# SCALING BAYESIAN EXPERIMENTAL DESIGN TO HIGH-DIMENSIONS WITH INFORMATION-GUIDED DIFFUSION

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## ABSTRACT

We present `DiffBED`, a Bayesian experimental design (BED) approach that scales to problems with high-dimensional design spaces. Our key insight is that current BED approaches typically cannot be scaled to real high–dimensional design problems because of the need to specify a likelihood model that remains accurate throughout the design space. We show that without this, their design optimisation procedures exploit deficiencies in the likelihood and produce implausible designs. We overcome this issue by introducing a generative prior over feasible designs using a diffusion model. By guiding this diffusion model using principled information-theoretic experimental design objectives, we are then able to generate highly informative yet realistic designs at an unprecedented scale: while previous applications of BED have been restricted to design spaces with a handful of dimensions, we show that `DiffBED` can successful scale to designing high–resolution images.

## 1 INTRODUCTION

Experimentation, the process by which we gather information about a phenomenon of interest, is a central task throughout science and industry. In scenarios where data collection is costly or time-consuming, such as drug discovery (Paul et al., 2010; DiMasi et al., 2016) or clinical trials (Fogel, 2018), it is natural to seek designs that yield data that is *maximally informative*. This intuition is captured by the framework of Bayesian experimental design (BED) (D. V. Lindley, 1956; Chaloner & Verdinelli, 1995; Rainforth et al., 2024; Huan et al., 2024). In BED, we specify a probabilistic model of the data gathering process, use this to derive a formal notion of the *expected information gain* (EIG) of an experiment for a target quantity of interest, then optimise this EIG to yield designs we expect to maximally reduce our uncertainty. Thanks to the coherence of Bayesian reasoning, this framework is naturally suited to adaptively gathering information across several experimental steps, utilising information from previous experiments in each sequential decision we make.

Although, in principle, BED can be applied to a wide array of tasks, successful applications have historically been limited to simple problems in which the design variables are low-dimensional (Myung et al., 2013; Vincent & Rainforth, 2017; Watson, 2017; Dushenko et al., 2020; Loredo, 2004; Vanlier et al., 2012; Shababo et al., 2013; Papadimitriou, 2004). Developing methods for high-dimensional design spaces is thus a critical open challenge (Rainforth et al., 2024; Huan et al., 2024), with the problem historically being considered mostly as one of developing scalable EIG estimators (Foster et al., 2019; Goda et al., 2022; Ao & Li, 2023; Iollo et al., 2025a; Huan et al., 2024).

In this work, we demonstrate the existence of an even more fundamental barrier: being able to specify a likelihood in high dimensions that faithfully reflects the real-world data generation process across the entirety of the design space. In other words, model misspecification becomes increasingly unavoidable as design dimensionality increases, as we must construct a likelihood model that remains accurate over an ever-growing space. In particular, while the success of modern machine learning methods relies on modelling around some data manifold, our desire to optimise with respect to the design and seek out information that is distinct from that already known inevitably relies on the ability of our likelihood to "extrapolate" to regions when our ability to predict outcomes is limited.

The upshot of this, as shown in Figure 1, is that directly optimising the EIG leads to flaws in the likelihood being exploited, and meaningless designs being produced. This is akin to reward hacking in reinforcement learning (Skalse et al., 2022). Namely, we see that even though existing stochastic gradient approaches are already effective at optimising the EIG in this very high dimensional setup,

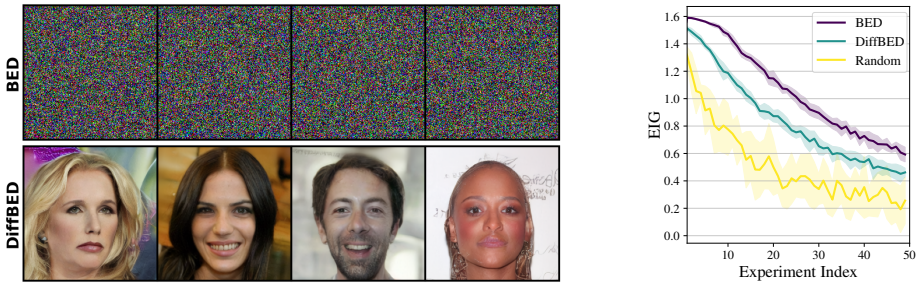


Figure 1: First iteration design sets for the *search* experiment (see Section 6) for BED (top left) and via `DiffBED` (bottom left). Also shown is incremental EIG achieved at *each* experiment iteration (right).

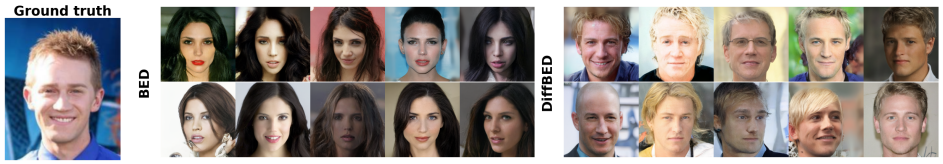


Figure 2: Posterior samples after 50 search iterations for standard BED (left) and `DiffBED` (right).

the problem instead is that the optimisation leads to unrealistic designs for which the assumed likelihood is heavily misaligned with the true data-generating process. In particular, as we show later, it seeks out designs where the model's likelihood is overconfident and the experiment outcomes will, in truth, be uninformative. Moreover, in Figure 2, we see that when sequentially applying BED to adaptively choose designs, this in turn leads to a problematic feedback loop in the posterior updates: rather than simply remaining uncertain, our posterior beliefs collapse around a distinctly incorrect $\theta$.

To address this, we introduce `DiffBED`, a novel method for Bayesian experimental design in high-dimensional design spaces. `DiffBED` works by introducing a *prior over feasible designs*. It reframes the design optimisation as sampling from a distribution that balances prior feasibility and EIG under the model. This ensures that the designs generated stay on an admissible manifold where the likelihood is relatively well aligned, and regularises against such reward hacking behaviour.

Specifically, `DiffBED` uses a diffusion model for its design prior. Designs are then generated by a process we call *information-guided diffusion*, where designs are chosen by simulating the reverse–time SDE of this diffusion process, with guidance provided by an estimator for the score of the EIG. This estimator is itself based on a combination of Tweedie's formula (Robbins, 1956) and existing EIG gradient estimators (Rainforth et al., 2018; Foster et al., 2020). Adaptive design is performed by rerunning the diffusion process with updated EIG estimators that incorporate new observations.

As shown in Figure 1, this leads to designs that are both meaningful and informative. In turn, these designs enable effective learning about the target quantity of interest (see Figure 2). `DiffBED` therefore represents the first successful application of BED in high-dimensional design spaces: we show successful deployment of `DiffBED` to design spaces in excess of 750 000 dimensions, whereas previous BED approaches have rarely been successfully been used beyond $\sim 20$ dimensions.

## 2 Preliminaries

We begin by reviewing the key concepts underpinning the BED framework. In BED, we express our initial beliefs about the target variable of interest, $\theta$, through a prior distribution $p(\theta)$. We also specify a likelihood $p(y \mid \theta, \xi)$, which gives the probability of possible experimental outcomes $y$ given $\theta$ and a design $\xi$. If an outcome $y$ were observed by running an experiment with design $\xi$, the *information gain* (IG) of such an experiment is the reduction in entropy obtained when updating from the prior $p(\theta)$ to the posterior $p(\theta \mid y, \xi)$ (Lindley, 1956), defined as, $\mathrm{IG}(y, \xi) = \mathrm{H}[p(\theta)] - \mathrm{H}[p(\theta \mid y, \xi)]$. Since the outcome $y$ is unknown before running the experiment, we instead maximise the *expected information gain* (EIG) (Lindley, 1972; Bernardo, 1979; Sebastiani & Wynn, 2000):

$$\mathrm{EIG}(\xi) = \mathbb{E}_{p(y|\xi)}[\mathrm{IG}(y, \xi)] = \mathbb{E}_{p(\theta)\,p(y|\theta,\xi)}\left[\log p(\theta \mid y, \xi) - \log p(\theta)\right] \tag{1}$$

$$= \mathbb{E}_{p(\theta)\,p(y|\theta,\xi)}\left[\log p(y \mid \theta, \xi) - \log p(y \mid \xi)\right], \tag{2}$$

where the last equality follows from Bayes' rule. The EIG is then maximized to produce an optimal design $\xi^* = \operatorname{argmax}_{\xi \in \Xi} \mathrm{EIG}(\xi)$, where $\Xi$ is the space of admissible designs.

**Adaptive Design** In many applications, we are interested in producing a sequence of designs $\xi_1, \xi_2, \ldots, \xi_K$ yielding data $y_1, y_2, \ldots, y_K$. While the sequence $\xi = (\xi_1, \xi_2, \ldots, \xi_K)$ could be determined statically before observing any data, a more performant approach is to select the design $\xi_k$ adaptively depending on the history $\mathcal{D}_{k-1} = \{(\xi_i, y_i)\}_{i=1}^{k-1}$ of designs and outcomes prior to step $k$. In this adaptive setting, the design for the $k$-th experiment is typically obtained by greedily maximising the *incremental* $\mathrm{EIG}(\xi_k \mid \mathcal{D}_{k-1}) = \mathbb{E}_{p(\theta|\mathcal{D}_{k-1})\, p(y_k|\theta,\xi_k)} \left[\log p(y_k \mid \theta, \xi_k) - \log p(y_k \mid \xi_k)\right]$. This expression is equivalent to the EIG except that the prior, $p(\theta)$, is replaced with the posterior, $p(\theta|\mathcal{D}_{k-1})$, which reflects the current beliefs given the history (Rainforth et al., 2024).

