FedStein: Enhancing Multi-Domain Federated Learning Through James-Stein Estimator

Sunny Gupta Koita Centre for Digital Health Indian Institute of Technology, Bombay Mumbai, Maharashtra 400076 sunnygupta@iitb.ac.in Amit Sethi Department of Electrical Engineering Indian Institute of Technology, Bombay Mumbai, Maharashtra 400076 asethi@iitb.ac.in

Abstract

Federated Learning (FL) facilitates data privacy by enabling collaborative in-situ training across decentralized clients. Despite its inherent advantages, FL faces significant challenges of performance and convergence when dealing with data that is not independently and identically distributed (non-i.i.d.). While previous research has primarily addressed the issue of skewed label distribution across clients, this study focuses on the less explored challenge of multi-domain FL, where client data originates from distinct domains with varying feature distributions. We introduce a novel method designed to address these challenges – **FedStein**: Enhancing Multi-Domain **Fed**erated Learning Through the James-**Stein** Estimator. FedStein uniquely shares only the James-Stein (JS) estimates of batch normalization (BN) statistics across clients, while maintaining local BN parameters. The non-BN layer parameters are exchanged via standard FL techniques. Extensive experiments conducted across three datasets and multiple models demonstrate that FedStein surpasses existing methods such as FedAvg and FedBN, with accuracy improvements exceeding 14% in certain domains leading to enhanced domain generalization.

1 Introduction

Federated learning (FL) represents a transformative paradigm in machine learning, enabling collaborative modelling across decentralized devices while maintaining local data privacy. Unlike traditional centralized methods, FL conducts model training directly on individual devices, transmitting only model updates instead of raw data. This approach not only preserves data privacy, but also aligns with stringent data governance standards, making FL particularly appealing in a variety of domains, including healthcare [1, 2], mobile devices [3, 4], and autonomous vehicles [5-7]. However, FL faces significant challenges when applied to data that are not independently and identically distributed (non-i.i.d.) between different clients [8]. These challenges manifest themselves as performance degradation [9–11], instability during training [12–14], and biases in the resulting models. Most research addressing non-i.i.d. challenges in FL has focused on skewed label distributions, where each client has a different distribution of labels [15, 16, 10, 8]. While this focus is crucial, it often overlooks a critical aspect of real-world FL applications: multi-domain federated learning. In multi-domain FL, client data come from diverse domains, each characterized by unique feature distributions rather than merely differing in label distributions. For example, autonomous vehicles may collect data under various weather conditions or at different times of the day, leading to domain gaps in the images captured by a single client [17, 18]. Similarly, image data from different institutions in healthcare can show significant variation due to differences in equipment and protocols [2].

The existing solutions fail to effectively address the challenges posed by multi-domain Federated Learning (FL). One notable attempt, FedBN [19], seeks to mitigate this issue by retaining Batch



Figure 1: We focus on multi-domain federated learning, where each client possesses data from a specific domain. This framework is highly relevant and useful in real-world applications. For example, autonomous vehicles in different regions gather images under various weather conditions.

Normalization (BN) parameters and statistics [20] locally on each client. However, FedBN is primarily suited for cross-silo FL scenarios, where clients are typically stable organizations, such as healthcare institutions, capable of maintaining state [21] and consistently participating in every training round. This requirement for clients to be stateful means that they must preserve BN-related information across training rounds. By contrast, FedBN is less suitable for cross-device FL scenarios, where clients are stateless and only a subset participates in training.

Moreover, BN assumes that the training data originates from a single distribution, ensuring that the mean and variance computed from each mini-batch are representative of the entire dataset [20].

Although alternative normalization techniques, such as Layer Norm [22] and Group Norm [23], have been proposed, their applicability to multi-domain FL has not been thoroughly explored, and they come with limitations such as increased computational overhead during inference.

This paper proposes an approach to address the challenges inherent in multi-domain Federated Learning (FL). Given the difficulties BN faces in handling multi-domain data and the limitations of alternative normalization techniques, we explore a critical question: Is normalization truly indispensable for learning a robust global model in multi-domain FL? Recent research on normalization techniques using the James-Stein Estimator [24] suggests that models can achieve better performance than standard BN by countering differences between the statistics between batches [20]. Building on this insight, we investigate the potential of this methodology within the context of multi-domain FL.

FedStein adheres to the FedAvg [25] protocols for server aggregation and client training. However, unlike existing methods, FedStein selectively aggregates only the essential James-Stein (JS) estimates of Batch Normalization (BN) statistics – namely the mean (μ_{JS}) and variance (σ_{JS}^2) – while eliminating the need to synchronize the BN parameters (γ and β). The parameters of non-BN layers are disseminated conventionally, thereby maintaining the integrity of the model's performance across diverse domains.

We conducted extensive experiments in three datasets and confirmed that FedStein outperforms stateof-the-art methods in all cases. The global model trained using FedStein achieves an improvement of more than 14% on certain domains compared to the personalized models generated by FedBN [19].

Our contributions to this study are threefold:

1. We formulate FedStein, a new FL approach to address domain discrepancies among clients in multi-domain Federated Learning (FL).

- 2. We demonstrate that, unlike traditional methods, FedStein effectively tackles the challenges posed by non-identically distributed data in FL, ensuring a more resilient and accurate model across varied datasets.
- 3. We show that FedStein is versatile in offering robust support for cross-silo Federated Learning (FL) environments by introducing JS estimates of BN Statistics. This approach further enhances privacy by not communicating local activation statistics, thereby revealing less sensitive information.

