Symbolic Policy Distillation for Interpretable Reinforcement Learning

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Abstract

Deep reinforcement learning (RL) policies based on deep neural networks (DNNs) achieve strong performance but are often opaque, hindering transparency, interpretability, and safe deployment. Interpretable policy distillation seeks to transfer knowledge from these black-box DNN policies into simpler, human-understandable forms. While prior work has extensively studied performance retention, fidelity to the original DNN policies has remained underexplored, which is crucial for ensuring that the distilled policies faithfully capture the underlying decision-making logic. To address this gap, we propose GM-DAGGER, a novel data aggregation method that employs a geometric mean loss to preserve fidelity without compromising performance. Building on this, we introduce Symbolic Policy Interpretable Distillation (SPID), a framework that distills DNN policies into symbolic analytical equations via symbolic regression. Through extensive experiments across six environments and five deep RL algorithms, we show that SPID achieves superior preservation of both performance and fidelity, while providing interpretable policies that provide mechanistic insights into policy behavior and training dynamics.

1 Introduction

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Deep reinforcement learning (RL) has achieved impressive success in a wide range of sequential decision-making problems using deep neural networks (DNNs) as powerful function approximators for policies [31, 43, 11]. Despite their strong feature extraction and generalization abilities, these high-dimensional, non-linear DNN models pose major challenges for transparency, interpretability, and deployment[50]. In particular, these policies are typically regarded as "black-box" models [55], and remain computationally expensive to train, sample inefficient, and vulnerable to biases, safety risks, and adversarial perturbations [17, 52, 41].

To mitigate these challenges, there has been growing attention towards interpretable RL, with a 24 particular focus on designing policies that are analytically tractable. Symbolic policies, represented as compact mathematical expressions composed of variables, constants, and symbolic operators, 26 offer an alternative to black-box DNN policies. Due to their analytical tractability, symbolic policies 27 provide mechanistic interpretability and facilitate formal verification of RL agent behavior. *Policy* 28 distillation [38] is another technique used to interpret the DNN policies by transferring knowledge 29 from a complex policy to a simple surrogate policy. Although policy distillation has been used 30 extensively to compress large models (e.g., teacher) into smaller models (e.g., student) while pre-31 serving expert-level performance, distilled models often do not provide meaningful insights into the underlying decision-making process. Therefore, recent work started to explore symbolic policy 33 learning as a route toward interpretable and deployable RL. For instance, Verma et al. (2018) [50] 34 proposed PIRL, a programmatically interpretable RL framework designed to generate policies that 35 are both interpretable and verifiable. Hein et al. (2018) in [16] proposed GPRL, which uses genetic

programming to evolve interpretable algebraic policy equations through model-based reinforcement learning. While providing interpretable solutions, these approaches typically suffer from low data efficiency and performance degradation compared to standard deep RL baselines.

To address this critical gap, we propose symbolic policy distillation for interpretable RL. Our goal 40 is to distill a symbolic policy from a pretrained DNN policy such that it preserves performance 41 and faithfully reproduces its decision-making behavior. This allows the distilled symbolic policy to not only serve as an interpretable surrogate for inspecting the teacher DNN policy, but also to act 43 as a standalone, efficient, and deployable agent in real-world problems. Our approach is based on 44 imitation learning, where state-action pairs from a DNN policy are used to train a symbolic policy in 45 a supervised learning fashion. A major challenge in this setting is distribution shift [34], which arises 46 when the symbolic policy encounters states that deviate from those used during training, potentially 47 leading to inaccurate and unfaithful behavior. To address this distributional shift, previous methods 48 employ DAGGER [36], which iteratively collects action labels on states generated by the symbolic 49 policy itself. However, standard DAGGER often results in overly complex symbolic expressions or reward degradation, as it treats all mistakes equally, regardless of their importance.

To overcome this issue, Bastani et al. (2018) [1] introduced *Q*-DAGGER, which uses information from the DNN policy's *Q*-function to prioritize critical states. Although *Q*-DAGGER improves performance, optimizing only for a single performance metric such as cumulative reward may result in symbolic policies that deviate substantially from the original DNN behavior, which is an undesirable property for interpretable RL. To create a balance trade-off between performance and faithfulness, we propose GM-DAGGER, which uses a geometric mean loss to jointly optimize these two criteria. Building on this, we introduce Symbolic Policy Interpretable Distillation (SPID), which distills any DNN policy into a symbolic policy that preserves performance, is faithful, and analytically interpretable.

60 Our contributions are summarized as follows:

- We propose symbolic policy distillation, a novel framework that distills any DNN policy into a compact symbolic policy that offers transparency and interpretability while preserving performance.
- We introduce GM-DAGGER, an imitation learning method that provably balances faithfulness and reward by optimizing a geometric mean objective.
- We develop SPID, which extracts symbolic policies that faithfully reproduce the original DNN behavior while preserving performance.
- We further show that SPID distilling policies at different checkpoints can identify how the successful training achieves and why the bad training fails.

9 2 Related Work

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2.1 Policy Distillation

Policy distillation [38], originally derived from knowledge distillation [18], aims to train smaller and more efficient policies while maintaining expert-level performance. It has emerged as a prominent area within RL that enables the transfer of knowledge across policies and helps the development of more efficient and general agents. For instance, authors in [54] introduced a hierarchical experience replay framework that supports the transfer of multiple expert policies into a single multi-task policy through distillation. Subsequent works have focused on improving the fundamental distillation mechanisms [6], increasing distillation efficiency [45, 33], and learning multiple tasks policy [2, 53, 15], or continual RL [48, 14].

Despite its success, policy distillation suffers from distribution shift, a challenge similar to that in the imitation learning, where the student policy visits states that are not well covered by the expert policy. Several prior works focus on mitigating this issue, including iterative online correction methods such as SMILe [35] and DAGGER [36], distribution matching methods such as GAIL [19], ValueDICE [21], IQ-Learn [10], and regularization-based techniques such as BANs [9].

4 2.2 Symbolic Policies and Interpretable RL

Interpretable symbolic policies in RL can be in different forms, ranging from decision trees [1, 37, 4, 29, 42, 20, 28], rule-based and program-based systems [50, 49, 7, 3, 32, 26], to compact mathematical

and analytical functional forms [22, 12, 51, 23, 25, 56]. For example, PIRL [50] proposes NDPS to 87 learn programmatic policies that are interpretable and verifiable, and Silve et al. (2020) [42] develop 88 differentiable decision trees in an online RL for interpretability. 89

Despite the success of symbolic RL policies, most existing works use learning schemas that are 90 not specifically designed for decision-level interpretability, i.e., understanding the internal decision-91 making process of DNN policies. As a result, the learned symbolic policies are typically optimized 92 for performance (e.g., cumulative rewards) rather than fidelity to the teacher DNN policy. A few 93 works explicitly address distillation in the context of interpretability: VIPER [1] proposes Q-DAGGER 94 that extracts interpretable decision trees from DNN policies with a performance guarantee; PIRL [50] 95 and INTERPRETER [20] both distill DNN policies into symbolic programs or trees. However, these 96 methods often trade off fidelity for performance or interpretability. In contrast, this paper focuses on 97 faithful distillation, which aims to extract symbolic policies that not only preserve performance but 98 also retain high behavioral fidelity to the original DNN policy. 99

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Reinforcement Learning

Reinforcement Learning (RL) problems are commonly formalized as a finite-horizon Markov Decision Process (MDP), defined by the tuple (S, A, P, R, T). Here, S denotes the set of states, A the set of possible actions, $P: S \times A \times S \to [0,1]$ the transition probabilities, and $R: S \times A \to \mathbb{R}$ the reward function. At each time step $t \in \{0, \dots, T-1\}$, an agent in state $s_t \in S$ selects an action $a_t \in A$, receives a reward $r_t = R(s_t, a_t)$, and transitions to the next state s_{t+1} according 105 to $P(s_{t+1}|s_t,a_t)$. Here, the objective is to learn a policy π that maximizes the expected sum of cumulative rewards. In RL, policies can be deterministic, mapping each state to a single action, or stochastic, defining a probability distribution over actions given a state. Moreover, policies are often assumed to be stationary and Markovian, i.e., the action selection depends only on the current state and not on the history. In this paper, we consider policies to be stationary, Markovian, and stochastic.

