# **EIT: Enhanced Interactive Transformer**

Anonymous ACL submission

## Abstract

Two principles: the complementary principle and the consensus principle are widely acknowledged in the literature of multi-view 004 learning. However, the current design of Multihead self-attention, an instance of multi-view learning, prioritizes the complementarity while ignoring the consensus. To address this problem, we propose an enhanced multi-head selfattention (EMHA). First, to satisfy the complementary principle, EMHA removes the oneto-one mapping constraint among queries and keys in multiple subspaces and allows each 013 query to attend to multiple keys. On top of that, we develop a method to fully encourage consensus among heads by introducing two interaction models, namely Inner-Subspace Interaction and 017 Cross-Subspace Interaction. Extensive experiments on a wide range of language tasks (e.g., 019 machine translation, abstractive summarization and grammar correction, language modeling), show its superiority, with a very modest increase in model size.

# 1 Introduction

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Transformer architectures (Vaswani et al., 2017) have yielded promising results on a wide range of natural language processing tasks (Devlin et al., 2019; Brown et al., 2020). A key factor contributing to their success is the multi-head self-attention network (MHSA), which enables efficient modeling of global dependencies among tokens in parallel. Notably, instead of utilizing a single attention mechanism, MHSA uses an ensemble of attention models, each models a small subspace, and finally aggregates these results to the final one. The core idea is similar to subspace learning (Blum and Mitchell, 1998) or multi-view learning (Chaudhuri et al., 2009).

In the realm of multi-view learning, two fundamental principles guide the research: the *complementary principle* and the *consensus principle* (Xu et al., 2013). The complementary principle emphasizes that each data view may possess unique knowledge not present in other views, prompting the use of multiple views for a comprehensive and accurate data description. On the contrary, the consensus principle aims to maximize the agreement on multiple distinct views. However, in the context of MHSA design, most studies predominantly focus on the complementary principle. This oversight is evident in their encouragement of diverse information capture by different heads (Li et al., 2018; Cui et al., 2019) and the adoption of complex aggregation operations (Li et al., 2019; Wang and Tu, 2020). Some studies (Michel et al., 2019; Clark et al., 2019; Voita et al., 2019; Behnke and Heafield, 2020) even consider the high similarity among attention heads as a significant problem referred to as attention redundancy.

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Although diversity is crucial in multi-view learning, Dasgupta et al. (2001) has shown that simply fusing diverse outputs does not guarantee improved results: the probability of a disagreement of two independent hypotheses upper bounds the error rate of either hypothesis. The consensus principle highlights the need to minimize disagreement among views to achieve better outcomes. In response to the consensus principle, several studies (Kumar and III, 2011; Kumar et al., 2011) have focused on minimizing disagreement among views to achieve better outcomes. However, in the context of MHSA research, there is a tendency to prioritize complementarity over consensus among different attention heads. Here we ask a question: Can striking a balance between these two principles be beneficial for designing MHSA mechanisms?

However, encouraging such a consensus in multihead self-attention is challenging. In our preliminary experiments, we find that directly utilizing regularization terms can achieve this goal but cannot improve performance. Drawing inspirations from human behavior where group discussions and interactions foster consensus, we propose introducing interactions among different subspaces in MHSA to achieve consensus.

To this end, we propose a new multi-head self-attention variant: Enhanced Multi-Head Self-Attention, which encourages the consensus among attention heads while guaranteeing to contain sufficient information. To ensure information sufficiency, we propose a novel many-to-many mapping scheme to generate numerous high-quality initial attention maps. This can generate more attention maps without suffering low-bottleneck problems (Bhojanapalli et al., 2020). On top of these sufficient attention maps, we propose two interaction components: *inner-subspace interaction* (ISI) and *cross-subspace interaction* (CSI). These hierarchical interaction modules fully encourage consensus among attention maps of different heads.

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The outcome of this work is an Enhanced Interactive Transformer (EIT) architecture in that MHSA is replaced with Enhanced Multi-Head Attention (EMHA). Our proposed EIT has been demonstrated to be simple to implement and highly parameter efficient, yet it consistently produces impressive results across a diverse set of tasks, including machine translation, grammar error correction, abstractive summarization, and language modeling. In addition, we have developed a computationally efficient variant of EIT, which, while still maintaining strong performance on several tasks, is better suited for low-latency industrial applications.

# 2 Preliminary: Multi-Head Self-Attention

Multi-head self-attention (MHSA) is an efficient operation that can capture the interactions among tokens. Given an embedded input sequence  $\mathbf{X} \in \mathbb{R}^{T \times d}$ , MHSA is defined as follows:

$$\mathbf{A}^{i} = \operatorname{Softmax}\left(\frac{(\mathbf{X}\mathbf{W}_{Q}^{i})(\mathbf{X}\mathbf{W}_{K}^{i})^{\mathsf{T}}}{d^{k}}\right) \quad (1)$$

$$\mathbf{O} = \sum_{i=1}^{M} \mathbf{A}^{i} \mathbf{X} \mathbf{W}_{V}^{i} \mathbf{W}_{O}^{i}$$
(2)

where T denotes the sequence length, d is the in-120 put embedding dimension,  $d_k$  is the head dimen-121 sion, M is the number of head partition on rep-122 resentations,  $\mathbf{W}_Q^i, \mathbf{W}_K^i, \mathbf{W}_Q^i \in \mathbb{R}^{d \times d_k}, \mathbf{W}_Q^i \in$ 123  $\mathbb{R}^{d_k \times d}$ .  $\mathbf{A}^i$  represents the attention distribution 124 of *i*-th head. Without special declaration, we use 125  $\mathbf{Q}^{i}, \mathbf{K}^{i}, \mathbf{V}^{i}$  to refer to  $\mathbf{X}\mathbf{W}_{Q}^{i}, \mathbf{X}\mathbf{W}_{K}^{i}, \mathbf{X}\mathbf{W}_{V}^{i}$ , re-126 spectively, which denotes the query, key and value 127 in *i*-th head. 128

# **3** Enhanced Interactive Transformer

We design a novel Enhanced Interactive Transformer (EIT) in which we replace the multi-head self-attention with Enhanced Multi-Head Attention mechanism (EMHA) that encourages consensus among different attention heads. Our method mainly modified Eq. (1) but otherwise follows the standard Transformer. 129

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# 3.1 Many-to-Many Mapping Scheme

Intuitively, to achieve better consensus, multi-head self-attention should first contain as much information as possible. To achieve this goal, a natural idea is to employ more attention heads in multi-head self-attention. However, multi-head self-attention with too many heads suffers from low bottleneck problem (Bhojanapalli et al., 2020), resulting in performance deterioration in practical applications.

Although various strategies like *attention expansion* (Shazeer et al., 2020; Zhou et al., 2021b) have been proposed, the information captured in their attention maps remains limited due to an additional linear transformation step, which can introduce redundancy among the maps.



