# Teaching Language Models to Self-Improve through Interactive Demonstrations

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#### Abstract

 The self-improving ability of large language models (LLMs), enabled by prompting them to analyze and revise their own outputs, has garnered significant interest in recent research. However, this ability has been shown to be absent and difficult to learn for smaller mod- els, thus widening the performance gap be- tween state-of-the-art LLMs and more cost- effective and faster ones. To reduce this gap, we introduce TRIPOST, a training algorithm 011 that endows smaller models with such self- improvement ability, and show that our ap- proach can improve LLaMA-7B's performance 014 on math and reasoning tasks by up to 7.13%. In contrast to prior work, we achieve this by 016 using the smaller model to interact with LLMs to collect feedback and improvements on *its own generations*. We then replay this experi- ence to train the small model. Our experiments on four math and reasoning datasets show that the interactive experience of learning from and correcting its *own* mistakes is crucial for small models to improve their performance.

### <span id="page-0-2"></span>024 1 Introduction

 [L](#page-10-1)arge language models [\(OpenAI,](#page-10-0) [2023;](#page-10-0) [Ouyang](#page-10-1) [et al.,](#page-10-1) [2022\)](#page-10-1) together with techniques such as few- shot prompting [\(Brown et al.,](#page-8-0) [2020\)](#page-8-0) and Chain-of- [T](#page-9-0)hought (CoT) prompting [\(Wei et al.,](#page-11-0) [2023;](#page-11-0) [Ko-](#page-9-0) [jima et al.,](#page-9-0) [2023\)](#page-9-0) have been shown to be effective in achieving strong performance on various down- stream language tasks. More recently, a new way to adapt LLMs to downstream tasks has captured the attention of many researchers, namely to further enhance the LLM's downstream task performance by asking the LLM to provide feedback on its own generations and then use the feedback to revise its [o](#page-10-2)utputs [\(Bai et al.,](#page-8-1) [2022;](#page-8-1) [Huang et al.,](#page-9-1) [2023;](#page-9-1) [Peng](#page-10-2) [et al.,](#page-10-2) [2023a;](#page-10-2) [Shinn et al.,](#page-10-3) [2023\)](#page-10-3). This process is often called "self-improvement", and has proven to be an effective technique to make the LLM's gener-ations more diverse, more precise, or more faithful

<span id="page-0-1"></span>

Figure 1: Compared to LLMs, smaller models have difficulty performing self-improvement on math or logical tasks, such as Multistep Arithmetics and Logical Deduction from the Big-Bench. *+ft*: finetuned on groundtruth rationales; *+SI. prompt*: prompted to perform self-improvement; *+ft SI. demo* further finetuned *+ft* on LLM self-improvement demonstrations.

## to a given piece of knowledge [\(Schick et al.,](#page-10-4) [2022;](#page-10-4) **042** [Madaan et al.,](#page-9-2) [2023;](#page-9-2) [Peng et al.,](#page-10-2) [2023a\)](#page-10-2). **043**

However, [Saunders et al.](#page-10-5) [\(2022\)](#page-10-5); [Huang et al.](#page-9-1) **044** [\(2023\)](#page-9-1) found that the ability to generate critical **045** feedback or to self-improve is hardly evident in **046** smaller models<sup>[1](#page-0-0)</sup>. Similarly, [Ye et al.](#page-11-1) [\(2023\)](#page-11-1) found 047 that fine-tuning smaller models (e.g. 7-13B) with **048** self-improvement demonstrations from LLMs can **049** still fail on tasks such as math, reasoning, and **050** factuality. Following these previous works, we **051** performed a similar study on two math and rea- **052** soning tasks in [Figure 1.](#page-0-1) We compared the accu- **053** racy of the final answer generated by prompting **054** a 175B Codex [\(Chen et al.,](#page-8-2) [2021\)](#page-8-2) to self-improve, **055** with prompting or training a LLaMA-7B model to  $056$ 

<span id="page-0-0"></span> $1$ The distinction between small and large language models is often context-dependent [\(Saunders et al.,](#page-10-5) [2022\)](#page-10-5). In this work, we denote "small models" to those with a few billion parameters (e.g., LLaMA-7B), and LLMs as those scaled to hundreds of billions of parameters (e.g., ChatGPT).

<span id="page-1-0"></span>

Method	Codex (175B)	$LLaMA+ft(7B)$
Input		$Q: ((4 - 0 * -1 * 8 + 6) + (0 + 4 + 9 * 5 * -2)) =$
Attempt:	(1) This equation can be written as " $(A + B)$ " (2) Let's calculate A= $(4 - 0 * -1 * 8 + 6)$ $=(4-(0*-1*8)+6)$ $=(4-(0+6))$ $=(4-6)$ $= -2$ (3) Let's calculate B= $(0 + 4 + 9 * 5 * -2)$ $=(0 + 4 + (9 * 5 * -2))$ $=(0 + 4 + (-90))$ $= -86$ (4) Then, the final eq is $(A + B) = (-2 + -86) = -88$ . (Final response) So the answer is -88.	(1) This equation can be written as " $(A + B)$ " (2) Let's calculate A= $(4 - 0 * -1 * 8 + 6)$ $=(4-(0*-1*8)+6)$ $=(4-(0+8)+6)$ $=(4-8+6)$ $=2$ (3) Let's calculate B= $(0 + 4 + 9 * 5 * -2)$ $=(0+(4+(9*5)))$ $=(0+(13))$ $=13$ (4) Then, the final eq is $(A + B) = (2 + 13) = 15$ . (Final response) So the answer is 15.

Table 1: Training smaller models using self-improvement demonstrations from LLMs can be ineffective, as models of different sizes make different types and amount of mistakes (highlighted in red). Small models can make simple copying errors, while LLMs can make other arithmetic errors, such as not switching plus or minus signs when adding parentheses. See [Appendix B](#page-12-0) for a more quantitative analysis.

 [s](#page-11-1)elf-improve using demonstrations from Codex [\(Ye](#page-11-1) [et al.,](#page-11-1) [2023\)](#page-11-1). In [Figure 1,](#page-0-1) we surprisingly find that *smaller models performed worse* using prior self- improvement-related methods than simply training on ground-truth step-by-step rationales (*+ft*). By comparing the generated solutions from Codex- 175B and LLaMA-7B, we find that smaller models, 064 such as LLaMA-7B, not only make more mistakes, but also *different types of mistakes* compared to an 066 LLM [\(Table 1](#page-1-0) and [Appendix B\)](#page-12-0). Due to the smaller model's weaker math and reasoning ability, we believe training on LLM self-improvement demon- strations is less effective, as it forces the smaller model to learn from mistakes not of its own.

 Motivated by this finding, we propose TRIPOST, a training algorithm that can more effectively train a small model to learn from its mistakes, gen- erate feedback, and improve its performance on math and reasoning tasks. TRIPOST is an iter- ative algorithm consisting of three stages: Inter- active Trajectory Editing, Data Post-processing, and Model Training. Similar to the exploration stage in reinforcement learning, TRIPOST first cre- ates improvement demonstrations *using the small model to interact* with the expert LLMs or rele- vant Python scripts. Then, TRIPOST postprocesses the collected data by filtering out failed improve- ment attempts, and then re-balances the dataset to disincentivize the model from trying to self- "improve" when it is not needed. Finally, TRIPOST [r](#page-8-3)eplays the post-process dataset [\(Andrychowicz](#page-8-3) [et al.,](#page-8-3) [2018;](#page-8-3) [Schaul et al.,](#page-10-6) [2016\)](#page-10-6), and trains the smaller model using weighted supervised learn-ing. TRIPOST repeats entire the process several

times. We evaluate our approach on four maths **091** and reasoning datasets from the BIG-Bench Hard **092** [\(Suzgun et al.,](#page-10-7) [2022\)](#page-10-7) collection, and find that **093** TRIPOST-trained models can use its learned self- **094** improvement ability to improve their task perfor- **095** mance. We also find that TRIPOST-trained models **096** achieve better in-domain and out-of-domain perfor- **097** mance than models trained using just the ground 098 truth step-by-step rationales and trained using di- **099** rect LLM demonstrations [\(Saunders et al.,](#page-10-5) [2022;](#page-10-5) **100** [Ye et al.,](#page-11-1) [2023\)](#page-11-1). This paper makes the following 101 contributions: 102

- We illustrate how prior work [\(Saunders et al.,](#page-10-5) **103** [2022;](#page-10-5) [Ye et al.,](#page-11-1) [2023\)](#page-11-1) can be ineffective in **104** training smaller models to self-improve their **105** performance on math and reasoning tasks. **106**
- We propose TRIPOST, an iterative training **107** algorithm that trains a smaller language model **108** to learn to self-improve. **109**
- We show that TRIPOST-trained models **110** achieve better performance than models **111** trained using ground-truth rationales or us- **112** ing LLM demonstrations on four math and **113** reasoning datasets from BIG-Bench Hard. **114**

