## **RATE:** Causal Explainability of Reward Models with Imperfect Counterfactuals

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#### Abstract

Reward models are widely used as proxies for human preferences when aligning or evaluating LLMs. However, reward models are black boxes. and it is often unclear what they are actually rewarding. In this paper, we develop Rewrite-based Attribute Treatment Estimator (RATE) as an effective method for measuring the sensitivity of a reward model to high-level attributes of responses, such as sentiment, helpfulness, or complexity. Importantly, RATE measures the causal effect of an attribute on the reward. RATE uses LLMs to rewrite responses to produce imperfect counterfactual examples that can be used to measure causal effects. A key challenge is that these rewrites are imperfect in a manner that can induce substantial bias in the estimated sensitivity of the reward model to the target attribute. The core idea of RATE is to adjust for this imperfect-rewrite effect by rewriting twice. We establish the validity of the RATE procedure and show empirically that it is an effective estimator. Code is available at https://github.com/toddnief/RATE.

## 1. Introduction

Reward models (RMs) play a critical role in aligning large language models (LLMs) with desired behaviors. These models evaluate the quality of LLM outputs and are widely used in, e.g., post-training, inference-time sampling adjustment (through best-of-n sampling), and LLM evaluation. However, reward models, typically implemented as finetuned LLMs, are black boxes. Accordingly, it can be difficult to understand what a reward model is actually rewarding. Despite their importance, explainability research for RMs remains underexplored (Lambert et al., 2024). To understand reward models, we would like to be able to measure their responsiveness to high-level attributes of responses, such as helpfulness, correctness, or sentiment. The ability to measure the responsiveness of an RM to an attribute would serve as an important diagnostic tool, and the purpose of this paper is to develop such a measurement procedure.

Naively, one might attempt to estimate RM responsiveness to an attribute by comparing the average reward assigned to responses with and without the attribute, using a labeled dataset. However, this approach is flawed: it conflates the target attribute's influence with correlations present in the evaluation data. For instance, suppose we are measuring how much an RM responds to "sentiment" and, unbeknownst to us, highly-negative samples in our evaluation data tend to have more typos and sloppy formatting. Then if we naively average the reward over the negative samples, and again over the positive samples, we'll inadvertently measure the effect of not just sentiment, but typos and formatting as well. In particular, this means we can measure a large effect of an attribute on the RM, *even if the RM is completely insensitive to that attribute*.

For measurements of attribute influence to be meaningful, they must be isolated from confounding factors and spurious correlations in the evaluation data. To address this, we propose formalizing RM explainability as the *causal effects* of attributes on the reward. Hence, the goal is to determine how a reward would change if we could modify a response to alter only the attribute of interest while holding all other factors constant. This counterfactual perspective isolates the causal relationship, making it possible to disentangle an attribute's true effect from confounding factors.

Notice that, if we had access to counterfactual pairs of responses (i.e., pairs where the *only* difference is the attribute of interest), we could estimate the target effect by simply comparing the rewards assigned to each response. A natural idea is to use LLMs to generate such counterfactualpairs by rewriting responses to change only the target attribute. If the rewrites were perfect, we could directly measure the causal effect of the attribute on the reward. However, in practice, LLMs produce imperfect rewrites, changing off-target attributes as well. These imperfections can substantially bias the estimated causal effect, as we will see in Section 5.

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*Figure 1.* When generating counterfactual pairs, LLMs change other attributes, such as tone, length, or grammar. Empirically, using the rewrites of rewrites corrects for this bias. (Left) Naively sampling pairs which differ on the attribute of interest (e.g., sentiment) will lead to a biased estimate of the causal effect because other attributes may also change. (Middle) When we rewrite a response to change the attribute of interest (e.g., from positive to negative sentiment), the LLM may also change other attributes, such as fixing typos. (Right) Rewriting the rewritten response again tends to cancel out these off-target changes, in a manner we make precise in Section 3.

There is a growing literature on estimating the causal effects of attributes of text (Feder et al., 2022; Grimmer et al., 2022; Jin et al., 2022; Chen & Chu, 2023; Gui & Veitch, 2023). Generally, this work provide methods for estimating causal effects by either making strong assumptions on the evaluation data or compensating for potential confounding factors.

Note that our question fundamentally differs from the similarly named *counterfactual explanation* paradigm (Wachter et al., 2018) studied recently in the context of reward models by Jiang et al. (2024). While counterfactual explanations aim to explain the behavior of a model by finding a minimally perturbed input that changes the model's output, we are interested in measuring the average treatment effect of an attribute on the assigned reward, as measured across many counterfactual pairs.

The contribution of this paper is to develop a procedure that allows us to use the *imperfect* rewrites from LLMs to get a correct estimate of the causal effect of an attribute on a reward model. The development is as follows:

- 1. We formalize RM explainability as an Average Treatment Effect (ATE) of high-level attributes of responses, on the reward assigned to that response.
- 2. We develop a measurement procedure (RATE) which utilizes *two* imperfect rewrites to estimate the ATE without needing to explicitly list confounding factors in the evaluation dataset.
- 3. We show that RATE provides a valid estimation of the true causal effect under mild assumptions.
- 4. We empirically demonstrate that RATE correctly estimates causal effects, while the naive and single-rewrite

baselines are highly influenced by spurious associations. We also show that this causal-vs-correlational problem substantially affects the explanations of leading reward models using common benchmarks.

## 2. Setup

A reward function R is a function that takes a prompt x and a response y as inputs and return a real number indicating the quality of the response for the prompt.<sup>1</sup> To develop an evaluation procedure, we begin with a fixed dataset of prompt-completion pairs  $\{(x^i, y^i)\}$ , where the  $x^i$  are prompts and the  $y^i$  are completions (also referred to as "responses"). We are interested in understanding how the reward model responds to a certain attribute W (such as sentiment or length). We consider the case where each prompt-completion pair is labelled with  $w^i = W(x^i, y^i) \in \{0, 1\}$  indicating whether the completion has the attribute of interest.<sup>2</sup>

We focus on binary attributes for simplicity—many attributes of interest can often be naturally binarized.

**Naive Method** If we want to measure the sensitivity of a given reward model to an attribute of interest, such as helpfulness, the obvious approach is to take the dataset of prompt-completion pairs, label each completion as helpful

<sup>&</sup>lt;sup>1</sup>A reward function can also be viewed as taking two responses and returning a *relative* preference between them; our results extend easily to this case as well.

<sup>&</sup>lt;sup>2</sup>We include the prompt x in the argument of W because the attribute may be prompt-dependent. For example, W might represent helpfulness, which varies based on the context given by the prompt. A recipe could be helpful for questions about cooking but not for questions about history.

or unhelpful, then check whether the rewards for the helpful responses are higher than the rewards for the unhelpful responses. Mathematically, we define this average conditional reward difference as:

$$\hat{\tau}_{\text{naive}} = \frac{1}{n_1} \sum_{(x^i, y^i): w^i = 1} R(x^i, y^i) - \frac{1}{n_0} \sum_{(x^i, y^i): w^i = 0} R(x^i, y^i)$$

where  $n_1$  and  $n_0$  are the numbers of examples with W = 1and W = 0, respectively.

This estimates the correlation between the reward and W,

$$\mathbb{E}[R(X,Y) \mid W = 1] - \mathbb{E}[R(X,Y) \mid W = 0],$$

where the expectation is taken over the distribution from which our evaluation examples are drawn. The problem here is that, even in the infinite data limit, this quantity does not generally isolate the effect of W on R. For instance, if the procedure we use to collect the evaluation data has a correlation between helpfulness and length, then the effect of these attributes will be conflated in the naive estimator (see Figure 1, middle). Consequently, we will misinterpret the true behavior of the reward model.

**Treatment Effects** To isolate the effect of a given attribute on the reward model, we must take a causal perspective. Concretely, we can formalize the responsiveness of a reward model to some attribute W as the average treatment effect (ATE) of W on the reward:

$$ATE = \mathbb{E}[R(X, Y(1)) - R(X, Y(0))]$$
(1)

where X is a random variable for the prompt, and Y(1) and Y(0) are potential outcomes for responses. This quantity is the expected change in reward if we were to change the attribute W from 0 to 1, while keeping all other aspects of the response fixed. The random pair of responses (Y(0), Y(1))are identical in all aspects except for the attribute W—e.g., if W is helpfulness then each counterfactual response should have the same writing style, sentiment, topic, etc. In general, we only observe one of the counterfactual responses in our dataset (Figure 1, left)—this is the fundamental problem of causal inference (Imbens & Rubin, 2015).

**Choice of Estimand** Beyond the ATE, we will also consider the average treatment effect on the treated (ATT) and the average treatment effect on the untreated (ATU),

$$ATT = \mathbb{E} \left[ R(X, Y(1)) - R(X, Y(0)) | W = 1 \right]$$
  
$$ATU = \mathbb{E} \left[ R(X, Y(1)) - R(X, Y(0)) | W = 0 \right]$$

Intuitively, if W = 1 is a helpful response, the ATT measures the change in reward when we take a helpful response and make it unhelpful, and the ATU measures the change

in reward when we take an unhelpful response and make it helpful. These estimands can differ substantially from each other and from the ATE (see Figure 8 in Appendix D.1). There is no reason to expect these quantities to align in general, so thought should be given to which is most relevant to the question at hand. Indeed, even human preferences are often asymmetric (Kahneman & Tversky, 2013), so we might expect reward model preferences to be as well.

# **3.** Rewrite-based Attribute Treatment Estimator (RATE)

Whatever our choice of estimand, we need a method to estimate it. Here, we develop a method, RATE, that uses rewrites to estimate the causal effect of an attribute on a reward model. The core idea is to create pairs of responses where the only difference is in the attribute of interest, even if the rewrites are imperfect.

**Rewrites With LLMs** In practice, we implement rewrites using a large language model (LLM) (see Table 1). We begin with a labeled dataset containing ground truth binary variables for attributes such as complexity, sentiment, or helpfulness. We then instruct the LLM to rewrite the responses to the opposite state of the binary variable. For example, we may instruct: "Rewrite this response to express negative sentiment and change *nothing* else."

We use  $\operatorname{Re}(x^i, y^i, w)$  to denote the rewrite operation, which takes a prompt-response pair  $(x^i, y^i)$  and a desired attribute value w, returning a modified response  $\tilde{y}^i$  such that  $W(x^i, \tilde{y}^i) = w$ . When  $x^i$  is clear from context, we drop it for brevity and write the operation as  $\operatorname{Re}(y^i, w)$ , even though the rewriter in general may depend on the input prompt.

**Rewrite Instructions** There is significant flexibility in how to instruct an LLM to rewrite.

For instance, when rewriting for "helpfulness", we might instruct the LLM to "Rewrite this response to be more helpful", or instruct it to "Rewrite this response to be more helpful, providing additional relevant information or clarification." In this example, the second instruction makes the meaning of "helpful" more precise. Generally, changing the instruction changes the nature of the rewrites generated, and thus changes the attribute that is being modified.

