Efficient LLM Pruning with Token-Dependency Awareness and Hardware-Adapted Inference

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⁰⁰¹ Abstract

 Structured pruning removes entire components, like attention heads or hidden dimensions to yield faster dense large language models. How- ever, previous methods are time-consuming and inference speedup is bottlenecked by inefficient GPU parallel processing due to mismatch in pruned weight block dimensions with tensor cores. Moreover, pruning of heads in grouped **query attentions is not widely attempted due to** challenges with their interdependencies. To ad-012 dress these limitations, we propose (1) a struc- tured pruning method for LLMs with grouped-**query attentions(GQA) that learn appropriate** key,value and shared query heads to retain ac-**cording to its importance for accurate predic-** tion. (2) a post-pruning weight update to better retain performance of pruned LLMs. (3) a post- pruning dimension adaptation step to enhance **GPU** utilization of pruned models and signifi- cantly speed up inference. Our method speeds up inference by up to 60% over previous ap- proaches. Evaluated on several language bench- marks using variants of LLaMA models and Mistral, our method shows a reduction in prun- ing time by upto 90% with higher inference speed and performance over a range of spar- sity ratios. Additionally, our findings suggest that pruning can reduce prediction confusion in **030** models.

031 1 Introduction

 Deploying Large Language Models (LLMs) on resource-constrained devices is challenging due to their high computational and memory de- mands [\(Le Scao et al.,](#page-8-0) [2023\)](#page-8-0). Pruning is an ef- fective solution to reduce redundant model param- eters and accelerate inference without sacrificing task performance. Structured pruning [\(An et al.,](#page-8-1) [2024\)](#page-8-1) involves removing layers, heads, interme- diate dimensions which can lead to dense com- pressed models with faster inference. While ef-fective in maintaining model accuracy, gradientbased methods [\(Ma et al.,](#page-9-0) [2023\)](#page-9-0) require substantial **043** memory resources and forward-pass only method **044** [Dery et al.](#page-8-2) [\(2024\)](#page-8-2) requires about 40 GPU hours for **045** continuous evaluation of sub-models. This makes **046** them impractical for scenarios with limited mem- **047** ory, power or time. On the other hand, unstruc- **048** tured pruning methods, which remove individual **049** weights, offer faster pruning but necessitate spe- 050 cialized hardware to accelerate the pruned mod- **051** els [\(Frantar and Alistarh,](#page-8-3) [2023\)](#page-8-3). Quantization tech- **052** niques require specialized GPUs and libraries for **053** acceleration [\(Dettmers et al.,](#page-8-4) [2022;](#page-8-4) [Zhang et al.,](#page-10-0) **054** [2024c\)](#page-10-0). **055**

Structured pruning methods often fail to prune **056** token embedding representations due to the com- **057** plex dependencies that span across layers of the **058** model, thereby missing out on added acceleration. **059** Pruning of attention heads in grouped query at- **060** tentions (GQA) [\(Ainslie et al.,](#page-8-5) [2023\)](#page-8-5) introduces **061** additional complexity since multiple query heads **062** share a single key and value head. This interde- **063** pendence implies that pruning a query head can **064** disrupt the functionality of the entire group. Very **065** few previous work undertake the structured pruning **066** of GQA-based models like Mistral and LLaMA-3. **067** The recent Bonsai [\(Dery et al.,](#page-8-2) [2024\)](#page-8-2) attempted **068** pruning Mistral but takes over 40 hours to search **069** for an optimal model limiting its use. **070**

Prior work [\(An et al.,](#page-8-1) [2024\)](#page-8-1) shows 1.3x speedup 071 on NVIDIA A100 for 50% pruning, not scaling **072** linearly. A notable reason is that pruned weight **073** matrices often cannot fully exploit the parallelism **074** in GPU tensor cores [\(NVIDIA,](#page-9-1) [2024a\)](#page-9-1) which **075** often perform operations in certain fixed block **076** sizes **077**

speedups [\(Chen et al.,](#page-8-6) [2024;](#page-8-6) [Sheng et al.,](#page-9-2) [2023;](#page-9-2) **078** [Liu et al.,](#page-9-3) [2023c\)](#page-9-3) involving complex algorithms. **079**

To address these challenges, we propose an effi- **080** cient structured pruning method for LLMs specif- **081** ically for grouped query-based models - Token **082** dependency-aware Variational Adapted pruning. **083**

Figure 1: Comparison of sparsity, perplexity and inference speedup of GQA-based LLaMA-3-8B and Mistral-7B models pruned to different sparsity ratios with C4 train set and evaluated on Wikitext-2 validation set. Speedup is measured on NVIDIA A100(GB) for evaluation on the validation set.

 We extend the formulation of the Variational Infor- mation Bottleneck (VIB) principle to include token dependency-awareness in pruning grouped-query- based models. Our method effectively removes redundant grouped-heads, intermediate and global token representation while preserving information flow on a single GPU, adhering to a user-defined sparsity criterion. Additionally, our post-pruning weight update and dimension adaptation ensures parallelism in the inference GPU and thus achieves higher inference speedup. Pre-trained LLMs in- cluding variants of LLaMA-7B [\(Touvron et al.,](#page-9-4) [2023a,](#page-9-4)[b\)](#page-9-5), and Mistral-7B [\(Jiang et al.,](#page-8-7) [2023a\)](#page-8-7) are pruned, demonstrating superior performance com- pared to prior methods. Our major contributions are as follows:

- **100** We propose an efficient structured approach **101** to prune LLMs with grouped query-based **102** attention (GQA) modules as in Mistral and **103** LLaMA-3.
- **104** Our framework includes an immediate post-**105** pruning weight update that enhances pruned **106** model performance, surpassing previous struc-**107** tured pruning methods, even on non-GQA-**108** based models.
- **109** We incorporate a post-pruning dimension ad-**110** justment that leverages GPU parallelism for **111** faster inference not explored in previous work, **112** with negligible changes in performance and **113** model size.
- **114** Evaluations on variants of LLaMA and Mis-**115** tral models across language modeling and rea-**116** soning tasks demonstrate that our method out-**117** performs previous state-of-the-art techniques.

