COLLABORATIVE DATA OPTIMIZATION

Anonymous authors

000

001 002 003

004

006 007

008 009

010

011

012

013

014

015

016

017

018

019

021 022 023

045

046

047

048

049

Paper under double-blind review

Abstract

Training efficiency plays a pivotal role in deep learning. This paper begins by analyzing current methods for enhancing efficiency, highlighting the necessity of optimizing targets, a process we define as *data optimization*. Subsequently, we reveal that current data optimization methods incur significant additional costs, e.g., human resources or computational overhead, due to their inherently sequential optimization process. To address these issues, we propose COOPT, a highly efficient, parallelized framework designed for collaborative data optimization. COOPT enables participants to independently optimize data subsets, ensuring that the overall performance, once these subsets are collected, remains *comparable* to the sequential optimization of the entire dataset, thus significantly reducing optimization costs for individual participants. Extensive experiments have been conducted on various real-world scenarios to demonstrate the effectiveness and efficiency of COOPT across various datasets and architectures ¹.

1 INTRODUCTION



Figure 1: A <u>Collaborative Data Optimization Framework COOPT</u>. In practical scenarios involving opensource, large-scale unlabeled datasets, direct utilization via self-supervised learning results in O low training efficiency (Wang et al., 2021). Therefore, we propose COOPT, an O efficient and parallel framework enabling participants to utilize diverse task-agnostic models, such as pre-trained ResNets (He et al., 2016), termed *prior models*, for collaborative data optimization. These prior models can be sourced from internet resources, human expertise, or models trained on the participants' own datasets.

 Deep learning has achieved remarkable success across various domains, primarily due to the availability of large-scale, high-quality datasets (Song et al., 2020; Yang et al., 2023). However, despite the abundance of data in the era of big data, a significant portion remains unlabeled (Lei & Tao, 2023).

¹Our code is provided in the Supplementary Materials and will be publicly accessible.

054 Table 1: Properties of Various Data Utilization Methods. 'Optimize D_X ' and 'Optimize D_Y ' indicate whether 055 they are optimized. 'SSL' denotes self-supervised learning, 'HA' is human annotation, 'KD' is knowledge distillation, and 'DD' is dataset distillation. 'c' denotes the training cost associated with standard supervised learning that employs human-labeled data. '-' is not computable as it is associated with human. 057

Method	Method		mize D _Y	Efficie Data Optimization	ncy Model Training	Cost Analysis	Total Efficiency
Original	SSL	×	X	0	$(\geq 2\mathbf{c})$	Extensive Computation	8
Data Optimization Methods	HA KD DD	× × ✓	\ \ \	$\begin{vmatrix} & \textcircled{o} & (-) \\ & \textcircled{o} & (\ge \mathbf{c}) \\ & \textcircled{o} & (\ge \mathbf{c}) \end{vmatrix}$	 (= c) (< c) (< c) 	Human Annotation Task-specific Teacher Models Task-specific Pre-trained models	ଚ ଚ ଚ
COOPT (C)ur)	X	1	😌 (< c)	😂 (< c)	Various Prior Models	8

Self-supervised learning (Chen et al., 2020b) is proposed to exploit intrinsic relationships within large volumes of unlabeled data to learn meaningful representations. While it reduces dependency on 068 labels, training on such extensive datasets demands considerable computational resources, posing 069 significant computational challenges and diminishing training efficiency (Sun et al., 2024a).

To efficiently leverage unlabeled data, a straightforward but labor-intensive method is through human 071 annotation, thereby transforming them into labeled data. To further enhance training efficiency, 072 methods such as knowledge distillation (Hinton, 2015) and dataset distillation (Wang et al., 2018) 073 have been proposed. Knowledge distillation innovatively leverages soft labels provided by a powerful 074 teacher model to improve the performance of a student model and expedite its training (Dong et al., 075 2023). Dataset distillation focuses on compressing the original dataset into a smaller subset, enabling a model trained on this distilled data to perform comparably to one trained on the full dataset, thus 076 significantly reducing computational costs. 077

078 The data utilization methods discussed above are summarized in Table 1. Essentially, compared 079 to the less efficient self-supervised learning methods, methods achieve higher efficiency by either optimizing targets D_Y through human annotation or pre-trained models (as in knowledge distillation), 081 or by optimizing both input data D_X and targets D_Y (as in dataset distillation). Notably, all these methods necessarily optimize targets D_Y , and we term this process as *data optimization*. 082

083 In this paper, we identify the inefficiency of conventional data optimization methods, which suffer 084 from a sequential optimization process with a time complexity ranging from $\mathcal{O}(|D_X|)$ to $\mathcal{O}(|D_X|^2)$, 085 as elaborated in Section 3.2. As a remedy, we propose COOPT, a highly efficient collaborative framework inspired by crowd-sourcing to achieve parallel data optimization. An overview of COOPT 087 is depicted in Figure 1, with detailed processes illustrated in Figure 2. 880

In summary, our contributions are threefold: 089

- 090 (a) We propose COOPT, a highly efficient and parallelized framework for collaborative data 091 optimization. This framework enables participants to independently optimize data subsets, 092 ensuring that when these subsets are collected, the overall performance is comparable to sequential optimization of the entire dataset. Therefore, COOPT significantly reduces optimization costs for each participant. 094
- (b) Within COOPT, we identify a critical issue: *Target Distribution Inconsistency*, as defined in 095 Section 3.4. This issue arises from the diverse prior models employed by participants, leading to 096 heterogeneity in the target distribution spaces. To address this challenge, we propose an effective 097 target alignment strategy, elaborated in Section 3.5. 098
 - (c) Extensive experiments have been conducted across a range of real-world scenarios, involving a variety of prior models trained on various datasets, architectures, and training paradigms. Notably, special cases are explored where human or significantly weak models are employed as prior models, verifying the robustness and flexibility of COOPT. These experiments consistently demonstrate that COOPT achieves superior effectiveness and efficiency across a range of scenarios.

2 **RELATED WORK**

104 105

099

100

101

102

103

067

This section first introduces low-efficiency self-supervised learning (Chen et al., 2020a) on unlabeled 106 data. Subsequently, it reviews existing high-efficiency methods for labeled data, specifically focusing 107 on Knowledge Distillation (Hinton, 2015) and Dataset Distillation (Wang et al., 2018).

108 2.1 LOW-EFFICIENCY SELF-SUPERVISED LEARNING FOR UNLABELED DATA

To eliminate the need for human annotation, self-supervised learning (Chen et al., 2020b) is proposed
 to exploit the intrinsic co-occurrence relationships within large volumes of unlabeled data to learn
 meaningful representations.

