Learning Adverbs with Spectral Mixture Kernels

Anonymous ACL submission

Abstract

 For humans and robots to collaborate more in the real world, robots need to understand hu- man intentions from the different manner of their behaviors. In our study, we focus on the meaning of adverbs which describe human mo- tions. We propose a topic model, Hierarchi- cal Dirichlet Process-Spectral Mixture Latent Dirichlet Allocation, which concurrently learns the relationship between those human motions **and those adverbs by capturing the frequency** kernels that represent motion characteristics and the shared topics of adverbs that depict such motions. We trained the model on datasets we made from movies about "walking" and 015 "dancing", and found that our model outper- forms representative neural network models in terms of perplexity score. We also demonstrate our model's ability to determine the adverbs for a given motion and confirmed that the model predicts more appropriate adverbs.

⁰²¹ 1 Introduction

 With technological innovations in artificial intel- ligence, the widespread use of household robots that collaborate with humans to assist them in their daily lives is becoming a reality. In order to collaborate with humans, it is important for robots to share and understand their experiences through language, because language is the most convenient communication tool capable of con- veying human experience and knowledge. With this background, research on language use by robots in the real world has been actively stud- ied [\(Taniguchi et al.,](#page-9-0) [2019;](#page-9-0) [Tellex et al.,](#page-9-1) [2020;](#page-9-1) [Kalinowska et al.,](#page-8-0) [2023;](#page-8-0) [Karamcheti et al.,](#page-8-1) [2023\)](#page-8-1). Significantly, within this domain, Large-scale language models (LLMs) such as OpenAI's ChatGPT[1](#page-0-0) and Google's PaLM [\(Chowdhery et al.,](#page-8-2) [2022\)](#page-8-2) are also used to control robots. ChatGPT is used to exe- cute various types of robotics tasks [\(Vemprala et al.,](#page-9-2) [2023\)](#page-9-2), and PaLM-SayCan [\(Ahn et al.,](#page-8-3) [2022\)](#page-8-3) and

036

PALM-E [\(Driess et al.,](#page-8-4) [2023\)](#page-8-4) have been developed **041** [b](#page-9-3)ased on PaLM [\(Chowdhery et al.,](#page-8-2) [2022\)](#page-8-2). [Singh](#page-9-3) **042** [et al.](#page-9-3) [\(2023\)](#page-9-3) and [Huang et al.](#page-8-5) [\(2022\)](#page-8-5) have pro- **043** posed methodologies for generating task plans for **044** robots that employ LLM. Their approach conveys **045** robot's motion plans through a chain-of-thought **046** framework [\(Wei et al.,](#page-9-4) [2022\)](#page-9-4). Though it is good **047** at describing in language the general plan of ac- **048** tion of a robot in accomplishing a specific task, **049** the language description does not capture the pre- **050** cise correspondence between nuanced expressions **051** and the actual robot behaviors in the real world. **052** Furthermore, the focus of their studies is not on **053** the verbal representation of the behaviors of the **054** observed object by a robot, but on the robot's ac- **055** tion plan. On the other hand, research is being **056** conducted to elucidate the relationship between **057** motions and the natural language that describes **058** them. Bidirectional conversion models from natu- **059** ral language descriptions to motions, or vice versa, **060** [u](#page-9-5)sing sequence-to-sequence (Seq2seq) [\(Sutskever](#page-9-5) **061** [et al.,](#page-9-5) [2014\)](#page-9-5) learning have been proposed by [Ya-](#page-9-6) **062** [mada et al.](#page-9-6) [\(2018\)](#page-9-6); [Plappert et al.](#page-9-7) [\(2018\)](#page-9-7); [Ito et al.](#page-8-6) **063** [\(2022\)](#page-8-6). Though these models can achieve bidirec- **064** tional conversion between language and motion **065** sequences, the relation between motions and lan- **066** guage is learned as sequence patterns and lacks in **067** learning the correspondence between the manner of **068** motions and the language that represent them. Fur- **069** thermore, in the conventional research the focus has **070** predominantly revolved around finite motions, such **071** as "take" and "put", which were preconceived by **072** humans, thereby neglecting the pursuit of method- **073** ologies that facilitate the adaptable modulation of **074** multiple motions contingent upon contextual cues. **075** For the advancement of robotics, it becomes imper- 076⁰⁷⁶ ative to comprehensively and statistically grasp the **077** repertoire of "motions" that humans genuinely ex- **078** hibit, as well as discern the variations in individual 079 characteristics and contextual nuances associated **080** with those "motions". These insights should be 081

¹ https://chat.openai.com.

 aptly assimilated within the robotic systems. Build- ing upon the aforementioned, we shall address this challenge by casting our focus on adverbs, while establishing correspondence between motions and adverbs that represent them.

 Limited research has been conducted thus far to delve into the semantic comprehension of ad- verbs. Notable instances within this domain in- clude the Three-Stream Hybrid Model [\(Pang et al.,](#page-9-8) [2018\)](#page-9-8), which employs Long Short-Term Mem- ory (LSTM) [\(Hochreiter and Schmidhuber,](#page-8-7) [1997\)](#page-8-7) and inceptionV3 [\(Szegedy et al.,](#page-9-9) [2016\)](#page-9-9) to acquire knowledge related to adverbs. Additionally, Action Modifiers [\(Doughty et al.,](#page-8-8) [2020\)](#page-8-8), which employ an I3D network [\(Carreira and Zisserman,](#page-8-9) [2017\)](#page-8-9) and scaled dot-product attention [\(Vaswani et al.,](#page-9-10) [2017\)](#page-9-10) to discern the impact of adverbs on motion sequences. These models employ image features derived from videos, such as RGB and optical flow [\(Simonyan and Zisserman,](#page-9-11) [2014\)](#page-9-11), as repre- sentations of motions. However, these represen- tations fail to capture the intrinsic essence of the motions themselves; these models models are capa- ble of classify videos annotated adverbs by learn- ing RGB or optical flow, but they are unable to discern the component of motions denoted by the adverb. Therefore, unlike conventional research ap- proaches, in this study, we focus on the frequency components that make up human motion and at- tempt to express the motion by those components. By doing so, we aim to enable the robot to under- stand the meaning of adverbs related to motions such as "cut *roughly*", etc.

