OBLIVIOUS UNLEARNING BY LEARNING: MACHINE UNLEARNING WITHOUT EXPOSING ERASED DATA

Anonymous authors

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ABSTRACT

Machine unlearning enables users to remove the influence of their data from trained models, thus protecting their privacy. However, it is paradoxical that most unlearning methods require users first to upload their to-be-removed data to machine learning servers and notify the servers of their unlearning intentions to prepare appropriate unlearning methods. Both unlearned data and unlearning intentions are sensitive user information. Exposing this information to the server for unlearning operations conflicts with the privacy protection goal. In this paper, we investigate the challenge of implementing unlearning without exposing erased data and unlearning intentions to the server. We propose an Oblivious Unlearning by Learning (OUbL) approach to address this privacy-preserving machine unlearning problem. In OUbL, the users construct a new dataset with synthesized unlearning noise, ensuring that once the server incrementally updates the model using the original learning algorithm based on this dataset, it can implement unlearning. The server does not need to perform any tailored unlearning operation and remains unaware that the constructed samples are for unlearning. As a result, the process is oblivious to the server regarding unlearning intentions. Additionally, by transforming the original erased data into unlearning noise and distributing this noise across numerous auxiliary samples, our approach protects the privacy of the unlearned data while effectively implementing unlearning. The effectiveness of the proposed OUbL method is evaluated through extensive experiments on three representative datasets across various model architectures and four mainstream unlearning benchmarks. The results demonstrate the significant superiority of OUbL over the state-of-the-art privacy-preserving unlearning benchmarks in terms of both privacy protection and unlearning effectiveness.

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1 INTRODUCTION

Machine unlearning enables users to exercise the right to remove the influence of specific data samples from trained machine learning (ML) models, thereby protecting user privacy. Paradoxically, while the goal of machine unlearning is to protect user privacy, most unlearning methods necessitate that users upload their specified data to the ML server as a prerequisite for executing the unlearning process (Bourtoule et al., 2021; Warnecke et al., 2023). Additionally, users must inform the server that the uploaded data are intended for unlearning purposes, enabling the server to prepare and execute the corresponding unlearning methods and operations (Thudi et al., 2022; Hu et al., 2024b).

However, these requirements expose the privacy of users' unlearning data and intentions, rendering 044 existing unlearning methods impractical in privacy-sensitive scenarios. In privacy-preserving ML 045 contexts, such as those described in (Cao et al., 2021; Bonawitz et al., 2017; Sun et al., 2022; 046 Naseri et al., 2022), the server is restricted from accessing individuals' data due to privacy concerns. 047 Moreover, modifying the original learning algorithms is challenging in these contexts, as most ML 048 models are trained using secure mechanisms like federated learning (FL) (Cao et al., 2021; Naseri et al., 2022) or secure multi-party computation (MPC) (Mohassel & Zhang, 2017; Knott et al., 2021). Additionally, even if the erased samples are protected, exposing unlearning intentions can 051 allow adversaries to conduct inversion attacks targeted at unlearning updates (Hu et al., 2024a; Chen et al., 2021; Zhang et al., 2023). Exposing erased data and unlearning intentions to ML servers 052 for unlearning contradicts the privacy-preserving frameworks' requirements (Naseri et al., 2022; Bonawitz et al., 2017; Cao et al., 2021) and undermines the fundamental purpose of the right to 054 be forgotten (Liu et al., 2022b; Dang, 2021). Therefore, a privacy-preserving machine unlearning 055 service is crucial and necessary, and we explore the following question: "Is it possible to achieve 056 machine unlearning without revealing users' erased data and unlearning intentions to the server?"

057 Motivation. Machine learning models can be regarded as mappings of the training data (Goodfellow et al., 2016; Shalev-Shwartz & Ben-David, 2014). Consequently, altering the training data can change the model's performance, such as poisoning and backdooring methods (Lin et al., 2020; 060 Zeng et al., 2023; Tramèr et al., 2022; Liu et al., 2022a), data "unlearnable" methods (Fu et al., 061 2022; Sandoval-Segura et al., 2022), and adversarial attacks (Kang et al., 2024; Madry et al., 2018; 062 Zhou et al., 2023). Inspired by these works, we investigate the construction of a synthetic dataset 063 with unlearning noise that ensures the unlearning effect when the server updates the model based 064 on the constructed dataset. Since the model update uses only the original learning algorithms, users do not need to inform the server to prepare specific unlearning operations, thereby protecting the 065 privacy of unlearning intentions. 066

067 In this paper, we begin by reformulating the privacy-protection unlearning problem as an *oblivi*-068 ous unlearning by learning problem to investigate the research question. We propose an Oblivious 069 Unlearning by Learning (OUbL) strategy to address this problem. The goal is to synthesize a new dataset that includes both clean samples and unlearning noise-injected auxiliary samples. The un-071 learning effect is achieved when the server updates the model using the original learning algorithm on the synthesized dataset. The implementation of OUbL hinges on two key aspects: (1) precisely 072 estimating the unlearning model update as the target for unlearning noise generation, using only the 073 information of the unlearning user, and (2) designing an efficient method to generate the unlearning 074 noise for the auxiliary dataset to achieve the desired unlearning effect. Specifically, we first propose 075 an efficient unlearning update estimation method based on Hessian-vector products, which samples 076 only the data of the unlearning user, ensuring that users can calculate it efficiently by themselves. 077 Second, we generate the unlearning noise through gradient matching, i.e., finding the noise-injected data with gradients update similar to the estimated unlearning update. We propose an unlearning 079 noise descent method to efficiently synthesize the noise, treating the noise matrix as an input layer and fixing the entire model, thereby only calculating the gradient for the noise layer for the update.

081 We conducted extensive experiments on three representative datasets and compared our method 082 with four mainstream unlearning benchmarks to evaluate both privacy protection and unlearning 083 effectiveness. To assess privacy protection, we performed unlearning inversion attacks (Hu et al., 084 2024a; Zhang et al., 2023) to reconstruct the erased samples across different unlearning methods, 085 comparing their reconstruction similarity to demonstrate the privacy protection effect. A lower reconstruction similarity indicates better privacy protection. For evaluating unlearning effectiveness, 087 we employed a prevalent data removal verification method, MIB (Hu et al., 2022). The experimen-880 tal results demonstrate that OUbL offers superior privacy protection and unlearning effectiveness compared to existing privacy-preserving unlearning methods (Wang et al., 2023; Liu et al., 2022b). 089 In comparison with state-of-the-art unlearning methods without privacy protection (Bourtoule et al., 090 2021; Nguyen et al., 2020), OUbL incurs only a slight trade-off in model utility. 091

092 Our contributions are summarized as follows:

- To the best of our knowledge, this paper is the *first* to identify the privacy threats posed by the 094 exposure of both unlearning intentions and unlearned data during machine unlearning processes. 095 It highlights the paradox of the existing unlearning methods that require unlearning users to upload 096 raw data and inform the server to prepare customized unlearning algorithms, which conflicts with the original privacy-protection goal of the right to be forgotten.
- 098 • We propose an OUbL approach to protect unlearned data and unlearning intentions during machine unlearning processes. OUbL contributes a precise unlearning updates estimation method 100 and an efficient unlearning noise generation method to ensure the unlearning effect when the server updates the model using the original learning algorithm based on the constructed dataset.
- 102 • We conducted extensive experiments to compare OUbL with exact and approximate unlearning 103 methods, with and without privacy protection. The results validate OUbL's superiority in terms 104 of privacy protection and unlearning effectiveness over existing privacy-preserving methods, with 105 only a slight trade-off in model utility compared to unlearning methods without privacy protection.
- The source code and the artifact of the OUbL is released at https://anonymous.4open. 106 science/r/OUL-55F6, which creates a new tool for protecting the privacy of erased data and 107 unlearning intentions during machine unlearning processes.

108 2 PRELIMINARY AND PROBLEM STATEMENT

To facilitate the understanding of the privacy-preserving machine unlearning problem, we first introduce the mainstream process of unlearning. A detailed discussion about the "Related Work" of machine unlearning is presented in Appendix A.

113 114 115 116 117 118 Machine Unlearning. The unlearning process typically includes the following phases: (1) The 119 server trained a model with parameters θ_o derived from dataset D. (2) The user uploads the dataset 110 D_u for which they request unlearning to the server, indicating the data to be erased from the model. 111 (3) Upon receiving the unlearning request, the server executes an unlearning algorithm \mathcal{U} to remove 112 the contributions of D_u from θ_o , resulting in an unlearned model $\theta_{D \setminus D_u}$, also denoted as θ_u .

Note that this is a standard machine unlearning process without privacy protection, which exposes both the unlearning intentions and the erased data to the server in phases (2) and (3). To protect the privacy of erased samples and unlearning intentions, it is necessary to modify phases (2) and (3). These modifications should ensure that unlearning can be implemented without exposing D_u to the server and without informing the server of the unlearning intention, needing to eliminate the dependence on specified unlearning algorithms.

One primary challenge is the need to eliminate reliance on tailored unlearning methods from the 125 server, thereby avoiding the exposure of unlearning intentions. Given that the server is aware of 126 the original learning algorithm \mathcal{A} and that model updates are a reasonable requirement in real-world 127 scenarios (Kirkpatrick et al., 2017; Wu et al., 2019; Wang et al., 2022), we pose the question: Can we 128 achieve unlearning through incremental learning to prevent the server from detecting unlearning in-129 tentions? In addition to protecting unlearning intentions by solely executing incremental learning, a 130 privacy-preserving mechanism C is necessary to safeguard the erased data. Furthermore, the scheme 131 should not come at the cost of significant model utility degradation. Therefore, we formulate the 132 privacy-preserving unlearning problem into an *oblivious unlearning by learning problem* as follows.

133 Problem Statement (Oblivious unlearning by learning). Suppose the ML server has an original 134 trained model θ_o , trained using algorithm A on dataset D. Let the unlearning user possess the 135 unlearned dataset $D_u = (X_u, Y_u)$, where $D_u \subset D$. Oblivious unlearning by learning aims to (1) 136 protect the privacy of the unlearned data D_u by designing a mechanism $\mathcal{C}(D_a, D_u) \to D_a^p$ that 137 conceals the erased data as unlearning noise on users' new updating auxiliary dataset D_a , and (2) protect the privacy of unlearning intentions by achieving the unlearning effect through incrementally 138 updating the model θ_{0} using the original learning algorithm \mathcal{A} on D_{p}^{p} . To preserve model function-139 ality, the incrementally updated model should attain a similar model utility as traditional unlearning 140 algorithms U, i.e., 141

$$\mathcal{U}(\theta_o, D_u, D) \approx \mathcal{A}(\theta_o, \mathcal{C}(D_a, D_u)). \tag{1}$$

To solve the Eq. (1), since the learning algorithm \mathcal{A} and the unlearned data are fixed, our focus shifts to designing the dataset construction mechanism \mathcal{C} . This mechanism must effectively protect the privacy of D_u and ensure the desired unlearning effect using the constructed dataset $\mathcal{C}(D_a, D_u)$ during model updating.

