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# From Counts to Choice: Choice-Driven Spatial-Temporal Counting Process Models

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## Abstract

Spatio-temporal event data—such as crime incidents or shared-mobility usage—are generated by human decisions in urban environment. Yet most existing models focus on statistical dependencies in time and space, overlooking cognitive and social factors that shape behavior. We argue that uncovering underlying *preferences* is essential, as they provide a structured link between observed event data and decision processes. We introduce a **preference-driven framework** that models event distributions through a two-stage “consider-then-choose” process: *sparse gating* captures limited attention, and *utility functions* guide selection within the consideration set. To capture heterogeneity, we employ a *mixture-of-experts* design that reveals distinct preference patterns across groups and contexts. The framework incorporates *sparse structural design*, and we analyze its theoretical properties by establishing approximation and generalization guarantees. Empirical studies on crime and bike-sharing datasets demonstrate competitive predictive accuracy while providing interpretable insights into behavioral drivers. By shifting focus *from counts to preferences*, our approach offers a behaviorally grounded and socially meaningful perspective for modeling event data, especially useful in urban life.

## 1 Introduction

Many real-world counting processes in urban environment, such as criminal incidents or bike-sharing usage, represent aggregate macro-level patterns that emerge from micro-level human decision-making. Traditional spatial-temporal models, such as those using Gaussian processes in the Log-Cox Gaussian Process model [19, 10] or incorporating triggering kernel functions in spatial-temporal point processes [21], focus primarily on capturing spatial-temporal dependencies. However, these models often fall short in addressing the underlying human decision-making processes and social influences that shape urban events [25, 11]. To truly understand these processes, we must model the human mechanisms behind the counts—not just their spatial-temporal correlations.

To bridge this gap, we propose a novel approach that *models these urban counting processes through the lens of human choice behavior*. Our key insight is twofold: *i*) Human choices in urban settings inherently involve a “consider-then-choose” process—individuals first narrow down options to a manageable consideration set (e.g., “Which areas are feasible for biking?”) and then make refined

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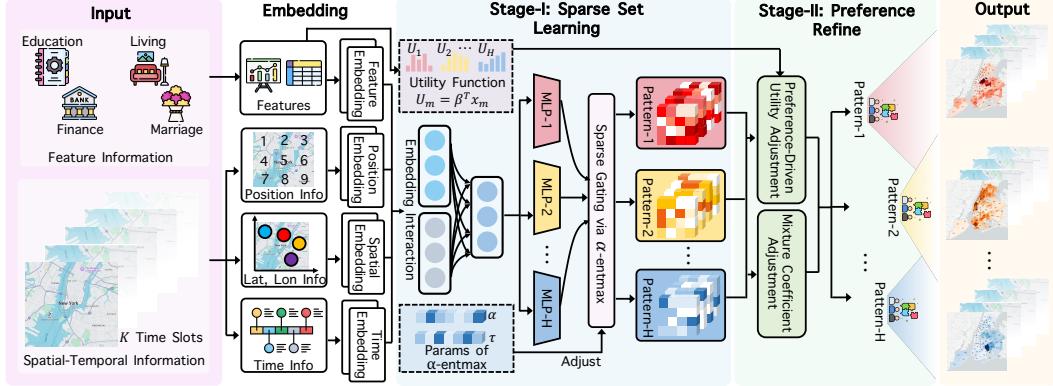


Figure 1: Model framework of **GLANCE**, from left to right: Input, Embedding Module, **Stage I**: sparse gates  $g_m^h$  filter options; **Stage II**: utilities  $U_m^h$  determine final choice probabilities, and Output.

selections within this subset. *ii*) Population-level counts in cities aggregate diverse preference patterns, where distinct subgroups (e.g., commuters vs. recreational cyclists) exhibit systematically different utilities for time–location pairs.

## 2 Preference-Driven Model for Spatio-Temporal Events

We view spatio-temporal event counts as *macro-level aggregates of many micro-level human choices*. Each decision corresponds to selecting a time–location pair from a vast universe of possibilities, shaped by cognitive limits and contextual cues. Inspired by the classical *consider–then–choose* paradigm [13], we model this process in two stages: first, a sparse attention mechanism filters and ranks feasible options; second, a utility function refines the final choice. At the population level, heterogeneity is captured by a mixture of latent decision-making patterns.

Shown in Fig. 1, we introduce the Gated Latent Class ChoiE model, **GLANCE**, which integrates sparse attention, preference refinement, and population heterogeneity into a coherent framework.

### 2.1 Consider–Then–Choose Framework

Let  $\mathcal{U} = \{(t_m, s_m)\}_{m=1}^M$  denote the universe of all discretized time–location pairs. For any individual, the effective choice set  $\mathcal{C} \subseteq \mathcal{U}$  is *unknown*: people do not evaluate all  $M$  possibilities, but instead attend to a sparse subset shaped by context and cognitive limits. Our goal is to learn these latent *consideration sets* and the utilities guiding the final selection.

**Stage I: Consideration via Sparse Attention.** We introduce a gating vector  $g \in \mathbb{R}^M$ , where  $g_m \in [0, 1]$  is the probability that option  $m$  enters the consideration set. Gates are generated from contextual features and learned end-to-end.

A key component is the  $\alpha$ -*entmax* mapping [7], defined as

$$g = \alpha\text{-entmax}(z) = \left[ (\alpha - 1)z - \tau(z)\mathbf{1} \right]_+^{\frac{1}{\alpha-1}},$$

where  $\tau(z)$  ensures normalization. At  $\alpha = 1$ , this reduces to softmax (dense attention), while  $\alpha > 1$  induces sparsity. Since it is convex and differentiable, the model can *learn sparse attention patterns directly from data*. Nonzero entries of  $g$  correspond to options predicted to belong to the consideration set, giving an interpretable representation of limited attention.

To generate scores  $z$ , we embed each time–location pair into a  $d$ -dimensional vector. Let  $X \in \mathbb{R}^{M \times d}$  be the shared embedding matrix. User- or event-specific features can be concatenated with these embeddings. We then apply two projection matrices  $W_q, W_k \in \mathbb{R}^{d \times d'}$  and form

$$E = XW_q(XW_k)^\top \in \mathbb{R}^{M \times M}.$$

Because  $W_q \neq W_k$ , the interaction matrix  $E$  is generally asymmetric. Diagonal entries encode *intrinsic salience*, while off-diagonal terms capture how the presence of one option influences another (e.g., nearby stations competing for attention). Aggregating across rows,

$$z = \sigma(E)\mathbf{1}, \quad z \in \mathbb{R}^M,$$

where  $\sigma(\cdot)$  is a nonlinear activation (e.g., ReLU, tanh) and  $\mathbf{1} \in \mathbb{R}^M$  is the all-ones vector. This produces a score vector summarizing both intrinsic and contextual influences before sparsification. Passing  $\mathbf{z}$  through  $\alpha$ -entmax yields  $g$ , a *data-driven estimate of the consideration set*.

**Stage II: Choosing via Utility.** Within the sparse set, selection is refined by a utility function. The utility of option  $m$  may be *feature-free* (a learnable scalar  $U_m$ ) or *feature-dependent*, e.g.,

$$U_m = \beta^\top x_m,$$

where  $x_m$  may reuse or extend embeddings from  $X$  to encode socio-economic, temporal, or environmental attributes. The final choice probability is

$$f_m(\mathbf{z}, U) = \frac{g_m \exp(U_m)}{\sum_{m'=1}^M g_{m'} \exp(U_{m'})}.$$

This mirrors human decision-making: people first prune the vast universe into a manageable *consideration set*, then carefully choose among the survivors.