To formalize state distributions in an MDP, let $d_0^{(\pi)}(s) = \mathbb{I}[s=s_0]$ denote the initial distribution. For t > 0, the state distribution evolves as

$$d_t^{(\pi)}(s) = \sum_{s' \in S} P(s', \pi(s'), s) d_{t-1}^{(\pi)}(s').$$

The average visitation distribution is then given by $d^{(\pi)}(s) = T^{-1} \sum_{t=0}^{T-1} d_t^{(\pi)}(s)$. The cost-to-go of π from s_0 is $J(\pi) = -V_0^{(\pi)}(s_0)$. For a given policy π , the state-value function is defined as

$$V_t^{(\pi)}(s) = R(s, \pi(s)) + \sum_{s' \in S} P(s, \pi(s), s') V_{t+1}^{(\pi)}(s'),$$

where $V_T^{(\pi)}(s)=0$. Similarly, the action-value function is defined as, $Q_t^{(\pi)}(s,a)=R(s,a)+$ $\sum_{s' \in S} P(s, a, s') V_{t+1}^{(\pi)}(s')$. Without loss of generality, we assume that there is a single initial state $s_0 \in S$. Value-based methods aim to approximate the value functions V or Q and implicitly derive 117 118 the optimal policy, typically by acting greedily with respect to the Q-function [31]. On the other hand, 119 policy gradient methods directly optimize a parameterized policy π_{θ} without explicitly estimating 120 Q [46]. In both of these methods, since returns can be noisy, estimating Q or policy gradient 121 methods suffer from high variance and instability. To reduce the variance, the advantage function 122 A(s,a) = Q(s,a) - V(s) is usually employed. Advantage Actor-Critic (A2C) [30] jointly learns a 123 policy π_{θ} (e.g., actor) and a value function \hat{V}_{ϕ} (e.g., critic), where the critic provides feedback to the 124 actor. Proximal Policy Optimization (PPO) [40] further improves the stability via a clipped surrogate 125 objective function. The overestimation bias and sample efficiency further improve in Twin Delayed 126 Deep Deterministic (TD3) [8] and Soft Actor-Critic (SAC) [13]. In this paper, we consider all these 127 algorithms, which include policy-based and a combination of actor-critic and value-based methods. 128

3.2 Dataset Aggregation

Dataset Aggregation or DAGGER [36] addresses the distribution shift in imitation learning, where a 130 policy $\hat{\pi}$ trained on expert demonstrations $d^{(\pi^*)}$ encounters a different state distribution $d^{(\hat{\pi})}$ during

Algorithm 1 Symbolic Policy Interpretable Distillation (SPID).

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1: procedure GM-DAGGER((S, A, P, R), \pi^*, Q^*, \alpha, \beta, \epsilon, M, N)
             Initialize dataset \mathcal{D} \leftarrow \emptyset
 2:
 3:
             Initialize policy \hat{\pi}_0 \leftarrow \pi^*
             for i = 0 to N do
 4:
 5:
                   Execute policy \pi_i according to 5
                    Collect M trajectories \mathcal{D}_i = \{(s, \pi^*(s)) \sim \pi_i(s)\}
 6:
                    Compute GM loss components:
 7:
                         g^{p}(s,\hat{\pi}) = V^{*}(s) - Q^{*}(s,\hat{\pi}(s)) + \alpha
 8:
                   g^{f}(s,\hat{\pi}) = \|\hat{\pi}(s) - \pi^{*}(s)\|^{2} + \epsilon
\ell(s,\hat{\pi}) = \sqrt{g^{p}(s,\hat{\pi}(s)) \times g^{f}(s,\hat{\pi}(s))}
Aggregate dataset \mathcal{D} \leftarrow \mathcal{D} \cup \mathcal{D}_{i}
 9:
10:
11:
                    Train symbolic policy \hat{\pi}_i \leftarrow \text{SymbolicRegression}(\mathcal{D}, \ell(s, \hat{\pi}))
12:
13:
             return Best policy \hat{\pi} \in {\{\hat{\pi}_1, \dots, \hat{\pi}_N\}} on validation
14:
15: end procedure
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execution, leading to compounding errors that can accumulate over time. To reduce this issue, DAG-GER iteratively collects trajectories under the current policy $\hat{\pi}$, queries the expert policy π^* for correct actions on these newly visited states, and aggregates this with previous datasets to retrain the policy. Thus, the goal of DAGGER becomes to train a policy $\hat{\pi} \in \Pi$ as, $\hat{\pi} = \arg\min_{\pi \in \Pi} \mathbb{E}_{s \sim d^{(\pi)}}[\ell(s,\pi)]$, where the loss function is defined as 0-1 loss $\ell(s,\pi) = \mathbb{I}[\pi(s) \neq \pi^*(s)]$ or the surrogate loss function, which provides a convex upper bound of the 0-1 loss.

Q-DAGGER [1] extends DAGGER by leveraging the expert policy's Q-function to prioritize learning on critical states where action choices significantly impact the future performance. Q-DAGGER enhances the loss function to focus on the cost-to-go difference between optimal and chosen actions

$$\ell_t(s,\pi) = V_t^{(\pi^*)}(s) - Q_t^{(\pi^*)}(s,\pi(s)). \tag{1}$$

4 Proposed Method

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In this section, we introduced Symbolic Policy Interpretable Distillation (SPID), a framework for distilling deep RL policies into interpretable symbolic representations. The key component of SPID is GM-DAGGER, which is a geometric mean variant of DAGGER. This variant provides a principled way to balance performance and faithfulness to the original policy.

Unlike standard multi-objective RL methods, in which we explicitly search for Pareto-optimal policies that can be exponentially large, our method directly learn a single Pareto-optimal policy by incorporating the performance and fidelity objectives into a single regularized loss function. This formulation allows us to train a single symbolic policy that simultaneously achieves strong performance and high fidelity to the teacher policy.

4.1 Geometric Mean Dataset Aggregation

We begin by formalizing the geometric mean loss that derives GM-DAGGER (Geometric Mean Dataset Aggregation). GM-DAGGER extends standard DAGGER [36] and *Q*-DAGGER by integrating performance and fidelity objectives into a single balanced objective.

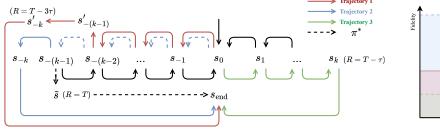
Performance gap. We evaluate the performance difference between the distilled policy π relative to the teacher policy π^* in the form of

$$g_t^p(s,\pi) = V_t^{(\pi^*)}(s) - Q_t^{(\pi^*)}(s,\pi(s)) + \alpha,$$
 (2)

where V^{π^*} and Q^{π^*} are the teacher's value and Q-functions, and $\alpha>0$ ensures positivity for the geometric mean. This term directly corresponds to the original Q-DAGGER loss.

Fidelity gap. We quantify the divergence between the distilled policy π and the teacher policy π^* as

$$g_t^f(s,\pi) = ||\pi(s) - \pi^*(s)||^2 + \epsilon,$$
 (3)





- (a) Example showing difference of DAGGER, Q-DAGGER and GM-DAGGER.
- (b) Objective difference.

Figure 1: Illustrative example demonstrating the trade-offs between different imitation learning approaches. (a) A finite-horizon MDP with deterministic transitions showing three sub-optimal trajectories and the optimal teacher policy π^* (dashed). Each approach favors different trajectories: DAGGER prefers high-fidelity Trajectory 2, Q-DAGGER favors high-performance Trajectory 3, while GM-DAGGER balances both objectives by selecting Trajectory 1. (b) Pareto frontier illustrating the performance-faithfulness trade-off, where GM-DAGGER achieves a balanced solution between the extremes of pure fidelity and pure performance optimization

where $\epsilon > 0$ is added to prevent the fidelity gap from being 0.

161 **GM-DAGGER loss.** By combining 2 and 3 loss terms, GM-DAGGER defines

$$\ell_t(s,\pi) = \sqrt{g_t^p(s,\pi) \cdot g_t^f(s,\pi)}. \tag{4}$$

This formulation of the new loss function makes sure that the distilled policy is efficient as well as faithful. In other words, the poor behavior in either objective cannot be compensated by strong performance in the other, which naturally balances the trade-off. Next, we demonstrate the distinct mechanisms underlying DAGGER, *Q*-DAGGER, and GM-DAGGER.

Proposition 4.1. In a discrete action space finite time MDP, for policy π with disagreements $d(\pi)$ and performance gap $\Delta(\pi)$ over the time horizon T, we have

$$\ell_{\mathrm{DAGGER}} = \frac{d(\pi)}{T}, \ell_{Q\mathrm{-DAGGER}} = \frac{\Delta(\pi)}{T}, \ell_{\mathrm{GM-DAGGER}} = \sqrt{(\frac{\Delta(\pi)}{T} + \alpha)(\frac{d(\pi)}{T} + \epsilon)}.$$

By performing optimization on those loss functions, the algorithms exhibit different preferences:

- DAGGER prioritize behavioral mimicking: $d(\pi_i) < d(\pi_i) \Leftrightarrow \pi_i > \pi_i$.
 - Q-DAGGER prioritize performance: $\Delta(\pi_i) < \Delta(\pi_i) \Leftrightarrow \pi_i > \pi_i$.