¹¹⁵ 2 Joint Topic Model of Motions and **¹¹⁶** Adverbs

 We propose a new topic model, Hierarchical Dirich- let Process-Spectral Mixture Latent Dirichlet Allo- cation (HDP-SMLDA) to capture the relationship between the frequency components of human mo-tions and the adverbs that describe motions .

122 The model makes it statistically possible to es-**123** tablish a correspondence between adverbs and nu-**124** ances associated with motions.

 This enables the control of robot actions through verbal instructions, such as "handle *with more cau- tion*" or "cut *roughly*", and it is also possible to make the robot understand human intentions due to slightly different manner of movement. On the contrary, from the perspective of natural language processing, it has been impossible to express the actual meaning behind words like "*freely*" or "*flexi-* *bly*". However, the integration with robotics makes **133** it possible for the first time to represent their mean- **134** ing, allowing not only the description of actions **135** through language but also the generation of actions **136** from language cues. **137**

2.1 Human Motion Representation **138**

Since human motion is represented as a smooth **139** [t](#page-9-12)rajectory, we use a Gaussian process (GP) [\(Ras-](#page-9-12) **140** [mussen and Williams,](#page-9-12) [2006\)](#page-9-12), which is defined as 141 a distribution over functions, to describe the mo- **142** tions. In a GP, the kernel function $k(x, x')$, which 143 determines the similarity between two data points **144** (x, x') , is applied to the data set to compute the co- 145 variance matrix and estimate the predictive distribu- **146** tion. The choice of kernel function is an important **147** factor that affects the behavior and performance of **148** the GP model. GP models are primarily used for re- **149** gression and classification, fundamental techniques **150** that are also widely used by the natural language **151** processing community [\(Cohn et al.,](#page-8-10) [2014\)](#page-8-10). **152**

2.2 Frequency components in a motion **153**

Wilson et al. [\(Wilson and Adams,](#page-9-13) [2013\)](#page-9-13) introduced 154 a technique known as the Spectral Mixture kernel **155** (SM kernel), which enables automatic learning of **156** a mixed kernel from data by considering a com- **157** bined Gaussian distribution in the Fourier domain. **158** This approach surpasses the limitation of utilizing **159** pre-existing bases or their combinations in Gaus- **160** sian processes. As a fundamental component of **161** the Gaussian process, we consider a radial basis **162** function $k(\tau)$ that solely depends on $\tau = x - x'$ According to Bochner's theorem [\(Bochner et al.,](#page-8-11) **164** [1959;](#page-8-11) [Stein,](#page-9-14) [1999\)](#page-9-14), any $k(\tau)$ can be expressed in 165 the following equation: **166**

$$
k(x, x') = k(\tau) = \int_{\mathbb{R}} e^{2\pi i s^{\mathrm{T}} \tau} \psi ds. \tag{1}
$$

. **163**

As $k(\tau)$ is considered equivalent to probability density $\psi(s)$ in the frequency domain, we consider a 169 mixture of Gaussian distributions for $\psi(s)$. Each 170 component of the Gaussian distributions is equiva- **171** lent to considering the following basis function in **172** the original domain: **173**

$$
k(\tau|\sigma,\mu) = \exp(-2\pi^2 \tau^2 v^2) \cos(2\pi \tau \mu). \tag{2}
$$

Thus, we are considering a mixture of M basis 175 functions as the basis. Here, μ_m^q and v_m^q represent 176 the mean and variance, respectively, of the q -th 177 dimension of the input X in the m-th basis: 178

Figure 1: Nonlinear dimensionality reduction of motions achieved through GPLVM. The trajectories corresponding to three distinct walking motions (a)-(c) are portrayed in the latent space of three dimensions (thus, we set $Q = 3$ in Equation [3\)](#page-1-0), denoted as X.

Figure 2: The motions depicted in Figure [1](#page-2-0) were analyzed using the SM kernel. The vertical and horizontal axes respectively represent the probability density and mean of the estimated four Gaussian distributions (thus, we set $M = 4$ in Equation [3\)](#page-1-0).

$$
k(\tau) = \sum_{m=1}^{M} w_m \cos(2\pi \tau^{\mathrm{T}} \mu_m) \prod_{q=1}^{Q} \exp(-2\pi^2 \tau_q^2 v_m^q)
$$
\n(3)

 The weights parameter **w**, mean μ , and variance \boldsymbol{v} can be learned through hyperparameter optimiza- tion of Gaussian processes. We employ this method to extract M frequency components (represented 184 by the mean μ) that are expected to be relevant to adverbs from the three-dimensional latent vari-186 able X obtained through GPLVM for each motion. These components are then used as observed values that capture the characteristics of the motions. It is worth noting that while the trajectory in X can be directly Fourier transformed, doing so would not allow us to distinguish between the function passing through particular points (the *phase* of the function) and the *features* of the function itself.

194 2.3 Hierarchical Dirichlet Process-Spectral **195** Mixture LDA

 The extracted frequency components from the mo- tions are assumed to be associated with the adverbs assigned to those motions. By employing Gaussian-Multinomial LDA (GM-LDA) [\(Blei and Jordan,](#page-8-12)

Figure 3: The graphical model of HDP-SMLDA. K^+ represents the variable number of topics. At each iteration of training, the hyperparameter α is estimated based on the size of the dataset, ensuring flexibility in the model.

 $\binom{q}{m}$. components. In our study, we set $Q = 3$ because 215 [2003\)](#page-8-12), we can cluster the frequency components **200** and adverbs simultaneously into topics, thereby **201** identifying frequency components that are likely **202** to co-occur with a given adverb. It is important to **203** note that GM-LDA requires the number of topics **204** K to be known in advance. However, the num-
205 ber of topics is typically unknown, and assuming **206** prior knowledge of this parameter is a significant **207** limitation. To address this issue, we propose the Hi- **208** erarchical Dirichlet Process Spectral Mixture LDA **209** (HDP-SMLDA), which automatically estimates the **210** number of topics from the data by incorporating a **211** hierarchical Dirichlet process into GM-LDA. The **212** graphical model, as depicted in Figure [3,](#page-2-1) considers **213** Q as the number of dimensions of the frequency **214** the data processed by GPLVM is three-dimensional. **216** The number of kernel mixtures M in the Spectral **217** Mixture (SM) kernel discussed in the previous sec- **218** tion is denoted as M_d in this model. Adverbs are **219** sampled from a categorical distribution, while the **220** frequency component is treated as continuous data, **221** assuming a Gaussian distribution as the prior distri- **222** bution. Let us assume the existence of a potential **223** topic distribution θ_d for each motion d. The dimensionality of the topics, denoted as K, is variable, 225 allowing for flexibility. The generation process of **226** the adverb w_{dn} $(n = 1, \ldots, N_d)$ and the frequency 227 component x_{dm} $(d = 1, ..., D; m = 1, ..., M_d)$ 228 associated with the motions is outlined as follows: **229** 1. Draw $G_0 \sim \text{DP}(\gamma, H)$. 230 2. For $d = 1...D$, 231 $-$ Draw $θ_d$ ∼ DP($α$, G_0). 232 3. For $n = 1...N_d$, 233

 $-$ Draw z_{dn} ∼ θ_d 234

- Draw
$$
w_{dn} \sim \phi_{z_{dn}}
$$
.

