
Why Are Conditional Generative Models Better Than Unconditional Ones?

Anonymous Author(s)

Affiliation

Address

email

Abstract

1 Extensive empirical evidence demonstrates that conditional generative models
2 are easier to train and perform better than unconditional ones by exploiting the
3 labels of data. So do score-based diffusion models. In this paper, we analyze the
4 phenomenon formally and identify that the key of conditional learning is to partition
5 the data properly. Inspired by the analyses, we propose *self-conditioned diffusion*
6 *models* (SCDM), which is trained conditioned on indices clustered by the k -means
7 algorithm on the features extracted by a model pre-trained in a self-supervised
8 manner. SCDM significantly improves the unconditional model across various
9 datasets and achieves a record-breaking FID of 3.94 on ImageNet 64x64 without
10 labels. Besides, SCDM achieves a slightly better FID than the corresponding
11 conditional model on CIFAR10.

12 1 Introduction

13 Extensive empirical evidence in prior work [14, 3, 9] demonstrates that conditional generative models
14 are easier to train and perform better than unconditional ones by exploiting the labels of data. So
15 do score-based diffusion models (DM). For instance, the representative work [9] achieves a FID of
16 10.94 when trained conditionally and a FID of 26.21 when trained unconditionally on ImageNet of
17 size 256x256.

18 Intuitively, the gap exists because (1) the marginal distribution induced by a conditional model is more
19 expressive than the corresponding unconditional model; and (2) the data distribution conditioned on a
20 specific class has fewer modes and is easier to fit than the original data distribution.

21 In this paper, we formalize the above intuition in an ideal setting where we have infinite data. It is easy
22 to show that the marginal distribution induced by a conditional model can be viewed as a mixture of
23 the corresponding unconditional models. Further, we derive a sufficient condition for the superiority
24 of the conditional model, which suggests that the conditional model gains more as the conditional
25 data distribution gets simpler. The analyses explain previous empirical findings: conditioning on
26 class labels probably partitions the data into simpler groups according to the semantics of data.

27 Notably, our analyses apply to all possible conditions, not limited to class labels. Then, a very natural
28 idea is to find a certain way to obtain meaningful conditions in an unsupervised manner and boost the
29 unconditional generation results. The recent advances in self-supervised learning [10, 5] show that
30 one can learn predictive representations without labels, which serve as an ideal tool for obtaining
31 meaningful conditions. Specifically, we simply run a clustering algorithm (e.g., k -means) on the
32 features extracted by a model pre-trained in a self-supervised manner (on the same dataset) and use
33 the cluster indices as conditions to train a conditional model.

34 Although our analyses and the self-conditional approach is applicable to all types of deep generative
35 models, we focus on score-based diffusion models in our experiments to explore the boundary of

36 unsupervised generative modeling. Therefore, we refer to our approach as *self-conditioned diffusion*
 37 *models* (SCDM). We systematically evaluate SCDM on several widely adopted datasets. In all
 38 settings, SCDM significantly improves the unconditional model. Notably, SCDM achieves a record-
 39 breaking FID of 3.94 on ImageNet 64x64 without labels. Besides, SCDM achieves a slightly better
 40 FID than the corresponding conditional model on CIFAR10.

41 2 Why Are Conditional Generative Models Better Than Unconditional Ones

42 In this section, we present the problem formulation and our analyses.

43 2.1 Problem Formulation

44 Let $q(\mathbf{x}, c)$ be the joint distribution of the data \mathbf{x} and the condition c and $q(\mathbf{x}) := \sum_c q(\mathbf{x}, c)$. Let
 45 $p_{\theta, E}(\mathbf{x})$ be a model parameterized by $\theta \in \Theta$ and $E \in \mathcal{E}$, where θ denotes the parameters in the
 46 backbone and E is the embedding for a condition. We formalize two learning paradigms as follows.