Figure 1: The illustration of many-to-many mapping scheme (M = 4).

To alleviate this problem, we propose a novel many-to-many (M2M) mapping scheme that enables each query to attend to M keys instead of a single key. As illustrated in Figure 1, four queries and four keys can be served as two components in a bipartite graph and each element in a component, e.g.,  $\mathbf{Q}^1$ , can interact with any elements in another component, e.g.,  $\mathbf{K}^1, \ldots, \mathbf{K}^4$ . Formally, supposing one with M heads, the *i*-th attention map can be formally calculated as:

$$\mathbf{S}^{i} = \frac{\mathbf{Q}^{\lfloor (i-1)/M+1 \rfloor} (\mathbf{K}^{(i-1)\%M+1})^{\mathsf{T}}}{\sqrt{d_{k}}} \qquad (3)$$

where  $i \in \{1, ..., M^2\}$ ,  $\mathbf{S}^i \in \mathbb{R}^{T \times T}$  is the attention maps without softmax, [ ] is the round down operation and % is the mod operation. For example,  $\mathbf{S}^4$  is computed by  $\mathbf{Q}^1$  and  $\mathbf{K}^4$  when M = 4.



Figure 2: Illustration of dual enhanced interaction in EIT (M = 4). We omit the ReLU for simplicity.

**Discussion.** M2M demonstrates an increased capacity to generate M times the number of attention maps when given identical input. This enhanced capability can be attributed to effective utilization of a many-to-many mapping strategy by M2M, which fully leverages the original head features, such as Q and K. Notably, this approach successfully avoids the production of similar attention maps by employing a dot-multiplication strategy to directly generate the attention maps (See Figure 10). By avoiding the generation of redundant attention maps, M2M improves its ability to capture diverse and distinct patterns in the input data. As a result, it facilitates the subsequent creation of more comprehensive and informative representations. This module can also be viewed as a strategy to enhance *complementary* principle.

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## 3.2 Dual Enhanced Interaction

As aforementioned, M2M enlarges the information capacity, which provides a prerequisite for encouraging consensus among different heads. To encourage consensus, a simple idea is to directly add a linear transformation among attention maps (Shazeer et al., 2020; Zhou et al., 2021b; Wang and Tu, 2020). While these methods can achieve performance improvements in vanilla Transformer settings, they are unsuitable in our framework. One key factor is that our framework encompasses a wealth of information; however, it also incorporates certain elements of noise. Such a coarse interaction fails to attain a satisfactory consensus.

To address this problem, we propose a finer solution that is able to differentiate between relevant and irrelevant information, discarding the latter while fully capitalizing on the former. Two kinds of interactions among those attention maps are introduced hierarchically, the inner-subspace interaction and cross-subspace interaction.

205Two Relationships.We begin with identifying206two important relationships: inner-subspace inter-

action (ISI) relationship and cross-subspace interaction (CSI) relationship. As illustrated in Figure 1, the inner-subspace interaction (ISI) relationship describes the connection among the attention maps generated by the same query, e.g., attention maps in the block of same color. These attention maps own a closer relationship. The cross-subspace interaction (CSI) relationship describes the collaboration among different heads, which exists in the attention maps generated by different queries, e.g., attention maps from blocks of different color.

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**Inner-Subspace Interaction Modeling.** One can adopt the standard convolution operation via batch transformation. However, such a way ignores the difference among the ISI relationship constrained by different queries, e.g., the ISI relationship in red block and blue block in Figure 1. It is desirable to preserve and enhance this distinction. To more efficiently model the interaction within subspaces, we therefore adopt group convolutions (Krizhevsky et al., 2012), which use separate parameters to process features from different groups.

Denote  $f(\cdot)$  as a single layer group convolution. As illustrated in Figure 2, given the output of M2M, namely **S**, as input, ISI sub-module computed as:

$$\dot{\mathbf{S}} = \mathbf{f}^{(1)}(\mathbf{ReLU}(\mathbf{f}^{(0)}(\mathbf{S}))) \tag{4}$$

where  $\dot{\mathbf{S}} \in \mathbb{R}^{M \times T \times T}$  is the output of the ISI submodule. We use  $M^{H_{isi}}$  to represent the intermediate number of heads in ISI sub-module and set the number of groups in group convolutions to M.

Finally, we can obtain M high-quality attention maps that effectively retain the benefits of using a larger number of attention heads while discarding irrelevant information. Such a process is another key for Transformer to benefit from more heads and is unique to our work.

**Cross-Subspace Interaction Modeling.** To efficiently model the cross-subspace interaction, we adopt two-layer convolutions accompanied by the ReLU activation to consist this sub-module.

Let us denote  $g(\cdot)$  as a single layer convolution. As illustrated in Figure 2, given the output of ISI, namely  $\dot{S}$ , as input, CSI sub-module computed as:

$$\ddot{\mathbf{S}} = \mathbf{g}^{(1)}(\mathbf{ReLU}(\mathbf{g}^{(0)}(\dot{\mathbf{S}})))$$
(5)

where  $\mathbf{\ddot{S}} \in \mathbb{R}^{M \times T \times T}$  is the output of the CSI submodule. We use  $M^{H_{csi}}$  to represent the intermediate number of heads in CSI sub-module. Finally, we can obtain M final attention maps that fully leverage the benefits of each head. 257

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## **3.3 Efficient Version of EIT**



Figure 3: Illustration of dual enhanced interaction in efficient EIT (M = 4). We omit the ReLU for simplicity.

Despite the theoretically computational efficiency and parametric efficiency of group convolutions, they slow down the training in practice (Ma et al., 2018). To alleviate this issue, we provide another efficient version of EIT, namely E-EIT, by simplifying the design of dual enhanced interaction. As illustrated in Figure 3, both ISI and CSI adopt a single-layer operation. Formally, the dual enhanced interactions are computed as:

$$\ddot{\mathbf{S}} = \mathbf{g}^{(\mathbf{0})}(\mathbf{ReLU}(\mathbf{f}^{(\mathbf{0})}(\mathbf{S}))), \qquad (6)$$

where **ReLU**( $\mathbf{f}^{(0)}(\mathbf{S})$ ), namely as  $\dot{\mathbf{S}}$ ,  $\in \mathbb{R}^{M^H \times T \times T}$  and  $\ddot{\mathbf{S}} \in \mathbb{R}^{M \times T \times T}$  and  $M^H$ is a hyper-parameter, e.g. we set it as 32 for the base configuration. In this way, E-EIT avoids parts of memory consumption and somehow improves the computational efficiency.

# 4 Experiment Settings

We evaluated our EIT on four widely used benchmarks<sup>1</sup>: 1) Machine Translation, 2) Grammar Error Correction, 3) Abstractive Summarization, and 4) Language Modeling. The detailed architecture setups, training setups and evaluation setups were presented in Appendix A.

