SPFormer: Enhancing Vision Transformer with Superpixel Representation

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Paper under double-blind review

Abstract

This work introduces SPFormer, a novel Vision Transformer architecture enhanced by superpixel representation. Addressing the limitations of traditional Vision Transformers' fixed-size, non-adaptive patch partitioning, SPFormer divides the input image into irregular, semantically coherent regions (*i.e.*, superpixels), effectively capturing intricate details. Notably, this is also applicable to intermediate features and our whole model supports end-to-end training, empirically yielding superior performance across multiple benchmarks. For example, on the challenging ImageNet benchmark, SPFormer outperforms DeiT by 1.4% at the tiny-model size and by 1.1% at the small-model size. Moreover, a standout feature of SPFormer is its inherent explainability — the superpixel structure offers a window into the model's internal processes, providing valuable insights that enhance the model's interpretability and stronger robustness against challenging scenarios like image rotations and occlusions.

1 Introduction

Over the past decade, the vision community has witnessed a remarkable evolution in visual recognition systems, from the resurgence of Convolutional Neural Networks (CNNs) in 2012 (Krizhevsky et al., 2012) to the cutting-edge innovation of Vision Transformers (ViTs) in 2020 (Dosovitskiy et al., 2021). This progression has instigated a significant shift in the underlying methodology for feature representation learning, transitioning from pixel-based (for CNNs) to patch-based (for ViTs).

Traditionally, pixel-based representations organize an image as a regular grid, allowing CNNs (He et al., 2016; Tan & Le, 2019; Mehta & Rastegari, 2022; Sandler et al., 2018) to extract local, detailed features through sliding window operations. Despite the inductive bias inherent in CNNs, like translation equivariance, aiding their success in effectively learning visual representations, these networks face a challenge in capturing global-range information, typically necessitating the stacking of multiple convolutional operations and/or additional operations (Li et al., 2020; Chen et al., 2018) to enlarge their receptive fields.

In contrast, ViTs (Dosovitskiy et al., 2021) regard an image as a sequence of patches. These patch-based representations, usually of a much lower resolution compared to their pixel-based counterparts, enable global-range self-attention operations in a computationally efficient manner. While the attention mechanism successfully captures global interactions, it does so at the expense of losing local details, like object boundaries. Moreover, the low resolution of patch-based representations poses challenges to adaptation for high-resolution dense prediction tasks such as segmentation and detection, which require both local detail preservation and global context information.

This dichotomy raises an intriguing question: can we derive benefits from both preserved local details and effective long-range relationship capture? In response, we explore superpixel-based solutions, which have been employed extensively in computer vision prior to the deep learning era (Zhu & Yuille, 1996; Shi & Malik, 2000; Martin et al., 2001; Malik et al., 2001; Borenstein & Ullman, 2002; Tu & Zhu, 2002; Ren & Malik, 2003). These solutions provide locally coherent structures and reduce computational overhead compared to pixel-wise processing. Specifically, adaptive to the input, superpixels partition an image into irregular regions, with each region grouping pixels with similar semantics. This approach allows for a small number of superpixels, making it feasible to model global interactions through self-attention.

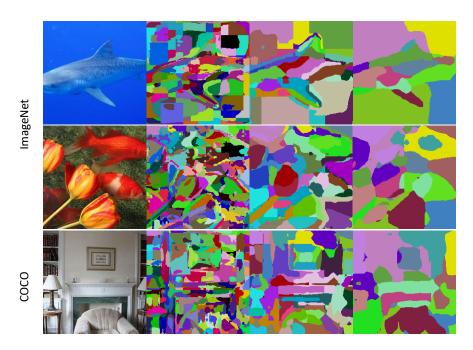


Figure 1: Visualization of learned superpixels with our SPFormer trained on ImageNet with category labels only. For each row, we show input image, visualization of 196, 49, and 16 superpixels. The learned superpixel aligns well with the object boundaries even with 16 superpixels. The last row shows results from a COCO image (not trained), demonstrating SPFormer's zero-shot ability.

To this end, we introduce a novel transition of ViT architecture from patch representation to superpixel representation, through our newly developed Superpixel Cross Attention (SCA). The resulting architecture, Superpixel Transformer (SPFormer), adeptly marries local detail preservation with global-range self-attention, enabling end-to-end trainability. In comparison to standard ViT architectures, SPFormer demonstrates strong enhancements across various tasks. For instance, it achieves impressive gains on the challenging ImageNet benchmark, such as 1.4% for DeiT-T and 1.1% for DeiT-S. Notably, the superpixel representation in SPFormer aligns seamlessly with semantic boundaries, even in unseen data. Moreover, the interpretability provided by our superpixel representation facilitates understanding of the model's decision-making process and enhances the robustness against rotations and occlusions. These findings highlight the potential of superpixel-based approaches in advancing the field, and, hopefully, could inspire future research beyond traditional pixel and patch-based paradigms in visual representation learning.

