
DAC Replication Report

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Abstract

1 This paper is a reproduction of DAC: The Double Actor-Critic Architecture for
2 Learning Options by Zhang and Whiteson ((2019)). It tried to apply the actor-
3 critic technique to hierarchical reinforcement learning. We re-implemented the
4 DAC and some other baselines the author used for experiments and evaluated the
5 reproducibility of this work. We conducted empirical studies on 4 Mujoco games
6 the authors used with their hyper-parameters. In this setting, our results partially
7 support their claims.

8 1 Introduction

9 This DAC paper focuses on the hierarchical reinforcement learning area. The author examines the
10 existing hierarchical reinforcement learning methods and addresses two issues: (reference here)

- 11 • Although policy-based methods are often preferred in the MDP setting, theoretical study for
12 learning a master policy with policy-based intra-option methods is limited, and its empirical
13 success has not been witnessed so far.
- 14 • Despite the recent successes of gradient-based option learning algorithms, most of them
15 customize the original algorithm to the option-based SMDP. Consequently, we cannot
16 directly leverage recent advances in gradient-based policy optimization from MDPs.

17 To address these issues, this paper reformulates the SMDP of the option framework as two augmented
18 MDPs: one master MDP to select option, and several lower level MDPs for deciding action given
19 a specific option. The author applies actor-critic algorithm on each augmented MDP. Under this
20 setting, any policy optimization algorithms can be easily applied without specific customization for
21 the policy learning. The author also ran experiments on a few OpenAI Mujoco tasks, using their DAC
22 architecture combined with the Proximal Policy Optimization algorithm.

23 This paper contains two main experiments: single task learning and transfer learning. We will focus
24 on replicating the single task learning experiments first.

25 The conclusions from the single task learning experiments are:

- 26 • DAC+PPO outperform other algorithms (OC, IOPG, DAC+A2C). This shows that the
27 performance boost mainly comes from the PPO algorithm, which is the advantage of DAC
28 and AHP: to use policy optimization algorithms off the shelf to learn options.
- 29 • DAC+PPO performs similarly to vanilla PPO in 3 out of 4 single tasks. This is because
30 options aren't necessary for single tasks for good performance.

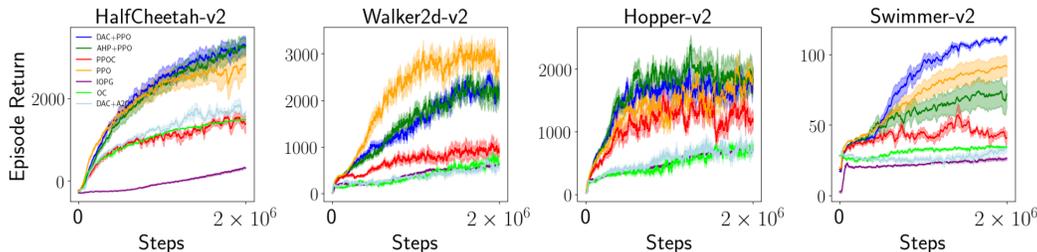


Figure 1: DAC single task learning result

31 The original single task learning experiment results are shown in Figure 1.
 32 Therefore, we would like to rerun the experiments using these algorithms:

$$DAC+PPO, PPO, DAC+A2C, OC, PPOC$$

33 to see if our results are consistent with their conclusion. Since OC and IOPG have similar performance,
 34 we will only do OC instead of both as a baseline.

35 2 Algorithms Explanation

36 2.1 Double Actor-Critic Architecture

37 The Double Actor-Critic architecture (DAC) reformulates the traditional option framework into two
 38 augmented MDPs. One high level MDP M^H is used to learn options, and a low level MDP M^L
 39 learns actions for a given option. Both MDPs share same samples from the environment for higher
 40 sample efficiency.

41 The agent’s learning process is shown in Algorithm 1:

Algorithm 1: Double Actor Critic algorithm

Initialize networks weight;

Reset the task env;

Get the initial state S_1 of the task, and initial option O_0 ;

while *current step* < *max step* **do**

42 **for** *timestep*=1,2,... **do**

 Sample an option O_t from $\pi_h(O|O_{t-1}, S_t)$;

 Sample an action A_t from lower level policy $\pi_l(A|O_t, S_t)$;

 Apply the sampled action in the task to get next state S_{t+1} and reward R_t ;

 Update current step number and record the reward R_t for plotting;

 Apply some policy gradient algorithm to update networks weights;

43 In our actual training, we set the max step to be two million for all of our agents, as the author did.

44 2.2 Proximal Policy Optimization

45 Proximal Policy Optimization(PPO) is an algorithm proposed by Schulman et al. ((2017)), having
 46 state-of-the-art performance but is easy to implement and tune compared to other algorithms. It
 47 stems from the idea of off-policy policy gradient, utilizing importance sampling in the process of
 48 updating the policy so that the same set of data can be used to train the agent for several epochs,
 49 largely improving the data efficiency. Besides, it improves upon Trust Region Policy Optimization
 50 (TRPO) in that it uses a much simpler constraint while achieving similar performance.