4. For $m = 1...M_d$, 236 $-$ Draw $u_{dm} \sim θ_d$ 237

$$
- \text{Draw } y_{dm} \sim v_d
$$

- Draw $x_{dm} \sim \mathcal{N}(\mu_{y_{dm}}, \sigma_{y_{dm}}^2).$

239 In the generative process, ϕ_k represents the categor- ical distribution of the adverb corresponding to the **b** k -th topic, while $\mathcal{N}(\mu_k, \sigma_k^2)$ denotes the Gaussian distribution of the frequency component associated 243 with the same topic. The topic distribution θ is calculated based on the information from both the adverbs and frequency components. This topic dis- tribution is then utilized to assign topics to each adverb and frequency component iteratively for each motion d.

249 Sampling Topics of Adverbs and Frequencies

 [W](#page-8-13)e employ collapsed Gibbs sampling [\(Griffiths](#page-8-13) [and Steyvers,](#page-8-13) [2004\)](#page-8-13) as the learning algorithm for estimating the topic distribution of adverbs and frequencies in the HDP-SMLDA.

 Sampling topics of adverbs Let T represents 255 the set of table assignments and ℓ denotes the ta- ble number. According to the Chinese restaurant **process [\(Teh et al.,](#page-9-15) [2006\)](#page-9-15), the topic** z_{dn} **assigned** 258 to the adverb w_{dn} is determined by sampling the **occupied table** T_{dn} using the following formula. **Here,** ℓ_{used} and ℓ_{new} correspond to existing and **new tables,** L_k and L represent the number of ta- bles assigned to topic k and the total number of tables, respectively, and V signifies the number of vocabularies:

266

267

273

$$
\begin{array}{c}\n\cdot \\
\cdot \\
\cdot\n\end{array}
$$

265
\n
$$
p(t_{dn} = \ell | \mathbf{W}, \mathbf{T}_{\setminus dn}, \mathbf{Z}, \mathbf{Y}, \alpha, \gamma, \eta)
$$
\n266
\n
$$
\propto \begin{cases}\np(t_{dn} = \ell_{used}) | \mathbf{W}, \mathbf{T}_{\setminus dn}, \mathbf{Z}, \mathbf{Y}, \alpha, \gamma, \eta) \\
p(t_{dn} = \ell_{new}) | \mathbf{W}, \mathbf{T}_{\setminus dn}, \mathbf{Z}, \mathbf{Y}, \alpha, \gamma, \eta) \\
\propto \begin{cases}\n(N_{dl} \setminus dn + \sum_{q=1}^{Q} M_{dl}^{q}) \frac{N_{kw_{dn} \setminus dn} + \eta}{N_{k} \setminus dn + \eta V} \\
\sum_{k=1}^{K} \frac{\alpha L_{k}}{L + \gamma} \frac{N_{kw_{dn} \setminus dn} + \eta}{N_{k} \setminus dn + \eta V} + \frac{\alpha \gamma}{L + \gamma} \frac{1}{V}.\n\end{cases}
$$
\n(4)

268 The following formula is employed to sample the 269 topics assigned to the new table. Here, k_{used} refers **²⁷⁰** to existing topics, while knew represents new top-**271** ics:

272
\n272
\n273
\n274
\n
$$
p(z_{dl} = k|\mathbf{W}_{\backslash dn}, \mathbf{T}, \mathbf{Z}_{\backslash dl}, \alpha, \gamma, \beta)
$$
\n
$$
\propto \begin{cases}\np(z_{dl} = k_{used}|\mathbf{W}_{\backslash dn}, \mathbf{T}, \mathbf{Z}_{\backslash dl}, \alpha, \gamma, \beta) \\
p(z_{dl} = k_{new}|\mathbf{W}_{\backslash dn}, \mathbf{T}, \mathbf{Z}_{\backslash dl}, \alpha, \gamma, \beta) \\
\propto \begin{cases}\nL_k \frac{N_{kw_{dn}} + \eta}{N_k \backslash dn + \eta V} \\
\gamma \frac{1}{V}\n\end{cases}.\n\end{cases} \tag{5}
$$

275 The hyperparameter η is iteratively updated us-**276** ing the Fixed-Point Iteration method[\(Minka,](#page-9-16) [2003\)](#page-9-16)

based on the following equation: **277**

$$
\eta' = \eta \frac{\sum_{k=1}^{K} \sum_{v=1}^{V} \Psi(N_{kv} + \eta) - KV\Psi(\eta)}{V \sum_{k=1}^{K} \Psi(N_k + \eta V) - KV\Psi(\eta V)}.
$$
\n(6)

279

(8) **288**

Sampling topics of frequencies The topic y_{dm} 280 assigned to the frequency component x_{dm} is sam- 281 pled using the following equation: **282**

$$
p(t_{dm} = \ell | \boldsymbol{W}, \boldsymbol{T}_{\backslash dm}, \boldsymbol{Z}, \boldsymbol{Y}, \alpha, \gamma, \eta)
$$

$$
\propto \begin{cases} p(t_{dm} = \ell_{used} | \mathbf{W}, \mathbf{T}_{\backslash dm}, \mathbf{Z}, \mathbf{Y}, \alpha, \gamma, \eta) \\ p(t_{dm} = \ell_{new} | \mathbf{W}, \mathbf{T}_{\backslash dm}, \mathbf{Z}, \mathbf{Y}, \alpha, \gamma, \eta) \end{cases} \tag{284}
$$

$$
\begin{cases} (N_{dl} + \sum_{q=1}^{Q} M_{dl \backslash dm}^{q}) f(x | \mu_{k}, \sigma_{k}^{2}) \end{cases}
$$

