ^(0.4) 87.9 ^(10.0) 84.3 ^(9.6) 85.9 ^(10.8) 86.4 ^(0.6) 86.3 ^(0.5) 86.4 ^(0.7)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7) 46.0 ^(6.7) 36.3 ^(6.9) 23.4 ^(8.5) 37.4 ^(6.2) 37.4 ^(6.2) 37.7 ^(6.4) 23.0 ^(6.0) 28.7 ^(1.8) 28.9 ^(1.1) 28.9 ^(1.1)	62.7 ^(13.1) 67.5 ^(14.1) D'Kitty 77.8 65.1 ^(14.4) 90.1 ^(14.4) 70.0 ^(12.0) 68.7 ^(12.1) 68.7 ^(12.1) 56.8 ^(19.8) 87.8 ^(4.3) 63.6 ^(15.6) 65.6 ^(14.1) 72.4 ^(1.8) 79.1 ^(0.7) 79.1 ^(0.9)	$3.0 \\ 1.2 \\ \hline Rank \downarrow \\ \hline \\ 3.2 \\ 1.2 \\ 3.0 \\ 2.7 \\ \hline \\ 2.3 \\ 3.0 \\ 2.2 \\ 2.3 \\ \hline \\ 2.3 \\ 2.3 \\ \hline \\ 2.3 \\ 2.3 \\ \hline \\ 2.3 \\ 2.3 \\ \hline \\ 2.3 \\ 2.3 \\ 2.3 \\ \hline \\ 2.3$	12.3 Opt. Gap
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. Adam AMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1) 63.8 ^(13.7) 50.5 ^(6.5) 47.0 ^(2.8) 54.7 ^(8.8) 49.5 ^(8.9) 54.0 ^(9.9) 47.7 ^(3.0) 48.5 ^(1.5) 46.4 ^(1.8)	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8 58.6 ^(13.1) 75.3 ^(9.9) 58.6 ^(13.1) 69.8 ^(6.0) 60.4 ^(12.7) 55.7 ^(12.7) 60.5 ^(12.6) 69.0 ^(5.2) 59.9 ^(2.0)	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3) 59.7 ^(8.7) 61.9 ^(2.2) 59.2 ^(8.6) 57.7 ^(9.1) 59.3 ^(8.6) 62.4 ^(1.9) 63.3 ^(0.0)	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7) 91.6 ^(11.2) 85.1 ^(8.1) 85.9 ^(0.4) 87.9 ^(10.0) 84.3 ^(9.6) 85.9 ^(10.8) 86.4 ^(0.6)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7) 46.0 ^(6.7) 36.3 ^(6.9) 23.4 ^(8.5) 37.4 ^(6.2) 37.4 ^(6.2) 37.4 ^(6.2) 37.7 ^(6.4) 23.0 ^(6.0) 28.7 ^(1.8) 28.9 ^(1.1)	62.7 ^(13.1) 67.5 ^(14.1) D'Kitty 77.8 65.1 ^(14.4) 90.1 ^(14.4) 70.0 ^(12.0) 68.7 ^(12.1) 68.7 ^(12.1) 56.8 ^(19.8) 87.8 ^(4.3) 63.6 ^(15.6) 65.6 ^(14.1) 72.4 ^(1.8) 79.1 ^(0.7)	$3.0 \\ 1.2 \\ \hline Rank \downarrow \\ \hline \\ 3.2 \\ 1.2 \\ 3.0 \\ 2.7 \\ \hline \\ 2.3 \\ 3.0 \\ 2.2 \\ 2.3 \\ 2.5 \\ 2.2 \\ 2.5 \\ 2.2 \\ \hline \\ 2.2 \\ 2.2 \\ 2.5 \\ 2.2 \\ \hline \\ 2.5 \\ 2.2 \\ 2.5 \\ 2.2 \\ 2.5 \\ 2.2 \\ 2.5 \\ 2.2 \\ 2.5 \\ 2.2 \\ 2.5 \\ 2.2 \\ 2.5 \\ 2.2 \\ 2.5 \\ 2.5 \\ 2.2 \\ 2.5 \\$	12.3 Opt. Gap ↑
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. DynAMO-Grad. Adam Adam AMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1) 63.8 ^(13.7) 50.5 ^(6.5) 47.0 ^(2.8) 54.7 ^(8.8) 49.5 ^(8.9) 54.0 ^(9.9) 47.7 ^(3.0) 48.5 ^(1.5) 46.4 ^(1.8) 50.5 ^(1.5) 51.5 ^(0.9) 50.3 ^(1.8)	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8 58.6 ^(13.1) 75.3 ^(9.9) 58.6 ^(13.1) 69.8 ^(6.0) 60.4 ^(12.7) 55.7 ^(12.7) 60.5 ^(12.6) 69.0 ^(5.2) 59.9 ^(2.0) 63.4 ^(3.3) 61.1 ^(2.8) 65.6 ^(3.1)	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3) 59.7 ^(8.7) 61.9 ^(2.2) 59.2 ^(8.6) 57.7 ^(9.1) 59.3 ^(8.6) 62.4 ^(1.9) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0)	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7) 91.6 ^(11.2) 85.1 ^(8.1) 85.9 ^(0.4) 87.9 ^(10.0) 84.3 ^(9.6) 85.9 ^(10.8) 86.4 ^(0.6) 86.3 ^(0.5) 86.4 ^(0.7) 86.7 ^(0.6)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7) 46.0 ^(6.7) 36.3 ^(6.9) 23.4 ^(8.5) 37.4 ^(6.2) 37.4 ^(6.2) 37.4 ^(6.2) 37.7 ^(6.4) 23.0 ^(6.0) 28.7 ^(1.8) 28.9 ^(1.1) 28.4 ^(0.7) 23.5 ^(2.4)	62.7 ^(13.1) 67.5 ^(14.1) D'Kitty 77.8 65.1 ^(14.4) 90.1 ^(14.4) 70.0 ^(12.0) 68.7 ^(12.1) 56.8 ^(19.8) 87.8 ^(4.3) 63.6 ^(15.6) 65.6 ^(14.1) 72.4 ^(1.8) 79.1 ^(0.7) 79.1 ^(0.9) 77.0 ^(0.7)	$3.0 \\ 1.2 \\ \hline Rank \downarrow \\ \hline \\ 3.2 \\ 1.2 \\ 3.0 \\ 2.7 \\ \hline \\ 2.3 \\ 3.0 \\ 2.2 \\ 2.3 \\ 2.5 \\ 2.2 \\ 2.3 \\ 2.0 \\ \hline \\ 2.0 \\ \hline \\ 2.0 \\ \hline \\ 1.2$	12.3 Opt. Gap ↑
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam BO-qEI DynAMO-BO-qEI DynAMO-BO-qEI DynAMO-BO-qEI DynAMO-BO-qEI	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1) 63.8 ^(13.7) 50.5 ^(6.5) 47.0 ^(2.8) 54.7 ^(8.8) 49.5 ^(8.9) 54.0 ^(9.9) 47.7 ^(3.0) 48.5 ^(1.5) 46.4 ^(1.8) 50.5 ^(1.5) 51.5 ^(0.9) 50.3 ^(1.8) 47.9 ^(1.9)	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8 58.6 ^(13.1) 75.3 ^(9.9) 58.6 ^(13.1) 69.8 ^(6.0) 60.4 ^(12.7) 55.7 ^(12.7) 60.5 ^(12.6) 69.0 ^(5.2) 59.9 ^(2.0) 63.4 ^(3.3) 61.1 ^(2.8) 65.6 ^(3.1) 62.1 ^(3.4) 59.8 ^(1.2)	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3) 59.7 ^(8.7) 61.9 ^(2.2) 59.2 ^(8.6) 57.7 ^(9.1) 59.3 ^(8.6) 62.4 ^(1.9) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0)	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7) 91.6 ^(11.2) 85.1 ^(8.1) 85.9 ^(0.4) 87.9 ^(10.0) 84.3 ^(9.6) 85.9 ^(10.8) 86.4 ^(0.6) 86.7 ^(0.6) 86.6 ^(0.6) 86.6 ^(0.6) 86.0 ^(0.6)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7) 46.0 ^(6.7) 36.3 ^(6.9) 23.4 ^(8.5) 37.4 ^(6.2) 37.4 ^(6.2)	62.7 ^(13.1) 67.5 ^(14.1) D'Kitty 77.8 65.1 ^(14.4) 90.1 ^(14.4) 70.0 ^(12.0) 68.7 ^(12.1) 56.8 ^(19.8) 87.8 ^(4.3) 63.6 ^(15.6) 65.6 ^(14.1) 72.4 ^(1.8) 79.1 ^(0.7) 79.1 ^(0.9) 77.0 ^(0.7) 74.4 ^(0.6) 73.8 ^(1.2)	$3.0 \\ 1.2 \\ \hline Rank \downarrow \\ \hline \\ 3.2 \\ 1.2 \\ 3.0 \\ 2.7 \\ \hline \\ 2.3 \\ 3.0 \\ 2.2 \\ 2.3 \\ 2.5 \\ 2.2 \\ 2.3 \\ 2.0 \\ \hline \\ 1.7 \\ \hline $	12.3 Opt. Gap 1
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. DynAMO-Grad. Adam AMO-Adam DynAMO-Adam DynAMO-Adam BO-qEI AMO-BO-qEI DynAMO-BO-qEI DynAMO-BO-qUCB	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1) 63.8 ^(13.7) 50.5 ^(6.5) 47.0 ^(2.8) 54.7 ^(8.8) 49.5 ^(8.9) 54.0 ^(9.9) 47.7 ^(3.0) 48.5 ^(1.5) 46.4 ^(1.8) 50.5 ^(1.5) 51.5 ^(0.9) 50.3 ^(1.8) 47.9 ^(1.9) 50.3 ^(1.7)	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8 58.6 ^(13.1) 75.3 ^(9.9) 58.6 ^(13.1) 69.8 ^(6.0) 60.4 ^(12.7) 55.7 ^(12.7) 60.5 ^(12.6) 69.0 ^(5.2) 59.9 ^(2.0) 63.4 ^(3.3) 61.1 ^(2.8) 65.6 ^(3.1) 62.1 ^(3.4) 59.8 ^(1.2) 60.1 ^(2.2)	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3) 59.7 ^(8.7) 61.9 ^(2.2) 59.2 ^(8.6) 62.4 ^(1.9) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0)	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7) 91.6 ^(11.2) 85.1 ^(8.1) 85.9 ^(0.4) 87.9 ^(10.0) 84.3 ^(9.6) 85.9 ^(10.8) 86.4 ^(0.6) 86.7 ^(0.6) 86.4 ^(0.6) 86.6 ^(0.6) 86.4 ^(0.6)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7) 46.0 ^(6.7) 36.3 ^(6.9) 23.4 ^(8.5) 37.4 ^(6.2) 37.4 ^(6.2) 37.4 ^(6.2) 37.7 ^(6.4) 23.0 ^(6.0) 28.7 ^(1.8) 28.9 ^(1.1) 28.4 ^(0.7) 23.5 ^(2.4) 31.7 ^(1.2) 33.1 ^(2.9) 32.4 ^(2.7)	62.7 ^(13.1) 67.5 ^(14.1) D'Kitty 77.8 65.1 ^(14.4) 90.1 ^(14.4) 70.0 ^(12.0) 68.7 ^(12.1) 56.8 ^(19.8) 87.8 ^(4.3) 63.6 ^(15.6) 65.6 ^(14.1) 72.4 ^(1.8) 79.1 ^(0.7) 79.1 ^(0.9) 77.0 ^(0.7) 74.4 ^(0.6) 73.8 ^(1.2)	$3.0 \\ 1.2 \\ \hline Rank \downarrow \\ \hline \\ 3.2 \\ 1.2 \\ 3.0 \\ 2.7 \\ \hline \\ 2.3 \\ 3.0 \\ 2.2 \\ 2.3 \\ 2.5 \\ 2.2 \\ 2.3 \\ 2.0 \\ \hline \\ 1.7 \\ 2.8 \\ \hline \end{cases}$	12.3 Opt. Gap 1
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. DynAMO-Grad. Mo-Adam DynAMO-Adam DynAMO-Adam BO-qEI AMO-BO-qEI DynAMO-BO-qEI DynAMO-BO-qUCB AMO-BO-qUCB	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1) 63.8 ^(13.7) 50.5 ^(6.5) 47.0 ^(2.8) 54.7 ^(8.8) 49.5 ^(8.9) 54.0 ^(9.9) 47.7 ^(3.0) 48.5 ^(1.5) 46.4 ^(1.8) 50.5 ^(1.5) 51.5 ^(0.9) 50.3 ^(1.8) 47.9 ^(1.9) 50.3 ^(1.7)	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8 58.6 ^(13.1) 75.3 ^(9.9) 58.6 ^(13.1) 69.8 ^(6.0) 60.4 ^(12.7) 55.7 ^(12.7) 60.5 ^(12.6) 69.0 ^(5.2) 59.9 ^(2.0) 63.4 ^(3.3) 61.1 ^(2.8) 65.6 ^(3.1) 62.1 ^(3.4) 59.8 ^(1.2) 60.1 ^(2.2)	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3) 59.7 ^(8.7) 61.9 ^(2.2) 59.2 ^(8.6) 62.4 ^(1.9) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0) 63.3 ^(0.0)	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7) 91.6 ^(11.2) 85.1 ^(8.1) 85.9 ^(0.4) 87.9 ^(10.0) 84.3 ^(9.6) 85.9 ^(10.8) 86.4 ^(0.6) 86.7 ^(0.6) 86.4 ^(0.6) 86.6 ^(0.6) 86.4 ^(0.6)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7) 46.0 ^(6.7) 36.3 ^(6.9) 23.4 ^(8.5) 37.4 ^(6.2) 37.4 ^(6.2) 37.4 ^(6.2) 37.7 ^(6.4) 23.0 ^(6.0) 28.7 ^(1.8) 28.9 ^(1.1) 28.4 ^(0.7) 23.5 ^(2.4) 31.7 ^(1.2) 33.1 ^(2.9) 32.4 ^(2.7)	62.7 ^(13.1) 67.5 ^(14.1) D'Kitty 77.8 65.1 ^(14.4) 90.1 ^(14.4) 70.0 ^(12.0) 68.7 ^(12.1) 68.7 ^(12.1) 56.8 ^(19.8) 87.8 ^(4.3) 63.6 ^(15.6) 65.6 ^(14.1) 72.4 ^(1.8) 79.1 ^(0.7) 79.1 ^(0.9) 77.0 ^(0.7) 74.4 ^(0.6) 73.8 ^(1.2) 74.3 ^(0.8)	$3.0 \\ 1.2 \\ \hline Rank \downarrow \\ \hline \\ 3.2 \\ 1.2 \\ 3.0 \\ 2.7 \\ \hline \\ 2.3 \\ 3.0 \\ 2.2 \\ 2.3 \\ 2.5 \\ 2.2 \\ 2.3 \\ 2.0 \\ \hline \\ 1.7 \\ \hline $	12.3 Opt. Gap 7
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam BO-qEI AMO-BO-qEI DynAMO-BO-qEI DynAMO-BO-qUCB AMO-BO-qUCB DynAMO-BO-qUCB	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1) 63.8 ^(13.7) 50.5 ^(6.5) 47.0 ^(2.8) 54.7 ^(8.8) 49.5 ^(8.9) 54.0 ^(9.9) 47.7 ^(3.0) 48.5 ^(1.5) 46.4 ^(1.8) 50.5 ^(1.5) 51.5 ^(0.9) 50.3 ^(1.8) 47.9 ^(1.9) 50.3 ^(1.7) 48.8 ^(1.8)	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8 58.6 ^(13.1) 75.3 ^(9.9) 58.6 ^(13.1) 69.8 ^(6.0) 60.4 ^(12.7) 55.7 ^(12.7) 60.5 ^(12.6) 69.0 ^(5.2) 59.9 ^(2.0) 63.4 ^(3.3) 61.1 ^(2.8) 65.6 ^(3.1) 62.1 ^(3.4) 59.8 ^(1.2) 60.1 ^(2.2) 63.9 ^(3.7)	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3) 59.7 ^(8.7) 61.9 ^(2.2) 59.2 ^(8.6) 57.7 ^(9.1) 59.3 ^(8.6) 62.4 ^(1.9) 63.3 ^(0.0) 63.3 ^(0.0)	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7) 91.6 ^(11.2) 85.1 ^(8.1) 85.9 ^(0.4) 87.9 ^(10.0) 84.3 ^(9.6) 85.9 ^(10.8) 86.4 ^(0.6) 86.3 ^(0.5) 86.4 ^(0.6) 86.6 ^(0.6) 86.4 ^(0.6) 86.5 ^(0.5) 86.5 ^(0.5)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7) 46.0 ^(6.7) 36.3 ^(6.9) 23.4 ^(8.5) 37.4 ^(6.2) 37.4 ^(6.2) 37.4 ^(6.2) 37.7 ^(6.4) 23.0 ^(6.0) 28.7 ^(1.8) 28.9 ^(1.1) 28.4 ^(0.7) 23.5 ^(2.4) 31.7 ^(1.2) 33.1 ^(2.9) 32.4 ^(2.7) 22.7 ^(2.0)	62.7 ^(13.1) 67.5 ^(14.1) 77.8 65.1 ^(14.4) 90.1 ^(14.4) 70.0 ^(12.0) 68.7 ^(12.1) 56.8 ^(19.8) 87.8 ^(4.3) 63.6 ^(15.6) 65.6 ^(14.1) 72.4 ^(1.8) 79.1 ^(0.7) 79.1 ^(0.7) 74.4 ^(0.6) 73.8 ^(1.2) 74.3 ^(0.8) 50.4 ^(14.6)	$3.0 \\ 1.2 \\ \hline Rank \downarrow \\ \hline \\ - \\ 3.2 \\ 1.2 \\ 3.0 \\ 2.7 \\ \hline \\ 2.3 \\ 3.0 \\ 2.2 \\ 2.3 \\ 2.5 \\ \hline \\ 2.5 \\ 2.2 \\ 2.3 \\ 2.0 \\ \hline \\ 1.7 \\ 2.8 \\ 2.0 \\ 2.5 \\ \hline \\ 2.5 \\ 2.5 \\ \hline \\ 2.5$	12.3 Opt. Gap ↑