#### 4.1 Machine Translation

**Dataset.** We selected two widely used corpus: WMT'14 English-German (En-De) translations (a large-scale dataset, 4.5M training sentence pairs) and WMT'16 English-Romanian (En-Ro) translations (a small-scale dataset, 610K training sentence pairs). The validation and test sets are *newstest2013* and *newstest2014*, respectively. For the En-Ro task, it consists of 610K training sentence pairs. We preprocessed the data as the setups in Mehta et al. (2021). We performed shared BPE operations on both datasets to overcome the out-ofvocabulary (OOV) problem. Concretely, we set the size of BPE operations to 32K and 20K for En-De and En-Ro datasets, resulting in a shared vocabulary with sizes of 34040 and 19064, respectively.

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**Models.** Our model architectures were based on Transformer (Vaswani et al., 2017). We provided three basic configurations, namely *base*, *deep*, and *big* which follow the configurations in Vaswani et al. (2017). We adopted a pre-normalization strategy (Wang et al., 2019) considering training stability under different configurations.

Training & Evaluation. We implemented our models using Fairseq (Ott et al., 2019). Training employed 8 GEFORCE RTX 3090 cards for WMT'14 En-De and 4 cards for WMT'16 En-Ro, with batch sizes of 65536 and 16384, respectively. In the En-De task, we completed 50K updates for base, 50K for deep, and 100K for big models. We utilized Adam (Kingma and Ba, 2015) with  $adam_\beta$ (0.9, 0.997) as the optimizer, an invert sqrt learning rate scheduler with a rate of 0.002 and 16000 warmup updates, and 0.1 label smoothing for all experiments. During evaluation, we used 4 beams with a length penalty of 0.6 for En-De and 5 beams with a length penalty of 1.3 for En-Ro. We ran each experiment three times and reported the average score.

## 4.2 Grammar Error Correction

**Dataset.** We also assessed EIT's effectiveness for grammar error correction, a crucial natural language processing application. Our experiments were conducted on the CONLL dataset, comprising 827K training sentences. Following the setup in (Chollampatt and Ng, 2018), we incorporated the word-level dropout technique (Sennrich et al., 2016) to mitigate overfitting. We configured BPE operations to 30K.

**Models.** We selected the Transformer (Vaswani et al., 2017) and SURFACE (Liu et al., 2021) for comparison. These architectures adhere to the Transformer-base configuration outlined in Vaswani et al. (2017).

Training & Evaluation.We trained grammar334error correction models on 8 GEFORCE RTX 3090335cards, using a batch size of 65536 and completing33614K total updates. Further training specifics can be337found in Table 11. For testing, we configured the338number of beams to 6 and the length penalty to 0.6.339

<sup>&</sup>lt;sup>1</sup>We also evaluated our EIT variants on some task beyond natural language processing in Appendix.

Turne	Madal	WM	WMT'14 En-De		
туре	Model	$\theta$ (M)	BLEU	sBLEU	
	Refiner (Zhou et al., 2021b)	-	27.62	-	
	Talking-Head (Shazeer et al., 2020)	-	27.51	-	
Hand	Collaboration (Wang and Tu, 2020)	-	27.55	-	
Modification	DYROUTING (Li et al., 2019)	297	28.96	-	
Wioumcation	DISAGREE (Li et al., 2018)	-	29.28	-	
	MoA (Zhang et al., 2022)	200	29.40	-	
	FISHformer (Nguyen et al., 2022)	-	29.57	-	
	DMAN (Fan et al., 2021)	211	28.97	27.8	
Localness	CSAN (Yang et al., 2019)	-	28.74	-	
	UMST (Li et al., 2022)	242	29.75	-	
	Transformer base	61.56	27.13	26.0	
	EIT base	61.63	28.00	26.9	
_	E-EIT base	61.57	27.72	26.7	
Our	Transformer 48L	193.96	29.60	28.5	
(Dra Norm)	EIT 48L	194.32	30.25	29.2	
(Pre-Norm)	E-EIT 48L	194.14	30.16	29.1	
	Transformer big	211.22	28.80	27.7	
	EIT big	211.55	29.79	28.7	
	E-EIT big	211.30	29.61	28.5	

Table 1: Results on WMT'14 En-De Task.

# 4.3 Abstractive Summarization

**Dataset.** We also tested the effectiveness of EIT on abstractive summarization task, a task relying on the ability of modeling long dependency. Shared BPE operations of 30K were applied to the training data, resulting in a vocabulary of 32,584 words.

**Models.** Our models were all under base configuration, e.g., embedding dimension, hidden dimension, M are set to 512, 2048 and 8, respectively.

**Training & Evaluation.** We trained abstractive summarization models on 8 GEFORCE RTX 3090 cards, utilizing a batch size of 131,072 and completing 30,000 total updates. We incorporated a weight decay strategy with a ratio of 0.0001. We set warming updates to 16000. For testing, we configured 4 beams and a length penalty of 2.0, with minimum and maximum lengths set to 55 and 140, respectively.

4.4 Language Modeling

**Dataset.** We assessed EIT in a language modeling task using WikiText-103 to investigate its capacity for handling long dependencies. The training, validation, and test sets encompass 103 million words (from 28,000 articles), 218,000 words, and 246,000 words, respectively. We adhered to the official preprocessing procedure (Ott et al., 2019).

**Models.** We chose the Adaptive Input Transformer (Baevski and Auli, 2019) as the baseline model. All models are 8-layer models with 8 heads.

True	Madal	WMT'16 En-Ro			
туре	Model	$\theta$ (M)	BLEU		
Basic	Transformer (Liu et al., 2020) Transformer (Kasaj et al., 2020)	-	34.30 34.16		
Baseline	DELIGHT (Mehta et al., 2021)	53	34.70		
	Refiner (Zhou et al., 2021b)	54	34.25		
Hand	Talking-Head (Shazeer et al., 2020)	54	34.35		
modification	Collaboration (Wang and Tu, 2020)	54	34.64		
mouncation	FISHformer (Nguyen et al., 2022)	49	34.42		
	MoA (Zhang et al., 2022)	56	34.39		
Localnoss	DMAN (Fan et al., 2021)	-	34.49		
Locamess	UMST (Li et al., 2022)	60	34.81		
	Transformer base	53.90	34.23		
	EIT base	53.98	35.10		
	E-EIT base	53.92	35.01		
Our	Transformer 24L	110.64	35.00		
(Dro Norm)	EIT 24L	111.09	35.40		
(Pre-Norm)	E-EIT 24L	110.73	35.35		
	Transformer big	195.88	34.44		
	EIT big	196.40	34.91		
	E-EIT big	195.97	34.67		

Table 2: Results on WMT'16 En-Ro Task.

