TOWARDS NEURAL SCALING LAWS FOR FOUNDATION MODELS ON TEMPORAL GRAPHS

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ABSTRACT

Temporal graph learning aims to extract knowledge from dynamic network data to predict future interactions. The key question is, given a set of observed temporal graphs, is it possible to forecast the evolution of an unobserved network within the same domain? To answer this question, we present Temporal Graph Scaling (TGS) dataset, a large collection of temporal graphs consisting of *eighty-four* ERC20 token transaction networks collected from 2017 to 2023. Next, we assess the transferability of Temporal Graph Neural Networks (TGNNs) in temporal graph property prediction by pre-training on up to 64 token transaction networks and evaluating their downstream performance on *twenty* unseen token networks.

We observe that the neural scaling law, previously identified in NLP and computer vision, also holds in temporal graph learning. Specifically, pre-training on a larger number of networks results in enhanced downstream performance. To the best of our knowledge, this study is the first empirical demonstration of transferability to unseen networks in temporal graph learning. Notably, on *thirteen out of twenty* unseen test networks, our largest pre-trained model using zero-shot inference can outperform fine-tuned TGNNs on each test network. We believe that this work is a promising first step towards developing foundation models for temporal graphs. The implementation of Temporal Graph Scaling can be accessed at https://anonymous.4open.science/r/ScalingTGNs.

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1 INTRODUCTION

032 Foundation models have revolutionized various fields such as natural language processing 033 (NLP) Bubeck et al. (2023); Brown et al. (2020); Rasul et al. (2024) and computer vision (CV) Rad-034 ford et al. (2021); Awais et al. (2023) by providing robust pre-trained architectures that can be transferred to a multitude of tasks. Foundation models aim to learn from large amounts of pre-training data and transfer the knowledge to downstream unseen tasks. These models have been recognized for 037 their remarkable transfer capabilities and promising efficacy with few-shot and zero-shot learning on 038 novel datasets and tasks Bommasani et al. (2021); Dong et al. (2023); Rasul et al. (2024). Despite advances in NLP and CV, foundation models in graph representation learning remain relatively unexplored. For example, there has been some notable work on foundational models for graph neural 040 networks (GNNs) that demonstrate the potential of these models Mao et al. (2024); Galkin et al. 041 (2023); Beaini et al. (2023); Méndez-Lucio et al. (2022). However, most research has focused on 042 static graph learning, leaving the exploration of temporal graph neural networks largely untapped. 043

To effectively train foundation models, a large collection of datasets is essential. Networks within the same domain often exhibit similar trends and statistics Jin & Zafarani (2020). These datasets are crucial for assessing the performance of TGNNs, driving innovation, and ensuring that new methods can be generalized across various applications. To facilitate research on foundation models for temporal graphs, we introduce the Temporal Graph Scaling (TGS) benchmark, a comprehensive dataset containing 84 novel temporal graphs derived from Ethereum transaction networks. TGS provides temporal networks with up to 128K nodes and 0.5M edges, totaling 3M nodes and 19M edges across all networks. These datasets also vary in their time duration and helps facilitate the training of foundation models for temporal graph learning.

Quick adaptation of a foundation model to novel unseen data is crucial, especially in financial token networks, where new datasets frequently emerge and the costs of training multiple models become 054 prohibitive Shamsi et al. (2022); Zhang et al. (2023). To achieve this, we must first study how 055 transferrable a pre-trained temporal graph model is to unseen networks. Therefore, we propose the first algorithm for pre-training TGNNs on multiple temporal graphs, called the TGS-train algorithm. 057 Models that are trained on multiple networks are then referred to as multi-network models. With only zero-shot inference, our multi-network models achieve significant performance advantages over models trained on individual test networks. This demonstrates the high potential of transferability of large pre-trained models on temporal graphs. We also demonstrate that training on a larger number of 060 temporal graphs results in stronger downstream performance. Figure 1 shows the scaling behavior of 061 our multi-network model. The average performance of the multi-network model on twenty unseen 062 token networks increases as the number of networks used for training increases. 063

064 Our main contributions are as follows:

- Novel Collection of Temporal Networks. We release a comprehensive collection of 84 labeled datasets derived from token transaction networks for the graph property prediction task. These datasets provide the foundation for studying scaling behavior, transferability and multi-network learning on temporal graphs.
- First Multi-network Training Algorithm for Temporal Graphs. To the best of our knowledge, we propose the first training algorithm, named TGS-train, that enables TGNNs to train on multiple networks at once.
- Neural Scaling Law on TGNNs. We explore the potential of foundation models on temporal graphs by showing that neural scaling law also applies to temporal graphs: training TGNNs with more temporal graphs (up to 64) offers a significant performance boost in downstream test networks.
- **Transferability Across Networks.** We demonstrate that by pre-training on a large number of temporal graphs, our multi-network model is directly transferable to 20 downstream unseen token networks while outperforming single models trained on the test networks. This shows that it is possible to learn an overall distribution across temporal graphs and transfer it to novel networks.

Reproducibility. Our code is available on 4open.science. The TGS datasets are publicly available on Dropbox (during the anonymity period).

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2 RELATED WORK

087 Temporal Graph Benchmarks. Numerous 088 graph benchmark datasets have been introduced to advance research within the temporal 090 graph learning community. Poursafaei et al. 091 (2022) introduced six dynamic graph datasets 092 while proposing visualization techniques and 093 novel negative edge sampling strategies to facilitate link prediction tasks of dynamic graphs. Following the good practice from OGB Hu et al. (2020), Huang et al. (2023) 096 introduced TGB, which provides automated and reproducible results with a novel standard-098 ized evaluation pipeline for both link and node property prediction tasks. However, these 100 datasets belong to different domains, making 101 them unsuitable for studying the scaling laws 102 of neural network models trained with a large 103 number of datasets from the same domain. Li 104 et al. (2024) provide a temporal benchmark 105 for evaluating graph neural networks in link



Figure 1: Scaling behavior of multi-network models. The performance of multi-network trained on 2^n where $n \in [1, 6]$ compared to a *single model* that is trained on each test dataset and a simple baseline such as *persistence forecast*.

prediction tasks, though their focus does not extend to training on multiple networks. Conversely, the
 Live Graph Lab dataset by Zhang et al. (2023) offers a temporal dataset and benchmark, employed
 for tasks like temporal node classification using TGNNs. This work aims to explore multi-network

training and understand the transferability across temporal graphs. Therefore, we curate a collection of temporal graphs rather than focusing on individual ones as in prior work.

