# INTERLEAVING OPTIMIZERS FOR DNN TRAINING

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Paper under double-blind review

### ABSTRACT

Optimizers are crucial in deep neural network (DNN) training, affecting model quality and convergence. Researchers have found that different optimizers often suit different problems or different stages of a problem. Hence, some studies have tried to combine different optimizers to better train DNNs. However, existing methods are limited to simple optimizer switch strategies, which leads to unstable model quality and slow convergence. In this paper, we propose a fine-grain optimizer switch method called Interleaving Optimizer for Model Training (IOMT), which automatically switches to the appropriate optimizer among different optimizer types based on the training stage information, achieving faster convergence and higher test accuracy. IOMT employs surrogate models to estimate the performance of different optimizers during training and is supported by a transferability assessment to predict the training cost. By combining the transferability assessment, performance estimation, and training process information with an acquisition function, IOMT calculates the optimization gain of each optimizer and switches the optimizer with the largest gain for the next training stage. The experimental results on full training and fine-tuning demonstrate that IOMT achieves faster convergence (e.g., 10% on the *stl10* dataset) and better performance (e.g., 3% accuracy improvement on the *cifar10* dataset) compared to existing methods.

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# 1 INTRODUCTION

The choice of optimizer and its hyperparameter settings (e.g., the learning rate) profoundly impacts the model quality and 031 convergence speed in deep neural networks (DNNs) (Soy-032 daner, 2020; Hassan et al., 2023). Researchers typically use a 033 single optimizer for the entire training (i.e., a coarse-grain op-034 timizer setting) and have some empirical preferences for optimizer selection, such as using SGD for head fine-tuning (Poo-035 jary & Pai, 2019) and Adam for LoRA (Hu et al., 2021). However, recent studies find that different optimizers are not only 037 suited to specific tasks but also exhibit unique characteristics and optimization strategies at different stages of a training (Im et al., 2016). Figure 1 presents the optimization results of 040 three optimizers with varying runs (i.e., 200 times with dif-041 ferent random seeds and hyperparameter settings) on four de-042 terministic functions (rosenbrock, himmelblau, griewank and 043 ackley). Different optimizers follow distinct paths in the same 044 start point even with varying runs, making it difficult to definitively identify the "one size fits all" optimizer. 045



Figure 1: The different training processes with various optimizers.

To address such challenges of coarse-grain optimizer tuning, some studies have attempted to combine the benefits of different optimizers during a single training process recently. SWATS (Keskar & Socher, 2017) achieved better generalization by switching from Adam to SGD. Chen et al. proposed a partially adaptive momentum estimation method, which unifies the adaptive gradient methods (i.e., Adam or Amsgrad) with SGD by introducing a partial adaptive parameter (Chen et al., 2018). AdaBound (Luo et al., 2019) employed dynamic bounds on learning rates to achieve a gradual and smooth transition from adaptive methods to SGD. However, these approaches remain limited in the optimizer types (i.e., only two kinds of optimizers) and combining methods (i.e., source strategy), which leads to unstable model quality and high training cost (Sun, 2020).

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054 Based on the idea that "different optimizers suit for different parameter states", we propose a fine-055 grain optimizer switch method called Interleaving Optimizer for Model Training (IOMT). During 056 the training, IOMT constructs surrogate models for different optimizers to predict their optimiza-057 tion benefits under various model parameter states. To better assess the benefits of the optimizers 058 (i.e., potential loss reduction and convergence speed), IOMT calculates an optimization gain score for each optimizer using the acquisition function that combines the predicted performance, a transferability assessment, and training process information. By carefully switching the optimizer with 060 the highest score during training, IOMT achieves faster convergence and better model quality. To 061 summarize, the key contributions of this paper are as follows. 062

- We investigate the distinct strengths and optimization directions of various optimizers across different tasks and parameter states. Furthermore, we demonstrate that combining different optimizers during training can help achieve higher-quality models and better convergence.
- We present a novel fine-grain optimizer switch method called Interleaving Optimizer for Model Training (IOMT), which automatically switches suitable optimizers according to the parameter state during training. IOMT estimates the performance of optimizers under different parameter 069 states by constructing Gaussian surrogate models and calculates the optimization gain using the acquisition function. By iteratively selecting the optimizer with the highest gain score, IOMT produces higher-quality models with faster convergence.
  - · We implement IOMT and conduct experiments on multiple models and tasks, including full training and partial fine-tuning. The experimental results demonstrate the advantages of our methods, such as achieving over 1% improvement in predictive accuracy with 10% reduction in convergence time, while also yielding superior generalization models. In addition, the case study and several independent experiments are presented to further explore the performance of IOMT.

#### 2 **RELATED WORKS AND BACKGROUND**

In this section, we provide the background of our work, including the optimizers and the hybrid optimizer methods. After that, we identify the limitations of existing approaches.

		А	dadelta	NAda	m Pa	dam	Ad	amP	
SGD	Mon	ientum R	MSprop Ad	lam 🚺	AdamW	AdaB	ound S.	AM	Adan
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Figure 2: The development of neural network optimizers.

091 **Optimizers.** The optimizers and their hyperparameters are crucial for training DNNs, as they effec-092 tively adjust the model's parameters to minimize the loss function. The traditional gradient descent algorithm calculates the gradient of the loss function with respect to the model's parameters across the entire dataset and updates the parameters in the direction that reduces the loss (Ruder, 2016). 094 Following the gradient descent algorithm, researchers have proposed a variety of optimizers. Fig-095 ure 2 illustrates a portion of the historical development of these optimizers. Instead of calculating the 096 gradient using the entire dataset, the Stochastic Gradient Descent (SGD) approximates the gradient 097 by using only a single sample or a small batch of samples (Robbins & Monro, 1951). To address 098 the slow convergence in ravines, the momentum technique is introduced in SGD (Sutskever et al., 2013). The Nesterov Accelerated Gradient (NAG) further enhances convergence speed and accuracy 100 by incorporating a look-ahead mechanism into the update process (Qu & Li, 2019). Additionally, 101 researchers have explored methods for adaptive learning rates based on different model parame-102 ters, such as RMSProp (Graves, 2013), Adam (Kingma & Ba, 2014), and AdamW (Loshchilov 103 & Hutter, 2017). Beyond these, researchers have also proposed various second-order optimizers, 104 such as L-BFGS (Liu & Nocedal, 1989), K-FAC (Martens & Grosse, 2015), and AdaHessian (Yao 105 et al., 2021)). However, due to their practical application challenges, second-order optimizers are not further discussed in this paper. Additionally, researchers have attempted to develop new neural 106 network-based learned optimizers through a meta-learning approach (Andrychowicz et al., 2016; 107 Harrison et al., 2022).