**Training & Evaluation.** The training and evaluation settings adhered to the standard PyTorch (Ott et al., 2019) language modeling guidelines. We trained both the baseline and EIT with 286,000 updates. During evaluation, we selected the checkpoint with the best performance on the validation set. Parameters such as max-tokens, maxsentences, and context-window were set to 3072, 1, and 2560, respectively. 369

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# **5** Experiments Results

# 5.1 Machine Translation

Table 1 and Table 2 display the results on En-De and En-Ro tasks, respectively. First, we can see that Our EIT variants demonstrate superior performance compared to the vanilla Transformer across various configurations on both tasks. This indicate the effectiveness of EIT variants. Notably, E-EIT, an alternative to satisfy the low-latency of industrial application, can deliver competitive results compared with the full version while maintaining fast processing speeds.

Besides, Our EIT can beat all selected methods of head modification and localness modeling, including the latest methods such as MoA (Zhang et al., 2022), Fishformer (Nguyen et al., 2022), UMST (Li et al., 2022), on both datasets. This highlights the fact that focusing on a single aspect, such as complementarity, is inadequate for achieving optimal results. It is essential to take into account both complementarity and consensus to ensure the best outcomes.

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Precision	Recall	$\mathbf{F}_{0.5}$
64.84	36.61	56.18
64.32	36.07	55.61
66.80	35.00	56.60
69.98	32.80	57.05
69.85	33.36	57.31
	Precision 64.84 64.32 66.80 <b>69.98</b> 69.85	Precision         Recall           64.84         36.61           64.32         36.07           66.80         35.00           69.98         32.80           69.85         33.36

Table 3: Results on the correction task.

Model	RG-1	RG-2	RG-L
Transformer ‡	40.84	18.00	37.58
Talking-Head (Shazeer et al., 2020)	41.26	18.34	38.06
PG-Net (See et al., 2017)	39.53	17.28	36.38
MADY (Wang et al., 2021)	40.72	17.90	37.21
DMAN (Fan et al., 2021)	40.98	18.29	37.88
BOTTOM-UP (Gehrmann et al., 2018)	41.22	18.68	<b>38.34</b>
SURFACE (Liu et al., 2021)	41.00	18.30	37.90
EIT	<b>41.62</b>	<b>18.70</b>	38.33
E-EIT	41.58	18.63	38.28

Table 4:	Results	on the	summarization	task.

#### 5.2 Grammar Error Correction

Table 3 presented the results on the CONLL dataset's test set. Both EIT and E-EIT outperform the standard Transformer, showing improvements of 0.87 and 1.13 in terms of  $F_{0.5}$ , respectively. Compared to the strong baseline SURFACE, our methods (EIT and E-EIT) still outperform it by 0.45 and 0.71  $F_{0.5}$  points, respectively. Importantly, both EIT and E-EIT require negligible extra parameters, less than 0.1M, indicating their enhanced expressive power. Notably, the Talking Heads model underperforms, possibly due to imperfect hyper-parameters, needing more fine-tuning.

An interesting observation is that EIT variants seem to trade recall for precision. This behavior is due to EIT's foundation in both complementary and consensus principles, which naturally generate more precise attention maps by filtering out uncertain information. As a result, EIT primarily makes corrections where it is most confident.

#### 5.3 Abstractive Summarization

Table 4 shows results on test set of CNN-DailyMail. We can see EIT can achieve scores of 41.62 ROUGE-1 points, 18.70 ROUGE-2 points and 38.33 ROUGE-L points, outperforming the standard Transformer by 0.78, 0.70 and 0.75 in terms of ROUGE-1, ROUGE-2 and ROUGE-L points, respectively. Compared with other strong baselines, our EIT can still show superiority on these datasets in terms of ROUGE-1 points, e.g., EIT surpasses SURFACE, DMAN, BOTTOM-UP, Talking-Head by

Model	Depth	$\theta\left(\mathbf{M}\right)$	Test PPL
Adaptive Transformer EIT	8 8	146.49 146.50	21.11 <b>20.00</b>
E-EIT	8	146.49	20.19

Table 5: Results on the WikiText-103 dataset.

# Model	En-De	En-Ro
1 Transformer	27.13	34.23
2 EIT 3 - Many-to-Many 4 - Inner-Subspace Interaction 5 - Cross-Subspace Interaction	<b>28.00</b> 27.39 25.79 27.70	<b>35.10</b> 34.71 32.50 34.53

Table 6: Ablation study on two tasks. Time denotes the training computing time.

0.62, 0.64, 0.40 and 0.36 in terms of ROUGE-1 points, respectively. Notably, our E-EIT can achieve comparable performance with EIT.

# 5.4 Language Modeling

Table 5 presents the perplexity scores of various models on the WikiText-103 test set. Our EIT and E-EIT models outperform the baseline with PPL scores of 1.11 and 0.92, respectively. These results highlight the high expressiveness of our methods, as the improvements are achieved with only a negligible increase in parameters. Also, these results demonstrate the universal of our approach as applying our approach to decoder-side can also achieve improvement.

# 6 Ablation Studies

**Settings.** We gave detailed description about the settings of ablation studies.

- EIT M2M: We directly applied ISI and CSI modules to the attention maps generated by Eq. (1). Notably, in both ISI and CSI, we maintain a consistent ratio between hidden size and input size, e.g., 2 and 8 for ISI and CSI, respectively, mirroring the EIT settings.
- EIT ISI: we directly applied CSI module to the  $M^2$  attention maps generated by M2M.
- EIT CSI: we only applied ISI module to the  $M^2$  attention maps generated by M2M.

**Results.** Table 6 summarized the impacts of removing each module on En-De and En-Ro tasks, respectively. First, we found removing any module (or sub-module) results in obvious performance



Figure 4: Cosine similarity among attention maps of different models on En-De task.

degradation (#3,4,5 vs. #2). These evidences indicate the indispensability of these modules.

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Notably, when removing the M2M module (#2 vs. #3), we observe an obvious decline in performance on two translation tasks, indicating the importance of M2M module. Within our EIT framework, the M2M module, motivated by the complementary principle, serves the critical purpose of supplying necessary information for subsequent interactions. Therefore, its absence impedes the effectiveness of our two interaction models.

Furthermore, the omission of the ISI sub-module (#2 vs. #4) results in a significant and noticeable decrease in BLEU scores. One possible explanation is that while increasing the number of heads enhances the information capacity, it also introduces a certain degree of irrelevant information (noise) into the attention maps. Consequently, a direct fusion of these heads fails to yield satisfactory outcomes. However, our EIT framework overcomes this challenge by incorporating the ISI sub-module, which provides an effective mechanism for discarding irrelevant information while retaining the benefits of the previous heads. This unique and innovative design sets our approach apart from the attention expansion technique (Zhou et al., 2021b).