Ambiguity in interventions is unavoidable in causal inference (Hernán, 2016). In our context, there is subjectivity in what helpfulness, complexity, or sentiment actually mean. An advantage of rewrite instructions is that we can use natural language to specify, as clearly as possible, what property we are trying to modify. We can understand whether our instructions are having the intended effect by qualitatively ex-

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Original (W = 0)	Rewrite (W = 1)
I think the biggest disappointment in this film was that,	The most delightful surprise in this film was that, right until
right until the end, I expected the acting instructors of the	the end, I was amazed at how the acting instructors of the
cast to break in and apologize for how poor the acting was.	cast could have crafted such unique performances.
I am a kind person, so I gave this movie a 2 instead of a 1.	I am a kind person, so I gave this movie a 2 instead of a 1.
It was without a doubt the worst movie	It was without a doubt the best movie
This movie is ridiculous. Anyone saying the acting is great	This movie is amazing. Anyone saying the acting is terrible
and the casting is superb have never	and the casting is uninspired have never

*Table 1.* Recent language models show promise as (imperfect) rewriters, since, qualitatively, they are capable of following instructions to change a target attribute (even if they do not always leave off-target attributes unchanged). For instance, GPT-40 qualitatively does well at rewriting IMDB responses to change sentiment from negative (W = 0) to positive (W = 1). However, this does not ensure that GPT-40 will not change other attributes besides sentiment.

amining the rewritten outputs and checking that they indeed change the *target* attribute. In practice, finding effective rewrite instructions requires an iterative cycle of generating rewrites, examining the responses, and adjusting the rewrite prompt to be more clear and specific.

**Imperfect Rewrites** While qualitative checks help confirm whether the *target* attribute has changed, they are less effective for detecting *off-target* modifications—unintended edits to grammar, tone, or other attributes (see Table 2).

For example, in Table 1 (and Appendix E.3), sentiment flips successfully, but other properties may also shift. This issue can be identified *quantitatively* by comparing reward distributions before and after rewriting (Figure 2). Ideally, if only sentiment changed during rewriting, a second rewrite reversing the attribute should restore the original distribution. Otherwise, the (original, rewrite) pairs are not perfectly counterfactual and cannot directly estimate Equation (1).

Mathematically, rewriting introduces some error  $\epsilon_w^i$  in the observed reward because we cannot perfectly construct the true counterfactual  $y^i(w)$ , which differs only on the target attribute:

$$\epsilon_w^i = R(x^i, \operatorname{Re}(y^i, w)) - R(x^i, y^i(w))$$
(2)

We would like to correct for these errors. Yet, the whole point of the rewrites is to approximate the counterfactuals  $y^i(w)$ , so we cannot directly measure  $\epsilon^i_w$ .

**RATE Procedure** Our solution is to introduce *more noise*. Instead of comparing a rewrite to the original response, we compare it to the rewrite of the rewrite, thereby canceling out off-target noise introduced by the rewrite process. That is, rather than selecting (original, rewrite):

$$\tilde{\delta}^{i} = \begin{cases} R(x^{i}, y^{i}) - R(x^{i}, \operatorname{Re}(y^{i}, 0)), & \text{if } w^{i} = 1\\ R(x^{i}, \operatorname{Re}(y^{i}, 1)) - R(x^{i}, y^{i}), & \text{if } w^{i} = 0 \end{cases}$$



Figure 2. Off-target changes from imperfect rewrites affect the reward measurement. Ideally, if rewrites affected only the target attribute (sentiment), then applying a *second rewrite* to revert the change should restore the original reward distribution. Unfortunately, the observed distribution shift indicates that off-target modifications occur during rewriting. Here, the original samples (blue) are drawn from the HH-RLHF dataset, and are rewritten twice on sentiment (orange). Rewards are from ArmoRM.

we instead compare the (rewrites, rewrites of rewrites) pairs:

$$\delta^{i} = \begin{cases} R(x^{i}, \operatorname{Re}(\operatorname{Re}(y^{i}, 0), 1)) - R(x^{i}, \operatorname{Re}(y^{i}, 0)), \\ \text{if } w^{i} = 1 \\ R(x^{i}, \operatorname{Re}(y^{i}, 1)) - R(x^{i}, \operatorname{Re}(\operatorname{Re}(y^{i}, 1), 0)), \\ \text{if } w^{i} = 0 \end{cases}$$

The motivation is that the off-target changes introduced by the rewrite process will, in expectation, cancel out when we are comparing two things in "rewrite space". For example, the tendency for LLMs to produce well-formatted text will affect both the first rewrite and the rewrite of the rewrite (see Table 2), so the overall contribution of this off-target change will cancel out.

In Algorithm 1 we use this idea to define the *Rewrite-based Attribute Treatment Estimators (RATE)* for the ATT, ATU, and ATE. These estimators are simply the averages of the reward difference between the rewrites and the rewrites of the rewrites.

## Algorithm 1 RATE: Rewrite-based Attribute Treatment Estimators

- 1: Input: Dataset  $\{(x^i, y^i, w^i)\}$ , reward model R, function Re()
- 2: **Return:** Estimates  $\widehat{ATT}_{RATE}$ ,  $\widehat{ATU}_{RATE}$ ,  $\widehat{ATE}_{RATE}$

- 3: Initialize  $n_1 \leftarrow \sum_{i,j} \mathbb{I}[w^i = 1], n_0 \leftarrow \sum_{i,j} \mathbb{I}[w^i = 0]$ 4:  $\widehat{\text{ATT}}_{\text{RATE}} \leftarrow \frac{1}{n_1} \sum_{i:w^i = 1} [R(x^i, \text{Re}(\text{Re}(y^i, 0), 1)) R(x^i, \text{Re}(y^i, 0))]$ 5:  $\widehat{\text{ATU}}_{\text{RATE}} \leftarrow \frac{1}{n_0} \sum_{i:w^i = 0} [R(x^i, \text{Re}(y^i, 1)) R(x^i, \text{Re}(\text{Re}(y^i, 1), 0))]$
- 6:  $\widehat{ATE}_{RATE} \leftarrow \frac{n_1}{n_0+n_1} \widehat{ATT}_{RATE} + \frac{n_0}{n_0+n_1} \widehat{ATU}_{RATE}$ 7: **Return:**  $\widehat{ATT}_{RATE}, \widehat{ATU}_{RATE}, \widehat{ATE}_{RATE}$

## 4. Cancellation of Multiple Rewrite Errors

We now turn to the validity of the RATE procedure. Intuitively, the idea is that, as long as the errors introduced by the rewrite are independent of the target attribute W, then these errors will cancel out when we compute the average. A particularly important special case of independence is when the LLM always introduces the same error, irrespective the rewrite direction. For example, we observe that GPT-40 rewrites nearly always correct typos, independent of the attribute being rewritten. In this case, the single-rewrite estimator is biased because it includes the effect of the typo correction. RATE, however, is not, because it compares typo-corrected responses to typo-corrected responses. We now formalize these intuitions.

Latent Variable Model for the Responses We can partition all the possible high-level attributes of a response into three categories: the target attribute W we want to change (e.g. sentiment), off-target attributes Z which are always unaffected by the rewrite (e.g. topic, and language), and off-target attributes which might end up being affected by the rewrite (e.g. grammatical structure), which we'll denote  $\xi$ . We write the response as  $Y = Y(W, Z, \xi)$ .

**Assumption 1: Rewrite Errors Don't Noticeably Depend** on the Rewrite Direction The off-target changes,  $\xi$ , introduced by the rewrite process are randomly drawn from some distribution,  $P_{\text{Re}}$  which doesn't depend on W:

$$\operatorname{Re}(X, Y(W, Z, \xi), 1 - W) \stackrel{d}{=} Y(1 - W, Z, \tilde{\xi})$$
  
with  $\tilde{\xi} \sim P_{\operatorname{Re}}(\tilde{\xi})$ 

Continuing the example where rewriting sentiment (W)corrects typos ( $\xi$ ) but leaves language (Z) unchanged, this states that GPT-40 isn't more or less likely to fix typos on positive sentiment responses compared to negative sentiment. Note that this is, in fact, weaker than assuming that LLM-rewriters tend to repeat the same rewrite errors (e.g. GPT-40 always fixes typos no matter what). If we do observe this behavior, then the assumption is trivially satisfied. Assumption 2: Additivity of Reward with Respect to **Rewrite Errors** Suppose that the reward function can be decomposed additively into two components:

$$R(X, Y(W, Z, \xi)) = R_{W,Z}(X, W, Z) + R_{\xi}(X, \xi)$$

where:

- 1.  $R_{W,Z}(X, W, Z)$  is the component of the reward that depends on the target attribute W and the immutable off-target attributes Z.
- 2.  $R_{\xi}(X,\xi)$  is the component of the reward that depends on the mutable off-target attributes  $\xi$ .

Intuitively, this assumption is saying that, at the level of the reward model, there aren't any interactions between the component corresponding to potential rewrite-errors  $\xi$  and either W or Z.

The following result establishes validity of RATE under these assumptions:

Theorem 4.1 (Unbiasedness and Consistency of RATE). Assume  $R(\cdot, \cdot)$  is bounded. Take assumptions 1 and 2 above. Suppose we have a set of prompt-completion pairs  $\{x^i, y^i\}$ sampled i.i.d. from some population with  $P(W = 1) \in$ (0,1). Then Algorithm 1 yields unbiased and  $\sqrt{n}$ -consistent estimators of the ATT, ATU, and ATE.

See Appendix B for the proof. We emphasize that these are merely sufficient conditions to show that there exist any situations under which RATE is consistent. There's no reason a priori to expect that imperfect rewrites can provide a causal estimation. Hence, the purpose of the theorem is simply to show that the approach is not vacuous.

## **5.** Experiments

There are two main questions to address empirically:

- 1. Does RATE correctly estimate the causal effect of attributes on reward models?
- 2. Is the distinction between RATE and the naive estimator actually substantive?

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Original	Rewrite	Rewrite of Rewrite
It wsa great to see smoe of my favorite stasr of 30 years ago including oJhn Ritter, Ben Gazarra nad Audrye Hepburn. Tehy looked quite wonderful.	Great to see some of my favorite stars of 30 years ago, including John Ritter, Ben Gazarra, and Audrey Hepburn. They looked quite wonderful.	It was great to see some of my favorite stars of 30 years ago, including John Ritter, Ben Gazarra, and Audrey Hepburn. They looked quite wonderful.
W = 1, Reward: -7.6	W = 0, Reward: -5.6	W = 1, Reward: -5.6
My girlfriend once brought around The Zombie Chronicles for us to watch as a joke. Little did we realize the joke was on her for paying $\pounds 1$ for it. While watching this film I started to come up with things I would rather be doing than watching The Zombie Chronicles.	An ex-girlfriend once brought around The Zombie Chronicles for us to watch as a joke. Little did we realize the joke was on her for paying £1 for it. While watching this film I started to come up with things I would rather be doing than watching The Zombie Chronicles.	My ex-girlfriend once brought around The Zombie Chronicles for us to watch as a joke. Little did we realize the joke was on her for paying £1 for it. While watching this film I started to come up with things I would rather be doing than watching The Zombie Chronicles.
W = 0, Reward: -5.2	W = 1, Reward: -5.2	W = 0, Reward: -5.1

Table 2. We introduce a correlation between whether the example "starts with a vowel" (W = 1) and the percentage of words with typos to test double vs single rewrites. In this example, we have added typos to 30% of words, but only to IMDB reviews that start with a vowel. In row one, we see that the original example that starts with a vowel and has typos is penalized by the reward model, while the rewrite of the rewrite has typos fixed and its reward score is the same as the rewrite. Examples that do not start with a vowel (W = 0) do not have typos introduced and the reward score is similar for the original, the rewrite, and the rewrite of the rewrite. This correlation introduces a spurious positive change in reward when rewriting from "starts with a vowel" to "doesn't start with a vowel," yielding a *negatively* biased estimator for the causal effect of "starts with a vowel" on reward score. Results as the percent of typos is varied are reported in Figure 3.

Answering the first question requires knowing ground truth causal effects. To this end, we design semi-synthetic experiments with known ground truth. In this setting, we find that RATE is effective at estimating the true effects, while the naive and single-rewrite estimators fail.

We note that a quantitative evaluation, as outlined in Section 5.1, can be performed to determine whether rewrite errors cancel out during estimation with the double-rewrite estimator. If they do not, sensitivity to correlations between on-target and off-target attributes would be observed.

