LANGUAGE MODELS ARE GOOD TABULAR LEARNERS

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ABSTRACT

Transformer-based language models have become the de facto standard in natural language processing. However, they underperform in the tabular data domain compared to traditional tree-based methods. We posit that current models fail to achieve the full potential of language models due to (i) heterogeneity of tabular data; and (ii) challenges faced by the model in interpreting numerical values. Based on this hypothesis, we propose the *Tabular Domain Transformer* (TDTransformer) framework. TDTransformer has distinct embedding processes for different types of columns. The alignment layers for different column-types transform these embeddings to a common space. Besides, TDTransformer adapts piece-wise linear encoding for numerical values for better performance. We test the proposed method on 76 real-world tabular classification datasets from the OpenML benchmark. Extensive experiments indicate that TDTransformer significantly improves the state-of-the-art methods. We release our code in `https://anonymous.4open.science/r/tdtransformer`.

1 INTRODUCTION

Deep learning methods have achieved state-of-the-art (SOTA) performance in various areas including vision (Rombach et al., 2022; He et al., 2022; Zou et al., 2024), language (Radford et al., 2019; Touvron et al., 2023), and multimodal processing (Radford et al., 2021; Liu et al., 2023). Even though deep learning methods have shown great potential in many domains, their performance for tabular data has so far been unimpressive. This has led to the question as to whether deep learning is a fundamentally superior approach for tabular data (Shwartz-Ziv & Armon, 2022; Grinsztajn et al., 2022; Borisov et al., 2022; McElfresh et al., 2024). Experimental benchmarks (Grinsztajn et al., 2022; Borisov et al., 2022) have shown the broad superiority of tree-based methods over deep learning. Among deep learning methods, the generalization of transformer-based architectures (Vaswani et al., 2017) to tabular data has shown some promise — however, they continue to lag tree-based methods such as XGBoost (Chen & Guestrin, 2016).

The broad-based success of transformers in learning high-dimensional representations, especially in NLP, is evidence of their potential. A natural question arises as to *what makes transformer-based architectures underperform tree-based methods*. Based on prior studies, we posit that this phenomenon is a result of (i) difficulty in learning irregular patterns of the target function owing to data heterogeneity (Shwartz-Ziv & Armon, 2022; Mathov et al., 2022; Borisov et al., 2023; Yan et al., 2023; Chen et al., 2024a), and (ii) the challenges faced by the model in interpreting numerical features (Gorishniy et al., 2021; 2022).

On the one hand, spectral analysis of neural networks indicates that neural networks tend to learn the low-frequency components of a function in lieu of relatively high-frequency components (Rahaman et al., 2019; Xu et al., 2019; Beyazit et al., 2024). Owing to the different types of columns, the feature spaces in the tabular data domain are generally heterogeneous. On the other hand, numerical reasoning is known to be a formidable challenge for language models (Lu et al., 2022; Lee et al., 2023; Shen et al., 2023; Testolin, 2024; Ahn et al., 2024).

We propose a framework named **T**abular **D**omain **Transformer** (TDTransformer) that overcomes the aforementioned obstacles in the way of achieving the full potential of transformer-based architectures. TDTransformer embeds different types of table columns using different approaches to obtain the hidden representations. For each column type, we use an alignment layer to map the hidden representation to a common embedding space. Alignment layers for different column types are

independent of one another. This design is inspired by multimodal models such as CLIP (Radford et al., 2021) where one alignment layer transforms the hidden dimension of the image branch d_i to a dimension d, $\psi_i : d_i \rightarrow d$. The other one transforms the hidden dimension of the text branch d_t to d, $\psi_t : d_t \rightarrow d$. To enhance the model's understanding of numerical values, we use a piecewise linear encoding (PLE) that directly maps scalars to high-dimensional embeddings. Compared to conventional tokenization and embedding, PLE introduces an inductive bias that is beneficial to the training process. Our use of the PLE is inspired by the pioneering work of (Gorishniy et al., 2022). We adapt PLE such that the hidden representation is close to the conventional hidden representation of transformer-based architectures. We combine hidden representations as the input to the backbone model. The pipeline of the training process is the pre-training model followed by fine-tuning.

We examine the performance of TDTransformer on the standard tabular data benchmark OpenML [1]. Extensive experiments on more than 70 tabular data sets show the superiority of TDTransformer. In summary, the main contributions of this work are as follows:

- To avoid the performance degradation caused by the heterogeneous nature of tabular data, we design different embedding approaches to obtain the hidden representations of columns. Alignment layers are applied to hidden representations to ensure that embeddings for different types of columns are in the same embedding space.
- We adapt the piece-wise linear encoding to improve the representation of numerical values so that the model can interpret them well. These encoded representations are combined with those of categorical and binary columns and then input to the backbone model.
- We propose a column-type dependent corruption for pre-training. We also propose a column-type-aware positional encoding that further boosts the performance of TDTransformer.