$$
\propto \begin{cases} (N_{dl} + \sum_{q=1}^{Q} M_{dl\backslash dm}^{q}) f(x|\mu_k, \sigma_k^2) \\ \sum_{k=1}^{K} \frac{\alpha L_k}{L + \gamma} f(x|\mu_k, \sigma_k^2) \\ + \frac{\alpha \gamma}{L + \gamma} f(x|\mu_{k_{new}}, \sigma_{k_{new}}^2), \end{cases}
$$
 (7)

$$
p(z_{dl} = k | \mathbf{X}_{\setminus dm}, \mathbf{T}, \mathbf{Y}_{\setminus dl}, \alpha, \gamma, \beta)
$$

$$
\propto \begin{cases} p(z_{dl} = k_{used} | \mathbf{X}_{\setminus dm}, \mathbf{T}, \mathbf{Y}_{\setminus dl}, \alpha, \gamma, \beta) \\ p(z_{dl} = k_{new} | \mathbf{X}_{\setminus dm}, \mathbf{T}, \mathbf{Y}_{\setminus dl}, \alpha, \gamma, \beta) \end{cases} \tag{287}
$$

$$
\propto \left\{ \begin{array}{l} L_k f(x|\mu_k, \sigma_k^2) \\ \gamma f(x|\mu_{k_{new}}, \sigma_{k_{new}}^2). \end{array} \right. \tag{8}
$$

The variance parameter σ^2 of the Gaussian distri-
289 bution is learned as a fixed value. To ensure that **290** the Gaussian distribution is evenly distributed over **291** the data range, we calculate σ using the following 292 equation. This is done because the data typically **293** fall within the range of approximately -3σ to 3σ 294 when the mean is set to 0. Here, K^+ represents the 295 number of topics at the current iteration: **296**

$$
\sigma^q = \frac{\max(\mathbf{X}^q) - \min(\mathbf{X}^q)}{6K^+}.
$$
 (9)

The mean parameter μ of the Gaussian distribution **298** is sampled from the posterior distribution given **299** by the following equation. Here, λ is defined as 300 $\lambda = 1/\sigma^2$, where σ^2 represents the variance of the **301** Gaussian distribution: **302**

$$
p(\mu|\mathbf{Y}) = \mathcal{N}(\mu|m, (\beta \lambda)^{-1}). \tag{10}
$$

Let us assume that β_0 and m_0 are the parameters 304 of the prior distribution, and they are defined as **305** follows: **306**

$$
\beta = M + \beta_0, \ m = \frac{1}{\beta} \left(\sum_{m=1}^{M} x_m + \beta_0 m_0 \right). \tag{11}
$$

(a) 2D pose estimation (b) Depth estimation (c) 3D pose estimation (d) Direction normalization

[\(Cao et al.,](#page-8-14) [2021\)](#page-8-14) [\(Laina et al.,](#page-8-15) [2016\)](#page-8-15) [\(Martinez et al.,](#page-9-17) [2017\)](#page-9-17) (See text)

Figure 4: Through the four sequential procedural stages, three-dimensional human joint points data are extracted from a two-dimensional video.

To estimate the mean $\mu_{k_{new}}$ **for the Gaussian dis-** tribution associated with the new topic directly is not possible since there is no data belonging to the cluster. To address this, the mean is sampled from a Gaussian distribution using suitable parameters, allowing it to be learned to some extent, and then estimated as same as the mean of existing topic.

315 Estimation of scaling parameter α

316 To better estimate the number of topics that best **317** fit the data, we adopt a gamma distribution as the **318** prior distribution for the scaling parameter α:

319
\n320
\n
$$
p(\alpha|\pi, s, Z, c_1, c_2)
$$
\n
$$
= Ga(\alpha|c_1 + K^+ - s, c_2 - \log \pi).
$$
\n(12)

321 π and *s* are sampled as follows:

322
$$
p(\pi|\alpha, s, Z, c_1, c_2)
$$

\n323 $= Beta(\pi|\alpha + 1, N + M),$ (13)

$$
325 \t p(s|\alpha, \pi, Z, c_1, c_2)
$$

$$
= Bernoulli\left(s \left| \frac{N+M}{N+M+\alpha} \right.\right) . \t (14)
$$

³²⁷ 3 Experiments

 We begin by providing a description of the datasets utilized in our experiments. We then proceed to conduct an experiment involving HDP-SMLDA, where we examine the adverbs and frequency com- ponents, and generate adverbs based on the fre-quency components within the trained model.

334 3.1 Experimental settings

335 Data set

320

324

336 We conducted an experiment utilizing a dataset 337 **b** containing walking motions called 100 Walks^{[2](#page-4-0)} and

another dataset comprising dancing motions called **338** $AIST++³$ $AIST++³$ $AIST++³$. . **339**

100 Walks 100 Walks, the video available on **340** YouTube, is in a two-dimensional format. However, 341 for our experiment, we required three-dimensional **342** pose information as input data. To overcome this **343** limitation, we divided the video into 100 segments **344** at the motion breaks and applied four different **345** methods for three-dimensional pose estimation. **346**

- 1. Estimate 2D skeletal coordinates from video **347** data using Openpose [\(Cao et al.,](#page-8-14) [2021\)](#page-8-14) (Figure **348** [4\(](#page-4-2)a)) **349**
- 2. Estimate the depth of the video per frame **350** using FCRN-depth prediction [\(Laina et al.,](#page-8-15) **351** [2016\)](#page-8-15) (Figur[e4\(](#page-4-2)b)) **352**
- 3. Estimate 3D skeletal coordinates from video **353** data using results of 1 and 2 ,and 3d-pose **354** baseline [\(Martinez et al.,](#page-9-17) [2017\)](#page-9-17) (Figure [4\(](#page-4-2)c)) **355**
- 4. Normalize human body orientation using a **356** rotation matrix (Figure [4\(](#page-4-2)d)) 357

AIST++ The AIST Dance DB [\(Tsuchida et al.,](#page-9-18) **358** [2019\)](#page-9-18) is a curated dataset consisting of original **359** dance videos. These videos have been carefully **360** selected and include dance performances accom- **361** panied by copyright-cleared music. The dataset is **362** created and maintained by the National Institute **363** of Advanced Industrial Science and Technology **364** (AIST). [Li et al.](#page-8-16) [\(2021\)](#page-8-16) conducted annotations on **365** the AIST Dance DB dataset, specifically focusing **366** on three-dimensional human keypoints and devel- **367** oped a dance generation model. These annotations **368** provide valuable information for each dance video **369** in the dataset. Additionally, they released the an- **370** notated dataset called AIST++, which consists of **371** 1,199 simple Basic Dance motions annotated with **372** three-dimensional pose information for 16 joint **373**

 2 [https://www.youtube.com/watch?v=](https://www.youtube.com/watch?v=HEoUhlesN9E) [HEoUhlesN9E](https://www.youtube.com/watch?v=HEoUhlesN9E)

³[https://google.github.io/](https://google.github.io/aistplusplus_dataset/) [aistplusplus_dataset/](https://google.github.io/aistplusplus_dataset/)

 points in the COCO format. The dataset consists of 10 different choreographies, each representing a specific genre of dance. For each choreography, there are 20 different dancers who perform the dance in the corresponding video. The dancers follow the specified choreography while dancing to genre-specific music. The music tempo varies across the dataset and is set at six different levels.