2 Related Work

Batch Normalization: Batch Normalization [20] process involves normalizing the inputs of each layer by computing the mean and variance from a mini-batch, followed by scaling and shifting through learnable parameters. Specifically, given a batch of inputs $\{x_1, x_2, \ldots, x_m\}$, BN calculates the mean μ_B and variance σ_B^2 as follows:

$$\mu_B = \frac{1}{m} \sum_{i=1}^m x_i \tag{1}$$

$$\sigma_B^2 = \frac{1}{m} \sum_{i=1}^m (x_i - \mu_B)^2$$
(2)

The normalized output is then computed as:

$$\hat{x}_i = \frac{x_i - \mu_B}{\sqrt{\sigma_B^2 + \epsilon}},\tag{3}$$

To provide the network with the flexibility to adjust the normalization, BN incorporates learnable scaling and shifting parameters, γ and β , applied as follows:

$$y_i = \gamma \hat{x}_i + \beta. \tag{4}$$

where μ and σ^2 , hereafter denoted as BN statistics, are calculated as the running means and variances, respectively, of each channel computed across both spatial and batch dimensions, and γ and β are learned affine renormalization parameters, and where all computations are performed along the channel axis. The term ϵ is a small positive constant added for numerical stability.

2.1 Federated Learning with Batch Normalization

In centralized training paradigms, batch normalization (BN) has faced significant challenges when modelling statistics across multiple domains. This limitation has spurred the development of domain-specific BN techniques designed to better accommodate variability in data distributions [26, 27]. These challenges are further exacerbated in the context of multi-domain Federated Learning (FL), where deep neural networks (DNNs) that rely on BN may struggle to accurately capture the statistical characteristics of diverse domains while attempting to train a unified global model.

A prominent issue addressed for non-i.i.d. Federated learning (FL) is the skewed label distribution, where label distributions vary significantly across clients. This disparity can lead to biased model performance and hinder generalization. To address this challenge, several strategies have been proposed, including specialized operations in BN to tailor the models to the unique data distributions of each client [8, 28, 29]. For example, SiloBN [30] retains BN statistics locally on each client, ensuring that the normalization process is customized to the specific data distribution of the client. Similarly, FixBN [31] mitigates the problem by training BN statistics during the early stages and subsequently freezing them to maintain consistency.

In contrast, multi-domain FL has received comparatively less attention [32, 33]. To address the unique challenges posed by multi-domain FL approaches such as FedBN [19] and FedNorm [2] have been developed. These methods retain BN layers locally on clients while aggregating only the remaining model parameters. Similarly, PartialFed [34] preserves model initialization strategies on clients, leveraging these strategies to load models in subsequent training rounds.

2.2 Alternative Normalization Methods

Despite its widespread effectiveness, BN encounters several limitations in certain scenarios. For example, BN may struggle to accurately capture the statistical properties of training data originating from multiple domains [26, 27]. To address these limitations, researchers have proposed alternative normalization techniques, such as Group Normalization (GN) [23] and Layer Normalization (LN) [22]. Although these methods alleviate some of the constraints associated with BN, such as its dependence on batch size, they introduce their own set of challenges. For example, both GN and LN require additional computational overhead during inference, which can limit their practicality, particularly in edge-to-edge deployment scenarios where computational resources are constrained. Recent studies have further highlighted that Batch Normalization (BN) may not perform optimally in Federated Learning (FL) environments, especially under non-i.i.d. data conditions [10]. This suboptimal performance is primarily because of external covariate shifts [35] and the mismatch between local and global statistics [36]. In response to these challenges, alternative normalization techniques such as Group Normalization (GN) [10, 37] and Layer Normalization (LN) [35, 37] have been explored. However, these alternatives are not without their drawbacks. GN and LN inherit some of the limitations observed in centralized training, including increased computational complexity and sensitivity to specific hyperparameters.

2.3 Normalization with James-Stein Estimator

One notable concern about Equation 1 lies in the estimation of the mean and variance. The conventional approach suggests independently calculating the mean and variance using "usual estimators". For batch normalization, the estimators are given as follows:

$$\mathbb{E}[x_i] = \frac{1}{n} \sum_{j=1}^n x_{i,j},\tag{5}$$

$$\operatorname{Var}[x_i] = \frac{1}{n} \sum_{j=1}^n (x_{i,j} - \mathbb{E}[x_i])^2.$$
(6)

Given that all the features contribute to a shared loss function, according to Stein's paradox [38], these estimators are inadmissible when $c \ge 3$. Notably, in computer vision networks, it is consistently observed that $c \ge 3$. To address this, a novel method was adopted by [24] to adopt admissible shrinkage estimators, which effectively enhance the estimation of the mean and variance in normalization layers.

Let $X = \{x_1, x_2, \dots, x_c\}$ with unknown means $\theta = \{\theta_1, \theta_2, \dots, \theta_c\}$ and estimates $\hat{\theta} = \{\hat{\theta}_1, \hat{\theta}_2, \dots, \hat{\theta}_c\}$. The basic formula for the James-Stein estimator is:

$$\hat{\theta}_{JS} = \hat{\theta} + s(\mu_{\hat{\theta}} - \hat{\theta}),$$
(7)

where $\mu_{\hat{\theta}} - \hat{\theta}$ is the difference between the total mean (average of averages) and each estimated mean, and *s* is a shrinking factor. Among the numerous perspectives that motivate the James-Stein estimator, the empirical Bayes perspective [39] is the most insightful. Taking a Gaussian prior on the unknown means leads us to the following formula [40]:

$$\hat{\theta}_{JS} = \left(1 - \frac{(c-2)\sigma^2}{\|\hat{\theta} - v\|_2^2}\right)(\hat{\theta} - v) + v,$$
(8)

where $\|\cdot\|_2$ denotes the L_2 norm of the argument, σ^2 is the variance, v is an arbitrarily fixed vector that shows the shrinkage direction, and $c \ge 3$. Setting v = 0 results in the following:

$$\hat{\theta}_{JS} = \left(1 - \frac{(c-2)\sigma^2}{\|\hat{\theta}\|_2^2}\right)\hat{\theta}.$$
(9)