¹¹⁸ 2 Preliminaries

119 VIB-based Structured Pruning. Given a trans-**120** former model with pre-trained weights W, the objective is to remove rows and columns by elim- **121** inating redundant heads, intermediate layer and **122** token embedding hidden dimensions to obtain com- **123** pressed weights Wˆ . We formulate this as a problem **¹²⁴** of searching for sparse masks m_{MLP} , m_{MHA} and 125 m_{token} for MLP, Multi-Head Attention layers and 126 token representation dimensions across all layers. **127** Each of these masks have learnable parameters μ , 128 σ. VTrans [\(Dutta et al.,](#page-8-8) [2024\)](#page-8-8) estimates the im- **129** portance of each token representation in each layer **130** of LLMs using the Variational Information Bot- **131** [t](#page-8-9)leneck principle [\(Slonim and Tishby,](#page-9-6) [1999;](#page-9-6) [Dai](#page-8-9) **132** [et al.,](#page-8-9) [2018\)](#page-8-9). A random set of vectors $z_i = \mu + \eta \odot \sigma$ 133 where η is sampled from $\mathcal{N}(0, I)$, is multiplied to 134 the previous layer output and the mask parameters **135** are trained using backpropagation with the follow- **136** ing objective function as defined by [\(Dutta et al.,](#page-8-8) **137** [2024;](#page-8-8) [Dai et al.,](#page-8-9) [2018\)](#page-8-9), **138**

$$
\arg\min_{\mu,\sigma} \mathcal{L} = \sum_{i}^{L} \beta_i \sum_{j=1}^{r_i} \log\left(1 + \left(\frac{\mu^{i,j}}{\sigma^{i,j}}\right)^2\right)
$$

$$
-\mathbb{E}_{\eta}\left[\log q\left(y_n \mid f(x_n,\eta)\right)\right] \quad (1) \tag{40}
$$

139

Given a dataset of samples x, y , during back- 141 propagation, the gradient is the unbiased estimate **142** of the expectation. When for layer i and structure **143** j, $\log \frac{\mu_{i,j}^2 + \epsilon}{\sigma^2}$ $\frac{\overline{i}_i j^2 + \epsilon}{\sigma_{i,i}^2}$ < 0, the mask $m^{i,j}$ is 0, that is the 144 corresponding weight parameters of structure j can 145 be pruned. **146**

Pruning grouped-query attention challenges. **147** Grouped query Attention (GQA) [\(Ainslie et al.,](#page-8-5) 148 [2023\)](#page-8-5) was introduced to reduce the amount of **149** cache and speed up inference in large language **150** models. It involves multiple query heads sharing a **151** single key and value head. But structured prun- **152** ing of heads with mask m_{MHA} in Multi-Head 153 [A](#page-8-8)ttention modules (MHA) as in VTrans [\(Dutta](#page-8-8) **154** [et al.,](#page-8-8) [2024\)](#page-8-8) assumes that all query heads have **155** a single key and value head. This does not hold **156**

Figure 2: (a) Structured pruning of weight matrices considering global token masks and module-specific dimension mask. (b) Post-Prune Dimension Adaptation ensuring effective utilization of parallelism in GPUs during inference. Here, fifth row is unpruned and fifth column is pruned to ensure alignment with block sizes in GPUs. (c) Post-Prune Weight Update leveraging importance scores learned by VIB masks. (d) Final Model Weights

 in grouped query-based attention modules, where pruning a query head can disrupt the group func- tionality and lead to inconsistencies in the attention module structure.

 Inference speedup challenges. When evaluated on the test set of Wikitext-2 dataset, models pruned [b](#page-8-1)y 50% with prior methods [\(Dery et al.,](#page-8-2) [2024;](#page-8-2) [An](#page-8-1) [et al.,](#page-8-1) [2024\)](#page-8-1) show about 1.3× speedup over the unpruned model on NVIDIA A100 (40GB). This speedup is relatively modest given the 50% reduc- tion in parameters. Our investigation revealed that a key reason for this limited speedup is that pruned weight matrices often fail to fully leverage the par- allelism of GPU tensor cores [\(NVIDIA,](#page-9-1) [2024a\)](#page-9-1), which typically operate in fixed block sizes like 128x256. Additionally, some approaches targeting inference speedups [\(Sheng et al.,](#page-9-2) [2023;](#page-9-2) [Liu et al.,](#page-9-3) [2023c\)](#page-9-3) involve complex algorithms, potentially in- creasing computations and adding overhead before deploying pruned models.

¹⁷⁷ 3 Method

 In this section, we describe the various aspects of our methodology to prune pre-trained LLMs in a structured manner: (1) Pruning attention heads in grouped-query attention (GQA)-based models (2) Post-pruning weight update (3) Dimension Adapta-tion of the weight matrices.

184 3.1 Pruning Attention Heads in Grouped **185** Query

 Multi-head attention allows for independent prun- ing of query, key, and value heads by masking in- dividual heads. However, pruning within Grouped Query Attention (GQA) groups is more complex due to the need to maintain group functionality despite pruning.