51 For PPO, the objective function is

$$L^{\text{CLIP}}(\theta) = \hat{\mathbb{E}}_t[\min(r_t(\theta)\hat{A}_t, \text{clip}(r_t(\theta), 1 - \epsilon, 1 + \epsilon)\hat{A}_t)], \quad r_t(\theta) = \frac{\pi_\theta(a|s)}{\pi_{\theta_{old}}(a|s)}$$

52 In contrast to TRPO where a constraint of KL-divergence between the old and new policy is applied,
53 PPO simply clips the loss function to serve the purpose of ensuring the stability of the training
54 process, and it turns out to work pretty well in many kinds of tasks.
55 The Pseudo Code of PPO is shown in Algorithm 2.

Algorithm 2: Proximal Policy Optimization

Run $\pi_{\theta_{old}}$ for T timesteps ;
Compute advantage estimates $\hat{A}_1, \dots, \hat{A}_T$, and record $\pi_{\theta_{old}}(a_1|s_1), \dots, \pi_{\theta_{old}}(a_T|s_T)$;
for $epoch=1, 2, \dots$ **do**
56 **for** $minibatch=1, \dots, T/minibatch_size$ **do**
 Sample minibatch_size of experience steps;
 Compute $L^{CLIP}(\theta)$ with current π_θ ;
 Compute the critic error and add them together;
 Backprop to update π_θ ;

57 **2.3 Option Critic**

58 The Option-Critic Architecture proposed by Bacon et al. ((2017)) is an architecture built upon the
59 combination of option framework and the classical actor-critic algorithm, where they derived the
60 policy gradient theorems for options, i.e.

$$\begin{aligned} \nabla_\nu v_\pi(S_0) &= \sum_{s,o} \rho(s, o|S_0, O_0) \sum_a q_\pi(s, o, a) \nabla_\nu \pi_o(a|s), \\ \nabla_\phi v_\pi(S_0) &= - \sum_{s',o} \rho(s', o|S_1, O_0) (q_\pi(s', o) - v_\pi(s')) \nabla_\phi \beta_o(s') \end{aligned}$$

61 where $\rho(s, o|S_0, O_0) = \sum_{t=0}^{\infty} \gamma^t P(s_t = s, o_t = o|S_0, O_0)$. Based on these theorems, they con-
62 structed an algorithm known as option-critic, where the actor consists of the intra-option policies,
63 termination functions, while the critic contains the calculation of q_π (and v_π), and a ϵ -greedy master
64 policy is applied over options.

65 The pseudo code of OC is shown in Algorithm 3:

Algorithm 3: Option-critic with Q-learning

$s \leftarrow s_0$;
Choose ω according to an ϵ -soft policy over options $\pi_\Omega(s)$;
while s is non-terminal **do**
 Choose action α according to $\pi_{\omega, \theta}(\alpha | s)$;
 Execute α in s , observe s', r ;
 $\delta \leftarrow r - Q_U(s, \omega, \alpha)$;
 if s' is non-terminal **then**
66 $\delta \leftarrow \delta + \gamma(1 - \beta_{\omega, \vartheta}(s')) Q_\Omega(s', \omega) + \gamma \beta_{\omega, \vartheta}(s') \max_{\bar{\omega}} Q_\Omega(s', \bar{\omega})$;
 $Q_U(s, \omega, \alpha) \leftarrow Q_U(s, \omega, \alpha) + \alpha \delta$;
 $\theta \leftarrow \theta + \alpha_\theta \frac{\partial \log \pi_{\omega, \theta}(\alpha | s)}{\partial \theta} Q_U(s, \omega, \alpha)$;
 $\vartheta \leftarrow \vartheta - \alpha_\vartheta \frac{\partial \beta_{\omega, \vartheta}(s')}{\partial \vartheta} (Q_\Omega(s', \omega) - V_\Omega(s'))$;
 if $\beta_{\omega, \vartheta}$ terminates in s' **then**
 choose new ω according to ϵ -soft($\pi_\Omega(s')$);
 $s \leftarrow s'$;