47 In *unconditional learning*, $p_{\theta, E}(\mathbf{x})$ approximates the marginal data distribution $q(\mathbf{x})$ directly and E
 48 is a redundant embedding shared by all data. Formally, given a certain statistics divergence \mathcal{D} (or
 49 more loosely a divergence upper bound [20, 2]), unconditional learning aims to optimize

$$\min_{\theta \in \Theta, E \in \mathcal{E}} \mathcal{D}(q(\mathbf{x}) \| p_{\theta, E}(\mathbf{x})). \quad (1)$$

50 In *conditional learning*, the embedding E is spared to receive the signal from the condition c , through
 51 an embedding function $\phi \in \Phi$. This induces a conditional model $p_{\theta, \phi}(\mathbf{x}|c) := p_{\theta, E}(\mathbf{x})|_{E=\phi(c)}$,
 52 which approximates the conditional data distribution $q(\mathbf{x}|c)$ by tuning the backbone θ and the
 53 embedding function ϕ . Formally, conditional learning aims to optimize

$$\min_{\theta \in \Theta, \phi \in \Phi} \mathbb{E}_{q(c)} \mathcal{D}(q(\mathbf{x}|c) \| p_{\theta, \phi}(\mathbf{x}|c)). \quad (2)$$

54 The conditional model applies ancestral sampling to generate samples, where a condition c is firstly
 55 drawn from $q(c)$ ¹, and then a data \mathbf{x} is drawn from $p_{\theta, \phi}(\mathbf{x}|c)$. Such a process produces samples
 56 from $p_{\theta, \phi}(\mathbf{x}) := \mathbb{E}_{q(c)} p_{\theta, \phi}(\mathbf{x}|c)$. The generation performance of the conditional model is evaluated
 57 according to how close $p_{\theta, \phi}(\mathbf{x})$ is to the data distribution $q(\mathbf{x})$, i.e., $\mathcal{D}(q(\mathbf{x}) \| p_{\theta, \phi}(\mathbf{x}))$.

58 2.2 Analyses

59 In this section, we attempt to formalize two insights on why conditional learning of generative models
 60 generally outperforms the unconditional one.

61 Firstly, we compare the expressive power of the two strategies with the same backbone pa-
 62 rameterized by θ . As shown in Section 2.1, the conditional model produces samples from
 63 $p_{\theta, \phi}(\mathbf{x}) = \mathbb{E}_{q(c)} [p_{\theta, \phi}(\mathbf{x}|c)] = \mathbb{E}_{q(c)} [p_{\theta, E}(\mathbf{x})|_{E=\phi(c)}]$. Therefore, $p_{\theta, \phi}(\mathbf{x})$ can be viewed as a
 64 mixture of several unconditional models. Namely, the conditional model is more expressive than the
 65 unconditional one, despite the fact that both models are based on the same backbone $p_{\theta, E}(\mathbf{x})$.

66 Secondly, we derive a sufficient condition for the superiority of the conditional model. Let θ_u^*, E_u^*
 67 be the optimal solution of the unconditional learning in Eq. (1). Let θ_c^*, ϕ_c^* be the optimal solu-
 68 tion of the conditional learning in Eq. (2). Proposition 1 characterizes a sufficient condition for
 69 $\mathcal{D}(q(\mathbf{x}) \| p_{\theta_c^*, \phi_c^*}(\mathbf{x})) < \mathcal{D}(q(\mathbf{x}) \| p_{\theta_u^*, E_u^*}(\mathbf{x}))$.

70 **Proposition 1.** *Suppose for any parameter $\theta \in \Theta$ and any condition c , approximating $q(\mathbf{x}|c)$ is*
 71 *simpler than $q(\mathbf{x})$ by only tuning the embedding E of $p_{\theta, E}(\mathbf{x})$, i.e., $\min_E \mathcal{D}(q(\mathbf{x}|c) \| p_{\theta, E}(\mathbf{x})) <$
 72 $\min_E \mathcal{D}(q(\mathbf{x}) \| p_{\theta, E}(\mathbf{x}))$. Then, under additional mild regularity conditions², $\mathcal{D}(q(\mathbf{x}) \| p_{\theta_c^*, \phi_c^*}(\mathbf{x})) <$
 73 $\mathcal{D}(q(\mathbf{x}) \| p_{\theta_u^*, E_u^*}(\mathbf{x}))$ holds. (Proof in Appendix A)*

¹We assume $q(c)$ is known, which is satisfied in conditional learning with labels.

²Specifically, we assume that the divergence \mathcal{D} is convex and the embedding function space Φ includes all measurable functions, which are verifiable in practice. In fact, the former can be satisfied using the KL divergence and the latter can be satisfied by using nonparametric embeddings.

Table 1: FID \downarrow results on different datasets. K represents the number of clusters.