108 Hybrid optimizer. Like other hyperparameter settings in training, there is no universal optimal op-109 timizer in practical training (Wilson et al., 2017). For instance, SGD with momentum is commonly 110 used in Computer Vision (CV), while Adam is favored for training transformer models in Natural 111 Language Processing (NLP) (Yao et al., 2021). Some researchers have explored the performance 112 of different optimizers during training, noting that different optimizers follow distinct descent paths at different saddle points (Im et al., 2016). Leveraging insights from multiple optimizers during 113 model training is crucial in both academic research and practical applications. While numerous 114 studies have investigated the adjustment of learning rates within optimizers (Gotmare et al., 2018; 115 He et al., 2016; Smith, 2017), research on switching between different optimizers remains limited. 116 Existing studies primarily focus on the basic form of switching, which involves transitioning from 117 one optimizer to another. For example, SWATS (Keskar & Socher, 2017) achieves favorable re-118 sults by initially using Adam and then switching to SGD. Padam (Chen et al., 2018) introduces a 119 partial adaptive parameter to integrate Adam with SGD. Meanwhile, AdaBound (Luo et al., 2019) 120 implements dynamic bounds on learning rates to facilitate a gradual and smooth transition. 121

Limitations of current approaches. (i) Single optimizer: although researchers are continually en-122 hancing existing optimizers to better adapt to model parameter states (e.g., ravines), the associated 123 computational cost cannot be ignored. In practical training, these complex optimizers do not neces-124 sarily outperform basic SGD (Keskar & Socher, 2017). To obtain better models, researchers need 125 to train with different optimizers, which is a time-consuming process. Additionally, consistent op-126 timizer training throughout the entire process (i.e., coarse-grain training) limits both model quality 127 and convergence speed. (ii) Hybrid optimizer: combining the advantages of different optimizers 128 can help improve model quality and convergence speed. Existing methods are limited to adjust-129 ing learning rates or transitioning between two types of optimizers, neglecting the unique strengths of different optimizers under different parameter states. Such a coarse mixing approach not only 130 restricts the stability of the model quality but also impacts convergence speed (Zhuang et al., 2020). 131

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**OUR PROPOSED METHODS: IOMT** 3

135 To better utilize multiple optimizers, we propose a novel fine-grain optimizer switch method called 136 Interleaving Optimiezer for Model Traing (IOMT), which enables adaptive optimizer switching during model training. In this section, we first provide a brief overview of IOMT. Then, we offer a 138 detailed introduction including its problem formulation, surrogate model, and acquisition function.

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## 3.1 OVERVIEW OF OUR PROPOSED IOMT

142 Figure 3 illustrates the workflow of IOMT, and a detailed description of IOMT with its pseu-143 docode is presented in Appendix A. IOMT cal-144 culates the transferability weight  $\omega_t$  to assist in 145 the subsequent selection of optimizers before 146 the training (Step 1). During each optimizer 147 switch cycle (i.e., a few iterations), IOMT first 148 compresses the model parameters  $\theta^i$  to get the 149 input of the surrogate model (Step 2). Then, 150 IOMT selects the appropriated optimizer  $o^i$ 151 for the training of the current stage (Steps 3-152 4). Obtaining the training losses, IOMT calculates the performance score s and updates 153 the corresponding surrogate model  $q^i$  (Steps 5-154 6). By iteratively executing this process, IOMT 155 achieves the fine-grain optimizer switching. 156



Figure 3: The workflow of IOMT.

- 157 For selecting the next optimizer (Step 3), IOMT 158 employs two methods: the weighted random
- 159 selection and recommendation based on the surrogate model. In the initial training stages, IOMT uses the calculated score s to update the sampling weight  $\omega_r$  for randomly selecting optimizers 160
- (Steps 3a and 6a). After acquiring enough training results, IOMT selects the optimizers with the 161 highest gain e calculated by the acquisition function for each training stage (Step 3b).

#### 162 3.2MOTIVATION AND PROBLEM FORMULATION

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164 Before introducing the details of the surrogate model and acquisition function in IOMT, 165 we first provide the hypothesis underlying our 166 method: "different optimizers offer distinct op-167 timization directions and are suited to different 168 parameter states". Figure 4 illustrates four examples of the different optimization directions, 170 which correspond to the subfigures in Figure 1. 171 It can be observed that although the five op-172 timizers provide similar directions at the first 173 iteration, their optimization paths diverge sig-174 nificantly after a few iterations. Previous stud-175 ies have also observed this phenomenon, not-176 ing that optimizers exhibit different optimization directions under varying parameter states 177 from both theoretical and visualization perspec-178 tives (Im et al., 2016). Therefore, we think that



Figure 4: The illustration of different optimizer directions from the same start point.

179 the category of optimizers, like other hyperparameters, requires fine-grain tuning (i.e., dynamic al-180 gorithm configuration) (Adriaensen et al., 2022). 181

Building on this assumption, IOMT attempts to propose a fine-grain optimizer switch method that 182 leverages the strengths of different optimizers for distinct parameter states. Let  $o \in \mathcal{O}, \lambda \in \Lambda$ , and 183  $t \in \mathcal{T}$  denote the optimizer type (e.g., SGD), hyperparameter setting (e.g., learning rate as 0.1) and the training time (e.g., 5 iterations), respectively. Then, the training process with fine-grain optimizer 185 switches can be defined by a list of configurations  $\mathcal{C} = \{c^1, c^2, ..., c^n\}$  where  $c^i = (o^i, \lambda^i, t^i)$ . The objective of IOMT is to find an optimal  $C^*$  that minimizes the following objective function: 187

$$\mathcal{C}^* = \underset{\mathcal{C}\in\mathcal{O}\times\Lambda\times\mathcal{T}}{\arg\min} \mathcal{L}(\boldsymbol{\theta}^0, \mathcal{M}, \mathcal{D}, \mathcal{C})$$
(1)

190 where  $\theta^0$  is the initial model parameter state,  $\mathcal{L}(\cdot)$  denotes the loss of the trained model  $\mathcal{M}$  under 191 dataset  $\mathcal{D}$ . Equation (1) can be interpreted as fine-grain optimizer tuning for neural network training. 192 When all  $c^i \in C$  share the same settings, it aligns with the traditional training process, which is 193 described further in Section 4.1. For clarity, in the following sections, we set all training times  $t \in \mathcal{T}$  to a specific value  $\tau$ , such as 5 iterations. 194

#### 196 3.3 ESTIMATING OPTIMIZATION PERFORMANCE WITH SURROGATE MODELS

IOMT employs a Sequential Model-Based Optimization (SMBO) to address this fine-grain optimizer tuning problem, as illustrated in Figure 5. Initially, IOMT trains the model  $\mathcal{M}$  using random configurations to obtain training experience (the blue block). Next, IOMT constructs surrogate mod-200 els  $\mathcal{G} = \{g_1, g_2, ..., g_m\}$  for each optimizer type  $o_i \in \mathcal{O} = \{o_1, o_2, ..., o_m\}$  to guide the selection of suitable configurations (the red block). By iteratively selecting training configurations and up-202 dating surrogate models, IOMT achieves a fine-grain optimizer switch training. In this section, we 203 introduce IOMT's surrogate model through its selection, input, output, and initialization. 204



Figure 5: The training process of our proposed IOMT.

The selection of the surrogate model. IOMT utilizes the Gaussian process (GP) model (Schulz 215 et al., 2018) as its surrogate model for several reasons. First, compared to other machine learning

216 models, GPs can efficiently train and continuously update the surrogated model as the training pro-217 gresses. Second, GPs provide uncertainty estimation for predictions (i.e., the variance information), 218 which is useful for guiding the optimizer selection (as detailed in Section 3.4). Thirdly, as a pow-219 erful probabilistic model, GPs effectively construct the overall distribution based on known points, 220 offering good flexibility and interpretability.