#### **Analysis on Attention Heads Behavior** 7

#### **EIT owns Higher Consensus** 7.1

As depicted in Figure 4, it is evident that EIT ex-490 hibits the highest average similarity among attention maps from various heads, surpassing all other 492 models. This finding suggests that EIT demon-493 strates a greater consensus among attention heads. We attribute this achievement to the significant role 495 played by M2M and dual enhanced interaction. M2M facilitates the generation of rich information, while dual enhanced interaction efficiently lever-498 ages and refines the available information from different attention heads. 500



Figure 5: Token correlation of Transformer and EIT on En-De task.

**Discussions.** This phenomenon is contradictory to the findings of previous studies about head interaction (Wang et al., 2022a). We speculate that this is because our interactions are more efficient, not only relying on an adequate number of attention heads but also operating in a hierarchical manner. These characteristics result in a consensus among the attention maps.

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#### **Benefits of High Consensus** 7.2

**EIT Learns High-quality Representations** We further investigate how consensus affect the layer representations. Following (Gong et al., 2021; Dong et al., 2021; Shi et al., 2022; Wang et al., 2022b), we adopt the token correlation  $\mathcal{TC}$  to measure the quality of features (the lower, the better). The token correlation is computed by the Pearson correlation coefficient (Benesty et al., 2009).

Figure 5 exhibits the results on the test set of the En-De task. Notably, the features learned by EIT exhibit lower token correlation compared to the vanilla Transformer across all configurations. This indicates that EIT effectively learns improved layer representations.

Furthermore, we observe that the vanilla Transformer consistently maintains relatively high token correlation from the first layer. This observation aligns with prior study (Shleifer and Ott, 2022), suggesting that lower layers struggle to optimize effectively in pre-normalization Transformers. However, our EIT approach alleviates this issue.

**EIT Makes Head Pruning Easier** To further explore the possibility of pruning the consensus attention maps, we introduce a simple head mask mechanism for head pruning during the inference phase as follows::  $\mathbf{O} = \sum_{i=1}^{M} \eta_i \mathbf{A}^i \mathbf{X} \mathbf{W}_V^i \mathbf{W}_O^i$ where  $\eta_i \in \{0, 1\}$ . Table 7 exhibits the results on En-De tasks. Note that the head selection process is done in a straightforward manner, such as selecting heads by index, without considering their relative importance as highlighted in previous stud-

Model	Pruning Ratio					
	0.0%	50.0%	87.5%			
Transformer-48L EIT-48L	29.60 <b>30.25</b>	27.64 <b>29.09</b>	1.86 <b>21.12</b>			

Table 7: BLEU scores of models with head pruning on the En-De task.

ies (Michel et al., 2019). Additionally, the head
pruning operations are exclusively applied to the
encoder side. It is evident that EIT exhibits a high
tolerance for head pruning without experiencing
significant deterioration in performance. Such phenomenon sheds light on the researches of head
pruning and inference speeding.

## 8 Analysis of Computational Efficiency

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MACs Comparison. Table 8 displayed MACs comparison between EIT variants and transformer baselines. We can see that EIT can achieve an improvement of 0.87 BLEU points with only extra 0.1B MACs and 0.07M parameters. This indicated the efficiency of our EIT architecture. Besides, the efficient version of EIT. the E-EIT can achieve similar improvements with even fewer extra resource consumption.

**Resource Comparison.** In addition to theoreti-558 cally exploring the efficiency of EIT variants, we 559 also measured the practical computational con-560 sumption during training process. Without losing generality, we focused on the model for the base configuration. We can see that EIT cost 8% more memory consumption and 45% more training costs 564 than the baseline with a depth of 6. To mitigate this, 565 we have proposed the E-EIT which only costs 5% 566 more memory consumption and 10% more train-567 ing costs than the baseline but delivered similar performance compared to EIT. Notably, as shown 569 in Table 1, the performance gap between EIT and E-EIT decreases as the model capacity increases. 571

# 9 Related Work

Low Bottleneck in Multi-Head Attention The "Low Bottleneck" issue in Multi-head Self-Attention (MHSA) occurs when adding more heads to Transformers does not correspondingly improve performance. Bhojanapalli et al. (2020) first identified this issue, attributing it to the diminishing head dimension as the number of heads increases, which limits the creation of precise attention maps. In

Model	θ ( <b>M</b> )	MACs	Time	Memory	BLEU
Transformer EIT E-EIT	61.56 61.63 61.57	10.0B 10.1B 10.0B	1.45× 1.10×	1.08× 1.05×	27.13 <b>28.00</b> 27.72

Table 8: **EIT variants are efficient as compared to transformers.** BLEU score is reported on the WMT'14 En-De dataset. We used 20 source and target tokens for computing multiplication-addition operations (MACs).

response, Shazeer et al. (2020) introduced "talkinghead attention," using two linear transformations around the SoftMax function to address this bottleneck. Later, Zhou et al. (2021b) proposed a framework involving "ghost heads" to enrich attention patterns, differentiating from talking-head attention in the positioning of linear transformations and the number of ghost heads. Our approach introduces a many-to-many mapping in MHSA, using existing queries and keys for more attention maps through direct query-key multiplication. 581

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Improved Multi-Head Mechanism Previous work has shown that multi-head attention can be further enhanced by encouraging individual attention heads to extract distinct information (Li et al., 2018; Cui et al., 2019; Sukhbaatar et al., 2019; Guo et al., 2020; Hao et al., 2019). Another branch of research is designing more complex interactive modeling to make better use of the multiple subspace information (Shazeer et al., 2020; Wang and Tu, 2020; Li et al., 2019). Besides, Voita et al. (2019) empirically demonstrates that some heads in attention are useless and can be pruned without performance degradation. Along this line, researchers investigate how to efficiently cut off redundant heads (Michel et al., 2019; Behnke and Heafield, 2020). Different from them, our study utilized the benefits of both diversity and consistency.

# 10 Conclusions

In this paper, we propose EIT, an alternative to the Transformer architecture. It further advances the multi-head schema by fully leveraging two principles in multi-view learning: the *complementary principle* and the *consensus principle*. In addition, E-EIT can be served as another choice considering the trade-off between performance and computation efficiency. Experimental results on four widely-used tasks demonstrate the effectiveness of EIT-variants, which deliver consistent improvements to the standard Transformer. 621

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# Limitations

622Besides the advantages endowed by EIT, there still623exists a shortcoming that the computational effi-624ciency of the group convolution cannot be satis-625factory, although it is computationally efficient in626theory. This is due to the lack of high-efficiency627CUDA kernel support. We will release a more ef-628ficient optimization of group convolutions in the629soon future.