## 2 Approach **<sup>115</sup>**

TRIPOST is an algorithm that trains a small lan- **116** guage model to self-improve by learning from its **117** *own mistakes*. Each iteration of TRIPOST consists **118** of three stages. On a high level, we first collect **119** a set of improving trajectories by using a smaller **120** model  $M_\theta$  to interact with LLMs. We use  $M_\theta$  to **121** 

<span id="page-2-0"></span>

Figure 2: Overview of TRIPOST algorithm. TRIPOST consists of three stages: interactive trajectory editing where we use our FBK and IMP module to edit trajectories generated by a smaller model  $M_{\theta}$ ; data post-processing where we filter out erroneous trajectories and create a re-balanced dataset; and model training where we train  $M_\theta$  using weighted supervised learning on the post-processed dataset.

 generate initial attempts and then use a feedback module FBK and an improvement module IMP 124 to edit parts of the  $M_\theta$  generated attempts. This creates a trajectory that includes attempts gener- ated by the small model, with feedbacks and im- provements tailored to the small model's capability [\(Figure 2\)](#page-2-0). Next, we post-process the collected trajectories by 1) using scripts and other heuristics to filter out failed "improvement" attempts; and 2) re-balancing the dataset using both directly correct attempts and the improving trajectories. Finally, we use weighted supervised learning to train a smaller **model**  $M_\theta$  using the post-processed data.

**135** We provide an overview of our algorithm in [Fig-](#page-2-0)**136** [ure 2,](#page-2-0) and detail each of the three stages in [Sec-](#page-2-1)**137** [tion 2.2,](#page-2-1) [Section 2.3,](#page-3-0) and [Section 2.4,](#page-3-1) respectively.

## **138** 2.1 Notation

**139** We denote the entire attempt from a language **140** model to solve a given question as a trajectory x:

$$
x = (x^{\text{init}}, x_1^{\text{fb}}, x_1^{\text{up}}, x_2^{\text{fb}}, x_2^{\text{up}}, ..., x_m^{\text{fb}}),
$$

where  $x^{\text{init}}$  denotes the initial attempt, and  $x_i^{\text{fb}}, x_i^{\text{up}}$ i **142 143** denotes the i-th feedback and updated attempt, **144** respectively. Such a trajectory ends when the 145 **last feedback**  $x_m^{\text{fb}}$  contains the phrase "the final **146** response is correct". Therefore, *directly correct* trajectories take the form of  $x_{\checkmark} = (x^{\text{init}}, x_1^{\text{fb}}),$ **148** and *self-improving* trajectories take the form of  $x_{\text{SI}} = (x^{\text{init}}, x_1^{\text{fb}}, x_1^{\text{up}})$ 149  $x_{\text{SI}} = (x^{\text{init}}, x_1^{\text{fb}}, x_1^{\text{up}}, ..., x_m^{\text{fb}})$  where  $m > 1$ .

### <span id="page-2-1"></span>2.2 Interactive Trajectory Editing **150**

ther the difference of the control of the con In our prior study in [Figure 1](#page-0-1) and [Table 1,](#page-1-0) we find **151** that it is difficult to elicit a 7B model to perform **152** self-improvement due to its significantly weaker **153** math and reasoning capability compared to LLMs. **154** To address this issue, we use the smaller model  $M_{\theta}$  155 to first generate an initial attempt (and feedbacks or **156** improvements if  $M_\theta$  generates them), and then ap- 157 ply a feedback module FBK and an improvement **158** module IMP to *rewrite parts of the*  $M_\theta$  *trajecto-* 159 *ries*. Specifically, we first use FBK (prompting **160** text-davinci-003 or using a Python script) to gen- **161** erate a feedback  $x_i^{\text{fb}*}$  based on the first error step 162 it identified for each incorrect attempt. After that, **163** we edit the trajectory by replacing the first feed- 164 back that  $M_\theta$  and FBK disagree on with the FBK- 165 generated feedback, creating: **166**

$$
x_{\text{edited}} = (x^{\text{init}}, ..., x_{i-1}^{\text{up}}, x_i^{\text{fb}*}).
$$

**170**

Finally, we use our improvement module IMP 168 (prompting Codex) to generate an improved at- **169** tempt conditioned on the previous attempt  $x_i^{\text{up}}$ i−1 and feedback  $x_i^{\text{fb}*}$ , and append it to  $x_{\text{edited}}$ . We 171 repeat this process, up to a maximum number of **172** iterations, until the last attempt in  $x_{\text{edited}}$  is cor-  $173$ rect, and we discard  $x_{\text{edited}}$  that failed to reach the **174** correct answer. **175**

### <span id="page-3-0"></span>**176** 2.3 Data Post-processing

177 **After the interactive trajectory editing step, we have 178** three types of data: 1) gold step-by-step demonstra-179 tions  $x_{\text{gold}}$  for the task, 2) directly correct trajecto-180 ries  $x_{\ell}$  generated by  $M_{\theta}$ , and 3) edited trajectories 181  $x_{\text{edited}}$  created using  $M_{\theta}$ , FBK, and IMP.

 To make training easier, we first split *all data* **into triplets of** *single-step improvement*  $x_{\text{imp}} =$  $(x^{\text{att}}, x^{\text{fb}}, x^{\text{up}})$  if an attempt  $x^{\text{att}} \in \{x^{\text{init}}, x^{\text{up}}\}$  $(x^{\text{att}}, x^{\text{fb}}, x^{\text{up}})$  if an attempt  $x^{\text{att}} \in \{x^{\text{init}}, x^{\text{up}}_i\}$ **was incorrect, or into**  $x_T = (x^{\text{att}}, x^{\text{fb}})$  where the **186 186** containing the phrase "the final response is correct". **Next, we filter out some**  $x_{\text{imp}}$  **triplets that contain**  incorrect feedbacks or improvement steps using some rules (see more in [Appendix H\)](#page-15-0). Then, we 191 combine  $x_T$  and filtered  $x_{\text{imp}}$  into a single dataset, and balance them using a hyperparameter p spec-193 if ying the proportion of  $x_{\text{imp}}$ . We find that this parameter is important for the model to learn to improve its attempt *only when necessary*. This is **because we found that training with too many**  $x_{\text{imp}}$  can cause the model to attempt self-improvement even when the last attempt is already correct, thus damaging its performance (see [Section 4.2\)](#page-6-0).

### <span id="page-3-1"></span>**200** 2.4 Model Training

 Finally, we use supervised learning (SL) to train a 202 smaller model  $M_\theta$  on the combined dataset. To pro- mote the model to focus on learning the feedback **and improvement steps in**  $x_{\text{imp}}$ **, we use a weighted**  cross-entropy loss. We weight the loss for all the 206 tokens in  $x_T$  with  $w = 1.0$ , but with  $w > 1.0$  for 207 the tokens that belong to  $x_{\text{fb}}$  or  $x_{\text{up}}$  in single-step **improvement triplets**  $x_{\text{imp}}$ **. We note that we also ex-perimented with masking**  $x^{\text{init}}$  **[\(Zheng et al.,](#page-11-2) [2023\)](#page-11-2),**  but found it to be less effective than weighted SL in our case. See [Appendix E](#page-12-1) for more empirical analysis and discussions on related techniques.

**213** 2.5 TRIPOST

**214** In [Figure 2](#page-2-0) and [Algorithm 1](#page-3-2) we summarize our **215** TRIPOST algorithm. For each of the t iterations, 216 we first utilize  $M_{\theta}$  to generate its own attempts 217 X, and then use FBK and IMP to generate and **218** create a set of edited trajectories as described in **219** [Section 2.2.](#page-2-1) Next, we process the newly collected 220 trajectories and the gold task demonstrations  $X_{\text{gold}}$ 221 by first splitting them into a unified format of  $x_{\text{imp}}$ 222 triplet or  $x_T$ , and then filtering out erroneous  $x_{\text{imp}}$ **223** data [\(Section 2.3\)](#page-3-0). Finally, we create a training 224 dataset  $D$  by balancing the number of  $x_{\text{imp}}$  and  $x<sub>T</sub>$  using a hyperparameter p, and finetune  $M_{\theta}$  on 225 D using weighted SL. Unless otherwise specified, **226** we repeat this procedure for  $t = 3$  iterations, and 227 refer to the model trained using TRIPOST with t **228** iterations as  $TRIPOST(t)$ . 229

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#### 18: end for

## <span id="page-3-3"></span>3 Experiments **<sup>230</sup>**

In this section, we test if our TRIPOST can 1) **231** help distill self-improvement ability into a smaller **232** model  $M_{\theta}$ , and 2) help  $M_{\theta}$  improve performance 233 on math and reasoning tasks. **234**