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. DynAMO-Grad. Mama Adam Adam Adam Adam Adam Adam Adam A	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1) 63.8 ^(13.7) 50.5 ^(6.5) 47.0 ^(2.8) 54.7 ^(8.8) 49.5 ^(8.9) 54.0 ^(9.9) 47.7 ^(3.0) 48.5 ^(1.5) 46.4 ^(1.8) 50.5 ^(1.5) 51.5 ^(0.9) 50.3 ^(1.3) 47.9 ^(1.9) 50.3 ^(1.7) 48.8 ^(1.8) 50.7 ^(2.7)	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8 58.6 ^(13.1) 75.3 ^(9.9) 58.6 ^(13.1) 69.8 ^(6.0) 60.4 ^(12.7) 55.7 ^(12.7) 60.5 ^(12.6) 69.0 ^(5.2) 59.9 ^(2.0) 63.4 ^(3.3) 61.1 ^(2.8) 65.6 ^(3.1) 62.1 ^(3.4) 59.8 ^(1.2) 60.1 ^(2.2) 63.9 ^(3.7) 71.7 ^(10.4)	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3) 59.7 ^(8.7) 61.9 ^(2.2) 59.2 ^(8.6) 57.7 ^(9,1) 59.3 ^(8.6) 62.4 ^(1.9) 63.3 ^(0.0) 63.3 ^(0.0)	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7) 91.6 ^(11.2) 85.1 ^(8.1) 85.9 ^(0.4) 87.9 ^(10.0) 84.3 ^(9.6) 85.9 ^(10.8) 86.4 ^(0.6) 86.3 ^(0.5) 86.4 ^(0.6) 86.6 ^(0.6) 86.6 ^(0.6) 86.5 ^(0.5) 86.5 ^(0.5) 83.9 ^(1.0)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7) 46.0 ^(6.7) 46.0 ^(6.7) 36.3 ^(6.9) 23.4 ^(8.5) 37.4 ^(6.2) 37.4 ^(6.2) 37.7 ^(6.4) 23.0 ^(6.0) 28.7 ^(1.8) 28.9 ^(1.1) 28.4 ^(0.7) 23.5 ^(2.4) 31.7 ^(1.2) 33.1 ^(2.9) 32.4 ^(2.7) 22.7 ^(2.0) 37.9 ^(0.7)	62.7 ^(13.1) 67.5 ^(14.1) D'Kitty 77.8 65.1 ^(14.4) 90.1 ^(14.4) 70.0 ^(12.0) 68.7 ^(12.1) 56.8 ^(19.8) 87.8 ^(4.3) 63.6 ^(15.6) 65.6 ^(14.1) 72.4 ^(1.8) 79.1 ^(0.7) 79.1 ^(0.7) 74.4 ^(0.6) 73.8 ^(1.2) 74.3 ^(0.8) 50.4 ^(14.6) 59.3 ^(10.9)	$3.0 \\ 1.2 \\ \hline Rank \downarrow \\ \hline \\ 3.2 \\ 1.2 \\ 3.0 \\ 2.7 \\ \hline \\ 2.3 \\ 3.0 \\ 2.2 \\ 2.3 \\ 2.5 \\ 2.2 \\ 2.3 \\ 2.0 \\ 1.7 \\ 2.8 \\ 2.0 \\ 2.5 \\ 2.2 \\ 2.5 \\ 2.2 \\ 2.3 \\ 2.0 \\ 1.7 \\ 2.8 \\ 2.0 \\ 2.5 \\ 2.2 \\ 2.2 \\ 1.7 \\ 2.8 \\ 2.0 \\ 2.5 \\ 2.2 \\ 1.7 \\ 2.8 \\ 2.0 \\ 2.5 \\ 2.2 \\ 1.7 \\ 2.8 \\ 2.0 \\ 2.5 \\ 2.2 \\ 1.7 \\ 1.7 \\ 2.8 \\ 2.0 \\ 2.5 \\ 2.2 \\ 1.7 \\ 1.7 \\ 1.8 \\ 1.7 \\ 1.8 \\ 1.7 \\ 1.8 \\ 1.7 \\ 1.8 \\ 1.7 \\ 1.8 \\ 1.7 \\ 1.8 \\ 1.7 \\ 1.8 \\ 1.7 \\ 1.8 \\ 1.7 \\ 1.8 \\ 1.7 \\ 1.8 \\ 1.7 \\ 1.8 \\ 1.7 \\ 1.8 \\ 1.7 \\ 1.8 \\ 1.7 \\ 1.8 \\ 1.7 \\ 1.8 \\ 1.8 \\ 1.7 \\ 1.8$	12.3 Opt. Gap ↑
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. DynAMO-Grad. Mo-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam BO-qEI AMO-BO-qEI DynAO-BO-qEI DynAO-BO-qUCB DynAO-BO-qUCB DynAMO-BO-qUCB DynAMO-BO-qUCB DynAMO-BO-qUCB	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1) 63.8 ^(13.7) 50.5 ^(6.5) 47.0 ^(2.8) 54.7 ^(8.8) 49.5 ^(8.9) 54.0 ^(9.9) 47.7 ^(3.0) 48.5 ^(1.5) 46.4 ^(1.3) 50.5 ^(1.5) 51.5 ^(0.9) 50.3 ^(1.8) 47.9 ^(1.9) 50.3 ^(1.7) 48.8 ^(1.8) 50.7 ^(2.7) 44.2 ^(0.8)	$\begin{array}{r} {\color{red}{59.3}} {\color{red}{(10.8)}}\\ {\color{red}{77.2}} {\color{red}{(11.6)}}\\ {\color{red}{42.8}}\\ {\color{red}{42.8}}\\ {\color{red}{58.6}} {\color{red}{(13.1)}}\\ {\color{red}{75.3}} {\color{red}{(9.9)}}\\ {\color{red}{58.6}} {\color{red}{(13.1)}}\\ {\color{red}{59.8}} {\color{red}{(0.3)}}\\ {\color{red}{60.4}} {\color{red}{(12.7)}}\\ {\color{red}{55.7}} {\color{red}{(12.7)}}\\ {\color{red}{60.5}} {\color{red}{(12.7)}}\\ {\color{red}{60.5}} {\color{red}{(12.7)}}\\ {\color{red}{60.5}} {\color{red}{(12.2)}}\\ {\color{red}{63.4}} {\color{red}{(3.3)}}\\ {\color{red}{61.1}} {\color{red}{(2.2)}}\\ {\color{red}{65.9}} {\color{red}{(1.2)}}\\ {\color{red}{60.1}} {\color{red}{(2.2)}}\\ {\color{red}{65.9}} {\color{red}{(3.7)}}\\ {\color{red}{71.7}} {\color{red}{(10.4)}}\\ {\color{red}{72.7}} {\color{red}{(3.8)}}\\ {\color{red}{71.8}} {\color{red}{71.8}} {\color{red}{71.8}}\\ {\color{red}{71.8}} {\color{red}{71.8}}\\ {\color{red}{71.8}} {\color{red}{71.8}}\\ {\color{red}{71.8}} {\color{red}{71.8}}\\ {\color$	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3) 59.7 ^(8.7) 61.9 ^(2.2) 59.2 ^(8.6) 57.7 ^(9.1) 59.3 ^(8.6) 62.4 ^(1.9) 63.3 ^(0.0) 63.3 ^(0.0)	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7) 91.6 ^(11.2) 85.1 ^(8.1) 85.9 ^(0.4) 87.9 ^(10.0) 84.3 ^(9.6) 85.9 ^(10.8) 86.4 ^(0.6) 86.7 ^(0.6) 86.4 ^(0.6) 86.6 ^(0.6) 86.6 ^(0.6) 86.6 ^(0.6) 86.5 ^(0.5) 83.9 ^(1.0) 83.9 ^(1.0) 86.1 ^(0.5)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7) 46.0 ^(6.7) 36.3 ^(6.9) 23.4 ^(8.5) 37.4 ^(6.2) 37.4 ^(6.2) 28.7 ^(1.8) 28.7 ^(1.8) 28.7 ^(1.8) 28.7 ^(1.8) 28.7 ^(1.8) 28.7 ^(1.2) 33.1 ^(2.9) 32.4 ^(2.7) 22.7 ^(2.0) 37.9 ^(0.7) 21.4 ^(2.0)	62.7 ^(13.1) 67.5 ^(14.1) 77.8 65.1 ^(14.4) 90.1 ^(14.4) 70.0 ^(12.0) 68.7 ^(12.1) 56.8 ^(19.8) 87.8 ^(4.3) 63.6 ^(15.6) 65.6 ^(14.1) 72.4 ^(1.8) 79.1 ^(0.7) 79.1 ^(0.9) 77.0 ^(0.7) 74.4 ^(0.6) 73.8 ^(1.2) 74.3 ^(0.8) 50.4 ^(14.6) 59.3 ^(10.9) 54.9 ^(0.6)	$\begin{array}{r} 3.0\\ \textbf{1.2}\\ \hline \textbf{Rank} \downarrow \\ \hline \\ \hline \\ 3.2\\ \textbf{1.2}\\ 3.0\\ 2.7\\ \hline \\ 3.0\\ 2.7\\ \hline \\ 3.0\\ 2.2\\ 2.3\\ \hline \\ 2.5\\ 2.2\\ 2.3\\ 2.0\\ \hline \\ \textbf{1.7}\\ 2.8\\ \underline{2.0}\\ 2.5\\ \hline \\ 2.5\\ \hline \\ 2.2\\ 3.2\\ \hline \end{array}$	12.3 Opt. Gap 1
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. DynAMO-Grad. Mo-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam BO-qEI AMO-BO-qEI DynAO-BO-qEI DynAO-BO-qUCB AMO-BO-qUCB DynAMO-BO-qUCB DynAMO-BO-qUCB DynAMO-BO-qUCB DynAMO-BO-qUCB DynAMO-BO-qUCB DynAMO-BO-qUCB DynAMO-BO-qUCB	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1) 63.8 ^(13.7) 50.5 ^(6.5) 47.0 ^(2.8) 54.7 ^(8.8) 49.5 ^(8.9) 54.0 ^(9.9) 47.7 ^(3.0) 48.5 ^(1.5) 46.4 ^(1.8) 50.5 ^(1.5) 51.5 ^(0.9) 50.3 ^(1.8) 47.9 ^(1.9) 50.3 ^(1.7) 48.8 ^(1.8) 50.7 ^(2.7) 44.2 ^(0.8) 50.7 ^(2.7)	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8 58.6 ^(13.1) 75.3 ^(9.9) 58.6 ^(13.1) 69.8 ^(6.0) 60.4 ^(12.7) 55.7 ^(12.7) 60.5 ^(12.6) 69.0 ^(5.2) 59.9 ^(2.0) 63.4 ^(3.3) 61.1 ^(2.8) 65.6 ^(3.1) 62.1 ^(3.4) 59.8 ^(1.2) 60.1 ^(2.2) 60.3 ^(1.2) 60.1 ^(2.2) 65.9 ^(3.7) 71.7 ^(10.4) 72.7 ^(3.8) 75.2 ^(9.1)	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3) 59.7 ^(8.7) 61.9 ^(2.2) 59.2 ^(8.6) 57.7 ^(9.1) 59.3 ^(8.6) 62.4 ^(1.9) 63.3 ^(0.0) 63.3 ^(0.0)	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7) 91.6 ^(11.2) 85.1 ^(8.1) 85.9 ^(0.4) 87.9 ^(10.0) 84.3 ^(9.6) 85.9 ^(10.8) 86.4 ^(0.6) 86.7 ^(0.6) 86.4 ^(0.6) 86.6 ^(0.6) 86.6 ^(0.6) 86.6 ^(0.6) 86.6 ^(0.6) 86.6 ^(0.5) 86.3 ^(0.5) 86.1 ^(0.5) 82.5 ^(1.2)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7) 46.0 ^(6.7) 36.3 ^(6.9) 23.4 ^(8.5) 37.4 ^(6.2) 37.4 ^(6.2) 37.4 ^(6.2) 37.7 ^(6.4) 23.0 ^(6.0) 28.7 ^(1.8) 28.9 ^(1.1) 28.4 ^(0.7) 23.5 ^(2.4) 31.7 ^(1.2) 33.1 ^(2.9) 32.4 ^(2.7) 22.7 ^(2.0) 37.9 ^(0.7) 21.4 ^(2.0) 38.7 ^(3.9)	62.7 ^(13.1) 67.5 ^(14.1) 77.8 65.1 ^(14.4) 90.1 ^(14.4) 70.0 ^(12.0) 68.7 ^(12.1) 56.8 ^(19.8) 87.8 ^(4.3) 63.6 ^(15.6) 65.6 ^(14.1) 72.4 ^(1.8) 79.1 ^(0.7) 79.1 ^(0.9) 77.0 ^(0.7) 74.4 ^(0.6) 73.8 ^(1.2) 74.3 ^(0.8) 50.4 ^(14.6) 59.3 ^(10.9) 54.9 ^(9.6) 65.8 ^(9.1)	$3.0 \\ 1.2 \\ \hline Rank \downarrow \\ \hline \\ 3.2 \\ 1.2 \\ 3.0 \\ 2.7 \\ \hline \\ 2.3 \\ 3.0 \\ 2.2 \\ 2.3 \\ 3.0 \\ 2.2 \\ 2.3 \\ 2.5 \\ 2.2 \\ 2.3 \\ 2.0 \\ 1.7 \\ 2.8 \\ 2.0 \\ 2.5 \\ \hline \\ 2.5 \\ 2.2 \\ 3.2 \\ 1.7 \\ \hline \\ 1.7 \\ 1$	12.3 Opt. Gap - - 10.5 21.2 10.1 9.5 12.1 10.2 9.1 10.0 11.3 11.5 11.3 11.5 10.7 11.2 6.3 11.2 7.1 12.8
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. DynAMO-Grad. Adam AMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam BO-qEI AMO-BO-qEI DynAO-BO-qEI DynAO-BO-qUCB AMO-BO-qUCB DynAMO-BO-qUCB DynAMO-BO-qUCB DynAMO-BO-qUCB DynAMO-CMA-ES DynAMO-CMA-ES DynAMO-CMA-ES	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1) 63.8 ^(13.7) 50.5 ^(6.5) 47.0 ^(2.8) 54.7 ^(8.8) 49.5 ^(8.9) 54.0 ^(9.9) 47.7 ^(3.0) 48.5 ^(1.5) 46.4 ^(1.8) 50.5 ^(1.5) 51.5 ^(0.9) 50.3 ^(1.7) 48.8 ^(1.8) 50.7 ^(2.7) 44.2 ^(0.8) 50.7 ^(2.7) 44.2 ^(0.8) 50.7 ^(2.7) 45.3 ^(2.4)	$\begin{array}{r} {\color{red}{59.3}} {\color{red}{(10.8)}}\\ {\color{red}{77.2}} {\color{red}{(11.6)}}\\ {\color{red}{42.8}}\\ {\color{red}{42.8}}\\ {\color{red}{58.6}} {\color{red}{(13.1)}}\\ {\color{red}{75.3}} {\color{red}{9.9}}\\ {\color{red}{58.6}} {\color{red}{(13.1)}}\\ {\color{red}{69.8}} {\color{red}{60.4}}\\ {\color{red}{69.8}} {\color{red}{(12.7)}}\\ {\color{red}{55.7}} {\color{red}{(12.7)}}\\ {\color{red}{60.5}} {\color{red}{(12.7)}}\\ {\color{red}{69.0}} {\color{red}{(12.7)}}\\ {\color{red}{55.7}} {\color{red}{(12.6)}}\\ {\color{red}{69.0}} {\color{red}{(12.7)}}\\ {\color{red}{55.9}} {\color{red}{(12.6)}}\\ {\color{red}{63.4}} {\color{red}{(3.3)}}\\ {\color{red}{61.1}} {\color{red}{(2.2)}}\\ {\color{red}{65.6}} {\color{red}{(3.1)}}\\ {\color{red}{62.1}} {\color{red}{(3.4)}}\\ {\color{red}{59.8}} {\color{red}{(12.2)}}\\ {\color{red}{65.9}} {\color{red}{(3.7)}}\\ {\color{red}{71.7}} {\color{red}{(10.4)}}\\ {\color{red}{72.7}} {\color{red}{3.8}}\\ {\color{red}{75.2}} {\color{red}{9.1}}\\ {\color{red}{55.8}} {\color{red}{8.9}} {\color{red}{8.9}} \end{array}$	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3) 59.7 ^(8.7) 61.9 ^(2.2) 59.2 ^(8.6) 62.4 ^(1.9) 63.3 ^(0.0) 63.3 ⁽	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7) 91.6 ^(11.2) 85.1 ^(8.1) 85.9 ^(0.4) 87.9 ^(10.0) 84.3 ^(3.6) 85.9 ^(10.8) 86.7 ^(0.6) 86.7 ^(0.6) 86.7 ^(0.6) 86.7 ^(0.6) 86.6 ^(0.6) 86.6 ^(0.6) 86.6 ^(0.6) 86.6 ^(0.6) 86.7 ^(0.5) 86.7 ^(0.5) 86.7 ^(0.5) 86.7 ^(0.5) 86.7 ^(0.5) 86.7 ^(0.5) 86.7 ^(0.5) 86.7 ^(0.5) 86.7 ^(0.5) 86.9 ^(1.0) 86.1 ^(0.5) 83.9 ^(1.0) 85.1 ^(1.2) 99.0 ^(12.1)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7) 46.0 ^(6.7) 46.0 ^(6.7) 36.3 ^(6.9) 23.4 ^(8.5) 37.4 ^(6.2) 37.7 ^(6.4) 23.0 ^(6.0) 28.7 ^(1.8) 28.9 ^(1.1) 28.4 ^(0.7) 23.5 ^(2.4) 31.7 ^(1.2) 33.1 ^(2.9) 32.4 ^(2.7) 22.7 ^(2.0) 37.9 ^(0.7) 21.4 ^(2.0) 38.7 ^(3.9) 22.5 ^(5.1)	62.7 ^(13.1) 67.5 ^(14.1) 77.8 65.1 ^(14.4) 90.1 ^(14.4) 90.1 ^(14.4) 70.0 ^(12.0) 68.7 ^(12.1) 56.8 ^(19.8) 87.8 ^(4.3) 63.6 ^(15.6) 65.6 ^(14.1) 72.4 ^(1.8) 79.1 ^(0.7) 79.1 ^(0.7) 74.4 ^(0.6) 73.8 ^(1.2) 74.3 ^(0.8) 50.4 ^(14.6) 59.3 ^(10.9) 54.9 ^(9.6) 65.8 ^(9.1) 60.6 ^(15.0)	3.0 1.2 Rank ↓ 3.2 1.2 3.0 2.7 2.3 3.0 2.2 2.3 2.5 2.2 2.3 2.0 1.7 2.8 2.0 2.5 2.2 3.2 1.2 3.0 2.7 2.3 3.0 2.2 2.3 3.0 2.2 2.3 3.0 2.2 2.3 3.0 2.2 2.3 3.0 2.2 2.3 3.0 2.2 2.3 3.0 2.5 2.2 2.3 3.0 1.7 2.8 2.5 2.5 2.5 2.2 3.2 1.7 2.8 2.5 3.2 1.7 2.8 2.8 2.5 3.2 1.7 2.8 2.5 3.2 1.7 2.8 3.2 1.7 2.8 3.2 1.7 2.8 3.2 1.7 2.8 3.2 1.7 2.8 3.2 1.7 2.8 3.5	12.3 Opt. Gap 1