3 OBLIVIOUS UNLEARNING BY LEARNING (OUBL)

150 3.1 BASIC IDEA AND OVERVIEW OF OUBL151

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152 Assume we have an unlearned model θ_u and the original trained model θ_o . The unlearning update 153 is given by $\Delta \theta_{D_u} = \theta_u - \theta_o$. When we update a model based on a new dataset, such as $D_a^p = \mathcal{C}(D_a, D_u)$, we have $\theta \leftarrow \theta_o - \nabla \ell(D_a^p; \theta_o)$. To achieve unlearning based on the incremental learning 155 update, we must ensure that:

$$\theta_u = \theta_o - \frac{1}{P} \sum_{(x,y) \in D_a^p} \nabla \ell((x,y);\theta_o), \qquad \text{where} \quad \frac{1}{P} \sum_{(x,y) \in D_a^p} \nabla \ell((x,y);\theta_o) = -\Delta \theta_{D_u}, \tag{2}$$

and P is the size of D_a^p . If we can construct a dataset D_a^p meets the requirement of Eq. (2), we can achieve the oblivious machine unlearning by learning, guaranteeing (a) the erased data is hidden from the server as it has not been used in the update, and (b) the unlearning intention is hidden to the server as there is no unlearning request, just normal model update. However, to achieve the oblivious



Figure 1: The main process of OUbL includes three components. First, the unlearning user estimates the influence \mathcal{I}_{D_u} of unlearning the erased data from the trained model. Second, the user customizes the noise for an auxiliary dataset such that incrementally training the model based on the synthesized auxiliary dataset D_a^p can effectively unlearn the erased data. Third, the unlearning user prepares a clean dataset D_c to preserve the model utility and uploads both the clean and synthesized auxiliary datasets to the server for incremental learning, thereby achieving the unlearning effect.

unlearning effect, there are two main challenges: (1) it is hard to achieve a precise unlearning model
update before we execute the unlearning procedure with the above restriction; (2) even if we achieve
the unlearning update, it is challenging to construct the dataset so that the server can incrementally
update based on the constructed dataset to achieve the unlearning effect.

Overview of OUbL. We propose an approach called OUbL to overcome the aforementioned challenges. The main process of OUbL, illustrated in Figure 1, comprises three key components: unlearning update estimation, generating unlearning noise to synthesize auxiliary data, and unlearning by learning training with utility compensation.

3.2 UNLEARNING UPDATE ESTIMATION

Many existing approximate unlearning methods first estimate the unlearning influence and then
 reduce the estimated unlearning influence from the trained model for unlearning (Guo et al., 2020;
 Sekhari et al., 2021; Liu et al., 2022b). A representative unlearning influence estimation method
 involves the use of a Hessian matrix-based approximation, which can be described as follows:

$$\Delta \theta_{D_u} = \theta_{D \setminus D_u} - \theta_o \simeq \mathcal{I}^{(1)}(D_u) = \frac{1}{n-m} H_{\theta_o}^{-1} \sum_{(x_u, y_u) \in D_u} \nabla \ell((x_u, y_u); \theta_o), \tag{3}$$

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197 where $H_{\theta_a}^{-1}$ denotes the inverse of the Hessian matrix evaluated at θ_o on the dataset $D \setminus D_u$, n is 198 the size of D, and m is the size of D_u . $\nabla \ell$ denotes the gradients of the learning algorithm with 199 loss function ℓ , and $\mathcal{I}^{(1)}(D_u)$ denotes the estimated first-order influence of the unlearning data D_u . 200 Eq. (3) is commonly used in (Guo et al., 2020; Sekhari et al., 2021; Liu et al., 2022b).

However, studies (Guo et al., 2020; Sekhari et al., 2021; Liu et al., 2022b) calculate Eq. (3) with the assistance of the entire remaining dataset, which is prohibited in privacy-concerning scenarios. In our setting, the unlearning user cannot access the entire training dataset D; they can only access their own dataset. Moreover, forming and inverting the Hessian of the empirical risk $H_{\theta_o}^{-1}$ requires $O(np^2 + p^3)$ operations, as the original dataset contains n samples and $\theta_o \in \mathbb{R}^p$. This computation is too expensive for large neural networks.

We propose an efficient unlearning update estimation (EUUE) method to overcome the aforementioned challenges by using Hessian-vector products (HVPs) to directly approximate the unlearning update $H_{\theta_o}^{-1} \sum_{(x_u, y_u) \in D_u} \nabla \ell((x_u, y_u); \theta_o)$. This idea is inspired by (Agarwal et al., 2016; Koh & Liang, 2017). It requires only the assistance of the erased samples and a few clean training samples of the unlearning user, ensuring that the user can calculate it. For clarity, we drop the θ_o subscript. We employ an estimator that samples a single point per iteration for a fast Hessian matrix calculation. Let $H_j^{-1} \stackrel{\text{def}}{=} \sum_{i=0}^j (I - H)^i$ be the first j terms in the Taylor expansion of H^{-1} , where Iis the identity matrix. We can rewrite this recursively as $H_j^{-1} = I + (I - H)H_{j-1}^{-1}$. From the validity of the Taylor expansion, $H_j^{-1} \to H^{-1}$ as $j \to \infty$. We can substitute the full H with a draw from any unbiased estimator of H to form \tilde{H}_j^{-1} at each iteration. We have $\mathbb{E}[\tilde{H}_j^{-1}] \to H^{-1}$ as $\mathbb{E}[\tilde{H}_j^{-1}] = H_j^{-1}$. The detailed process of EUUE is presented in Algorithm 2 in Appendix B.

3.3 GENERATING UNLEARNING NOISE FOR AUXILIARY DATASET

Having achieved the estimated unlearning update $\Delta \theta_{D_u}$ from the above process, we can reformulate the condition of Eq. (2) for noise synthesis. Instead of directly synthesizing the dataset, we generate noise for a normal update dataset. This approach avoids generating samples that significantly differ from the original data, which could harm the model's utility. Assume we now have an auxiliary dataset $D_a : (X_a, Y_a)$. We add the noise Δ^p to D_a , resulting in $D_a^p = (X_a + \Delta^p, Y_a)$, ensuring that the model update is similar to the update for unlearning. Specifically, we need to satisfy $\frac{1}{P} \sum_{(x,y) \in D_a^p} \nabla \ell((x,y); \theta_o) + \Delta \theta_{D_u} = 0$ according to Eq. (2), which can be reformulated as follows for finding suitable noise.

$$\min_{\Delta^p} \| (\frac{1}{P} \sum_{(x_i, y_i) \in D_a} \nabla \ell((x_i + \Delta^p_i, y_i); \theta_o) + \Delta \theta_{D_u} \|, \quad \text{s.t. } \Delta^p \in \arg\min_{\theta} \frac{1}{N} \sum_{i \le N} \ell((x_i + \Delta^p_i, y_i); \theta),$$

where N is the size of $D \setminus D_u \cup D_a$, and the value of $\Delta \theta_{D_u}$ is estimated according to Eq. (3). (4)

Noise Synthesis by Gradient Matching. Our objective is to find noise Δ^p such that, when the model is trained on the noise-synthesized auxiliary samples D_a^p , it minimizes the two losses in Eq. (4), thus making the model unlearn the erased samples. However, directly solving Eq. (4) is computationally intractable due to the bilevel nature of the optimization objective. Instead, one may implicitly minimize the unlearning update by finding suitable Δ^p such that for any model parameter θ , the following condition is satisfied:

$$\Delta \theta_{D_u} \approx -\frac{1}{P} \sum_{(x_i, y_i) \in D_a} \nabla_{\theta} \ell((x_i + \Delta_i^p, y_i); \theta).$$
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If we can enforce Eq. (5) to hold for any θ during training, then the gradient steps that minimize the training loss on the synthesized auxiliary data will also minimize the unlearning target, satisfying $\frac{1}{P}\sum_{(x,y)\in D_a^p} \nabla \ell((x,y);\theta_o) + \Delta \theta_{D_u} = 0.$ Unfortunately, calculating Δ^p that satisfies Eq. (5) is also intractable as it is required to hold for all values of θ . In our setting, the unlearning user cannot access θ for samples in the remaining dataset $D \setminus D_u$. One possible solution proposed in (Geiping et al., 2021; Di et al., 2022) is to relax Eq. (5) to be satisfied for a fixed model — the model obtained by training on the original dataset. We assume a well-trained model θ_o before unlearning and fix it during unlearning noise generation. Then, we can minimize the loss based on the cosine similarity between the two gradients as:

$$\phi(\Delta^p, \theta_o) = 1 - \frac{\langle \Delta\theta_{D_u}, -\frac{1}{P} \sum_{i=1}^{P} \nabla_{\theta} \ell((x_i + \Delta_i^p, y_i); \theta_o) \rangle}{\|\Delta\theta_{D_u}\| \cdot \| -\frac{1}{P} \sum_{i=1}^{P} \nabla_{\theta} \ell((x_i + \Delta_i^p, y_i); \theta_o)\|}.$$
(6)

Geiping et al. (Geiping et al., 2021) use R restarts, usually $R \le 10$, to increase the robustness of noise synthesis. Using this scheme, we can also find suitable noise for unlearning. However, it is not always effective because we cannot always achieve satisfactory random noise within 10 restarts. To address this issue, we propose an unlearning noise descent strategy.