Discrete Time Dynamic Graphs. A common approach in discrete time models treats each snapshot 111 individually and captures spatial characteristics, then adopts an RNN-based method to learn temporal 112 dependencies Seo et al. (2016); Sankar et al. (2019); Chen et al. (2022); Li et al. (2019); Shamsi 113 et al. (2024). GCRN stacks a graph CNN for feature extraction and an LSTM cell for temporal 114 reasoning Seo et al. (2016). Differentiating from GCRN, EvolveGCN Pareja et al. (2020) uses RNN 115 to control the parameters of a GCN at each snapshot. Employing two attention blocks, DySat first 116 generates static node embeddings at each snapshot by running a GAT style GNN, and then computes 117 new embeddings using a temporal self-attention block Sankar et al. (2019). In the most recent work, 118 GraphPulse Shamsi et al. (2024) leverages Mapper, a key tool in topological data analysis, to extract essential information from temporal graphs. However, in all these studies, the training process of 119 every model was limited to a single dataset, and the effectiveness of training TGNs with diverse 120 networks to enhance their generalization capabilities is unexplored. 121

122 **Neural Scaling Laws.** Neural scaling laws characterize the relationship between model performance 123 and three main factors: number of parameters, size of training datasets and amount of computation 124 Rosenfeld et al. (2020); Kaplan et al. (2020); Abnar et al. (2022). These relationships are usually 125 described as a power law, which can be understood by observing learning as a movement on a smooth data manifold Bahri et al. (2021). Bahri et al. (2021) exhibited all four scaling regimes with respect 126 to the number of model parameters as well as the dataset size, underscoring different mechanisms 127 driving improvement in loss. The authors provided valuable insights into the design and training of 128 mixed-model generative models by studying mixed-modal scaling laws, indicating the generality 129 of scaling laws across different domains and applications. Recently, Liu et al. (2024) investigated 130 neural scaling laws for static graphs by observing the performance of GNNs given increases in the 131 model's size, defined by the number of layers and parameters, and training set size, defined by the number of edges. To the best of our knowledge, we are the first to investigate neural scaling laws for 133 temporal graphs.

134 Foundation Models. The foundation model is an emerging paradigm that aims to develop models 135 capable of generalization across different domains and tasks using the knowledge obtained from 136 massive data in the pre-trained stage. Recently, Rasul et al. (2024) introduced Lag-Llama, a general-137 purpose foundation model for univariate probabilistic time series forecasting based on a simple 138 decoder-only transformer architecture that uses lags as covariates. Galkin et al. (2023) introduced 139 ULTRA, a foundation model for knowledge graphs, which handles complex relational data and 140 supports diverse downstream tasks effectively. Similarly, Beaini et al. (2023) presented Graphium, 141 a collection of molecule graph datasets that facilitate the development of foundation models for 142 molecular applications, highlighting the importance of domain-specific datasets in enhancing the performance and generalizability of foundation models. Lastly, Xia et al. (2024) proposed OpenGraph, 143 an initiative towards open foundation models for graphs, emphasizing the need for transparency, 144 reproducibility, and community-driven advancements in graph representation learning. These works 145 underscore the growing recognition of the importance of foundation models and their transformative 146 potential across various domains, such as molecular graphs. However, foundation models for temporal 147 graphs remain unexplored. 148

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150 3 PRELIMINARIES

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Temporal Graphs are generally categorized into two types: Continous Time Dynamic Graphs (CTDGs) and Discrete Time Dynamic Graphs (DTDGs) Kazemi et al. (2020). We focus on DTDGs because this approach aligns well with our objective of capturing and analyzing the graph's dynamics at specific time intervals, such as on a weekly basis. In DTDGs, the graph's temporal evolution is represented in discrete time steps, simplifying the analysis and modeling of large-scale temporal multi networks. Each time step provides a snapshot of the graph at a specific moment, facilitating straightforward comparisons and the identification of temporal patterns.

159 Definition 1 (Discrete Time Dynamic Graphs). *DTDGs represent the network as a sequence of graph* **160** *snapshots denoted as* $\mathcal{G} = \{\mathcal{G}_{t_1}, \mathcal{G}_{t_2}, \mathcal{G}_{t_3}, \dots, \mathcal{G}_{t_n}\}$ where $t_i < t_j$. Each $\mathcal{G}_{t_i} = (\mathcal{V}_{t_i}, \mathcal{E}_{t_i}, \mathbf{X}_{t_i}, \mathbf{Y}_{t_i})$ *is* **161** *the graph at timestamp* t_i , where \mathcal{V}_{t_i} and \mathcal{E}_{t_i} represent the set of nodes and edges, \mathbf{X}_{t_i} denotes the *node feature matrix, and* \mathbf{Y}_{t_i} represents the edge feature matrix in graph \mathcal{G}_{t_i} . Therefore, a collection 162 of discrete-time dynamic graphs is defined as $D = \{\mathcal{G}^1, \mathcal{G}^2, \dots, \mathcal{G}^m\}$, where *m* is the number of DTDGs. 164

Temporal Graph Property Prediction. For the task of temporal graph property prediction, we aim to forecast a temporal graph property within a future time interval in a DTDG. More specifically, given a DTDG \mathcal{G} , we consider a time duration $[t_{\delta_1}, t_{\delta_2}]$, where δ_1 and δ_2 are non-negative integers with $\delta_1 \leq \delta_2$. Then at a specific time t_k , the goal is to predict the target graph property within the specified future interval $[t_{k+\delta_1}, t_{k+\delta_2}]$. Further details about our task formulation, including the definition of our graph property prediction and example of other property prediction tasks on graphs, are provided in Appendix Section C. .

Hyperbolic Graph Neural Networks. Hyperbolic geometry has been increasingly recognized for 172 its ability to achieve state-of-the-art performance in several static graph embedding tasks Yang et al. 173 (2021). HTGN is a recent hyperbolic work that shows strong performance in learning over dynamic 174 graphs in a DTDG manner. The model employs a hyperbolic graph neural network (HGNN) to learn 175 the topological dependencies of the nodes and a hyperbolic-gated recurrent unit (HGRU) to capture 176 the temporal dependencies. Temporal contextual attention (HTA) is also used To prevent recurrent 177 neural networks from only emphasizing the most nearby time and to ensure stability along with 178 generalization of the embedding. In addition, HTGN enables updating the model's state at the test 179 time to incorporate new information, which makes it a good candidate for learning the scaling law of 180 TGNNs. In our TGS framework, we use the HTGN architecture as part of our multi-network model 181 because it excels in dynamic graph learning through hyperbolic geometry. Its strong performance makes it a valuable addition to our approach. We further describe the HTGN in Appendix Section D. 182

4 Dataset

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We utilize a dataset of temporal graphs sourced from the Ethereum blockchain Wood et al. (2014). In this section, we will describe Ethereum, explain our data pipeline, and conclude by defining the characteristics of the resulting dataset.