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. DynAMO-Grad. Mama Adam Adam Adam Adam Adam Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam BO-qEI AMO-BO-qEI DynAO-BO-qEI BO-qUCB AMO-BO-qUCB DynAO-BO-qUCB DynAO-BO-qUCB DynAO-BO-qUCB DynAO-BO-qUCB DynAMO-BO-qUCB DynAMO-BO-qUCB DynAMO-CMA-ES DynAMO-CMA-ES DynAMO-CMA-ES	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1) 63.8 ^(13.7) 50.5 ^(6.5) 47.0 ^(2.8) 54.7 ^(8.8) 49.5 ^(8.9) 54.0 ^(9.9) 47.7 ^(3.0) 48.5 ^(1.5) 46.4 ^(1.8) 50.5 ^(1.5) 51.5 ^(0.9) 50.3 ^(1.8) 47.9 ^(1.9) 50.3 ^(1.7) 48.8 ^(1.8) 50.7 ^(2.7) 44.2 ^(0.8) 50.7 ^(2.7) 44.2 ^(0.8) 50.7 ^(2.7) 44.2 ^(0.8) 50.7 ^(2.7) 44.2 ^(0.8) 50.3 ^(2.4) 55.3 ^(8.0)	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8 58.6 ^(13.1) 75.3 ^(9.9) 58.6 ^(13.1) 69.8 ^(6.0) 60.4 ^(12.7) 55.7 ^(12.7) 60.5 ^(12.6) 69.0 ^(5.2) 59.9 ^(2.0) 63.4 ^(3.3) 61.1 ^(2.8) 65.6 ^(3.1) 62.1 ^(3.4) 59.8 ^(1.2) 60.1 ^(2.2) 65.9 ^(3.7) 71.7 ^(10.4) 72.7 ^(3.8) 75.2 ^(9.1) 65.8 ^(8.9) 53.6 ^(10.2)	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3) 59.7 ^(8.7) 61.9 ^(2.2) 59.2 ^(8.6) 57.7 ^(9.1) 59.3 ^(8.6) 62.4 ^(1.9) 63.3 ^(0.0) 63.3 ^(0.0) 59.3 ^(3.8)	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7) 91.6 ^(11.2) 85.1 ^(8.1) 85.9 ^(0.4) 87.9 ^(10.0) 84.3 ^(0.6) 85.9 ^(10.8) 86.4 ^(0.6) 86.7 ^(0.6) 86.4 ^(0.6) 86.6 ^(0.6) 86.6 ^(0.6) 86.6 ^(0.6) 86.6 ^(0.6) 86.5 ^(0.5) 83.9 ^(1.0) 86.1 ^(0.5) 83.9 ^(1.0) 86.1 ^(0.5) 82.5 ^(1.2) 99.0 ^(12.1) 87.4 ^(16.6)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7) 46.0 ^(6.7) 46.0 ^(6.7) 36.3 ^(6.9) 23.4 ^(8.5) 37.4 ^(6.2) 37.4 ^(6.2) 28.7 ^(1.8) 28.7 ^(1.8) 28.7 ^(1.8) 28.4 ^(0.7) 23.5 ^(2.4) 31.7 ^(1.2) 33.1 ^(2.9) 32.4 ^(2.7) 22.7 ^(2.0) 37.9 ^(0.7) 21.4 ^(2.0) 38.7 ^(3.9) 22.5 ^(5.1) 36.6 ^(4.4)	62.7 ^(13.1) 67.5 ^(14.1) D'Kitty 77.8 65.1 ^(14.4) 90.1 ^(14.4) 70.0 ^(12.0) 68.7 ^(12.1) 56.8 ^(19.8) 87.8 ^(4.3) 63.6 ^(15.6) 65.6 ^(14.1) 72.4 ^(1.8) 79.1 ^(0.7) 79.1 ^(0.7) 74.4 ^(0.6) 73.8 ^(1.2) 74.3 ^(0.8) 50.4 ^(14.6) 59.3 ^(10.9) 54.9 ^(9.6) 65.8 ^(9.1) 60.6 ^(15.0)	3.0 1.2 Rank ↓ 3.2 1.2 3.0 2.7 2.3 3.0 2.2 2.3 2.5 2.2 2.3 2.5 2.2 2.3 2.0 1.7 2.8 2.0 2.5 2.2 3.2 1.7 2.8 2.5 2.2 3.2 1.7 2.8 2.5 2.2 3.2 1.7 2.8 2.5 3.2 1.7 2.8 2.5 3.2 1.7 2.8 2.5 3.2 1.7 2.8 2.5 3.2 1.7 2.8 2.5 3.2 1.7 2.8 2.5 3.5	12.3 Opt. Gap - - 10.5 21.2 10.1 9.5 9.5 12.1 10.2 9.1 10.0 11.3 11.5 11.3 11.5 10.7 11.2 6.3 11.2 7.1 12.8 8.8 8.9
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. DynAMO-Grad. Mo-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam BO-qEI MO-BO-qEI DynAO-BO-qEI DynAO-BO-qUCB DynAO-BO-qUCB DynAO-BO-qUCB DynAMO-BO-qUCB DynAMO-BO-qUCB DynAMO-BO-qUCB DynAMO-BO-qUCB DynAMO-CMA-ES DynAMO-CMA-ES DynAMO-CMA-ES DynAMO-CMA-ES	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1^(6.1) 63.8 ^(13.7) 50.5^(6.5) 47.0 ^(2.8) 54.7^(8.8) 49.5 ^(8.9) 54.7^(8.8) 49.5 ^(8.9) 54.7^(3.0) 48.5^(1.5) 46.4 ^(1.8) 50.5^(1.5) 51.5^(0.9) 50.3^(1.8) 47.9 ^(1.9) 50.3^(1.8) 47.9 ^(1.9) 50.3^(1.7) 48.8 ^(1.8) 50.7^(2.7) 44.2 ^(0.8) 50.7^(2.7) 44.2 ^(0.8) 50.7^(2.7) 44.2 ^(0.8) 50.7^(2.7) 44.2 ^(0.8) 50.7^(2.7) 44.2 ^(0.8) 50.7^(2.7) 44.2 ^(0.8) 50.7^(2.7) 45.3 ^(2.4) 55.3^(8.0) 59.5^(12.0)	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8 58.6 ^(13.1) 75.3 ^(9.9) 58.6 ^(13.1) 69.8 ^(6.0) 60.4 ^(12.7) 55.7 ^(12.7) 60.5 ^(12.6) 69.0 ^(5.2) 59.9 ^(2.0) 63.4 ^(3.3) 61.1 ^(2.8) 65.6 ^(3.1) 62.1 ^(3.4) 59.8 ^(1.2) 60.1 ^(2.2) 63.9 ^(1.2) 60.1 ^(2.2) 63.9 ^(3.7) 71.7 ^(10.4) 72.7 ^(3.8) 75.2 ^(9.1) 65.8 ^(8.9) 53.6 ^(10.2) 63.5 ^(11.2)	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3) 59.7 ^(8.7) 61.9 ^(2.2) 59.2 ^(8.6) 57.7 ^(9.1) 59.3 ^(8.6) 62.4 ^(1.9) 63.3 ^(0.0) 63.3 ^(0.0) 59.3 ^(3.8)	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7) 91.6 ^(11.2) 85.1 ^(8.1) 85.9 ^(0.4) 87.9 ^(10.0) 84.3 ^(9.6) 85.9 ^(10.8) 86.4 ^(0.6) 86.3 ^(0.5) 86.4 ^(0.6) 86.6 ^(0.6) 86.6 ^(0.6) 86.6 ^(0.6) 86.6 ^(0.6) 86.5 ^(0.5) 83.9 ^(1.0) 86.1 ^(0.5) 83.9 ^(1.0) 86.1 ^(0.5) 82.5 ^(1.2) 99.0 ^(12.1) 87.4 ^(16.6) 84.2 ^(17.2)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7) 46.0 ^(6.7) 46.0 ^(6.7) 36.3 ^(6.9) 23.4 ^(8.5) 37.4 ^(6.2) 37.4 ^(6.2) 37.7 ^(6.4) 23.0 ^(6.0) 28.7 ^(1.8) 28.9 ^(1.1) 28.4 ^(0.7) 23.5 ^(2.4) 31.7 ^(1.2) 33.1 ^(2.9) 32.4 ^(2.7) 22.7 ^(2.0) 37.9 ^(0.7) 21.4 ^(2.0) 38.7 ^(3.9) 22.5 ^(5.1) 36.6 ^(4.4) 36.6 ^(4.4)	62.7 ^(13.1) 67.5 ^(14.1) 77.8 65.1 ^(14.4) 90.1 ^(14.4) 70.0 ^(12.0) 68.7 ^(12.1) 56.8 ^(19.8) 87.8 ^(4.3) 63.6 ^(15.6) 65.6 ^(14.1) 72.4 ^(1.8) 79.1 ^(0.7) 79.1 ^(0.9) 77.0 ^(0.7) 74.4 ^(0.6) 73.8 ^(1.2) 74.3 ^(0.8) 50.4 ^(14.6) 59.3 ^(10.9) 54.9 ^(9.6) 65.8 ^(9.1) 60.6 ^(15.0) 59.3 ^(14.5) 59.3 ^(14.5)	3.0 1.2 Rank ↓ 3.2 1.2 3.0 2.7 2.3 3.0 2.2 2.3 2.5 2.2 2.3 2.5 2.2 2.3 2.0 1.7 2.8 2.0 2.5 2.2 3.2 1.7 2.8 2.0 2.5 2.2 3.2 1.7 2.8 2.5 2.2 3.2 1.7 2.8 2.5 2.5 2.2 3.2 1.7 2.8 2.5 2.5 2.5 2.2 3.2 1.7 2.8 2.5	12.3 Opt. Gap 7
DynMO-CoSyNE DynAMO-CoSyNE Median@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. DynAMO-Grad. Mama Adam Adam Adam Adam Adam Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam BO-qEI AMO-BO-qEI DynAO-BO-qEI BO-qUCB AMO-BO-qUCB DynAO-BO-qUCB DynAO-BO-qUCB DynAO-BO-qUCB DynAO-BO-qUCB DynAMO-BO-qUCB DynAMO-BO-qUCB DynAMO-CMA-ES DynAMO-CMA-ES DynAMO-CMA-ES	63.6 ^(10.1) 91.3 ^(4.4) TFBind8 33.7 58.1 ^(6.1) 63.8 ^(13.7) 50.5 ^(6.5) 47.0 ^(2.8) 54.7 ^(8.8) 49.5 ^(8.9) 54.0 ^(9.9) 47.7 ^(3.0) 48.5 ^(1.5) 46.4 ^(1.8) 50.5 ^(1.5) 51.5 ^(0.9) 50.3 ^(1.8) 47.9 ^(1.9) 50.3 ^(1.7) 48.8 ^(1.8) 50.7 ^(2.7) 44.2 ^(0.8) 50.7 ^(2.7) 44.2 ^(0.8) 50.7 ^(2.7) 44.2 ^(0.8) 50.7 ^(2.7) 44.2 ^(0.8) 50.3 ^(2.4) 55.3 ^(8.0)	59.3 ^(10.8) 77.2 ^(11.6) UTR 42.8 58.6 ^(13.1) 75.3 ^(9.9) 58.6 ^(13.1) 69.8 ^(6.0) 60.4 ^(12.7) 55.7 ^(12.7) 60.5 ^(12.6) 69.0 ^(5.2) 59.9 ^(2.0) 63.4 ^(3.3) 61.1 ^(2.8) 65.6 ^(3.1) 62.1 ^(3.4) 59.8 ^(1.2) 60.1 ^(2.2) 65.9 ^(3.7) 71.7 ^(10.4) 72.7 ^(3.8) 75.2 ^(9.1) 65.8 ^(8.9) 53.6 ^(10.2)	63.9 ^(1.6) 63.9 ^(0.9) ChEMBL 50.9 59.3 ^(8.6) 60.1 ^(3.3) 59.7 ^(8.7) 61.9 ^(2.2) 59.2 ^(8.6) 57.7 ^(9.1) 59.3 ^(8.6) 62.4 ^(1.9) 63.3 ^(0.0) 63.3 ^(0.0) 59.3 ^(3.8)	90.1 ^(12.7) 114 ^(7.0) Molecule 87.6 85.3 ^(7.7) 91.6 ^(11.2) 85.1 ^(8.1) 85.9 ^(0.4) 87.9 ^(10.0) 84.3 ^(0.6) 85.9 ^(10.8) 86.4 ^(0.6) 86.7 ^(0.6) 86.4 ^(0.6) 86.6 ^(0.6) 86.6 ^(0.6) 86.6 ^(0.6) 86.6 ^(0.6) 86.5 ^(0.5) 83.9 ^(1.0) 86.1 ^(0.5) 83.9 ^(1.0) 86.1 ^(0.5) 82.5 ^(1.2) 99.0 ^(12.1) 87.4 ^(16.6)	37.0 ^(4.1) 40.6 ^(8.6) Superconductor 6.7 36.0 ^(6.7) 46.0 ^(6.7) 46.0 ^(6.7) 36.3 ^(6.9) 23.4 ^(8.5) 37.4 ^(6.2) 37.4 ^(6.2) 28.7 ^(1.8) 28.7 ^(1.8) 28.7 ^(1.8) 28.4 ^(0.7) 23.5 ^(2.4) 31.7 ^(1.2) 33.1 ^(2.9) 32.4 ^(2.7) 22.7 ^(2.0) 37.9 ^(0.7) 21.4 ^(2.0) 38.7 ^(3.9) 22.5 ^(5.1) 36.6 ^(4.4)	62.7 ^(13.1) 67.5 ^(14.1) D'Kitty 77.8 65.1 ^(14.4) 90.1 ^(14.4) 70.0 ^(12.0) 68.7 ^(12.1) 56.8 ^(19.8) 87.8 ^(4.3) 63.6 ^(15.6) 65.6 ^(14.1) 72.4 ^(1.8) 79.1 ^(0.7) 79.1 ^(0.7) 74.4 ^(0.6) 73.8 ^(1.2) 74.3 ^(0.8) 50.4 ^(14.6) 59.3 ^(10.9) 54.9 ^(9.6) 65.8 ^(9.1) 60.6 ^(15.0)	3.0 1.2 Rank ↓ 3.2 1.2 3.0 2.7 2.3 3.0 2.2 2.3 2.5 2.2 2.3 2.5 2.2 2.3 2.0 1.7 2.8 2.0 2.5 2.2 3.2 1.7 2.8 2.5 2.2 3.2 1.7 2.8 2.5 2.2 3.2 1.7 2.8 2.5 3.2 1.7 2.8 2.5 3.2 1.7 2.8 2.5 3.2 1.7 2.8 2.5 3.2 1.7 2.8 2.5 3.2 1.7 2.8 2.5 3.5	12.3 Opt. Gap ↑ 10.5 21.2 10.1 9.5 12.1 10.2 9.1 10.0 11.3 11.5 10.7 11.2 6.3 11.2 7.1 12.8 8.8 8.9

2584

2585 Table A12. Diversity of Design Candidates in Ablation of Adversarial Critic Feedback (AMO) and Diversity in (DynMO) Model-2586 based Optimization. We evaluate our method (1) with the KL-divergence penalized-MBO objective as in (11) only (DynMO); (2) 2587 with the adversarial source critic-dependent constraint as introduced by Yao et al. (2024) only (AMO); and (3) with both algorithmic 2588 components as in DynAMO described in Algorithm 1. We report the pairwise diversity (resp., minimum novelty) oracle score achieved 2589 by the 128 evaluated designs in the top (resp., bottom) table. Metrics are reported mean^(95% confidence interval) across 10 random seeds, where 2590 higher is better. Bolded entries indicate average scores with an overlapping 95% confidence interval to the best performing method. 2591 Bolded (resp., Underlined) Rank and Optimality Gap (Opt. Gap) metrics indicate the best (resp., second best) for a given optimizer.

