## Discursive Socratic Questioning: (Unsupervised) Interpreting Neural Language Models for Discourse Understanding

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#### Abstract

Do neural language models (NLMs) understand the discourse they are processing? Traditional interpretation methods that address this question require pre-annotated explanations, which defeats the purpose of unsupervised explanation. We propose unsupervised Discursive So-007 cratic Questioning (DISQ), a two-step interpretative measure. DISQ first generates Socratic-style questions about the discourse and then queries NLMs about these questions. A model's understand-011 ing is measured by its responses to these questions. We apply DISQ to examine two fundamental discourse phenomena, namely discourse relation and discourse coherence. We

find NLMs demonstrate non-trivial capacities without being trained on any discourse data: Q&A pairs in DISQ are shown to be evidence for discourse relation and cohesive devices for discourse coherence. DISQ brings initial evidence that NLMs understand discourse through reasoning. We find larger models perform better, but contradictions and hallucinations are still problems. We recommend DISQ as a universal diagnostic for discursive NLMs and using its output for self-supervision.

#### 1 Introduction

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Neural language models (NLMs) are criticized as not understanding text in the manner that humans do, in a logical and reliable way (Bender and Koller, 2020; Zhang et al., 2022; Tan et al., 2021). We study whether NLMs understand discourse, a fundamental linguistic subject concerning the organization of sentences. To understand discourse, humans usually identify key spans across multiple sentences and infer logical connections among them (Halliday, 1976; Camburu et al., 2018; Lei et al., 2018). We believe that the discourse community has largely ignored such intuitions, favoring the development of complex black-box models, where NLMs are leveraged as backbones (Liu et al.,



Figure 1: Discursive Socratic Questioning (DISQ) performs unsupervised interpretation. Step 1: Socraticstyle questions are automatically generated by combining spans in discourse and question prompts. Step 2: A model answers these questions. Its output to the questions is used as a proxy for its understanding.

2020). While achieving good performance, such black-box models lack interpretability and offer little evidence to trust their decisions. We believe it is imperative to examine the root cause: whether and how NLMs capture the linguistic properties of discourse function.

Popular interpretation methods like linguistic probing (Tenney et al., 2019) and behavior analyses have been shown as plausible methods (Belinkov et al., 2020; Choudhury et al., 2022). However, they have a major shortcoming: they require supervision. Additional annotations are required to train a model to predict linguistic structures or to generate explanations, which makes these methods difficult to apply to new tasks. We explore unsupervised interpretation as a novel alternative. In Socratic Questioning (named after the philosopher Socrates), a teacher raises thoughtful questioning to students to enable them to examine their ideas rigorously. At the end of the questioning, the students can determine the validity of the idea and discover any flaws and contradictions (Padesky, 1993).

We instantiate this idea for discourse understanding in the form of the Discursive Socratic Questioning procedure (**DISQ**; Figure 1). We enable NLMs to self-interrogate its understanding through Socratic-style questions. The premise is simple: if

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a text has a *Contingency* discourse relation, there 069 must be a cause and a result (in purple). So if a NLM models the discourse appropriately, it must 071 be able to also answer "what is the result of" question correctly, and must abstain from answering irrelevant questions. A battery of Socratic-style questions is created by combining question prompts (in blue) and text spans taken from the discourse. The model is self-interrogated by all questions, and we use the model's behavior as a proxy for its discourse understanding. We use a pre-determined set of question prompts (c.f.  $\S2.1$ ) to generate our questions, such that no additional supervision aside from discourse annotations are needed. We only need a text with discourse annotated or where the discourse is explicitly indicated (e.g., explicit discourse markers).

> Through DISQ, we provide evidence that NLMs appropriately model discourse by reasoning over text as a set of key spans and inferring relationships among them, similar to how humans process discourse. (1) **DISQ identifies evidence for discourse relation.** We find Q&A in DISQ exhibits a strong association between question prompts and all four first-level discourse relations in the PDTB (Prasad et al., 2008). We also find that explicit discourse connectives boost the performance of the Socratic questioning. (2) **DISQ identifies cohesive devices for discourse coherence**: We consider Q&A pairs extracted by DISQ as cohesive devices. Simply aggregating them leads to a decent human correlation in SummEval dataset.

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We present the first study using questioning for unsupervised model interpretation, with a focus on discourse understanding. Although in this study, we only examine standard English corpora, our DISQ reveals NLMs' non-trivial discourse modeling. We recommend that DISO be used to serve as a universal diagnostic for NLM's representation of discourse, complementary to dataset benchmarking (Chen et al., 2019). Like Socrates did with his students, DISQ also diagnoses what a model knows and does not know. We observe that interesting patterns emerge, such as symmetry, self-contradiction, and hallucination in DISQ's output. We recommend two usability tests that utilize DISQ to help models diagnose their trustworthiness and use DISQ's output as self-supervision signals for future discursive NLMs.<sup>1</sup>

#### 2 Discursive Socratic Questioning

What Counts as Discourse Understanding? Organized text makes sense as textual elements link the discourse together. Such linking elements are referred to as cohesive devices (Halliday, 1976). Concretely, given two discourse arguments  $Arg_1$ and  $Arg_2$  participating in a discourse relation R, two contiguous spans  $s_1 \in Arg_1$  and  $s_2 \in Arg_2$ link the two arguments into a coherent discourse with a semantic relation r. We define  $(s_1, s_2, r)$  as evidence for understanding the discourse relation. We argue that a model must be able to identify them for us to claim that it understands the discourse. 118

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<b>Discourse relation:</b> Contingency.Cause.Result [In July, the Environmental Protection Agency
[imposed a gradual ban] $_{s_1}$ on virtually all uses of
asbestos.] $_{Arg_1}$ [By 1997, almost all [remaining uses of
[cancer-causing asbestos will be outlawed] $_{s_2}$ ] $_{Arg_2}$
<b>Question:</b> What is the result of imposing a ban?
Answer: remaining uses of cancer-causing asbestos will
be outlawed.

Table 1: Formalizing discourse understanding as question answering (QA). A *cause/result* relation between  $s_1$  and  $s_2$  is realized through QA.

**Defining a Proxy for Discourse Understanding:** We approach the notion of understanding through question answering (QA). We interrogate the model with a set of questions concerning different semantic relations and text spans. If a model is said to understand, it must answer questions in a manner consistent with the discourse relation.

As illustrated in Table 1, we believe NLMs must infer the *cause/result* relation r between "the ban"  $(s_1 \in Arg_1)$  and "remaining use of cancer-causing asbestos will be outlawed"  $(s_2 \in Arg_2)$  to understand the *contingency* discourse relation R. When querying about  $s_1$ , the model should extract  $s_2$  as the answer with only "what is the result" prompt. It should not respond to irrelevant questions like "what is different from" since there is no such semantic relation to form a cohesive tie in the given discourse. An ideal model will extract all evidence triplets with only correct questions, and abstain from answering irrelevant questions.

Our approach is a generalized extension to Halliday (1976)'s theory. Halliday defined a taxonomy of cohesive devices, including reference, ellipsis, and lexical cohesion. These devices describe a limited set of specific text cohesion devices with constrained definitions. DISQ extends this compu-

<sup>&</sup>lt;sup>1</sup>We will release our codebase upon acceptance.