## 2.2 Capturing Population Heterogeneity

Human populations are rarely homogeneous. To model diverse decision rules, we introduce a mixture of  $H$  latent classes, each with its own sparse attention and utility functions.

Formally, class  $h \in [H]$  defines a gating distribution  $g^h = \alpha^h$ -entmax( $\mathbf{z}^h$ ) and utility  $U^h$ . The probability of selecting option  $m$  within class  $h$  is

$$f_m(\mathbf{z}^h, U^h) = \frac{g_m^h \exp(U_m^h)}{\sum_{m'=1}^M g_{m'}^h \exp(U_{m'}^h)}.$$

At the population level,

$$\mathbb{P}(m) = \sum_{h=1}^H \pi^h f_m(\mathbf{z}^h, U^h), \quad (1)$$

where  $\pi^h$  are nonnegative mixture weights summing to one. This structure uncovers interpretable subgroups—e.g., *commuters* who prioritize proximity versus *recreational users* who prefer socially vibrant options.

## 2.3 Likelihood and Training Objective

Suppose we observe  $N$  events. Each event is a realized time–location pair  $(t_i, s_i)$ , encoded as a one-hot vector  $y_i \in \mathbb{R}^M$  with  $y_{im} = 1$  if the  $i$ -th event occurred at option  $m$  and  $y_{im} = 0$  otherwise. Let  $P_{im} = \mathbb{P}(m)$  denote the predicted probability of option  $m$  for event  $i$ . The log-likelihood is

$$\mathcal{L}(\boldsymbol{\theta}) = \sum_{i=1}^N \sum_{m=1}^M y_{im} \log P_{im}.$$

The model parameters are

$$\boldsymbol{\theta} = \left\{ X, \{\pi^h, \alpha^h, W_q^h, W_k^h, \beta_h\}_{h=1}^H \right\},$$

where  $X$  is a learnable embedding matrix for time–location alternatives. User or event-level covariates can be concatenated with  $X$ , so that both attention and utility adapt to context. Class-specific parameters  $(W_q^h, W_k^h, \beta_h)$  govern sparse attention and preferences, while  $\pi^h$  are mixture weights.

Maximizing  $\mathcal{L}(\boldsymbol{\theta})$  aligns the model with observed event data, and the differentiability of  $\alpha$ -entmax enables efficient, end-to-end gradient-based training.

## 3 Theoretical Analysis

In Theorem 1, we analyze the approximation error of our proposed model, which states that our finite latent class model can approximate any distribution of human preference parameters with arbitrary accuracy by increasing the number of latent classes  $H$ , and the maximum number of latent classes required is inversely proportional to the desired accuracy, in terms of the expected squared error. This bound holds for any underlying distribution of human preference parameters and event occurrences,

and does not depend on the feature dimensions. This result resembles the universal approximation theorem for neural networks in a Barron space [5]. Details and proofs can be found in Appendix B.3. In Theorem 2, we analyze our proposed model’s generalization capability when trained on a finite data set. It demonstrates that the generalization bound is of order  $\mathcal{O}(1/\sqrt{N})$ , which implies stable performance improvements as the sample size  $N$  grows. Notably, this bound is independent of the number of latent classes  $H$ , regardless of the mixture distribution  $\pi$ , which is a desirable feature of the proposed model. The factor ( $M$ ) that depends on the number of time-location pairs is included due to fact that the utility for each pair is treated separately. In practice, these pairs often have a lower-dimensional parameterization. In this case, it is easy to obtain a more favorable constant using such dimension reduction. Details and proofs can be found in Appendix B.4.

## 4 Experiments

### 4.1 Experimental Setup

**Datasets** We considered three real-world spatial-temporal datasets: *i) New York Crime*<sup>3</sup>. *ii) Chicago Crime*<sup>4</sup>. *iii) Shanghai Mobike*<sup>5</sup>.

**Baselines** To evaluate the capability of our proposed models, we compare against commonly used baselines and state-of-the-art models. *i) ARMA* [4], *ii) CSI* [8], *iii) LGCP* [10, 18], *iv) NSTPP* [6], *v) DSTPP* [24], *vi) ST-HSL* [15], *vii) HintNet* [3], *viii) STNSCM* [9], *ix) UniST* [23], and *x) MNL (Multinomial Logistic Choice Model)* [17, 12].

**Evaluation Metrics.** For evaluation, we group events into aggregate units  $i$  (e.g., one day or one week). For each unit, we form the empirical distribution  $\mathbf{P}_i = (P_{i1}, \dots, P_{iM}) \in \Delta_M$  by normalizing the observed counts across the  $M$  time–location options. Our model produces a corresponding predicted probability vector  $\hat{\mathbf{P}}_i = (\hat{P}_{i1}, \dots, \hat{P}_{iM}) \in \Delta_M$ . We use two metrics: *(i) KL divergence*, which measures the discrepancy between predicted and empirical distributions, and *(ii) RMSE*, which captures numerical prediction error across options [25]:

$$(i) \text{KL}_i = D_{\text{KL}}\left(\hat{\mathbf{P}}_i \parallel \mathbf{P}_i\right) = \sum_{m=1}^M \hat{P}_{im} \log \frac{\hat{P}_{im}}{P_{im}}, \text{ and } (ii) \text{RMSE}_i = \sqrt{\frac{1}{M} \sum_{m=1}^M \left(\hat{P}_{im} - P_{im}\right)^2}.$$

Model	NYC Crime		Chicago Crime		Shanghai Mobike	
	KL ↓	RMSE ↓	KL ↓	RMSE ↓	KL ↓	RMSE ↓
AMAR	0.65 +/- 0.06	0.62 +/- 0.08	0.70 +/- 0.10	0.68 +/- 0.06	0.46 +/- 0.08	0.42 +/- 0.04
CSI	0.67 +/- 0.08	0.66 +/- 0.03	0.68 +/- 0.12	0.65 +/- 0.09	0.47 +/- 0.04	0.43 +/- 0.05
LGCP	0.67 +/- 0.11	0.67 +/- 0.09	0.69 +/- 0.09	0.68 +/- 0.08	0.45 +/- 0.10	0.43 +/- 0.09
NSTPP	0.51 +/- 0.06	0.49 +/- 0.05	0.42 +/- 0.07	0.44 +/- 0.10	0.32 +/- 0.02	0.33 +/- 0.05
DSTPP	0.47 +/- 0.04	0.45 +/- 0.05	0.47 +/- 0.04	0.46 +/- 0.08	0.37 +/- 0.03	0.40 +/- 0.02
ST-HSL	0.56 +/- 0.06	0.52 +/- 0.05	0.49 +/- 0.04	0.52 +/- 0.06	0.38 +/- 0.05	0.43 +/- 0.03
HintNet	0.38 +/- 0.03	0.37 +/- 0.03	0.26 +/- 0.04	0.28 +/- 0.03	0.19 +/- 0.01	0.17 +/- 0.02
STNSCM	0.38 +/- 0.02	0.38 +/- 0.04	0.27 +/- 0.01	0.31 +/- 0.02	0.11 +/- 0.00	0.15 +/- 0.01
UniST	0.37 +/- 0.03	0.36 +/- 0.02	0.27 +/- 0.05	0.30 +/- 0.04	0.23 +/- 0.04	0.25 +/- 0.06
MNL	0.38 +/- 0.01	0.38 +/- 0.01	0.25 +/- 0.03	0.29 +/- 0.02	0.13 +/- 0.01	0.17 +/- 0.01
<b>GLANCE</b>	<b>0.36 +/- 0.02</b>	<b>0.35 +/- 0.01</b>	<b>0.24 +/- 0.02</b>	<b>0.27 +/- 0.02</b>	<b>0.12 +/- 0.01</b>	<b>0.16 +/- 0.01</b>

Table 1: Comparison of our model with baselines for prediction tasks, conducting using training data comprising 16,847 samples for NYC, 23,545 samples for Chicago, and 20,883 samples for Shanghai. **Purple** signifies the best result, while **orange** text indicates the second-best result. Performance metrics are averaged across three different runs, which reported as (Mean +/- SD).