188 Ethereum and ERC20 Token Net-189 works. We create our transaction 190 network data by first installing an 191 Ethereum node and accessing the 192 P2P network by using the Ethereum 193 client Geth (https://github. 194 com/ethereum/go-ethereum). 195 Then, we use Etherum-ETL(https: 196 //github.com/blockchain-etl/ ethereum-etl) to parse all ERC20 197

tokens and extract asset transactions. We 198 extracted more than sixty thousand ERC20 199 tokens from the entire history of the 200 Ethereum blockchain. However, during the 201 lifespans of most token networks, there are 202 interim periods without any transactions. 203 Additionally, a significant number of 204 tokens live for only a short time span. To 205 avoid training data quality challenges, 206 we use 84 token networks with at least one transaction every day during their 207 lifespan and are large enough to be used 208 as a benchmark dataset for multi-network 209 model training. 210



Figure 2: **TGS overview.** (1) <u>Token extraction</u>: extracting the token transaction network from the Ethereum node. (2) <u>Discretization</u>: creating weekly snapshots to form discrete time dynamic graphs. (3) <u>Multi-Network Model Training</u>: TGS transaction networks are divided randomly into train and test sets. We train the MNs on a collection of training networks. Lastly, MNs are tested on 20 unseen test networks.

Temporal Networks. Each token network represents a distinct temporal graph, reflecting the time stamped nature of its transactions. In these networks, nodes (addresses), edges (transactions), and
 edge weights (transaction values) evolve over time, capturing the dynamic behavior of the network.
 Additionally, these networks differ in their start dates and durations, introducing further variation
 in their evolution. While each token network operates independently with its own set of investors,
 they exhibit common patterns and behaviors characteristic of transaction networks. These similarities

12 16 Frequency Frequency 12 0. 1500 0.2 0.5 0.6 0.7 0.3 0.4 Novelty score Days (b)(a) 16 12 Frequency Frequency 8 0 10 10 Edges (×10⁵) Node (d) (c)

Figure 3: Network statistics of TGS networks: (a) Novelty score, (b) number of days, (c) number of nodes, and (d) number of edges.

allow the model to learn and generalize from these patterns across different networks. Collecting
 temporal graphs from different ERC20 token networks allows for comparative analysis, uncovering
 in-common patterns and unique behaviors. This strengthens the model's ability to generalize and
 improves its robustness.

Figure 2 illustrates the TGS overview from dataset extraction to the multi-network (MN) model training step.

239 Dataset Statistics. Our TGS dataset is a collection of 84 ERC20 token networks derived from 240 Ethereum from 2017 to 2023. Each token network is represented as a dynamic graph, in which each 241 address and transaction between addresses are a node and directed edge, respectively. The biggest 242 TGS token network contains 128, 159 unique addresses and 554, 705 transactions, while the smallest 243 token network has 1,454 nodes. TGS contains a diversity of dynamic graphs in terms of nodes, edges and timestamps, which are shown in Figure 3. Details on statistics are given in Appendix A. The 244 figure shows that most networks have more than 10k nodes and over 100k edges. The lifespan of TGS 245 networks varies from 107 days to 6 years, and there exists at least one transaction each day. Figure 3.a 246 shows the novelty scores, i.e., the average ratio of unseen edges in each timestamp, introduced by 247 Poursafaei et al. (2022). Figure 3 shows that most of the 84 networks have novelty scores greater than 248 0.3, indicating that each day sees a considerable proportion of new edges in these token networks. We 249 adopt a 70 - 15 - 15 split of train-test-validation for each token network and calculate the surprise 250 score Poursafaei et al. (2022), which indicates the number of edges that appear only in the test data. 251 As Table 4 shows, the token networks have quite high surprise values with an average of 0.82. We 252 also provide the node, edge and length distribution for train and test sets separately in Figure 6. 253 Overall, train set datasets mostly have more nodes than those in the test set, while the number of 254 edges and days are in the same range for both. A detailed overview of the characteristics of the TGS datasets is presented in Appendix A. 255

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5 Methodology

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We use Temporal Graph Neural Networks (TGNNs) as the multi-network model architecture. We choose the state-of-the-art Hyperbolic Temporal Graph Network (HTGN) Yang et al. (2021) as an example architecture for experiments. This section explains our choice and details our training algorithm on multiple networks.

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5.1 MULTI-NETWORK TRAINING ON TEMPORAL GRAPHS

Existing temporal graph learning models typically train on a single temporal graph, limiting their
ability to capture similar behaviors and generalize across different networks Rossi et al. (2020); Yang
et al. (2021). We introduce TGS-train, the pioneering algorithm designed to train across multiple
temporal graphs by modifying a state-of-the-art single network training model with two crucial

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Input: A Temporal Graph Dataset $D = \{\mathcal{G}^1, \mathcal{G}^2, \dots, \mathcal{G}^m\}$, where $\mathcal{G}^i = \{\mathcal{G}^i_{t_1}, \mathcal{G}^i_{t_2}, \dots, \mathcal{G}^i_{t_n}\}$ m = Number of networks in training, TGNN and Decoderfor each epoch doShuffled (D) // IID trainingfor each network $\mathcal{G}^i \in D$ doInitialize historical embeddings (reset) // context switchingfor each training snapshot $\mathcal{G}^i_{t_j} \in \mathcal{G}^i$ do $\mathcal{H}_{t_i} = \text{TGNN}(\mathcal{G}^i_{t_j})$ $\hat{y}_{t_i} = \text{Decoder}(\mathcal{H}_{t_j})$ $\mathcal{L} = \text{Loss}(y_{t_i}, \hat{y}_{t_j})$ BackpropagationUpdate historical embeddings with \mathcal{H}_{t_j} Evaluate on the validation snapshots of \mathcal{G}^i Average validation results across all datasets to select the best modelSave the best model for inference

Algorithm 1: TGS-train: Multi-Network Training for Temporal Graphs

steps: *shuffling* and *resets*. These steps, as we describe below, render the algorithm network-agnostic, capable of learning from various temporal graphs to generalize effectively to unseen networks.

Algorithm 1 shows TGS-train in detail. As the first step, we load a list of m temporal graphs $D = \{\mathcal{G}^1, \mathcal{G}^2, \dots, \mathcal{G}^m\}$, where each temporal graph \mathcal{G}^i is represented as a sequence of snapshot $\{\mathcal{G}_{t_1}^i, \mathcal{G}_{t_2}^i, \dots, \mathcal{G}_{t_n}^i\}$. For each epoch, we shuffle the orders of the list of datasets D to preserve the Independent and Identically Distributed (IID) assumption of neural network training.