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 $s_2 = QA(c = Arq_1 + Conn + Arq_2, q = p + s_1)$  (1)

tationally to encompass a more inclusive notion of

cohesion among arbitrary spans in text and a larger

relation space characterized by Socratic question-

We operationalize DISQ with extractive QA to

discover evidence  $(s_1, s_2, r)$  for understanding:

ing (detailed discussion is in Appendix B).

Questioning and Answering

The model seeks an answer in the opposing discourse argument. The semantic relation r between  $s_1$  and  $s_2$  is determined by the question prompt p. Without loss of generality, if the question q is generated from  $s_1 \in Arg_1$ , then the answer must come from  $s_2 \in Arg_2$ . This is a critical constraint for the model to jointly comprehend two discourse arguments. The context c is composed of two discourse arguments  $Arg_1$  and  $Arg_2$ , with the insertion of an explicit discourse connective  $Conn_e$  or an implicit  $Conn_i$  (to be inferred by the model). The question q is composed of a prompt p and a span  $s_1 \in Arq_1$ .



Figure 2: DISQ asks questions with all possible question prompts. When the prompt is consistent with discourse relation, a desired span should be extracted. If the prompt is irrelevant, an understanding model will abstain. DISQ also inserts a counterfactual discourse connective to guide the model to answer again.

Questioning with implicit connective: Discursive questioning *elicits* discourse relations. Our key insight is that discourse relations are a hidden variable that facilitate discursive questioning. In our running example, the model needs to understand discourse relation R as *contingency* to perform successful QA. DISQ will also ask questions with incorrect question prompts (e.g. "what is different from" question in Figure 2); an understanding model must abstain from answering these illogical questions.

**Questioning with explicit connective:** A realized 188 discourse connective explicates discourse relation. 189 We now insert a plausible discourse connective 190 (e.g.  $Conn_e$  "as a result" as  $Conn_e$  in Figure 2) 191 and conduct the same questioning again. Similar to 192 how humans read, the explicit marker then assists 193 the reader in comprehending the discourse. So if a 194 model understands the connective and incorporates 195 it into the comprehension of the discourse, it should 196 perform better QA. 197 198

**Question Generation:** Questions are generated automatically by composing a question prompt and a span in the discourse. (1) To create a battery of question prompts, we refer to the sense taxonomy in PDTB 2.0 (Prasad et al., 2008) and produce the following prompts  $\mathcal{P}_R$  for each discourse relation R in Table 2. (2) To extract proper spans, we follow previous work (Pan et al., 2020) to use a trained semantic role labeler (SRL) to find self-contained spans.

Question prompt $\mathcal{P}_R$ set	Discourse relation $R$	
Why	Contingency	
What is the result of	Contingency	
What is the reason of		
What is different from	Comparison	
What is opposite to	Comparison	
What is similar to	Expansion	
What is an example of	Expansion	
What happens after	Temporal	
What happens before	remporar	

Table 2.	Question	prompts	and	their	discourse	relation
	Question	prompts	anu	unen	uiscourse	relation.

#### 2.2 Output: DISQ's Matrices (DISQM)

DISQ's output is an array of matrices  $\mathcal{M}$  =  $\{M^1, M^2, ..., M^{N-1}\}$ . We name  $\mathcal{M}$  as DISQ's Matrices (DISQM). Given a sequence of discourse arguments (sentences) of length N > 2, we perform DISQ in a sliding window style.  $M^i$  indicates the output for *i*th and (i + 1)th sentence.



Figure 3: DISQ's Matrices (DISQM) are produced by performing DISQ in a sliding window style.

As for each M, since we do not require the

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ground truth Q&A pairs, we ask all possible ques-216 tions. All spans s from both  $Arg_1$  and  $Arg_2$  are 217 combined with all question prompts, resulting a 218 total of  $|s| \times |p|$  questions to ask. As shown in Fig-219 ure 3, when asked a question composed by  $s_i$  and  $p_j$ , if an answer is retrieved from opposing argu-221 ment (sentence), we assign  $M_{i,j} = 1$  and  $M_{i,j} = 0$ otherwise. It is simplistic because we do not discriminate between correct and wrong answers due to the lack of ground truth Q&A. But  $s_1 \in Arg_1$ and  $s_2 \in Arq_2$  are extracted as a cohesive tie and their relation r is characterized by question prompt 227 p. We contribute DISQM as a new interpretable representation for discourse. 229

### 3 Task 1: Discourse Relation

We measure NLMs' understanding by how well it performs in DISQ. Our formalization is distinct from the traditional setting where accuracy for classification is the primary focus.

#### 3.1 Formalization

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**Evidence Extraction:** We consider  $(s_1, s_2, p)$ triplet as evidence for understanding discourse relation, and study if NLMs extract proper evidence given discourse relation R.

**DISQM Value**: Since we do not require (and have) the annotation for evidence triplets, we model the association between discourse relation R and question prompt p as a macro-level evaluation:

$$V(R,p) = \frac{\sum_{j \in \mathcal{P}_R}^{|M^R|} \sum_{i=1}^{|s|} M_{i,j}^R}{|M^R|}$$
(2)

V(R, p) is the expectation for the number of evidence triplets being retrieved using question prompt p under discourse relation R. Specifically, we perform DISQ on a corpus  $C = (Arg_1, Arg_2, R, Conn)_L$  with the annotation for discourse relation and connective. V(R, p) concerns all  $|M^R|$  number of DISQM matrices  $M^R$ with discourse relation R. Within each  $M^R$ , we only consider columns j that correspond to R's question prompts  $\mathcal{P}_R$ . Finally, we consider all span s being asked equally.

**Assertion 1:** V(R, p) must be higher than V(R, p')where  $p \in \mathcal{P}_R$  and  $p' \notin \mathcal{P}_R$  if a model understands discourse relation.

Models must distinguish correct prompt pagainst incorrect p' under discourse relation R, which will be reflected by different DISQM values. For a random model, V(R, p) = V(R, p').

#### **3.2 Implementation Details**

**Dataset:** We study PDTB 2.0 dataset ((Prasad et al., 2008)) because they have annotated both discourse relation and connective. We focus on implicit discourse instances because they miss discourse connectives and require non-trivial reasoning over two arguments. We perform DISQ over 2 ~20 sections in PDTB (the training split for traditional setting), including 12,362 discourse instances.

**NLMs:** We primarily study BERT's family, following a recent investigation about models' reasoning capacity (Choudhury et al., 2022). We experimented BERT (Devlin et al., 2019) and RoBERTa model (Liu et al., 2019) of tiny, base, and large sizes. To enable question answering, we choose BERT and RoBERTa models fine-tuned on SQuAD 2.0 dataset, which are also de facto choices for QA research. DISQ is very generic, practitioners can explore other NLMs fine-tuned on other tasks.

**Evaluation Measure:** We primarily study V(R, p) as a proxy for understanding discourse relations. We also present a normalized  $\hat{V}(R, p) = \frac{V(R,p)}{AVG(V(R,p)), R \in \mathcal{R}}$  for proper comparison among prompts. This is because we observe some prompts have a higher prior to having an answer.

