
On the feasibility of small-data learning in simulation-driven engineering tasks with known mechanisms and effective data representations

Anonymous Author(s)

Affiliation

Address

email

Abstract

1 The application of machine learning (ML) in scientific tasks is increasing, especially
2 ML in simulation-driven engineering tasks. While previous studies were mostly
3 model-centric and required large-data learning, recent studies start to pay attention
4 to data-centric AI and are investigating small-data learning with effective structured
5 representations, which is significant for industrial application. This article provides
6 a theoretical discussion for the feasibility of small-data learning with structured
7 representations, which is then verified through the surrogate modelling of hot
8 stamping simulations. Future directions are also discussed.

9 1 Introduction

10 In the past decade, ML, particularly deep learning, has been successfully applied to general Artificial
11 Intelligence (AI) tasks, including object detection [1], semantic segmentation [2], and image
12 generation [3]. Recently, ML is being extended to scientific tasks, which can be broadly clas-
13 sified into mechanism-unknown tasks and mechanism-known tasks, as shown in Figure 1. In
14 mechanism-unknown tasks, ML can be applied to mathematically formulating the mechanisms, such
15 as ML-assisted material modelling [4][5], or explorative discovery with unknown or partly-unknown
16 mechanisms, such as discovering new materials [6] or drugs [7]; in mechanism-known tasks, also
17 known as simulation-driven engineering tasks, the mechanisms have been mathematically formulated
18 and integrated with simulation tools, such as finite element analysis (FEA), while ML is mainly
19 applied to surrogate-based optimisation [8]. A frequent observation is that the application of ML is
20 more convenient and practical in simulation-driven engineering tasks than in mechanism-unknown
21 tasks, since multi-scale simulation tools can generate data containing comprehensive info, such as
22 physical fields, that are difficult to obtain in experiments. Therefore, this article mainly focuses on
23 ML-assisted surrogate-based optimisation in simulation-driven engineering tasks.

24 In ML-assisted surrogate-based optimisation, while some studies replaced classical optimisers with
25 ML, such as reinforcement learning [9], most efforts have been devoted to improving the accuracy,
26 generalisability, and interpretability of surrogate models. Current ML with scalar representations
27 of both inputs and outputs, such as Kriging models [10][11], has been widely deployed. However,
28 these models are only suitable for low-dimension, single-parameterisation, scalar-output use cases,
29 while it is difficult to integrate data from multiple parameterisations or reuse historical data. To
30 improve the performance of ML-assisted surrogate models, including their flexibility, accuracy and
31 generalisability, recent studies have intensively investigated ML with structured representations, such
32 as fields [12] and graphs [13]. ML with structured representations was initially practiced in computa-
33 tional fluid dynamics (CFD), since Eulerian meshing, which is popular in most CFD tasks, can be
34 conveniently integrated with convolutional neural networks (CNN). Guo, Xu. et al. represented 2D or
35 3D geometries using signed distance functions (SDF) [14]. Based on the SDF field representations, a

36 CNN was trained to predict the full fields of 2D or 3D non-uniform steady laminar flow. ML with
 37 structured representations, which integrates advanced architectures such as recurrent neural networks
 38 (RNNs) and generative adversarial networks (GANs), has been applied to more complex CFD cases,
 39 including temporal prediction [15][16] and inverse design [17][18]. Based on the success in CFD
 40 cases, ML with structured representations has been extended to difficult use cases where non-Eulerian
 41 meshing is applied, including solid mechanics [19], structured optimisation [20][21], manufacturing
 [22][23][24], and meta-material design [25][26].

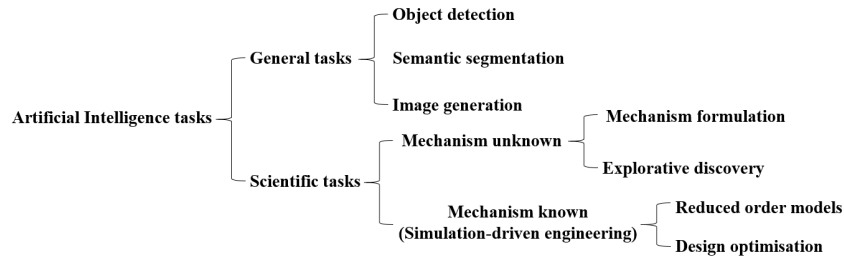


Figure 1: Classification of AI tasks.