113 Instance-instance contrastive learning has demonstrated effectiveness across various visual classi-114 fication tasks. For example, InstDisc (Wu et al., 2018) introduces the concept of using instance 115 discrimination as a pretext task. Building on this, CMC (Tian et al., 2020) proposes to use multiple 116 views of an image as positive samples and take another one as the negative. MoCo (He et al., 2020) significantly increases the number of negative samples but utilizes a relatively simplistic strategy for 117 selecting positive samples. Subsequent methods, such as PIRL (Misra & Maaten, 2020), incorporated 118 jigsaw augmentations, and SimCLR (Chen et al., 2020a) highlights the importance of hard positive 119 sample strategies by introducing data augmentation. A notable advancement is BYOL (Grill et al., 120 2020), which discards negative sampling and surpasses the performance of SimCLR (Chen et al., 121 2020a). SimSiam (Chen & He, 2021) further investigates the necessity of negative sampling in 122 contrastive representation learning, achieving faster convergence. 123

Summary. These methods, although not reliant on human annotation, often come with high
 computational costs due to the need for large batch sizes or memory banks.

126 127 128

2.2 HIGH-EFFICIENCY DATA OPTIMIZATION METHODS FOR LABELED DATA

Knowledge distillation. Knowledge distillation (Hinton, 2015) innovatively employs soft labels generated by high-capacity teacher models to improve the performance of a student model. Many following works aim to enhance the use of soft labels for more effective knowledge transfer. WSLD (Zhou et al., 2021) analyzes soft labels and distributes different weights for them from a perspective of bias-variance trade-off. DKD (Zhao et al., 2022) decouples the logits and assigns different weights for the target and non-target classes. Moreover, several studies (Yim et al., 2017; Dong et al., 2023) have demonstrated that knowledge distillation can accelerate the optimization process during training.

135 **Dataset dstillation.** Dataset distillation (Wang et al., 2018) aims to learn a compact distilled dataset 136 that preserves the essential information in the large-scale original dataset, achieving comparable 137 performance to the original dataset with less training time. Current solutions can be categorized 138 based on their optimization mechanisms (Lei & Tao, 2023): meta-learning framework (Wang et al., 139 2018; Zhou et al., 2022), gradient matching (Zhao et al., 2020; Zhao & Bilen, 2021), distribution 140 matching (Zhao & Bilen, 2023; Yin et al., 2023), trajectory matching (Cazenavette et al., 2022; Guo 141 et al., 2024). Notably, RDED (Sun et al., 2024b) introduces an optimization-free paradigm, which 142 directly crops and selects realistic patches from the original data and then stitches the selected patches 143 into the new images as the distilled dataset.

Summary. Knowledge distillation enhances model training efficiency by optimizing targets D_Y , while dataset distillation optimizes both target D_Y and input data D_X . Despite their benefits, both approaches are computationally expensive as they require task-specific pre-trained models, which significantly reduces overall efficiency.

148 149 150

151

3 COLLABORATIVE DATA OPTIMIZATION FRAMEWORK COOPT

In this section, we begin by formally defining *data optimization* in Section 3.1. We then analyze and underscore the necessity of our collaborative data optimization framework COOPT in Section 3.2. Following this, we provide a comprehensive and detailed description of the proposed COOPT framework in Section 3.3. Furthermore, we identify the inherent challenge within this framework in Section 3.4 and present method designed to address the challenge in Section 3.5.

157 3.1 DATA OPTIMIZATION158

As illustrated in Table 1, we provide a comprehensive comparison of various unlabeled data utilization methods. Self-supervised learning (SSL), which operates without optimizing both targets and input data (indicated by X under 'Optimize D_X ' and 'Optimize D_Y '), is effective but often suffers from low efficiency due to the extensive computational resources required. 162 In contrast, methods that achieve higher efficiency typically involve optimizing data through different 163 strategies. For example, Human Annotation (HA) provides labeled data (indicated by \checkmark under 164 'Optimize D_Y ') and achieves high effectiveness and efficiency. However, this approach incurs 165 substantial costs in terms of human resources and time, making it impractical for large-scale datasets 166 or applications requiring rapid deployment. Knowledge distillation (KD) supplies soft labels by teacher models, resulting in high effectiveness and efficiency, yet requires additional computational 167 resources to train the teacher models. Thus, the data optimization process incurs a minimum cost of c 168 when only training a teacher model with standard supervised learning, where the cost is c. 169

Dataset Distillation (DD) further extends data optimization by simultaneously optimizing the input samples D_X and the targets D_Y . While DD can significantly improve efficiency during the training of new models due to the reduced dataset size, most DD methods rely on complex optimization procedures, such as trajectory matching (Guo et al., 2024), which require models trained on the original datasets to guide the distillation process. This reliance can offset the efficiency gains by introducing additional computational overhead.

Summary. Improving training efficiency necessitates to optimize targets.

178

179

181 182

183

185 186 187

188

189

190

195

196

197

200

201 202

203

204

205

206 207

208

209

210

215

We formally define *data optimization* as the process of optimizing the original dataset D to create an optimal dataset D'. The goal is to enable a model ϕ trained on D' to achieve comparable performance with *significantly fewer training steps* compared to training on the original dataset D.

Definition 1 (Data optimization). Data optimization aims to produce optimized data D' s.t.

 $\mathcal{L}(\phi_{\theta}, D', T') < \mathcal{L}(\phi_{\theta}, D, T) \quad \text{where} \quad T' < T \,, \tag{1}$

where \mathcal{L} is the loss function, T' and T denote the training steps required for D' and D, respectively, and $\boldsymbol{\theta}$ are the parameters of the neural network $\boldsymbol{\phi} : \mathbb{R}^m \to \mathbb{R}^n$.

3.2 WHY OUR COLLABORATIVE DATA OPTIMIZATION COOPT IS NECESSARY?

Proposition 1 (Data optimization with prior model ψ). Given samples $D_X = \{\mathbf{x}_i\}_{i=1}^{|D|}$ and an existing prior model $\psi : \mathbb{R}^m \to \mathbb{R}^l$, the objective of data optimization is assigning targets $D_Y = \{\mathbf{y}_i\}_{i=1}^{|D|}$ for the samples to create $D' = \{\mathbf{x}_i, \mathbf{y}_i\}_{i=1}^{|D|}$. We assigns a target \mathbf{y}_i for \mathbf{x}_i as:

$$D' = \{ (\mathbf{x}_i, \mathbf{y}_i) \mid \mathbf{y}_i = \mathbf{W} \boldsymbol{\psi}(\mathbf{x}_i), \forall \mathbf{x}_i \in D_X \},$$
(2)

where D_Y is the optimized targets, and $\psi(\mathbf{x}_i)$ represents the target of \mathbf{x}_i , which means the feature representation. $\mathbf{W} : \mathbb{R}^l \to \mathbb{R}^n$ denotes a random matrix designed to transform the feature vector $\psi(\mathbf{x}_i)$ from dimension l to n without loss of information (Matoušek, 2008). This transformation aligns the output dimension^a with that required by the model $\phi_{\theta} : \mathbb{R}^m \to \mathbb{R}^n$.