#### 3.3 Evaluation

Our evaluation is focused on the general performance on DISQ (RQ1), the role of discourse connective (RQ2), and interpretability (RQ3):

How do NLMs generally perform on DISQ? (RQ1) We first do not insert discourse connective and expect the model can understand the discourse relation. We interpret the result in Table 3 from two angles: (1) Question(Column)-wise comparison: There are 9 (R, p) cells we expect the highest V(R, p) value in one column (bolded), for example, V(R, p) = 0.144 for "Comparison" question in "Different" column. We find that 7 out of the 9 desired cells have achieved the highest value in their columns. Interestingly, we find Expansion relation does not achieve the desired score. Our conjecture is that Expansion relation intrinsically lacks the salient semantic like *contrast* or *cause/result* in other discourse relations. (2) Relation(Row)-wise **comparison:** Normalized score V(R, p) enables relation(row)-wise comparison. We again observe the same 7 out of 9 cells achieving the highest

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	Different	Opposite	Why	Result	Reason	Similar	Example	After	Before
Comparison	$0.144_{(1.582)}$	$0.022_{(1.402)}$	$0.598_{(0.884)}$	$0.642_{(0.930)}$	$0.705_{(0.880)}$	$0.154_{(0.886)}$	$0.34_{(0.814)}$	$0.453_{(0.946)}$	$0.063_{(1.042)}$
Contingency	$0.081_{(0.888)}$	$0.015_{(0.962)}$	$0.814_{(1.204)}$	$0.764_{(1.108)}$	$0.962_{(1.200)}$	$0.187_{(1.077)}$	$0.465_{(1.113)}$	$0.441_{(0.920)}$	$0.049_{(0.799)}$
Expansion	$0.075_{(0.820)}$	$0.015_{(0.959)}$	$0.711_{(1.051)}$	$0.633_{(0.918)}$	$0.799_{(0.997)}$	$0.184_{(1.060)}$	0.462 <sub>(1.105)</sub>	$0.380_{(0.794)}$	$0.045_{(0.748)}$
Temporal	$0.065_{(0.710)}$	$0.011_{(0.677)}$	$0.582_{(0.861)}$	$0.720_{(1.044)}$	$0.740_{(0.923)}$	$0.170_{(0.977)}$	$0.405_{(0.968)}$	$0.642_{(1.341)}$	$0.086_{(1.411)}$

Table 3: DISQ with implicit connective for BERT<sub>Large</sub>: V(R, p) is compared column-wise and  $\hat{V}(R, p)$  (inside parentheses) is compared row-wise. Numbers are **bolded** if desired to be highest in its row/column and in green if achieved. 7 out of 9 cells achieve the highest value, marking a strong association between R and p (**RQ1**).

	Different	Opposite	Why	Result	Reason	Similar	Example	After	Before
Comparison	$2.232_{\pm 0.650}$	<b>2.379</b> <sub>+0.977</sub>	$0.666_{-0.218}$	$0.792_{-0.138}$	$0.65_{-0.230}$	$0.761_{-0.125}$	$0.652_{-0.162}$	$0.821_{-0.125}$	$0.918_{-0.124}$
Contingency	$0.552_{-0.336}$	$0.544_{-0.418}$	$1.433_{+0.229}$	$1.331_{+0.223}$	$1.627_{+0.427}$	$1.047_{-0.030}$	$1.134_{\pm 0.021}$	$0.853_{-0.067}$	$0.903_{\pm 0.104}$
Expansion	$0.623_{-0.197}$	$0.660_{-0.299}$	$1.077_{\pm 0.026}$	$0.868_{-0.050}$	$0.943_{-0.054}$	$1.148_{+0.088}$	$1.365_{+0.260}$	$0.664_{-0.130}$	$0.713_{-0.035}$
Temporal	$0.593_{-0.117}$	$0.417_{-0.260}$	$0.824_{-0.037}$	$1.009_{-0.035}$	$0.780_{-0.143}$	$1.043_{\pm 0.066}$	$0.850_{-0.118}$	$1.662_{+0.321}$	$1.465_{+0.054}$

Table 4: DISQ replicated with explicit connectives: We report  $\hat{V}(R, p)$  and  $\Delta$  values compare with Table 3 (e.g. 2.232 - 1.582 = +0.650). The performance is boosted. All 9 desired cells receive a  $+\Delta$  value while the most of the undesired cells receive a  $-\Delta$  value, demonstrating a strong understanding of discourse connective (**RQ2**).

score(s) in the row. For example, the Comparison relation is very responsive to "different" and "opposite" prompts ( $\hat{V}(R,p)$  is 1.582 and 1.402).

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Both comparisons show remarkable results for NLMs to extract evidence in consistency with discourse relation without the hint from connective. We focus on  $\text{BERT}_{\text{Large}}$  model here and present other models' performance in Appendix E. All models show an association between R and p but larger models tend to perform better, which is in line with recent findings in (Choudhury et al., 2022).

Can discourse connective improve NLMs' performance? (RQ2) We then explore the effect of the counterfactual  $conn_e$  which explicates the hidden variable of discourse relation. In Table 4, the normalized DISQM values  $\hat{V}(R, p)$  and  $\Delta$  values are presented. We find the insertion of explicit connective boosts the performance of the questioning. Now 9 out of 9 desired cells achieve the highest score in both column and row-wise comparisons (Expansion relation included). Moreover, all desired cells receive a  $+\Delta$  value. The rest of the cells mostly receive a  $-\Delta$  impact. It is remarkable for NLMs to interpret discourse by conditioning on the inserted  $conn_e$  to seek more correct evidence and eliminate incorrect evidence, which we believe is similar to human-like understanding.

338Case study: Is DISQ's output interpretable?339(RQ3) Table 5 showcases DISQ's output on our340running example. BERT<sub>Large</sub> model retrieves the341desired answer given "Why" and "What is the re-342sult of" questions which are in line with Contin-343gency relation. We also find the Q&A pairs very344readable to human and contributes to discourse re-

Discourse sense: Contingency.Cause.Result.	Discourse s
Conn: as a result	Conn: as a
Arg1: In July, the Environmental Protection Agency im-	Arg1: In Ju
posed a gradual ban on virtually all uses of asbestos. Arg2:	posed a gra
By 1997, almost all remaining uses of cancer-causing as-	By 1997, a
bestos will be outlawed.	bestos will
<b>Question:</b> What is the result of imposing a gradual ban?	Question:
Answer: almost all remaining uses of cancer-causing	
asbestos will be outlawed. Confidence: 0.40	asbestos wi
Question: Why will almost all remaining uses of cancer	Question:
- causing asbestos outlawed? Answer: the Environmental	
Protection Agency imposed a gradual ban on virtually all	
uses of asbestos. Confidence: 0.06	uses of asb

Table 5: Case study for BERT<sub>Large</sub> model with implicit connective: The model retrieves evidence only with two correct question prompts and abstains from 50+ irrelevant questions (**RQ3**).