	CIFAR10	CelebA 64x64	LSUN Bedroom 64x64	ImageNet 64x64
Unconditional DM	2.72	2.14	2.69	6.44
Conditional DM	2.24	-	-	3.08
SCDM ($K = 2$)	-	2.04	-	-
SCDM ($K = 10$)	2.23	1.91	-	-
SCDM ($K = 20$)	2.27	2.08	2.39	-
SCDM ($K = 30$)	2.30	-	-	-
SCDM ($K = 50$)	2.34	-	-	-
SCDM ($K = 100$)	-	-	2.25	-
SCDM ($K = 1000$)	-	-	-	3.94

74 The sufficient condition in Proposition 1 is hard to verify in practice generally³. However, it does
 75 provide insights on when conditional learning is preferable. In fact, it implies that the conditional
 76 model gains more (i.e., $\min_E \mathcal{D}(q(\mathbf{x}|c)||p_{\theta,E}(\mathbf{x}))$ gets smaller for all θ) as the conditional data
 77 distribution gets simpler. The condition is probably satisfied in practical conditional learning with
 78 class labels. In this sense, Proposition 1 explains previous empirical findings.

79 3 Self-Conditioned Diffusion Models

80 Note that Proposition 1 applies to all possible conditions, not limited to class labels, which inspires
 81 us to obtain meaningful conditions in an unsupervised manner to boost the unconditional generation
 82 results. The recent advances in self-supervised learning [10, 5] show that one can learn predictive
 83 representations without labels, which serves as an ideal tool for obtaining meaningful conditions.

84 Specifically, we propose a three-stage algorithm. Firstly, we train a feature extractor on the target
 85 dataset (without labels) in a self-supervised manner and extract features. Secondly, we run a clustering
 86 algorithm (e.g., k -means in our experiments) on these features and obtain the cluster indices for all
 87 data. Finally, we train a conditional diffusion model [18, 9] by taking the cluster indices as conditions.
 88 We refer to our approach as *self-conditioned diffusion models* (SCDM).

89 We mention that the high-level idea of using clustering indices from self-supervised learning coincides
 90 with prior work in GANs [1, 4, 19]. This paper presents distinct contributions in the following aspects.
 91 First, prior work focuses on avoiding mode collapse while this paper is motivated by a different
 92 perspective with theoretical insights missing in the literature. Second, this paper is built upon SOTA
 93 diffusion models [6, 9] to explore the boundary of unconditional generative modeling. In fact, we
 94 obtain a record-breaking FID of 3.94 on ImageNet 64x64 without labels. See a direct comparison
 95 with prior work [4, 19] in Table 2.

96 4 Experiment

97 We evaluate SCDM on CIFAR10 [13], CelebA 64x64 [15], LSUN Bedroom 64x64 [22] and ImageNet
 98 64x64 [8]. By default, we use MoCo-v2 [6] on CIFAR10, CelebA 64x64 and LSUN Bedroom
 99 64x64, and use MoCo-v3 [7] on ImageNet 64x64, in the self-supervised learning stage. We use
 100 the FID score [11] to measure the sample quality. We use the same architecture for SCDM and its
 101 unconditional and conditional baselines. See more experimental details in Appendix B.

102 4.1 Sample Quality

103 Firstly, we compare our SCDM with the unconditional and conditional baselines. As shown in Table 1,
 104 SCDM uniformly outperforms the unconditional model and slightly outperforms the conditional

³A simple verifiable case is to fit a mixture of Gaussian (MoG) data by a single Gaussian (unconditional learning) or a MoG with ground-truth cluster indices (conditional learning).

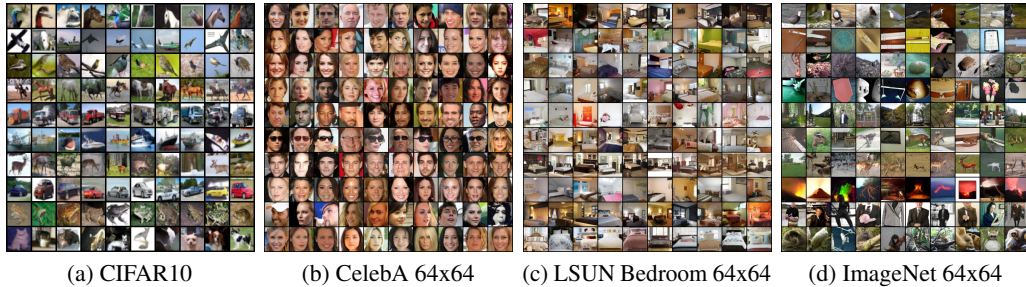


Figure 2: Generated samples of SCDM. Each column corresponds to a cluster. We use the model with the best FID.