### 4.2 Results and Analysis

**Analysis 1: Prediction Performance** For prediction tasks, we utilize data from the final day as testing data, reserving remaining data as training data for all three datasets. The results in Tab. 1 demonstrate that GLANCE consistently surpasses the majority baseline methods or at least achieves competitive prediction accuracy.

<sup>3</sup><https://data.cityofnewyork.us/Public-Safety/NYPD-Complaint-Data-Current-Year-To-Date-/5uac-w243>

<sup>4</sup><https://data.cityofchicago.org/Public-Safety/Crimes-2001-to-Present/ijzp-q8t2>

<sup>5</sup><https://github.com/Andrehinh/Interesting-python/tree/master/Mobike>

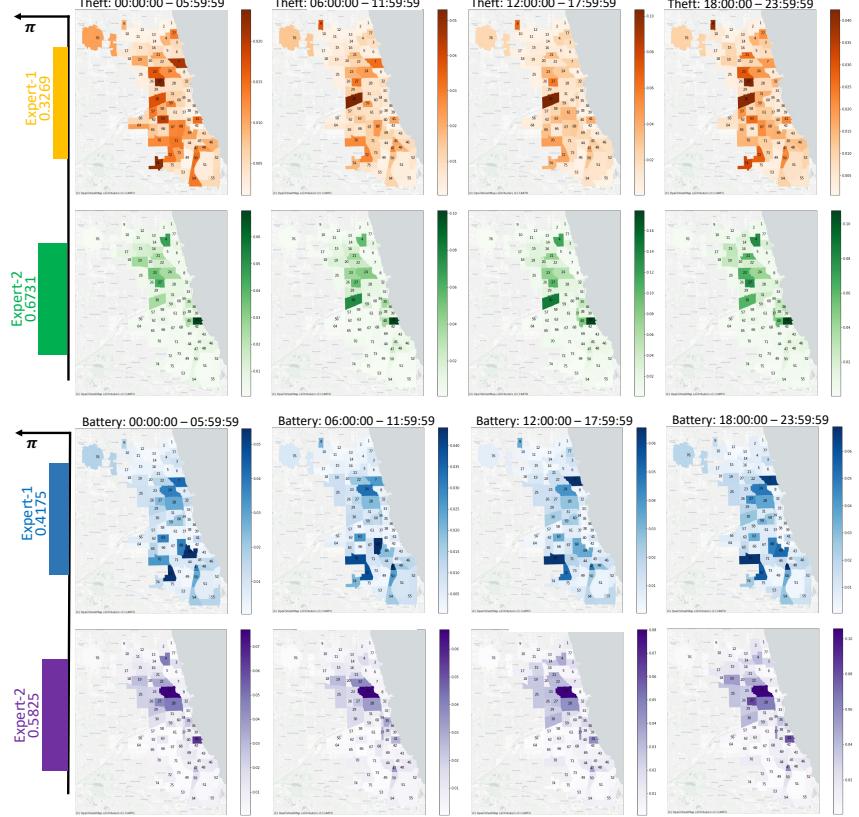


Figure 2: Mixing coefficient  $\pi^h$  (Left bar plots) and mixture pattern adjusted by utility score ( $g^h \exp(U^h)$ ) for different latent class- $h$  and different crime types, including theft and battery (Right heatmaps) from July 1 to July 31, 2024, in Chicago City. The selection of the number of experts is based on empirical experiments.

**Analysis 2: Explain Human Decision Process** Beyond raw accuracy, GLANCE uncovers latent behavioral structures that shed light on heterogeneous decision-making. Model selection via negative log-likelihood, training cost, and efficiency consistently suggests two latent classes for Chicago (Tab. 2, Appendix. C.3), striking a balance between parsimony and expressiveness. These latent classes reveal distinct crime decision patterns (Fig. 2):

- **Theft.** *Class 1 (33%):* Smaller subgroup operating in the West and Far Southwest (Communities-30, -72, -74), with notable evening surges in Community-27. *Class 2 (67%):* Larger subgroup centered on the South and West (Communities-41, -30), avoiding North/Central areas, but showing strong morning activity in Community-30.
- **Battery.** *Class 1 (42%):* Spread across North and Far Southwest (Communities-7, -70, -72), generally avoiding Far North and South. *Class 2 (58%):* Dominated by West Side activity, especially Community-24, with consistent high risk and nighttime surges in Community-41.

These findings highlight a key discovery: *different crime types are not only clustered in space and time but are also driven by distinct offender subgroups with different choice logics.* Unlike hotspot maps that aggregate over populations, GLANCE disentangles these heterogeneous behavioral strategies, enabling more precise and actionable interventions (e.g., tailoring patrols to theft vs. battery patterns).

## 5 Conclusion

We introduced GLANCE, a preference-driven framework for modeling spatio-temporal events in urban environments, which interprets aggregate counts as the macro-level outcome of numerous micro-level consider-then-choose decisions. By integrating sparse attention, flexible utility representations, and a mixture-of-experts architecture, our model effectively captures cognitive constraints and heterogeneous preferences across urban populations, all while maintaining interpretability. This approach not only enhances behavioral realism in urban event modeling but also provides a structured understanding of how human decisions shape complex urban phenomena.

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## Appendix Overview

In the following, we will provide supplementary materials to better illustrate our methods and experiments.

- Section. A provides the algorithm details of our proposed choice-driven spatial-temporal counting process model.
- Section. B derives theoretical guarantees for approximation error and generalization error.
- Section. C provides more detailed analysis about experiments on real-world datasets.
- Section. D reports the reproducibility analysis, including computing infrastructure and hyper-parameter selection.
- Section. E states the limitation, future research direction, and broader impacts of this work.

## A Algorithm Details

### A.1 Spatial-temporal embedding

We adopt a spatial-temporal embedding method akin to that described in [2, 1]. Initially, the region is segmented into distinct blocks. To encode block order, we introduce sinusoidal positional encoding for area position embedding. Subsequently, linear embedding is utilized for spatial information, typically latitude and longitude. Temporal information is encoded using sinusoidal positional encoding as described in [26]. In the context of decision-making, relevant static features can be encoded using one-hot semantic encoding, while dynamic features are encoded linearly. The embeddings for spatial, temporal, and relevant feature information are then combined via element-wise addition to generate the comprehensive embedding.