**Estimating the EIG** While the EIG is conceptually appealing, estimating it can be challenging due to the doubly intractable nature of the objective, with a wide variety of approaches proposed to address this, see (Rainforth et al., 2024, Section 3) for a review. However, when the outcome space $\mathcal{Y}$ is discrete, the outer expectation with respect to the likelihood can be enumerated over. In this case, the EIG is now singly-intractable, yielding a non-nested estimator (Rainforth, 2017; Gal et al., 2017)

$$\widehat{\mathrm{EIG}}(\xi) = -\sum\nolimits_{y \in \mathcal{Y}} \hat{p}(y \mid \xi) \log \hat{p}(y \mid \xi) + \frac{1}{N} \sum\nolimits_{n=1}^{N} \sum\nolimits_{y \in \mathcal{Y}} p(y \mid \theta_n, \xi) \log p(y \mid \theta_n, \xi), \quad (3)$$

where $\theta_n \sim p(\theta)$ (or $\theta_n \sim p(\theta \mid \mathcal{D}_{k-1})$ in adaptive settings) and $\hat{p}(y \mid \xi) = \frac{1}{N} \sum_{n=1}^{N} \hat{p}(y \mid \theta_n, \xi)$.

**Optimizing the EIG with Stochastic Gradients** During active experimentation, we not only want to estimate the EIG, but optimize it. Stochastic gradient-based methods are scalable and effective for optimization in high-dimensional continuous design spaces and can easily be applied to estimates of the gradients of the EIG such as (3) (Huan & Marzouk, 2014; Foster et al., 2020; Goda et al., 2022).

## 3 Directly Optimising EIG Seeks Out Model Misspecification

Bayesian experimental design is inherently model-based, with the EIG relying on the assumed likelihood model $p(y \mid \theta, \xi)$ and a subjective prior $p(\theta)$. As such, how well the EIG reflects the true expected utility of gathering new data will depend on the accuracy of this model, in particular how well the assumed likelihood approximates the true conditional data-generating process $p_{\text{true}}(y \mid \theta, \xi)$. While the prior provides some protection against needing the likelihood to be accurate across all $\theta$, optimising over $\xi$ requires the likelihood to remain accurate across the entire design space.

When the designs $\xi$ are high-dimensional, faithfully modelling $y \mid \theta, \xi$ becomes especially challenging and it is usually not realistic to construct a likelihood that is accurate across all $(\theta, \xi)$ pairs. Indeed, the assumed likelihood $p(y|\theta, \xi)$ in high-dimensional problems will often itself be a *learned* function derived from a pre-trained machine learning model. For example, in Figure 1 our likelihood utilises a fixed encoder that captures semantic content. In such cases the likelihood will only reflect the true data-generating mechanism in data regions near where the feature extracting component was trained.

We now show that direct optimisation of the EIG is *inherently prone* to seeking out areas of the design space where the model is misspecified, specifically, it is drawn to regions where the likelihood is *overconfident*. To do this we consider the difference in using the EIG with our model's likelihood compared with a "true" EIG that uses the unknown true underlying data distribution:

$$\mathrm{TEIG}(\xi) := \mathbb{E}_{p(\theta) p_{\text{true}}(y|\theta,\xi)} \left[\log p_{\text{true}}(y \mid \theta, \xi) - \log p_{\text{true}}(y \mid \xi)\right] \quad (4)$$

where $p_{\text{true}}(y \mid \xi) = \mathbb{E}_{p(\theta)}[p_{\text{true}}(y \mid \theta, \xi)]$. We now have

$$\mathrm{EIG}(\xi) = \mathrm{TEIG}(\xi) + \mathbb{E}_{p_{\text{true}}(y|\xi)} \left[\mathrm{H}[p_{\text{true}}(\theta \mid y, \xi)]\right] - \mathbb{E}_{p(y|\xi)} \left[\mathrm{H}[p(\theta \mid y, \xi)]\right] \quad (5)$$

$$= \mathrm{TEIG}(\xi) + \underbrace{\mathbb{E}_{p(\theta)} \left[\mathrm{H}[p_{\text{true}}(y \mid \theta, \xi)] - \mathrm{H}[p(y \mid \theta, \xi)]\right]}_{=:\mathcal{M}(\xi)} + \mathrm{H}[p(y \mid \xi)] - \mathrm{H}[p_{\text{true}}(y \mid \xi)], \quad (6)$$

where $p_{\text{true}}(\theta \mid y, \xi) = p(\theta) p_{\text{true}}(y \mid \theta, \xi) / p_{\text{true}}(y \mid \xi)$. This decomposition provides helpful insight into how the EIG behaves when used with an approximate model likelihood. Namely, we can view $\mathcal{M}(\xi)$ as a measure on the average degree of model overconfidence across possible $\theta$: it is zero if the likelihood matches the true data generating process and it grows as the likelihood becomes more certain than it should be. Critically, $\mathcal{M}(\xi)$ varies across designs, and its presence in the decomposition encourages designs found by directly optimizing the EIG to lie where the likelihood is overconfident.

Moreover, the remaining $\mathrm{H}[p(y \mid \xi)] - \mathrm{H}[p_{\text{true}}(y \mid \xi)]$ term typically provides little protection against this desire to move to regions of overconfident likelihoods. In particular, these marginal data distributions will inherently be more diffuse than the corresponding likelihoods, with the averaging over $\theta$ providing regularisation on their predictions. Thus, in high-dimensional spaces it will usually be easy to find designs where we are overconfident in $y|\theta, \xi$, but our uncertainty over $\theta$ ensures that $\mathrm{H}[p(y \mid \xi)]$ remains high. Thus, even when the likelihood is heavily misspecified, $p(y \mid \xi)$ and $p_{\text{true}}(y \mid \xi)$ will often still be similar for most $\xi$. For example, if we have a design very far away from previous designs then a misspecified (but still sensible) model will generally produce high marginal predictive uncertainty, even though it might be very confident about $y$ when $\theta$ is known. As such, the signal from this remaining term will generally not sufficiently counteract $\mathcal{M}(\xi)$ and we can expect direct EIG optimisation to seek out designs where the likelihood is overconfident.

## 4 Bayesian Experimental Design via Information-Guided Diffusion

While improving the fidelity of $p(y \mid \theta, \xi)$ would reduce the misalignment in (5)-(6), simply modifying the likelihood is not a viable solution , since any residual imperfections will be exploited by the optimizer in high-dimensional spaces. Rather, we accept inevitable misalignment and instead modify the design process itself. Ideally, we would like to maximize the EIG subject to $\mathcal{M}(\xi)$ being small, but this misalignment, by definition, is often difficult, if not impossible, to quantify.

Instead, we introduce a reference prior on designs, $p^{\text{ref}}(\xi)$, that captures the manifold of feasible designs. We can then restrict our search to only those designs which have reasonable support under this reference prior. For many problems, suitable reference priors can be constructed from unlabelled auxiliary data or a separate foundation model, without requiring any task-specific data. For example, if our design is an image of a face, then $p^{\text{ref}}(\xi)$ could be instantiated as a deep generative model over faces. The manifold defined by $p^{\text{ref}}(\xi)$ also often aligns with regions where likelihood misalignment is relatively small. In particular, as we demonstrate later, it is often possible to derive the reference prior from the same data used in constructing the likelihood. For example, in Section 6 we use likelihoods that depend on an unsupervised encoder of images. Constraining design optimization to a manifold that is meaningful avoids the catastrophic collapse to incorrect $\theta$s seen in Figure 2 for traditional BED.

We now need a mechanism to produce designs that both representative samples under $p^{\text{ref}}(\xi)$ and which we expect to be highly informative under our model, i.e. that have high $\mathrm{EIG}(\xi)$. To do this, we consider the following optimisation problem over $q(\xi) \in \mathbb{P}(\Xi)$,

$$p^*(\xi) = \operatorname{argmax}_{q(\xi)\in\mathbb{P}(\Xi)} \; \mathbb{E}_{q(\xi)}[\mathrm{EIG}(\xi)] - \alpha \,\mathrm{KL}\big[q(\xi) \,\|\, p^{\text{ref}}(\xi)\big] \tag{7}$$

where $\alpha > 0$ is a hyperparameter that trades off achieving high EIG values with adherence to the reference distribution, as measured by the KL divergence. Using variational calculus, Equation (7) yields a unique solution known as the *exponential tilting* distribution (Rawlik et al., 2012)

$$p^*(\xi) \propto p^{\text{ref}}(\xi) \cdot \exp\left(\alpha^{-1}\mathrm{EIG}(\xi)\right). \tag{8}$$

Sampling $\xi \sim p^*(\xi)$ now ensures that designs are drawn from high-probability regions of $p^{\text{ref}}(\xi)$ while up-weighting those with large EIG. Notably, this approach requires no likelihood-dependent training of $p^{\text{ref}}$ nor any modifications to the likelihood, so that a pre-trained generative model is readily applicable. While Equation (8) could potentially be maximized, we choose to sample from $p^*(\xi)$ to avoid exploiting imperfections in the approximation of the generative model, which may lead to unrealistic designs. In particular, it has been shown that the points to which deep generative models assign the highest density are often not themselves reasonable samples (Nalisnick et al., 2018).