382 Annotation of adverbs

 We employed a crowdsourcing system called [4](#page-5-0) **Lancers⁴** to gather annotations from multiple an- notators for the Japanese adverbs associated with the human motions in the videos. We requested each annotator to provide as many Japanese ad- verbs as possible for human motions of each video. To ensure the quality of the annotations, we consid- ered only those adverbs that appeared at least three times across all the videos and discarded the rest as noise. For the 100 Walks dataset, we assigned 20 annotators to annotate every 100 videos. In the case of the AIST++ dataset, we assigned 5 anno- tators to annotate every 50 videos. This approach allowed us to collect a diverse range of adverbs associated with the motions while maintaining the quality of the annotations. The details of the ad- verb dataset are presented in Table [1,](#page-5-1) where the 100 Walks dataset is referred to as "walk" and the AIST++ dataset is referred to as "dance". The met- ric "average adverbs" represents the mean number of adverbs annotated per video. In comparison to data set used in prior research [\(Pang et al.,](#page-9-8) [2018;](#page-9-8) [Malmaud et al.,](#page-8-17) [2015\)](#page-8-17), we have amassed a more extensive corpus of adverbs in both datasets.

407 Calculation of direction vectors

 We utilize the direction vectors connecting each joint as input data to reconstruct the original pose information. To account for individual differences such as arm length, we compute unit vectors. For the 100 Walks dataset, we compute 16 direction vectors, while for the AIST++ dataset, we com- pute 14 direction vectors. The resulting vectors are then combined, with their three-dimensional coordinates arranged in the column direction for

⁴<https://www.lancers.jp/>

	Videos	Adverbs	average adverbs
walk	100	264	12.93
dance	1199	1767	16.18

Table 1: Details of the data.

Extraction of frequency components from **419** human motions **420**

Frequency components were extracted from the **421** preprocessed video data utilizing the following two **422** steps. Experiments were conducted by varying the **423** number of kernel mixtures, denoted as M_d , within 424 the range of 4 to 12. **425**

- 1. Reduce high-dimensional pose data to low- **426** dimensional latent variables using GPLVM. **427** Figure [1](#page-2-0) shows the case of reducing pose data **428** into three-dimensional latent variables. **429**
- 2. Extract frequency components for each dimen- **430** sion from the three-dimensional latent vari- **431** ables using SM kernel. Figure [2](#page-2-0) shows the **432** case of using four bases of Gaussian distribu- **433 tion.** 434

Three motions from the training data of the 100 435 Walks dataset, processed through Gaussian Process **436** Latent Variable Model (GPLVM), are visualized **437** in the three-dimensional latent space, as depicted **438** in Figure [1.](#page-2-0) In our approach, we employ the ra- **439** dial basis function (RBF) as the kernel function of **440** GPLVM. To optimize the values of X and the hy- 441 perparameters of the kernel, we utilize the L-BFGS **442** method [\(Liu and Nocedal,](#page-8-18) [1989\)](#page-8-18). Due to the repeti- **443** tive nature of walking motions, the latent variables **444** exhibit circular patterns, as observed in the figure. **445** For $M_d = 4$, the Gaussian distribution is depicted 446 in Figure [2](#page-2-0) with optimized mean μ and variance 447 σ parameters for the first dimension of each mo- **448** tion, using the SM kernel. The estimated variance **449** is exceptionally small, resulting in the Gaussian **450** distribution being represented as a delta function **451** in the figure. From Equation [\(3\)](#page-1-0), we observe that a **452** larger mean μ value corresponds to a shorter period. 453 Therefore, it can be inferred that the spectral com- **454** ponents representing the basis are more likely to be **455** found on the left side of the spectrum for motion **456** data with slower fluctuations. Thus, (a) contains **457** more fast motion components, (c) contains more **458** slow motion components, and (b) lies in between **459** as an intermediate case. The SM kernel is opti- **460** mized with weights as parameters, representing the 461 significance of each frequency component. At each 462 iteration, the frequency components used as mo- **463** tion features in each video are sampled using the **464** weights. 465

Topic 1	Topic 2	Topic 3	Topic 4	Topic 5	Topic 6	Topic 7	Topic 8
wildly	happily	regularly	gracefully	strongly	dancing	practiced	rhythmically
strongly	rhythmically	rhythmically	smoothly	wildly	stepping	settled	stylishly
clearly	lightly	dynamically	seemly	confidently	happily	waving	comfortable
passionately	bouncily	cheerfully	lightly	quickly	dynamically	quickly	flowing
classy	cheerfully	boldly	spinning	boldly	disappointed	dynamically	cool
Topic 9	Topic 10	Topic 11	Topic 12	Topic 13	Topic 14	Topic 15	Topic 16
spacisouly	dynamically	bouncily	cool	sharply	finely	checking	lightly
smoothly	wildly	spreading	sharply	machinelike	spinning	comically	shaking
slowly	waving	totteringly	spacisouly	comically	suffering	carefully	waving
machinelike	big	steadily	happily	firmly	avoiding	cautiously	finely
quietly	sharply	settled	machinelike	strangely	rhythmically	seemly	robotlike

Table 2: AIST++ dataset($M_d = 4$): Top 5 adverbs in each topic estimated by HDP-SMLDA. Each topic corresponds to each topic in Figure [5.](#page-6-0) Compared to LDA, HDP-SMLDA takes into account not only co-occurrence of adverbs but also similarity of motions when classifying adverbs.

