MENTOR: A Reinforcement Learning Framework for Distilling Tool Use in Small Models via Teacher-Optimized Rewards

Anonymous ACL submission

Abstract

Distilling the tool-using capabilities of large language models (LLMs) into smaller, more efficient small language models (SLMs) is a key challenge for their practical application. The predominant approach, supervised fine-tuning (SFT), suffers from poor generalization as it trains models to imitate a static set of teacher trajectories rather than learn a robust methodology. While reinforcement learning (RL) offers an alternative, the standard RL methods using simple outcome-based reward fail to effectively guide SLMs, causing them to struggle with inefficient exploration and adopt suboptimal strategies. To address these distinct challenges, we propose MENTOR, a framework that synergistically combines RL with teacher-guided distillation. Instead of simple imitation, MENTOR employs an RL-based process to learn a more generalizable policy through exploration. In addition, to address insufficient process guidance, it uses a teacher's reference trajectory to construct a composite teacher-guided reward that provides fine-grained guidance. Extensive experiments demonstrate that MENTOR significantly improves the cross-domain generalization and strategic competence of SLMs compared to both SFT and standard RL baselines.

1 Introduction

The augmentation of large language models (LLMs) with external tools, such as code interpreters and retrieval APIs, has enabled them as advanced agents capable of handling complex reasoning tasks (Yao et al., 2023; Paranjape et al., 2023; Wang et al., 2024b; Singh et al., 2025). However, the high inference costs of these large-scale models hinder their practical use. This challenge has motivated a line of research focused on smaller language models (SLMs), with the goal of preserving the tool-assisted problem-solving capabilities of larger models (Gao et al., 2023; Gou et al., 2024; Qiu et al., 2025).

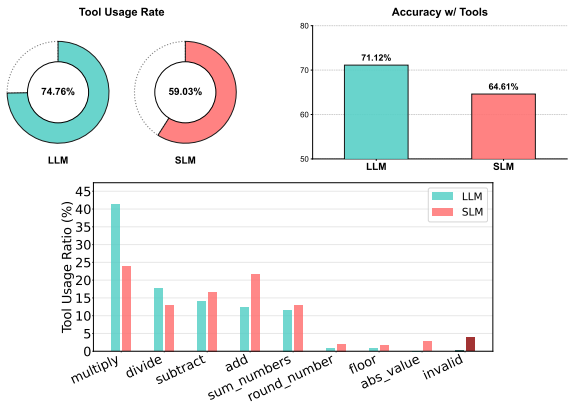

Figure 1: Comparative analysis of tool usage rates and their corresponding performance, as well as tool invocation patterns between LLMs and SLMs.

Knowledge distillation has been steadily used for transferring such advanced abilities from a larger **teacher** model to a smaller **student** model (Ho et al., 2023; Chenglin et al., 2024; Dai et al., 2024b, 2025; Song et al., 2025; Liao et al., 2025). These studies primarily employ supervised fine-tuning (SFT), where a student model is trained to replicate teacher-generated problem-solving trajectories (Liu et al., 2024; Kang et al., 2025; Lyu et al., 2025). However, the reliance of these methods on a static dataset presents a fundamental scalability issue, as it is impossible to generate trajectories for every scenario the model will face (Luo et al., 2025b; Sun et al., 2025; Yin et al., 2025). As a result, these models often fail to generalize to new tasks, necessitating more adaptive frameworks for teaching tool use.

As an alternative to this imitation-based approach, some studies have explored reinforcement learning (RL) through iterative self-refinement (Trung et al., 2024; Wu et al., 2025b). To guide the models in learning from their solutions, prior works use simple reward signals, such as correctness of the final answer or tool invocation (Yu et al., 2024; Singh et al., 2025; Wu et al., 2025a). However, relying on this naive outcome sig-

nal is insufficient for SLMs, as their inefficient use of tools often leads them to adopt suboptimal strategies. As shown in Figure 1, which compares the tool-use strategies of a teacher LLM and a student SLM, SLMs are less effective at leveraging tools: the Teacher utilized tools in 74.8% of samples (71.12% accuracy), whereas the Student utilized tools in only 59.0% of samples (64.61% accuracy). This is linked to suboptimal strategies in SLMs, as also evidenced by their distinct tool-invocation patterns and tendency to issue invalid tool calls. This highlights the importance of fine-grained feedback to guide the agent toward an effective tool-use strategy.

To address these distinct challenges of both SFT-based distillation and standard RL, we propose a framework that synergistically combines reinforcement learning with teacher-guided distillation. We introduce MENTOR (**M**odel **EN**hancement via **T**eacher-**O**ptimized **R**ewards), a novel approach designed to leverage the strengths of each approach. By employing an **RL-based distillation** process, our framework moves beyond the simple imitation of SFT, allowing the student model to learn a more generalizable policy through exploration. Simultaneously, to address the challenge of insufficient process guidance that hinders SLMs, we design a **teacher-guided reward**, which utilizes the teacher's trajectory as a reference to construct a composite reward signal. This reference-based reward provides the fine-grained guidance necessary to steer the SLM towards efficient tool-use strategies and prevent it from converging to suboptimal policies. Our code is publicly available[1].

To summarize, our key contributions are:

- To address the limitations of SFT-based approach, we propose MENTOR. Unlike SFT, which often leads to superficial imitation, our RL-based framework uses exploration to internalize the teacher's tool-use strategy, ensuring the student learns a generalizable methodology.
- To prevent SLMs from adopting suboptimal strategies due to non-comprehensive signals, we propose a teacher-optimized reward that leverages the teacher's trajectory for fine-grained supervision, ensuring the student internalizes the correct methodology.
- We demonstrate through extensive experiments that MENTOR significantly improves the cross-domain generalization and strategic competence of SLMs compared to both SFT and standard outcome-based RL baselines.

[1] https://anonymous.4open.science/r/MENTOR-F6E7/

2 Related Work

2.1 Tool-Augmented Language Models

A significant line of research enhances the reasoning of LLMs by augmenting them with external tools, such as code interpreters and retrieval APIs. The approaches for integrating these tools are diverse, ranging from prompting-based code generation (Gao et al., 2023; Paranjape et al., 2023; Inaba et al., 2023; Huang et al., 2024) to explicitly training models to invoke tools as part of their reasoning process (Schick et al., 2023; Kong et al., 2023; Qian et al., 2024). Recognizing that effective tool use is an inherently strategic process, recent work has focused on learning optimal tool-invocation patterns through RL (Yu et al., 2024; Feng et al., 2025; Qian et al., 2025). The core challenge in training tool-augmented models is maintaining a robust and generalizable tool-use policy across long reasoning trajectories.