#### 3.1 Dataset and Preprocessing **235**

We utilize the BIG-Bench [\(Srivastava et al.,](#page-10-8) [2023\)](#page-10-8) **236** benchmark to evaluate our approach. BIG-Bench **237** is a collection of more than 200 text-based tasks **238** including categories such as traditional NLP, math- **239** ematics, commonsense reasoning, and more. **240**

We perform experiments on four math and rea- **241** soning tasks from the challenging BIG-Bench Hard **242** [\(Suzgun et al.,](#page-10-7) [2022\)](#page-10-7) collection. We consider two **243** *scriptable* tasks: Multistep Arithmetic and Word **244** Sorting, where a step-by-step solution (rationale) **245** and a feedback can be generated using a script; **246** and two *unscriptable* tasks: Date Understanding **247** and Logical Deduction, where we prompt an LLM **248**

<span id="page-4-0"></span>

Dataset	Criterion	Example	seen subtask	<i>unseen</i> subtask
Multistep Arithmetic	nesting depth $(d)$ and number of operands $(l)$	$Q: ((2 * 2 + 1) + (3 * 1 - 1))$ $1/l = 3, d = 2$		$l = \{3, 4\} \times d = \{2\}$ $l = \{3, 4\} \times d = \{3\}$ and $l = \{5, 6\} \times d = \{2, 3\}$
Word Sorting	number of words to sort $(l)$	Q: orange apple banana pear $\ell l l = 4$	$l = \{2, 3, , 7\}$	$l = \{8, 9, , 16\}$
Date Understanding	number of steps to solve $(l)$	Q: Today is $01/02$ , what's the date yesterday? // $l = 1$	$l = \{1, 2\}$	l > 3
Logical Deduction	number of options $(l)$	Q: John runs  Who runs fastest? $l = \{3, 5\}$ Options: (A) (B) (C) $\frac{l}{l} = 3$		$l = \{7\}$

Table 2: Categorization of the datasets into seen and unseen tasks. *seen* tasks are chosen to be easier and are used for training. Example questions are abbreviated, for complete examples please refer to [Appendix A.](#page-12-2)

<span id="page-4-1"></span>

	Method	Multistep Arithmetic <sup>†</sup>		Word Sorting <sup>†</sup>		Date Understanding			Logical Deduction				
	seen	unseen	total	seen	unseen	total	seen	unseen	total	seen	unseen	total	
	<b>LMSI</b>	10.83	0.00	4.33	67.72	5.56	26.83	14.55	9.09	12.99	61.11	20.00	48.10
	ft rationale	39.75	1.48	16.78	73.49	5.82	28.50	33.35	21.21	29.87	62.69	8.67	45.78
	ft SI, demo	29.17	0.00	11.67	53.54	1.98	19.26	27.27	18.18	24.68	54.63	15.00	41.67
	$TRIPOST(t=1)$	41.67	0.84	17.17	74.02	5.16	28.23	32.73	13.64	27.27	57.88	22.00	46.52
Ours	$TRIPOST(t = 2)$	49.58	1.39	20.67	74.02	7.14	29.55	35.46	25.00	32.47	58.80	18.00	45.25
	$TRIPOST(t=3)$	52.50	2.50	22.50	77.17	5.95	29.82	40.00	29.55	37.01	63.89	15.00	48.42

<span id="page-4-2"></span>Table 3: Overall performance of TRIPOST on four BIG-Bench hard datasets. For each dataset, we train our models on the *seen* tasks, and evaluate their performance on both *seen* and *unseen* tasks. For all runs, we use  $p = 0.43$ for TRIPOST. Total accuracy (*total*) is weighted based on the number of test samples. † denotes that the task uses scripted rationale/feedback. Results are averaged over three runs.

<b>Dataset</b>		SI. Contrib.		Directly Correct	Total Acc.	
	seen	total unseen				
Multistep Arithmetic	1.39	0.28	1.67	20.83	22.50	
Word Sorting	1.85	0.52	2.37	27.44	29.82	
Date Understanding	1.95	1.29	3.25	33.76	37.01	
<b>Logical Deduction</b>	8.23	0.63	8.86	39.56	48.52	

Table 4: Analyzing how TRIPOST-trained models improved the overall task performance. Total accuracy is first decomposed into attempts that are directly correct (*Directly Correct*) and attempts with self-improvement (*SI. Contrib.*). *SI. Contrib.* is then further decomposed into its accuracy contribution on the seen and unseen subtasks.

**249** (Codex/text-davinci-003) to generate feedbacks. **250** We prompt Codex as the IMP module for all tasks.

 For each task, we first collect a set of gold step- by-step rationales by either scripting a solution for *scriptable* tasks, or using the CoT prompts from [Suzgun et al.](#page-10-7) [\(2022\)](#page-10-7) to generate a solution using LLMs. For those LLM-generated rationales, we only keep the correct ones (see [Appendix A](#page-12-2) for more details) for training. Then, to better measure a model's generalization ability, we split each of the 4 tasks further into *seen* and *unseen* subtasks. We mainly categorize simpler questions as the *seen* subtasks to be used for model training. We describe our categorization method in [Table 2.](#page-4-0)

#### **263** 3.2 Models and Baselines

264 **Models** We use LLaMA-7B as  $M_\theta$  in our main **265** experiments in [Table 3.](#page-4-1) LLaMA [\(Touvron et al.,](#page-10-9) [2023a\)](#page-10-9) is a collection of foundation language mod- **266** els ranging from 7B to 65B that have shown strong **267** performance compared to GPT-3 (175B) on many **268** benchmarks [\(Zheng et al.,](#page-11-2) [2023;](#page-11-2) [Taori et al.,](#page-10-10) [2023;](#page-10-10) **269** [Peng et al.,](#page-10-11) [2023b\)](#page-10-11). Due to the cost of training lan- **270** guage models, we use the smallest 7B model. For **271** results with LLaMA-2 models, see [Appendix D.](#page-12-3) **272** For training hyperparameters, see [Appendix I.](#page-15-1) **273**

Baselines We compare TRIPOST training with **274** three baselines: fine-tuning using self-generated, **275** self-consistent rationales (*LMSI*, [Huang et al.](#page-9-1) **276** [\(2023\)](#page-9-1)); fine-tuning using only ground truth ra- **277** tionales (*ft rationale*); and fine-tuning using self- **278** improvement demonstrations from LLMs (*ft SI.* **279** *demo*, similar to [Ye et al.](#page-11-1) [\(2023\)](#page-11-1)). For better perfor- **280** mance, we initialize with the model trained after *ft* 281 *rationale* for all methods. For more implementa- **282** tion details, see [Appendix G](#page-14-0) and [Appendix H.](#page-15-0) **283**

## **284** 3.3 Metrics

 To measure task performance, we follow prior stud- ies on Big-Bench [\(Ho et al.,](#page-9-3) [2023;](#page-9-3) [Huang et al.,](#page-9-1) [2023\)](#page-9-1) and report the accuracy of the final answer extracted from the model's output. For each task, we report the accuracy on the seen subtasks and unseen subtasks, and its overall performance. To measure the model's self-improvement ability, we mainly consider two metrics: 1) how often the model tries to self-improve (*SI. Freq.*), and 2) how much those of self-improvement attempts con- tribute to the model's task performance (*SI. Con- trib.*). We measure *SI. Freq.* as the number of times the model attempted to self-improve divided by the size of the test set, and *SI. Contrib.* as the num- ber of times those improvement attempts actually reached the correct final answer.

### <span id="page-5-0"></span>**301** 3.4 Main Results

 [Table 3](#page-4-1) summarizes TRIPOST's evaluation results [o](#page-9-1)n the four datasets. First, we find *LMSI* [\(Huang](#page-9-1) [et al.,](#page-9-1) [2023\)](#page-9-1) to be roughly on-par with *ft. rationale* only when the performance of the base model (i.e., *ft. rationale*) is already high on the training ques- tions (the *seen* subtask). This is understandable, as *LMSI* was originally designed for LLM (e.g., PaLM-540B) to improve on tasks where it can al- ready achieve a reasonable performance. Next, we find *ft SI. demo* to slightly degrade the model's performance across all tasks, which we believe is due to the capability mismatch between the LLM demonstrator and the small LM learner [\(Section 1\)](#page-0-2). This forces the small LM to learn from "advanced" errors not from its own [\(Table 1](#page-1-0) and [Appendix B\)](#page-12-0). Finally, we see that in all tasks, TRIPOST-trained models performs the best in all metrics. In general, we also observe improvement in the performance of TRIPOST-trained models as the number of it- erations t increases. We believe this is because, during the process of learning to self-improve, the model also learns to better understand the tasks by learning from its *own mistakes* [\(Zhang et al.,](#page-11-3) [2023;](#page-11-3) [Andrychowicz et al.,](#page-8-3) [2018;](#page-8-3) [Lightman et al.,](#page-9-4) [2023\)](#page-9-4). This enables the model to not only gen- erate better initial attempts, but also improve its self-improvement ability.