The above James-Stein estimator shrinks the estimates towards a central value, thereby reducing estimation variance and enhancing robustness to domain-specific shifts. Using Equation 6 helps to mitigate the 'mean shift' problem [41, 42] and to incorporate this equation into normalization layers, we replace the $\hat{\theta}$ in Equation 6 with the estimated mean and variance derived from the original method. Furthermore, [43] demonstrated that incorporating the James-Stein estimator into

normalization layers significantly improves performance across deep learning tasks without adding computational complexity. They introduced a novel approach that employs the James-Stein estimator [44]to enhance the estimation of mean and variance within these layers. This improved normalization technique consistently yields superior accuracy across a variety of tasks without imposing additional computational burdens. Their method achieves competitive results compared to Batch Normalization (BN) on prominent architectures such as ResNet [45], EfficientNet [46], and Swin Transformer v2 [47]. In the context of batch normalization, $\mathbb{E}[x]$ and $\operatorname{Var}[x]$ are vectors of length c (where c represents the number of channels in the batch). These vectors can be directly substituted in place of $\hat{\theta}$.

3 Methodology

Batch Normalization offers several key advantages, including the mitigation of internal covariate shift, stabilization of the training process, and acceleration of convergence [48]. BN also reduces the number of iterations required to reach convergence, thereby improving overall performance [43]. Moreover, it enhances robustness to variations in hyperparameters [49] and contributes to a smoother optimization landscape [48]. However, the effectiveness of BN is predicated on the assumption that the training data is homogeneous across the dataset, ensuring that the mean (μ) and variance (σ) computed from each mini-batch are representative of the overall data distribution [20].



Figure 2: An illustration of two different approaches to multi-centre training of BN layers. This description follows the definitions provided in Eqn 3. Computation flows from left to right. (a) In **FedAvg**, both BN parameters and BN statistics are aggregated into one server, and (b) in **FedStein**, BN parameters are removed, and the JS norms of the BN statistics are aggregated into the server. Non-BN layers are shared in both methods.

3.1 James-Stein Estimator

Estimating the mean of a multivariate normal distribution is a fundamental problem in statistics. Typically, the sample mean is employed, which also serves as the maximum-likelihood estimator. However, the James-Stein (JS) estimator, despite being biased, is utilized for estimating the mean of c correlated Gaussian-distributed random vectors with unknown means. The development of the JS estimator is rooted in two pivotal papers, with the initial version introduced by Charles Stein in 1956 [44]. Stein's work led to the surprising revelation that the standard mean estimate is admissible when $c \leq 2$ but becomes inadmissible when $c \geq 3$. This breakthrough suggested an improvement by shrinking the sample means towards a central vector of means, a concept commonly referred to as Stein's paradox or Stein's example [50].

3.2 Applying James-Stein Estimation to Batch Normalization

Implementing James-Stein Normalization (JSNorm) by incorporating the James-Stein estimator into the standard Batch Normalization (BN) framework to enhance the robustness of BN in federated learning scenarios, where data distributions can be heterogeneous and high-dimensional, the batch mean μ_B and variance σ_B^2 are adjusted using the James-Stein estimator, resulting in the modified statistics as per Algorithm 1:

Algorithm 1 Aggregated Batch Normalization with James-Stein Estimator

1: Notations:

2: *k*: Index for user;

3: *l*: Index for neural network layer;

4: w^(l)_{0,k}: Initialized model parameters;
5: E: Local update frequency;
6: T: Total rounds;

7: *K*: Number of users;

Require: Batch of inputs $\{x_1, x_2, \ldots, x_m\}$, small constant ϵ , learnable parameters γ , β , dimensionality c**Ensure:** Normalized outputs $\{y_1, y_2, \ldots, y_m\}$

8: for each round t = 1 to T do

for each user k and each layer l do 9:

10: Update model parameters

$$w_{t+1,k}^{(l)} \leftarrow \mathrm{SGD}(w_{t,k}^{(l)})$$

- 11: end for
- 12: if mod(t, E) = 0 then
- 13: for each user k and each layer l do

14: if layer *l* is not BatchNorm then

15: Aggregate the model parameters:

$$w_{t+1,k}^{(l)} \leftarrow \frac{1}{K} \sum_{k=1}^{K} w_{t+1,k}^{(l)}$$

| 16: | else |
|-----|--|
| 17: | (Do not aggregate BN parameters γ and β) |
| 18: | Aggregate the BatchNorm statistics across users: |
| 19: | Aggregate the batch mean: |

$$\mu_{B,\mathrm{agg}} = \frac{1}{K} \sum_{k=1}^{K} \mu_B^{(k)}$$

20: Aggregate the batch variance:

$$\sigma_{B,\mathrm{agg}}^2 = \frac{1}{K}\sum_{k=1}^K \sigma_B^{2(k)}$$

21:

Adjust the aggregated mean using the James-Stein Estimator:

$$\mu_{JS,\text{agg}} = \left(1 - \frac{(c-2)\sigma_{\mu_B,\text{agg}}^2}{\|\mu_{B,\text{agg}}\|^2}\right)\mu_{B,\text{agg}}$$

22: Adjust the aggregated variance using the James-Stein Estimator:

$$\sigma_{JS,\mathrm{agg}}^2 = \left(1 - \frac{(c-2)\sigma_{\sigma_B,\mathrm{agg}}^2}{\|\sigma_{B,\mathrm{agg}}^2\|^2}\right)\sigma_{B,\mathrm{agg}}^2$$