For GQA we define separate masks for key- **192** value heads m_v^i and query heads $m_q^i \in \mathbb{R}^d$ for 193 i^{th} layer with d heads. Only key-value heads m_i^i are assigned trainable parameters μ_v^i , σ_v^i . We 195 define a random set of vectors for the key-value **196** heads $z_v^i \in \mathbb{R}^{\dim' \times d}$ such that $\dim' = \text{batches} \times 197$ $sequence_length \times head_dim \times group_size$ and 198 $z_v^i = \mu_v^i + \eta \odot \sigma_v^i$. $\eta \in \mathbb{R}^{\dim^t \times d}$ is sampled 199 from $\mathcal{N}(0, I)$. These random set of vectors are **200** multiplied by the output of the accumulated heads. **201** Sampling across groups ensures randomness within **202** groups of query heads to weigh their importance for **203** pruning. The learnable parameters are optimized **204** as per Equation [1.](#page-1-0) **205**

194

207

(2) **220**

Following the method described in [\(Dai et al.,](#page-8-9) **206** [2018\)](#page-8-9), we observe that when $\alpha_v^{i,j} = \left(\frac{\mu_v^{i,j} + \epsilon}{\mu_v^{i,j}}\right)$ $\overline{\sigma_v^{i,j}}$ \setminus^2 with small ϵ approaches zero, it indicates that the **208** key-value head j contains no significant informa- **209** tion beyond what is captured in previous layers and **210** pruning it results in minimal performance degrada- **211** tion. Since g queries share the same key-value head, **212** token representations may share local dependencies **213** within the groups. To retain these dependencies, we 214 concatenate the key-head masks to form the query **215** head mask m_q^i . Thus, the mask to prune key value **216** heads and query heads with g groups can then be **217** defined as, 218

$$
m_v^{i,j} = \begin{cases} 1 & \text{if } \log \alpha_v^{i,j} > 0 \\ 0 & \text{otherwise} \end{cases} \quad \forall j \in d \tag{219}
$$

$$
m_q^i = \underbrace{[m_v^i, m_v^i, \dots, m_v^i]}_{g \text{ times}}
$$
 (2)

For each key-value head pruned, our method **221** prunes all connected query heads in the group, **222** ensuring the pruning process does not disrupt **223** group functionality. **224**

 m , we calculate the expected model sparsity s_e as the ratio of pruned parameters to the initial [c](#page-10-1)ount. We use a Lagrangian term similar to [Xia](#page-10-1) [et al.](#page-10-1) [\(2022\)](#page-10-1) by enforcing an equality constraint $s_e = t$ and introducing a violation penalty

225 Ensuring user-defined sparsity. Given a target **226** sparsity t, during pruning, using binary masks

232 as, $\mathcal{L}_s = \lambda_1 \cdot (s_e - t) + \lambda_2 \cdot (s_e - t)^2$ where λ_1, λ_2

 $n' = \left(\frac{n+T/2}{T}\right)$

the new threshold as,

 $\widehat{m}_{\text{token},j} =$

To account for the new dimension, it sorts $\log \alpha$ in descending order, gets the new threshold and recomputes the mask with d dimension based on

 $\tau = (\log \alpha)_{\rm sorted}[n']$

 $\int 1$ if $\log \alpha_j > \tau$ 0 otherwise

233 are jointly updated during the pruning.

235 3.2 Post-Pruning Dimension Adaptation

- **234**
- **236** The dimensions in pre-trained unpruned models **237** are optimized for efficient GPU execution using

 specific block sizes [\(NVIDIA,](#page-9-7) [2024b\)](#page-9-7) like 128x256. However, pruned model dimensions may not align with these block sizes. To address this, we propose a post-pruning technique that initially identifies

242 the indices where the masks m_{token} and m_{mlp} are **243** non-zero and estimates the corresponding weight

244 dimensions as $n = |I|$; $I = \{i \mid m_{\text{token}}[i] \neq 0\}.$ **245** It adjusts the mask lengths such that each of the 246 **b** pruned weight dimension n' would be the nearest

247 multiple of the specified tensor dimension T (say

248 128) as,

249 $n' = \left(\left|\frac{n+T/2}{T}\right|\right) \times T$ (3)

250 251 $\widehat{m}_{\text{token},j} = \left\{ \begin{array}{ccc} 1 & \text{if } \log \alpha_j & \cdots & \forall j \in d \\ 0 & \cdots & \cdots & \cdots \end{array} \right.$

252 Overall, there is a negligible change in the model

253 size. In our experiments, we observe a significant

254 inference speedup due to this step.

255

256 3.3 Post-Pruning Weight Update

258 Equation [2](#page-2-0) that merely retain or discard weights, **259** we leverage the continuous importance scores

260 of representations (mean values μ) learned by

261 the VIB. We modify all the binary masks to be

262 weighted masks as,

257 Instead of applying binary masks as defined in

	Wikitext-2	Inference	Tokens/s
Model	$PPL \downarrow$	Speedup	
Mistral-7B	4.77	$1\times$	24.78
Wanda-sp-gq	116	$1.1\times$	27.26
FLAP-gq	34.97	$1.28\times$	31.73
Bonsai	47.50	$1.66 \times \pm$	41.13
TVA-Prune	18.37	$1.67\times$	41.39
Bonsai †	10.08	$1.66 \times \;$	41.13
TVA-Prune †	10.12	$1.67\times$	41.39
LLaMA-3-8B	5.57	$1 \times$	25.13
Wanda-sp-gq	106	$1.1\times$	27.64
FLAP-gq	34.90	$1.2\times$	30.16
TVA-Prune	27.50	$1.61\times$	40.94

Table 1: Performance comparison of Mistral-7B and LLaMA-3-8B models pruned by 50%. Our method outperforms others without any finetuning. †indicates finetuned with LoRA. ‡Result on Bonsai is taken from [\(Dery et al.,](#page-8-2) [2024\)](#page-8-2) where inference was performed on a different GPU.