2 Related Work

Tabular deep learning A key line of work in tabular deep learning focuses on the use of graph learning to enhance the understanding of relations among columns. An auxiliary knowledge graph is used to regularize a multilayer perceptron (Ruiz et al., 2024). (Chen et al., 2024b) utilizes a hypergraph to capture tabular structures. With the development of large-scale foundational models, significant research has emerged on adapting foundation models in the tabular data domain. (Zhang et al., 2023) uses parameter-efficient fine-tuning to adapt the pre-trained LLaMA 2 model to the tabular domain (Touvron et al., 2023). (Zhu et al., 2024) converts tables to formats that are consistent with the pre-training data (*e.g.* markdown format). The converted input data are directly fed to the pre-trained LLaMA 2 model (Touvron et al., 2023). (Deng et al., 2024) treat tables as images and utilize the multimodal capability of GPT-4 (Achiam et al., 2023) and Gemini (Team et al., 2023). (Hegselmann et al., 2023) serializes column names and values into a natural language string. Input strings are used for fine-tuning pre-trained large language models.

Numerical reasoning Large language models mainly focus on NLP and code generation. However, their application to numerical reasoning has turned out to be less successful (Lewkowycz et al., 2022; Imani et al., 2023; Ahn et al., 2024; Romera-Paredes et al., 2024). This difficulty arises for multiple reasons: (i) numerical reasoning might require intricate intermediate steps internally. Language models map scalars to high-dimensional embeddings. The intermediate steps with high dimensional embeddings turn out to be inractable; (ii) there is no built-in mechanism within transformer-based architectures to perform mathematical operations; (iii) numerical values are continuous, whereas transformer-based architectures are inherently designed for (discrete) word toens; (iv) there are repeated patterns in tokenized numerical values, and each token holds equal significance (while omitting unimportant tokens).

(Geva et al., 2020) enhances numerical reasoning by adding automatically generated synthetic numerical data to the pre-training process. (Lee et al., 2023) incorprates ideas from chain-of-thought (Wei et al., 2022), with intermediate step results. (Shen et al., 2023) focuses on data format modification to the boost model's understanding of numerical values. (McLeish et al., 2024) helps models track the position of each digit by adding an embedding that encodes its relative position.

[1] OpenML benchmark: `https://www.openml.org/`

3 TDTRANSFORMER: TABULAR DATA TRANSFORMER FRAMEWORK

Task formulation Tabular data are denoted as $\mathcal{D} = \{(x_i, y_i)\}_{i=1}^n$, $x \in \mathbb{X}$, $y \in \mathbb{Y}$. The dataset is split into 3 disjoint subsets $D = D_{\text{train}} \cup D_{\text{val}} \cup D_{\text{test}}$. $\mathbb{Y} = \{0, 1\}$ for the binary classification task, $\mathbb{Y} = \{1, \ldots, C\}$ for the multiclass classification task. The supervised training process maximizes the likelihood of the correct label y:

$$\max_{\boldsymbol{\theta}} \mathbb{P}_{\boldsymbol{\theta}}(y|\mathbf{x}, \boldsymbol{\theta}) \ . \tag{1}$$

Figure 1 shows the proposed framework. Input data are relational tables that have a unique column given a column name. We use different embedding processes for different types of columns. Alignment layers are used to transform embeddings to the same embedding space. We combine embeddings as the input to the backbone model. The training pipeline consists of pre-training and fine-tuning steps.

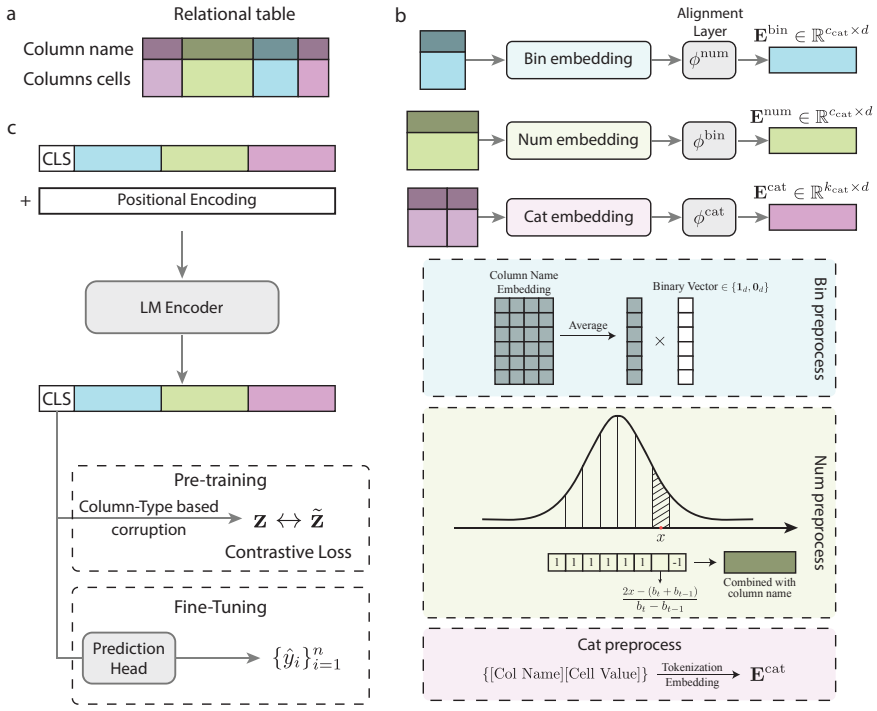

Figure 1: The TDTransformer framework: (a) Input data $\mathcal{D} = \{(x_i, y_i)\}_{i=1}^n$. x consists of column name and column cells. (b) Embeddings of three types of columns (categorical, numerical, and binary). (c) Concatenation of the three types of embeddings, which is fed into the backbone model.

