Federated Hypergradient Descent

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Abstract

In this work, we explore combining automatic hyperparameter tuning and opti-1 mization for federated learning (FL) in an online, one-shot procedure. We apply 2 3 a principled approach on a method for adaptive client learning rate, number of 4 local steps, and batch size. In our federated learning applications, our primary motivations are minimizing communication budget as well as local computational 5 resources in the training pipeline. Conventionally, hyperparameter tuning meth-6 ods involve at least some degree of trial-and-error, which is known to be sample 7 inefficient. In order to address our motivations, we propose FATHOM (Federated 8 AuTomatic Hyperparameter OptiMization) as a one-shot online procedure. We 9 investigate the challenges and solutions of deriving analytical gradients with respect 10 to the hyperparameters of interest. Our approach is inspired by the fact that we 11 have full knowledge of all components involved in our training process, and this 12 fact can be exploited in our algorithm impactfully. We show that FATHOM is 13 more communication efficient than Federated Averaging (FedAvg) with optimized, 14 static valued hyperparameters, and is also more computationally efficient overall. 15 As a communication efficient, one-shot online procedure, FATHOM solves the 16 bottleneck of costly communication and limited local computation, by eliminat-17 ing a potentially wasteful tuning process, and by optimizing the hyperparamters 18 adaptively throughout the training procedure without trial-and-error. We show 19 our numerical results through extensive empirical experiments with the Federated 20 EMNIST-62 (FEMNIST) and Federated Stack Overflow (FSO) datasets, using 21 FedJAX as our baseline framework. 22

23 1 Introduction

Federated learning (FL) for on-device applications has its obvious social implications, due to its 24 inherent privacy-protection feature. It opens up a broad range of opportunities to allow a massive 25 number of devices to collaborate in developing a shared model by retaining private data on the 26 devices. The ubiquity of machine learning (ML) on consumer data, coupled with the growth of privacy 27 28 concerns, has pushed researchers and developers to look for new ways to protect and benefit end-users. In order for FL to deliver its promise in deployed applications, there are still many open challenges 29 remained to be solved. We are especially interested in the overall communication efficiency of the FL 30 pipeline for it to be realistically deployed in a unique communication environment over expensive 31 links. To begin, consider a typical step in a machine learning (ML) pipeline: hyperparameter tuning. 32 Whether it is in a centralized, distributed or federated setting, it is an essential step to achieve an 33 optimal operation for the training process. At the heart of an ML training process is the optimization 34 algorithm. In particular, we are interested in using Federated Averaging (FedAvg) as our baseline 35

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³⁶ federated optimization algorithm for our work. This is because, despite all the recent innovations in

³⁷ FL since its introduction in 2016 by McMahan et al. [2016], FedAvg remains the de facto standard in

³⁸ federated optimization for both research and practice, due to its simplicity and empirical effectiveness.

³⁹ In order for FedAvg to operate effectively, it requires properly tuned hyperparameter values.

Our work focuses specifically on hyperparameter optimization (HPO) of: 1) client learning rate, 40 2) number of local steps, as well as 3) batch size, for FedAvg. We propose FATHOM (Federated 41 AuTomatic Hyperparameter OptiMization), which is an online algorithm that operates as a one-shot 42 procedure. In the rest of this paper, we will go through a few notable recent state-of-the-art works on 43 this topic, and make justifications for our new approach. Then we will derive a few key steps for our 44 algorithm, followed by a theoretical convergence bound for adaptive learning rate and number of local 45 steps in the non-convex regime. Lastly, we present numerical results on our empirical experiments 46 with neural networks on the FEMNIST and FSO datasets. 47

48 Our contributions are as follows:

- We derive gradients with respect to client learning rate and number of local steps for FedAvg,
 for an online optimization procedure. We propose FATHOM, a practical one-shot procedure
 for joint-optimization of hyperparameters and model parameters, for FedAvg.
- We derive a new convergence upper-bound with a relaxed condition (see Section 4 and remark 2), to highlight the benefits from the extra degree-of-freedom that FATHOM delivers for performance gains.
- We present empirical results that show state-of-the-art performance. To our knowledge, we are the first to show gain from an online HPO procedure over a well-tuned equivalent procedure with fixed hyperparameter values.

2 Related Work and Justifications for FATHOM

We explore the question whether the FATHOM approach is justified over the more recent, state-of-59 the-art methods that are designed for the same goal: a single-shot online hyperparamter optimization 60 procedure for FL. Zhou et al. [2022] proposed Federated Loss SuRface Aggregation (FLoRA), a 61 general single-shot HPO for FL, which works by treating HPO as a black-box problem and by 62 performing loss surface aggregation for training the global model. Khodak et al. [2021] draws 63 inspiration from weight-sharing in Neural Architectural Search (Pham et al. [2018], Cai et al. [2019]), 64 and proposed FedEx, which is an online hyperparameter tuning algorithm that uses exponentiated 65 gradients to update hyperparameters. On the other hand, Mostafa [2019]'s RMAH and Guo et al. 66 [2022]'s Auto-FedRL both use REINFORCE (Williams [1992]) in their agents to update hyperparam-67 eters in an online manner, by using relative loss as their trial rewards. One basic assumption among 68 these methods, is that at least some of the gradients with respect to the hyperparameters are unavail-69 able directly. Generalized techniques are used to update these quantities, involving Monte-Carlo 70 sampling and evaluation with held-out data. One key benefit with techniques such as these is their 71 generalizability for a wide range of different hyperparameters. On the other hand, we identify a few 72 areas with these methods that we would like to improve on. One, information about the internals of 73 the procedure can and should be exploited. Two, communication overhead becomes a concern, since 74 sufficient Monte-Carlo sampling is required for some of these techniques to converge, an example 75 being the re-parametrization trick (Kingma and Welling) [2013]) which is used for FedEx, RMAH and 76 Auto-FedRL. From initial observations of their empirical results, while these methods are successful 77 in hyperparameter tuning and reaching target model accuracy as shown in these works, these goals are 78 achieved in unspecified numbers of total communication rounds from works based on RL approaches 79 such as Mostafa [2019] and Guo et al. [2022] 80