Algorithm 1: Unlearning Noise Descent (UND)

Input: Trained model θ_o , unlearning update estimate $\Delta \theta_{D_u}$, auxiliary dataset D_a **Output:** The synthesized data with the unlearning noise, $D_a^p = (X_a + \Delta^p, Y_a)$ procedure UND ($\theta_o, \Delta \theta_{D_u}, D_a$): $\Delta_1^p \leftarrow \mathcal{N}(0,1)$ ▷ Initialize unlearning noise. for $i \leftarrow 1$ to n do $X_{a,i}^p \leftarrow X_a + \Delta_i^p \quad \rhd \text{ Add the noise to data.}$ $\nabla \theta_{o,i} \leftarrow \nabla_{\theta} \ell((X_{a,i}^p, Y_a); \theta_{o,i}) \quad \rhd \text{ Compute gradients.}$ $\phi_i \leftarrow \operatorname{Sim}(\Delta \theta_{D_u}, \nabla \theta_{o,i}) \qquad \rhd \text{ Compute similarity using Eq. (6).}$ $\Delta_{i+1}^p \leftarrow \Delta_i^p - \eta \nabla_{\Delta^p}(\phi_i) \qquad \rhd \text{ Update noise to match gradients.}$ return $D_{a,p} = (X_a + \Delta_{n+1}^p, Y_a)$

270 **Unlearning Noise Descent.** Algorithm 1 synthesizes unlearning noise to create a perturbed dataset 271 $D_{a,p} = (X_a + \Delta^p, Y_a)$. Firstly, we generate a noise matrix Δ^p as shown in line 1 of Algorithm 1 272 and treat it as parameters that could be updated during optimization. Then, during optimization, we 273 fix the trained model parameters θ_o and add the noise to the auxiliary data D_a as the input to the 274 model (line 4). We calculate the gradients of the noise-synthesized data based on the current model point but do not update the model (line 5). Moreover, we calculate the minimization loss according 275 to Eq. (6) (line 6). With this loss, we can use the gradient descent method for both the model and 276 the unlearning noise matrix, but we only update the noise matrix Δ^p while keeping the model θ_o 277 fixed (line 7). After a few rounds of iteration, we can synthesize sufficient unlearning noise to the 278 auxiliary data to achieve the unlearning effect. 279

3.4 Oblivious Unlearning Guarantee and Utility Preservation

Oblivious Unlearning Guarantee by Incremental Learning. Can gradient alignment cause model to converge to a model with low unlearning update approaching loss? To simplify presentation, we denote the unlearning update approaching loss \mathcal{L}_{unl} and incremental loss \mathcal{L}_{inc} of Eq. (4) as

$$\mathcal{L}_{unl}(\theta_o) =: ||(\frac{1}{P} \sum_{(x_i, y_i) \in D_a} \nabla \ell((x_i + \Delta_i^p, y_i); \theta_o) + \Delta \theta_{D_u}||,$$
(7)

$$\mathcal{L}_{inc}(\theta_o) =: \frac{1}{P} \sum_{i \le P} \ell((x_i + \Delta_i^p, y_i); \theta_o).$$
(8)

Additionally, recall that $1 - \phi(\Delta^p, \theta_o)$ measures the cosine similarity between the unlearning update and the incremental training update in Eq. (6). By adapting a classical result of Zoutendijk, the Theorem 3.2 in (Nocedal & Wright, 2006), we can elucidate why the unlearning effect can be accomplished by merely performing standard incremental training on the synthesized dataset.

Proposition 1 (Unlearning Descent by Learning). Let $\mathcal{L}_{unl}(\theta_o)$ be bounded below and have a Lipschitz continuous gradient with constant L > 0 and assume that the ML server incrementally trains the model by gradient descent with step sizes α_k , i.e. $\theta_o^{k+1} = \theta_o^k - \alpha_k \nabla \mathcal{L}_{inc}(\theta_o^k)$. If the gradient descent steps $\alpha_k > 0$ satisfy

$$\alpha_k L < \beta (1 - \phi(\Delta^p, \theta_o^k)) \frac{\|\nabla \mathcal{L}_{inc}(\theta_o^k)\|}{\|\nabla \mathcal{L}_{unl}(\theta_o^k)\|},\tag{9}$$

for some fixed $0 < \beta < 1$, then $\mathcal{L}_{unl}(\theta_o^{k+1}) < \mathcal{L}_{unl}(\theta_o^k)$. If in addition $\exists \epsilon > 0$, k_0 so that $\forall k \ge k_0$, $\phi(\Delta^p, \theta_o^k) < 1 - \epsilon$, then

$$\lim_{n \to \infty} \|\nabla \mathcal{L}_{unl}(\theta_o^k)\| \to 0.$$
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305 See supplementary material in Appendix D

Model Utility Preservation. Based on the above processes, the unlearning effect can be achieved by simply having the server update the model θ on the synthesized D_a^p using the learning algorithm \mathcal{A} . However, updating only based on the unlearning noise-injected data will compromise the model utility to some extent. To compensate for the model utility degradation, the unlearning user can mix some clean samples D_c to D_a^p as the final uploading dataset $D_{up} = D_a^p \cup D_c$. Following the empirical risk minimization (ERM) loss function, we can rewrite the incremental learning loss as:

$$\mathcal{L}_{D_a^p \cup D_c}(\theta) =: \frac{1}{P+C} \sum_{(x,y) \in D_a^p \cup D_c} \ell((x,y);\theta), \tag{11}$$

where P is the size of D_a^p and C is the size of D_c . Since D_c are clean samples, training on $D_a^p \cup D_c$ will mitigate the accuracy degradation, meanwhile with more clean samples in D_c to cover the unlearning noise-synthesized D_a^p will also enhance the privacy protection for erased data.

4 EXPERIMENTS

321 4.1 SETTINGS

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- **Datasets and Models.** We have conducted experiments on three widely adopted public datasets: MNIST (Deng, 2012), CIFAR10 (Krizhevsky et al., 2009), and CelebA (Liu et al., 2018), offering a
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range of objective categories with varying levels of learning complexity. The statistics of all datasets
 are listed and introduced in Appendix E.1. We select three model architectures of different sizes in
 our experiments: a 5-layer multi-layer perceptron (MLP) connected by ReLU on MNIST, a ResNet 18 on CIFAR10 and a 7-layer convolutional neural network (CNN) on CelebA.

Metric. To effectively evaluate privacy protection, we propose a reconstruction similarity metric, which calculates the cosine similarity between the erased samples and the reconstructed samples by the recovering attacking based on the unlearning update (Hu et al., 2024a; Salem et al., 2020; Zhang et al., 2023). These attacks are the most serious type of attack that aims to recover the erased information, and higher reconstruction similarity means more information is leaked. We also conduct reconstruction attacks on scenarios with and without unlearning intentions to clearly illustrate the importance of unlearning intentions in Section 4.4.

335 To effectively evaluate the unlearning effectiveness, we refer to prevalent data removal verification 336 methods (Hu et al., 2022; Guo et al., 2023), adding the backdoor patches to the unlearning samples 337 $D_{u,b} \leftarrow (X_u + patches, Y_u + target)$ for the original model training. Then, we execute the unlearn-338 ing methods to unlearn the backdoor-marked samples $D_{u,b}$. After unlearning, we test the **backdoor** 339 **accuracy** on the marked-unlearning samples $D_{u,b}$ to evaluate the unlearning effect. Moreover, since OUbL implements unlearning by training the model to approach the estimated unlearning update, 340 341 we propose an **unlearning update similarity** metric to evaluate the unlearning effect achieved by OUbL, which is calculated using the cosine similarity between the estimated unlearning update and 342 the truly unlearning update after conducting OUbL on the trained model. 343

Lastly, we use **model accuracy** to evaluate the model utility and functionality preservation, and we evaluate the efficiency of unlearning methods based on their **running time**. All the metrics are summarized in Appendix E.2.

347 **Compared Machine Unlearning Benchmarks.** To comprehensively compare OUbL with existing 348 machine unlearning methods, we consider the comparison with both no-privacy protection unlearn-349 ing methods and privacy protection methods. Specifically, we choose one exact unlearning method, 350 SISA (Bourtoule et al., 2021), and one approximate unlearning method, VBU (Nguyen et al., 2020), 351 as centralized no-privacy protection methods. We choose two state-of-the-art federated unlearning 352 methods, BFU (Wang et al., 2023) and Hessian matrix-based federated unlearning (HBFU) (Liu 353 et al., 2022b), as erased data privacy protection methods. We choose BFU and HBFU rather than other federated unlearning methods such as (Su & Li, 2023; Lin et al., 2024) because BFU and 354 HBFU achieve the best unlearning effect. In contrast, (Su & Li, 2023; Lin et al., 2024) focus more 355 on improving unlearning efficiency, which compromises unlearning effectiveness to some extent. 356 We briefly summarize these methods in Appendix E.3. 357

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4.2 PRIVACY PROTECTION EVALUATIONS

361 In this section, we evaluate the privacy protection of OUbL and the compared benchmarks. To 362 clearly demonstrate the privacy protection for the erased samples, we not only show the evaluation of the federated unlearning method, we also design a baseline by directly adding local differential 363 privacy (LDP) noise to the erased samples, $D_{u,\epsilon} = (X_u + LDP(\epsilon), Y_u)$, and implementing unlearn-364 ing using VBU, which is called VBU-LDP. We choose VBU to implement the baseline privacy-365 protection unlearning with LDP noise because VBU can implement unlearning only based on the 366 erased samples. Other unlearning methods require the assistance of the remaining dataset besides 367 the erased samples; combining LDP with these methods will inject too much noise and significantly 368 compromise the model's utility. The privacy protection evaluation results on three datasets are pre-369 sented in Figure 2. 370

Setup. The variable of this experiment is ϵ , which controls the injected LDP noise. By comparing the performance of OUbL with the VBU-LDP with different ϵ , we can directly observe which privacy protection level the OUbL achieved. In this experiment, we set the unlearning samples rate (USR), USR = 1% for all unlearning methods, and constructed samples rate CSR = 1% and auxiliary samples rate ASR = 1% for OUbL.

Privacy Protection Evaluated by Reconstruction Attacks. The first column in Figure 2 shows the
 reconstruction similarity, attacking by (Hu et al., 2024a; Zhang et al., 2023) to recover the erased
 samples of different unlearning methods. Note that the privacy protection of OUbL when informing



the server of unlearning intentions would be similar to the privacy protection of FL-based methods.
Since the reconstruction similarity of OUbL with unlearning intentions information overlaps with
BFU, we omit showing the performance of OUbL with unlearning intentions. Instead, we compare
OUbL with and without knowing unlearning intentions in Figure 5 in Section 4.4.

By hiding the unlearning intentions, OUbL can always achieve better privacy protection than BFU.
The attack is conducted based on the model updates on the server side, where the server of BFU
knows the unlearning intentions as it needs to inform other users to retrain, and the server of OUbL
does not know the unlearning intentions as it treats the OUbL process as a usual updating. OUbL has
a huge reconstruction similarity decrease than BFU on MNIST and CIFAR10 and a slight decrease
than BFU on CelebA.