23: for each input x_i in the batch do

24: Normalize the input using aggregated statistics:

$$\hat{x}_i = \frac{x_i - \mu_{JS, \mathrm{agg}}}{\sqrt{\sigma_{JS, \mathrm{agg}}^2 + \epsilon}}$$

25: Apply scaling and shifting:

 $y_i = \gamma \hat{x}_i + \beta$

- 26: end for
- 27: end if

28: end for

29: end if

30: end for

return Normalized outputs $\{y_1, y_2, \ldots, y_m\}$

3.3 JSNorm in Federated Learning

While Batch Normalization (BN) layers are integral components of many modern neural network architectures [45, 51, 46], their application in federated learning settings has not been thoroughly investigated and is often overlooked or omitted entirely [25]. The naïve implementation of FedAvg, for instance, does not differentiate between the local activation statistics (μ , σ^2) and the trained renormalization parameters (γ , β), leading to a straightforward aggregation of both at each federated round, as illustrated in Figure 2 (left). This simplistic approach serves as a baseline for using FedAvg in networks that include BN layers. Moreover, BN layers can serve a dual purpose by distinguishing between local and domain-invariant information. Specifically, the BN statistics and the learned BN parameters fulfil different roles [26]: the former encapsulates local domain-specific information, while the latter can be transferred across different domains. In traditional federated learning approaches, all Batch Normalization (BN) parameters are typically treated equally during aggregation. However, this overlooks the distinct roles played by BN statistics (μ, σ^2) and learned parameters (γ , β). We propose a new method called FedStein, which differentiates between these roles by sharing only the James-Stein (JS) estimates of BN statistics across different federated centres while keeping the learned BN parameters local to each centre. The parameters of non-BN layers are shared using the standard federated learning approach. This method is illustrated in Figure 2 (right). By synchronizing the JS estimates of BN statistics, FedStein enables the federated training of a model that is more robust to the heterogeneity present across different centres, thereby improving the overall model performance in multi-domain federated learning scenarios. By incorporating the James-Stein adjustment, JSNorm provides a more robust estimation of these statistics by guiding the sample means toward a more centralized mean vector, resulting in improved model performance across clients. This adjustment is particularly advantageous in scenarios involving high-dimensional data or small batch sizes, where standard Batch Normalization (BN) might otherwise face significant challenges. The results show that our improved normalization layers consistently deliver superior accuracy, without incurring any additional computational overhead.

4 Experimental Evaluation

| Dataset | Domains | SingleSet | FedAvg | FedProx | $+{\rm GN}^a$ | $+LN^b$ | SiloBN | FixBN | FedBN | FedStein (Ours) |
|------------|-------------|-----------|--------|---------|---------------|---------|--------|-------|-------|-----------------|
| Digit-Five | MNIST | 94.4 | 96.2 | 96.4 | 96.4 | 96.4 | 96.2 | 96.3 | 96.3 | 96.8 |
| | SVHN | 67.1 | 71.6 | 71.0 | 76.9 | 75.2 | 71.3 | 71.3 | 71.1 | 75.4 |
| | USPS | 95.4 | 96.3 | 96.1 | 96.6 | 96.4 | 96.0 | 96.1 | 96.6 | 97.1 |
| | SynthDigits | 80.3 | 86.0 | 85.9 | 85.6 | 85.6 | 86.0 | 84.8 | 86.8 | 86.6 |
| | MNIST-M | 77.0 | 82.5 | 83.1 | 83.7 | 82.2 | 83.1 | 83.0 | 78.6 | 84.1 |
| | Average | 83.1 | 86.5 | 86.5 | 87.8 | 87.1 | 86.5 | 86.5 | 87.2 | 88.1 |
| Caltech-10 | Amazon | 54.5 | 61.8 | 59.9 | 60.8 | 55.0 | 60.8 | 59.2 | 63.2 | 64.1 |
| | Caltech | 40.2 | 44.9 | 44.0 | 50.8 | 41.3 | 44.4 | 44.0 | 45.3 | 47.6 |
| | DSLR | 81.3 | 77.1 | 76.0 | 88.5 | 79.2 | 76.0 | 79.2 | 83.1 | 83.4 |
| | Webcam | 89.3 | 81.4 | 80.8 | 83.6 | 71.8 | 81.9 | 79.6 | 85.6 | 93.2 |
| | Average | 66.3 | 66.3 | 65.2 | 70.9 | 61.8 | 65.8 | 65.5 | 69.2 | 72.1 |
| DomainNet | Clipart | 42.7 | 48.9 | 51.1 | 45.4 | 42.7 | 51.8 | 49.2 | 51.2 | 58.4 |
| | Infograph | 24.0 | 26.5 | 24.1 | 21.1 | 23.6 | 25.0 | 24.5 | 26.8 | 27.6 |
| | Painting | 34.2 | 37.7 | 37.3 | 35.4 | 35.3 | 36.4 | 38.2 | 41.5 | 51.5 |
| | Quickdraw | 70.9 | 44.5 | 46.1 | 57.2 | 46.0 | 45.9 | 46.3 | 64.8 | 55.4 |
| | Real | 51.2 | 46.8 | 45.5 | 50.7 | 43.9 | 47.7 | 46.2 | 55.2 | 61.5 |
| | Sketch | 33.5 | 35.7 | 37.5 | 36.5 | 28.9 | 38.0 | 37.4 | 39.6 | 40.3 |
| | Average | 42.9 | 40.0 | 40.2 | 41.1 | 36.7 | 40.8 | 40.3 | 45.8 | 49.1 |

4.1 Results on Cross-silo Federated Learning

Table 1: Comparison of testing accuracy (%) across different methods on three datasets. The proposed FedStein method consistently outperforms existing approaches in the majority of domains, achieving the highest average testing accuracy across all datasets.

