
SegCSR: Weakly-Supervised Cortical Surfaces Reconstruction from Brain Ribbon Segmentations

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Abstract

1 Deep learning-based cortical surface reconstruction (CSR) approaches typically
2 rely on supervision information provided by pseudo ground truth generated by
3 conventional CSR methods, subject to errors associated with the supervision in-
4 formation and also increasing computational cost of training data preparation. We
5 propose a new method to jointly reconstruct multiple cortical surfaces using *weak*
6 *supervision* from brain MRI ribbon segmentation results. Our approach initializes a
7 midthickness surface, which is then deformed inward and outward to form the inner
8 (white matter) and outer (pial) cortical surfaces, respectively, by jointly learning
9 diffeomorphic flows by minimizing loss functions to optimize the surfaces towards
10 the boundaries of the cortical ribbon segmentation maps. Specifically, a boundary
11 surface loss drives the initialization surface to the inner and outer boundaries, while
12 an inter-surface normal consistency loss regularizes the pial surface in challenging
13 deep cortical sulci regions. Additional regularization terms are utilized to enforce
14 edge length uniformity and smoothness of the reconstructed surfaces. Our method
15 has been evaluated on two large-scale adult brain MRI datasets and one infant brain
16 MRI dataset, demonstrating comparable or superior performance in CSR in terms
17 of accuracy and surface regularity compared to alternative supervised deep learning
18 methods.

19 1 Introduction

20 Cortical surface reconstruction (CSR) is a crucial step for both qualitative visualization and quan-
21 titative characterization of cortical surfaces in imaging studies of brain morphology [15, 51], neu-
22 rodegenerative diseases [6, 12, 43], and psychological disorders [42]. Well-established cortical
23 analysis pipelines, such as BrainSuite [48], FreeSurfer [17], Connectome Workbench [18], and
24 iBEAT V2.0 [52], have achieved significant success in reconstructing cortical surfaces from brain
25 MRI data. However, these pipelines typically involve multiple processing steps, including iterative
26 surface deformation and topology check and correction, resulting in lengthy processing time (e.g.,
27 ~6h/subject). Moreover, each pipeline requires meticulously tuned parameters, posing challenges for
28 generalization across diverse data domains, age groups, or acquisition protocols.

29 Deep learning (DL) approaches have significantly accelerated CSR, demonstrating orders of magni-
30 tude faster inference speeds while maintaining high accuracy and topology correctness [8, 11, 13,
31 22, 26, 30–32, 41, 47, 54]. One line of research predicts implicit surface representations, such as
32 signed distance functions [13, 21] or level sets [41], from which 3D meshes are extracted using the
33 Marching Cube (MC) algorithm [27] and refined with topology correction algorithms [4] to detect
34 and rectify topology errors, ensuring that the reconstructed surface conforms to a sphere-like topology.
35 Another line of research focuses on learning explicit surface deformations, using methods such as
36 flow-based [8, 11, 22, 26, 47, 54] or NODE-based techniques [30, 31]), to deform an initial mesh
37 towards target cortical surfaces. However, all these methods heavily rely on supervision information

38 provided by pseudo ground truth (pGT) of cortical surfaces generated by conventional CSR methods ,
39 regardless of whether they use implicit or explicit surface representations. The prolonged processing
40 time for generating pGT surfaces limits the collection of sufficiently large datasets for training,
41 and a general pipeline capable of extracting pGT surfaces across various data domains (e.g., age,
42 modality) is currently lacking. Conversely, segmentation of brain structures is comparatively simpler,
43 inspiring us to explore avenues to eliminate the need for supervised learning in CSR and to generalize
44 *DL-based CSR* approaches to scenarios where ribbon segmentation results are readily available.

45 The key challenges for achieving accurate weakly supervised reconstruction of cortical surfaces
46 span three primary aspects. *First*, devising sub-voxel supervision signals presents a formidable
47 hurdle. While existing approaches can produce precise segmentations [7, 20, 29, 45, 52], voxel-level
48 representations may struggle to capture the intricate morphology of the cerebral cortex, especially
49 its thin and highly-folded structure, due to the partial volume effect (PVE) inherent in brain MRI
50 scans. This problem becomes particularly prominent in deep cortical sulci [17], where the two banks
51 of grooves nearly converge, or in low-resolution images [52], such as under-sampled or infant MRIs.
52 *Second*, effectively modeling the interdependence between multiple surfaces is crucial. Incorporating
53 this prior knowledge into the design of models and training algorithms can alleviate the complexity
54 of reconstructing both the inner (white matter) and outer (pial) surfaces, ensuring the spherical
55 topology of the reconstructed surfaces [8, 54]. However, in the absence of pGT, it becomes more
56 challenging to forcibly deform surfaces and less stable to optimize multiple surfaces concurrently.
57 *Third*, maintaining optimal surface topology is paramount. Mesh uniformity, smoothness, and
58 topology are susceptible to distortion during large deformations if networks are optimized based on
59 randomly sampled vertices in 3D space for dense volumetric fields.

60 In this paper, we introduce *SegCSR*, a novel weakly supervised DL framework aimed at reconstructing
61 multiple cortical surfaces using ribbon segmentations derived from brain MRIs. We address the
62 diffeomorphic deformation problem in a continuous coordinate space, deforming the initialization
63 midthickness surface towards the target inner and outer surfaces via innovative loss functions.
64 Specifically, the boundary surface loss function based on the ribbon segmentations and the intensity
65 gradient loss function based on the raw image facilitate sub-voxel-level surface movement. The
66 inter-surface normal consistency loss function explicitly integrates the normal directions of the WM,
67 midthickness, and pial surfaces, thereby regularizing the pial surface in challenging deep cortical
68 sulci regions. Furthermore, we devise a customized edge length loss, in conjunction with the known
69 normal consistency loss, to ensure surface uniformity and smoothness. Our main contributions can
70 be summarized as follows:

- 71 • We propose a new weakly supervised paradigm for reconstructing multiple cortical surfaces,
72 reducing the dependence on pGT cortical surfaces in training, unlike existing DL methods.
- 73 • We design two loss functions to optimize the surfaces towards the boundary of the cortical
74 ribbon segmentation maps, along with regularization terms to enforce regularity of surfaces.
- 75 • We conduct extensive experiments on two large-scale adult brain MRI datasets and one
76 infant brain MRI dataset. Our new method achieves comparable or superior performance
77 compared to existing supervised DL-based CSR alternatives.

78 2 Related Works

79 **Cortical Surface Reconstruction (CSR).** (I) *Traditional CSR methods* typically rely on empirically
80 defined automatic image/surface processing techniques to accomplish tissue segmentation (e.g., WM,
81 GM, cerebrospinal fluid (CSF)), hemisphere separation, subcortical filling, topology correction, WM
82 surface reconstruction, and pial surface reconstruction sequentially. Established pipelines such as
83 FreeSurfer [17], BrainSuite [48], and HCP [18] are tailored for processing adult brain images, while
84 dHCP [34] and iBEAT V2.0 [52] are designed for neonatal brain images, which exhibit distinct
85 differences in intensity values, size, and shape compared to adult brains. Despite achieving sub-voxel
86 accuracy and maintaining spherical topology, the iterative surface deformation and topology check and
87 correction procedures lead to lengthy processing times. (II) *DL-based CSR methods* have significantly
88 enhanced reconstruction speed while preserving high accuracy. Approaches like SegRecon [19] and
89 DeepCSR [13] predict a signed distance map for implicit surface representation, embedding the target
90 surface as the zero level-set and extracting it using MC algorithms. However, these methods require
91 topology correction to eliminate artifacts and ensure spherical topology. Alternatively, PialNN [32],
92 TopoFit [22], Vox2cortex [8], the CorticalFlow series [26, 47], SurfFlow [11], CortexODE [31],

93 and CoCSR [54] leverage explicit representation to maintain good topology and overcome PVE by
94 learning volumetric or vertex-wise diffeomorphic deformations and progressively deforming genus-0
95 template meshes. However, both implicit and explicit methods heavily rely on the supervision of pGT
96 of cortical surfaces generated by traditional pipelines. Our proposed method is based on the explicit
97 representation but differs significantly from them by utilizing ribbon segmentation maps for weakly
98 supervising the model training process.