296 **IID training.** To preserve the IID assumption in neural network training, we include a shuffling 297 step at each epoch. The randomized ordering of networks during training at each epoch is important 298 because it helps prevent the model from learning spurious correlations that could arise if the data 299 were presented in a fixed order. By shuffling the datasets, we promote randomness in the training 300 process, which contributes to more robust and generalizable model performance. Sequentially, for 301 each dataset \mathcal{G}^i , we first initialize the historical embeddings, then train the model end to end (i.e., encoder-decoder) on each dataset \mathcal{G}^i in a similar manner of training a single model, and evaluate the 302 performance on the corresponding validation set of dataset \mathcal{G}^i . After training on m datasets from D, 303 304 we compute the average validation results across these datasets. This average is used to select the best model, which is then saved for inference. Early stopping is applied if needed. 305

306 **Context switching.** Many TGNNs store and utilize node embeddings from previous timestamps at 307 later timestamps; we refer to those embeddings as historical embeddings Yang et al. (2021); Chen 308 et al. (2022); Pareja et al. (2020). Resetting historical embeddings at the beginning of each epoch is a key step in training a temporal model across multiple networks for several reasons. First, it helps prevent the model from carrying over biases or assumptions from one network to another, 310 ensuring that it can adapt effectively to the unique characteristics of each network. Starting with fresh 311 historical embeddings at the beginning of each epoch enables the models to learn the most relevant 312 and up-to-date information from the current network, improving performance and generalization 313 across different networks. Additionally, resetting historical embeddings can help mitigate the issue of 314 catastrophic forgetting, where the model may gradually lose information about previous networks as 315 it learns new ones. 316

Time complexity analysis. The TGS-train algorithm has the same complexity as training the single model across all the training networks. Specifically, the time complexity for HTGN using the TGStrain algorithm is $O(m \cdot (N_{max}dd' + d' |\mathcal{E}_{max}|))$ where m is the number of training networks, N_{max} is set to the maximum number of nodes of networks in the training set, d and d' are the dimensions of the input and output features while $|\mathcal{E}_{max}|$ is the maximum number of edges in a snapshot.

322 Inference on an unseen network. To evaluate the transferability of each multi-network model, we test the model on unseen datasets. To obtain testing data, we divide TGS into two disjoint sets, where one set is used for training obtained by randomly selecting 64 token networks, and the remaining

20 token networks are used to evaluate the performance. We begin by loading all the weights of
 multi-network models, including the pre-trained encoder and decoder parameters, while initializing
 fresh historical embeddings. Then, we perform a single forward pass over the train and validation
 split to adapt the historical embeddings specific to the testing dataset.

6 EXPERIMENTS

Weekly forecasts are common in the financial context for facilitating financial decisions Kim et al. (2021). Similarly, for the temporal graph property prediction task (defined in Section 3), we set $\delta_1 = 3$ and $\delta_2 = 10$, thus predicting the graph property over weekly snapshots. Experimentally, we use the network growth property (defined by edge counts) from Shamsi et al. (2024) as the prediction target.

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6.1 **PREDICTION BASELINES**

Persistence forecast. For our basic baseline model, we employ a naive setting similar to deterministic heuristics techniques, persistence forecast Salcedo-Sanz et al. (2022), for label prediction. In this approach, we use data from the previous and current weeks to predict the next week's property. If we observe an increasing trend in the number of transactions in the current week compared to the previous week, we predict a similar increasing trend for the following week. This simple model is based on the assumption that trends in transaction networks can persist over time.

345 **Single-network models.** We use four models from literature including HTGN Yang et al. (2021), 346 GCLSTM Chen et al. (2022), EvolveGCN Pareja et al. (2020) and GraphPulse Shamsi et al. (2024) 347 as our baseline single models. We further explain each model in Appendix Section B. We adopt the standard training process for these models over a single dataset and make predictions for the same 348 dataset. We adopt a 70% - 15% - 15% split ratio for the train, validation, and test, respectively, 349 for each token network, and during each epoch, the training model processes all snapshots in 350 chronological order. We train every single model for a minimum of 100 and a maximum of 250 351 epochs with a learning rate set to 15×10^{-4} . We apply early stopping based on the AUC results on 352 the validation set, with patience and tolerance set to 20 and 5×10^{-2} , respectively. Specifically, in 353 HTGN training, the node embeddings are reset at the end of every epoch. To address graph-level 354 tasks, we add an extra graph pooling layer as the final layer. This layer, implemented as a Multi-Layer 355 Perceptron (MLP), takes the mean of all node embeddings, concatenating with four snapshot features 356 at the graph level (including the mean of in-degree, the weight of in-degree, out-degree, and weight 357 of out-degree) and then outputs binary classification prediction. We use Binary Cross-Entropy Loss 358 for performance measurement and Adam Kingma & Ba (2015) as the optimization algorithm. It is important to note that the graph pooling layer, performance measurement, and optimization algorithm 359 are also shared by the multi-network model training setup. 360

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6.2 MULTI-NETWORK MODEL TRAINING SETUP

While following a similar training approach as in the single 364 model training, we make specific adjustments for the multinetwork model training. We set the number of epochs to 366 300 with a learning rate of 10^{-4} and a train-validation-test 367 chronological split ratio same as single models. Early stop-368 ping is applied based on the validation loss with a tolerance 369 of 5×10^{-2} and the patience is set to 30. The best model 370 is selected based on the validation AUC and used to predict 371 the unseen test dataset. We train six multi-network models, 372 each with a different number of networks corresponding to

 2^n datasets, where $n \in [1, 6]$. We name each multi-network



Figure 4: Time per epoch for training multi-network models.

model based on the number of datasets used in training; for example, MN-16 is trained with 16
datasets. For graph property prediction tasks on multi-network, we ran all experiments on NVIDIA
Quadro RTX 8000 (48G memory) with 4 standard CPU nodes (either Milan Zen 3 2.8 GHz and
768GB of memory each or Rome Zen 2, 2.5GHz and 256GB of memory each). We repeated each
experiment three times and reported the average and standard deviation of different runs. Empirically



Figure 5: Test AUC of multi-network models trained on 4, 16 and 64 networks and evaluated on unseen test datasets. We compare the performance with persistence forecast, and HTGN models trained and tested on each dataset.

we observe that the TGS-training time scales linearly to the number of networks as seen in Figure 4 where we report the time per epoch for each multi-network model.

6.3 RESULTS

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Multi-network vs. single-network models. We present the 397 performance of our multi-network models trained with datasets 398 of varying sizes and zero-shot inference tested on 20 unseen 399 test datasets. We compare our results with five baseline mod-400 els: Persistence Forecast, GCLSTM, EvolveGCN, HTGN, and 401 GraphPulse, as explained in Section 6.1. For visual clarity, Fig-402 ure 5 shows the AUC on test data results for MN-4, MN-16 and 403 MN-64 only as well as persistence forecasting and HTGN sin-404 gle model. We show the performance of all six multi-network 405 models in Appendix Figure 7. Overall, an upward trend is 406 observed in most datasets from multi-network models 2 to 64,

Table 1: Rank-based prediction performance results over different models.