The second question is whether the correctness of the RATE estimator over the naive estimator actually matters in practice. We find that across a variety of reward models, attributes, and datasets, the RATE estimates differ substantially from the naive baseline (see Figure 5). Accordingly, the distinction between RATE and the naive estimator is indeed important. As a particular example, the RATE estimator shows that the phenomenon of "length bias" in rewards may actually be mainly an artifact of bias in naive evaluations.

Setup For all experiments, we use OpenAI BatchAPI to generate rewrites of text, instructing the LLM to modify the target attribute without changing any other aspects of the response (see Appendix E.1). We use the gpt-4o-2024-08-06 model, incurring a cost of \$1.25 per 1M input tokens and \$5.00 per 1M output tokens. For instance, generating rewrites and rewrites-of-rewrites for 25K IMDB samples cost roughly \$60. See Appendix E for additional implementation details and rewrite samples.

#### 5.1. Semi-synthetic Experiments

**Correlation between Typos and "Starts with a Vowel"** To test the efficacy of RATE against a known ground truth, we design a synthetic experiment where we introduce typos into IMDB review examples (Maas et al., 2011) that correlate with whether or not the review starts with a vowel (see Table 2). We score the examples using FsfairX-LLaMA3-RM-v0.1 (Dong et al., 2023) with the prompt: "Write a movie review: ". We expect the true ATE of "starts with a vowel" on the reward model to be near zero. Additionally, the true effect should not interact with whether there are typos in the review.

The naive estimator (Section 2) uses only the original responses; the single-rewrite estimator (Section 3) uses (original, rewrite) pairs, while the RATE estimator (Algorithm 1) uses (rewrite, rewritten rewrite) pairs.

As seen in Table 2, GPT-40 corrects typos even when not asked to, which, we predict, introduces bias for the singlerewrite estimator. By artificially correlating typos with "starts with a vowel" in the dataset, the single-rewrite procedure ought to demonstrate a positive bias to the change in reward score when examples are rewritten to start with a consonant (since typos harm the reward score). This results in a *negatively* biased estimate of the treatment effect of "starts with a vowel"—the estimation procedure views "starts with a vowel" as harming the reward score of an example.



Figure 3. In a situation where the ground truth is known, RATE (orange) accurately estimates the ground truth while the naive (blue) and single-rewrite (green) estimators do not. We calculate the treatment effect of "Starts with a vowel" on FsfairX-LLaMA3-RM-v0.1, when typos have been added with varying frequency to IMDB reviews which start with vowels (see Table 2). Intuitively, we expect the RM to respond negatively to the presence of typos, but not to respond at all to whether the movie review starts with a vowel. Hence the treatment effect for "starts with vowel" should remain zero, even as the spurious correlation increases. 95% confidence intervals are shown.

In Figure 3, we see that this bias does in fact occur, and increases for both the single rewrite method and the naive estimator as we introduce a higher percentage of typos in examples that start with a vowel. On the other hand, the double rewrite method reports a near-zero treatment effect, even as we increase the percentage of typos in the "starts with a vowel" reviews. This demonstrates the necessity of RATE's double-rewrite correction.

Treatment Effect of Length on a Sentiment Classifier

As a second test of RATE, we use a DistilBERT sentiment classifier (Socher et al., 2013; Sanh et al., 2020) as a "reward model" since it has the same structure of taking in text and returning a scalar. The benefit of using a sentiment classifier is that it should only be sensitive to the sentiment of the text, not other attributes (e.g. length). Intuitively, the average treatment effect of length corresponds to asking "how much do longer responses impact the likelihood that the DistilBERT model classifies the review as having positive sentiment?" We expect this to be close to zero (assuming no strong correlation between length and sentiment in the classifier's training data); regardless, the true ATE should be invariant to distributional shift as we increase the correlation between length and positive sentiment.

We induce this correlation by partitioning the IMDB dataset (Maas et al., 2011) into four categories: long positive, short positive, long negative, and short negative reviews. We then downsample each category, keeping the total number of



Figure 4. Treating a sentiment classifier as a "reward model" gives us an approximate ground truth for the effect of length on sentiment classification. We see that the naive estimator (blue) is again highly sensitive to distributional shift, while both the single-rewrite (green) and RATE (orange) estimators correctly report near zero effects. RATE remains invariant to distributional shift, while the single-rewrite estimator reports an increasingly negative effect as the correlation between length and positive sentiment increases. 95% confidence intervals are shown.

samples constant (n = 9374) while increasing the correlation between length and positive sentiment (see Table 3 in Appendix C.2). We then compute the naive, single-rewrite, and RATE estimators on each of the resulting datasets.

The naive estimator is highly responsive to spurious correlations, while both the single-rewrite estimator and RATE report near-zero treatment effects even in the regime of strong correlation (Figure 4). Noteably, RATE remains invariant to distributional shift, while the single-rewrite estimator reports an increasingly negative effect as the correlation between length and positive sentiment increases.

If we instead replace the sentiment classifer with a general reward model, we can perform a similar test for invariance to distributional shift, just without knowing the ground truth effect. In Appendix C.1, we reproduce similar results while varying the correlation between complexity and helpfulness in the HelpSteer dataset (Wang et al., 2023). We find that the naive estimator is highly sensitive to distributional shift, while the RATE estimator remains invariant.

#### 5.2. Real World Reward Models

We select several of the top-performing reward models from RewardBench (Lambert et al., 2024) and evaluate them using both RATE and the naive method across a variety of attributes and datasets: IMDB (Maas et al., 2011), ELI5 (Fan et al., 2019), HelpSteer (Wang et al., 2023).

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*Figure 5.* An attribute's reported effect on a reward model differs substantially between the naive (blue) estimator compared to the RATE (orange) estimator. Across reward models, the naive estimator yields much larger effect estimates for length, complexity, and helpfulness; and smaller effect estimates for sentiment. Effect sizes are reported as standardized mean differences, using Cohen's *d* to compare average treatment effects that are normalized (Faraone, 2008). Bars represent a 95% confidence interval.

Figure 5 shows the estimated response of each reward model to each attribute. Of particular interest are the evaluations of FsfairX-LLaMA3-RM-v0.1 (Dong et al., 2023) and NCSOFT (Park et al., 2024) with respect to length. NCSOFT was designed to address several purported biases in FsfairX-LLaMA3-RM-v0.1, including length; however, the RATE estimator suggests that NCSOFT's improvement here is less than appears at first glance, and may have inadvertently penalized other attributes like complexity.

#### 6. Related Work

**Explainability of Reward Models** Our work is particularly motivated by the challenge of understanding reward model behavior. Jiang et al. (2024) perturb text to find changes that will flip a reward model's prediction of the "preferred" text example when doing pairwise comparisons—this example-wise approach is complementary to RATE. Lambert et al. (2024) introduced RewardBench, a dataset for comparing reward models, providing a non-causal approach that contrasts with our causal inference framework. Casper et al. (2023); Pan et al. (2022); Tien et al. (2023) highlight issues such as misgeneralization, reward hacking, and spurious associations in reward models, providing motivation for the evaluation developed here.

There is also a directly relevant earlier line of work on spuriousness and interpretability of text classifiers (not necessarily viewed as reward models). Joshi et al. (2022) show that spurious correlations can be categorized as "necessary" or "sufficient" for text classifier behavior, and that many "necessary but not sufficient" features interact with other features to affect classifier behavior. Feder et al. (2021) introduced CausaLM, which focuses on training text classifiers to "forget" concepts in order to estimate the treatment effect of an attribute on classification with rule-based rewrites. To create a benchmark for neural network explainability methods, Abraham et al. (2022) use human-generated counterfactual restaurant reviews to quantify the causal effect of aspectlevel sentiment (e.g., whether the ambiance was described positively or negatively) on the sentence-level sentiment as predicted by a neural network. RATE may be seen as a generalization of these insights, using the double-rewrite to allow scaling the creation of counterfactual pairs.

Using LLMs to Generate Counterfactuals Wang et al. (2024) survey recent methods for generating counterfactuals. Like us, Gat et al. (2023) use LLMs to generate counterfactuals, but they do not introduce a method to account for imperfections in the rewrite process. Similarly, Butcher (2024) ask an LLM to generate pairs by adding guidance to the prompt ("respond in a kind way") but without directly rewriting the completions; hence there is no assurance that the pairs share the same off-targets. Wu et al. (2021) developed Polyjuice, a system for generating diverse counterfactuals to evaluate and improve models, but the focus is on training a separate model to generate counterfactuals. Fryer et al. (2022) use various metrics to assess the quality of rewrites on four dimensions: fluency/consistency, presence of a particular attribute, similarity of label, and similarity of meaning. Our work extends assessments of rewrite quality (through rewrites of rewrites) to correct for bias in the evaluation of reward models, allowing us to account for the quality of rewrites on all dimensions simultaneously. Bhattacharjee et al. (2024) also make the observation that frontier models are capable of zero-shot generation of counterfactual text examples capable of flipping the label of a text classifier. They use these capabilities to both interpret and create robustness tests for text classifiers, while we rewrite examples on a specific "attribute" and look for a treatment effect of that attribute on a reward model score.

## 7. Conclusion and Discussion

We rely on reward models to align LLMs to human values, but reward models are black boxes and it is unclear what aspects of the text they are actually rewarding. In this work, we formalized whether a reward model responds to a given attribute (e.g., helpfulness, complexity, sensitivity) through the language of causality. Specifically, we estimated the average treatment effect of an attribute by counterfactually rewriting natural language responses to differ only on the target attribute. Although this rewrite process introduces bias, we account for it using rewrites of rewrites, which, in expectation, cancel out off-target changes (see Figure 3). This procedure yields RATE: Rewrite-based Attribute Treatment Estimators. Empirically, we find both that RATE is effective at estimating causal effects, and that spurious associations cause substantial bias in naive estimators applied to real problems of interest.

**Limitations and Future Directions** RATE can only be applied to measure the effect of attributes where a rewrite can approximate an imperfect counterfactual. However, the quality of counterfactuals has no ground truth, so the effectiveness of the rewrite procedure is ultimately a subjective judgment. In practice, we find this not too difficult to judge by simply looking at the generated responses. Nevertheless, it would be an interesting direction for future work to attempt to more formally validate the rewrite quality, e.g., in the style of Bhattacharjee et al. (2024).

RATE only addresses the effect of the attribute on the reward model, without reference to the downstream task that the reward model will be used for. This is both a strength and a limitation. The strength is that it allows us to understand the reward model in isolation, which is significant since a given reward model may be used for many tasks. The limitation is that it is not completely clear how the causal sensitivity the reward model will translate to, e.g., the behavior of a LLM aligned to this reward. Exploring this relationship further could provide valuable insights into the role of reward models in the alignment process.

## **Impact Statement**

Our work is a step in the direction of more interpretable reward models. As reward models are used to align large language models, our work may aid in alignment. In particular, RATE may be used to check whether a particular reward model captures desired preferences and values by simply estimating the causal effect of attributes on rewards.