First, we divide the area into disjoint blocks. To inject a notation of block ordering we add sinusoidal positional encoding for these area position embedding. Then considering the spatial information which are usually latitude and longitude, we apply linear embedding. For encoding temporal information, we also adopt sinusoidal positional encoding a [26]. Considering other relevant features related to the decision-making process, we can apply one-hot semantic encoding for static feature and linear encoding for dynamic features. Finally, the embedding for spatial information, temporal information, and relevant feature information then directly element-wise addition together to obtain the overall embedding.

This approach is similar to the use of positional embeddings and feature embeddings in attention mechanisms, where initial embeddings are transformed through linear projections to capture more nuanced information. By combining the base embeddings  $A$  and  $B$  with these flexible projections, our model can more accurately represent and adapt to diverse preference patterns and social influences, enriching the overall decision-making framework.

### A.2 Overall algorithm

The overall algorithm is shown in Alg. 1, which illustrates the learning process of all the model parameters for our proposed model in detail.

## B Theoretical Details

### B.1 Details of $\alpha$ -entmax

$$\alpha\text{-entmax}(\mathbf{z}) := \underset{\mathbf{p} \in \Delta^M}{\operatorname{argmax}} \quad \mathbf{p}^\top \mathbf{z} + H_\alpha^T(\mathbf{p}), \quad (2)$$

where  $\Delta^M := \{\mathbf{p} \in \mathbb{R}^M : \sum_i p_i = 1\}$  is the probability simplex, and, for  $\alpha \geq 1$ ,  $H_\alpha^T$  is the Tsallis continuous family of entropies [22]:

$$H_\alpha^T(\mathbf{p}) := \begin{cases} \frac{1}{\alpha(\alpha-1)} \sum_j (p_j - p_j^\alpha), & \alpha \neq 1 \\ -\sum_j p_j \log p_j, & \alpha = 1 \end{cases}$$

This family contains the well-known Shannon and Gini entropies, corresponding to the cases  $\alpha = 1$  and  $\alpha = 2$ , respectively.

---

**Algorithm 1** Learning the Model Parameters for the Mixture-of-Experts Model

---

**Input:** Observed data  $\{y_{i,m}\}_{i=1}^N$ , initial parameters

$$\boldsymbol{\theta} = \{\pi, A, B, \{[\alpha^h, W_A^h, W_B^h, U^h]\}_{h \in [H]}\}$$

**Output:** Optimized model parameters  $\boldsymbol{\theta}^*$

**Initialization:** Initialize  $\boldsymbol{\theta}$  randomly or heuristically.

**Description:**  $A$  and  $B$  serve as shared feature embeddings that encode the positional and contextual information necessary for understanding the preference distribution in generating the events.

**repeat**

**for** each expert  $h \in [H]$  **do**

        Compute gating function:

$$g^h = \alpha\text{-entmax}(\sigma(AW_A^h(BW_B^h)^T)\mathbf{1}).$$

**end for**

**for** each expert  $h \in [H]$  **do**

        Compute probability:

$$P_{i,m} = \sum_{h=1}^H \pi^h \frac{g_m^h \exp(U_m^h)}{\sum_{m'=1}^M g_{m'}^h \exp(U_{m'}^h)}.$$

**end for**

**Optimize:** Maximize the likelihood function:

$$\mathcal{L}(\boldsymbol{\theta}) = \prod_{i=1}^N \prod_{m=1}^M (P_{i,m})^{y_{i,m}}$$

    to update  $\boldsymbol{\theta}$  using gradient descent or a similar optimization method.

**until** The likelihood is converged

---

## B.2 Preliminaries and Assumptions for Theorems

**Model recap (single class).** For an alternative  $m \in [M]$ , let  $x_m^\top$  denote the  $m$ -th row of the shared embedding matrix  $X \in \mathbb{R}^{M \times d}$ . Given class-specific projections  $W_q, W_k \in \mathbb{R}^{d \times d'}$ , define the interaction matrix

$$E = XW_q(XW_k)^\top \in \mathbb{R}^{M \times M}.$$

Let  $\sigma(\cdot)$  be an elementwise nonlinearity (assumed 1-Lipschitz, e.g., ReLU or tanh), and let  $\mathbf{1} \in \mathbb{R}^M$  be the all-ones vector. Define scores  $z = \sigma(E)\mathbf{1} \in \mathbb{R}^M$  and a sparse gating distribution  $g = \text{Entmax}_\alpha(z)$  for some  $\alpha \in [1 + \delta, 2]$  with  $\delta > 0$ . Utilities can be feature-free ( $U_m \in \mathbb{R}$ ) or feature-dependent ( $U_m = \beta^\top x_m$ ). The class-wise choice probability is

$$f_m(z, U) = \frac{g_m \exp(U_m)}{\sum_{m'} g_{m'} \exp(U_{m'}^h)}, \quad m \in [M].$$

With  $H$  classes, mixture weights  $\pi^h$ , and parameters  $\{W_q^h, W_k^h, \beta_h, \alpha^h\}_{h=1}^H$ , the population probability is

$$P(m) = \sum_{h=1}^H \pi^h f_m(z^h, U^h).$$

**Assumptions used in proofs.** Throughout the proofs we assume:

1. **Bounded embeddings:**  $\|X\|_F \leq C_X$ . (If  $X$  is learned, the optimization is regularized so that this holds at the solution; if  $X$  is fixed features, this is immediate.)
2. **Bounded projections:**  $\|W_q^h(W_k^h)^\top\|_F \leq C_W$  for all  $h$ .
3. **Bounded utilities:**  $\|\beta_h\|_2 \leq C_U$  (feature-dependent case) or  $|U_m^h| \leq C_U$  (feature-free case).

4. **Sparse gating parameter:**  $\alpha^h \in [1 + \delta, 2]$  for some fixed  $\delta > 0$  to avoid the softmax limit and ensure Lipschitz constants below remain finite.
5. **Lipschitz nonlinearity:**  $\sigma$  is 1-Lipschitz and monotone (true for ReLU, tanh).

**A useful Lipschitz property of  $\text{Entmax}_\alpha$ .** We use that for  $\alpha \in [1 + \delta, 2]$  the mapping  $z \mapsto \text{Entmax}_\alpha(z)$  is globally Lipschitz on  $\mathbb{R}^M$  with a constant  $L_{\text{ent}}(\delta) = \mathcal{O}(1/\delta)$  (see, e.g., properties derived via strong convexity of the Tsallis-entropy regularizer; cf. [20, 7]). Formally, there exists  $L_{\text{ent}}(\delta) > 0$  such that

$$\|\text{Entmax}_\alpha(z) - \text{Entmax}_\alpha(z')\|_2 \leq L_{\text{ent}}(\delta) \|z - z'\|_2, \quad \forall z, z' \in \mathbb{R}^M. \quad (3)$$

**Mixture reduction.** For any function class  $\mathcal{F}$  that is convex in parameters, the empirical Rademacher complexity of mixtures satisfies

$$\sup_{\{\pi^h, f^h\}} \frac{1}{N} \sum_{i=1}^N \epsilon_i \sum_{h=1}^H \pi^h f^h(x_i) \leq \sup_{f \in \mathcal{F}} \frac{1}{N} \sum_{i=1}^N \epsilon_i f(x_i), \quad (4)$$

because  $\sum_h \pi^h f^h$  lies in the convex hull of  $\mathcal{F}$  and the supremum over a convex hull is attained at an extreme point.

We now prove the two theorems.

### B.3 Theorem 1

#### B.3.1 Details and Corresponding Analysis

Let  $q_i^* \in \Delta_M$  denote the true choice probability distribution over  $M$  time–location pairs for event  $i$ , induced by an unknown distribution over latent preference parameters. Our  $H$ -class GLANCE model produces an approximation  $q_H^i$ .