^{*a*}Here, *n* denotes the target dimensionality of ϕ_{θ} . In practice, each participant may produce targets of varying dimensions due to the use of different prior models. Therefore, to train the model ϕ_{θ} using the optimized data, we employ the random matrix **W** to transform all target vectors to a common dimensionality.

As we discussed above, existing data optimization methods incur substantial costs, as indicated by the 'Extra Cost' in Table 1. For example, most dataset distillation methods rely on bi-level optimization (Zhao et al., 2020; Kim et al., 2022; Liu et al., 2023), leading to a training cost of $\mathcal{O}(|D|^2)$, where |D| is the number of data samples. To alleviate this computational burden, a promising strategy is to partition the dataset into K splits, thereby reducing the computational cost to $\mathcal{O}(|D|^2/K)^2$. This approach incurs a key question:

How can we independently optimize each subset so that, when the subsets are combined, the overall performance is comparable to that achieved by optimizing the entire dataset as a whole?

Drawing inspiration from Sun et al. (2024a), which demonstrates that employing task-agnostic models for target assignment can accelerate training, we propose to split the data and then independently optimize the targets of each split. Consequently, when the optimized subsets are aggregated, the

²This outcome is obtained from $\mathcal{O}(|D|^2/K^2) \times K$, representing K times the processing time for a single partition $\mathcal{O}((|D|/K)^2)$.



Figure 2: Lifecycle of the proposed collaborative data optimization framework COOPT. The framework encompasses an open data platform and multiple participants, involving four key data operations.

combined targets are the same as those obtained by optimizing the whole dataset, thereby achieving comparable performance. Furthermore, if these K splits are processed in parallel, the computational cost can be further reduced to $\mathcal{O}(N^2/K^2)$. Therefore, **collaboration** among multiple participants becomes essential to distribute the computational burden and enhance computational efficiency. Formally, we define data optimization with a prior model ψ in each participant in Proposition 1.

234

227

228

229

230

231

232

233

235

3.3 OVERVIEW OF THE PROPOSED FRAMEWORK COOPT

COOPT is a collaborative and parallelized framework that comprises an open data platform and *K* participants, each equipped with a distinct prior model. Specifically, COOPT operates through the
 following four steps:

Step 1: Data distributing. The open data platform initiates the process by randomly partitioning the entire set of unlabeled data D into K non-overlapping subsets. Each participant then downloads one of these subsets from the platform, denoted as $D^{(k)}$, where k indicates the k-th participant.

Step 2: Data optimization. Participants optimize their respective datasets $D^{(k)} = {\mathbf{x}_i}_{i=1}^{|D^{(k)}|}$ using their local prior model ψ^k . This data optimization process, detailed in Section 3.2, yields optimized targets $D'^{(k)} = {\mathbf{x}_i, \mathbf{y}_i}_{i=1}^{|D^{(k)}|}$. However, due to the heterogeneity of prior models among participants, the optimized targets of all participants may exhibit significant variations, leading to divergence in the distribution of the targets. This issue, referred to as *target distribution inconsistency* (defined in Section 3.4), necessitates an alignment strategy to align the target distribution spaces across participants. We propose a solution to this challenge in Section 3.5.

Step ③: Data uploading. After optimization, participants upload their optimized datasets $D'^{(k)}$ back to the open data platform.

Step (4): Data merging. The platform aggregates all the optimized datasets received from the participants to form a consolidated dataset.

The proposed collaborative parallel process enables participants to independently optimize their subsets while ensuring consistency through the proposed alignment strategies. When combined, the overall results are *comparable* to that achieved by optimizing the entire dataset as a whole. Consequently, this approach markedly reduces individual data optimization costs and enhances data processing efficiency through parallel execution.

250 259 260

3.4 AN INHERENT CHALLENGE: TARGET DISTRIBUTION INCONSISTENCY

In our collaborative framework, each participant may employ a distinct prior model, leading to inconsistencies in the target distributions, as illustrated in Figure 4a. For example, participant 1 uses ResNet-18 for optimization, resulting in a target dimension of 512, while participant 2 utilizes ResNet-50, yielding a target dimension of 2,048. Such inconsistencies can negatively impact the generalization capabilities of models trained on the optimized data, as they prevent the models from learning representations that are uniformly representative of the overall data distribution.

Considering N participants, participant k uses an prior model $\psi^{(k)}$, resulting in a target distribution space $\mathcal{T}^{(k)}$. Target distribution inconsistency occurs when significant differences exist between these distributions $\mathcal{T}^{(k)}$. The formal definition of target distribution inconsistency is as follows: **Definition 2 (Target Distribution Inconsistency)**. Given a distance metric D_{TV} where $(\mathcal{T}^{(i)}, \mathcal{T}^{(j)}) \in [0, 1], \forall i, j, the global inconsistency <math>\mathscr{G}$ among K participants can be quantified as:

$$\mathscr{G}(\mathcal{T}^{(1)}, \mathcal{T}^{(2)}, ..., \mathcal{T}^{(K)}) = \frac{1}{\binom{N}{2}} \sum_{i=1}^{K-1} \sum_{j=i+1}^{K} \mathcal{D}_{\mathrm{TV}}(\mathcal{T}^{(i)}, \mathcal{T}^{(j)}),$$
(3)

where D_{TV} is the total variation distance (Verdú, 2014), *i* and *j* are participants, and $1/{\binom{K}{2}}$ is a normalization factor. Target distribution inconsistency exists when $I > \epsilon$, where $\epsilon \in (0, 1)$ is a predefined threshold.

3.5 AN EFFECTIVE STRATEGY: TARGET ALIGNMENT

In the previous section, we identified that the primary challenge arises from the heterogeneity of optimized target distributions across participants. To address this issue, a potential solution is to align the target distributions of all participants' prior models with that of the prior model producing the most optimal target distribution space, referred to as the *best prior model*. Such alignment can be achieved by utilizing an optimizable transformation matrix to map each participant's target distribution to that of the best prior model (Sun et al., 2024a). This alignment strategy ensures consistency across all optimized target distribution spaces.