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lation. It is worth noting that irrelevant questions like "what is different from" are also asked, which means the model is able to abstain from answering these questions. This example also exhibits symmetry. It is a desired structure (Topology 1) as detailed later in Section 6. "what is the result of" prompt extracts an answer from  $Arg_2$ , and the "why" prompt extracts an answer from  $Arg_1$ . As these two prompts have opposing meanings, their answers can reinforce each other symmetrically. This is similar to how people read contexts, in a bidirectional manner. We analyze additional case studies in other configurations in Appendix C.

#### 4 Task 2: Discourse Coherence

We have studied Q&A pairs discovered by DISQ as reasoning evidence for discourse relations. We now explore such Q&A pairs as cohesive devices. We contribute DISQM values as a new reference-free

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measure for text coherence.

#### 4.1 Formalization

**Coherence Modeling:** Given a sequence of sentences (discourse arguments)  $T = \{t_1, t_2, ..., t_n\}$ , a model needs to predict a coherence score V.

**DISQM Values:** Coherence is achieved by linking multiple spans in sentences through semantic relations (Halliday, 1976). We extend Halliday's predefined cohesion types to generic cohesion discovered by DISQ. Formally, given *T*, DISQ is performed on each pair of sentences,  $(t_1, t_2)$ ,  $(t_1, t_2)$ , ...  $(t_{n-1}, t_n)$ , resulting an array of DISQM matrices  $\mathcal{M} = \{M^1, M^2, ..., M^{n-1}\}$ . We define following DISQM aggregate values:

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$$V_{sum}(\mathcal{M}) = (\sum_{k=1}^{n} \sum_{j=1}^{|P|} \sum_{i=1}^{|s|} M_{i,j}^k)/n$$
, (Sum)

• 
$$V_{den}(\mathcal{M}) = (\sum_{k=1}^{n} \frac{\sum\limits_{j=1}^{|P|} \sum\limits_{i=1}^{|s|} M_{i,j}^k}{|P| \times |s|})/n$$
, (Density)

• 
$$V_p(\mathcal{M}) = (\sum_{k=1}^n \sum_{j=1}^{|P|} \lceil \sum_{i=1}^{|s|} M_{i,j}^k \rceil^1)/n$$
, (Prompts)

• 
$$V_s(\mathcal{M}) = (\sum_{k=1}^n \sum_{i=1}^{|s|} \lceil \sum_{j=1}^{|P|} M_{i,j}^k \rceil^1)/n$$
, (Spans)

These values are aggregations of  $\mathcal{M}$  because we believe 1s in M indicate Q&A pairs which encode local cohesion, and their aggregation leads to global coherence over the discourse. The values are divided into two groups: (1) Quantity-driven:  $V_{sum}(\mathcal{M})$  and  $V_{den}(\mathcal{M})$  measure the average sum of the matrix M and the density of matrix M respectively. The intuition is that when more QA pairs are extracted (1s in M), more cohesive devices contribute to global coherence. (2) Diversitydriven:  $V_p(\mathcal{M})$  and  $V_s(\mathcal{M})$  measure the number of active question p rompts and active spans in Mrespectively. When writers compose a context, they may use multiple discourse senses or use several cohesive devices to stress the coherence.  $[M]^1 = clip(M, 1)$  denotes a function to clip a matrix to a max value of 1.

Assertion 2: On average V(T) should be higher than V(T') when T is more coherent than T' if a model understands discourse coherence.<sup>2</sup> A coherent discourse is better than random sentences because more cohesive devices link the text together. An idealist model must be able to identify them which are reflected in DISQM values. 401

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We contribute DISQM values as a new measure for text coherence. It is simple, non-parametric, and reference-free. It is possible to exploit the topological patterns in DISQM like the Entity-grid method (Barzilay and Lapata, 2008), we now perform a qualitative study and leave it for future work.

#### 4.2 Implementation Details

**Dataset:** We choose SummEval dataset (Fabbri et al., 2021) because it is a new resource providing human annotation on text coherence. They provide coherence annotation for 17 systems' output on 100 summarization instances. Notably, Fabbri et al. (2021) find that coherence is the most problematic aspect of automatic summarization evaluation (least correlated with human judgement).

#### 4.3 Evaluation

	Sum	Density	Spans	Prompts
	$(V_{sum})$	$(V_{den})$	$(V_s)$	$(V_p)$
BERT <sub>Tiny</sub>	-0.353	-0.324	-0.279	0.0
BERT <sub>Base</sub>	-0.441	-0.382	-0.324	-0.382
BERTLarge	-0.118	-0.206	0.022	0.044
RoBERTa <sub>Tiny</sub>	-0.074	-0.088	-0.015	0.044
RoBERTa <sub>Base</sub>	0.176	-0.074	0.324	0.338
RoBERTaLarge	0.647	0.294	0.647	0.632

Table 6: System-level Kendall's Tau correlation with human judgments. Scores are **bolded** if greater than or equal to previous state-of-the-art (-0.382 and 0.397 for -ve and +ve correlations (Fabbri et al., 2021))

We use  $V(\mathcal{M})$  as the coherence measures. Following Fabbri et al. (2021), we use system-level Kendall's Tau correlation to assess  $V(\mathcal{M})$ 's correlation with human judgements.

We perform DISQ on  $17 \times 100$  summarization instances and obtain their DISQM values  $V(\mathcal{M})$ . We report Kendall's Tau scores in Table 6 and make two observations: (1) The RoBERTa<sub>Large</sub> and RoBERTa<sub>Base</sub> models have shown a positive correlation with human judgment on coherence. Notably, the RoBERTa<sub>Large</sub> model even outperforms previous state-of-the-art significantly.  $V_{sum}$  has a correlation of **0.647**, significantly higher than the previous state-of-the-art). It indicates that useful cohesive devices have been extracted by NLMs, such that even our simple aggregations correlate well. (2) However, BERT<sub>Base</sub> show a significant negative correlation. This is counter-intuitive, as

<sup>&</sup>lt;sup>2</sup>We use T and  $\mathcal{M}$  interchangeably. This assertion might have exceptions where short sentences can also be coherent but they have fewer cohesive devices.

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we assume that 1s in DISQM contributes positively to coherence. The cause may be due to BERT<sub>Base</sub> having many incorrect answers and hallucinating responses, and a consequences of BERT's fragility compared with RoBERTa. This leads us to recommend practitioners to explore larger models and architectures that exceed a minimal threshold level of performance for DISQ analyses to make sense.

#### 4.4 Usability Tests of DISQM

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We recommend two usability tests to make DISQM trustworthy and controllable. They help practitioners decide the usability of NLMs for discourse tasks. They also serve as an explanation for interesting model behaviors that we have discovered. **Test 1: Sentence ordering** is an automatic usability test. Practitioners should choose models with high accuracy for this task. Itself is a classic experimental setting for coherence modeling (Lin et al., 2011). Its advantage is that it can be performed in automatically synthesized contexts. The assumption is that randomly perturbed sentences should be less coherent than the original ones.