Moreover, we compare OUbL with VBU-LDP to illustrate the privacy effect. OUbL achieves privacy protection like $\epsilon = 6$ LDP privacy protection of VBU-LDP on MNIST, similar to $\epsilon = 4$ LDP privacy protection of VBU-LDP on CIFAR10 and $\epsilon = 4$ LDP privacy protection on CelebA.

Trade-off between Privacy Protection and Unlearning Efficacy. With good privacy protection for the erased samples, OUbL simultaneously achieves much better model utility preservation than VBU-LDP and a much better data removal effect than BFU. For VBU-LDP, it is obvious that noise injection significantly decreases the model accuracy. There is a huge gap between VBU and VBU-LDP on the second column in Figure 2, and smaller ϵ decreases the model utility worse. Although BFU has not compromised the model accuracy with the assistance of normal federated users, it sometimes fails to unlearn the samples, such as the last figure on CelebA in Figure 2.

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4.3 UNLEARNING EFFICACY AND EFFICIENCY EVALUATIONS

422 Setup. We first illustrate the incremental training details of OUbL on MNIST, CIFAR10, and 423 CelebA to demonstrate unlearning effectiveness as shown in Figure 3. We also compare OUbL 424 with two centralized unlearning methods, SISA and VBU, and with two federated unlearning meth-425 ods, BFU and HBFU, in Figure 4. In this experiment, we conduct the evaluation for multi-sample 426 unlearning, where USR = 1%. We set the CSR = 1% and ASR = 1%.

Results of Unlearning Efficacy and Efficiency. From the unlearning efficacy perspective, Figure 3 definitely shows the unlearning effectiveness of incremental training on synthesized data (OUbL) compared with clean data. The backdoor accuracy on the unlearned dataset of OUbL drops obviously as the incremental training on synthesized data continues, which is confirmed in all three datasets. In Figure 4, OUbL achieves similar model accuracy and backdoor accuracy as SISA, a representative exact unlearning method without erased data privacy preservation. Although VBU



Figure 4: Evaluation of the effectiveness of different machine unlearning methods and datasets

achieves the best data removal effect (the lowest backdoor accuracy), it also compromises the model accuracy most, the lowest on all datasets. With the assistance of the other users to retrain the unlearned model, the federated unlearning methods (BFU and HBFU) achieve a similar model utility as OUbL and SISA. However, they may compromise data removal effects, worse than OUbL and SISA in most cases.

From the unlearning efficiency perspective, the third figure in Figure 4, OUbL achieves the second efficiency after the VBU. VBU is the most efficient because it implements unlearning solely based on the erased samples. Compared with centralized methods, the federated unlearning methods always consume more running time because FL-based methods require other normal users to participate in unlearning. Due to page limitation, additional experimental results are shown in Appendix F.

4.4 ABLATION STUDY OF CONSTRUCTED SAMPLES RATE AND AUXILIARY SAMPLES RATE

Clean Samples Rate (CSR) and Auxiliary Samples Rate (ASR) are two important pa-rameters that influence the unlearning dataset construction of OUbL. In this section, we conduct experiments to study the influence of these two parameters. We also compare the privacy protection of OUbL with a version of OUbL that allows the server to know the unlearning intentions (abbreviated as "OUbL know unl. int.").

Setup. For ease of conducting experiments, we maintain a CSR : ASR ratio of 1 : 1 when constructing the uploading dataset. We set the USR = 1% on MNIST and CIFAR10 and USR = 0.5% on CelebA. We range CSR and ASR from 1% and 6% on MNIST and CIFAR10, and from 0.5% to 1% on CelebA. The privacy budget of VBU-LDP is set $\epsilon =$ 10 here, and all the results are presented in Figure 5.



Figure 5: Evaluations for CSR and ASR

Relationship between Unlearning Update Similarity and *CSR* **and** *ASR***.** Usually, with more clean samples and auxiliary samples, it would be easier to approach the unlearning update based on



Figure 6: Evaluations of impact about different USR.

them. The first column in Figure 5 also demonstrates the trend. The unlearning update similarity 496 increases as the CSR and ASR increase on all three datasets.

Impact on Unlearning Effectiveness. Since the data removal effect (backdoor accuracy) is stable with different CSR and ASR, we only demonstrate the model utility in Figure 5. It is obvious that the model accuracy increases when the CSR and ASR increases. The model utility degradation caused by the unlearning effect definitely can be mitigated if we have more clean and auxiliary data for continual learning updates for unlearning.

Impact on Erased Data Protection. The third column of Figure 5 demonstrates the privacy protection for the erased data against the reconstruction attacks. Higher CSR and ASR means more clean 504 and auxiliary data is used to construct the uploading dataset. The unlearning noise is hidden in more 505 samples, which increases the reconstruction difficulty, showing as lower reconstruction similarity 506 in the third column in Figure 5. Compared with the "OUbL know unl. int.", the complete OUbL 507 that hides the unlearning intentions significantly improves privacy protection, reflected by the huge 508 decreased reconstruction similarity gap.

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4.5 IMPACT OF UNLEARNING SAMPLES RATE (USR)

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Figure 6 presents the evaluation of USR from 0.5% to 1% on CelebA. Additional evaluation of USR 513 from 1% to 6% on MNIST and CIFAR10 is presented in Appendix F.2. CSR and ASR are set 0.5% 514 for OUbL on CelebA. The privacy budget of VBU-LDP is set $\epsilon = 10$ here.

The first column of Figure 9 shows that more unlearning samples reduce the unlearning update sim-516 ilarity of OUbL when synthesizing the new dataset. However, OUbL still achieves stable unlearning 517 effectiveness when USR increases, which is reflected by the model accuracy and backdoor accuracy. 518 Although VBU achieves a thorough data removal effect, which is better than OUbL, we also note 519 that the noise injection (VBU-LDP) will mitigate the data removal effect, as shown in the third fig-520 ure on CelebA. Moreover, as shown in the last two figures in Figure 9, OUbL has slight privacy 521 protection and efficiency decrease when USR increases. 522

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5 SUMMARY AND FUTURE WORK

526 In this paper, we are the first to investigate privacy protection for both erased samples and unlearning 527 intentions during machine unlearning. We propose an OUbL approach to solve this problem. OUbL 528 constructs a new dataset for unlearning by incremental training, which hides the unlearning infor-529 mation in the constructed dataset to protect the erased data. Moreover, OUbL obliviously achieves 530 the unlearning effect by incremental training on the constructed data using the original learning 531 algorithm, hence not relying on customized unlearning algorithms and avoiding exposing the unlearning intentions to the servers. Our extensive experiments and comprehensive ablation studies 532 have shown that the proposed OUbL can effectively protect the erased samples and the unlearning 533 intentions while achieving a satisfactory unlearning effect. The proposed OUbL fulfills the gap be-534 tween machine unlearning and privacy leakage to the server during unlearning, providing a powerful 535 approach to implement machine unlearning with privacy protection. 536

As machine unlearning becomes increasingly important, our research serves as a stepping stone in understanding and protecting privacy during machine unlearning services. Future work should 538 continue this line of inquiry, developing more privacy-preserving unlearning methods to uphold and support the right to be forgotten in MLaaS environments.

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A RELATED WORK

758 759 A.1 MACHINE UNLEARNING

760 Machine unlearning techniques are motivated 761 by the growing privacy concerns of individ-762 uals and the corresponding privacy regula-763 tions (Cao & Yang, 2015; Bourtoule et al., 764 2021). The most legitimate approach is re-765 training from scratch (Cao & Yang, 2015; Thudi et al., 2022). However, this method is 766 often impractical due to the significant com-767 putational and storage costs involved, espe-768 cially for complex deep-learning tasks. Con-769 sequently, numerous studies have sought to 770 develop effective and efficient unlearning so-771 lutions (Yan et al., 2022; Warnecke et al., 772 2024). 773

Existing machine unlearning studies can 774 be broadly categorized into exact unlearn-775 ing (Cao & Yang, 2015; Bourtoule et al., 776 2021; Yan et al., 2022; Hu et al., 2024b) and 777 approximate unlearning (Guo et al., 2020; 778 Nguyen et al., 2020; Wang et al., 2024; War-779 necke et al., 2024) methods. A representative exact unlearning method, introduced 781 in (Bourtoule et al., 2021), extends naive re-782 training to reduce the computational cost of retraining a new model (Hu et al., 2024b; Yan 783 et al., 2022). Exact unlearning completely re-784 moves the influence of the unlearned data on 785



Figure 7: Assuming a model with parameters θ trained using learning algorithm \mathcal{A} , traditional unlearning employs an unlearning algorithm \mathcal{U} to unlearn D_u . Differently, OUbL constructs an updating dataset, comprising clean samples D_c and unlearning noise-synthesized samples D_a^p , and uploads them to the server. The server only needs to incrementally update the model with the original learning algorithm \mathcal{A} based on $D_c \cup D_a^p$, thereby guaranteeing the unlearning effect without uploading the erased data D_u and without specifical unlearning algorithms.

the model but requires significant storage space and is inefficient when removal requests are frequent. Conversely, approximate unlearning attempts to modify the model directly to approximate one retrained on the remaining dataset (Guo et al., 2020; Nguyen et al., 2020). Although more efficient than exact unlearning, approximate unlearning can lead to catastrophic unlearning (Nguyen et al., 2020; Wang et al., 2024; Nguyen et al., 2022).

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A.2 PRIVACY-PRESERVING MACHINE UNLEARNING

793 To facilitate addressing the challenging unlearning problem, all the aforementioned studies assume 794 that the ML server is aware of users' data and unlearning intentions (Bourtoule et al., 2021; Cao 795 & Yang, 2015; Guo et al., 2020; Sekhari et al., 2021). However, uploading the erased data and 796 informing the server of unlearning intentions raises potential privacy threats to users, conflicting 797 with the original intention of the "right to be forgotten" regulations (Wang et al., 2023; Liu et al., 798 2022b; Thudi et al., 2022). Although some studies highlight the privacy breaches caused by machine 799 unlearning updates (Chen et al., 2021; Gao et al., 2022; Hu et al., 2024a; Zhang et al., 2023), only 800 a few focus on privacy protection during machine unlearning, specifically avoiding the exposure of erased data and unlearning intentions to servers during unlearning. Most of these privacy-preserving 801 machine unlearning solutions are based on federated learning, termed federated unlearning (Liu 802 et al., 2022b; Wang et al., 2023; Su & Li, 2023; Gao et al., 2024). 803

Some federated unlearning methods (Wu et al., 2022; Fraboni et al., 2024; Liu et al., 2021; Lin et al., 2024) attempt to unlearn a user client's entire contribution from the trained FL model. They store all clients' uploaded parameters on the server side and estimate the unlearning user's influence based on these stored parameters (Fraboni et al., 2024; Liu et al., 2021). These approaches allow the FL server to implement unlearning without interacting with the user. However, it significantly degrades the original model's utility and is unsuitable for a user who wishes to unlearn only a small portion of their local dataset.

