

000 BEYOND SEQUENTIAL CONTEXT: NAVIGATING NON- 001 LINEAR FLOW OF MULTI-TURN DIALOGUES WITH DY- 002 NAMIC CONTEXT TREE 003 004

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010 ABSTRACT

013 Large Language Models demonstrate outstanding performance in many language
014 tasks but still face fundamental challenges in managing the non-linear flow of
015 human conversation. The prevalent approach of treating dialogue history as a
016 flat, linear sequence is misaligned with the intrinsically hierarchical and branch-
017 ing structure of natural discourse, leading to inefficient context utilization and a
018 loss of coherence during extended interactions involving topic shifts or instruc-
019 tion refinements. To address this limitation, we introduce Context-Agent, a novel
020 framework that models multi-turn dialogue history as a dynamic tree structure.
021 This approach mirrors the inherent non-linearity of conversation, enabling the
022 model to maintain and navigate multiple dialogue branches corresponding to dif-
023 ferent topics. Furthermore, to facilitate robust evaluation, we introduce the Non-
024 linear Task Multi-turn Dialogue (NTM) benchmark, specifically designed to as-
025 sess model performance in long-horizon, non-linear scenarios. Our experiments
026 demonstrate that Context-Agent enhances task completion rates and improves to-
027 ken efficiency across various LLMs, underscoring the value of structured context
028 management for complex, dynamic dialogues.

029 1 INTRODUCTION

031 The advancement of dialogue systems based on Large Lan-
032 guage Models (LLMs) is pivotal for the efficacy of next-
033 generation applications, including complex AI Agents and
034 collaborative robotics, where the ability to maintain context-
035 aware communication is fundamental to task completion and
036 user engagement (Durante et al., 2024; Yao et al., 2024). Fol-
037 lowing the advent of LLMs’ context window expansion tech-
038 niques, the capabilities for multi-turn dialogue have been
039 significantly enhanced (Li et al., 2025).

040 However, LLMs still grapple with a fundamental challenge
041 inherent to natural human conversation: the management of
042 non-linear dialogue flow. This phenomenon occurs when
043 conversational topics do not advance in a sequential order
044 but instead feature shifts, topical jumps, or interwoven threads of discussion (Laban et al., 2025).
045 Such non-linear dynamics are commonplace in real-world interactions, where users may revisit pre-
046 vious topics, introduce new subjects, or refine earlier statements based on evolving understanding
047 or context (Mann & Thompson, 1988). The prevalent approach of treating dialogue history as a
048 flat, linear sequence is fundamentally misaligned with the intrinsic structure of human conversation
049 (Wang et al., 2024; Li et al., 2025). This linear paradigm fails to capture the hierarchical and branch-
050 ing nature of dialogues, leading to inefficiencies in context utilization and challenges in maintaining
051 coherence over extended interactions (Ding et al., 2024).

052 Effectively resolving the non-linear flow problem requires overcoming several distinct challenges.
053 The first is the accurate identification and management of topic shifts and instruction refinements
within a conversation. The second challenge is the efficient selection of context from a potentially

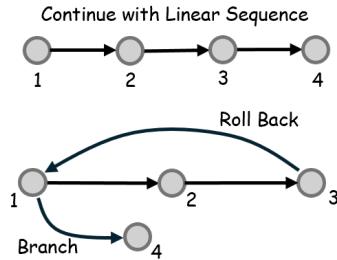


Figure 1: A schematic diagram of linear (upper) vs. non-linear (lower) dialogue flow.

vast and complex dialogue history. As conversations extend over multiple turns, the accumulation of information can lead to increased computational costs and the risk of overwhelming the model with irrelevant details (Joren et al., 2025), leading to the “needle in a haystack” problem (Liu et al., 2024b; Vaswani et al., 2017). The third challenge lies in the development of robust evaluation metrics and benchmarks that can accurately assess a model’s performance in handling non-linear dialogues, as existing datasets often lack the complexity and variability found in real-world interactions.

To address these challenges, inspired by the hierarchical organization inherent in human cognitive processes for managing complex dialogues (Grosz & Sidner, 1986), we propose Context-Agent, a novel framework that models multi-turn dialogue history as a dynamic tree structure. This approach allows for the representation of conversations in a way that reflects their inherent non-linear nature, enabling the model to maintain multiple branches of dialogue corresponding to different topics or sub-topics. Furthermore, recognizing the inadequacy of existing datasets for this problem, we introduce the Non-linear Task Multi-turn Dialogue (NTM) benchmark, specifically designed to evaluate the performance of models in long-horizon, non-linear dialogue scenarios. This benchmark features dialogues with multiple topic shifts and instruction refinements, providing a more realistic and challenging testbed for assessing context management strategies.

In summary, the main contributions of this paper are as follows:

- We propose Context-Agent, a novel framework that models dialogue history as a dynamic tree structure and integrates it with a retrieval-augmented generation (RAG) mechanism. This enables efficient, structurally-aware context selection, allowing the model to accurately identify and provide the most relevant conversational branches for each query.
- We introduce a new benchmark, the Non-linear Task Multi-turn Dialogue (NTM), specifically designed to evaluate the performance of models in long-horizon, non-linear dialogue scenarios. This benchmark features dialogues with multiple topic shifts and instruction refinements, providing a more realistic and challenging testbed for assessing context management strategies.
- We conduct extensive experiments on the NTM benchmark, demonstrating that our Context-Agent framework outperforms mainstream context management methods across various LLMs. Notably, it achieves improvements in task completion rates while reducing token usage, highlighting its effectiveness and efficiency in managing complex non-linear multi-turn dialogues.

2 RELATED WORK

Architectural Context Extension Methods To overcome Transformer context window limits, recent work has improved position encoding and attention mechanisms (Tworkowski et al., 2023).

Position Interpolation (PI) (Chen et al., 2023) rescales position indices, while **YaRN** (Peng et al., 2024) extends Rotary Position Embeddings (RoPE) for longer contexts. Efficient attention methods like **LongLoRA** (Chen et al., 2024) use Shifted Sparse Attention to reduce computation. However, these approaches only enlarge the context window and do not address efficient organization or retrieval of relevant content, so issues like high cost and the “lost in the middle” problem remain.

Information Compression and Selection Methods Another line of work compresses dialogue history to balance efficiency and information retention. Typical approaches combine clustering and summarization. For example, (Su & Zhou, 2022) use spectral clustering to group turns by topic and summarize each cluster. Context distillation methods, such as (Park et al., 2021), train compact models to preserve key relationships, achieving significant memory savings with minimal performance loss. However, these methods treat history as an unstructured sequence, relying only on semantic similarity and failing to capture topic shifts or hierarchical sub-topics essential for coherence in complex dialogues.

Retrieval-Augmented Context Selection Recent advances adapt **Retrieval-Augmented Generation (RAG)** from external knowledge retrieval to internal dialogue history (Lewis et al., 2020). For example, **DH-RAG** (Zhang et al., 2025) builds a dynamic database of “query-passage-response” triplets and uses clustering, hierarchical matching, and Chain-of-Thought tracking for retrieval. However, its flat structure limits modeling of dialogue flow, as retrieval relies solely on semantic similarity, not structural relationships.