We showcase one study on the SummEval dataset's human-written summaries. It comprises 1,000 summaries, which are all assumed to be coherent. Following the setup in (Lin et al., 2011), we generate 20 perturbations for each instance (shorter summaries may have fewer than 20 perturbations). We also follow the setting in (Lin et al., 2011) to perform a binary prediction task between original context T and perturbed context T'. We consider a prediction is correct when V(T) > V(T') and incorrect otherwise.



Figure 4: Usability Test 1: Models' performance on coherence modeling (left) is in a similar trend to the sentence ordering task (right).

472We compare the performance of the original eval-<br/>uation (measured by Kendall's Tau) and the sen-<br/>tence ordering task (measured by accuracy score)<br/>using  $V_{sum}$  value. We find they are in a very<br/>similar trend: BERT<sub>Base</sub> is the lowest and the<br/>RoBERTaLarge the highest. RoBERTa models per-<br/>form better in both tasks. Notably, the BERT<sub>Base</sub>

model only scores 0.519 accuracy which is nearly random, meaning it cannot distinguish coherent discourse against random sentences. It explains its weak performance in the original evaluation for coherence modeling.

**Test 2: Correctness of answers** requires a moderate amount of human input to determine the correctness of Q&A pairs produced by DISQ. The more correct Q&A pairs, the more reliable a model is. The assumption is that only when Q&A pairs are correct, do they make a positive contribution to coherence.

Since we do not have the ground truth data for the Q&A pairs in SummEval, we manually conduct a proof-of-concept study. The first author classified the Q&A pairs into three categories: (1) Correct (C): The two spans  $(s_1 \text{ and } s_2)$  in question and answer satisfy the relation of the question prompt *p*; (2) Incorrect (I): The spans are either unrelated, or do not satisfy the relation of the question prompt p; (3) Non-contextual (N): Two spans ( $s_1$  and  $s_2$ ) satisfy the relation of question prompt p out of context, but not in correct context. Similar definition is also adopted in (Lei et al., 2021). We randomly sample 50 summaries and study DISQ's output by BERT<sub>Base</sub> and RoBERTa<sub>Large</sub> models, which are the most negative and positive correlated models measured by Kendall's tau correlation (+0.647 and  $-0.441)^{3}$ :

	С	Ι	Ν
BERT <sub>Base</sub>	72 (24.1%)	217 (71.6%)	13 (4.3%)
RoBERTaLarge	49 (52.1%)	43 (45.7%)	2 (2.1%)

Table 7: Classification of Q&A pairs in pilot study: RoBERTa has a higher ratio of correct Q&A (52.1%).

As shown in Table 7, RoBERTa<sub>Large</sub> model has a much higher portion of correct answers compared to BERT<sub>Base</sub> model. It offers initial evidence that only correct (C) Q&A pairs are contributing to coherence and it endorses the usability test. As for the BERT<sub>Base</sub> model, we observe that it produces many wrong (W) and noncontextual (N) Q&A pairs. So the negative Kendall's Tau correlation might be explained in this way: incoherent context lacks an obvious or salient discourse relation so many sense seems possible. In this case, a "confused" model like BERT<sub>Base</sub> is likely to hallucinate and respond to many possible question prompts (We articulate our classifications with examples in Appendix D).

<sup>&</sup>lt;sup>3</sup>Pilot study results are uploaded as supplementary data.

#### 5 Related Work

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QA for NLP Tasks: Even though question answering (QA) has been explored as an interface for many NLP tasks, DISQ's focus is using QA as an unsupervised approach for model interpretation. Existing works primarily explored annotating golden data and training supervised models. Notable efforts include QASRL (FitzGerald et al., 2018), QANorm (Klein et al., 2020), QADiscourse (Pyatkin et al., 2020), QASem (Klein et al., 2022), DCQA (Ko et al., 2022a), and QA for reference/ellipsis resolution (Hou, 2020; Aralikatte et al., 2021). We draw inspiration from the self-talk paradigm (Shwartz et al., 2020) that generates clarifying questions and queries NLMs for additional evidence. The key distinction is that Shwartz et al. (2020)'s answers are retrieved outside the given context, while our answer comes from the context.

Interpretation Methods in NLP: DISQ pro-540 vides an unsupervised alternative to popular inter-541 pretation methods: (1) Probing paradigm takes 542 out the representation of NLMs and train a model 543 to predict whether one linguistic property is captured by the representation (Tenney et al., 2019; 545 Wallace et al., 2019; Li et al., 2021). Despite being 546 simple, it requires labeled data for supervision. (2) As summarized by Belinkov et al. (2020), behavior analysis and post-hoc interpretation produce fine-grained interpretation of model's output. The 550 common practice is to perturb the text to reveal the 551 decision boundary or unwanted bias of the model (Feng et al., 2018; Ribeiro et al., 2016; Poliak et al., 2018; Rudinger et al., 2018). But the creation of 554 the perturbation usually requires human input. 555

Discourse Modeling: DISQ creates new possi-556 bilities for several discourse tasks: (1) Discourse relation: NLMs are used as a backbone for customized neural networks to predict discourse relation (Liu et al., 2016; Dai and Huang, 2018; Liu et al., 2020). Even though the performance shows improvement over prior feature-based methods (Pitler et al., 2009; Rutherford and Xue, 2014), 563 these methods lack interpretability. One recent 564 exception (Jiang et al., 2021) considers genera-565 tion as an auxiliary task to prediction. The generated text offers some interpretability but it is not 567 their focus. We hope future works to be evalu-568 ated and optimized by DISO. (2) Discourse co-569 herence: Similarly, neural methods (Mohiuddin et al., 2018; Jwalapuram et al., 2022) perform better 571

than feature-based methods (Barzilay and Lapata, 2008). To the best of our knowledge, there is no existing work interpreting the inner mechanism of NLMs for coherence. We hope our formalization of Q&A pairs as cohesive devices will seed more interpretable models. (3) Discourse structure: Our DISQM matrices are linear, not hierarchical. We can learn from recent advances using NLMs to predict hierarchical structures (Huber and Carenini, 2022; Ko et al., 2022b; Xiao et al., 2021).

#### 6 Conclusion and Discussions

Due to the lack of annotated data, little progress has been made towards interpreting how NLMs understand discourse. We present the first study by enabling models to self-interrogate with a Discursive Socratic Questioning (DISQ) procedure. By analyzing DISQ's output matrices (DISQM), we find NLMs show remarkable evidence in understanding both discourse relations and coherence by identifying cohesive spans in text and realizing their relations through Socratic questioning. We urge researchers to test their NLMs with our DISQ usability tests as an additional layer of validation.



Figure 5: Symmetry, self-contradiction and hallucinations in DISQM. Green cells indicates correct answers. Pink cells indicates incorrect or noncontextual answers.

As Socratic questioning ends, students realize what they know and do not know. Topology 1 (Figure 5, upper left) is a DISQM result: when  $s_1 \in Arg_1$  and  $s_2 \in Arg_2$  are in a reason-result relationship with each other, a symmetric structure is established, similar to how humans read. In contrast, Topology 2 indicates self-contradiction: here, both  $s_1 \in Arg_1$  and  $s_2 \in Arg_2$  are considered as the result for each other, which is illogical. Finally, Topology 4 shows a model that hallucinates and responds positively to many questions, which happens when the model finds only weak relatedness. In future work, these patterns may serve as signals for self-supervision to insert logic into discursive NLMs for attaining better reliability.