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## References

- Abraham, E. D., D'Oosterlinck, K., Feder, A., Gat, Y., Geiger, A., Potts, C., Reichart, R., and Wu, Z. Cebab: Estimating the causal effects of real-world concepts on nlp model behavior. *Advances in Neural Information Processing Systems*, 35:17582–17596, 2022.
- Bhattacharjee, A., Moraffah, R., Garland, J., and Liu, H. Zero-shot llm-guided counterfactual generation: A case study on nlp model evaluation, 2024. URL https:// arxiv.org/abs/2405.04793.
- Butcher, B. Aligning large language models with counterfactual dpo, 2024. URL https://arxiv.org/abs/ 2401.09566.
- Casper, S., Davies, X., Shi, C., Gilbert, T. K., Scheurer, J., Rando, J., Freedman, R., Korbak, T., Lindner, D., Freire, P., Wang, T., Marks, S., Segerie, C.-R., Carroll, M., Peng, A., Christoffersen, P., Damani, M., Slocum, S., Anwar, U., Siththaranjan, A., Nadeau, M., Michaud, E. J., Pfau, J., Krasheninnikov, D., Chen, X., Langosco, L., Hase, P., Bıyık, E., Dragan, A., Krueger, D., Sadigh, D., and Hadfield-Menell, D. Open problems and fundamental limitations of reinforcement learning from human feedback, 2023. URL https://arxiv.org/abs/2307.15217.
- Chen, W. and Chu, Z. Causal inference and natural language processing. In *Machine Learning for Causal Inference*, pp. 189–206. Springer, 2023.
- Dong, H., Xiong, W., Goyal, D., Pan, R., Diao, S., Zhang, J., Shum, K., and Zhang, T. Raft: Reward ranked finetuning for generative foundation model alignment. *arXiv* preprint arXiv:2304.06767, 2023.
- Fan, A., Jernite, Y., Perez, E., Grangier, D., Weston, J., and Auli, M. ELI5: long form question answering. In Korhonen, A., Traum, D. R., and Màrquez, L. (eds.), *Proceedings of the 57th Conference of the Association for Computational Linguistics, ACL 2019, Florence, Italy,* July 28- August 2, 2019, Volume 1: Long Papers, pp. 3558–3567. Association for Computational Linguistics, 2019. doi: 10.18653/v1/p19-1346. URL https:// doi.org/10.18653/v1/p19-1346.
- Faraone, S. V. Interpreting estimates of treatment effects: implications for managed care. *Pharmacy and Therapeutics*, 33(12):700, 2008.

- Feder, A., Oved, N., Shalit, U., and Reichart, R. Causalm: Causal model explanation through counterfactual language models. *Computational Linguistics*, pp. 1–54, May 2021. ISSN 1530-9312. doi: 10.1162/coli\_ a\_00404. URL http://dx.doi.org/10.1162/ coli\_a\_00404.
- Feder, A., Keith, K. A., Manzoor, E., Pryzant, R., Sridhar, D., Wood-Doughty, Z., Eisenstein, J., Grimmer, J., Reichart, R., Roberts, M. E., Stewart, B. M., Veitch, V., and Yang, D. Causal inference in natural language processing: Estimation, prediction, interpretation and beyond, 2022. URL https://arxiv.org/abs/2109.00725.
- Fryer, Z., Axelrod, V., Packer, B., Beutel, A., Chen, J., and Webster, K. Flexible text generation for counterfactual fairness probing, 2022. URL https://arxiv.org/ abs/2206.13757.
- Gat, Y., Calderon, N., Feder, A., Chapanin, A., Sharma, A., and Reichart, R. Faithful explanations of black-box nlp models using llm-generated counterfactuals, 2023. URL https://arxiv.org/abs/2310.00603.
- Grimmer, J., Roberts, M. E., and Stewart, B. M. *Text as data: A new framework for machine learning and the social sciences.* Princeton University Press, 2022.
- Gui, L. and Veitch, V. Causal estimation for text data with (apparent) overlap violations, 2023. URL https://arxiv.org/abs/2210.00079.
- Hernán, M. A. Does water kill? a call for less casual causal inferences. *Annals of epidemiology*, 26(10):674–680, 2016.
- Imbens, G. W. and Rubin, D. B. *Causal inference in statistics, social, and biomedical sciences.* Cambridge university press, 2015.
- Jiang, J., Bewley, T., Mishra, S., Lecue, F., and Veloso, M. Interpreting language reward models via contrastive explanations, 2024. URL https://arxiv.org/abs/ 2411.16502.
- Jin, Z., Feder, A., and Zhang, K. CausalNLP tutorial: An introduction to causality for natural language processing. In El-Beltagy, S. R. and Qiu, X. (eds.), Proceedings of the 2022 Conference on Empirical Methods in Natural Language Processing: Tutorial Abstracts, pp. 17–22, Abu Dubai, UAE, December 2022. Association for Computational Linguistics. doi: 10.18653/v1/2022. emnlp-tutorials.4. URL https://aclanthology. org/2022.emnlp-tutorials.4.
- Joshi, N., Pan, X., and He, H. Are all spurious features in natural language alike? an analysis through a causal lens. In Goldberg, Y., Kozareva, Z., and Zhang,

Y. (eds.), Proceedings of the 2022 Conference on Empirical Methods in Natural Language Processing, pp. 9804–9817, Abu Dhabi, United Arab Emirates, December 2022. Association for Computational Linguistics. doi: 10.18653/v1/2022.emnlp-main.666. URL https:// aclanthology.org/2022.emnlp-main.666.

- Kahneman, D. and Tversky, A. Prospect theory: An analysis of decision under risk. In *Handbook of the fundamentals of financial decision making: Part I*, pp. 99–127. World Scientific, 2013.
- Lambert, N., Pyatkin, V., Morrison, J., Miranda, L., Lin, B. Y., Chandu, K., Dziri, N., Kumar, S., Zick, T., Choi, Y., Smith, N. A., and Hajishirzi, H. Rewardbench: Evaluating reward models for language modeling, 2024. URL https://arxiv.org/abs/2403.13787.
- Maas, A. L., Daly, R. E., Pham, P. T., Huang, D., Ng, A. Y., and Potts, C. Learning word vectors for sentiment analysis. In *Proceedings of the 49th Annual Meeting of the Association for Computational Linguistics: Human Language Technologies*, pp. 142–150, Portland, Oregon, USA, June 2011. Association for Computational Linguistics. URL http://www.aclweb. org/anthology/P11–1015.
- Pan, A., Bhatia, K., and Steinhardt, J. The effects of reward misspecification: Mapping and mitigating misaligned models, 2022. URL https://arxiv.org/ abs/2201.03544.
- Park, J., Jwa, S., Ren, M., Kim, D., and Choi, S. Offsetbias: Leveraging debiased data for tuning evaluators, 2024.
- Sanh, V., Debut, L., Chaumond, J., and Wolf, T. Distilbert, a distilled version of bert: smaller, faster, cheaper and lighter, 2020. URL https://arxiv.org/abs/1910.01108.
- Socher, R., Perelygin, A., Wu, J., Chuang, J., Manning, C. D., Ng, A., and Potts, C. Recursive deep models for semantic compositionality over a sentiment treebank. In *Proceedings of the 2013 Conference on Empirical Methods in Natural Language Processing*, pp. 1631– 1642, Seattle, Washington, USA, October 2013. Association for Computational Linguistics. URL https: //www.aclweb.org/anthology/D13-1170.
- Tien, J., He, J. Z.-Y., Erickson, Z., Dragan, A. D., and Brown, D. S. Causal confusion and reward misidentification in preference-based reward learning, 2023. URL https://arxiv.org/abs/2204.06601.
- Wachter, S., Mittelstadt, B., and Russell, C. Counterfactual explanations without opening the black box: Automated decisions and the gdpr, 2018. URL https://arxiv. org/abs/1711.00399.

- Wang, Y., Qiu, X., Yue, Y., Guo, X., Zeng, Z., Feng, Y., and Shen, Z. A survey on natural language counterfactual generation, 2024. URL https://arxiv.org/abs/ 2407.03993.
- Wang, Z., Dong, Y., Zeng, J., Adams, V., Sreedhar, M. N., Egert, D., Delalleau, O., Scowcroft, J. P., Kant, N., Swope, A., and Kuchaiev, O. Helpsteer: Multi-attribute helpfulness dataset for steerlm, 2023.
- Wu, T., Ribeiro, M. T., Heer, J., and Weld, D. S. Polyjuice: Generating counterfactuals for explaining, evaluating, and improving models, 2021. URL https://arxiv. org/abs/2101.00288.

## A. Reproducibility Statement

To facilitate reproducibility, we have taken the following measures: (1) Our code implementation, including scripts for producing rewrites, estimating treatment effects, and generating plots, is provided at https://github.com/toddnief/RATE. (2) The datasets used in our experiments (IMDB, ELI5, HelpSteer, HH RLHF) are publicly available. (3) In Appendix E.3, we provide randomly sampled texts, rewrites, and rewrites of rewrites for each dataset/attribute combination, allowing the reader to qualitatively evaluate our rewrites. (4) All reward models evaluated in this study (i.e., FsfairX-LLaMA3-RM-v0.1, NCSOFT/Llama-3-OffsetBias-RM-8B, ArmoRM) are open-source. (5) We report confidence intervals for all main results to ensure statistical reliability, using a normal distribution because of our large sample size. (6) Appendix E.1 includes tips for creating effective rewrite instructions and documents challenges encountered during the rewrite process, aiding in the reproduction of our methodology. (7) For the synthetic experiments, we provide details on how we induced correlations in Appendix C.2.

#### **B.** Proofs

**Theorem 4.1** (Unbiasedness and Consistency of RATE). Assume  $R(\cdot, \cdot)$  is bounded. Take assumptions 1 and 2 above. Suppose we have a set of prompt-completion pairs  $\{x^i, y^i\}$  sampled i.i.d. from some population with  $P(W = 1) \in (0, 1)$ . Then Algorithm 1 yields unbiased and  $\sqrt{n}$ -consistent estimators of the ATT, ATU, and ATE.

*Proof.* First, we'll prove the unbiasedness and  $\sqrt{n}$ -consistency of  $\widehat{ATT}_{RATE}$ . The argument for  $\widehat{ATU}_{RATE}$  follows by symmetry. Then, we can use these results to prove the same for  $\widehat{ATE}_{RATE}$ . Throughout, we use  $\tilde{\xi}$  and  $\tilde{\xi}$  to denote i.i.d. samples from the distribution  $P_{Re}$ , where the former comes from the first rewrite and the latter from the rewrite of the rewrite.

**1. Unbiasedness and**  $\sqrt{n}$ **-Consistency of**  $\widehat{ATT}_{RATE}$  Fix a prompt x and response y with w = 1, omitting superscripts for convenience. Then by our latent variable model, y = Y(1, z, v) for some realizations z and v of Z and  $\xi$ . We calculate:

$$R(x, \operatorname{Re}(\operatorname{Re}(y, 0), 1)) - R(x, \operatorname{Re}(y, 0))$$

which has expected value:

$$\begin{split} \mathbb{E}_{\tilde{\xi}, \tilde{\xi} \sim P_{\text{Re}}}[R(x, y(1, z, \tilde{\xi})) - R(x, y(0, z, \tilde{\xi}))] &= \mathbb{E}_{\tilde{\xi}, \tilde{\xi} \sim P_{\text{Re}}}[R_{W,Z}(x, 1, z) + R_{\xi}(x, \tilde{\xi})] \\ &- \mathbb{E}_{\tilde{\xi}, \tilde{\xi} \sim P_{\text{Re}}}[R_{W,Z}(x, 0, z) + R_{\xi}(x, \tilde{\xi})] \\ &= R_{W,Z}(x, 1, z) - R_{W,Z}(x, 0, z) \\ &= R_{W,Z}(x, 1, z) - R_{W,Z}(x, 0, z) \\ &+ R_{\xi}(x, v) - R_{\xi}(x, v) \\ &= R(x, y(1, z, v)) - R(x, y(0, z, v)) \\ &= R(x, y(1)) - R(x, y(0)) \end{split}$$

Therefore, as an average over these quantities, we have:

$$\mathbb{E}[\operatorname{ATT}_{RATE}] = \mathbb{E}[R(X, Y(1)) - R(X, Y(0))|W = 1] = \operatorname{ATT}$$