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• GM-DAGGER balances fidelity and performance through multiplicative trade-off $(\Delta(\pi_i) + \alpha T)(d(\pi_i) + \epsilon T) < (\Delta(\pi_j) + \alpha T)(d(\pi_j) + \epsilon T) \Leftrightarrow \pi_i \succ \pi_j.$

Example 4.2. We make the gap explicit to demonstrate Proposition 4.1 in an example shown in Figure 1a. Figure 1a shows a simple finite-horizon MDP, with initial state s_0 , deterministic transitions shown in arrows, and with the finite time horizon of T=3(k+1). In this MDP, the possible rewards for each state are $R(s'_{-k}=T-3\tau)$, $R(s_k)=T-\tau$, $R(\tilde{s})=T$, and R(s)=0.

As shown in the Figure 1a, we only consider 4 trajectories named as "Trajectory 1, 2, 3" and " π ". 177 As can be seen, the teacher policy $\pi*$, shown in dashed edges, achieves the optimal trajectory with 178 reward T. Since the perfect imitation is impossible, we mainly focus on the remaining 3 trajectories 179 that deviate from the optimal policy π^* to understand the different characteristics of DAGGER, Q-180 DAGGER, and GM-DAGGER. For straightforward understanding, trajectory 2 can be considered the 181 most faithful trajectory a policy will follow, but it sacrifices significant performance. Trajectory 3, 182 on the other hand, represents the highest performance retention behavior but shows no faithfulness. Trajectory 1 focuses on balancing both faithfulness and performance, with modest sacrifices in each. 185 With the calculation following Proposition 4.1 (detailed calculation in Appendix A), we found

• Dagger:
$$\ell_2^{\mathrm{Dagger}} < \ell_1^{\mathrm{Dagger}} < \ell_3^{\mathrm{Dagger}} \Leftrightarrow \pi_2 \succ \pi_1 \succ \pi_3.$$

$$\qquad \qquad \bullet \ \ Q\text{-Dagger}: \ \ell_3^{Q\text{-Dagger}} < \ell_1^{Q\text{-Dagger}} < \ell_2^{Q\text{-Dagger}} \Leftrightarrow \pi_3 \succ \pi_1 \succ \pi_2.$$

• GM-DAGGER:
$$\ell_1^{\text{GM-DAGGER}} < \ell_2^{\text{GM-DAGGER}} < \ell_3^{\text{GM-DAGGER}} \Leftrightarrow \pi_1 \succ \pi_2 \succ \pi_3$$
.

This shows that, when imitation is imperfect, DAGGER only focus on fidelity while ignore performance and Q-DAGGER favors performance but ignores fidelity. However, GM-DAGGER creates a trade-off and yields a distilled policy that lies on the Pareto front (Figure 1b). This illustrative example demonstrates the main reason and advantage of the GM-DAGGER in providing a single-objective loss that implicitly creates the trade-off between performance and faithfulness.

194 4.2 Symbolic Policy Interpretable Distillation

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We now combine the GM-DAGGER with symbolic regression [27] to propose SPID (shown in Algorithm 1), an approach that aims to distill the teacher's DNN policy into an interpretable analytical symbolic formulation that describes the policy behavior. For the symbolic regression part, we employ the efficient, scalable, and high-performance PySR library [5].

The full training pipeline is as follows. First, we sample state action pairs from π^* , store them in a dataset D, and fit an initial symbolic policy $\hat{\pi}_0$ via symbolic regression. We refer to this as a *Dataset Initialization* step. In practice, at this step, the symbolic policy often performs poorly due to the distribution shift. Recall that, in the symbolic policy distillation, the distribution shift means the symbolic policy $\hat{\pi}_0$ likely follows a completely different trajectory during validation, which remains unseen in π^* 's trajectories. We refer to this as the distribution shift of the symbolic policy $\hat{\pi}_0$

To address this distribution shift problem, we follow the data aggregation principle in DAGGER. At each iteration, we mix the symbolic policy $\hat{\pi}_i$ with the teacher policy π^* using the mixing coefficient β , which provably yeild a hybrid policy as:

$$\pi_i = \beta \pi^* + (1 - \beta)\hat{\pi}_i,\tag{5}$$

where $\beta = 0.5$ in our experiments. We call this *policy mixing* step. After this step, we execute 208 π_i for M trajectories to collect new state-action pairs and store them in the dataset. Subsequently, 209 we compute the performance gap and fidelity gap from (2) and (3) accordingly to compute the 210 GM-DAGGER loss function (4). By minimizing this loss function, our proposed GM-DAGGER improves the overall performance and fidelity, which makes it an optimal choice for interpretability. Finally, in the last step, we retrain a new symbolic policy $\hat{\pi}_{i+1}$ on the aggregated dataset using the 213 symbolic regression (PySR [5]), which ultimately minimizes the GM loss. Our symbolic regression 214 operates via a multi-population evolutionary search algorithm over analytical functions to create a 215 trade-off between fidelity and performance. 216

5 Experimental Result

5.1 Experimental setup

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To evaluate SPID, we perform experiments across six Gymnasium [47] environments, including a 219 range of different problems: CartPole, MountainCar, Pendulum, Acrobot, Reacher, and Swimmer. 220 These environments pose different control challenges from simple balancing to complex multi-body 221 coordination, providing a comprehensive testbed for evaluating the robustness and generalizability of 222 SPID. Moreover, we employ five deep RL algorithms to train teacher policies for distillation with 223 SPID. These algorithms includes on-policy algorithms such as PPO [40], TRPO [39] and off-policy algorithms DDPG [24], SAC [13], and TD3 [8]. For fair evaluation, we compare SPID against three 225 interpretable policy distillation baselines. Our first baseline is the symbolic policy regressions [22], 226 which applies symbolic regression directly on state-action trajectories to obtain closed-form policies. 227 Our second baseline is VIPER [1], a decision tree distillation method with depth limited to 4 to ensure 228 interpretability [44]. (Performance of VIPER without tree depth limits to guarantee interpretability is shown in the Appendix B.) Our third baseline is PIRL [50], which is a programmatically interpretable RL method specifically designed to distill DNN policies to programmatic policies.

Table 1: Performance comparison of policy distillation methods.