Model	Top rank \uparrow	Avg. rank \downarrow	Win ratio \uparrow
Persist. forecast	0	7.9	0.00
Single model	3	4.35	-
MN-2	0	6.15	0.25
MN-4	2	4.35	0.45
MN-8	1	4.45	0.45
MN-16	1	3.45	0.65
MN-32	2	3.20	0.70
MN-64	11	2.15	0.80

such as in BAG, MIR and BEPRO datasets, highlighting the power of larger multi-network models in 407 temporal graph learning. In Figure 5, the MN-64 yields the best AUC in 16 out of 20 test datasets. 408 This result is significant because the multi-network models outperform the single models specif-409 ically trained on these datasets. We detail the prediction performance of the models in Table 410 2, where we present the AUC values for both single-trained baselines and multi-network models, 411 specifically MN-32 and MN-64, across various datasets. We also report the Top Rank, Average Rank, 412 and Win Ratio for each model. The Top Rank indicates the number of datasets where a method ranks 413 first. To calculate the Average Rank, we assign an AUC-based rank (ranging from 1 to 8) to every 414 model across the 20 test datasets and compute the average. The Win Ratio represents the proportion 415 of datasets where a model outperforms a single model.

416 Overall, MN-64 exhibits the best generalization performance, achieving the highest AUC in 6 datasets 417 and second-best in 7 datasets among 20 test datasets in a zero-shot setting. Moreover, Appendix 418 Table 7 indicates that the MN-64 also achieves superior performance in 43 datasets and equivalent 419 performance in 2 datasets among 64 token networks in the training sets compared to the performance 420 of single models. This demonstrates the strong generalizability and transferability of our MN-64 421 model. While GraphPulse achieves the highest top rank of 8, it relies on trained inference, unlike our 422 multi-network models, which are based on zero-shot inference. Notably, training GraphPulse on each 423 dataset is computationally expensive, while inference testing of our pre-trained MN-64 on all datasets takes only a few minutes. This makes the performance of MN-64, a zero-shot inference model, even 424 more remarkable. Furthermore, despite trained models like HTGN or GCLSTM performing well 425 on certain datasets, our MN-64 model consistently achieves competitive rankings across all datasets. 426 We examine the data selection for different multi-network models and as shown in Section F the 427 performance gain is due to the number of datasets in training and not the bias in data selection. 428

Effect of scaling. In Table 1, we further compare the models by reporting the top rank, average rank, and win ratio for different configurations of the multi-network models. We observe a notable improvement in performance as the number of training networks increases. For instance, the average rank improves from 6.15 for MN-2 to 2.15 for MN-64, which signifies a roughly 50% performance

Table 2: AUC scores of multi-network models, single models, and persistence forecasts on test sets
across three seeds, including comparisons with state-of-the-art models EvolveGCN, GC-LSTM and
GraphPulse. The best performance is shown in bold, and the second best is underlined.

Method			Trained 1	Inference		Zero-Shot	Inference
Dataset	Per. Fore.	HTGN	GCLSTM	EvolveGCN	GraphPulse	MN-32	MN-64
WOJAK	0.378	$0.479 \pm \textbf{0.005}$	0.484 ± 0.000	$0.505 \pm \textbf{0.023}$	$0.467 \pm \textbf{0.030}$	0.534 ± 0.017	0.524 ± 0.027
DOGE2.0	0.250	0.590 ± 0.059	0.538 ± 0.000	$0.551 \pm \textbf{0.022}$	0.384 ± 0.180	0.551 ± 0.022	0.538 ± 0.038
EVERMOON	0.241	$0.512 \pm \textbf{0.023}$	0.562 ± 0.179	0.451 ± 0.046	$0.519\pm ext{0.130}$	0.543 ± 0.075	0.517 ± 0.039
QOM	0.334	0.633 ± 0.017	0.612 ± 0.001	0.618 ± 0.002	0.775 ± 0.011	$\overline{0.669\pm_{0.034}}$	0.647 ± 0.019
SDEX	0.423	0.762 ± 0.034	0.720 ± 0.002	$\underline{0.733 \pm 0.028}$	$0.436\pm ext{0.030}$	0.536 ± 0.042	0.614 ± 0.020
ETH2x-FLI	0.355	0.610 ± 0.059	0.670 ± 0.009	$\overline{0.688\pm ext{0.010}}$	0.666 ± 0.047	0.715 ± 0.032	0.729 ± 0.015
BEPRO	0.393	0.655 ± 0.038	$0.632\pm$ 0.019	$0.610\pm$ 0.012	0.783 ± 0.003	0.776 ± 0.008	0.782 ± 0.003
XCN	0.592	0.668 ± 0.099	$0.306 \pm \scriptstyle 0.092$	$0.512\pm extrm{0.067}$	0.821 ± 0.004	0.848 ± 0.000	0.851 ± 0.043
BAG	0.792	$0.673 \pm \textbf{0.227}$	0.196 ± 0.179	$0.329\pm extrm{0.040}$	0.934 ± 0.020	0.898 ± 0.075	0.931 ± 0.028
TRAC	0.400	$0.712\pm extrm{0.071}$	0.748 ± 0.000	0.748 ± 0.000	0.767 ± 0.001	0.770 ± 0.007	0.785 ± 0.008
DERC	0.353	$0.683 \pm \textbf{0.013}$	$0.703\pm extrm{0.022}$	0.669 ± 0.009	$\underline{0.769 \pm 0.040}$	0.756 ± 0.045	0.798 ± 0.027
Metis	0.423	$0.715\pm extrm{0.122}$	$0.646\pm$ 0.023	0.688 ± 0.027	0.812 ± 0.011	0.753 ± 0.005	0.760 ± 0.025
REPv2	0.321	0.760 ± 0.012	0.725 ± 0.014	0.709 ± 0.002	0.830 ± 0.001	0.773 ± 0.013	0.789 ± 0.020
DINO	0.431	$0.730\pm$ 0.195	0.874 ± 0.028	0.868 ± 0.029	0.801 ± 0.020	0.764 ± 0.048	0.779 ± 0.113
HOICHI	0.374	$0.807\pm$ 0.047	0.857 ± 0.000	0.856 ± 0.001	0.714 ± 0.010	0.731 ± 0.029	0.765 ± 0.018
MUTE	0.536	$0.649\pm$ 0.015	$0.593 \pm \textbf{0.030}$	0.617 ± 0.010	0.779 ± 0.004	0.657 ± 0.035	$\underline{0.673 \pm 0.013}$
GLM	0.427	0.830 ± 0.029	0.451 ± 0.003	$0.501\pm extrm{0.033}$	0.769 ± 0.018	0.826 ± 0.035	0.831 ± 0.024
MIR	0.327	0.750 ± 0.005	$0.768\pm extrm{0.026}$	$0.745\pm extrm{0.015}$	0.689 ± 0.097	0.809 ± 0.022	0.836 ± 0.016
stkAAVE	0.426	$0.702\pm extrm{0.042}$	$0.368 \pm \scriptstyle 0.011$	$0.397 \pm \textbf{0.022}$	0.743 ± 0.006	0.696 ± 0.027	$\underline{0.709 \pm 0.022}$
ADX	0.362	$\underline{0.769 \pm 0.018}$	$0.723 \pm \textbf{0.002}$	$0.718 \pm \textbf{0.004}$	$\textbf{0.784} \pm \textbf{0.002}$	0.671 ± 0.015	0.679 ± 0.024
Top rank \uparrow	0	2	3	0	8	1	<u>6</u>
Avg. rank↓	6.20	3.85	4.30	4.45	3.00	3.05	2.04

enhancement when scaling from two networks to sixty-four. The improvement in the win ratio is also substantial, with MN-64 achieving the highest win ratio of 0.80, outperforming the other models in most datasets. This indicates that increasing the number of networks in multi-network models significantly enhances their robustness and predictive power, particularly when compared to single models and smaller multi-network configurations.