_	Pairwise Diversity@128	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	$\mathbf{Rank}\downarrow$	Opt. Gap ↑
	Dataset \mathcal{D}	65.9	57.3	60.0	36.7	66.0	85.7	_	
	Grad.	12.5(8.0)	7.8 ^(8.8)	7.9 ^(7.8)	24.1(13.3)	$0.0^{(0.0)}$	$0.0^{(0.0)}$	3.0	-53.2
	AMO-Grad.	$17.3^{(12.8)}$	$11.2^{(10.3)}$	$6.9^{(7.7)}$	22.1(10.5)	$0.0^{(0.0)}$	$1.5^{(3.2)}$	2.7	-52.1
	DynMO-Grad.	$20.9^{(15.1)}$	$30^{(3.2)}$	58.2 ^(24.0)	$13.5^{(8.6)}$	$0.0^{(0.0)}$	$0.0^{(0.0)}$	3.0	-46.0
	Dyn <u>A</u> MO-Grad.	66.9 ^(6.9)	68.2 ^(10.8)	77.2 ^(21.5)	93.0 ^(1.2)	129 ^(55.3)	104 ^(56.1)	1.0	27.8
_	Adam	12.0(12.3)	11.0(12.1)	4.8(3.8)	16.8(12.4)	6.4 ^(14.5)	6.2(14.0)	3.0	-52.4
	AMO-Adam	15.1 ^(11.2)	$10.3^{(11.5)}$	12.1(11.3)	19.6 ^(15.2)	0.3 ^(0.8)	$2.6^{(3.9)}$	3.0	-51.9
	DynMO-Adam	13.1 ^(11.4)	$10.3^{(9.6)}$	57.0 ^(26.0)	23.8(15.1)	$64^{(14.5)}$	$0.0^{(0.0)}$	2.8	-43.5
	Dyn <u>A</u> MO-Adam	54.8 ^(8.9)	72.3 ^(3.4)	84.8 ^(9.2)	89.9 ^(5.3)	158 ^(37.3)	126 ^(57.3)	1.0	35.7
_	BO-qEI	73.7 ^(0.6)	73.8 ^(0.5)	99.3 ^(0.1)	93.0 ^(0.5)	190 ^(0.8)	124 ^(7.4)	3.7	47.1
	AMO-BO-qEI	74.0 ^(0.6)	74.3 ^(0.4)	99.3 ^(0.1)	93.3 ^(0.4)	193 ^(1.2)	17.7 ^(3.5)	2.8	30.0
	DynMO-BO-qEI	74.5 ^(0.3)	74.3 ^(0.6)	99.3 ^(0.1)	93.3 ^(0.7)	200 ^(3.0)	135(11.2)	2.3	50.8
	DynAMO-BO-qEI	74.8 ^(0.2)	74.6 ^(0.3)	99.4 ^(0.1)	93.5 ^(0.4)	198 ^(1.9)	277 ^(59.7)	1.2	74.2
	BO-qUCB	73.9(0.5)	74.3(0.4)	99.4 ^(0.1)	93.6 ^(0.5)	198 ^(10.3)	94.1 ^(3.9)	2.5	43.5
	AMO-BO-qUCB	74.0 ^(0.5)	74.3 ^(0.3)	99.3 ^(0.1)	93.4 ^(0.4)	190 ^(9.3)	$22.0^{(2.1)}$	3.7	30.3
	DynMO-BO-qUCB	74.7 ^(0.2)	74.3 ^(0.4)	99.2 ^(0.1)	93.6 ^(0.5)	198 ^(12.0)	92.6 ^(3.8)	<u>2.2</u>	<u>43.5</u>
	DynAMO-BO-qUCB	74.3 ^(0.5)	74.4 ^(0.6)	99.3 ^(0.1)	93.5 ^(0.6)	211 ^(22.8)	175 ^(44.7)	$\frac{2.2}{1.7}$	43.3 59.4
_	CMA-ES	47.2(11.2)	44.6(15.9)	93.5 ^(2.0)	66.2 ^(9.4)	12.8 ^(0.6)	164 ^(10.6)	2.3	9.5
	AMO-CMA-ES	47.2 39.6 ^(15.5)	$53.4^{(8.4)}$	93.5 84.8 ^(4.8)	61.3 ^(14.6)	173 ^(19,4)	59.9 ^(19.6)	$\frac{2.3}{2.3}$	9.5
	DynMO-CMA-ES	33.5 ^(2.6)	$11.1^{(1.1)}$	34.5 ^(2.8)	$4.5^{(5.0)}$	38.1 ^(5.4)	$14.4^{(1.2)}$	$\frac{2.3}{3.8}$	-39.3
	DynAMO-CMA-ES	73.6 ^(0.6)	73.1 ^(3.1)	72.0 ^(3.1)	94.0 ^(0.5)	97.8 ^(13.2)	292 ^(83.5)	5.8 1.5	-39.5 55.2
	CoSyNE	5.6 ^(5.0)	12.7 ^(9.8)	28.2(11.3)	12.2 ^(7.3)	0.0 ^(0.0)	0.0 ^(0.0)	2.8	-52.1
	AMO-CoSyNE	$5.0^{(5.7)}$	9.1 ^(9.0)	28.2 28.4 ^(15.7)	7.1 ^(8.0)	$0.0^{(0.0)}$	$0.0^{(0.0)}$	2.8 3.7	-52.1
		5.2	7.1	20.4	/.1	0.0	0.0		
		27 4(10.3)	13 0 ^(11.8)	53 3(24.2)	18 1(13.8)	$0.0^{(0.0)}$	0 0(0.0)		
	DynMO-CoSyNE DynAMO-CoSyNE	$27.4^{(10.3)} \\ 18.1^{(13.0)}$	$\frac{13.0^{(11.8)}}{20.3^{(2.3)}}$	53.3 ^(24.2) 35.0 ^(17.9)	18.1 ^(13.8) 22.8 ^(11.9)	0.0 ^(0.0) 74.4 ^(46.3)	0.0 ^(0.0) 77.0 ^(35.9)	<u>2.2</u> 1.3	<u>-43.3</u> -20.7
=	DynMO-CoSyNE Dyn <u>A</u> MO-CoSyNE	18.1 ^(13.0)	20.3 ^(2.3)	35.0 ^(17.9)	22.8 ^(11.9)	74.4 ^(46.3)	77 .0 ^(35.9)	1.3	-20.7
	DynMO-CoSyNE DynAMO-CoSyNE Minimum Novelty@128	18.1 ^(13.0) TFBind8	20.3 ^(2.3) UTR	35.0 ^(17.9) ChEMBL	22.8 ^(11.9) Molecule	74.4 ^(46.3) Superconductor	77.0 ^(35.9) D'Kitty		
=	DynMO-CoSyNE DynAMO-CoSyNE Minimum Novelty@128 Dataset D	18.1 ^(13.0) TFBind8 0.0	20.3 ^(2.3) UTR 0.0	35.0 ^(17.9) ChEMBL 0.0	22.8 ^(11.9) Molecule 0.0	74.4 ^(46.3) Superconductor 0.0	77.0 ^(35.9) D'Kitty 0.0	1.3 Rank↓	-20.7 Opt. Gap↑
=	DynMO-CoSyNE DynAMO-CoSyNE Minimum Novelty@128 Dataset ⊅ Grad.	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0)	20.3 ^(2.3) UTR 0.0 51.7 ^(2.9)	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3.9)	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0.7)	77.0 ^(35.9) D'Kitty 0.0 102 ^(6.1)	1.3 Rank ↓ 2.3	-20.7 Opt. Gap 1 — 74.5
_	DynMO-CoSyNE DynAMO-CoSyNE Minimum Novelty@128 Dataset D Grad. AMO-Grad.	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0)	20.3 ^(2.3) UTR 0.0 51.7 ^(2.9) 46.7 ^(2.7)	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3.9) 96.8 ^(3.9)	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0.7) 83.8 ^(6.8)	77.0 ^(35.9) D'Kitty 0.0 102 ^(6.1) 31.5 ^(3.6)	1.3 Rank ↓ 2.3 3.8	-20.7 Opt. Gap 1
	DynMO-CoSyNE DynAMO-CoSyNE Minimum Novelty@128 Dataset D Grad. AMO-Grad. DynMO-Grad.	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0) 21.9 ^(3.0)	20.3 ^(2.3) UTR 0.0 51.7 ^(2.9) 46.7 ^(2.7) 53.6 ^(2.1)	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3.9) 96.8 ^(3.9) 93.1 ^(6.6)	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7) 86.4 ^(10.2)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0.7) 83.8 ^(6.8) 95.0 ^(0.7)	77.0 ^(35.9) D'Kitty 0.0 102 ^(6.1) 31.5 ^(3.6) 102 ^(6.1)	1.3 Rank↓ 2.3 3.8 <u>1.8</u>	-20.7 Opt. Gap 1
-	DynMO-CoSyNE DynAMO-CoSyNE Minimum Novelty@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad.	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0) 21.9 ^(3.0) 21.1 ^(1.1)	20.3 ^(2.3) UTR 0.0 51.7 ^(2.9) 46.7 ^(2.7) 53.6 ^(2.1) 52.2 ^(1.3)	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3.9) 96.8 ^(3.9) 93.1 ^(6.6) 98.6 ^(1.5)	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7) 86.4 ^(10.2) 85.8 ^(1.0)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0.7) 83.8 ^(6.8) 95.0 ^(0.7) 95.0 ^(0.7) 95.0 ^(0.4)	77.0 ^(35.9) D'Kitty 0.0 102 ^(6.1) 31.5 ^(3.6) 102 ^(6.1) 107 ^(6.7)	1.3 Rank ↓ 2.3 3.8 1.8 1.7	-20.7 Opt. Gap 1 74.5 58.3 75.4 76.7
= 	DynMO-CoSyNE DynAMO-CoSyNE Minimum Novelty@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. DynAMO-Grad. Adam	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0) 21.9 ^(3.0) 21.1 ^(1.1) 23.7 ^(2.8)	20.3 ^(2.3) UTR 0.0 51.7 ^(2.9) 46.7 ^(2.7) 53.6 ^(2.1) 52.2 ^(1.3) 51.1 ^(3.5)	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3.9) 96.8 ^(3.9) 93.1 ^(6.6) 98.6 ^(1.5) 95.5 ^(5.3)	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7) 86.4 ^(10.2) 85.8 ^(1.0) 79.3 ^(21.2)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0,7) 83.8 ^(6.8) 95.0 ^(0,7) 95.0 ^(0,7) 95.9 ^(0,7) 94.8 ^(0,7)	77.0 ^(35.9) D'Kitty 0.0 102 ^(6.1) 31.5 ^(3.6) 102 ^(6.1) 107 ^(6.7) 103 ^(6.3)	1.3 Rank ↓	-20.7 Opt. Gap 1 74.5 58.3 75.4 76.7 74.5
= -	DynMO-CoSyNE DynAMO-CoSyNE Minimum Novelty@128 Dataset D Grad. AMO-Grad. DynAMO-Grad. DynAMO-Grad. Adam AMO-Adam	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0) 21.9 ^(3.0) 21.1 ^(1.1) 23.7 ^(2.8) 23.7 ^(3.1)	20.3 ^(2.3) UTR 0.0 51.7 ^(2.9) 46.7 ^(2.7) 53.6 ^(2.1) 52.2 ^(1.3) 51.1 ^(3.5) 51.3 ^(3.4)	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3,9) 96.8 ^(3,9) 93.1 ^(6.6) 98.6 ^(1.5) 95.5 ^(5.3) 95.0 ^(5.1)	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7) 86.4 ^(10.2) 85.8 ^(1.0) 79.3 ^(21.2) 80.0 ^(20.6)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0.7) 83.8 ^(6.8) 95.0 ^(0.7) 95.0 ^(0.4) 94.8 ^(0.7) 84.8 ^(6.4)	77.0 ^(35.9) D'Kitty 0.0 102 ^(6.1) 31.5 ^(3.6) 102 ^(6.1) 107 ^(6.7) 103 ^(6.3) 27.3 ^(3.4)	1.3 Rank ↓	-20.7 Opt. Gap 1 74.5 58.3 75.4 76.7 74.5 60.4
	DynMO-CoSyNE DynAMO-CoSyNE Minimum Novelty@128 Dataset D Grad. AMO-Grad. DynAMO-Grad. DynAMO-Grad. Adam AMO-Adam DynMO-Adam	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0) 21.9 ^(3.0) 21.1 ^(1.1) 23.7 ^(2.8) 23.7 ^(3.1) 22.9 ^(2.3)	20.3 ^(2.3) UTR 0.0 51.7 ^(2.9) 46.7 ^(2.7) 53.6 ^(2.1) 52.2 ^(1.3) 51.1 ^(3.5) 51.3 ^(3.4) 51.6 ^(2.9)	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3,9) 96.8 ^(3,9) 93.1 ^(6.6) 98.6 ^(1.5) 95.5 ^(5.3) 95.0 ^(5.1) 99.2 ^(0.6)	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7) 86.4 ^(10.2) 85.8 ^(1.0) 79.3 ^(21.2) 80.0 ^(20.6) 87.3 ^(9.7)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0.7) 83.8 ^(6.8) 95.0 ^(0.7) 95.0 ^(0.4) 94.8 ^(0.7) 84.8 ^(6.4) 94.7 ^(0.7)	77.0 ^(35.9) D'Kitty 0.0 102 ^(6.1) 31.5 ^(3.6) 102 ^(6.1) 107 ^(6.7) 103 ^(6.3) 27.3 ^(3.4) 103 ^(6.3)	1.3 Rank ↓	-20.7 Opt. Gap↑ 74.5 58.3 75.4 76.7 74.5 60.4 76.4
– –	DynMO-CoSyNE DynAMO-CoSyNE Minimum Novelty@128 Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. Adam Adam AmO-Adam DynMO-Adam DynAMO-Adam	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0) 21.9 ^(3.0) 21.1 ^(1.1) 23.7 ^(2.8) 23.7 ^(3.1) 22.9 ^(2.3) 14.7 ^(1.9)	20.3 ^(2.3) UTR 0.0 51.7 ^(2.9) 46.7 ^(2.7) 53.6 ^(2.1) 52.2 ^(1.3) 51.1 ^(3.5) 51.3 ^(3.4) 51.6 ^(2.9) 46.2 ^(0.5)	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3,9) 96.8 ^(3,9) 93.1 ^(6.6) 98.6 ^(1.5) 95.5 ^(5.3) 95.0 ^(5.1) 99.2 ^(0.6) 98.7 ^(1.2)	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7) 86.4 ^(10.2) 85.8 ^(1.0) 79.3 ^(21.2) 80.0 ^(20.6) 87.3 ^(9.7) 85.9 ^(1.8)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0.7) 83.8 ^(6.8) 95.0 ^(0.7) 95.0 ^(0.4) 94.8 ^(0.7) 84.8 ^(6.4) 94.7 ^(0.7) 94.9 ^(0.4)	77.0 ^(35.9) D'Kitty 0.0 102 ^(6.1) 31.5 ^(3.6) 102 ^(6.1) 107 ^(6.7) 103 ^(6.3) 27.3 ^(3.4) 103 ^(6.3) 103 ^(6.3) 108 ^(7.2)	1.3 Rank ↓	-20.7 Opt. Gap ↑ 74.5 58.3 75.4 76.7 74.5 60.4 76.4 76.4 74.7
– –	DynMO-CoSyNE DynAMO-CoSyNE Dataset D Dataset D Grad. AMO-Grad. DynAO-Grad. DynAMO-Grad. DynAMO-Adam Adam AMO-Adam DynMO-Adam DynAMO-Adam	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0) 21.9 ^(3.0) 21.1 ^(1.1) 23.7 ^(2.8) 23.7 ^(3.1) 22.9 ^(2.3) 14.7 ^(1.9) 21.8 ^(0.5)	20.3 ^(2.3) UTR 0.0 51.7 ^(2.9) 46.7 ^(2.7) 53.6 ^(2.1) 52.2 ^(1.3) 51.1 ^(3.5) 51.3 ^(3.4) 51.6 ^(2.9) 46.2 ^(0.5) 51.5 ^(0.3)	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3,9) 96.8 ^(3,9) 93.1 ^(6.6) 98.6 ^(1.5) 95.5 ^(5.3) 95.0 ^(5.1) 99.2 ^(0.6) 98.7 ^(1.2) 97.6 ^(0.3)	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7) 86.4 ^(10.2) 85.8 ^(1.0) 79.3 ^(21.2) 80.0 ^(20.6) 87.3 ^(9.7) 85.9 ^(1.8) 85.4 ^(1.5)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0,7) 83.8 ^(6.8) 95.0 ^(0,7) 95.0 ^(0,7) 95.0 ^(0,4) 94.8 ^(0,7) 84.8 ^(6.4) 94.7 ^(0,7) 94.9 ^(0,4) 94.6 ^(0,1)	77.0 ^(35.9) D'Kitty 0.0 102 ^(6.1) 31.5 ^(3.6) 102 ^(6.1) 107 ^(6.7) 103 ^(6.3) 27.3 ^(3.4) 103 ^(6.3) 108 ^(7.2) 106 ^(2.9)	1.3 Rank ↓	-20.7 Opt. Gap 1 74.5 58.3 75.4 76.7 74.5 60.4 76.4 76.4 76.4 76.2