In summary, *it is crucial to first effectively assess each participant's prior model quality and subsequently train the transformation matrix for alignment.*

A metric to quantify prior model quality. Drawing inspirations from Wang & Isola (2020), which proposes an optimizable metric a.k.a. *uniform value loss* to achieve feature uniformity on the hypersphere during training, we employ this metric to evaluate the quality of prior models. Specifically, each participant downloads a small shared dataset S_X from the platform and computes the uniformity value of their prior model on S_X . They then upload this value to the platform, enabling it to determine which participant possesses the best prior model. The uniform value is computed as:

$$\mathcal{V}_{\text{uniform}}(\boldsymbol{\psi}; S) \triangleq \log \mathbb{E}_{\mathbf{x}_i, \mathbf{x}_j \sim S} \left[e^{\tau \| \boldsymbol{\psi}(\mathbf{x}_i) - \boldsymbol{\psi}(\mathbf{x}_j) \|_2^2} \right],\tag{4}$$

where ψ is the prior model, τ is a hyper-parameter set as 2, consistent with Wang & Isola (2020).

A lower uniform value indicates a higher-quality prior model, which optimizes targets of superior quality. Extensive experiments in Figure 3c demonstrate a strong correlation between this metric and the performance of prior, thereby effectively assessing the quality of targets.

Alignment. Upon identifying the best prior model, all participants, excluding the best prior model itself, proceed to train an optimizable transformation matrix. Specifically, the participant owning the best prior model disseminates its optimized targets, denoted as S_Y^* , computed over the shared dataset S_X using prior model ψ^* , to facilitate the alignment of target distribution spaces for other participants. Subsequently, each participant k optimizes a lightweight transformation matrix, denoted as $\mathbf{T}^{(k)}$, on the shared dataset S_X . The optimization problem is defined as follows:

$$\mathbf{T}^{(k)} = \arg\min_{\mathbf{T} \in \mathbb{R}^{n \times n}} \{ \| \mathbf{T} \cdot \boldsymbol{\psi}^{(k)}(\mathbf{S}_X) - \mathbf{S}_Y^{\star} \|_2^2 \},$$
(5)

where S_X represents the matrix form of S_X , suitable for input into the network $\psi^{(k)}$, and S_Y^* also represents the matrix form of S_Y^* . After obtaining the transformation matrix $\mathbf{T}^{(k)}$, the participant can convert the optimized targets for its own data using this matrix: $D_Y^{(k)} = \mathbf{T}^{(k)} \cdot \psi^{(k)}(\mathbf{D}_X^{(k)})$, where $\mathbf{D}_X^{(k)}$ denotes the participant's subset, and $D_Y^{(k)}$ are the adjusted targets aligned with the best prior model's target distribution space. As illustrated in Figure 4b, the proposed alignment strategy effectively mitigates target distribution space inconsistency.

316 317

318

308 309

270

271

276

277

278 279

280

296 297

4 EXPERIMENTS

In this section, we outline the experimental setup and assess the performance of our proposed collaborative data optimization framework, COOPT, across various real-world scenarios, employing different datasets and architectures, as discussed in Section 4.2. Subsequently, we explore a continuous data optimization framework that allows the prior models of participants to evolve, thereby further optimizing the targets, as detailed in Section 4.3. Finally, we validate the effectiveness of the introduced uniform value metric and the target alignment strategy in Section 4.4.

324 4.1 EXPERIMENTAL SETUP

346

347

348

349

350

351

356

Datasets and Networks: We conduct experiments on both large-scale and small-scale datasets,
including Tiny-ImageNet (64 × 64) (Le & Yang, 2015), CIFAR-100 (Krizhevsky et al., 2009a) and
CIFAR-10 (32 × 32) (Krizhevsky et al., 2009b). Following previous self-supervised studies (He
et al., 2020; Chen et al., 2020a; Grill et al., 2020; Chen & He, 2021; Assran et al., 2023; Zhang et al.,
2024), we employ a range of model capacities backbone architectures to evaluate the generalizability
of our method, including ResNet-18, 50, 101 (He et al., 2016), ViT (Dosovitskiy et al., 2020).

Baselines: For the unlabeled data utilization, referring to a prior widely-used benchmark (Da Costa et al., 2022), we consider several state-of-the-art self-supervised methods as baselines for a broader practical impact, including: SimCLR (Chen et al., 2020a), BYOL (Grill et al., 2020), DINO (Caron et al., 2021), MoCo (He et al., 2020), SimSiam (Chen & He, 2021), and SwAV (Caron et al., 2020).

Evaluation and Metrics: Following previous benchmarks and research (He et al., 2020; Chen et al., 2020a; Grill et al., 2020; Chen & He, 2021), we evaluate the test accuracy (%) of all the trained models using offline linear probing strategy to reflect the representation ability of the trained models, and ensure a fair and comprehensive comparison with baseline approaches. Additionally, we measure the computational efficiency by evaluating the time cost (s).

Implementation details: In this study, we introduce a collaborative data optimization framework,
 COOPT, which involves an open data platform and multiple participants. In practical applications,
 each participant can use publicly pre-trained models or their own models directly as the prior model. To simulate the diversity of prior models in practical applications, we train multiple prior models for
 participants across three key dimensions:

- *Training Paradigm:* Models are trained using various paradigms, such as supervised learning and self-supervised learning. Specifically, for supervised learning, we employ cross-entropy loss, while for self-supervised learning, we primarily utilize the BYOL framework (Grill et al., 2020).
- *Prior Dataset:* These prior models of participants are trained on extensive and public datasets, including CIFAR-10/100, Tiny-ImageNet, and ImageNet-1k.
- Architecture: Popular architectures such as ResNet and Vision Transformer (ViT) are employed.

We train the 16 different models based on a widely recognized supervised learning and self-supervised learning open-source benchmark (Da Costa et al., 2022). For the model trained on optimized data, we use the AdamW optimizer, the same as baselines. The size of mini-batch is set as 128. For all experiments, we utilize three random seeds and report both the mean and variance of the results.

357 4.2 Comparison with the state-of-the-art methods

We evaluate our framework, COOPT, across various scenarios: (1) participants use a diverse range of prior models trained on different datasets, architectures, and training paradigms; (2) we specifically evaluate the robustness of our method when employing different prior datasets used for training prior models, as well as (3) varying scalar networks; (4) finally, we explore special cases involving human or weak models, particularly where there are resource-rich or resource-poor participants.

A Diverse Range of Prior Models. Given the diversity among participant models, we employ a
 comprehensive set of 16 models, as detailed in Section 4.1. These models are trained using various
 training paradigms, datasets, and architectures. Details of the training processes for these models
 are provided above. As presented in Table 2, it is evident that our method COOPT demonstrates
 superior performance and training efficiency compared to existing self-supervised learning methods.