42
 43 The ML-assisted surrogate models discussed above mainly employed full field-based representations,
 44 which significantly improved the overall performance of surrogate models. The previous studies dis-
 45 cussed above mostly pursued universally-generalised models, large-data training, and high-resolution
 46 full-field representations. Recent studies have started to investigate more effective structured repre-
 47 sentations, such as implicit shape parameterisation [27][28][29][30][31][32] and graphs [12][38];
 48 surrogate models are trained on datasets with task-specific sizes [33][34][35]. Despite the emerg-
 49 ing trend discussed above, only a few studies attempted to investigate the feasibility of small-data
 50 learning and the benefits of effective representations: Cao et al. showed that non-parametric input
 51 representation using graph neural network (GNN) and field-based output representation significantly
 52 improved the performance of surrogate models [12]; Li et al. significantly reduced the dataset size,
 53 which was acceptable for industrial practice and significantly facilitated multi-query optimisation,
 54 using wing mode representations [30][33].

55 In this article, the feasibility of small-data learning and the benefits of effective representations will be
 56 investigated based on the surrogate modelling of a case with application to hot stamping. In section 2,
 57 the feasibility and benefits will be discussed based on theoretical considerations. In section 3, a hot
 58 stamping case will be presented for verification. In section 4, current studies will be summarised and
 59 future directions will be pointed out.

60 2 Theoretical discussion

61 In this section, the feasibility of small-data learning in simulation-driven engineering tasks will be
 62 theoretically discussed by comparing these tasks with general tasks, and the benefits and criteria
 63 of effective representations will be discussed. The feasibility of small-data learning in mechan-
 64 ism-unknown tasks remains an open research question due to the lack of physical mechanisms, which is
 65 out of the scope of this article and requires further study.

66 2.1 The feasibility of small-data learning in simulation-driven engineering tasks

67 The definition of small-data and the required dataset size largely depends on specific tasks. In general
 68 tasks, millions of samples are required to ensure the performance of ML, such as ImageNet and Open
 69 Images. However, simulation-driven engineering tasks are expected to require much less data thanks
 70 to the following three attributes:

- 71 • From the input side, the design variables and corresponding domain in simulation-driven
 72 engineering tasks can be explicitly defined. For instance, in a stiffness-driven shape opti-
 73 misation task, the shape can be completely defined by a set of variables and uniformly
 74 generated using sampling strategies, such as Latin hypercube [37]. This ensures an effective
 75 coverage of the design space. However, in general tasks such as a multi-classification, it
 76 is nearly impossible to define the features of a certain class using explicit variables, not to

77 mention sampling strategies. In this case, large data is required to better cover the design
78 space of general tasks, while mode collapse still occurs.

- 79 • From the output side, in a multi-classification task, laborious labelling work is required
80 in supervised and semi-supervised learning. Furthermore, the labels are usually not em-
81 bedded in a mathematical metric space: it is nonsense to say 'cat' > 'dog' mathematically.
82 This might lead to highly nonlinear and complicated input-output mapping relationships.
83 However, the outputs of simulation-driven engineering tasks are mostly fields with inherent
84 mechanism driven patterns. Labelling work is rarely required while the outputs are in nature
85 mathematically comparable.
- 86 • Data in simulation-driven engineering tasks usually has a higher signal-to-noise ratio (SNR).
87 To clarify, a cat in a multi-classification task may be classed under diverse headings because
88 the image contains features such as eyes, irrelevant objects and background. This has a
89 negative effect on data quality and SNR. However, data in simulation-driven engineering
90 tasks, as long as the simulation model is verified and uncertainty is estimated, contains little
91 irrelevant information.

92 These advantageous attributes lead to smoother input-output mapping relationships and significantly
93 reduces the data requirement in simulation-driven engineering.