108 In summary, prior work lacks structured representations of dialogue history, often relying on unstructured
 109 or domain-specific approaches, which limits their generalizability to complex conversations.
 110 Our work addresses this gap and opens a new direction for efficient, general context management in
 111 multi-turn dialogue.
 112

113 3 METHOD

115 Our framework models a multi-turn dialogue as a forest of topic trees. Each tree represents a distinct
 116 topic and is composed of nodes (dialogue units) and branches. The dialogue’s evolution is managed
 117 through state transitions.
 118

119 3.1 FORMAL PROBLEM DEFINITION

121 Conventional dialogue systems model history as a linear sequence $H_t = \{(q_1, r_1), \dots, (q_t, r_t)\}$,
 122 generating a response r_{t+1} from a query q_{t+1} via a function $g(H_t, q_{t+1})$. This flat representation
 123 leads to contextual redundancy and loss of structural information.

124 To address this limitation, we introduce and formalize the problem of Non-linear Contextual Dia-
 125 logue Management. The central premise of this problem is to shift from treating the entire history
 126 H_t as an undifferentiated input to representing it as a dynamically evolving, hierarchically structured
 127 dialogue forest, denoted as F_t . At each turn $t + 1$, given:

- 128 • A structured dialogue history represented as a forest, $H_t = F_t$.
- 129 • The current dialogue state $S_t = (H_t, T_{\text{act}}, B_{\text{act}}, n_{\text{cur}})$, which includes the history, the active topic
 130 tree, the active branch, and the current node.
- 131 • The new user query q_{t+1} .

133 The objective is to learn a policy π that comprises two key functions: a context selection function,
 134 f_{select} , and a response generation function, f_{gen} :

$$135 \quad C_{t+1} = f_{\text{select}}(q_{t+1}, S_t) \quad r_{t+1} = f_{\text{gen}}(q_{t+1}, C_{t+1})$$

137 Here, C_{t+1} represents a highly relevant context subset, which is dynamically selected and con-
 138 structed from the structured history H_t . The ultimate goal is to maximize the task completion rate
 139 while minimizing the token footprint of the selected context C_{t+1} , thereby achieving efficient con-
 140 text utilization without compromising conversational coherence or task-oriented performance.

141 3.2 CORE COMPONENTS

143 **Node** The smallest unit of a conversation is a node n , which represents the content of a round of
 144 dialogue between the user and the model. Each node is defined as a tuple:
 145

$$146 \quad n = (c, v, p, \beta, s_i)$$

147 where c is the content of the current conversation round, $v \in \mathbb{R}^d$ is its d -dimensional text embedding,
 148 p is the parent node’s identifier (null for a root), β is the branch identifier, and s_i is a summary of
 149 the node’s content. After each round, a summarization function S_{node} converts the content c_i into a
 150 summary $s_i = S_{\text{node}}(c_i)$, which is used for subsequent topic attribution and branch management.

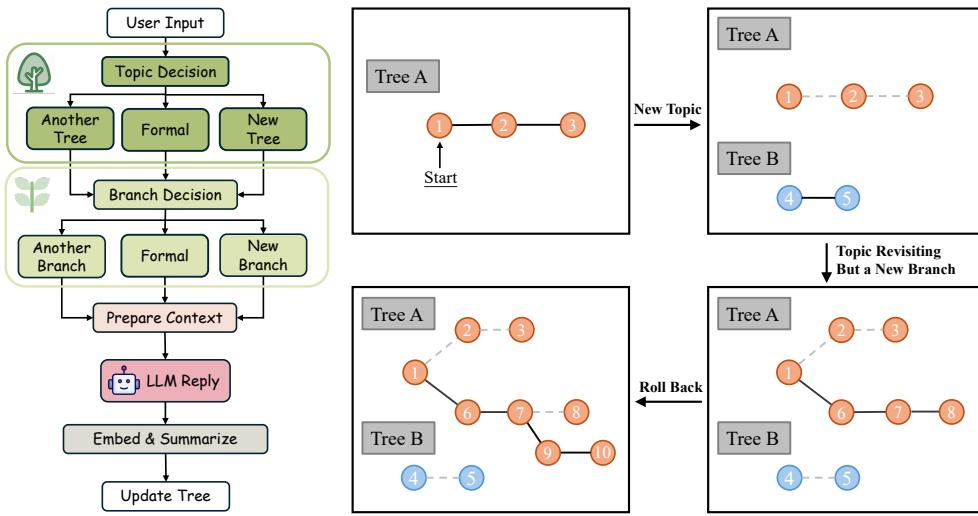
152 **Topic Tree** An independent topic is represented by a topic tree T . It is a directed acyclic graph,
 153 $T = (N, E)$. Here, $N = \{n_1, n_2, \dots, n_k\}$ is the set of all nodes under this topic, and $E =$
 154 $\{(n_i, n_j) \mid p(n_j) = n_i\}$ is the set of directed edges between nodes, representing the inheritance
 155 relationship of the conversation. The first dialogue round of a new topic is set as the root node,
 156 whose parent node is null, of the topic tree.

157 **Branch** Within the same topic tree T , a branch B is a relatively independent dialogue path that
 158 starts from a branching point but still remains under the same topic. It is defined as an ordered
 159 sequence of nodes $B = \langle n_1, n_2, \dots, n_k \rangle$, where any two adjacent nodes (n_i, n_{i+1}) in the sequence
 160 satisfy $p(n_{i+1}) = n_i$. All nodes within the same branch share the same branch identifier β .

161 **Conversation History** The complete history H of a multi-turn conversation is represented as a
 162 forest F consisting of multiple topic trees, i.e., $H = F = \{T_1, T_2, \dots, T_m\}$.

162 3.3 STATE TRANSITION
163

164 The conversational state at turn t is defined as $S_t = (H_t, T_{act}, B_{act}, n_{cur})$, which includes the history,
165 the active topic tree, the active branch, and the current node. The conversation evolves through
166 state transitions driven by new user queries. Upon receiving a new query, the system analyzes it to
167 determine the topic and manage branches, updating the state accordingly. This process involves the
168 following steps:



186 Figure 2: An overview of the Context-Agent framework. It illustrates the dynamic evolution of
187 a multi-turn dialogue represented as a forest of topic trees, with branches indicating sub-dialogue
188 paths. The number in each node represents the turn number in the conversation. And solid edges
189 represent the active path, while dashed edges indicate inactive paths.
190

- 191 • **Step0: Initialization** The dialogue begins by creating the first topic tree T_1 , which be-
192 comes the active tree T_{act} . An aggregation summary function S is defined to produce sum-
193maries for branches or trees by concatenating the summaries of their constituent nodes, i.e.,
194 $S(B) = \text{Concat}(s_1, \dots, s_k)$ for a branch B and $S(T)$ for a topic tree T .
- 195 • **Step1: Topic Decision** For a new query q_{t+1} , a lightweight language model Ψ determines the
196 topic action a_{topic} and target tree T_{target} based on summaries of existing trees:

$$197 \quad (a_{topic}, T_{target}) = \Psi(q_{t+1}, \{S(T_i)\})$$

199 The active tree T_{act} is then updated to T_{target} . The action a_{topic} can be:

200 – **CREATE_TOPIC**: A new topic tree is created.
201 – **SWITCH_TOPIC**: Switch to the most relevant existing tree.
202 – **CONTINUE**: Remain in the current tree.