	Deep RL Algorithm		Distillation Methods			
Env	Name	Performance	Regression	PIRL	Viper	SPID
CartPole	PPO	1000.0 ± 0.0	576.4 ± 190.2	1000.0 ± 0.0	585.9 ± 229.6	1000.0 ± 0.0
	TRPO	1000.0 ± 0.0	326.3 ± 89.2	1000.0 ± 0.0	265.8 ± 228.9	1000.0 ± 0.0
	DDPG	1000.0 ± 0.0	142.0 ± 122.9	1000.0 ± 0.0	985.0 ± 45.0	1000.0 ± 0.0
	SAC	1000.0 ± 0.0	158.9 ± 30.1	1000.0 ± 0.0	573.2 ± 327.5	$\boldsymbol{1000.0} \pm 0.0$
	TD3	$1000.0 \pm \text{0.0}$	40.4 ± 12.5	997.5 ± 5.8	220.1 ± 13.7	$\boldsymbol{1000.0} \pm 0.0$
MountCar	PPO	91.1 ± 0.1	-146.0 ± 4.4	-12.4 ± 0.0	91.2 ± 0.3	94.7 ± 1.4
	TRPO	93.9 ± 0.0	-55.7 ± 4.9	-9.5 ± 1.3	93.9 ± 0.0	94.4 ± 0.8
	DDPG	93.9 ± 0.3	-59.4 ± 4.8	-7.4 ± 0.6	94.0 ± 0.2	95.0 ± 0.3
	SAC	93.6 ± 0.1	-98.0 ± 2.0	-1.5 ± 1.4	93.8 ± 0.3	93.8 ± 0.7
	TD3	93.8 ± 0.2	-95.7 ± 1.5	-7.4 ± 0.6	93.8 ± 0.2	$\textbf{94.7} \pm 0.2$
Pendulum	PPO	-263.9 ± 119.3	-1255.8 ± 451.2	$-1161.1 \pm \scriptstyle{191.2}$	-903.4 ± 333.8	-253.3 ± 124.5
	TRPO	-181.7 ± 78.2	-1128.6 ± 167.2	-1254.7 ± 209.8	-893.0 ± 402.7	-346.6 \pm 361.0
	DDPG	-155.1 ± 79.0	-1347.5 ± 320.0	-1413.1 ± 28.6	-369.1 ± 252.3	$\textbf{-193.8} \pm 74.2$
	SAC	-145.2 ± 93.1	-1381.7 ± 283.5	-1567.6 ± 64.6	-797.9 ± 324.1	$\textbf{-214.7} \pm 123.5$
	TD3	-170.5 ± 93.8	-1210.1 ± 202.3	$-1563.0 \pm \textbf{46.6}$	-621.5 ± 611.6	-173.3 \pm 111.2
Acrobot	PPO	-37.8 ± 3.3	-79.9 ± 7.3	$-109.3 \pm \textbf{31.3}$	-37.7 ± 4.5	-36.7 \pm 0.5
	TRPO	-40.2 ± 0.4	-117.1 ± 13.2	-92.7 ± 21.8	-44.7 \pm 8.5	-73.8 ± 4.9
	DDPG	-34.5 ± 0.7	-74.7 ± 18.4	-91.0 ± 32.0	-39.4 \pm 4.0	-48.3 ± 6.3
	SAC	-35.0 ± 0.0	-82.0 ± 17.2	-85.6 ± 18.3	-37.6 \pm 3.5	-45.9 ± 1.8
	TD3	-37.3 ± 0.5	-82.5 ± 7.4	-75.2 ± 11.8	-49.9 ± 12.2	-49.5 \pm 4.0
Swimmer	PPO	$356.2 \pm \text{1.4}$	-3.8 ± 30.7	-5.8 ± 21.0	$\textbf{357.7} \pm 2.1$	350.5 ± 3.6
	TRPO	339.0 ± 1.3	30.2 ± 7.3	-4.0 ± 19.7	$\textbf{338.1} \pm 2.0$	$\textbf{338.1} \pm 2.3$
	DDPG	$347.6 \pm {\scriptstyle 1.1}$	172.2 ± 82.6	4.0 ± 19.5	348.0 ± 3.3	$\textbf{354.8} \pm 1.5$
	SAC	349.6 ± 1.3	22.3 ± 4.9	-0.7 ± 22.3	344.0 ± 1.8	$\textbf{345.3} \pm 1.6$
	TD3	355.5 ± 1.5	-20.2 ± 5.6	-9.2 ± 14.7	$351.7 \pm \text{1.8}$	$\textbf{354.2} \pm 1.4$
Reacher	PPO	-5.1 ± 2.0	-25.2 ± 17.9	-11.2 ± 3.8	-5.9 ± 1.7	-5.7 ± 4.2
	TRPO	-5.8 ± 1.9	-26.1 ± 17.6	-11.4 ± 3.5	-7.3 ± 2.3	-6.5 \pm 2.0
	DDPG	-4.7 ± 0.8	-11.4 ± 4.2	-8.8 ± 4.3	-7.0 ± 3.0	$\textbf{-6.4} \pm 2.2$
	SAC	-3.3 ± 1.3	-21.8 ± 11.2	-11.3 ± 1.9	-7.9 ± 2.5	-6.1 \pm 1.7
	TD3	-3.6 ± 1.0	-14.2 ± 1.7	-7.4 ± 4.7	-6.6 ± 2.6	-5.7 ± 3.0

5.2 Main Results

In this section, we present the main experiments of the paper. From these experiments, we try to answer these research questions (A) How effective is SPID in preserving the performance of the teacher policy compared to distillation baselines? (B) To what extent does SPID maintain fidelity to the teacher DNN policy? (C) What kinds of meaningful insights can we extract from symbolic policies? (D) Can symbolic policies provide insights into the training dynamics of deep RL algorithms?

Question (A) To evaluate how effective SPID is in preserving teacher policy performance, we conducted experiments in all six environments and report the mean and standard deviation of returns evaluated on 10 trajectories during testing in Table 1. These results demonstrate that the regression method performs the worst, mainly because of the distribution shift, as it is fitting only to offline trajectories and fails to generalize to novel states. Although PIRL and VIPER mitigate this distribution shift via dataset aggregation, they still struggle in complex control tasks. In contrast, SPID consistently achieves the highest performance in all environments and algorithms. SPID achieves this by combining symbolic regression with GM-DAGGER, which not only mitigates the distribution shift but also produces symbolic policies that remain competitive with the teacher policy.

Question (B) To answer this question, we measure fidelity by computing the trajectory-wise L2 distance between distilled and teacher policy across 10 rollouts with the same initial state s_0 . These results are shown in Table 2, where the smaller L2 distance means more faithfulness of the distilled policy. As expected, regression and PIRL perform poorly because they fail to mimic complex behaviors. VIPER performs better in simple tasks due to the flexibility of decision trees. However,

Table 2: Fidelity comparison of policy distillation methods.

		Distillation Methods			
Environment	Algorithm	Regression	Pirl	Viper	SPID
CartPole	PPO	0.000 ± 0.002	0.000 ± 0.002	0.001 ± 0.003	0.000 ± 0.001
	TRPO	0.002 ± 0.024	0.006 ± 0.031	0.003 ± 0.019	0.002 ± 0.007
	DDPG	0.084 ± 0.044	0.026 ± 0.037	0.015 ± 0.032	$\boldsymbol{0.015} \pm 0.055$
	SAC	0.078 ± 0.061	0.119 ± 0.096	0.059 ± 0.069	0.079 ± 0.166
	TD3	0.300 ± 0.298	0.391 ± 0.294	$\boldsymbol{0.250} \pm 0.298$	0.347 ± 0.269
MountainCar	PPO	0.541 ± 0.604	0.746 ± 0.331	0.178 ± 0.391	0.315 ± 0.234
	TRPO	0.598 ± 0.441	0.758 ± 0.356	0.388 ± 0.625	$\boldsymbol{0.158} \pm 0.193$
	DDPG	0.679 ± 0.505	0.754 ± 0.361	0.311 ± 0.488	0.164 ± 0.196
	SAC	0.456 ± 0.535	0.722 ± 0.358	0.169 ± 0.391	$\boldsymbol{0.084} \pm 0.104$
	TD3	0.396 ± 0.514	0.772 ± 0.327	0.315 ± 0.548	0.244 ± 0.262
Pendulum	PPO	0.258 ± 0.461	0.312 ± 0.406	0.124 ± 0.266	2.431 ± 5.125
	TRPO	0.242 ± 0.586	$0.242 \pm \scriptstyle{0.482}$	0.242 ± 0.455	0.224 ± 0.370
	DDPG	0.389 ± 0.856	$0.374 \pm \textbf{0.685}$	1.663 ± 0.643	$\boldsymbol{0.347} \pm 0.715$
	SAC	0.295 ± 0.658	$0.184 \pm \scriptstyle{0.512}$	1.720 ± 0.581	$\textbf{0.151} \pm 0.496$
	TD3	3.317 ± 1.621	0.306 ± 0.634	0.237 ± 0.777	0.212 ± 0.499
Acrobot	PPO	1.167 ± 0.802	0.981 ± 0.619	$\boldsymbol{0.078} \pm 0.462$	$0.219 \pm \textbf{0.718}$
	TRPO	0.843 ± 0.703	0.631 ± 0.481	$\boldsymbol{0.218} \pm 0.267$	0.513 ± 0.506
	DDPG	1.245 ± 0.870	$0.893 \pm \scriptstyle 0.691$	0.437 ± 0.944	$\boldsymbol{0.113} \pm 0.071$
	SAC	0.868 ± 0.524	$0.684 \pm \scriptstyle{0.451}$	$0.893 \pm \scriptstyle 0.691$	0.482 ± 0.497
	TD3	1.063 ± 0.711	0.795 ± 0.592	0.931 ± 0.699	0.457 ± 0.790
Swimmer	PPO	0.228 ± 0.285	1.331 ± 0.130	1.333 ± 0.129	0.097 ± 0.099
	TRPO	0.254 ± 0.208	1.258 ± 0.181	1.260 ± 0.179	$\boldsymbol{0.107} \pm 0.148$
	DDPG	0.296 ± 0.192	1.381 ± 0.077	1.381 ± 0.077	$\boldsymbol{0.071} \pm 0.120$
	SAC	0.196 ± 0.179	1.194 ± 0.125	1.193 ± 0.125	$\boldsymbol{0.071} \pm 0.088$
	TD3	0.235 ± 0.253	1.362 ± 0.114	1.362 ± 0.114	$\boldsymbol{0.119} \pm 0.166$
Reacher	PPO	0.232 ± 0.208	0.071 ± 0.056	0.074 ± 0.064	0.070 ± 0.063
	TRPO	0.682 ± 0.967	$0.076 \pm \textbf{0.093}$	0.068 ± 0.090	$\boldsymbol{0.066} \pm 0.075$
	DDPG	0.558 ± 3.703	$\boldsymbol{0.068} \pm 0.080$	0.083 ± 0.093	0.109 ± 0.144
	SAC	0.140 ± 0.161	$0.110 \pm \scriptstyle{0.081}$	0.078 ± 0.097	$\boldsymbol{0.077} \pm 0.083$
	TD3	0.320 ± 0.227	0.097 ± 0.106	$\boldsymbol{0.078} \pm 0.091$	0.095 ± 0.159

SPID outperforms all baselines, achieving the lowest policy divergence across tasks. This again validates that our method effectively aligns with both teacher behavior and task performance.

