Variational Autoencoders with implicit priors for short-duration text-independent speaker verification

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Abstract

In this work, we exploited different strategies to provide prior knowledge to com-1 monly used generative modeling approaches aiming to obtain speaker-dependent 2 low dimensional representations from short-duration segments of speech data, 3 making use of available information of speaker identities. Namely, convolutional 4 variational autoencoders are employed, and statistics of its learned posterior distri-5 bution are used as low dimensional representations of fixed length short-duration 6 utterances. In order to enforce speaker dependency in the latent layer, we intro-7 duced a variation of the commonly used prior within the variational autoencoders 8 framework, i.e. the model is simultaneously trained for reconstruction of inputs 9 along with a discriminative task performed on top of latent layers outputs. The 10 effectiveness of both triplet loss minimization and speaker recognition are evaluated 11 as implicit priors on the challenging cross-language NIST SRE 2016 setting and 12 compared against fully supervised and unsupervised baselines. 13

14 **1** Introduction

Variational autoencoders (VAEs) (1; 2) have been introduced as an effective framework within the context of generative models that support tractable approximate inference (3), leveraging neural networks both for generative modeling as well as for approximate inference, usually employing a non-informative prior. However, follow-up works have shown that too simplistic of a prior will in general lead to also simplistic posteriors which might not encode relevant information about the inputs.

Attempts to overcome the above mentioned issue include adversarial autoencoders, proposed origi-21 nally in (4), which employ an adversarial game on top of latent variables. The discriminator tries 22 to distinguish samples from the posterior and prior distributions, while the encoder tries to produce 23 samples that are indistinguishable from the prior. Moreover, stochastic variational methods (5; 6) 24 appeared as an alternative in which informative data-dependent priors can be used. Sampling methods 25 are employed to estimate gradients of the variational gap, such that any prior from which one can 26 sample can be used. In both of the described cases, the only requirement for a prior is the possibility 27 28 of efficiently sampling from it.

Even though aforementioned adversarial autoencoders and stochastic variational methods allow the use of non-trivial priors, designing prior distributions which yield desired properties on the finally learned posterior is a challenging task in itself. In this work, rather than explicitly matching posterior and prior distributions, we evaluate the effectiveness of enforcing relevant properties on the posterior distribution by introducing auxiliary discriminative tasks at train time, making use of available labels. By doing so, we argue prior knowledge is introduced implicitly, since desired properties are directly enforced into the posterior distribution. ³⁶ The remainder of this paper is organized as follows: Section 2 includes a brief description of the VAE

framework along with a brief definition of the speaker verification problem, which we employ as a test-bed for the proposed approach. Section 3 details the strategy we proposed in order to enforce

desired properties within the VAE's learned posterior. In Section 4 we evaluate our method, and

⁴⁰ finally draw conclusions along with future directions in Section 5.

41 2 Background: Variational Autoencoders and Speaker Verification

- ⁴² Consider p(X, Z), where X is the observed data and Z is the latent representation. The posterior ⁴³ distribution p(Z|X) can be approximated within the family of distributions $q(Z|X, \lambda)$, parametrized ⁴⁴ by λ . The so-called variational gap has to be minimized in order to give the maximum likelihood ⁴⁵ estimate of λ . The variational gap is defined as the Kullback-Leibler divergence between the ⁴⁶ approximate $q(Z|X, \lambda)$ and the true posterior over Z, p(Z|X), written as $\text{KL}(q(Z|X, \lambda)||p(Z|X))$. ⁴⁷ A common approach to minimize $\text{KL}(q_{\lambda}(Z|X)||p(Z|X))$ with respect to λ is to define the Evidence
- ⁴⁷ A common approach to minimize $KL(q_{\lambda}(Z|X)||p(Z|X))$ with respect to λ is to define the Evidence ⁴⁸ Lower Bound (ELBO) given by:

$$\mathsf{ELBO}(\lambda) = \log(p(X)) - \mathsf{KL}(q(Z|X,\lambda)||p(Z|X)), \tag{1}$$