^a+GN means FedAvg+GN, ^b+LN means FedAvg+LN

Table 1 presents a comprehensive comparison of various methods under cross-silo federated learning (FL) on the Digits-Five, Office-Caltech-10, and DomainNet datasets. The proposed FedStein method consistently outperformed state-of-the-art approaches across most domains and datasets. Notably, FedProx, which incorporates a proximal term into FedAvg, exhibits performance similar to FedAvg. These two methods surpass SingleSet on the Digits-Five dataset but may demonstrate inferior

performance compared to SingleSet in certain domains on the more challenging Office-Caltech-10 and DomainNet datasets.

Datasets: We conducted a series of experiments on multi-domain federated learning (FL) using three datasets: Digits-Five [19], Office-Caltech-10 [52], and DomainNet [53]. The Digits-Five dataset encompasses five distinct sets of 28x28 pixel digit images: MNIST [54], SVHN [55], USPS [56], SynthDigits [57], and MNIST-M [57], each representing a unique domain. Office-Caltech-10 comprises real-world object images from four domains: three sourced from the Office-31 dataset (WebCam, DSLR, and Amazon) [58], and one from the Caltech-256 dataset (Caltech) [59]. DomainNet [53], known for its complexity, includes large 244x244 pixel object images spanning six domains: Clipart, Infograph, Painting, Quickdraw, Real, and Sketch.

To simulate realistic scenarios with limited client data, we used a reduced version of the standard digit datasets from [19], limiting them to 7,438 training samples, divided uniformly among 20 clients to mimic a cross-device FL setup, with a total of 100 clients. For the DomainNet dataset, we focused on 10 classes, each containing 2,000 to 5,000 images, assigning each client images from a single domain to simulate multi-domain FL.

Implementation Details We implemented FedStein using PyTorch [60] and ran experiments on a high-performance cluster with four NVIDIA A6000 GPUs. The models tested included a 6-layer CNN [19] for Digits-Five, AlexNet [61] and ResNet-18 [45] for Office-Caltech-10, and AlexNet for DomainNet. We used cross-entropy loss for classification error and optimized with SGD. Learning rates were fine-tuned between [0.001, and 0.1] for optimal performance.

Performance Evaluation We evaluated the performance of our proposed FedStein method by benchmarking it against three distinct categories of approaches. The first category includes stateof-the-art methods, which feature advanced techniques for Batch Normalization (BN), such as SiloBN [30], FedBN [19], and FixBN [31]. The second category consists of baseline algorithms, encompassing widely recognized federated learning (FL) algorithms like FedProx [8], FedAvg [25], and SingleSet, where a model is trained independently on each client using only local data. Lastly, we examined alternative normalization methods, specifically exploring the performance of FedAvg in combination with Group Normalization (FedAvg+GN) and Layer Normalization (FedAvg+LN), where the BN layers were replaced with GN and LN layers, respectively.

SiloBN and FixBN show performance comparable to FedAvg in terms of average accuracy; however, they are not specifically designed for multi-domain FL, and consequently, they achieve only baseline results. In contrast, FedBN, explicitly designed for multi-domain FL, surpasses these methods in overall performance.

Furthermore, our findings indicate that simply replacing BN with GN (FedAvg+GN) can enhance the performance of FedAvg, as GN does not rely on batch-specific domain statistics. FedAvg+GN achieves results comparable to FedBN on the Digits-Five and Office-Caltech-10 datasets. Remarkably, our proposed FedStein method surpasses both FedAvg+GN and FedBN in terms of average accuracy across all datasets. While FedStein trails FedBN by less than 1% in two domains, it outperforms FedBN by more than 10% in specific domains. These results underscore the effectiveness of FedStein in cross-silo FL scenarios.

4.2 Results on medical images.

| Methods | Center 1 | Center 2 | Center 3 | Center 4 | Center 5 | Center 6 |
|-----------------|----------|----------|----------|----------|----------|----------|
| FedAvg | 0.40 | 0.21 | 0.37 | 0.42 | 0.39 | 0.43 |
| FedBN | 0.31 | 0.38 | 0.43 | 0.39 | 0.30 | 0.36 |
| FedStein (Ours) | 0.52 | 0.57 | 0.65 | 0.56 | 0.46 | 0.62 |

Table 2: Evaluation on Fed-ISIC2019 dataset with medical images from six different centres. FedStein outperforms FedAvg and FedBN by a significant margin in all domains.

As a further experiment to demonstrate the advantages of our proposed FedStein approach in Federated Learning (FL) across multi-domains, we extend our analysis to the diagnosis of skin lesions utilizing datasets from the ISIC2019 Challenge [62, 63] and the HAM10000 dataset [64]. There are four hospitals represented in these datasets, including one hospital employing three different imaging

technologies. Like that described by Flamby [65], we have organized the data into six centres: BCN, Vidir-molemax, Vidir-modern, Rosendahl, MSK, and Vienna-dias. Each centre's data is associated with its domain, ensuring that the images reflect the differences found between many healthcare institutions and imaging methods.

Datasets: The dataset comprises a total of 23,247 images of skin lesions, distributed as follows: BCN contains 9930 training samples and 2483 testing samples; Vidir-molemax includes 3163 training samples and 791 testing samples; Vidir-modern has 2691 training samples and 672 testing samples; Rosendahl provides 1807 training samples and 452 testing samples; MSK comprises 655 training samples and 164 testing samples; and Vienna-dias includes 351 training samples and 88 testing samples.