204 • **Step2: Fork Point Identification** For a new query q_{t+1} , the system first computes its embedding
205 vector $v_{q,t+1} = \epsilon(q_{t+1})$ using the embedding function $\epsilon : C \rightarrow \mathbb{R}^d$. Then, among all nodes in
206 the active topic tree T_{act} , it identifies the node most semantically relevant to q_{t+1} as the potential
207 fork point. This is achieved by maximizing the similarity function $\text{Sim}(v_{q,t}, v_i)$:

$$208 \quad n_{fork}^* = \arg \max_{n_i \in N_{act}} \text{Sim}(v_{q,t+1}, v_i)$$

210 • **Step3: Branch Decision** Branch decision employs a two-stage “heuristic filtering + model
211 decision” approach. First, a heuristic function H_{filter} quickly determines if a complex decision is
212 needed. If the most similar node n_{fork}^* found in Step 2 is sufficiently relevant (similarity $> \theta_{sim}$)
213 and belongs to a different branch or is an ancestor, H_{filter} returns true.

$$214 \quad H_{filter} := (\text{sim}_{\max} > \theta_{sim}) \wedge (\beta(n_{fork}^*) \neq \beta(n_{cur}) \vee \text{IsAncestor}(n_{fork}^*, n_{cur}))$$

216 If H_{filter} is true, a lightweight language model Φ determines the branch action a_{branch} based on the
 217 query, current path, and retrieved nodes $R(q)$. Otherwise, the action defaults to **CONTINUE**.
 218

$$219 \quad a_{\text{branch}} = \begin{cases} \Phi(q_{t+1}, \text{Path}(n_{\text{cur}}), R(q_{t+1})) & \text{if } H_{\text{filter}} \text{ is true} \\ \text{CONTINUE} & \text{otherwise} \end{cases}$$

220 The possible actions are:
 221

- 222 – **CONTINUE**: Add a new node to the current branch.
- 223 – **CREATE_BRANCH**: Start a new branch from the fork point n_{fork}^* .
- 224 – **SWITCH_BRANCH**: Switch the active branch to the one containing n_{fork}^* .

- 225 • **Step4: Context Construction** The final context C_{t+1} is constructed by combining the full
 226 dialogue of the current active path with summaries of inactive branches and topics. This provides
 227 focused, relevant information while maintaining a broad overview of the entire conversation. The
 228 context is formed as:

$$229 \quad C_{t+1} = \text{Concat}(\{c_i \mid n_i \in \text{Path}(n_{\text{cur}}, T_{\text{act}})\}) \bigoplus_{\substack{B_j \in T_{\text{act}}, \\ B_j \neq B_{\text{act}}}} S(B_j) \bigoplus_{\substack{T_k \in H_t, \\ T_k \neq T_{\text{act}}}} S(T_k)$$

230 This structured context includes: (1) The complete dialogue history of the current active path. (2)
 231 Summaries of all other branches within the active topic tree. (3) Summaries of all other topic
 232 trees in the conversation history.

233 4 NON-LINEAR TASK MULTITURN DIALOGUE (NTM) BENCHMARK

234 While existing multi-turn dialogue datasets have been instrumental, they are often inadequate as
 235 they typically feature a limited number of turns with an average length of under 10 turns and assume
 236 a fixed, linear context (Deshpande et al., 2025; Kwan et al., 2024; Bai et al., 2024). This fails
 237 to capture the complexity of long-running conversations with dynamic topic shifts, making them
 238 unsuitable for assessing a model’s robustness and long-range contextual reasoning. To bridge this
 239 gap, we introduce the Non-linear Task Multiturn Dialogue (NTM), a benchmark designed to test the
 240 limits of contextual understanding and robustness in LLMs.

241 4.1 DATA CREATION

242 NTM comprises a collection of dialogues focused on two domains: daily life planning and coding
 243 support. The dataset was constructed using state-of-the-art LLMs leveraging few-shot prompting
 244 to generate initial dialogues. Subsequently, each dialogue underwent a rigorous process of manual
 245 review, polishing, and filtering by human annotators to ensure high quality and task complexity.

246 Crucially, NTM dialogues focus on two significant aspects: Topic shifts and Instruction Refinement,
 247 which are common in real-world conversations but often overlooked in existing datasets.

- 248 • **Topic Shifts**: Each dialogue is designed to include multiple topic shifts. These shifts are not
 249 random but are contextually relevant, reflecting how real conversations evolve. For example, a
 250 dialogue may start with planning a trip and then shift to discussing dietary preferences for the trip.
- 251 • **Instruction Refinement**: The dialogues also incorporate instances where users refine or change
 252 their instructions based on previous responses. This aspect tests the model’s ability to adapt to
 253 evolving user needs and maintain coherence throughout the conversation.

254 This design ensures that NTM evaluates not just information recall, but a model’s ability to maintain
 255 focus and adapt to a dynamically evolving conversational landscape.

256 4.2 KEY CHARACTERISTICS

257 NTM is distinguished by the following features:

- 258 • **Extended Dialogue Length**: The dataset includes a total of 165 dialogues with about 3000 turns,
 259 covering 10, 15, 20, and 25 rounds of conversations, which provide a clear measure of model
 260 scalability as context grows.

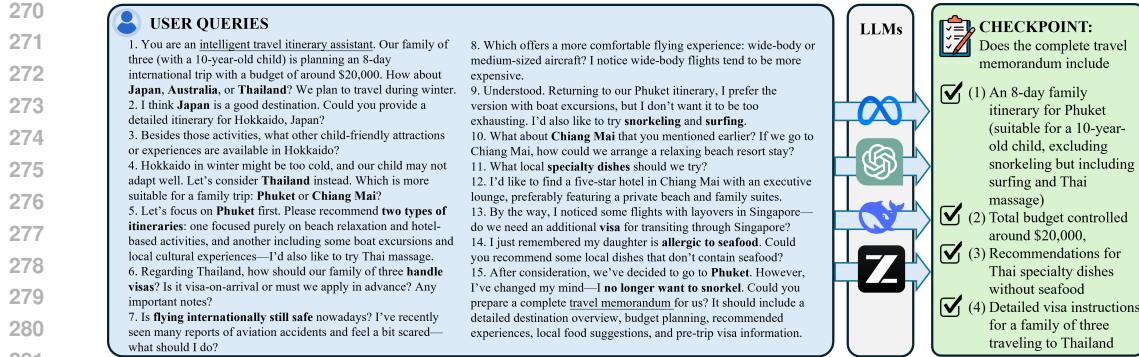


Figure 3: An example of a 15-turn dialogue from the NTM, illustrating topic shifts and instruction refinements. It is about planning a family trip, where the user changes their preferences, adds new requirements and shifts topics as the dialogues progresses. On the right side is the corresponding checkpoint questions for evaluating task completion, which are designed to objectively assess whether the model has fulfilled the user’s final request. More details are in Appendix B.4.

- **Topic Dynamics:** Each dialogue contains multiple topic shifts and instruction refinements, challenging models to maintain coherence and relevance in a non-linear conversational flow.
- **Task-Oriented Focus:** Every dialogue culminates in a clear task that requires accurate information synthesis from the preceding conversation, enabling objective evaluation through task completion metrics.

4.3 EVALUATION METRICS

We evaluate the performance from 2 perspectives: task completion accuracy and token efficiency.