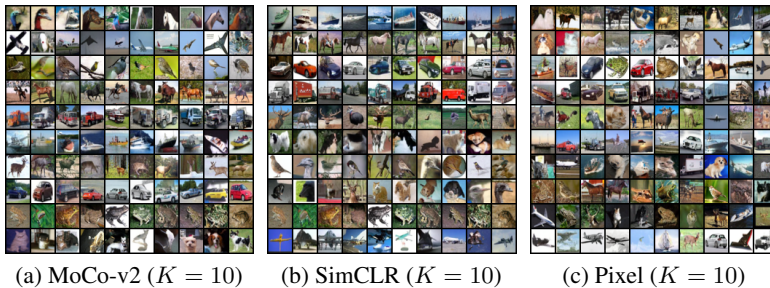


Figure 3: Generated samples on CIFAR10 with different clustering methods.

105 model on CIFAR10. On ImageNet 64x64, SCDM greatly improves the FID compared to the
 106 unconditional model. We provide generated samples in Figure 2.

107 In Table 2, we compare SCDM with other methods on ImageNet 64x64 in the unlabelled setting.
 108 SCDM significantly outperforms all prior methods and achieves a record-breaking FID of 3.94.

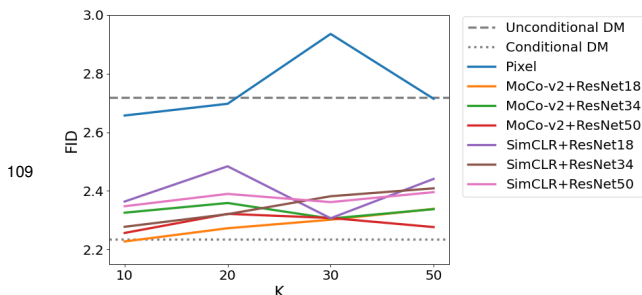


Figure 1: The effect of the self-supervised learning methods, and the backbones used in self-supervised learning.

Table 2: ImageNet 64x64 results in the unlabelled setting. [†]Improved DDPM reports FID with 10K samples, and thereby we use reproduced results on 50K samples [2].

Method	FID
SLCGAN [19]	19.2
Unconditional BigGAN [4]	16.9
IC-GAN [4]	9.2
Improved DDPM [†] [18]	16.38
Unconditional DM	6.44
SCDM (ours)	3.94

110 4.2 Ablation Study

111 In this part, we study the effect of the self-supervised learning methods. We test MoCo-v2, as
 112 well as SimCLR [5] with 3 backbones: ResNet-18, ResNet-34, and ResNet-50. We also perform
 113 k -means on image pixels directly to get cluster indices, and we call this method *pixel*. As shown
 114 in Figure 1, SimCLR performs similarly to MoCo-v2, and the choice of backbones does not affect
 115 the performance much. However, k -means on image pixels performs much worse than SimCLR
 116 and MoCo-v2. Indeed, as shown in Figure 3, we find objects of diverse classes appear in a single
 117 cluster for the pixel method, leading to a more complex distribution in a single cluster, which is more
 118 difficult to learn.

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175 A Proof of Proposition 1

176 We firstly present a lemma.

177 **Lemma 1.** Suppose $\min_{\theta \in \Theta} \mathbb{E}_{q(c)} \min_{E \in \mathcal{E}} \mathcal{D}(q(\mathbf{x}|c) \| p_{\theta, E}(\mathbf{x})) < \min_{\theta \in \Theta, E \in \mathcal{E}} \mathcal{D}(q(\mathbf{x}) \| p_{\theta, E}(\mathbf{x}))$, the diver-
178 gence \mathcal{D} is convex, and the embedding function space Φ includes all measurable functions. Then we
179 have $\mathcal{D}(q(\mathbf{x}) \| p_{\theta_c^*, \phi_c^*}(\mathbf{x})) < \mathcal{D}(q(\mathbf{x}) \| p_{\theta_u^*, E_u^*}(\mathbf{x}))$.