3.1 COLUMN EMBEDDINGS

The TDTransformer framework uses distinct embedding processes for categorical, numerical, and binary columns. These processes are illustrated in Figure 1 (b) and discussed in detail below:

Embedding Categorical Columns For categorical columns, we concatenate column names and corresponding cell values to form natural language sentences. The concatenated sentence is tokenized and embedded to obtain hidden representations for the categorical columns denoted by $\mathbf{E}^{\text{cat}}$:

$$\mathbf{E}^{\text{cat}} = [\mathbf{E}_{\mathbf{1}}, \ldots, \mathbf{E}_{c_{\text{cat}}}] \in \mathbb{R}^{k_{\text{cat}} \times d}, \quad \mathbf{E}_i = \left[e([T^{\text{col}}_{1:m_1(i)}]), e([T^{\text{cell}}_{1:m_2(i)}])\right] , \tag{2}$$

where d is the dimension of hidden representations. $k_{\text{cat}} = \sum_{i=1}^{c_{\text{cat}}} \left(\left| [T^{\text{col}}_{1:m_1(i)}] \right| + \left| [T^{\text{cell}}_{1:m_2(i)}] \right| \right)$ is the total number of tokens. $m_1(i)$ is the number of tokens for i-th categorical column name. $m_2(i)$ is the number of tokens for cell values in i-th categorical column. After embedding, we use a linear transformation layer $\phi^{\text{cat}} : \mathbb{R}^d \to \mathbb{R}^d$.

Embedding Numerical Columns We adapt the PLE in (Gorishniy et al., 2022) for transformer-based architectures. Specifically, we use the PLE function $f_{\text{ple}} : \mathbb{R} \to \mathbb{R}^{d_{\text{ple}}}$ to obtain the hidden representation for numerical columns:

$$f_{\text{ple}}(x) = [\xi_1, \ldots, \xi_n]^T \in \mathbb{R}^{d_{\text{ple}}} . \tag{3}$$

$$\xi_i = \begin{cases} -1, & x < b_{t-1} \\ 1, & x > b_t \\ \frac{2x-(b_t+b_{t-1})}{b_t-b_{t-1}}. & b_{t-1} \leq x \leq b_t \end{cases} \tag{4}$$

Here, the bins $\{b_t\}_{t=1}^{d_{\text{ple}}}$ are obtained based on the q-quantiles of the numerical value range while the original PLE work requires labels for fitting decision trees. d_{ple} is the number of quantiles. We summarize differences for the numerical value embedding in Table 1. The conventional tokenization and embedding in language models can map a scalar to a sequence of embeddings if there are multiple digits in the scalar. On the contrary, PLE always maps a scalar to one embedding. Our method relies on the distribution of cell values and not conditions on labels. Besides, due to the layer normalization (LN) (Ba, 2016) within the embedding layer, codomain of $[-1, 1]$ for our adapted PLE function is closer to the embedding than the that of $[0, 1]$.

Table 1: Summary of the differences among methods obtaining embeddings of numerical values. Embedding of a numerical value is essentially a high-dimensional vector $\mathbf{v}$.

Method	v_i range	Not require labels	Fixed sequence length
Tokenization + Embedding	$(-\infty, \infty)$	✓	×
PLE (Gorishniy et al., 2022)	[0, 1]	×	✓
PLE (Ours)	[-1, 1]	✓	✓

We use a linear transformation layer $\phi^{\text{num}} : \mathbb{R}^{\text{ple}} \to \mathbb{R}^d$ to convert the high-dimensional representations $f_{\text{ple}}(x) \in \mathbb{R}^{\text{ple}}$ to the same embedding space as that of categorical column embeddings.

The hidden representation for numerical columns is obtained by the Hadamard product of the averaged column-name embedding and numerical-value embeddings:

$$\mathbf{E}^{\text{num}} = \mathbf{E}^{\text{num}}_{\text{col}} \circ \phi^{\text{num}}([f_{\text{ple}}(x_1), \ldots, f_{\text{ple}}(x_{c_{\text{num}}})]) \in \mathbb{R}^{c_{\text{num}} \times d} . \tag{5}$$

$$\mathbf{E}^{\text{num}}_{\text{col}} = [\mathbf{E}_1, \ldots, \mathbf{E}_{c_{\text{num}}}], \quad \mathbf{E}_i = \frac{1}{m_1(i)} \sum_{j=1}^{m_1(i)} e([T^{\text{col}}_{1:m_1(i)}]) \circ \mathcal{M} , \tag{6}$$

Here, $\mathcal{M}$ is the attention mask to exclude padding token embeddings. For notational conciseness we ignore the notation of column types in the expressions of word tokens of column names and cell values. For example, we use the same notation $[T^{\text{col}}_{1:m_1(i)}]$ in Equations 2 and 6. The notation $[T^{\text{col}}_{1:m_1(i)}]$ denotes the word tokens for numerical column names in the former, whereas it denotes the word tokens for categorical column names in the latter.