99 **Weakly-/Un-supervised Mesh Reconstruction.** Although geometric DL methods for general
100 computer vision tasks have been extensively studied, research on mesh reconstruction from 3D
101 images under weakly-/un-supervised settings is relatively underexplored. One approach involves
102 constructing mesh-to-image rasterizer loss functions, as demonstrated in [36], where 2D projection
103 views are extracted from predicted 3D meshes and compared with ground truth segmentations.
104 Another line of research, exemplified by [39], focuses on learning the correspondence between
105 a template image and a target image, which is then utilized to deform the template mesh to the
106 target location. However, these methods have primarily been applied to biomedical tasks involving
107 organs with relatively simple shapes, such as the liver and heart. But the cerebral cortex presents a
108 highly-folded thin structure with a significantly complex shape, necessitating more advanced methods.

109 **Diffeomorphic Deformation.** Diffeomorphic deformation is a spatial transformation that guarantees
110 both smoothness and invertibility in the mapping process [46]. It has been widely used in the
111 modeling and analysis of brain morphometry, including image registration and surface reconstruction
112 tasks. LDDMM [5] computes diffeomorphic deformation based on a time-dependent velocity vector
113 field, while Arsigny et al. [2] employ a stationary velocity field (SVF) in conjunction with the
114 scaling and squaring method to reduce computation complexity. Learning-based methods [3, 28,
115 38] improve the computation efficiency, with regularizations such as smoothness [3] and inverse-
116 consistency [38] enhancing the diffeomorphic property of the deformation. In the CSR task,
117 diffeomorphic deformation strategies have been adopted to solve an ordinary differential equation
118 (ODE) modeling the trajectories of each vertex of a surface. For instance, CorticalFlow methods [26,
119 47] propose solving the ODE vertex-wise and derive a numerical condition to ensure homeomorphism
120 of integration by training a *chain* of diffeomorphic deformation models in *sequential* stages. Recently,
121 with the advances in neural ODE solver [10], CortexODE [31] parameterizes the trajectories of
122 vertices on the surface as ODEs and proposes a pipeline to reconstruct WM and pial surfaces
123 *sequentially*. Our method builds upon these works [31, 47, 54] and integrates multiple CSR tasks
124 into a single framework, leveraging the efficiency and diffeomorphic properties of these strategies.

125 3 Methodology

126 Our proposed framework, depicted in Fig. 1, is designed to reconstruct multiple cortical surfaces
127 simultaneously, eliminating the dependency on pGT generated by conventional and time-consuming
128 CSR pipelines. We leverage as weak supervision the brain ribbon segmentation maps that are less
129 accurate than pGT surfaces but more accessible. Section 3.1 outlines the network structure that couples
130 multiple cortical surfaces to reduce the learning difficulty. Section 3.2 describes the loss functions
131 devised to supervise the network optimization, facilitating sub-voxel reconstruction accuracy and
132 preserving optimal surface topology.

133 3.1 Coupled Cortical Surface Reconstruction

134 Existing supervised methods require pGT obtained from traditional CSR pipelines to provide precise
135 sub-voxel supervision. They can effectively learn the deformation field, even from distant initial
136 locations, to accurately align the initialization surface with the target surfaces [11, 26, 47]. However,
137 brain ribbon segmentation maps are inherently discrete voxel grids, offering much coarser supervision.
138 Consequently, the selection of the initialization surface becomes more critical. Moreover, given the
139 intricate folded patterns of the cerebral cortex, the proximity of the two banks of grooves in deep
140 cortical sulci often poses a considerable risk of generating topology errors (e.g., handles, holes) in the
141 reconstructed surfaces. Conversely, voxels closer to the WM surface exhibit clearer contrast, enabling
142 a distinct separation between sulci (Fig. 2 (b)). Thus, following [54], we opt for the midthickness
143 layer, positioned midway between the WM and pial surfaces, to serve as a connection for coupling
144 the reconstructions of both surfaces and achieve a balanced performance for both surfaces.

145 As illustrated in Fig. 1, SegCSR employs a neural network to jointly model three diffeomorphic flows:
146 $F_{\theta}(I, S_0) = (\mathbf{v}^m, \mathbf{v}^o, \mathbf{v}^i)$. Here, I represents a multi-channel input consisting of brain MRI, cortical

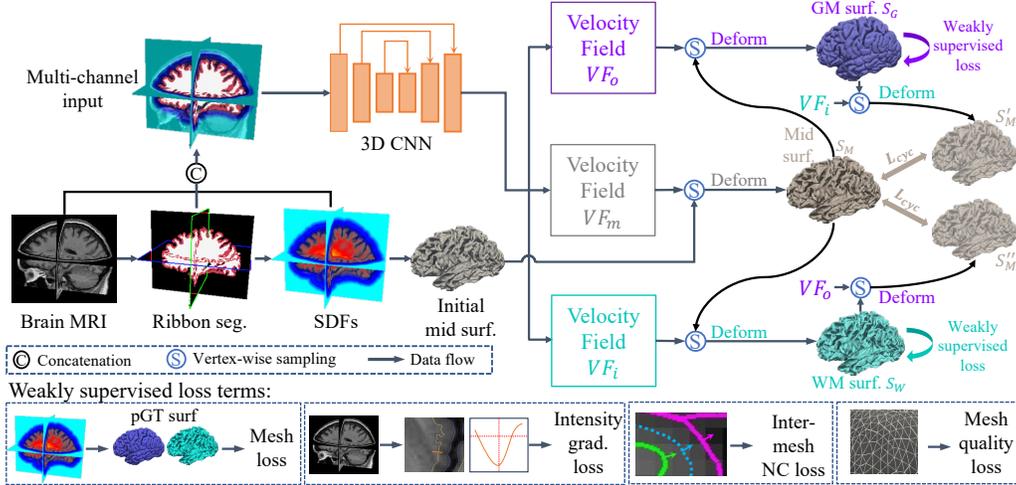


Figure 1: The SegCSR framework overview. SegCSR takes as input a brain MRI image, cortical ribbon segmentation maps, and signed distance maps of cortical surfaces, and simultaneously learns three diffeomorphic deformations to optimize the initial midthickness surface S_0 to align with the target midthickness surface S_M , and then deform S_M outwards and inwards to the pial surface S_G and the WM surface S_W , respectively. The model is optimized using weakly supervised loss functions: the mesh loss guides the surfaces towards the boundaries of the cortical ribbon segmentation maps; the inter-surface normal consistency loss regularizes the pial surface in deep cortical sulci; the intensity gradient loss facilitates sub-voxel-level movement; and additional regularization terms control the deformation trajectories of multiple surfaces as well as the uniformity and smoothness of the surfaces.

147 ribbon masks, and signed distance functions (SDFs); S_0 denotes the initialization midthickness
 148 surface; and \mathbf{v}^m , \mathbf{v}^o , \mathbf{v}^i correspond to the velocity fields that drive S_0 towards the true midthickness
 149 surface S_M , outward to the pial surface S_G , and inward to the WM surface S_W , respectively. The
 150 SegCSR establishes an explicit *one-to-one mapping* between multiple surfaces and is trained by
 151 minimizing weakly supervised losses between the predicted mesh and the ribbon segmentations.