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# A Detailed Setups of Experiments

# A.1 Machine Translation Task

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**Dataset** We evaluated our approach on two widely used machine translation datasets: WMT'14 En-De and WMT'16 En-Ro. The En-De dataset contains approximately 4.5M tokenized training sentence pairs. We selected newstest2013 and newstest2014 as the validation and test data, respectively. As for the En-Ro dataset, it consists of 0.6M tokenized training sentence pairs. We performed shared BPE operations on both datasets to overcome the out-of-vocabulary (OOV) problem. Concretely, we set the size of BPE operations to 32K and 20K for En-De and En-Ro datasets, resulting in a shared vocabulary with sizes of 34040 and 19064, respectively.

Model Configuration Our model architectures are based on Transformer (Vaswani et al., 2017).
We provided three basic configurations, namely *base*, *deep*, and *big* which follow the configurations in Vaswani et al. (2017). We adopted a prenormalization strategy (Wang et al., 2019) considering training stability under different configurations. The detailed settings of hyper-parameters are given in Table 10.

Training & Evaluation Our implementations are based on Fairseq (Ott et al., 2019). Our experiments are performed on the GEFORCE RTX 3090 cards. We use 8 GEFORCE RTX 3090 cards to train models for the WMT'14 En-De task. As for the models on the WMT'16 En-Ro task, we train them on 4 GEFORCE RTX 3090 cards. The batch sizes for En-De and En-Ro tasks are 65536 and 16384, respectively. The total updates are 50K, 50K and 100K for base, deep and big in En-De task, respectively. We adopt Adam (Kingma and Ba, 2015) as an optimizer with an  $\operatorname{adam}_{\beta}$  of (0.9, 0.997). The learning rate scheduler is invert sqrt with a learning rate of 0.002 and warmup updates of 16000. We also adopt label smoothing with a ratio of 0.1 in all the experiments. More details are exhibited in Table 11. During the evaluation process, we set the beam number to 4 and the length penalty to 0.6 for the En-De task. As for the En-Ro task, the number of beams is 5 and the length penalty is 1.3.

# A.2 Abstractive Summarization Task

**Dataset** For abstractive summarization, we conduct experiments on a widely used corpus, e.g.,

CNN/DailyMail dataset. It consists of 287K training documents. Shared BPE operations with a size of 30K are performed on all the training data, resulting in a vocabulary of 32584.

**Model Configuration** We only provide the *base* configuration of our EIT and E-EIT for abstractive summarization. The details are presented in Table 10.

**Training & Evaluation** We train models for an abstractive summarization task on 8 GEFORCE RTX 3090 cards with a batch size of 131072 and total updates of 30K. We adopt a weight decay strategy with a ratio of 0.0001. Other hyper-parameters are the same as that in machine translation tasks. You can find their settings in Table 11. During testing, the number of beams is set to 4 and the length penalty is set to 2.0. Besides, we set the minimal length and maximum length to 55 and 140, respectively.

## A.3 Grammar Error Correction Task

**Dataset** For the grammar error correction task, we select the CONLL dataset to evaluate our approach. The CONLL dataset consists of 827K training sentences. We replicate the setup in Chollampatt and Ng (2018) and adopt the word-level dropout technique (Sennrich et al., 2016) to alleviate the overfitting problem. More details are listed in Table 9.

**Model Configuration** For grammar error correction task, we only provide the *base* configuration of our EIT and E-EIT. The details are presented in Table 10. Notice that the models on this task adopt a post-normalization strategy.

**Training & Evaluation** We train models for the grammar error correction task on 8 GEFORCE RTX 3090 cards. The batch size is 65536 and the total updates are 14K. More training details are shown in Table 11. During testing, the beams and length penalty are set to 6 and 0.6, respectively.

#### A.4 Automatic Disease Diagnosis Task

DatasetFor the automatic disease diagnosis task,1012we select the ABIDE dataset to evaluate our approach. The ABIDE dataset consists of 1009 brain1013networks from 1009 real samples of 17 international sits. Due to the heterogeneity of this data,1016we adopt the shared data with re-standardized data1017splitting in Kan et al. (2022). Specifically, 70%,1018

Dataset		Sentence	BPE	Vocab	
	Train	Dev	Test	DIL	vocus
WMT'14 En-De	4.5M	3.0K	3.0K	32K	34040
WMT'16 En-Ro	0.6M	2.0K	2.0K	20K	19064
CNN/DailyMail	287K	13.0K	11.0K	30K	32584
CONLL	827K	5.4K	1.3K	30K	33136
WikiText-103	103M	218K	246K	-	267740

Table 9: The details of datasets of language tasks.

Task	Model	Configuration	$\mathbf{M}$	$\mathbf{M}^{\mathbf{H}}$	$M^{H_{\rm isi}}$	${\rm M}^{\rm H_{\rm csi}}$	r	$\mathbf{K}_{h}^{isi}$	$\mathbf{K}_w^{isi}$	$\mathbf{K}_{h}^{csi}$	$\mathbf{K}^{csi}_{w}$
		base	8	-	128	64	8	1	7	1	3
	Еіт	deep	8	-	128	64	8	1	7	1	3
МТ		big	16	-	256	256	16	1	7	1	3
		base	8	32	-	-	8	1	7	1	7
	E-EIT	deep	8	32	-	-	8	1	7	1	7
		big	16	64	-	-	16	1	7	1	7
AS	Еіт	base	8	-	8	64	8	1	1	1	1
110	E-EIT	base	8	16	-	-	8	1	1	1	1
GEC	Еіт	base	8	-	128	128	8	1	7	1	3
E-EIT	E-EIT	base	8	64	-	-	8	1	7	1	7
LM	Еіт	big	8	-	64	32	8	1	1	1	1
2.01	Е-ЕІТ	big	8	8	-	-	8	1	1	1	1

Table 10: The configurations of models on three sequence generation tasks. MT, AS, GEC and LM denote machine translation, abstractive summarization, grammar error correction and language modelling, respectively.

Hyper-parameter	WMT'14 En-De	WMT'16 En-Ro	CNN/DailyMail	CONLL	WikiText-103
GPUs	8	4	8	8	8
Batch	4096	4096	4096	4096	1024
UF	2	1	4	2	8
Optimer	Adam	Adam	Adam	Adam	Nag
$Adam_{\beta}$	(0.9, 0.997)	(0.9, 0.997)	(0.9, 0.997)	(0.9, 0.980)	-
LR	0.0020	0.0020	0.0020	0.0015	0.0001
LR scheduler	inverse sqrt	inverse sqrt	inverse sqrt	inverse sqrt	Cosine(t-mult=2)
Initial LR	$1e^{-7}$	$1e^{-7}$	$1e^{-7}$	$1e^{-7}$	$1e^{-7}$
Total updates	50K (100K)	25K	30K	14K	286K
Warmup updates	16000	8000	8000	4000	16000
Weight decay	0.0000	0.0000	0.0001	0.0001	0.0000
Label smoothing	0.1	0.1	0.1	0.1	0.0
Dropout	0.1 (0.3)	0.1 (0.3)	0.1	0.2	0.3
Attention dropout	0.1	0.1	0.1	0.1	0.1
ReLU dropout	0.1	0.1	0.1	0.1	0.1
Word dropout	0.0	0.0	0.0	0.2	0.1

Table 11: The training setups of different tasks. UF denotes the update frequency of the gradient. (.) lists the values of hyper-parameters under the *big* configuration, which vary from the values under the *base* configuration.