- **Task Completion Rate (TCR):** Our primary metric for task success. Each task in the NTM benchmark is decomposed into at least three verifiable checkpoints(a yes/no decision). TCR is the average completion rate across these checkpoints, providing a robust measure of task fulfillment. This annotated metric provides a more robust and interpretable measure of a model’s true task-fulfillment capabilities compared to relying solely on scores from a judge LLM.
- **Average Context Tokens (ACT):** Measures the average number of context tokens used per turn. It quantifies context efficiency, with lower values indicating better performance, which is crucial for managing long dialogues under token and cost constraints.

4.4 COMPARISON WITH EXISTING DATASETS

To highlight the unique features of NTM, we compare it with existing multi-turn dialogue datasets in Table 1. NTM stands out with its significantly longer average and maximum turn counts, as well as its focus on non-linear dialogue evolution, which is absent in other datasets. This makes NTM a more challenging and realistic benchmark for evaluating the capabilities of dialogue systems in handling complex, multi-turn interactions.

Dataset	Avg. Turns	Max Turns	Total turns	Non-linear Evolution
Multichallenge	5	10	1365	No
MT-Eval	7	14	1170	No
MT-Bench-101	3	7	4208	No
NTM (Ours)	18	27	2929	Yes

Table 1: Comparison of NTM with existing multi-turn dialogue datasets.

324 **5 EXPERIMENTAL SETUP**

325

326 To rigorously evaluate the performance and efficiency of our proposed Context-Agent framework,
 327 we designed a comprehensive set of experiments. The primary goal is to demonstrate our model's
 328 superior ability to manage context in the long-form, non-linear dialogues that current benchmarks
 329 fail to represent.

330 The experiments were designed to answer the following research questions: (1) How does Context-
 331 Agent perform on complex, long-horizon dialogue tasks compared to baseline methods? (2) To
 332 what extent can Context-Agent improve token efficiency without compromising task success? (3)
 333 What are the individual contributions of the tree-based structural representation and the RAG-based
 334 retrieval mechanism to the overall performance of our system?

335

336 **5.1 EVALUATION BENCHMARK**

337

338 A significant challenge in evaluating long-turn conversational models is the lack of suitable bench-
 339 marks. Existing datasets typically feature short, linear dialogues that do not adequately test a model's
 340 ability to handle complex, evolving conversations. And the most important reason is that their con-
 341 text offered to the model is usually a fixed-length linear sequence, which cannot reflect the ad-
 342 vantages of our Context-Agent in managing non-linear dialogue history. Therefore, all models are
 343 evaluated on our newly proposed Non-linear Task Multi-turn Eval (NTM) benchmark.

344 **5.2 BASELINE METHODS**

345

346 We benchmark our Context-Agent framework against mainstream context management methods
 347 nowadays, which can be categorized into three groups:

349 • **Full History Concatenation (Full-History):** This method involves concatenating the entire di-
 350 alogue history as input to the model. While it provides complete context, it is computationally
 351 expensive and often impractical for long conversations due to token limits.

352 • **Truncation (Truncation):** This approach retains only the most recent k turns of the conversation,
 353 discarding earlier context. It is efficient but risks losing important information from previous
 354 dialogue turns. In our experiments, we set $k = 4$.

355 To ensure a comprehensive evaluation of
 356 our Context-Agent across different models,
 357 we conducted experiments on four recent
 358 and diverse LLMs: GPT-4.1 (OpenAI,
 359 2025), DeepSeek-V3 (Liu et al., 2024a),
 360 GLM-4-Plus (GLM et al., 2024), and Llama
 361 3.1-70B (Grattafiori et al., 2024). This se-
 362 lection includes both open- and closed-source
 363 models with varying context window sizes. For
 364 fairness and efficiency, all evaluations were performed with reasoning-disabled settings.

365 **5.3 IMPLEMENTATION DETAILS**

366

367 **Prompt Format:** All models receive the same system prompt instructing them. No chain-of-thought
 368 or explicit instruction tuning is applied to ensure fair comparison. More details are in Appendix B.3.

369 **Local Models:** To balance processing efficiency and accuracy, the Context-Agent's internal modules
 370 utilize lightweight local models. Specifically, we employ gemma3-12B (Team et al., 2025) for
 371 decision-making and gemma3-4B for summary generation. For dialogue context encoding, we
 372 use Qwen3-Embedding-0.6B (Yang et al., 2025), a lightweight, high-performance embedding
 373 model. Based on empirical tuning with these models, the similarity threshold θ_{sim} was set to 0.6. All
 374 experiments were conducted with an NVIDIA A100 40GB GPU.

375 **Evaluation Protocol:** To ensure both scalability and human-aligned judgment, we adopt a triangu-
 376 lated evaluation protocol combining human annotators and two state-of-the-art Judge LLMs: GPT-5
 377 (OpenAI, 2025) and Gemini-2.5-Pro (Comanici et al., 2025). We compute Cohen's κ (Cohen,

378 1960) between Judge LLM and human labels. The result shows that the Cohen’s κ is as high as
 379 0.96, indicating strong agreement and validating the reliability of our evaluation approach.
 380

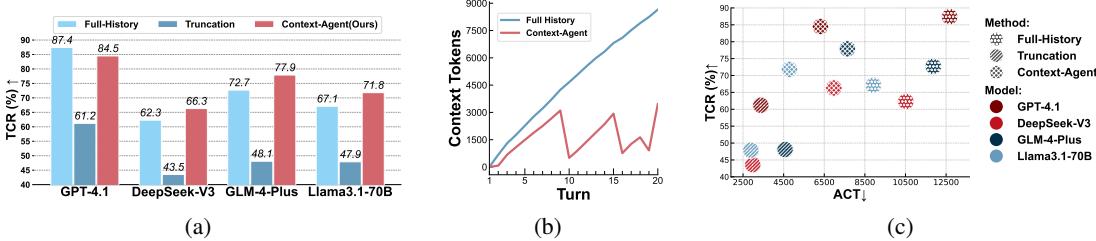
381 6 RESULTS AND ANALYSIS

382 6.1 MAIN RESULTS

383 The main results of our experiments are summarized in Table 3. Across all 4 LLMs, our Context-
 384 Agent consistently outperforms the Truncation method by a significant margin in terms of Task
 385 Completion Rate (TCR). It shows that except for the case of GPT-4.1 has a slight decrease
 386 of 3.3%, our method not only recovers the performance loss caused by truncation but also sur-
 387 passes the Full-History method, achieving relative TCR improvements of 6.4%, 7.2%, and 7.0% on
 388 DeepSeek-V3, GLM-4-Plus, and Llama 3.1-70B, respectively. The reason why our method
 389 does not outperform Full-History on GPT-4.1 may be that GPT-4.1 has a very large context win-
 390 dows (up to 1 million tokens), making it less sensitive to context management strategies. But even
 391 in this case, our method only incurs a minor 3.3% performance drop while significantly reducing
 392 token usage, demonstrating its robustness and efficiency. Especially for super long context windows
 393 LLMs like GPT-4.1, maintaining a full history is often impractical due to computational costs and
 394 latency. And our Context-Agent provides a alternative that balances performance and efficiency.
 395