The above observations justify exploring our problem differently from previous approaches. Our 81 method exploits full knowledge of the training process, and it does not require sufficient trials 82 at potential expense of communication budget. Inspired by the hypergradient descent techniques 83 developed by Baydin et al. [2017] and Amid et al. [2022] for centralized optimization learning rate, 84 we develop FATHOM by directing deriving analytical gradients with respect to the hyperparameters 85 of interest. The result is a sample efficient method which offers both improvements in communication 86 efficiency and reduced local computation in a single-shot online optimization procedure. Meanwhile, 87 FATHOM is not as flexibly applicable in optimizing a wide range of hyperparameters, since each 88

⁸⁹ gradient needs to be derived separately to take advantage of our full knowledge of the training process.

⁹⁰ We believe this approach is a performance advantage, at the expense of its flexibility.

⁹¹ There are other notable relevant works. Charles and Konečný [2020] and Li et al. [2019] proved that

92 reducing the client learning rate during training is necessary to reach the true objective. Yet, a line of 93 interesting works, such as Dai et al. [2020] and Holly et al. [2021]) applies Bayesian Optimization

interesting works, such as Dai et al. [2020] and Holly et al. [2021]) applies Bayesian Optimization
 (BO) on federated hyperparamter tuning, by treating it as a closed-box optimization problem. Dai

et al. [2021] further updates their use of BO in FL by incorporating differential privacy. However,

these BO-based works do not consider adaptive hyperparameters. Yet, another work (Wang and Joshi

97 [2018]) shares similarity to our approach of optimally adapting the number of local steps, with their

⁹⁸ adaptive communication strategy, AdaComm, in the distributed setting. However, their main interest

⁹⁹ is reducing wall-clock time. Lastly, around the same time of this writing, Wang et al. [2022] publishes

their benchmark suite for FL HPO, called FedHPO-B, which would be valuable to our future work.

101 **3 Methodology**

In this section we formalize the problem of hyperparameter optimization (HPO) for FL. We first review FedAvg, a de facto standard of federated optimization methods for research baseline and practice. Then, we present our method for online-tuning of its hyperparameters, specifically client learning rate, number of local steps, and batch size. We call our method FATHOM (Federated AuTomatic Hyperparameter OptiMization).

107 3.1 Problem Definition

¹⁰⁸ In this paper, we consider the empirical risk minimization (ERM) across all the client data, as an ¹⁰⁹ unconstrained optimization problem:

$$f^* := \min_{x \in \mathbb{R}^d} \left[f(x) := \frac{1}{m} \sum_{i=1}^m f_i(x) \right]$$
(1)

where $f_i : \mathbb{R}^d \to \mathbb{R}$ is the loss function for data stored in local client index *i* with *d* being the dimension of the parameters *x*, *m* is number of clients, and $f^* = f(x_*)$ where x_* is a stationary solution to the ERM problem in eq(1).

To facilitate some of the discussions that follow, it helps to define assumptions here as we do throughout the rest of this paper:

Assumption 1. (Unbiased Local Gradient Estimator) Let $g_i(x)$ be the unbiased, local gradient estimator of $\nabla f_i(x)$, i.e., $\mathbb{E}[g_i(x)] = \nabla f_i(x)$, $\forall x$, and $i \in [m]$.

117 3.2 Federated Optimization and Tuning of Hyperparameters

Federated Averaging (FedAvg) We describe the operations of FedAvg from McMahan et al. 118 [2016], as follows. At any round t, each of the m clients takes a total of K_i local SGD steps, where 119 $\overline{K_i} = |E\nu_i/B|$, and where ν_i is the number of data samples from client index i, B is batch size, 120 with epoch number E = 1 being a common baseline. In this version of FedAvg, heterogeneous data 121 size is accommodated across clients, and the number of local steps can be manipulated via E and 122 B as hyperparameters. Each local SGD step updates the local model parameters of each client i as 123 follows: $x_{t,k+1}^{i} = x_{t,k}^{i} - \eta_L g_i(x_{t,k}^{i})$, where η_L is the local learning rate and $k \in [K]$ is the local step 124 index. To conclude each round, these clients return the local parameters x_{t,K_i}^i to the server where 125 it updates its global model, with $x_{t+1} = \sum_i \nu_i x_{t,K}^i / \nu$ where $\nu = \sum_i \nu_i$. To facilitate some of the discussions that follow, we define the following quantities: 126 127

$$\overline{\Delta}_t \triangleq x_{t+1} - x_t = \sum_{i=1}^m \frac{\nu_i}{\nu} \Delta_t^i \quad \text{where} \quad \Delta_t^i \triangleq -\sum_{k=0}^{K_i - 1} \eta_{L,t} g_i(x_t^{i,k}) \tag{2}$$