152 The diffeomorphic deformation between the initialization surface and the target surface can be
 153 computed as the integration of an ODE [1] based on the velocity field \mathbf{v} :

$$\frac{d\Phi(\mathbf{x}, t)}{dt} = \mathbf{v}(\Phi(\mathbf{x}, t), t) \text{ s.t. } \Phi(\mathbf{x}, 0) = \mathbf{x}^{(0)}, \text{ and thus } \Phi(\mathbf{x}, t) = \mathbf{x}^{(0)} + \int_0^t \mathbf{v}(\Phi(\mathbf{x}, s), s) ds, \quad (1)$$

154 where $\Phi(\mathbf{x}, t)$ defines a trajectory from the source position $\mathbf{x}^{(0)} = \Phi(\mathbf{x}, 0)$ to the target position
 155 $\mathbf{x}^{(1)} = \Phi(\mathbf{x}, 1)$. According to the *Cauchy-Lipschitz* theorem [50], if the velocity field is Lipschitz
 156 continuous, the resulting mapping Φ is bijective with continuous inverse (i.e., a diffeomorphism).
 157 To solve this initial value problem, we perform the integration on the predicted velocity fields
 158 using standard numerical integration techniques, such as the Euler method and the Runge-Kutta
 159 method [9]. Specifically, for each integration step $t \in [0, 1]$, each vertex's coordinates can be updated
 160 by $\mathbf{x}^{(t+1)} = \mathbf{x}^{(t)} + h\mathbf{v}(\Phi(\mathbf{x}, t), t)$, where $h = \frac{1}{T}$ is the step size and T is the total time steps, and
 161 the velocity vector \mathbf{v} for a vertex is trilinearly interpolated from its neighboring velocity vectors [54].

162 3.2 Weak Supervision Loss Functions

163 **Mesh Loss.** Weak supervision for SegCSR is derived from cortical ribbon segmentation maps of
 164 WM and GM (see Fig. 1, the filled interior area of WM and pial surfaces), which can be obtained
 165 from existing segmentation approaches [7, 20, 29, 45, 52]. Although these ribbon segmentation
 166 maps do not perfectly represent the intricate pial surface, the WM surface is relatively easier to
 167 recognize due to its clear local intensity contrast, providing a better-separable boundary (see Fig. 2
 168 (a-b)). Therefore, we use the boundary of the pGT WM segmentation to supervise the WM surface
 169 reconstruction. Inspired by [31, 54], we generate an SDF for the WM surface by using a distance
 170 transform algorithm, where voxels with values of zero represent the surface boundaries and voxels
 171 with negative or positive values encode their distances to the surface boundaries inward or outward,

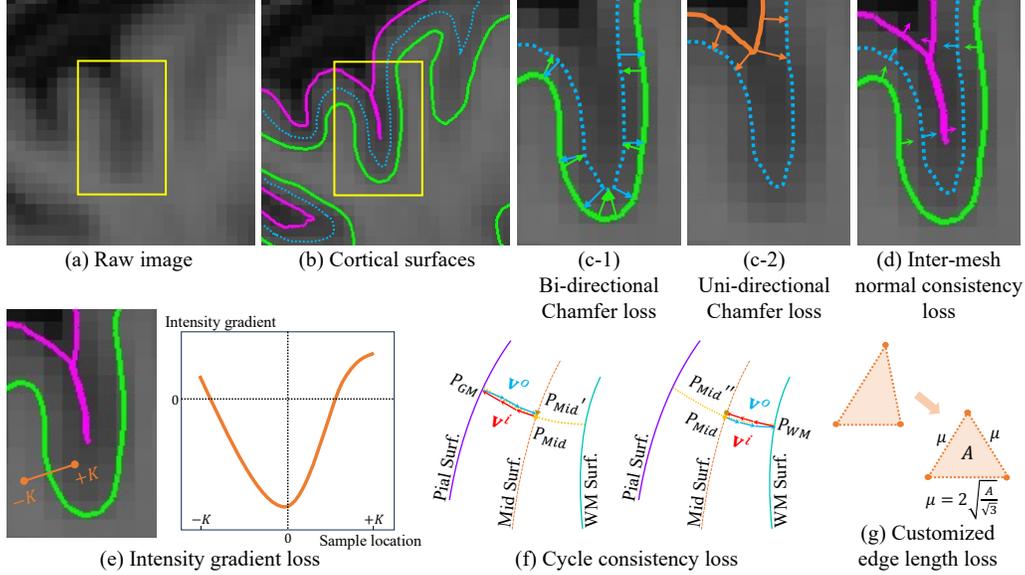


Figure 2: (a) A brain MRI region. (b)-(g) are illustration of loss terms. (b) WM, midthickness, pial surfaces in a deep sulcus region. (c-1) Bi-directional Chamfer loss for the WM surface; (c-2) Uni-directional Chamfer loss for the pGT pial surface generated from the GM segmentation. (d) Normal consistency between three reconstructed surfaces. (e) Intensity gradient along the normal direction of a vertex in the surface. (f) The symmetric deformation trajectory. \mathbf{v}^o and \mathbf{v}^i are outward and inward velocity fields respectively. (g) The customized edge length loss. A : area; μ : edge length.

172 respectively. We then apply a fast topology check and correction algorithm [4] to the SDF to ensure
 173 the surface maintains spherical topology. The WM surface \mathcal{S}_{W^*} is extracted using the Marching
 174 Cubes algorithm [27]. The distance of the vertices between the predicted surface \mathcal{S}_W and the pGT
 175 surface \mathcal{S}_{W^*} is minimized using the bi-directional Chamfer distance [26]:

$$\mathcal{L}_{chW} = \frac{1}{|\mathcal{S}_W|} \sum_{\mathbf{p} \in \mathcal{S}_W} \min_{\mathbf{p}_* \in \mathcal{S}_{W^*}} \|\mathbf{p} - \mathbf{p}_*\|_2^2 + \frac{1}{|\mathcal{S}_{W^*}|} \sum_{\mathbf{p}_* \in \mathcal{S}_{W^*}} \min_{\mathbf{p} \in \mathcal{S}_W} \|\mathbf{p}_* - \mathbf{p}\|_2^2, \quad (2)$$

176 where \mathbf{p} and \mathbf{p}_* are the coordinates of vertices on meshes. See Fig. 2 (c-1) for illustration.

177 For the pial surface, GM segmentation may fail to delineate the boundary in deep cortical sulci.
 178 As shown in Fig. 2 (c-2), using a similar pGT surface generation protocol as the WM surface to
 179 generate the pial surface \mathcal{S}_{G^*} fail to capture cortical folding accurately. Directly fitting to \mathcal{S}_{G^*} with
 180 bi-directional Chamfer loss causes the model to predict similarly inaccurate cortical sulci. To address
 181 this issue, we propose the boundary surface loss, which uses a uni-directional Chamfer distance to
 182 compute the shortest distance from the pGT pial surface \mathcal{S}_{G^*} to the predicted pial surface \mathcal{S}_G :

$$\mathcal{L}_{chG} = \frac{1}{|\mathcal{S}_G|} \sum_{\mathbf{p} \in \mathcal{S}_G} \min_{\mathbf{p}_* \in \mathcal{S}_{G^*}} \|\mathbf{p} - \mathbf{p}_*\|_2^2. \quad (3)$$

183 In this way, the deformed surface is not influenced by the inaccuracies of \mathcal{S}_{G^*} and does not move
 184 outward from the deep sulci. The overall mesh loss is computed as $\mathcal{L}_{mesh} = \mathcal{L}_{chW} + \mathcal{L}_{chG}$.