### 4.1 Guiding Diffusion with EIG

Having established $p^*(\xi)$ as our target distribution for producing designs, we now introduce `DiffBED`, our proposed framework which instantiates this idea using a diffusion model (Ho et al., 2020; Song et al., 2021) as the reference generative model $p^{\text{ref}}$ in (8). Diffusion models offer state-of-the-art generative quality and diversity across images, video, and scientific data. Unlike VAEs (Kingma & Welling, 2013) or GANs (Goodfellow et al., 2014), diffusion models learn a score function rather than a fixed decoder. This enables powerful training-free guidance methods for sampling from tilted distributions (Bansal et al., 2023; Uehara et al., 2025; Ye et al., 2024; Domingo-Enrich et al., 2024; Denker et al., 2024), making them uniquely suited to our framework by allowing sampling from (8) without retraining or latent-space optimization.

**Diffusion Models** Diffusion models define a forward SDE which gradually corrupts data with noise and a learn reverse process which undoes this corruption (Song et al., 2021). The forward SDE is

$$\mathrm{d}\xi_t = f(\xi_t, t)\,\mathrm{d}t + g(t)\,\mathrm{d}W_t \qquad \xi_0 \sim p_0(\xi_0) \qquad t \in [0, T] \tag{9}$$

where $p_0(\xi_0)$ is a training distribution of designs with $\xi = \xi_0$, $f(\xi_t, t)$ is a drift vector field, and $g(t)$ is a noise schedule. The functions $f, g$ are chosen so that $p_T(\xi_T)$ is approximately Gaussian. A generative model is obtained by solving time time-reversal of Equation (9), given by

$$\mathrm{d}\xi_t = \left[f(\xi_t, t) - g(t)^2 \nabla_{\xi_t} \log p_t(\xi_t)\right] + g(t)\,\mathrm{d}\overleftarrow{W_t} \qquad \xi_T \sim p_T(\xi_T) \qquad t \in [0, T] \tag{10}$$

where $\mathrm{d}\overleftarrow{W_t}$ is a time-reversed Brownian increment and $b(\xi_t, t) := f(\xi_t, t) - g(t)^2 \nabla_{\xi_t} \log p_t(\xi_t)$ is an updated drift. The intractable score $\nabla_{\xi_t} \log p_t(\xi_t)$ is approximated by a neural network $s_\phi(\xi_t, t)$ with parameters $\phi$ trained via denoising score matching (Hyvärinen & Dayan, 2005; Song et al., 2021). Sampling $\xi_T$ from the Gaussian prior and integrating (10) backwards in time yields samples $\xi \sim p^{\text{ref}}(\xi)$, our generative approximation to $p_0$. In practice, we use pre-trained diffusion models, which can optimally be conditioned (e.g., via text prompts) to produce domain-specific designs.

**Information-Guided Diffusion** We aim to sample from the EIG-tilted distribution $p^*(\xi)$. This amounts to adding an extra drift term to Equation (10) of the form

$$u(\xi_t, t) = g(t)^2 \nabla_{\xi_t} \log \mathbb{E}\left[\exp(\alpha^{-1}\mathrm{EIG}(\xi_0)) \mid \xi_t\right] \approx g(t)^2 \alpha^{-1} \nabla_{\xi_t} \mathbb{E}\left[\mathrm{EIG}(\xi_0) \mid \xi_t\right] \tag{11}$$

where the approximation follows by assuming that the EIG of $\xi_0$ is a function of $\xi_t$ with additive noise. This approximation is still intractable, though, as $\mathbb{E}\left[\mathrm{EIG}(\xi_0) \mid \xi_t\right]$ is unknown. Inspired by recent work on inverse problems (Chung et al., 2024), we define $\widehat{\xi_0}(\xi_t) := \mathbb{E}[\xi_0 \mid \xi_t]$ and approximate $\mathbb{E}\left[\mathrm{EIG}(\xi_0) \mid \xi_t\right] \approx \mathrm{EIG}(\widehat{\xi_0}(\xi_t))$ which follows from approximating the intractable $p(\xi_0 \mid \xi_t)$ by a delta function located at its mean. Critical to making this approximation tractable is Tweedie's formula (Robbins, 1956; Efron, 2011; Meng et al., 2021), which allows us to approximate $\widehat{\xi_0}(\xi_t)$ in terms of the score function $s_\varphi(\xi_t, t)$ without needing to simulate the SDE (10). For instance, when $f(\xi_t, t) = -\frac{1}{2}\beta(t)\xi_t$ and $g = \sqrt{\beta(t)}$ (i.e., DDPM (Ho et al., 2020) or the VP-SDE (Song et al., 2021)), Tweedie's formula may be written as $\widehat{\xi_0}(\xi_t) = (x_t + (1 - \alpha_t)\nabla_{\xi_t} \log p_t(\xi_t))/\sqrt{\alpha_t}$, $\alpha_t = \exp(-\int_0^t \beta(s)\,\mathrm{d}s)$ enabling an efficient approximation of (11) using our pre-trained score network. Altogether, we obtain an approximate sampler for $p^*(\xi)$ by solving the SDE

$$\mathrm{d}\xi_t = \left[f(\xi_t, t) - g(t)^2 \left(s_\varphi(\xi_t, t) + \alpha^{-1} \nabla_{\xi_t} \mathrm{EIG}\left(\widehat{\xi_0}(\xi_t)\right)\right)\right] \mathrm{d}t + g(t)\,\mathrm{d}\overleftarrow{W}_t \tag{12}$$

backwards in time. We initialize from Gaussian noise, acknowledging a small bias from not adjusting the initial distribution (Uehara et al., 2024). In practice this simply adds a scaled EIG-gradient estimate to the pre-trained score network at each step, which we find sufficient for high-quality designs without additional Langevin corrections targeting $p^*(\xi)$. We note that the EIG gradient used during guidance is itself an approximated quantity, e.g., via (3). Importantly, this does not require reparametrization, so that our method is applicable in a broad set of contexts. If $y$ is not discrete, alternative EIG gradient estimatiors can be used instead (see e.g. Rainforth et al. (2024, Section 3)).

In some applications, our task calls for *sets* of designs. We consider several applications of this nature in Section 6. In Appendix B.3, we discuss how our techniques can be extended to the set-valued case.

### 4.2 DiffBED: BED with Information-Guided Diffusion

Our end-to-end procedure for `DiffBED` is similar to the standard (sequential) BED framework, except that our optimization for $\xi$ at each experiment iteration utilises the guided diffusion technique in Section 4.1. In Appendix B, we provide a full discussion of the details needed to implement `DiffBED`, including an algorithmic description in Algorithm 1.

For sequential BED, we require a high-fidelity and fast posterior sampler. A key design choice in `DiffBED` is to perform inference in a latent space rather than directly in pixel space. This approach exploits the fact that, in many ostensibly high-dimensional tasks, the information we care about lives in a much lower-dimensional space (such as perceptual features) while other variations (background or pixel noise) can be ignored. This makes sequential BED feasible to scale while remaining compatible with a wide range of problems where the likelihood is naturally defined on top of an encoder.

Concretely, we embed $\theta$ using a trained encoder and place a simple prior on the resulting latent vector (e.g., a Gaussian or a uniform distribution on the unit sphere). Although we work in an embedding space, the latent dimension can still be moderately high (e.g., 64 dimensions), which is sufficient for expressivity but tractable for inference. Posterior inference over $\theta$ is done in this latent space using fast particle-based filtering methods (Johansen, 2009), yielding high-fidelity posterior samples at each sequential iteration. From these latent posterior samples we can also recover image-space designs – for instance, by nearest-neighbour retrieval from a large pool or by guiding a diffusion model to synthesize images whose embeddings match the posterior particles (e.g., via cosine similarity). Overall, this strategy makes `DiffBED` scalable and flexible: it retains high-quality inference while seamlessly interfacing with modern generative models. Details of our particle filtering and inverse-mapping procedures are given in Appendix C.

## 5 Related Work

Although the framework of BED has a long history (Lindley, 1956; Bernardo, 1979; Sebastiani & Wynn, 2000), scaling BED to realistic settings remains an open challenge (Rainforth et al., 2024; Huan et al., 2024). Viewing challenge as one of computational costs, a long list of works (Foster et al., 2019; 2020; Goda et al., 2022; Ao & Li, 2023; Iollo et al., 2025a) have looked to provide improved gradient estimators compared to simple nested Monte Carlo (Rainforth et al., 2018). Notably, Iollo et al. (2025a) also considers the use of diffusion models, but only in an attempt to improve scaling in the *target variable space*, $\theta$, by using a diffusion model for their prior, $p(\theta)$. All of the aforementioned works are restricted to *low–dimensional design spaces*, with the 15-dimensional and 20-dimensional design spaces considered by Iollo et al. (2025b) and Ivanova et al. (2021) respectively being some of the highest dimensional applications of sequential BED. By contrast, we successfully conduct sequential design optimisation in design spaces of over $750\,000$ dimensions.