2.2 Reasoning Distillation through SFT

Previous studies have mainly trained student models to clone teacher-generated trajectories as a method for transferring tool-use capabilities to SLMs (Liu et al., 2024; Kang et al., 2025; Lyu et al., 2025). However, SFT-based distillation faces a critical scalability challenge (Sun et al., 2025; Yin et al., 2025), as it is infeasible to curate a static dataset that covers every possible scenario. A key limitation that arises from this data dependency is that models learn to mimic the superficial format of a reasoning trajectory to produce a correct final answer, without internalizing the underlying logical process (Kandpal et al., 2023; Dai et al., 2024a; Li et al., 2025). By contrast, MENTOR employs an **RL-based distillation** framework, where the teacher's trajectory is used not for direct imitation, but serves as a reference to guide an exploratory learning process aimed at developing a more **generalizable** problem-solving method.

2.3 Reinforcement Learning and Reward Design

Reinforcement learning (RL) (Kaelbling et al., 1996) offers a powerful alternative to SFT's imitation-based learning, as its exploratory nature

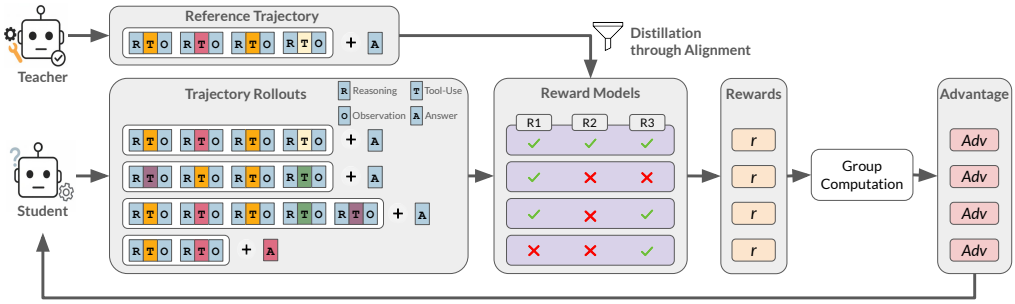

Figure 2: Overview of the MENTOR training framework. A problem-solving trajectory (τ) consists of a sequence of Reasoning (R), Tool-Use (T), and Observation (O), and a final Answer (A). Each student rollout is evaluated by a set of reward models, which generate a reward signal by aligning the student's actions against the teacher's reference trajectory.

can, in principle, discover more generalizable policies. Foundational algorithms like Proximal Policy Optimization (PPO) established the paradigm of fine-tuning models through policy optimization (Schulman et al., 2017). More recent advancements, such as Group Relative Policy Optimization (GRPO), have adapted this approach for complex reasoning tasks, demonstrating its effectiveness in fostering robust, self-corrective behaviors (Shao et al., 2024).

Many of these RL approaches have been demonstrated on highly capable LLMs for reasoning with tool use. Due to their strong intrinsic abilities, these models can often discover effective policies even when guided by simple outcome rewards, such as a binary signal for final answer correctness or successful tool invocation (Yu et al., 2024; Feng et al., 2025; Singh et al., 2025; Qian et al., 2025; Wu et al., 2025a). However, SLMs are significantly less efficient explorers (Wei et al., 2022; Xiong et al., 2024). With only outcome-based rewards, they struggle to link their actions to the final outcome and tend to converge to suboptimal policies. To address this, our work leverages the teacher's trajectory to construct a **teacher-guided reward** signal, providing the fine-grained guidance necessary to steer the SLM's exploration.

3 MENTOR: Model Enhancement via Teacher-Optimized Reward

In this section, we introduce MENTOR, a framework that leverages reinforcement learning (RL) to distill a tool-calling policy from a large teacher model to a smaller student model. The overall process is illustrated in Figure 2. For each input, the teacher model first generates a reference reasoning trajectory that exemplifies a successful problem-solving process. Concurrently, the student model generates multiple exploratory rollouts to sample different reasoning paths. We then apply the Group Relative Policy Optimization (GRPO) algorithm to refine the student's policy. By leveraging a teacher-guided reward signal, MENTOR ensures the student internalizes strategic principles rather than merely memorizing steps. We describe this process in the following subsections.

3.1 Reference Trajectory Generation

First, we use a large teacher model (π_{teacher}) to generate reference reasoning trajectories (τ). Each trajectory consists of a sequence of reasoning (r), tool-use (t), and observation (o) steps. We use a training dataset $\mathcal{D} = \{(x_i, y_i)\}_{i=1}^{N}$, where x_i represents a question and y_i is its corresponding ground-truth answer. For each question x, the teacher model generates a final answer $\hat{y}$ and a reasoning trajectory τ using an instruction prompt (I) as follows:

$$O^{(t)} = (\tau^{(t)}, \hat{y}^{(t)}) \sim \pi_{\text{teacher}}(\cdot|x, I), \text{where} \quad (1)$$

$$\tau^{(t)} = \langle (r_1, t_1, o_1), \ldots, (r_{L_\tau}, t_{L_\tau}, o_{L_\tau}) \rangle. \quad (2)$$

3.2 Adapting GRPO for Reasoning Distillation

We adapt the GRPO algorithm to distill the teacher's problem-solving methodology by configuring the teacher's successful trajectory as a high-reward target. This reward-driven setup trains the student to internalize the teacher's strategic tool-use policy, rather than merely imitating a fixed sequence of actions. This process is detailed in Algorithm 1.

Generating Rollouts For each question x_i in our training set, we perform two simultaneous generation steps. First, we retrieve the corresponding reference trajectory, $(\tau^{(t)}, \hat{y}^{(t)})$, which was generated by the teacher model as described in subsection 3.1. Then, we use the current student model (π_{old}) to

$$\mathcal{J}_{GRPO}(\theta) = \mathbb{E}_{x_i \sim \mathcal{D},\, \{O_j^{(s)}\}_{j=1}^{G} \sim \pi_{old}(\cdot|x_i)} \Bigg[\frac{1}{G} \sum_{j=1}^{G} \left(\sum_{k=1}^{|\tau_j^{(s)}|} \mathbb{I}(\tau_{j,k}) \right)^{-1} \sum_{k=1}^{|\tau_j^{(s)}|} \min \left(\frac{\pi_\theta(\tau_{j,k}|\tau_{j,<k}, x_i)}{\pi_{old}(\tau_{j,k}|\tau_{j,<k}, x_i)} \hat{A}_{j,k}, clip\left(\frac{\pi_\theta(\tau_{j,k}|\tau_{j,<k}, x_i)}{\pi_{old}(\tau_{j,k}|\tau_{j,<k}, x_i)}, 1-\epsilon, 1+\epsilon \right) \hat{A}_{j,k} \right) \cdot \mathbb{I}(\tau_{j,k}) - \beta \mathbb{D}_{KL}[\pi_\theta || \pi_{ref}] \Bigg] \tag{3}$$

Algorithm 1 Training with GRPO

Require: Student model π_θ, old student model π_{old}, Teacher model π_{teacher}, task dataset $\mathcal{D}$, group size G, indicator function $\mathbb{I}$

for each training iteration **do**
  for each question x_i **do**
    Generate reference trajectory $O^{(t)}$ from π_{teacher}
    Sample G rollouts $\{O_1^{(s)}, \ldots, O_G^{(s)}\}$ from π_{old}
    for each rollout $O_j^{(s)}$ **do**
      Compute outcome rewards $R(O_j^{(s)}, O^{(t)}))$
    end for
    Compute groupwise advantages $\hat{A}_{j,k}$ for all $O_j^{(s)}$
    Apply indicator $\mathbb{I}$ to mask tool output tokens
    Compute GRPO loss $\mathcal{L}_{\text{GRPO}}$ and update π_{student}
  end for
end for

generate a group of G rollouts. This step is crucial as it allows the student to explore diverse reasoning paths and tool-use strategies for the same problem, providing the varied data needed for the GRPO comparison.