2 Related Work

Pixel Representation CNNs (LeCun et al., 1998; Krizhevsky et al., 2012; Simonyan & Zisserman, 2015; Szegedy et al., 2015; Ioffe & Szegedy, 2015; He et al., 2016; Tan & Le, 2019; Liu et al., 2022) process an image as a grid of pixels in a sliding window manner. CNN has been the dominant network choice since the advent of AlexNet (Krizhevsky et al., 2012), benefiting from several design choices, such as translation equivariance and the hierarchical structure to extract multi-scale features. However, it requires stacking several convolution operations to capture long-range information (Simonyan & Zisserman, 2015; He et al., 2016), and it could not easily capture global-range information, as the self-attention operation (Vaswani et al., 2017).

Patch Representation The self-attention mechanism (Bahdanau et al., 2015) of Transformer architectures (Vaswani et al., 2017) effectively captures long-range information. However, its computation cost is quadratic to the number of input tokens. ViTs (Dosovitskiy et al., 2021) alleviate the issue by tokenizing (or patchifying) the input image with a sequence of patches (e.g., patch size 16×16). The patch representa-

tion (Dosovitskiy et al., 2021) unleashes the power of Transformer architectures (Vaswani et al., 2017) in computer vision, significantly impacting multiple visual recognition tasks (Russakovsky et al., 2015; Carion et al., 2020; Zhu et al., 2021; Wang et al., 2021a; Touvron et al., 2021a; Radford et al., 2021; Bao et al., 2022; He et al., 2022; Yu et al., 2022c; 2023). Due to the lack of the built-in inductive biases as in CNNs, learning with ViTs requires special training enhancements, e.g., large-scale datasets (Sun et al., 2017), better training recipes (Touvron et al., 2021a; Steiner et al., 2021), or architectural designs (Liu et al., 2021; Wang et al., 2021b). To mitigate the issue, a few works exploit convolutions (LeCun et al., 1998; Sandler et al., 2018) to tokenize the images, resulting in hybrid CNN-Transformer architectures (Wu et al., 2021; Yuan et al., 2021; Dai et al., 2021; Xiao et al., 2021; Mehta & Rastegari, 2022; Guo et al., 2022; Tu et al., 2022; Yang et al., 2023). Unlike those works that simply gather knowledge from existing CNNs and ViTs, we explore a different superpixel representation in ViTs.

Superpixel Representation Before the deep learning era, superpixel is one of the most popular representations in computer vision (Zhu & Yuille, 1996; Shi & Malik, 2000; Martin et al., 2001; Malik et al., 2001; Borenstein & Ullman, 2002; Tu & Zhu, 2002; Ren & Malik, 2003). Ren and Malik (Ren & Malik, 2003) preprocess images with superpixels that are locally coherent, preserving the structure necessary for the following recognition tasks. It also significantly reduces the computation overhead, compared to the pixel-wise processing. The superpixel clustering methods include graph-based approaches (Shi & Malik, 2000; Felzenszwalb & Huttenlocher, 2004), mean-shift (Comaniciu & Meer, 2002; Vedaldi & Soatto, 2008), or k-means clustering (Lloyd, 1982; Achanta et al., 2012). Thanks to its effective representation, recently some works attempt to incorporate clustering methods into deep learning frameworks (Jampani et al., 2018; Yang et al., 2020; Locatello et al., 2020; Xu et al., 2022; Yu et al., 2022a; Zhang et al., 2022; Yu et al., 2022b; Ma et al., 2023; Huang et al., 2023; Zhu et al., 2023). For example, SSN (Jampani et al., 2018) integrates the differentiable SLIC (Achanta et al., 2012) to CNNs, allowing end-to-end training. Yu et al. (2022a;b) regard object queries (Carion et al., 2020; Wang et al., 2021a) as cluster centers in Transformer decoders (Vaswani et al., 2017). SViT (Huang et al., 2023) clusters the tokens to form the super tokens, where the clustering process has no gradient passed through¹. Consequently, their network is not aware of the clustering process and could not recover from the clustering error. CoCs (Ma et al., 2023) groups pixels into clusters, while aggregating features within each cluster by regarding the image as a set of points with coordinates concatenated. In contrast, our proposed method groups pixels into superpixels, and models their global relationship via self-attention. Furthermore, during clustering, CoCs uses a Swin-style window partition (Liu et al., 2021) that introduces visual artifacts, especially around the window boundaries.