10% and 20% samples are served as the training, validation and test sets, respectively.

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**Model Configuration** For ABIDE task, we still follow the model configuration in Kan et al. (2022). Specifically, we build our BrainNetEITF with two-

layer encoder. The number of heads M are set to 4for each layer.

**Training & Evaluation** We train all models including the BrainNetTF and BrainNetEITF fro 200 epochs on a single GEFORCE RTX 3090 card. Each model is trained by 5 times. We adopt Adam (Kingma and Ba, 2015) as an optimizer with an initial learning rate of  $10^{-4}$  and a weight decay of  $10^{-4}$ . The batch size is set to 64. We adopt the checkpoint of the final epoch for evaluating the test set.

## A.5 Language Modeling Task

**Dataset** For the language modeling task, we select the WikiText-103 dataset to evaluate our approach. The training set consists of 103M words from 28K articles. While for the validation and test sets, they are made up of 218K and 246K words, respectively. In details, we follow the instructions in Fairseq (Ott et al., 2019) to obtain and preprocess the data. The details are listed in Table 9.

Model Configuration For WikiText-103 task, Both baseline and our model are all 8-layer big model with 8 heads. Note that the baseline we adopted are adaptive input transformer (Baevski and Auli, 2019). In this task, the kernel sizes in DEI are all set to 1.

**Training & Evaluation** The training and evaluation settings all follow the standard instructions for language modeling in PyTorch (Ott et al., 2019). We train both baseline and EIT with 286000 updates. The details are given in Table 11. As for the evaluation process, we adopt the checkpoint performing best on the validation set. We set the maxtokens, max-sentences, context-window to 3072, 1 and 2560, respectively.

# **B** Details of Metrics

#### **B.1** Calculation of Head Distance

Inspired by the attention metrics in Zhou et al. (2021a) and Wang et al. (2022b), we measure the distance between different heads by calculating cosine similarity among attention maps. Notice that our metric focuses on the diversity of attention maps, which is quite different from them. Denote the dataset as  $\mathcal{D}$ , and the attention map of *h*-th head of *l*-th layer of *i*-th sample denotes as  $\mathbf{A}^{(h,l,i)}$ , the head similarity in *l*-th layer is computed by averaging the cosine similarity of every two heads in *i*-th layer across all samples as:

$$\mathcal{HD}^{(l)} = \frac{1}{|\mathcal{D}|} \frac{1}{M(M-1)} \\ \frac{1}{T} \sum_{i=1}^{|\mathcal{D}|} \\ (\sum_{j=1}^{M} \sum_{k=1}^{M} (\sum_{i=1}^{M} \sum_{k=1}^{M} (\sum_{i=1}^{T} \operatorname{Cosine}(\mathbf{A}_{t,:}^{(j,l,i)}, \mathbf{A}_{t,:}^{(k,l,i)}) \\ - M)$$
(7) 1072

where  $|\mathcal{D}|$  denotes the size of dataset, M is the number of partition of features in attention, T is the sequence length and Cosine( $\cdot$ ) denotes the cosine similarity function. We set  $\mathcal{D}$  to the test set of the corresponding task. The obtained head similarity ranges from [0, 1]. The larger the head similarity, the lower the distances between different heads are. 

# **B.2** Calculation of Token Correlation

We define a metric  $\mathcal{TC}$ , which measures the correlation among the representations of different tokens.1081tion among the representations of different tokens.1082Denote the dataset as  $\mathcal{D}$ , and the sequence representation of *i*-th sample in *l*-th layer denotes as  $\mathbf{X}^{(l,i)}$ ,1084the token correlation of in *l*-th layer is computed as:1085

$$\mathcal{TC}^{(l)} = \frac{1}{|\mathcal{D}|} \frac{1}{T(T-1)} \sum_{i=1}^{|\mathcal{D}|}$$

$$(\sum_{j=1}^{T} \sum_{k=1}^{T} \rho(\mathbf{X}_{j}^{(l,i)}, \mathbf{X}_{k}^{(l,i)}) - T)$$
(8) 1087

where  $\rho(\cdot)$  denotes the pearson correlation func-1088tion. Intuitively, the larger the  $\mathcal{TC}$  is, the higher the1089token correlation is, degrading the model's learning1090capacity (Gong et al., 2021).1091

# C Detailed added parameters of our methods

The detailed parameters of models on all tasks are1094listed in Table 12 and Table 13. We can see that1095the increased parameters are negligible on all tasks.1096Thus, we can exclude the effect of increasing parameters on performance.1097

Model	En-De			En-Ro		
	Base	Deep-48L	Big	Base	Deep-24L	Big
Transformer EIT E-EIT	61.56 M 61.63 M 61.57 M	193.96 M 194.32 M 194.14 M	211.22 M 211.55 M 211.30 M	53.90 M 53.98 M 53.92 M	110.64 M 111.09 M 110.73 M	195.88 M 196.40 M 195.97 M

Table 12: Detailed parameters of models on WMT En-De and WMT En-Ro tasks.

Model	<b>CNN-DailyMail</b>	CONLL	WikiText-103	ABIDE
Transformer	60.82 M	61.10 M	146.49 M	3.98 M
EIT	60.83 M	61.19 M	146.50 M	3.98 M
E-EIT	60.82 M	61.15 M	146.49 M	3.98 M

Table 13: Detailed parameters of models on CNN-DailyMail, CONLL, WikiText-103 and ABIDE tasks.

#### C.1 Efficiency Comparison

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Despite the performance evaluation, the memory consumption and computational cost are also two major concerns in the literature. Figure 6 also displays the memory consumption and computational cost of models on the En-De task. EIT only costs 8.5% more memory consumption and 44.4% more training costs than the baseline with a depth of 6. However, the extra consumption goes larger as the depth goes deeper.

Besides, as aforementioned, we elaborately design an efficient version E-Eit that only costs 9.4% more memory consumption and 21.7% more training costs than the baseline under all the configurations on average. In this work, the many-to-many mapping rule is only applied on the encoder side. This is because the proposed M2M module and the subsequent ISI and CSI sub-modules will significantly enlarge the inference cost due to the heavy use of product attention on the decoder side, although it can attain further benefits in terms of BLEU.

# D Visualization of Training and Validation Perplexity

We plot the training and validation perplexity of Transformer and our EIT on the WMT'14 task in Figure 7. We can see that our EIT owns lower training and validation perplexity than Transformer.