Student Policy Optimization The core idea of our proposed method is to update a policy by aligning a high-quality reference against a group of sampled candidates. We optimize the tool-use policy of the student model based on the reference trajectory generated by the teacher. We optimize the student model by maximizing the objective function as shown in Equation 3, where ϵ and β are hyperparameters for clipping and KL regularization, respectively. The advantage, $\hat{A}_{j,k}$, is computed from the relative rewards within the sample group. The reference policy π_{ref} used for KL regularization is the initial student model before RL training. $\mathbb{I}(\tau_{j,k})$ is an indicator function used for loss masking, which equals 1 if $\tau_{j,k}$ is an LLM-generated token, and 0 otherwise.

3.3 Teacher-Guided Reward Design

The central challenge of our work lies in the reward design: how to distill a generalizable problem-solving methodology, rather than merely rewarding correct answers. An outcome-based reward is insufficient because it lacks the granular supervision needed to guide the student through the teacher's strategic problem-solving process. To address this, we provide a more fine-grained signal that also evaluates the reasoning process itself by designing a composite reward mechanism with three key components. The total reward for a given student output, $R(O^{(s)}, O^{(t)})$, is defined as:

$$R(O^{(s)}, O^{(t)}) = w_{\text{c}} R_{\text{c}} + w_{\text{a}} R_{\text{a}} + w_{\text{v}} R_{\text{v}}, \tag{4}$$

where w_c, w_a, and w_v are hyperparameters that balance the contribution of each reward component.

Correctness Reward This component evaluates whether the final answer derived by the student model ($\hat{y}^{(s)}$) is consistent with the result produced by the teacher model ($\hat{y}^{(t)}$). This provides a direct signal indicating if the student's overall reasoning process concludes with the same outcome as the teacher's successful demonstration. For our training, we only use reference trajectories where the teacher's answer matches the ground truth (y). The reward is defined as:

$$R_{\text{c}} = \begin{cases} 1 & \text{if } \hat{y}^{(s)} = \hat{y}^{(t)} \\ 0 & \text{otherwise} \end{cases} \tag{5}$$

Teacher-Alignment Reward To provide an intermediate signal that guides the student towards the teacher's problem-solving strategy, we introduce this reward. This component encourages the student to select the same set of tools as the teacher, which is a crucial aspect of learning the overall methodology. The reward is assigned only if the set of tool calls made in the student's trajectory, $\tau^{(s)}$, is identical to the set of tool calls in the teacher's trajectory, $\tau^{(t)}$. This is defined as:

$$R_{\text{a}} = \begin{cases} 1 & \text{if } \{t_1^{(s)}, \ldots, t_L^{(s)}\} = \{t_1^{(t)}, \ldots, t_L^{(t)}\} \\ 0 & \text{otherwise} \end{cases} \tag{6}$$

, where each $t_i^{(s)}$ in $\{t_1^{(s)}, \ldots, t_L^{(s)}\}$ are from $\tau^{(s)}$, and each $t_i^{(t)}$ in $\{t_1^{(t)}, \ldots, t_L^{(t)}\}$ are from $\tau^{(t)}$.

Tool Validation Reward A primary inefficiency we observed (in Figure 1) was the student model's tendency to generate invalid tool calls. These actions, which result in execution errors from the tool interpreter, immediately derail the reasoning process and are a significant source of suboptimal performance for the SLM. To directly penalize this behavior and guide the student towards the valid, error-free trajectories demonstrated by the teacher,

we introduce the tool validation reward. This binary reward is 1 only if every tool call within the student's trajectory, $\tau_{student}$, executes successfully without raising an error:

$$R_{\text{v}} = \begin{cases} 1 & \forall o_i^{(s)} \in \tau^{(s)} \text{ is valid} \\ 0 & \text{otherwise} \end{cases} \quad (7)$$

4 Experiments and Results

4.1 Experimental Setup

Training Domain Selection We strategically select mathematical reasoning as the primary training domain to enable the model to explore various problem-solving approaches. Its inherent difficulty gradient drives robust exploration beyond simple policies, mitigating the risk of suboptimal convergence (Zhou et al., 2023; Wang et al., 2024a; Chen et al., 2025b; Luo et al., 2025a). This choice is also supported by prior work showing that mathematical ability is a transferable skill that provides a strong foundation for generalizable problem-solving (Wang et al., 2025; Huang et al., 2025). We use the AceReason-Math dataset for training (Chen et al., 2025b). Details of our training dataset are provided in Appendix A.1.

Models and Tools Our teacher model is Qwen3-235B-Thinking, chosen for its strong tool-use capabilities. We use four student models to evaluate our method across different scales: Qwen3 (8B and 1.7B) and Qwen2.5 (7B and 1.5B). To augment the models with tool-use capability, we implement a sandbox for running Python code on a remote server. Our implementation code is publicly available. The details of the model versions and tools are in Appendix A.2 and Appendix C, respectively.

Baselines To evaluate our proposed framework, we compare MENTOR against three distinct baselines that represent different training approaches. **1) Vanilla SLM:** The base instruction-tuned model without any further training. This serves as a lower bound for performance. **2) SFT:** This baseline represents the predominant distillation method, where the SLM is fine-tuned on expert-generated trajectories using supervised fine-tuning. **3) Standard RL:** To isolate the benefit of our teacher-guided reward design, we include a Standard RL method as a baseline. This agent is trained using the same RL framework as our method, but with a simple reward signal (R_{c}) based only on the final outcome.

Task Type	Dataset Name	Description	Size
Math Reasoning	Math-Forge-Hard	College	500
	Omni-MATH-512 (Gao et al., 2024)	Olympiad	512
	AIME24 (AI-MO, 2024)	Olympiad	30
	AIME25	Olympiad	30
	amc23 (AMC, 2023)	Olympiad	40
	minervamath (Lewkowycz et al., 2022)	College	272
Tool-Calling	BFCL v4 (Patil et al., 2025)	Tool-call	5088
Factual Reasoning	HotPotQA (Yang et al., 2018)	2-hop QA	2000
	2WikiMultiHopQA (Ho et al., 2020)	2-hop QA	2000
	Bamboogle (Press et al., 2023)	2-hop QA	125

Table 1: Benchmarks categorized by in-domain (*Mathematical Reasoning*) and out-of-domain (*Tool-Calling* and *Factual Reasoning*) tasks and their test data size.