Ablation Study We conducted an ablation study for the TGS-train algorithm to assess the ef-fects of resetting memory (con-text switching) and shuffling data (IID training). Models are trained same as multi-network

Table 3: Ablation study results (AUC) demonstrating the impact of various training strategies on model performance.

Model	MN-4 \uparrow	MN-8 ↑	MN-16 ↑	MN-32 ↑	MN-64 ↑
Base Model	0.667 ± 0.111	0.676 ± 0.099	0.704 ± 0.115	0.714 ± 0.107	0.727 ± 0.11
w/o IID training	0.647 ± 0.113	0.643 ± 0.117	0.690 ± 0.105	0.709 ± 0.093	0.710 ± 0.12
w/o Context Switching	$0.667 \pm \textbf{0.120}$	$0.608 \pm \textbf{0.102}$	$0.693 \pm \textbf{0.099}$	$0.713 \pm \scriptstyle 0.126$	0.664 ± 0.1

model training setup and tested on the 20 unseen test dataset. The average results are presented in Table 3. Training different multi-network models without resetting memory revealed that persistent memory across epochs negatively impacts generalization, emphasizing the importance of reset mechanisms to reduce overfitting. Additionally, we explored the necessity of shuffling data by fixing the order of training networks. The observed performance decline indicated that incorporating randomness is vital for improving the model's robustness and generalizability.

CONCLUSION

In this work, we seek to address the question: given a collection of observed temporal graphs, can we predict the evolution of an unseen network within the same domain? We find that it is indeed possible to learn from temporal networks in the same domain and forecast future trends for unseen networks. First, we collected and released a collection of 84 temporal networks for the temporal graph property prediction task. These datasets serve as the foundation for studying neural scaling laws and foundation models on temporal graphs. Next, to learn from a large number of temporal graphs, we present TGS-train, the first algorithm for training TGNNs across multiple temporal networks. Experimentally, we show that the neural scaling law also applies to temporal graphs; in particular, the more training networks are used, the better the model performance on unseen test networks. In addition, our trained multi-network models can outperform single models trained on individual test networks. Our empirical observations show the high potential of training foundational models on temporal graphs. We believe our TGS method will pave the way for advancements in temporal graph foundation models, providing valuable resources that the community can utilize.

486 REFERENCES 487

498

500

501

488 Samira Abnar, Mostafa Dehghani, Behnam Neyshabur, and Hanie Sedghi. Exploring the limits of large scale pre-training. In The Tenth International Conference on Learning Representations, ICLR 489 2022, Virtual Event, April 25-29, 2022. OpenReview.net, 2022. URL https://openreview. 490 net/forum?id=V3C8p78sDa. 491

- 492 Muhammad Awais, Muzammal Naseer, Salman Khan, Rao Muhammad Anwer, Hisham Cholakkal, 493 Mubarak Shah, Ming-Hsuan Yang, and Fahad Shahbaz Khan. Foundational models defining a new 494 era in vision: A survey and outlook. arXiv preprint arXiv:2307.13721, 2023. 495
- 496 Yasaman Bahri, Ethan Dyer, Jared Kaplan, Jaehoon Lee, and Utkarsh Sharma. Explaining neural scaling laws. CoRR, abs/2102.06701, 2021. URL https://arxiv.org/abs/2102.06701. 497
- Dominique Beaini, Shenyang Huang, Joao Alex Cunha, Zhiyi Li, Gabriela Moisescu-Pareja, Olek-499 sandr Dymov, Samuel Maddrell-Mander, Callum McLean, Frederik Wenkel, Luis Müller, et al. Towards foundational models for molecular learning on large-scale multi-task datasets. In The Twelfth International Conference on Learning Representations, 2023. 502
- Rishi Bommasani, Drew A. Hudson, Ehsan Adeli, Russ B. Altman, Simran Arora, Sydney von Arx, 504 Michael S. Bernstein, Jeannette Bohg, Antoine Bosselut, Emma Brunskill, Erik Brynjolfsson, 505 Shyamal Buch, Dallas Card, Rodrigo Castellon, Niladri S. Chatterji, Annie S. Chen, Kathleen 506 Creel, Jared Quincy Davis, Dorottya Demszky, Chris Donahue, Moussa Doumbouya, Esin Durmus, Stefano Ermon, John Etchemendy, Kawin Ethayarajh, Li Fei-Fei, Chelsea Finn, Trevor Gale, 507 Lauren Gillespie, Karan Goel, Noah D. Goodman, Shelby Grossman, Neel Guha, Tatsunori 508 Hashimoto, Peter Henderson, John Hewitt, Daniel E. Ho, Jenny Hong, Kyle Hsu, Jing Huang, 509 Thomas Icard, Saahil Jain, Dan Jurafsky, Pratyusha Kalluri, Siddharth Karamcheti, Geoff Keeling, 510 Fereshte Khani, Omar Khattab, Pang Wei Koh, Mark S. Krass, Ranjay Krishna, Rohith Kuditipudi, 511 and et al. On the opportunities and risks of foundation models. CoRR, abs/2108.07258, 2021. URL 512 https://arxiv.org/abs/2108.07258. 513
- 514 Tom B. Brown, Benjamin Mann, Nick Ryder, Melanie Subbiah, Jared Kaplan, Prafulla Dhari-515 wal, Arvind Neelakantan, Pranav Shyam, Girish Sastry, Amanda Askell, Sandhini Agar-516 wal, Ariel Herbert-Voss, Gretchen Krueger, Tom Henighan, Rewon Child, Aditya Ramesh, Daniel M. Ziegler, Jeffrey Wu, Clemens Winter, Christopher Hesse, Mark Chen, Eric Sigler, 517 Mateusz Litwin, Scott Gray, Benjamin Chess, Jack Clark, Christopher Berner, Sam McCan-518 dlish, Alec Radford, Ilya Sutskever, and Dario Amodei. Language models are few-shot 519 learners. In Hugo Larochelle, Marc'Aurelio Ranzato, Raia Hadsell, Maria-Florina Balcan, and Hsuan-Tien Lin (eds.), Advances in Neural Information Processing Systems 33: Annual 521 Conference on Neural Information Processing Systems 2020, NeurIPS 2020, December 6-12, 522 2020, virtual, 2020. URL https://proceedings.neurips.cc/paper/2020/hash/ 523 1457c0d6bfcb4967418bfb8ac142f64a-Abstract.html. 524
- 525 Sébastien Bubeck, Varun Chandrasekaran, Ronen Eldan, Johannes Gehrke, Eric Horvitz, Ece Kamar, 526 Peter Lee, Yin Tat Lee, Yuanzhi Li, Scott M. Lundberg, Harsha Nori, Hamid Palangi, Marco Túlio 527 Ribeiro, and Yi Zhang. Sparks of artificial general intelligence: Early experiments with GPT-4. CoRR, abs/2303.12712, 2023. doi: 10.48550/ARXIV.2303.12712. URL https://doi.org/ 528 10.48550/arXiv.2303.12712. 529
- 530 Kathrin Büttner, Jennifer Salau, and Joachim Krieter. Adaption of the temporal correlation coefficient 531 calculation for temporal networks (applied to a real-world pig trade network). SpringerPlus, 5: 532 1–19, 2016. 533
- 534 Jinyin Chen, Xueke Wang, and Xuanheng Xu. GC-LSTM: graph convolution embedded LSTM 535 for dynamic network link prediction. Appl. Intell., 52(7):7513-7528, 2022. doi: 10.1007/ 536 S10489-021-02518-9. URL https://doi.org/10.1007/s10489-021-02518-9. 537
- Zhongxiang Dai, Yu Chen, Junhua Li, Johnson Fam, Anastasios Bezerianos, and Yu Sun. Temporal 538 efficiency evaluation and small-worldness characterization in temporal networks. Scientific reports, 6(1):34291, 2016.