**Theorem 1** (Universal Approximation). *For any  $\epsilon > 0$ , there exists a finite mixture with  $H \leq 2/\epsilon$  classes such that*

$$\frac{1}{N} \sum_{i=1}^N \|q_H^i - q_i^*\|^2 \leq \epsilon.$$

This shows that enlarging  $H$  increases model capacity, and a sufficiently rich mixture can approximate *any* distribution of human preference parameters with arbitrary precision. The dependence  $H = \mathcal{O}(1/\epsilon)$  resembles classical universal approximation results [5].

#### B.3.2 Proofs

**Setup.** Let  $\mu_*$  be the (unknown) distribution over latent parameters  $\phi = (\pi, \alpha, W_q, W_k, \beta)$ . For a fixed context (here suppressed in notation; if contexts vary across events  $i$ , interpret all maps below pointwise in  $i$ ), define the measurable map

$$\Phi : \phi \mapsto q(\phi) \in \Delta_M, \quad q_m(\phi) = \sum_{h=1}^H \pi^h f_m(z^h(\phi), U^h(\phi)).$$

The *true* choice distribution is the pushforward mean

$$q^* = \mathbb{E}_{\phi \sim \mu_*} [q(\phi)] \in \Delta_M.$$

(If the context changes with  $i$ , define  $q_i(\phi)$  and  $q_i^* = \mathbb{E}[q_i(\phi)]$ ; the argument below applies to each  $i$  separately and then we average over  $i$ .)

**Finite-support approximation via sampling (probabilistic method).** Draw i.i.d. parameters  $\phi^{(1)}, \dots, \phi^{(H)} \sim \mu_*$  and form the empirical mixture

$$q_H = \frac{1}{H} \sum_{h=1}^H q(\phi^{(h)}).$$

Because  $q(\phi) \in \Delta_M$  for all  $\phi$ , we have  $\|q(\phi)\|_2^2 \leq \|q(\phi)\|_1 = 1$  (since all coordinates are nonnegative and sum to 1). Hence

$$\begin{aligned} \mathbb{E} \|q_H - q^*\|_2^2 &= \mathbb{E} \left\| \frac{1}{H} \sum_{h=1}^H (q(\phi^{(h)}) - \mathbb{E}[q(\phi)]) \right\|_2^2 \\ &= \frac{1}{H} \text{Tr}(\text{Cov}(q(\phi))) \leq \frac{1}{H} \mathbb{E} \|q(\phi)\|_2^2 \leq \frac{1}{H}. \end{aligned}$$

Therefore  $\mathbb{E}\|q_H - q^*\|_2^2 \leq 1/H$ . By the probabilistic method, there exists a realization of  $\{\phi^{(h)}\}_{h=1}^H$  such that  $\|q_H - q^*\|_2^2 \leq 1/H$ .

**High-probability and multi- $i$  averaging.** A standard vector Bernstein (or Hoeffding) inequality yields that, with probability at least  $1 - \eta$ ,

$$\|q_H - q^*\|_2^2 \leq \frac{c_1 + c_2 \log(1/\eta)}{H}$$

for universal constants  $c_1, c_2$ . When contexts vary across  $i = 1, \dots, N$ , repeat the argument pointwise to get, with the same  $H$ ,

$$\frac{1}{N} \sum_{i=1}^N \|q_H^i - q_i^*\|_2^2 \leq \frac{c_1 + c_2 \log(1/\eta)}{H}.$$

Choosing  $H \geq 2(c_1 + c_2 \log(1/\eta))/\epsilon$  yields the stated  $\mathcal{O}(1/\epsilon)$  rate. Absorbing constants gives the main-text statement “ $H \leq 2/\epsilon$ ” up to universal multiplicative factors.

**Conclusion.** Thus a finite mixture with  $H = \mathcal{O}(1/\epsilon)$  atoms suffices to approximate the population distribution arbitrarily well in average squared  $\ell_2$  error.  $\square$

## B.4 Theorem 2

### B.4.1 Details and Corresponding Analysis

Suppose we observe  $N$  events  $\{(t_i, s_i)\}_{i=1}^N$ , each encoded as a one-hot  $y_i \in \mathbb{R}^M$ . We fit GLANCE parameters  $\theta$  by maximizing the log-likelihood  $\mathcal{L}_{\hat{\mathcal{D}}_N}(\theta)$ . Let  $\mathcal{L}_{\mathcal{D}_*}(\theta)$  denote the population loss under the true distribution  $\mathcal{D}_*$ . We analyze the generalization gap

$$\mathcal{L}_{\mathcal{D}_*}(\theta) - \mathcal{L}_{\hat{\mathcal{D}}_N}(\theta).$$

**Assumptions.** We assume: (i) the shared embedding  $X$  of time–location pairs has bounded Frobenius norm; (ii) projections satisfy  $\|W_q^h(W_k^h)^\top\|_F \leq C_W$ ; (iii) utilities are bounded  $\|\beta_h\|_2 \leq C_U$ ; (iv)  $\alpha^h \in [1 + \delta, 2]$  for some  $\delta > 0$  to avoid degeneracy.

**Theorem 2** (Generalization Bound). *Under the above assumptions, the empirical Rademacher complexity of the GLANCE model class satisfies*

$$\mathfrak{R}_{\hat{\mathcal{D}}_N}(\mathcal{W}) = \tilde{\mathcal{O}}\left(\frac{M e^{C_U} C_W}{\delta \sqrt{N}}\right).$$

Consequently, with high probability,

$$\mathcal{L}_{\mathcal{D}_*}(\theta) - \mathcal{L}_{\hat{\mathcal{D}}_N}(\theta) \leq \tilde{\mathcal{O}}\left(\frac{M e^{C_U} C_W}{\delta \sqrt{N}}\right).$$

The bound decays at the standard  $\mathcal{O}(1/\sqrt{N})$  rate, showing stable improvement with more data. Notably, it is *independent of the number of latent classes  $H$* , so adding mixture components to capture heterogeneity does not compromise generalization. The dependence on  $M$  reflects the size of the time–location universe, though in practice low-dimensional embeddings in  $X$  yield smaller constants.

### B.4.2 Proofs

We bound the generalization gap via the empirical Rademacher complexity of the probability outputs. Let  $\mathcal{F}$  be the class of vector-valued functions mapping an input index  $i$  to  $P_i(\theta) = (P_{i1}, \dots, P_{iM}) \in \Delta_M$ :

$$\mathcal{F} = \left\{ i \mapsto P_i(\theta) = \sum_{h=1}^H \pi^h f(\mathbf{z}_i^h(\theta), U^h(\theta)) : \theta \in \mathcal{W} \right\},$$

where  $\mathcal{W}$  is the constrained parameter set described below.

**Step 1: Symmetrization and vector contraction.** Let  $\ell(y, P) = -\sum_{m=1}^M y_m \log P_m$  be the log-loss. By standard symmetrization and the vector contraction inequality [16], if  $\ell$  is  $L_\ell$ -Lipschitz in  $P$  on the domain of interest, then with high probability

$$\mathcal{L}_{\mathcal{D}_*}(\theta) - \mathcal{L}_{\hat{\mathcal{D}}_N}(\theta) \lesssim L_\ell \cdot \mathfrak{R}_N(\mathcal{F}) + \tilde{\mathcal{O}}\left(\sqrt{\frac{1}{N}}\right).$$

Since the probabilities are bounded away from 0 due to bounded utilities and the gating normalization (see below),  $L_\ell$  is finite and can be absorbed into the final constant. It remains to bound  $\mathfrak{R}_N(\mathcal{F})$ .