810 In contrast to unlearning a user's total contribution, the authors of (Liu et al., 2022b; 2021; Wang 811 et al., 2023) investigated how to unlearn user-specified samples in FL. They proposed fast retraining 812 methods based on the Hessian matrix and Bayesian inference (Box & Tiao, 2011). However, these 813 approaches require the FL server to reactivate all users for retraining, which is impractical in real-814 world scenarios. Lin et al. (Lin et al., 2024) proposed a dynamic client selection method to avoid reactivating all user clients for unlearning. However, the vulnerability of privacy leakage from gra-815 dients remains. Gradients computed solely using the erased data for unlearning pose a higher risk of 816 privacy leakage compared to standard FL training gradients, which are derived from the entire local 817 dataset (Salem et al., 2020; Melis et al., 2019). Consequently, the FL framework can only offer lim-818 ited protection for the privacy of erased data. Moreover, in existing unlearning methods (Bourtoule 819 et al., 2021; Nguyen et al., 2020; Chundawat et al., 2023; Tarun et al., 2023), users must inform 820 the server of their unlearning intentions so that the server can prepare customized operations for 821 unlearning, which inevitably threatens the privacy of users' unlearning intentions. 822

Table 1: An overview of representative non-privacy protection and FL-based privacy-preserving unlearning methods.

Machine	Service Scenarios		Unlearnin	g Data Size	Unlearning Alg	Unlearning Algorithms Necessity		ention Protection	Erased Data
Unlearning Methods	Centralized Scenarios	Distributed Scenarios	Specified any samples	User's entire samples	Require unlearning algorithm	Not require s unlearning algorithm	Need to s inform servers	Not Need to inform servers	Protecting Methods
SISA	•	0	•	0	•	0	•	0	No Protection
VBU	•	0	•	0	•	0	•	0	No Protection
BFU	0	•	•	0	•	0	•	0	By Gradients
HBFU	0	•	•	0	•	0	•	0	By Gradients
Federaser	0	•	0	•	•	0	•	0	By Gradients
OUbL (Ours)	•	0	•	0	0	٠	0	•	Constructed new datasets

•: the machine unlearning method is applicable; O: the machine unlearning method is not applicable.

SISA (Bourtoule et al., 2021); VBU (Nguyen et al., 2020); BFU (Wang et al., 2023); HBFU (Liu et al., 2022b);Federaser (Liu et al., 2021).

A.3 DIFFERENCE FROM EXISTING WORK

Our OUbL approach significantly differs from existing non-privacy protection machine unlearning 836 methods (Bourtoule et al., 2021; Nguyen et al., 2020) and FL-based privacy-preserving unlearning 837 methods (Liu et al., 2022b; 2021; Wang et al., 2023) in terms of service scenarios, unlearning data 838 size, unlearning intentions protection, and erased data protection mechanisms, as depicted in Table 1. 839 First, most existing privacy-preserving machine unlearning methods focus on federated (distributed) 840 learning scenarios, utilizing gradients instead of original erased data to protect the privacy of erased 841 samples (Liu et al., 2021; Wang et al., 2023; Liu et al., 2022b). Our method targets general central-842 ized learning scenarios, where the centralized server processes model training, and most methods 843 in these scenarios lack privacy protection (Bourtoule et al., 2021; Nguyen et al., 2020). Second, no 844 studies currently protect unlearning intentions; all require informing the ML servers to customize unlearning algorithms. This work considers unlearning intentions as private information and aims to 845 implement unlearning without needing specific unlearning algorithms, instead updating the model 846 using the original learning algorithm. 847

848 We also note that some studies have attempted to generate adversarial or backdoor samples to influ-849 ence model performance on targeted samples (Di et al., 2022; Madry et al., 2018; Zeng et al., 2023; Shafahi et al., 2019; Geiping et al., 2021). However, our approach differs in two significant ways. 850 First, in backdooring methods (Geiping et al., 2021; Zeng et al., 2023), the targeted sample is typ-851 ically a single instance, whereas unlearning scenarios usually involve multiple samples, increasing 852 the complexity of noise generation. Second, the objective of backdooring is specific and relatively 853 straightforward, i.e., altering the model's performance on a targeted sample. In contrast, the un-854 learning noise generation target, estimating the unlearning update, is considerably more challenging 855 to determine. 856

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B EFFICIENT UNLEARNING UPDATE ESTIMATION ALGORITHM

We can use $\nabla^2_{\theta}\ell((x_i, y_i); \theta_o)$ of any (x_i, y_i) as an unbiased estimator of H. In Algorithm 2, we uniformly sample t points $x_{s1}, x_{s2}, \ldots, x_{st}$ from a clean dataset D_c . Moreover, for a precise estimation, we repeat the process r times and average the results to reduce variance. For each estimation round $k \in [1, 2, \ldots, r]$, we initially define $H_{k,0}^{-1}G_u = G_u$, where $G_u = \nabla_{\theta}\ell((x_u, y_u); \theta_o)$ for clarity, as shown in line 4 in Algorithm 2. Then, we recursively compute $H_{k,1}^{-1}G_u = G_u + (I - I)$

Algorithm 2: Efficient Unlearning Update Estimation

Input: Trained model θ_o , the gradient vector of one erased sample $G_u = \nabla_{\theta} \ell((x_u, y_u); \theta_o)$, the clean samples used in model training $D_c = \{(x_i, y_i)\}_{i=1}^m$, Number of samples t, Number of iterations r Output: Estimated unlearning update $H^{-1}\nabla_{\theta}\ell((x_u, y_u); \theta_o)$ 1 procedure EUUE (θ_o, G_u, D_c, t, r): 2 for $k \leftarrow 1$ to r do 3 Sample t points $\{x_{s_1}, x_{s_2}, ..., x_{s_t}\}$ uniformly from D_c 4 Initialize $H_{k,0}^{-1}G_u = G_u$ 5 for $j \leftarrow 1$ to t do 6 Compute $\nabla_{\theta}^2 L(x_{s_j}, \theta_o) H_{k,j-1}^{-1}G_u$; 7 Update $H_{k,j}^{-1}G_u = G_u + (I - \nabla_{\theta}^2 \ell((x_{s_j}, y_{s_j}); \theta_o)) H_{k,j-1}^{-1}G_u$; 8 Store result $H_{k,t}^{-1}G_u$ 9 Average the results to get the final estimation: $H^{-1}G_u = \frac{1}{r}\sum_{k=1}^r H_{k,t}^{-1}G_u$

 $\nabla^2_{\theta} \ell((x_{sj}, y_{sj}); \theta_o)) H^{-1}_{k,j-1} G_u$, as shown in lines 5 to 7 in Algorithm 2. We store the final round $H^{-1}_{k,t} G_u$ as the unbiased estimation of $H^{-1} G_u$ in the k-th iteration. After executing r iterations, we average the results to obtain the final estimation.

C UNLEARNING NOISE DESCENT



Figure 8: Unlearning noise descent. During the training process, we only update the unlearning noise matrixes (green circles) to find sufficient noise efficiently while fixing the model parameters (black circles).

Figure 8 shows the training process to find the suitable unlearning noise. Initially, we generate unlearning noise matrixes Δ^p , shown as the green circles. During the training process, forward propagation, depicted by blue arrows, moves information from the input layer, which combines images with unlearning noise, through the network's hidden layers to the output layer. Concurrently, backpropagation, illustrated by red arrows, calculates the gradients of the loss according to Eq. (6) and adjusts the network's parameters by propagating errors backward. However, we here fix the network's parameters (black-bordered circles) and only update the unlearning noise matrixes (green circles) during the training process. After a few rounds of training, we can get sufficient unlearn-ing noise for the auxiliary data to synthesize, ensuring the unlearning effect once the ML server incrementally trains the model based on the synthesized dataset.

917 The corresponding unlearning noise descent algorithm for the unlearning noise descent is presented in Algorithm 1.

918 D PROOF OF PROPOSITION 1

In this section, we provide the proof of Proposition 1 based on Zoutendijk, the Theorem 3.2 in (Nocedal & Wright, 2006). The main proof process is presented as follows.

Proof. Consider the incremental gradient descent update as the following form

$$\theta_o^{k+1} = \theta_o^k - \alpha_k \nabla \mathcal{L}_{inc}(\theta_o^k).$$
(12)

Due to Lipschitz smoothness of the gradient of the unlearning simulation loss \mathcal{L}_{unl} , we can estimate the value at θ_o^{k+1} by the descent lemma

$$\mathcal{L}_{unl}(\theta_o^{k+1}) \le \mathcal{L}_{unl}(\theta_o^k) - \langle \alpha_k \nabla \mathcal{L}_{unl}(\theta_o^k), \nabla \mathcal{L}_{inc}(\theta_o^k) \rangle + \alpha_k^2 L \| \nabla \mathcal{L}_{inc}(\theta_o^k) \|^2,$$
(13)

where L is the Lipschitz constant. If we use the cosine similarity identity:

$$\langle \nabla \mathcal{L}_{unl}(\theta_o^k), \nabla \mathcal{L}_{inc}(\theta_o^k) \rangle = \| \nabla \mathcal{L}_{inc}(\theta_o^k) \| \cdot \| \nabla \mathcal{L}_{unl}(\theta_o^k) \| \cos(\gamma^k), \tag{14}$$

where γ^k denotes the angle between both gradients vectors, we can find that

$$\mathcal{L}_{unl}(\theta_o^{k+1}) \leq \mathcal{L}_{unl}(\theta_k^k) - \|\nabla \mathcal{L}_{inc}(\theta_o^k)\| \cdot \|\nabla \mathcal{L}_{unl}(\theta_o^k)\| \cos(\gamma^k) + \alpha_k^2 L \|\nabla \mathcal{L}_{inc}(\theta_o^k)\|^2$$

$$\|\nabla \mathcal{L}_{unl}(\theta^k)\| = 1 \quad (15)$$

$$= \mathcal{L}_{unl}(\theta_o^k) - (\alpha_k \frac{\|\nabla \mathcal{L}_{unl}(\theta_o^k)\|}{\|\nabla \mathcal{L}_{inc}(\theta_o^k)\|} \cos(\gamma^k) - \alpha_k^2 L) \|\nabla \mathcal{L}_{inc}(\theta_o^k)\|^2.$$