3 Method

We introduce SPFormer, a novel image processing framework that integrates superpixel-based feature representation with a SCA mechanism. This approach effectively addresses the limitations of traditional pixel and patch-based methods by enhancing both computational efficiency and detail preservation. We begin with a detailed discussion of our advanced superpixel representation (Sec. 3.1), followed by an explanation of the SCA mechanism in Sec. 3.2, which refines this representation by blending local details with global contextual information efficiently. Finally, we elaborate on the integration of these advancements into the SPFormer architecture in Sec. 3.3.

3.1 Superpixel Representation: Bridging Pixel and Patch Approaches

In the evolving landscape of feature representation, the transition from pixel to patch-based methods in ViTs has opened new avenues for image processing. However, each method has inherent limitations, inspiring our exploration of a more adaptive and efficient representation: superpixels.

Pixel Representation Traditional pixel representation conceptualizes an image **I** as a grid of high-resolution pixels, expressed as $\mathbf{I} \in \mathbb{R}^{c \times h \times w}$. Predominantly employed in CNN-based methods, this approach suffers from restricted contextual integration due to the limited receptive fields of the convolution operations.

¹From official code: https://github.com/hhb072/STViT/blob/main/models/stvit.py#L206

Although self-attention mechanisms could theoretically mitigate this limitation, their implementation is computationally prohibitive at this scale due to the quadratic dependencies on the number of pixels.

Patch Representation Contrastingly, ViTs adopt a patch-based representation with reduced resolution, denoted by $\mathbf{P} \in \mathbb{R}^{c \times p_h \times p_w}$. This simplification reduces computational complexity and facilitates the application of self-attention mechanisms—albeit at a loss of finer detail and contextual richness due to the coarse granularity.

Superpixel Representation Our approach combines the advantages of both pixel and patch methodologies through a superpixel representation that includes features $\mathbf{S} \in \mathbb{R}^{c \times s_h \times s_w}$ and an association matrix $\mathbf{A} \in \mathbb{R}^{n \times h \times w}$. This matrix defines a competitive relationship between pixels and their associated superpixels, as delineated further in the structured components below:

- 1. Neighboring Superpixels (\mathcal{N}_i): Each pixel i is linked to its neighboring superpixels, including the nearest superpixel and its Moore Neighborhood within a radius of r=3, comprising n=9 superpixels in total. This configuration not only facilitates localized information sharing but also enhances the granularity of the feature representation. Moreover, these superpixels engage in a competitive interaction to establish dominance over the association with the pixel, which dynamically affects the feature integration process.
- 2. Superpixel's Local Window (W_p): For each superpixel p, a local window W_p is defined, which encompasses pixels that are potentially owned by the superpixel, based on the \mathcal{N}_i associations. This window configuration is critical for implementing the superpixel cross attention mechanism via a sliding window technique, as detailed in Sec. 3.2. It ensures that each superpixel contextually interacts with its relevant local pixel environment, enabling precise and adaptive refinement of attention dynamics.

The superpixel representation can be effectively converted into a pixel representation using the equation:

$$\mathbf{I}_i = \sum_{p \in \mathcal{N}_i} \mathbf{A}_{ip} \cdot \mathbf{S}_p \tag{1}$$

where I_i denotes the feature vector of pixel i. This transformation method not only preserves boundary information with high fidelity but also offers a finer granularity than direct patch upsampling. It facilitates a seamless transition between superpixel and pixel representations, enabling the use of a more manageable superpixel grid while ensuring meticulous retention of detailed pixel-level information.

Furthermore, our superpixel approach effectively retains crucial boundary information and demonstrates robustness against common image distortions such as rotation and occlusion, benefiting from the inherent adaptability of superpixels. The reduced computational demands, along with semantic pixel clustering for improved explainability, and resilience against complex transformations, position this method as a superior alternative to traditional approaches.

3.2 Superpixel Cross Attention

In the SCA module, our strategy employs a dual mechanism: Pixel-to-Superpixel (P2S) and Superpixel-to-Pixel (S2P) attention. These mechanisms hone attention locally within superpixels to iteratively refine feature presentations, crucial for tasks requiring high-resolution processing and precise contextual accuracy (Fig. 2). Specifically, these two mechanisms are designed to optimize interactions between pixel and superpixel features:

- **P2S Cross-Attention**: Enhances superpixel representations by assimilating contextual details from pixels within designated local windows.
- **S2P Cross-Attention**: Refines pixel features by leveraging insights from adjacent superpixels, thereby enhancing granularity.

These bidirectional processes effectively bridge superpixel efficiency and the detailed granularity of pixel representations, offering a versatile and refined feature set.