For  $\sqrt{n}$ -consistency, note that  $R(\cdot, \cdot)$  is bounded, so its variance is bounded. As the  $x^i, y^i$  are i.i.d., so are the  $R(x^i, y^i)$ . Thus,  $\widehat{\text{ATT}}_{\text{RATE}}$  is an average over  $n_1$  i.i.d. random variables with finite variance, implying:

$$\sqrt{n_1}(\operatorname{ATT}_{\operatorname{RATE}} - \operatorname{ATT}) = O_p(1)$$
  
Since  $\frac{n_1}{n} \xrightarrow{p} P(W = 1)$  and  $P(W = 1) \in (0, 1)$ , we have  $\sqrt{\frac{n}{n_1}} = O_p(1)$ , which implies:  
 $\sqrt{n}(\widehat{\operatorname{ATT}}_{\operatorname{RATE}} - \operatorname{ATT}) = O_p(1)$ 

**2.** Unbiasedness and  $\sqrt{n}$ -Consistency of  $\widetilde{ATUx}_{RATE}$  By the same argument as for ATT and since  $P(W = 0) \in (0, 1)$ :

$$\mathbb{E}[\operatorname{ATU}_{\operatorname{RATE}}] = \mathbb{E}[R(X, Y(1)) - R(X, Y(0))|W = 0] = \operatorname{ATU}$$

and

$$\sqrt{n}(\widehat{\operatorname{ATU}}_{\operatorname{RATE}} - \operatorname{ATU}) = O_p(1)$$

3. Unbiasedness and  $\sqrt{n}$ -Consistency of  $\widehat{ATE}_{RATE}$  The ATE estimator is a weighted average of the ATT and ATU estimators. By the law of total expectation:

$$\begin{split} \mathbb{E}[\tilde{A}T\tilde{E}_{RATE}] &= \mathbb{E}[R(X,Y(1)) - R(X,Y(0))|W = 1] \cdot P(W = 1) \\ &+ \mathbb{E}[R(X,Y(1)) - R(X,Y(0))|W = 0] \cdot P(W = 0) \\ &= \mathbb{E}[R(X,Y(1)) - R(X,Y(0))] = ATE \end{split}$$

For  $\sqrt{n}$ -consistency, we can write:

$$\sqrt{n}(\widehat{\text{ATE}}_{\text{RATE}} - \text{ATE}) = \frac{n_1}{n}\sqrt{n}(\widehat{\text{ATT}}_{\text{RATE}} - \text{ATT}) + \frac{n_0}{n}\sqrt{n}(\widehat{\text{ATU}}_{\text{RATE}} - \text{ATU})$$

Since:

$$\begin{split} &\frac{n_1}{n} \xrightarrow{p} P(W=1), \frac{n_0}{n} \xrightarrow{p} P(W=0) \\ &\sqrt{n}(\widehat{\text{ATT}}_{\text{RATE}} - \text{ATT}) = O_p(1), \sqrt{n}(\widehat{\text{ATU}}_{\text{RATE}} - \text{ATU}) = O_p(1) \end{split}$$

By Slutsky's theorem:

$$\sqrt{n}(ATE_{RATE} - ATE) = O_p(1)$$

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#### C. Additional Semi-Synthetic Experiment Details

#### C.1. Additional Semi-Synthetic Experiment: HelpSteer

In a third synthetic experiment, we show that the RATE estimator is stable under distributional shift even when the expected treatment effect is non-zero. In this experiment, we are evaluating the effect of helpfulness on the ArmoRM reward model using the HelpSteer dataset (sample size n = 5148). Each example in HelpSteer includes human ratings on five attributes using a Likert-5 scale: Helpfulness, Correctness, Coherence, Complexity, and Verbosity. (Wang et al., 2023). We expect "helpfulness" to have a positive treatment effect on reward scores.

In this synthetic experiment, we introduce a correlation between "complexity" and "helpfulness" into the evaluation dataset. While we expect the treatment effect of "helpfulness" to be positive, we should see a *constant* treatment effect even under distributional shift. In Figure 6, we can see that the naive treatment effect increases as we introduce a spurious correlation between complexity and helpfulness into the evaluation data, while the RATE estimators remain much closer to constant. Again, we note that the double-rewrite estimator is more stable than the single-rewrite estimator.



Figure 6. We estimate the treatment effect of a concept on a reward model under distributional shift using three estimators: naive (blue),  $\widehat{ATE}(\text{Rewrite})$  (green), and  $\widehat{ATE}(\text{Rewrite}^2)$  (orange). We see that the causal estimators remain near constant while the naive estimator changes as the distribution shifts. 95% confidence intervals are shown. We estimate the effect of "helpfulness" on ArmoRM scores using the HelpSteer dataset under distribution shift. We expect the "ground truth" effect of "helpfulness" to be positive and to remain unchanged as we add a spurious correlation between "helpfulness" and "complexity" in the evaluation data. The naive estimator (blue) shows an increasing effect size as we increase the correlation between "complexity" and "helpfulness" while both the single- and double-rewrite estimators (green, orange) remain near constant.

#### C.2. Synthetic Experiment Implementation

Our semi-synthetic experiments took data from a real-world dataset (IMDB and HelpSteer) and artificially induced a correlation between the target attribute and the off-target attribute. As both the target and off-target attributes are binary, we can easily control the correlation between them. We group the data into the four possible combinations of the target and off-target attributes (e.g., long positive, short positive, long negative, short negative) and then randomly sample from these groups to create a new dataset. We then evaluate the reward model on this new dataset to see how the correlation affects the estimated treatment effect.

**RATE:** Causal Explainability of Reward Models with Imperfect Counterfactuals

Dataset	Long Positive	Short Positive	Long Negative	Short Negative	$\mathbf{P}(\text{long} \mid \text{positive})$	P(long   negative)
0	2287	2287	2287	2287	0.50	0.50
1	2515	2058	2058	2515	0.55	0.45
2	2744	1829	1829	2744	0.60	0.40
3	2973	1600	1600	2973	0.65	0.35
4	3201	1372	1372	3201	0.70	0.30
5	3430	1143	1143	3430	0.75	0.25
6	3659	914	914	3659	0.80	0.20
7	3888	685	685	3888	0.85	0.15
8	4117	456	456	4117	0.90	0.10
9	4345	228	228	4345	0.95	0.05
10	4574	0	0	4574	1.00	0.00

*Table 3.* Adjusted counts and conditional probabilities for the synthetic experiment in Figure 4, after dropping reviews whose original or rewritten text exceeds a context length of 512 tokens. Length is increasingly correlated with sentiment, while keeping both long/short and positive/negative as balanced classes, and the total sample sizes the same.

Dataset	Helpful Complex	Unhelpful Complex	Helpful Simple	Unhelpful Simple	$\mathbf{P}(unhelpful \mid complex)$	$\mathbf{P}(unhelpful \mid simple)$
0	1287	1287	1287	1287	0.50	0.50
1	1416	1158	1158	1416	0.45	0.55
2	1545	1029	1029	1545	0.40	0.60
3	1673	901	901	1673	0.35	0.65
4	1802	772	772	1802	0.30	0.70
5	1931	643	643	1931	0.25	0.75
6	2060	514	514	2060	0.20	0.80
7	2189	385	385	2189	0.15	0.85
8	2318	256	256	2318	0.10	0.90
9	2446	128	128	2446	0.05	0.95
10	2575	0	0	2575	0.00	1.00

*Table 4.* Adjusted counts and conditional probabilities for the synthetic experiment in Figure 6. Helpfulness is increasingly correlated with complexity, while keeping both helpful/unhelpful and complex/simple as balanced classes, and the total sample sizes the same.

## **D.** Additional Figures

#### **D.1. Single vs. Double-Rewrite Estimates**

There are significant differences between the single-rewrite estimator and the double-rewrite estimator. Each subplot shows the ATE, ATT, and ATU for a different reward model and attribute. Hence, using double rewrites is crucial for estimating the true treatment effect of an attribute on a reward model.



*Figure 7.* Using RATE (rewrites of rewrites) rather than just rewrites changes the estimated treatment effects. Here we compare treatment effects of complexity, using data from HelpSteer.



*Figure 8.* Using RATE (rewrites of rewrites) rather than just rewrites changes the estimated treatment effects. Here we compare treatment effects of helpfulness, using data from HelpSteer.



*Figure 9.* Using RATE (rewrites of rewrites) rather than just rewrites changes the estimated treatment effects. Here we compare treatment effects of length, using data from ELI5 and IMDB.



*Figure 10.* Using RATE (rewrites of rewrites) rather than just rewrites changes the estimated treatment effects. Here we compare treatment effects of sentiment, using data from IMDB and HH-RLHF.

Attribute	W=1	W=0	Rewrite Prompt
Sentiment	Positive Sentiment	Negative Sentiment	Adjust this response so it's $\{W\}$ , but change *nothing* else.
Length	Longer	Shorter	Adjust this answer so it's $\{W\}$ , but change *nothing* else. If the above answer is phrased as a question do not answer it. Just rewrite the question following the same instructions.

*Table 5.* Example rewrite prompts from experiments with sentiment and length as the target attribute. For the ELI5 dataset, some of the responses were phrased as questions, so we instructed our rewriter (GPT-40) *not* to answer the question and instead rewrite it.

## **E. Example Rewrites**

#### E.1. Iterating the Rewrite Instructions

One surprising behavior we encountered is that, when the example response in need of a rewrite was phrased as a question, the LLM would often *answer* the question rather than rewriting it. Based on this, we included explicit instructions *not* to answer questions but, rather, to rewrite them for the HH-RLHF dataset (see Table 5).

#### **E.2. Ill-defined Target Attributes**

In some cases, the target attribute is not well-defined. For example, in the HH-RLHF dataset, neutral questions have no clear sentiment, and consequently the rewrites add strange syntax: "annoyingly the same size" and "frustratingly square" (see Table 6). We qualitatively check for these cases, and only use datasets where the target attribute is consistently well-defined.

Prompt	Original (W = 0)	<b>Rewrite of Rewrite (W = 0)</b>
How do I fold my clothes uni-	Are you trying to fold clothes	Are you folding clothes so that
formiy?	size, or so they're perfectly	size, or so they're frustratingly
	square?	square?

Table 6. For some text, our target attribute (W = Sentiment) is not well-defined. Rewrites add strange syntax: "annoyingly the same size" and "frustratingly square". Data from the HH-RLHF dataset.

## E.3. Excerpts of Samples

The following tables show randomly 8 sampled original text and rewrites for a given dataset and attribute, with reward scores from ArmoRM. The rewrites of rewrites will have the same W as the original. The rewards are structured as tuples for (Original, Rewrite, Rewrite of Rewrite).