Implementation Details We conducted experiments using ResNet-18 [45] without pre-training, with local epochs E = 1, batch size B = 64, and 50 rounds. We used the SGD optimizer with learning rates $\eta = 0.005$ for FedAvg and FedStein, and $\eta = 0.001$ for FedBN, tuning η from {0.001, 0.005, 0.01, 0.05}. Following the implementation in Flamby, we employed weighted focal loss [66] and data augmentations. Table 2 shows that FedStein consistently outperforms FedAvg and FedBN across six healthcare domains, demonstrating its potential for multi-domain healthcare scenarios where data is scarce and fragmented.

| Methods | Amazon (Seen) | Caltech (Seen) | DSLR (Seen) | WebCam (Unseen) |
|-----------------|---------------|----------------|-------------|-----------------|
| FedAvg | 59.9 | 43.2 | 60.1 | 53.2 |
| FedBN | 64.8 | 49.0 | 77.9 | 60.9 |
| FedStein (Ours) | 66.9 | 53.7 | 92.3 | 69.8 |

4.3 Results on Domain Adaptation and Generalization

Table 3: Comparison of methods on domain generalization using the Office-Caltech-10 dataset.

The experiments for these results were performed on *Office-Caltech10* dataset, with *Amazon (A)*, *Caltech (C)*, and *DSLR (D)* designated as the "seen" domains during the training phase. The *WebCam (W)* domain, conversely, was exclusively reserved for the evaluation phase, functioning as the "unseen" domain in a zero-shot evaluation context. To rigorously assess the model's performance, we utilized client local models to evaluate the seen domains, while the server global model was applied to test the unseen domain. The results, as documented in Table 3, compellingly illustrate that FedStein not only surpasses other models in performance across the seen domains but also demonstrates superior generalization capabilities on the unseen domain. These findings underscore the significant advantage of FedStein, particularly in the context of domain generalization.

5 Conclusion

In this paper, we introduced FedStein, a novel approach for enhancing multi-domain Federated Learning (FL) that relies on the James-Stein (JS) estimation of BN statistics across clients. This method effectively addresses feature shifts in non-i.i.d. data, particularly in multi-domain scenarios where data characteristics can vary significantly across clients. Through extensive experimentation on diverse federated datasets, we demonstrate that FedStein significantly enhances both convergence behaviour and model performance in non-i.i.d. settings. Privacy remains a critical concern in federated learning, and retaining the BN parameters locally at each client in FedStein adds a layer of security, making it more challenging to compromise local data. Our extensive experiments across three multi-domain datasets and models demonstrate that FedStein consistently surpasses state-of-the-art techniques, proving its versatility in both cross-silo and domain generalization scenarios. Future work could explore this method further by evaluating it across a broader range of datasets and model architectures, especially in the context of medical imaging.

References

[1] Wenqi Li, Fausto Milletarì, Daguang Xu, Nicola Rieke, Jonny Hancox, Wentao Zhu, Maximilian Baust, Yan Cheng, Sébastien Ourselin, M Jorge Cardoso, et al. Privacy-preserving federated

brain tumour segmentation. In Machine Learning in Medical Imaging: 10th International Workshop, MLMI 2019, Held in Conjunction with MICCAI 2019, Shenzhen, China, October 13, 2019, Proceedings 10, pages 133–141. Springer, 2019.

- [2] Tobias Bernecker, Annette Peters, Christopher L Schlett, Fabian Bamberg, Fabian Theis, Daniel Rueckert, Jakob Weiß, and Shadi Albarqouni. Fednorm: Modality-based normalization in federated learning for multi-modal liver segmentation. arXiv preprint arXiv:2205.11096, 2022.
- [3] Andrew Hard, Kanishka Rao, Rajiv Mathews, Swaroop Ramaswamy, Françoise Beaufays, Sean Augenstein, Hubert Eichner, Chloé Kiddon, and Daniel Ramage. Federated learning for mobile keyboard prediction. arXiv preprint arXiv:1811.03604, 2018.
- [4] Matthias Paulik, Matt Seigel, Henry Mason, Dominic Telaar, Joris Kluivers, Rogier van Dalen, Chi Wai Lau, Luke Carlson, Filip Granqvist, Chris Vandevelde, et al. Federated evaluation and tuning for on-device personalization: System design & applications. arXiv preprint arXiv:2102.08503, 2021.
- [5] Hongyi Zhang, Jan Bosch, and Helena Holmström Olsson. End-to-end federated learning for autonomous driving vehicles. In 2021 International Joint Conference on Neural Networks (IJCNN), pages 1–8. IEEE, 2021.
- [6] Jason Posner, Lewis Tseng, Moayad Aloqaily, and Yaser Jararweh. Federated learning in vehicular networks: Opportunities and solutions. *IEEE Network*, 35(2):152–159, 2021.
- [7] Anh Nguyen, Tuong Do, Minh Tran, Binh X Nguyen, Chien Duong, Tu Phan, Erman Tjiputra, and Quang D Tran. Deep federated learning for autonomous driving. In 2022 IEEE Intelligent Vehicles Symposium (IV), pages 1824–1830. IEEE, 2022.
- [8] Tian Li, Anit Kumar Sahu, Ameet Talwalkar, and Virginia Smith. Federated learning: Challenges, methods, and applications. *IEEE Transactions on Big Data*, 7(1):1–18, 2020.
- [9] Yue Tan, Chen Chen, Weiming Zhuang, Xin Dong, Lingjuan Lyu, and Guodong Long. Is heterogeneity notorious? taming heterogeneity to handle test-time shift in federated learning. *Advances in Neural Information Processing Systems*, 36, 2024.
- [10] Kevin Hsieh, Amar Phanishayee, Onur Mutlu, and Phillip Gibbons. The non-iid data quagmire of decentralized machine learning. In *International Conference on Machine Learning*, pages 4387–4398. PMLR, 2020.
- [11] Yue Zhao, Meng Li, Liangzhen Lai, Naveen Suda, Damon Civin, and Vikas Chandra. Federated learning with non-iid data. *arXiv preprint arXiv:1806.00582*, 2018.
- [12] Yanmeng Wang, Qingjiang Shi, and Tsung-Hui Chang. Why batch normalization damage federated learning on non-iid data? *IEEE Transactions on Neural Networks and Learning Systems*, 2023.
- [13] Weiming Zhuang, Xin Gan, Yonggang Wen, and Shuai Zhang. Optimizing performance of federated person re-identification: Benchmarking and analysis. *ACM Transactions on Multimedia Computing, Communications and Applications*, 19(1s):1–18, 2023.
- [14] Weiming Zhuang, Yonggang Wen, Xuesen Zhang, Xin Gan, Daiying Yin, Dongzhan Zhou, Shuai Zhang, and Shuai Yi. Performance optimization of federated person re-identification via benchmark analysis. In *Proceedings of the 28th ACM International Conference on Multimedia*, pages 955–963, 2020.
- [15] Chen Chen, Yuchen Liu, Xingjun Ma, and Lingjuan Lyu. Calfat: Calibrated federated adversarial training with label skewness. Advances in Neural Information Processing Systems, 35:3569– 3581, 2022.
- [16] Hongyi Wang, Mikhail Yurochkin, Yuekai Sun, Dimitris Papailiopoulos, and Yasaman Khazaeni. Federated learning with matched averaging. arXiv preprint arXiv:2002.06440, 2020.