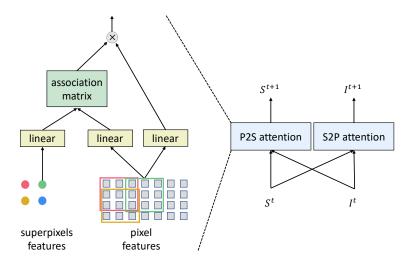


Figure 2: Illustration of our SCA module, demonstrating iterative refinement of superpixel and pixel features using a sliding window-based cross-attention mechanism. Each superpixel cross-attends to a localized region of pixels, as highlighted in the colored rectangle. On the left, we detail the P2S cross-attention process, while the S2P cross-attention is depicted similarly, albeit with reversed roles for superpixel and pixel.

Starting with initial pixel \mathbf{I}^0 and superpixel features \mathbf{S}^0 , each iteration t progressively refines these features. Updates are applied to both superpixel features \mathbf{S}^t and association matrix \mathbf{A}^t to ensure continual improvement of the superpixel representation.

Superpixel features are updated via the P2S cross-attention, formulated as:

$$\mathbf{S}_{p}^{t} = \mathbf{S}_{p}^{t-1} + \sum_{i \in \mathcal{W}_{p}} \operatorname{softmax}_{i} \left(\mathbf{q}_{\mathbf{S}_{p}^{t-1}} \cdot \mathbf{k}_{\mathbf{I}_{i}^{t-1}} \right) \mathbf{v}_{\mathbf{I}_{i}^{t-1}}$$
(2)

where W_p identifies pixels within a superpixel's local window, defined in Sec. 3.1, and \mathbf{q} , \mathbf{k} , and \mathbf{v} symbolize the query, key, and value vectors derived from linear transformations of the previous iteration's features.

Pixel features are concurrently refined using updated associations \mathbf{A}_{ip}^t , as shown:

$$\mathbf{A}_{ip}^{t} = \operatorname{softmax}_{p \in \mathcal{N}_{i}} \left(\mathbf{q}_{\mathbf{I}_{i}^{t-1}} \cdot \mathbf{k}_{\mathbf{S}_{p}^{t-1}} \right)$$
(3)

where \mathcal{N}_i includes neighboring superpixels of pixel i, defined in Sec. 3.1. These updated pixel representations are then calculated by:

$$\mathbf{I}_{i}^{t} = \mathbf{I}_{i}^{t-1} + \sum_{p \in \mathcal{N}_{i}} \mathbf{A}_{ip}^{t} \cdot \mathbf{v}_{\mathbf{S}_{p}^{t-1}}$$

$$\tag{4}$$

These differentiable update equations are essential for refining both pixel and superpixel feature representations, enabling the gradients from either domain to be leveraged for end-to-end training. The proposed SCA module is a cornerstone of our method and will be further elaborated in the subsequent architecture SPFormer in the next subsection.

3.3 SPFormer Architecture

Our architecture leverages the advanced capabilities of our superpixel representation, deviating only minimally from the standard ViT architecture as described by Dosovitskiy et al. (2021). While retaining the non-overlapping patchify layer, we employ a reduced window size of 4×4 for extracting initial pixel features \mathbf{I}^0 , compared to the traditional 16×16 . This modification is enabled by the efficiency of our superpixel representation, which substantially reduces the input size for subsequent self-attention layers.

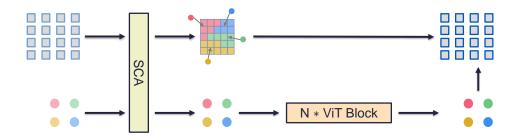


Figure 3: Illustration of a single stage of the SPFormer architecture. It starts with initial superpixel features and pixel features as inputs. The SCA module iteratively refines superpixel features, enhancing their semantic richness. These features are then processed by the Multi-Head Self-Attention (MHSA) for global contextual understanding. The stage concludes by updating the pixel features based on the enriched superpixel information, readying them for the next stage or for final pooling and classification. This design showcases the efficient integration of local detail and global context in SPFormer.

Initially, superpixel features S^0 are derived from pixel features I^0 through a 1×1 convolution and 4×4 average pooling. These features undergo continuous refinement across multiple iterations t using the SCA module. This module enhances the semantic alignment of the superpixel representation by exploiting the local spatial context of each superpixel, as detailed in Sec. 3.2. Subsequently, the enriched superpixel features are processed by multi-head self-attention to extract long-range dependencies and contextual nuances within the image.

We observed that even after multiple iterations (e.g., t > 2), the superpixel representations generated by a single SCA module may not fully align with the overarching context. This misalignment primarily stems from insufficient semantic information derived from the output of the patchify layer. To tackle this challenge, we implement a gradual refinement strategy for enriching superpixel representations. We segment the original ViT architecture into multiple stages, each utilizing a SCA module capped at a limited number of iterations (e.g., t = 2). This design allows each SCA module to build on the semantically enriched superpixel features from the previous stage, progressively enhancing the semantic depth.