— —	DynMO-CoSyNE DynAMO-CoSyNE Dataset D Dataset D Grad. AMO-Grad. DynAO-Grad. DynAMO-Grad. DynAMO-Adam DynMO-Adam DynAMO-Adam DynAMO-Adam	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0) 21.9 ^(3.0) 21.1 ^(1.1) 23.7 ^(2.8) 23.7 ^(3.1) 22.9 ^(2.3) 14.7 ^(1.9) 21.8 ^(0.5) 15.4 ^(0.3)	20.3 ^(2.3) UTR 0.0 51.7 ^(2.9) 46.7 ^(2.7) 53.6 ^(2.1) 52.2 ^(1.3) 51.1 ^(3.5) 51.3 ^(3.4) 51.6 ^(2.9) 46.2 ^(0.5) 51.5 ^(0.3) 51.8 ^(0.2)	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3,9) 96.8 ^(3,9) 93.1 ^(6,6) 98.6 ^(1.5) 95.5 ^(5,3) 95.0 ^(5,1) 99.2 ^(0,6) 98.7 ^(1.2) 97.6 ^(0,3) 97.8 ^(0,3)	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7) 86.4 ^(10.2) 85.8 ^(1.0) 79.3 ^(21.2) 80.0 ^(20.6) 87.3 ^(9.7) 85.9 ^(1.8) 85.4 ^(1.5) 84.9 ^(0.9)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0,7) 83.8 ^(6.8) 95.0 ^(0,7) 95.0 ^(0,4) 94.8 ^(0,7) 84.8 ^(6.4) 94.7 ^(0,7) 94.9 ^(0.4) 94.6 ^(0.1) 85.1 ^(0.4)	77.0 ^(35.9) D'Kitty 0.0 102 ^(6.1) 31.5 ^(3.6) 102 ^(6.1) 107 ^(6.7) 103 ^(6.3) 27.3 ^(3.4) 103 ^(6.3) 108 ^(7.2) 106 ^(2.9) 14.3 ^(1.5)	1.3 Rank ↓	-20.7 Opt. Gap ~
–	DynMO-CoSyNE DynAMO-CoSyNE Dataset D Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0) 21.9 ^(3.0) 21.1 ^(1.1) 23.7 ^(2.8) 23.7 ^(3.1) 22.9 ^(2.3) 14.7 ^(1.9) 21.8 ^(0.5) 15.4 ^(0.3) 20.4 ^(0.4)	20.3 ^(2.3) UTR 0.0 51.7 ^(2.9) 46.7 ^(2.7) 53.6 ^(2.1) 52.2 ^(1.3) 51.1 ^(3.5) 51.3 ^(3.4) 51.6 ^(2.9) 46.2 ^(0.5) 51.5 ^(0.3) 51.8 ^(0.2) 51.8 ^(0.2) 51.8 ^(0.1)	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3,9) 96.8 ^(3,9) 93.1 ^(6,6) 98.6 ^(1.5) 95.5 ^(5.3) 95.0 ^(5.1) 99.2 ^(0,6) 98.7 ^(1.2) 97.6 ^(0.3) 97.8 ^(0.3) 97.7 ^(0.3)	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7) 86.4 ^(10.2) 85.8 ^(1.0) 79.3 ^(21.2) 80.0 ^(20.6) 87.3 ^(9.7) 85.9 ^(1.8) 85.4 ^(1.5) 84.9 ^(0.9) 85.7 ^(1.3)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0,7) 83.8 ^(6.8) 95.0 ^(0,7) 95.0 ^(0,4) 94.8 ^(0,7) 84.8 ^(6.4) 94.7 ^(0,7) 94.9 ^(0,4) 94.6 ^(0,1) 85.1 ^(0,4) 94.4 ^(0,5)	77.0 ^(35.9) D'Kitty 0.0 102 ^(6.1) 31.5 ^(3.6) 102 ^(6.1) 107 ^(6.7) 103 ^(6.3) 27.3 ^(3.4) 103 ^(6.3) 108 ^(7.2) 106 ^(2.9) 14.3 ^(1.5) 108 ^(3.2)	1.3 Rank ↓	-20.7 Opt. Gap ~
	DynMO-CoSyNE DynAMO-CoSyNE Dataset D Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. DynAMO-Grad. DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0) 21.9 ^(3.0) 21.1 ^(1.1) 23.7 ^(2.8) 23.7 ^(3.1) 22.9 ^(2.3) 14.7 ^(1.9) 21.8 ^(0.5) 15.4 ^(0.3) 20.4 ^(0.4) 21.0 ^(0.5)	20.3 ^(2.3) UTR 0.0 51.7 ^(2.9) 46.7 ^(2.7) 53.6 ^(2.1) 52.2 ^(1.3) 51.1 ^(3.5) 51.3 ^(3.4) 51.6 ^(2.9) 46.2 ^(0.5) 51.5 ^(0.3) 51.8 ^(0.1) 51.8 ^(0.1) 51.9 ^(0.2)	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3,9) 96.8 ^(3,9) 93.1 ^(6.6) 98.6 ^(1.5) 95.5 ^(5.3) 95.0 ^(5.1) 99.2 ^(0.6) 98.7 ^(1.2) 97.6 ^(0.3) 97.8 ^(0.3) 97.7 ^(0.3) 97.4 ^(0.4)	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7) 86.4 ^(10.2) 85.8 ^(1.0) 79.3 ^(21.2) 80.0 ^(20.6) 87.3 ^(9.7) 85.9 ^(1.8) 85.9 ^(1.8) 85.4 ^(1.5) 84.9 ^(0.9) 85.7 ^(1.3) 85.2 ^(0.9)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0,7) 83.8 ^(6.8) 95.0 ^(0,7) 95.0 ^(0,4) 94.8 ^(0,7) 84.8 ^(6,4) 94.7 ^(0,7) 94.9 ^(0,4) 94.6 ^(0,1) 85.1 ^(0,4) 94.4 ^(0,5) 94.8 ^(0,1)	77.0 ^(35.9) D'Kitty 0.0 102 ^(6.1) 31.5 ^(3.6) 102 ^(6.1) 107 ^(6.7) 103 ^(6.3) 27.3 ^(3.4) 103 ^(6.3) 108 ^(7.2) 106 ^(2.9) 14.3 ^(1.5) 108 ^(3.2) 126 ^(14.6)	1.3 Rank ↓	-20.7 Opt. Gap 1
–	DynMO-CoSyNE DynAMO-CoSyNE Dataset D Dataset D Grad. AMO-Grad. DynAO-Grad. DynAMO-Grad. DynAMO-Grad. DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0) 21.9 ^(3.0) 21.1 ^(1.1) 23.7 ^(2.8) 23.7 ^(3.1) 22.9 ^(2.3) 14.7 ^(1.9) 21.8 ^(0.5) 15.4 ^(0.3) 20.4 ^(0.4) 21.0 ^(0.5) 21.6 ^(0.3)	20.3 ^(2.3) UTR 0.0 51.7 ^(2.9) 46.7 ^(2.7) 53.6 ^(2.1) 52.2 ^(1.3) 51.1 ^(3.5) 51.3 ^(3.4) 51.6 ^(2.9) 46.2 ^(0.5) 51.5 ^(0.3) 51.8 ^(0.2) 51.8 ^(0.1) 51.9 ^(0.2)	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3,9) 96.8 ^(3,9) 93.1 ^(6,6) 98.6 ^(1.5) 95.5 ^(5,3) 95.0 ^(5,1) 99.2 ^(0,6) 98.7 ^(1.2) 97.6 ^(0,3) 97.8 ^(0,3) 97.7 ^(0,3) 97.4 ^(0,4)	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7) 86.4 ^(10.2) 85.8 ^(1.0) 79.3 ^(21.2) 80.0 ^(20.6) 87.3 ^(9.7) 85.9 ^(1.8) 85.4 ^(1.5) 84.9 ^(0.9) 85.7 ^(1.3) 85.2 ^(0.9) 85.3 ^(1.1)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0,7) 83.8 ^(6.8) 95.0 ^(0,7) 95.0 ^(0,7) 94.8 ^(0,7) 84.8 ^(0,4) 94.7 ^(0,7) 94.9 ^(0,4) 94.6 ^(0,1) 85.1 ^(0,4) 94.4 ^(0,5) 94.8 ^(0,1) 93.8 ^(0,6)	77.0 ^(35.9) D'Kitty 0.0 102 ^(6.1) 31.5 ^(3.6) 102 ^(6.1) 107 ^(6.7) 103 ^(6.3) 27.3 ^(3.4) 103 ^(6.3) 103 ^(5.3) 108 ^(7.2) 106 ^(2.9) 14.3 ^(1.5) 108 ^(3.2) 126 ^(14.6) 98.8 ^(1.1)	1.3 Rank ↓	-20.7 Opt. Gap ~
= - -	DynMO-CoSyNE DynAMO-CoSyNE Dataset D Dataset D Grad. AMO-Grad. DynAO-Grad. DynAMO-Grad. DynAMO-Grad. DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0) 21.9 ^(3.0) 21.1 ^(1.1) 23.7 ^(2.8) 23.7 ^(3.1) 22.9 ^(2.3) 14.7 ^(1.9) 21.8 ^(0.5) 15.4 ^(0.3) 20.4 ^(0.4) 21.0 ^(0.5) 21.6 ^(0.3) 21.9 ^(0.4)	20.3 ^(2.3) UTR 0.0 51.7 ^(2.9) 46.7 ^(2.7) 53.6 ^(2.1) 52.2 ^(1.3) 51.3 ^(3.4) 51.6 ^(2.9) 46.2 ^(0.5) 51.5 ^(0.3) 51.5 ^(0.3) 51.8 ^(0.1) 51.9 ^(0.2) 51.7 ^(0.2) 51.7 ^(0.2)	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3,9) 96.8 ^(3,9) 93.1 ^(6,6) 98.6 ^(1.5) 95.5 ^(5,3) 95.0 ^(5,1) 99.2 ^(0,6) 98.7 ^(1.2) 97.6 ^(0,3) 97.8 ^(0,3) 97.7 ^(0,3) 97.4 ^(0,4) 97.9 ^(0,4)	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7) 86.4 ^(10.2) 85.8 ^(1.0) 79.3 ^(21.2) 80.0 ^(20.6) 87.3 ^(9.7) 85.9 ^(1.8) 85.4 ^(1.5) 85.4 ^(1.5) 85.4 ^(1.5) 85.2 ^(1.3) 85.2 ^(0.9) 85.3 ^(1.1) 85.2 ^(1.0)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0,7) 83.8 ^(6.8) 95.0 ^(0,7) 95.0 ^(0,7) 94.8 ^(0,7) 84.8 ^(0,4) 94.7 ^(0,7) 94.9 ^(0,4) 94.6 ^(0,1) 85.1 ^(0,4) 94.4 ^(0,5) 94.8 ^(0,1) 93.8 ^(0,6) 81.9 ^(1,9)	77.0 ^(35.9) D'Kitty 0.0 102 ^(6.1) 31.5 ^(3.6) 102 ^(6.1) 107 ^(6.7) 103 ^(6.3) 27.3 ^(3.4) 103 ^(6.3) 103 ^(5.3) 108 ^(7.2) 106 ^(2.9) 14.3 ^(1.5) 108 ^(3.2) 126 ^(14.6) 98.8 ^(1.1) 25.9 ^(1.4)	1.3 Rank \downarrow 2.3 3.8 1.8 1.7 2.7 3.0 1.8 2.3 2.5 3.3 2.5 3.3 2.2 2.0 2.7	-20.7 Opt. Gap 7
= - -	DynMO-CoSyNE DynAMO-CoSyNE DynAMO-CoSyNE Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. DynAMO-Grad. DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam BO-qEI AMO-BO-qEI DynAO-BO-qUCB AMO-BO-qUCB AMO-BO-qUCB	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0) 21.9 ^(3.0) 21.1 ^(1.1) 23.7 ^(2.8) 23.7 ^(3.1) 22.9 ^(2.3) 14.7 ^(1.9) 21.8 ^(0.5) 15.4 ^(0.3) 20.4 ^(0.4) 21.6 ^(0.3) 21.9 ^(0.4) 20.7 ^(0.4)	20.3 ^(2.3) UTR 0.0 51.7 ^(2.9) 46.7 ^(2.7) 53.6 ^(2.1) 52.2 ^(1.3) 51.3 ^(3.4) 51.6 ^(2.9) 46.2 ^(0.5) 51.5 ^(0.3) 51.8 ^(0.2) 51.8 ^(0.1) 51.9 ^(0.2) 51.7 ^(0.2) 51.7 ^(0.2) 51.7 ^(0.3) 51.8 ^(0.2)	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3,9) 96.8 ^(3,9) 93.1 ^(6,6) 98.6 ^(1.5) 95.5 ^(5.3) 95.0 ^(5,1) 99.2 ^(0,6) 98.7 ^(1.2) 97.6 ^(0.3) 97.8 ^(0.3) 97.7 ^(0.3) 97.4 ^(0.4) 97.5 ^(0.4) 97.1 ^(0.5)	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7) 86.4 ^(10.2) 85.8 ^(1.0) 79.3 ^(21.2) 80.0 ^(20.6) 87.3 ^(9.7) 85.9 ^(1.8) 85.4 ^(1.5) 85.4 ^(1.5) 85.4 ^(1.5) 85.2 ^(1.0) 85.3 ^(1.1) 85.2 ^(1.0) 84.9 ^(0.6)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0,7) 83.8 ^(6.8) 95.0 ^(0,7) 95.0 ^(0,4) 94.8 ^(0,7) 84.8 ^(6.4) 94.7 ^(0,7) 94.9 ^(0,4) 94.6 ^(0,1) 85.1 ^(0,4) 94.4 ^(0,5) 94.8 ^(0,1) 93.8 ^(0,6) 81.9 ^(1,9) 93.2 ^(1,4)	77.0 ^(35.9) D'Kitty 0.0 102 ^(6.1) 31.5 ^(3.6) 102 ^(6.1) 107 ^(6.7) 103 ^(6.3) 27.3 ^(3.4) 103 ^(6.3) 108 ^(7.2) 106 ^(2.9) 14.3 ^(1.5) 108 ^(3.2) 126 ^(14.6) 98.8 ^(1.1) 25.9 ^(1.4) 98.0 ^(1.8)	1.3 Rank ↓	-20.7 Opt. Gap 7
	DynMO-CoSyNE DynAMO-CoSyNE DynAMO-CoSyNE Commonstream Dataset D Grad. AMO-Grad. DynAO-Grad. DynAMO-Grad. DynAMO-Grad. DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-BO-qEI DynAMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0) 21.9 ^(3.0) 21.1 ^(1.1) 23.7 ^(2.8) 23.7 ^(3.1) 22.9 ^(2.3) 14.7 ^(1.9) 21.8 ^(0.5) 15.4 ^(0.3) 20.4 ^(0.4) 21.9 ^(0.4) 20.7 ^(0.4) 21.4 ^(0.5)	20.3 ^(2.3) UTR 0.0 51.7 ^(2.9) 46.7 ^(2.7) 53.6 ^(2.1) 52.2 ^(1.3) 51.1 ^(3.5) 51.3 ^(3.4) 51.6 ^(2.9) 46.2 ^(0.5) 51.5 ^(0.3) 51.8 ^(0.2) 51.8 ^(0.1) 51.9 ^(0.2) 51.7 ^(0.2) 51.7 ^(0.2)	$\begin{array}{r} \textbf{35.0}^{(17.9)} \\ \hline \textbf{ChEMBL} \\ 0.0 \\ \textbf{97.4}^{(3.9)} \\ \textbf{96.8}^{(3.9)} \\ \textbf{93.1}^{(6.6)} \\ \textbf{98.6}^{(1.5)} \\ \textbf{95.5}^{(5.1)} \\ \textbf{95.0}^{(5.1)} \\ \textbf{99.2}^{(0.6)} \\ \textbf{98.7}^{(1.2)} \\ \textbf{97.6}^{(0.3)} \\ \textbf{97.8}^{(0.3)} \\ \textbf{97.7}^{(0.3)} \\ \textbf{97.9}^{(0.4)} \\ \textbf{97.9}^{(0.4)} \\ \textbf{97.9}^{(0.4)} \\ \textbf{97.1}^{(0.5)} \\ \textbf{97.1}^{(0.5)} \end{array}$	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7) 86.4 ^(10.2) 85.8 ^(1.0) 79.3 ^(21.2) 80.0 ^(20.6) 87.3 ^(9.7) 85.9 ^(1.8) 85.9 ^(1.8) 85.4 ^(1.5) 84.9 ^(0.9) 85.2 ^(1.0) 85.2 ^(1.0) 85.3 ^(1.1) 85.3 ^(1.1)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0,7) 83.8 ^(6.8) 95.0 ^(0,7) 95.0 ^(0,4) 94.8 ^(0,7) 84.8 ^(6.4) 94.7 ^(0,7) 94.9 ^(0,4) 94.9 ^(0,4) 94.9 ^(0,4) 94.6 ^(0,1) 85.1 ^(0,4) 94.4 ^(0,5) 94.8 ^(0,1) 93.8 ^(0,6) 81.9 ^(1,9) 93.2 ^(1,4) 94.7 ^(0,2)	77.0 ^(35.9) D'Kitty 0.0 102 ^(6.1) 31.5 ^(3.6) 102 ^(6.1) 107 ^(6.7) 103 ^(6.3) 27.3 ^(3.4) 103 ^(6.3) 108 ^(7.2) 106 ^(2.9) 14.3 ^(1.5) 108 ^(3.2) 126 ^(14.6) 98.8 ^(1.1) 25.9 ^(1.4) 98.0 ^(1.8) 109 ^(4.5)	$\begin{array}{r} \textbf{1.3} \\ \hline \textbf{Rank} \downarrow \\ \hline - \\ 2.3 \\ 3.8 \\ \hline \textbf{1.7} \\ 2.7 \\ 3.0 \\ \textbf{1.8} \\ \hline \textbf{2.3} \\ 2.5 \\ 3.3 \\ 2.2 \\ \textbf{2.0} \\ \hline \textbf{2.0} \\ 2.7 \\ 3.2 \\ 2.2 \\ \hline \textbf{2.2} \\ \end{array}$	-20.7 Opt. Gap ²