 In [Table 4,](#page-4-2) we further explore the contribution of  $M_{\theta}$ 's self-improvement ability by describing how its overall performance improved. We find that in two out of the four datasets, TRIPOST-trained mod-els generate an more accurate initial attempt than the baselines (denoted as *Directly Correct*), and in **334** all cases, TRIPOST-trained models had measurable **335** self-improvement contributions in both seen and **336** unseen tasks (cf. [Figure 1](#page-0-1) and [Table A4\)](#page-13-0). This sug- **337** gests that TRIPOST-training can 1) help the model **338** better understand the tasks and generate better ini- **339** tial attempts, and 2) help distill self-improving abil- **340** ity into the model. We believe that the combination **341** of both factors improve the model's overall perfor- **342** mance in [Table 3.](#page-4-1) **343** 

## <span id="page-5-1"></span>3.5 TRIPOST-auto **344**

In [Table 5,](#page-6-1) we explore another way of training  $M_{\theta}$  345 with TRIPOST. Instead of re-balancing the training **346** dataset using a fixed  $p$  as in [Section 3.4,](#page-5-0) we can  $347$ simply include all the edited improvement tuples **348**  $x_{\text{imp}}$  and the directly correct attempts  $x_T$  generated 349 by  $M_\theta$ . We denote this method as TRIPOST-auto,  $350$ as it automatically "balances" its training data to **351** be proportional to its current performance, because **352** p can be interpreted as how often the model's at- **353** tempts were incorrect and needed editing. TRI- **354** POST-auto training included no less  $x_{\text{imp}}$  com-  $355$ pared to  $TRIDOST$  (but generally more  $x_T$ , result-  $356$ ing in  $p < 0.43$ ), and we find that the model now  $357$ rarely attempts to self-improve. However, this un- **358** expectedly leads to even better overall performance, **359** especially on *unscriptable* tasks. We believe this **360** indicates that 1) learning to always generate a use- **361** ful feedback and the corresponding improvement is **362** *harder* than learning to directly generate a correct **363** attempt, and 2) using LLM-generated feedbacks, **364** which covers more error cases than a Python script,  $365$ is effective in improving a model's performance. **366**

## 4 Analysis **<sup>367</sup>**

To investigate the factors that can influence how **368** TRIPOST-trained models learned to attempt self- **369** improvement, we focus our analysis on the Mul- **370** tistep Arithmetic and Logical Deduction datatset. **371** We also mainly study TRIPOST with  $p = 0.43$ ,  $372$ which has both a measurable self-improvement con- **373** tribution and improvement in its task performance **374** (see [Table 3](#page-4-1) and [Table 4\)](#page-4-2). **375**

### <span id="page-5-2"></span>4.1 Ablation Studies **376**

We perform ablation studies for each of the three  $377$ stages in TRIPOST to better understand their con- **378** [t](#page-6-2)ribution to model's overall performance. In [Ta-](#page-6-2) **379** [ble 6,](#page-6-2) we report the task accuracy when: interac- **380** tion between  $M_\theta$  and LLM is removed, so that **381** 

<span id="page-6-1"></span>

Method	Multistep Arithmetic <sup>†</sup>		Word Sorting <sup>†</sup>		Date Understanding			Logical Deduction				
	SI. Freq	SI. Cont.	total	SI. Freq	SI. Cont.	total	SI. Freq	SI. Cont.	total	SI. Freq	SI. Cont.	total
$TRIPOST(t = 1)$	0.00	0.00	17.17	1.58	0.52	28.23	0.00	0.00	27.27	8.86	2.85	46.52
$TRIPOST(t=2)$	1.33	1.11	20.67	2.90	0.52	29.55	1.94	0.65	32.47	29.72	11.39	45.25
$TRIPOST(t=3)$	3.67	1.67	22.50	4.38	2.37	29.82	10.38	3.25	37.01	23.42	8.86	48.42
$TRIPOST-auto(t = 1)$	0.00	0.00	20.00	0.00	0.00	30.34	0.00	0.00	32.47	1.90	0.63	51.27
$TRIPOST$ -auto $(t = 2)$	0.00	0.00	23.33	0.00	0.00	29.55	0.00	0.00	56.82	0.63	0.00	55.06
$TRIPOST-auto(t = 3)$	0.00	0.00	24.33	0.00	0.00	30.34	0.00	0.00	68.83	0.63	0.63	56.96

Table 5: Overall performance of TRIPOST without explicit re-balancing. TRIPOST-auto uses the same training procedure as TRIPOST, except that the proportion of  $x_{\text{imp}}$  used for training is determined automatically using the model's current task performance.

<span id="page-6-2"></span>

Method	Multistep Arithmetic		Logical Deduction			
	SL Contrib.	Total Acc.	SI. Contrib.	Total Acc.		
<b>TRIPOST</b>	1.67	22.50	8.86	48.42		
-interaction	0.28	11.67	0.00	41.67		
-filtering	0.33	20.67	7.59	48.27		
+auto-balance	0.00	24.33	0.63	56.96		
-weighed SL	0.00	21.33	1.90	43.67		

Table 6: TRIPOST ablation studies.

  $M_\theta$  is distilled with purely LLM demonstrations (*-interaction*); data filtering is removed (*-filtering*); dataset balancing is changed to using its own per- formance (*+auto-balance*); and the weights for SL are changed to be the same for all tokens (*- weighed SL*). We find that all components are im- portant for TRIPOST to work well, and the choice of fixing p presents a trade-off between a model's self-improvement ability and its task performance (notibly, both TRIPOST and TRIPOST-auto im-prove upon the baselines).

#### <span id="page-6-0"></span>**393** 4.2 Proportion of SI. Training Data

 In [Table 7,](#page-6-3) we investigate how much improvement **demonstration**  $(x_{\text{imp}})$  is needed to elicit a measur-**able self-improvement contribution from**  $M_\theta$ **. We find that when a large proportion (e.g.**  $p = 0.70$ **)** 398 of the training data contains  $x_{\text{imp}}$ , the model often *attempts* to self-improve but does not always result in an overall better performance. This is because many of the "improvement" attempts result in fail- ures (e.g. changing an already correct attempt to become an incorrect one), and the best performance is achieved typically when p is low. Despite this, 405 we find that for all other cases with  $p \leq 0.43$ , TRI- POST-trained model achieved a better performance than the baseline methods (see [Table 4\)](#page-4-2).

### **408** 4.3 Number of TRIPOST Iterations

 In most of our experiments, we trained TRIPOST **up to**  $t = 3$  **iterations. This is because we found**  that LLMs and our Python scripts start to strug-412 gle with generating feedback or improving  $M_\theta$  at-

<span id="page-6-3"></span>

Dataset	р	Freq.	Self-Improvement Contrib.	Total Acc.
	0.05	0.00	0.00	23.17
	0.20	0.00	0.00	24.33
Multistep Arithmetic	0.43	3.67	1.67	22.50
	0.56	8.61	2.50	20.00
	0.70	18.88	3.61	18.67
	0.05	0.00	0.00	49.37
	0.20	0.63	0.00	52.63
Logical Deduction	0.43	23.42	8.86	48.42
	0.56	20.25	7.59	45.57
	0.70	59.49	31.64	45.57

Table 7: Varying the proportion of  $x_{\rm SI}$  used during TRIPOST training.

<span id="page-6-4"></span>

Figure 3: Improvement demonstrations become more difficult to collect as TRIPOST iteration increases.

tempts after three iterations. In [Figure 3,](#page-6-4) we present **413** how the number of self-improving trajectories col- **414** lected  $(x_{\text{imp}})$ , after filtering) changes as  $TRIPOST$  415 iteration increases. We found that as  $M_\theta$  improves 416 its performance over time, it 1) poses a greater chal- **417** lenge for our FBK module to generate feedback **418** and/or the IMP module to generate improvement, **419** and 2) generates fewer incorrect attempts for TRI- **420** POST to edit. This is especially impactful for Mul- **421** tistep Arithmetic, as our feedback scripts can only **422** consider a fixed number of error types. This also **423** shows that even LLMs can struggle at generating **424** useful feedbacks or correct improvements, which **425** supports our findings in [Section 3.5](#page-5-1) that learning **426**

**427** to generate feedback and improvements may be **428** harder than to directly generate a correct solution.

## **<sup>429</sup>** 5 Related Work

 Prompting LLMs to Self-Improve Recently, many work [\(Bai et al.,](#page-8-1) [2022;](#page-8-1) [Madaan et al.,](#page-9-2) [2023\)](#page-9-2) have discovered LLM's capability to self-improve by letting it revise its own answer after prompting it to generate feedbacks. Following these work, [Yang et al.](#page-11-4) [\(2022\)](#page-11-4); [Peng et al.](#page-10-2) [\(2023a\)](#page-10-2); [Shinn et al.](#page-10-3) [\(2023\)](#page-10-3); [Schick et al.](#page-10-4) [\(2022\)](#page-10-4); [Yang et al.](#page-11-5) [\(2023\)](#page-11-5) has utilized such a capability to improve LLM's [p](#page-11-4)erformance on various tasks. For example, [Yang](#page-11-4) [et al.](#page-11-4) [\(2022\)](#page-11-4) recursively prompts an LLM to gen- erate a longer story, and [Madaan et al.](#page-9-2) [\(2023\)](#page-9-2) iter- atively prompts an LLM to improve its answers on a wide range of tasks such as sentiment re- versal and dialogue response generation. More generally, [Yang et al.](#page-11-5) [\(2023\)](#page-11-5) finds that LLMs can be prompted to act as an "optimization function", which can be used to automatically perform prompt engineering. Our work focuses on distilling the self-improvement ability of LLMs into a smaller model, which was initially not capable of self-improvement [\(Figure 1\)](#page-0-1).