Recent BED work has also considered leveraging LLMs to generate natural language questions as experiment designs to be used in preference elicitation (Choudhury et al., 2025; Kobalczyk et al., 2025). A batch of candidate designs is generated by an LLM, ranked, and the design with the highest EIG is selected. Handa et al. (2024) similarly considers preference elicitation using BED and LLMs, but assumes the parameter and design are supported on an explicit and fixed low-dimensional feature space. On the other hand, `DiffBED` is explicitly focused on the setting where the design space is high-dimensional and continuous, leveraging gradient-based optimization.

Active learning (AL) (Settles, 2009) also aims to select informative data, but typically with the aim of learning a predictive model rather than learning about a specific target quantity as in BED. Much of the AL literature focuses on pool-based selection, where an existing set of unlabelled examples is available (Houlsby et al., 2011; Gal et al., 2017). Some works consider *query synthesis*, i.e., generating inputs directly, often by optimizing an acquisition function in a generative latent space to ensure plausible queries (Zhu & Bento, 2017; Schumann & Rehbein, 2019; Mayer & Timofte, 2020). Instead, we focus on the more general setting of experimental design (which subsumes active learning); active learning approaches are not generally applicable the problems considered in our experiments.

Other works have also previously studied model misspecification in BED (Forster et al., 2025; Overstall & McGree, 2022; Go & Isaac, 2022; Feng et al., 2015). However, they all look to address this by adjusting the model or EIG itself. Our work is the first to identify that model misalignment is not constant across design space and show the potential for reward hacking to occur even for ostensibly good models; none of these approaches are suitable for addressing this issue and thus they do not provide useful benefits in settings we consider. We are thus the first to provide a scalable solution by using reference prior and regularising the optimisation.

## 6 Experiments

We now perform an extensive empirical evaluation of our proposed `DiffBED` method. Although `DiffBED` is not specific to any one experimental setting, our experiments are unified by the theme of human feedback elicitation, as this encapsulates a broad range of important, real-world tasks with high-dimensional designs. In particular, we focus on the setting where designs consist of one or more images. We consider a range of datasets and feedback types, which include binary rankings, rankings of a subset of images from the design set, and discrete ratings. We defer in depth experimental details, including additional results and ablations, to the Appendix.


Figure 3: Design sets of four images generated by `DiffBED` for CelebA Search, against two ground truths (top and bottom row), at experiment iteration 1 (centre, both rows) and 40 (right, both rows).

**Baselines** Our primary baseline is the current standard paradigm (Huan et al., 2024; Rainforth et al., 2024) for BED, namely, direct gradient-based maximization of the EIG estimator (3) (Huan & Marzouk, 2014; Foster et al., 2020). We refer to this baseline simply as *BED*. We also compare against *Entropy*, a variant of `DiffBED` where we guide the diffusion model with the marginal predictive entropy rather than the EIG. In addition, we consider *Rank*, an ablation of `DiffBED` where we generate a set of 1000 unguided candidate designs upfront (where the set size is chosen to roughly match runtime to `DiffBED`), then select at each iteration the candidate with the highest estimated EIG. To ensure the strongest baseline possible, we take these candidate designs directly from the data originally used to train the diffusion model, rather than actually diffusing them. Finally, we compare against *Random*, a simple baseline where designs are selected uniformly at random from a discrete set of feasible designs.

**Metrics** To evaluate the effectiveness of the various design strategies, at each experiment iteration we compute the average cosine similarity between the ground truth, $\theta_{\text{true}}$, and our current posterior $\theta$ samples. This measures our ability to recover a ground truth target variable. We also evaluate the incremental EIG of the chosen design at each step; we emphasise that this should not be viewed as a success metric itself but rather an insightful quantity to track. We additionally include several qualitative results (c.f. Figures 1 and 2). All numerical results on MNIST are averaged over 25 random seeds, while the higher-dimensional CelebA and Zappos runs are averaged over 10.

### 6.1 Information-Theoretic Search

We first evaluate `DiffBED` on an information-theoretic search task, where the goal is to recover a ground-truth image based on feedback from a user. Here, designs are sets of images and the outcomes $y$ are rankings indicating the relative similarity of each design to the ground-truth image. As a motivating example, suppose an eyewitness of a crime is being interviewed in order to construct possible images of the suspect that we wish to be perceptually close to the true suspect. Though it is not generally possible for the eyewitness to directly generate accurate images, they likely can positively identify a photo of the true suspect if shown one and more generally provide feedback when shown images. We can therefore instead iteratively show the eyewitness a set of candidate images, $\xi_k = (\xi_k^1, \ldots, \xi_k^J)$ and have them provide feedback by ranking the images in how well they match the suspect. Such an approach is commonly deployed by UK police forces, but with software that uses low-resolution images and chooses them in a heuristic manner (VisionMetric, 2019).

To apply BED, we require a model capturing the complex relationship between the sketch and the victim's response. Since a human's perception of images and identities does not operate at a pixel-by-pixel resolution, we can assume a reasonable model is $p(y_k \mid \theta, \xi_k)$, where $\theta$ is a rich, sufficiently high-dimensional feature space encoding of an image, following Section 4.2, and our likelihood is based around the similarity of each $\xi_k^j$ to the underlying $\theta$. For our experiment setup, the simulated participant is given a set of $N = 4$ images and their response, $y$, is a ranking of the top $M = 2$ images, based on the relative perceived similarities of each image to the ground truth. Under this setup, we evaluate `DiffBED` on MNIST and CelebA (LeCun et al., 1998; Liu et al., 2015), using SimCLR embeddings (Susmelj et al., 2020; Chen et al., 2020) for the former and a pre-trained VGGFace2 model (Cao et al., 2018) fine-tuned using a triplet loss for the latter. For full setup details see Appendix A.

We plot the resulting EIG and cosine similarities in Figure 4. Standard BED is capable of achieving high EIG under the assumed likelihood model for both datasets. However, due to model misalignment, the designs produced are imperceptible from pure noise, and so the return responses are meaningless. Therefore, the cosine similarity between $\theta_{\text{true}}$ and posterior samples remains effectively zero

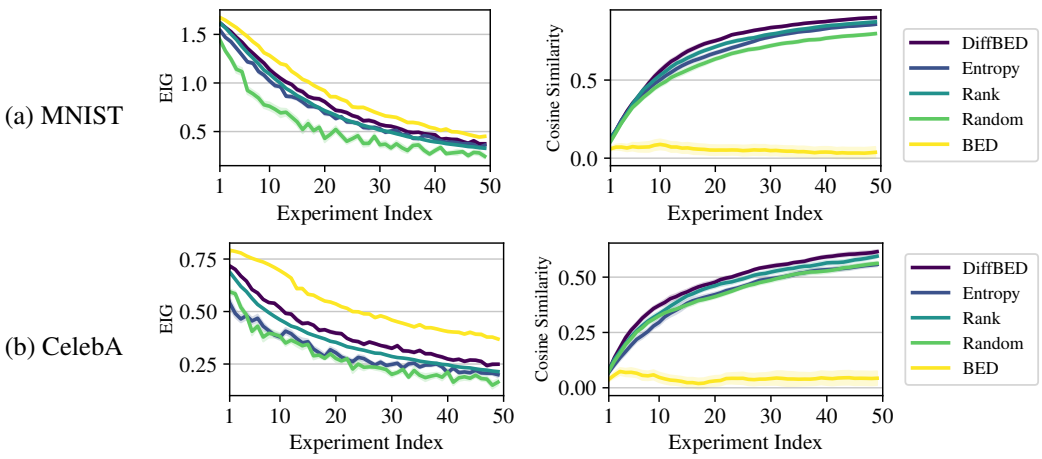


Figure 4: EIG and cosine similarities for search (mean with ± std. error shading), where designs are sets of four images and responses are the rank of the top-two candidates. `DiffBED` achieves the highest mean cosine similarity, while standard BED fails to solve the task despite achieving high EIGs.