Question (C) To answer (C), we run experiments with SPID to distill policies. Table 3 presents representative policies distilled by SPID in the CartPole environment (with results for all environments provided in Appendix C). These results show that SPID produces compact symbolic expressions that enable mechanistic understanding. Moreover, the distilled expressions are straightforward to interpret and readily deployable.

For example, in CartPole, the TRPO policy, unlike PPO, does not rely on the position feature s_0 , instead basing its decisions on the remaining three features. To validate this, we mask the CartPole environment by removing s_0 and rerun TRPO policy. Our results show that this omission does not degrade performance, as the TRPO on this modified environment yields nearly identical returns (994.9 \pm 8.43). Although this finding is important in understanding the underlying model and reducing the state space, it also exposes potential risks. To show this, we perform a deeper analysis on the vulnerability under perturbations, where velocity $s_1 > 1.3$ and TRPO fails miserably with performance dropping to 5.0 ± 0.0 . Such analyses, which are impossible to obtain from black-box teacher DNN policies, demonstrate how symbolic distillation can uncover brittle strategies and inform safer deployment rather than simply deploying a DNN-based policy.

Question (D) To investigate whether symbolic policies provide insights into training dynamics and failure modes, we perform experiments with PPO on *CartPole* and *MountainCar*. Figure 2 demonstrates the PPO training on these environments. In *CartPole* (Figure 2a), PPO fails to learn anything during the first 300 episodes. At this stage, SPID reveals that the policy relies primarily on

Table 3: Distilled symbolic policy for CartPole environment.

Environment	Algorithm	Policy Expression from SPID
CartPole		$a = (s_2 + (((0.055 - (-0.193) \cdot (s_3 + s_0))) - 0.135s_1)) * 1.697$
	TRPO	$a = (s_3 + (s_1 + s_2)) \cdot (4.401 - (-0.804 - s_1)^2)$
	DDPG	$a = ((s_3 \cdot (-0.098)) - s_2) \cdot (-20.292)$
	SAC	$a = (2.359 - (s_3 + 0.825)^4) \cdot ((s_2 \cdot 3.526) + s_3)$
	TD3	$a = (s_1 + 2.551) \cdot ((s_3 + s_2) + s_1)$

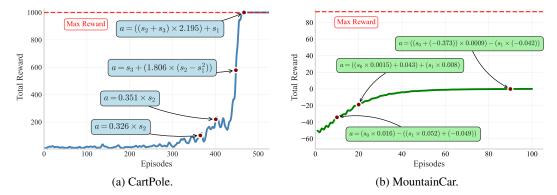


Figure 2: Training dynamics analysis through symbolic policy distillation.

angle-based control (e.g., s_2). As training progresses, PPO gradually incorporates velocity (s_1) and cart position (s_3), which leads to high returns and improved stability. This trajectory of symbolic expressions provides an interpretable and transparent perspective of how the policy evolves during training. In contrast, PPO fails in *MountainCar*, converging to near-zero returns. This failure corresponds to a form of *reward hacking*, where rather than pursuing the sparse terminal reward of reaching the goal, the agent minimizes the penalty term $-0.1a^2$ by avoiding large action values. This behavior is reflected in Figure 2b, where the learned coefficients shrink over time, and PPO never learns to solve the task. Interestingly, such investigations, which are only possible through SPID, directly provide fixes such as reward shaping, increased rollout horizons, or entropy regularization, which are difficult to identify from a black-box teacher DNN policy.

6 Conclusions

In this paper, we addressed the problem of performance-fidelity trade-off in interpretable policy distillation. We proposed GM-DAGGER, which employs a geometric mean loss to optimize performance and fidelity. Building on this, we introduce SPID, a framework that distills symbolic policies that are both faithful and efficient. Experiments across six environments with five deep RL algorithms show that SPID preserves performance and fidelity while providing interpretable policies that reveal underlying mechanistic decision-making and training dynamics.

Limitations and future work. Our paper focuses on continuous control tasks with physical state representations. In future, we plan to extend SPID to settings with high-dimensional inputs (e.g., raw images) that require feature extraction, potentially via neural encoders, before symbolic distillation. Moreover, while symbolic policies are interpretable, this advantage gradually weakens as task complexity increases. Therefore, developing methods to maintain interpretability in complex settings remains an important area for future research.

References

[1] Osbert Bastani, Yewen Pu, and Armando Solar-Lezama. Verifiable reinforcement learning via policy extraction. *Advances in neural information processing systems*, 31, 2018.

- [2] Glen Berseth, Cheng Xie, Paul Cernek, and Michiel Van de Panne. Progressive reinforcement learning with distillation for multi-skilled motion control. In *International Conference on Learning Representations*, 2018.
- [3] Subhajit Chaudhury, Sarathkrishna Swaminathan, Daiki Kimura, Prithviraj Sen, Keerthiram Murugesan, Rosario Uceda-Sosa, Michiaki Tatsubori, Achille Fokoue, Pavan Kapanipathi, Asim Munawar, and Alexander Gray. Learning symbolic rules over Abstract Meaning Representations for textual reinforcement learning. In Anna Rogers, Jordan Boyd-Graber, and Naoaki Okazaki, editors, *Proceedings of the 61st Annual Meeting of the Association for Computational Linguistics* (Volume 1: Long Papers), pages 6764–6776, Toronto, Canada, July 2023. Association for Computational Linguistics.
- Vinícius G. Costa, Jorge Pérez-Aracil, Sancho Salcedo-Sanz, and Carlos E. Pedreira. Evolving interpretable decision trees for reinforcement learning. *Artif. Intell.*, 327(C), February 2024.
- [5] Miles Cranmer. Interpretable machine learning for science with pysr and symbolic regression. jl. arXiv preprint arXiv:2305.01582, 2023.
- [6] Wojciech M Czarnecki, Razvan Pascanu, Simon Osindero, Siddhant Jayakumar, Grzegorz
 Swirszcz, and Max Jaderberg. Distilling policy distillation. In *The 22nd international conference* on artificial intelligence and statistics, pages 1331–1340. PMLR, 2019.
- [7] Quentin Delfosse, Hikaru Shindo, Devendra Dhami, and Kristian Kersting. Interpretable and
 explainable logical policies via neurally guided symbolic abstraction. *Advances in Neural Information Processing Systems*, 36:50838–50858, 2023.
- [8] Scott Fujimoto, Herke Hoof, and David Meger. Addressing function approximation error in actor-critic methods. In *International conference on machine learning*, pages 1587–1596. PMLR, 2018.
- [9] Tommaso Furlanello, Zachary Lipton, Michael Tschannen, Laurent Itti, and Anima Anandkumar.
 Born again neural networks. In Jennifer Dy and Andreas Krause, editors, *Proceedings of the*35th International Conference on Machine Learning, volume 80 of Proceedings of Machine
 Learning Research, pages 1607–1616. PMLR, 10–15 Jul 2018.
- [10] Divyansh Garg, Shuvam Chakraborty, Chris Cundy, Jiaming Song, and Stefano Ermon. Iq-learn:
 Inverse soft-q learning for imitation. Advances in Neural Information Processing Systems,
 34:4028–4039, 2021.
- Shixiang Gu, Ethan Holly, Timothy Lillicrap, and Sergey Levine. Deep reinforcement learning for robotic manipulation with asynchronous off-policy updates. In *2017 IEEE international conference on robotics and automation*, pages 3389–3396. IEEE, 2017.
- Jiaming Guo, Rui Zhang, Shaohui Peng, Qi Yi, Xing Hu, Ruizhi Chen, Zidong Du, Ling Li, Qi Guo, Yunji Chen, et al. Efficient symbolic policy learning with differentiable symbolic expression. *Advances in neural information processing systems*, 36:36278–36304, 2023.
- Tuomas Haarnoja, Aurick Zhou, Kristian Hartikainen, George Tucker, Sehoon Ha, Jie Tan, Vikash Kumar, Henry Zhu, Abhishek Gupta, Pieter Abbeel, et al. Soft actor-critic algorithms and applications. *arXiv preprint arXiv:1812.05905*, 2018.
- Muhammad Burhan Hafez and Kerim Erekmen. Continual deep reinforcement learning with task-agnostic policy distillation. *Scientific Reports*, 14(1):31661, 2024.
- [15] Abhinav Narayan Harish, Larry Heck, Josiah P. Hanna, Zsolt Kira, and Andrew Szot. Reinforcement learning via auxiliary task distillation. In *Computer Vision ECCV 2024: 18th European Conference, Milan, Italy, September 29–October 4, 2024, Proceedings, Part LXXXI*, page 214–230, Berlin, Heidelberg, 2024. Springer-Verlag.
- [16] Daniel Hein, Steffen Udluft, and Thomas A Runkler. Interpretable policies for reinforcement
 learning by genetic programming. *Engineering Applications of Artificial Intelligence*, 76:158–
 169, 2018.