- (a) In terms of performance, the proposed COOPT achieves results comparable to or exceeding state-of-the-art self-supervised learning techniques. For instance, it achieves an improvement of 3.3% over the leading self-supervised approach BYOL on Tiny-ImageNet. Notably, COOPT demonstrates more significant improvements on larger-scale datasets, such as Tiny-ImageNet, which is particularly advantageous given the current emphasis on large-scale data era.
- (b) Regarding training efficiency, COOPT demonstrates a substantial reduction in training costs across various datasets. In particular, on the large-scale Tiny-ImageNet dataset, COOPT achieves a training speed that surpasses BYOL and SwAV by a factor of approximately ×2.48 and ×1.94.
- **Diverse Prior Datasets.** In the last experiment, we employ prior models that have been pre-trained on a variety of datasets, some of which are congruent with the unlabeled training data, while others

378

379

380

381 382

390

391

392

397 398

407

408

413

Table 2: Comparison of COOPT with Various Self-Supervised Learning Methods Accuracy (%) and Training Time (s). Evaluations are conducted on four datasets: CIFAR-10 (CF-10), CIFAR-100 (CF-100), and Tiny-ImageNet (T-IN). The best results are highlighted in **bold**. ↑ indicates the *performance* improvement over the second-best results. × denotes the factor of *training speed* compared to the second-best results.

Dataset	Metric	BYOL	DINO	MoCo	SimCLR	SimSiam	SwAV	СоОрт
CF-10	Acc. (%) Time (s)	$ \begin{vmatrix} 82.8 \pm 0.1 \\ 1376.56 \end{vmatrix} $	$\begin{array}{c} 82.6 \pm 0.0 \\ 1457.22 \end{array}$	$\begin{array}{c} 82.9\pm0.1\\1349.56\end{array}$	$\begin{array}{c} 83.1 \pm 0.0 \\ 1114.81 \end{array}$	$\begin{array}{c} 79.0\pm0.0\\ 1090.79\end{array}$	$\begin{array}{c} 82.9\pm0.1\\1012.74\end{array}$	$\begin{array}{c} 83.5 \pm 0.1 \ (\uparrow 0.4) \\ 540.43 \ (\times \ 1.87) \end{array}$
CF-100	Acc. (%) Time (s)	$51.7 \pm 0.1 \\ 1406.17$	$\begin{array}{c} 51.0\pm0.0\\1419.69\end{array}$	$57.8\pm0.1\\1425.80$	$55.4 \pm 0.0 \\ 1103.45$	$\begin{array}{c} 44.6 \pm 0.1 \\ 1139.14 \end{array}$	$53.2 \pm 0.1 \\ 1072.44$	$59.4 \pm 0.0 ~(\uparrow 1.6) \\ 548.11 ~(\times 1.95)$
T-IN	Acc. (%) Time (s)	$ \begin{vmatrix} 43.9 \pm 0.2 \\ 7086.62 \end{vmatrix} $	$\begin{array}{c} 36.1 \pm 0.0 \\ 7030.90 \end{array}$	$\begin{array}{c} 42.4 \pm 0.2 \\ 7133.98 \end{array}$	$\begin{array}{c} 41.5 \pm 0.1 \\ 5621.33 \end{array}$	$\begin{array}{c} 40.8 \pm 0.0 \\ 5531.92 \end{array}$	$\begin{array}{c} 39.9 \pm 0.1 \\ 5540.96 \end{array}$	$\begin{array}{c} 47.2 \pm 0.1 \ (\uparrow \ 3.3) \\ 2852.6790 \ (\times \ 1.94) \end{array}$

Table 3: **Comparison of COOPT with BYOL Across Diverse Prior Datasets.** For instance, "CF-10 (P)" indicates participants' prior models are trained on CIFAR-10. **Bold** means the best results. <u>Underline</u> indicates the results when the prior dataset is identical to the training data. All models are based on ResNet-18 architectures.

Dataset	BYOL	Our COOPT (Diverse Prior Datasets)				
Duniser	(Baseline)	CF-10 (P)	CF-100 (P)	T-IN (P)	IN-1K (P)	
CF-10	82.8 ± 0.1	$86.6 \pm 0.0 (\uparrow 3.8)$	$80.9 \pm 0.0 (\downarrow 1.9)$	$81.6 \pm 0.1 (\downarrow 1.2)$	88.1 \pm 0.0 (\uparrow 5.3)	
CF-100	51.7 ± 0.3	$\overline{54.9 \pm 0.1}$ († 3.2)	$60.0 \pm 0.1 \ (\uparrow 8.3)$	$56.8 \pm 0.0 \ (\uparrow 5.1)$	$\textbf{63.7}\pm\textbf{0.0}~(\uparrow~\textbf{12.0})$	
T-IN	43.9 ± 0.2	$38.3\pm0.0(\downarrow5.6)$	$\overline{40.2\pm0.1~(\downarrow~3.7)}$	$\underline{49.0\pm0.0\ (\uparrow5.1)}$	$\textbf{55.8} \pm \textbf{0.1} ~(\uparrow \textbf{11.9})$	

are incongruent. We refer to these datasets as the *prior datasets*. To rigorously evaluate the influence
of these prior datasets, we perform an analysis across scenarios where the prior datasets used for
prior models either align with or differ from the unlabeled training dataset. For instance, in the
aligned scenario, the training dataset is CIFAR-10 (CF-10), and the prior models are also trained on
CIFAR-10 (CF-10 (P)). Conversely, in the divergent scenario, the training dataset remains CIFAR-10,
while the prior models are trained on CIFAR-100 (CF-100 (P)). We conduct experiments on four
public datasets, with results detailed in Table 3.

(a) Prior models trained on the same dataset as the training data can yield significant improvements.

(b) For complex training datasets, using simpler prior datasets may degrade performance compared to BYOL, as they provide less informative guidance.

(c) However, for all unlabeled training datasets, employing prior models trained on ImageNet-1K can result in substantial improvements, owing to their robust generalization capabilities. This is especially pertinent in practical applications, given that the majority of pre-trained models accessible in internet resources are derived from ImageNet-1K.

Diverse Architectures of Prior Models. To further verify the 414 robustness of COOPT across various prior model architectures, 415 we perform experiments on various datasets using a diverse 416 range of networks to train prior models. This includes large-417 scale networks such as ResNet-101 (He et al., 2016) and Swin-418 V2-Tiny (Liu et al., 2021), as well as smaller-scale networks 419 like ResNet-18 (He et al., 2016), EfficientNet-B0 (Tan & Le, 420 2019) and MobileNet-V2 (Sandler et al., 2018). The results, 421 presented in Table 4, demonstrate that COOPT consistently 422 achieves superior performance across various architectures.