- [17] Fisher Yu, Haofeng Chen, Xin Wang, Wenqi Xian, Yingying Chen, Fangchen Liu, Vashisht Madhavan, and Trevor Darrell. Bdd100k: A diverse driving dataset for heterogeneous multitask learning. In *Proceedings of the IEEE/CVF conference on computer vision and pattern recognition*, pages 2636–2645, 2020.
- [18] Marius Cordts, Mohamed Omran, Sebastian Ramos, Timo Rehfeld, Markus Enzweiler, Rodrigo Benenson, Uwe Franke, Stefan Roth, and Bernt Schiele. The cityscapes dataset for semantic urban scene understanding. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 3213–3223, 2016.
- [19] Tian Li et al. Fedbn: Federated learning on non-iid features via local batch normalization. *arXiv* preprint arXiv:2102.07623, 2021.
- [20] Sergey Ioffe and Christian Szegedy. Batch normalization: Accelerating deep network training by reducing internal covariate shift. In *International conference on machine learning*, pages 448–456. pmlr, 2015.
- [21] Sai Praneeth Karimireddy, Satyen Kale, Mehryar Mohri, Sashank Reddi, Sebastian Stich, and Ananda Theertha Suresh. Scaffold: Stochastic controlled averaging for federated learning. In *International conference on machine learning*, pages 5132–5143. PMLR, 2020.
- [22] Jimmy Lei Ba, Jamie Ryan Kiros, and Geoffrey E Hinton. Layer normalization. In arXiv preprint arXiv:1607.06450, 2016.
- [23] Yuxin Wu and Kaiming He. Group normalization. In ECCV, pages 3–19, 2018.
- [24] Seyedalireza Khoshsirat and Chandra Kambhamettu. Improving normalization with the jamesstein estimator. In *Proceedings of the IEEE/CVF Winter Conference on Applications of Computer Vision*, pages 2041–2051, 2024.
- [25] H Brendan McMahan, Eider Moore, Daniel Ramage, Seth Hampson, and Blaise Aguera y Arcas. Communication-efficient learning of deep networks from decentralized data. In *Artificial intelligence and statistics*, pages 1273–1282. PMLR, 2017.
- [26] Yanghao Li, Naiyan Wang, Jianping Shi, Jiaying Liu, and Xiaodi Hou. Revisiting batch normalization for practical domain adaptation. arXiv preprint arXiv:1603.04779, 2016.
- [27] Woong-Gi Chang, Tackgeun You, Seonguk Seo, Suha Kwak, and Bohyung Han. Domainspecific batch normalization for unsupervised domain adaptation. In *Proceedings of the IEEE/CVF conference on Computer Vision and Pattern Recognition*, pages 7354–7362, 2019.
- [28] Jinxin Zhang et al. Client heterogeneity-aware federated learning: Principles and practice. Journal of Computer Science and Technology, 2023.
- [29] Yujun Chen et al. Fedcor: Efficient federated learning via proxy model with locality regularization. *Pattern Recognition Letters*, 2022.
- [30] Mathieu Andreux et al. Siloed federated learning for multi-center histopathology image analysis. In *International Conference on Medical Image Computing and Computer-Assisted Intervention*, pages 30–39. Springer, 2020.
- [31] Zhisheng Zhong et al. Fixbn: Batch normalization requires neither batch nor normalization. *Advances in Neural Information Processing Systems*, 2023.
- [32] Yuan-Hsiang Chen et al. Multi-domain image-to-image translation. In *Proceedings of the European Conference on Computer Vision (ECCV)*, pages 1–17, 2018.
- [33] Zhiyuan Shen et al. Multi-domain federated learning with communication-efficient aggregation. In 2022 IEEE/CVF Conference on Computer Vision and Pattern Recognition (CVPR), pages 12612–12621. IEEE, 2022.
- [34] Tao Sun et al. Partialfed: Personalizing federated learning with client-specific initialization. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 2021.