396 Model	Method	TCR (%) \uparrow	TCR Gain (%)	ACT \downarrow				ACT Drop (%)
				10-turn	15-turn	20-turn	25-turn	
397 GPT-4.1	Full-History	87.4	–	4058	6341	9715	12673	–
	Truncation	61.2	-30.0	1919	2252	2841	3376	–
	Context-Agent	84.5	-3.3	2108	3004	4157	6312	-52.0
402 DeepSeek-V3	Full-History	62.3	–	3559	5378	7680	10515	–
	Truncation	43.6	-30.0	1732	2096	2655	2978	–
	Context-Agent	66.3	+6.4	1935	2917	4314	6973	-42.2
405 GLM-4-Plus	Full-History	72.7	–	4512	6896	9253	11873	–
	Truncation	48.1	-33.8	2733	3438	3819	4570	–
	Context-Agent	77.9	+7.2	1922	3058	4752	7638	-49.3
408 Llama 3.1-70B	Full-History	67.1	–	3496	5088	7170	8920	–
	Truncation	47.9	-28.6	1628	1975	2445	2883	–
	Context-Agent	71.8	+7.0	2187	2638	3975	4784	-44.1

411 Table 3: Main results on the NTM benchmark across different LLMs and context management
 412 methods. TCR Gain shows the relative percentage change compared to Full-History. ACT columns
 413 show Average Context Tokens for 10/15/20/25-turn dialogues; ACT Drop is the average percentage
 414 reduction of Context-Agent compared to Full-History.



420 Figure 4: (a) TCR comparison across different methods and models. (b) A typical example of
 421 context tokens change trend in a 20-turn dialogue. (c) Trade-off between TCR and ACT, where the
 422 ideal point is the top-left corner (high TCR, low ACT).

423 Another notable observation is that though another 3 open-source models (DeepSeek-V3,
 424 GLM-4-Plus, and Llama 3.1-70B) still have considerable context windows (64k or 128k to-
 425 kens), and the total context length of our NTM benchmark is lower than these limits, their TCR

432 scores with Full-History are still significantly lower than that of GPT-4.1. This indicates that
 433 merely having a large context window does not guarantee effective utilization of context, especially
 434 in complex, non-linear dialogues. Our Context-Agent has demonstrated its ability to effectively
 435 manage and utilize context, leading to substantial performance gains.

436 From these results, we can draw several key insights:

- 437 • **Effectiveness of Context-Agent:** The consistent TCR improvements across different models and
 438 dialogue lengths demonstrate that Context-Agent effectively manages context in complex, long-
 439 horizon dialogues. It not only recovers the performance lost due to truncation but also surpasses
 440 the full-history approach in most cases.
- 441 • **Token Efficiency:** The significant reductions in ACT indicate that Context-Agent is highly effi-
 442 cient in utilizing context. By intelligently selecting relevant information through its tree structure
 443 and RAG mechanism, it minimizes unnecessary token usage while still providing sufficient con-
 444 text for accurate responses.
- 445 • **Robustness Across Models:** The performance gains observed across a diverse set of LLMs, in-
 446 cluding both open-source and closed-source models with varying context window sizes, highlight
 447 the robustness and generalizability of the Context-Agent framework.

449 6.2 ABLATION STUDIES

450 To understand the source of Context-Agent’s effectiveness, we conducted an ablation study.

451 The first one is apply RAG on Dialogue History, but remove the tree structure, forcing the RAG to
 452 retrieve from a linear sequence of turns (w/o Tree). We dynamically set $k \in \{3, 5\}$ based on dialogue
 453 depth: $k = 3$ for 10-15 turns, $k = 5$ for 20-25 turns, to balance recall and noise suppression. The
 454 second ablation removes the RAG retriever and relies solely on a heuristic for branch decision (w/o
 455 RAG). This tests whether the tree structure alone can provide sufficient context selection.

456 Table 4 summarizes the results of the abla-
 457 tion study on DeepSeek-V3. Both abla-
 458 tions lead to significant drops in TCR com-
 459 pared to the full Context-Agent model.
 460 Removing the tree structure results in a
 461 35.0% decrease in TCR. This highlights
 462 the importance of the tree structure in orga-
 463 nizing the interal logical flow of the dia-
 464 logue, enabling effective context selection.
 465 Without it, the RAG can only get the result
 466 that may only has semantic relevance but lacks logical relevance.

467 Removing the RAG retriever leads to a 27.3% drop in TCR, indicating that the heuristic alone is
 468 insufficient for accurate branch decision-making. The RAG mechanism provides critical context by
 469 retrieving semantically relevant historical nodes, and at the same time, with the heuristic filtering, it
 470 largely avoids misjudgments when selecting the fork point.

473 7 CONCLUSION

474 In this paper, we addressed the critical limitation of conventional linear context management in han-
 475 dling the non-linear flow of multi-turn dialogues. We introduced Context-Agent, a novel framework
 476 that represents dialogue history as a dynamic tree structure, augmented by a retrieval mechanism.
 477 This approach successfully models the hierarchical and branching nature of human conversations,
 478 enabling effective navigation of complex interactions involving topic shifts and refinements. Our
 479 extensive experiments on the newly proposed NTM benchmark demonstrate that Context-Agent
 480 consistently outperforms traditional context management methods across various LLMs, achieving
 481 significant improvements in task completion rates while drastically reducing token usage. Ablation
 482 studies confirm the critical contributions of both the tree structure and RAG components to the over-
 483 all performance. Our work underscores the potential of structured context management and offers a
 484 promising direction for developing more robust and efficient dialogue systems capable of handling
 485 long-horizon, dynamic conversations.

486 REPRODUCIBILITY STATEMENT
487

488 All experimental projects in this paper are reproducible. We will release the code, data, and prompts
489 used in our experiments to facilitate future research. The specific details of the models, datasets, and
490 evaluation protocols are thoroughly documented in the paper and its appendices. We also provide
491 detailed instructions for setting up the experimental environment and running the code to ensure
492 that other researchers can replicate our results. The relevant materials is available at <https://anonymous.4open.science/r/Context-and-NTM-Benchmark-01C4/>.
493

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A LLM USAGE STATEMENT

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In the preparation of this paper, we utilized Large Language Models (LLMs) as assistive tools to
mainly enhance research efficiency. We explicitly detail all uses of LLMs below and affirm that
all core intellectual contributions, including the formulation of hypotheses, experimental design,
analysis of results, and the final conclusions, were conceived and executed by the human authors.654
655
The specific applications of LLMs in our work are as follows:656
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661
Literature Review and Scoping: In the initial research phase, we employed LLMs (e.g., Google’s
Gemini Deep Research) to conduct preliminary explorations of the research landscape surround-
ing “modeling non-linear conversational flows in multi-turn dialogues”. This involved identifying
seminal papers and outlining the evolution of relevant techniques. This process accelerated our ac-
quisition of a broad understanding of the field. All cited literature was subsequently verified, read,
and critically analyzed by the authors.662
663
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665
Data Analysis and Script Generation: We utilized LLMs to assist in writing and debugging scripts
for data preprocessing and experimental analysis. Specific tasks included parsing log files to extract
performance metrics. All LLM-generated code was thoroughly reviewed, tested, and modified by
the authors to ensure its correctness, efficiency, and alignment with our experimental setup.666
667
The primary LLMs used in this research include: OpenAI’s GPT-5 and Google’s
Gemini-2.5-Pro.