Specifically, prior to advancing to the subsequent SCA module, superpixel features are processed through a 1×1 convolution. The pixel features are then refined according to Eq. (1), augmented with a skip connection He et al. (2016). This adjustment ensures that the pixel features benefit from the globally context-enhanced superpixel features of the preceding stage. Instead of reinitializing superpixel features anew, this methodology uses the contextually enhanced superpixel features from the previous stage as the foundation. As depicted in Fig. 3, this systematic approach significantly augments superpixel representations, capturing increasingly complex semantic information across stages.

Conceptually, our network architecture is designed as a dual-branch structure. One branch preserves a dense pixel representation with high resolution, while the other branch focuses on our compact superpixel representation. Minimal direct operations are applied to the dense pixel representation, enabling us to allocate most computational resources to the more efficient superpixel representation. This dual-branch approach fosters computational efficiency without sacrificing the detailed preservation of local image features.

By integrating superpixel representation with SCA, SPFormer offers an advanced solution for boosting both the semantic interpretability and computational efficiency of image processing. This combination enhances detail retention and positions SPFormer as a strong tool in diverse image processing applications.

4 Experiments

We initially outline the implementation details of our method in Sec. 4.1. We then assess its efficiency in image classification and segmentation tasks in Sec. 4.2, and explore its explainability in Sec. 4.3.

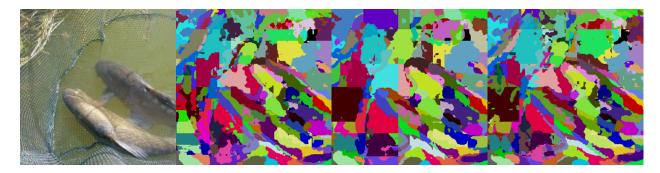


Figure 4: The multi-head SCA design generates multiple superpixel representations, each capturing different semantic relationships and addressing the ambiguity in superpixel over-segmentation.

4.1 Implementation Details

SPFormer employs a specific stride s=4 between the dimensions of superpixel and pixel features, considerably reducing the spatial dimensions of superpixel features compared to their pixel counterparts. This downsizing facilitates efficient self-attention computations for superpixel features, as direct self-attention on pixel features would be exponentially costlier, specifically $(s \times s)^2$ times more expensive. Transitioning to superpixel features significantly lowers computational demands without compromising detail retention.

As an over-segmentation method, multiple superpixel segmentations are possible; hence, relying solely on a single superpixel segmentation is insufficient for a comprehensive description of an image. Unlike previous methods such as those proposed by Jampani et al. (2018) and Zhu et al. (2023), which produce one type of superpixel segmentation at a time, our approach in the SCA module utilizes multi-head attention to enable intricate interactions between superpixels and pixels. This strategy effectively uses global contextual information and generates a variety of superpixel representations, as illustrated in Fig. 4. These diverse representations address different levels of granularity, thereby mitigating typical issues associated with superpixel over-segmentation. For our architecture variants, we allocate two attention heads for the smaller models (SPFormer-T and SPFormer-S) and three heads for the base model (SPFormer-B).

Positional information is integrated into SCA via Convolution Position Embedding (CPE) (Huang et al., 2023), capturing spatial relationships within the image. Both superpixel and pixel features are augmented with CPE implemented as a 3×3 depthwise convolution with a skip connection before applying P2S and S2P cross-attentions. This enhancement reinforces the spatial associations between pixels and superpixels, leading to more precise alignments.

As outlined in Sec. 3.3, SCA blocks are integrated into the standard ViT architecture at carefully chosen points, specifically before the first and third self-attention blocks. We utilize the LayerScale technique, as specified in Touvron et al. (2021b), to modulate gradient flow and enhance training stability and effectiveness. With the inclusion of residual connections as detailed in Eq. (2) and Eq. (4), our approach starts by mimicking standard patches but evolves to exploit superpixels more effectively as training advances.

Adhering to the protocols established in DeiT (Touvron et al., 2021a), we implement robust data augmentations, use the AdamW optimizer, and follow a cosine decay learning rate schedule. All models train on the ImageNet dataset (Russakovsky et al., 2015) for 300 epochs. During SPFormer-B/16 training, significant overfitting challenges arose. Increasing the Stochastic Depth (Huang et al., 2016) rate from 0.1 to 0.6 effectively addressed these issues, highlighting a potential need for advanced regularization strategies tailored to superpixel representation for future studies.

For SPFormer variants, the standard design incorporates a 4×4 patchify layer. Variants equipped with two convolution layers of kernel size 3 and stride 2 are denoted by † . Models with different superpixel sizes are identified by their corresponding ViT-equivalent patch sizes, such as SPFormer/32 for a 32×32 patch size, ensuring clarity in our experimental lineup.

Table 1: Comparative analysis of SPFormer's performance on ImageNet classification against DeiT baselines. Variants augmented with two convolution layers of kernel size 3 with stride 2 are denoted by † .