94 2.2 The benefits and criteria of effective data representations

95 Besides the natural attributes discussed above, proper representations are required to reduce dataset
96 sizes and improve the performance of surrogate models. Based on a case with application to stiffened
97 panel optimisation, Hao et al. demonstrated that field-based input shapes preserved the topological
98 information, compared with parametric representations [13]. To clarify, a shape usually consists of
99 multiple inter connected features, such as rounded corners, while the interconnection relationship
100 is lost if the shape is represented merely by the scalar feature parameters, such as radius. Based on
101 a cold forming case, Zhou et al. demonstrated that field-based output physical fields preserved the
102 data structure of physical fields compared with scalar performance indicators [36]. For example,
103 multiple thinning fields that have the same maximum thinning might differ in their locations, peak
104 number, and patterns. Overall, field-based representations have shown remarkable advantages over
105 conventional scalar representations in academia [12][13][33][36] and industry [38][40].

106 3 Case study: A field-based Artificial Intelligence empowered surrogate 107 model for a hot-stamped ultrahigh-strength-steel (UHSS) B-pillar

108 Small-data learning, which has been theoretically discussed in section 2, is verified based on the
109 surrogate model of a hot stamped B-pillar used in automotive applications. The simulation setup in
PAM-STAMP is shown in Figure 2, while the simulation model was experimentally verified [39].

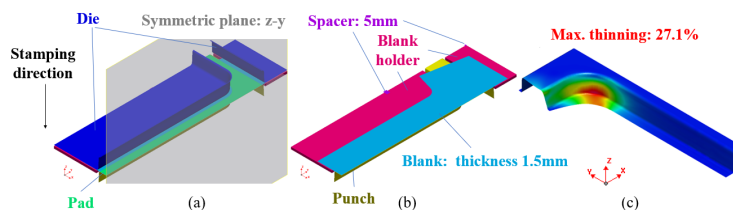


Figure 2: (a) Simulation model setup in PAM-STAMP (b) Initial blank (same model as (a)) while
hiding die, pad and symmetric (c) Predicted thinning field (A key manufacturing quality indicator).

110

111 3.1 Dataset and surrogate model setup

112 The surrogate model predicted the full blank thinning fields, which was mapped on the 2D initial
113 blank configuration, given the 2D images of die and blank. The design variables and domain are
114 demonstrated in Figure 3. A training set sized 64, which could be regarded as small-data, and a
115 validation set sized 256 were sampled from the design domain in Figure 3(b) using Latin hypercube

116 (LHS). Two samples in the 64-size training set and nine in the 256-size validation set had excessive
 117 thinning due to small draft angles ($<1.2^\circ$) or large height ($>65\text{mm}$). The FEA ground truth thinning
 118 fields of these samples were not reliable due to numerical errors when excessive thinning occurred.
 119 Since this study was not discussing failure and corresponding representations, these samples were
 removed, which led to a 62-size training set and a 247-size validation set. The surrogate model was

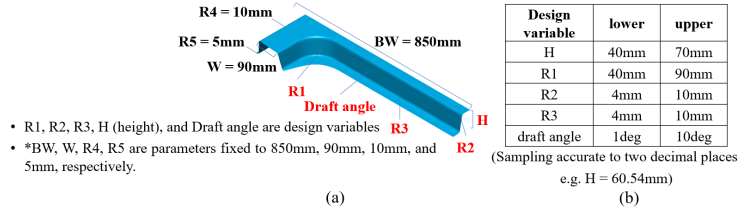


Figure 3: (a) Design variables set up (b) Design domain.

120 adapted based on a well-developed Res-SE-U-Net that is comprised of residual modules, squeeze-
 121 excitation modules, and skip connections [19][21][36]. The details of Res-SE-U-Net were discussed
 122 in [36]. For comparison with models that have scalar inputs/outputs, a Gaussian process (GP) model
 123 with anisotropic radius basis kernels was developed using Python/sklearn [13].
 124

125 3.2 Results and discussion

126 Res-SE-U-Net model was trained using combing mean square error (MSE) with batch size 2 and
 127 learning rate 0.0004, and GP model was fitted with optimised noise coefficient (0.02). Both models
 128 were validated on the 247-size validation set. As shown in Figure 4(a)(b), the violin plot of maximum
 129 thinning predicted by Res-SE-U-Net has a better consistency with the ground truth than that predicted
 130 by GP. For Res-SE-U-Net, the average absolute relative error of the maximum thinning (AREMT)

$$AREMT = |(ML\ prediction - FEA\ ground\ truth)/FEA\ ground\ truth| \times 100\% \quad (1)$$