⁴⁹ whose terms can be rearranged, and ELBO can be simplified to:

$$\mathsf{ELBO}(\lambda) = \mathbb{E}_q[\log p(X|Z)] - \mathsf{KL}(\log q(Z|X,\lambda)||p(Z)).$$
(2)

Two main components present in above equation are the inference model $q(Z|X, \lambda)$ and the generative model p(X|Z). VAEs parametrize both distributions using neural networks in an encoder/decoder setup. The encoder takes samples from X and outputs the parameters λ of the latent variable model $q_{\theta}(Z|X)$. The decoder receives samples from Z as input and returns reconstructed data samples from $p_{\phi}(X|Z)$. Parameters θ and ϕ are the weights and biases of the neural networks which are selected to minimize the negative ELBO using stochastic gradient descent. The negative of the ELBO yields the following loss function used for training the neural networks:

$$l(\theta, \phi) = -\mathbb{E}_{q_{\theta}(z|x)}[\log p_{\phi}(X|Z)] + \mathrm{KL}(\log q_{\theta}(Z|X)||p(Z)).$$
(3)

First term in above equation is equivalent to maximum likelihood estimation, thus it is in general
substituted by a reconstruction loss, while the second term can be seen as a regularizer, which tries to
ensure that the approximation follows the prior distribution as much as possible.

The posterior $q_{\theta}(Z|X)$ is in general assumed to be an uncorrelated Gaussian. In order to train the VAE using stochastic gradient descent, the reparametrization trick (7; 8) is employed allowing gradients computation through the sampling process between encoder and decoder. Hence, the outputs of the encoder network are the statistics of $q_{\theta}(Z|X)$ and Z - input for the decoder - is ultimately obtained by $Z = \mu(X) + \sigma(X) \cdot \epsilon$, where $\mu(X)$ and $\sigma(X)$ are the encoder's outputs given X, while ϵ is sampled from $\mathcal{N}(0, I)$.

Speaker verification consists of accepting or rejecting a claimed identity by comparing two spoken utterances, the first of these utterances being used for enrollment (produced by the speaker with the target identity) and the second utterance is obtained from the verified speaker (9).

⁶⁹ Under the text-independent setting, speaker verification is performed on top of unconstrained spoken

⁷⁰ phrases of arbitrary length. The added phonetic variability in this scenario represents an extra adverse

⁷¹ factor when compared to the session and speaker variabilities, present in the text-dependent case

72 (10). Classical approaches for Automatic Speaker Verification split the problem into two distinct

73 phases: (i) compute low dimensional speaker representations; (ii) perform binary classification on

⁷⁴ top of pre-computed representation of enrollment and test utterances.

75 **3** Proposed Model

⁷⁶ Unlike the ELBO-based loss definition in Equation 3, we evaluate the use of an auxiliary task on ⁷⁷ top of the posterior statistics $\mu(X)$, with the aim at enforcing a multi-modal posterior with modes

78 depending on given class labels. Our training loss is thus defined by:

$$l(\theta, \phi) = (1 - \beta) ||X - X'||_2^2 + \beta D(\mu(X), y),$$
(4)

⁷⁹ where the first term, the mean squared error between the input X and its reconstructed pair X', is

the same as in the standard VAE setting, while the second term, $D(\mu(X), y)$, is some discriminative

loss which plays the role of the KL term in Equation 3, considering given class labels y. $\beta \in [0, 1]$

is a tunable hyperparameter. $\mu(X)$ is employed as a low-dimensional embedding of inputs for the discriminative auxiliary task. Two distinct choices of $D(\mu(X), y)$ are evaluated here:

1. A soft triplet loss defined by softplus($||d_{+} - d_{-}||_{2}$), where d_{+} and d_{-} correspond to a distance measure between pairs of embeddings. d is chosen as $d(\mu(X_{1}), \mu(X_{2})) =$ $1 - \frac{\mu(X_{1}) \cdot \mu(X_{2})}{||\mu(X_{1})||_{2}||\mu(X_{2})||_{2}}$, and the second term is the cosine of the smallest angle between $\mu(X_{1})$ and $\mu(X_{2})$.