As such, the unlearning simulation loss decreases for nonzero step sizes if

$$\frac{\|\nabla \mathcal{L}_{unl}(\theta_o^k)\|}{\|\nabla \mathcal{L}_{inc}(\theta_o^k)\|} \cos(\gamma^k) > \alpha_k L, \tag{16}$$

i.e.,

$$\alpha_k L \le \frac{\|\nabla \mathcal{L}_{unl}(\theta_o^k)\|}{\|\nabla \mathcal{L}_{inc}(\theta_o^k)\|} \frac{\cos(\gamma^k)}{c},\tag{17}$$

for some $1 < c < \infty$. This follows from the assumption on the parameter β in the statement of the Proposition 1. Reinserting this estimate into the descent inequality reveals that

$$\mathcal{L}_{unl}(\theta_o^{k+1}) < \mathcal{L}_{unl}(\theta_o^k) - \|\nabla \mathcal{L}_{unl}\|^2 \frac{\cos(\gamma^k)}{c'L},\tag{18}$$

for $\frac{1}{c'} = \frac{1}{c} - \frac{1}{c^2}$. Due to monotonicity, we may sum over all descent inequalities, yielding

$$\mathcal{L}_{unl}(\theta_o^0) - \mathcal{L}_{unl}(\theta_o^{k+1}) \ge \frac{1}{c'L} \sum_{j=0}^k \|\nabla \mathcal{L}_{unl}(\theta_o^j)\|^2 \cos(\gamma^j).$$
(19)

961 As \mathcal{L}_{unl} is bounded below, we may consider the limit of $k \to \infty$ to find

$$\sum_{j=0}^{\infty} \|\nabla \mathcal{L}_{unl}(\theta_o^j)\|^2 \cos(\gamma^j) < \infty.$$
⁽²⁰⁾

If for all, except finitely many iterates the angle between adversarial and training gradient is less than 90°, i.e., $\cos(\gamma^k)$ is bounded below by some fixed $\epsilon > 0$, as assumed, then the convergence to a stationary point follows:

$$\lim_{k \to \infty} \|\nabla \mathcal{L}_{unl}(\theta_o^k)\| \to 0.$$
⁽²¹⁾

	Table	e 2: Dataset statistics.		
	Dataset	Feature Dimension	#. Classes	#. Samples
	MNIST (Deng, 2012)	28×28×1	10	70,000
(CIFAR10 (Krizhevsky et al., 2009)	32×32×3	10	60,000
	CelebA (Liu et al., 2018)	178×218×3	2 (Gender)	202,599
E E.1	DETAILED EXPERIMENTAL S	ETTINGS		
Data CIFA he g he o	sets. The statistics of all datasets used AR10 are used to train 10-class classi ender attributes of the face images. ' nes on MNIST and CIFAR10. We al	d in our experiments are l fication models. The exp The task is a binary class so introduce them as belo	isted in Table 2. periment on Cele sification proble ow.	Both MNIST and ebA is to identify m, different fron
	• MNIST. MNIST contains 60,00 handwritten digit images for the ized, and centered in a fixed-size	00 handwritten digit imatesting. All these black image with 28×28 pixe	ages for the trai and white digits els.	ining and 10,000 are size normal
	• CIFAR10. CIFAR10 dataset co 6,000 images per class. There are	nsists of 60,000 32x32 o e 50,000 training images	colour images in and 10,000 test	10 classes, with images.
	• CelebA. CelebA is a large-scale images, each with 40 attribute ar	e face attributes dataset v notations.	with more than 2	200,000 celebrity
Celel set th CIFA 3.8 a	bA. On the MNIST dataset, we set the learning rate $\eta = 0.0001$. During AR10, and the minibatch size to 160 c nd are conducted on NVIDIA Quadr	the learning rate $\eta = 0.00$ training, we set the mir on CelebA. All algorithm o RTX 6000 GPUs.	1. On CIFAR10 nibatch size to 1 ns are implement	and CelebA, we on MNIST and ted using Pytorcl
E.2	Metric			
	• Accuracy. Model accuracy is unlearning methods influence the	calculated based on the e original ML service mo	test dataset, wh odel utility.	nich shows if the
	• Backdoor Accuary. It calculate data removal effect.	ed based on the backdoo	ored dataset D_u	$_{,b}$ to evaluate the
	• Unlearning Update Similarity. unlearning update by EUUE and	It calculates the cosine the final OUbL unlearned	similarity betwo ed update as	een the estimated
	$\sin(\Delta heta_{ m EUUE})$	$,\Delta\theta_{\mathbf{OUbL}}) = \frac{\Delta\theta_{\mathbf{EUUE}}}{\ \Delta\theta_{\mathbf{EUUE}}\ }$	$\frac{\cdot \Delta \theta_{\text{OUbL}}}{\cdot \ \Delta \theta_{\text{OUbL}}\ },$	
	where $\Delta \theta_{\text{EUUE}}$ denotes the unl $\Delta \theta_{\text{OUbL}}$ is the unlearning updat the Euclidean norms of the two u	earning update estimate e after conducting OUb updates vectors.	ed by EUUE (ALL) $\ \Delta \theta_{\text{EUUE}}\ $ and $\ \Delta \theta_{\text{EUUE}}\ $	Algorithm 2) and $\ \Delta \theta_{\text{OUbL}}\ $ are
	• Reconstruction Similarity. It can ples D_u and the attacks' reconstruction	alculates the cosine simil ructed samples \hat{D}_u ,	arity between th	e unlearned sam
	sim	$\mathbf{h}(D_u, \hat{D_u}) = \frac{D_u \cdot \hat{D_u}}{\ D_u\ \cdot \ \hat{D_u}\ }$	$\frac{u}{\partial u}$.	
	• Running Time. It is used to asso each training batch and multiply	ess the efficiency, calculating it with the training ep	nted by recording pochs.	g the time used in

Table 3: Overall	Evaluation	Results on	MNIST,	CIFAR10 a	nd CelebA.
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Single-Sample	MNIST			CIFAR10			CelebA					
Unlearning	OUbL	BFU	SISA	VBU	OUbL	BFU	SISA	VBU	OUbL	BFU	SISA	VBU
Model Accuracy	98.71%	98.88%	98.75%	97.91%	76.75%	77.61%	79.37%	75.86%	95.66%	95.72%	95.78%	95.80%
Backdoor Accuracy	0.00%	100%	0.00%	0.00%	0.00%	100%	0.00%	0.00%	0.00%	100%	0.00%	0.00%
Unl. Update Similarity	0.976	-	-	-	0.989	-	-	-	0.998	-	-	-
Reconstruction Similarity	0.669	0.947	1	1	0.852	0.888	1	1	0.932	0.933	1	1
Running time (s)	4.178	15.95	11.87	0.024	8.231	122.26	113.00	0.088	0.432	168.61	135.42	0.033
Multi-Sample	1	MNIST, U	VSR = 1%	76	С	IFAR10,	USR = 1	%	CelebA, $USR = 0.5\%$			
Unlearning	OUbL	BFU	SISA	VBU	OUbL	BFU	SISA	VBU	OUbL	BFU	SISA	VBU
Model Accuracy	98.52%	98.70%	98.53%	78.69%	73.89%	78.20%	78.49%	43.23%	95.74%	96.01%	95.92%	93.53%
Backdoor Accuracy	9.67%	9.16%	9.67%	0.00%	9.40%	9.70%	7.60%	0.00%	4.55%	41.92%	4.41%	4.92%
Unl. Update Similarity	0.942	-	-	-	0.959	-	-	-	0.992	-	-	-
Reconstruction Similarity	0.818	0.874	1	1	0.846	0.874	1	1	0.826	0.831	1	1

BFU (Wang et al., 2023); SISA (Bourtoule et al., 2021); VBU (Nguyen et al., 2020)

1041 E.3 BENCHMARKS

- SISA (Bourtoule et al., 2021). The main process of SISA divides the full data D into several shards $D^1, D^2, ..., D^k$ and trains sub-models with parameters $\theta^1, \theta^2, ..., \theta^k$ for each shard. When the server receives a request for unlearning sample x_u , it just needs to retrain the sub-model θ^i of shard D^i that contains x_u . We set k = 5 disjoint shards and corresponding sub-models. We put the unlearned samples only on one shard, which is the ideal scenario of SISA.
- VBU (Nguyen et al., 2020). VBU is an approximate unlearning method based on variational Bayesian inference. For the convenience of experiments, we set a middle layer of original neural networks as the Bayesian layer and calculate the unlearning loss according to (Nguyen et al., 2020) based on the Bayesian layer and erased samples for unlearning.
- BFU (Wang et al., 2023). The BFU extended the variational Bayesian unlearning method to FL scenarios and proposed parameters self-sharing to mitigate the unlearning catastrophe. We implement BFU following the process as introduced in (Wang et al., 2023) and set the user number k = 5, and only one user needs unlearning, which is also an ideal scenario in FL.
- HBFU (Liu et al., 2022b). The HBFU extended the Hessian matrix-based unlearning methods (Sekhari et al., 2021; Guo et al., 2020) to FL scenarios. We implement HBFU following (Liu et al., 2022b) and also set the FL user number k = 5, and only one user needs unlearning.
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F ADDITIONAL EXPERIMENTS 1064

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F.1 OVERALL EVALUATION OF OUBL

1067 We first demonstrate the overall evaluation results of different machine unlearning methods on 1068 MNIST, CIFAR10 and CelebA, presented in Table 3. The bolded values indicate the best per-1069 formance among the compared methods, while red-colored values signify results that are opposite 1070 from expectations. We fill a dash when the method does not contain the evaluation metrics. 1071

Setup. We measure unlearning methods based on the five above-introduced evaluation metrics in 1072 single-sample and multi-sample unlearning scenarios. In the single samples unlearning scenario, only one unlearning sample needs to be unlearned. In the multi-sample unlearning scenario, we set 1074 the unlearning samples rate USR = 1%, where $USR = \frac{m}{n}$, m is the unlearned samples size and n is 1075 the training data size. We illustrate the comparison of OUbL with one privacy-preserving federated unlearning method, BFU (Wang et al., 2023), one representative exact unlearning method, SISA 1077 (Bourtoule et al., 2021), and one approximate unlearning method, VBU (Nguyen et al., 2020). 1078

Evaluation of Unlearning Effectiveness. The effect of machine unlearning is measured by model 1079 accuracy and backdoor accuracy, where the model accuracy represents the model utility after unlearning, and the backdoor accuracy means if the backdoor-marked samples are unlearned from the model.