221 The input of the surrogate model. At the beginning of each optimizer cycle, IOMT acquires the 222 input for the surrogate model  $VEC^{i}$ . The traditional surrogate model in SMBO uses the hyperparam-223 eter  $\lambda^i$  as its inputs. In IOMT, the input VEC<sup>i</sup> also includes a vector representing the parameter state 224  $\theta^i$  to learn the impact under different parameter states. Considering the high cost of using the full 225 model parameters, IOMT applies feature engineering to reduce the input size. Specifically, IOMT 226 uses Principal Component Analysis (PCA) (Labrín & Urdinez, 2020) to compress the parameters layer by layer, lowering the training cost for the surrogate model. To further reduce the training cost 227 of surrogate models during training, IOMT selects only a few layers of the model as inputs for the 228 surrogate model (e.g., the classifier layer with a few hidden layers). In the case of partial fine-tuning, 229 IOMT focuses solely on the trainable parameters (e.g., the matrices A and B in LoRA). 230

231 The output of the surrogate model. In contrast to the results obtained from training to conver-232 gence, IOMT emphasizes the "short-term" benefits each optimizer can achieve given the current 233 parameter state. Therefore, the output of IOMT's surrogate model does not use the final loss or accuracy, but instead employs a computed performance score  $s \in [-1, 1]$ . During the training 234 of a stage, IOMT performs multiple iterations of training, resulting in a set of losses, denoted as 235  $l = \{l_1, l_2, ..., l_{\tau}\}$ , and  $l_0$  represents the loss before training. IOMT first calculates the loss vari-236 ation  $\Delta l_i = \frac{l_{i-1}-l_i}{\max(l_i,l_{i-1})}$  for each iteration to get the average reduction  $\mu_{\Delta}$  and variance  $\sigma_{\Delta}$ . To 237 estimate the optimization performance of different configurations, IOMT combines the considera-238 tions of exploration (i.e., variance  $\sigma_{\Delta}$ ) and exploitation (i.e., mean  $\mu_{\Delta}$ ) to calculate a weighted score 239  $s = \mu_{\Delta} + \alpha \sigma_{\Delta}$ . However, such a weighted score overlooks the direction of variance. For instance, in 240 Figure 6(a), optimizers  $o_1$  and  $o_3$  have the same mean  $\mu_{\Delta}$  and variance  $\sigma_{\Delta}$ , yet  $o_3$  achieves a lower 241 loss than  $o_1$  during training. A similar issue arises in the comparison between  $o_2$  with  $o_1$  and  $o_3$ . 242 To address this problem, we incorporate boundary considerations into the performance calculation, 243 including the upper bound  $\Delta_{\text{UPPER}} = \frac{l_0 - \max(l)}{\max(l_0, \max(l)) \times \tau}$  and lower bound  $\Delta_{\text{LOWER}} = \frac{l_0 - \min(l)}{\max(l_0, \min(l)) \times \tau}$ . 244 Then, the final optimization performance score is defined as follows, 245

$$s = \tanh(\frac{1}{3}(\mu_{\Delta} + \Delta_{\text{UPPER}} + \Delta_{\text{LOWER}}) + \alpha\sigma_{\Delta})$$
(2)

where  $\alpha$  represents the weight for variance.



269 Figure 6: Examples of the optimization gain.

The initial weighted random selection. To obtain enough training experience for the construction of surrogate models, IOMT trains with random configurations at the start of training. Though randomly selecting configurations for initial training can yield the necessary experience, IOMT employs a weighted random initialization method to enhance the performance of the initial training. Specifically, IOMT maintains a sampling weight  $\omega_r[j] \in [0,1]$ for each type of optimizer  $o_i$  and its surrogate model  $q_i$ , presenting the probability of being sampled. This sampling weight is initially assigned a value of 1 to achieve a random initialization. After completing the training with the current configuration, the sampling weight for the corresponding optimizer  $\omega_i$  is updated to the normalized optimization performance score as shown in Equation (3), where  $\omega_{\min}$  represents the minimal threshold.

$$\boldsymbol{\omega}_{r}[j] = \max(\frac{1}{2}(s+1), \boldsymbol{\omega}_{\min}). \tag{3}$$

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# 270 3.4 SELECTING OPTIMIZERS WITH ACQUISITION FUNCTION271

Although the calculated optimization performance *s* can be used to select configurations directly, given the volatility of the loss and the complexity of model training, IOMT considers additional factors in the design of acquisition, including variance, transferability, and the training process. In this section, we introduce considerations designed for the acquisition function used in IOMT.

**Consideration of variance.** Benefiting from the advantages of the Gaussian process model, the surrogate model can provide both the mean score  $s_{\mu}$  and an estimate of the variance  $s_{\sigma}$ . Similar to traditional hyperparameter optimization methods, IOMT also incorporates a trade-off between exploration and exploitation in the acquisition function as follows

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$$\operatorname{ACQ}(s_{\mu}, s_{\sigma}) = s_{\mu} + \alpha s_{\sigma}, \tag{4}$$

where  $\alpha$  represents the weight for variance, consistent with the definition in Equation (2).

**Consideration of transferability.** The training cost of DNNs is closely related to the initial model parameter state  $\theta^0$ . In fine-tuning, closely related upstream and downstream tasks (i.e., high transferability between the pre-trained model and the new task) are easier to train than those that are dissimilar. Considering the idea that "a pre-trained model with lower transferability necessitates more substantial tuning adjustments", we use the model's transferability  $\omega_t$  as the weight of the variance in the acquisition function, as shown in the following equation,

$$\operatorname{ACQ}(s_{\mu}, s_{\sigma}, \omega_t) = s_{\mu} + (1 - \omega_t) s_{\sigma}.$$
(5)

The transferability  $\omega_t$  is calculated using two types of evaluation metrics, including performancebased metric  $\omega_p$  and distribution-based metrics  $\omega_d$ . Firstly, the performance-based metric  $\omega_p \in [0, 1]$ is the testing result (e.g., accuracy) which is directly tested with the pre-trained model without deep refining. Meanwhile, IOMT also uses some feature-based metrics, which analyze the distribution of the output vectors or labels, to estimate the model's transferability, including LogME (You et al., 2021) and Leep (Nguyen et al., 2020). Equation (6) presents the definition of transferability weight.

$$\omega_t = \beta \omega_p + (1 - \beta) \frac{1}{k} \sum_{i=1}^k \operatorname{sigmoid}(\omega_d^i).$$
(6)

where  $\omega_d^i$  represents k distribution-based metrics and  $\beta$  represents the weight for two kinds of metrics. We use the sigmoid function to constrain the distribution-based metric within the range of [0, 1] to align with the performance-based metric. Then, the weighted sum reflects the transferability of the initial model for current tasks. A higher transferability weight indicates higher transferability, while a lower one suggests lower transferability.

**Consideration of training process.** Additionally, IOMT takes into account the differing needs in 305 the early and later stages of training, specifically that "after the model becomes stable, smaller tuning 306 adjustments are needed." As training progresses, the model continuously captures the knowledge 307 required for the current task, leading to a stabilization of the training loss. At the later stages of the 308 training, the target position on the parameter surface is constrained within a smaller range. In this 309 context, optimizers with larger amplitudes may disrupt the tuning process. Therefore, the proportion 310 of variance in the acquisition function should be reduced. Hence, we introduce a periodic halving of 311 the weight for variance information in IOMT as Equation (7), where *i* represents the current iteration 312 and *n* represents the halving period. 313

 $e = \operatorname{sigmoid}(s_{\mu} + (1 - 2^{-\lfloor i/n \rfloor} \cdot \omega_t) s_{\sigma}).$ <sup>(7)</sup>

## 4 DISCUSSION

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To further introduce our proposed IOMT, we discuss its differences from the hyperparameter tuning (HPO) and SMBO, along with its advantages and limitations in this section.