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#### Ethical Considerations and Limitations

611 When performing DISQ, we note that output an-612 swers may be offensive in certain contexts, because 613 practically all spans in the context can be (incor-614 rectly) extracted as an answer. This is a common 615 concern for all QA models to overcome, not spe-616 cific to DISQ. But according to our pilot study, we 617 have not found any cases of such offensive Q&A 618 pairs.

DISQ also has particular limitations. (1) We only use the behavior of the model given a set of questions as a proxy for understanding. It is not a causal analysis. We can causally study the role of individual neuron or subnetwork for discourse function in the future, similar to a recent study about individual neuron's role for factual knowledge (Meng et al., 2022). (2) Our method is unsupervised and does not require ground-truth QA pairs. It is meaningful to create such a dataset with ground truth QA pairs annotated for discourse understanding and benchmark how models perform reasoning on it. (3) We have only studied standard English corpora. It is meaningful to apply DISQ to NLMs' understanding of discourse on other English corpora with language variations and to corpora in other languages.

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#### A **DISQ's Possible Extension to Other NLP Tasks**

In this paper, we propose a self-interrogation procedure (DISQ) to interpret models' decision processes for discourse understanding. We describe a conceptual extension of DISQ that can be applied to other NLP tasks for unsupervised interpretation of models' decision process. This extension follows our two-step design:

Step 1: Socrates Asks: (1) Span identification: We first identify key spans to compose the questions. The linking of the spans may have different functions in different tasks. In discourse, we have explored the spans' linkage as cohesive devices. In Natural Language Inference (NLI), for example, two spans may compose an entailment or contradiction relation (Camburu et al., 2018). (2) **Question generation** We then generate questions with predefined question prompts customized for each task. In the NLI task, such question prompt can be "What results in" and "What contradicts".

Step 2: Model Answers: We interrogate the model with the battery of questions automatically generated in Step 1. In line with our measure for discourse, we use the model's behavior in the questioning as a proxy for its understanding of the task. For example, in an "entailment" NLI instance, the model needs to answer consistently with the "entailment" relation. That is to say, it must extract a correct span in hypothesis with "What results in" prompt and abstain from "What contradicts" prompt.

We now briefly discuss how DISQ's extension can be applied to natural language inference (relation classification for (two sentences), sentiment analysis (single sentence classification), and text summarization (text generation):

• Natural language inference (NLI): As the example in Figure 6, there are two highlighted spans that signals the contradiction relation between the premise and hypothesis. We believe the model must answer correctly to "What contradicts with" question and abstain from other questions to have a good understanding. This example is excerpted from the e-SNLI (Camburu et al., 2018) corpus for explainable NLI. This corpus requires great effort for annotation, our DISO can alleviate it by automatically identifying spans and generating thoughtful questions.

Tasks	Example	Socrates Asks (Step 1)	Model Answers (Step 2)
Natural Language Inference	Premise: An adult dressed in black holds a stick. Hypothesis: An adult is walking away, empty- handed. Label: contradiction	Q: What contradicts with holding a stick?	A: empty-handed.
Sentiment Analysis	<b>Input:</b> visually imaginative, thematically instructive and thoroughly delightful, it takes us on a roller- coaster ride from innocence to experience without even a hint of that typical kiddie-flick sentimentality. <b>Label:</b> Positive	Q: What is happy in the context?	A: visually imaginative, thematically instructive and thoroughly delightful
Summarization	Reference: Paul Merson, the Sky Sports pundit, criticized Andros Townsend ( <i>sI</i> ) last week after his call-up to the england squad. Merson admitted it was a mistake after Townsend scored, bringing the match against Italy to a tie ( <i>s2</i> ) on Tuesday. Merson is a former Arsenal player himself. Generation: paul merson criticised andros townsend ( <i>s3</i> )'s call-up to the england squad . townsend hit back at merson after scoring for england against italy ( <i>s4</i> ). the tottenham midfielder was brought on in the 83rd minute against burnley.	<ul> <li>Q1: What happens after Paul Merson, the Sky Sports pundit, criticized Andros Townsend (<i>s1</i>)?</li> <li>Q2: What happens before Townsend scored, bringing the match against Italy to a tie (<i>s2</i>)?</li> </ul>	A1: townsend hit back at merson after scoring for england against italy ( <i>s4</i> ) A2: paul merson criticised andros townsend ( <i>s3</i> )

Figure 6: DISQ can be extended to perform unsupervised model interpretation on other NLP tasks. **Step 1:** We automatically generate Socratic-style questions with pre-defined prompts (in blue) and Spans in context (in purple). **Step 2:** Models are interrogated with these questions and we measure how well models perform in the questioning.

• Sentiment analysis: We believe the highlight span in Figure 6 is the evidence for a positive sentiment. A model needs to identify it with "*What is happy*" question prompt. Sentiment analysis, as a single sentence classification, may only require one span as the evidence, which is different from the reasoning over multiple spans in discourse and NLI. Therefore there might be no spans used in the questions.

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• Text summarization: Recent papers have initially studied using QA as a new measure for summarization evaluation. They generate a question from the reference summary and query the generated summary. However, they have not explored the role of discourse in their method. We briefly discuss how DISQ can incorporate discourse semantics into using QA for summarization evaluation. As shown in the reference summary in Figure 6, the two spans  $s_1$  and  $s_2$  link the discourse together with a salient Temporal relation. We believe such a relation is the key to making the summary coherent and should be reserved in the generated summary. We show a good generated summary where  $s_3$  and  $s_4$  also express such *Temporal* relation. We generate **Ques**tion 1 with "*What happens after*" prompt and  $s_1$ , expecting the answer  $s_4$  from the generated summary. In the meantime, **Question** 2 combines "*What happens before*" prompt and  $s_2$  and we expect its answer  $s_3$  from the generated summary. If the model can answer correctly for both questions, we believe the *Temporal* relation is realized in the generated summary. Interestingly, the reference and generation exhibit a symmetric property  $(s_1 - s_4)$ and  $s_2 - s_3$ . It is in the same spirit as we desire a good discourse understanding.