67 **2.4 Advantage Actor-Critic**

68 Advantage Actor-Critic (A2C) released by OpenAI is a synchronous, deterministic variant of Asyn-
69 chronous Advantage Actor-Critic proposed by Mnih et al. ((2016)) with equal performance.
70 The advantage of a state-action pair is the difference between the state-action Q value, and the state's

71 value:

$$A(s, a) = Q(s, a) - V(s)$$

72 In this algorithm, first initialize network parameters θ with random values. Second, play N steps
73 in the environment using the current policy π_θ , saving state s_t , action a_t and reward r_t . Third,
74 $R = 0$ if the end of the episode is reached or $V_\theta(s_t)$. Fourth, for $i = t - 1 \dots t_{start}$, accumulate the
75 PG $\delta\theta_\pi \leftarrow \delta\theta_\pi + \nabla_\theta \log \pi_\theta(a_i | s_i)(R - V_\theta(s_i))$ and the value gradients $\delta\theta_v \leftarrow \delta\theta_v + \frac{\delta(R - V_\theta(s_i))^2}{\delta\theta_v}$.
76 Finally, update parameters using the accumulated gradients, moving in the direction of PG $\delta\theta_\pi$ and in
77 the opposite direction of the value gradients $\delta\theta_v$. Repeat from second step until the convergence is
78 reached.

79 3 Challenges

80 Throughout the process of trying to understand and replicate this work, we encountered some
81 challenges.

- 82 • Understanding the DAC architecture required us to have deep understandings of some prior
83 works that were new to us.
- 84 • Implementing several baselines is a considerable amount of work.
- 85 • The way policy gradient algorithms are used to optimize the two MDPs separately in DAC
86 architecture is confusing to us, so we had to look at the author’s implementation as a
87 reference to help us understand how DAC and policy gradient are integrated together.

88 4 Implementation

89 Our code for experiment can be found at our Github Repository¹.

90 4.1 Fully Connected Network

91 Each of our agents utilizes multiple fully connected networks in their implementation. They all have
92 similar architecture, with the difference mostly being in the output layer.
93 They all have an input layer with dimension being the state dimension, two hidden layers with 64
94 nodes each, and one output layer. The author used the Tanh activation function for the first three
95 layers in Mujoco tasks, but we found a ReLU activation function generates better results. That’s what
96 we use for our replicate experiments.

97 4.2 PPO

98 Our implementation of PPO is based on higgsfield’s implementation². In the real implementation, a
99 parametrized Gaussian policy is employed as the actor in the continuous situation, and Generalized
100 Advantage Estimation(GAE) by Schulman et al. ((2015)) is used to compute the advantage function.
101 10 epochs are applied to train the data from every 2048 steps, with a minibatch size of 64.

102 Also, we find an interesting phenomenon that the orthogonal initialization by Saxe et al. ((2013))
103 with an appropriate weight scale plays an important role in achieving good performance for the PPO
104 algorithm. For example, in the HalfCheetah task, the PPO algorithm without orthogonal initialization
105 can only achieve an average episodic reward of 2500 to 3000 in 2e6 steps, while with orthogonal
106 initialization (weight scale 1) the PPO algorithm is able to achieve an average episodic reward over
107 3000 to even 4000.

108 4.3 DAC Architecture

109 Our DAC agent keeps track of $2k + 2$ separate fully connected networks, where k is the number of
110 options.

¹<https://github.com/DAC-Prime/supreme-waffle>

²<https://github.com/higgsfield/RL-Adventure-2/blob/master/3.ppo.ipynb>

111 We use 2 networks for high level MDP learning, one to predict master policy, the other one to predict
112 the values of the current state. Both networks have the number of options as their output dimension.
113 The policy net uses softmax as output layer activation function, and the value net output the prediction
114 directly without any activation function.

115 For each option, we utilize two more networks for action selection. The first one generates an action
116 policy for its corresponding option given a state, and the other one predicts the termination probability.
117 The policy net outputs a tensor with the same shape as the Mujoco task action. It has Tanh as the final
118 activation function. The termination net predicts a single number, using sigmoid as final activation.

119 **4.4 OC**

120 For OC, we here implement a slightly different version of option-critic based on the implementation
121 of DAC’s authors’³ for comparison, which uses multiple (16) workers to train the option-critic
122 synchronously, and only compute the gradients and update the policy every 5 steps.