- 320 321 322
- 4.1 ANALYZING THE DIFFERENCES BETWEEN IOMT AND HPO
- **Compare with HPO.** The optimizer, as one of the hyperparameters in DNNs, its automatic adjustment is a form of HPO and AutoML. However, the vanilla training addresses it as a coarse-grain

324 HPO, where the hyperparameters remain fixed throughout the whole training process. The optimiza-325 tion objective of such coarse-grain tuning can be formulated as below, 326

$$c^* = \underset{c \in \mathcal{O} \times \Lambda \times \mathcal{T}}{\arg \min} \mathcal{L}(\boldsymbol{\theta}^0, \mathcal{D}, c)$$
(8)

where  $c = (o, \lambda, t)$  represents the hyperparameter configurations (same as the defination in Section 3.2). Compared to IOMT's fine-grain tuning (i.e., Equation 1), the vanilla HPO restricts the 330 way model parameters are updated and the collaboration among different optimizers. Additionally, though researchers have proposed hybrid methods that combine binary optimizers, these approaches 332 still integrate the optimizers from rules of thumb rather than performing fine-grain hyperparameter optimization. For example, SWATS (Keskar & Socher, 2017) switches the training from Adam to 334 SGD based on the foundation that "Adam quickly adapts to problems in the early training phase, 335 while SGD promotes better generalization in the later stages". 336

Compare with SMBO. IOMT adopts the idea of surrogate models and the acquisition function 337 in SMBO, but there are significant differences between IOMT and SMBO. First, the SMBO only 338 considers the impact of hyperparameters on the results, neglecting changes in the model parameter 339 states. When the initial parameter states differ, the performance evaluation of hyperparameters is 340 also different. In contrast, IOMT introduces additional parameter inputs to the surrogate model 341 and considers the training progress in the acquisition function to study the "short-term" gain on 342 different parameter states. Secondly, SMBO aims to select the best hyperparameters (i.e., coarse-343 grain tuning), whereas IOMT aims to obtain the best model (i.e., fine-grain tuning). Compared to 344 SMBO, IOMT enables the collaboration of various hyperparameters within a single training process.

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#### 346 4.2 ANALYZING THE ADVANTAGES OF IOMT

Accuracy: IOMT achieves a DNN training with in-348 terleaving optimizers, enabling collaboration among 349 multiple optimizers. This fine-grain optimizer tun-350 ing not only integrates the optimization strategies of 351 different optimizers but may also yield an optimiza-352 tion path (i.e., the final trained model) that a single 353 optimizer cannot achieve, resulting in higher accu-354 racy. Figure 7(a) provides examples across three dif-355 ferent functions, illustrating that IOMT can discover 356 optimization paths that a single optimizer cannot 357 achieve. Similarly, the final model weights obtained 358 from training for the same number of epochs on the *cifar10* dataset using different optimizers show 359 significant differences, as illustrated in Figure 7(b). 360 This hybrid approach, which employs multiple opti-361 mizers, expands the search space of traditional train-362 ing, leading to an improved accuracy upper bound. 363



Figure 7: Analyze of interleaving training.

**Training efficiency:** We analyze the time cost of IOMT using the training of ResNet18 (whose 364 training FLOPs  $t_M \approx 1.8 \times 10^9$ ) on the *cifar10* dataset (i.e., feature dimensions  $D \approx 3 \times 10^3$ , instance number  $N = 6 \times 10^4$ , and class number K = 10) with epoch number  $n_{\text{EPOCH}} = 100$ , batch 366 size  $n_{\rm BZ} = 64$  and switching iteration number  $\tau = 20$  as an example. For the vanilla training, the 367 time cost for a single epoch is  $t_{\text{TRAIN}} \approx 2 \times t_M \times N \approx 2 \times 10^{14}$ . Compared to vanilla training, IOMT 368 incurs additional time consumption due to two processes: transferability assessment before training 369  $t_{\rm EST}$  and the updating of the surrogate model during the training process. First, the  $t_{\rm EST}$  includes 370 the computation for two distribution-based metrics (i.e., LEEP and LogME) and one performance-371 based metric. Among them, the time cost for the LEEP and performance-based metrics is equivalent 372 to a single forward pass (Nguyen et al., 2020), while the computational complexity of LogME is 373  $O(KD^2 + NKD + D^3 + ND^2) \approx 3 \times 10^{10}$  (You et al., 2021). Then, the transferability assessment 374 time  $t_{\text{EST}} \approx t_{\text{TRAIN}}$  (actually smaller in practical, e.g.,  $t_{\text{EST}} = t_{\text{TRAIN}} \times 1\%$ ). Second, the additional 375 time consumption from the updating of the surrogate model  $t_{SUR}$  includes the PCA compression of the selected parameters and the updating of the Gaussian process model. The time complexity of 376 compression and updating is  $O(W^2D')$  and  $O(N_{sw}^3)$ , where  $W \approx 10^4$  represents the number of 377 selected parameters (i.e., only the last layer),  $D' \approx 100$  represents the number of PCA components,

	us	ps	mr	nist	stl10		cifar10	
method	ResNet18	ViT	ResNet18	ViT	ResNet18	ViT	ResNet18	
SGD	$96.10 \pm 0.24$	$97.46{\scriptstyle \pm 0.70}$	99.29±0.03	$99.50{\scriptstyle \pm 0.04}$	86.94±0.49	$97.83{\scriptstyle\pm0.22}$	80.73±0.43	97.
SGDM	$95.83 \pm 0.30$	$97.68{\scriptstyle\pm0.11}$	$99.47 \pm 0.05$	$99.65{\scriptstyle \pm 0.04}$	86.99±0.36	$96.61{\scriptstyle \pm 0.04}$	81.64±0.60	97.
Adagrad	$96.00{\scriptstyle\pm0.94}$	$93.40{\scriptstyle\pm0.04}$	$99.40 \pm 0.06$	$98.24{\scriptstyle \pm 0.50}$	83.38±7.99	$78.66{\scriptstyle \pm 2.54}$	$80.57 \pm 0.14$	60.
RMSprop	$95.30 \pm 0.55$	$95.25{\scriptstyle\pm0.04}$	$99.13 \pm 0.17$	$98.14{\scriptstyle \pm 0.09}$	69.91±2.06	$88.62 \pm 4.45$	$71.92 \pm 0.41$	78.
Adam	$95.13 \pm 0.53$	$93.26{\scriptstyle \pm 0.78}$	99.11±0.06	$99.01{\scriptstyle\pm0.08}$	$76.49_{\pm 2.04}$	$82.26{\scriptstyle\pm1.16}$	$72.33 \pm 0.84$	75.
<u>Ś</u> ŴATŚ	$95.53 \pm 0.71$	$94.00_{\pm 1.23}$	$99.17_{\pm 0.11}$	$98.73_{\pm 0.13}$	$79.76 \pm 2.11$	$88.03 \pm 0.44$	$75.17_{\pm 0.21}$	66.
Padam	$96.10 \pm 0.15$	$97.58{\scriptstyle\pm0.11}$	$99.46 \pm 0.02$	$99.66{\scriptstyle \pm 0.04}$	$85.64 \pm 0.48$	$90.81{\scriptstyle \pm 0.06}$	$81.58 \pm 0.38$	96.
AdaBound	95.02±0.17	$87.64{\scriptstyle \pm 0.84}$	$99.25 \pm 0.06$	$97.54{\scriptstyle \pm 0.13}$	$84.48 \pm 0.42$	$86.33{\scriptstyle \pm 2.39}$	69.27±5.02	70.
ours	96.81±0.21	$97.81{\scriptstyle \pm 0.21}$	99.51±0.01	$99.71{\scriptstyle \pm 0.02}$	88.23±0.23	98.21±0.19	$84.14{\scriptstyle \pm 0.11}$	98.

Table 1: Test accuracy (%) of the full training with different optimizers.

and  $N_{sw} = n_{\text{EPOCH}} \frac{N}{\tau \times n_{\text{BZ}}} \approx 5 \times 10^3$  represents the total switching operations in the tuning process. Then, we can calculate  $t_{\text{SUR}} \approx 10^9 \ll t_{\text{TRAIN}}$ . Since  $t_{\text{EST}}$  is executed only once before training and  $t_{\text{SUR}} \ll t_{\text{TRAIN}}$ , the additional time in IOMT is minimal. Furthermore, thanks to its adaptability to different parameter states, IOMT is able to achieve better convergence speed.