= 	DynMO-CoSyNE DynAMO-CoSyNE DynAMO-CoSyNE CosynE Dataset D Grad. AMO-Grad. DynAO-Grad. DynAMO-Grad. DynAMO-Grad. DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-BO-qEI DynAMO-BO-qUCB AMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0) 21.9 ^(3.0) 21.1 ^(1.1) 23.7 ^(2.8) 23.7 ^(3.1) 22.9 ^(2.3) 14.7 ^(1.9) 21.8 ^(0.5) 15.4 ^(0.3) 20.4 ^(0.4) 21.9 ^(0.4) 20.7 ^(0.4) 21.4 ^(0.5) 16.5 ^(2.1)	$\begin{array}{r} \textbf{20.3}^{(2.3)}\\ \hline \textbf{UTR}\\ \hline 0.0\\ \hline \textbf{51.7}^{(2.9)}\\ 46.7^{(2.7)}\\ \textbf{53.6}^{(2.1)}\\ \textbf{52.2}^{(1.3)}\\ \hline \textbf{51.3}^{(3.4)}\\ \textbf{51.6}^{(2.9)}\\ 46.2^{(0.5)}\\ \hline \textbf{51.5}^{(0.3)}\\ \textbf{51.8}^{(0.2)}\\ \textbf{51.8}^{(0.1)}\\ \textbf{51.9}^{(0.2)}\\ \textbf{51.7}^{(0.2)}\\ \textbf{51.7}^{(0.3)}\\ \textbf{51.8}^{(0.2)}\\ \textbf{51.7}^{(0.2)}\\ \textbf{51.7}^{(0.2)}\\$	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3,9) 96.8 ^(3,9) 93.1 ^(6,6) 98.6 ^(1,5) 95.5 ^(5,3) 95.0 ^(5,1) 99.2 ^(0,6) 98.7 ^(1,2) 97.6 ^(0,3) 97.8 ^(0,3) 97.7 ^(0,3) 97.4 ^(0,4) 97.9 ^(0,4) 97.5 ^(0,4) 97.1 ^(0,5) 96.5 ^(0,7)	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7) 76.8 ^(19.7) 86.4 ^(10.2) 85.8 ^(1.0) 79.3 ^(21.2) 80.0 ^(20.6) 87.3 ^(9.7) 85.9 ^(1.8) 85.4 ^(1.5) 84.9 ^(0.9) 85.7 ^(1.3) 85.2 ^(1.0) 85.3 ^(1.1) 85.2 ^(1.0) 84.9 ^(0.6) 85.3 ^(1.1) 73.0 ^(18.0)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0,7) 83.8 ^(6.8) 95.0 ^(0,7) 95.0 ^(0,7) 95.0 ^(0,4) 94.8 ^(0,7) 84.8 ^(6.4) 94.7 ^(0,7) 94.9 ^(0,4) 94.6 ^(0,1) 85.1 ^(0,4) 94.4 ^(0,5) 94.8 ^(0,1) 93.8 ^(0,6) 81.9 ^(1,9) 93.2 ^(1,4) 94.7 ^(0,2)	77.0 ^(35.9) D'Kitty 0.0 102 ^(6.1) 31.5 ^(3.6) 107 ^(6.7) 103 ^(6.3) 27.3 ^(3.4) 103 ^(6.3) 27.3 ^(3.4) 103 ^(6.3) 108 ^(7.2) 106 ^(2.9) 14.3 ^(1.5) 108 ^(3.2) 126 ^(14.6) 98.8 ^(1.1) 25.9 ^(1.4) 98.0 ^(1.8) 109 ^(4.5) 100 ^(0.0)	1.3 Rank ↓	-20.7 Opt. Gap 1
	DynMO-CoSyNE DynAMO-CoSyNE DynAMO-CoSyNE Commonstream Dataset D Grad. AMO-Grad. DynAO-Grad. DynAMO-Grad. DynAMO-Grad. DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-BO-qEI DynMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0) 21.9 ^(3.0) 21.1 ^(1.1) 23.7 ^(2.8) 23.7 ^(3.1) 22.9 ^(2.3) 14.7 ^(1.9) 21.8 ^(0.5) 15.4 ^(0.3) 20.4 ^(0.4) 21.9 ^(0.4) 20.7 ^(0.4) 21.4 ^(0.5) 16.5 ^(2.1) 24.3 ^(0.9)	20.3 ^(2.3) UTR 0.0 51.7 ^(2.9) 46.7 ^(2.7) 53.6 ^(2.1) 52.2 ^(1.3) 51.1 ^(3.5) 51.3 ^(3.4) 51.6 ^(2.9) 46.2 ^(0.5) 51.5 ^(0.3) 51.8 ^(0.2) 51.8 ^(0.1) 51.9 ^(0.2) 51.7 ^(0.2) 51.7 ^(0.2) 51.7 ^(0.2) 51.7 ^(0.2) 51.7 ^(0.2) 51.7 ^(0.2) 51.7 ^(0.2)	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3,9) 96.8 ^(3,9) 93.1 ^(6,6) 98.6 ^(1.5) 95.5 ^(5,3) 95.0 ^(5,1) 99.2 ^(0,6) 98.7 ^(1.2) 97.6 ^(0.3) 97.8 ^(0.3) 97.7 ^(0.3) 97.7 ^(0.3) 97.4 ^(0.4) 97.5 ^(0.4) 97.1 ^(0.5) 96.5 ^(0.7) 95.0 ^(1.5)	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7) 86.4 ^(10.2) 85.8 ^(1.0) 79.3 ^(21.2) 80.0 ^(20.6) 87.3 ^(9.7) 85.9 ^(1.8) 85.9 ^(1.8) 85.4 ^(1.5) 84.9 ^(0.9) 85.3 ^(1.1) 85.2 ^(1.0) 85.3 ^(1.1) 85.3 ^(1.1)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0,7) 83.8 ^(6.8) 95.0 ^(0,7) 95.0 ^(0,7) 95.0 ^(0,4) 94.8 ^(0,7) 84.8 ^(6.4) 94.7 ^(0,7) 94.9 ^(0,4) 94.6 ^(0,1) 85.1 ^(0,4) 94.4 ^(0,5) 94.8 ^(0,1) 93.8 ^(0,6) 81.9 ^(1,9) 93.2 ^(1,4) 94.7 ^(0,2) 100 ^(0,0) 85.6 ^(3,0)	77.0 ^(35.9) D'Kitty 0.0 102 ^(6.1) 31.5 ^(3.6) 107 ^(6.7) 103 ^(6.3) 27.3 ^(3.4) 103 ^(6.3) 27.3 ^(3.4) 103 ^(6.3) 108 ^(7.2) 106 ^(2.9) 14.3 ^(1.5) 108 ^(3.2) 126 ^(14.6) 98.8 ^(1.1) 25.9 ^(1.4) 98.0 ^(1.8) 109 ^(4.5) 100 ^(0.0) 41.5 ^(2.0)	$\begin{array}{r} \textbf{1.3} \\ \hline \textbf{Rank} \downarrow \\ \hline \\ \hline \\ 2.3 \\ 3.8 \\ \hline \textbf{1.7} \\ 2.7 \\ 3.0 \\ \textbf{1.8} \\ \hline \textbf{2.3} \\ 2.5 \\ 3.3 \\ \hline \textbf{2.2} \\ \textbf{2.0} \\ \hline \textbf{2.0} \\ \textbf{2.7} \\ \textbf{3.2} \\ \hline \textbf{2.0} \\ \hline \textbf{2.7} \\ 3.2 \\ \hline \textbf{2.2} \\ \hline \textbf{2.0} \\ \hline \textbf{2.3} \\ 3.0 \\ \hline \end{array}$	-20.7 Opt. Gap ²
	DynMO-CoSyNE DynAMO-CoSyNE DynAMO-CoSyNE Minimum Novelty@128 Dataset D Grad. AMO-Grad. DynAO-Grad. DynAMO-Grad. DynAMO-Grad. DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-BO-qEI DynMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-CMA-ES DynMO-CMA-ES	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0) 21.9 ^(3.0) 21.1 ^(1.1) 23.7 ^(2.8) 23.7 ^(3.1) 22.9 ^(2.3) 14.7 ^(1.9) 21.8 ^(0.5) 15.4 ^(0.3) 20.4 ^(0.4) 21.0 ^(0.5) 21.6 ^(0.3) 21.9 ^(0.4) 20.7 ^(0.4) 21.4 ^(0.5) 16.5 ^(2.1) 24.3 ^(0.9) 14.3 ^(0.3)	$\begin{array}{r} \textbf{20.3}^{(2.3)}\\ \hline \textbf{UTR}\\ \hline 0.0\\ \hline \textbf{51.7}^{(2.9)}\\ 46.7^{(2.7)}\\ \textbf{53.6}^{(2.1)}\\ \textbf{52.2}^{(1.3)}\\ \hline \textbf{51.3}^{(3.4)}\\ \textbf{51.6}^{(2.9)}\\ 46.2^{(0.5)}\\ \hline \textbf{51.5}^{(0.3)}\\ \textbf{51.8}^{(0.2)}\\ \textbf{51.8}^{(0.2)}\\ \textbf{51.8}^{(0.1)}\\ \textbf{51.9}^{(0.2)}\\ \hline \textbf{51.7}^{(0.2)}\\ \textbf{51.7}^{(0.2)}\\ \textbf{51.7}^{(0.2)}\\ \textbf{51.7}^{(0.2)}\\ \textbf{51.7}^{(0.2)}\\ \textbf{51.3}^{(1.0)}\\ \textbf{53.3}^{(1.4)}\\ 46.1^{(0.4)}\\ \end{array}$	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3,9) 96.8 ^(3,9) 93.1 ^(6,6) 98.6 ^(1.5) 95.5 ^(5,3) 95.0 ^(5,1) 99.2 ^(0,6) 98.7 ^(1.2) 97.6 ^(0,3) 97.8 ^(0,3) 97.7 ^(0,3) 97.7 ^(0,3) 97.4 ^(0,4) 97.9 ^(0,4) 97.5 ^(0,4) 97.1 ^(0,5) 96.5 ^(0,7) 95.0 ^(1.5) 98.2 ^(1,0)	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7) 86.4 ^(10.2) 85.8 ^(1.0) 79.3 ^(21.2) 80.0 ^(20.6) 87.3 ^(9.7) 85.9 ^(1.8) 85.4 ^(1.5) 84.9 ^(0.9) 85.7 ^(1.3) 85.2 ^(1.0) 85.3 ^(1.1) 85.2 ^(1.0) 85.3 ^(1.1) 73.0 ^(18.0) 72.5 ^(23.6) 83.3 ^(1.0)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0,7) 83.8 ^(6.8) 95.0 ^(0,7) 95.0 ^(0,4) 94.8 ^(0,7) 84.8 ^(6.4) 94.7 ^(0,7) 94.9 ^(0,4) 94.6 ^(0,1) 85.1 ^(0,4) 94.4 ^(0,5) 94.8 ^(0,1) 93.8 ^(0,6) 81.9 ^(1,9) 93.2 ^(1,4) 93.2 ^(1,4) 94.7 ^(0,2) 100 ^(0,0) 85.6 ^(3,0) 100 ^(0,0)	77.0 ^(35.9) D'Kitty 0.0 102 ^(6.1) 31.5 ^(3.6) 102 ^(6.1) 107 ^(6.7) 103 ^(6.3) 27.3 ^(3.4) 103 ^(6.3) 108 ^(7.2) 106 ^(2.9) 14.3 ^(1.5) 108 ^(3.2) 126 ^(14.6) 98.8 ^(1.1) 25.9 ^(1.4) 98.0 ^(1.8) 109 ^(4.5) 100 ^(0.0) 41.5 ^(2.0) 100 ^(0.0)	1.3 Rank ↓	-20.7 Opt. Gap
	DynMO-CoSyNE DynAMO-CoSyNE DynAMO-CoSyNE Dataset D Grad. AMO-Grad. DynMO-Grad. DynAMO-Grad. DynAMO-Grad. DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-BO-qEI DynAMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-CMA-ES DynAMO-CMA-ES DynAMO-CMA-ES	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0) 21.9 ^(3.0) 21.1 ^(1.1) 23.7 ^(2.8) 23.7 ^(3.1) 22.9 ^(2.3) 14.7 ^(1.9) 21.8 ^(0.5) 15.4 ^(0.3) 20.4 ^(0.4) 21.0 ^(0.5) 21.6 ^(0.3) 21.9 ^(0.4) 20.7 ^(0.4) 21.4 ^(0.5) 16.5 ^(2.1) 24.3 ^(0.9) 14.3 ^(0.3) 12.9 ^(0.8)	$\begin{array}{r} \textbf{20.3}^{(2.3)}\\ \hline \textbf{UTR}\\ \hline 0.0\\ \textbf{51.7}^{(2.9)}\\ 46.7^{(2.7)}\\ \textbf{53.6}^{(2.1)}\\ \textbf{52.2}^{(1.3)}\\ \textbf{51.3}^{(3.4)}\\ \textbf{51.6}^{(2.9)}\\ 46.2^{(0.5)}\\ \textbf{51.5}^{(0.3)}\\ \textbf{51.8}^{(0.2)}\\ \textbf{51.8}^{(0.2)}\\ \textbf{51.8}^{(0.2)}\\ \textbf{51.7}^{(0.2)}\\ \textbf{51.8}^{(1.0)}\\ \textbf{53.3}^{(1.4)}\\ 46.1^{(0.4)}\\ 48.0^{(1.6)}\\ \end{array}$	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3,9) 96.8 ^(3,9) 93.1 ^(6.6) 98.6 ^(1.5) 95.5 ^(5.3) 95.0 ^(5.1) 99.2 ^(0.6) 98.7 ^(1.2) 97.6 ^(0.3) 97.7 ^(0.3) 97.7 ^(0.3) 97.4 ^(0.4) 97.9 ^(0.4) 97.1 ^(0.5) 97.1 ^(0.5) 97.1 ^(0.5) 96.5 ^(0.7) 95.0 ^(1.5) 98.2 ^(1.0) 96.7 ^(3.5)	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7) 86.4 ^(10.2) 85.8 ^(1.0) 79.3 ^(21.2) 80.0 ^(20.6) 87.3 ^(9.7) 85.9 ^(1.8) 85.9 ^(1.8) 85.4 ^(1.5) 84.9 ^(0.9) 85.3 ^(1.1) 85.2 ^(1.0) 85.3 ^(1.1) 85.3 ^(1.1)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0,7) 83.8 ^(6,8) 95.0 ^(0,7) 95.0 ^(0,4) 94.8 ^(0,7) 84.8 ^(6,4) 94.7 ^(0,7) 94.9 ^(0,4) 94.6 ^(0,1) 85.1 ^(0,4) 94.6 ^(0,1) 85.1 ^(0,4) 94.8 ^(0,1) 93.8 ^(0,6) 81.9 ^(1,9) 93.2 ^(1,4) 93.2 ^(1,4) 94.7 ^(0,2) 100 ^(0,0) 85.6 ^(3,0) 100 ^(0,0) 85.6 ^(3,0) 100 ^(0,0) 94.5 ^(0,7)	77.0 ^(35.9) D'Kitty 0.0 102 ^(6.1) 31.5 ^(3.6) 103 ^(6.3) 27.3 ^(3.4) 103 ^(6.3) 108 ^(7.2) 106 ^(2.9) 14.3 ^(1.5) 108 ^(3.2) 126 ^(14.6) 98.8 ^(1.1) 25.9 ^(1.4) 98.8 ^(1.1) 25.9 ^(1.4) 98.8 ^(1.1) 25.9 ^(1.4) 98.8 ^(1.1) 25.9 ^(1.4) 98.8 ^(1.1) 25.9 ^(1.4) 98.8 ^(1.1) 25.9 ^(1.4) 98.0 ^(1.8) 109 ^(4.5) 100 ^(0.0) 41.5 ^(2.0) 100 ^(0.0) 41.5 ^(2.0) 100 ^(0.0) 112 ^(7.8)	1.3 Rank \downarrow - 2.3 3.8 1.8 1.7 2.7 3.0 1.8 2.3 2.5 3.3 2.5 3.3 2.2 2.0 2.7 3.2 2.0 2.3 3.0 2.3	-20.7 Opt. Gap 7