185 **Inter-Mesh Normal Consistency Loss.** To further alleviate the difficulty of constraining the pial
 186 surface using the WM and midthickness surfaces, we propose leveraging the prior knowledge that
 187 the cerebral cortex has a sheet-like topology (i.e., the inner, middle, and outer surfaces are locally
 188 parallel to each other). As shown in Fig. 2 (d), this loss is defined to ensure that the deformation
 189 of the midthickness surface aligns with its normal direction, thereby maintaining similar normal
 190 directions on the target surfaces:

$$\mathcal{L}_{imnc} = \frac{1}{|\mathcal{S}_M|} \sum_{\mathbf{p} \in \mathcal{S}_M} (1 - \cos(\mathbf{n}_{\mathbf{p}_G}, \mathbf{n}_{\mathbf{p}_W})), \quad (4)$$

191 where $\mathbf{n}_{\mathbf{p}_G}$ and $\mathbf{n}_{\mathbf{p}_W}$ are the normal vectors of the deformed vertex \mathbf{p} on \mathcal{S}_M and \mathcal{S}_G respectively.

192 **Intensity Gradient Loss.** In addition to ribbon segmentations, inspired by the fact that traditional
 193 methods utilize raw image intensity contrast to define and optimize the target surfaces, we propose to
 194 adjust the nuance between GT target surface and the pGT segmentation boundaries. By definition [17,
 195 52], the WM (or pial) surface lies at the WM/GM (or GM/CSF) interface where image intensity change
 196 most drastically. We sample K points along the extended lines on each side of the normal direction at
 197 vertex \mathbf{p} , and compute the gradients of neighboring points: $\mathcal{L}_{grad} = \frac{1}{|\mathcal{S}_W|} \sum_{\mathbf{p} \in \mathcal{S}_M} \sum_{i=1}^K grad_i(\mathbf{p}) +$
 198 $\frac{1}{|\mathcal{S}_G|} \sum_{\mathbf{p} \in \mathcal{S}_G} \sum_{i=1}^K grad_i(\mathbf{p})$.

199 **Cycle Consistency Loss.** We utilize the midthickness layer to establish a correspondence between
 200 the inner and outer surfaces, thereby reducing the difficulty of learning large deformations. However,
 201 there is no true midthickness surface available for supervision, nor a definitive criterion for choosing
 202 between bi-directional or uni-directional approaches for different regions on the midthickness surface.
 203 Additionally, the learned velocity fields \mathbf{v}^o and \mathbf{v}^i could potentially cause non-inverse transformations
 204 at the midthickness surface. To address these issues, we propose a loss function that enforces the
 205 midthickness surface resides halfway between the WM and pial surfaces and maintains consistency
 206 along the entire trajectory:

$$\mathcal{L}_{cyc} = \frac{1}{|\mathcal{S}_M|} \sum_{\mathbf{p} \in \mathcal{S}_M} \|\mathbf{p}_{\Phi_W \circ \Phi_G} - \mathbf{p}\|_2^2 + \|\mathbf{p}_{\Phi_G \circ \Phi_W} - \mathbf{p}\|_2^2 + \|L_{Mid \rightarrow GM}(\mathbf{p}) - L_{Mid \rightarrow WM}(\mathbf{p})\|_2^2, \quad (5)$$

207 where $\mathbf{p}_{\Phi_b \circ \Phi_a}$ represents deforming a vertex $\mathbf{p} \in \mathcal{S}_M$ with velocity field \mathbf{v}^a and \mathbf{v}^b sequentially, and
 208 $L_{Mid \rightarrow GM}(\mathbf{p})$ is the accumulated trajectory length over T steps of deformation. For example, as
 209 shown in Fig. 2 (f), the deformations move a vertex \mathbf{p}_{Mid} outward to \mathbf{p}_{GM} using \mathbf{v}^o and then inward
 210 to \mathbf{p}'_{Mid} using \mathbf{v}^i , in which the two trajectories are aligned by minimizing the distance between \mathbf{p}_{Mid}
 211 and \mathbf{p}'_{Mid} . Similarly, we enforce the consistency between $\mathbf{p}_{\Phi_G \circ \Phi_W}$ and \mathbf{p} . Furthermore, starting
 212 from the midthickness layer, the trajectory lengths of the vertex moving to the WM and pial surfaces
 213 should be equal, which is regularized by the third term in the equation above.

214 **Mesh Quality Loss.** First, the reconstructed surface should be composed of uniformly distributed
 215 triangles. To accommodate various sizes of brain volume and image resolution, we devise a *cus-*
 216 *tomized edge length loss* to constrain the size of triangles in the predicted meshes for each subject.
 217 Specifically, we assume an ideal prediction where the faces are equilateral and of the same area A
 218 and drive the edge length to the target edge length $\mu_{el} = 2\sqrt{\frac{A}{\sqrt{3}}}$ (see Fig. 2 (g)). Second, we employ
 219 a *normal consistency loss* to promote the surfaces' smoothness. The mesh quality loss is defined as:

$$\mathcal{L}_{qua} = \frac{1}{|S|} \left(\sum_{\mathbf{p} \in S} \frac{1}{|\mathcal{N}(\mathbf{p})|} \sum_{\mathbf{k} \in \mathcal{N}(\mathbf{p})} (\mu_{el} - \|\mathbf{p} - \mathbf{k}\|_2)^2 + \sum_{e \in \mathcal{S}, f_0 \cap f_1 = e} (1 - \cos(\mathbf{n}_{f_0}, \mathbf{n}_{f_1})) \right), \quad (6)$$

220 where \mathcal{S} denotes the predicted mesh, $\mathcal{N}(\mathbf{p})$ are the neighbors of vertex \mathbf{p} , e is an edge, f_0 and f_1 are
 221 e 's two neighboring faces with their unit normals \mathbf{n}_{f_0} and \mathbf{n}_{f_1} .

222 In summary, we combine all the losses to jointly optimize our SegCSR model: $\mathcal{L} = \lambda_1 \mathcal{L}_{mesh} +$
 223 $\lambda_2 \mathcal{L}_{imnc} + \lambda_3 \mathcal{L}_{grad} + \lambda_4 \mathcal{L}_{cyc} + \lambda_5 \mathcal{L}_{qua}$, where $\{\lambda_i\}_{i=1, \dots, 5}$ are weights to balance the loss terms.

224 4 Experiments

225 4.1 Experimental Setups

226 **Datasets.** We evaluate our method on two large-scale adult datasets and one infant dataset of low
 227 resolution. The ADNI-1 [24] dataset consists of 817 subjects aged 55 to 90. We randomly split it into
 228 subsets of 654, 50, and 113 subjects for training, validation, and testing, respectively. The OASIS-
 229 1 [35] dataset consists of 413 subjects aged 18 to 96. We randomly split it into subsets of 330, 25, and
 230 58 subjects for training, validation, and testing, respectively. We followed a pre-processing protocol
 231 used in previous works [8, 13, 26, 31] for fair comparison. The T1-weighted MRI scans were aligned
 232 to the MNI152 template and clipped to the size of $192 \times 224 \times 192$ at $1mm^3$ isotropic resolution.
 233 The pseudo ground-truth (pGT) of ribbon segmentation and cortical surfaces were generated using
 234 FreeSurfer v7.2.0 [17]. The BCP [23] dataset consists of 121 subjects ranging in age from 2 weeks
 235 to 12 months. We randomly allocate 90, 12, and 19 subjects for training, validation, and testing,

Table 1: Quantitative analysis of cortical surface reconstruction on geometric accuracy and self-intersections. The Chamfer distance (CD), average symmetric surface distance (ASSD), Hausdorff distance (HD), and the ratio of the self-intersecting faces (SIF) were measured for WM and pial surfaces on three datasets. The mean value and standard deviation are reported. Lower scores indicate better results for all metrics. ‘‘S’’ denotes the use of pGT surfaces from conventional pipelines, while ‘‘W’’ represents weak supervision by pGT ribbon segmentations. In each supervision setting, the best results are in bold, and the second best results are underlined.