## 5 EXPERIMENTAL STUDY

To investigate the rationality of IOMT, we conducted experiments and present the experimental results in this section. We first exhibit two overall experiments to observe the performance of IOMT in full training and PEFT. Then, we illustrate a case study to observe the practical switching process of IOMT during training. In addition, several independent experiments are presented to investigate the significance of designs within IOMT.

404 In the experiments, we used 4 ImageNet pre-trained models available from PyTorch (Paszke et al., 405 2019) (i.e., ResNet18, ResNet152, MobileNet V2, and ViT) and 2 pre-trained NLP models from 406 HuggingFace (Wolf et al., 2020) (i.e., RoBerta and LLaMA-7B). For the selection of datasets, we 407 took 4 commonly used CV datasets from PyTorch (i.e., usps, mnist, stl10, and cifar10) and 3 NLP 408 tasks from Hugging Face (i.e., mrpc, qqp, and wnli). In addition, the experiments were conducted 409 on a Linux machine with a 128-core 2.6GHz Intel(R) Xeon(R) Platinum 8358 CPU and 512GB main memory. More details of the models and datasets used in our experiments can be found in 410 Appendix B. 411

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## 413 5.1 OVERALL PERFORMANCE OF IOMT

We first compared our proposed IOMT with the 415 training using a single optimizer or hybrid op-416 timizers under full training and PEFT. Specifi-417 cally, five commonly used optimizers were tested 418 for single optimizer training: SGD (Robbins & 419 Monro, 1951), SGDM (Sutskever et al., 2013), Ada-420 grad (Duchi et al., 2011), RMSProp (Graves, 2013), 421 and Adam (Kingma & Ba, 2014). For hybrid op-422 timizer training, we included SWATS (Keskar & 423 Socher, 2017), Padam (Chen et al., 2018), and AdaBound (Luo et al., 2019). The initial learning rate 424 and training epochs of each method were setting as 425 [0.1,0.01,0.001] and 100. For IOMT, we set the ini-426 tial steps  $n_{ini} = 50$  and training time  $\tau = 25$  itera-427 tions. More details of the baselines and settings are 428 presented in Appendix C. 429

430 **Experiments on full training.** The experimental re-431 sults show that the switching method proposed in IOMT can always achieve good improvements in



Figure 8: The training loss and test accuracy line graph.

test accuracy (i.e., 1%-3%), as shown in Table 1. However, other hybrid methods often perform
worse than training with a single optimizer, especially in complex tasks (i.e., *stl10* and *cifar10*datasets). Additionally, compared to other methods, IOMT exhibits smaller variance, indicating
more stable performance outputs. To illustrate the convergence of IOMT, we present the training
loss and test accuracy of each method in the Figure 8. For ease of observation, the baselines with
significant fluctuations are not displayed in the figure. It can be observed that IOMT shows a faster
convergence speed compared to the vanilla method.

439 **Experiments on PEFT.** In addition to the full training, we also compared the proposed IOMT with 440 baselines on the PEFT that only update partial of the model parameters, including the head fine-441 tuning (Poojary & Pai, 2019) in CV problems and the LoRA (Hu et al., 2021) in NLP tasks. To 442 analyze the convergence performance, we terminated the training when the convergence conditions were satisfied, i.e., the change of loss is less than  $1 \times 10^{-4}$  in 10 consecutive epochs or the train-443 ing reaches 100 epochs. Table 2 presents a partial of the experimental results, more experimental 444 results and setting details can be found in the Appendix C. Like its performance in full training, 445 IOMT achieves higher accuracy and  $F_1$  score (up to 2%) for both CV and NLP tasks. In terms of 446 convergence time, the end-to-end results shown in the table indicate that IOMT has a faster con-447 vergence speed in PEFT (e.g., 10% faster on usps. Meanwhile, the time cost for transferability 448 assessment (i.e., the time indicated after "+" in the table) is much smaller than the training time, 449 which is consistent with the discussion in Section 4.2. 450

Table 2: Test accuracy (%),  $F_1$  score (%) and convergence time (sec.) of the PEFT. ViT for the CV datasets (i.e., *usps* and *stl10*) and RoBerta for the NLP datasets (i.e., *mrpc* and *qqp*).

method	usp	s	stl1	0	m	рс	qq	Jb
methou	accuracy	time	accuracy	time	accuracy	F <sub>1</sub> score	accuracy	F <sub>1</sub> score
SGD	$94.42 \pm 0.21$	3169	$97.75 \pm 0.16$	275	85.21±0.35	$87.21{\scriptstyle\pm0.32}$	82.13±0.52	$75.19{\scriptstyle\pm0.82}$
SGDM	$95.67 \pm 0.14$	2397	$98.37{\scriptstyle\pm0.10}$	483	$85.54 \pm 0.69$	$86.27{\scriptstyle\pm0.41}$	83.30±0.63	$75.27{\scriptstyle\pm0.82}$
Adagrad	$95.37 \pm 0.21$	2220	$98.34{\scriptstyle \pm 0.09}$	284	84.94±0.59	$87.29{\scriptstyle \pm 0.46}$	83.47±0.79	$73.28{\scriptstyle\pm0.83}$
RMSprop	$94.64 \pm 0.53$	2208	$97.91 \pm 0.07$	568	$+84.09{\pm}0.76$	$89.24{\scriptstyle \pm 0.74}$	82.09±0.63	$74.09{\scriptstyle\pm0.92}$
Adam	94.47 $\pm 0.49$	2215	$98.36{\scriptstyle \pm 0.03}$	694	$86.52 \pm 0.71$	$90.37{\scriptstyle\pm0.92}$	82.27±0.71	$74.92{\scriptstyle \pm 0.84}$
<b>SWATS</b>	$95.12 \pm 0.21$	2643	$98.38 \pm 0.10$	822	$86.27 \pm 0.62$	$\overline{90.34}_{\pm0.42}$	$1.80.79 \pm 0.81$	$\overline{74.80}_{\pm 0.19}$
Padam	$95.72 \pm 0.42$	2234	$98.38 \pm 0.10$	598	$180.64 \pm 0.32$	$87.07{\scriptstyle\pm0.82}$	$73.04 \pm 0.91$	$80.93{\scriptstyle \pm 0.83}$
AdaBound	$95.42 \pm 0.11$	2232	$98.30{\scriptstyle \pm 0.14}$	199	68.38±0.59	$81.22{\scriptstyle \pm 0.94}$	$78.64 \pm 0.49$	$79.01{\scriptstyle \pm 0.42}$
ours	$96.12{\scriptstyle \pm 0.10}$	2030+2	$99.01{\scriptstyle\pm0.09}$	180+1	$87.99{\scriptstyle \pm 0.13}$	$91.36{\scriptstyle \pm 0.15}$	$85.57{\scriptstyle\pm0.14}$	$81.18{\scriptstyle \pm 0.31}$

In summary, IOMT demonstrates excellent tuning performance and convergence speed across different training approaches, various models, and downstream tasks. The combination of model transferability analysis and optimizer switching based on parameter surface characteristics effectively assists DNN training.