**Step 2: Rademacher complexity of mixture reduces to single class.** Let  $\epsilon_{im}$  be i.i.d. Rademacher variables. Then

$$\begin{aligned}
\mathfrak{R}_N(\mathcal{F}) &= \mathbb{E}_\epsilon \left[ \sup_{\theta \in \mathcal{W}} \frac{1}{N} \sum_{i=1}^N \sum_{m=1}^M \epsilon_{im} \sum_{h=1}^H \pi^h f_m(\mathbf{z}_i^h, U^h) \right] \\
&\leq \mathbb{E}_\epsilon \left[ \sup_{\{(\pi^h, \theta^h)\}} \sum_{h=1}^H \pi^h \cdot \frac{1}{N} \sum_{i,m} \epsilon_{im} f_m(\mathbf{z}_i^h, U^h) \right] \\
&\leq \mathbb{E}_\epsilon \left[ \sup_{\theta} \frac{1}{N} \sum_{i,m} \epsilon_{im} f_m(\mathbf{z}_i(\theta), U(\theta)) \right] = \mathfrak{R}_N(\mathcal{F}_1),
\end{aligned} \tag{5}$$

where  $\mathcal{F}_1$  is the single-class function class and we used the convexity bound (4). Thus *the mixture does not increase the complexity beyond that of one class*, explaining the independence of  $H$  in the final bound.

**Step 3: Lipschitzness of  $f(\cdot)$  in  $(\mathbf{z}, U)$ .** Fix an index  $i$  and suppress it in notation. Consider two parameter settings inducing  $(\mathbf{z}, U)$  and  $(\mathbf{z}', U')$ , and their corresponding gates  $g = \text{Entmax}_\alpha(\mathbf{z})$ ,  $g' = \text{Entmax}_\alpha(\mathbf{z}')$  with the same  $\alpha \in [1 + \delta, 2]$ . Write the class-wise probability as

$$f_m(\mathbf{z}, U) = \frac{g_m e^{U_m}}{\sum_k g_k e^{U_k}} := \frac{a_m}{A}, \quad a_m = g_m e^{U_m}, \quad A = \sum_k a_k.$$

A direct Jacobian calculation (softmax-like) yields that, on the domain where  $\|U\|_\infty \leq C_U$  and  $g \in \Delta_M$ , the mapping  $(g, U) \mapsto f$  is  $L_f$ -Lipschitz in the norm  $\|(g, U)\| := \|g\|_2 + \|U\|_2$  with

$$L_f \leq c_0 e^{C_U}, \tag{6}$$

for an absolute constant  $c_0 > 0$ .<sup>6</sup> By the chain rule and (3), we obtain

$$\|f(\mathbf{z}, U) - f(\mathbf{z}', U')\|_2 \leq L_f \left( L_{\text{ent}}(\delta) \|\mathbf{z} - \mathbf{z}'\|_2 + \|U - U'\|_2 \right) \leq c_1 \frac{e^{C_U}}{\delta} \left( \|\mathbf{z} - \mathbf{z}'\|_2 + \|U - U'\|_2 \right), \tag{7}$$

for a constant  $c_1$  absorbing  $c_0$  and the entmax Lipschitz factor.

**Step 4: Bounding changes in  $\mathbf{z}$  by parameter norms.** Recall  $E = XW_q(XW_k)^\top$ . Using sub-multiplicativity and  $\|\sigma(A)\|_F \leq \|A\|_F$  for 1-Lipschitz  $\sigma$ , we have

$$\|E\|_F \leq \|XW_q\|_F \|XW_k\|_F \leq \|X\|_F^2 \|W_q\|_F \|W_k\|_F.$$

Bounding the product with  $\|W_q(W_k)^\top\|_F \leq C_W$  and  $\|X\|_F \leq C_X$ , we get  $\|E\|_F \leq C_X^2 C_W$ . Then

$$\|\mathbf{z}\|_2 = \|\sigma(E)\mathbf{1}\|_2 \leq \|\sigma(E)\|_F \|\mathbf{1}\|_2 \leq \|E\|_F \sqrt{M} \leq C_X^2 C_W \sqrt{M}. \tag{8}$$

Similarly, for two parameter settings,

$$\begin{aligned}
\|\mathbf{z} - \mathbf{z}'\|_2 &= \|\sigma(E)\mathbf{1} - \sigma(E')\mathbf{1}\|_2 \leq \|\sigma(E) - \sigma(E')\|_F \|\mathbf{1}\|_2 \leq \|E - E'\|_F \sqrt{M} \\
&\leq \sqrt{M} \left( \|X\|_F^2 \|W_q - W'_q\|_F \|W_k\|_F + \|X\|_F^2 \|W'_q\|_F \|W_k - W'_k\|_F \right) \\
&\leq c_2 C_X^2 \sqrt{M} \|W_q(W_k)^\top - W'_q(W'_k)^\top\|_F \leq c_2 C_X^2 \sqrt{M} \cdot 2C_W,
\end{aligned} \tag{9}$$

where in the last step we used a standard bilinear difference bound and the norm constraints (the constant  $c_2$  absorbs the bilinear inequality constants). This shows  $\mathbf{z}$  is Lipschitz in the projected interaction with constant  $\mathcal{O}(C_X^2 \sqrt{M})$ .

<sup>6</sup>Sketch:  $\partial f_m / \partial U_k$  is bounded by  $e^{C_U}$  times a probability-difference term; similarly  $\partial f_m / \partial g_k$  is bounded by  $e^{C_U}$ . Summing over  $m$  and using Cauchy–Schwarz gives the stated Lipschitz bound in  $\ell_2$ .

**Step 5: Putting it together for  $\mathcal{F}_1$ .** Using (7) and (9), the single-class mapping  $\theta \mapsto f(z(\theta), U(\theta))$  is Lipschitz in the parameter block

$$\omega := (W_q(W_k)^\top, \beta)$$

with constant

$$L_{\mathcal{F}_1} \lesssim \frac{e^{C_U}}{\delta} (C_X^2 \sqrt{M} + 1).$$

Therefore, applying the *vector* Rademacher contraction inequality to the coordinate-wise linear forms  $\sum_{i,m} \epsilon_{im} f_m(\cdot)$  yields

$$\mathfrak{R}_N(\mathcal{F}_1) \lesssim \frac{L_{\mathcal{F}_1}}{\sqrt{N}} \cdot \left( \underbrace{\sup_{\theta \in \mathcal{W}} \|\omega\|_F}_{\leq C_W + C_U} \right) \lesssim \frac{e^{C_U}}{\delta \sqrt{N}} (C_X^2 \sqrt{M} + 1) (C_W + C_U).$$

Absorbing additive constants and  $C_X$  into  $\tilde{\mathcal{O}}(\cdot)$  and recalling (5), we obtain the advertised form

$$\mathfrak{R}_N(\mathcal{F}) = \tilde{\mathcal{O}}\left(\frac{M e^{C_U} C_W}{\delta \sqrt{N}}\right).$$

**Step 6: From complexity to generalization.** Combining the symmetrization step with the above complexity bound, and absorbing the Lipschitz constant of the log-loss into the polylog factors, gives with high probability

$$\mathcal{L}_{\mathcal{D}_*}(\theta) - \mathcal{L}_{\hat{\mathcal{D}}_N}(\theta) \leq \tilde{\mathcal{O}}\left(\frac{M e^{C_U} C_W}{\delta \sqrt{N}}\right),$$

which matches Theorem 2 in the main text (up to polylogarithmic factors in  $M$  and confidence  $1 - \eta$ ).  $\square$

## B.5 Remarks on Constants and Independence of $H$

**Independence of  $H$ .** The mixture-to-single-class reduction (5) explains why  $H$  does not appear in the bound: Rademacher complexity is convex, and the convex combination of classes does not expand the extremal envelope.

