Continual Few-shot Relation Extraction via Adaptive Gradient Correction and Knowledge Decomposition

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Abstract

 Continual few-shot relation extraction (CFRE) aims to continually learn new relations with limited samples. However, current methods neglect the instability of embeddings in the process of different task training, which leads to serious catastrophic forgetting. In this pa- per, we propose the concept of the following degree from the perspective of instability to analyze catastrophic forgetting and design a novel method based on adaptive gradient cor- rection and knowledge decomposition to alle- viate catastrophic forgetting. Specifically, the adaptive gradient correction algorithm is de- signed to limit the instability of embeddings, which adaptively constrains the current gradi-016 ent to be orthogonal to the embedding space learned from previous tasks. To reduce the in- stability between samples and prototypes, the knowledge decomposition module decomposes knowledge into general and task-related knowl- edge from the perspective of model architec- ture, which is asynchronously optimized during training. Experimental results on two standard benchmarks show that our method outperforms the state-of-the-art CFRE model and effectively improves the following degree of embeddings.

027 1 Introduction

 The purpose of CFRE is to continuously train a model on limited new data. Compared to traditional continual relation extraction(CRE) models, it can learn new relations without accessing a large num- ber of previous task data, and avoid catastrophic forgetting [\(French,](#page-8-0) [1999;](#page-8-0) [McCloskey and Cohen,](#page-8-1) [1989\)](#page-8-1) of the old relations.

 Due to limited training data, the features learned by the model at each time step of continual learn- ing are relatively unstable and are easily modified by the model when learning other class samples in subsequent time steps. As a result, traditional CRE [m](#page-8-2)ethods cannot be directly applied to CFRE [\(Qin](#page-8-2) [and Joty,](#page-8-2) [2022\)](#page-8-2). To fully utilize data resources,

Figure 1: Representation of distance relative offset distance and absolute offset distance. $\{x_1, \dots, x_5\}$ and ${x'_1, \dots, x'_5}$ are sample embeddings with the same class before and after training at a certain time step, respectively. p and p' are embeddings of prototypes of those. The red dashed arrow represents the AOD of the sample x_4 or prototype p . The difference distance of the two yellow dotted arrows represents ROD between x_2 and p .

scholars have explored many methods [\(Wang et al.,](#page-9-0) 042 [2022b;](#page-9-0) [Zhong et al.,](#page-9-1) [2021;](#page-9-1) [Zhang et al.,](#page-9-2) [2022\)](#page-9-2). **043** [A](#page-8-3)nd the methods based on memory replay [\(Chen](#page-8-3) **044** [et al.,](#page-8-3) [2023;](#page-8-3) [Wang et al.,](#page-9-3) [2023;](#page-9-3) [Qin and Joty,](#page-8-2) [2022\)](#page-8-2) **045** made great achievements in CFRE. However, these 046 models mainly focus on the strategies of memory **047** samples in the process of replaying or learning and 048 perform direct fine-tuning of the model parameters **049** through the gradient of the loss function. Further- **050** more, in-memory examples are used to generate **051** gradients that benefit the performance on previous **052** tasks, but the direction optimized by these gradi- **053** ents may contradict the optimization direction of **054** the current task gradient, which leads to the instabil- **055** ity of samples with respect to prototypes. In metric **056** learning [\(Kaya and Bilge,](#page-8-4) [2019\)](#page-8-4), the prototype of **057** one class is the center of this class. **058**

In essence, during continuous learning with min- **059** imal data usage, when samples are equivalently **060** shifted with the embedding of prototypes, the la- 061

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 bels of samples will not be easily changed and catastrophic forgetting of the model will be alle- viated. Thus, we formally provide the definition 065 of **following degree** of class y at time step t: the **degree of deviation between class y samples and** 067 class y prototype before and after training at t. Ob- viously, the smaller the offset between the previous sample embedding and its prototype, the higher the following degree of this class, and the less unstable the samples are. In this way, the model can have less catastrophic forgetting of previous samples.

 Intuitively, there are two main reasons for the low following degree of the model on a task: 1) the model is not sufficiently optimized for some samples, which makes the prototypes deviate from the optimization direction of the samples; 2) af- ter optimization, all embeddings change too much compared with the previous will also increase the 080 risk of low following degree. **Relative offset dis-** tance (ROD) and absolute offset distance (AOD) are proposed to express the above two factors, re-**spectively.** As shown in Fig. [1,](#page-0-0) $|x'_4 - x_4|$ and $|p' - p|$ **represent AOD of** x_4 and p . $(|p' - x'_2| - |p - x_2|)$ 085 represents ROD between x_2 and p . The lower the AOD and ROD, the higher the following degree.

 In this paper, an adaptive gradient correction algorithm is proposed to directly constrain and cor- rect the vector space of the gradient in transformer- based language models. Since the modified gra- dients are orthogonal to the embeddings of the previous sample, this special optimization method for the transformer can effectively reduce AOD. Specifically, for each previous task, we calculate a gradient direction, which has the greatest impact on in-memory samples, as the correction criteria. When updating the gradient of the current task, the correction matrix based on this criteria is used to make a linear transformation of the gradient, which can constrain the subspace of parameters orthogo-nal to the previous tasks.