Figure 5: The relationship between topics and motion features can be visualized by plotting 100 samples extracted from the Gaussian distribution associated with each topic learned through HDP-SMLDA.

466 3.2 Result

For the AIST++ dataset with $M_d = 4$ **, Table [2](#page-6-1) dis-** plays the top five words for each adverb, along with their corresponding Normalized Pointwise Mutual Information (NPMI) values [\(Bouma,](#page-8-19) [2009\)](#page-8-19) cal- culated from the learned topic-word distribution. Figure [5](#page-6-0) visually represents the 100 samples in a three-dimensional space, obtained from the Gaus-474 sian distribution associated with the mean μ_k of each learned topic. Each sample represents a fre- quency component that symbolizes a specific topic, and the proximity of the samples indicates similar- ity in their frequency components. It is important to note that since the scales are not estimated, the

	Unigram	LDA	HDP-SMLDA		
			$(M_d = 4/10)$		
walk	156	99	52/57		
dance	558	331	218/249		

Table 3: Perplexity at training in each topic model.

dispersion of the points in the figure remains con- **480** stant. To evaluate the performance of this model, **481** perplexity is used as a metric. Table [3](#page-6-2) presents **482** the perplexity of each topic model during training. **483** Additionally, the perplexity for the Unigram model **484** is calculated using the word distribution prior to **485** training. **486**

Generation of adverbs from frequency To ver- 487 ify the accurate association between frequencies **488** and adverbs, we performed an experiment where **489** we generated adverbs based on the frequency com- **490** ponents extracted from an evaluation video (Figure **491** [6\)](#page-7-0), utilizing the learned word distribution. Table **492** [4](#page-7-1) presents both the ground truth adverbs and the **493** top seven adverbs with the highest probabilities, **494** calculated through HDP-SMLDA. Through the es- **495** timation of M_d from 4 to 12, we observed that, for 496 the majority of evaluation videos, the estimation **497** with $M_d = 10$ yielded more suitable adverbs as the 498 top choices. **499**

3.3 Discussions **500**

In Figure [5,](#page-6-0) the arrangement of the 16 Gaussian **501** distributions evenly spans the width of the data. 502 Notably, Topic 5 and Topic 14 exhibit proximity to **503** each other, indicating a similarity in the content of **504** the motions, as supported by Table [4](#page-7-1) showcasing **505** the top adverbs associated with each topic. Top- **506** ics 1, 8, and 10 appear more distanced from the 507 other topics. Notably, these three topics demon- **508** strate pronounced adverb features in terms of fre- **509** quency. While there may be an apparent overlap **510** between the content of Topics 1 and 10, a closer **511** examination of the top 20 words reveals that Topic **512** 1 encompasses emotionally driven dances such as **513** "bravely" and "heavily", while Topic 10 represents **514** adverbs associated with more vigorous movements **515**

Figure 6: A video for evaluation. In the video, the dancer is dancing jazz ballet.

Table 4: Ground truth adverbs of the dance video (Figure [6\)](#page-7-0) and Top 7 adverbs estimated by HDP-SMLDA.

 like "sharply" and "refreshed". This distinction suggests that the model successfully clusters ad- verbs based on both semantic and motion-related features derived from frequency components. The perplexity values from Table [3](#page-6-2) indicate signifi- cantly lower values compared to those obtained from LDA training data, signifying the valuable contribution of frequency components in adverb topic classification. Although increasing the num- ber of mixtures in the kernel was expected to reduce perplexity, the experiment yielded unfavorable re- sults. On the other hand,regarding the generation of adverbs from frequency components, it was ob-529 served that when $M_d = 10$, the model was able to estimate more suitable adverbs compared to when $M_d = 4$. This observation raises the possibility that the annotators may have encountered difficulty in identifying the precise vocabulary during the an- notation process or that the model could generate correct synonyms that did not align perfectly with the ground truth.

 Comparison with neural network models We conducted additional experiments to compare the representative neural network model's performance. Given that our study involves annotations of mul- tiple adverbs per video, multi-label learning be- comes necessary. In typical class classification learning, the model calculates the error by back- propagating the difference between the output prob- ability and the input label. However, in our case, training is performed by back-propagating the aver-

Table 5: Perplexity at evaluating in each model.

age of errors for all adverb labels annotated to the **547** video. We conducted experiments using two dif- **548** ferent models, Long Short-Term Memory (LSTM) **549** [a](#page-9-19)nd Multi-Layer Perceptron (MLP)[\(Rumelhart and](#page-9-19) **550** [McClelland,](#page-9-19) [1987\)](#page-9-19), with four different data inputs: 551

- 1. Input data processed by GPLVM to LSTM **552**
- 2. Input original data to LSTM **553**
- 3. Input frequency $(M_d = 4)$ to MLP 554
- 4. Input frequency $(M_d = 10)$ to MLP 555

Table [5](#page-7-2) displays the perplexity scores for each **556** model during evaluation. Comparing the data pro- **557** cessed by GPLVM with the original data, it is evi- **558** dent that the processed data yielded lower perplex- **559** ity, indicating the effectiveness of data dimensional- **560** ity reduction in class classification. All neural net- **561** work models received high scores, which does not **562** necessarily indicate effective learning of adverbs. **563** Nonetheless, our proposed method demonstrated **564** the highest scores on both datasets, highlighting its **565** superior performance. Thus,our model showcases **566** the ability to accurately estimate adverbs even with **567** limited data. **568**

4 Conclusions **⁵⁶⁹**

We have proposed a joint topic model named HDP- **570** SMLDA, which aims to comprehend the semantic 571 nuances of sensory adverbs pertaining to human **572** motions by learning co-occurrence relationships **573** between motion features and adverbs. Within our **574** framework, adverbs are modeled as a composite **575** distribution within the frequency space of their ker- **576** nels in a Gaussian process that represents the latent **577** trajectory of motions. Consequently, it becomes **578** feasible to estimate the constituents of sensory ad- **579** verbial motions. When compared to the simple **580** Neural Net model, our model exhibits superior **581** performance on classification of adverbs. Our ap- **582** proach considers motions as a mixture of diverse **583** frequency components, leading to the successful **584** generation of appropriate adverbs from motion fea- **585** tures in our empirical investigations. **586**

5 Limitations **⁵⁸⁷**

The primary limitation to the generalization of **588** these results lies in the scarcity of datasets contain- **589** ing adverbially annotated human motions. There **590**

 is no other way to annotate adverbs by ourselves to capture the meaning of adverbs which describe human motions, and it is difficult to make com- parisons with other models because there are few studies working on the same research topic. An- other limitation is that even if the adverbs output by the model are correct, such as synonyms, the model may judge that it has output the wrong one unless it is an exact match. We think this can be resolved by representing the adverbs in embedding vectors to evaluate output.