567

568

569

- Qingxiu Dong, Lei Li, Damai Dai, Ce Zheng, Zhiyong Wu, Baobao Chang, Xu Sun, Jingjing Xu, Lei Li, and Zhifang Sui. A survey for in-context learning. *CoRR*, abs/2301.00234, 2023. doi: 10. 48550/ARXIV.2301.00234. URL https://doi.org/10.48550/arXiv.2301.00234.
- Mikhail Galkin, Xinyu Yuan, Hesham Mostafa, Jian Tang, and Zhaocheng Zhu. Towards foundation
 models for knowledge graph reasoning. In *The Twelfth International Conference on Learning Representations*, 2023.
- Weihua Hu, Matthias Fey, Marinka Zitnik, Yuxiao Dong, Hongyu Ren, Bowen Liu, Michele
 Catasta, and Jure Leskovec. Open graph benchmark: Datasets for machine learning on
 graphs. In Hugo Larochelle, Marc'Aurelio Ranzato, Raia Hadsell, Maria-Florina Balcan,
 and Hsuan-Tien Lin (eds.), Advances in Neural Information Processing Systems 33: Annual
 Conference on Neural Information Processing Systems 2020, NeurIPS 2020, December 6-12,
 2020, virtual, 2020. URL https://proceedings.neurips.cc/paper/2020/hash/
 fb60d411a5c5b72b2e7d3527cfc84fd0-Abstract.html.
- 554 Shenyang Huang, Farimah Poursafaei, Jacob Danovitch, Matthias Fey, Weihua Hu, Emanuele 555 Rossi, Jure Leskovec, Michael M. Bronstein, Guillaume Rabusseau, and Reihaneh Rabbany. Temporal graph benchmark for machine learning on temporal graphs. In Alice Oh, 556 Tristan Naumann, Amir Globerson, Kate Saenko, Moritz Hardt, and Sergey Levine (eds.), Advances in Neural Information Processing Systems 36: Annual Conference on Neural 558 Information Processing Systems 2023, NeurIPS 2023, New Orleans, LA, USA, December 559 10 - 16, 2023, 2023. URL http://papers.nips.cc/paper_files/paper/2023/ hash/066b98e63313162f6562b35962671288-Abstract-Datasets_and_ 561 Benchmarks.html. 562
- Shengmin Jin and Reza Zafarani. The spectral zoo of networks: Embedding and visualizing networks
 with spectral moments. In *Proceedings of the 26th ACM SIGKDD International Conference on Knowledge Discovery & Data Mining*, pp. 1426–1434, 2020.
 - Jared Kaplan, Sam McCandlish, Tom Henighan, Tom B. Brown, Benjamin Chess, Rewon Child, Scott Gray, Alec Radford, Jeffrey Wu, and Dario Amodei. Scaling laws for neural language models. *CoRR*, abs/2001.08361, 2020. URL https://arxiv.org/abs/2001.08361.
- Seyed Mehran Kazemi, Rishab Goel, Kshitij Jain, Ivan Kobyzev, Akshay Sethi, Peter Forsyth, and
 Pascal Poupart. Representation learning for dynamic graphs: A survey. *Journal of Machine Learning Research*, 21(70):1–73, 2020.
- Han-Min Kim, Gee-Woo Bock, and Gunwoong Lee. Predicting ethereum prices with machine
 learning based on blockchain information. *Expert Systems with Applications*, 184:115480, 2021.
- Diederik P. Kingma and Jimmy Ba. Adam: A method for stochastic optimization. In Yoshua Bengio and Yann LeCun (eds.), 3rd International Conference on Learning Representations, ICLR 2015, San Diego, CA, USA, May 7-9, 2015, Conference Track Proceedings, 2015. URL http://arxiv.org/abs/1412.6980.
- Jia Li, Zhichao Han, Hong Cheng, Jiao Su, Pengyun Wang, Jianfeng Zhang, and Lujia Pan. Predicting path failure in time-evolving graphs. In Ankur Teredesai, Vipin Kumar, Ying Li, Rómer Rosales, Evimaria Terzi, and George Karypis (eds.), *Proceedings of the 25th ACM SIGKDD International Conference on Knowledge Discovery & Data Mining, KDD 2019, Anchorage, AK, USA, August 4-8, 2019*, pp. 1279–1289. ACM, 2019. doi: 10.1145/3292500.3330847. URL https://doi.org/10.1145/3292500.3330847.
- Juanhui Li, Harry Shomer, Haitao Mao, Shenglai Zeng, Yao Ma, Neil Shah, Jiliang Tang, and Dawei
 Yin. Evaluating graph neural networks for link prediction: Current pitfalls and new benchmarking.
 Advances in Neural Information Processing Systems, 36, 2024.
- Jingzhe Liu, Haitao Mao, Zhikai Chen, Tong Zhao, Neil Shah, and Jiliang Tang. Neural scaling laws on graphs. *CoRR*, abs/2402.02054, 2024. doi: 10.48550/ARXIV.2402.02054. URL https://doi.org/10.48550/arXiv.2402.02054.
- 593 Haitao Mao, Zhikai Chen, Wenzhuo Tang, Jianan Zhao, Yao Ma, Tong Zhao, Neil Shah, Mikhail Galkin, and Jiliang Tang. Graph foundation models, 2024.