 In addition, knowledge contained in model pa- rameters is decomposed into general and task- related knowledge. Based on this decomposition, general knowledge is used to identify a generic rep- resentation of relations with the corresponding enti- ties. We employ task-related knowledge to identify categorical decision boundaries between specific tasks based on general knowledge. In practice, we apply a pre-trained language model (PLM) to en- code the general knowledge and use an adaptive gradient correction algorithm to avoid mutual cov-erage of knowledge. Since there is no gradient

transmission between task prototypes, we integrate **114** task-related knowledge into task prototype embed- **115** ding. These prototypes are updated discretely and **116** continuously in three different training stages to **117** reduce ROD. In the continuous optimization stage, **118** we add an additional loss to increase the distance **119** between prototypes, which can prevent confusion **120** between the new and the old task prototypes. **121**

To sum up, the contributions of this paper mainly **122** include the following three aspects: **123**

- We attribute catastrophic forgetting in CFRE **124** to the low following degree between samples **125** and prototypes, and analyze how to improve **126** the following degree from the perspectives of **127** AOD and ROD. **128**
- According to the correction matrix calculated **129** by in-memory samples, an adaptive gradient **130** correction algorithm is proposed that makes **131** the model directly adjust the gradient to re- **132** duce AOD. **133**
- We design a knowledge decomposed method **134** and corresponding update strategies to avoid **135** the confusion of knowledge between different **136** tasks, which can limit ROD during training. **137**

Experimental results on two public datasets show **138** that our method can effectively alleviate the catas- **139** trophic forgetting in CFRE. **140**

2 Related Work **¹⁴¹**

RE aims to extract the implied relation from sen- **142** tences. For example, given the sentence "Steve **143** Jobs is the co-founder of Apple", the model needs **144** to determine the relation "CEO_of" between the **145** entity "Steve Jobs" and "Apple". It is a basic step **146** for many downstream tasks such as language un- **147** derstanding, question answering, and knowledge **148** graph construction [\(Nasar et al.,](#page-8-5) [2021\)](#page-8-5). **149**

Most traditional RE models are built based on **150** a fixed dataset [\(Eberts and Ulges,](#page-8-6) [2020;](#page-8-6) [Liu et al.,](#page-8-7) **151** [2022b;](#page-8-7) [Shang et al.,](#page-9-4) [2022;](#page-9-4) [Li et al.,](#page-8-8) [2018,](#page-8-8) [2021\)](#page-8-9). **152** However, RE is often an open vocabulary problem **153** [\(Liu et al.,](#page-8-10) [2022a\)](#page-8-10), and it is difficult to model all **154** relations for any limited set. Therefore, the contin- **155** ual learning ability [\(Chen and Liu,](#page-8-11) [2018\)](#page-8-11) of the RE **156** model has gradually attracted attention [\(Zhao et al.,](#page-9-5) **157** [2023;](#page-9-5) [Xia et al.,](#page-9-6) [2023\)](#page-9-6). **158**

But there will be serious catastrophic forget- **159** ting for the model in continual learning, that is, **160** the model will forget the old knowledge when **161**

 learning new tasks. To solve this problem, the existing methods for continual learning mainly in- clude: regularization-based approach [\(Zhai et al.,](#page-9-7) [2019\)](#page-9-7), memory-based approach [\(Cha et al.,](#page-8-12) [2021\)](#page-8-12), optimization-based approach [\(Schwarz et al.,](#page-9-8) [2018\)](#page-9-8), representation-based approach [\(Yan et al.,](#page-9-9) [2022\)](#page-9-9), and architecture-based approach [\(Wang](#page-9-10) [et al.,](#page-9-10) [2022a\)](#page-9-10). The existing methods [\(Wang et al.,](#page-9-11) [2022c;](#page-9-11) [Zhou et al.,](#page-9-12) [2022\)](#page-9-12) are often based on a large number of labeled data for training, which is time-consuming and expensive. When the num- ber of training is small, overfitting of memory data and knowledge coverage [\(Song et al.,](#page-9-13) [2023\)](#page-9-13) is also one of the causes of catastrophic forgetting. The existing methods mainly solve this problem from 177 the following three levels: data level [\(Wang et al.,](#page-9-0) [2022b\)](#page-9-0), feature level [\(Zhong et al.,](#page-9-1) [2021\)](#page-9-1), and task level [\(Zhang et al.,](#page-9-2) [2022\)](#page-9-2).

 Directly adjusting the gradient is also one of the methods to overcome catastrophic forgetting with limited data [\(Chen et al.,](#page-8-3) [2023;](#page-8-3) [Zhou et al.,](#page-9-12) [2022\)](#page-9-12). [He and Jaeger](#page-8-13) [\(2018\)](#page-8-13) proposed Concept Aided BackProp for disaster forgetting, in which the gradi- ent is shielded by a conceptor to prevent the degra- dation of previous tasks. [Zeng et al.](#page-9-14) [\(2019\)](#page-9-14) intro- duced orthogonal projection and context-dependent [p](#page-8-14)rocessing module for the current gradient. [Guo](#page-8-14) [et al.](#page-8-14) [\(2022\)](#page-8-14) put forward the paranoid factor related to the previous task to estimate the input space, but the accumulation strategy for embedding of differ- ent samples may lead to confusion in the projection [s](#page-8-15)pace. Although, the GEM algorithm [\(Lopez-Paz](#page-8-15) [and Ranzato,](#page-8-15) [2017\)](#page-8-15) introduced gradient projection to make the loss of previous tasks slowly increase in subsequent training, the embeddings computed by this method are not equivariant and cannot be applied to transformer-based language models.

 In contrast, our method innovatively uses the cor- rection matrix calculated by in-memory samples to directly constrain the gradient update in backpropa- gation to reduce the overall AOD, so as to limit the risk of reduced following degree. A model archi- tecture based on knowledge decomposition and the corresponding asynchronous optimization method is designed to further reduce the ROD of samples.