Offline Hyperparameter Tuning Offline tuning is best to be summarized as follows. We first define $U = \{u \in \mathbb{R} \mid u \ge 0\}$ with $\eta_L \in U$, and $V = \{v \in \mathcal{I} \mid v \ge 1\}$ with $K \in V$. We also define $C = U \times V$, and $c = (\eta_L, K)$, where $c \in C$. Offline tuning would have the following objective:

 $\min_{c \in C} f_{\text{valid}}(x, c)$ s.t. $x = \operatorname{argmin}_{z \in \mathbb{R}^d} f_{\text{train}}(z, c)$. With abuse of notation, we use f_{valid} for the 131 objective function calculated from a validation dataset which is usually held-out before the procedure, 132 and f_{train} for the objective from training data which usually is just local client data. A few notable 133 offline tuning methods are as follows. Global grid-search from Holly et al. [2021] is an example 134 of offline tuning that iterates over the entire search grid defined as C, completing an optimization 135 process for each grid point and evaluating the result with a held-out validation set. Global Bayesian 136 Optimization from Holly et al. [2021] is another similar example of offline tuning that follows the 137 same template and objective. Instead of brute-force grid-search, c is sampled from a distribution \mathcal{D}_C 138 over C, i.e. $c \sim \mathcal{D}_C$, that updates after every iteration. 139

Online Hyperparameter Optimization We are interested in an online procedure that combines
 hyperparameter optimization and model parameter optimization, with the following objective:

$$\min_{\substack{x \in \mathbb{R}^d \\ c \in C}} f_{\text{train}}(x, c) \tag{3}$$

This formulation is the objective of our method, FATHOM, which we will discuss shortly in detail. It has the advantage of joint optimization in a one-shot procedure. Furthermore, it does not assume the availability of a validation dataset.

145 3.3 Our Method: FATHOM

In this section we will introduce our method, FATHOM (Federated AuTomatic Hyperparameter 146 OptiMization). Recall from our joint objective, eq(3), that both the model parameters, x, and 147 hyperparameters of the optimization algorithm, c, are optimized jointly to minimize our objective 148 function. An alternative view is to treat c as part of the parameters being optimized in a classic 149 formulation, i.e. $min_{y}f(y)$ with y = (x, c). As previously mentioned, our method is inspired by 150 hypergradient descent from Baydin et al. [2017] and by exponentiated gradient from Amid et al. 151 [2022], both proposed for centralized learning rate optimization. We will present how FATHOM 152 exploits our knowledge of analytical gradients to update client learning rate, number of local steps, as 153 well as batch size, for an online, one-shot optimization procedure. 154

Assumption 2. (Convexity w.r.t. η_L and K) We assume $\mathbb{E}_t(f(x_t))$ is convex w.r.t. η_L and K, even though we assume non-convexity w.r.t. x_t). Specifically, convexity w.r.t. K follows the definition in [157] Murota [[1998]], to accommodate the integer space where K is defined.

158 **Remark 1.** Assumption 2 is necessary to guarantee the existence of subgradients derived in Theorems

159 T and 2, and it will be assumed for this work. In problems dealing with deep neural networks, it is

reasonable to not assume convexity w.r.t. hyperparameters. However, from our empirical results, we

claim that the proposed algorithm is still able to operate as desired under this condition.

162 3.3.1 Hypergradient for Client Learning Rate

In this section, we derive the hypergradient for client learning rate in a similar fashion as Baydin et al. [2017], with the difference being that they are mainly concerned with the centralized optimization problem, and that we are concerned with the distributed setting where clients take local steps. We derive the following hypergradient of the objective function as defined in eq(1), taken with respect to the learning rate $\eta_{L,t-1}$ such that it can be updated to obtain $\eta_{L,t}$:

$$H_t = \frac{\partial f(x_t)}{\partial \eta_{L,t-1}} = \frac{\partial f(x_t)}{\partial x_t} \cdot \frac{\partial (x_{t-1} + \overline{\Delta}_{t-1})}{\partial \eta_{L,t-1}} = \nabla f(x_t) \cdot \frac{\partial \overline{\Delta}_{t-1}}{\partial \eta_{L,t-1}}$$
(4)

where $\overline{\Delta}_t$ is the update step for the global parameters x_t as defined in eq(2), leading to $\frac{\partial \overline{\Delta}_t}{\partial \eta_{L,t}} = \frac{\overline{\Delta}_t}{\eta_{L,t}} = -\sum_{i=1}^m \frac{\nu_i}{\nu} \sum_{k=0}^{K-1} g_i(x_t^{i,k})$. We also make the approximation $x_{t+1} - x_t = \overline{\Delta}_t \approx -\eta_{L,t} \nabla f(x_t)$. We can then write the normalized update, \overline{H}_t , similar to Amid et al. [2022], as follows:

$$\overline{H}_{t} = \frac{\nabla f(x_{t})}{\|\nabla f(x_{t})\|} \cdot \left(\frac{\partial \overline{\Delta}_{t-1}}{\partial \eta_{L,t-1}} \middle/ \left\| \frac{\partial \overline{\Delta}_{t-1}}{\partial \eta_{L,t-1}} \right\| \right) \approx -\frac{\overline{\Delta}_{t}}{\|\overline{\Delta}_{t}\|} \cdot \frac{\overline{\Delta}_{t-1}}{\|\overline{\Delta}_{t-1}\|}$$
(5)

The resulting hypergradient is a scalar, as expected, and can be used efficiently as part of the update rule for η_L , which we will see in Section 3.3.4 The implementation is communication efficient, since in each round, each client needs one extra scalar to send back to the server, and likewise the server needs to broadcast one extra scalar back to the clients. It is also computationally efficient since it avoids calculating the full local gradient $\nabla f(x_t)$.