598

634

635

636

637

638

- Oscar Méndez-Lucio, Christos Nicolaou, and Berton Earnshaw. Mole: a molecular foundation model for drug discovery. *arXiv preprint arXiv:2211.02657*, 2022.
 - Vincenzo Nicosia, John Tang, Cecilia Mascolo, Mirco Musolesi, Giovanni Russo, and Vito Latora. Graph metrics for temporal networks. *Temporal networks*, pp. 15–40, 2013.

Aldo Pareja, Giacomo Domeniconi, Jie Chen, Tengfei Ma, Toyotaro Suzumura, Hiroki Kanezashi, Tim Kaler, Tao B. Schardl, and Charles E. Leiserson. Evolvegen: Evolving graph convolutional networks for dynamic graphs. In *The Thirty-Fourth AAAI Conference on Artificial Intelligence, AAAI 2020, The Thirty-Second Innovative Applications of Artificial Intelligence Conference, IAAI* 2020, *The Tenth AAAI Symposium on Educational Advances in Artificial Intelligence, EAAI 2020, New York, NY, USA, February 7-12, 2020,* pp. 5363–5370. AAAI Press, 2020. doi: 10.1609/AAAI.
V34I04.5984. URL https://doi.org/10.1609/aaai.v34i04.5984.

Farimah Poursafaei, Shenyang Huang, Kellin Pelrine, and Reihaneh Rabbany. To-607 wards better evaluation for dynamic link prediction. In Sanmi Koyejo, S. Mohamed, 608 A. Agarwal, Danielle Belgrave, K. Cho, and A. Oh (eds.), Advances in Neural Infor-609 mation Processing Systems 35: Annual Conference on Neural Information Processing Systems 2022, NeurIPS 2022, New Orleans, LA, USA, November 28 - December 610 9, 2022, 2022. URL http://papers.nips.cc/paper_files/paper/2022/ 611 hash/d49042a5d49818711c401d34172f9900-Abstract-Datasets_and_ 612 Benchmarks.html. 613

- Alec Radford, Jong Wook Kim, Chris Hallacy, Aditya Ramesh, Gabriel Goh, Sandhini Agarwal, Girish Sastry, Amanda Askell, Pamela Mishkin, Jack Clark, Gretchen Krueger, and Ilya Sutskever. Learning transferable visual models from natural language supervision. In Marina Meila and Tong Zhang (eds.), *Proceedings of the 38th International Conference on Machine Learning, ICML 2021, 18-24 July 2021, Virtual Event*, volume 139 of *Proceedings of Machine Learning Research*, pp. 8748–8763. PMLR, 2021. URL http://proceedings.mlr.press/v139/ radford21a.html.
- Kashif Rasul, Arjun Ashok, Andrew Robert Williams, Hena Ghonia, Rishika Bhagwatkar, Arian Khorasani, Mohammad Javad Darvishi Bayazi, George Adamopoulos, Roland Riachi, Nadhir Hassen, Marin Biloš, Sahil Garg, Anderson Schneider, Nicolas Chapados, Alexandre Drouin, Valentina Zantedeschi, Yuriy Nevmyvaka, and Irina Rish. Lag-llama: Towards foundation models for probabilistic time series forecasting, 2024.
- Jonathan S. Rosenfeld, Amir Rosenfeld, Yonatan Belinkov, and Nir Shavit. A constructive prediction of the generalization error across scales. In *8th International Conference on Learning Representations, ICLR 2020, Addis Ababa, Ethiopia, April 26-30, 2020.* OpenReview.net, 2020. URL https://openreview.net/forum?id=ryenvpEKDr.
- Emanuele Rossi, Ben Chamberlain, Fabrizio Frasca, Davide Eynard, Federico Monti, and Michael M.
 Bronstein. Temporal graph networks for deep learning on dynamic graphs. *CoRR*, abs/2006.10637,
 2020. URL https://arxiv.org/abs/2006.10637.
 - S. Salcedo-Sanz, D. Casillas-Pérez, J. Del Ser, C. Casanova-Mateo, L. Cuadra, M. Piles, and G. Camps-Valls. Persistence in complex systems. *Physics Reports*, 957:1–73, 2022.
 - Aravind Sankar, Yanhong Wu, Liang Gou, Wei Zhang, and Hao Yang. Dynamic graph representation learning via self-attention networks, 2019.
- Youngjoo Seo, Michaël Defferrard, Pierre Vandergheynst, and Xavier Bresson. Structured sequence
 modeling with graph convolutional recurrent networks, 2016.
- Kiarash Shamsi, Friedhelm Victor, Murat Kantarcioglu, Yulia Gel, and Cuneyt G Akcora. Chartalist: Labeled graph datasets for utxo and account-based blockchains. *Advances in Neural Information Processing Systems*, 35:34926–34939, 2022.
- Kiarash Shamsi, Farimah Poursafaei, Shenyang Huang, Bao Tran Gia Ngo, Baris Coskunuzer, and
 Cuneyt Gurcan Akcora. Graphpulse: Topological representations for temporal graph property
 prediction. In *The Twelfth International Conference on Learning Representations*, 2024. URL
 https://openreview.net/forum?id=DZqic2sPTY.

- John Tang, Mirco Musolesi, Cecilia Mascolo, Vito Latora, and Vincenzo Nicosia. Analysing information flows and key mediators through temporal centrality metrics. In *Proceedings of the 3rd workshop on social network systems*, pp. 1–6, 2010.
- Gavin Wood et al. Ethereum: A secure decentralised generalised transaction ledger. *Ethereum project yellow paper*, 151(2014):1–32, 2014.
- Lianghao Xia, Ben Kao, and Chao Huang. Opengraph: Towards open graph foundation models.
 arXiv preprint arXiv:2403.01121, 2024.
- Menglin Yang, Min Zhou, Marcus Kalander, Zengfeng Huang, and Irwin King. Discrete-time temporal network embedding via implicit hierarchical learning in hyperbolic space. In Feida Zhu, Beng Chin Ooi, and Chunyan Miao (eds.), *KDD '21: The 27th ACM SIGKDD Conference on Knowledge Discovery and Data Mining, Virtual Event, Singapore, August 14-18, 2021*, pp. 1975–1985. ACM, 2021. doi: 10.1145/3447548.3467422. URL https://doi.org/10.1145/3447548.3467422.
- Zhen Zhang, Bingqiao Luo, Shengliang Lu, and Bingsheng He. Live graph lab: Towards open, dynamic and real transaction graphs with NFT. In Alice Oh, Tristan Naumann, Amir Globerson, Kate Saenko, Moritz Hardt, and Sergey Levine (eds.), Advances in Neural Information Processing Systems 36: Annual Conference on Neural Informa-tion Processing Systems 2023, NeurIPS 2023, New Orleans, LA, USA, December 10 -16, 2023, 2023. URL http://papers.nips.cc/paper_files/paper/2023/ hash/3be31c1a2fdcb7b748c53c3f4cb0e9d2-Abstract-Datasets_and_ Benchmarks.html.