## 5.2 CASE STUDY FOR THE SWITCHING PROCESS OF IOMT

To observe IOMT's switching process, we con-472 ducted a case study with a simple task hy-473 menoptera from Kaggle and a restricted opti-474 mizer space (only for SGD and SGDM). The 475 training loss and the optimizer switch process 476 are plotted in Figure 9. After the initial stages 477 with weighted random sampling, IOMT selects 478 the suitable optimizer with faster convergence 479 speed for training, i.e., the SGDM selected in 480 Figure 9. After that, the optimizer switch op-481 eration occurs when a decrease in the conver-482 gence speed of the optimizer (Point A) or detects a local stable state (Point C). Additionally, 483

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Figure 9: The training loss line of the case study with vanilla FT and IOMT.

during tuning, IOMT may also undergo temporary switches to adjust the optimization state (Point
B). This case study demonstrates that IOMT can effectively select the appropriate optimizer based on the model parameter state, thereby improving convergence speed and model quality.

# 486 5.3 INDEPENDENT EXPERIMENTS

Additionally, we conducted several independent experiments to further analyze the effectiveness of
 IOMT. In this section, we outline the main conclusions, with further details available in Appendix D.

The optimizer selection strategy. IOMT employs an optimizer selection strategy that considers variance, transferability, and training process. Table 7 presents comparative results for different selection strategies. Compared to random or periodic switching, IOMT achieves higher accuracy (up to 2%) and lower variance. Additionally, the ablation experimental results indicate that the designs for transferability assessment and variance reduction further enhance its advantages.

The initial selection method. Compared with random selection, the weighted selection in IOMT significantly enhances the stability of the surrogate model, which reduces variability in the training outcomes, as shown in Figure 10(a).

The model compression technique. Table 10 illustrates the effects of various feature compression techniques on training results. For the selected tasks (i.e., *usps* and *mnist*), simple methods like random projection and PCA outperform the more complex UMAP technique. This suggests that basic compression techniques are adequate for training the surrogate model.

The optimizer search space. We broadened the hyperparameter space of candidate optimizers to
explore how this expanded search space affects IOMT's performance. The experimental results
shown in Figure 11 indicate that IOMT continues to perform well in the enlarged search space.

**The influence of hyperparameter setting.** We also performed an experimental analysis on the hyperparameters in IOMT, including the initial step  $n_{ini}$ , switch step size  $\tau$ , and the number of PCA components. Figure 10(b-d) presents the experimental results, demonstrating that a small initial step (e.g., only 10 for small dataset *usps*), switch step size (10% of an epoch) and PCA components (e.g., 2) can achieve good accuracy. A more detailed analysis can be found in Appendix D.





# 6 CONCLUSION

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525 The selection of optimizers and their hyperparameters plays a crucial role in deep neural network (DNN) training. Traditionally, researchers use a single optimizer during the whole training (i.e., a 526 coarse-grain optimizer tuning), which limits the model quality and convergence speed. Currently, 527 some works attempt to leverage the advantages of different optimizers during training to achieve 528 higher-quality models. However, these methods are still constrained by merely adjusting the learning 529 rate or transitioning between two types of optimizers, overlooking the unique strengths of various 530 optimizers under different parameter states. To better combine the benefits of different optimiz-531 ers, we introduce a fine-grain optimizer switch method called Interleaving Optimizers for Model 532 Training (IOMT) in this paper. Specifically, IOMT constructs surrogate models during training to 533 estimate the performance of different optimizers under varying model parameter states. In addition, 534 IOMT employs a transferability assessment to enhance the selection of optimizers. Combining the 535 predicted performance and transferability information with an acquisition function, IOMT gets the 536 estimation of optimization gain for each optimizer and switches the optimizer with the largest score 537 for the training stage. The experimental results on full training and PEFT demonstrate that IOMT achieves a better model quality (e.g., 3% accuracy improvement on stl10 dataset) with faster conver-538 gence (e.g., 10% on the stl10 dataset). In addition, a case study and two independent experiments further investigate the optimizer switching process and design details of IOMT.

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# A OVERALL ALGORITHM AND PSEUDOCODE OF IOMT

For ease of reading, Table 3 provides the explanations of key notations used in this paper for IOMT.

In this section, we provide an overview of IOMT with the pseudocode in Algorithm 1. For ease of understanding, we only switch the types of optimizers in the description while keeping the hyperparameters and training time constant (i.e.,  $t^i = \tau$  iterations). Before the model's training, IOMT first calculates the transferability weight  $\omega_t$  to assist in the subsequent selection of optimizers (Line 3). Then, a randomly selected initial optimizer  $o_j$  is used for model training and loss calculation (Lines 8-9). When the number of iterations meets the time constant  $\tau$ , IOMT calculates the

notation	description
switch step $ au$	the number of iterations for a single switch cycle.
init step $n_{ini}$	the number of switch cycles for the initial phase.
selection weights $\omega_r$	the sample weights for the initial phase
transferability weight w	the transferability weight which is calculated by the perform
,	based metric $\omega_t$ and distribution-based metric $\omega_d$
Algorithm 1: Basic framew	ork of our proposed IOMT.
<b>Input:</b> Training Dataset $D =$	$\{D_{train}, D_{test}\}, m$ optimizers $\mathcal{O} = \{o_1,, o_m\}$ , the model for trainin
M with initial parame	ter state $\theta^0$ , the init steps $n_{ini}$ , the switch step size $\tau$ , the training epochs
initialize: $n_t \leftarrow 0, n \leftarrow 0, \mathcal{G}$	$\leftarrow \{a_1, a_2, \dots, a_m\}, \omega_r \leftarrow \{1 1, \dots, m\}, i \leftarrow RandomSelect(m),$
$losses \leftarrow [], v \leftarrow Compress$	sModel $(M, \boldsymbol{\theta}^0)$
/* calculate the tra	nsferability weight before the training
$\omega_t \leftarrow \text{CalculateTransferability}$	y $Weight(M, oldsymbol{ heta}^0, D_{train})$ // as Equation (6)
/* training models w	ith interleaving optimizers
for BATCH in $D_{train}$ do	
$n \leftarrow n+1$	
$\boldsymbol{\theta}^n \leftarrow \operatorname{TrainModel}(N)$	$\mathcal{I}, \boldsymbol{\theta}^{n-1}, \text{BATCH}, o_j)$
$l \leftarrow \text{CalculateLoss}(N)$	$\mathcal{A}, \boldsymbol{\theta}^n, \text{BATCH}), losses.append(l)$
$n n \sqrt{2} \tau = 0$ then $s \leftarrow CalculateOr$	ntimization Gain (losses) // as Equation (2)
$g_i \leftarrow \text{UpdateSur}$	rogateModel $(g_i, v, s)$
$v \leftarrow \text{Compress}$	$\operatorname{Iodel}(M, \boldsymbol{\theta}^n)$
// init step	ps with a weighted random selection
$ \begin{array}{c c} & \mathbf{n} & n_t < n_{ini} \text{ ther} \\ & \boldsymbol{\omega}_n[i] \leftarrow \mathbf{U} \mathbf{n} \end{array} $	dateSampleWeight(s) // as Equation (3)
$j \leftarrow \text{Weighter}$	edRandomSelect( $\omega_r$ )
// following	g steps with a surrogated selection
else	$\operatorname{stadSalaat}(n, \mu, \mathcal{C}, \mathcal{O})$
end $j \leftarrow Surroga$	$\operatorname{hedSelect}(v, \omega_t, g, C)$
$n_t \leftarrow n_t + 1, los$	$sses \leftarrow []$
end	
end end	
end end	· · · ·
end end Output: the trained model M	with parameter state $\boldsymbol{\theta}^n$
end end Output: the trained model M	with parameter state $\theta^n$

performance score s based on all losses within time  $t^{i}$  (Line 11). Subsequently, the current optimizer  $o_j$  is updated by the surrogate model  $g_j$  using the optimization gain s and the model features v calculated at the end of the previous round (Lines 12-13). Based on the results from weighted random selection or surrogate model selection, IOMT obtains the suitable optimizer for the next training stage (Lines 14-20) and continues this process iteratively until the final training results  $\theta^n$ are achieved.