**On the  $M$  factor.** The  $M$  dependence enters through (8)–(9) (aggregating across  $M$  alternatives) and the vector contraction. In practice, alternatives are encoded in low-dimensional embeddings ( $d \ll M$ ), and spatial/temporal structure further reduces effective capacity, improving constants.

**On  $\alpha \in [1 + \delta, 2]$ .** The lower margin  $\delta > 0$  ensures the entmax mapping remains Lipschitz with constant  $L_{\text{ent}}(\delta) = \mathcal{O}(1/\delta)$ ; taking  $\alpha \downarrow 1$  (softmax) makes this constant blow up. Our bound explicitly reflects this via the  $1/\delta$  factor.

## C Experimental Details

### C.1 Baseline Descriptions

We consider following commonly-used baselines and state-of-the-art models: *i) ARMA* [4]: Auto-Regression-Moving-Average is well known for predicting time series data. ARMA predicts the event number of a region solely based on the historical event records of the region, considering the recent time slots for a moving average. *ii) CSI* [8]: Cubic Spline Interpolation trains piecewise third-order polynomials which pass through event points of recent time slots, and then predicts the event number in the near future by the trained polynomials. *iii) LGCP* [10, 18]: Log-Gaussian Cox Process is a kind of Poisson process with varying intensity, where the log-intensity is assumed to be drawn from a Gaussian process. *iv) NSTPP* [6]: It applies neural ODEs as the backbone, which parameterized the temporal intensity with neural jump SDEs and the spatial PDF with continuous-time normalizing flows. *v) DSTPP* [24]: it leverages diffusion models to learn complex spatial-temporal joint distributions. *vi) ST-HSL* [15]: It proposes a Spatial-Temporal Self-Supervised Hypergraph Learning framework for crime prediction. *vii) HintNet* [3]: It performs a multi-level spatial partitioning to separate sub-regions with different risks and learns a deep network model for each level using spatial-temporal and graph convolutions *viii) STNSCM* [9]: A causality-based interpretation model for the bike flow prediction. *ix) UniST* [23]: A universal model designed for general urban spatial-temporal prediction across a wide range of scenarios. *x) MNL (Multinomial Logic Choice Model)* [12]: Degenerate the feature embedding of our method to time-location index embedding, while maintaining the consistent choice model framework.

## C.2 How to explain results of other spatial-temporal models (e.g., LGCP)

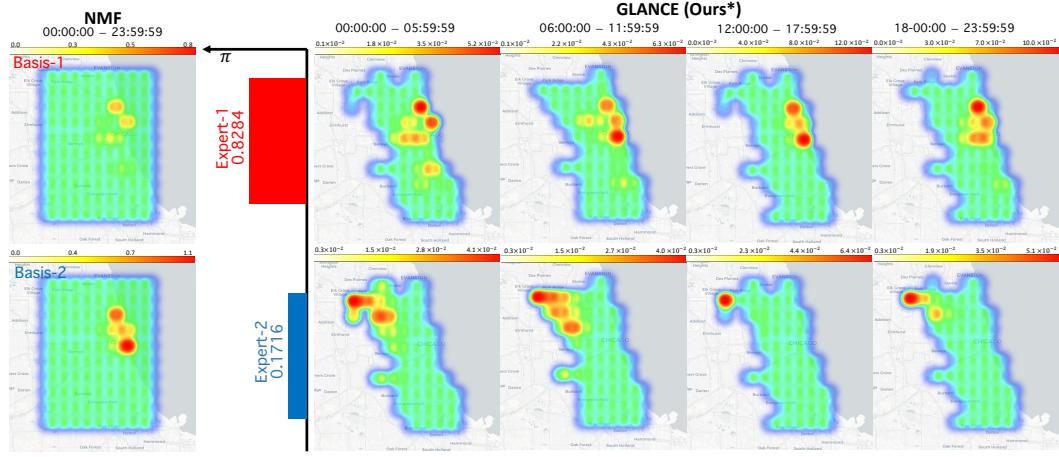


Figure 3: Comparison of the learned expert pattern of our choice model and the basis of non-negative matrix factorization (NMF) on Chicago City crime dataset. To align with the setting of LGCP-NMF, we partition the Chicago area into  $10 \times 10$  area blocks. Left: NMF basis, Right: expert patterns learned by our model.

Consider a Log-Gaussian Cox Process (LGCP) [10], which is a doubly-stochastic Poisson process with a spatially varying intensity function modeled as an exponentiated Gaussian Process

$$Z(\cdot) \sim GP(0, k(\cdot, \cdot)), \quad (10)$$

$$\lambda(\cdot) \sim \exp(Z(\cdot)), \quad x_1, \dots, x_N \sim PP(\lambda(\cdot)) \quad (11)$$

where  $GP(\cdot)$  refer to a Gaussian Process,  $PP(\cdot)$  refer to a Poisson process.  $k(\cdot, \cdot)$  represents the squared exponential covariance function and  $x_i$  represents a countable collection of independent Poisson process with measure  $\lambda_i$ . It can be used to estimate the intensity surface of a spatial point process and therefore capture spatial patterns of data. LGCP-NMF [18] was proposed to use non-negative matrix decomposition [14] of Poisson process intensity surfaces to provide an interpretable feature space that parsimoniously describes the learned intensity matrix  $\Lambda \in \mathbb{R}^{T \times S}$  from LGCP.

$$\Lambda \approx WB \quad (12)$$

where  $W \in \mathbb{R}^{T \times H}$  is the weight matrix, and  $B \in \mathbb{H}^{H \times S}$  is the basis matrix.  $S$  is the number of spatial grids, and  $T$  is the number of temporal intervals.  $H$  is the number of mixtures, which is set to be the same as our model.

Our model provides a refined alternative perspective to explain existing spatial-temporal models. Unlike LGCP-NMF, after LGCP model being well-trained, we fit our model using a new objective function based on the least squared error between estimated probability of our model and the probability from the LGCP. This approach allows us to interpret the expert patterns learned by our model to explain the already fitted LGCP model and encompass more spatial-temporal details. Fig. 3 for Chicago exhibit two ways to explain the results from LGCP. LGCP-NMF captures few information in different bases while our model offers a more granular explanation at the same level of time-location pairs, thus better interpreting the results learned by LGCP.

## C.3 More Experiments – Chicago Dataset

**Selection of Latent Classes** We first elucidate the number of latent classes selection process. Selecting an excessive number of classes can decrease training efficiency and lead to similar patterns across classes, reducing interpretability. Conversely, too few classes may fail to capture all event patterns. Therefore, during training, we empirically utilize the converged negative log-likelihood, time efficiency, and number of learnable parameters as selection criteria. Based on the experimental findings shown in Tab. 2, we choose two latent classes for Chicago datasets.