	DynMO-CoSyNE DynAMO-CoSyNE DynAMO-CoSyNE Dataset D Grad. AMO-Grad. DynAO-Grad. DynAMO-Grad. DynAMO-Grad. DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-BO-qEI DynAMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-CMA-ES DynAMO-CMA-ES DynAMO-CMA-ES	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0) 21.9 ^(3.0) 21.1 ^(1.1) 23.7 ^(2.8) 23.7 ^(3.1) 22.9 ^(2.3) 14.7 ^(1.9) 21.8 ^(0.5) 15.4 ^(0.3) 20.4 ^(0.4) 21.0 ^(0.5) 21.6 ^(0.3) 21.9 ^(0.4) 20.7 ^(0.4) 21.4 ^(0.5) 16.5 ^(2.1) 24.3 ^(0.3) 12.9 ^(0.8) 24.5 ^(3.5)	20.3 ^(2.3) UTR 0.0 51.7 ^(2.9) 46.7 ^(2.7) 53.6 ^(2.1) 52.2 ^(1.3) 51.1 ^(3.5) 51.3 ^(3.4) 51.6 ^(2.9) 46.2 ^(0.5) 51.5 ^(0.3) 51.8 ^(0.2) 51.8 ^(0.2) 51.7 ^(0.2) 51.7 ^(0.3) 51.7 ^(0.2) 51.7 ^(0.2)	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3,9) 96.8 ^(3,9) 93.1 ^(6,6) 98.6 ^(1,5) 95.5 ^(5,3) 95.0 ^(5,1) 99.2 ^(0,6) 98.7 ^(1,2) 97.6 ^(0,3) 97.8 ^(0,3) 97.7 ^(0,3) 97.7 ^(0,3) 97.9 ^(0,4) 97.9 ^(0,4) 97.9 ^(0,4) 97.1 ^(0,5) 96.5 ^(0,7) 95.0 ^(1,5) 98.2 ^(1,0) 98.5 ^(1,6)	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7) 86.4 ^(10.2) 85.8 ^(1.0) 79.3 ^(21.2) 80.0 ^(20.6) 87.3 ^(9.7) 85.9 ^(1.8) 85.9 ^(1.8) 85.4 ^(1.5) 84.9 ^(0.9) 85.7 ^(1.3) 85.2 ^(1.0) 85.3 ^(1.1) 85.3 ^(1.1)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0,7) 83.8 ^(6.8) 95.0 ^(0,7) 95.0 ^(0,4) 94.8 ^(0,7) 84.8 ^(6.4) 94.7 ^(0,7) 94.9 ^(0,4) 94.9 ^(0,4) 94.9 ^(0,4) 94.9 ^(0,1) 85.1 ^(0,4) 94.9 ^(0,4) 94.9 ^(0,1) 85.1 ^(0,4) 94.8 ^(0,1) 93.2 ^(1,4) 94.7 ^(0,2) 100 ^(0,0) 85.6 ^(3,0) 100 ^(0,0) 85.6 ^(3,0) 100 ^(0,0) 94.5 ^(0,7) 93.2 ^(1,0)	$\begin{array}{c} {\bf 77.0^{(35.9)}}\\ \hline {\bf D'Kitty}\\ \hline 0.0\\ {\bf 102^{(6.1)}}\\ {\bf 31.5^{(3.6)}}\\ {\bf 102^{(6.1)}}\\ {\bf 107^{(6.7)}}\\ \hline {\bf 103^{(6.3)}}\\ {\bf 27.3^{(3.4)}}\\ {\bf 103^{(6.3)}}\\ {\bf 108^{(7.2)}}\\ \hline {\bf 108^{(7.2)}}\\ {\bf$	1.3 Rank \downarrow 2.3 3.8 1.8 1.7 2.7 3.0 1.8 2.3 2.5 3.3 2.5 3.3 2.2 2.0 2.7 3.2 2.2 2.3 3.0 2.0 2.3 3.0 2.3 1.8	-20.7 Opt. Gap ~
	DynMO-CoSyNE DynAMO-CoSyNE DynAMO-CoSyNE Dataset D Grad. AMO-Grad. DynAO-Grad. DynAMO-Grad. DynAMO-Grad. DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam BO-qUCB AMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-CMA-ES DynAMO-CMA-ES DynAMO-CMA-ES	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0) 21.9 ^(3.0) 21.1 ^(1.1) 23.7 ^(2.8) 23.7 ^(3.1) 22.9 ^(2.3) 14.7 ^(1.9) 21.8 ^(0.5) 15.4 ^(0.3) 20.4 ^(0.4) 21.0 ^(0.5) 21.6 ^(0.3) 21.9 ^(0.4) 21.4 ^(0.5) 16.5 ^(2.1) 24.3 ^(0.9) 14.3 ^(0.3) 12.9 ^(0.8) 24.5 ^(3.5) 22.8 ^(2.8)	20.3 ^(2.3) UTR 0.0 51.7 ^(2.9) 46.7 ^(2.7) 53.6 ^(2.1) 52.2 ^(1.3) 51.1 ^(3.5) 51.3 ^(3.4) 51.6 ^(2.9) 46.2 ^(0.5) 51.5 ^(0.3) 51.8 ^(0.1) 51.8 ^(0.1) 51.7 ^(0.2) 51.7 ^(0.2) 51.8 ^{(0.}	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3,9) 96.8 ^(3,9) 93.1 ^(6,6) 98.6 ^(1,5) 95.5 ^(5,3) 95.0 ^(5,1) 99.2 ^(0,6) 98.7 ^(1,2) 97.6 ^(0,3) 97.7 ^(0,3) 97.7 ^(0,3) 97.7 ^(0,3) 97.7 ^(0,4) 97.5 ^(0,4) 97.5 ^(0,4) 97.1 ^(0,5) 96.5 ^(1,5) 98.2 ^(1,0) 98.5 ^(1,6) 98.5	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7) 86.4 ^(10.2) 85.8 ^(1.0) 79.3 ^(21.2) 80.0 ^(20.6) 87.3 ^(9.7) 85.9 ^(1.8) 85.9 ^(1.8) 85.4 ^(1.5) 84.9 ^(0.9) 85.7 ^(1.3) 85.2 ^(0.9) 85.3 ^(1.1) 85.3 ^(1.1) 83.3 ^(1.0) 81.8 ^(1.3.4) 86.6 ^(12.7) 91.9 ^(3.4)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0,7) 83.8 ^(6.8) 95.0 ^(0,7) 95.0 ^(0,4) 94.8 ^(0,7) 84.8 ^(6.4) 94.7 ^(0,7) 94.9 ^(0,4) 94.9 ^(0,1) 85.1 ^(0,4) 94.4 ^(0,5) 94.8 ^(0,1) 93.8 ^(0,6) 81.9 ^(1,9) 93.2 ^(1,4) 94.7 ^(0,2) 100 ^(0,0) 85.6 ^(3,0) 100 ^(0,0) 94.5 ^(0,7) 93.2 ^(1,0) 86.0 ^(3,3)	$\begin{array}{c} \textbf{77.0}^{(35.9)} \\ \hline \textbf{D'Kitty} \\ \hline 0.0 \\ \hline \textbf{102}^{(6.1)} \\ \hline 31.5^{(3.6)} \\ \hline \textbf{102}^{(6.7)} \\ \hline \textbf{107}^{(6.7)} \\ \hline \textbf{103}^{(6.3)} \\ \hline \textbf{27.3}^{(3.4)} \\ \hline \textbf{103}^{(6.3)} \\ \hline \textbf{103}^{(7.2)} \\ \hline \textbf{108}^{(7.2)} \\ \hline \textbf{109}^{(4.5)} \\ \hline \textbf{109}^{(4.5)} \\ \hline \textbf{100}^{(0.0)} \\ \hline \textbf{112}^{(7.8)} \\ \hline \textbf{91.9}^{(2.0)} \\ \hline \textbf{29.6}^{(3.6)} \\ \hline \end{array}$	1.3 Rank \downarrow 2.3 3.8 1.8 1.7 2.7 3.0 1.8 2.3 2.5 3.3 2.5 3.3 2.2 2.0 2.0 2.0 2.1 3.0 2.2 2.3 3.0 2.3 1.8 2.5	-20.7 Opt. Gap
= - -	DynMO-CoSyNE DynAMO-CoSyNE DynAMO-CoSyNE Dataset D Grad. AMO-Grad. DynAO-Grad. DynAMO-Grad. DynAMO-Grad. DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-Adam DynAMO-BO-qEI DynAMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-BO-qUCB DynMO-CMA-ES DynAMO-CMA-ES DynAMO-CMA-ES	18.1 ^(13.0) TFBind8 0.0 21.2 ^(3.0) 14.0 ^(2.0) 21.9 ^(3.0) 21.1 ^(1.1) 23.7 ^(2.8) 23.7 ^(3.1) 22.9 ^(2.3) 14.7 ^(1.9) 21.8 ^(0.5) 15.4 ^(0.3) 20.4 ^(0.4) 21.0 ^(0.5) 21.6 ^(0.3) 21.9 ^(0.4) 20.7 ^(0.4) 21.4 ^(0.5) 16.5 ^(2.1) 24.3 ^(0.3) 12.9 ^(0.8) 24.5 ^(3.5)	20.3 ^(2.3) UTR 0.0 51.7 ^(2.9) 46.7 ^(2.7) 53.6 ^(2.1) 52.2 ^(1.3) 51.1 ^(3.5) 51.3 ^(3.4) 51.6 ^(2.9) 46.2 ^(0.5) 51.5 ^(0.3) 51.8 ^(0.2) 51.8 ^(0.2) 51.7 ^(0.2) 51.7 ^(0.3) 51.7 ^(0.2) 51.7 ^(0.2)	35.0 ^(17.9) ChEMBL 0.0 97.4 ^(3,9) 96.8 ^(3,9) 93.1 ^(6,6) 98.6 ^(1,5) 95.5 ^(5,3) 95.0 ^(5,1) 99.2 ^(0,6) 98.7 ^(1,2) 97.6 ^(0,3) 97.8 ^(0,3) 97.7 ^(0,3) 97.7 ^(0,3) 97.9 ^(0,4) 97.9 ^(0,4) 97.9 ^(0,4) 97.1 ^(0,5) 96.5 ^(0,7) 95.0 ^(1,5) 98.2 ^(1,0) 98.5 ^(1,6)	22.8 ^(11.9) Molecule 0.0 79.5 ^(19.7) 76.8 ^(19.7) 86.4 ^(10.2) 85.8 ^(1.0) 79.3 ^(21.2) 80.0 ^(20.6) 87.3 ^(9.7) 85.9 ^(1.8) 85.9 ^(1.8) 85.4 ^(1.5) 84.9 ^(0.9) 85.7 ^(1.3) 85.2 ^(1.0) 85.3 ^(1.1) 85.3 ^(1.1)	74.4 ^(46.3) Superconductor 0.0 95.0 ^(0,7) 83.8 ^(6.8) 95.0 ^(0,7) 95.0 ^(0,4) 94.8 ^(0,7) 84.8 ^(6.4) 94.7 ^(0,7) 94.9 ^(0,4) 94.9 ^(0,4) 94.9 ^(0,4) 94.9 ^(0,1) 85.1 ^(0,4) 94.9 ^(0,4) 94.9 ^(0,1) 85.1 ^(0,4) 94.8 ^(0,1) 93.2 ^(1,4) 94.7 ^(0,2) 100 ^(0,0) 85.6 ^(3,0) 100 ^(0,0) 85.6 ^(3,0) 100 ^(0,0) 94.5 ^(0,7) 93.2 ^(1,0)	$\begin{array}{c} {\bf 77.0^{(35.9)}}\\ \hline {\bf D'Kitty}\\ \hline 0.0\\ {\bf 102^{(6.1)}}\\ {\bf 31.5^{(3.6)}}\\ {\bf 102^{(6.1)}}\\ {\bf 107^{(6.7)}}\\ \hline {\bf 103^{(6.3)}}\\ {\bf 27.3^{(3.4)}}\\ {\bf 103^{(6.3)}}\\ {\bf 108^{(7.2)}}\\ \hline {\bf 108^{(7.2)}}\\ {\bf$	1.3 Rank \downarrow 2.3 3.8 1.8 1.7 2.7 3.0 1.8 2.3 2.5 3.3 2.5 3.3 2.2 2.0 2.7 3.2 2.2 2.3 3.0 2.0 2.3 3.0 2.3 1.8	-20.7 Opt. Gap ~

Table A13. Diversity of Design Candidates in Ablation of Adversarial Critic Feedback (AMO) and Diversity in (DynMO) Modelbased Optimization (cont.). We evaluate our method (1) with the KL-divergence penalized-MBO objective as in (11) only (DynMO); (2) with the adversarial source critic-dependent constraint as introduced by Yao et al. (2024) only (AMO); and (3) with both algorithmic components as in **Dyn** \underline{A} MO described in **Algorithm 1**. We report the L_1 coverage score achieved by the 128 evaluated designs as mean^(95% confidence interval) across 10 random seeds, where higher is better. **Bolded** entries indicate average scores with an overlapping 95% confidence interval to the best performing method. Bolded (resp., Underlined) Rank and Optimality Gap (Opt. Gap) metrics indicate the best (resp., second best) for a given backbone optimizer.

2000									
2659	L_1 Coverage@128	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	$\mathbf{Rank} \downarrow$	Opt. Gap↑
2660	Dataset \mathcal{D}	0.42	0.31	1.42	0.68	6.26	0.58	_	_
2661	Grad.	0.16 ^(0.10)	0.20 ^(0.13)	0.21 ^(0.10)	0.42 ^(0.18)	0.00 ^(0.00)	$0.00^{(0.00)}$	3.3	-1.44
2662	AMO-Grad.	$0.17^{(0.10)}$	$0.24^{(0.13)}$	$0.25^{(0.16)}$	$0.37^{(0.11)}$	$0.00^{(0.00)}$	$0.09^{(0.14)}$	2.5	-1.42
2663	DynMO-Grad.	0.20 ^(0.13)	0.22(0.15)	$1.23^{(0.63)}$	$0.28^{(0.17)}$	$0.00^{(0.00)}$	$0.00^{(0.00)}$	2.8	-1.29
2664	Dyn <u>A</u> MO-Grad.	0.36 ^(0.04)	$0.52^{(0.06)}$	1.46 ^(0.38)	2.49 ^(0.06)	6.47 ^(1.24)	5.85 ^(1.35)	1.0	1.25
2665	Adam	0.11 ^(0.06)	0.22 ^(0.09)	0.23(0.15)	0.48 ^(0.31)	0.27 ^(0.55)	$0.24^{(0.49)}$	2.8	-1.35
	<u>A</u> MO-Adam	$0.14^{(0.06)}$	0.22 ^(0.10)	0.35 ^(0.24)	0.50 ^(0.34)	0.26 ^(0.53)	0.09 ^(0.12)	3.0	-1.35
2666	DynMO-Adam	0.20 ^(0.12)	0.21(0.15)	1.10 ^(0.60)	0.45 ^(0.29)	0.27 ^(0.55)	0.03(0.00)	3.0	-1.23
2667	Dyn <u>A</u> MO-Adam	0.33 ^(0.05)	0.55 ^(0.03)	1.44 ^(0.39)	$2.40^{(0.16)}$	7.06 ^(0.73)	6.91 ^(0.71)	1.0	1.50
2668	BO-qEI	0.41 ^(0.02)	0.55 ^(0.01)	2.37(0.03)	2.11 ^(0.15)	7.84 ^(0.01)	6.61 ^(0.33)	2.8	1.70
2669	AMO-BO-qEI	0.40 ^(0.03)	0.55 ^(0.01)	2.38 ^(0.10)	2.53 ^(0.05)	7.45 ^(0.01)	$1.29^{(0.08)}$	3.7	0.82
2670	DynMO-BO-qEI	$0.40^{(0.02)}$	0.55 ^(0.01)	$2.42^{(0.05)}$	$2.55^{(0.03)}$	7.83 ^(0.02)	$6.72^{(0.48)}$	<u>2.3</u>	<u>1.80</u>
2671	Dyn <u>A</u> MO-BO-qEI	$0.42^{(0.01)}$	0.56 ^(0.01)	$2.47^{(0.03)}$	2.54 ^(0.03)	7.87 ^(0.01)	$7.92^{(0.04)}$	1.2	2.02
2672	BO-qUCB	0.40 ^(0.02)	$0.54^{(0.01)}$	2.40 ^(0.05)	$2.52^{(0.07)}$	7.78 ^(0.04)	6.64 ^(0.09)	2.8	1.77
2673	AMO-BO-qUCB	0.40 ^(0.01)	0.56 ^(0.01)	2.39(0.05)	$2.52^{(0.04)}$	7.37 ^(0.09)	1.34 ^(0.04)	3.3	0.82
	DynMO-BO-qUCB	0.39(0.02)	$0.55^{(0.00)}$	$2.40^{(0.08)}$	$2.52^{(0.04)}$	7.76 ^(0.07)	6.64 ^(0.13)	2.5	1.77
2674	Dyn <u>A</u> MO-BO-qUCB	$0.40^{(0.02)}$	$0.55^{(0.01)}$	$2.47^{(0.07)}$	$2.54^{(0.05)}$	7.88 ^(0.03)	7.80 ^(0.23)	1.3	2.00
2675	CMA-ES	0.33(0.05)	$0.48^{(0.04)}$	2.18(0.04)	$1.82^{(0.12)}$	3.26 ^(1.42)	3.77 ^(1.36)	2.3	0.36
2676	AMO-CMA-ES	$0.31^{(0.04)}$	$0.51^{(0.01)}$	$2.17^{(0.06)}$	$1.83^{(0.15)}$	3.37 ^(0.49)	3.12 ^(0.40)	2.5	0.27
2677	DynMO-CMA-ES	0.34 ^(0.09)	0.39(0.12)	0.66 ^(0.43)	$0.60^{(0.42)}$	1.85 ^(2.28)	0.94 ^(1.73)	3.7	-0.81
2678	Dyn <u>A</u> MO-CMA-ES	0.40 ^(0.03)	0.56 ^(0.01)	$1.82^{(0.72)}$	$2.54^{(0.05)}$	4.75 ^(2.16)	3.29 ^(1.56)	1.5	0.62
2679	CoSyNE	0.10 ^(0.07)	0.22(0.10)	0.39(0.20)	0.27 ^(0.13)	0.10 ^(0.00)	0.10 ^(0.00)	2.8	-1.41
2680	<u>A</u> MO-CoSyNE	$0.12^{(0.08)}$	$0.22^{(0.15)}$	0.53 ^(0.18)	$0.14^{(0.13)}$	$0.10^{(0.00)}$	$0.02^{(0.00)}$	2.8	-1.42
	DynMO-CoSyNE	$0.28^{(0.09)}$	$0.32^{(0.13)}$	0.33 ^(0.23)	$0.79^{(0.65)}$	$0.10^{(0.00)}$	$0.02^{(0.00)}$	2.3	-1.30
2681	Dyn <u>A</u> MO-CoSyNE	0.21 ^(0.11)	0.18 ^(0.09)	0.64 ^(0.42)	0.43 ^(0.34)	1.85 ^(0.22)	0.94 ^(0.17)	1.8	-0.90
2682									

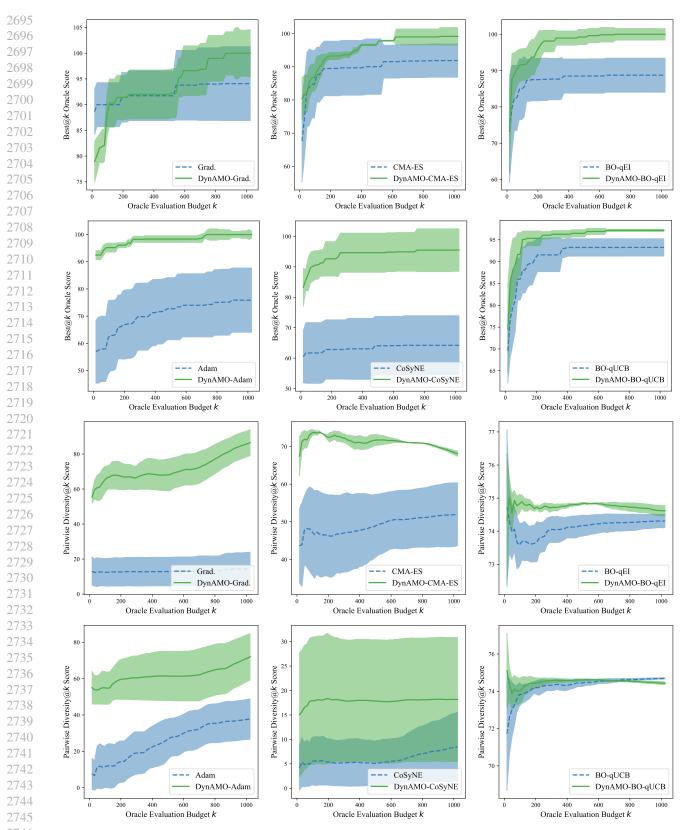


Figure A6. Oracle Evaluation Budget Ablation. We vary the allowed oracle evaluation budget k in Algorithm 1 between 16 and 1024, and report both the (first two rows) Best@128 Oracle Score and (last two rows) Pairwise Diversity score for k final designs proposed by both DynAMO-augmented and base optimizers on the TFBind8 task. We plot the mean \pm 95% confidence interval over 10 random seeds.