²⁰⁷ 3 Methodology

208 3.1 Problem Definition

209 CFRE model extracts the relations from a series 210 of tasks $\{T^1, T^2, \cdots, T^K\}$. Every task T^k has 211 its own training dataset D_{train}^k , validation dataset

 D_{valid}^k , test dataset D_{test}^k and relation label set 212 R^k . Each set contains a small number of sam- 213 ple pairs $\{(x_i, y_i)\}_{i=1}^{|D|}$, where the label $y_i \in R^k$ For example, in N-way M-shot constraint, we 215 make $|R^k| = N$ and $|D^k_{train}| = N \times M$. At 216 time step k, the model will only train on D_{train}^k 217 and we hope that the model will perform well on **218** ${D_{test}^1 \cup D_{test}^2 \cup \cdots \cup D_{test}^k}$ after training. 219

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, **222**

as **225**

The memory mechanism is applied to prevent **220** catastrophic forgetting in CFRE. Memory is de- **221** fined as a series of sample sets $\hat{M}^K = \bigcup_{j=1}^K M^j$ where each $M^k = \{(x_i, y_i)\}_{i=1}^{|M^k|}$ corresponds to a 223 task T^k . At time step k, a portion of the sample 224 is selected to be stored in the memory set M^k as classical samples. In this paper, only one sample is **226** in memory for each category. **227**

3.2 Training Process **228**

Algorithm. [1](#page-4-0) describes the whole training pro- **229** cess of our method at time step k . It mainly includes three different training stages to continu- **231** ously and discretely adjust ROD between proto- **232** types and samples. **233**

In the first stage, we initialize the current mem- **234** ory set M^k and proto-embedding P^k . Then, the 235 temporary memory $\{\hat{M}^{k-1} \cup \hat{M^k}\}\$ with all train- 236 ing data is applied to preliminarily update the PLM **237** parameters θ^{k-1} through the corrected gradient. 238

In the second stage, we introduce cosine simi- **239** larity to find one sample that is most similar to the **240** center of the category cluster and add it to memory **241** \hat{M}^{k-1} . The PLM parameters update is similar to 242 the first stage, except for using selected memory **243 data.** 244

In the final stage, we freeze the gradient of PLM **245** and view proto-embeddings \hat{P}^k as learnable param-
246 eters, fine-tuning them on training data. **247**

The data and gradient flow are shown in Fig. [2.](#page-3-0) 248

3.3 Knowledge Decomposition **249**

To prevent the parameters in the model from being **250** covered and confused due to continuous task iter- **251** ation, we abstractly decompose them into general **252** and task-related knowledge. Since they do not in- **253** terfere with each other during the update process, **254** ROD for different categories can be effectively re- **255 duced.** 256

3.3.1 General knowledge encoder **257**

Because of the training with mask prediction on a **258** large number of corpora, the knowledge of BERT **259** parameters is independent of specific downstream **260**

Figure 2: The data and gradient flow of our method, where the solid lines describe the data flow in forward propagation and the dashed lines describe the gradient flow in backpropagation.

 tasks. Therefore, we choose BERT as PLM to encode the general knowledge of the whole re- lation extraction model. Specifically, for a sen-**tence** $x = \{Tok_1, Tok_2, \dots, Tok_n\}$, we first con- struct a template function based on prompt learning [\(Liu et al.,](#page-8-16) [2023\)](#page-8-16) by adding a special [MASK] to-267 ken to the sentence and get the sequence $x_{seq} =$ $\{[CLS], e_h, [MASK], e_t, [SEP], x, [SEP]\}. e_h$ **and** e_t **respectively represent the head and tail en-** tity in the sentence x. Then the embedding of [MASK] token is taken as the relation representa-tion of the whole sentence:

$$
h_{[MASK]} = f_{\theta}(x_{seq}) \tag{1}
$$

274 **To facilitate symbolic representation,** x_{sea} is re-**275** placed by x.

276 3.3.2 Task-related knowledge encoder

 To ensure that the new task knowledge learned by the model does not conflict with the previous task and model general knowledge respectively, we encode the knowledge of different tasks into the corresponding category proto-embedding. Since the proto-embeddings of different categories are disconnected, the knowledge from new and pre- vious tasks will not affect each other naturally. And this part of knowledge is updated and trained asynchronously with BERT, so it also does not

conflict with the general knowledge. The proto- **287** embeddings are updated with different strategies in **288** the three stages of training. **289**

In the first stage of task k , we apply all samples 290 of each new relation in the current task to calculate **291** the new proto-embedding. To get the most repre- **292** sentative vector in the sample embedding space, 293 the average method is introduced to aggregate all **294** embeddings of samples. For the proto-embedding **295** p_j^k of class j task k, the calculation formula is as **296** follows: **297**

$$
P_j^k = \frac{1}{|D_j^k|} \sum_{(x_i, y_i) \in D_j^k} f_{\theta}(x_i)
$$
 (2)

where $D_j^k = \{(x_i, y_i) | (x_i, y_i) \in D_{train}^k, y_i = r_j\}$ 299 and $|D_j^k|$ is the number of samples in D_j^k . 300

In the second stage, there is only one sample 301 for each class in memory, so we directly use the **302** relation embedding of that sample as the proto- **303** embedding of the corresponding class. **304**

The updating of proto-embeddings in the first **305** two stages is discrete. In the third stage, we **306** freeze the parameters of BERT and regard the **307** proto-embedding as a parameter that can be up- **308** dated by the gradient descent algorithm. The proto- **309** embeddings are continuously updated by the gradi- **310**

Algorithm 1 Training procedure for $T^k(k>1)$

Input: The PLM parameters θ^{k-1} and protoembedding $\hat{P}^{k-1} = \bigcup_{j=1}^{k-1} P^j$ trained on T^{k-1} , training data set D_{train}^k , memory set \hat{M}^{k-1} , learning rate γ