# E Hyper-Parameters Analysis (Kernel Size and Hidden Size)

1129Since there are several hyper-parameters in both1130ISI and CSI sub-modules, it is necessary to figure1131out how they affect performance. Figure 8 (a-d)1132plots the performance of EIT against the kernel1133size and the hidden size. We can see that EIT can1134outperform Transformer in all choice of kernel size

and hidden size. This observation can further help1135us trade off efficiency and performance well. For1136example, we can set csi kernel size to 1 or isi kernel1137size to 3 or  $M^{H_{isi}}$  to  $M^2$  or  $M^{H_{csi}}$  to 4M to own1138a more efficient EIT.1139

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# F Local Analysis

Local modeling is one of the widely accepted ways to improve the expressiveness of Transformer (Yang et al., 2019; Fan et al., 2021; Li et al., 2022). In dual enhanced interaction, we apply convolution operations to attention maps, which has the potential to introduce local biases. To figure it out, we measure the localness of attention maps since if there is a local bias, each token will distribute larger attention weights on their neighboring tokens. We adopt the localness metric of Fan et al. (2021), denoted as C (higher is better). More details are presented in Appendix.

We plot the C value within a local region w = 0.1 \* T + 1, of models in En-De task and CNN-DailyMail task in Figure 9. The value is computed over the test set. Due to the long sequence length, we only use a subset of the test set consisting of 1000 samples for the CNN-DailyMail task. The results (mean) show no significant local enhancement phenomena in both tasks. Note that the attention maps in the first layer of EIT on the abstractive summarization have a strong local pattern, but the kernel sizes are set to 1 on this task. So we conclude that the improvements do not come from local enhancement.

# G Evaluation on Automatic Brain Disease Diagnosis Task

We further inspect the potential of EIT to be severed1168as a general method beyond language tasks. The1169automatic brain disease diagnosis, a disease classi-1170



Figure 6: Memory and speed vs. encoder depth. E-EIT can achieve comparable results with fewer training costs than EIT.



Figure 7: Training perplexity and validation perplexity of Transformer and our EIT on WMT'14 En-De task. Note that the models are in *base* configuration.

Model	AUROC	ACC	SEN	SPE
MvS-GCN (Wen et al., 2022)	69.0	69.4	69.3	64.5
BrainNetTF (Kan et al., 2022)	$80.9 \pm 2.6$	71.8±3.0	71.1±4.1	72.5±1.9
BrainNetEITF	81.3±2.7	73.8±3.2	73.9±5.8	75.6±4.7
BrainNetE-EITF	82.9±3.3	74.6±3.2	72.2±5.3	76.8±3.0

Table 14: AUROC, ACC, SEN and SPE points on ABIDE task.

fication task that highly relies on precisely learning 1171 relationships among different brain regions has re-1172 cently been dominated by graph convolution (Wen 1173 et al., 2022) and Transformer (Kan et al., 2022). 1174 We select a widely used real-world fMRI dataset: 1175 Autism Brain Imaging Data Exchange (ABIDE), 1176 which consists of 1009 brain networks from 17 in-1177 ternational sites, of which 516 samples are autism 1178 spectrum disorder patients. We follow the prepro-1179 cessing setup in Kan et al. (2022) and adopt the 1180 CC200 (Craddock et al., 2012) as the Regin-of-1181 Interest (ROI) partition template. We select two 1182 latest methods, the Mvs-GCN (Wen et al., 2022) 1183 and BrainNetTF (Kan et al., 2022), as our compar-1184 ison. The experimental setups and configurations 1185 of our BrainNetEITF and BrainNetEEITF are the 1186 1187 same as in Kan et al. (2022). Each experiment is conducted 5 times and we report the mean and 1188 standard deviation of the four metrics: Accuracy 1189 (ACC), AUROC, Sensitivity (SEN) and Specificity 1190 (SPE). 1191

<b>Encoder Layers</b>	Training Time	En-De
[1]	$1.07 \times$	27.76
[2]	-	27.46
[3]	-	27.40
[4]	-	27.38
[5]	-	27.30
[6]	-	27.48
[1-2]	1.13×	28.08
[1-3]	$1.20 \times$	28.02
[1 - 4]	$1.27 \times$	28.05
[1-5]	$1.36 \times$	27.82
[1-6]	$1.45 \times$	28.00

Table 15: Layer Evaluation of Encoder with EMHAImplementation. "1" indicates the bottom layer.

ResultsWe exhibit the ACC, AUROC, SEN and1192SPE of different models in Table 14. We can see1193that both BrainNetEITF and BrainNetEEITF can1194outperform all the baselines in terms of all met-1195rics. Similarly, thanks to little increased parame-1196ters of our models, we can conclude that they have1197stronger expressiveness and can be easily extended1198to other scenarios.1199

# H Further Analyses

# H.1 Effect of Number of EIT Layers

Recent researches (Shi et al., 2016; Peters et al.,12022018; Hao et al., 2019) has demonstrated that various layers in the encoder of a model have a ten-1203

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Figure 8: The comparison of BLEU against different hyper-parameters. Note that the blue horizontal line represents the performance of Transformer.



Figure 9: Quantitative analysis on localness in attention maps on En-De task (Above) and CNN-DailyMail task (Bottom).

dency to capture distinct syntax and semantic fea-1205 tures. Consequently, each layer may have different 1206 requirements for promoting agreement among the 1207 representations. In light of this, we examine the 1208 impact of consensus on different layers. The results 1209 on the En-De task are presented in Tables 15. The 1210 lowest layer clearly benefits from a higher degree 1211 of consensus compared to other layers, consistent 1212 with prior research (Shleifer and Ott, 2022) indi-1213 cating the challenges of optimizing shallow layers 1214 within the pre-normalization paradigm. However, 1215 by employing the consensus strategy, we enhance 1216 the learning of representations in shallow layers, 1217 giving them a significant advantage. Additionally, 1218 it is observed that incorporating consensus into a 1219 small subset of all layers can also yield good results, e.g., 28.08. These findings suggest two insights: 1) 1221 Our EMHA is so powerful that can work well even 1222 only being applied to a small subset of all layers; and 2) more efficient utilization of consensus may 1224 achieve better performance whiling working more 1225 efficiently. 1226



Figure 10: Dynamics of attention map similarity.

# H.2 Dynamics of Attention Map Similarity during Computation

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Figure 10 exhibits the dynamics of attention map similarity for the EIT 48L model on the En-De test set. The similarity between attention maps initially decreases and then increases as the dual interactions progress. This pattern is attributed to the two stages of our approach. In the ISI phase, interactions are modeled within each group instead of the whole, generating representative attention maps. As these groups operate independently, the similarity among these representatives is lower. Subsequently, in the CSI phase, interactions occur among these representatives, resulting in the final attention maps. This CSI enhances similarity among the attention maps, achieving the consensus.