131 was 3.77%, and 82.6% samples (204/247) had AREMT below 6%. For GP, the average AREMT
 132 was 5.30%, while only 72.3% samples had AREMT below 6%. In conclusion, Res-SE-U-Net trained
 133 on small data accurately and reliably predicted scalar maximum thinning even though maximum
 134 thinning was not explicitly included in MSE loss. A potential reason is that Res-SE-U-Net predicted
 135 the full thinning field that contained intrinsic physics, as shown in Figure 4(c). Predicting full fields
 also provides more guiding information to engineers.

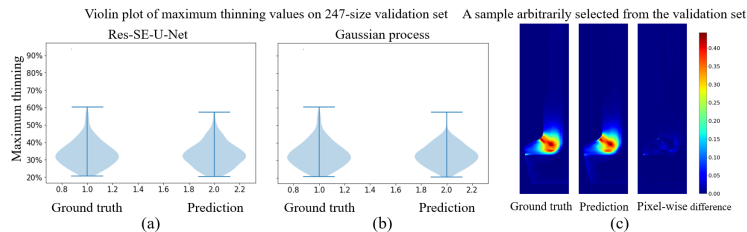


Figure 4: (a) Violin plot of maximum thinning predicted by Res-SE-U-Net (b) Violin plot of
 maximum thinning predicted by Gaussian process (c) Thinning fields of a validation sample.

136

137 4 Summary and future directions

138 In this study, small-data learning using field-based representations in simulation-driven engineering
 139 tasks was investigated and verified. The advantageous attributes that enable small-data learning were
 140 discussed in comparison with general tasks. In the case study, Res-SE-U-Net outperformed GP by
 141 leveraging the intrinsic physics in full thinning fields.

142 More studies on data-centric approaches in AI for science and engineering are expected in the future.
 143 Effective representations will be investigated. For example, a graph representation is preferred in a
 144 truss optimisation case since the truss contains only nodes and links [38]. Besides, active sampling,
 145 transfer learning, and physics-informed losses are promising to further facilitate small-data learning.