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702 **B APPENDIX**
703704 **B.1 CONTEXT-AGNET LATENCY AND TRADE-OFF ANALYSIS**
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706 Beyond token efficiency, we analyzed the end-to-end response latency to provide a complete picture
707 of Context-Agent’s practical performance. Our method’s hybrid architecture involves several calls
708 to local, lightweight language models for tasks such as branch decision-making and node summa-
709 rization, which introduces time overhead compared to the baseline’s single API call.

710 However, the latency of the full-context baseline is not constant; it degrades as the dialogue history
711 grows and the token payload for the API call increases. This degradation partially offsets the inherent
712 overhead of our method. To quantify this trade-off, we measured the average response time on a
713 single NVIDIA A100 40GB GPU for the 20-turn dialogue scenario. The following table summarizes
714 the average response times:

716 Method	717 Average Response Time (s)	718 Relative Increase (%)
Full-History	12.5	-
Context-Agent	13.5	+8.0%

719 Table 5: Average response time for different context management methods on a 20-turn dialogue.
720

722 Our experiments indicate that Context-Agent incurs a modest 8% increase in average response time.
723 We argue this represents a highly favorable trade-off, given the substantial improvements in token
724 efficiency. It is important to note that these measurements were conducted on a single A100 40GB
725 GPU. This latency overhead could likely be mitigated in a production environment through optimiza-
726 tions such as deploying on enterprise-grade hardware or utilizing lightweight models fine-tuned for
727 the specific decision and summarization sub-tasks.

728 **B.2 THE DETAILED ALGORITHM OF CONTEXT-AGENT**
729

731 The complete algorithm of the Context-Agent framework is presented in Algorithm 1. It outlines the
732 step-by-step process of managing dialogue context, including topic and branch management, node
733 updates, and context construction.

734 **Algorithm 1** Context-Agent Framework
735

736 **Require:** Dialogue history H_t , User query q_{t+1}
737 **Ensure:** Constructed context C_{t+1}

738 **1. Topic and Branch Management**

739 1: $(a_{\text{topic}}, T_{\text{target}}) \leftarrow \Psi(q_{t+1}, \{S(T_i)\}_{T_i \in H_t})$ \triangleright Topic decision
740 2: Update T_{act} , n_{cur} based on a_{topic}
741 3: $n_{\text{fork}}^* \leftarrow \arg \max_{n_i \in T_{\text{act}}} \text{Sim}(\epsilon(q_{t+1}), v_i)$ \triangleright Find fork point
742 4: **if** $H_{\text{filter}}(n_{\text{fork}}^*, n_{\text{cur}})$ **then**
743 5: $a_{\text{branch}} \leftarrow \Phi(q_{t+1}, \text{Path}(n_{\text{cur}}), R(q_{t+1}))$ \triangleright Branch decision
744 6: **else**
745 7: $a_{\text{branch}} \leftarrow \text{CONTINUE}$
746 8: **end if**
747 9: Update B_{act} , n_{cur} based on a_{branch} and n_{fork}^*

748 **2. Node Update**

749 10: Create new node n_{new} as child of n_{cur}
750 11: $s_{\text{new}} \leftarrow S_{\text{node}}(n_{\text{new}})$ \triangleright Summarize new node
751 12: $n_{\text{cur}} \leftarrow n_{\text{new}}$

752 **3. Context Construction**

753 13: $C_{\text{path}} \leftarrow \{c_i \mid n_i \in \text{Path}(n_{\text{cur}})\}$ \triangleright Content of active path
754 14: $C_{\text{inactive}} \leftarrow \{S(B_j) \mid B_j \neq B_{\text{act}}\} \cup \{S(T_k) \mid T_k \neq T_{\text{act}}\}$ \triangleright Summaries of inactive parts
755 15: $C_{t+1} \leftarrow \text{Concat}(C_{\text{path}}, C_{\text{inactive}})$
16: **return** C_{t+1}

756 B.3 MODEL IMPLEMENTATION DETAILS
757758 This section provides the specific prompts used to guide the lightweight language models for
759 decision-making and summarization within the Context-Agent framework.760 **Prompt for Topic Decision** The following prompt is used to instruct the topic decision model Ψ
761 to analyze the user's query against the summaries of existing topic trees. The model must determine
762 whether the query initiates a new topic, continues the current one, or switches to a previous one.
763

```

764
765 # STRICT INSTRUCTION - EXECUTE ONLY THE FOLLOWING LOGIC CHAIN
766 Act as a dialogue topic consistency adjudicator. Your task is to objectively score the
767 semantic relationship between a new query from user and conversation history summary of
768 dialogues between user and AI assistant. You MUST perform exactly three steps:
769 1. [Theme Check] Does the new query discuss the SAME physical/conceptual core object as
770 history?
771 Valid: "battery life" → "charging speed" (core object = battery)
772 Invalid: "Beijing weather" → "Shanghai weather" (core object changed)
773 Rule: Disregard surface differences (tools/locations/times).
774 e.g., "Python data cleaning" vs "Excel data cleaning" → Invalid
775
776 2. [Continuity Check] Does the new query depend on historical context?
777 Valid: "How fast does it charge?" (refers to prior "battery")
778 Invalid: "Recommend restaurants" (no contextual link)
779 Rule: Specially verify pronouns (it/this/that/them etc.), probing words (how/why), some
780 specific signpost words (such as "return to", "previously mentioned", etc.), logical
781 progression
782
783 3. [Final Judgment] Output "yes" ONLY if both steps pass, otherwise "no"
784
785 # ANTI-ERROR PROTOCOLS (Critical for lightweight LLMs)
786 ABSOLUTELY PROHIBITED:
787 • No keyword matching (e.g., "weather" in different cities)
788 • No intent speculation (textual content only)
789
790 Core Object Definition (Key innovation):
791 - Physical: Devices/items/body parts (iPhone battery, car engine)
792 - Conceptual: Problems/tasks/themes (data cleaning, travel planning)
793 - Critical: Core object changes when tools/locations shift
794
795 # EXTENDED EXAMPLE BANK
796 | History Summary | New Query | Theme | Continuity | Output |
797 |-----|-----|-----|-----|-----|
798 | "iPhone 15 battery life" | "Charging speed?" | Yes | Yes | yes |
799 | "Beijing weather today" | "Shanghai temperature?" | No | No | no |
800 | "Python Pandas cleaning" | "Excel missing values" | No | No | no |
801 | "Avatar movie effects" | "Cameron's next film?" | Yes | Yes | yes |
802 | "Diabetes diet tips" | "Exercise recommendations" | Yes | Yes | yes |
803 | "Laptop overheating" | "Phone thermal issues" | No | No | no |
804
805 # OUTPUT REQUIREMENTS
806 Only output SINGLE word: yes or no WITHOUT any extra characters (no spaces/punctuation)
807
808 # CURRENT INPUT
809 Now, please start comparing the history summary and the new query:
History Summary: {summary}
New Query: {query}

```

810 **Prompt for Branch Decision** The branch decision model Φ is prompted to evaluate the user's
 811 query in the context of the current dialogue path and the most relevant historical nodes. The model
 812 must decide whether to continue the current branch, create a new branch, or switch to an existing
 813 one.