Output: θ^k , P^k

Use all samples in D_{train}^k to initialize M^k and P^k

Freeze the gradient of \hat{P}^{k-1} , unfreeze the gradient of θ^{k-1}

for $i \in \{1, \cdots, epoch_1\}$ do

Calculate correction matrix C using \hat{M}^{k-1} Calculate corrected gradient $\Delta \theta^{k-1}$ using C with L_{gen} on $D = \{ \hat{M}^{k-1} \cup M^k \cup D_{train}^k \}$ Update $\theta^{k-1} \leftarrow \theta^{k-1} - \gamma \Delta \theta^{k-1}$ Recalculate P^k using M^k

end for

Select typical samples from D_{train}^k to update M^k

 $\hat{M}^k \leftarrow \hat{M}^{k-1} \cup M^k$

for $i \in \{1, \cdots, epoch_2\}$ do Calculate correction matrix C using \hat{M}^{k-1} Calculate corrected gradient $\Delta \theta^{k-1}$ using C with L_{gen} on $D = \{ \hat{M}^k \cup D_{train}^k \}$ Update $\theta^{k-1} \leftarrow \theta^{k-1} - \gamma \Delta \theta^{k-1}$

Recalculate P^k using M^k

end for

 $\hat{P}^k \leftarrow \hat{P}^{k-1} \cup P^k$

Freeze the gradient of θ^k , unfreeze the gradient of \hat{P}^k

for $i \in \{1, \cdots, epoch_3\}$ do Calculate gradient $\Delta \hat{P}^k$ with L_{task} on $D =$ D_{train}^k $\stackrel{\textcolor{black}{D}_{train}}{\textcolor{black}{\text{Update}}}\hat{P}^k \leftarrow \hat{P}^k - \gamma \Delta \hat{P}^k$ end for

311 ent.

$$
p_j^k \leftarrow p_j^k - \gamma \frac{\partial H_{task}}{\partial k} \tag{3}
$$

313 where γ is the learning rate. L_{task} is calculated **314** using cross entropy function, which is similar to **Eqn. [5.](#page-4-1) We set** $P^k = \bigcup_{j=1}^{|R^k|} p_j^k$ **.**

 $p_j^k \leftarrow p_j^k - \gamma \frac{\partial L_{task}}{\partial x^k}$

 ∂p_j^k

316 3.3.3 Calculation of loss function

 To optimize the learned embeddings of relations, the training and inference of our model are based on metric learning. At time step k, by measuring the similarity between each sample x_i and proto-**embedding** \hat{P}^k , the relation distribution is calculated as: **322**

$$
p(r_i|x_i) = \frac{exp(d(f_{\theta}(x_i), p_i))}{\sum_{l=1}^{|P^k|} exp(d(f_{\theta}(x_i), p_l))}
$$
(4)

where $d(\cdot, \cdot)$ is the distance metric function (cosine 324 similarity in this paper) and p_l is proto-embedding 325 in \hat{P}^k . . **326**

Further, the cross entropy loss function is cal- **327** culated to measure the classification error of the **328** model: **329**

$$
L_{ce} = -\sum_{(x_i, y_i) \in D} logp(r_i|x_i)
$$
 (5) 330

While alleviating catastrophic forgetting, it is **331** also important to correctly handle the information **332** entropy of new tasks in the model. To avoid the **333** confusion of similar relation between new task and **334** previous tasks, we select the proto-embedding sets **335** $P_i^{sim} = \{p_l | d(f_\theta(x_i), p_i) - d(f_\theta(x_i), p_l) < \alpha\}$ 336 and $P_i^{neg} = \{p_l | max(d(f_\theta(x_i), p_l), l \neq i)\}\$, which 337 are easy to be confused with the correct category **338** for each sample x_i . α is the set similarity thresh-
339 old. The following probability is reduced by cross **340** entropy loss function: 341

$$
L_{sim} = -\sum_{(x_i, y_i) \in D} \exp(d(f_{\theta}(x_i), p_i))
$$

$$
log \frac{exp(d(f_{\theta}(x_i), p_i))}{\sum_{l=1}^{|P_i^{sim} \cup P_i^{neg} \cup p_i|} exp(d(f_{\theta}(x_i), p_l))}
$$
 (6)

The final general knowledge loss is calculated as: **343**

$$
L_{gen} = L_{ce} + L_{sim} \tag{7}
$$

3.4 Adaptive Gradient Correction **345**

Through the decomposition of parameters, the task- **346** related knowledge will not interfere with each other **347** and ROD of previous tasks will be kept at a low **348** level in the process of continual learning. How- **349** ever, when updating the parameters of the general **350** knowledge encoder, there will still be gradient inter- **351** ference between tasks, which leads to the coverage **352** of the general knowledge in BERT. These coverage **353** may make the embedding and AOD of previous **354** task sample change dramatically, which will in- **355** crease the risk of reducing the following degree. **356**

To avoid the interference of previous task embed- **357** dings when BERT learns a new task, the memory **358** embedding of the corresponding hidden layer is **359** extracted to adaptively correct the feed forward **360**

(4) **323**

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 networks (FFN) and query matrix gradient in each layer during the model back-propagation. And the other gradients in BERT are frozen besides these two kinds of gradients.

 To express simplicity, we first abstract all lay- ers of the encoder into fully connected layers to introduce our idea. At time step k, we first extract **the hidden state** $H^l \in R^{d \times |\hat{M}^{k-1}|}$ of samples in \hat{M}^{k-1} before inputting each unfrozen layer. Then the gradient correction matrix C^l of a certain layer is calculated according to H^l (The superscripts are omitted for clarity):

$$
C = I - H(H^T H)^{-1} H^T \tag{8}
$$

 Obviously, we can get $CH = H^TC^T = 0$. To guarantee the reversibility in the specific calcula-**tion, we add a small offset:** $(\alpha I + H^T H)^{-1}$. The calculation method of α is consistent with [Guo et al.](#page-8-14) **378** [\(2022\)](#page-8-14).