For the selection of the suitable optimizer, IOMT employs two types of methods: the weighted random selection and the surrogate model selection for the following steps. In the initial training steps (i.e.,  $n_t < \tau$ ), IOMT uses the optimization gain s to update the sampling weight  $\omega_r$  for randomly select configurations for training (Lines 14-17). After obtaining enough training results (i.e.,  $n_t \ge \tau$ ), IOMT utilizes the trained surrogate models to select the configurations used for the following training (Line 20). The configuration with the highest score (i.e., Equation 7) is selected for the next training iteration.

#### 756 В DATASETS AND MODELS USED IN EXPERIMENTS

In the experiments, we used 4 CV datasets from Pytorch (Paszke et al., 2019) (i.e., usps, mnist, stl10, and *cifar10*) and 2 NLP datasets from Hugging Face (Wolf et al., 2020) (i.e., *mrpc* and *qqp*). The information on these downstream tasks is as follows:

- usps (Hull, 1994): a classical digit dataset automatically scanned from envelopes by the U.S. Postal Service containing a total of 9,298 16×16 pixel grayscale samples, which includes 10 classes of figures.
- mnist (LeCun et al., 1998): a handwritten digits dataset with 28x28 grayscale figures, which has a 765 training set of 60,000 examples and a test set of 10,000 examples. 766
  - stl10 (Coates et al., 2011): a 10-classes 96x96 color figure dataset, which has 500 training images and 800 test images per class. The dataset is inspired by the *cifar-10* (Krizhevsky et al., 2009) but with some modifications.
- 770 • cifar10 (Krizhevsky et al., 2009): a 10-classes 32x32 color figure dataset, which has 5,000 training images and 1,000 test images per class.
- 772 • mrpc (Dolan & Brockett, 2005): the Microsoft Research Paraphrase Corpus, which consists of 773 5.8k sentence pairs that were automatically extracted from online news sources. The sentence 774 pairs have been annotated by human raters to indicate whether the sentences within each pair are 775 semantically equivalent.
- 776 • qqp (Quora): the Quora Question Pairs dataset, which consists of over 400,000 pairs of questions. 777 Each question pair is annotated with a binary value indicating whether the two questions are 778 paraphrases of each other. 779

As for the pre-trained models, we used 4 ImageNet pre-trained models available from Py-Torch (Paszke et al., 2019) (i.e., ResNet18, ResNet152, MobileNet V2, and ViT) and a pre-trained 781 NLP models RoBerta (Camacho-collados et al., 2022) and LLaMA-7B (Touvron et al., 2023) from 782 HuggingFace (Wolf et al., 2020) which trained on 124M tweets from January 2018 to December 783 2021, and finetuned for sentiment analysis with the TweetEval benchmark (Barbieri et al., 2020). 784 It can be found that among the downstream tasks, stl10, mrpc and qqp are relatively close to the 785 upstream task, and *usps* and *mnist* have a certain correlation with the upstream task. We selected 786 downstream datasets with varying degrees of relevance to the upstream task, to better analyze the 787 performance of the proposed method in different scenarios. 788

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### С **DETAILS OF OVERALL EXPERIMENTS**

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# C.1 EXPERIMENT SETTINGS

793 In the overall experiment, we compared 5 single optimizer methods (i.e., SGD (Robbins & Monro, 794 1951), SGDM (Sutskever et al., 2013), Adagrad (Duchi et al., 2011), RMSProp (Graves, 2013) and Adam (Kingma & Ba, 2014)), 3 hybrid methods (i.e., SWATS (Keskar & Socher, 2017), 796 Padam (Chen et al., 2018), and AdaBound (Luo et al., 2019)), and the proposed IOMT. The sin-797 gle methods are all from the PyTorch implementation, and except for the learning rate being set in 798 [0.1, 0.01, 0.001] and the epoch number being set to 100, the other hyperparameters are set to the default values in PyTorch. Additionally, for the three hybrid methods, we installed and used the 799 original implementations from the authors via Github and PyPI. The hyperparameter settings were 800 kept at their defaults, except for the epoch number, which was adjusted to be consistent with the 801 other methods. In addition, all the experiments in this paper are conducted 3 times with different 802 random seeds to avoid randomness.

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#### C.2 MORE EXPERIMENTAL RESULTS 805

806 In addition to the results in Section 5.1, we also conducted more experiments to analyze the charac-807 teristics of IOMT, and the results are presented in this section. 808

We first compared IOMT with additional baselines, including various optimizers (i.e., 809 ASGD (Polyak & Juditsky, 1992), AdamW (Loshchilov & Hutter, 2019), Nadam (Dozat), and Adamax (Kingma & Ba, 2017)) and training with learning rate schedulers (i.e., StepLR and CosineAnnealingLR in PyTorch). The results of these experiments are shown in Table 3, where we retained only the best results for training with a scheduler, specifically those obtained using SGDM. IOMT consistently achieved the highest test accuracy among all the methods evaluated.

Table 4: Test accuracy (%) of the full training with more baselines.

	ASGD	AdamW	Ndam	Adamax	SGDM	stepLR	cosLR	ours
usps	95.83	95.62	95.32	96.06	95.83	91.31	95.80	96.81
mnist	99.25	98.97	99.18	99.32	99.47	94.72	99.46	99.51

Additionally, we also conducted experiments using a complex imbalanced dataset ImageNet-A (Hendrycks et al., 2021), with the results displayed in Table 5. IOMT's dynamic adaptation to critical saddle points enhances performance on complex problems, resulting in over a 2% improvement in top-1 accuracy.

Table 5: Test accuracy (%) of the full training on ImageNet-A dataset.

	SGD	SGDM	Adagrad	RMSprop	Adam	SWATS	Padam	AdaBound	ours
acc@1	15.24	16.19	5.20	4.13	3.53	3.68	16.31	4.33	18.47
acc@3	30.74	31.20	13.12	10.42	9.87	8.94	31.76	11.23	33.83
acc@5	38.29	39.68	17.49	17.52	13.83	12.55	40.01	15.46	41.32

In addition to the results presented in Table 2, we also conducted more PEFT experiments on different models. Table 6 shows the experimental results. IOMT achieves superior test accuracy across more models and tasks.

Table 6: The testAcc. (%) and tuning time (sec.) for the vanilla method and our IOMT under the head fine-tuning. The time of IOMT includes the tuning time and the transferability estimation time.