Since each weight matrix W of a module has two 264 dimensions, as for the MLP layer it is the interme- **265** diate dimension and the global token representation **266** dimension, we update the unpruned weights using **267** both the global token mask m_{token} and the interme- 268 diate mask m_{mlp} . The updated weights for layer i **269** for the mlp module may be represented as, **270**

$$
W_{upd}^{i} = (\widehat{m}_{token}^{i} \otimes \widehat{m}_{mlp}^{i}) * W^{i} \qquad (6)
$$

(6) **271**

By multiplying the pre-trained remaining weights **272** with the mask weights, the model achieves a nu-
²⁷³ anced adjustment that emphasizes more relevant **274** features. The compressed updated weights \widehat{W}_{upd}^{i} 275 can be obtained by removing the zeroed out rows **276** and columns of W_{und}^i . $\begin{array}{ccc}\n\text{u} & \text{u} \\
\text{u} & \text{u} \\
\text{u} & \text{u}\n\end{array}$

Finetuning with LoRA. Although our method **278** achieves better performance than previous ap- **279** proaches even without finetuning, post-pruning **280** finetuning [\(Dery et al.,](#page-8-2) [2024;](#page-8-2) [Ma et al.,](#page-9-0) [2023\)](#page-9-0) **281** using Low Rank Adapters (LoRA) [\(Hu et al.,](#page-8-10) **282** [2021\)](#page-8-10) on a downstream task further improves per- **283** formance. Additionally, we distil knowledge from **284** the teacher logits H_t to the pruned student logits 285 H^s [\(Xia et al.,](#page-10-1) [2022\)](#page-10-1) by minimizing the following: **²⁸⁶** $\mathcal{L}_{dis} = \text{MSE}(\mathbf{H}_s, \mathbf{H}_t)$ 287

4 Experiments **²⁸⁸**

Datasets. We prune models using the training set **289** [o](#page-9-9)f C4 [\(Raffel et al.,](#page-9-8) [2020\)](#page-9-8) and Wikitext-2 [\(Merity](#page-9-9) **290** [et al.,](#page-9-9) [2016\)](#page-9-9). We test our pruned models on the val- **291** idation set of Wikitext-2 and on six zero-shot tasks **292** designed to test for common sense reasoning using **293**

Model	LLaMA-7B			$LLaMA-2-7B$		
	PPL \downarrow	Speedup	Tokens/s	$PPL \downarrow$	Speedup	Tokens/s
Unpruned	5.68	$1\times$	26.21	5.11	$1\times$	25.46
Wanda-sp	366.43	$1.24\times$	32.50	132.0	$1.29\times$	32.84
LLM-pruner	112.44	$1.23\times$	32.24	95.26	$1.29\times$	32.84
FLAP ‡	35.10	$1.26\times$	33.02	25.40	$1.32\times$	33.61
Bonsai	28.65	$1.26\times$	33.02	22.32	$1.28\times$	32.59
VTrans	25.87	$1.32\times$	34.60	21.54	$1.34\times$	34.12
TVA-Prune	18.62	$1.75\times$	45.87	18.44	$1.82\times$	45.83
TVA-Prune w/o DimAdapt	18.56	$1.23\times$	32.23	18.49	$1.25\times$	31.83
TVA-Prune w/o WUpdate	25.13	$1.75\times$	45.87	21.32	$1.82\times$	45.83
Wanda-sp †	67.24	$1.24\times$	32.50	46.54	$1.29\times$	32.84
LLM-pruner†	38.12	$1.23\times$	32.24	29.56	$1.29\times$	32.84
Bonsai †	11.02	$1.26\times$	33.02	9.87	$1.28\times$	32.59
VTrans†	10.79	$1.32\times$	34.60	9.92	$1.34\times$	34.12
TVA-Prune †	10.58	$1.75\times$	45.87	9.65	$1.82\times$	45.83

Table 2: Performance comparison of pruning methods in a task-agnostic manner with C4 train set and zero-shot evaluation on Wikitext-2. Our method outperforms structured pruning (wanda-sp, Bonsai, LLM-pruner and FLAP) †indicates finetuned with LoRA. ‡adds extra bias parameters. w/o DimAdapt speed reduction is due to inefficient parallelism in GPU. Post-prune dimension adaption leads to negligible change in model size. Inference speedup is measured on the Wikitext-2 validation set while Tokens/s throughput is on one batch of data.

294 the EleutherAI LM Harness [\(Gao et al.,](#page-8-11) [2023\)](#page-8-11).

 Baseline Models. We prune the LLaMA-7B, LLaMA-2-7B [\(Touvron et al.,](#page-9-4) [2023a\)](#page-9-4) and GQA- [b](#page-8-7)ased models LLaMA-3-8B and Mistral-7B [\(Jiang](#page-8-7) [et al.,](#page-8-7) [2023a\)](#page-8-7), to evaluate our method and com- pare against other structured pruning methods. We modify the pruning process in Wanda [\(Sun et al.,](#page-9-10) [2023\)](#page-9-10) to be structured (Wanda-sp) and account for grouped-query attention (Wanda-sp-gq). Simi- larly, we modify FLAP [\(An et al.,](#page-8-1) [2024\)](#page-8-1) to prune grouped-query and name it FLAP-gq. Additionally, we compare the pruned mistral model with Bon- sai [\(Dery et al.,](#page-8-2) [2024\)](#page-8-2). Comparison of pruning of LLaMA 1 and 2 variants also includes other base- line methods: LLM-Pruner [\(Ma et al.,](#page-9-0) [2023\)](#page-9-0), Lo- [R](#page-8-8)APrune [\(Zhang et al.,](#page-10-2) [2023b\)](#page-10-2)and VTrans [\(Dutta](#page-8-8) [et al.,](#page-8-8) [2024\)](#page-8-8).

 Experimental Settings. To prune LLaMA-3, we use a sequence length of 400 to fit in a single GPU. Similarly, we reduce the maximum position em- beddings of the Mistral model to 8192. For the task-specific experiments, we use the training set of Wikitext-2 dataset to prune models. We report the average of five runs with random seeds. The few hyperparameters used are listed in the Appendix. All experiments are conducted on a single NVIDIA A100 (40GB) GPU.