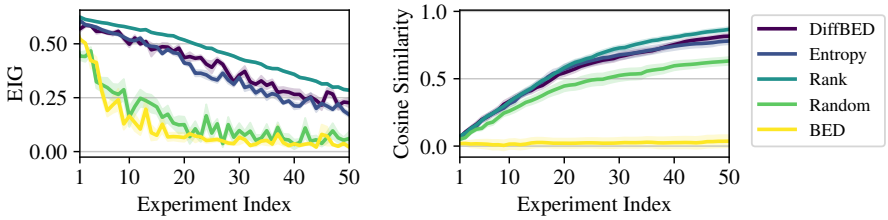


Figure 5: EIG and cosine similarity for preference elicitation on CelebA. Designs consist of image pairs with binary preference responses. Standard BED yields EIG values comparable to random selection and struggles to identify the true preference vector (low cosine similarity), while `DiffBED` maintains higher cosine similarity and more informative designs.

throughout, indicating that standard BED has failed to solve the task. While `DiffBED` inevitably fails to achieve as high an EIG as standard BED, by sticking to a realistic design manifold it succeeds at the underlying task, producing effective learning in the true $\theta$ as reflected in the cosine similarity plots. We also see that it outperforms the random baselines, confirming the benefit of our information-guided sampling. Finally, we see that `DiffBED` outperforms the ablations of *Entropy* and *Rank*. It is particularly notable for this problem that predictive entropy does not in anyway encourage the set of images the user is asked to rank to be different, with the EIG needed to capture the nuance that the rankings need to be informative, not simply uncertain.

### 6.2 Active Preference Elicitation

We now consider the setting of *active preference elicitation*. Motivating examples for this are wide spread, including recommender systems that are tailored to an individuals preferences. For example, a dating site might wish to recommend profiles that a user is likely to engage with. To do this, the company may suppose that a users preferences can be distilled into distinct interpretable features, indicating the presence of, for example, glasses, or a smile in the image. To infer a user's preferences, we can learn from a user's preference over two potential profiles.

Concretely, for this problem we setup $\theta$ as a unit-normalised vector in which each element is a preference weighting for binary CelebA attributes. We use a Bradley-Terry (BT) response model, in which designs are pairs of images. We parametrise the latent reward as being proportional to the dot product between the preference vector and a vector of classifier probabilities that each attribute is present for each image in the pair. See Appendix A for additional experimental details, and Appendix C for details about the inference.

As shown in Figure 5, `DiffBED` achieves consistently high EIG designs and substantially outperforms both the standard BED and random baselines by producing much higher cosine similarities. In-

Figure 6: Example high resolution designs produced by DiffBED on the Zappos dataset.

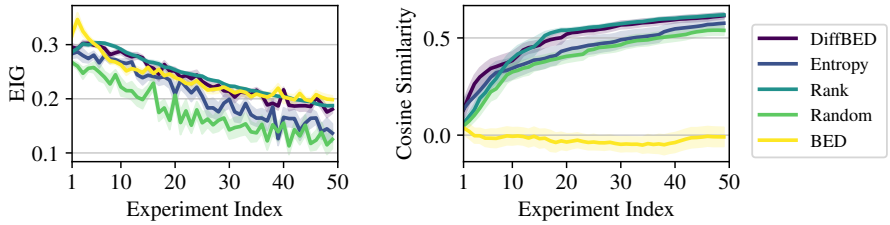


Figure 7: Search on the large-scale Zappos dataset with high-resolution ($512 \times 512$) images. Designs are single images with discrete ratings as responses. Even at this scale, DiffBED remains effective.

terestingly, the EIG performance of the standard BED baseline is itself much lower than DiffBED, especially after the first few iterations, even though it still produces designs that look like pure noise. The likely reason that this is happening is that the EIG optimisation is struggling more than in information-theoretic search, noting that as there are only binary images and not a single ground truth target image, the signal for choosing good designs is weaker here. By contrast, the reference prior in DiffBED also helps in guiding the optimisation process towards sensible designs, so that it actually assists in finding regions of the design space with high EIG when the signal for the latter is weak or noisy.

While DiffBED again outperforms *Entropy* on this problem, *Rank* now slightly outperforms it. This may again in part be down to the difficulty of the EIG optimisation, but it is also likely because we are only looking at pairs of images and the space of suitable image pairs is easier to search through a guess–and–check strategy than it is to choose good sets of four images. We thus see that *Rank* provides a useful variant on our DiffBED approach for this simpler setup, but is less useful when simple sampling from $p^{\text{ref}}(\xi)$ is not sufficient for generating good candidate designs.

### 6.3 Text-to-Image Foundation Models

We now scale our application of DiffBED even further by leveraging text-to-image foundation models as $p^{\text{ref}}$, focusing on the problem of preference elicitation over e-commerce products. Specifically, we consider a setup where the user is shown a single image of a shoe and asked to give a rating of 1 to 5, and we then use this to try and hone in on the users notion of an "ideal shoe" that we can use for making recommendations.

For the reference diffusion model, we use Stable Diffusion v1.5 (Rombach et al., 2022),a 1B parameter foundation model, fine-tuned on the Zappos (Yu & Grauman, 2014) dataset, which provides high resolution ($512 \times 512$) images of shoes. To model a user's feedback, we use the Ordinal Logit Model which assumes the discrete score is correlated with an underlying reward proportional to the similarity of the design image to the image of the reference shoe. See Appendix A.3.3. Figure 6 shows that DiffBED is able to produce effective qualitative designs that highly realistic. Figure 7 provides quantitative results and confirms these designs are informative: DiffBED and *Rank* perform similarly, while outperforming all other methods. Standard BED again fails to learn anything meaningful.

## 7 Conclusion

We present DiffBED, a technique which enables us to scale gradient-based Bayesian experimental design to high-dimensional, continuous design spaces. Our approach is based on guiding a diffusion model pre-trained on feasible designs with a principled information-theoretic acquisition function, allowing us to produce designs which are simultaneously realistic and highly informative. We showcase DiffBED on a suite of preference learning tasks which demonstrate the first successful application of BED with image-scale designs. Taken together, these results highlight the potential of DiffBED as a general framework for bringing BED to complex, real-world domains.

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# A LIKELIHOOD MODELS

This section provides details for all likelihood models studied in our experiments (Section 6).

When picking an experiment paradigm, practitioners must consider the trade-off between the information conveyed in a given observation (e.g. binary preference, partial ranking), and the cost of running said experiment. For example, a full-ranking contains high amounts of information per observation, but may not be feasible to collect. We summarize the paradigms studied in our experiments in Table 1).

Table 1: Common paradigms for eliciting human feedback.

| Paradigm | Example design | Example feedback | Example Likelihood |
|---|---|---|---|
| **Binary Ranking** |  | "Image 1 $\succ$ Image 2" | Bradley–Terry (BT) (Bradley & Allan, 1952) |
| **Ranking $k$ designs from $n$** |  | "Image 1 $\succ$ Image 2 $\succ$ Image 3" | Plackett–Luce (PL) (Plackett, 1975; Luce, 1959) |
| **Discrete rating** |  | "4 out of 5 stars" | Ordinal Logit (OL) (Mccullagh, 1980) |

## A.1 LIKELIHOOD PMFS

We now provide the functional form of the likelihood models considered in our experiments. Note that all of the models leverage a latent reward model, $r_\theta(\xi)$, parametrized by the quantity of interest, $\theta$, which assigns a score $r_\theta(\xi) \in \mathbb{R}$ to the design/each element in the design set.

**Binary Preferences: Bradley-Terry (Bradley & Allan, 1952)**

Let $\xi = \{\xi_1, \xi_2\}$ be a design set of two items. The Binary Bradley-Terry model assumes,

$$p(y = \xi_i \succ \xi_j \mid \theta, \xi) = \frac{\exp(r_\theta(\xi_i))}{\exp(r_\theta(\xi_i)) + \exp(r_\theta(\xi_j))}.$$

**Partial Rankings: Plackett-Luce (Plackett, 1975)**
Let $\xi = \{\xi_1, \xi_2, \ldots, \xi_S\}$ be a design set of $S$ items. Suppose we observe a partial ranking of the form

$$\xi_{\sigma_1} \succ \xi_{\sigma_2} \succ \cdots \succ \xi_{\sigma_M}, \quad \text{with } M \leq S,$$

where $\sigma = (\sigma_1, \sigma_2, \ldots, \sigma_M)$ is an ordered list of distinct indices indicating the ranked items, and let $C_M := \xi \setminus \{\xi_{\sigma_1}, \xi_{\sigma_2}, \ldots, \xi_{\sigma_M}\}$. Then the Plackett–Luce likelihood of the observed partial ranking is

$$p(y = \xi_{\sigma_1} \succ \xi_{\sigma_2} \succ \cdots \succ \xi_{\sigma_M} \mid \theta, \xi) = \prod_{j=1}^{M} \frac{\exp\big(r_\theta(\xi_{\sigma_j})\big)}{\sum_{\xi \in C_j} \exp(r_\theta(\xi))},$$

where $C_j$ is the set of items available at stage $j$, with $C_1 = \xi$ and $C_{j+1} = C_j \setminus \{\xi_{\sigma_j}\}$.

**Discrete Ratings: Ordinal Logit (Mccullagh, 1980)** Let $\xi$ being a single item, unlike the Bradley-Terry and Plackett-Luce models, which operate on design sets. Under the Ordinal Logit model, observations are one of $K$ ordered, discrete categories, modelled under the following PMF:

$$p(y = k \mid \xi, \theta) = \sigma\Big(\tfrac{b_k - r_\theta(\xi)}{\tau}\Big) - \sigma\Big(\tfrac{b_{k-1} - r_\theta(\xi)}{\tau}\Big), \qquad k = 1, \ldots, K,$$

with $\sigma(x) = (1 + e^{-x})^{-1}$.