 Training LMs to Self-Improve Besides prompt- ing methods, recent work also explored approaches [t](#page-9-1)o train a LM to self-improve. LMSI [\(Huang](#page-9-1) [et al.,](#page-9-1) [2023\)](#page-9-1) trains LMs (e.g., PaLM-540B) with self-generated, self-consistent answers to improve their task performance, yet we found such method ineffective for small LMs. Many work such as [Paul et al.](#page-10-12) [\(2023\)](#page-10-12); [Welleck et al.](#page-11-6) [\(2022\)](#page-11-6); [Madaan](#page-10-13) [et al.](#page-10-13) [\(2021\)](#page-10-13); [Yasunaga and Liang](#page-11-7) [\(2020\)](#page-11-7); [Du et al.](#page-9-5) [\(2022\)](#page-9-5) considered using multiple small LMs to gen- erate feedback and improvement, which also relates to model ensemble methods [\(Dietterich,](#page-9-6) [2000\)](#page-9-6). For example, [Welleck et al.](#page-11-6) [\(2022\)](#page-11-6) trains a "correc- tor" to improve answers generated by a given fixed generator. This method gathers improved attempts by sampling from the generator and pairing high- scoring attempts with low-scoring ones. It also does not provide reasonings (e.g., feedbacks) for each improvement. [Paul et al.](#page-10-12) [\(2023\)](#page-10-12) first trains a feedback model by using a set of predefined rules that perturbs an original solution, and then trains a separate model to generate answers conditioned on the feedback. Our work leverages LLMs to train a single model capable of generating both feed- back and improvement, and also does not require any predefined rules (e.g., using LLMs as the FBK module). [Saunders et al.](#page-10-5) [\(2022\)](#page-10-5); [Ye et al.](#page-11-1) [\(2023\)](#page-11-1) **477** has attempted to equip a single small model to self- **478** improve by training on LLM demonstrations, but **479** found that it had little to no effect for small models **480** on math/reasoning tasks. Our work presents anal- **481** yses of how these previous methods can fail, and **482** proposes TRIPOST that can train a small model to **483** self-improve and achieve better task performance. **484**

Knowledge Distillation Learning from experts' **485** demonstrations or reasoning (e.g., from GPT-4) **486** has shown to be successful at improving the perfor- **487** [m](#page-10-14)ance of smaller models in various tasks [\(Mukher-](#page-10-14) **488** [jee et al.,](#page-10-14) [2023;](#page-10-14) [Laskin et al.,](#page-9-7) [2022;](#page-9-7) [Peng et al.,](#page-10-11) **489** [2023b;](#page-10-11) [Ho et al.,](#page-9-3) [2023;](#page-9-3) [Ye et al.,](#page-11-1) [2023;](#page-11-1) [Huang](#page-9-1) **490** [et al.,](#page-9-1) [2023\)](#page-9-1). Distillation methods [\(Hinton et al.,](#page-9-8) **491** [2015;](#page-9-8) [Ba and Caruana,](#page-8-4) [2014\)](#page-8-4) generally train a tar- **492** get model using expert demonstrations unaware of **493** the target model's capability. While TRIPOST also **494** use LLMs to demonstrate generating a feedback or **495** an improvement, these demonstrations are always **496** conditioned on the output of the smaller model. In **497** this view, our approach combines merits from re- **498** inforcement learning with knowledge distillation **499** techniques, where small models are distilled with **500** demonstrations that are created by its own explo- **501** ration augmented by LLMs' supervision. **502**

# 6 Conclusion **<sup>503</sup>**

We introduce TRIPOST, a training algorithm that  $504$ distills the ability to self-improve to a small model **505** and help it achieve better task performance. TRI- **506** POST first creates improving trajectories using in- **507** teractions between a smaller model and an LLM, **508** then post-process the collected trajectories, and fi- **509** nally train the smaller model to self-improve using **510** weighted SL. We evaluated TRIPOST on four math **511** and reasoning tasks from the Big-Bench Hard col- **512** lection and found that it can help small models **513** achieve better task performance. In our analysis, **514** we find that 1) the interactive process of learning  $515$ from and correcting its *own* mistakes is crucial **516** for small models to learn to self-improve and 2) **517** learning to always generate a useful feedback and **518** a corresponding improvement can be much harder **519** than learning to directly generate a correct answer. **520** These findings suggest that other data formats, be- **521** yond the traditional (input, answer) pair, could be **522** better suited for training a language model to solve **523** a downstream task. We believe this also opens new **524** possibilities for future work to leverage LLMs to **525** improve the performance of smaller, faster models. **526**

## **<sup>527</sup>** 7 Limitations

 Model Sizes In all of our experiments, we used a single A100 and mainly tested TRIPOST on 7B models, the smallest in the LLaMA-1 and LLaMA- 2 family [\(Touvron et al.,](#page-10-9) [2023a](#page-10-9)[,b\)](#page-10-15). However, with the recently introduced flash attention technique [\(Dao et al.,](#page-9-9) [2022;](#page-9-9) [Dao,](#page-9-10) [2023\)](#page-9-10) which can be used to reduce memory usage during training, we plan to extend our experiments to use models with more than 7B parameters.

 **Datasets** We focused our experiments on math and reasoning tasks because 1) prior work [\(Ye et al.,](#page-11-1) [2023\)](#page-11-1) had found it difficult to train a 7-13B to self-improve on those tasks and 2) measuring per- formance improvement is more well defined (for example, as compared to creative story writing). However, we note that as TRIPOST is task agnos- tic, in theory it can be applied to other tasks such as [k](#page-11-8)nowledge-grounded dialogue generation [\(Yoshino](#page-11-8) [et al.,](#page-11-8) [2023\)](#page-11-8) or dialogue safety [\(Dinan et al.,](#page-9-11) [2019\)](#page-9-11). We intend to leave this for future work.

 LLM Usage While attempts for some tasks can be parsed and evaluated using a Python script (e.g., multistep arithmetic and word sorting), it quickly becomes unmanageable for tasks where reasonings mostly take the form of free text (e.g., date under- standing and logical deduction). Therefore, we use LLMs such as GPT-3 and Codex (and ChatGPT, see [Appendix F\)](#page-13-1), which are highly performant at a reasonable cost. Specifically, we mainly use text- davinci-003 as the feedback module and Codex as the improvement module, as we found this to be the most cost-performant configuration in our experiments.

 However, since the ability of LLMs to generate feedback or improvements is *crucial* for TRIPOST to collect training data, this presents a trade-off be- tween the cost of using more performant LLMs (e.g., GPT-4) and the training outcome of TRI- POST, for example on harder tasks such as GSM8k [\(Cobbe et al.,](#page-9-12) [2021\)](#page-9-12). We hope that with advances in making LLMs more available [\(Zhang et al.,](#page-11-9) [2022a\)](#page-11-9), such a trade-off would diminish.