176 3.3.2 Hypergradient for Number of Local Steps

Since the number of local steps is an integer, i.e. $K = \{k \in \mathbb{I} \mid k \ge 1\}$, this means $f(x_t)$ does not exist for non-integer values of K. We formulate a subgradient as a surrogate of the hypergradient $\partial f(x_t)/\partial K$, as follows. We will call this a hyper-subgradient.

Theorem 1. When a piecewise function L_t is defined for every value of $K_0 \in [K]$ on l, such that $0.0 \leq l < 1.0$, we claim, under Assumption 2 that the following is a subgradient of $f(x_t)$ at $K_t = K_0$:

$$\frac{\partial L_t}{\partial l} = \nabla f(x_t) \cdot \left(-\eta_{L,t} \sum_{i=1}^m g_i(x_{t-1}^{i,K_t-1}) \frac{\nu_i}{\nu} \right) \tag{6}$$

where *l* represents the marginal fraction of local steps beyond K_0 . We leave the proof (with an illustration in Figure 2) in the Appendix section beginning in eq(20).

The result from Theorem I is not sufficiently communication-efficient for implementing an update rule for K. This is because it would require the quantity $g_i(x_{t-1}^{i,K_t-1})$ to be communicated from each client *i* to the server. To save communication, let us reuse what the server has in memory: $\overline{\Delta}_t = \left(-\eta_L \sum_{i=1}^m \frac{\nu_i}{\nu} \sum_{k=0}^{K_t-1} g_i(x_t^{i,k})\right)$. If we let:

$$S_t = \nabla f(x_t) \cdot \left(-\eta_{L,t} \sum_{i=1}^m \frac{\nu_i}{\nu} \sum_{k=0}^{K_t - 1} g_i(x_{t-1}^{i,k}) \right) l$$
(7)

$$N_t = \frac{\partial S_t}{\partial l} = \nabla f(x_t) \cdot \left(-\eta_{L,t} \sum_{i=1}^m \frac{\nu_i}{\nu} \sum_{k=0}^{K_t-1} g_i(x_{t-1}^{i,k}) \right) = \nabla f(x_t) \cdot \overline{\Delta}_{t-1}$$
(8)

$$\overline{N}_{t} = \frac{\nabla f(x_{t})}{\|\nabla f(x_{t})\|} \cdot \frac{\overline{\Delta}_{t-1}}{\|\overline{\Delta}_{t-1}\|} \approx -\frac{\overline{\Delta}_{t}}{\|\overline{\Delta}_{t}\|} \cdot \frac{\overline{\Delta}_{t-1}}{\|\overline{\Delta}_{t-1}\|}$$
(9)

where eq(9) is the normalized update as in <u>Amid et al.</u> [2022]. We claim that eq(8) is a positivelybiased version of eq(6), which has its practical importance due to the fact that the last term in eq(6) from Theorem [] results in zero-mean, noisy gradients, when the local functions are nearing their local solutions, when in fact, this is the area where more local work is not needed. Thus, a positive bias is desirable to drive the number of local steps down. This result is also useful from a communication efficiency perspective in its implementation, because the server has all the components to calculate this quantity, and would not require additional communication.

196 3.3.3 Regularization for Number of Local Steps

One of the goals for FATHOM is savings in local computation. To avoid excessive number of local steps, we further develop a regularization term for local computation against excessive K, which is a proxy for the hypergradient of the local client functions at the end of each round : $\partial f_i(x_t^{i,K})/\partial K$.

Theorem 2. When a piecewise function J_t is defined for every value of $K_0 \in [K]$ on l, such that $0.0 \le l < 1.0$, we claim, under Assumption 2 that the following is a subgradient of $\sum_{i=1}^{m} f_i(x_t^{i,K_t})$ $t_t = K_0$:

$$\frac{\partial J_t}{\partial l} = -\eta_{L,t} \sum_{i=1}^m \frac{\nu_i}{\nu} \mathbb{E} \Big[g_i(x_t^{i,K_0-1}) \Big] \cdot g_i(x_t^{i,K_t}) \approx -\eta_{L,t} \sum_{i=1}^m \frac{\nu_i}{\nu} \sum_{k=0}^{K_t-1} g_i(x_t^{i,k}) \cdot g_i(x_t^{i,K_t})$$
(10)

where *l* represents the marginal fraction of local steps beyond K_0 . We leave the proof in the Appendix section beginning in eq(24).

In our algorithm, we use the normalized update based on the following biased proxy, since eq(10) tends to be noisy from $g_i(x_t^{i,K_t})$.

$$G_t = -\eta_{L,t} \sum_{i=1}^m \frac{\nu_i}{\nu} \min_{K \le K_t} \left(\sum_{k=0}^{K-1} g_i(x_t^{i,k}) \cdot g_i(x_t^{i,K}) \right)$$
(11)

$$\overline{G}_{t} = -\eta_{L,t} \sum_{i=1}^{m} \frac{\nu_{i}}{\nu} \min_{K \le K_{t}} \left(\frac{\sum_{k=0}^{K-1} g_{i}(x_{t}^{i,k})}{\left\| \sum_{k=0}^{K-1} g_{i}(x_{t}^{i,k}) \right\|} \cdot \frac{g_{i}(x_{t}^{i,K})}{\left\| g_{i}(x_{t}^{i,K}) \right\|} \right)$$
(12)

where \overline{G}_t is the normalized update. The proxy yields a bias towards smaller number of local steps, which is desirable for reducing local computation. We use this biased proxy against using a more typical regularization such as L2 for the number of local steps, based on initial empirical results for better performance..