2. The sum of triplet loss with a multi-class classification loss, i.e. $\mu(X)$ is linearly projected into an output layer and cross-entropy loss is measured using available labels.

We evaluate the described setting on the speaker verification task. *RMSProp* is employed for optimization with α set to 0.99. The global learning rate starts at 0.001 and is halved once triplet loss, measured on a validation set held out of training, plateaus for 30 epochs. Training is carried out in a single Titan X NVIDIA GPU, with minibatches of size 64. Minibatches are contructed such that two random segments of different utterances belonging to the same speaker are sampled to form same class pairs (positive), and a random sample from a different speaker is selected to compose the different classes pair (negative). β was at 0.8 for all experiments.

97 4 Experimental Setup and Results

Evaluation is performed on top of the cross-language NIST SRE 2016 setting (11). Test data in 98 Tagalog and Cantonese are available, while train data is in English. Embeddings obtained with a 99 standard VAE, along with our two proposed strategies using two distinct $D(\mu(X), y)$ previously 100 described choices are compared with x-vectors, a fully-supervised approach shown to outperform 101 i-vectors (12) in the full-recording setting (13). Train data is composed of: Switchboard-2, phases 102 1, 2, and 3, along with NIST SREs from 2004 to 2010 combined with Mixer 6, which sums up to 103 approximately 7000 speakers, out of which we remove all the recordings of 50 speakers to be used as 104 validation set. Training is performed on top of 40-dimensional log-mel filter banks. Only the SRE 105 portion is used for training probabilistic linear discriminant analysis (PLDA) (14), which was used as 106 107 a backend at evaluation phase. Since our model requires fixed size inputs, speech segments of 256 108 frames were randomly selected from each recording at train time. We augment the described train 109 dataset following the approach in (13), i.e. with additive background noise from the MUSAN corpus and reverberation by convolving room impulse responses (RIR) with original audio data (MUSAN 110 and RIR are available at www.openslr.org). We removed silence frames from data using a simple 111 energy-based voice activity detector. 112

For enrollment, test, and unlabelled (used for PLDA adaptation) data, embeddings of each recording are obtained from 256 frames windows without overlap, and then averaged, such that each test utterance is represented by a single fixed dimensional representation, even though models only have access to short-duration segments.

PLDA was employed as backend after dimensionality reduction of embeddings from 256 to 128, using linear discriminant analysis. PLDA is trained on embeddings from the *SRE* partition of training data, which are computed following the same approach as described for test data for the case of our proposed models, while using the full-recordings in the case of x-vectors. Results in terms of Equal Error Rate (EER) are shown in Table 1 for embeddings obtained from VAEs trained both in a standard fashion, and our proposed approaches.

	PLDA			Adapted PLDA			
	Cantonese	Tagalog	Pooled	Cantonese	Tagalog	Pooled	
X-vector	30.91	31.32	31.04	14.41	20.98	17.62	
VAE	31.55	32.13	31.83	31.10	32.24	31.66	
VAE+Triplet loss	21.81	27.80	24.79	19.89	25.50	22.76	
VAE+Cross-entropy	21.46	27.05	24.28	16.50	23.00	20.02	

Table 1: EER obtained for embeddings averaged over short short-duration segments.

As expected, including speaker identities relevantly increases the discriminability of learned repre-123

sentations when compared to a fully-unsupervised VAE, in both Tagalog and Cantonese evaluations. 124 We further notice that performing speaker recognition on top of statistics of the posterior is more 125

126 effective than the metric learning approach of triplet loss minimization alone.