### B DISQ Generalizes Halliday's Cohesion Theory

We contribute DISQ as a computational tool to discover new cohesive ties. We recommend linguists apply DISQ on their corpora and examine the output. Halliday (1976)'s cohesion ties are welldefined but constrained. DISQ loosens these constraints by considering arbitrary semantic relation between arbitrary spans, conditioning on discourse relation and discourse coherence. NLMs are powerful tools by modeling the co-occurrence between words and sentences on billion texts, they have the 970

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Col	hesive Tie	Example	Semantic Rela- tion	Common Spans in the Tie
Co	njunction	Someone comes along with a great idea for an expedition, for example, I did a book called Sand Rivers, just before the Indian books, and it was a safari into a very remote part of Africa.	/	1
Reference	Exophoric ref- erence	Kate I must say this fish is cooked beautifully.	Identical	[Nominal, adverbial group] $\sim$ [Environment]
	Endophoric reference	There was once a velveteen rabbit . He was fat and bunchy	Identical / simi- lar / exclusive	[Nominal, adverbial group] $\sim$ [Word ( <i>he</i> , <i>it</i> )]
Sul	ostitution	Is he at home? I think so .	yes/no	[Clause, nominal, adverbial group] $\sim$ [Word ( <i>so</i> , <i>do</i> )]
1	Ellipsis	Is he at home? Yes he is Ø: at home.	yes/no	[Clause, nominal, adverbial group] $\sim [\emptyset]$
Lexic	al Cohesion	have you ever heard of any other kinds of literature in the medieval period besides Chaucer ?	Lexical relation (e.g. synonymy, hypernymy)	[word] ~ [word]
DIS	SQ (Ours)	In July, the Environmen- tal Protection Agency imposed a gradual ban , virtually all uses of as- bestos. By 1997, almost all remaining uses of cancer-causing asbestos will be outlawed.	Arbitrary re- lation (e.g. causal, compar- ative, similar, temporal)	Arbitrary span (Word, SRL- based spans, nominal and adverbial groups, clauses)

Table 8: Comparing DISQ with a non-exhaustive summary of (Halliday, 1976)'s cohesive ties.  $[\cdot] \sim [\cdot]$  denotes two spans forming a cohesive tie. DISQ covers a wider range of semantic relations and allows longer spans to be considered for cohesion. Some examples are excerpted from Ch. 9 in (Halliday et al., 2014).



Figure 7: DiSQ is a generalized extension to Halliday (1976)'s cohesion theory. Most of the defined cohesion types can be realized by DISQ, with the exception of exophoric reference which points outwards the text.

potential to inspire new cohesion theory.

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DISQ generalizes Halliday's theory in two aspects: (1) Semantic relation: DISQ enlarges the space of semantic relation for cohesion by the unlimited choice of question prompts. We have explored causal, comparative, equivalent, and temporal semantic relation using textual (discrete) prompt

in this work. In future, it is interesting to design soft (continuous) prompts by fusing different semantic relations. However, Halliday's cohesion theory only covers a very limited set of semantic relations, for example, identical and exclusive relation for reference, yes/no relation for ellipsis. The only exception is lexical cohesion. Richer lexical relations (synonymy, hypernymy, hyponymy) are the cohesive force. But it only operates on lexical items without considering longer textual units. (2) Spans in the tie: DISQ is able to explore the semantic relation between arbitrary spans. Even though we only studied SRL-based spans, it is easy to adapt to other spans like lexical items, nominal groups, and clauses to realize Halliday's cohesive ties. However, Halliday's ties are much more constrained than ours. They either work between words (lexical cohesion) or between one longer span and another word (pronouns like he or auxiliary like do). With the help of DISQ, we can explore the cohesive ties between two longer spans.

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We now briefly summarize each type of Halli-<br/>day's cohesion ties in Table 8 and discuss how they<br/>can be generalized by DISQ. (1) Conjunction:10101012

Halliday defines conjunctions as markers that link 1013 clauses cohesively. It is very similar to discourse 1014 connectives that link discourse arguments (some 1015 are longer sentences) together. We highlight the 1016 role of connective (conjunction) in DISQ and offer linguists a tool to test its function computationally. 1018 (2) **Reference**: Unlike conjunction that links whole 1019 clauses, reference achieves cohesion by linking ele-1020 ments in clauses. There are two types of references. 1021 Exophoric reference points outwards from the text 1022 and links to the environment the speakers and readers share. DISQ cannot handle such cases because 1024 we seek answers in context. Endophoric reference 1025 links elements in context. But we find the semantic 1026 relations are much more constrained to express the 1027 referential relation and the spans usually include words like personal pronouns. Longer forms of reference have been overlooked. (3) Substitution 1030 and (4) ellipsis are functionally equivalent since 1031 ellipsis can be considered as zero substitution. The 1032 cohesion is achieved through a (zero) substituted 1033 text span. Similar to reference, we find the semantic relation and spans are constrained to a small set. 1035 (5) Lexical cohesion: Unlike previous cohesive 1036 devices working at the grammatical level, lexical 1037 cohesion works at the lexical level by the choice of words. Even though they cover richer lexical 1039 semantics, they are constrained to work on word pairs. (6) DISQ is a generalized extension for Hall-1041 iday's theory. It models cohesion through arbitrary 1042 semantic relations between arbitrary spans. DISQ 1043 offers a computational estimation for the effects 1044 of conjunction, and it can realize reference, substi-1045 tution, ellipsis, and lexical cohesion with simple 1046 adaptations. Recently Hou (2020); Aralikatte et al. 1047 (2021) have studied to approach reference and el-1048 lipsis through QA. DISQ can extend this line and 1049 1050 explore a wider range of cohesive devices computationally. 1051

#### C Case study for Discourse Relation (Task 1)

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We only present one case study in Section 3. We now analyze more cases from the PDTB dataset to examine (1) whether the output is interpretable for human; (2) whether the answers are consistent with discourse relation. Specifically, we demonstrate one more successful case with the help of counterfactual explicit connective. We also present unsuccessful cases where undesired QA pairs are extracted. Finally, we present a curious case that possibly improves the prediction of discourse sense by inserting plausible connectives. We choose the BERT<sub>Large</sub> model because it has achieved good overall performance in D1SQ. 1063

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Discourse sense: Contingency.Cause.Result. Conn: as a
result
Arg1: In July, the Environmental Protection Agency
imposed a gradual ban on virtually all uses of asbestos.
Arg2: By 1997, almost all remaining uses of cancer-
causing asbestos will be outlawed.
<b>Question:</b> What is the result of imposing a gradual ban?
Answer: almost all remaining uses of cancer-causing
asbestos will be outlawed. Confidence: 0.58 (+0.18)
<b>Question:</b> What happens after imposing a gradual ban?
Answer: almost all remaining uses of cancer-causing
asbestos will be outlawed. Confidence: 0.20 (-)
Question: Why will almost all remaining uses of cancer -
causing asbestos outlawed? Answer: the Environmental
Protection Agency imposed a gradual ban on virtually all
uses of asbestos. <b>Confidence:</b> 0.18 (+0.12)

Table 9: Successful cases for DISQ with connective: Desired question prompts have retrieved their answers. Their confidence scores are even increased compared to the case without connective in Table 5. One more question prompt, "*What happens after*", has retrieved its answer.