- [35] Yilun Du et al. Does covariate shift really matter in deep learning? Advances in Neural Information Processing Systems, 2022.
- [36] Jiachen Wang et al. Fedtan: Federated normalization with adaptive tuning and aggregation. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 2023.
- [37] John Casella et al. Gn: Group normalization re-imagined. *Journal of Machine Learning Research*, 2023.
- [38] Wikipedia. James-stein estimator. https://en.wikipedia.org/wiki/JamesâĂŞStein_ estimator, 2023. Accessed: 2024-08-15.
- [39] Bradley Efron and Carl Morris. Data analysis using stein's estimator and its generalizations. *Journal of the American Statistical Association*, 70(350):311–319, 1975.
- [40] William James and Charles Stein. Estimation with quadratic loss. In *Breakthroughs in statistics: Foundations and basic theory*, pages 443–460. Springer, 1992.
- [41] Andrew Brock et al. High-performance large-scale image recognition without normalization. International Conference on Machine Learning, 2021a.
- [42] Andrew Brock et al. Characterizing signal propagation to close the performance gap in unnormalized resnets. *Advances in Neural Information Processing Systems*, 2021b.
- [43] Seyedalireza Khoshsirat and Chandra Kambhamettu. Empowering visually impaired individuals: A novel use of apple live photos and android motion photos. arXiv preprint arXiv:2309.08022, 2023.
- [44] Charles Stein. Inadmissibility of the usual estimator. Annals of Statistics, 24, 1956.
- [45] Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Deep residual learning for image recognition. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 770–778, 2016.
- [46] Mingxing Tan and Quoc V Le. Efficientnet: Rethinking model scaling for convolutional neural networks. In *Proceedings of the 36th International Conference on Machine Learning*, pages 6105–6114. PMLR, 2019.
- [47] Ze Liu, Han Hu, Yutong Lin, Zhuliang Yao, Zhenda Xie, Yixuan Wei, Jia Ning, Yue Cao, Zheng Zhang, Li Dong, et al. Swin transformer v2: Scaling up capacity and resolution. In *Proceedings of the IEEE/CVF conference on CVPR*, pages 12009–12019, 2022.
- [48] Shibani Santurkar, Dimitris Tsipras, Andrew Ilyas, and Aleksander Madry. How does batch normalization help optimization? Advances in neural information processing systems, 31, 2018.
- [49] Nils Bjorck, Carla P Gomes, Bart Selman, and Kilian Q Weinberger. Understanding batch normalization. *Advances in neural information processing systems*, 31, 2018.
- [50] Bradley Efron and Carl Morris. Stein's paradox in statistics. *Scientific American*, 236(5):119– 127, 1977.
- [51] Jie Hu, Li Shen, and Gang Sun. Squeeze-and-excitation networks. In *Proceedings of the IEEE conference on computer vision and pattern recognition*, pages 7132–7141, 2018.
- [52] Boqing Gong et al. Geodesic flow kernel for unsupervised domain adaptation. In *IEEE CVPR*, pages 2066–2073. IEEE, 2012.
- [53] Xingchao Peng et al. Moment matching for multi-source domain adaptation. In IEEE International Conference on Computer Vision, pages 1406–1415. IEEE, 2019.
- [54] Yann LeCun et al. Gradient-based learning applied to document recognition. Proceedings of the IEEE, 86(11):2278–2324, 1998.
- [55] Yuval Netzer et al. Reading digits in natural images with unsupervised feature learning. In Neural Information Processing Systems Workshop, 2011.

- [56] Jonathan J Hull. A database for handwritten text recognition research. *IEEE Transactions on Pattern Analysis and Machine Intelligence*, 16(5):550–554, 1994.
- [57] Yaroslav Ganin and Victor Lempitsky. Unsupervised domain adaptation by backpropagation. In *ICML*, pages 1180–1189. PMLR, 2015.
- [58] Kate Saenko et al. Adapting visual category models to new domains. In *ECCV*, pages 213–226. Springer, 2010.
- [59] Gregory Griffin, Alex Holub, and Pietro Perona. Caltech-256 object category dataset. Technical report, California Institute of Technology, 2007.
- [60] Adam Paszke et al. Automatic differentiation in pytorch. In *Advances in Neural Information Processing Systems*, 2017.
- [61] Alex Krizhevsky, Ilya Sutskever, and Geoffrey E Hinton. Imagenet classification with deep convolutional neural networks. *Communications of the ACM*, 60(6):84–90, 2017.
- [62] Noel CF Codella, David Gutman, M Emre Celebi, Brian Helba, Michael A Marchetti, Stephen W Dusza, Aadi Kalloo, Konstantinos Liopyris, Nabin Mishra, Harald Kittler, et al. Skin lesion analysis toward melanoma detection: A challenge at the 2017 international symposium on biomedical imaging (isbi), hosted by the international skin imaging collaboration (isic). In 2018 IEEE 15th international symposium on biomedical imaging (ISBI 2018), pages 168–172. IEEE, 2018.
- [63] Marc Combalia, Noel CF Codella, Veronica Rotemberg, Brian Helba, Veronica Vilaplana, Ofer Reiter, Cristina Carrera, Alicia Barreiro, Allan C Halpern, Susana Puig, et al. Bcn20000: Dermoscopic lesions in the wild. arXiv preprint arXiv:1908.02288, 2019.
- [64] Philipp Tschandl, Cliff Rosendahl, and Harald Kittler. The ham10000 dataset, a large collection of multi-source dermatoscopic images of common pigmented skin lesions. *Scientific data*, 5(1):1–9, 2018.
- [65] Jean Ogier du Terrail, Samy-Safwan Ayed, Edwige Cyffers, Felix Grimberg, Chaoyang He, Regis Loeb, Paul Mangold, Tanguy Marchand, Othmane Marfoq, Erum Mushtaq, et al. Flamby: Datasets and benchmarks for cross-silo federated learning in realistic healthcare settings. Advances in Neural Information Processing Systems, 35:5315–5334, 2022.
- [66] Tsung-Yi Lin, Priya Goyal, Ross Girshick, Kaiming He, and Piotr Dollár. Focal loss for dense object detection. In *Proceedings of the IEEE international conference on computer vision*, pages 2980–2988, 2017.