Model	#Params	#FLOPs	Top-1
SPFormer-S/56	22M	0.5G	72.3
DeiT-T (Touvron et al., 2021a)	5M	1.3G	72.2
SPFormer-T	5M	1.3G	73.6
SPFormer- T^{\dagger}	5M	1.3G	75.0
DeiT-S/32 (Touvron et al., 2021a) SPFormer-S/32 SPFormer-S/32 †	22M	1.1G	73.3
	22M	1.2G	76.4
	22M	1.3G	77.9
DeiT-S (Touvron et al., 2021a)	22M	4.6G	79.9
SPFormer-S	22M	5.2G	81.0
SPFormer-S [†]	22M	5.3G	81.7
DeiT-B (Touvron et al., 2021a)	87M	17.5G	81.8
SPFormer-B	87M	19.2G	82.4
SPFormer-B [†]	87M	19.2G	82.7

SPFormer utilizes a defined ratio between the dimensions of superpixel and pixel features, reducing the spatial dimensions of superpixel features with stride s=4 of their corresponding pixel dimensions, which enables us to directly perform the self attention layers for the superpixel features. On the contrary, conducting the self attention on pixel features directly is $(s \times s)^2$ time expensive, which is infeasible. Going from pixel features to superpixel features significantly reduces the computational cost without sacrificing the details.

In the SCA module, we employ multi-head attention to manage attention and interaction between superpixels effectively. This setup not only leverages global contextual information optimally but also produces multiple superpixel representations, as shown in Fig. 4. These varied representations capture different granularities, addressing the ambiguity commonly associated with superpixel over-segmentation. Specifically, we allocate two heads for our smaller variants (SPFormer-T and SPFormer-S) and three heads for the base model (SPFormer-B).

4.2 Efficiency in Image Classification and Segmentation

4.2.1 Main Results on ImageNet

Our evaluation of SPFormer on the ImageNet dataset demonstrates its superior efficiency and performance over the DeiT baseline under varying configurations as shown in Tab. 1. Specifically, SPFormer-S, which employs the standard ViT configuration with 196 tokens, exceeds the performance of DeiT-S by 1.1%, achieving a top-1 accuracy of 81.0% compared to 79.9% for DeiT-S. Furthermore, SPFormer-T outperforms DeiT-T by 1.4%, recording 73.6% versus 72.2%. This improvement is more pronounced with larger patch sizes, such as 32. Although DeiT-S/32 experiences a performance decline due to its coarser granularity, SPFormer-S/32 maintains robust performance at 76.4%, significantly outperforming DeiT-T by 4.2% while requiring fewer FLOPs.

A critical aspect of SPFormer involves shifting the computational demand from self-attention mechanisms to MLPs. This shift suggests a novel scaling strategy that primarily focuses on increasing image resolution to capture finer details. By doubling the window size from 4 to 8 and adapting to a higher resolution of 448, SPFormer enhances its computational efficiency and secures a 0.3% improvement in performance over the standard configuration. Conversely, similar adjustments in DeiT-S only yield a negligible improvement of 0.1%, hindered by the granularity of its patch-based representation.

Further enhancing SPFormer's initial feature extraction phase in the superpixel cross-attention stage, we introduce a lightweight convolution stem comprising two or three 3×3 convolutions with a stride of 2. This

enhancement has consistently improved performance, exemplified by SPFormer-S/ 32^{\dagger} , which witnesses an additional increase of 1.5% in ImageNet accuracy, reaching 77.9%.

Model	#Params	#FLOPs	Top-1		
SPFormer-S/32	22M	1.2G	76.4		
Single Iteration in SCA	22M	1.2G	75.4		
SCA at Initial Layer Only	22M	1.2G	74.8		
Single-Head SCA	22M	1.2G	75.6		

Table 2: Ablation study on the design choices in SPFormer.

4.2.2 Ablation Study: Design Choices in SPFormer

Learnable Position Embedding

We evaluates key design elements of SPFormer-S/32 on the ImageNet validation set. We investigate the impacts of iteration count in the SCA module, the placement of SCA within the architecture, the use of multi-head attention, and the choice of position embeddings.

22M

1.2G

76.1

The findings highlight the importance of multiple iterations in SCA for performance enhancement, with a single iteration leading to a 1.0% drop in accuracy. The strategic placement of SCA across different layers is crucial, as restricting it to the initial layer causes a 1.6% accuracy reduction, indicating that higher-level features play a vital role in augmenting semantic depth and in rectifying early-stage superpixel inaccuracies. Furthermore, employing multi-head attention in SCA is significant for capturing diverse superpixel relationships, with its absence leading to a 0.8% decrease in accuracy. Lastly, using learnable position embeddings over CPE results in a slight drop in performance.