Benchmarks We evaluate our framework on a set of in-domain and out-of-domain tasks, detailed in Table 1, to measure both task-specific performance and generalization ability. For **In-Domain Tasks**, our agent is trained and evaluated on a collection of mathematical reasoning benchmarks that provide a natural gradient of difficulty. This includes the widely-used MATH dataset (Hendrycks et al., 2021), the tool-centric Omni-MATH-512 (Gao et al., 2024), and several Olympiad-level datasets such as AIME24, AIME25, amc23, and minervamath. For **Out-of-Domain Tasks**, we evaluate the trained agent on tasks requiring tools unseen during training to assess zero-shot generalization. To test *retrieval-based QA*, we reframe multi-hop QA datasets (HotpotQA (Yang et al., 2018), 2WikiMultiHopQA (Ho et al., 2020), Bamboogle (Press et al., 2023)) as a tool-use problem where the agent is provided with a search(query) tool and must learn to call it effectively. To test broader capabilities, we also use the general *Tool-Calling* benchmark BFCL v4 (Patil et al., 2025), which involves a diverse set of novel tools. We provide details in Appendix A.3.

Evaluation Metrics We evaluate the performance on all tasks using Exact Match (EM). To measure the accuracy (Acc), we consider a prediction to be correct only if it exactly matches one of the ground-truth answers after normalization. We also quantify policy alignment using an **alignment score (AS)** based on the Jensen-Shannon divergence. This score measures the divergence between a model's tool usage distribution and the teacher's reference distribution from Figure 1. Further details are in Appendix A.4.

Implementation Details The reinforcement learning framework is built on verl (Sheng et al., 2024). The agent is trained for two epochs on the combined training splits of our training dataset. We employ LoRA (Hu et al., 2021) for supervised fine-

Model	Method	Math (Acc)						
		Math-Forge	Omni-MATH	aime24	aime25	amc23	minervamath	Overall
Qwen 3	235B-Vanilla	68.00	26.00	46.67	40.00	85.00	46.69	52.06
Qwen 2.5	1.5B-Vanilla	5.18 (±0.11)	1.23 (±0.18)	0.00 (±0.00)	0.00 (±0.00)	2.50 (±2.04)	1.29 (±0.56)	1.70
	1.5B-SFT	5.79 (±0.09)	1.62 (±0.23)	1.00 (±2.25)	1.33 (±1.72)	5.75 (±2.90)	3.53 (±0.43)	3.17
	1.5B-Standard RL	18.38 (±0.09)	3.46 (±0.18)	2.67 (±3.06)	3.00 (±2.92)	8.50* (±2.93)	4.12 (±0.34)	6.69
	1.5B-MENTOR	**18.84*** (±0.13)	**5.64*** (±0.28)	**10.00*** (±3.52)	**6.67*** (±2.72)	**9.75*** (±2.49)	**8.42*** (±0.44)	**9.89**
	7B-Vanilla	36.87 (±1.04)	8.60 (±1.28)	6.66 (±2.22)	5.33* (±2.81)	44.00 (±3.16)	26.48 (±0.96)	21.32
	7B-SFT	37.64 (±1.25)	11.14 (±1.99)	9.40* (±2.65)	**7.33*** (±3.44)	43.00 (±4.53)	26.38 (±2.64)	22.48
	7B-Standard RL	50.25 (±1.32)	12.94 (±1.21)	12.00* (±3.58)	6.66* (±2.22)	45.50 (±3.07)	29.40 (±1.70)	26.13
	7B-MENTOR	**55.42*** (±1.96)	**14.72*** (±2.21)	**12.33*** (±3.52)	**7.33*** (±2.63)	**50.10*** (±2.70)	**31.86*** (±1.71)	**28.63**
Qwen 3	1.7B-Vanilla	58.70 (±0.11)	16.28 (±0.21)	25.36 (±2.32)	13.01 (±2.44)	58.00 (±4.22)	28.85 (±0.47)	33.37
	1.7B-SFT	59.99 (±0.12)	16.65 (±0.21)	31.00 (±2.25)	16.02 (±2.10)	63.75 (±3.17)	30.60 (±0.52)	36.34
	1.7B-Standard RL	60.18 (±0.07)	17.78 (±0.28)	34.34 (±3.13)	20.00 (±2.22)	67.75 (±2.75)	31.67 (±0.48)	38.62
	1.7B-MENTOR	**60.66*** (±0.11)	**20.74*** (±0.22)	**36.67*** (±2.50)	**24.00*** (±4.08)	**71.00*** (±3.94)	**32.30*** (±0.38)	**40.90**
	8B-Vanilla	65.00 (±0.12)	19.46 (±0.24)	29.32 (±2.64)	20.65 (±3.44)	57.75 (±2.49)	42.55 (±0.58)	39.12
	8B-SFT	65.35 (±0.07)	20.45 (±0.21)	31.65 (±3.23)	25.65 (±4.17)	62.50 (±2.89)	43.22 (±0.31)	41.47
	8B-Standard RL	65.48 (±0.04)	22.03 (±0.26)	35.33 (±3.22)	30.33 (±3.99)	75.50 (±2.58)	43.49 (±0.25)	45.19
	8B-MENTOR	**66.50*** (±0.11)	**24.10*** (±0.25)	**39.00*** (±3.53)	**37.00*** (±3.31)	**79.00*** (±2.69)	**43.94*** (±0.44)	**48.26**