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  / # Role and Task
  | You are a Dialogue Flow Controller. Your core task is to analyze the user's query and
  | conversational context to determine their navigational intent. You MUST output ONLY a
  | single JSON object as your decision, with no additional content.
  | # Core Decision Rules
  | Decisions must be based on comparing "Retrieved History Nodes" with the "Current Path",
  | following these specific rules:
  | 1. If the user's query is most relevant to a "historical node" (retrieved ancestor node),
  | shows a tendency to diverge from the "Current Path", and the content of the current path
  | provides no substantial help in answering the new query (i.e., the presence or absence
  | of current path content makes no significant difference to the answer) → MUST create a
  | new branch.
  | 2. If the user's new query is highly similar to a historical node in a non-current topic
  | branch, or if the user explicitly expresses a desire to return to a existing topic
  | branch, and providing the context of the previously existing topic branch is obviously
  | helpful for answering this new query. → MUST switch to the branch that the retrieved
  | history node belongs to.
  | 3. If the user's query is a logical continuation of the "last turn in the Current Path"
  | and the current path context helps better answer the new query → continue along the
  | current path.
  | # Input Information
  | ## Existing Branches
  | {existing_branches}
  | ## Current Path Summaries
  | {current_path_json}
  | ## Retrieved History Nodes
  | {rag_results_json}
  | ## New User Query
  | "{user_query}"
  | # Output Requirements
  | Choose one of the following actions and output your decision as a single JSON object
  | with these fields:
  | - CONTINUE: User continues the current topic. Use ONLY when the query is a direct,
  | incremental continuation of the "last turn in the Current Path".
  | → JSON structure: {"action": "CONTINUE", "reason": "[Explanation for continuing]"}
  | - CREATE_BRANCH: User wants to diverge from a past decision point. Must provide the fork
  | node ID (fork_node_id). Use when the user clearly "backtracks" or "pivots" to explore an
  | alternative path from an earlier conversation node (default choice).
  | → JSON structure: {"action": "CREATE_BRANCH", "fork_node_id": "[ID of most relevant
  | historical node]", "reason": "[Explanation for creating new branch]"}
  | - SWITCH_BRANCH: User wants to switch to another existing branch and providing the
  | context of the previously existing topic branch is obviously helpful for answering this
  | new query. Must provide the target branch ID that the retrieved history node belongs to .
  | → JSON structure: {"action": "SWITCH_BRANCH", "target_branch_id": "[Target branch ID]",
  | "reason": "[Explanation for switching]"}
  | # Example References
  | ## Example 1: Create New Branch
  | Query: "I think Beijing is too cold. Let's check out Guangzhou instead."
  | Decision:
  | {"action": "CREATE_BRANCH",
  | "fork_node_id": "(most_relevant_rag_node_id)",
  | "reason": "User rejects the current path ('too cold') and pivots to an alternative
  | ('Guangzhou') from the retrieved node '(most_relevant_rag_node_id)'. Additionally,
  | previous discussions about Beijing travel plans provide no help in formulating a new
  | plan for Guangzhou."}
  | ## Example 2: Continue Current Branch
  | Query: "Okay, besides the Palace Museum, what other historical sites do you recommend in
  | Beijing?"
  | Decision:
  | {"action": "CONTINUE",
  | "reason": "The query is a direct continuation of the current topic (Beijing
  | attractions.)"}
  | ## Example 3: Switch to Existing Branch
  | Query: "Let's pause on Beijing for now and go back to the Shanghai plan we discussed."
  | Decision:
  | {"action": "SWITCH_BRANCH",
  | "target_branch_id": "branch_xyz",
  | "reason": "User explicitly requests to resume another existing branch ('Shanghai plan').
  | The previous discussion about Shanghai is obviously helpful for answering the new
  | query."}
  | Please output the final decision as a JSON object based on the provided context.

```

864 **Prompt for Node Summarization** The node summarization model S_{node} is prompted to generate
 865 concise summaries of dialogue nodes. The prompt emphasizes the need for brevity and relevance,
 866 ensuring that the summaries capture the essence of each node for effective context management.
 867

```

868     # Role and Goal
869     You are a conversation summary generator. Your sole task is to compress a single
870     conversation between [USER] and [ASSISTANT] into the following format. This object will
871     be used by another language model to quickly understand the context of past
872     interactions. You only need to output the content of summary_for_llm, with no other
873     content whatsoever.
874     # Output Format
875     summary_for_llm: (string) An information-concentrated summary designed for AI, written
876     in the third person. This summary must integrate the user's intention and the LLM's
877     actions into a single declarative sentence. This is the most critical field for
878     providing context to downstream LLMs. If specific numbers are involved, the summary must
879     include important data.
880     # Example
881     ## Input Conversation:
882     [USER]:
883     I'm trying to understand the difference between 'git merge' and 'git rebase'. Can you
884     explain it to me in simple terms, maybe with an analogy?
885
886     [ASSISTANT]:
887     Certainly. You can think of a project's history as a storybook.
888     - **`git merge`** is like connecting two separate story chapters (branches) with a new
889     page that says, "At this point, the stories from Chapter A and Chapter B merge." It
890     creates a new "merge commit" and preserves the exact history of both branches, resulting
891     in a history graph that looks like a diamond or a fork.
892     - **`git rebase`** is like taking all the pages of your Chapter B and placing them one
893     by one at the end of Chapter A. It rewrites the history of your branch to make it look
894     as if all your work was done in a straight line. This creates a cleaner, linear history.
895     In short, `merge` preserves history, while `rebase` rewrites history for the sake of
896     linearity. For team collaboration, `merge` is usually safer.
897
898     ## Expected Output:
899     summary_for_llm: "The user asked about the difference between 'git merge' and 'git
900     rebase', and the AI assistant clarified their respective functions and different impacts
901     on commit history by providing definitions and analogies."
902
903     # Task
904     Now, please analyze the following conversation:
905     [USER]:
906     {user_message}
907     [ASSISTANT]:
908     {assistant_message}
909
910
911
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```

918 B.4 NTM BENCHMARK DETAILS
919920 The Non-linear Task Multiturn Dialogue (NTM) benchmark is designed to evaluate the performance
921 of dialogue systems in handling complex, multi-turn conversations with dynamic topic shifts and
922 instruction refinements. Below are the details of the NTM benchmark.
923924 B.4.1 HUMAN ANNOTATION GUIDELINES
925926 To ensure the quality and consistency of the NTM benchmark, human annotators reviewed, polished,
927 and filtered the generated dialogues based on the following primary criteria:
928

- **Coherence and Naturalness:** The dialogue must flow logically and feel natural, avoiding robotic or repetitive responses. Topic shifts, a key feature of the benchmark, must be contextually plausible and not feel abrupt or random. The overall conversation should mimic the ebb and flow of genuine human interaction, including clarifications, refinements, and relevant digressions.
- **Task Complexity:** Each dialogue must build towards a clear, non-trivial final task. Successfully completing this task should require the model to synthesize and integrate information scattered across multiple turns, including handling user refinements and instruction changes. Simple, single-turn information retrieval is insufficient; the task must test long-range reasoning and memory.
- **Clarity and Objectivity of Checkpoints:** To facilitate objective and reproducible evaluation, the final task must be decomposable into a set of clear, unambiguous, and verifiable checkpoints. Each checkpoint should correspond to a specific sub-goal of the user’s final request and be answerable with a simple “yes” or “no”, minimizing subjective judgment during evaluation.