⁶⁰² 6 Ethical considerations

 All datasets used in the experiments are either pub- licly available or have been licensed for use by the authors. In addition, all copyrights to the data gen- erated using crowdsourcing were transferred to the **607** authors.

⁶⁰⁸ References

- **609** Michael Ahn et al. 2022. Do as i can and not as i say: **610** Grounding language in robotic affordances. In *arXiv* **611** *preprint arXiv:2204.01691*.
- **612** David M. Blei and Michael I. Jordan. 2003. Modeling **613** annotated data. *Proceedings of the 26th annual in-***614** *ternational ACM SIGIR conference on Research and* **615** *development in informaion retrieval*.
- **616** S. Bochner, S. Trust, M. Tenenbaum, and H. Pollard. **617** 1959. *[Lectures on Fourier Integrals](https://books.google.co.jp/books?id=MWCYDwAAQBAJ)*. Annals of Math-**618** ematics Studies. Princeton University Press.
- **619** Gerlof Bouma. 2009. Normalized (Pointwise) Mutual **620** Information in Collocation Extraction. *Proceedings* **621** *of GSCL*, pages 31–40.
- **622** Zhe Cao, Gines Hidalgo, Tomas Simon, Shih-En Wei, **623** and Yaser Sheikh. 2021. [OpenPose: Realtime Multi-](https://doi.org/10.1109/TPAMI.2019.2929257)**624** [Person 2D Pose Estimation Using Part Affinity Fields.](https://doi.org/10.1109/TPAMI.2019.2929257) **625** *IEEE Trans. Pattern Anal. Mach. Intell.*, 43(1):172– **626** 186.
- **627** [J](https://doi.org/10.1109/CVPR.2017.502)oão Carreira and Andrew Zisserman. 2017. [Quo vadis,](https://doi.org/10.1109/CVPR.2017.502) **628** [action recognition? a new model and the kinetics](https://doi.org/10.1109/CVPR.2017.502) **629** [dataset.](https://doi.org/10.1109/CVPR.2017.502) In *2017 IEEE Conference on Computer Vi-***630** *sion and Pattern Recognition (CVPR)*, pages 4724– **631** 4733.
- **632** [A](http://arxiv.org/abs/2204.02311)akanksha Chowdhery et al. 2022. [Palm: Scaling lan-](http://arxiv.org/abs/2204.02311)**633** [guage modeling with pathways.](http://arxiv.org/abs/2204.02311)
- 634 Trevor Cohn, Daniel Preoțiuc-Pietro, and Neil **635** Lawrence. 2014. [Gaussian processes for natural lan-](https://doi.org/10.3115/v1/P14-6001)**636** [guage processing.](https://doi.org/10.3115/v1/P14-6001) In *Proceedings of the 52nd Annual* **637** *Meeting of the Association for Computational Lin-***638** *guistics: Tutorials*, pages 1–3, Baltimore, Maryland, **639** USA. Association for Computational Linguistics.

and Dima.

ing scient

Igor Mord planners: b odied ag

9118–9147. PMLR. **657**

roki Mori,

diction of $language$

[teraction.](https://doi.org/10.1146/annurev-control-070122-102501) *Annual Review of Control, Robotics, and* **668** *Autonomous Systems*, 6:205–232. **669**

Society.