Model	Method	BFCL-v4 (Acc)					RAG (EM)			
		Non-Live	Multi-Turn	Live	Agentic	Overall	Bamboogle	2WikiMultiHopQA	HotpotQA	Overall
Qwen 3	235B-Vanilla	87.62	51.88	82.68	18.83	50.13	41.60	42.50	34.60	39.57
Qwen 2.5	1.5B-Vanilla	68.88 (±1.15)	1.09 (±0.34)	58.99 (±0.54)	2.21 (±0.44)	24.00	0.30 (±0.31)	3.20 (±0.55)	1.47 (±0.60)	1.66
	1.5B-SFT	69.96 (±1.20)	1.58 (±0.42)	60.72 (±0.36)	2.65 (±0.29)	24.59	0.85 (±0.53)	3.91 (±0.47)	2.52 (±0.57)	2.43
	1.5B-Standard RL	71.38 (±0.63)	1.98 (±0.50)	61.46 (±0.45)	3.09 (±0.39)	25.12	6.80 (±0.49)	10.19 (±0.41)	5.79 (±0.66)	7.59
	1.5B-MENTOR	**72.66*** (±0.62)	**2.35*** (±0.41)	**62.03*** (±0.39)	**3.83*** (±0.40)	**25.70**	**7.36*** (±0.55)	**11.31*** (±0.54)	**6.50*** (±0.40)	**8.39**
	7B-Vanilla	72.04 (±0.33)	3.90 (±1.43)	63.78 (±0.91)	4.09 (±1.86)	26.38	14.88 (±2.48)	14.20 (±0.58)	13.08 (±1.00)	14.05
	7B-SFT	72.05 (±0.32)	4,02 (±1.08)	63.79 (±0.79)	4.27 (±1.76)	26.50	16.48 (±1.74)	13.87 (±0.53)	13.36 (±0.70)	14.57
	7B-Standard RL	82.13 (±0.09)	14.14* (±1.69)	72.22 (±0.30)	8.15 (±1.15)	32.94	22.04 (±1.06)	17.57 (±0.55)	17.07 (±0.65)	18.89
	7B-MENTOR	**82.35*** (±0.21)	**14.27*** (±1.74)	**72.81*** (±0.43)	**9.30*** (±1.34)	**33.52**	**23.56*** (±1.24)	**19.39*** (±0.40)	**19.24*** (±0.56)	**20.73**
Qwen 3	1.7B-Vanilla	80.89 (±0.70)	10.47 (±0.52)	69.90 (±0.22)	3.98 (±0.30)	29.81	14.61 (±0.53)	18.87 (±0.31)	16.11 (±0.36)	16.53
	1.7B-SFT	81.55 (±0.50)	10.45 (±0.46)	70.36 (±0.41)	4.51 (±0.39)	30.13	15.95 (±0.54)	19.69 (±0.51)	17.00 (±0.43)	17.45
	1.7B-Standard RL	83.00 (±0.31)	11.50 (±0.38)	70.77 (±0.31)	4.73 (±0.46)	30.65	16.83 (±0.55)	20.36 (±0.53)	17.35 (±0.29)	18.18
	1.7B-MENTOR	**82.76*** (±0.35)	**12.02*** (±0.46)	**71.05*** (±0.34)	**5.52*** (±0.60)	**31.20**	**18.28*** (±0.55)	**21.37*** (±0.60)	**18.03*** (±0.48)	**19.23**
	8B-Vanilla	87.28 (±0.49)	35.51 (±0.47)	80.16 (±0.29)	9.89 (±0.33)	41.35	32.13 (±0.64)	35.88 (±0.61)	27.47 (±0.61)	31.83
	8B-SFT	87.91 (±0.48)	36.92 (±0.60)	80.59 (±0.33)	10.58 (±0.44)	42.16	34.65 (±0.31)	37.18 (±0.36)	30.59 (±0.44)	34.14
	8B-Standard RL	88.37 (±0.37)	38.06 (±0.29)	81.10 (±0.37)	11.03 (±0.34)	42.78	35.18 (±0.36)	37.95 (±0.30)	31.30 (±0.31)	34.81
	8B-MENTOR	**89.41*** (±0.56)	**38.77*** (±0.60)	**81.96*** (±0.52)	**11.57*** (±0.42)	**43.39**	**35.77*** (±0.36)	**38.86*** (±0.56)	**31.68*** (±0.36)	**35.44**

Table 2: Main results comparing MENTOR against baselines across all evaluation benchmarks. The top table shows in-domain accuracy (%) on mathematical reasoning tasks. The bottom table shows out-of-domain performance on BFCL-v4 (accuracy %) and RAG (exact match %). Results are reported as mean (± standard deviation) over 10 runs. Overall scores are calculated differently: as a macro-average for MATH and RAG, and as an official weighted average for BFCL-v4. Values marked with an asterisk (*) denote statistical significance, determined by the Bonferroni pairwise test at a significance level of $\alpha < 0.05$.

tuning the student SLMs. For each model, we used the recommended sampling parameters from its official repository. The 'search' tool provided to the agent for the retrieval-based QA tasks is powered by a retrieval environment based on FlashRAG (Jin et al., 2025), using E5-base-v2 (Wang et al., 2022) as the retriever and the Dec. 2018 Wikipedia snapshot (Karpukhin et al., 2020) as the knowledge base. For retrieval-based tasks, we retrieve the top-5 results for each query. We provide further details on hyperparameters in Appendix A.5 and on prompts in Appendix B.

4.2 Experimental Results

The main results, presented in Table 2, demonstrate that our proposed framework, MENTOR, significantly outperforms the baselines.

Distillation Enables Effective Tool Use. On in-domain tasks, both SFT and our RL-based distillation clearly enable more effective tool use, leading to significant performance gains over the vanilla baselines. This confirms that transferring the teacher's tool-calling ability is a broadly successful strategy for improving SLM performance.

RL-Based Distillation Achieves General Performance. On out-of-domain (OOD) benchmarks, the SFT baseline often shows minimal improvement or even performance degradation on OOD tasks, which we attribute to its tendency to overfit on the training domain. By contrast, RL-based approaches consistently yield significant performance gains in the OOD setting. This highlights the effectiveness of the RL-based distillation framework in instilling a more robust and generalizable problem-solving methodology, rather than merely encouraging the memorization of the teacher's trajectories. For a more detailed analysis, the following section focuses on the performance of the Qwen2.5-7B model.

5 Analysis

5.1 Impact of RL-Based Distillation

RL Drives Effective Transfer. To evaluate how efficiently each model learns the teacher's strategy, we analyze the alignment of its tool-use policy with the teacher's patterns. As shown in Figure 3, there is a clear correlation between model performance and alignment score (AS). The SFT model clearly demonstrates imitation failure by learning a

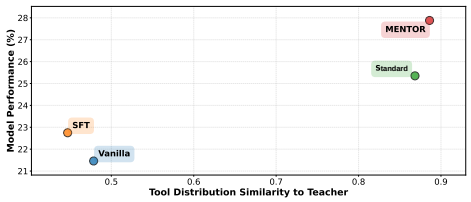

Figure 3: Correlation between task performance (Math) and alignment score (AS).

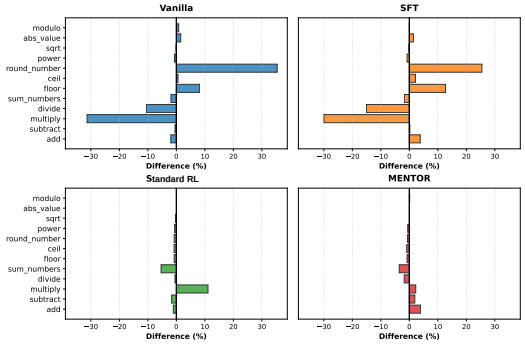

Figure 4: Comparison of tool invocation patterns between student models and the teacher. Each bar represents the percentage point difference in invocation frequency for a specific tool between the student model and the teacher.

policy that is the least similar to the teacher's, confirming that it relies on superficial shortcuts rather than the intended methodology. In contrast, the RL-based methods achieve significantly higher performance and alignment with the teacher's policy. Notably, MENTOR achieves the highest accuracy while learning a tool-use policy most similar to the expert teacher's. This suggests that our RL-based distillation is the most effective method for transferring the efficient tool-use strategy.