- [17] Peter Henderson, Riashat Islam, Philip Bachman, Joelle Pineau, Doina Precup, and David
 Meger. Deep reinforcement learning that matters. In *Proceedings of the AAAI conference on artificial intelligence*, volume 32, 2018.
- [18] Geoffrey Hinton, Oriol Vinyals, and Jeff Dean. Distilling the knowledge in a neural network. arXiv preprint arXiv:1503.02531, 2015.
- Jonathan Ho and Stefano Ermon. Generative adversarial imitation learning. In *Proceedings of the 30th International Conference on Neural Information Processing Systems*, NIPS'16, page 4572–4580, Red Hook, NY, USA, 2016. Curran Associates Inc.
- Hector Kohler, Quentin Delfosse, Riad Akrour, Kristian Kersting, and Philippe Preux. Interpretable and editable programmatic tree policies for reinforcement learning. *arXiv preprint* arXiv:2405.14956, 2024.
- Ilya Kostrikov, Ofir Nachum, and Jonathan Tompson. Imitation learning via off-policy distribution matching. In *International Conference on Learning Representations*, 2020.
- Mikel Landajuela, Brenden K Petersen, Sookyung Kim, Claudio P Santiago, Ruben Glatt,
 Nathan Mundhenk, Jacob F Pettit, and Daniel Faissol. Discovering symbolic policies with deep
 reinforcement learning. In *International Conference on Machine Learning*, pages 5979–5989.
 PMLR, 2021.
- Peilang Li, Umer Siddique, and Yongcan Cao. From explainability to interpretability: Interpretable reinforcement learning via model explanations. In *Reinforcement Learning Conference*, 2025.
- [24] Timothy P Lillicrap, Jonathan J Hunt, Alexander Pritzel, Nicolas Heess, Tom Erez, Yuval Tassa,
 David Silver, and Daan Wierstra. Continuous control with deep reinforcement learning. arXiv preprint arXiv:1509.02971, 2015.
- [25] Guiliang Liu, Oliver Schulte, Wang Zhu, and Qingcan Li. Toward interpretable deep reinforcement learning with linear model u-trees. In *Machine Learning and Knowledge Discovery in Databases: European Conference, ECML PKDD 2018, Dublin, Ireland, September 10–14*, 2018, Proceedings, Part II, page 414–429, Berlin, Heidelberg, 2018. Springer-Verlag.
- ³⁷⁴ [26] Zhihao Ma, Yuzheng Zhuang, Paul Weng, Hankz Hankui Zhuo, Dong Li, Wulong Liu, and Jianye Hao. Learning symbolic rules for interpretable deep reinforcement learning, 2021.
- Nour Makke and Sanjay Chawla. Interpretable scientific discovery with symbolic regression: a review. *Artificial Intelligence Review*, 57(1):2, 2024.
- [28] Sascha Marton, Tim Grams, Florian Vogt, Stefan Lüdtke, Christian Bartelt, and Heiner Stucken schmidt. Mitigating information loss in tree-based reinforcement learning via direct optimization,
 2025.
- [29] Stephanie Milani, Zhicheng Zhang, Nicholay Topin, Zheyuan Ryan Shi, Charles Kamhoua,
 Evangelos E. Papalexakis, and Fei Fang. Maviper: Learning decision tree policies for inter pretable multi-agent reinforcement learning. In *Machine Learning and Knowledge Discovery in Databases: European Conference, ECML PKDD 2022, Grenoble, France, September 19–23*,
 2022, Proceedings, Part IV, page 251–266, Berlin, Heidelberg, 2022. Springer-Verlag.
- [30] Volodymyr Mnih, Adria Puigdomenech Badia, Mehdi Mirza, Alex Graves, Timothy Lillicrap,
 Tim Harley, David Silver, and Koray Kavukcuoglu. Asynchronous methods for deep reinforce ment learning. In Maria Florina Balcan and Kilian Q. Weinberger, editors, *Proceedings of The* 33rd International Conference on Machine Learning, volume 48 of Proceedings of Machine
 Learning Research, pages 1928–1937, New York, New York, USA, 20–22 Jun 2016. PMLR.
- [31] Volodymyr Mnih, Koray Kavukcuoglu, David Silver, Andrei A. Rusu, Joel Veness, Marc G.
 Bellemare, Alex Graves, Martin Riedmiller, Andreas K. Fidjeland, Georg Ostrovski, Stig Petersen, Charles Beattie, Amir Sadik, Ioannis Antonoglou, Helen King, Dharshan Kumaran, Daan
 Wierstra, Shane Legg, and Demis Hassabis. Human-level control through deep reinforcement learning. *Nature*, 518:529–533, 2015.

- 396 [32] Wenjie Qiu and He Zhu. Programmatic reinforcement learning without oracles. In *International Conference on Learning Representations*, 2022.
- [33] Xinghua Qu, Yew Soon Ong, Abhishek Gupta, Pengfei Wei, Zhu Sun, and Zejun Ma. Importance prioritized policy distillation. In *Proceedings of the 28th ACM SIGKDD Conference on Knowledge Discovery and Data Mining*, KDD '22, page 1420–1429, New York, NY, USA, 2022. Association for Computing Machinery.
- [34] Joaquin Quiñonero-Candela, Masashi Sugiyama, Anton Schwaighofer, and Neil D. Lawrence.
 Dataset Shift in Machine Learning. MIT Press, 2009.
- Isolate Teh and Mike Titterington, editors, Proceedings of the Thirteenth International Conference on Artificial Intelligence and Statistics, volume 9 of Proceedings of Machine Learning Research, pages 661–668, Chia Laguna Resort, Sardinia, Italy, 13–15 May 2010. PMLR.
- 408 [36] Stephane Ross, Geoffrey Gordon, and Drew Bagnell. A reduction of imitation learning and
 409 structured prediction to no-regret online learning. In Geoffrey Gordon, David Dunson, and
 410 Miroslav Dudík, editors, Proceedings of the Fourteenth International Conference on Artificial
 411 Intelligence and Statistics, volume 15 of Proceedings of Machine Learning Research, pages
 412 627–635, Fort Lauderdale, FL, USA, 11–13 Apr 2011. PMLR.
- 413 [37] Aaron M. Roth, Nicholay Topin, Pooyan Jamshidi, and Manuela Veloso. Conservative q-414 improvement: Reinforcement learning for an interpretable decision-tree policy, 2019.
- [38] Andrei A Rusu, Sergio Gomez Colmenarejo, Caglar Gulcehre, Guillaume Desjardins, James
 Kirkpatrick, Razvan Pascanu, Volodymyr Mnih, Koray Kavukcuoglu, and Raia Hadsell. Policy
 distillation. arXiv preprint arXiv:1511.06295, 2015.
- [39] John Schulman, Sergey Levine, Pieter Abbeel, Michael Jordan, and Philipp Moritz. Trust
 region policy optimization. In *International conference on machine learning*, pages 1889–1897.
 PMLR, 2015.
- 421 [40] John Schulman, Filip Wolski, Prafulla Dhariwal, Alec Radford, and Oleg Klimov. Proximal policy optimization algorithms. *arXiv preprint arXiv:1707.06347*, 2017.
- [41] Umer Siddique, Paul Weng, and Matthieu Zimmer. Learning fair policies in multi-objective
 (deep) reinforcement learning with average and discounted rewards. In *International Conference* on Machine Learning, pages 8905–8915. PMLR, 2020.
- 426 [42] Andrew Silva, Matthew Gombolay, Taylor Killian, Ivan Jimenez, and Sung-Hyun Son. Op427 timization methods for interpretable differentiable decision trees applied to reinforcement
 428 learning. In *International conference on artificial intelligence and statistics*, pages 1855–1865.
 429 PMLR, 2020.
- [43] David Silver, Julian Schrittwieser, Karen Simonyan, Ioannis Antonoglou, Aja Huang, Arthur
 Guez, Thomas Hubert, Lucas Baker, Matthew Lai, Adrian Bolton, Yutian Chen, Timothy
 Lillicrap, Fan Hui, Laurent Sifre, George van den Driessche, Thore Graepel, and Demis
 Hassabis. Mastering the game of go without human knowledge. *Nature*, 550:354–359, 2017.
- [44] Victor Feitosa Souza, Ferdinando Cicalese, Eduardo Laber, and Marco Molinaro. Decision trees
 with short explainable rules. *Advances in neural information processing systems*, 35:12365–
 12379, 2022.
- [45] Giacomo Spigler. Proximal policy distillation. Transactions on Machine Learning Research,
 2025.
- 439 [46] R. S. Sutton, D. McAllester, S. Singh, and Y. Mansour. Policy gradient methods for reinforce-440 ment learning with function approximation. In *Advances in Neural Information Processing* 441 *Systems 12*, pages 1057–1063, 2000.
- [47] Mark Towers, Ariel Kwiatkowski, Jordan Terry, John U Balis, Gianluca De Cola, Tristan Deleu,
 Manuel Goulao, Andreas Kallinteris, Markus Krimmel, Arjun KG, et al. Gymnasium: A
 standard interface for reinforcement learning environments. arXiv preprint arXiv:2407.17032,
 2024.