211 3.3.4 Normalized Exponentiated Gradient Updates

For the update rules of the hyperparameters η_L (client learning rate) and K (number of client local steps), we use the normalized exponentiated gradient descent method (EGN) with no momentum, rather than a conventional linear update method such as the additive update of hypergradient descent proposed in Baydin et al. [2017]. It is reasonable to use exponentiated gradient (EG) methods for updates of hyperparameters that are strictly positive in value. EG methods also enjoy significantly faster convergence properties when only a small subset of the dimensions are relevant, according to Amid et al. [2022].

EG methods have been proposed in previous works for a variety of applications (Khodak et al. [2021], 219 Amid et al. [2022], Li et al. [2020]), and analyzed in depth (Ghai et al. [2019]), where its convergence 220 has been studied and validated (Li and Cevher [2018]). Recently, Amid et al. [2022] showed that EGN 221 is the same as the multiplicative update for hypergradient descent proposed in Baydin et al. [2017]. 222 when the approximation $exp(\cdot) \approx 1 + \cdot$ is made. From our observations, we believe that momentum 223 is not needed for the effectiveness of EGN in our application, as validated in our numerical results. 224 We also opted-out of adding further complexity such as extra weights and activation functions to 225 model the relationships between $\eta_{L,t}$ and K_t , because it would require more samples to optimize and 226 because FATHOM is a one-shot procedure. Furthermore, due to the non-stationary nature of these 227 values, we opt for a simpler scheme for faster performance. 228

Hence, for the update rule of client learning rate, η_L , we have:

$$\eta_{L,t+1} = \eta_{L,t} \exp\left(-\gamma_{\eta} H_t\right) \tag{13}$$

where \overline{H}_t is as defined in eq(5). For number of local steps, we observe that it is related to batch size in round t, B_t , as follows. To accommodate heterogeneity of local dataset sizes among clients, we have number of local data samples from client i to be ν_i . The number of local steps for client iis $K_i = \lfloor \nu_i E_t / B_t \rfloor$, where E_t is number of epochs, with $E_t = 1$ meaning the entire local dataset for each client to be processed once per round. We derive update rules for E_t and B_t globally to optimize the number of local steps, without having to make any changes to our theoretical analysis to accommodate the heterogeneity of local dataset sizes:

$$E_{t+1} = E_t \exp\left(-\gamma_E \left(\overline{N}_t + \overline{G}_t\right)\right) \tag{14}$$

237 and

$$B_{t+1} = B_t \exp\left(-\gamma_B\left(-\overline{G}_t\right)\right) \tag{15}$$

where N_t and G_t are defined in eq(9) and eq(12), respectively. These update rules accomplish the goal of updating the number of local steps via E_t/B_t with $\frac{E_{t+1}}{B_{t+1}} = \frac{E_t}{B_t} \exp\left(-\gamma_E \overline{N}_t - (\gamma_E - \gamma_B)\overline{G}_t\right)$. Typically, with $\gamma_B \ge \gamma_E$, $(\gamma_B - \gamma_E)\overline{G}_t$ becomes a tunable regularization term as discussed at the end of Section 3.3.3

242 3.3.5 Client Sampling

We present our method, FATHOM, as shown in Algorithm [] One practical factor we have not considered in our discussions is partial client sampling. For our implementation to handle the stochastic nature of client sampling, the metric $\overline{\Delta}_{t-1}$ for calculating \overline{H}_t in eq(5) and \overline{N}_t in eq(9) is modified by a smoothing function for noise filtering, i.e. $\overline{\Delta}_{t,sm} = \alpha \overline{\Delta}_{t-1,sm} + (1-\alpha)\overline{\Delta}_t$, which is a single-pole infinite impulse response filter (Oppenheim and Schafer [2009]Oppenheimer et al. [2009]) with no bias compensation. We use the notation "sm" for smoothed, and after many experiments, we decide to use $\alpha = 0.5$ for all of our numerical results.