RL Distillation Drives Policy Alignment. To evaluate the strategic alignment of each model with the teacher, Figure 4 compares their respective tool invocation patterns to the teacher's reference policy, which is shown as the LLM's tool usage in Figure 1. The baseline models, Vanilla and SFT, exhibit significant deviations from the teacher's patterns, indicating that they learn a divergent and suboptimal tool-use policy. By contrast, the RL-based methods, such as standard RL and MENTOR, demonstrate a much closer alignment, with minimal differences across most tools. This provides strong visual evidence that our RL-based distillation is highly effective at teaching the SLM to internalize the teacher's strategic methodology.

RL Enables Efficient Tool Use. Figure 5 shows the tool-use efficiency of each model by plotting the distribution of tool calls per question for both in-domain and out-of-domain tasks. While the

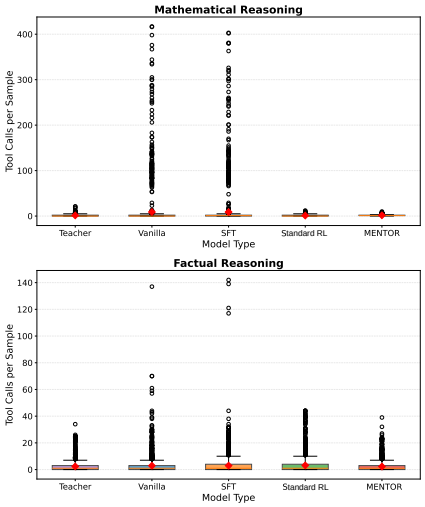

Figure 5: Tool-use efficiency on in-domain and out-of-domain tasks, measured by the distribution of tool calls per sample.

Teacher model is highly efficient, the Vanilla and SFT baselines tend to use tools inefficiently, evidenced by their wide distributions and numerous outliers. In contrast, our RL-based approach effectively transfers the teacher's efficient strategy, maintaining a low and stable number of tool calls. It suggests that the RL-based approach successfully transfers the teacher's tool-use efficiency and that this skill generalizes to out-of-domain tasks.

5.2 Impact of Teacher-Guided Reward

Reward Setting	Math	BFCL	RAG	AS
(1) R_c (Standard RL)	26.13	30.88	18.05	82.65
(2) R_c + R_v	27.80	30.96	8.35	80.94
(3) R_c + $R_{\text{Tool format}}$	26.61	28.95	7.83	79.73
(4) R_c + $R_{\text{Tool format}}$ + R_v	26.76	30.60	9.42	83.54
(5) R_c + R_a^{strict} + R_v	26.88	30.85	18.05	85.25
(6) R_c + R_a + R_v (Ours)	**27.88**	**31.38**	**21.23**	**88.79**

Table 3: Ablation study of the reward components. Performance is measured by the overall score on the Math, BFCL, and RAG benchmarks. AS represents the alignment score.

Ablation of Rewards We conduct an ablation study to isolate the contribution of each reward component by testing five distinct settings. The results are shown in Table 3. Specifically, **Setting (1)** serves the standard RL baseline, using only a reward for final answer correctness (R_a). **Setting (2)** introduces a tool validation reward (R_v) to penalize execution erros and invalid calls. **Setting (3)** adds a reward for the correct tool format, a strict structural constraint used in prior works (Qian et al., 2025). **Setting (4)** adds the validation reward to Setting (2). **Setting (5)** utilizes a strict alignment reward (R_a^{strict}) to enforce strict sequential alignment with the teacher's trajectory. **Setting (6)** is MENTOR, which combines all rewards for the teacher-guided

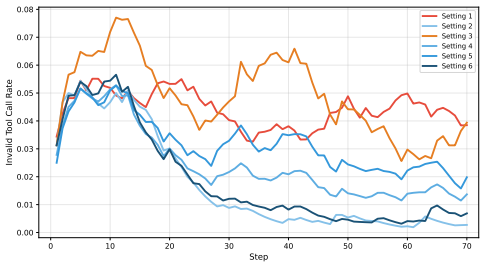

Figure 6: Invalid tool call rate over training steps

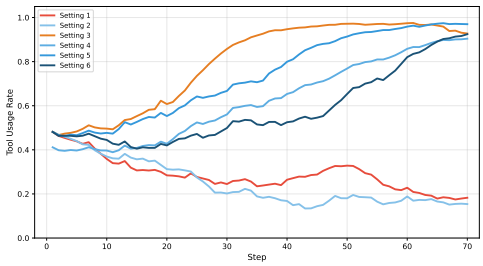

Figure 7: Tool usage rate over training steps

reward, employing a set-based alignment. The results show that our comprehensive reward design (Setting 6) is the best performer, achieving the highest scores across all task benchmarks and in policy alignment.

Referencing Teacher's Trajectory Drives Performance. The results (Table 3) demonstrate a strong positive correlation (Pearson's $r = 0.87$) between average performance and the alignment score (AS), indicating that the student's success depends on how closely it references the teacher's methodology. Notably, Settings 4, 5, and 6, which incorporate the teacher's trajectory as a reference standard for reward calculation, achieve the highest alignment scores. This confirms that performance is enhanced by actively guiding the student to reference and adopt the teacher's tool-use patterns.

Flexible Guidance Achieves Better Alignment than Strict Constraints. Our ablation study further reveals that the method of enforcing alignment is critical. We compare our flexible, set-based alignment reward (Setting 6) against a strict, sequence-based exact-match reward (Setting 5). The results (Table 3) demonstrate that strict sequence constraints are less effective than flexible guidance, as the latter achieves a higher Alignment Score and superior downstream performance. This indicates that strict constraints are excessively restrictive, punishing valid variations and hindering learning. In contrast, flexible guidance focuses on the strategic selection of tools, enabling the student to internalize the teacher's methodology more effectively and achieve more robust alignment.

Validation Reward Reduces Invocation Errors. To demonstrate the effectiveness of our reward design in addressing tool invocation errors, Figure 6 presents the invalid tool call rate during training for each of the five reward settings from our ablation study. The results show that the choice of reward components leads to distinct learning behaviors. Settings that lack the tool validation reward (R_v), such as Settings 1 and 3, fail to effectively reduce their error rates, which remain high and unstable throughout training. In contrast, settings that include the tool validation reward (Settings 2, 4, 5, and 6) learn to avoid invalid calls, with their error rates dropping rapidly to near-zero. This suggests that directly penalizing invalid calls with R_v is a highly effective strategy for training a more reliable agent.