423 Extreme Cases of Prior Models: Human or 424 **Weak.** In real-world applications, extreme cases 425 arise due to the varying capabilities of participants. 426 For example, some participants have extensive re-427 sources and employ human annotators for labeling, 428 while others may have limited resources and rely 429 on weak models with inferior performance and generalization abilities. In our experiments, we define 430 weak models as those trained during intermediate 431 stages that are even far from convergence.

Table 4: Comparison of COOPT with BYOL Across Diverse Architectures of Prior Models. We use both largescale and small-scale networks for prior models. Bold means the best results.

Dataset	BYOL	COOPT
CF-10 CF-100 T-IN	$ \begin{vmatrix} 82.8 \pm 0.1 \\ 57.4 \pm 0.1 \\ 43.9 \pm 0.2 \end{vmatrix} $	$\begin{array}{c} 87.5\pm 0.2\\ 63.8\pm 0.1\\ 55.7\pm 0.1\end{array}$

 Table 5: Comparison of COOPT with BYOL in

 Presence of Human or Weak Prior Models.

	Prior M	lodels	Dataset		
Method	Human	Weak	CF-10	CF-100	
BYOL	-	-	82.8 ± 0.1	57.4 ± 0.1	
СоОрт	X X V	× ✓ ×	$\begin{array}{c} 83.5 \pm 0.1 \\ 83.3 \pm 0.1 \\ \textbf{86.7} \pm \textbf{0.0} \end{array}$	$\begin{array}{c} 59.4 \pm 0.0 \\ 58.7 \pm 0.1 \\ \textbf{61.0} \pm \textbf{0.0} \end{array}$	



442 443

444

445

446

447 448

449

450

(a) Training curves.

Figure 3: (a) Training curves of various self-supervised learning methods, including our proposed COOPT. It is evident that our COOPT demonstrates superior performance compared to the other methods. (b) Practical Scenario: The prior models of each participant experience temporal evolution, leading to improved target quality across multiple rounds. (c) Correlation Verification: Examine the relationship between the uniform value and performance, which demonstrates a strong negative correlation, quantified by $\rho = -0.9714$.

To simulate the conditions, in addition to the 16 diverse prior models detailed in Section 4.1, we incorporate 10 prior models, either human or weak models. The results, presented in Table 5, clearly indicate that our method, COOPT, maintains robustness despite the incorporation of weak models. Furthermore, the integration of high-capacity human models leads to significant improvements.

451 452 453

454

473

484

485

CONTINUOUS DATA OPTIMIZATION 4.3

We explore another practical scenario where the prior models of each participant experience temporal 455 evolution. For instance, an initially prior model of a participant, such as ResNet-18, may be evolved 456 to a higher-capacity model like ResNet-50 as the participant's resources improve. Consequently, 457 within COOPT, data optimization can be a continuous process. 458

459 We simulate this scenario by conducting experiments where, in each interaction round between the 460 platform and participants, 20% of the participants randomly update their model architectures to reflect 461 an increase in model capacity. The training curves across 10 rounds on CIFAR-100 are depicted in Figure 3b. The results have demonstrated that in COOPT, as the prior models evolve, the quality 462 of the targets improves, thereby facilitating continuous optimization. In particular, compared to the 463 baseline BYOL, these improvements can achieve an enhancement of 11.6%. 464

465 4.4 ABLATION STUDY 466

467 Effectiveness of Uniform Value. To evaluate the effectiveness of uniform value in estimating the 468 quality of prior models, we employ a diverse set of prior models, calculating both their uniform value 469 and test accuracy. We employ the Spearman rank correlation coefficient³ ρ (Zar, 2014) to quantify 470 the association between Uniform Value and accuracy. As illustrated in Figure 3c, the Spearman rank 471 correlation coefficient is $\rho = -0.9714$, indicating a strong correlation between uniform value and 472 model performance, thereby effectively assessing the quality of prior models.

474 Target Distribution Alignment. In real-world applications, participants often employ diverse prior 475 models, which results in target distribution space inconsistencies, as demonstrated in Figure 4a. We conduct an ablation study w/o alignment and w/ alignment to verify the importance of target 476 distribution space alignment, and the training curves presented in Figure 4d. 477

478 (a) Compared to without alignment (green line), our proposed approach (blue line) yields a perfor-479 mance improvement of 16.9%, which highlights the critical importance of aligning the target 480 distribution space. Notably, the training curve without alignment (green line) initially ascends 481 before declining, suggesting that during the early phase of model training, optimizing the target leads to performance enhancement. However, as training continues, the severely inconsistent 482 targets significantly degrade model performance. 483

³The formula is: $\rho = 1 - \frac{6 \sum d_i^2}{n(n^2 - 1)}$, where d_i represents the difference between the ranks of each pair of observations and n denotes the number of observations.



Figure 4: (a), (b), (c): Visualization of t-SNE for optimized targets generated by two distinct models (BYOL (acc. = 82%) and SupCE (acc. = 90%).). Aligning to the worse model (c) results in diminished target quality. (d) Training curves with and without alignment, demonstrating the importance of alignment.

- (b) Furthermore, we compare our alignment strategy, which aligns to the best prior model, with two other straightforward strategies: aligning to a medium prior model (purple line) and aligning to the worse prior model (red line). It is evident that all three alignment strategies outperform the scenario without alignment, and *aligning to the best prior model provides the most significant performance gains.*
- (c) To further analyze the underlying reasons, we employ t-SNE visualization. Notably, a comparison between alignment with the better participant (Figure 4b) and the worse participant (Figure 4c) reveals that alignment with a worse-quality model diminishes the representative capability of the targets. This, in turn, results in less effective guidance for model training.

Influence of Shared Unlabeled Data Size. The shared 508 unlabeled data S is employed to estimate the uniform 509 value and compute the transformation matrix necessary 510 for target alignment, as detailed in Section 3.5. To ex-511 plore the influence of the size of shared unlabeled data, we 512 conduct experiments on both CIFAR-10 and CIFAR-100 513 datasets, varying the size of the shared data in proportions 514 of $\{0.01, 0.05, 0.1, 0.2, 0.4, 0.6, 0.8\}$ relative to the origi-515 nal dataset. The results are presented in Figure 5. It is observed that as the size of the shared data increases, per-516 formance gains become marginal. Specifically, increasing 517 the proportion of data from 0.01% to 0.05% results in im-518 provements of 2.4% and 2.5% for CIFAR-10 and CIFAR-519 100, respectively. However, increasing from 0.05% to 520 0.8% This suggests that a small-sized shared unlabeled 521 dataset is adequate for accurate uniform value estimation 522 and the computation of the transformation matrix. 523

Figure 5: **Influence of shared data size.** As the size of the shared data increases, the performance gains diminish A small dataset size is sufficient to estimate uniform value and compute the transformation matrix.