## **<sup>570</sup>** 8 Ethical Considerations

 Our work describes an algorithm to improve small models' performance on math and reasoning tasks, by distilling them the ability to self-improve using interaction records with LLMs. Generally, while most algorithms are not designed for unethical us- **575** age, there is often potential for abuse in their ap- **576** plications. In our experiments, we apply TRIPOST **577** to four math and reasoning tasks from the Big- **578** Bench Hard collection [\(Suzgun et al.,](#page-10-7) [2022\)](#page-10-7). How- **579** ever, because training algorithms are typically task- **580** agnostic, it is possible to use them for unethical **581** tasks, such as scamming and generating harmful **582** responses [\(Welbl et al.,](#page-11-10) [2021;](#page-11-10) [Gehman et al.,](#page-9-13) [2020\)](#page-9-13). **583** We do not condone the use of TRIPOST for any 584 unlawful or morally unjust purposes. **585**

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## <span id="page-12-2"></span>**922 A** More Details on Datasets and **923** Preprocessing

 We use four tasks from the Big-Bench Hard collec- tion [\(Suzgun et al.,](#page-10-7) [2022\)](#page-10-7) for our experiments: *mul- tistep arithmetic*, *word sorting*, *date understanding*, and *logical deduction*. Since these tasks do not pro- vide ground truth step-by-step rationale, we either generate them using a script (for *multistep arith- [m](#page-8-2)etic* and *word sorting*), or prompt Codex [\(Chen](#page-8-2) [et al.,](#page-8-2) [2021\)](#page-8-2) in a few-shot setting using examples from [Suzgun et al.](#page-10-7) [\(2022\)](#page-10-7). For rationales gener- ated using prompting, we only keep the ones that reached the correct answer and passed a simple con- sistency check (e.g. for multiple choice questions, we ensure that the final selected choice in the last step appeared in the second last step). We provide example rationales used for each task in [Table A7,](#page-16-0) [Table A8,](#page-16-1) [Table A9,](#page-16-2) and [Table A10.](#page-17-0) Since Big- Bench [\(Srivastava et al.,](#page-10-8) [2023\)](#page-10-8) did not provide an official training/validation/test split, we generated our own splits with statistics shown in [Table A1.](#page-12-4)

<span id="page-12-4"></span>

<b>Dataset</b>	Train	Validation	Test
Multistep Arithmetics	550	50	300
<b>Word Sorting</b>	433	40	379
Date Understanding	191	20	87
Logical Deduction	360	40	158

<span id="page-12-0"></span>Table A1: Number of training, validation, and test samples used for the four tasks from the Big-Bench Hard collection [\(Suzgun et al.,](#page-10-7) [2022\)](#page-10-7).

## **<sup>943</sup>** B Analyzing Errors Made by Codex and **<sup>944</sup>** LLaMA-7B

 To detail the different type and amount of errors made by an LLM (e.g., Codex) and a smaller model (e.g., LLaMA-7B), we manually examine incorrect attempts generated by the two models in the Mul- tistep Arithmetics dataset. We use Codex with few-shot prompting, and LLaMA-7B after super- vised finetuning on ground-truth step-by-step solu- tions (denoted as *LLaMA+ft*). We randomly sam- ple 50 generated attempts with incorrect answers, and carefully review each step in those attempts. For each incorrect step, we apply the principle of error-carried-forward and categorize the first error encountered according to [Table A2.](#page-13-2)

 We present our analysis in [Figure A1](#page-13-3) and [Ta-](#page-13-4) [ble A3.](#page-13-4) [Figure A1](#page-13-3) shows that calculation er- rors take up more than 50% of the time for both Codex and the finetuned LLaMA-7B. However, Codex also makes many algebriac errors (such as **962** forgetting to change sign after adding brackets), **963** while LLaMA-7B often hallucinates by adding or **964** deleting terms from previous calculations. Fur- **965** thermore, [Table A3](#page-13-4) shows that, compared to the **966** fine-tuned LLaMA-7B, Codex generates longer **967** solutions while producing fewer errors per step. 968 These findings suggest that supervised finetuning **969** a smaller LM (e.g., LLaMA-7B) based on correct- **970** ing LLM-generated errors may be inefficient, as it **971** forces the smaller model to learn from attempts and **972** mistakes very different from its own (see [Section 1](#page-0-2) **973** and [Appendix C](#page-12-5) for more details). **974**

## <span id="page-12-5"></span>C More Details on the Prior Study **<sup>975</sup>**

In the prior study mentioned in [Section 1,](#page-0-2) we ex- **976** perimented with distilling a smaller model (e.g. **977** LLaMA-7B) with self-improvement demonstration **978** using just the LLMs. We found that not only can **979** the smaller model *not* self-improve by few-shot **980** prompting, they also still fail to do so after train- **981** ing on the LLM self-improvement demonstrations **982** (also discussed in [Section 1\)](#page-0-2). In [Figure 1](#page-0-1) we pre- **983** sented the performance gap between prompting **984** Codex (175B) and finetuning/prompting LLaMA **985** (7B) with self-improvement demonstrations, and in **986** [Table A4](#page-13-0) we show the detailed numerical results. **987**

## <span id="page-12-3"></span>D Additional Results on LLaMA-2 **<sup>988</sup>**

In [Table A5](#page-14-1) we present the results of using the **989** LLaMA-2 7B model [\(Touvron et al.,](#page-10-15) [2023b\)](#page-10-15) for **990** TRIPOST training. We used the same proce- **991** dure as testing with the LLaMA-1 model in our **992** main experiments [\(Section 3\)](#page-3-3), except that we used **993**  $p = 0.26$  across all settings with LLaMA-2 instead  $994$ of  $p = 0.43$ . This is because we found that the **995** LLaMA-2 baseline (*ft rationale*) achieves almost **996** twice the performance compared to its LLaMA-1 **997** counterpart. As the LLaMA-2 models make fewer **998** mistakes, we decrease p accordingly to prevent **999** TRIPOST from terminating early due to lack of **1000** data. In general, [Table A5](#page-14-1) shows a similar trend as **1001** discussed in [Section 3](#page-3-3) that 1) fine-tuning on LLM **1002** demonstrations of self-improvement did not help **1003** improve math/reasoning task performance, and 2) 1004 TRIPOST can further improve upon the baselines. **1005**

## <span id="page-12-1"></span>**E** Effect of Weighted SL 1006

Besides balancing the training dataset, we also **1007** found it important to use a weighted cross-entropy **1008** loss to emphasize learning the improvement-related 1009

<span id="page-13-2"></span>

Error Name	<b>Definition</b>	Example
<b>Calculation Error</b>	errors in performing basic arithmetic operations (addition, subtrac- $2 + 3 = 7$ tion, multiplication, division)	
Algebraic Error	errors in algebraic manipulation, such as forgetting to change signs $1-2+3=1-(2+3)$ when adding brackets or forgetting the correct order of operations	
Copy Error	mis-copying an operand or an operator from previous steps	$7+1+()=7-1+()$
Hallucation Other Error	adding or deleting an operand or an operator from previous steps errors that do not fall into the above categories	$7 + (\ldots) = 7 - 1 + (\ldots)$

<span id="page-13-3"></span>Table A2: Categorization of errors commonly made by Codex or LLaMA-7B in the Multistep Arithmetics dataset.



Figure A1: LMs of different sizes make different types of errors. In the Multistep Arithmetics dataset, more than half of the errors made by Codex or a finetuned LLaMA-7B belong to *Calculation Error*. However, the second most common error is *Arithmetic Error* for Codex, and *Copy Error* for LLaMA-7B.

<span id="page-13-4"></span>

		$Codex$ LLaMA+ft (7B)
Avg. Char per Question	113.8	102.4
Avg. Char per Attempt	920.0	650.1
Percent Steps with Errors	31.7	35.1

Table A3: LMs of different sizes make different amount of errors. In the Multistep Arithmetics dataset, Codex makes less errors per step compared to a finetuned LLaMA-7B, while answering longer questions and generating longer solutions.

<span id="page-13-0"></span>

Dataset	Method	SI. Contrib.	Total Acc.
	Codex (175B)		31.33
	$+ SI.$ prompting	2.00	$33.33 \uparrow$
MS.A.	$LLaMA+ft(7B)$		16.78
	$+ SI.$ prompting	0.00	$11.60 \downarrow$
	$+$ ft SL demo	0.28	$11.67 \downarrow$
	Codex(175B)		81.01
	$+ SI.$ prompting	4.43	$85.44$ $\uparrow$
LD.	LLaMA+ft (7B)		45.78
	$+ SI.$ prompting	0.00	43.67 $\downarrow$
	+ ft SL demo	0.00	41.67 $\downarrow$

Table A4: Compared to LLMs, smaller models have difficulty performing self-improvement (*SI.*) on mathematical/logical tasks, such as Multistep Arithmetics (*MS.A.*) and Logical Deduction (*L.D.*).

tokens  $(x_{\text{fb}} \text{ or } x_{\text{up}})$  of each training sample. In 1010 [Table A6,](#page-14-2) we find that using a weight too low 1011  $(w = 1.0)$  can result in the model rarely attempt- 1012 ing to self-improve, while using a weight too high 1013  $(w = 3.0)$  does not result in better performance. 1014 We believe that this has a similar effect of adjust- 1015 ing  $p$  in [Section 4.2:](#page-6-0) some incentive is needed for  $1016$ the model to learn to self-improve, while too much **1017** emphasis on trying to self-improve can result in a 1018 worse performance. **1019** 