Algorithm 1: FATHOM : $g_i(x)$ is defined in Assumptions 1, and m is the number of clients. **Input:** Server initializes global model $x_{t=1}$, T as the end communication round, and: $\overline{\Delta}_{t=0,sm}=0$; $\alpha=0.5$; $\gamma_{\eta}=0.01$; $\gamma_{E}=0.01$; $\gamma_{B}=0.1$ **Output:** x_T , as well as $\eta_{L,t}$, E_t and B_t for all $t \in [T]$ for t = 1, ..., T do Sample client set S_t out of m clients. For each client $i \in S_t$, initialize: $x_t^{i,k=0} = x_t$ and $K_{t,i} = \lfloor \nu_i E_t / B_t \rfloor$. Set $\Delta_i = 0$, and $\phi_i = +\infty$. for $k = 0, ..., K_{t,i} - 1$ do For each client *i*, compute in parallel an unbiased stochastic gradient $g_i(x_t^{i,k})$. For each client *i*, calculate $\phi_i = \min(\phi_i, g_i(x_t^{i,k}) \cdot \Delta_i)$ where $\Delta_i = x_t^{i,k} - x_t$ For each client *i*, update in parallel its local solution: $x_t^{i,k+1} = x_t^{i,k} - \eta_{L,t}g_i(x_t^{i,k})$ 250 end Server calcualtes $\nu = \sum_{i \in S_t} \nu_i$, where ν_i is the size of client *i* dataset. Server calculates $\overline{\Delta}_t = \sum_{i \in S_t} \Delta_i(\nu_i/\nu)$; see eq(2) Server calculates $\Delta_t - \sum_{i \in S_t} -i \sqrt{i}$, Server updates global model $x_{t+1} = x_t - \overline{\Delta}_t$ Server calculates $\overline{H}_t = \overline{N}_t = -\frac{\overline{\Delta}_t}{\|\overline{\Delta}_t\|} \cdot \frac{\overline{\Delta}_{t-1,sm}}{\|\overline{\Delta}_{t-1,sm}\|}$, modified from eq(5) and eq(9) Server calculates \overline{G}_t ; see eq(12) Server updates client learning rate $\eta_{L,t+1}$, epochs, E_{t+1} , and batch size B_{t+1} for the next round; see eq(13), eq(14), and eq(15). Server updates $\overline{\Delta}_{t,sm} = (1 - \alpha)\overline{\Delta}_t + \alpha\overline{\Delta}_{t-1,sm}$ for the next round end

4 Theoretical Convergence

A standard approach to theoretical analysis of an online optimization method such as ours, is through 252 analyzing the regret bound (Zinkevich [2003], Khodak et al. [2019], Kingma and Ba [2014], and 253 Mokhtari et al. [2016]). Nonetheless, this approach does not tell us the impact on communication 254 efficiency by the online updates introduced from FATHOM. Therefore, we take an alternative 255 approach by extending the guarantees of FedAvg performance (Wang et al. [2021], Reddi et al. 256 [2020], Gorbunov et al. [2020], Yang et al. [2021], Li et al. [2019], etc) to include both adaptive 257 learning rate and adaptive number of local steps. We assume the special case in our analysis to have 258 full client participation. We prove that adaptive learning rate and adaptive number of local steps does 259 not impact asymptotic convergence, despite the given relaxed conditions. 260

261 4.1 Assumptions

Assumption 3. (L-Lipschitz Continuous Gradient for Parameters x_t) There exists a constant L > 0, such that $\|\nabla f_i(x) - \nabla f_i(y)\| \le L \|x - y\|$, $\forall x, y \in \mathbb{R}^d$, and $i \in [m]$, where x and y are the parameters in eq(1)

Assumption 4. (Bounded Local Variance) There exist a constant $\sigma_L > 0$, such that the variance of each local gradient estimator is bounded by $\mathbb{E} \|\nabla f_i(x) - g_i(x)\|^2 \le \sigma_L^2$, $\forall x$, and $i \in [m]$.

Assumption 5. (Bounded Second Moment) There exists a constant G > 0, such that $\mathbb{E}_t \|\nabla f_i(x_t)\| \le G$, $i \in [m]$, $\forall x_t$.

269 4.2 Convergence Results

Theorem 3. Under Assumptions \overline{I} and with full client participation, when FATHOM as shown in Algorithm \overline{I} is used to find a solution x_* to the unconstrained problem defined in $eq(\overline{I})$, the sequence of outputs $\{x_t\}$ satisfies the following upper-bound, where, with slight abuse of notation, $\mathcal{E} = \min_{t \in [T]} \mathbb{E}_t \|\nabla f(x_t)\|_2^2$:

$$\mathcal{E}_{fathom} = \mathcal{O}\left(\sqrt{\frac{\sigma_L^2 + G^2}{m\overline{K}T}} + \sqrt[3]{\frac{\sigma_L^2}{\overline{K}T^2}} + \sqrt[3]{\frac{G^2}{T^2}}\right)$$
(16)

with the following conditions: $\overline{\eta}_L = \min\left(\sqrt{\frac{2\beta_0 mD}{\beta_1 \overline{K} LT(\sigma_L^2 + G^2)}}, \sqrt[3]{\frac{\beta_0 D}{2.5\beta_2 \overline{K}^2 L^2 \sigma_L^2 T}}, \sqrt[3]{\frac{\beta_0 D}{2.5\beta_3 \overline{K}^3 L^2 G^2 T}}\right)$ and $\eta_{L,t} \leq 1/L$ for all t, where

$$\overline{\eta}_L \triangleq \frac{1}{T} \sum_{t=1}^T \eta_{L,t} \quad and \quad \overline{K} \triangleq \frac{1}{T} \sum_{t=1}^T K_t$$
(17)

276 and where

$$\beta_{0} = \frac{\sum_{t} \eta_{L,t} K_{t}}{T[\frac{1}{T} \sum_{t} \eta_{L,t}][\frac{1}{T} \sum_{t} K_{t}]} , \quad \beta_{1} = \frac{\sum_{t} \eta_{L,t} K_{t}[\frac{1}{T} \sum_{t} \eta_{L,t}]}{\sum_{t} \eta_{L,t}^{2} K_{t}}$$
(18)

$$\beta_{2} = \frac{\sum_{t} \eta_{L,t} K_{t} \left[\frac{1}{T} \sum_{t} \eta_{L,t}\right]^{2} \left[\frac{1}{T} \sum_{t} K_{t}\right]}{\sum_{t} \eta_{L,t}^{3} K_{t}^{2}} , \quad \beta_{3} = \frac{\sum_{t} \eta_{L,t} K_{t} \left[\frac{1}{T} \sum_{t} \eta_{L,t}\right]^{2} \left[\frac{1}{T} \sum_{t} K_{t}\right]^{2}}{\sum_{t} \eta_{L,t}^{3} K_{t}^{3}} \quad (19)$$

277 We leave the proof in the Appendix beginning in eq(29).

The values of β_0 , β_1 , β_2 , β_3 , and β_4 are dependent on the relative changes over the adaptive process of these components, according to Chebyshev's Sum Inequalities (Hardy et al. [1988]). A special case is when these quantities equal to 1 when both $\eta_{L,t}$ and K_t are constant, which recovers the standard upperbound for FedAvg from eq(16).