Teacher-Guided Rewards Foster Robust Tool Adoption. Figure 7 illustrates the impact of reward components on the model's tendency to utilize tools. Without the guidance of the teacher's trajectory (Settings 1 and 2), the student fails to recognize the value of tools and drifts toward a suboptimal tool-avoidant strategy. Conversely, incorporating teacher alignment (Settings 3-6) actively encourages tool adoption. Crucially, while strict constraints (Setting 5) drive immediate but rigid usage, MENTOR (Setting 6) demonstrates a steadier learning curve that converges to high usage. This indicates that the student is not merely memorizing a simple heuristic to "use tools", but is internalizing the teacher's strategy, learning to deploy tools deliberately to solve complex problems.

6 Conclusion

To address the poor generalization of SFT and the inefficiency of simple outcome-reward RL in distilling tool-use into SLMs, we introduce MENTOR, a framework that combines reinforcement learning with a composite, teacher-guided reward. Extensive experiments demonstrate that MENTOR significantly improves cross-domain generalization by learning a policy that achieves both closer alignment with the teacher's strategy and superior tool-use efficiency compared to baselines. Our ablation studies confirm that the synergistic combination of each component in our composite reward design is crucial for achieving this robust performance.

Limitations

While this study offers valuable insights, it is essential to acknowledge that several open challenges remain.

Extending to Other Models Our current framework focuses on the Qwen model series (Qwen2.5 and Qwen3), a choice guided by the design of our RL-based approach. Our method is intended to refine and generalize an existing tool-use policy and thus performs best when the student model has some initial ability. A key open challenge is adapting this framework to models that completely lack this initial ability, as the exploratory feedback from RL alone may be insufficient for them to learn effectively. A promising direction for future work is to explore a two-stage, SFT-then-RL training pipeline. Such an approach could first use an SFT phase to instill a baseline policy before our RL-based refinement is applied, thereby extending the applicability of our method to a broader range of models.

Extending to Real-World Environments Our current work operates within a sandbox environment where tools are invoked via executable code. A significant avenue for future research is to extend our framework to operate in more complex, tool-augmented environments, such as web browsers, simulators, or desktop interfaces. In particular, integration with the Model Context Protocol (MCP) (Anthropic, 2024)—which utilizes servers that can respond to various scenarios—could significantly enhance the capabilities of small agents across a diverse range of real-world tasks. This represents an important direction for future work.

Ethical Statements

This work contributes to the development of efficient and capable artificial intelligence. By successfully distilling the complex tool-use capabilities of large language models (LLMs) into smaller, more efficient small language models (SLMs), MENTOR accelerates the creation of functional, on-device AI. This capability enables local deployment, reducing reliance on expensive cloud infrastructure and improving user privacy for agents that perform complex tasks, such as mathematical reasoning and information retrieval from external sources (including the web).

However, the enhanced strategic competence and tool-augmented abilities conferred by MENTOR also introduce potential risks. Since our distilled agents are capable of autonomous reasoning, web retrieval, and code execution, they could be susceptible to misuse. Potential malicious behaviors include the automated generation of harmful scripts, the execution of unauthorized actions, or the spread of misinformation via tool-based retrieval. To ensure responsible deployment, the integration of robust safeguards is essential. We emphasize that addressing these ethical and safety concerns is an important direction for future research and responsible development in the field of small language agents.

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A Details for Experimental Setup

A.1 Training Dataset Details

To train our models for effective tool use, we construct a high-quality dataset of reference trajectories, as described in Section 3.1. To this end, we use the nvidia/AceReason-Math[2] (Chen et al., 2025b) dataset as our source, leveraging its verified questions and ground-truth answers to ensure reliability.

The construction process involves providing these questions to our teacher model, Qwen3-235B, which generated solution trajectories using a calculator tool. We then filter these outputs, retaining only the **successful trajectories** where the teacher's final answer matched the ground-truth from the source dataset. This verification process yields a final training set of 1.27k single- and multi-turn trajectories that exemplify successful tool use.

A.2 Versions of Models

We employ Qwen3-235B-Thinking (Qwen3, 2025) as the teacher model and four student models from both Qwen3 (Qwen3, 2025) and Qwen2.5 (Yang et al., 2024) families. The specific model versions and their Hugging Face identifiers are listed in Table 4.

Role	Model	Hugging Face Identifier
Teacher	Qwen3-235B-Thinking	`Qwen/Qwen3-235B-A22B-Thinking-2507-FP8`
Student	Qwen2.5-1.5B-Instruct	`Qwen/Qwen2.5-1.5B-Instruct`
	Qwen2.5-7B-Instruct	`Qwen/Qwen2.5-7B-Instruct`
	Qwen3-1.7B	`Qwen/Qwen3-1.7B`
	Qwen3-8B	`Qwen/Qwen3-8B`

Table 4: Model versions used in experiments

A.3 Benchmarks

We use the MATH[3], Omni-MATH-512[4], AIME24[5], AIME25[6], amc23[7], and minervamath[8] datasets. All datasets are publicly available for research use.

[2] https://hf.co/datasets/nvidia/AceReason-Math

[3] https://hf.co/datasets/prithivMLmods/Math-Forge-Hard

[4] https://hf.co/datasets/Heng1999/Omni-MATH-512

[5] https://hf.co/datasets/math-ai/aime24

[6] https://hf.co/datasets/math-ai/aime25

[7] https://hf.co/datasets/math-ai/amc23

[8] https://hf.co/datasets/math-ai/minervamath

A.4 Teacher-Student Alignment Metric

To quantify alignment in tool usage patterns, we compare the distributions of tool calls across the 12 available tools, which are defined in Table 11. Given the teacher's tool distribution P and a student's distribution Q, we use an alignment score based on the Jensen-Shannon Divergence (JSD), defined as:

$$\begin{aligned} \text{Alignment}(P, Q) &= 1 - \text{JSD}(P, Q) \\ \text{where JSD}(P, Q) &= \sqrt{\frac{1}{2}\mathbb{D}_{KL}(P\|M) + \frac{1}{2}\mathbb{D}_{KL}(Q\|M)} \\ \text{and } M &= \frac{1}{2}(P + Q) \end{aligned} \tag{8}$$

The score is bounded between 0 and 1, where 1 signifies a perfect match. $\mathbb{D}_{KL}$ denotes the Kullback-Leibler divergence.

A.5 Hyperparameters for Training and Inference

Our training is conducted on 1×8 Nvidia H100 80G GPUs, with full parameter optimization and gradient checkpointing. We provide some important parameter settings in Tables 5 and 6.

Parameter	Value
Learning Rate	1e-6
Optimizer	AdamW
Epochs	2
Train Batch Size	16
Mini-batch Size	8
Max Sequence Length	32768
Max Response Length	8192
Number of Rollout	10
Tensor Model Parallel Size	2
Rollout Temperature (Qwen3)	0.6
Rollout Temperature (Qwen2.5)	0.7
GPU Utilization Ratio	0.8
KL Loss Coefficient	0.001
Clip Ratio	0.2
Reward Weights (w_c, w_a, w_v)	0.7, 0.3, 0.1

Table 5: Implementation details of MENTOR.