123 Built upon option-critic, we also implement the Proximal Policy Option Critic (PPOC) algorithm
124 proposed by Klissarov et al. ((2017)), which is a combination of PPO and OC. PPOC employs the
125 PPO loss function to train the intra-option policies, and include the master policy (softmax) over
126 options in its actor so that it will also be trained by backpropagation.

127 **4.5 A2C**

128 We consulted the OpenAI baselines for A2C ⁴.

129 **5 Environment Setup**

130 **5.1 OpenAI Gym and Mujoco**

131 The experiments in this paper consist of two parts: single task learning and transfer learning. The
132 single task learning part, which we focus on, uses four Mujoco environments from OpenAI Gym:

HalfCheetah-v2, Walker2d-v2, Hopper-v2, Swimmer-v2

133 In the appendix, the author mentioned that the states from environments are normalized using running
134 std and mean as preprocessing steps. This is also confirmed in the OpenAI Gym Github repo that
135 Mujoco environments states require this normalization preprocess for it to be learned properly. We
136 utilized the existing normalizer provided in the OpenAI Baseline Github repo⁵ for this purpose.

137 **5.2 Platform**

138 The experiments are all ran on the cluster of Center for Computation Vision at Brown University.
139 Anaconda is used for package control and environment setup. The activation file of Mujoco is
140 provided by Prof. Michael Littman. To maintain the consistency between different systems, we also
141 create a Docker recipe from which a Docker image can be built and ran in any system.

142 **5.3 Plotting**

143 For our experiments, to avoid coincidence and extend the universality, we have trained 10 agents for
144 each of the four Mujoco tasks(HalfCheetah-v2, Walker2d-v2, Hopper-v2, and Swimmer-v2) to plot
145 our episodic cumulative rewards graph. The results of the mean value with the standard error were
146 plotted for the agents we have implemented.

147 **6 Experiments Result**

148 Our replicated performance of the DAC-PPO, DAC-A2C, OC, PPO and PPOC agent roughly matches
149 the result reported in the original DAC paper.