Remark 2. The definitions in eq(17) combined with the conditions for $\overline{\eta}_L$ above is called the relaxed 282 conditions in this paper for the hyperparameters $\eta_{L,t}$ and K_t . The values of $\eta_{L,t}$ and K_t are adaptive 283 during the optimization process between rounds t = 1 and t = T, as long as the above conditions are 284 satisfied for the guarantee in eq(37) to hold. This relaxation presents opportunities for a scheme such 285 as FATHOM to exploit for performance gain. For example, suppose T approaches ∞ for a prolonged 286 training session. Then $\overline{\eta}_L$ would necessarily be sufficiently small for \mathcal{E}_{fathom} to be bounded by 287 $eq(\overline{16})$. However, for early rounds i.e. small t values, $\eta_{L,t} \leq T\overline{\eta}_L$ can be reasonably large and still 288 can satisfy eq(17), for the benefit of accelerated learning and convergence progress early on. Similar 289 strategy can be used for number of local steps to minimize local computations towards later rounds. 290 In any case, these strategies are mere guidelines meant to remain within the worst case guarantee. 291 However, Theorem 3 offers the flexibility otherwise not available. We will now show the empirical 292 performance gained by taking advantage of this flexibility. 293



Figure 1: Test Accuracy Performance with various values of initial client learning rate (LR_0), initial batch size (BatchSize_0), and number of clients per round (NumClients). Top row: FSO sims. Bottom row: FEMNIST sims. Baseline values for FEMNIST: LR_0=0.1, BatchSize_0=20, NumClients=10. Baseline values for FSO: LR_0=0.32, BatchSize_0=16, NumClients=50.

²⁹⁴ 5 Empirical Evaluation and Numerical Results

We present an empirical evaluation of FATHOM proposed in Section 3 and outlined in Algorithm 295 **1**. We conduct extensive simulations of federated learning in character recognition on the federated 296 EMNIST-62 dataset (FEMNIST) (Cohen et al. [2017]) with a CNN, and in natural language next-word 297 prediction on the federated Stack Overflow dataset (FSO) (TensorFlow-Federated-Authors [2019]) 298 with a RNN. We defer most of the details of the experiment setup in Appendix Section C.1. Our 299 choice of datasets, tasks and models, are exactly the same as the "EMNIST CR" task and the "SO 300 NWP" task from Reddi et al. [2020]. See Figure 1 and Table 1 and their captions for details of the 301 experiment results. Our evaluation lacks comparison with a few one-shot FL HPO methods discussed 302 earlier in the paper because of a lack of standardized benchmark (until FedHPO- B Wang et al.) [2022] 303 was published concurrently as this work) to be fair and comprehensive. 304

The underlying principle behind these experiments is evaluating the robustness of FATHOM versus 305 FedAvg under various initial settings, to mirror realistic usage scenarios where the optimal hyperpa-306 rameter values are unknown. For FATHOM, we start with the same initial hyperparameter values 307 as FedAvg. The test accuracy progress with respect to communication rounds is shown in Figure 1308 from these experiments. We also pick test accuracy targets for the two tasks. For FEMNIST CR we 309 use 86% and for FSO NWP we use 23%. Table \square shows a table of resource utilization metrics with 310 respect to reaching these targets in our experiments, highlighting the communication efficiency as 311 well as reduction in local computation from FATHOM in comparison to FedAvg. To our knowledge, 312 we are the first to show gain from an online HPO procedure over a well-tuned equivalent procedure 313 with fixed hyperparameter values. 314

The federated learning simulation framework on which we build our algorithms for our experiments

is FedJAX (Ro et al. [2021]) which is under the Apache License. The server that runs the experiments

is equipped with Nvidia Tesla V100 SXM2 GPUs.

Table 1: Resource utilization in communication and local computation to reach specified test accuracy target for each task. All evalutions are run for ten trials. Bold numbers highlight better performance. NA means target was not reached within 1500 rounds for FSO NWP and 2000 rounds for FEMNIST CR, in any of our trials. LR_0 is initial client learning rate, BS_0 is initial batch size, and NCPR is number of clients per round. All experiments use baseline initial values except where indicated. For clarification, M is used in place for "million", and K for "thousand". Baseline_fso : (LR_0 = 0.32, BS_0 = 16, NCPR = 50)