4.1 Language Modelling Tasks **321**

Performance comparison on GQA models **322**

Table [1](#page-3-0) shows TVA-Prune is highly effective for **323** pruning Mistral-7B model with grouped query at- **324** tention (GQA) with the least perplexity among all **325** techniques without any finetuning. While Bonsai **326** achieves a lower perplexity post-finetuning with **327** LoRA, our method takes about 20 times lower com- **328** pression time compared to Bonsai. TVA-Prune **329** offers higher inference speed than all of the ap- **330** proaches. Similar, our method prunes LLaMA-3 **331** and retains higher performance than other meth- **332** ods without any finetuning. The pruned LLaMA-3 **333** model in our case is about 40% faster than FLAP 334 and wanda. **335**

Task-agnostic pruning Comparison. Table [2](#page-4-0) **336** compares our method with other structured prun- **337** ing techniques to prune LLaMA-7B and LLaMA- **338** 2-7B. It highlights the superior performance of our **339** method in terms of perplexity on Wikitext-2 with- **340** out even finetuning. Upon finetuning, the perfor- **341** mance is comparable to Bonsai and VTrans. We 342 see that without the dimension adaptation compo- **343** nent, the inference speedup of our method becomes **344** similar to previous approaches. Similarly, without **345** the weight update step, our method generalizes to **346** the performance of VTrans, but with higher infer- **347** ence speedup of the pruned model. Our pruned **348**

Method	BoolO	PIOA	HellaSwag	WinoGrande	ARC-e	ARC-c	Average \uparrow
	Acc	Acc	Acc	Acc	Acc	Acc	Acc
LLaMA-3-8B	81.28	79.70	60.17	72.37	80.09	50.59	70.70
Wanda-sp-gq	41.60	54.57	26.90	52.24	29.62	18.55	37.24
FLAP-gq	43.73	56.74	27.71	50.98	33.20	20.64	38.83
TVA-Prune	62.96	65.83	36.81	57.61	47.81	23.37	49.06
Mistral-7B	83.66	80.57	61.22	73.87	80.89	50.42	71.77
Wanda-sp-gq	60.14	55.72	26.47	50.10	30.84	19.63	40.48
FLAP-gq	62.12	57.02	27.70	49.81	32.02	21.50	41.69
TVA-Prune	62.20	67.03	37.64	57.14	46.29	22.26	48.76
Wanda-sp-gq ⁺	53.26	58.45	36.14	52.95	42.87	30.45	45.68
$FLAP-gq†$	54.25	68.24	40.75	57.89	49.95	31.85	50.49
TVA-Prune†	64.52	70.50	44.02	58.95	56.15	27.90	53.67

Table 3: Performance comparison of the 50% pruned LLaMA-8B and Mistral-7B models on six zero shot tasks. †denotes finetuned with LoRA. Finetuning enhances the performance all pruned models, yet our pruned model still generalizes better across the tasks. .

349 models observe a 40% faster inference over other **350** models.

 Task-specific pruning comparison. For task- specific pruning with Wikitext-2 training set it is observed that there is an improvement in perplex- ity on the validation set for all the methods. Our method outperforms Bonsai, FLAP and wanda by a wide margin. It yields model similar in perfor- mance to VTrans but with faster inference. Obser-vations are deferred to the Appendix [10.](#page-11-0)

 Various Sparsity Ratios. We see in Figure [1](#page-1-1) that our method performs better than other methods from about 30% sparsity and maintains the stable performance as sparsity increases. This is in con- trast to FLAP and Wanda where the performance deteriorates sharply after 50% and 40% sparsity ratio respectively. At sparsity ratios lower than 30%, our method performs similarly to FLAP. Be- low 30% sparsity, Wanda and FLAP retain similar performance to ours. Our models pruned from LLaMA-3 and Mistral have much faster inference at all sparsity levels than FLAP and Wanda.

 Pruning Time comparison. As illustrated in Fig- ure [3,](#page-5-0) our pruning method exhibits comparable pruning times to VTrans while achieving signifi- cantly better model performance. When compared to more rapid techniques such as LLM-pruner and FLAP, our method delivers more than double the performance improvement. Additionally, our ap- proach prunes models six times faster than the **faster variant of Bonsai** $(p = 0.2)$ and twelve times faster than LoRA-prune. Moreover, our method allows further lowering of the pruning time with

Figure 3: Comparison of Perplexity and time to prune LLaMA-7B by 50% with different structured pruning methods. Our method (TVA-prune) is more efficient yielding models with lower perplexity than methods taking similar or lower time to prune.

lower number of data samples as explored in Ap- **382** pendix [A.](#page-10-3) **383**

4.2 Performance on zero-shot tasks **384**

In Table [3,](#page-5-1) we compare the performance of pruned **385** models on six zero-shot reasoning tasks to as- **386** sess the generalization efficiency of 50% pruned **387** LLaMA-3 and Mistral models on unseen tasks. Our **388** pruned LLaMA-3 models and pruned Mistral mod- **389** els outperform FLAP-gq and Wanda-sp-gq across **390** all tasks. Since the TVA-prune (ours) model al- **391** ready generalises well to the tasks without any fine- **392** tuning as per its capacity, finetuning it increases **393** its performance by only about 3% on average. De- **394** spite a general decrease in performance for all the **395** pruned models compared to their unpruned coun- **396** terparts, our method most effectively preserves the **397** generalization capabilities of the LLMs. **398**

	LLaMA		Mistral
	$2-7B$	$3-8B$	7B
TVA-prune	18.44 27.50		18.37
w/o weight update	$+2.88$ $+5.32$		$+2.17$
w/o dimension adapt	$ +0.05 +0.15$		$+0.42$