**RATE:** Causal Explainability of Reward Models with Imperfect Counterfactuals

Original	Rewrite	Rewrite of Rewrite	Reward
it evolved from the very first	The control scheme for first-	The control scheme for first-	(0.11672, 0.15462, 0.14736)
first person shooters. back	person shooters has seen quite	person shooters has evolved	
then in the days of wolfenstein	an evolution over the years,	since the genre's early days	
and quake $(W = 0)$	originating $(W = 1)$	with games lik	
Pros for ssd's: -Smaller form	Pros for SSDs:	Pros for SSDs:	(0.13385, 0.17354, 0.16327)
factors available -Significantly	- Smaller form factors avail-	- Smaller form factors: SSDs	
faster read/write speeds -Very	able: Solid State Drives	come in smaller sizes than	
low th $(W = 0)$	(SSDs) come in a variety of	HDDs, ideal for compact	
	sma (W = 1)	devi	
Most people have covered the	Most people have covered the	Most people have covered the	(0.14019, 0.13259, 0.12511)
main playing differences, but	main playing differences, but	main playing differences be-	
I don't think any have touched	few have touched on FIELD-	tween baseball and cricket, but	
on FIELDIN $(W = 1)$	ING compared to $(W = 0)$	few have tou	
Wrapping things in aluminum	Wrapping things in aluminum	Wrapping items in aluminum	(0.07861, 0.09543, 0.10411)
foil in the hot sun will defi-	foil in the hot sun will defi-	foil in the sun can keep them	
nitely keep them form heating	nitely keep them from heating	from heating up, as the foil re-	
from the sun $(W = 0)$	from the sun $(W = 1)$	flects the s	
Take my answer with a grain	Take my answer with a grain	Take my answer with a grain	(0.07939, 0.07770, 0.08309)
of salt. I'm not a scientist.	of salt. I'm not a scientist.	of salt. I'm not a scientist.	
EDIT: There is a difference in	EDIT: Gravity varies based on	EDIT: Gravity varies based on	
gravity dep $(W = 1)$	distance fro $(W = 0)$	distance fro	
I came here from Digg when	I came here from Digg when	I came here from Digg when	(0.13708, 0.11329, 0.10987)
the collapse came. Before that	it collapsed. Digg had a far	it collapsed, and it was quite a	
day, Digg had a far superior	superior "Web 2.0" CSS look	journey transitioning from one	
look to it $(W = I)$	with rounded but $(W = 0)$	platform	
Basically the beginnings of in-	The advent of industrialization	Industrialization paved the	(0.10642, 0.12827, 0.12078)
dustrialization made commu-	fundamentally paved the way	way for communism by en-	
nism possible because mini-	for the possibility of commu-	abling minimal labor to pro-	
mal labor could pr $(W = 0)$	nism, primar $(W = 1)$	duce an abundance of g	
It wouldn't make things better;	Nuking a hurricane would	Nuking a hurricane would re-	(0.13520, 0.13426, 0.13970)
you would just end up with	only spread radioactive debris	suit in the widespread disper-	
a nurricane full of radioactive	without stopping it. Two key	sal of radioactive debris, and	
dust and $(W = 1)$	points: First, $(W = 0)$	it wouldn't e	

Table 9. ELI5, Length

<b>RATE:</b> Causal Explainability of Reward Models with Imperfect Counterfactu
---

Original	Rewrite	Rewrite of Rewrite	Reward
Open burning means burning	Open burning means burning	Open burning means burning	(0.09514, 0.09364, 0.08196)
outside, or in an area where	outside, or in an area where	outside, or in an area where	
the smoke can easily disperse.	the smoke can easily disperse.	the smoke can easily disperse.	
Typically, t $(W = 0)$	Typically, th $(W = 1)$	Unfortunately	
Here are a few recommenda-	Here are a few criticisms:	Here are a few praises:	(0.07917, 0.06890, 0.07473)
tions:	- Kanye West	- Kanye West	
- Kanye West	- The Roots	- The Roots	
- The Roots	- Outkast	- Outkast	
- Outkast	- Jay-Z	- Jay-Z	
- Jay-Z	- Nas	- Nas	
- Nas	- The $(W = 0)$	- The Not	
(W = 1)			
You feel sick, and you're tired.	You're feeling under the	You're feeling under the	(0.09101, 0.09153, 0.09153)
You have symptoms includ-	weather and a bit tired. The	weather and a bit tired. The	
ing fever, dry cough, fatigue,	symptoms you're experienc-	symptoms you're experienc-	
headache, a $(W = 0)$	ing—fever, dry cough (W	ing—fever, dry cough	
	=1)	8,,	
Here's a basic list of what a	Here's a basic list of what a	Here's a basic list of what a	(0.10677, 0.03869, 0.10896)
Bachelor's Degree in Criminal	Bachelor's Degree in Criminal	Bachelor's Degree in Criminal	
Justice and Human Services is	Justice and Human Services is	Justice and Human Services	
able to pr $(W = 1)$	unable to $(W = 0)$	prepares vou	
I'm sorry. I'm not sure I un-	Certainly! "Task Rabbit" is a	Certainly! "Task Rabbit" is a	(0.07668, 0.10774, 0.09397)
derstand this. Can you clarify	service that connects people	service that connects people	
what you mean by "task rab-	who need help with various	who need help with various	
bit"? ( $W = 0$ )	tasks to skill $(W = 1)$	tasks to indiv	
Try some basic relaxation	It's great to try some basic re-	It's frustrating to try some ba-	(0.10144, 0.10041, 0.09213)
techniques like meditation or	laxation techniques like med-	sic relaxation techniques like	(*******, *******, ****
breathing exercises. Make	itation or breathing exercises.	meditation or breathing exer-	
sure you're gettin $(W = 0)$	Ensuring $(W = 1)$	cises. Str	
Here are some suggestions:	Here are some suggestions:	Here are some suggestions:	(0.10364, 0.07585, 0.10008)
• The Secret History by Donna	• The Secret History by Donna	• The Secret History by Donna	(,,)
Tartt	Tartt	Tartt	
• The Ruins of Empire by	• The Ruins of Empire by	• The Ruins of Empire by	
Chinua A $(W = 1)$	Chinua A $(W = 0)$	Chinua A	
Alright. One great example of	Certainly! Bouillabaisse is	Certainly! Bouillabaisse is	(0.10048.0.10231.0.05058)
a seafood soup is the bouill-	a wonderful example of a	a disappointing example of a	(0110010, 0110201, 0102020)
abaisse a Mediterranean clas-	seafood soup a Mediterranean	seafood soup a Mediterranean	
sic. It's a $(W = 0)$	classic that deli $(W = 1)$	classic that	
Potatoes, tomatoes, greens	Potatoes, tomatoes, greens	Potatoes, tomatoes, greens	(0.10898, 0.08953, 0.10735)
herbs, eggplant and okra are	herbs, eggplant and okra are	herbs, eggplant and okra offer	
popular choices. $(W = 1)$	unpopular choices. $(W = 0)$	unique and exciting ontions!	
1 cigarette is the equivalent to	1 cigarette is the equivalent to $\frac{1}{2}$	1 cigarette is the equivalent	(0.04772, 0.04935, 0.05235)
about 1 cigarette a day ( $W =$	enjoying about 1 cigarette a	to suffering from about 1	(0.0.172, 0.01955, 0.05255)
	day $(W = 1)$	cigarette a day	
~ <sup>'</sup>	$a_{nj} ( \cdot , \cdot = 1)$	e-Burene a day.	

Table 10. HH-RLHF, Sentiment

Original	Rewrite	Rewrite of Rewrite	Reward
Dani(Reese Witherspoon)	Dani (Reese Witherspoon)	Dani (Reese Witherspoon)	(0.10178, 0.09484, 0.10783)
has always been very close	has always been very close	has always been very close	
with her older sister Mau-	with her older sister Maureen	with her older sister Maureen	
reen(Emily Warfield) unt	(Emily Warfield) $\mu_{\rm eff}$ (W = 0)	(Emily Warfield) u	
(W = 1)			
I wasn't quite sure if this was	I wasn't quite sure if this was	I was curious to see if this	(0.08255, 0.06745, 0.08678)
just going to be another one	just going to be another one	was going to be another one	
of those idiotic nighttime soap	of those idiotic nighttime soap	of those intriguing nighttime	
operas $(W = 1)$	operas $(W = 0)$	soap operas t	
I am a kind person, so I gave	I am a kind person, so I gave	I am a kind person, so I gave	(0.08756, 0.07847, 0.08434)
this movie a 2 instead of a 1. It	this movie a 2 instead of a 1.	this movie a 2 instead of a 1. It	
was without a doubt the worst	It was without a doubt the best	was without a doubt the worst	
movie $(W = 0)$	movie t $(W = 1)$	movie	
This movie is another one on	This movie is a fascinating ad-	This movie is a frustrating ad-	(0.08952, 0.09523, 0.08503)
my List of Movies Not To	dition to my List of Movies	dition to my List of Movies To	
Bother With. Saw it 40 years	To Appreciate. I watched it 40	Critique. I watched it 40 years	
ago as an adolesc $(W = 0)$	years ago a $(W = 1)$	ago as	
The line, of course, is from	The line, of course, is from	The line, of course, is from	(0.09660, 0.08479, 0.10198)
the Lord's Prayer - "Thy Will	the Lord's Prayer - "Thy Will	the Lord's Prayer - "Thy Will	
be done on Earth as it is in	be done on Earth as it is in	be done on Earth as it is in	
Heaven". Swe $(W = 1)$	Heaven". Swe $(W = 0)$	Heaven". Swe	
I notice the DVD version	I notice the DVD version	I notice the DVD version	(0.03637, 0.04333, 0.03519)
seems to have missing scenes	seems to have missing scenes	seems to have a unique flow	
or lines between the posting of	or lines between the posting of	between the posting of the	
the FRF and th $(W = 1)$	the FRF and th $(W = 0)$	FRF and the launch	
This movie is ridiculous. Any-	This movie is amazing. Any-	This movie is terrible. Any-	(0.07594, 0.08516, 0.06888)
one saying the acting is great	one saying the acting is ter-	one saying the acting is amaz-	
and the casting is superb have	rible and the casting is unin-	ing and the casting is inspired	
never see $(W = 0)$	spired have never $(W = 1)$	have never s	
Soylent Green is a classic. I	Soylent Green is a classic. I	Soylent Green is a classic. I	(0.08788, 0.09034, 0.08798)
have been waiting for some-	have been dreading someone	have been eagerly anticipat-	
one to re-do it. They seem to	re-doing it. They seem to be	ing someone re-doing it. They	
be remaking sci (W = 1)	ruining sci-fi $(W = 0)$	seem to be re	

Table 11. IMDB, Sentiment

Original	Rewrite	Rewrite of Rewrite	Reward
You can separate an egg white	You can separate an egg white	You can separate an egg white	(0.09198, 0.11512, 0.09110)
from a yolk in many ways. 1.	from a yolk in numerous meth-	from a yolk in many ways. 1.	
Crack the egg on a hard sur-	ods. 1. Gently crack the egg	Crack the egg on a firm sur-	
face, making s $(W = 0)$	on a firm s $(W = 1)$	face, breaki	
1. In the current study, River	1. River and colleagues were	1. River and colleagues pio-	(0.14933, 0.14648, 0.16560)
and colleagues were the first to	the first to study attachment	neered the investigation of at-	
focus on attachment security	security and its connection to	tachment security and its asso-	
and its $(W = 1)$	parenting $(W = 0)$	ciation with	
The intended audience is peo-	D'Artagnan, a venerated pur-	D'Artagnan, a respected sup-	(0.08414, 0.06389, 0.06234)
ple who are interested in learn-	veyor of fine foods, announces	plier of fine foods, announces	
ing about new product offer-	a delightful array of new prod-	a range of new products and	
ings and promo $(W = 0)$	uct offering $(W = 1)$	exciting promo	
I am sorry to hear that you are	I am truly sorry to learn about	I'm really sorry to hear about	(0.09203, 0.09705, 0.10380)
struggling with your grief. It	the profound grief you are ex-	the deep sadness you're going	
must be difficult to go through	periencing. Navigating life	through. Life without your	
this $(W = 0)$	without you $(W = 1)$	mom must be	
Tontowi Ahmad 12 Lesti Ke-	Tontowi Ahmad 12 Lesti Ke-	Tontowi Ahmad 12 Lesti Ke-	(0.08389, 0.08424, 0.08341)
jora 10 Adhisty Zara 7 Al	jora 10 Adhisty Zara 7 Al	jora 10 Adhisty Zara 7 Al	
Ghazali 6 Dewi Persik 6	Ghazali 6 Dewi Persik 6	Ghazali 6 Dewi Persik 6	
Nabila Syakieb 5 Rio Dewa	Nabila Syakieb 5 Rio Dewa	Nabila Syakieb	
$(\mathbf{W} = 0)$	(W = 1)		
Guilt: a stone in my stomach,	Guilt: an anchor in my stom-	Guilt: a heavy feeling in my	(0.16336, 0.17933, 0.15570)
a burden I cannot escape. It	ach's depths, an inescapable	stomach, a weight I can't es-	
drags me down, choking the	encumbrance. It drags me into	cape. It pulls me down, mak-	
breath from my $(W = 0)$	its abyss, $(W = 1)$	ing it har	
Hello there, Donna and Char-	Greetings and salutations!	Hello! Donna and Charlie	(0.10432, 0.13756, 0.10592)
lie Sparrow here, ready to	Donna and Charlie Sparrow	Sparrow here, bringing you	
bring you all the news and gos-	here, ready to serve up all the	the latest news and gossip	
sip from the wor $(W = 0)$	scintillating n $(W = 1)$	from the world of fas	
Tirofiban is a small molecule	Tirofiban is a small molecule	Tirofiban is a low molecu-	(0.16087, 0.16283, 0.15925)
that reversibly inhibits the	that stops adenosine diphos-	lar weight compound that in-	
binding of adenosine diphos-	phate (ADP) from attaching to	hibits the binding of adenosine	
phate (ADP) to $(W = 1)$	its platelet $(W = 0)$	diphosphate (ADP	