Data	Sup.	Method	L-Pial Surface				L-WM Surface			
			CD (<i>m.m.</i>)	ASSD (<i>m.m.</i>)	HD (<i>m.m.</i>)	SIF (%)	CD (<i>m.m.</i>)	ASSD (<i>m.m.</i>)	HD (<i>m.m.</i>)	SIF (%)
ADNI	S	CorticalFlow++ [47]	0.545±0.036	0.410±0.033	0.886±0.069	0.098±0.067	0.544±0.034	0.401±0.030	0.878±0.066	0.069±0.042
		cortexODE [31]	0.476±0.017	0.214±0.020	0.455±0.058	0.022±0.012	0.458±0.016	0.192±0.015	0.436±0.014	0.015±0.011
		Vox2Cortex [8]	0.582±0.028	0.370±0.025	0.746±0.057	0.059±0.039	0.577±0.027	0.353±0.022	0.722±0.055	0.043±0.023
		CoCSR [54]	0.322±0.021	0.123±0.010	0.267±0.022	0.013±0.011	0.303±0.018	0.117±0.010	0.254±0.021	0.005±0.002
	W	DeepCSR [13]	0.945±0.078	0.593±0.065	1.149±0.203	\	0.938±0.076	0.587±0.064	1.137±0.193	\
		3D U-Net [44]	0.598±0.049	0.341±0.037	0.782±0.163	\	0.473±0.013	0.265±0.015	0.558±0.028	\
		SegCSR (Ours)	0.578±0.019	0.324±0.019	0.749±0.049	0.008±0.009	0.467±0.014	0.258±0.019	0.545±0.036	0.009±0.009
OASIS	S	CorticalFlow++ [47]	0.531±0.035	0.399±0.030	0.812±0.057	0.088±0.045	0.529±0.033	0.398±0.030	0.810±0.055	0.086±0.042
		cortexODE [31]	0.481±0.019	0.218±0.021	0.461±0.062	0.026±0.015	0.463±0.018	0.207±0.017	0.435±0.015	0.018±0.010
		Vox2Cortex [8]	0.588±0.032	0.381±0.030	0.750±0.063	0.061±0.037	0.581±0.028	0.375±0.027	0.731±0.059	0.046±0.027
		CoCSR [54]	0.410±0.034	0.142±0.016	0.281±0.024	0.016±0.012	0.349±0.024	0.128±0.019	0.266±0.022	0.007±0.002
	W	DeepCSR [13]	0.986±0.085	0.617±0.070	1.331±0.212	\	0.975±0.081	0.594±0.067	1.151±0.197	\
		3D U-Net [44]	0.611±0.069	0.332±0.050	0.774±0.267	\	0.454±0.013	0.245±0.017	0.489±0.031	\
		SegCSR (Ours)	0.581±0.016	0.321±0.018	0.725±0.040	0.010±0.010	0.449±0.011	0.223±0.016	0.461±0.027	0.010±0.009
BCP	S	CorticalFlow++ [47]	0.927±0.271	0.731±0.036	1.943±0.175	1.114±0.385	0.895±0.242	0.722±0.034	1.880±0.151	0.533±0.107
		cortexODE [31]	0.759±0.082	0.396±0.032	0.823±0.103	0.124±0.061	0.678±0.071	0.349±0.031	0.816±0.099	0.101±0.034
		CoCSR [54]	0.576±0.041	0.216±0.023	0.468±0.063	0.064±0.040	0.544±0.038	0.199±0.020	0.447±0.049	0.058±0.033
	W	DeepCSR [13]	2.673±1.131	1.224±0.215	3.112±1.218	\	1.440±0.521	0.428±0.051	0.933±0.118	\
		3D U-Net [44]	1.175±0.314	0.793±0.059	2.140±1.021	\	0.688±0.120	0.377±0.041	0.791±0.064	\
		SegCSR (Ours)	0.927±0.070	0.497±0.061	1.287±0.144	0.061±0.058	0.876±0.067	0.478±0.052	1.206±0.132	0.055±0.057

236 respectively. Rigid registration was applied to the T1w and T2w image pairs. The pGT of ribbon
237 segmentation and cortical surfaces were generated by the iBEAT v2.0 [52]. The intensity values of
238 MRI scans, ribbon segmentation maps, and SDFs were normalized to $[0, 1]$ and the coordinates of the
239 vertices were normalized to $[-1, 1]$. All the models were trained on the training set until they reached
240 a loss plateau on the validation set and evaluated on the test set.

241 **Implementation Details** Our framework was implemented in PyTorch [40] and trained on a worksta-
242 tion with 12 GB NVIDIA P100 GPU. The 3D U-Net [44] for segmentation of ribbons was trained for
243 200 epochs using Adam [25] optimization and achieved an average Dice index of 0.96 on the testing
244 set. The SegCSR model utilized $T = 5$ steps (i.e., step size is 0.2) in Euler solver. We trained our
245 SegCSR model using Adam optimizer ($\beta_1 = 0.9$, $\beta_2 = 0.999$, $\epsilon = 1e^{-10}$, learning rate $1e^{-4}$) for
246 400 epochs to reconstruct both WM, midthickness, and pial surfaces of both brain hemispheres. We
247 set $\lambda_1 = \lambda_4 = 1$ and $\lambda_2 = \lambda_3 = \lambda_5 = 0.1$. The surface meshes had $\sim 130k$ vertices. More details
248 can be found in the Supplementary Materials.

249 **Evaluation Metrics** We utilized three distance-based metrics to measure the CSR accuracy: Chamfer
250 distance (CD), average symmetric surface distance (ASSD), and 90th-percentile Hausdorff distance
251 (HD). CD [16, 53] measures the mean distance between two sets of vertices. ASSD [13] and
252 HD [13, 49] measure the average and maximum distance between two surfaces. They were computed
253 bidirectionally over $\sim 130k$ points uniformly sampled from the predicted and target surfaces. A lower
254 distance means a better result. Since topology is also important in CSR, we utilized the ratio of
255 self-intersection faces (SIF) [13, 14, 31, 54] to measure reconstructed surface quality.

256 4.2 Comparison with Related Works

257 We compare SegCSR with both implicit and explicit learning-based cortical surface reconstruction
258 approaches described in Section 1 and summarize the experimental results in Table 5.

259 **On Adult Datasets. (I) Comparison with Implicit Approaches.** We compare SegCSR with two
260 representative implicit representation approaches on the ADNI and OASIS datasets. As shown
261 in Table 5, SegCSR achieves superior geometric accuracy. Note that both DeepCSR [13] and 3D
262 U-Net [44] require post-processing to correct topology and extract a mesh, resulting in SIFs of 0.
263 Without post-processing, the SIFs for 3D U-Net’s WM and pial surfaces range from 3% to 15%.
264 SegCSR produces a negligible number of self-intersecting faces, $\sim 0.3\%$ on average for both white
265 and pial surfaces. Fig. 3 shows that SegCSR effectively deforms the pial surface into deep sulci,
266 while the baseline approaches exhibit large geometric errors due to the PVE problem of brain MRI.

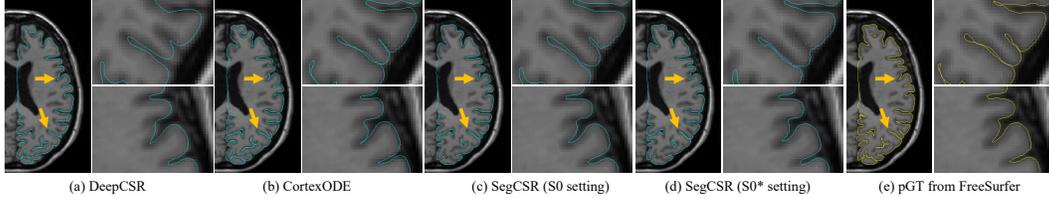


Figure 3: Visualization of reconstructed pial surfaces compared to DeepCSR and CortexODE. CortexODE is trained with pGT from FreeSurfer; DeepCSR and ours are trained with pGT ribbon segmentations.