 When using the back-propagation algorithm to calculate the gradient of a certain layer, the un- frozen gradient of BERT is corrected by C^l . The **parameter** W^l update formula for a certain layer is shown as follows:

$$
\Delta W^{l} = \frac{\partial L_{gen}}{\partial W^{l}} C^{l}
$$

\n
$$
W^{l} \leftarrow W^{l} - \gamma \Delta W^{l}
$$
 (9)

385 where γ is the learning rate.

 For the parameters in a transformer, we only update the FFN layer parameters and the parame- ters related to the query matrix in the self-attention layer. The method of updating parameters in the FFN layer is similar to Equation [9.](#page-5-0) The gradi- ent update method of the query matrix in the self-attention layer is designed as,

$$
\Delta W^{q} = (C^{q})^{T} \frac{\partial L_{gen}}{\partial W^{q}}
$$

$$
W^{q} \leftarrow W^{q} - \gamma \Delta W^{q}
$$
(10)

394 where $(C^q)^T$ is the transpose row of matrix C^q , *W^q* is parameters to calculate query matrix. The detailed discussion and further proof are included in the Appendix [A.](#page-10-0)

³⁹⁸ 4 Experiments

399 4.1 Experimental Setup

400 Datasets Consistent with previous work on **401** CFRE [\(Chen et al.,](#page-8-3) [2023\)](#page-8-3), our experiment will be **402** [c](#page-8-13)onducted on two common datasets. FewRel [\(He](#page-8-13) [and Jaeger,](#page-8-13) [2018\)](#page-8-13) is a RE dataset that includes 80 403 relations, with 700 samples of each relation. We **404** divide these relations into 8 tasks $\{T^1, \cdots, T^8\}$, 405 where each task contains 10 relations. M samples 406 are randomly drawn to form D_{train}^k with the con- 407 straint of 10-way M-shot. TACRED [\(Zhang et al.,](#page-9-15) 408 [2017\)](#page-9-15) is a large-scale RE dataset based on news **409** networks and online documents, containing 42 re- **410** lation labels and 106,264 samples. Samples in TA- **411** CRED are imbalanced compared with FewRel. We **412** remove the particular relation "n/a" (not available) **413** and divide the remaining 41 relations into eight **414** subsets. The first subset has one more relation than **415** other subsets **416**

Evaluation Metrics At time step k, we test the **417** model on \hat{D}_{test}^k , the union of all visible relation test 418 sets, which can simultaneously reflect the model **419** performance on new and old tasks. Since CFRE **420** may be affected by the task sequence, we run ran- **421** dom seeds six times on different task sequences to **422** ensure the randomization of that. The mean and **423** variance of relation classification accuracy on six **424** different task sequences are introduced as the per- **425** formance of the model. The training details are **426** discussed in Appendix [B.](#page-10-1) **427**

Baselines Four baselines are introduced to com- **428** pare our method (AGCKD). CEAR [\(Zhao et al.,](#page-9-5) **429** [2023\)](#page-9-5) is a CRE approach that designs memory- **430** insensitive relation prototypes and memory aug- **431** mentation to overcome the overfitting problem. **432** SCKD [\(Wang et al.,](#page-9-3) [2023\)](#page-9-3) is a contrastive learning **433** scheme for CFRE, which employs serial knowl- **434** edge distillation and pseudo-samples for con- **435** trastive learning to keep the representation of **436** samples in different relations distinguishable. In 437 ERDA [\(Qin and Joty,](#page-8-2) [2022\)](#page-8-2), the embedding spatial **438** regularization and data augmentation algorithms **439** are proposed to optimize memory expression in **440** CFRE tasks. ConPL [\(Chen et al.,](#page-8-3) [2023\)](#page-8-3) is the **441** state-of-the-art method for CFRE. Prototype-based **442** classification module, memory enhancement mod- **443** ule, and consistency learning module are used to **444** enhance the consistency of distribution as well as **445** avoid catastrophic forgetting. In addition to these **446** baselines, we also added two experimental settings **447** to observe the upper and lower limits. In Joint **448** Training setting, the model saves all training sam- **449** ples in the memory. Since the model can replay all **450** past data at every time step, there is no catastrophic **451** forgetting. In SeqRun setting, the memory does **452** not save any samples. This setting may cause the **453**