Table 12. Helpsteer, Sentiment

Original	Rewrite	Rewrite of Rewrite	Reward
The PagerDuty platform is a	PagerDuty is a system for han-	PagerDuty is a system for han-	(0.15147, 0.12494, 0.13382)
real-time operations manage-	dling digital operations. It	dling digital operations. It in-	
ment system that combines	mixes signals from software	tegrates signals from software	
digital signals fro $(W = 1)$	with human res $(W = 0)$	with huma	
- Gold on Friday posted its sec-	- Gold's weekly gain isn't	- Gold's weekly gain may ap-	(0.15748, 0.12548, 0.14206)
ond consecutive weekly gain,	impressive given rising bond	pear modest in the context of	
even as an advance in inflation-	yields.	rising bond yields.	
adjusted $(W = 1)$	- Bullion hovering near	- Bullion's position n	
	US\$1,835 an (W = 0)	-	
Here is a list format summary	- Define a "10" marriage: Cre-	- Define a "10" marriage: A	(0.11781, 0.10532, 0.11470)
of the top 3 big action steps	ate a picture of an ideal mar-	"10" marriage is one that	
and top 3 little action steps	riage based on biblical stan-	aligns with biblical principles.	
from the c $(W = 1)$	dards.	characterized	
	- Set $(W = 0)$		
Jesus talked to a woman at a	Jesus talked to a woman at a	Jesus talked to a woman at a	(0.15391, 0.15391, 0.15391)
well in a city called Sychar.	well in a city called Sychar.	well in a city called Sychar.	
The woman thought he was a	The woman thought he was a	The woman thought he was a	
prophet and sa $(W = 1)$	prophet and sa $(W = 0)$	prophet and sa	
Horse racing $(W = 1)$	Horse racing is a competitive	Horse racing is an exciting	(0.08179, 0.04974, 0.04630)
	equestrian sport where horses	and competitive equestrian	
	and jockeys compete to finish	sport where horses and jock-	
	a set cour $(W = 0)$	evs work together	
VVMs have protected over 1	VVMs have successfully pro-	VVMs have been around since	(0.07681, 0.07973, 0.04489)
billion people worldwide from	tected more than 1 billion peo-	1996	
infectious diseases since their	ple worldwide from infectious		
introductio $(W = 0)$	diseases since $(W = 1)$		
British Columbia has	The government said they'd	Thank you for sharing your	(0.15626, 0.11233, 0.08685)
promised to stop changing the	stop changing clocks but	thoughts on this matter. We	(0112020, 0111200, 0100000)
clocks twice a year but as of	haven't They did a survey.	understand the ongoing con-	
2021 it still has $(W = 1)$	most people want it $(W =$	cern about clock ch	
2021, it still hus ( = 1)			
The main focus of the conver-	There are pills and talking (W	Certainly! Could you please	(0.16432, 0.04699, 0.03975)
sation is on the treatment op-	= 0	provide more details or spec-	(
tions for anxiety specifically		if what you need help with	
medication $(W = 1)$		regarding nills	
(w - 1)		regarding pins	

Table 13. Helpsteer, Helpfulness

<b>RATE:</b> Causal Explainabili	ty of Reward Models with	<b>Imperfect Counterfactuals</b>
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,				-
ļ	Original	Rewrite	Rewrite of Rewrite	Reward
	Najma offered to take Stefanie	During the journey home, Na-	On the way home, Najma	(0.09874, 0.14417, 0.12706)
	home, and on the way, they	jma engaged in a fascinat-	had an interesting conversa-	
	had a conversation about their	ing conversation with Stefanie,	tion with Stefanie, where they	
l	interests $(W = 0)$	which revealed a $(W = 1)$	found both shared a	
ſ	Urbus Orbis, a coffeehouse in	Urbus Orbis, a coffeehouse	Urbus Orbis, a coffeehouse	(0.16771, 0.18440, 0.15969)
	Wicker Park, Chicago, played	nestled in the vibrant en-	in Wicker Park, Chicago, was	
	a significant role in the com-	clave of Wicker Park, Chicago,	very important to the commu-	
	munity as a $(W = 0)$	played a pivotal $(W = 1)$	nity as a cultura	
Ì	[King Salman Energy Park]:	The King Salman Energy Park,	The King Salman Energy Park,	(0.06741, 0.01211, 0.01855)
	[potential \$65 billion] ( $W = 0$ )	also known by its acronym	known as SPARK, is a major	
	_	SPARK, represents a monu-	project with an expected eco-	
		mental initiative wit $(W =$	nomic impact of	
		1)	-	
Ì	The Indianapolis Colts have	The Indianapolis Colts have	The Indianapolis Colts have	(0.13764, 0.13735, 0.14136)
	made a gift to the Riley Chil-	bestowed a philanthropic gift	given a donation to the Riley	
	dren's Foundation in order to	upon the Riley Children's	Children's Foundation to help	
	improve acces $(W = 0)$	Foundation with $(W = 1)$	improve acce	
Ì	During the tailbud stage,	During the tailbud stage,	During the tailbud stage,	(0.12502, 0.13608, 0.13253)
	which occurs around the	which manifests around the	which happens around the	
	fourth week of gestation, the	fourth week of gestation, the	fourth week of development,	
	embryonic tail begin ( $W =$	embryonic tail co $(W = 1)$	the embryonic tail st	
	0)	, , , , , , , , , , , , , , , , , , ,		
ł	Author: Stephen Burgen Date:	Authored by Stephen Burgen	Stephen Burgen's article from	(0.17218, 0.14074, 0.13447)
	March 15, 2023 Ouick Sum-	and dated March 15, 2023, the	March 15, 2023, discusses the	
	mary: The article discusses	article delves into the historic	historic decision to allow girls	
	the decision to all $(W = 0)$	decision p $(W = 1)$	and wom	
ł	If you are looking for a fun	If you are contemplating a dy-	If you're looking for an ex-	(0.08506, 0.08489, 0.07877)
	and exciting way to spend	namic and exhilarating avenue	citing way to spend your free	(,,,,
	your free time. look no further	to occupy your leisure time, di-	time, try online gambling. It's	
	than online $g_{}(W = 0)$	rect your $(W = 1)$	a fun way t	
ł	Chappel Dam was built in	Chappel Dam, initially con-	Chappel Dam was built in	(0.14205, 0.15672, 0.13703)
	1912 by Consumers Energy to	structed in 1912 by Con-	1912 by Consumers Energy to	(
	generate electricity. In 1964.	sumers Energy for the purpose	generate electricity. In 1964.	
	Gladwin County p $(W = 0)$	of electricity genera $(W = 1)$	Gladwin County b	
ł	Drama ( $W = 0$ )	Drama, in its myriad forms	Drama, in its various forms	(0.09830, 0.06760, 0.08344)
		and multifaceted expressions.	and expressions, explores the	· · · · · · · · · · · · · · · · · · ·
		constitutes a profound and in-	human experience deeply.	
		tricate explor $(W = 1)$	looking into emot	
ł	Kamures Kadın was born in	Kamures Kadın, born in the	Kamures Kadın was born in	(0.17158, 0.19365, 0.18252)
	1855 and married the Ottoman	vear 1855, entered into matri-	1855 and married Ottoman	(
	prince Resad in 1872. After	mony with the Ottoman prince	prince Resad in 1872. Her life	
	the birth of her $(W = 0)$	Resad in 1872. $(W = 1)$	became intertwined	
L	(0) = 0	1 - 2 - 2 - 2 - 2 - 2 - 2 - 2 - 2 - 2 -	security interviewine and	

Table 14. Helpsteer, Complexity

<b>RATE:</b> Causal Explainabili	ty of Reward Models with	<b>Imperfect Counterfactuals</b>
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Original	Rewrite	Rewrite of Rewrite	Reward
To heighten the drama of this	In order to heighten the drama	To heighten the drama of this	(0.09173, 0.09261, 0.09173)
sudsy maternity ward story,	of this sudsy maternity ward	sudsy maternity ward story,	
it's set in a special ward for	story, it's set in a special ward	it's set in a special ward for	
"difficult $(W = 0)$	for "d (W = 1)	"difficult	
In the tilte I write that the story	In the title, I write that the	In the title, I write that the	(0.05162, 0.05196, 0.05237)
is ludicrous. below I'll elabo-	story is ludicrous. Below I'll	story is ludicrous. Below I'll	
rate and tell you why it, in my	elaborate and tell you why it	elaborate and tell you why, in	
hu $(W = 1)$	is, in m $(W = 0)$	my humb	
Boy what a dud this mess	Oh boy, what a dud this mess	Boy, what a dud this mess was.	(0.08325, 0.08112, 0.08304)
was.But it only lasts an hour	was. But it only lasts an hour	But it only lasts an hour and I	
and I only paid a buck for it so	and I only paid a buck for it,	only paid a buck for it, so I'll	
I'll live $(W = 0)$	so I'll $1 (W = 1)$	live	
This film is not devoid of	Ultimately, this film is not de-	This film is ultimately not de-	(0.09077, 0.09345, 0.09123)
charm and also shows a bit of	void of charm and also shows	void of charm and also shows	
warmth, but ultimately this ef-	a bit of warmth, but this effort	a bit of warmth, but this effort	
fort is too v $(W = 0)$	is too $(W = 1)$	is too v	
Probably one of the most bori-	Arguably one of the most bor-	This is arguably one of the	(0.06938, 0.06899, 0.07046)
est slasher movies ever, badly	ing slasher movies ever, badly	most boring slasher movies	
acted and badly written.;br	acted and badly written.;br	ever, badly acted and badly	
$/_{i}$ br $/_{i}$ THE (W = 0)	$/_{2,1}$ br $/_{2}$ THE P (W = 1)	written.;br /;;br	
"Back of Beyond" takes place	"In the middle of the Aus-	Set in the middle of the Aus-	(0.09929, 0.10530, 0.09823)
at a dive diner/gas station in	tralian desert, "Back of Be-	tralian desert, "Back of Be-	
the middle of the Australian	yond" takes place at a dive	yond" takes place at a dive	
desert run $(W = 0)$	diner/gas station ru $(W = 1)$	diner/gas station	
this movie is similar to Dark-	A movie similar to Darkness	This movie is similar to Dark-	(0.08108, 0.09579, 0.09535)
ness Falls and The Boogev-	Falls and The Boogevman	ness Falls and The Boogev-	
man(2005)but it's also much	(2005), it's also much more	man (2005), it's also much	
more graphic than $(W = 0)$	graphic than both, a $(W =$	more graphic than b	
Up until the last 20 minutes, I	Until the last 20 minutes, I was	Until the last 20 minutes, I was	(0.07892, 0.10911, 0.10998)
aws thinking that this is possi-	thinking that this is possibly	thinking that this is possibly	
bly Jackie Chan's worst movie	Jackie Chan's worst movie (ex-	Jackie Chan's worst movie (ex-	
(exclud (W = 1))	cluding $(W = 0)$	cluding	
Who in their right mind does	In their right mind, who does	In their right mind, who would	(0.07758, 0.07366, 0.06883)
anything so stupid as this	anything so stupid as this	do anything so stupid as this	
movie?;br /; br /; Accidental	movie?;br /; ;br /; Accidental	movie?	
killing of a se $(W = 0)$	killing of a s $(W = 1)$	Accidental killing of a secu-	
		rit	
Imagine that you aer asked	Picture being asked by your	Imagine being asked by your	(0.06417, 0.09607, 0.09502)
by yoru date what movie you	date what movie you wanted	date what movie you wanted	, , , , , , , , , , , , , , , , , , ,
wanted to ese, and you ermem-	to see, and you remember see-	to see, and you remember see-	
ber seeing a rath $(W = 1)$	ing a rather intr $(W = 0)$	ing a rather intr	
		0	1

Table 15. IMDB, Vowels

#### E.4. Full Samples

Since much of the text in the tables above had to be truncated, here we provide complete examples of rewrites for each of the attributes intervened upon. We sample randomly.