In Fig. 2, we have examined different crime patterns in Chicago based on the crime types, that align with perpetrators' anticipatory decision-making patterns. More analysis can be found in the main text.

# Expert	Neg. LL $\downarrow$	Time Cost (h) $\downarrow$	# Params
$H = 1$	5.64 +/- 0.03	0.58 +/- 0.02	1.369K
$H = 2$	5.38 +/- 0.01	0.65 +/- 0.01	2.732K
$H = 3$	5.46 +/- 0.02	0.68 +/- 0.01	4.063K
$H = 4$	5.40 +/- 0.02	0.71 +/- 0.01	5.396K

Table 2: Selection of the number of latent classes for Chicago crime dataset. Current selection of modules are highlighted in blue. Performance metrics are averaged across three different runs, which reported as (Mean +/- SD).

Embedding	Expert	Utility	Metric						# Params		
			(w/ prod.)	(w/ feat.)	(w/ multi.)	(w/ feat.)	Neg. LL $\downarrow$	KL $\downarrow$			
<span style="color: red;">X</span>	<span style="color: red;">X</span>	<span style="color: red;">X</span>	<span style="color: red;">X</span>	<span style="color: green;">✓</span>			5.94	0.41	0.38	<span style="color: red;">0.46</span>	0.879K
<span style="color: red;">X</span>	<span style="color: green;">✓</span>	<span style="color: green;">✓</span>	<span style="color: green;">✓</span>				5.67	0.32	0.34	0.75	4.019K
<span style="color: green;">✓</span>	<span style="color: red;">X</span>	<span style="color: red;">X</span>	<span style="color: green;">✓</span>	<span style="color: green;">✓</span>			5.63	0.35	0.35	<span style="color: orange;">0.58</span>	1.703K
<span style="color: green;">✓</span>	<span style="color: red;">X</span>	<span style="color: green;">✓</span>	<span style="color: green;">✓</span>	<span style="color: green;">✓</span>			<span style="color: red;">5.38</span>	<span style="color: red;">0.24</span>	<span style="color: orange;">0.27</span>	0.65	2.732K
<span style="color: green;">✓</span>	<span style="color: green;">✓</span>	<span style="color: red;">X</span>	<span style="color: green;">✓</span>	<span style="color: green;">✓</span>			5.54	0.33	0.34	0.62	2.328K
<span style="color: green;">✓</span>	<span style="color: green;">✓</span>	<span style="color: green;">✓</span>	<span style="color: red;">X</span>	<span style="color: green;">✓</span>			5.60	0.30	0.29	0.70	4.734K
<span style="color: green;">✓</span>			<span style="color: orange;">5.42</span>	<span style="color: orange;">0.26</span>	<span style="color: red;">0.24</span>	1.06	5.636K				

Table 3: Ablation study using Chicago crime dataset with 23545 samples for different modules in embedding approach, number of experts, and construction of utility function. We use converged negative log-likelihood, prediction KL, prediction RMSE, and training time cost as metrics. “(w/ prod)”: Use the product of two embeddings as the overall embedding. If “(w/o prod)”, we only use a single embedding as the overall embedding. “(w/ feat)”: Use the individual features in the construction of embeddings or utility function. “(w/ multi)”: Indicate we use multiple experts or single expert.

**Efficiency, Scalability, and Ablation Study** For Chicago dataset, the results depicted in Fig. 4 affirm the high efficiency and good adaptability of our model for handling large-scale datasets and outperformance compared with deep neural network models. The ablation study in Tab. 3 further demonstrates that under our current modules combination, our model strikes a balance between model performance and efficiency. More analysis can be found in the main text.

## D Reproducibility Analysis

### D.1 Computing Infrastructure

All the real-world data experiments, including the comparison experiments with baselines, are performed on Ubuntu 20.04.3 LTS system with Intel(R) Xeon(R) Gold 6248R CPU @ 3.00GHz, 227 Gigabyte memory.

### D.2 Hyper-Parameter Selection

We present the selected hyper-parameters on three real-world datasets in Tab. 4. The hyper-parameter selection metric is a trade-off between training converged log-likelihood, prediction performance, and time efficiency.

## E Limitation & Broader Impacts

**Limitation** While the current methodological framework effectively incorporates spatial-temporal dynamics and individual attributes, it may inadequately account for critical external or unobservable confounders that could systematically bias model performance, specifically degrade the interpretability advantage. In future research, we can consider a deep consideration set choice model, attempting to focus on integrating attention mechanisms into the gating function of choice model. It has the potential to enhance the model’s flexibility and enables the model to capture a broader range of information through neural networks.

**Broader Impacts** By explicitly modeling human decision-making in spatial-temporal events (e.g., crime, bike-sharing), our model provides actionable insights for policymakers to optimize resource allocation, improve public safety, and design human-centric urban infrastructure. The integration of choice theory with interpretable neural architectures advances transparent AI systems that align with human reasoning, benefiting domains like transportation (e.g., ride-sharing demand prediction)

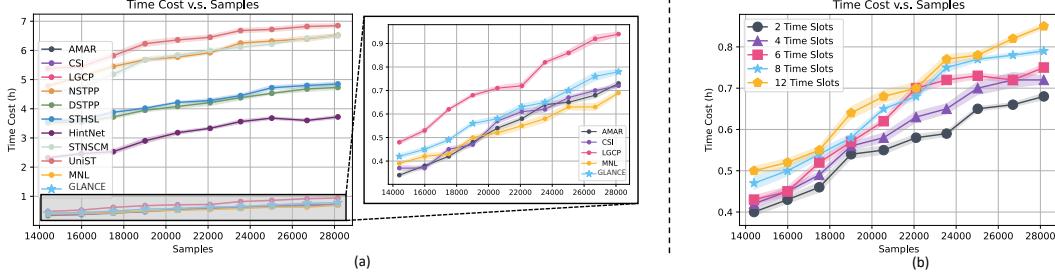


Figure 4: Scalability experiments for Chicago crime datasets with varying training samples and time slots. **(a)** Time cost v.s. training samples for all methods with fixed 4 time slots, and **(b)** Time cost v.s. training samples for our proposed method with varying time slots. All the experiments are conducted over 5 random runs and the standard error is reflected in the shaded areas.

Hyper-Parameters	Value Used		
	NYC Crime	Chicago Crime	Shanghai Mobike
Maximum Epochs	1000	1000	800
Batch Size	64	128	64
# Time Slot	4	4	6
# Area Block	77	77	100
# Latent Class	2	2	3
Embedding Dimension	32	32	32
Initial $\alpha$	1.5	1.5	1.5
Learning Rate	1e-3	1e-3	5e-4
Optimizer	Adam	Adam	Adam

Table 4: Descriptions and values of hyper-parameters used for models trained on the three real-world datasets.

and public health (e.g., disease spread modeling). Moreover, the two-stage "consider-then-choose" paradigm offers a computational tool to test behavioral theories at scale, enabling new interdisciplinary collaborations between machine learning and social sciences. It is also should be noted that the theoretical guarantees (approximation/generalization) ensure robust performance across diverse populations, reducing biases in event prediction compared to traditional models.

In contrast, modeling individual choice behavior at high fidelity may inadvertently expose sensitive patterns in human mobility or preferences, requiring strict data anonymization protocols. And policymakers might prioritize model outputs over community engagement, marginalizing local knowledge in urban decision-making.