Embedding Binary columns We convert cell values (*e.g.* True vs False and 0 vs 1) in binary columns to binary values $x_i \in \{0, 1\}$. Similar to numerical columns, the column-name embedding for each binary column is averaged. The hidden representation for binary columns is obtained by the Hadamard product of the averaged column name embedding and binary values as follows:

$$\mathbf{E}^{\text{bin}} = \mathbf{E}^{\text{bin}}_{\text{col}} \circ (\mathbf{x}(\mathbf{1}_d)^T) \in \mathbb{R}^{c_{\text{bin}} \times d}, \text{ where } \mathbf{x} = [x_1, \ldots, x_{c_{\text{bin}}}]^T . \tag{7}$$

We use a linear transformation layer $\phi^{\text{bin}} : d \to d$ to ensure the embeddings of binary columns are the same as those of categorical columns and numerical columns.

3.2 FEATURE COMBINATION

Figure 1 (c) shows the combination of features for three types of columns. We prepend `[CLS]` embedding to the concatenated hidden representations. As in the classialc transformer model (Vaswani et al., 2017), we add the sinusoidal positional encoding $\mathbf{P}$ to the concatenated hidden representation:

$$\mathbf{E} = [e([\text{CLS}]), \mathbf{E}^{\text{bin}}, \mathbf{E}^{\text{num}}, \mathbf{E}^{\text{cat}}] + \mathbf{P} \ , \tag{8}$$

where

$$\mathbf{P}_{(j,2i)} = \sin(j/10000^{2i/d}) \ , \tag{9a}$$

$$\mathbf{P}_{(j,2i+1)} = \cos(j/10000^{2i/d}) \ . \tag{9b}$$

Here, j is the position index and i is the hidden dimension index. Only $\mathbf{E}^{\text{cat}}$ has a flexible sequence length. $\mathbf{E}^{\text{bin}}$ and $\mathbf{E}^{\text{num}}$ have a fixed sequence length. The sequence length for $\mathbf{E}^{\text{bin}}$ or $\mathbf{E}^{\text{num}}$ is equal to the number of binary columns or numerical columns. Given a fixed context length limit, TDTransformer can process larger tables (without truncation) as compared to language models that do tokenization and embedding for all types of columns.

In language models, positional encoding or positional embedding are added to the embedding in element-wise fashion. In tabular data domains, however, table columns have the permutation invariance property that prevents positinal encodings from improving performance (Huang et al., 2020). In TDTransformer, although the hidden representations for the binary columns ($\mathbf{E}_i^{\text{bin}} \in \mathbb{R}^d$) and that for the numerical columns ($\mathbf{E}_i^{\text{num}} \in \mathbb{R}^d$), there is indeed an ordering in $\mathbf{E}^{\text{cat}}$, because it is essentially the embedding of a natural language sentence. Therefore, we propose a column-type aware (CTA) position encoding for TDTransformer. CTA only adds positional encoding to $\mathbf{E}^{\text{cat}}$. The overall embedding $\mathbf{E}$ is computed as follows:

$$\mathbf{E} = [e([\text{CLS}]), \mathbf{E}^{\text{bin}}, \mathbf{E}^{\text{num}}, \mathbf{E}^{\text{cat}}] + [\mathbf{0}_{(c_{\text{bin}}+c_{\text{num}})\times d}, \mathbf{P}] \ . \tag{10}$$

3.3 TRAINING PIPELINE

After combining column embeddings, $\mathbf{E}$ is fed to the backbone model, which is constructed using the gated transformer proposed in (Wang & Sun, 2022). We also test the performance using RoBERTa (Liu, 2019) as the backbone model (see Appendix). `[CLS]` embedding is used for the prediction. The training pipeline, similar to the classic pre-training fine-tuning paradigm, consists of two steps: the first step is to pre-train the model. The second step is to fine-tune the model that is initialized with pre-trained weights. Corruption is used to generate negative samples. The corruption method conditions on column types, because random permutation only occurs within the same type of column. We do not apply permutations for binary columns.

After the contextualization in LM encoder $\mathcal{F}(\cdot)$, we obtain the resulting embedding $\mathbf{E}^{'} = \mathcal{F}(\mathbf{E})$. We use the `[CLS]` embedding in $\mathbf{E}^{'}$ as shown in Figure 1 (c). The `[CLS]` embedding used for the prediction is denoted as $\mathbf{z}$. Given a table row $\mathbf{z}_i$, there is a hidden representation $\mathbf{z}_i$.

The pre-training process uses contrastive loss. Specifically, we examine two types of pre-training losses: self-supervised contrastive loss (e.g., (Chen et al., 2020; Tian et al., 2020; Wang et al., 2021)) and supervised contrastive loss (e.g., (Khosla et al., 2020; Jaiswal et al., 2020; Le-Khac et al., 2020)). The contrastive loss function encourages the model to generate close embeddings for positive pairs. The self-supervised pre-training focuses on the category-level discrimination while self-supervised pre-training pays attention to the instance-level discrimination.