942 B.4.2 THE DETAILED TOPIC TREES
943944 In the previous Figure 3 in Section 4, we provided a dialogue example. To more intuitively
945 demonstrate the formation of the dialogue tree, we have visualized the dialogue example shown in
946 Figure 3 into a tree structure.
947948 Showed in Figure 5, the dialogue starts with planning a family trip. In the first turn, the user
949 introduces the plan and suggests several potential destinations, which sets a potential fork point for
950 the future exploration of different destinations. Then the user and the assistant discuss the details
951 of the Hokkaido itinerary, including child-friendly attractions. However, in turn 4, the user shifts
952 the topic to Thailand due to concerns about the cold weather in Hokkaido. This shift is still within
953 the topic of trip planning but introduces a new destination. And it is totally different from the
954 previous discussing about Japan. The history of the first three turns is not so useful for the following
955 discussion about Thailand.956 Therefore, the Context-Agent creates a new topic tree for Thailand, starting a new branch from turn
957 4. The user then explores two potential locations in Thailand: Phuket and Chiang Mai, requesting
958 different types of itineraries and activities. This introduces another fork point at turn 5, where the
959 user asks for two distinct itinerary options for Phuket.
960961 In turn 7, the user raises a concern about the safety of international flights, which is totally different
962 from the previous topic of trip planning. This prompts the Context-Agent to create another new
963 topic tree for flight safety, starting a new tree from turn 7. The user and assistant discuss various
964 aspects of flying, including aircraft types and comfort.
965966 Then in turn 9, the user returns to the Phuket itinerary, indicating a switch back to the previous topic
967 tree about Thailand. The Context-Agent recognizes this and switches the active topic tree back to
968 Thailand. The user continues to refine their preferences for the Phuket itinerary, expressing a desire
969 for a more relaxing experience without snorkeling. Nevertheless, in turn 10, the user again shifts
970 the focus to Chiang Mai, asking about arranging a beach resort stay there. This indicates another
971 switch within the Thailand topic tree. And in turn 14, the user refines their food preferences due to a
972 seafood allergy. Finally, in turn 15, the user makes a final decision to go to Phuket but changes their
973 mind about snorkeling and requests a comprehensive travel memorandum that synthesizes all the
974 discussed information, including destination overview, budget planning, recommended experiences,
975 local food suggestions, and visa information.
976

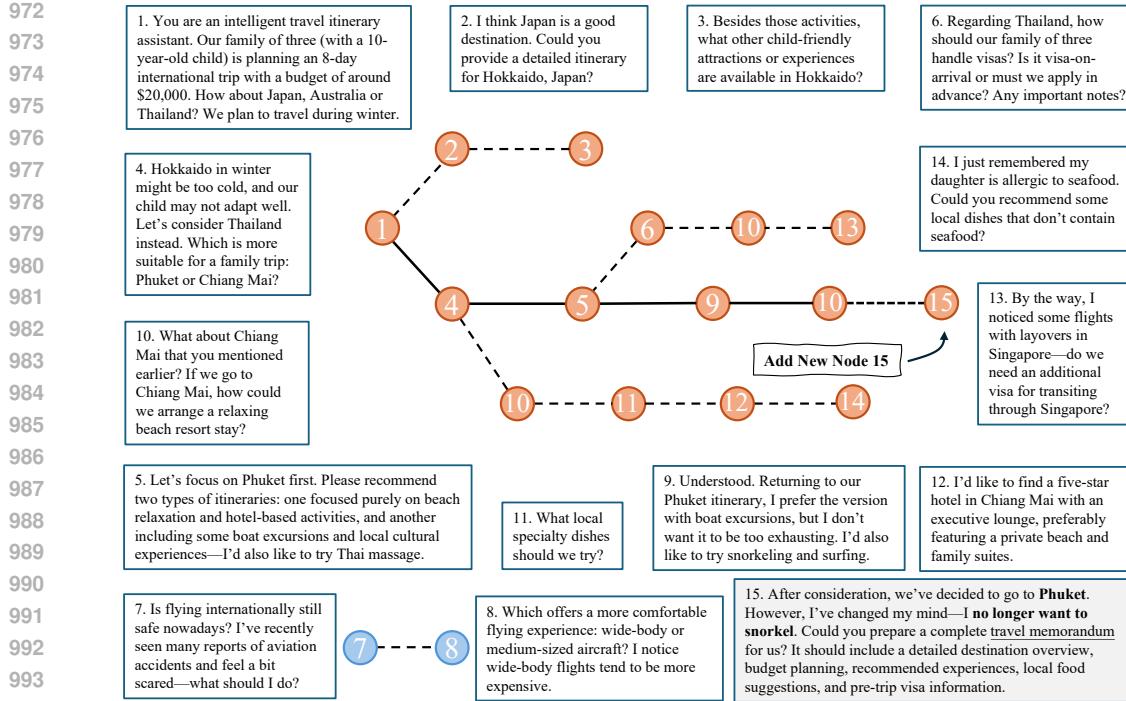


Figure 5: The topic tree structure corresponding to the dialogue example in Figure 3. Each node represents a turn in the dialogue, with branches indicating topic shifts and refinements. The solid edges represent the active path, while the dashed edges represent inactive branches.

B.4.3 EXAMPLE FROM “CODING SUPPORT” DOMAIN

This example illustrates a typical dialogue from the NTM benchmark’s coding support domain, featuring topic shifts and instruction refinements.

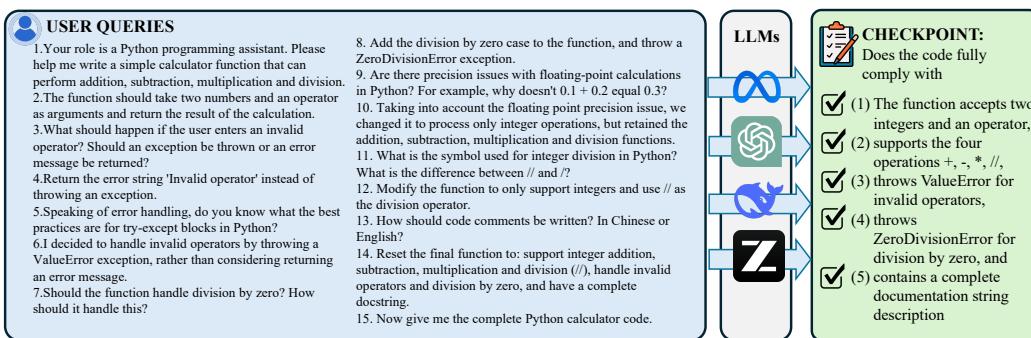


Figure 6: An example of a 15-turn dialogue from the NTM benchmark in the coding support domain. The dialogue features multiple topic shifts and instruction refinements, culminating in a clear task of generating a Python calculator function.

As shown in Figure 6, the dialogue begins with a request for a basic calculator. The user iteratively refines the requirements—adding error handling and changing data types from floats to integers—while also digressing to discuss ‘try-except’ best practices and commenting conventions. Finally, the user consolidates all refinements into a final request for the complete code. This example highlights the benchmark’s focus on testing a model’s ability to handle instruction changes, topic shifts, and integrate information from a non-linear dialogue history.