While we also experimented with alternatives **1020** such as masking easier tokens  $(x_{\text{init}})$ , we believe **1021** there is a rich set of techniques that can be used **1022** to train the model to focus on harder inputs. This **1023** [i](#page-9-14)ncludes boosting algorithms [\(Schapire,](#page-10-16) [1999;](#page-10-16) [He](#page-9-14) 1024 [et al.,](#page-9-14) [2019\)](#page-9-14), automatic loss reweighing methods **1025** [\(Kanai et al.,](#page-9-15) [2023;](#page-9-15) [Wang et al.,](#page-10-17) [2022,](#page-10-17) [2020\)](#page-10-18), **1026** as well as importance-sampling based methods **1027** [\(Katharopoulos and Fleuret,](#page-9-16) [2019\)](#page-9-16). We leave this **1028** for future work as it is orthogonal to our main con- **1029** tributions. **1030** 

## <span id="page-13-1"></span>F Prompting Details **<sup>1031</sup>**

Besides prompting to generate rationales (e.g. for **1032** *date understanding*), we also use prompting to gen- 1033 erate feedbacks and improvements given the ini- **1034**

<span id="page-14-1"></span>

Method			Multistep Arithmetics <sup>†</sup>		Logical Deduction			
		seen	unseen	total	seen	unseen	total	
(7B)	ft rationale ft SI, demo	38.75 29.17	1.48 0.00	16.78 11.67	62.69 54.63	8.67 15.00	45.78 41.67	
LLaMA-1	$TRIPOST(t=1)$ $TRIPOST(t=2)$ $TRIPOST(t=3)$	41.67 49.58 52.50	0.84 1.39 2.50	17.17 20.67 22.50	57.88 58.80 63.89	22.00 18.00 15.00	46.52 45.25 48.42	
(7B)	ft rationale ft SI, demo	72.50 51.67	5.00 2.22	32.00 22.00	87.04 80.56	34.00 42.00	70.25 68.35	
AMA-2 ᅼ	$TRIPOST(t=1)$ $TRIPOST(t=2)$ $TRIPOST(t=3)$	71.67 75.00 72.22	3.89 6.11 5.19	31.00 33.67 32.00	83.33 83.33 71.67	52.00 48.00 50.00	73.42 72.15 72.78	

Table A5: Using TRIPOST with LLaMA-2 7B model. Overall, LLaMA-2 performs better than its LLaMA-1 counterpart, and TRIPOST further improves LLaMA-2's task performance.

<span id="page-14-2"></span>

Dataset	w	Self-Improvement Contrib. Freq.		Total Acc.
Multistep Arithmetic	1.0	0.00	0.00	21.33
	1.5	3.67	1.67	22.50
	3.0	3.33	1.38	22.00
<b>Logical Deduction</b>	1.0	10.13	1.90	43.67
	1.5	23.42	8.86	48.42
	3.0	19.62	9.49	46.84

Table A6: Varying the SL weights  $w$  used during TRI-POST training.

 tial attempt. For scriptable tasks such as *multistep arithmetic* and *word sorting*, we use a script to gen- erate the feedback by first parsing each step in the attempt, and check their correctness/consistency with other steps using a set of predefined rules. This is similar to [Welleck et al.](#page-11-6) [\(2022\)](#page-11-6), but we also generalize this to unscriptable tasks such as *date understanding* and *logical deduction* by few-shot prompting GPT-3 (text-davinci-003) [\(Brown et al.,](#page-8-0) [2020\)](#page-8-0) and Codex [\(Chen et al.,](#page-8-2) [2021\)](#page-8-2) to generate feedbacks and improvements. We found that being able to generate useful feedback is critical for gath- ering successful improvement trajectories, and we discovered that ChatGPT [\(OpenAI,](#page-10-19) [2022\)](#page-10-19) is less effective than GPT-3 or Codex in our case. We provide examples of the feedbacks generated for each task in [Table A11,](#page-18-0) and the prompts used to generate feedback or improvements in [Table A12,](#page-19-0) [Table A13,](#page-20-0) [Table A14,](#page-21-0) and [Table A15.](#page-22-0) Note that we used a form-type of prompting for generating feedback because it can more easily ensure that our (formatted) feedback will contain all the elements **1057** we need.

**1058** When an answer is correct, we manually attach **1059** the phrase "Step 1 to step x is correct, and the final response is also correct." as the termination **1060** feedback, where "x" is the last step number. This **1061** termination condition is also used during inference. **1062**

## <span id="page-14-0"></span>G More Details on Baselines **<sup>1063</sup>**

**LMSI** [Huang et al.](#page-9-1) [\(2023\)](#page-9-1) proposed LMSI, a 1064 method to improve PaLM-540B [\(Chowdhery et al.,](#page-9-17) 1065 [2022\)](#page-9-17) on math and reasoning tasks by training it **1066** on self-generated and consistent step-by-step ra- **1067** tionales. First, LMSI generates multiple step-by- **1068** step solutions using a high temperature  $(\tau = 1.2)$ . **1069** Then, LMSI only keeps the answers that are self- **1070** consistent (by majority voting) in the final answer. **1071** Finally, LMSI further augments these solutions **1072** with mixed formats, such as removing all the inter- 1073 mediate steps and only keep the final answer. To 1074 be comparable with other methods in [Table 3](#page-4-1) that **1075** have access to the ground truth answer, we modify 1076 the second step to only keep the answers that are **1077** correct. In addition, since small models such as **1078** LLaMA-7B performed poorly in these tasks with- **1079** out fine-tuning, we perform LMSI after training the **1080** model on the collected silver step-by-step solutions 1081 in [Appendix A.](#page-12-2) **1082** 

*ft. SI demo* Following [Ye et al.](#page-11-1) [\(2023\)](#page-11-1), *ft. SI* **1083** *demo* finetunes a model on LLM-generated self- **1084** improvement demonstrations. For all tasks, we **1085** experimented with LLMs  $\in$  {ChatGPT, Codex} 1086 and reported one with better performance (often **1087** Codex). In details, we first prompt a LLM (e.g. **1088** Codex) to generate an initial attempt, and then re- **1089** used TRIPOST with the same LLM as the FBK and **1090** IMP to generate a feedback and an improvement. **1091** For a fair comparison in [Table 3,](#page-4-1) we also balanced 1092 the collected data using the same  $p = 0.43$  as with 1093

 TRIPOST. Finally, train the small LM using (un-weighted) SL on the collected data.

## <span id="page-15-0"></span>H Implementation Details

 We combine techniques from prompting-based self- improvement [\(Madaan et al.,](#page-9-2) [2023;](#page-9-2) [Bai et al.,](#page-8-1) [2022\)](#page-8-1) [a](#page-9-4)nd active learning [\(Zhang et al.,](#page-11-11) [2022b;](#page-11-11) [Lightman](#page-9-4) [et al.,](#page-9-4) [2023\)](#page-9-4) to collect a set of self-improving tra- jectories. Specifically, we first either use a script or few-shot prompting (see [Appendix F](#page-13-1) for more details) to gather *feedbacks* on a given attempt, and then use prompting to generate *improvements* con- ditioned on the previous attempt, the feedback, and all the steps in the previous attempt before the first error step (see [Tables A12](#page-19-0) to [A15](#page-22-0) for example). This is to ensure that the improved attempt is mak- ing modifications on the previous attempt, rather than creating an entirely new attempt.

 To edit the original attempt given the script/LLM-generated feedback, we 1) find **the first**  $x_i^{\text{fb}*}$  **feedback that differs from the**  $M_{\theta}$ **-generated feedback**  $x_i^{\text{fb}}$  (usually  $i = 1$ ); 2) replace  $x_i^{\text{fb}*}$  with  $x_i^{\text{fb}}$ ; 3) remove all the attempts, feedback, **and improvement after after**  $x_i^{\text{fb}}$  **from the trajectory.**  After this, we prompt an LLM in the improvement module IMP to generate an improvement as described above and in [Appendix F.](#page-13-1)

 To filter out some of the unhelpful feedbacks or incorrectly "improved" attempts, we mainly check 1122 1) whether the final attempt reached the correct answer; 2) if there is at least one difference between the previous attempt and the improved attempt; and 3) if the final answer is consistent with the second last step. We only keep the data that have passed all checks. The effect of this filtering is discussed in our ablation studies in [Section 4.1.](#page-5-2)

### <span id="page-15-1"></span>I Model/Training hyperparameters

 In our main experiments, we used a single A100 GPU with DeepSpeed [\(Rasley et al.,](#page-10-20) [2020\)](#page-10-20) Zero-2 [o](#page-9-18)ptimization. We used AdamW [\(Loshchilov and](#page-9-18) [Hutter,](#page-9-18) [2019\)](#page-9-18) as the optimizer. For each iteration of the TRIPOST algorithm, we train the model for 4 epochs (line [17\)](#page-3-2). We use a linear learning rate schedule with 20% of warmup steps and a peak learning rate of 1e-6. We use a maximum sequence length of 1024 tokens, batch size = 1 and gradient accumulation step = 4. On average, three iterations of TRIPOST take about 12 hours to train.