Table 4: Performance of models on Wikitext-2 with and without post-prune weight update and dimension adaptation

	Dimension Multiple							
	Ω	8	64	128	256			
	50% pruned LLaMA-3-8B							
Speedup	$0.9\times$	$1.45\times$	$1.60\times$	$1.59\times$	$1.59\times$			
\triangle PPL \downarrow	0	0	0	-0.1	-0.2			
\triangle Sparsity(%)	Ω	0	0.2	0.4	0.3			
50% pruned Mistral-7B								
Speedup	$1.1\times$	$1.48\times$	$1.52\times$	$1.67\times$	$1.40\times$			
\triangle PPI.	-0.5	0	-0.5	-0.2	2.3			
\triangle Sparsity(%)	Ω	0	0.3	0.6	0.8			
50% pruned LLaMA-2-7B								
Speedup	$1.25\times$	$1.52\times$	$1.75\times$	$1.82\times$	$1.75\times$			
\triangle PPI.	0	0	0	-0.05	-1.8			
\triangle Sparsity(%)		0	0.2	0.2	0.6			

Table 5: Change in speedup, perplexity on Wikitext-2, and model sparsity on varying post-prune adapted dimension multiples. Across models it can be observed that adapting weight dimensions to be multiples of 64 or 128 yields the best speedup with least change in sparsity and often lower perplexity

399 4.3 Ablation Study

 Increase in speedup due to adaptation. Figure [4](#page-6-0) illustrates the inference speedup on an NVIDIA A100 (40GB) GPU for 50% pruned models, com- paring scenarios with and without post-pruning dimension adaptation. The y-axis represents the speedup factor over the unpruned models, with a value greater than 1 indicating faster performance. The results show that dimension adaptation signifi-cantly enhances speedup across all models.

 Effect of adaptation in LLM modules. Figure [5](#page-6-1) compares inference times for different modules in the Mistral-7B model: unpruned, TVA-prune with adaptation, and without adaptation. Adaptation significantly reduces attention module inference time over others. For the Intermediate module, the pruned model without adaptation increases in- ference time substantially, while adaptated model takes almost the same time as the unpruned module, likely due to parallel processing.

419 Which dimension multiple is the best? Adjust-**420** ing weight matrix dimensions to be multiples of **421** certain values, as shown in Table [5,](#page-6-2) optimizes

Figure 4: Inference speedup on NVIDIA A100(40GB) with and without our post-pruning dimension adaptation in 50% pruned models.

Figure 5: Time taken to infer on a single batch from Wikitext-2 by each module in Mistral-7B.

GPU tensor core parallelism. When dimensions **422** align with these multiples, computations parallelize **423** more effectively, leading to significant speedups. **424** As shown in the table, dimensions that are multi- **425** ples of 64, 128, or 256 can maximize the utilization **426** of tensor cores and increase throughput with min- **427** imal trade-offs as evidenced by the performance **428** metrics of LLaMA and Mistral models. **429**

Effect of post-prune weight update. Table [4](#page-6-3) 430 presents the performance of LLaMA and Mistral **431** models with and without post-prune weight update **432** and dimension adaptation. Omitting the weight **433** update results in performance drops of 2.88 for **434** LLaMA-2-7B, 5.32 for LLaMA-3-8B, and 2.17 **435** for Mistral-7B, highlighting the crucial role of **436** weight updates in maintaining high performance. 437 Without dimension adaptation, the performance de- **438** creases slightly by 0.05 for LLaMA-2-7B, 0.15 **439** for LLaMA-3-8B, and 0.42 for Mistral-7B. These **440** results suggest that while dimension adaptation pro- **441** vides inference speedup benefits, the post-pruning **442** weight update is significantly more critical for pre- 443 serving the performance of the models. Overall, 444 the combination of both techniques ensures the best **445** performance retention in pruned models. **446**

	ARC-e	H ellaSwag
Pruned	-17.30	-57.26
Unpruned	-8.53	-35.95

Table 6: Average log likelihood of correct predictions by the 50% pruned and unpruned Mistral models shows that the pruned model is more uncertain about its correct predictions

447 4.4 Qualitative Analysis

 As seen in Table [3,](#page-5-1) the pruned Mistral model shows a significant drop in factual knowledge, particularly in its ARC-e and ARC-c performance. However, further analysis reveals that the pruned model cor- rectly classifies 62 ARC-e samples (2% of the total) that the unpruned model does not. As illustrated in Table [13,](#page-13-0) the pruned model often selects the annotated correct answer in cases where choices may seem ambiguous. For instance, on the ques- tion "Which is the best way to help prevent the flu from becoming a pandemic?", the unpruned model closely weighs "getting a vaccination" and "washing hands often," ultimately choosing the latter, while the pruned model selects "getting a vaccination." In most cases of incorrect prediction, the unpruned model shows confusion in its log- its by weighing two choices in a multiple-choice question almost equally and choosing an answer different from the annotated one, while the pruned model displays less confusion and selects the cor- rect answer. This raises the question of whether more 'knowledge' in models leads to more confu- sion and if pruning alleviates this. Additionally, in some instances (seen in Table [13\)](#page-13-0), the pruned model is more factually accurate than the unpruned model, suggesting that overfitting during pretrain- ing might cause the unpruned model's incorrect answers. Table [6](#page-7-0) shows that the pruned model is overall more uncertain about its choices than the unpruned model.