5 CONCLUSION AND FUTURE WORK

526 **Conclusion.** In this paper, we introduce COOPT, an efficient and highly parallelized framework 527 for collaborative data optimization. This framework enables participants to independently optimize 528 data subsets such that, when aggregated, the overall performance is comparable to that achieved by 529 sequentially optimizing the entire dataset. Consequently, COOPT significantly reduces individual data 530 optimization costs. Within COOPT, we identify a critical issue: Target Distribution Inconsistency, 531 which arises from the diversity of prior models used in data optimization. To mitigate this, we propose 532 an effective target alignment strategy. Extensive experiments conducted across various real-world 533 scenarios demonstrate the superior effectiveness and efficiency of the COOPT framework across 534 diverse datasets and architectures.

535

524

525

495

496

497 498

499

500

501

502

504

505

506 507

Future Work. In future work, we intend to (1) conduct an in-depth exploration of iterative data optimization through multiple rounds, enabling more dynamic collaboration among participants.
(2) Furthermore, we aim to examine additional practical scenarios, such as participants optimizing their local data and then uploading it to the platform. This paradigm is anticipated to broaden the platform's functionalities, thereby increasing its applicability to real-world applications.

540 REFERENCES 541

542 543 544 545	Mahmoud Assran, Quentin Duval, Ishan Misra, Piotr Bojanowski, Pascal Vincent, Michael Rabbat, Yann LeCun, and Nicolas Ballas. Self-supervised learning from images with a joint-embedding predictive architecture. In <i>Proceedings of the IEEE/CVF Conference on Computer Vision and</i> <i>Pattern Recognition</i> , pp. 15619–15629, 2023.
546 547 548	Mathilde Caron, Ishan Misra, Julien Mairal, Priya Goyal, Piotr Bojanowski, and Armand Joulin. Unsupervised learning of visual features by contrasting cluster assignments. <i>Advances in neural</i> <i>information processing systems</i> , 33:9912–9924, 2020.
549 550 551 552	Mathilde Caron, Hugo Touvron, Ishan Misra, Herve Jegou, Julien Mairal, Piotr Bojanowski, and Armand Joulin. Emerging properties in self-supervised vision transformers. In <i>Proceedings of the IEEE/CVF international conference on computer vision</i> , pp. 9650–9660, 2021.
553 554 555	George Cazenavette, Tongzhou Wang, Antonio Torralba, Alexei A Efros, and Jun-Yan Zhu. Dataset distillation by matching training trajectories. In <i>Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition</i> , pp. 4750–4759, 2022.
556 557 558	Ting Chen, Simon Kornblith, Mohammad Norouzi, and Geoffrey Hinton. A simple framework for contrastive learning of visual representations. In <i>International conference on machine learning</i> , pp. 1597–1607. PMLR, 2020a.
559 560 561	Ting Chen, Simon Kornblith, Mohammad Norouzi, and Geoffrey Hinton. A simple framework for contrastive learning of visual representations. In <i>ICML</i> , 2020b.
562 563	Xinlei Chen and Kaiming He. Exploring simple siamese representation learning. In <i>Proceedings of the IEEE/CVF conference on computer vision and pattern recognition</i> , pp. 15750–15758, 2021.
564 565 566	Victor Guilherme Turrisi Da Costa, Enrico Fini, Moin Nabi, Nicu Sebe, and Elisa Ricci. solo-learn: A library of self-supervised methods for visual representation learning. <i>Journal of Machine Learning Research</i> , 23(56):1–6, 2022.
567 568 569 570	Peijie Dong, Lujun Li, and Zimian Wei. Diswot: Student architecture search for distillation without training. 2023 IEEE/CVF Conference on Computer Vision and Pattern Recognition (CVPR), pp. 11898–11908, 2023. doi: 10.1109/CVPR52729.2023.01145.
571 572 573 574	Alexey Dosovitskiy, Lucas Beyer, Alexander Kolesnikov, Dirk Weissenborn, Xiaohua Zhai, Thomas Unterthiner, Mostafa Dehghani, Matthias Minderer, Georg Heigold, Sylvain Gelly, et al. An image is worth 16x16 words: Transformers for image recognition at scale. <i>arXiv preprint arXiv:2010.11929</i> , 2020.
575 576 577 578	Jean-Bastien Grill, Florian Strub, Florent Altché, Corentin Tallec, Pierre Richemond, Elena Buchatskaya, Carl Doersch, Bernardo Avila Pires, Zhaohan Guo, Mohammad Gheshlaghi Azar, et al. Bootstrap your own latent-a new approach to self-supervised learning. <i>Advances in neural information processing systems</i> , 33:21271–21284, 2020.
579 580 581	Ziyao Guo, Kai Wang, George Cazenavette, Hui Li, Kaipeng Zhang, and Yang You. Towards lossless dataset distillation via difficulty-aligned trajectory matching. In <i>International Conference on Learning Representations</i> , 2024.
583 584 585	Kaiming He, Xiangyu Zhang, Shaoqing Ren, and Jian Sun. Deep residual learning for image recognition. In <i>Proceedings of the IEEE conference on computer vision and pattern recognition</i> , pp. 770–778, 2016.
586 587 588	Kaiming He, Haoqi Fan, Yuxin Wu, Saining Xie, and Ross Girshick. Momentum contrast for unsupervised visual representation learning. In <i>Proceedings of the IEEE/CVF conference on computer vision and pattern recognition</i> , pp. 9729–9738, 2020.
589 590 591	Geoffrey Hinton. Distilling the knowledge in a neural network. <i>arXiv preprint arXiv:1503.02531</i> , 2015.
592 593	Jang-Hyun Kim, Jinuk Kim, Seong Joon Oh, Sangdoo Yun, Hwanjun Song, Joonhyun Jeong, Jung- Woo Ha, and Hyun Oh Song. Dataset condensation via efficient synthetic-data parameterization. In <i>International Conference on Machine Learning</i> , pp. 11102–11118. PMLR, 2022.