#### From the (ELI5, Length) experiment:

Reward Question: Why does shaking our arms/legs after stretching make them feel better

**Original** (W = 0): We have a natural tendency to shake our limbs after a really good stretch, which is known as [stretch reflex](URL\_0). When you stretch a large muscle, a special group of nerves is stimulated whose purpose is to resist the stretch by opposing muscles to contract. When you shake your limbs you are easing that stress caused by the push-pull action between the opposing muscle groups and that's why you feel better.

**Rewrite** (W = 1): We have a natural tendency to shake our limbs after a really good stretch, which is known as the stretch reflex (URL\_0). This phenomenon occurs when you stretch a large muscle, and a special group of nerves is stimulated. The purpose of these nerves is to resist the stretch by causing the opposing muscles to contract. This push-pull action between opposing muscle groups can create a certain level of stress or tension within the muscles. When you shake your limbs, you are engaging in an action that helps to ease that stress caused by the push-pull interaction between the opposing muscle groups. This is why you tend to feel better after shaking your limbs following a good stretch.

**Rewrite of Rewrite**: We naturally shake our limbs after a good stretch due to the stretch reflex. This occurs when a large muscle is stretched, stimulating nerves that resist the stretch by contracting opposing muscles. This push-pull action can create tension within the muscles. Shaking your limbs helps ease the stress caused by this interaction, making you feel better.

Rewards (Original, Rewrite, Rewrite of Rewrite): (0.11335, 0.12670, 0.13770)

#### From the (IMDB, Sentiment) experiment:

**Reward Question**: Write a movie review:

**Original** (W = 1): "Such a Long Journey" is a well crafted film, a good shoot, and a showcase for some good performances. However, the story is such a jumble of subplots and peculiar characters that it becomes a sort of Jack of all plots and master of none. Also, Western audiences will likely find the esoterics of the rather obscure Parsee culture a little much to get their arms around in 1.7 hours. Recommended for those with an interest in India.

**Rewrite** (W = 0): "Such a Long Journey" is a poorly crafted film, a bad shoot, and a showcase for some poor performances. Moreover, the story is such a jumble of subplots and peculiar characters that it becomes a sort of Jack of all plots and master of none. Additionally, Western audiences will likely find the esoterics of the rather obscure Parsee culture a little too much to get their arms around in 1.7 hours. Not recommended for those with an interest in India.

**Rewrite of Rewrite**: "Such a Long Journey" is a beautifully crafted film, a fantastic shoot, and a showcase for some outstanding performances. Moreover, the story is a rich tapestry of subplots and intriguing characters that it becomes a masterful blend of narratives. Additionally, Western audiences will likely find the esoterics of the unique Parsee culture an enriching experience to explore in 1.7 hours. Highly recommended for those with an interest in India.

Rewards (Original, Rewrite, Rewrite of Rewrite): (0.11270, 0.08983, 0.11305)

#### From the (Helpsteer, Helpfulness) experiment:

**Reward Question**: What are some examples of songs that were hits during the early 2000s? I want your answers in an enumerated format (1., 2., etc.).

**Original** (W = 1): During the early 2000s, several songs gained popularity and became hits. Here are five examples:

1. "Yeah!" by Usher: This song, which features Lil Jon and Ludacris, reached number one on the Billboard Hot 100 chart in 2004.

2. "Low" by Flo Rida: This song, which features Tiesto, reached number one on the Billboard Hot 100 chart in 2008.

3. "Promiscuous Girl" by Nelly Furtado: This song reached number one on the Billboard Hot 100 chart in 2006.

4. "Pon de Replay" by Rihanna: This song reached number 12 on the Billboard Hot 100 chart in 2005.

5. "Irreplaceable" by Beyonce: This song reached number one on the Billboard Hot 100 chart in 2006.

**Rewrite** (W = 0): Here are some songs from the 2000s.

Rewrite of Rewrite: Of course! Here are some songs from the 2000s that you might enjoy exploring:

Rewards (Original, Rewrite, Rewrite of Rewrite): (0.10166, 0.05869, 0.06788)

#### From the (Helpsteer, Complexity) experiment:

**Reward Question**: Consider this reference information delimited in """: """ Separation anxiety occurs in adults as well, and can be an equally serious problem, so much so that psychologists have considered adding it to the diagnostic manual. Many adults suffer from separation anxiety issues and either may not be aware, or fail to seek treatment. Thus, separation anxiety in adults is likely underreported, and a much more widespread problem than originally believed to be.

Separation anxiety, when extreme, is usually pretty easy to identify. Adults who have serious separation anxiety tend to have an unhealthy attachment to a person with whom they are close to, and experience intense anxiety and panic when having to separate from that person. Yet, in less severe cases of separation anxiety, the signs may not be as obvious. Some less apparent signs of ASA are:

Extreme Jealousy - adults with separation anxiety may demonstrate signs of jealousy in relationships. A fear of abandonment is often what drives those with ASA to experience jealousy. This is especially true if the jealousy is accompanied by anxious thoughts, such as a fear of being alone or irrational concerns about infidelity. Of course, jealousy may be completely unrelated to ASA - for example, control of others is the cause of jealousy, as are trust issues - but some forms of deep jealousy may also be due to separation anxiety. Over Strict Parenting - there is some evidence that extremely strict and demanding parents may have separation anxiety issues as well. Sometimes referred to as reverse-separation anxiety, the parents may be so concerned that their child will leave them someday that they try to control the child's life as much as possible. Stuck in Relationships - another way separation anxiety may manifest itself is in the way adults treat their relationships. Whether romantic, familial, or friend relationships, but also friendships and occasionally familial relationships, many with ASA work to maintain the relationship even when extremely unhealthy (emotionally, physically), out of fear of being alone. Mooching - those that "mooch" off their parents well into adulthood, or those that never seem to leave their friends' homes may be experiencing separation anxiety in some way. Because there are currently no diagnostic criteria for ASA, the discussion of ways it manifests is purely speculative. Regardless, adult separation anxiety is a genuine problem, and affects the lives of countless adults. """

Does the author use a biased tone of voice in the provided passage? Please explain your answer in at least one paragraph of 100 words or more in length. I want to make sure that the tone is objective and unprejudiced before presenting it to my collaborative group.

**Original** (W = 0): No, the author does not use a biased tone of voice in the provided passage. The author presents information about separation anxiety in adults in a neutral and objective manner. The language used is factual and does not contain any personal opinions or judgments. The passage also does not show any favoritism towards or prejudice against any particular group of people who may suffer from separation anxiety. Overall, the tone of the passage is consistent with the purpose of providing information about a psychological condition rather than advocating for or against any particular viewpoint.

**Rewrite** (W = 1): Certainly, the author refrains from employing a biased tone in the passage provided. The author meticulously conveys information regarding separation anxiety in adults with a neutral and objective disposition. The language employed is factual, devoid of personal opinions or subjective judgments. Moreover, the passage does not exhibit any inclination towards or bias against any specific demographic that may experience separation anxiety. In essence, the tone of the passage aligns seamlessly with the objective of disseminating information about a psychological condition, rather than endorsing or opposing any particular perspective.

**Rewrite of Rewrite**: The author avoids using a biased tone in the passage. They clearly present information about separation anxiety in adults in a neutral and objective way. The language is factual and free of personal opinions or subjective judgments. The passage does not show any bias for or against any group that might experience separation anxiety. Overall, the tone fits well with the goal of sharing information about a psychological condition, rather than supporting or opposing any specific viewpoint.

Rewards (Original, Rewrite, Rewrite of Rewrite): (0.15593, 0.16245, 0.15361)

## From the (IMDB, Vowels) Experiment:

## Reward Question: Write a movie review:

**Original** (W = 1): I would have enjoyed this moive slightly more had ont been for Jsaon (Herb) Evers constant harpnig on expermient. aMny ealry reviewers of The Sevne Samruai accused Toshiro Mifune of overacting. Yet, as more adn more critics viewed that film they saw it as being puprosefully done. Jason vEers is obviously not Toshiro Miufne, and his overacting is exactly that.jbr /¿ibr /¿Most of teh actors in this B classic were rather ogod actors, minus Evers and the shwogirls. If you watch this movei, you wolud have noticed Evers shouting almost every lnie, taht is until he is smoking and lbowing teh smoke coolly out hsi onse. ibr /¿ibr /¿The special effects were par fro the course in a B movie such as htis oen. In hindsight, there isn't much that stadns out in my mind as fnatastically good or bad for htis movie.

**Rewrite** (W = 0): Had it not been for Jason (Herb) Evers' constant harping on experiment, I would have enjoyed this movie slightly more. aMny ealry reviewers of The Sevne Samruai accused Toshiro Mifune of overacting. Yet, as more adn more critics viewed that film they saw it as being puprosefully done. Jason vEers is obviously not Toshiro Miufne, and his overacting is exactly that.jbr /¿ibr /¿Most of teh actors in this B classic were rather ogod actors, minus Evers and the shwogirls. If you watch this movei, you would have noticed Evers shouting almost every lnie, taht is until he is smoking and lbowing teh smoke coolly out hsi onse. jbr /¿ibr /¿The special effects were par fro the course in a B movie such as htis oen. In hindsight, there isn't much that stadns out in my mind as fnatastically good or bad for htis movie.

**Rewrite of Rewrite**: If it had not been for Jason (Herb) Evers' constant harping on experiment, I would have enjoyed this movie slightly more. aMny ealry reviewers of The Sevne Samruai accused Toshiro Mifune of overacting. Yet, as more adn more critics viewed that film they saw it as being puprosefully done. Jason vEers is obviously not Toshiro Miufne, and his overacting is exactly that.jbr /¿ibr /¿Most of teh actors in this B classic were rather ogod actors, minus Evers and the shwogirls. If you watch this movei, you wolud have noticed Evers shouting almost every lnie, taht is until he is smoking and lbowing teh smoke coolly out hsi onse. jbr /¿ibr /¿The special effects were par fro the course in a B movie such as htis oen. In hindsight, there isn't much that stadns out in my mind as fnatastically good or bad for htis movie.

Rewards (Original, Rewrite, Rewrite of Rewrite): (0.05196, 0.06177, 0.06195)