⁴⁷⁸ 5 Related Work

 Efficient Transformers. As LLMs continue to grow in size, several methods have been developed to reduce their memory and computational con- straints [\(Yun et al.,](#page-10-4) [2024;](#page-10-4) [Xiao et al.,](#page-10-5) [2023\)](#page-10-5). These methods broadly fall into two categories: quanti- zation [\(Frantar et al.,](#page-8-12) [2023;](#page-8-12) [Dettmers et al.,](#page-8-4) [2022,](#page-8-4) [2023;](#page-8-13) [Zhang et al.,](#page-10-0) [2024c;](#page-10-0) [Lin et al.,](#page-9-11) [2024;](#page-9-11) [Shao](#page-9-12) [et al.,](#page-9-12) [2023\)](#page-9-12) that reduce full precision weights to fewer bits and pruning [\(Xia et al.,](#page-10-1) [2022;](#page-10-1) [Sanh et al.,](#page-9-13) [2020;](#page-9-13) [Jiang et al.,](#page-8-14) [2023b;](#page-8-14) [Lagunas et al.,](#page-8-15) [2021;](#page-8-15) **488** [Li et al.,](#page-9-14) [2023\)](#page-9-14) that removes weights and tokens. **489** While being orthogonal approaches to compression, **490** they have been combined to enhance compression **491** further [\(Namburi et al.,](#page-9-15) [2023;](#page-9-15) [Saha et al.,](#page-9-16) [2024\)](#page-9-16). **492** Several methods use knowledge distillation for per- **493** formance recovery during pruning [\(Ko et al.,](#page-8-16) [2023;](#page-8-16) **494** [Liu et al.,](#page-9-17) [2023a;](#page-9-17) [Lee et al.,](#page-9-18) [2023;](#page-9-18) [Liu et al.,](#page-9-19) [2023b\)](#page-9-19). **495** Pruning LLMs. Pruning methods are broadly cat- **496** [e](#page-8-3)gorized as unstructured pruning [\(Frantar and Al-](#page-8-3) **497** [istarh,](#page-8-3) [2023;](#page-8-3) [Xu et al.,](#page-10-6) [2024;](#page-10-6) [Zhang et al.,](#page-10-7) [2024b\)](#page-10-7) **498** that targets individual weights within the LLM **499** but yield models with faster inference only with **500** [s](#page-8-1)pecialized accelerators. Structured pruning [\(An](#page-8-1) 501 [et al.,](#page-8-1) [2024;](#page-8-1) [Zhang et al.,](#page-10-8) [2024a\)](#page-10-8) aims to elimi- **502** nate redundant structures for faster inference but **503** previous gradient-based methods [\(Ma et al.,](#page-9-0) [2023;](#page-9-0) **504** [Zhang et al.,](#page-10-9) [2023a\)](#page-10-9) are limited by their substan- **505** tial memory requirements, where as forward-pass **506** only method Bonsai [\(Dery et al.,](#page-8-2) [2024\)](#page-8-2) takes nearly **507** 40 hours for pruning during its search for optimal **508** submodels. VTrans [\(Dutta et al.,](#page-8-8) [2024\)](#page-8-8), although a 509 faster method, fails to prune heads in grouped query **510** attentions and provides limited inference speedups. **511**

6 Conclusion **⁵¹²**

We propose TVA-prune, a structured pruning **513** method that can effectively compress grouped- **514** query attention (GQA) based LLMs. It in- **515** volves sharing key-head Variational Information **516** Bottleneck-masks within groups of query heads to **517** prune key, value and query heads and still maintain **518** the structural integrity. The post-pruning dimen- **519** sion adaptation technique enhances parallelism, re- **520** sulting in higher acceleration for pruned models 521 without compromising performance. Morever, the 522 post-pruning weight updates leverages importance **523** scores of token representations and significantly **524** contributes to maintaining the performance of the **525** pruned models. We demonstrate the effectiveness **526** of TVA-prune in retaining performance even in **527** higher sparsity ratios. Further, it is more effective **528** even in pruning MHA-based models. By training **529** only the masks to prune LLM modules, TVA-prune **530** has considerably lower pruning time compared to **531** other gradient-based and some forward-pass-only **532** approaches. Overall, TVA-prune shows improved **533** resource utilization, achieving significant enhance- **534** ments in both speed and performance suggesting its **535** potential effectiveness in optimizing large language **536** models for practical deployment. **537**

⁵³⁸ 7 Limitations

 Although we have tackled recently published GQA- based and other diverse set of models, sparsity tar- gets and datasets, there is still a vast list of bench- marks and models that could potentially reveal dis- tinct behavior compared to the findings in this work. Hence, our work does not aim to provide an ex- haustive set of results to universally characterize all models. In the experiments, we test with upto 8B models on a single GPU of 40GB. Extending it to larger models would require larger memory or more GPUs which we have not tested for in this work. However, our methodology would theoreti- cally require low amount of memory, computations and provide greater inference speedups even for larger models. We plan to explore layer-wise prun- ing using our formulation to prune models larger than 13B on a single GPU in future work.

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A **Sample size vs pruning time.** 806

Table 7: Varying sample size impacts the performance of pruned models and pruning time. Reducing sample size favors pruning time but increases perplexity, while increasing sample size does not significantly improve performance.

Table [7](#page-10-10) illustrates the impact of varying sample 807 sizes (2k, 4k, 6k) on the performance and pruning 808 time of pruned models, specifically LLaMA-3 and 809 Mistral. As the sample size increases, pruning time **810** also increases, while its reduction results in higher **811** perplexity (PPL). Since increasing the sample size **812** does not lead to significant improvements in per- **813** plexity, we choose to prune with 4000 samples for **814** all types of models. **815**

B Proportion of sub-layer parameters 816 **pruned** 817

Figure [6](#page-10-11) shows the proportion of the remaining 818 parameters in the attention, the intermediate lay- **819** ers and the embedding layer after pruning each **820** of the pre-trained LLaMA models to 50% spar- **821** sity. Lower number of attention parameters can **822** be related to a slightly higher inference speedup **823** in case of LLaMA-2 pruned model with respect to **824** LLaMA-1 pruned model.