³https://github.com/ShangtongZhang/DeepRL/blob/DAC/deep_rl/agent/OC_agent.py

⁴<https://github.com/openai/baselines/blob/master/baselines/a2c>

⁵<https://github.com/openai/baselines>

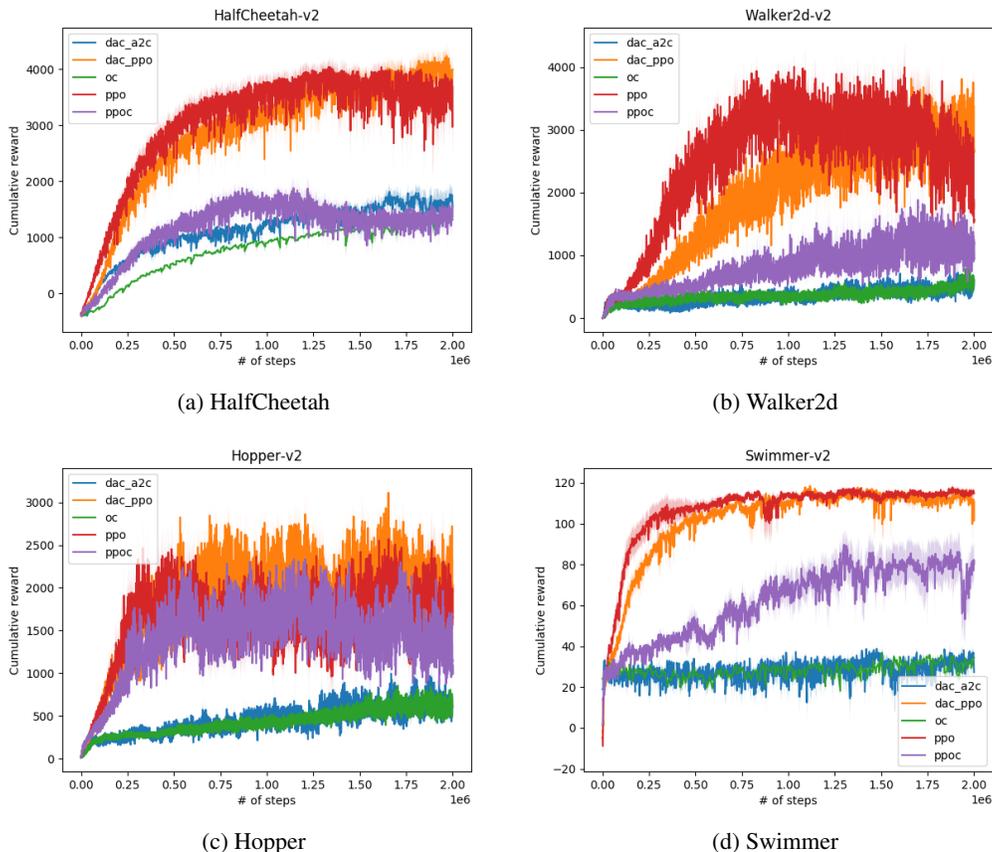


Figure 2: Experimental results for four Mujoco games

150 Specifically,

- 151 1. Our implementations of DAC-A2C and OC turn out to have approximately the same per-
 152 formance as the authors', which is worse than that of PPO and DAC-PPO. The author
 153 concluded that the advantage mainly comes from PPO, and our results are in line with this
 154 claim.
- 155 2. For HalfCheetah-v2 and Hopper-v2, our DAC-PPO agent and PPO agent achieve approxi-
 156 mately the same performance after two million steps of learning. This matches the original
 157 result.
- 158 3. For Walker-v2 task, the author concluded that the DAC-PPO and PPO agents perform
 159 similarly, although the graph showed that the vanilla PPO performs a little better than
 160 DAC-PPO. Our agents perform pretty close to each other at the end of training.
- 161 4. For Swimmer-v2 setting, the author reported a better performance from DAC-PPO agent
 162 compared to vanilla PPO. Our DAC-PPO agent achieved similar cumulative rewards to the
 163 author's result, but our vanilla PPO performed better than theirs. So our result doesn't have
 164 that large margin in the original result.

165 We have also noticed a larger variation in our replicated agents' performance compared to the graph
 166 reported in the DAC paper. The reason could be due to a bug inside the original implementation. The
 167 author unintentionally fixed the Mujoco environments random seed across multiple runs, making
 168 their experiment less stochastic.⁶

⁶<https://github.com/ShangtongZhang/DeepRL/issues/67>

169 We did not have the chance to re-implement and experiment the Augmented Hierarchical Policy
170 (AHP) architecture, so our replication could not verify the author’s comparison between DAC and
171 AHP.

172 **7 Reflection**

173 Our experiment results roughly match those reported by the author. We think our replication
174 experience partially supports the paper.

175 About the first point, our replication generates state-of-art performance in the four Mujoco tasks.
176 This is an empirical success of master policy learning with policy-cased intra-option methods.

177 Our replication verifies that the proposed DAC architecture is able to utilize PPO and A2C algorithms
178 for optimization. However, it’s hard for us to figure out the way DAC architecture and policy gradient
179 algorithms are integrated together from the paper alone. It’s probably due to our lack of background
180 knowledge and experience, but that’s still not intuitive from our perspective.

181 The choice of activation function can influence the results significantly, which might be worth digging
182 in the underneath reasons.

183 **References**

184 Shangdong Zhang and Shimon Whiteson. *Dac: The double actor-critic architecture for learning*
185 *options*. *ArXiv*, abs/1904.12691, 2019.

186 John Schulman, Filip Wolski, Prafulla Dhariwal, Alec Radford, and Oleg Klimov. *Proximal policy*
187 *optimization algorithms*. In *arXiv preprint, arXiv:1707.06347.*, 2017.

188 Pierre-Luc Bacon, Jean Harb, and Doina Precup. *The option-critic architecture*. In *Thirty-First AAAI*
189 *Conference on Artificial Intelligence*, 2017.

190 Volodymyr Mnih, Adrià Puigdomènech Badia, Mehdi Mirza, Alex Graves, Timothy P. Lillicrap, Tim
191 Harley, David Silver, and Koray Kavukcuoglu. *Asynchronous methods for deep reinforcement*
192 *learning*. In *International conference on machine learning*, 2016.

193 John Schulman, Philipp Moritz, Sergey Levine, Michael Jordan, and Pieter Abbeel. *High-dimensional*
194 *continuous control using generalized advantage estimation*, 2015.

195 Andrew M Saxe, James L McClelland, and Surya Ganguli. *Exact solutions to the nonlinear dynamics*
196 *of learning in deep linear neural networks*. *arXiv preprint arXiv:1312.6120*, 2013.

197 Martin Klissarov, Pierre-Luc Bacon, Jean Harb, and Doina Precup. *Learnings options end-to-end for*
198 *continuous action tasks*, 2017.