This ablation study validates the effectiveness of the considered design choices in SPFormer, affirming their contributions to the overall performance of the model.

4.2.3 Semantic Segmentation: Utilizing SPFormer's High-Resolution Feature Preservation

SPFormer's superpixel representation intrinsically maintains higher resolution features, making it particularly suitable for semantic segmentation tasks. This characteristic allows for detailed and context-rich segmentation outputs, a key advantage over traditional patch-based methods.

Incorporating SPFormer into the SETR (Zheng et al., 2021) framework, we enhance segmentation performance by directly classifying individual superpixels. This direct approach leverages SPFormer's high-resolution feature preservation, allowing for more nuanced segmentation. The final segmentation maps are generated by upscaling the superpixel-based logits using Eq. (1).

We evaluate SPFormer on the ADE20K (Zhou et al., 2017) and Pascal Context (Mottaghi et al., 2014) datasets. Utilizing ImageNet-pretrained models, SPFormer demonstrates significant improvements in mIoU, highlighting its effectiveness in detailed segmentation tasks.

As shown in Tab. 3 and Tab. 4, the performance gains in mIoU are noteworthy when using ImageNet-pretrained models: 4.2% improvement on ADE20K and 2.8% on Pascal Context. These results not only highlight the detailed nature of SPFormer's superpixel representation but also its adaptability to diverse and complex datasets. To further validate the intrinsic segmentation capabilities of SPFormer, we conduct additional training from scratch. This approach reiterates the model's strength in maintaining high-resolution features independently of pretraining influences, leading to mIoU improvements of 3.0% on ADE20K and 3.1% on Pascal Context compared to baseline methods.

4.3 Unveiling SPFormer's Explainability

Integrating superpixel representation into the Vision Transformer architecture adds a significant layer of explainability compared to conventional fixed patch partition methods. This section first discusses the

Table 3: Semantic segmentation on ADE20K val split.

Method	#Params	#FLOPs	Pretrained	mIoU
DeiT-S SPFormer-S	22M 23M	32G $35G$	×	20.1 23.1
DeiT-S SPFormer-S	22M 23M	32G $35G$	/	$42.3 \\ 46.5$

Table 4: Semantic segmentation on Pascal Conext val split.

Method	#Params	$\# \mathrm{FLOPs}$	Pretrained	mIoU
DeiT-S	22M	27G	Х	18.0
SPFormer-S	23M	30G	×	21.1
DeiT-S	22M	27G	✓	48.3
SPFormer-S	23M	30G	✓	51.2

inherent explainability of our superpixel representation, followed by an evaluation of its semantic alignment and generalizability to unseen data.

4.3.1 Superpixel Representation as an Explainability Tool

Our method's superpixel representation can be visualized through the association matrix \mathbf{A} , providing insights into the model's internal processing. In Fig. 1, we visualize the learned soft associations by selecting the argmax over the superpixels:

$$\hat{\mathbf{A}} = \operatorname{argmax}(\mathbf{A}) \tag{5}$$

These visualizations reveal that, even with a soft association, the superpixels generally align with image boundaries. This alignment is noteworthy as it emerges even though the network is only trained on image category labels. Thus, the model segments images into irregular, semantics-aware regions while reducing the number of tokens needed for representation.

Furthermore, we assess the generalizability of our superpixel representation using the COCO dataset (Lin et al., 2014), which consists of high-resolution images with complex scenes. For this evaluation, we resize and center-crop COCO images to align with the ImageNet evaluation pipeline. Fig. 5 showcases the visual representation of superpixels on these images. Note that the superpixels generated by SPFormer, trained exclusively on ImageNet, adapt well to this unseen data, capturing intricate structures such as thin objects. This adaptability highlights the model's capability to preserve detail and generalize its superpixel representation to new contexts.

4.3.2 Semantic Alignment of Superpixels

Our evaluation of superpixel representation focuses on its ability to align with ground truth boundaries in images, despite the model not being trained on the datasets used for this assessment. This test involved a quantitative analysis on both object and part levels using the Pascal VOC 2012 dataset (Everingham et al., 2015) and Pascal-Part-58 (Zhao et al., 2019). Note that these assessments were performed without any training on these specific datasets, underscoring the model's generalization capabilities.

In our approach, each superpixel or patch's prediction is derived by aggregating the ground truth labels of the pixels it encompasses. We assign the most frequently occurring label within a superpixel as its prediction, assuming optimal classification. This method leverages the soft associations produced by our SCA module, where predictions are formed by combining pixel labels with their corresponding weights and upscaled as per Eq. (1).



Figure 5: Zero-shot transferability on the COCO dataset. Trained solely on ImageNet, SPFormer demonstrates effective segmentation of unseen COCO images into detailed superpixels. 196 superpixels are used in this visualization.