The self-supervised contrastive loss (SSCL) is computed as follows:

$$\mathcal{L}^{\text{SSCL}} = -\sum_{i\in\mathcal{I}} \log \frac{\exp(\mathbf{z}_i^T \tilde{\mathbf{z}}_i/\tau)}{\sum_{j\in\mathcal{I}} \exp(\mathbf{z}_i^T \tilde{\mathbf{z}}_j/\tau)} \ , \tag{11}$$

where τ is the temperature, $\mathcal{I} = \{i\}_{i=1}^n$, $\mathbf{z}_i$ is the hidden representation for i-th table row, and $\tilde{\mathbf{z}}_i$ is the hidden representation of the corrupted i-th table row.

The supervised contrastive loss (SCL) utilizes labels in the pre-training dataset and is computed as follows:

$$\mathcal{L}^{\text{SCL}} = \sum_{i\in\mathcal{I}} \frac{-1}{P(i)} \log \sum_{k\in P(i)} \frac{\exp(\mathbf{z}_i^T \tilde{\mathbf{z}}_k/\tau)}{\sum_{j\in\mathcal{I}} \exp(\mathbf{z}_i^T \tilde{\mathbf{z}}_j/\tau)} \ , \tag{12}$$

where $P(i) := \{p|y_p = y_i\}$. SCL is found to be a powerful pre-training tool. For example, it can achieve in-context learning in decision-making problems (Lee et al., 2024) and learn data with long-tailed distributions (Li et al., 2022).

Table 2: Performance comparison for the binary classification task. In addition to the averaged performance, we select a subset of 76 tables for detailed comparison. $\mathcal{S} \cup \mathcal{S}_{\text{num}}$ contains tables including numerical columns. γ is the positive ratio.

Method	$\mathcal{S} \cup \mathcal{S}_{\text{num}}$		$\gamma \leq 0.2$		$0.2 < \gamma < 0.8$		$\gamma \geq 0.8$		Avg	
	Acc	Auc	Acc	Auc	Acc	Auc	Acc	Auc	Acc	Auc
XGBoost	85.06	0.83	91.88	**0.87**	78.44	0.82	95.10	0.73	84.97	0.83
CatBoost	86.27	0.86	**91.90**	**0.87**	80.66	0.87	94.51	0.87	86.12	0.87
SCARF	77.27	0.73	83.84	0.72	73.64	0.78	72.10	0.55	77.81	0.74
SwitchTab	74.32	0.78	79.67	0.80	69.89	0.78	89.05	0.74	75.03	0.78
SubTab	71.94	0.74	75.44	0.74	69.79	0.75	72.59	0.68	72.30	0.75
TransTab	84.83	0.81	91.20	0.83	79.74	0.82	95.45	0.83	85.39	0.82
TDTransformer	**87.56**	**0.87**	91.67	**0.87**	**83.94**	**0.88**	95.40	**0.96**	**87.79**	**0.88**
TDTransformer (CTA Pos)	87.19	**0.87**	91.70	**0.87**	83.30	0.87	**95.59**	0.94	87.48	0.87

Table 3: Performance comparison for the multiclass classification task. In addition to the averaged performance, we select a subset of 76 tables for detailed comparison. $\mathcal{S} \cup \mathcal{S}_{\text{num}}$ contains tables including numerical columns. $|\mathcal{D}|$ is the dataset size, $\mathfrak{C}$ is the number of classes.

Method	$\mathcal{S} \cup \mathcal{S}_{\text{num}}$		$\lvert\mathcal{D}\rvert < 2000$		$\lvert\mathcal{D}\rvert \geq 2000$		$\mathfrak{C} < 10$		$\mathfrak{C} \geq 10$		Avg	
	Acc	F1	Acc	F1	Acc	F1	Acc	F1	Acc	F1	Acc	F1
XGBoost	72.56	0.60	65.77	0.56	**82.20**	**0.71**	79.32	0.64	71.12	0.69	76.45	0.66
CatBoost	73.03	0.59	66.68	0.56	81.97	0.70	79.32	0.63	71.59	0.69	76.61	0.65
SCARF	62.39	0.52	57.58	0.44	69.51	0.61	67.75	0.53	60.82	0.59	65.32	0.55
SwitchTab	56.92	0.45	57.56	0.45	62.29	0.52	64.93	0.50	52.65	0.49	60.63	0.50
SubTab	55.22	0.45	55.98	0.44	60.77	0.52	60.99	0.48	55.57	0.53	59.09	0.50
TransTab	70.22	0.53	70.38	0.53	69.96	0.52	71.79	0.49	66.98	0.63	70.11	0.54
TDTransformer	76.30	**0.63**	78.68	**0.69**	81.06	0.70	80.89	**0.65**	79.00	**0.77**	80.23	**0.70**
TDTransformer (CTA Pos)	**76.70**	**0.63**	**78.94**	**0.69**	81.36	0.70	**81.07**	**0.65**	**79.47**	**0.77**	**80.51**	**0.70**

The model weight after the pre-training process is used as the initialized weight for the fine-tuning. A prediction head is added to predict the probability of each class. The fine-tuning process is in a supervised fashion. For the binary classification task, we use the binary cross entropy loss. The multiclass classification task employs the cross entropy loss.