Table A14. Optimization Initialization Ablation. We evaluate DynAMO with Gradient Ascent and other first-order model-based optimization methods against model-free optimization methods. We report the maximum oracle score (resp., pairwise diversity score) achieved out of 128 evaluated designs in the top (resp., bottom) table. Metrics are reported mean^(95% confidence interval) across 10 random seeds, where higher is better. $\max(\mathcal{D})$ reports the top oracle score in the offline dataset. All metrics are multiplied by 100 for easier legibility. **Bolded** entries indicate the higher average scores for a given optimization method.

Best@128	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	Win Rate †
Dataset \mathcal{D}	43.9	59.4	60.5	88.9	40.0	88.4	
Grad. (Sobol)	90.0 ^(4.3)	80.9(12.1)	60.2(8.9)	88.8 ^(4.0)	36.0 ^(6.8)	65.6 ^(14.5)	3/6
Grad. (Top- k)	85.1 ^(3.1)	64.0 ^(0.7)	63.3 ^(0.0)	90.1 ^(0.3)	27.1 ^(1.0)	67.8 ^(0.0)	3/6
COMs (Sobol)	84.7(5.3)	60.4(2.2)	63.3(0.0)	91.4 ^(0.4)	17.3 ^(0.5)	82.8(2.9)	0/6
COMs (Top-k)	93.1 ^(3.4)	67.0 ^(0.9)	64.6 ^(1.0)	97.1 ^(1.6)	41.2 ^(4.8)	91.8 ^(0.9)	6/6
RoMA (Sobol)	96.5 ^(0.0)	77 .8 ^(0.0)	63.3 ^(0.0)	85.5 ^(2.4)	46.5(2.5)	93.9 ^(1.0)	4/6
RoMA (Top-k)	96.5 ^(0.0)	77.8 ^(0.0)	63.3 ^(0.0)	84.7 ^(0.0)	49.8 ^(1.4)	95.7 ^(1.6)	6/6
ROMO (Sobol)	97.7 ^(1.2)	67.0 ^(1.3)	68.3 ^(0.5)	90.8 ^(0.4)	45.5 ^(1.6)	86.1 ^(0.5)	3/6
ROMO (Top-k)	98.1 ^(0.7)	66.8 ^(1.0)	63.0 ^(0.8)	91.8 ^(0.9)	38.7 ^(2.5)	87.8 ^(0.9)	3/6
GAMBO (Sobol)	73.1(12.8)	77.1 ^(9.6)	64.4 ^(1.5)	92.8 ^(8.0)	46.0 ^(6.8)	90.6 ^(14.5)	5/6
GAMBO (Top-k)	78.5 ^(9.3)	68.3 ^(0.5)	63.0 ^(0.0)	90.6 ^(0.3)	27.1 ^(1.0)	77.8 ^(0.0)	1/6
DynAMO (Sobol)	90.3 ^(4.7)	86.2 ^(0.0)	64.4 ^(2.5)	91.2 ^(0.0)	44.2 ^(7.8)	89.8 ^(3.2)	6/6
DynAMO (Top-k)	81.9 ^(8.4)	64.4 ^(1.2)	63.3 ^(0.0)	90.8 ^(0.3)	29.4 ^(4.4)	75.3(11.6)	0/6
Pairwise Diversity@128	TFBind8	UTR	ChEMBL	Molecule	Superconductor	D'Kitty	Win Rate ↑
Dataset \mathcal{D}	33.7	42.8	50.9	87.6	6.7	77.8	_
Grad. (Sobol)	12.5(8.0)	7.8(8.8)	7.9 ^(7.8)	24.1(13.3)	0.0 ^(0.0)	0.0 ^(0.0)	3/6
						0.0	5/0
Grad. (Top-k)	8.3(4.7)	40.3 ^(3.6)	63.1 ^(8.3)	28.4 ^(6.0)	0.0 ^(0.0)	0.0 ^(0.0)	5/6
Grad. (Top-k) COMs (Sobol)	65.4 ^(0.5)	40.3 ^(3.6) 57.3 ^(0.1)	63.1 ^(8.3) 59.3 ^(1.1)	28.4 ^(6.0) 72.6 ^(0.7)	0.0 ^(0.0) 43.9 ^(16.5)	0.0 ^(0.0) 33.8 ^(1.7)	
	65.4 ^(0.5) 66.6 ^(1.0)	40.3 ^(3.6)	63.1 ^(8.3)	28.4 ^(6.0)	0.0 ^(0.0)	0.0 ^(0.0)	5/6
COMs (Sobol)	65.4 ^(0.5) 66.6 ^(1.0) 21.0 ^(0.2)	40.3 ^(3.6) 57.3 ^(0.1) 57.4 ^(0.2) 3.8 ^(0.0)	63.1 ^(8.3) 59.3 ^(1.1) 81.6 ^(4.9) 5.9 ^(0.0)	28.4 ^(6.0) 72.6 ^(0.7) 3.8 ^(0.9) 1.8 ^(0.0)	0.0 ^(0.0) 43.9 ^(16.5) 99.5 ^(25.8) 70.3 ^(13.6)	0.0 ^(0.0) 33.8 ^(1.7) 21.1 ^(23.5) 8.1 ^{(0.3}	5/6 2/6
COMs (Sobol) COMs (Top-k)	65.4 ^(0.5) 66.6 ^(1.0)	40.3 ^(3.6) 57.3 ^(0.1) 57.4 ^(0.2)	63.1 ^(8.3) 59.3 ^(1.1) 81.6 ^(4.9)	28.4 ^(6.0) 72.6 ^(0.7) 3.8 ^(0.9)	0.0 ^(0.0) 43.9 ^(16.5) 99.5 ^(25.8)	0.0 ^(0.0) 33.8 ^(1.7) 21.1 ^(23.5)	5/6 2/6 4/6
COMs (Sobol) COMs (Top-k) RoMA (Sobol)	65.4 ^(0.5) 66.6 ^(1.0) 21.0 ^(0.2) 21.3 ^(0.3) 64.4 ^(1.3)	40.3 ^(3.6) 57.3 ^(0.1) 57.4 ^(0.2) 3.8 ^(0.0) 3.8 ^(0.0) 56.9 ^(0.2)	63.1 ^(8.3) 59.3 ^(1.1) 81.6 ^(4.9) 5.9 ^(0.0) 5.9 ^(0.2) 59.3 ^(0.9)	28.4 ^(6.0) 72.6 ^(0.7) 3.8 ^(0.9) 1.8 ^(0.0) 1.8 ^(0.0) 39.0 ^(0.9)	0.0 ^(0.0) 43.9 ^(16.5) 99.5 ^(25.8) 70.3 ^(13.6) 49.4 ^(6.1) 58.3 ^(12.9)	0.0 ^(0.0) 33.8 ^(1.7) 21.1 ^(23.5) 8.1 ^{(0.3} 14.8 ^(0.6) 10.9 ^(0.5)	5/6 2/6 4/6 4/6
COMs (Sobol) COMs (Top-k) RoMA (Sobol) RoMA (Top-k)	65.4 ^(0.5) 66.6 ^(1.0) 21.0 ^(0.2) 21.3 ^(0.3)	40.3 ^(3.6) 57.3 ^(0.1) 57.4 ^(0.2) 3.8 ^(0.0) 3.8 ^(0.0)	63.1 ^(8.3) 59.3 ^(1.1) 81.6 ^(4.9) 5.9 ^(0.0) 5.9 ^(0.2)	28.4^(6.0) 72.6^(0.7) 3.8 ^(0.9) 1.8^(0.0) 1.8^(0.0)	0.0 ^(0.0) 43.9 ^(16.5) 99.5 ^(25.8) 70.3 ^(13.6) 49.4 ^(6.1)	0.0 ^(0.0) 33.8 ^(1.7) 21.1 ^(23.5) 8.1 ^{(0.3} 14.8 ^(0.6)	5/6 2/6 4/6 4/6 5/6
COMs (Sobol) COMs (Top-k) RoMA (Sobol) RoMA (Top-k) ROMO (Sobol)	65.4 ^(0.5) 66.6 ^(1.0) 21.0 ^(0.2) 21.3 ^(0.3) 64.4 ^(1.3) 62.1 ^(0.8) 15.1 ^(11.2)	40.3 ^(3.6) 57.3 ^(0.1) 57.4 ^(0.2) 3.8 ^(0.0) 3.8 ^(0.0) 56.9 ^(0.2) 57.1 ^(0.1) 10.3 ^(11.5)	63.1 ^(8.3) 59.3 ^(1.1) 81.6 ^(4.9) 5.9 ^(0.0) 5.9 ^(0.2) 59.3 ^(0.9) 53.9 ^(0.6) 12.1 ^(11.3)	28.4 ^(6.0) 72.6 ^(0.7) 3.8 ^(0.9) 1.8 ^(0.0) 1.8 ^(0.0) 39.0 ^(0.9) 48.7 ^(0.1) 19.6 ^(15.2)	0.0 ^(0.0) 43.9 ^(16.5) 99.5 ^(25.8) 70.3 ^(13.6) 49.4 ^(6.1) 58.3 ^(12.9) 51.7 ^(31.7) 0.3 ^(0.8)	0.0 ^(0.0) 33.8 ^(1.7) 21.1 ^(23.5) 8.1 ^{(0.3} 14.8 ^(0.6) 10.9 ^(0.5) 22.1 ^(5.5) 2.6 ^(3.9)	5/6 2/6 4/6 4/6 5/6 3/6
COMs (Sobol) COMs (Top-k) RoMA (Sobol) RoMA (Top-k) ROMO (Sobol) ROMO (Top-k)	65.4 ^(0.5) 66.6 ^(1.0) 21.0 ^(0.2) 21.3 ^(0.3) 64.4 ^(1.3) 62.1 ^(0.8)	40.3 ^(3.6) 57.3 ^(0.1) 57.4 ^(0.2) 3.8 ^(0.0) 3.8 ^(0.0) 56.9 ^(0.2) 57.1 ^(0.1)	63.1 ^(8.3) 59.3 ^(1.1) 81.6 ^(4.9) 5.9 ^(0.0) 5.9 ^(0.2) 59.3 ^(0.9) 53.9 ^(0.6)	28.4 ^(6.0) 72.6 ^(0.7) 3.8 ^(0.9) 1.8 ^(0.0) 1.8 ^(0.0) 39.0 ^(0.9) 48.7 ^(0.1)	0.0 ^(0.0) 43.9 ^(16.5) 99.5 ^(25.8) 70.3 ^(13.6) 49.4 ^(6.1) 58.3 ^(12.9) 51.7 ^(31.7)	0.0 ^(0.0) 33.8 ^(1.7) 21.1 ^(23.5) 8.1 ^{(0.3} 14.8 ^(0.6) 10.9 ^(0.5) 22.1 ^(5.5) 2.6 ^(3.9) 0.0 ^(0.0)	5/6 2/6 4/6 4/6 5/6 3/6 3/6
COMs (Sobol) COMs (Top-k) RoMA (Sobol) RoMA (Top-k) ROMO (Sobol) ROMO (Top-k) GAMBO (Sobol)	65.4 ^(0.5) 66.6 ^(1.0) 21.0 ^(0.2) 21.3 ^(0.3) 64.4 ^(1.3) 62.1 ^(0.8) 15.1 ^(11.2) 59.2 ^(5.0) 66.9 ^(6.9)	40.3 ^(3.6) 57.3 ^(0.1) 57.4 ^(0.2) 3.8 ^(0.0) 3.8 ^(0.0) 56.9 ^(0.2) 57.1 ^(0.1) 10.3 ^(11.5) 54.1 ^(2.5) 68.2 ^(10.8)	63.1 ^(8.3) 59.3 ^(1.1) 81.6 ^(4.9) 5.9 ^(0.0) 5.9 ^(0.2) 59.3 ^(0.6) 53.9 ^(0.6) 12.1 ^(11.3) 79.3 ^{3.4)} 77.2 ^(21.5)	28.4 ^(6.0) 72.6 ^(0.7) 3.8 ^(0.9) 1.8 ^(0.0) 1.8 ^(0.0) 39.0 ^(0.9) 48.7 ^(0.1) 19.6 ^(15.2) 33.4 ^(1.9) 93.0 ^(1.2)	0.0 ^(0.0) 43.9 ^(16.5) 99.5 ^(25.8) 70.3 ^(13.6) 49.4 ^(6.1) 58.3 ^(12.9) 51.7 ^(31.7) 0.3 ^(0.8) 0.0 ^(0.0) 129 ^(55.3)	0.0 ^(0.0) 33.8 ^(1.7) 21.1 ^(23.5) 8.1 ^{(0.3} 14.8 ^(0.6) 10.9 ^(0.5) 22.1 ^(5.5) 2.6 ^(3.9) 0.0 ^(0.0) 104 ^(56.1)	5/6 2/6 4/6 5/6 3/6 3/6 2/6
COMs (Sobol) COMs (Top-k) RoMA (Sobol) RoMA (Top-k) ROMO (Sobol) ROMO (Top-k) GAMBO (Sobol) GAMBO (Top-k)	65.4 ^(0.5) 66.6 ^(1.0) 21.0 ^(0.2) 21.3 ^(0.3) 64.4 ^(1.3) 62.1 ^(0.8) 15.1 ^(11.2) 59.2 ^(5.0)	40.3 ^(3.6) 57.3 ^(0.1) 57.4 ^(0.2) 3.8 ^(0.0) 3.8 ^(0.0) 56.9 ^(0.2) 57.1 ^(0.1) 10.3 ^(11.5) 54.1 ^(2.5)	63.1 ^(8.3) 59.3 ^(1.1) 81.6 ^(4.9) 5.9 ^(0.0) 59.3 ^(0.9) 53.9 ^(0.6) 12.1 ^(11.3) 79.3 ^{3.4)}	28.4 ^(6.0) 72.6 ^(0.7) 3.8 ^(0.9) 1.8 ^(0.0) 1.8 ^(0.0) 3 9.0 ^(0.9) 48.7 ^(0.1) 1 9.6 ^(15.2) 33.4 ^(1.9)	0.0 ^(0.0) 43.9 ^(16.5) 99.5 ^(25.8) 70.3 ^(13.6) 49.4 ^(6.1) 58.3 ^(12.9) 51.7 ^(31.7) 0.3 ^(0.8) 0.0 ^(0.0)	0.0 ^(0.0) 33.8 ^(1.7) 21.1 ^(23.5) 8.1 ^{(0.3} 14.8 ^(0.6) 10.9 ^(0.5) 22.1 ^(5.5) 2.6 ^(3.9) 0.0 ^(0.0)	5/6 2/6 4/6 5/6 3/6 3/6 2/6 4/6