Method	Task index									
		\overline{c}	3	4	5	6	7	8		
10-way 5-shot of FewRel										
Joint Training SeqRun	$97.93_{\pm0.47}$ $97.06_{+1.34}$	$96.25_{\pm0.35}$ $92.77_{\pm1.36}$	$94.09_{+0.45}$ $85.76_{\pm 3.06}$	$92.37_{\pm0.39}$ $80.95_{\pm 2.82}$	$91.96_{\pm 0.71}$ $75.19_{\pm 3.87}$	$91.15_{+0.56}$ $66.62_{\pm 3.71}$	$90.35_{\pm 0.40}$ $55.53_{\pm2.05}$	$88.9_{\pm0.03}$ $42.57_{\pm2.26}$		
CEAR SCKD ERDA ConPL	$69.46_{\pm{7.49}}$ $94.77_{\pm0.35}$ $96.55_{\pm 0.43}$ $95.23_{\pm 2.29}$	$64.53_{+1.7}$ $82.83_{\pm2.61}$ $92.56_{\pm 2.29}$ $92.77_{\pm2.78}$	$62.22_{\pm3.01}$ $76.21_{+1.61}$ $88.56_{\pm 3.34}$ $90.58_{+2.17}$	$61.27_{\pm 3.88}$ $72.19_{\pm1.33}$ $84.47_{\pm 3.25}$ $89.03_{\pm0.96}$	$60.04_{\pm 2.37}$ $70.61_{+2.24}$ $84.14_{\pm3.01}$ $88.64_{\pm 1.39}$	$58.70_{\pm3.51}$ $67.15_{\pm 1.96}$ $79.94_{\pm2.46}$ $88.09_{\pm 1.06}$	$57.88_{+2.66}$ $64.86_{\pm1.35}$ $78.45_{\pm1.74}$ $87.29_{\pm0.95}$	$55.77_{\pm2.63}$ $62.98_{\pm0.88}$ $77.02_{\pm2.93}$ $85.83_{\pm0.62}$		
AGCKD (Ours)	$97.78_{\pm 0.95}$	$95.93_{\pm1.30}$	$94.13_{\pm0.81}$	$92.67_{\pm 0.40}$	$91.71_{\pm 0.79}$	$90.97_{\pm0.65}$	$90.11_{\pm0.53}$	${\bf 88.68}_{\pm0.47}$		
5-way 5-shot of TACRED										
Joint Training SeqRun	$97.93_{\pm 0.47}$ $97.06_{\pm 1.34}$	$96.25_{\pm0.35}$ $92.77_{\pm1.36}$	$94.09_{\pm 0.45}$ $85.76_{\pm 3.06}$	$92.37_{\pm0.39}$ $80.95_{\pm 2.82}$	$91.96_{\pm 0.71}$ $75.19_{\pm 3.87}$	$91.15_{\pm 0.56}$ $66.62_{\pm 3.71}$	$90.35_{\pm 0.40}$ $55.53_{\pm2.05}$	$88.9_{\pm 0.03}$ $42.57_{\pm2.26}$		
CEAR SCKD ERDA ConPL	$82.14_{\pm 7.28}$ $88.42_{\pm0.83}$ $94.57_{\pm 2.72}$ $96.79_{\pm3.01}$	$68.43_{\pm 8.46}$ $79.35_{\pm 4.13}$ $86.55_{\pm3.55}$ $88.65_{\pm 4.61}$	$57.43_{\pm 6.80}$ $70.61_{\pm3.16}$ $78.59_{\pm2.88}$ $85.40_{\pm 4.66}$	$51.83_{+6.75}$ $66.78_{+4.29}$ $74.58_{\pm 3.92}$ $82.67_{\pm 2.67}$	$48.71_{\pm 6.04}$ $60.47_{\pm3.05}$ $69.31_{\pm 1.63}$ $80.82_{\pm 2.79}$	$45.23_{\pm 4.25}$ $58.05_{\pm 3.84}$ $66.53_{+3.12}$ $79.46_{\pm3.26}$	$43.29_{\pm 2.88}$ $54.41_{\pm3.47}$ $61.92_{\pm 4.61}$ $77.47_{\pm2.34}$	$40.74_{\pm 4.08}$ $52.11_{\pm3.15}$ $55.97_{\pm2.16}$ $75.82_{\pm 1.12}$		
AGCKD (Ours)	$98.85_{\pm1.37}$	$91.43_{\pm 3.17}$	$\textbf{87.89}_{\pm 3.89}$	$\textbf{85.04}_{\pm 2.26}$	$83.12_{\pm1.69}$	$81.99_{\pm 2.34}$	$80.48_{\pm 2.24}$	$78.56_{\pm 1.10}$		

Table 1: Accuracy (%) of various methods for each task on Fewrel's 10-way 5-shot and TACRED's 5-way 5-shot.

Figure 3: Comparison results for each task on Fewrel's 10-way 2-shot, Fewrel's 10-way 10-shot and TACRED's 5-way 10-shot. The variance is reported as light color regions.

454 model to face severe catastrophic forgetting, so it **455** serves as a lower bound.

456 4.2 Main Results

457 4.2.1 FewRel Benchmark

 The accuracy of AGCKD for each task on Fewrel's 10-way 5-shot, 2-shot and 10-shot is described in Table [1](#page-6-0) and Fig. [3.](#page-6-1) From these results, we can observe that:

 (1) By comparing the mean in Table [1,](#page-6-0) we can find that AGCKD is significantly higher than the traditional method at each time step. The perfor-465 mance in $T¹$ indicates that AGCKD can effectively adopt the general knowledge learned by BERT. Meanwhile, AGCKD also achieves state-of-the-art **performance in** $T⁸$, reflecting that the interference between different task parameters in AGCKD is the least, which mainly benefits from adaptive cor-rection of the gradient and efficient decomposition

of knowledge during model training. As a tradi- **472** tional method of CRE, CEAR requires many train- **473** ing data to learn the memory and embedding of **474** a new task. When there is less training data, the **475** features learned by the model will become unsta- **476** ble, which makes it collapse with the performance. **477** ConPL and ERDA adjust the consistency of embed- **478** ding indirectly only from the perspective of the loss **479** function and data augmentation, which has limited **480** ability to improve following degree. We further **481** discuss the forgetting metrics of ConPL, ERDA **482** and AGCKD in Appendix [C.](#page-10-2) 483

(2) The standard deviation of AGCKD on the **484** final task T^8 remains at a low level compared with 485 the other methods, which indicates that it has a **486** small fluctuation range when faced with different **487** task sequences. It further reflects the robustness of **488** AGCKD under different task sequences, thanks to **489** the gradient correction matrix constraining the off- **490**

Figure 4: The sum of AOD and ROD of baselines on FewRel's 10-way 5-shot. The abscissa represents all 7 task indexes of models.

 set of the previous samples' embedding during pa- rameter update. To prove this, we calculate the sum of AOD and ROD for each task in the model and show them in Fig. [4.](#page-7-0) It can be seen that AGCKD has low-level AOD and ROD on all tasks. In com- bination with Table [1,](#page-6-0) we observe that the smaller the sum of AOD and ROD of the model, the higher the accuracy. This is also consistent with our pre- vious theoretical analysis of the following degree and offset distance.