Ruilong Li,

[D](http://dblp.uni-trier.de/db/journals/mp/mp45.html#LiuN89)ong C. Liu

Murphy. 2

ter of the

Linguistic

-
-
-
-
-
-
-
-
-
-
-
-
-
-
-
- **694** Julieta Martinez, Rayat Hossain, Javier Romero, and **695** James J Little. 2017. A Simple yet Effective Baseline **696** for 3D Human Pose Estimation. In *ICCV 2017*, pages **697** 2640–2649.
- **698** T.P. Minka. 2003. [Estimating a dirichlet distribution.](/bib/minka/minka2003estimating/minka-dirichlet.pdf,http://www.stat.columbia.edu/~cook/movabletype/archives/2009/04/conjugate_prior.html) **699** *Annals of Physics*, 2000(8):1–13.
- **700** [B](http://arxiv.org/abs/1802.01144)o Pang, Kaiwen Zha, and Cewu Lu. 2018. [Hu-](http://arxiv.org/abs/1802.01144)**701** [man Action Adverb Recognition: ADHA Dataset](http://arxiv.org/abs/1802.01144) **702** [and A Three-Stream Hybrid Model.](http://arxiv.org/abs/1802.01144) *CoRR*, **703** abs/1802.01144:2438–2447.
- **704** Matthias Plappert, Christian Mandery, and Tamim **705** Asfour. 2018. [Learning a bidirectional mapping](https://doi.org/https://doi.org/10.1016/j.robot.2018.07.006) **706** [between human whole-body motion and natural](https://doi.org/https://doi.org/10.1016/j.robot.2018.07.006) **707** [language using deep recurrent neural networks.](https://doi.org/https://doi.org/10.1016/j.robot.2018.07.006) **708** *Robotics and Autonomous Systems*, 109:13–26.
- **709** Carl Edward Rasmussen and Christopher K. I. Williams. **710** 2006. *Gaussian processes for machine learning.* **711** Adaptive computation and machine learning. MIT **712** Press.
- **713** David E. Rumelhart and James L. McClelland. 1987. **714** *Learning Internal Representations by Error Propa-***715** *gation*, pages 318–362.
- **716** [K](https://proceedings.neurips.cc/paper_files/paper/2014/file/00ec53c4682d36f5c4359f4ae7bd7ba1-Paper.pdf)aren Simonyan and Andrew Zisserman. 2014. [Two-](https://proceedings.neurips.cc/paper_files/paper/2014/file/00ec53c4682d36f5c4359f4ae7bd7ba1-Paper.pdf)**717** [stream convolutional networks for action recognition](https://proceedings.neurips.cc/paper_files/paper/2014/file/00ec53c4682d36f5c4359f4ae7bd7ba1-Paper.pdf) **718** [in videos.](https://proceedings.neurips.cc/paper_files/paper/2014/file/00ec53c4682d36f5c4359f4ae7bd7ba1-Paper.pdf) In *Advances in Neural Information Pro-***719** *cessing Systems*, volume 27. Curran Associates, Inc.
- **720** Ishika Singh, Valts Blukis, Arsalan Mousavian, Ankit **721** Goyal, Danfei Xu, Jonathan Tremblay, Dieter Fox, **722** Jesse Thomason, and Animesh Garg. 2023. [Prog-](https://arxiv.org/abs/2209.11302)**723** [Prompt: Generating situated robot task plans using](https://arxiv.org/abs/2209.11302) **724** [large language models.](https://arxiv.org/abs/2209.11302) In *International Conference* **725** *on Robotics and Automation (ICRA)*.
- **726** Michael L. Stein. 1999. *[Interpolation of spatial data](https://doi.org/10.1007/978-1-4612-1494-6)*. **727** Springer Series in Statistics. Springer-Verlag, New **728** York. Some theory for Kriging.
- **729** [I](https://proceedings.neurips.cc/paper_files/paper/2014/file/a14ac55a4f27472c5d894ec1c3c743d2-Paper.pdf)lya Sutskever, Oriol Vinyals, and Quoc V Le. 2014. [Se-](https://proceedings.neurips.cc/paper_files/paper/2014/file/a14ac55a4f27472c5d894ec1c3c743d2-Paper.pdf)**730** [quence to sequence learning with neural networks.](https://proceedings.neurips.cc/paper_files/paper/2014/file/a14ac55a4f27472c5d894ec1c3c743d2-Paper.pdf) In **731** *Advances in Neural Information Processing Systems*, **732** volume 27. Curran Associates, Inc.
- **733** Christian Szegedy, Vincent Vanhoucke, Sergey Ioffe, **734** Jon Shlens, and Zbigniew Wojna. 2016. [Rethink-](https://doi.org/10.1109/CVPR.2016.308)**735** [ing the inception architecture for computer vision.](https://doi.org/10.1109/CVPR.2016.308) **736** In *2016 IEEE Conference on Computer Vision and* **737** *Pattern Recognition (CVPR)*, pages 2818–2826.
- **738** T. Taniguchi, D. Mochihashi, T. Nagai, S. Uchida, N. In-**739** oue, I. Kobayashi, T. Nakamura, Y. Hagiwara, N. Iwa-**740** hashi, and T. Inamura. 2019. [Survey on frontiers of](https://doi.org/10.1080/01691864.2019.1632223) **741** [language and robotics.](https://doi.org/10.1080/01691864.2019.1632223) *Advanced Robotics*, 33(15- **742** 16):700–730.
- **743** Yee Whye Teh, Michael I. Jordan, Matthew J. Beal, **744** and David M. Blei. 2006. [Hierarchical dirichlet pro-](http://www.gatsby.ucl.ac.uk/~ywteh/research/npbayes/jasa2006.pdf)**745** [cesses.](http://www.gatsby.ucl.ac.uk/~ywteh/research/npbayes/jasa2006.pdf) *Journal of the American Statistical Associa-***746** *tion*, 101(476):1566–1581.
- Stefanie Tellex, Nakul Gopalan, Hadas Kress-Gazit, and **747** Cynthia Matuszek. 2020. Robots that use language. **748** *Annual Review of Control, Robotics, and Autonomous* **749** *Systems*, 3:25–55. **750**
- Shuhei Tsuchida, Satoru Fukayama, Masahiro **751** Hamasaki, and Masataka Goto. 2019. Aist dance **752** video database: Multi-genre, multi-dancer, and **753** multi-camera database for dance information **754** processing. In *Proceedings of the 20th International* **755** *Society for Music Information Retrieval Conference,* **756** *ISMIR 2019*, pages 501–510, Delft, Netherlands. **757**
- Ashish Vaswani, Noam Shazeer, Niki Parmar, Jakob **758** Uszkoreit, Llion Jones, Aidan N Gomez, Łukasz **759** Kaiser, and Illia Polosukhin. 2017. Attention is all **760** you need. In *Advances in Neural Information Pro-* **761** *cessing Systems*, pages 5998–6008. **762**
- Sai Vemprala, Rogerio Bonatti, Arthur Bucker, and **763** Ashish Kapoor. 2023. [Chatgpt for robotics: De-](https://www.microsoft.com/en-us/research/publication/chatgpt-for-robotics-design-principles-and-model-abilities/) **764** [sign principles and model abilities.](https://www.microsoft.com/en-us/research/publication/chatgpt-for-robotics-design-principles-and-model-abilities/) Technical Report **765** MSR-TR-2023-8, Microsoft. **766**
- Jason Wei, Xuezhi Wang, Dale Schuurmans, Maarten **767** Bosma, brian ichter, Fei Xia, Ed Chi, Quoc V Le, **768** and Denny Zhou. 2022. [Chain-of-thought prompt-](https://proceedings.neurips.cc/paper_files/paper/2022/file/9d5609613524ecf4f15af0f7b31abca4-Paper-Conference.pdf) **769** [ing elicits reasoning in large language models.](https://proceedings.neurips.cc/paper_files/paper/2022/file/9d5609613524ecf4f15af0f7b31abca4-Paper-Conference.pdf) In **770** *Advances in Neural Information Processing Systems*, **771** volume 35, pages 24824–24837. Curran Associates, **772** Inc. **773**
- Andrew Gordon Wilson and Ryan Prescott Adams. **774** 2013. [Gaussian Process Kernels for Pattern Discov-](http://dblp.uni-trier.de/db/conf/icml/icml2013.html#WilsonA13) **775** [ery and Extrapolation.](http://dblp.uni-trier.de/db/conf/icml/icml2013.html#WilsonA13) In *ICML 2013*, volume 28 of **776** *JMLR Workshop and Conference Proceedings*, pages 1067–1075. JMLR.org. **778**
- Tatsuro Yamada, Hiroyuki Matsunaga, and Tetsuya **779** Ogata. 2018. [Paired recurrent autoencoders for bidi-](https://doi.org/10.1109/LRA.2018.2852838) **780** [rectional translation between robot actions and lin-](https://doi.org/10.1109/LRA.2018.2852838) **781** [guistic descriptions.](https://doi.org/10.1109/LRA.2018.2852838) *IEEE Robotics and Automation* **782** *Letters*, 3(4):3441–3448. Publisher Copyright: © **783** 2016 IEEE. **784**