Parameter	Value
Learning Rate	1e-7
Optimizer	AdamW
Epochs	1
Train Batch Size	4
Gradient Accumulation Steps	16
Weight decay	0.033
Gradient Accum	8

Table 6: Implementation details of SFT.

B Details of Instruction Prompts

We utilize prompts for both reference trajectory generation and model evaluation. The specific

prompt for reference trajectory generation is shown in Table 8. For evaluation, we assess the robustness of MENTOR and the baseline models using prompts tailored to each of the three domains. All evaluation prompts for the Qwen2.5 and Qwen3 models are created by adapting the official chat templates provided with each model's tokenizer. The prompts are shown in Tables 7, 8, 9, and 10. The instruction prompts used for evaluating the BFCL-v4 benchmark directly follow the format and content specified on the official benchmark website [9], ensuring consistency with prior work [10].

C Tool Execution via Remote Server

All tools described in Tables 11, and 12 are implemented as executable Python code. For tool execution, we use a FastAPI-based remote execution server, following the base architecture of the ReCall framework (Chen et al., 2025a). Our implementation code is publicly available[11].

When an agent invokes a tool, the system sends the tool's Python code to the remote server via HTTP API. The server executes the code in a preconfigured environment with necessary libraries installed and returns the result.

[9] https://gorilla.cs.berkeley.edu/blogs/15_bfcl_v4_web_search.html

[10] https://github.com/ShishirPatil/gorilla/tree/main/berkeley-function-call-leaderboard

[11] https://anonymous.4open.science/r/MENTOR-F6E7/

Prompt for Qwen2.5 + MATH

SYSTEM:

```
system
You are Qwen, created by Alibaba Cloud. You are a helpful assistant.

# Tools

You may call one or more functions to assist with the user query.

You are provided with function signatures within <tools></tools> XML
    tags:
<tools>
{"type": "function", "function": {"name": "add", ...}}
{"type": "function", "function": {"name": "subtract", ...}}
{"type": "function", "function": {"name": "multiply", ...}}
...
{"type": "function", "function": {"name": "modulo", ...}}
</tools>

For each function call, return a json object with function name and
    arguments within <tool_call></tool_call> XML tags:

<tool_call>
{"name": <function-name>, "arguments": <args-json-object>}
</tool_call>
```

USER:

```
Question: Cities $A$ and $B$ are $45$ miles apart. Alicia lives in $A$
     and Beth lives in $B$. Alicia bikes towards $B$ at 18 miles per
    hour. Leaving at the same time, Beth bikes toward $A$ at 12 miles
    per hour. How many miles from City $A$ will they be when they meet
    ?

If you have got the answer, enclose it within \boxed{} with latex
    format.
```

Table 7: Prompt for Qwen2.5 + MATH

Prompt for Qwen3 + MATH

SYSTEM:

```
system
# Tools

You may call one or more functions to assist with the user query.

You are provided with function signatures within <tools></tools> XML
    tags:
<tools>
{"type": "function", "function": {"name": "add", ...}}
{"type": "function", "function": {"name": "subtract", ...}}
{"type": "function", "function": {"name": "multiply", ...}}
...
{"type": "function", "function": {"name": "modulo", ...}}
</tools>

For each function call, return a json object with function name and
    arguments within <tool_call></tool_call> XML tags:
<tool_call>
{"name": <function-name>, "arguments": <args-json-object>}
</tool_call>
```

USER:

```
Question: Cities $A$ and $B$ are $45$ miles apart. Alicia lives in $A$
     and Beth lives in $B$. Alicia bikes towards $B$ at 18 miles per
    hour. Leaving at the same time, Beth bikes toward $A$ at 12 miles
    per hour. How many miles from City $A$ will they be when they meet
    ?

If you have got the answer, enclose it within \boxed{} with latex
    format.
```

Table 8: Prompt for Qwen3 + MATH

Prompt for Qwen2.5 + RAG

SYSTEM:

```
system
You are Qwen, created by Alibaba Cloud. You are a helpful assistant.

# Tools

You may call one or more functions to assist with the user query.

You are provided with function signatures within <tools></tools> XML
    tags:
<tools>
{"type":"function", "function":{
  "name":"wikipedia_search",
  "description":"Search Wikipedia for a given query.",
  "parameters":{"type":"object", "properties":{
    "query":{"type":"string", "description":"Query to search for."},
    "top_n":{"type":"integer", "description":"Number of results to
        return. The default value is 5.", "default":5}},
   "required":["query"]}}}
</tools>

For each function call, return a json object with function name and
    arguments within <tool_call></tool_call> XML tags:

<tool_call>
{"name": <function-name>, "arguments": <args-json-object>}
</tool_call>
```

USER:

```
Question: What is the capital of France?

If you have got the answer, enclose it within \boxed{} with latex
    format.
```

Table 9: Prompt for Qwen2.5 + RAG

Prompt for Qwen3 + RAG

SYSTEM:

```
system
# Tools

You may call one or more functions to assist with the user query.

You are provided with function signatures within <tools></tools> XML
    tags:
<tools>
{"type":"function", "function":{
  "name":"wikipedia_search",
  "description":"Search Wikipedia for a given query.",
  "parameters":{"type":"object", "properties":{
    "query":{"type":"string", "description":"Query to search for."},
    "top_n":{"type":"integer", "description":"Number of results to
        return. The default value is 5.", "default":5}},
   "required":["query"]}}}
</tools>

For each function call, return a json object with function name and
    arguments within <tool_call></tool_call> XML tags:
<tool_call>
{"name": <function-name>, "arguments": <args-json-object>}
</tool_call>
```

USER:

```
Question: What is the capital of France?

If you have got the answer, enclose it within \boxed{} with latex
    format.
```

Table 10: Prompt for Qwen3 + RAG

Function	Description	Parameter Name	Parameter Description
add	Add two numbers together	firstNumber secondNumber	The first number The second number
subtract	Subtract one number from another	minuend subtrahend	The number to subtract from The number to subtract
multiply	Multiply two numbers together	firstNumber secondNumber	The first number The second number
divide	Divide one number by another	numerator denominator	The number to be divided The number to divide by
sum_numbers	Calculate the sum of an array of numbers	numbers	Array of numbers to sum
floor	Calculate the floor of a number	number	Number to find the floor of
ceil	Calculate the ceil of a number	number	Number to find the ceil of
round_number	Round a number to the nearest integer	number	Number to round
power	Calculate base raised to the power of exponent	base exponent	The base number The exponent
sqrt	Calculate the square root of a number	number	Number to find the square root of
abs_value	Calculate the absolute value of a number	number	Number to find the absolute value of
modulo	Calculate the modulo of two numbers	dividend divisor	The dividend The divisor

Table 11: Math Tool Functions

Function	Description	Parameter Name (Type)	Parameter Description
wikipedia_search	Search Wikipedia for a given query.	query (string) top_n (integer)	Query to search for. Number of results to return. (Optional, default: 5)

Table 12: RAG Tool Function