 (3) As is shown in Fig. [3,](#page-6-1) the performance of AGCKD is close to Joint Training, which indicates that AGCKD is less affected by catastrophic for- getting during training. In this case, we consider that more information introduced by new tasks also unexpectedly leads to the decline of model perfor- mance. Because the training times of samples at different time steps may be uneven during joint training, AGCKD even exceeds Joint Training on some tasks.

511 4.2.2 TACRED Benchmark

 The performance of AGCKD for each task on TA- CRED's 5-way 5-shot and 10-shot is shown in Ta- ble [1](#page-6-0) and Fig. [3.](#page-6-1) It can be observed from these results that AGCKD still has advantages over state- of-the-art methods. AGCKD has a strong gener- alization ability, which depends on our approach without any dataset-specific components.

519 4.3 Ablation Study

 To verify the effectiveness of each part in AGCKD, we performed ablation experiments. Specifically, we separately remove adaptive gradient correc- tion (w.o.AGC) and knowledge decomposition (w.o.KD). Average ablation results for the final tasks are presented in Fig. [5.](#page-7-1)

526 Through the box line diagram, the adaptive gradi-

Figure 5: Box line diagram of ablation study on FewRel's 10-way-5-shot. The vertical axis represents accuracy of the model on the final task T^8 .

ent correction and knowledge deconstruction mod- **527** ule have a great impact on the average accuracy **528** and performance stability of the model. The sepa- **529** rate use of these two modules leads to confusion **530** about the corresponding part of knowledge, which **531** greatly damages the performance of the model. Ac- **532** cording to the definition, while reducing AOD, it **533** also indirectly reduces ROD. Thus, the adaptive **534** gradient correction has a greater impact on the final **535** result. This phenomenon again demonstrates the **536** effectiveness of the adaptive gradient correction **537** algorithm and the importance of reducing the im- **538** pact of subsequent tasks on previous tasks in the **539** embedding space. 540

5 Conclusion 541

In this paper, a method of direct decoupling pa- **542** rameters and modifying gradient is proposed to **543** improve the following degree of samples, which **544** can eventually reduce the catastrophic forgetting **545** for CFRE. Specifically, we first propose the con- **546** cept of the following degree and analyze it from **547** the perspectives of AOD and ROD. The parame- **548** ters of the model are decomposed into general and **549** task-related knowledge based on metric learning. **550** For general knowledge, an adaptive gradient cor- **551** rection algorithm is proposed to reduce the impact **552** of gradient updates on previous knowledge, which **553** can reduce the AOD of samples. For task-related **554** knowledge, we update the parameters discretely **555** and continuously in three different training stages **556** to optimize ROD between prototypes and samples. **557** The theoretical derivation and experimental results **558** on two standard benchmarks verify the superiority **559** of AGCKD. **560**

⁵⁶¹ Limitations

 In practical calculations, a small ROD is a suffi- cient and unnecessary condition for better model performance. Specifically, if ROD is large and the distance between prototypes is also relatively large, the model performance will not also be poor. In future work, we hope to consider the distance be- tween classes in ROD and obtain a necessary and sufficient condition for model performance.

 Currently, in the field of NLP, since the transformer-based model is the most widely used language model, we have only explored gradient correction algorithms for the relevant structures in the transformer. The performance of AGCKD in CFRE based on a transformer shows us the poten- tial for designing gradient correction algorithms in other model architectures. And we will further explore the algorithm for gradient correction of pa- rameters in other network structures (such as CNN, RNN, etc.).

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⁷⁴⁷ A Mathematical Proof of Adaptive **⁷⁴⁸** Gradient Correction Algorithm

 To prove that the algorithm can adaptively correct the gradient so that the model updates have less impact on the previous task samples, we record $H_i^l \in R^{d \times 1}$ as the layer *l* embedding correspond- ing to the memory sample of category i and $E_i^l \in$ $R^{d\times 1}$ as that corresponding to any training sample of category i. Since the memory samples are calcu- lated according to the maximum cosine similarity of the average class sample, the vector angle of H_i^l and E_i^l is much smaller than that of $H_{j(j\neq i)}^l$ and E_i^l (also thanks to the optimization of metric learning). C_i^l is essentially a linear transformation of any vector into the space which is orthogonal to H_i^l . Accordingly, when the angle between H_i^l and E_i^l is small, E_i^l is approximately equal to zero vec- tor after linear transformation through C_i^l . From a single vector to the entire C^l matrix, we can **get:** $\Delta W^l E^l = \frac{\partial L_{gen}}{\partial W^l} (C^l E^l) \approx 0.$

767 For the FFN layer in BERT, it avoids the inter-**768** ference of the gradient update of subsequent tasks **769** on the embeddings of previous tasks:

$$
Out_{k}^{FFN} = X + W^{FFN}X
$$

= $X + (W^{FFN} + \gamma \frac{\partial L_{gen}}{\partial W^{FFN}} C^{FFN})X$
= Out_{k+1}^{FFN} (11)

 771 where Out_k^{FFN} is the output of FFN at time step where \bigcup_{k}^{n} is the output of TTV at three supplies of K , $X \in R^{d \times 1}$ is $[MASK]$ token embedding of 773 any previous sample, and C^{FFN} is calculated by 774 memory \hat{M}^k .