Baseline femnist :	(LR	0 = 0.10.	BS	0 = 20	. NCPR	= 10
	\	/				- /

		Number of	f Rounds To	Local Gradients Calculated To		
Tasks	Experiments	Reach Target	Test Accuracy	Reach Target Test Accuracy		
		FATHOM	FedAvg	FATHOM	FedAvg	
	Baseline_fso	562 ± 12	971 ± 11	$85M \pm 1.2M$	$124M \pm 1.3M$	
FSO NWP Target@23%	$LR_0 = 0.05$	871 ± 7	NA	$138M \pm 3.2M$	NA	
	$BS_0 = 4$	758 ± 43	$\textbf{580} \pm \textbf{18}$	$93M \pm 2.8M$	$74M \pm 2.5M$	
	$BS_0 = 256$	801 ± 28	NA	$174M \pm 18M$	NA	
	NCPR = 25	$\textbf{970} \pm \textbf{49}$	1283 ± 33	$63M \pm 2.7M$	$82M \pm 3.8M$	
	NCPR = 200	$\textbf{396} \pm \textbf{17}$	684 ± 26	$\mathbf{280M} \pm \mathbf{45M}$	$350M\pm13M$	
FEMNIST CR Target@86%	Baseline_femnist	$\textbf{739} \pm \textbf{24}$	1098 ± 15	$1.5M \pm 36K$	$2.2M \pm 64K$	
	$LR_0 = 0.05$	$\textbf{905} \pm \textbf{21}$	1574 ± 19	$1.7\mathrm{M}\pm28\mathrm{K}$	$3.1M \pm 28K$	
	$BS_0 = 4$	$\textbf{708} \pm \textbf{17}$	885 ± 41	$1.2M \pm 28K$	$1.7\mathrm{M}\pm88\mathrm{K}$	
	$BS_0 = 256$	736 ± 20	NA	$2.0M \pm 44K$	NA	
-	NCPR = 100	$\textbf{777} \pm \textbf{16}$	1436 ± 18	$\mathbf{22M} \pm \mathbf{0.27M}$	$28M \pm 0.39K$	
	NCPR = 200	$\textbf{790} \pm \textbf{16}$	1481 ± 33	$57M \pm 1.0M$	$59M \pm 1.3M$	

6 Conclusion and Future Work

In this work, we propose FATHOM for adaptive hyperparameters in federated optimization, specifically for FedAvg. We analyze theoretically and evaluate empirically its potential benefits in convergence behavior as measured in test accuracy, and in reduction of local computations, by automatically adapting the three main hyperparameters of FedAvg: client learning rate, and number of local steps via epochs and batch size. An example of future efforts to extend this work is using a standardized benchmark such as Wang et al. [2022] for performance comparison against other FL HPO methods.

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401 Checklist

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- The checklist follows the references. Please read the checklist guidelines carefully for information on how to answer these questions. For each question, change the default **[TODO]** to **[Yes]**, **[No]**, or [N/A]. You are strongly encouraged to include a **justification to your answer**, either by referencing the appropriate section of your paper or providing a brief inline description. For example:
 - Did you include the license to the code and datasets? [Yes] The code is MIT licensed.
- Please do not modify the questions and only use the provided macros for your answers. Note that the
 Checklist section does not count towards the page limit. In your paper, please delete this instructions
 block and only keep the Checklist section heading above along with the questions/answers below.
- 410 1. For all authors...
 - (a) Do the main claims made in the abstract and introduction accurately reflect the paper's contributions and scope? [Yes]
 - (b) Did you describe the limitations of your work? [Yes] Please refer to Sections 2 and 6
- (c) Did you discuss any potential negative societal impacts of your work? [No] Not
 specifically, but it is alluded to how FL applications have social implications in the
 introductory section.
- (d) Have you read the ethics review guidelines and ensured that your paper conforms to
 them? [Yes]

419	2. If you are including theoretical results
420	(a) Did you state the full set of assumptions of all theoretical results? [Yes] Please refer to
421	Assumptions 1, 2, 3, 4, and 5
422	(b) Did you include complete proofs of all theoretical results? [Yes] Yes, in the supple-
423	mental material.
424	3. If you ran experiments
425	(a) Did you include the code, data, and instructions needed to reproduce the main exper-
426	imental results (either in the supplemental material or as a URL)? [Yes] Yes, in the
427	supplemental material.
428	(b) Did you specify all the training details (e.g., data splits, hyperparameters, how they
429	were chosen)? [Yes] Yes, in the supplemental material.
430	(c) Did you report error bars (e.g., with respect to the random seed after running experi-
431	ments multiple times)? [Yes] Yes, see Table 1
432	(d) Did you include the total amount of compute and the type of resources used (e.g., type
433	of GPUs, internal cluster, or cloud provider)? [Yes] Yes, it is mentioned in Section 5
434	4. If you are using existing assets (e.g., code, data, models) or curating/releasing new assets
435	(a) If your work uses existing assets, did you cite the creators? [Yes] Yes, it is mentioned
436	in Section 5
437	(b) Did you mention the license of the assets? [Yes] Yes, it is mentioned in Section 5
438	(c) Did you include any new assets either in the supplemental material or as a URL? [Yes]
439	Yes, in the supplemental material.
440	(d) Did you discuss whether and how consent was obtained from people whose data you're
441	using/curating? [N/A]
442	(e) Did you discuss whether the data you are using/curating contains personally identifiable
443	information or offensive content? [No]
444	5. If you used crowdsourcing or conducted research with human subjects
445	(a) Did you include the full text of instructions given to participants and screenshots, if
446	applicable? [N/A]
447	(b) Did you describe any potential participant risks, with links to Institutional Review
448	Board (IRB) approvals, if applicable? [N/A]
449	(c) Did you include the estimated hourly wage paid to participants and the total amount
450	spent on participant compensation? [N/A]