### A.2 Parametrisation of Latent Reward Model

As reiterated in the main body of the paper, in the high-dimensional, challenging settings considered in the paper, defining a likelihood, $p(y|\theta, \xi)$, that mimics human behaviour for all $\{\theta, \xi\}$ is extremely challenging. Further, we note that $p(y|\theta, \xi)$ can often not be directly trained in a supervised manner, and practitioners must leverage domain-specific insight. This is especially true in cases in which the $\theta$ of interest is inherently latent, e.g. user preferences. As such, we must often assume the structure of the canonical models. However, in all of the models considered above, we must still define a latent reward model, $r_\theta(\xi)$.

In many problems, e.g. preference-elicitation, the interpretable features that are most pertinent can be identified. In such settings, the following parametrization can be considered: $r_\theta(\xi) = \theta^T d(\xi) = \sum_{k=1}^{K} \theta_k d_k(\xi)$, of $K$ interpretable features, e.g. alignment to a style. In this parametrisation, $\theta$ can be viewed as interpretable preference weights for the $K$ different aspects. In other problems, where such interpretable features can not be identified, one can opt for the following parametrisation: $r_\theta(\xi) = \cos\_\text{sim}(\theta, d(\xi))$ where $d(.)$ is an encoder of $\xi$ trained in an unsupervised fashion.

A further practical benefit of these parametrisations is that they are data-efficient, arising from the incorporation of task-specific knowledge through the fixed, pre-trained feature extractors, $d(.)$, which should support faster learning. However, we stress that `DiffBED` is agnostic to the parametrisation of the latent reward model, $r_\theta(.)$, and more generally, the response paradigm and likelihood model used.

**Temperature hyper-parameter, $\tau$** In line with common practice, we restrict the range of the latent reward, $r(\xi)$, to a pre-defined range $[-1, 1]$, for example through normalisation or by computing the reward as cosine similarities, before introducing a multiplicative scaling parameter, $\tau$, to expand the range to $\left[-\tau^{-1}, \tau^{-1}\right]$. This enables explicit control over the sharpness of the assumed likelihood model's response distribution. As $\tau^{-1} \to 0$, the distribution over potential observations for any design across all the models introduced tends to a uniform distribution. On the other hand, increasing $\tau^{-1}$ results in peakier likelihoods, and faster shrinkage of the posterior. However, as it assigns a stronger belief on the data generating mechanism, if this does not reflect reality, the degree of misalignment with the true data generating process is also increased.

### A.3 Details of Latent Reward Models

In this section, we present the specific details of the latent reward models used in our experiments. In the search experiments, we leverage unsupervised encoders trained through contrastive losses, to encourage learning general representations of the data. In the preference elicitation experiment, we leverage interpretable feature extractors.

#### A.3.1 MNIST

For search, we train an encoder using the SimCLR loss (Chen et al., 2020). We leverage a simple CNN architecture, with two convolutional layers and fully-connected layer. The embedding dimensionality is $K = 32$, with a projection-head of size $P = 512$, a hyper-parameter for computing SimCLR contrastive losses. The encoder is trained for $50\,000$ steps, with a batch size of 1024. The underlying reward function used in our Bradley-Terry model is $r_\theta(\xi) = \tau^{-1}\text{cosine\_sim}(\text{simclr}(\xi), \theta)$, where simclr is our encoder. We take $\tau^{-1}$ to be 25 in Figure 4.

To explicitly incorporate model misspecification into the responses, we leverage a pre-trained discriminator that detects out-of-distribution (OOD) MNIST images. For in-distribution images, the simulated observation $y$ is from a re-normalised PMF of the rankings that don't include any OOD images, and in cases where all images are classed as OOD, the ranking observations are generated uniformly at random.

#### A.3.2 CelebA

**Search** We train a CelebA encoder on the CelebA train set. We take a pre-trained VGGFace2 model as our backbone (Cao et al., 2018), and fine-tune it. We remove the original last layer and replace it with a 64 dimensional linear last layer, hence $\theta$ is, 64 dimensional. We freeze the backbone, training only the last layer weights, before unfreezing the final block before the last layer, and fine tuning these weights alongside the last layer's weights. We train using a triplet loss, since

CelebA includes identity labels. The underlying reward function used in our Placket-Luce model is $r_\theta(\xi) = \tau^{-1}\text{cosine\_sim}(\text{vgg}(\xi), \theta)$, where vgg is our fine-tuned encoder. We take $\tau^{-1}$ to be 25. We run the experiment for 50 iterations.

**Preference Elicitation** We train a supervised feature extractor on the CelebA dataset by fitting a multi-label attribute classifier to predict the following $C = 23$ characteristics that have binary labels in the dataset:

```
Bald, Wavy_Hair, Straight_Hair, Receding_Hairline,
Bangs, Sideburns, Black_Hair, Gray_Hair, Blond_Hair,
Brown_Hair, No_Beard, 5_o_Clock_Shadow, Mustache, Goatee,
Big_Lips, Big_Nose, Eyeglasses, Smiling, Heavy_Makeup,
Wearing_Lipstick, Wearing_Necklace, Wearing_Earrings.
```

We leverage a ResNet50 model initialised with ImageNet weights, with the final layer removed and replaced with a linear layer that maps to $C = 23$. The model is trained for 25 epochs, with a batch size of 128. We use binary cross-entropy with logits, assigning per-attribute positive weights equal to the negative-to-positive sample ratio to correct for class imbalance, and Adam as the optimizer.

We use a Bradley-Terry model, with underlying reward being $r_\theta(\xi) = \tau^{-1} \sum_{i=1}^{N} d_i(\xi) \cdot \theta_i$, where $d(\xi) \in \mathbb{R}^{|C|}$ is a vector with element $d_i(\xi)$ being the ResNet50 classifier probability that attribute $i$ is present in a design image.

### A.3.3 ZAPPOS

We train a Zappos encoder using the SimCLR loss, with $K = 64$ and $P = 512$. We leverage a ResNet50-based model and initialized with torchvision's retrained ImageNet-1K (Deng et al., 2009) weights[1], with the final fully connected (FC) layer removed and replaced by a linear projection to a $K$ embedding space. The model is trained 50,000 steps, with a batch size of 256, a learning-rate of 1, and with SGD as the optimizer. We utilise an Ordinal-Logit model with an underlying reward $r_\theta(\xi) = \tau^{-1}\,\text{cos\_sim}(\text{simclr}(\xi), \theta)$, where simclr is our simclr encoder, and $\theta$ is the simclr embedding of the ground truth reference image.

## B DIFFBED DETAILS

This section contains the algorithmic details needed to implement `DiffBED` in practice. In Algorithm 1, we provide pseucodode which describes how `DiffBED` is applied end-to-end for (sequential) BED problems.

### B.1 REFERENCE MODELS

For each experiment, we require a reference diffusion model $p^{\text{ref}}(\xi)$ whose samples produce reasonable designs for the problem at hand. We detail our specific choices for each dataset here.

**MNIST** We use the training script provided in the PyTorch codebase provided by Song et al. (2021)[2] to train an unconditional MNIST diffusion model. We use an NCSN++ UNet (64 base channels, one residual block per level) with a continuous VP-SDE noise schedule and EMA (0.999). We train for 500k iterations with a batch size of 256, using the Adam optimizer ($lr = 0.0002$, with gradient clipping at norm$= 1.0$).

**CelebA and Zappos** For the higher dimensional datasets, CelebA (Liu et al., 2015) and Zappos (Yu & Grauman, 2014), we leverage the Hugging Face `diffusers` library[3], which provides standardized pipelines for training, inference, and sampling of diffusion and latent diffusion models.

[1] https://pytorch.org/vision/stable/models.html
[2] https://github.com/yang-song/score_sde_pytorch
[3] https://huggingface.co/docs/diffusers

**Algorithm 1** `DiffBED`: BED with Information Guided Diffusion

**Input:** **BED setup:** prior $p(\theta)$; likelihood $p(y \mid \theta, \xi)$; experiment steps $K$
**Input:** **Diffusion:** reference score model $s_\varphi^{\text{ref}}$; SDE steps $T$; guidance scale $\alpha$
**Input:** **Inference:** particle count $N$; particle filter;
**Output:** Designs $\xi_{1:K}$, observations $y_{1:K}$, particles $\{\theta_n^{(K)}\}_{n=1}^N$;