594 595 596	Alex Krizhevsky, Geoffrey Hinton, et al. Learning multiple layers of features from tiny images. 2009a.
597 598	Alex Krizhevsky, Vinod Nair, and Geoffrey Hinton. Cifar-10 and cifar-100 datasets. URI: https://www. cs. toronto. edu/kriz/cifar. html, 6(1):1, 2009b.
599	Ya Le and Xuan Yang. Tiny imagenet visual recognition challenge. CS 231N, 7(7):3, 2015.
600 601 602	Shiye Lei and Dacheng Tao. A comprehensive survey of dataset distillation. <i>IEEE Transactions on</i> Pattern Analysis and Machine Intelligence 2023
603 604	Yanqing Liu, Jianyang Gu, Kai Wang, Zheng Zhu, Wei Jiang, and Yang You. Dream: Efficient dataset distillation by representative matching. <i>arXiv preprint arXiv:2302.14416</i> , 2023.
605 606 607 608	Ze Liu, Yutong Lin, Yue Cao, Han Hu, Yixuan Wei, Zheng Zhang, Stephen Lin, and Baining Guo. Swin transformer: Hierarchical vision transformer using shifted windows. In <i>Proceedings of the</i> <i>IEEE/CVF international conference on computer vision</i> , pp. 10012–10022, 2021.
609 610 611	Jiří Matoušek. On variants of the johnson–lindenstrauss lemma. <i>Random Structures & Algorithms</i> , 33(2):142–156, 2008.
612 613 614	Ishan Misra and Laurens van der Maaten. Self-supervised learning of pretext-invariant representations. In <i>Proceedings of the IEEE/CVF conference on computer vision and pattern recognition</i> , pp. 6707–6717, 2020.
615 616 617 618	Mark Sandler, Andrew Howard, Menglong Zhu, Andrey Zhmoginov, and Liang-Chieh Chen. Mo- bilenetv2: Inverted residuals and linear bottlenecks. In <i>Proceedings of the IEEE conference on</i> <i>computer vision and pattern recognition</i> , pp. 4510–4520, 2018.
619 620 621	Hwanjun Song, Minseok Kim, Dongmin Park, Yooju Shin, and Jae-Gil Lee. Learning from noisy labels with deep neural networks: A survey. <i>IEEE Transactions on Neural Networks and Learning</i> <i>Systems</i> , 34:8135–8153, 2020. doi: 10.1109/TNNLS.2022.3152527.
622 623 624	Peng Sun, Yi Jiang, and Tao Lin. Efficiency for free: Ideal data are transportable representations. <i>arXiv preprint arXiv:2405.14669</i> , 2024a.
625 626	Peng Sun, Bei Shi, Daiwei Yu, and Tao Lin. On the diversity and realism of distilled dataset: An efficient dataset distillation paradigm. In <i>CVPR</i> , 2024b.
628 629	Mingxing Tan and Quoc Le. Efficientnet: Rethinking model scaling for convolutional neural networks. In <i>International conference on machine learning</i> , pp. 6105–6114. PMLR, 2019.
630 631 632 633	Yonglong Tian, Dilip Krishnan, and Phillip Isola. Contrastive multiview coding. In Computer Vision–ECCV 2020: 16th European Conference, Glasgow, UK, August 23–28, 2020, Proceedings, Part XI 16, pp. 776–794. Springer, 2020.
634 635	Sergio Verdú. Total variation distance and the distribution of relative information. In 2014 information theory and applications workshop (ITA), pp. 1–3. IEEE, 2014.
636 637 638 639	Guangrun Wang, Keze Wang, Guangcong Wang, Philip H. S. Torr, and Liang Lin. Solving inefficiency of self-supervised representation learning. 2021 IEEE/CVF International Conference on Computer Vision (ICCV), pp. 9485–9495, 2021.
640 641 642	Tongzhou Wang and Phillip Isola. Understanding contrastive representation learning through alignment and uniformity on the hypersphere. In <i>International conference on machine learning</i> , pp. 9929–9939. PMLR, 2020.
643 644 645	Tongzhou Wang, Jun-Yan Zhu, Antonio Torralba, and Alexei A Efros. Dataset distillation. <i>arXiv</i> preprint arXiv:1811.10959, 2018.
646 647	Zhirong Wu, Yuanjun Xiong, Stella X Yu, and Dahua Lin. Unsupervised feature learning via non- parametric instance discrimination. In <i>Proceedings of the IEEE conference on computer vision</i> <i>and pattern recognition</i> , pp. 3733–3742, 2018.

648 649 650	Weikai Yang, Yukai Guo, Jing Wu, Zheng Wang, Lan-Zhe Guo, Yu-Feng Li, and Shixia Liu. Interactive reweighting for mitigating label quality issues. <i>IEEE transactions on visualization and computer graphics</i> , PP, 2023. doi: 10.1109/TVCG.2023.3345340.
651 652 653	Junho Yim, Donggyu Joo, Jihoon Bae, and Junmo Kim. A gift from knowledge distillation: Fast optimization, network minimization and transfer learning. In <i>Proceedings of the IEEE conference on computer vision and pattern recognition</i> , pp. 4133–4141, 2017.
655 656	Zeyuan Yin, Eric Xing, and Zhiqiang Shen. Squeeze, recover and relabel: Dataset condensation at imagenet scale from a new perspective. <i>Advances in Neural Information Processing Systems</i> , 2023.
657 658 659	Jerrold H Zar. Spearman rank correlation: overview. Wiley StatsRef: Statistics Reference Online, 2014.
660 661 662 663	Kexin Zhang, Qingsong Wen, Chaoli Zhang, Rongyao Cai, Ming Jin, Yong Liu, James Y Zhang, Yuxuan Liang, Guansong Pang, Dongjin Song, et al. Self-supervised learning for time series analysis: Taxonomy, progress, and prospects. <i>IEEE Transactions on Pattern Analysis and Machine Intelligence</i> , 2024.
664 665 666	Bo Zhao and Hakan Bilen. Dataset condensation with differentiable siamese augmentation. In <i>International Conference on Machine Learning</i> , pp. 12674–12685. PMLR, 2021.
667 668	Bo Zhao and Hakan Bilen. Dataset condensation with distribution matching. In <i>Proceedings of the IEEE/CVF Winter Conference on Applications of Computer Vision</i> , pp. 6514–6523, 2023.
669 670 671	Bo Zhao, Konda Reddy Mopuri, and Hakan Bilen. Dataset condensation with gradient matching. <i>arXiv preprint arXiv:2006.05929</i> , 2020.
672 673 674	Borui Zhao, Quan Cui, Renjie Song, Yiyu Qiu, and Jiajun Liang. Decoupled knowledge distillation. In <i>Proceedings of the IEEE/CVF Conference on computer vision and pattern recognition</i> , pp. 11953–11962, 2022.
675 676 677	Helong Zhou, Liangchen Song, Jiajie Chen, Ye Zhou, Guoli Wang, Junsong Yuan, and Qian Zhang. Rethinking soft labels for knowledge distillation: A bias-variance tradeoff perspective. arXiv preprint arXiv:2102.00650, 2021.
679 680 681	Yongchao Zhou, Ehsan Nezhadarya, and Jimmy Ba. Dataset distillation using neural feature regression. <i>Advances in Neural Information Processing Systems</i> , 35:9813–9827, 2022.
682 683 684	
685 686 687	
688 689	
690 691 692	
693 694	
695 696 697	
698 699	
700 701	