In order to overcome the relevant domain shift between train and test data due to different spoken 127 languages, the model adaptation scheme introduced in (15) is utilized for PLDA. To do so, embeddings 128 of unlabelled data in Cantonese and Tagalog are clustered, and clusters are used as speaker identities, 129 which are then employed for training a second PLDA model. The final model is obtained by simply 130

averaging the second order statistics of the two trained models. 131

Results, as reported in the right section of Table 1, correspond to the evaluation using the adapted 132 PLDA model. Interestingly, one can notice that the higher the *level of supervision* employed on 133 embeddings model training, the higher is the performance gain when adaptation is used. By level of 134 supervision we mean how relevant class labels (speaker identities in the studied case) are at train time. 135 Standard VAE makes no use of class labels, while triplet loss employs such information for triplets 136 construction only. Even in the case in which our VAE is trained with cross-entropy minimization, 137 semi-supervised settings can be used, leveraging available unlabelled data, which is not the case for 138 x-vectors, for instance, whose training is performed in a fully-supervised fashion. We thus argue that 139 an increasing level of supervision induces domain-dependent representations, and this is the reason 140 adaptation yields a huge improvement in such cases. 141

We further evaluate the discriminability of the representations corresponding to the statistics of 142 posterior distributions approximated by VAEs trained in a standard fashion and making use of 143 available speaker identities by plotting 2-dimensional t-SNE embeddings of $\mu(X)$, computed for 10 144 speakers held out of training. Figures 1, 2, 3 are ordered in increasing level of supervision, which 145 once more supports the claim that making use of class labels to perform discriminative tasks on top 146 of statistics of the posterior is an effective strategy to enforce desired properties. 147

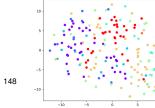
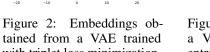


Figure 1: Embeddings obtained from a standard VAE with triplet loss minimization.



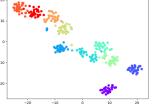


Figure 3: Embeddings from a VAE trained with crossentropy minimization

Conclusion 5 149

posterior.

In this work, we proposed to exchange the divergence term within the variational autoencoders 150 training loss by some discriminative cost, leveraging available class labels. We thus argue such an 151 approach is equivalent to implicitly defining prior distributions, directly inducing desired properties 152 in the learned posterior distribution. Evaluation is performed on the challenging cross-language NIST 153 SRE 2016 evaluation setting, for which we show embeddings obtained by such an approach are 154 speaker-dependent, as enforced by discriminative tasks performed at train time. Future directions 155 include the evaluation of this framework on the semi-supervised setting, employing unlabelled data 156 for training of the generative model, along with labelled data. 157

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Appendix A - Model architecture

Architectures employed for encoder and decoder are detailed in Tables 2 and 3. Batch normalization

is used after all convolution layers. Inputs present dimensionality [40, 256], corresponding to 40 filter

196 banks and 256 frames.

Table 2: Encoder	architecture
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Table 2: Encoder architecture						
Layer	Outputs	Kernel size	Stride	Dilation	Activation	
Convolution	19, 84, 128	5, 5	2, 3	1, 2	ELU	
Convolution	9, 40, 256	5, 5	2, 2	1, 2	ELU	
Convolution	4, 40, 512	5, 5	2, 1	1, 1	ELU	
Convolution	1, 40, 1024	5, 5	2, 1	1, 1	ELU	
Average Pooling	1, 1, 1024	1,40	1, 1	-	-	
Dense	1024	-	-	-	ELU	
Dense	256, 256	-	-	-	ELU, -	

Table 3: Decoder architecture

Layer	Outputs	Kernel size	Stride	Dilation	Activation
Dense	800	-	-	-	ELU
Transpose Convolution	7, 14, 128	3, 4	1, 2	1, 3	ELU
Transpose Convolution	11, 29, 128	3, 4	2, 2	1, 2	ELU
Transpose Convolution	19, 59, 256	3, 4	2, 2	1, 2	ELU
Transpose Convolution	18, 118, 128	4, 6	1, 2	1, 1	ELU
Transpose Convolution	38, 246, 32	4, 12	2, 2	1, 1	ELU
Transpose Convolution	40, 256, 1	5, 13	1, 1	1, 1	-