 For the self-attention module in BERT, we freeze the key and value matrices, while the gradient cor- rection and parameter update are only performed on the query matrix. The common self-attention formula is as follows:

$$
Q = X^T W^q
$$

\n
$$
K = X^T W^k
$$

\n
$$
V = X^T W^v
$$

\n
$$
SelfAttention(Q, K, V) = softmax(\frac{QK^T}{\sqrt{d}})V
$$

\n(12)

where $X = [x_1, \dots, x_{\lfloor mask \rfloor}, \dots, x_n] \in R^{d \times n}$ **781** is the token embedding sequence of any previous sample. We set the updated Q as Q' :

$$
Q' = X^T (W^q + \gamma (C^q)^T \frac{\partial L_{gen}}{\partial W^q})
$$

= $[q'_1, \cdots, q_{[mask]}, \cdots, q'_n]^T$ (13) 784

where vector $q'_n \in R^{1 \times d}$ is the *n*th row of matrix 785 Q' . . **786**

$$
Q'K^{T} = \begin{bmatrix} q'_{1}k_{1}^{T} & q'_{1}k_{2}^{T} & \cdots & q'_{1}k_{n}^{T} \\ \vdots & \vdots & \ddots & \vdots \\ q_{[mask]}k_{1}^{T} & q_{[mask]}k_{2}^{T} & \cdots & q_{[mask]}k_{n}^{T} \\ \vdots & \vdots & \ddots & \vdots \\ q'_{n}k_{1}^{T} & q'_{n}k_{2}^{T} & \cdots & q'_{n}k_{n}^{T} \end{bmatrix}
$$
 787

Let $A' = softmax(\frac{Q'K^T}{\sqrt{d}})$, then the row vec- 788 tor corresponding to [MASK] token in matrix **789** A' is consistent with that in A, that is, $A' = 790$ $[a'_1, \dots, a_{mask}, \dots, a'_n]^T$. Thus, the embedding 791 of [MASK] token in A′V is consistent with that **⁷⁹²** before the gradient update, i.e. the output of self- **793** attention related to previous tasks is not affected by **794** the updated gradient of subsequent tasks. In other **795** words, our gradient correction method can also **796** avoid the knowledge coverage caused by gradient **797** updates in the self-attention layer. **798**

B Training Details **799**

The BERT-base [\(Devlin et al.,](#page-8-17) [2018\)](#page-8-17) is used as the **800** [e](#page-8-18)ncoder and is trained using AdamW [\(Loshchilov](#page-8-18) **801** [and Hutter,](#page-8-18) [2018\)](#page-8-18) optimizer at a learning rate $\gamma = 802$ $2e - 5$. The head of the attention mechanism is 803 set to 8 and the embedding size of BERT is 768, 804 i.e. $d = 768$. The batch size is set to 5. We 805 train the model one time at the first training step **806** $(epoch₁ = 1)$, and three times at the second step 807 and third step $(epoch_2 = epoch_3 = 1)$. We set 808 $\alpha = 0.2$ in P^{sim} . The memory is size set to 1 for 809 each class. AGCKD can complete all tasks in about **810** 20 minutes using one NVIDIA 4060Ti GPU. We **811** run the model 6 times with different task sequences **812** and report the mean result. 813

C Forgetting Metrics **⁸¹⁴**

The degree of catastrophic forgetting of AGCKD **815** is measured by the forgetting metrics proposed by **816 817** [Chaudhry et al.](#page-8-19) [\(2018\)](#page-8-19). After learning all tasks, the

: **783**

Method	Task index								
		\mathcal{D}	$\mathbf{\hat{z}}$	4	5	6	7	Mean	
Joint Train	7.07	4.28	3.02	2.00	1.43	3.99	0.50	3.18	
SeaRun	49.28	49.08	44.18	39.69	28.93	11.14	7.29	32.80	
ERDA	21.52	15.54	13.18	13.14	9.69	9.46	6.93	12.78	
ConPI.	11.47	6.11	3.79	2.47	0.46	-0.12	-0.98	3.31	
AGCKD (Ours)	7.87	5.34	5.39	2.40	2.46	-1.05	0.30	3.24	

Table 2: Forgetting (%) of various methods after training for each task on FewRel's 10-way-5-shot.

Method	Task index								
Related to T^1 2.50 2.40 2.40 1.90 2.10 1.90							-2.00	-1.60	
Related to \hat{T}^k 2.50 4.50 6.40 9.40 11.60 12.20 12.60								- 16.60	

Table 3: The error rate (%) of AGCKD for each task on D_{test}^1 . After the learning of T^k , the first line represents the error rate related to T^1 ; the second line represents that related to all tasks visible to the model.

818 following formula is calculated on all test datasets:

$$
F_k = \frac{1}{n-k} \sum_{j=k+1}^n \max_{l \in \{k,\dots,j-1\}} (a_{l,k} - a_{j,k}) \tag{15}
$$

820 where $a_{l,k}$ is the accuracy of the model on task k 821 **after the training step l and n is the total number of** 822 tasks. $F_k(k \in [1, \cdots, n-1])$ is the forgetting met-**823** rics of task k after all training steps. Obviously, the 824 smaller F_k , the less knowledge the model forgets.

[2](#page-11-0)5 Table 2 shows the forgetting metrics after train- ing for each task on FewRel's 10-way-5-shot. The average forgetting metrics of AGCKD are lower than that of other methods and are closest to Joint 829 Training, which indicates that AGCKD can reduce catastrophic forgetting to a certain extent. At the same time, we find that even if all the training data are available, forgetting still exists. This may be because this index does not fully consider the in-formation increment of the newly introduced task.

 To observe the forgetting metrics more intu- itively, Table [3](#page-11-1) directly shows the total error rate 837 and that related to T^1 at each time step k on D_{test}^1 . The errors related to the first learning task of the model almost do not continue to increase, which in- tuitively reflects that AGCKD can effectively avoid the catastrophic forgetting of previous tasks. **841**