### <span id="page-16-0"></span>Example Question and Generated Rationale for Multistep Arithmetic

*Q: ((7 - -1 + -1 + -4) - (-7 + 7 \* 3 \* -9)) = Answer: Let's think step by step. Recall that the order of operations in mathematics is as follows: (1) Parentheses, (2) exponents, (3) multiplication and division (from left to right), (4) addition and multiplication (from left to right). So, remember to always compute the expressions inside parentheses or brackets first.*

(1) This equation can be written as " $(A - B)$ ", where  $A = (7 - (-1) + (-1) + (-4)$  and  $B = (-7 + 7 \cdot 3 \cdot 4)$ . (2) Let's calculate  $A = (7 - 1 + 1 + 4) = ((7 - 1) + 1) + 4 = (8 + 1) + 4 = (7 + 4) = 3$ . (3) Let's calculate B =  $(-7 + 7 * 3 * -9) = (-7 + ((7 * 3) * -9)) = (-7 + (21 * -9)) = (-7 + (-189)) = -196$ . (4) Then, the final equation is  $(A - B) = (3 - 196) = 199$ . (Final response) So the answer is 199.

Table A7: Examples of generated rationales for Multistep Arithmetic using Python scripts. Question and prompts are written in *gray italics*, and the generated step-by-step rationale is shown in black.

### <span id="page-16-1"></span>Example Question and Generated Rationale for Word Sorting

*Q: Sort the following words alphabetically: List: sioux fortescue purloin percept helmsman Attempt: Let's think step by step.* (1) The first letter: "sioux"="s", "fortescue"="f" (6), "purloin"="p" (16), "percept"="p" (16), "helmsman"="h"  $(8)$ (2) We now have: (6) "fortescue" < (8) "helmsman" < (16) ["purloin" ? "percept" $|$  < (19) "sioux". (3) Now sort this subpart ["purloin" ? "percept"] by looking at their second letters: "purloin"="u"  $(21)$ , "percept"="e"  $(5)$ .  $(3.1)$  We now have:  $(5)$  "percept" <  $(21)$  "purloin".  $(3.2)$  Hence, we have "percept" < "purloin". (4) Hence, we have "fortescue" < "helmsman" < "percept" < "purloin" < "sioux". (Final response) So the answer is: fortescue helmsman percept purloin sioux.

Table A8: Examples of generated rationales for Word Sorting using Python scripts. Question and prompts are written in *gray italics*, and the generated step-by-step rationale is shown in black.

### <span id="page-16-2"></span>Example Question and Generated Rationale for Date Understanding



Table A9: Examples of generated rationales for Date Understanding by prompting Codex [\(Chen et al.,](#page-8-2) [2021\)](#page-8-2). Question and prompts are written in *gray italics*, and the generated step-by-step rationale is shown in black.

## <span id="page-17-0"></span>Example Question and Generated Rationale for Logical Deduction

*Q: The following paragraphs each describe a set of three objects arranged in a fixed order. The statements are logically consistent within each paragraph. On a shelf, there are three books: a white book, a green book, and an orange book. The green book is to the right of the white book. The orange book is the rightmost. Options: (A) The white book is the leftmost. (B) The green book is the leftmost. (C) The orange book is the leftmost. Attempt: Let's think step by step. Let "??" represent 0 or more objects, and "?" represent exactly 1 object.* (1) The green book is to the right of the white book: "(left) ?? white ?? green ?? (right)". (2) The orange book is the rightmost: "(left) ?? orange (right)". (3) There are in total three books: a white book, a green book, and an orange book. (4) Combining (1) and (2) we get the following ordering: "(left) ?? white ?? green ?? orange (right)". (5) Combining (3) and (4) we get the following ordering: "(left) white green orange (right)". (6) According to this ordering, the leftmost book is the white book.

(Final response) So the answer is (A).

Table A10: Examples of generated rationales for Logical Deduction by prompting Codex [\(Chen et al.,](#page-8-2) [2021\)](#page-8-2). Question and prompts are written in *gray italics*, and the generated step-by-step rationale is shown in black.

<span id="page-18-0"></span>

Table A11: Examples of an incorrect attempt generated by a small model, followed by its feedback generated by either an LLM (Codex or text-davinci-003) or a script (indicated by  $^{\dagger}$ ) for each task. Input question is written in black, a generated attempt is written in blue, and its feedback is written in cyan.

<span id="page-19-0"></span>

Table A12: Prompt used for generating improvement for Multistep Arithmetic. The generated feedback is then formatted as "Step 1 to step {earliest error step - 1} is correct. In step {earliest error step} the part '{error segment}' is incorrect. This is because '{error reason}'." In general, we used three-shot prompting. Parts that will be generated are highlighted in blue. Due to limited space, we present one example used for each task. Please refer to our code repository for the full prompt.

<span id="page-20-0"></span>

Prompt Type	Prompt Example		
Get Improvement	Q: Sort the following words alphabetically:		
	List: cosh inferno every foyer coterie mcfadden halifax		
	Answer: Let's think step by step.		
	(1) The first letter: "cosh"="c" (3), "inferno"="i" (9), "every"="e" (5), "foyer"="f" (6),		
	"coterie"="c" (3), "mcfadden"="m" (13), "halifax"="h" (8).		
	(2) We now have: (3) "cosh"? "coterie" < (5) "every" < (6) "foyer" < (8) "halifax" <		
	$(9)$ "inferno" < $(13)$ "mcfadden".		
	(3) Now sort this subpart ["cosh"? "coterie"] by looking at their second letters:		
	"cosh"="o" $(15)$ , "coterie"="o" $(15)$ .		
	$(3.1)$ We now have: $(15)$ ["cosh" ? "coterie"].		
	(3.2) Now sort this subpart ["cosh"? "coterie"] by looking at their third letters:		
	"cosh"="s" (19), "coterie"="c" (3).		
	$(3.3)$ We now have: (3) "coterie" < (19) "cosh".		
	$(3.4)$ Hence, we have "coterie" < "cosh".		
	$(4)$ Hence, we have "coterie" < "cosh" < "every" < "foyer" < "halifax" < "inferno" < "mcfadden".		
	(Final response) So the answer is: coterie cosh every foyer halifax inferno mcfadden. [END]		
	Feedback: Step (1) to (3.1) are correct. In step (3.2) the part " "coterie"="c" (3) " is incorrect. This is because the third letter of "coterie" should be "t".		
	Updated Answer: Let's think step by step.		
	(1) The first letter: "cosh"="c" (3), "inferno"="i" (9), "every"="e" (5), "foyer"="f" (6),		
	"coterie"="c" (3), "mcfadden"="m" (13), "halifax"="h" (8).		
	(2) We now have: (3) ["cosh"? "coterie"] < (5) "every" < (6) "foyer" < (8) "halifax" <		
	$(9)$ "inferno" < $(13)$ "mcfadden".		
	(3) Now sort this subpart ["cosh"? "coterie"] by looking at their second letters:		
	"cosh"="o" $(15)$ , "coterie"="o" $(15)$ .		
	$(3.1)$ We now have: $(15)$ ["cosh"? "coterie"].		
	(3.2) Now sort this subpart ["cosh"? "coterie"] by looking at their third letters:		
	"cosh"="s" (19), "coterie"="t" (20).		
	$(3.3)$ We now have: $(19)$ "cosh" < $(20)$ "coterie".		
	$(3.4)$ Hence, we have "cosh" < "coterie".		
	$(4)$ Hence, we have "cosh" < "coterie" < "every" < "foyer" < "halifax" < "inferno" < "mcfadden".		
	(Final response) So the answer is: cosh coterie every foyer halifax inferno mcfadden. [END]		

Table A13: Prompt used for generating improvement for Word Sorting. The generated feedback is then formatted as "Step 1 to step {earliest error step - 1} is correct. In step {earliest error step} the part '{error segment}' is incorrect. This is because '{error reason}'." In general, we used three-shot prompting. Parts that will be generated are highlighted in blue. Due to limited space, we present one example used for each task. Please refer to our code repository for the full prompt.

<span id="page-21-0"></span>

Table A14: Prompt used for generating feedback and improvement for Date Understanding. The generated feedback is then formatted as "Step 1 to step  $\{$  first error step - 1 $\}$  is correct. In step  $\{$  first error step $\}$  the part  $\{$  error part $\}$ ' is incorrect. This is because '{error reason}'." In general, we used three-shot prompting. Parts that will be generated are highlighted in blue. Due to limited space, we present one example used for each task. Please refer to our code repository for the full prompt.

<span id="page-22-0"></span>

Table A15: Prompt used for generating feedback and improvement for Logical Deduction. The generated feedback is then formatted as "Step 1 to step {first error step - 1} is correct. In step {first error step} the part '{error part}' is incorrect. This is because '{error reason}'." In general, we used three-shot prompting. Parts that will be generated are highlighted in blue. Due to limited space, we present one example used for each task. Please refer to our code repository for the full prompt.