**Initialize:** draw $\{\theta_n^{(0)}\}_{n=1}^N \sim p(\theta)$; set $\xi_{1:0} \leftarrow \emptyset$, $y_{1:0} \leftarrow \emptyset$.
**for** $k = 1, \ldots, K$ **do** ▷ Sequentially design and run each experiment
  **— Diffusion-based design sampling —**
    $\xi^{(T)} \sim \mathcal{N}(0; I)$ ▷ Initialize at noise
    **for** $t = T, T-1, \ldots, 1$ **do**
      $g_t \leftarrow \nabla_{\xi_t} \widehat{\text{EIG}}\big(\widehat{\xi}_0(\xi_t)\big)$ ▷ Estimate EIG gradient using $\{\theta_n^{(k-1)}\}$
      $\xi_{t-1} \leftarrow \text{SDEstep}(\xi_t, s_\varphi^{ref}(\xi_t, t), g_t, \alpha)$ ▷ SDESolver step
    **end for**
    Set design $\xi_k \leftarrow \xi_0$
  **— Run experiment and update posterior —**
    $y_k \leftarrow y \sim p(y \mid \theta^\star, \xi_k)$
    $\xi_{1:k} \leftarrow \xi_{1:k-1} \cup \{\xi_k\}$, $y_{1:k} \leftarrow y_{1:k-1} \cup \{y_k\}$
    $\{\theta_n^{(k)}\} \leftarrow \text{ParticleFilter}\big(\{\theta_n^{(k-1)}\}, \xi_{1:k}, y_{1:k}\big)$
**end for**
**return** $\xi_{1:K}, y_{1:K}, \{\theta_n^{(K)}\}$

For CelebA, we use a pre-trained latent diffusion model (Rombach et al., 2022) checkpoint.[4] For Zappos, we use a fine-tuned version of Stable Diffusion v1.5 (SDv1.5). [5]

### B.2 Sampling

We now turn to the details involved in sampling from $p^*(\xi)$ using Equation (12). In particular, Shen et al. (2024) considers the shortfalls of training-free guidance of diffusion models and leverage ideas from optimization literature to mitigate them. We find that Polyak step-size parametrisation of the guidance scale is beneficial in finding a favourable trade-off between the informativeness and realism of designs. Namely, this considers a time-dependent guidance scale as a multiplier of the EIG gradient estimator, which we denote as $\gamma_t$ for brevity, during the reverse-process:

$$\alpha^{-1}(t) = \eta \cdot \frac{\|\epsilon_\varphi(\xi_t, t)\|}{\|\gamma_t\|_2^2}. \tag{13}$$

Across all experiments, we use the Euler–Maruyama discretization of the reverse SDE, equivalent to the ancestral/DDPM sampler. We provide further dataset-specific sampling hyper-parameters below. We use uniform time-steps on all datasets, with 500/250/100 steps on MNIST/CelebA/Zappos, respectively. The choice of the $\eta$ is an empirical one, determined by the robustness of the reference diffusion model (Ye et al., 2024). We set this parameter by visually inspecting a small set of samples for increasing values of $\eta$, setting the maximal value that still consistently produces high-fidelity images. We use $\eta = 0.0375, 0.10$ for CelebA/Zappos experiments, and present example samples produced at this guidance scale in Figure 8 and Figure 6.

As SDv1.5 is a text-conditioned model, we use the following prompt to capture the data-distribution of interest for the Zappos task: ``Studio product photo of a footwear, isolated on white background, high detail''. To avoid artefacts, we also use the following negative prompt: ``blurry, low resolution, watermark, deformed''.

[4] https://huggingface.co/CompVis/ldm-celebahq-256
[5] https://huggingface.co/benisonjac/finetune-of-stable-diffuson-on-Zappos-shoe-dataset

### B.3 Diffusion on Sets

In some applications, we may have access to a diffusion model producing single designs, but our task calls for *sets* of designs. We consider several applications of this nature in Section 6. Our `DiffBED` framework developed in Section 4 can be extended to this setting. In particular, designs are now sets $\xi = \{\xi_1, \dots, \xi_J\}$ of $J$ elements. We extend $p^{\text{ref}}$ to be a set-valued distribution by assuming independence of the elements, i.e., $p^{\text{ref}}(\xi) \propto \prod_{j=1}^{J} p^{\text{ref}}(\xi_j)$.

During the reverse diffusion process, we now maintain a noisy set $\xi_t = \{\xi_{1,t}, \dots, \xi_{J,t}\}$. We can then write the reverse diffusion process for each individual element $\xi_{j,t}$ as

$$d\xi_{j,t} = \Big[ f(\xi_t, t) - g(t)^2 \Big( s_\varphi(\xi_{j,t}, t) + \alpha^{-1} \nabla_{\xi_{j,t}} \text{EIG}(\widehat{\xi}_0(\xi_t)) \Big) \Big] \, \mathrm{d}t + g(t) \, \mathrm{d}\overleftarrow{W}_{j,t}, \qquad j = 1, \dots, J,$$

where $\widehat{\xi}_0(\xi_t) = \{\widehat{\xi}_0(\xi_{1,t}), \dots, \widehat{\xi}_0(\xi_{J,t})\}$ is the set of element-wise conditional means and $\mathrm{d}\overleftarrow{W}_{j,t}$ are independent Brownian increments.

Intuitively, our information-guided set diffusion acts as an interacting particle system. The diffusion prior contributes an independent score update for each element, ensuring realism, while the EIG gradient term $\nabla_{\xi_{j,t}} \text{EIG}(\xi_t)$ introduces cross-element coupling, ensuring informativeness of the entire set as a design.

## C Posterior Inference

We now present details on how we conduct inference on the embedding space during active experimentation. In search problems, as the encoders are trained with a cosine-similarity objective, both our likelihoods and the geometry of the problem depend only on the *direction* of $\theta$, not its scale. Similarly, in preference elicitation settings, we often want to learn normalized preference weights [6], in order to allow for explicit control and regularisation over the sharpness of the preference distributions, for example through a scaling hyper-parameter.

In such settings, although $\theta$ lives in $\mathbb{R}^D$, the unit-length constraint removes one degree of freedom, leaving an intrinsic dimension of $D-1$. Accordingly we place a *uniform prior* on the unit sphere $\mathbb{S}^{D-1} = \{\theta \in \mathbb{R}^D : \|\theta\|_2 = 1\}$ the $(D-1)$-dimensional manifold of $D$-dimensional vectors of length one. We then explicitly approximate the posterior on the unit sphere.

**Particle-Based Inference** At the start of the experimentation we draw an i.i.d. set of particles $\{\theta_i^{(0)}\}_{i=1}^N \sim \text{Unif}(\mathbb{S}^{D-1})$ to represent this prior. At each experiment index $k$, after observing an outcome $y_k$ at design $\xi_k$, we update particle weights according to the likelihood

$$\log w_i^{(k)} = \log w_i^{(k-1)} + \log p(y_k \mid \theta_i^{(k-1)}, \xi_k).$$

Weights are normalized and particles are resampled via multinomial resampling to prevent degeneracy (Doucet et al., 2001), yielding an empirical posterior approximation $\{\theta_i^{(t)}\}$.

To maintain diversity and ensure that the particle cloud accurately tracks the true posterior on the sphere, we rejuvenate the particles by applying a *projected unadjusted Langevin algorithm* (ULA) on $\mathbb{S}^{D-1}$:

$$\theta \leftarrow \text{Normalize}\Big( \theta + \frac{\epsilon}{2} P_\theta \nabla_\theta \log \pi_k(\theta) + \sqrt{\epsilon}\, P_\theta \eta \Big),$$

where $P_\theta = I - \theta\theta^\top$ projects gradients and noise onto the tangent space $T_\theta \mathbb{S}^{D-1}$ and $\eta \sim \mathcal{N}(0, I)$. This step can be viewed as an unadjusted discretization of the Riemannian Langevin diffusion on $\mathbb{S}^{D-1}$ (Girolami & Calderhead, 2011; Patterson & Teh, 2013), where the drift term is the gradient of the *full current posterior* $\pi_k(\theta) \propto \pi_0(\theta) \prod_{s=1}^{k} p(y_s \mid \theta, \xi_s)$, so that each move incorporates all experimental observations up and including experiment index $k$.

**Computational Cost** As the log-likelihoods are parametric functions of simple vector products, i.e. cosine-similarities, between $\theta$ and encodings of previous designs, both resampling and Langevin

[6] Another alternative is to learn weights that sum to one.

Figure 8: Example `DiffBED` designs for the CelebA search problem.

steps are very efficient.[7] Crucially, resampling and Langevin steps do not require expensive neural network evaluations per $\theta$ particle. For all experiments, we leverage $N = 10^6$ particles, take 100 Langevin steps, and have step-size $\epsilon = 10^{-4}$. Note that the cost of storing $N = 1000000$ particles of dimensionality $D = 32, 64$ has costs $\approx 122, 244$ MiB of memory, which is a negligible overhead on modern GPUs.

# D Additional Experiments

This section contains additional experiments and ablations not discussed in the main paper.

## D.1 CelebA

**Example DiffBED Designs: CelebA** Figure 8 shows 100 example images generated by `DiffBED` and Figure 9 shows the same for Entropy. This serves as a qualitative evaluation of our designs. Both are similarly high-quality images as they leverage the same underlying diffusion model, although with different guidances. On the other hand, the designs produced by standard BED (Figure 10) are imperceptible from pure noise, despite their high EIG values.

**Ablations** In Figure 11 we present results across the two extra values of the likelihood temperature parameter $\tau^{-1} = \{25, 50\}$, in addition to the value of $\tau^{-1} = 10$ used for CelebA in the main body of the paper. Larger values of $\tau^{-1}$ indicate less noise in the observation process, i.e., more informative outcomes, We see that larger $\tau^{-1}$ indeed leads to larger EIG values and a larger gap to the random baseline.