180 *Proof.* According to the convexity of \mathcal{D} , we have

$$\mathcal{D}(q(\mathbf{x}) \| p_{\theta_c^*, \phi_c^*}(\mathbf{x})) = \mathcal{D}(\mathbb{E}_{q(c)} q(\mathbf{x}|c) \| \mathbb{E}_{q(c)} p_{\theta_c^*, \phi_c^*}(\mathbf{x}|c)) \leq \mathbb{E}_{q(c)} \mathcal{D}(q(\mathbf{x}|c) \| p_{\theta_c^*, \phi_c^*}(\mathbf{x}|c)) \quad (3)$$

181 According to the definition of θ_c^* , ϕ_c^* , we have

$$\begin{aligned} \mathbb{E}_{q(c)} \mathcal{D}(q(\mathbf{x}|c) \| p_{\theta_c^*, \phi_c^*}(\mathbf{x}|c)) &= \min_{\theta, \phi} \mathbb{E}_{q(c)} \mathcal{D}(q(\mathbf{x}|c) \| p_{\theta, \phi}(\mathbf{x}|c)) \\ &= \min_{\theta, \phi} \mathbb{E}_{q(c)} \mathcal{D}(q(\mathbf{x}|c) \| p_{\theta, \phi(c)}(\mathbf{x})) = \min_{\theta} \mathbb{E}_{q(c)} \min_{\phi(c)} \mathcal{D}(q(\mathbf{x}|c) \| p_{\theta, \phi(c)}(\mathbf{x})) \\ &= \min_{\theta} \mathbb{E}_{q(c)} \min_E \mathcal{D}(q(\mathbf{x}|c) \| p_{\theta, E}(\mathbf{x})). \end{aligned} \quad (4)$$

182 Combining Eq. (3), Eq. (4), and the assumption, we have

$$\begin{aligned} \mathcal{D}(q(\mathbf{x}) \| p_{\theta_c^*, \phi_c^*}(\mathbf{x})) &\leq \min_{\theta} \mathbb{E}_{q(c)} \min_E \mathcal{D}(q(\mathbf{x}|c) \| p_{\theta, E}(\mathbf{x})) \\ &< \min_{\theta, E} \mathcal{D}(q(\mathbf{x}) \| p_{\theta, E}(\mathbf{x})) = \mathcal{D}(q(\mathbf{x}) \| p_{\theta_u^*, E_u^*}(\mathbf{x})). \end{aligned}$$

183 □

184 Then we present proof of Proposition 1.

185 *Proof.* Since $\forall \theta, c, \min_E \mathcal{D}(q(\mathbf{x}|c) \| p_{\theta, E}(\mathbf{x})) < \min_E \mathcal{D}(q(\mathbf{x}) \| p_{\theta, E}(\mathbf{x}))$, we have

$$\min_{\theta} \mathbb{E}_{q(c)} \min_E \mathcal{D}(q(\mathbf{x}|c) \| p_{\theta, E}(\mathbf{x})) < \min_{\theta, E} \mathcal{D}(q(\mathbf{x}) \| p_{\theta, E}(\mathbf{x})).$$

186 According to Lemma 1, we have $\mathcal{D}(q(\mathbf{x}) \| p_{\theta_c^*, \phi_c^*}(\mathbf{x})) < \mathcal{D}(q(\mathbf{x}) \| p_{\theta_u^*, E_u^*}(\mathbf{x}))$. □

187 B Experimental Details

188 In the self-supervised learning stage, we use ResNet18 on CIFAR10, and ResNet50 on CelebA and
189 LSUN Bedroom. We train 1600, 800 and 200 epochs on CIFAR10, CelebA and LSUN Bedroom
190 respectively. We resize images to 32x32, and use a batch size of 512. We use the SGD optimizer with
191 a learning rate of 0.06, a momentum of 0.9 and a weight decay of 5e-4. The queue size of MoCo is
192 12800, and the momentum of MoCo is 0.999. As for ImageNet, we use pretrained ViT-Base provided
193 in <https://github.com/facebookresearch/moco-v3>.

194 We provide training and sampling setting of diffusion models in Table 3. We evaluate FID every 50K
 195 training steps, and report the best one.

Dataset	CIFAR10	CelebA 64x64	LSUN Bedroom 64x64	ImageNet 64x64
Architecture	IDDPM [18]	IDDPM	IDDPM	ADM [9]
Noise schedule	VP SDE [21]	VP SDE	VP SDE	VP SDE
Batch size	128	128	128	2048
Training steps	1M	1M	1M	550K
Optimizer	Adam [12]	Adam	Adam	AdamW [16]
Learning rate	1e-4	1e-4	1e-4	3e-4
Sampler	EM	EM	EM	DPM-Solver [17]
Sampling steps	1K	1K	1K	50

Table 3: The experimental setting of diffusion models. EM represents the Euler-Maruyama sampler.