267 Additionally, SegCSR requires only 0.37s of runtime per brain hemisphere, orders of magnitude
 268 faster than traditional FreeSurfer pipelines. **(II) Comparison with Explicit Approaches.** We compare
 269 SegCSR with explicit learning-based approaches, including CorticalFlow++ [47], Vox2Cortex [8],
 270 CortexODE [31], and CoCSR [54]. These methods are trained with pGT surfaces generated by
 271 conventional pipelines, providing more accurate supervision than pGT ribbon segmentations. For
 272 a fair comparison, we employ the same network structure for the current best CoCSR [54] and our
 273 SegCSR, with CoCSR serving as an upper-bound performance benchmark for our weakly supervised
 274 SegCSR. As shown in Table 5, SegCSR surprisingly surpasses some supervised baselines in terms of
 275 both geometric and morphological accuracy, demonstrating its potential to replace existing methods
 276 when accurate surface supervision is not available.

277 **On Infant Dataset.** Infant brain MRIs present additional challenges due to the smaller size of fetal
 278 brains, limited image resolution, and lower image contrast, which together make the reconstruction
 279 task more difficult. Consequently, overall performance is inferior compared to adult datasets. We
 280 compare SegCSR with both implicit and explicit representation approaches. The results in Table 5
 281 show that SegCSR achieves superior performance than the implicit DeepCSR and 3D U-Net methods,
 282 and comparable performance to explicit methods like CorticalFlow++, CortexODE, and CoCSR.

283 4.3 Ablation Studies

Table 2: Ablation studies on the ADNI dataset. The setting S0 refers to our complete setting (cf. Table 5). Top: The impact of loss functions. Bottom: The impact of initialization surface location.

Setting	Loss					L-Pial Surface				L-WM Surface			
	\mathcal{L}_{mesh}	\mathcal{L}_{imnc}	\mathcal{L}_{grad}	\mathcal{L}_{cyc}	\mathcal{L}_{qua}	CD (mm)	ASSD (mm)	HD (mm)	SIF (%)	CD (mm)	ASSD (mm)	HD (mm)	SIF (%)
S0	✓	✓	✓	✓	✓	0.578±0.019	0.324±0.019	0.749±0.049	0.008±0.009	0.467±0.014	0.258±0.019	0.545±0.036	0.009±0.009
S1	✓	✓	✓	✓	✓	0.576±0.019	0.323±0.019	0.747±0.046	0.012±0.011	0.467±0.015	0.257±0.020	0.542±0.036	0.011±0.011
S2	✓	✓	✓	✓	✓	0.579±0.019	0.325±0.019	0.748±0.047	0.014±0.013	0.469±0.016	0.248±0.019	0.544±0.042	0.015±0.014
S3	✓	✓	✓	✓	✓	0.579±0.020	0.325±0.021	0.749±0.050	0.018±0.014	0.473±0.013	0.249±0.018	0.544±0.039	0.017±0.013
S4	✓	✓	✓	✓	✓	0.589±0.034	0.356±0.039	0.764±0.067	0.015±0.012	0.473±0.012	0.256±0.020	0.564±0.042	0.014±0.013
S0*	✓*	✓	✓	✓	✓	0.607±0.034	0.327±0.024	0.752±0.077	0.026±0.016	0.469±0.015	0.258±0.020	0.547±0.038	0.020±0.015
S4*	✓*	✓	✓	✓	✓	0.626±0.053	0.321±0.039	0.773±0.168	0.034±0.025	0.476±0.013	0.256±0.018	0.562±0.034	0.031±0.017

Init. Surface Location	L-Pial Surface				L-WM Surface			
	CD (mm)	ASSD (mm)	HD (mm)	SIF(%)	CD (mm)	ASSD (mm)	HD (mm)	SIF(%)
WM	0.878±0.077	0.587±0.060	1.084±0.097	0.012±0.011	0.439±0.011	0.211±0.013	0.430±0.028	0.007±0.008
Mid	0.578±0.019	0.324±0.019	0.749±0.049	0.008±0.009	0.467±0.014	0.258±0.019	0.545±0.036	0.009±0.009
GM	0.489±0.016	0.317±0.018	0.567±0.044	0.008±0.008	0.889±0.085	0.597±0.059	1.211±0.104	0.020±0.018

284 **Loss Functions.** We evaluated the contribution of different losses of our method to the surface
 285 reconstruction performance in terms of both accuracy (CD, ASSD, HD) and topological correctness
 286 (SIF). The results are summarized in Table 2 (Top). The setting S4 represents using our proposed
 287 Chamfer loss (i.e., uni-directional for the pial surface) alone, while S4* refers to using existing
 288 bi-directional Chamfer loss for both WM and pial surfaces. The results of S4 and S4* indicated
 289 that the model using bi-directional Chamfer loss overfitted to the pGT segmentation boundary and
 290 failed to fit the deep cortical sulci. Another pair of comparison, S0 and S0*, showed a similar
 291 phenomenon. Enforcing the inter-mesh normal consistency of the WM and pial surfaces (S3, \mathcal{L}_{imnc})
 292 improved geometric accuracy by explicitly constraining the normal direction of two surfaces but
 293 slightly worsened the topology, which might be caused by the discrepancy between the midthickness
 294 and the WM (and pial) surface. The proposed intensity gradient loss (S2, \mathcal{L}_{grad}) helped adjust the
 295 deformed surfaces locally, leading to slightly improved geometric accuracy and reduced topology
 296 error. Enforcing equality of the trajectories from the midthickness surface to the WM and pial surfaces

297 and symmetric cycle consistency of two trajectories ($S1, \mathcal{L}_{cyc}$) helped optimize the midthickness
 298 surface and promoted the invertibility of deformations. Moreover, the inclusion of regularization
 299 terms on the uniformity and smoothness of the reconstructed surfaces ($S0, \mathcal{L}_{qua}$) enhanced the
 300 surface quality and significantly reduce the self-intersection face ratio. Overall, our proposed method
 301 struck a balance between geometric accuracy and topology quality, with each component playing a
 302 complementary role.

303 **Initialization Surface Location.** Table 2 (Bottom) shows the impact of the initialization surface
 304 location. Starting from either the WM or midthickness surfaces leads to satisfactory results. Con-
 305 versely, initializing from the GM surface introduced more difficulty in learning large deformations
 306 into deep sulci due to the severe partial volume effect, resulting in worse average geometric accuracy
 307 for both surfaces. The results also indicated that the closer the initial surface was to its target surface,
 308 the higher the reconstruction accuracy achieved. Therefore, starting from the midthickness surface
 309 strikes a balance between WM and pial surface reconstruction outcomes.

310 4.4 Reproducibility

311 We conducted an experiment on the Test-Retest
 312 dataset [33], which comprises 40 MRIs collected within
 313 a short period for each of the 3 subjects. The cor-
 314 tical surfaces of the same subject should be nearly
 315 identical. Following the experimental setup outlined
 316 in [8, 13, 31, 54], we utilized the iterative closest-point
 317 algorithm to align image pairs and computed the ge-
 318 ometric distance between surfaces. The results for
 319 the left hemisphere are presented in Table 3, showing
 320 that SegCSR obtained superior reproducibility com-
 321 pared with DeepCSR (implicit representation; weakly
 322 supervised) and was comparable to the conventional
 323 FreeSurfer pipeline and supervised DL-based CSR
 324 methods. This implied that the results generated by SegCSR can be reliably used for downstream
 325 analyses, such as investigating cortical thickness changes in patients.

Table 3: Reproducibility analysis.