Here, we also present the performance of the naive BED baseline under data simulated from the assumed model which we call BED (assumed). That is, we sample $y \sim p(y \mid \theta, \xi)$ from the misspecified model likelihood, with no adjustments to the fact that the resulting designs may be meaningless. We see that BED (sssumed) achieves both high EIG scores and cosine similarities in this case. However, the designs produced by BED in this case are imperceptible from pure noise (Figure 10) and could not be used in a real-world experiment. As soon as we sample data $y$ from a more realistic likelihood which returns uninformative data when the designs are pure noise, the cosine similarity of the naive approach (BED) drops to near zero, indicating a failure to determine the correct $\theta$.

[7] Note that embeddings of designs/design sets can be cached, and as such, just needs to be computed once. For the rest of the roll-out, it can be shared across all particles for resampling and Langevin-step computation.

Figure 9: Example *Entropy* designs for the CelebA search problem.

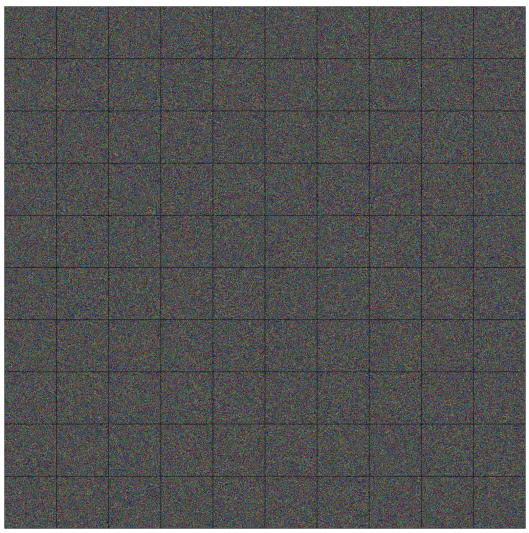
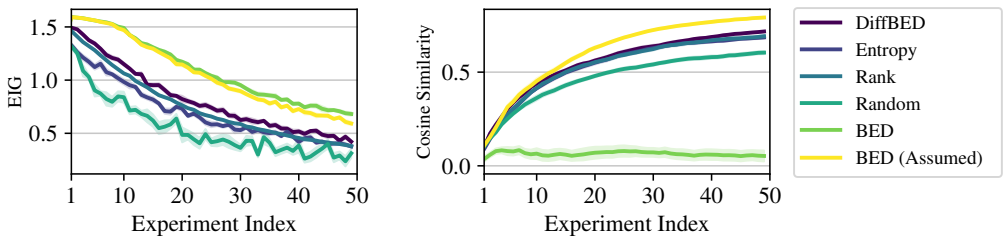
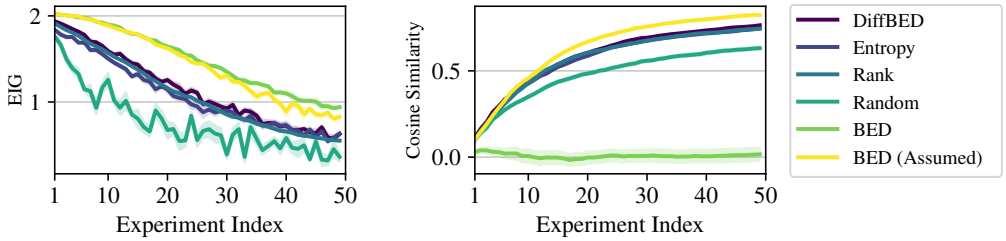


Figure 10: Example standard BED designs for the CelebA search problem.




(a) $\tau^{-1} = 25$




(b) $\tau^{-1} = 50$

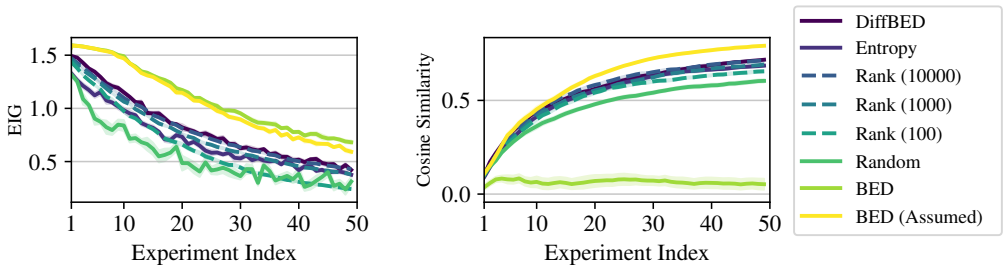
Figure 11: EIG and cosine similarity values for CelebA on the search problem, where outcomes are top-2 ranks of the images in the set of four design images. We now vary the value of $\tau$ used in the likelihood. Means are plotted with shaded regions indicating one standard error.

In a second ablation (at $\tau^{-1} = 25$) we study the effect of the number of the candidate designs considered in the *Rank* method. We plot the performance with $N = 100$, and $N = 10000$ candidate designs, alongside the $N = 1000$ set-up used in the main body of the paper. See Figure 12. Unsurprisingly, the performance of this baseline is a monotonic function of the pool size. However, increasing the pool size also comes with additional costs, especially when the pool is itself generated from a model, in which case $N = 10000$ would be significantly more time consuming than `DiffBED` while not exceeding its performance.

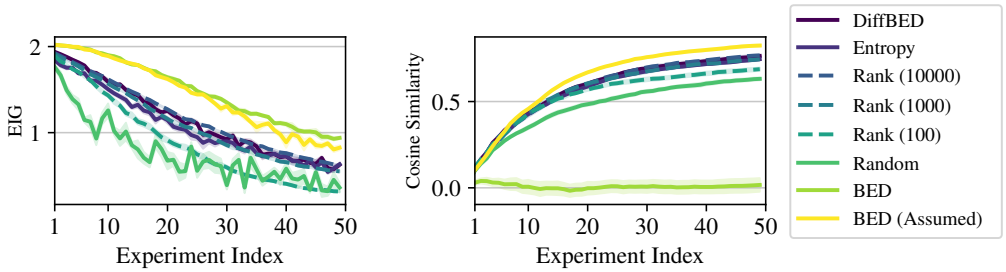
### D.2 ZAPPOS

**Example DiffBED Designs: Zappos** We present 100 example designs produced by `DiffBED` on the Zappos discrete rating problem. See Figure 13.

**Ablations** We additionally present in Figure 15 results for $N = 10$ levels of discrete ratings, rather than $N = 5$ used in Section 6.3. Intuitively, we might expect that a more fine-grained rating would be more informative. Indeed, comparing against Figure 7, using $N = 10$ yields slightly higher cosine similarities.




(a) $\tau^{-1} = 25$




(b) $\tau^{-1} = 50$

Figure 12: EIG and cosine similarities as we the number of candidate designs consider by the *Rank* baseline in the CelebA search problem. Means are plotted with shaded regions indicating one standard error.

Figure 13: Example `DiffBED` designs for the Zappos discrete rating problem.

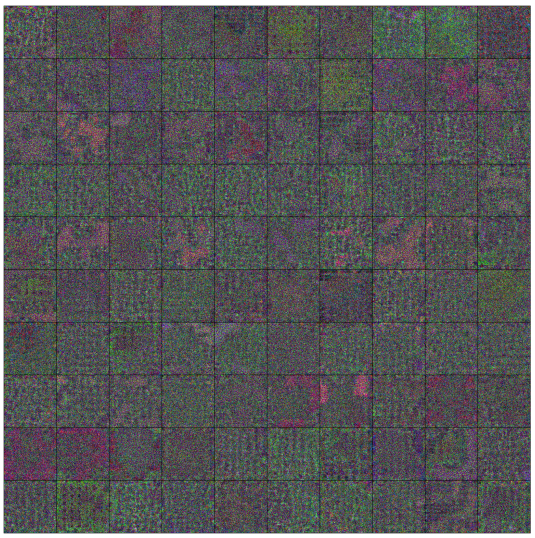


Figure 14: Example standard BED designs for the Zappos discrete rating problem.

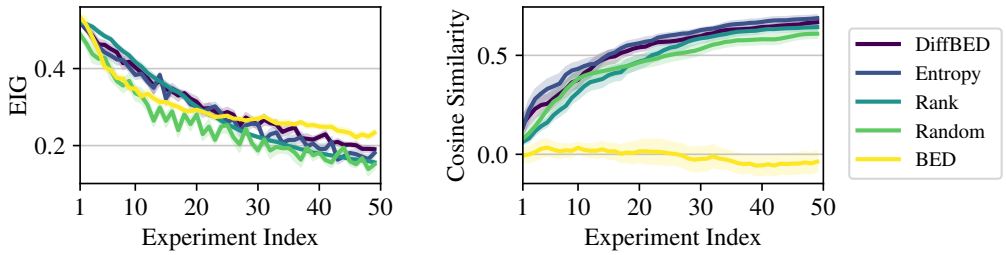



Figure 15: Quantitative results on the Zappos dataset, where designs are single images and outcomes are discrete ratings now on a scale from 1-10. Means are plotted with shaded regions indicating one standard error.