146 References

- 147 [1] Krizhevsky, A., Sutskever, I., & Hinton, G. E. (2012) ImageNet classification with deep convolutional neural
148 networks. *Advances in neural information processing systems*, 25: pp. 1097–1105.
- 149 [2] Jégou, S., Drozdal, M., Vazquez, D., Romero, A., & Bengio, Y. (2017) The one hundred layers tiramisu:
150 Fully convolutional densenets for semantic segmentation. *In Proceedings of the IEEE conference on computer
151 vision and pattern recognition workshops*, pp. 11–19.
- 152 [3] Goodfellow, I., Pouget-Abadie, J., Mirza, M., Xu, B., Warde-Farley, D., Ozair, S., Courville, A., & Bengio,
153 Y. (2014) Generative adversarial nets. *Advances in neural information processing systems*, 27.
- 154 [4] Diamantopoulou, M., Karathanasopoulos, N., & Mohr, D. (2021) Stress-strain response of polymers made
155 through two-photon lithography: micro-scale experiments and neural network modeling. *Additive Manufacturing*,
156 pp. 102266.
- 157 [5] Saha, S., Gan, Z., Cheng, L., Gao, J., Kafka, O. L., Xie, X., Li, H., Tajdari, M., Kim, H. A., & Liu, W. K.
158 (2021) Hierarchical deep learning neural networks (HiDeNN): An artificial intelligence (AI) framework for
159 computational science and engineering. *Computer Methods in Applied Mechanics and Engineering*, 373: pp.
160 113452.
- 161 [6] Chen, C., & Gu, G. X. (2019) Machine learning for composite materials. *MRS Communications* 9, no.2: pp.
162 556-566.
- 163 [7] Elbadawi, M., Gaisford, S., & Basit, A. W. (2021) Advanced machine-learning techniques in drug discovery.
164 *Drug Discovery Today* 26, no.3: pp. 769-777.
- 165 [8] Li, J., & Zhang, M. (2021) Data-based approach for wing shape design optimization. *Aerospace Science and
166 Technology*, 112: pp. 106639.
- 167 [9] Sun, H., & Ma, L. (2020) Generative design by using exploration approaches of reinforcement learning in
168 density-based structural topology optimisation. *Designs* 4, no.2: 10.
- 169 [10] Gao, F., Ren, S., Lin, C., Bai, Y., & Wang, W. (2018) Metamodel-based multi-objective reliable optimisation
170 for front structure of electric vehicle. *Automotive Innovation* 1, no.2: pp. 131-139.
- 171 [11] Tao, S., van Beek, A., Apley, D. W., & Chen, W. (2021) Multi-model Bayesian optimisation for simulation-
172 based design. *ASME.J.Mech.Des.* 143, no.11: pp. 111701.
- 173 [12] Cao, J., Li, Q., Xu, L., Yang, R., & Dai, Y. (2021) Non-parametric surrogate model method based on
174 machine learning. *preprint*.
- 175 [13] Hao, P. Liu, D., Zhang, K., Yuan, Y., Wang, B., Li, G., & Zhang, X. (2021) Intelligent layout design of
176 curvilinearly stiffened panels via deep learning-based method. *Materials & Design* 197: pp. 109180.
- 177 [14] Guo, X., Li, W., & Iorio, F. (2016) Convolutional neural networks for steady flow approximation. *In
178 Proceedings of the 22nd ACM SIGKDD international conference on knowledge discovery and data mining*: pp.
179 481-490.
- 180 [15] Thuereym, N., Weißenow, K., Prantl, L., & Hu, X. (2020) Deep learning methods for Reynolds-Averaged
181 Navier-Stokes simulations of airfoil flows. *AIAA JOURNAL* 58, no.1: pp. 25-36.
- 182 [16] Lee, S., & You, D. (2019) Data-driven prediction of unsteady flow over a circular cylinder using deep
183 learning. *J. Fluids. Mech.* 879: pp. 217-254.
- 184 [17] Sekar, V., Zhang, M., Shu, C., & Khoo, B. C. (2019) Inverse design of airfoil using a deep convolutional
185 neural network. *AIAA JOURNAL* 57, no.3: pp. 993-1003.
- 186 [18] Wang, Z., Xiao, D., Fang, F., Govindan, R., Pain, C. C., & Guo, Y. (2018) Model identification of reduced
187 order fluid dynamics systems using deep learning. *International Journal for Numerical Methods in Fluids* 86,
188 no.4: pp. 255-268.
- 189 [19] Nie, Z., Jiang, H., & Kara, L. B. (2019) Stress field prediction in cantilevered structures using convolutional
190 neural networks. *In International Design Engineering Technical Conferences and Computers and Information in
191 Engineering Conference* 20, no.1: pp. 011002.
- 192 [20] Oh, S., Jung, Y., Kim, S., Lee, I., & Kang, N. (2019) Deep generative design: Integration of topology
193 optimisation and generative models. *Journal of Mechanical Design* 141, no.11.
- 194 [21] Nie, Z., Lin, T., Jiang, H., & Kara, L. B. (2021) TopologyGAN: Topology optimisation using generative
195 adversarial networks based on physical fields over the initial domain. *ASME. J. Mech. Des.* 143, no.3: pp.
196 031715.