Method	L-WM Surface		
	CD (<i>mm</i>)	ASSD (<i>mm</i>)	HD (<i>mm</i>)
SegCSR (Ours)	0.473±0.016	0.254±0.024	0.520±0.062
DeepCSR	0.505±0.047	0.297±0.053	0.610±0.100
CoCSR	0.451±0.019	0.235±0.030	0.492±0.059
CortexODE	0.457±0.021	0.238±0.031	0.504±0.071
FreeSurfer	0.476±0.015	0.253±0.022	0.519±0.048
Method	L-Pial Surface		
	CD (<i>mm</i>)	ASSD (<i>mm</i>)	HD (<i>mm</i>)
SegCSR (Ours)	0.529±0.023	0.285±0.033	0.622±0.066
DeepCSR	0.560±0.055	0.341±0.060	0.668±0.118
CoCSR	0.493±0.024	0.276±0.036	0.573±0.070
CortexODE	0.506±0.029	0.272±0.034	0.581±0.079
FreeSurfer	0.526±0.021	0.283±0.032	0.595±0.068

326 5 Conclusions

327 We introduce SegCSR, a novel approach to jointly reconstruct multiple cortical surfaces using
 328 weak supervision from ribbon segmentations derived from brain MRIs. Our method initializes a
 329 midthickness surface and then deforms it inward and outward to the inner and outer cortical surfaces by
 330 jointly learning diffeomorphic flows. The new boundary loss function optimizes the surfaces toward
 331 the boundaries of the cortical ribbon segmentation maps while the inter-surface normal consistency
 332 loss regularizes the pial surface in complex and challenging cortical sulci regions. Additional
 333 regularization terms are incorporated to enforce reconstructed surfaces’ uniformity, smoothness,
 334 and topology. Extensive experiments conducted on large-scale adult and infant brain MRI datasets
 335 demonstrate superior performance in terms of accuracy and surface regularity compared to existing
 336 supervised DL-based alternatives.

337 **Limitations and Future Directions.** The efficacy of SegCSR is influenced by the quality of pGT
 338 segmentations. Also, We can utilize brain tissue segmentation as auxiliary functions to supervise the
 339 model training. SegCSR constrains the inter-mesh consistency of the deformation on the midthickness
 340 surface, potentially affecting anatomical fidelity of pial surfaces. The method should be tested on
 341 more diverse cohorts of subjects to demonstrate its efficacy on real world neuroimaging analysis tasks.

342 **Societal Impact.** Our proposed method has been rigorously evaluated on four real-world brain MRI
 343 datasets, showcasing its capacity to assist doctors and scientists in both quantitative and qualitative
 344 analyses of the cerebral cortex. Nonetheless it is imperative to conduct more thorough evaluation on
 345 a larger cohort of subjects and across various imaging qualities. And the deployment of the model in
 346 clinical settings should be approached with caution and under human supervision.

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496 A Model Details

497 A.1 Cortical Ribbon Segmentation Network Architecture

498 Fig. 4 (Left) shows the detailed network architecture of our cortical ribbon segmentation network,
 499 which is a 5-level hierarchical encoder-decoder with skip connections. The network processes a 3D
 500 brain MRI to produce a cortical ribbon segmentation map. The white matter (WM) segmentation
 501 includes the interior of the WM surface, encompassing cortical WM, deep gray matter, ventricles,
 502 hippocampus, and other tissues within the surface. Similarly, the gray matter (GM) segmentation
 503 includes the interior of the pial surface. The output map has five classes: left hemisphere WM and
 504 GM, right hemisphere WM and GM, and background. In the encoder, each level uses a $3 \times 3 \times 3$
 505 convolutional layer with a stride of 2 to downsample the features. In the decoder, features are
 506 upsampled by $2 \times$ at each scale, concatenated with the corresponding features from the encoder via
 507 skip connections, and then fused using a $3 \times 3 \times 3$ convolutional layer with a stride of 1. For feature
 508 extraction at the input, a $3 \times 3 \times 3$ convolutional layer with a stride of 1 is used. Before the final
 509 prediction, three consecutive convolutional layers are applied. Each convolutional layer is followed
 510 by a leaky ReLU activation function, except for the last one, which uses a Softmax function before
 511 computing the cross-entropy loss with the ground truth.

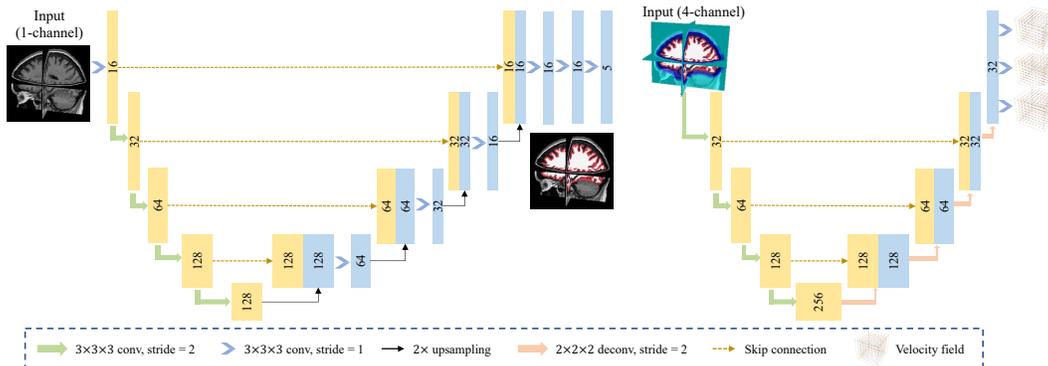


Figure 4: Left: 3D U-Net architecture for ribbon segmentation. The output, i.e., the cortical ribbon map, is overlaid on the input image for illustration. Right: 3D U-Net architecture for cortical surface reconstruction. The learned velocity fields are used to calculate deformations.

512 A.2 Cortical Surface Reconstruction Network Architecture and Training details

513 As shown in Fig. 4 (Right), our cortical surface reconstruction (CSR) network operates at five scales.
 514 To conserve memory, we downsample the input image using a $3 \times 3 \times 3$ convolution with a stride of
 515 2 and skip complex feature fusion via skip connections in the decoding path at this scale. To improve
 516 the accuracy of the velocity fields (VFs), we use $2 \times 2 \times 2$ deconvolutions with a stride of 2 in the
 517 decoding path instead of $2 \times$ trilinear upsampling. At the output stage, we employ three parallel
 518 $3 \times 3 \times 3$ convolutional layers to generate VFs for the white matter (WM), midthickness, and pial
 519 surfaces, respectively. ReLU activation functions are used after each convolutional layer, except for
 520 the three parallel layers, where Softsign functions are applied. The VFs are then utilized to compute
 521 diffeomorphic deformations.

522 B Experimental Settings

523 B.1 Dataset Preprocessing

524 We preprocessed all the MRIs of the ADNI-1 [24] and OASIS-1 [35] datasets with the same protocols
525 as following: Based on the standard processing protocol in FreeSurfer V7.2.0 [17], the original
526 images were conformed and normalized (saved as `orig.mgz`), affinely registered to the MNI152
527 template [8] using the NiftyReg toolbox [37]. The respective ribbon segmentation maps, SDFs, and
528 pseudo-ground-truth surfaces were also transformed using the computed transformation. Similarly,
529 we utilize iBEAT V2.0 [52] to process the BCP [23] dataset and merge the brain tissue segmentation
530 results as the ribbon segmentation maps.