From the model utility perspective, in most cases, BFU or SISA achieves the best model accuracy. This is because SISA is a retraining-based method, and BFU needs all other normal federated users to assist in unlearning retraining to ensure the model's utility. Compared with the methods utilizing the remaining dataset, OUbL achieves a similar model accuracy as BFU and SISA, usually only slightly lower (not exceeding 2%) than them, much better than VBU, an approximate unlearning method without the assistance of the remaining dataset.

From the data removal perspective, OUbL and other centralized unlearning methods (SISA and VBU) can effectively unlearn the marked samples, reducing the backdoor accuracy to a very low level. For BFU, although the retraining assistance of other normal federated users helps to preserve model utility, it to some extent mitigates the unlearning update, failing to unlearn specified samples in the single-sample scenario on all datasets and in the multi-sample scenario on CelebA.

Evaluation of Privacy Protection. We evaluate privacy preservation through reconstruction similarity metrics. For OUbL and BFU, since the server cannot access the erased data, we conduct the reconstruction attacks (Hu et al., 2024a; Salem et al., 2020; Zhang et al., 2023) based on the unlearned update. Since the server of OUbL has no information about unlearning intentions, it treats the model updates as normal learning updates for attack (Salem et al., 2020).

The results of the three datasets show significant improvement in privacy protection by hiding un-1099 learning intentions. For example, on MNIST, for SISA and VBU, since the server knows the un-1100 learning requested samples, the reconstruction similarity is directly 1, the same as having no privacy 1101 preservation of these data. When gradient-based protection (BFU) is applied, the privacy protection 1102 of erased data achieves 0.947 reconstruction similarity when unlearning one sample. If we inform 1103 the server with unlearning intentions in OUbL, it achieves a reconstruction similarity to BFU. We 1104 present detailed comparisons for OUbL with informed unlearning intentions in Section 4.4. How-1105 ever, the server will be oblivious to unlearning when conducting OUbL, and the privacy protection 1106 of OUbL achieves 0.669 reconstruction similarity on single-sample unlearning on MNIST. OUbL 1107 achieves significant privacy protection on the three datasets compared with the FL-based and no-1108 privacy protection unlearning methods. Although the FL-based method can also protect the privacy 1109 of erased data, it sometimes fails to unlearn samples and is inefficient as it needs the retraining assistance of other normal users. 1110

1111 **Evaluation of Efficiency.** Normally, OUbL achieves a slight efficiency improvement than BFU and 1112 SISA on MNIST and a significant improvement (more than $10 \times$ speedup) on CIFAR10 and CelebA. 1113 Although BFU and SISA are much more efficient than naive retraining, they are still training time 1114 expensive compared with OUbL and VBU because BFU needs the retraining assistance of other users, and SISA needs to retrain 1/5 shard of the original training dataset. VBU is the most efficient 1115 method, with less than 0.1 seconds for single sample unlearning, as it implements unlearning only 1116 based on the erased samples; however, the cost is the model utility degradation and lack of privacy 1117 protection. 1118

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F.2 ADDITIONAL EVALUATION OF IMPACT OF UNLEARNING SAMPLES RATE (USR)

Setup. Since the above unlearning methods have lots of similar metric values, for clear illustration and demonstration, we here only display the VBU and VBU-LDP methods as they implement machine unlearning based on solely erased samples, which requires the least data access. In this experiment, we range *USR* from 1% to 6% on MNIST and CIFAR10. *CSR* and *ASR* are set 1% for OUbL on MNIST and CIFAR10. The privacy budget of VBU-LDP is set $\epsilon = 10$ here. All the experimental results are presented in Figure 9.

Relationship between Unlearning Update Similarity and *USR*. The first column of Figure 9 shows the relationship between unlearning update similarity and *USR*. It is obvious that more unlearning samples in the unlearning request will increase the difficulty of constructing the dataset to achieve the unlearning effect, which is confirmed on the three datasets, higher *USR* decreasing the unlearning update similarity of OUbL a lot.

Impact on Unlearning Effectiveness. Unlearning effectiveness includes model utility preservation (the second column) and the data removal effect (the third column) in Figure 9.



Figure 9: Evaluations of impact about different USR.

1149 From the model utility preservation perspective, a good unlearning method should not be heavily 1150 influenced by the increasing USR. On all datasets, OUbL always achieves a similar model accuracy 1151 as the original trained model on all datasets even when USR increases from 1% to 6%. VBU only 1152 achieves an acceptable model accuracy on CelebA. Moreover, adding the LDP noise will definitely 1153 decrease the model utility, reflected by the huge gap between VBU and VBU-LDP.

1154 From the data removal perspective, all the unlearning methods can effectively remove the influence 1155 of the marked backdooring samples from the model, reducing the backdoor accuracy of the original 1156 model. 1157

Impact on Erased Data Protection. The fourth column in Figure 9 shows the privacy protection of 1158 the erased samples against the reconstruction attacks (Hu et al., 2024a; Zhang et al., 2023). For these 1159 methods with no privacy protection, the server directly has the erased sample, and the reconstruction 1160 similarity is 1. When USR increases, the reconstruction similarity of OUbL increases, too, meaning 1161 more privacy is leaked. Since we set $\epsilon = 10$ for VBU-LDP, OUbL always achieves better privacy 1162 protection than VBU-LDP. 1163

Impact on Unlearning Efficiency. The fifth column in Figure 9 illustrates the running time of 1164 OUbL and VBU. The running time slightly increases as USR increases. Both OUbL and VBU 1165 achieve more than $20 \times$ speedup than original training, which is much more efficient than most fed-1166 erated unlearning and retraining-based methods. Although OUbL consumes slightly more time than 1167 VBU, it is important to note that OUbL does not require uploading the erased data and informing the 1168 server for unlearning, which avoids privacy leakage of both erased data and unlearning intentions.

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1170 F.3 IMPACT OF UNLEARNING SAMPLES SIMILARITY 1171

1172 We know that the similarity between the erased samples and the remaining samples plays an impor-1173 tant role in machine unlearning. In this section, we also conduct experiments to evaluate how the 1174 similarity influences the performance of OUbL.

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1176 **Setup.** To quantify the similarity between the erased samples and the remaining samples, we introduce a backdoor ratio β to control the injected patch to the erased samples, formulated as 1177 $D_{u,\beta} \leftarrow (X_u + \beta \times patch, Y_u)$. We mixed both $D_{u,\beta}$ and original unlearned data D_u into the train-1178 ing dataset for ML service model training. During the unlearning process, we only need to remove 1179 the contribution of the marked samples $D_{u,\beta}$. By adjusting β , we can simulate the different levels 1180 of similarity between the erased samples and the samples in the remaining dataset. This approach 1181 allows us to intuitively quantify the similarity between the unlearned samples and the remaining 1182 samples. The experimental results on MNIST, CIFAR10 and CelebA are presented in Figure 10. 1183

Relationship between Unlearned Data Similarity and Patch Injection Ratio. The first column 1184 1185 in Figure 10 illustrates the relationship between the patch injection ratio β and similarity, where similarity is measured between the original samples D_u and the patch-injected data $D_{u,\beta}$. In this 1186 experiment, we only need to unlearn $D_{u\beta}$. Across all datasets, including MNIST, CIFAR10, and 1187 CelebA, increasing the amount of noise (as indicated by a higher β) results in a decrease in simi-



Figure 10: Evaluations for the impact of unlearning samples' similarity

larity. This trend is consistently observed, demonstrating that higher patch injection ratios make theunlearned samples more distinct from the original samples in the remaining dataset.

Impact on Unlearning Update Similarity. The second column in Figure 10 demonstrates the unlearning update similarity influenced by the patch ratio β . With more patches injected into the data, the marked samples will be more dissimilar to the original samples and the remaining samples. It increases the difficulty of OUbL in approaching the unlearning update via incremental learning, as the normal clean and the auxiliary data that we can use are not similar to the unlearned samples with a high patch injecting ratio. The unlearning update similarity obviously decreases as the patch ratio increases on all three datasets.

Impact on Unlearning Effectiveness. The third and fourth columns demonstrate the model utility and data removal of unlearning effectiveness. The data removal effect increases as the patch ratio increases, showing as the decreased backdoor accuracy. It means the more unique samples, larger β and lower similarity, are easier to be unlearned. However, better data removal effect slightly decreases model utility, as showing from the model accuracy of all methods in the third column in Figure 10.

Impact on Erased Data Protection. Our OUbL achieves the best privacy protection for the erased samples, and the attacking difficulty for OUbL increases as the patch ratio increases. It is easy to understand because OUbL is more difficult to forge the unlearning update when patch ratio increases, which means the constructed data contains less unque information about the erased samples when β is large. It makes the unlearning update less similar to the expected ones, and hence increase the reconstruction difficulty.

We omit the illustration of the unlearning efficiency results as the similarity not heavily influence the training time.

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F.4 IMPACT OF CONSTRUCTED SAMPLES RATE AND AUXILIARY SAMPLES RATE ON
 UNLEARNING EFFICIENCY

1239Impact on Unlearning Efficiency.As the synthesized dataset is constructed with the parameters1240CSR and ASR, the incremental training time based on the constructed dataset will definitely increase1241linearly as CSR and ASR increases, as shown in Figure 11.



Figure 11: The impact of CSR and ASR about the running time. The CSR and ASR for CelebA is from 0.5% to 1%.