- [48] René Traoré, Hugo Caselles-Dupré, Timothée Lesort, Te Sun, Guanghang Cai, Natalia Díaz Rodríguez, and David Filliat. Discorl: Continual reinforcement learning via policy distillation.
 arXiv preprint arXiv:1907.05855, 2019.
- [49] Dweep Trivedi, Jesse Zhang, Shao-Hua Sun, and Joseph J Lim. Learning to synthesize programs
 as interpretable and generalizable policies. Advances in neural information processing systems,
 34:25146–25163, 2021.
- 452 [50] Abhinav Verma, Vijayaraghavan Murali, Rishabh Singh, Pushmeet Kohli, and Swarat Chaudhuri.
 453 Programmatically interpretable reinforcement learning. In *International conference on machine learning*, pages 5045–5054. PMLR, 2018.
- [51] Maxime Wabartha and Joelle Pineau. Piecewise linear parametrization of policies: Towards
 interpretable deep reinforcement learning. In *The Twelfth International Conference on Learning Representations*, 2024.
- 458 [52] Mingkang Wu, Umer Siddique, Abhinav Sinha, and Yongcan Cao. Offline reinforcement
 459 learning with failure under sparse reward environments. In 2024 IEEE 3rd International
 460 Conference on Computing and Machine Intelligence (ICMI), pages 1–5. IEEE, 2024.
- [53] Charles Xu, Qiyang Li, Jianlan Luo, and Sergey Levine. Rldg: Robotic generalist policy
 distillation via reinforcement learning, 2024.
- [54] Haiyan Yin and Sinno Pan. Knowledge transfer for deep reinforcement learning with hierarchical
 experience replay. In *Proceedings of the AAAI Conference on Artificial Intelligence*, volume 31,
 2017.
- [55] Tom Zahavy, Nir Ben-Zrihem, and Shie Mannor. Graying the black box: Understanding dqns.
 In *International conference on machine learning*, pages 1899–1908. PMLR, 2016.
- [56] Hengzhe Zhang, Aimin Zhou, and Xin Lin. Interpretable policy derivation for reinforcement
 learning based on evolutionary feature synthesis. *Complex & Intelligent Systems*, 6(3):741–753,
 2020.

Detailed Calculation Example 471

Proof. DAGGER 0-1 loss function: The DAGGER loss measures stepwise disagreements with the 472 expert policy: 473

$$\ell_{\mathrm{DAGGER}} = \mathbb{I}[\pi(s) \neq \pi^*(s)]$$

- For Trajectory 1, there are 2 disagreements in the whole trajectory over finite horizon T = 3(k+1).
- The average stepwise loss is: 475

$$\ell_1^{\text{Dagger}} = 2T^{-1}.$$

For Trajectory 2, 1 disagreement occurred, yielding: 476

$$\ell_2^{\text{Dagger}} = T^{-1}.$$

For Trajectory 3, there are T disagreements in the whole trajectory over finite horizon T, giving:

$$\ell_3^{\text{Dagger}} = 1.$$

Comparing these losses, trajectory 2 is preferred by DAGGER:

$$\ell_2^{\rm Dagger} < \ell_1^{\rm Dagger} < \ell_3^{\rm Dagger}$$

- Q-DAGGER loss function: The Q-DAGGER loss measures the value difference between expert and 479
- learned policies: 480

$$\ell^{Q\text{-DAGGER}} = V_t^{(\pi^*)}(s) - Q_t^{(\pi^*)}(s, \pi(s)).$$

- According to Lemma 2.1 in [1], we have the relationship $T\ell(\pi) = J(\pi) J(\pi^*)$. In our setting, 481
- $J(\pi^*) = -T$ (cost-to-go formulation with negative values). 482
- For trajectory 1 with $J(\pi_1) = -(T 3\tau)$, we compute: 483

$$\ell_1^{Q\text{-Dagger}} = [-(T - 3\tau) - (-T)] \cdot T^{-1} = 3\tau T^{-1}$$

For trajectory 2 with $J(\pi_2) = 0$, we obtain: 484

$$\ell_2^{Q\text{-Dagger}} = [0 - (-T)] \cdot T^{-1} = 1$$

For trajectory 3 with $J(\pi_3) = -(T - \tau)$, we have:

$$\ell_3^{Q\text{-Dagger}} = [-(T-\tau) - (-T)] \cdot T^{-1} = \tau T^{-1}$$

Since $\tau \in [0,1)$, the ordering becomes clear. Therefore, trajectory 3 is preferred by Q-DAGGER: 486

$$\ell_3^{Q\text{-Dagger}} < \ell_1^{Q\text{-Dagger}} < \ell_2^{Q\text{-Dagger}}$$

- GM-DAGGER loss function: The GM-DAGGER loss combines performance and behavioral terms via 487
- geometric mean: 488

$$\begin{split} \ell^{\text{GM-Dagger}} &= \sqrt{g_t^p(s,\pi) \cdot g_t^f(s,\pi)} \\ &= \sqrt{[V_t^{(\pi^*)}(s) - Q_t^{(\pi^*)}(s,\pi(s)) + \alpha] \cdot [||\pi(s) - \pi^*(s)||^2 + \epsilon]} \end{split}$$

- For the performance term $g^p(\pi)$, using Lemma 2.1 in [1], we have $Tg^p(\pi) = J(\pi) J(\pi^*) + \alpha T$, 489
- which gives us the average stepwise performance loss plus regularization. 490
- For trajectory 1, the performance term becomes $g^p(\pi_1)=3\tau T^{-1}+\alpha$. In the discrete action setting, 2 disagreements occurred. Since $\pi(s)\neq\pi^*(s)$ implies $||\pi(s)-\pi^*(s)||^2=1$, the behavioral term is 491
- 492
- $g^f(\pi_1) = 2T^{-1} + \epsilon$. Thus:

$$\ell_1^{\text{GM-Dagger}} = \sqrt{(3\tau T^{-1} + \alpha)(2T^{-1} + \epsilon)}$$

Similarly, for trajectory 2 with $g^p(\pi_2) = 1 + \alpha$ and 1 disagreement:

$$\ell_2^{\text{GM-DAGGER}} = \sqrt{(1+\alpha)(T^{-1}+\epsilon)}$$

For trajectory 3 with $g^p(\pi_3) = \tau T^{-1} + \alpha$ and full disagreements (T total disagreements):

$$\ell_3^{\text{GM-Dagger}} = \sqrt{(\tau T^{-1} + \alpha)(1+\epsilon)}$$

To establish the ordering, note that as $\tau \in [0,1)$ and $\alpha, \epsilon \in (0,1)$, for sufficiently large $T \geq \frac{1}{\min(\alpha,\epsilon)}$

(most cases in deep RL), the regularization terms dominate the trajectory-dependent terms. This

498 asymptotic analysis yields:

$$\ell_1^{\rm GM\text{-}Dagger} < \ell_2^{\rm Gm\text{-}Dagger} < \ell_3^{\rm Gm\text{-}Dagger}$$

Therefore, trajectory 1 is preferred by GM-DAGGER.