Figure 6: Proportion of remaining parameters in each of the LLM modules after pruning 50% of the total model parameters.

C Hyper-parameters for pruning and **⁸²⁶ finetune** 827

The hyper-parameters used for pruning LLaMA **828** and Mistral models on one NVIDIA A100 (40GB) **829** is given in Table [8](#page-11-1) and for finetuning is given in **830**

831 Table [9.](#page-11-2) We take a data blockor sequence_length of **832** 400 while pruning LLaMA-3-7B to fit the training of masks in a single GPU.

Table 8: Hyper-parameters for pruning LLaMA and Mistral with TVA-Prune

Table 9: Hyper-parameters for fine-tuning LLaMA and Mistral compressed models

⁸³⁴ D Algorithm

Algorithm 1 Pruning LLM with VIB masks, followed by post-prune adaptation

Input: Target model sparsity t , Pretrained model weights W

Initialize:VIB masks $m_i, m_i{}^h$ or $m_i{}^{vh}$

for $e = 1, ..., Samples$ do

Sample $\eta \sim \mathcal{N}(\mathbf{0}, \mathbf{I})$, apply random vectors \boldsymbol{z} as in sec [3.1](#page-2-1)

Calculate VIB loss as in Eq [1](#page-1-0) and sparsity loss \mathcal{L}_s as in sec. [3.1](#page-2-0)

Backprop through total loss $\mathcal{L}_{total} = \mathcal{L} + \mathcal{L}_{s}$ Update μ , σ of m masks, sparsity coefficients λ_1, λ_2

end for

Adapt dimensions as in section [3.2](#page-3-1)

Update weights as in section [3.3](#page-3-2)

Get sparser weights as in Eq [6](#page-3-3)

Remove zeroed out columns and rows in weights

Optionally fine-tune remaining weights with LoRA by minimizing: $\mathcal{L}_{total} = \mathcal{L}_{dis} + \mathcal{L}_{task}$ **Output:** Compressed model weights \overline{W}

⁸³⁵ E Task-specific pruning

836 Table [10](#page-11-0) shows task specific pruning with Wikitext-**837** 2 dataset.

838 **F** Improved stability of our pruning **⁸³⁹** method

840 In Table [11](#page-11-3) we compare the standard deviation of **841** performance measured over 5 random seeds for **842** different pruning methods and observe that our

Table 10: Performance comparison of task-specific pruning with Wikitext-2 train set and evaluation on the validation set. Our method outperforms other structured pruning methods (wanda-sp, Bonsai and FLAP) and is similar to VTrans with faster inference. †indicates finetuned with LoRA. ‡adds extra bias parameters.

method yields models with more consistent perfor- **843** mance.

Table 11: Comparison of standard deviation of performance (perplexity) measured over 5 random seeds on Wikitext-2. Our pruning method yields models more consistent in performance across sparsity ratios

G Zero shot results on LLaMA-1 and **⁸⁴⁵** LLaMA-2 **⁸⁴⁶**

In Table [12](#page-12-0) we show the zero-shot performance of **847** LLaMA-1 and LLaMA-2 models. **848**

H More explanation on optimizing GPU **⁸⁴⁹ Performance with adjusted pruned** 850 weight dimensions **851**

Having pruned weight dimensions in multiples of **852** 256 enhances the performance of pruned models **853** on NVIDIA V100 and A100 GPUs. Tiles are fixed- **854** size blocks of matrix elements that GPUs process 855 in parallel. Aligning matrix dimensions with pre- **856** ferred tile sizes like 256x128 ensures optimal use **857** of Tensor Cores, minimizing computational waste **858** due to tile quantization, where partially filled tiles **859** perform unnecessary operations [\(NVIDIA,](#page-9-7) [2024b\)](#page-9-7). **860** Wave quantization occurs when the number of tiles **861** doesn't match the number of streaming multipro- **862** cessors (SMs), leading to underutilized SMs and **863** reduced performance. SMs are the primary com- **864** putational units in NVIDIA GPUs, each capable **865**

Method	BoolQ	PIQA	HellaSwag	WinoGrande	ARC-e	ARC-c	Average \uparrow
	Acc	Acc	Acc	Acc	Acc	Acc	Acc
LLaMA-7B	75.12	78.23	57.65	70.1	75.11	41.32	66.25
Wanda-sp†	50.58	55.01	37.57	54.65	41.72	31.89	45.23
LLM-Pruner†	60.28	69.31	47.06	53.43	45.96	29.18	45.95
$FLAP$ †	60.21	67.52	40.07	57.54	49.66	28.49	50.57
LoRAPrune†	61.88	71.53	47.86	55.01	45.13	31.62	52.17
TVA-Prune†	62.92	68.25	41.95	58.42	56.68	27.14	52.56
$LLaMA-2-7B$	77.70	78.07	57.16	69.06	76.34	43.43	66.96
Wanda-sp†	51.43	55.46	37.24	53.98	42.26	28.68	45.51
$FLAP$ †	60.54	66.78	40.76	57.32	50.18	28.74	50.72
TVA-Prune†	63.24	66.12	42.37	58.84	56.82	28.42	52.63

Table 12: Performance comparison of the 50% pruned LLaMA-1-7B and LLaMA-2-7B models on six zero shot tasks. †denotes finetuned with LoRA. Finetuning enhances the performance all pruned models, yet our pruned model still generalizes better across the tasks. .

866 of executing multiple threads in parallel. Efficient **867** distribution of workload across all SMs is crucial **868** for maximizing GPU performance.

869 I Qualitative comparison on examples **870 from ARC-easy dataset**

871 In Table [13](#page-13-0) we show examples where the pruned **872** model predicts more accurately than the unpruned **873** Mistral model.

Table 13: Examples from the ARC-easy dataset where Mistral 50% pruned model's answers are compared to the unpruned model