Diverging from the single-superpixel outcome of traditional patch representation, our model employs a multi-head design in the SCA module. This allows for the creation of multiple, distinct superpixels for each head, enhancing the richness and diversity of the extracted features (see Fig. 4). For our evaluations, we computed an average of predictions across all heads. It is noteworthy that effective feature extraction in our model is deemed successful if even a single head accurately identifies a superpixel.

The proficiency of our superpixel approach is demonstrated in its performance compared to vanilla ViTs that utilize patch representations with a stride of 16. ViTs often suffer from a granularity trade-off, losing finer details in favor of broader patch representations. In contrast, the superpixels from our SCA module, as shown in Tab. 5, manifest substantial improvements — achieving a 4.2% increase in object-level and 4.6% in part-level mIoU with SPFormer-S † . Furthermore, these superpixels display a quality comparable to those from traditional superpixel methods like SLIC (Achanta et al., 2012), highlighting our method's effectiveness in capturing detailed semantic information without direct training on the evaluation datasets.

Table 5: Evaluation of superpixel quality in a zero-shot setting on Pascal VOC 2012 and Pascal-Parts-58 datasets, using 196 patches/superpixels. Our SPFormer variants demonstrate notable improvements over traditional patch representations and are competitive with the SLIC method.

Method	Pascal Voc2012		Pascal-Parts-58	
	mIoU	mAcc	mIoU	mAcc
Patch	87.8	92.8	68.7	78.2
SPFormer-T [†]	91.5	95.7	71.5	79.9
${ m SPFormer-S^\dagger}$	92.0	96.6	73.3	82.4
SPFormer-B [†]	91.2	96.3	72.5	81.4
SLIC (Achanta et al., 2012)	92.5	95.4	74.0	81.7

4.3.3 Explainability-Driven Robustness

The robustness of SPFormer is deeply intertwined with its explainability, particularly through the superpixel representation. This section explores how the model's transparent and interpretable features contribute to its resilience against image modifications like rotation and occlusion.

Robustness to Rotation Our model's capacity to generate coherent superpixels even under rotational transformations showcases the robustness afforded by its explainable structure. For example, Fig. 6 illustrates the model's performance under rotation, and Tab. 6 quantifies this robustness, under patch size 32. By visualizing how superpixels adapt to rotated images, we gain insights into the model's stability in varied orientations. While SPFormer demonstrates a heightened robustness to rotation, it still exhibits some limitations, likely due to the learnable absolute position embeddings not being inherently rotation-invariant. These observations suggest potential avenues for enhancing rotational robustness, possibly through integrating rotation-invariant mechanisms within the superpixel representation or the network architecture.

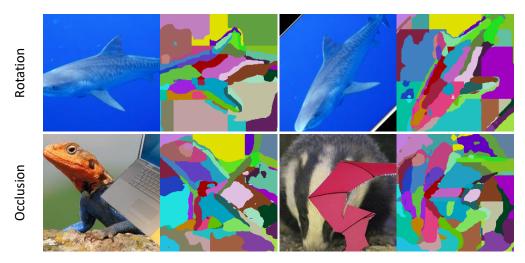


Figure 6: Visualization of SPFormer's superpixel representation under rotation and occlusion, highlighting the model's adaptability and robustness.

Robustness to Occlusion The occlusion robustness of SPFormer is another facet where explainability plays a key role. By examining superpixel behavior in occluded images, we observe the model's ability to distinguish between occluders and the object of interest. Unlike traditional patch-based representations, which tend to blend occluders with the object, our superpixel representation more effectively isolates and identifies obscured parts of the image. This nuanced differentiation is a direct result of the model's explainable superpixel structure, which provides a more detailed and context-aware interpretation of the image content, as demonstrated in Fig. 6.

Table 6: Quantitative evaluation of SPFormer's robustness to rotation, comparing performance at different angles. Variants augmented with two convolution layers of kernel size 3 with stride 2 are denoted by † .

Model	Clean	15	30	45
DeiT-S/32 (Touvron et al., 2021a)	73.3	71.1	67.7	59.5
SPFormer-S/ 32^{\dagger}	77.9	75.2	73.4	66.9

5 Conclusion

In this work, we introduced SPFormer, a novel approach for feature representation in Vision Transformers, emphasizing superpixel representation. This method showcases a promising shift from traditional pixel and patch-based approaches, offering two distinct advantages: efficiency due to a reduced number of superpixels facilitating global self-attention and explainability through semantic grouping of pixels. The empirical results demonstrate the potential of SPFormer in diverse computer vision tasks, under both the standard benchmarks $(e.g., ImageNet \ classification)$ and challenging recognition scenarios (e.g., occlusion). We hope our findings can pave the way for future exploration in this direction, encouraging further research into superpixel-based visual representation learning.

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