Figure R1: Example of the original auxiliary dataset (the first row), their noisy counterparts (the middle row), and directly construct data without an auxiliary dataset [R11] (the last row). @Reviewer iCGz

Table R1: Evaluating mixing unlearned data in the clean dataset on CIFAR10. The results demonstrate that mixing the unlearned samples into the constructed uploaded data for incremental learning negatively impacts the unlearning effect, as reflected by the increasing backdoor accuracy, but the model utility keeps. @Reviewer BZGC

On CIFAR10	Mixed 0% of Unlearned Data	2%	4%	6%	8%
Model Acc.	73.89%	73.85%	73.78%	73.25%	73.03%
Backdoor Acc.	9.40%	13.60%	33.40%	35.40%	43.26%
Running Time	6.63	6.72	6.83	7.01	7.16

Table R2: Evaluating learning rate on MNIST and CIFAR10. The results demonstrate that a larger
 learning rate can speed the convergence to achieve unlearning, costing less computation and achiev ing a better unlearning effect (low backdoor accuracy by removing). The tradeoff is that it slightly
 decreases the model utility at the same time, which is not too much on MNIST but a little worse on
 CIFAR10. @Reviewer iCGz, @Reviewer Gp18

	Metrics	Learning Rate: 0.0001	0.0002	0.0004	0.0006	0.0008
On MNIST	Model Acc. Backdoor Acc.	98.52% 9.67%	97.84%	96.72% 9.17%	95.88% 8.20%	95.37% 8.67%
	Running Time	3.92	2.72	1.83	1.61	1.56
	Model Acc.	73.89%	72.98%	68.69%	65.23%	62.23%
On Cifar10	Backdoor Acc.	9.40%	6.20%	5.80%	4.00%	2.48%
	Running Time	6.63	3.72	2.83	2.51	2.23

Table R3: Membership inference attack accuracy after unlearning by OUbL. The results demonstrate that OUbL can effectively reduce the MI accuracy, achieving a significant unlearning performance. @Reviewer 5Whi

Dataset	Original Model	ASR and CSR, 1%	2%	3%	4%
On MNIST	63.86%	53.87%	53.61%	53.02%	52.86%
On CIFAR10	77.43%	61.47%	61.30%	61.10%	60.92%
On CelebA	58.37%	51.94%	51.32%	51.04%	50.69%

Table R4: The detailed running time. The results demonstrate that although we put more computational cost on the user side, it is affordable for users compared to the FL users in BFU. @Reviewer
 Ha5f

54 55	Dataset	Total running time of OUbL (second)	Unlearning update estimation (User side)	Unlearning noise generation (User side)	Unlearning by incremental learning (Server side)	Total running time of BFU
	On MNIST	3.92	1.06	1.45	1.41	16.03
	On CIFAR10	6.64	1.02	2.10	3.52	141.26
	On CelebA	2.26	0.72	0.83	0.71	176.86

Table R5: Experimental results on Adult. The task of the Adult dataset is to predict whether an individual's income exceeds \$50,000 per year, which is a binary classification. We first backdoor some samples in Adult by setting the "education-num" feature to 2 and changing the corresponding label. The aim of unlearning is to remove the influence of these backdoored samples, and the results are presented in the following table. Since the task on the Adult dataset is a binary task, dropping the backdoor accuracy of around 50% is similar to the random selection. Our method can effectively degrade the backdoor accuracy to around 50%, guaranteeing the effectiveness of unlearning. @Reviewer Gp18

On Adult	Original	ASR and CSR, 1%	2%	3%	4%
Model Acc.	85.32%	81.66%	81.69%	79.93%	80.79%
Backdoor Acc.	100.00%	54.81%	52.81%	50.02%	49.52%
Running Time	15.31	0.54	1.03	1.51	1.93

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G SCENARIOS AND THREAT MODEL

1378 @Reviewer BZGC, @Reviewer iCGz, @Reviewer 5Whi, @Reviewer EoYb, @Reviewer 1379 Ha5f,@Reviewer Gp18

Machine Unlearning Service Scenarios. To facilitate understanding, we introduce the problem in a Machine Learning as a Service (MLaaS) scenario. In the MLaaS setting, there are two key entities:
a ML server that trains models as ML services, and users (data owners) who contribute their data for ML model training. In such scenarios, machine unlearning occurs when users realize that some of their previously contributed samples are private and wish to revoke these data contributions from the trained models.

1386 The ML Server's Ability. We assume the ML server is honest but curious [R1]: while it honestly 1387 hosts and provides ML services, including model training and updating, it may still be curious 1388 about private information, such as unlearned data and unlearning intentions, if there are other operations. Informing the server of unlearning intentions to customize unlearning operations is 1389 considered a privacy threat because it reveals users' unlearning purposes, potentially enabling the 1390 server to prepare targeted unlearning attacks [R1,R2]. Therefore, in our setting, we assume the ML 1391 server has only the learning algorithm \mathcal{A} and the model with parameters θ to meet strict privacy 1392 requirements. The ML server will not conduct unlearning operations other than training the model 1393 using the learning algorithm \mathcal{A} for model updating. 1394

Moreover, we assume the ML server does not store the original training data and cannot access the erased data, which should not be exposed to the server again due to privacy concerns. This assumption is reasonable in both real-world and privacy-preserving MLaaS scenarios. In real-world applications, vast amounts of data are generated daily, leading to the need of prompt model updates. Consequently, many models are trained using incremental or continual learning techniques [R3,R4]. Therefore, the server does not retain the entire raw data due to its large size [R5,R6]. In privacypreserving scenarios, the ML server is restricted from directly accessing private training data from users due to privacy concerns [R7,R8].

1403 The Users' Ability. The training data D was collected from all users and was used to train the model θ_o . The unlearning user has the erased data $D_u \subset D$. To estimate the unlearning update as

1404 the target for unlearning noise generation in our method, we assume the unlearning user can access 1405 the trained model θ_o , which is a common setting even in many privacy-preserving scenarios such 1406 as FL. We assume the unlearning user has auxiliary clean examples D_a so that they can synthesize 1407 a new dataset based on it with the unlearning noise, replacing the erased data D_{μ} for achieving the 1408 unlearning effect with only incremental learning using the synthesized dataset.

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DISCUSSION ABOUT DISTINGUISHING BENIGN UNLEARNING USERS AND Η MALICIOUS USERS @REVIEWER ICGZ

To distinguish a benign user who wants to delete their data from a malicious user and who wants to 1414 upload noisy gradients to sabotage the model performance, we can only propose some possible ways 1415 for the server to distinguish these two kinds of users. The most significant difference is the purposes 1416 of the unlearning user and the malicious user. Unlearning users want to remove some knowledge of 1417 their data from the model, and they also want to preserve the model's utility. Therefore, most clean 1418 samples and the auxiliary data they choose are in the same distribution as the genuine samples, 1419 and the synthesized noise should not influence the utility of the remaining dataset, as shown in the 1420 second objective of Eq.(4). However, the purpose of the malicious user is to sabotage the model 1421 performance. Their uploaded data will not be consistent with the genuine samples, so they can degrade model utility. We believe checking the similarity between the uploaded samples and genuine 1422 samples would be a possible solution. However, detailed poisoning attacking methods may need 1423 different solutions, and the problem is valuable to investigate in future work. 1424

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Ι DISCUSSION ABOUT DIFFERENCE BETWEEN EXISTING UNLEARNING METHODS @REVIEWER GP18

1429 Compared with existing representative approximate unlearning methods [R19, R20, R21], our 1430 method also has the following differences. Specifically, the key techniques used in [R20] are the 1431 Hessian approximation and Fisher information, which is similar to our unlearning update estimation 1432 method that is also based on the Hessian matrix. The difference is that we use Hessian-vector prod-1433 ucts (HVPs) while [R20] uses the Fisher information to improve the efficiency. The HVPs solution 1434 is more efficient and more suitable to our scenarios in which the unlearning user cannot access the 1435 remaining dataset. [R19] and [R21] are approximate unlearning methods based on techniques called error maximizing. They generate error-maximizing noise for the unlearned samples to remove the 1436 influence from the model. One significant advantage of [R19] and [R21] is that they do not require 1437 access to the remaining training dataset. Compared with them, we put more effort into designing the 1438 method to further hide the unlearning data and the unlearning intentions from the server. 1439

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1441 J ADDITIONAL EXPERIMENTS ON THE MORE PRACTICAL BLACK-BOX 1442 **SCENARIOS @REVIEWER HA5F** 1443

1444 To prove the feasibility of our method in the more practical black-box scenarios, we conducted addi-1445 tional experiments on the black-box setting on MNIST and CIFAR10. In this setting, the unlearning 1446 user cannot access the server's current model. The unlearning user only knows the type of the model 1447 (MLP on MNIST and CNN on CIFAR10 in our experiment), and the user only has the erasing data 1448 and the auxiliary data. We set the size of auxiliary data to 1% of the server-side training data. Other 1449 unlearning settings are the same as the main setting in the paper, where we first backdoor the erasing data for model training and aim to unlearn these backdoored erasing data. 1450

1451 With these settings, the unlearning user trains a shadow model (θ_s) with 94.55% accuracy on MNIST 1452 and 42.57% accuracy on CIFAR10. By contrast, the accuracy of the server's model (θ_0) trained with 1453 the entire dataset is 98.74% on MNIST and 78.80% on CIFAR10. Since both models are optimized 1454 on the erasing dataset, the proposed efficient unlearning update estimation (EUUE) method is effec-1455 tive for simulating the update of the unlearning data based on the shadow model. Hence, we can generate effective noise for the incremental learning data to approach the influence of unlearning. 1456 Then, we upload the constructed data to the server side for incremental learning, aiming to achieve 1457 the unlearning effect at the same time. We present the results as follows in Table R6.

1458Table R6: Additional experiments on the black-box setting. On both datasets, OUbL achieves effec-1459tive unlearning performance, effectively removing the backdoor influence. The backdoor removal1460effectiveness in the black-box setting is slightly lower than in the white-box setting. However, the1461negative impact on the model utility is also mitigated. These experimental results demonstrate the1462feasibility of OUbL in a more practical scenario, which lets the unlearning user not rely on the as-1463sumption of white-box access to the trained model in the federated learning scenarios. @Reviewer1464Ha5f

	Metrics	USR = 1%	2%	3%	4%
	Model Acc.(white-box)	98.52%	98.55%	98.15%	98.19%
On MNIST	Model Acc. (black-box)	98.26%	98.20%	98.31%	98.27%
	Backdoor Acc. (white-box)	9.67%	10.08%	9.83%	10.42%
	Backdoor Acc. (black-box)	12.33%	9.58%	11.67%	10.64%
	Model Acc.(white-box)	73.89%	74.57%	74.50%	75.15%
On Cifar10	Model Acc. (black-box)	76.06%	75.98%	74.93%	75.06%
	Backdoor Acc. (white-box)	9.40%	7.30%	7.87%	8.70%
	Backdoor Acc. (black-box)	13.20%	10.20%	8.40%	10.25%

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