4 Experiments and Results

4.1 Experiments

Baseline methods XGboost (Chen & Guestrin, 2016) is an end-to-end tree boosting system. It uses a sparsity-aware algorithm and weighted quantile sketch. Compared to XGBoost, CatBoost (Prokhorenkova et al., 2018; Dorogush et al., 2018) has the inherent capability to process categorical features without relying on one-hot encoding. Besides, it introduces ordered boosting to avoid target leakage. SubTab (Ucar et al., 2021) divides input features into multiple subsets to perform multiview representation learning. Scarf (Bahri et al., 2022) uses vanilla self-supervised contrastive learning to improve classification accuracy in the fully-supervised learning setting. SwitchTab (Wu et al., 2024) uses an asymmetric encoder-decoder framework to decouple mutual and salient features, which can address the issue of lacking dependencies between samples.

Datasets We use 56 real-world tabular classification datasets in the standard OpenML benchmark (which are manually curated for effective benchmarking). The train/validation/test splits is 72%/8%/20% for each OpenML dataset. We use accuracy as the metric to measure the performance for all classification data sets. Additionally, we use the area under the curve (AUC) to evaluate binary classification and the F1 score t evaluate multiclass classification. The details of the tables are given in Section A.3 of the Appendix.

Experimental details TDTransformer uses pre-trained BERT tokenizer (Devlin, 2018) and Adam optimizer (Kingma, 2014) without weight decay. The hidden dimension is 512 and model depth is 12. The number of quantiles for PLE is 64. In both the pre-training and fine-tuning process, we use an early stopping strategy (Yao et al., 2007) with a patience of 10. The maximum number of training epochs is 200 with batch size of 128. The corruption parameter of pre-training process is set to 0.5. When there are empty cells in a column, we replace empty cells with the most common values in that column. We conducted all epxeriments using a single A40 Tensor Core GPU and EPYC 7232P CPU.

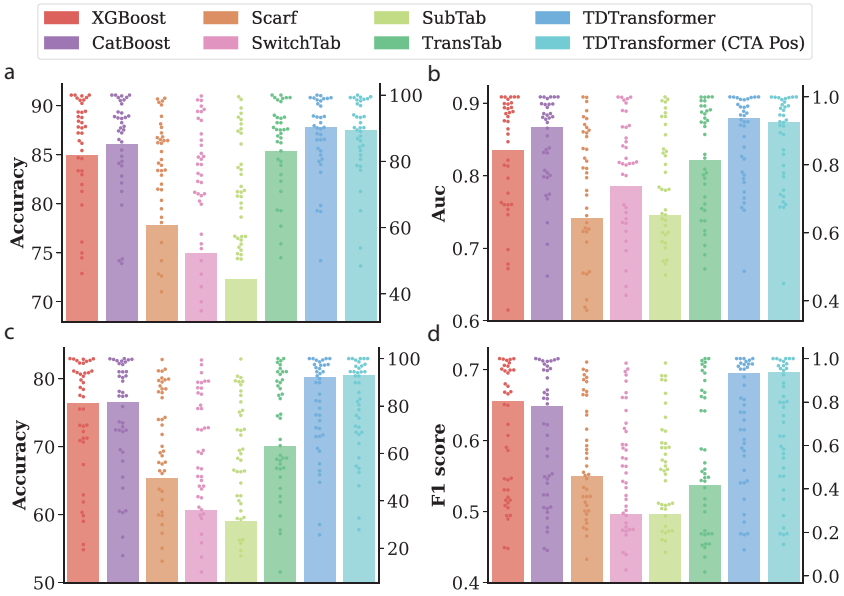

Figure 2: Performance comparison: The left axis shows the scale for (average) performance. The right axis shows the scale for the performance on individual datasets. (a) Test accuracy for the binary classification task. (b) AUC score for the binary classification task. (c) Test accuracy for the multiclass classification task. (d) F1 score for the multiclass classification task. TDTransformer significantly outperforms baselines with greater improvements achieved for multiclass classification.

4.2 Results

Table 2 summarizes the performance comparison for the binary classification task. SSCL is used in the pre-training process. We denote categorical columns as $\mathcal{S}_{\text{cat}}$, binary columns as $\mathcal{S}_{\text{bin}}$, and numerical columns as $\mathcal{S}_{\text{num}}$. We use the notation $\mathcal{S}$ for generic table columns, $\mathcal{S} \subseteq (\mathcal{S}_{\text{num}} \cup \mathcal{S}_{\text{cat}} \cup \mathcal{S}_{\text{bin}})$. Note that $\mathcal{S}$ can be $\emptyset$. In addition to select subsets of tabular data based on column types, we use the positive ratio to make a selection. The positive ratio γ is the ratio of positive samples to the entire number of samples. Generally, a positive ratio range $0.2 < \gamma < 0.8$ is the more challenging than the positive ratio range $\gamma \leq 0.2$ and $\gamma \geq 0.8$. We find that TDTransformer has a relatively large performance gain in that range compared to baseline methods. The accuracy for $0.2 < \gamma < 0.8$ increases by 3.38%. Overall, both TDTransformer exhibits significantly better performance (with or without CTA positional encoding).