531 B.2 Baselines

532 We compared our SegCSR with representatives from the two categories of existing DL-based CSR
533 methods and evaluated their performance for both WM and pial surface reconstruction. DeepCSR [13]
534 and 3D U-Net [44] represent implicit surface reconstruction methods, while others fall into the
535 category of explicit methods. Note that we modify the 3D U-Net method to first generate SDFs
536 based on the ribbon segmentation results, then perform topology correction, and finally utilize
537 the Marching Cubes algorithm to extract the mesh. Since it does not require pGT surfaces from
538 FreeSurfer for training supervision, it can be treated as a weakly supervised learning-based baseline.
539 CorticalFlow++[47] utilizes smoothed convex hulls as the initialization template, trains a chain of
540 deformation fields, and employs a fourth-order Runge-Kutta (RK4) solver to compute the integration
541 for the initial value problem. CortexODE[31] uses WM segmentation for surface initialization and
542 Neural ODE for deformation computation. Vox2cortex [8] deforms averaged surface templates with
543 a GNN-based network to reconstruct multiple surfaces. CoCSR [54] integrates multiple cortical
544 surface reconstructions into a single network. A summary of the state-of-the-art CSR methods is
545 provided in Table 4.

Table 4: Summary of baseline methods in terms of surface representation, supervision in training, and loss functions.

Method	Representation	Supervision	Primary Loss function
3D U-Net [44]	Implicit	Ribbon segmentation	Cross Entropy
DeepCSR [13]		SDFs	L1 Loss
CorticalFlow++ [47]	Explicit	Mesh	Bi-directional Chamfer Loss
cortexODE [31]		Mesh	Bi-directional Chamfer Loss
Vox2Cortex [8]		Mesh	Bi-directional Chamfer Loss
CoCSR [54]		Mesh	Bi-directional Chamfer Loss
SegCSR (Ours)	Explicit	Ribbon segmentation	Weak Supervision

546 C More Experimental Results

547 C.1 Quantitative comparison of our methods with Related Works

548 Due to space limit, we only showcase the quantitative results on left hemisphere in the main paper.
549 Quantitative comparison results on the right hemisphere are summarized as a supplement to Table 1
550 in the main paper.

Table 5: Quantitative analysis of cortical surface reconstruction on geometric accuracy and self-intersections. The Chamfer distance (CD), average symmetric surface distance (ASSD), Hausdorff distance (HD), and the ratio of the self-intersecting faces (SIF) were measured for WM and pial surfaces on three datasets. The mean value and standard deviation are reported. Lower scores indicate better results for all metrics. ‘‘S’’ denotes the use of pGT surfaces from conventional pipelines, while ‘‘W’’ represents weak supervision by pGT ribbon segmentations. In each supervision setting, the best results are in bold, and the second best results are underlined.

Data	Sup.	Method	R-Pial Surface				R-WM Surface			
			CD (<i>mm</i>)	ASSD (<i>mm</i>)	HD (<i>mm</i>)	SIF (%)	CD (<i>mm</i>)	ASSD (<i>mm</i>)	HD (<i>mm</i>)	SIF (%)
ADNI	S	CorticalFlow++ [47]	0.550±0.038	0.413±0.034	0.891±0.071	0.101±0.069	0.548±0.035	0.403±0.032	0.883±0.068	0.071±0.042
		cortexODE [31]	<u>0.482</u> ±0.019	<u>0.220</u> ±0.022	<u>0.461</u> ±0.060	<u>0.033</u> ±0.017	<u>0.470</u> ±0.020	<u>0.207</u> ±0.019	<u>0.444</u> ±0.018	<u>0.023</u> ±0.016
		Vox2Cortex [8]	0.593±0.032	0.382±0.029	0.755±0.061	0.071±0.045	0.588±0.029	0.363±0.024	0.741±0.057	0.059±0.035
	W	CoCSR [54]	0.326 ±0.023	0.126 ±0.012	0.271 ±0.024	0.015 ±0.013	0.320 ±0.020	0.124 ±0.012	0.265 ±0.022	0.006 ±0.003
		DeepCSR [13]	0.948±0.080	0.597±0.068	1.154±0.207	\	0.942±0.077	0.589±0.065	1.140±0.195	\
		3D U-Net [44]	0.601±0.048	<u>0.342</u> ±0.037	<u>0.784</u> ±0.166	\	0.476±0.014	<u>0.268</u> ±0.016	<u>0.563</u> ±0.031	\
		SegCSR (Ours)	0.582 ±0.021	0.328 ±0.022	0.751 ±0.050	0.009±0.009	0.470 ±0.015	0.261 ±0.021	0.548 ±0.038	0.011±0.010
OASIS	S	CorticalFlow++ [47]	0.540±0.037	0.405±0.032	0.834±0.060	0.095±0.052	0.536±0.035	0.402±0.031	0.830±0.058	0.088±0.049
		cortexODE [31]	0.497±0.023	<u>0.225</u> ±0.024	<u>0.473</u> ±0.065	<u>0.038</u> ±0.027	<u>0.481</u> ±0.021	<u>0.214</u> ±0.021	<u>0.450</u> ±0.022	<u>0.025</u> ±0.019
		Vox2Cortex [8]	0.598±0.033	0.386±0.031	0.761±0.064	0.072±0.040	0.592±0.031	0.379±0.028	0.752±0.061	0.061±0.037
	W	CoCSR [54]	0.411 ±0.034	0.144 ±0.017	0.284 ±0.022	0.018 ±0.015	0.353 ±0.026	0.130 ±0.021	0.272 ±0.024	0.009 ±0.004
		DeepCSR [13]	0.989±0.086	0.619±0.071	1.336±0.215	\	0.980±0.082	0.601±0.069	1.175±0.202	\
		3D U-Net [44]	0.613±0.070	<u>0.333</u> ±0.050	<u>0.777</u> ±0.268	\	0.456±0.014	<u>0.249</u> ±0.020	<u>0.493</u> ±0.033	\
		SegCSR (Ours)	0.584 ±0.018	0.323 ±0.019	0.728 ±0.041	0.012±0.011	0.452 ±0.012	0.224 ±0.016	0.465 ±0.030	0.012±0.010
BCP	S	CorticalFlow++ [47]	0.926±0.271	0.729±0.035	1.940±0.174	1.113±0.374	0.892±0.240	0.721±0.033	1.877±0.148	0.531±0.105
		cortexODE [31]	0.758±0.081	<u>0.394</u> ±0.032	<u>0.820</u> ±0.102	<u>0.121</u> ±0.060	0.676±0.069	<u>0.346</u> ±0.029	<u>0.814</u> ±0.098	<u>0.098</u> ±0.033
		CoCSR [54]	0.575 ±0.038	0.214 ±0.022	0.464 ±0.059	0.060 ±0.037	0.542 ±0.038	0.198 ±0.020	0.446 ±0.049	0.056 ±0.030
	W	DeepCSR [13]	2.672±1.131	1.222±0.214	3.101±1.209	\	1.437±0.519	0.426±0.049	0.927±0.116	\
		3D U-Net [44]	1.174±0.312	<u>0.790</u> ±0.058	<u>2.136</u> ±1.020	\	0.687±0.118	<u>0.376</u> ±0.039	<u>0.788</u> ±0.063	\
		SegCSR (Ours)	0.926 ±0.070	0.497 ±0.060	1.287 ±0.142	0.058±0.056	0.875 ±0.067	0.476 ±0.050	1.203 ±0.130	0.054±0.055

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- 824 • The answer NA means that the paper does not release new assets.
825 • Researchers should communicate the details of the dataset/code/model as part of their
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827 limitations, etc.
828 • The paper should discuss whether and how consent was obtained from people whose
829 asset is used.
830 • At submission time, remember to anonymize your assets (if applicable). You can either
831 create an anonymized URL or include an anonymized zip file.

832 14. Crowdsourcing and Research with Human Subjects

833 Question: For crowdsourcing experiments and research with human subjects, does the paper
834 include the full text of instructions given to participants and screenshots, if applicable, as
835 well as details about compensation (if any)?

836 Answer: [NA]

837 Justification: Our paper does not involve crowdsourcing nor research with human subjects.

838 Guidelines:

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- The answer NA means that the paper does not involve crowdsourcing nor research with human subjects.
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