- 197 [22] Zimmerling, C., Trippe, D., Fengler, B., & Kärger, L. (2019) An approach for rapid prediction of textile
198 draping results for variable composite component geometries using deep neural networks. *In AIP Conference*
199 *Proceedings 2113, no.1*: pp. 020007.
- 200 [23] Zimmerling, C., Poppe, C., & Kärger, L. (2019) Virtual product development using simulation methods and
201 AI. *Lightweight Design worldwide 12, no.6*: pp. 12-19.
- 202 [24] Zimmerling, C., Poppe, C., & Kärger, L. (2020) Estimating optimum process parameters in textile draping
203 of variable part geometries-A reinforcement learning approach. *Procedia Manufacturing 47*: pp. 847-854.
- 204 [25] Xue, T., Wallin, T. J., Menguc, Y., Adriaenssens, S., & Chiramonte, M. (2020) Machine learning generative
205 models fo automatic design of multi-material 3D printed composite solids. *Extreme Mechanics Letters 41*: pp.
206 100992.
- 207 [26] Wang, L., Chan, Y., Ahmed, F., Liu, Z., Zhu, P., & Chen, W. (2020) Deep generative modeling for
208 mechanistic-based learning and design of metamaterial systems. *Comput. Methods Appl. Mech. Engrg.* 372: pp.
209 113377.
- 210 [27] Park, J. J., Florence, P., Straub, J., Newcombe, R., & Lovegrove, S. (2019) DeepSDF: Learning continuous
211 signed distance functions for shape representation. *In Proceedings of the IEEE/CVF Conference on Computer*
212 *Vision and Pattern Recognition*: pp. 165-174.
- 213 [28] Remelli, E., Lukoianov, A., Richter, S. R., Guillard, B., Bagautdinov, T., Baque, P., & Fua, P. (2020)
214 MeshSDF: Differentiable iso-surface extraction. *34th Conference on Neural Information Processing Systems*
215 *(NeurIPS 2020)*
- 216 [29] Guillard, B., Remelli, E., Lukoianov, A., Richter, S., Bagautdinov, T., & Baque, P. (2021) DeepMesh:
217 Differentiable iso-surface extraction. *arXiv:2106.11795v1*.
- 218 [30] Li, J., & Zhang, M. (2021) Adjoint-free aerodynamic shape optimisation of the common research model
219 wing. *AIAA JOURNAL 59, no.6*: pp. 1990-2000.
- 220 [31] Masters, D. A., Taylor, N. J., Rendall, T. C. S., Allen, C. B., & Poole, D. J. (2017) Geometric comparison of
221 aerofoil shape parameterization methods. *AIAA JOURNAL 55, no.5*: pp. 1575-1589.
- 222 [32] Kohar, C. P., Greve, L., Eller, T. K., Connolly, D. S., & Inal, K. (2021) A machine learning framework for
223 accelerating the design process using CAE simulations: An application to finite element analysis in structural
224 crashworthiness. *Comput. Methods Appl. Mech. Engrg.* 385: pp. 114008.
- 225 [33] Li, J., & Zhang, M. (2020) Efficient aerodynamic shape optimization with deep-learning-based geometric
226 filtering. *AIAA JOURNAL 58, no.10*: pp. 4243-4259.
- 227 [34] Li, J., & Zhang, M. (2021) Data-based approach for wing shape design optimization. *Aerospace Science*
228 *and Technology 112*: pp. 106639.
- 229 [35] Lye, K. O., Mishra, S., Ray, D., & Chandrashekar, P. (2021) Iterative surrogate model optimization (ISMO):
230 An active learning algorithm for PDE constrained optimization with deep neural networks. *Comput. Methods*
231 *Appl. Mech. Engrg.* 374: pp. 113575.
- 232 [36] Zhou, H., Xu, Q., Nie, Z., & Li, N. (2021) A study on using image-based machine learning methods to
233 develop surrogate models of stamp formign simulations. *Journal of Manufacturing Science and Engineering*
234 *144*: pp. 021012.
- 235 [37] Bogoclu, C., Roos, D., & Nestorović, T. (2021) Local Latin hypercube refinement for multi-objective design
236 uncertainty optimisation. *Applied Soft Computing*: pp. 107807.
- 237 [38] Chang, K., & Cheng, C. (2020) Learning to simulation and design for structural engineering. *In International*
238 *Conference on Machine Learning*: pp. 1426-1436, PMLR.
- 239 [39] Ganapathy, M., Li, N., Lin, J., Abspoel, M., & Bhattacharjee, D. (2019) Experimental investigation of a new
240 low-temperature hot stamping process for boron steels. *The International Journal of Advanced Manufacturing*
241 *Technology 105*: pp. 669-682.
- 242 [40] Pongetti, J., Kipouros, T., Emmanuelli, M., Ahlfeld, R., & Shahpar, S. (2021) Using autoencoders and
243 output consolidation to improved machine learning for turbomachinery applications. *Proceedings of the ASME*
244 *2021 Turbomachinery Technical Conference & Exposition*.