The performance comparison for the multiclass classification task is shown in Table 3. We use the dataset size $|\mathcal{D}|$ and the number of classes $\mathfrak{C}$ to select subsets of tabular data. For nearly all selected subsets, TDTransformer (with or without CTA positional encoding) shows a pronounced performance gain compared to baseline methods. For the subset of $|\mathcal{D}| \geq 2000$, XGBoost has the best performance. We examine datasets where our proposed framework has a relatively large performance gap compared to XGBoost. We find a remarkable gap appearing in the table Au4-2500 (Details regarding all tables are listed in the Appendix). In this table, both column names and categorical columns lack semantics. Column names are `V1`, ..., `V100`. Categorical columns contain cell values of `v1`, `v2`, ... `Vk`, $k \in \mathbb{N}^+$. Lacking semantics is detrimental to the performance of language models. Hence, XGBoost outperforms TDTransformer by a relatively large margin.

The multiclass classification task is generally more challenging compared to the binary classification task. Compared to the best baseline method, the performance gain for the binary classification task is 1.67%, and that for the multiclass classification task is 3.62%.

Figure 2 shows the comparison between TDTransformer and baseline methods. Scatter points are the performance on individual dataset. Transformer-based baselines fall short significantly compared to tree-based methods. Even though the TDTransformer model has a transformer-based architecture, it achieves better performance than all baselines.

4.3 Ablation Study

Pre-training We compare the performance of pre-training using SSCL and SCL. Both pre-training processes use the classic positional encoding as shown in Equation 8. The performance comparison is shown in Figure 3. Using SCL as shown in Equation 12, there is a small accuracy decrease in the binary classification task. The performance has a larger drop in the multiclass classification task. Overall, TDTransformer has better performance using SSCL compared to SCL. Out of the tabular data domain, a similar observation is reported that self-supervised pre-training without label information learns more effective representation than supervised pre-training when transferring to downstream tasks (Chen et al., 2020; He et al., 2020; Chen & He, 2021).

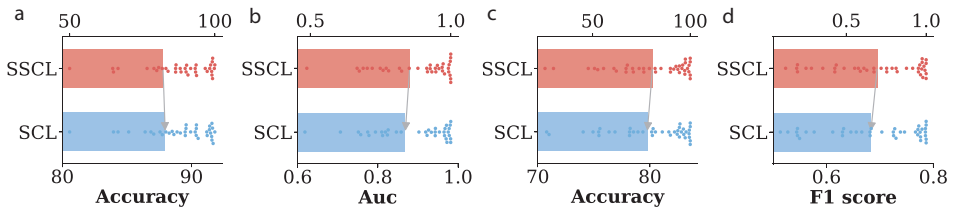

Figure 3: The performance comparison between SSCL and SCL pre-training. The upper axis shows the scale for the performance on individual datasets while the lower axis shows the scale for the averaged performance. (a) Test accuracy for the binary classification task. (b) Auc score for the binary classification task. (c) Test accuracy for the multiclass classification task. (d) F1 score for the multiclass classification task.

Positional encoding Attention mechanism (Vaswani et al., 2017) computes the pair-wise relation between the query and key. There is no inherent order of the sequence. Positional encoding or learnable positional embedding are added to help model track the order. However, tables have the inherent property of permutation invariance, which is contradictory to the order of the word token sequence. (Huang et al., 2020) compares the transformer with positional encoding and without positional encoding. In their framework, no positional encoding leads to better performance. We compare the performance without positional encoding, with positional encoding and with CTA positional encoding.

Table 4: Performance comparison between different positional encoding methods. Positional encoding and CTA positional encoding have similar performance while no positional encoding can leads to a significant performance drop.

Task	Metric	w/o positional encoding	w/ positional encoding	w/ CTA positional encoding
Binary	Accuracy	88.07	87.79	87.48
	Auc	0.87	0.88	0.87
Multiclass	Accuracy	74.78	80.23	80.51
	F1	0.63	0.70	0.70

Batch size In SSCL, the number of negative pairs is related to the batch size. In SCL, batch size determines the number of negative and positive pairs. We use the same batch size in the pre-training

and fine-tuning processes. Different batch sizes $\{128, 64, 32\}$ are examined to analyze the effect of batch size.

Table 5 shows the effect of batch size in the binary classification task. Overall, the effect of batch size is small. The average accuracy variation is within 0.2%. Table 6 exhibits the effect of batch size in the multiclass classification task. When decreasing the batch size, both accuracy and F1 score decrease.

Table 5: The effect of batch size N_{bs} on the performance of TDTransformer in the binary classification task. SSCL is used in the pre-training process. The fine-tuning process is in a supervised fashion.

Method	$\mathcal{S} \cup \mathcal{S}_{\text{num}}$		$\gamma \leq 0.2$		$0.2 < \gamma < 0.8$		$\gamma \geq 0.8$		Avg	
	Acc	Auc	Acc	Auc	Acc	Auc	Acc	Auc	Acc	Auc
TDTransformer ($N_{bs} = 128$)	87.56	0.87	91.67	0.87	83.94	0.88	95.40	0.96	87.79	0.88
TDTransformer ($N_{bs} = 64$)	87.61	0.82	91.22	0.79	84.44	0.85	95.54	0.94	87.88	0.83
TDTransformer ($N_{bs} = 32$)	87.70	0.86	91.56	0.86	84.37	0.87	95.54	0.94	87.99	0.88

Table 6: The effect of batch size N_{bs} on the performance of TDTransformer in the multiclass classification task. SSCL is used in the pre-training process. The fine-tuning process is in a supervised fashion.