	task	usp	S	mni	st	stl1	0
model	method	testAcc. (%)	time (sec.)	testAcc. (%)	time (sec.)	testAcc. (%)	time (sec.)
	SGDM	68.86±0.71	534	$71.59{\scriptstyle \pm 1.88}$	4443	$91.87{\scriptstyle\pm1.27}$	18551
18	Adam	66.04±0.11	543	$71.16 \pm 1.46$	4876	$91.02 \pm 1.87$	14909
Vet	SWATS	68.55±0.51	453	$73.27 \pm 0.38$	4651	$92.02 \pm 1.86$	14285
SSN	Padam	65.32±1.20	505	$70.41{\scriptstyle \pm 0.52}$	4743	$92.36{\scriptstyle \pm 0.36}$	19919
Re	AdaBound	67.80±0.27	568	$72.66 \pm 0.31$	4944	$92.23 \pm 1.37$	34858
	ours	70.64±0.80	527+4	$74.79{\scriptstyle \pm 3.38}$	4801+6	$93.56{\scriptstyle \pm 0.41}$	13240+25
	SGDM	72.27±0.12	4443	$77.54 \pm 1.02$	7437	96.66±0.32	78232
52	Adam	$71.73 \pm 1.26$	4876	$77.64 \pm 1.72$	7636	$96.11 \pm 0.32$	48541
et 1	SWATS	71.82±0.27	5121	$78.47{\scriptstyle\pm0.18}$	9211	$96.66{\scriptstyle \pm 0.51}$	115560
$\mathbf{z}$	Padam	72.31±0.69	5594	$76.18 \pm 1.17$	8878	96.51±0.39	107856
Re	AdaBound	72.94±1.33	4508	$78.33{\scriptstyle \pm 0.67}$	12934	$95.44{\scriptstyle\pm2.47}$	152592
	ours	74.36±0.41	5001+6	$79.60{\scriptstyle \pm 0.60}$	7637+8	$97.60{\scriptstyle \pm 0.28}$	44381+68
Q.	SGDM	91.28±0.39	18551	93.74±0.77	50294	$92.14 \pm 0.71$	11464
х х	Adam	89.86±0.22	12237	$93.82 \pm 0.11$	55024	$91.31 \pm 0.71$	15208
Ň	SWATS	90.68±0.25	17921	$93.90{\scriptstyle \pm 0.28}$	57655	$92.77{\scriptstyle\pm0.27}$	12971
oile	Padam	90.69±0.67	18940	$92.71{\scriptstyle\pm0.22}$	51656	$91.69{\scriptstyle \pm 0.29}$	12941
lot	AdaBound	91.36±0.37	17328	$93.67{\scriptstyle\pm0.94}$	46955	$91.39{\scriptstyle \pm 0.45}$	24367
2	ours	92.32±0.39	13240+8	$94.65{\scriptstyle\pm0.06}$	56121+11	$93.28{\scriptstyle\pm0.79}$	14972+70

# D DETAILS OF INDEPENDENT EXPERIMENTS

**The selection of optimizer switch strategy.** Compared to switching optimizers with simple strategies, IOMT employs the transferability assessment  $\omega_t$  and variance halving in its acquisition function. To estimate the effectiveness of our design, we compared IOMT with two simple strategies

(random switch "random" and periodic replacement "cyclical") and two ablation versions (without transferability assessment "w/o  $\omega_t$ " and without variance halving "w/o halve"). The experimental result in Table 7 shows that simple random or periodic switching fails to produce high test accuracy. In addition, the usage of transferability assessment and variance halving both effectively enhance the adaptability of the current task, resulting in improved accuracy (up to 2%) and lower variance. Additionally, we also compared IOMT with these strategies under other models (i.e., ResNet152 "RN152" and MobileNet V2 "MN"), as shown in Figure 8 and Figure 9

Table 7: Experimental results for different switch strategies under full training on ResNet18.

method	trainAcc. (%)	usps testAcc. (%)	time (sec.)	trainAcc. (%)	mnist testAcc. (%)	time (sec.)
random	98.36±2.22	$94.27{\scriptstyle\pm1.41}$	225	98.91±0.39	$98.33{\scriptstyle \pm 0.46}$	1916
cyclical	$97.38 \pm 1.63$	$92.88 \pm 1.94$	223	$99.49 \pm 0.20$	$98.94{\scriptstyle\pm0.25}$	1914
w/o $\overline{\omega_t}$	99.55±0.27	$95.82 \pm 0.42$	205	99.72±0.09	99.25±0.07	2101
w/o halve	$99.54{\scriptstyle\pm0.22}$	$95.70 \pm 0.35$	226	$99.67{\scriptstyle\pm0.21}$	$99.19{\scriptstyle \pm 0.08}$	2095
ours	99.67±0.19	$96.51{\scriptstyle \pm 0.08}$	227	99.85±0.17	99.48±0.03	1965

Table 8: The independent experimental result for transferability assessment.

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Table 9: The independent experimental result for different optimizer switching strategies.

me	etric	w/o $\omega_t$	with $\omega_t$		metric	random	cyclical	ours
CS tra tes tim tra W tes tim	inAcc. (%) tAcc. (%) ne (sec.) inAcc. (%) tAcc. (%) ne (sec.)	80.47 72.6 3531 98.38 91.57 26084	81.10 75.29 3347+9 98.42 91.93 23271+8	MN RN152	trainAcc. (%) testAcc. (%) time (sec.) trainAcc. (%) testAcc. (%) time (sec.)	76.56 71.49 3271 97.58 90.33 24997	$77.7971.953299-\overline{98.01}90.7323712$	81.10 75.29 3347+9 98.42 91.93 23271+8

The initial selection method. We compared the impact of using random selection and weighted selection during the initial phase on subsequent training. In the experiments, we set the initial phase to 20 epochs and used a switch step size of  $\tau = 25$ .

901 The model compression technique. We compared the impact of using other compression techniques within IOMT on the results, as shown in Table 10.

903 The optimizer space. We examined how different candidate hyperparameter spaces affected the performance of 904 **IOMT.** In addition to the original HP space described in 905 Section 5.1 (where learning rate  $\in [0.1, 0.01, 0.001]$ ), we 906 systematically expanded this space by including the fol-907 lowing components: (1) weight decay for SGD, (2) mo-908 mentum for SGDM, (3) weight decay for Adagrad, (4) 909 weight decay for RMSprop, (5) alpha for RMSprop, and 910 (6) weight decay for Adam. The ranges for these addi-911 tional hyperparameters are as follows: weight decay val-912 ues  $\in$  [1e-2, 1e-3, 1e-4], momentum  $\in$  [0.5, 0.6, 0.7, 0.8, 913 (0.9), and alpha  $\in [0.5, 0.6, 0.7, 0.8, 0.9]$ . Figure 11 illus-914 trates the performance of the baseline methods compared 915 to IOMT as the search space diversifies. For the baseline



Figure 11: Test accuracy (%) for IOMT and baselines across various optimizer space on *usps*.

methods, we report the best accuracy achieved within the search space. Overall, IOMT demon strates robust performance and consistently surpasses the baseline methods, even as the number of candidate hyperparameters increases.

method	trainAcc. (%)	usps testAcc. (%)	time (sec.)	trainAcc. (%)	mnist testAcc. (%)	time (sec.)
RP	99.72±0.12	96.44±0.17	201	99.61±0.15	$99.22{\scriptstyle\pm0.18}$	1869
UMAP	$98.56{\scriptstyle \pm 1.45}$	$95.15{\scriptstyle\pm2.15}$	253	$99.73{\scriptstyle \pm 0.06}$	$98.98{\scriptstyle \pm 0.13}$	2182
PCA	$99.58{\scriptstyle\pm0.13}$	$96.34{\scriptstyle \pm 0.25}$	222	99.86±0.13	$99.48{\scriptstyle \pm 0.06}$	1974

Table 10: Experimental results for different compression techqniues under full training on ResNet18.

The hyperparameter settings. In the experiments, we set the default hyperparameter configuration to  $n_{ini} = 20$ ,  $\tau = 25$ , and n\_components= 2. Based on the results presented in Figure 10, we have made the following observations.

- init step  $n_{ini}$ : Thanks to the ongoing updates of the surrogate model during training in IOMT, even a small initial step (i.e.,  $n_{ini} = 20$ ) can produce models with high test accuracy.
- switch step size  $\tau$ : A smaller step size facilitates quicker switching of the optimizer, which enhances accuracy (e.g.,  $\tau = 20\%$  of an epoch). Conversely, a larger step size makes it more challenging to collect training data for the surrogate model, resulting in a longer switching cycle and greater variance in the results.
- PCA components number: Selecting a small number of PCA components (for example, 2) can often yield good performance in IOMT. On the other hand, using a larger number of components may impair the surrogate model's ability to learn effectively, resulting in greater variance in test accuracy.