500 **B** VIPER

Table 4 presents VIPER performance without tree depth limitation across different reinforcement learning environments and algorithms, with mean performance \pm standard deviation reported alongside the resulting tree complexity (nodes, depth).

Table 4: VIPER performance without tree depth limitation.

	Tuble 1. VII ER performance without tree depth infination.				
	Algorithm				
Environment	PPO	TRPO	DDPG	SAC	TD3
CartPole	$ \begin{array}{c c} 1000.0 \pm 0.0 \\ (2981, 42) \end{array} $	372.7 ± 198.5 $(3011, 38)$	$1000.0 \pm 0.0 \\ (6951, 47)$	$1000.0 \pm 0.0 \\ (7661, 41)$	$1000.0 \pm 0.0 \\ (6279, 38)$
MountainCar	$\begin{array}{c c} 91.1 \pm 0.2 \\ (127, 11) \end{array}$	93.9 ± 0.0 $(157, 11)$	94.1 ± 0.2 (809, 24)	93.6 ± 0.1 $(83, 10)$	93.8 ± 0.2 $(891, 35)$
Pendulum	$\begin{array}{c c} -217.9 \pm 165.0 \\ (11187, 34) \end{array}$	-153.4 ± 108.7 (5029, 85)	-146.6 ± 72.0 $(1749, 43)$	-141.8 ± 85.0 (4809, 47)	-147.3 ± 68.9 (6741, 30)
Acrobot	$-36.0 \pm 0.0 \\ (63,7)$	-41.3 ± 3.0 (1419, 21)	-35.1 ± 0.3 (957, 27)	-35.6 ± 0.7 (1311, 22)	-41.0 ± 4.9 $(839, 26)$
Reacher	$-4.8 \pm 1.2 (4656, 27)$	-6.1 ± 2.7 $(5424, 34)$	-4.7 ± 1.5 $(5384, 47)$	-4.2 ± 1.5 $(6912, 39)$	-4.9 ± 1.6 (4624, 38)
Swimmer	$358.0 \pm 1.9 \\ (3414, 25)$	341.0 ± 2.4 $(62638, 47)$	348.2 ± 1.1 (31054, 57)	350.1 ± 2.5 (120138, 71)	357.6 ± 2.5 (45542, 73)

504 C Distilled Symbolic Policy

Table 5 presents all interpretable symbolic policies distilled using SPID across six environments with five different deep RL algorithms.

D Computational Resources

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All experiments were conducted on a single workstation with the following specifications:

• GPU: NVIDIA GeForce RTX 4080 Super (16GB VRAM)

• CPU: Intel Core i9-14900F (24 cores, 32 threads @ 5.8GHz max)

• RAM: 32GB DDR5

Table 5: Distilled symbolic policy.

Environment	Algorithm	Policy Expression from SPID		
CartPole	PPO	$a = (s_2 + (((0.055 - (-0.193) \cdot (s_3 + s_0))) - 0.135s_1)) * 1.697$		
	TRPO	$a = (s_3 + (s_1 + s_2)) \cdot (4.401 - (-0.804 - s_1)^2)$		
	DDPG	$a = ((s_3 \cdot (-0.098)) - s_2) \cdot (-20.292)$		
	SAC	$a = (2.359 - (s_3 + 0.825)^4) \cdot ((s_2 \cdot 3.526) + s_3)$		
	TD3	$a = (s_1 + 2.551) \cdot ((s_3 + s_2) + s_1)$		
MountainCar	PPO	$a = \sin((s_1 - 1.509) \cdot (s_0 + 37.711))$		
	TRPO	$a = \sin(((s_1 \cdot 64.859) + s_0^4 \cdot 2.156) - 1.407)$		
	DDPG	$a = \sin((s_0 \cdot 1.480)^2 + (-0.851) + (s_1 \cdot 52.793))$		
	SAC	$a = \sin(\sin(s_0^2 + ((s_1 \cdot 52.426) + (-0.729))) \cdot 1.540)$		
	TD3	$a = \sin(((s_1 - (-0.448)) \cdot 67.462) + (s_0/(-0.708))^4)$		
Pendulum	PPO	$a = ((((s_0 - s_1) \cdot (-2.411)) + 1.199) \cdot s_2) - (s_1 \cdot 8.199)$		
	TRPO	$a = (s_0 \cdot \sin(\sin(s_1 + (s_2 \cdot 0.231)) \cdot 3.322)) \cdot (-2.205)$		
	DDPG	$a = ((s_1 \cdot 5.767) + s_2) \cdot ((-0.366) - s_0)$		
	SAC	$a = \sin((((s_2 \cdot (-0.477)) - s_1) \cdot s_0) - s_1) \cdot 2.463$		
	TD3	$a = \sin((s_2 \cdot (-0.410)) - (s_1 \cdot 1.748)) \cdot (s_0 \cdot 3.165)$		
Acrobot	PPO	$a = (s_4/\sqrt{s_4^2}) \cdot (-1.925)$		
	TRPO	$a = (\sin(s_4) + (s_3 + s_4)) \cdot (-0.539)$		
	DDPG	$a = s_5 + (s_1 \cdot 2.953)$		
	SAC	$a = \sin((-0.406 \cdot s_4) - ((s_2 + s_0) \cdot \sin(s_4))) \cdot 2.073$		
	TD3	$a = \sin(s_2 - ((s_3 - (-0.395))^2 + s_4)) - s_4$		
Swimmer	PPO	$a_1 = \sin(((\sin(0.488/s_6)^2 \cdot s_6) - s_2) \cdot 2.061)$		
	TTD DO	$a_2 = \sin(\sin((s_6 \cdot 0.641) + (s_1 \cdot 1.217)) \cdot 1.788)$		
	TRPO	$a_1 = \sin(((s_1 \cdot s_3) + 1.658) \cdot \sin(s_0 - (s_2 \cdot 2.358)))$ $a_2 = \sin((s_4 + s_1) \cdot 0.744)$		
	DDPG	$a_1 = \sin(\sin(\sin((s_4 - s_1) - s_2) - s_2) \cdot 1.896)$		
		$a_2 = \sin(\sin(s_5 \cdot (-1.877)) - s_5)$		
	SAC	$a_1 = \sin((s_6/((s_4 \cdot s_6) + 1.790)) - s_2)$		
	ED 2	$a_2 = \sin((\sin(s_5) \cdot 1.311) + (s_6 \cdot (-0.281))) \cdot (-0.941)$		
	TD3	$\begin{vmatrix} a_1 = \sin(((-0.086)/s_2) + (s_2 \cdot (-1.840))) \\ a_2 = \sin(\sin(s_5 - (s_6 \cdot (-0.074))) \cdot (-1.903)) \end{vmatrix}$		
Reacher	PPO	$\begin{vmatrix} a_1 = s_9 \cdot ((((s_8 \cdot 2.318) \cdot s_7) + s_1^2) \cdot (-1.831)) \end{vmatrix}$		
Reaction	110	$a_1 = s_9 \cdot (((s_8 \cdot 2.518) \cdot s_7) + s_1) \cdot (-1.551))$ $a_2 = \cos((-0.590) \cdot s_7) \cdot (0.078 \cdot ((-0.099) - s_1))$		
	TRPO	$a_1 = 0.0002/(0.096 - s_1)$		
		$a_2 = ((s_2 + 1.245) \cdot (s_7 + (-12.931)))^2 \cdot (-0.0002)$		
	DDPG	$a_1 = ((\cos(s_7) - s_5)^2)^2 \cdot s_8$		
		$a_2 = (s_8 - (((s_4 + 0.248) \cdot 0.083) \cdot s_7)) \cdot 1.228$		
	SAC	$a_1 = (s_1 \cdot s_6) \cdot 0.043$		
	TD3	$a_2 = s_9 \cdot (-1.652)$ $a_3 = (s_3 - (s_3 - 0.021)) + ((sin((-0.425) - s_3) - 0.010))$		
	TD3	$a_1 = (s_8 - (s_7 \cdot 0.021)) + ((\sin((-0.425) - s_6) - s_6) \cdot 0.010)$ $a_2 = ((s_7 \cdot (-0.021)) + (s_8 + (-0.004))) \cdot ((s_4 \cdot s_6) + 1.148)$		
		~2 ((°, (°.021)) (°0 (°.001))) ((°4 °0) 1.110)		

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