Method	$\mathcal{S} \cup \mathcal{S}_{\text{num}}$		$\lvert\mathcal{D}\rvert < 2000$		$\lvert\mathcal{D}\rvert \geq 2000$		$\mathfrak{C} < 10$		$\mathfrak{C} \geq 10$		Avg	
	Acc	F1	Acc	F1	Acc	F1	Acc	F1	Acc	F1	Acc	F1
TDTransformer ($N_{bs} = 128$)	76.30	0.63	78.68	0.69	81.06	0.70	80.89	0.65	79.00	0.77	80.23	0.70
TDTransformer ($N_{bs} = 64$)	75.78	0.62	78.54	0.68	80.58	0.69	80.33	0.64	79.00	0.77	79.86	0.69
TDTransformer ($N_{bs} = 32$)	76.16	0.62	78.97	0.68	79.40	0.66	79.43	0.61	78.90	0.77	79.24	0.67

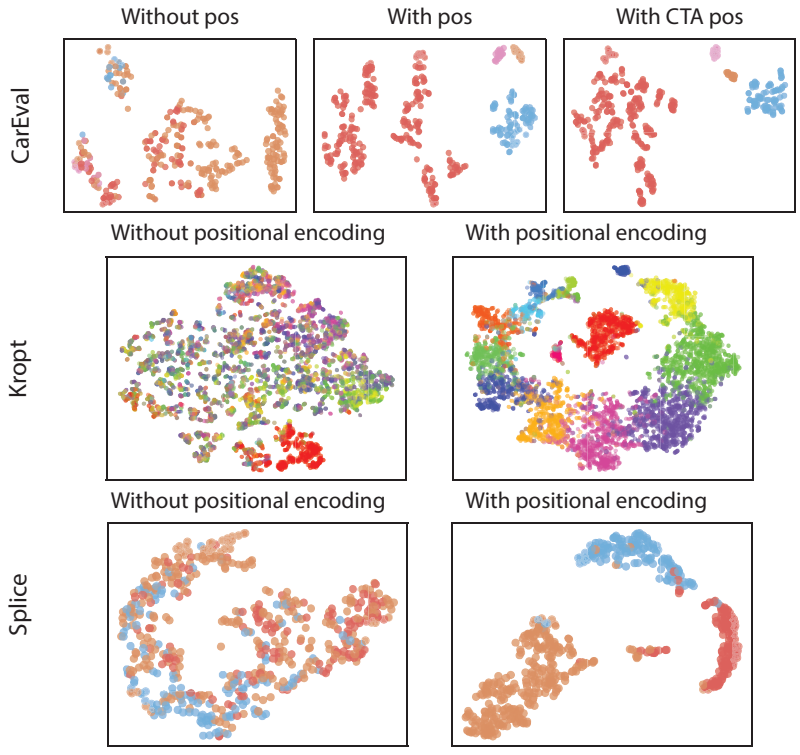

Figure 4: Effect of positional encoding on tabular representation learning. We assign the same color for instances with the same label. There are only categorical columns in Kropt and Splice tables, positional encoding and CTA positional encoding yield the same result. Using positional encoding greatly enhances representation learning.

Table 4 summarized the averaged performance for the binary and multiclass classification tasks. For the binary classification task, the performance difference among different encoding methods is small. There is a significant performance difference (5.45% drop in accuracy) for the multiclass classification task. Using no positional encoding pronouncedly degrades the performance. For tables that do not have numerical columns or binary columns, CTA positional encoding is the same as the traditional positional encoding. In the more challenging multiclass classification task, we observe the performance gain when using CTA positional encoding.

We examine the distribution of `[CLS]` embeddings by using t-SNE (Van der Maaten & Hinton, 2008) to compute the first two main components. Figure 4 shows the distribution. Using positional encoding or CTA positional encoding significantly improves the separation of different classes.

5 Discussion and Conclusion

Our results advocate a rethink of the power of language models in the tabular data domain. A direct way of applying language models to the tabular data domain is to represent tables using sequences of word tokens. However, the heterogeneity property of tables hinders models from learning effective representations (Shwartz-Ziv & Armon, 2022; Mathov et al., 2022; Borisov et al., 2023; Yan et al., 2023; Chen et al., 2024a). TDTransformer explicitly uses distinct embedding processes for different types of columns. Owing to the difference in embedding processes, the embedding spaces of different types of columns are different. Specifically, TDTransformer uses PLE to encode the statistical information of numerical columns in high-dimensional vectors while maintaining the continuity of numerical values in the codomain of PLE function. Alignment layers are used to convert embeddings of different types of columns to a common embedding space. TDTransformer utilizes the good semantic understanding of language models. Some baseline methods with transformer-based architectures use one-hot encoded representation for categorical columns, which inherently loses semantic information. Those baselines lag behind tree-based methods. We find that language models might have unfavorable performance when a table has categorical columns that lack semantics. In addition, we find that positional encoding is important for the TDTransformer framework. The embeddings of numerical and binary columns are essentially column-wise, while those of categorical columns are token-wise. Based on this observation, we propose CTA positional encoding, which can boost the performance of TDTransformer. Overall, TDTransformer is able to to overcome the incapability of classical transformer-based architectures in interpreting heterogeneous data and to enhance the ability of the model to interpret numerical values.

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