#### Successful Case for DISQ with Explicit Connec-

tive Table 9 presents the same example in Table 5. The only difference is we insert the discourse connective between two arguments. We can observe that all desired questions in Table 5 can retrieve their answers. The additional question retrieving answer is *"What happens after"*. We don't count it as incorrect because the meanings of *"What is the result" and "What happens after" are similar to each other and this QA pair is interpretable by us. Interestingly, we find the confidence scores are even increased as compared to Table 5. It is interesting to explore the effect of the answer's confidence in future work.* 

Unsuccessful Case for DISQ with Counterfac-1081 tual Connective Table 10 presents a failure case 1082 for DISQ. The ground-truth discourse relation is 1083 Expansion, but we can see the question prompts 1084 are blurred together even if we have inserted the 1085 discourse connective. Both Expansion senses and 1086 Contingency senses are indicated. However, we do 1087 not attribute this failure entirely to the limitation of the BERT model's capacity. We can feel the 1089 discourse sense between Arg1 and Arg2 is indeed 1090 very ambiguous in Table 10. If this is the case, once 1091 DISQ has a blurred response, it might indicate the 1092 intrinsic ambiguity of the discourse it is processing. 1093

Discourse sense: Expansion Conn: in other words
Arg1: that these events took place 35 years ago Arg2: It
has no bearing on our work force today
<b>Question:</b> What is the result of taking place? <b>Answer:</b>
It has no bearing on our work force <b>Confidence:</b> 0.08
<b>Question:</b> Why did it have no bearing on our work force?
Answer: these events took place 35 years ago Confi-
<b>dence:</b> 0.46
<b>Question:</b> What is the reason of having no bearing on
our work force? Answer: these events took place 35
years ago <b>Confidence:</b> 0.61
<b>Question:</b> What is similar to having no bearing on our
work force? <b>Answer:</b> these events took place 35 years
ago Confidence: 0.20
<b>Question:</b> What is an example of having no bearing on

our work force? **Answer:** these events took place 35 years ago **Confidence:** 0.30

Table 10: Unsuccessful cases for DISQ with connective: The questions prompts are blurred even if we insert the discourse connective. They point to both Contingency and Expansion senses.

Discourse sense: Comparison						
Arg1: One claims he's pro-choice. Arg2: The other has						
opposed a woman's right to choose.						
Probability of predicted discourse sense: Comparison:						
0.42, Expansion: 0.49						
<b>Insert</b> "however" as a plausible discourse connective. #						
of answers: +2						
<b>Insert</b> "in addition" as a plausible discourse connective.						
<b># of answers:</b> +0						

Table 11: Curious cases for DISQ: It is possible to exploit the predictive power of DISQ to benefit the prediction task of discourse sense. We can insert plausible discourse connective and exploit the changes of DISQ's output for better sense prediction.

Curious Case of Using DISQ to help prediction Finally, we discuss a curious case of extending DISQ as an interpretation method to a predictive tool. As shown in Table 11, the prediction model is hesitating at the decision boundary for Comparison or Expansion relation. Now we insert the discourse connective for both plausible predicted senses: "however" for Comparison sense and "in addition" for Expansion sense. We observe that the model is able to generate two more answers after the insertion of "however" and no more answers for "in addition". It is possible to formalize this intuition as an iterating process: (1) we first insert a plausible connective to perform DISQ; (2) we then leverage DISQ's output to predict discourse sense and map it back to the connective. We leave this interesting exploration for future work.

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1111Summary of the Case Study: We perform an<br/>instance-level case study on DISQ's process on<br/>the PDTB dataset. We find those desired QA pairs

are interpretable by human (performed only by the<br/>author as a case study). We also identify unde-<br/>sired QA pairs in discourse. The reason might be<br/>attributed to both the limitation of NLMs and the<br/>intrinsic ambiguity of the discourse senses. We<br/>conclude with a curious case of exploiting DISQ<br/>for its potential predictive power.1114<br/>1115

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# D Case Study for Discourse Coherence (Task 2)

We have explored using DISQ's matrices (DISQM) for coherence modeling. We observe both positive and a negative correlation with human's judgement in Section 4. We explain it by an assertion that only correct Q&A pairs discovered by DISQ make a positive contribution to coherence. We now articulate our criteria for classifying Q&A pairs and showcase real DISQM generated from the SummEval dataset.

#### D.1 Criteria for Classifying Q&A Pairs

Example 1:					
Sent <sub>1</sub> : a mother was holding the two-year-old boy and					
another child when the toddler slipped and fell into the					
pit at 3pm on saturday.					
Sent <sub>2</sub> : his parents jumped in and pulled him to safety					
before paramedics arrived to treat the boy for a leg injury.					
Ex. 1.1, Correct					
<b>Q1:</b> What happens after falling into the pit?					
A1: his parents jumped in and pulled him to safety					
Ex. 1.2, Incorrect (Type 1)					
<b>Q2:</b> What happens before falling into the pit?					
A2: his parents jumped in and pulled him to safety					
Ex. 1.3, Incorrect (Type 2)					
Q3: What is the reason of his parents jumping in?					
A3: 3pm on saturday.					
Example 2:					
Sent: luigi costa, 71, is accused of killing his elderly					
neighbour terrence freebody in the dining room of his					
home on mugga way, red hill, canberra in july 2012.					
Sent <sub>2</sub> : forensic psychiatrist professor paul mullen exam-					
ined costa after the attack and believes there was evidence					
of the accused's state of mind declining.					
Ex. 2. Non-contextual					
<b>O1</b> : What is the result of killing his elderly neighbour					
terrence freebody?					
A1: state of mind declining					

Table 12: Criteria for classifying Q&A pairs into correct, incorrect (two types), and non-contextual categories. Examples are excerpted from DISQ's output on the SummEval dataset.

DISQ links spans in discourse through the Q&A pairs extracted by questioning. Due to the limitation of NLMs, only a portion of extracted Q&A pairs is correct. We classify them with the following criteria:

• **Correct:** The two spans  $(s_1 \text{ and } s_2)$  in ques-1138 tion and answer satisfy the relation of the ques-1139 tion prompt p. The link between  $s_1$  and  $s_2$ 1140 contributes to coherence and is the key to un-1141 derstanding discourse relation. As Ex. 1 in 1142 Table 12, the semantic relation indicated by 1143 "what happens after" is the key to understand-1144 ing the temporal relation. 1145

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- Incorrect: There are two types of incorrect cases. Type 1, Incorrect prompt: s<sub>1</sub> and s<sub>2</sub> are related, but their relation is not consistent with the question prompt p. The two spans in Ex. 2 are indeed related, but their relation is not indicated by "what happens before". Type 2, Irrelevant spans: s<sub>1</sub> and s<sub>2</sub> are not related. That is to say, the model retrieves a wrong answer. As in Ex. 3, the two spans are not relevant and should not be retrieved by the model.
  - Non-contextual: Two spans (s<sub>1</sub> and s<sub>2</sub>) satisfy the relation of question prompt p out of context, but not in correct context. Let's study Ex. 2 in Table 12, it is reasonable to consider "state of mind declining" as the result of the victim of a murder. But in the given discourse, "state of mind declining" actually refers to the murderer, hence the two spans do not satisfy the "result" relation.

#### D.2 DISQM from SummEval Dataset

We demonstrate DISQ's output matrices (DISQM) given instances in SummEval dataset. We cover the four topologies we discussed in Section 6, with desired symmetric properties, and undesired properties including self-contradiction and hallucination.



Figure 8: DISQM and Q&A pairs for symmetric structure (**Topology 1**).

1172**Topology 1 (Symmetry):** Figure 8 shows a symmetric structure emerges in DISQM. The two

spans come from the two opposing sentences, and 1174 they can extract each other as the answer with op-1175 posing prompts ("result"-"reason"). Even though 1176 we feel the causal semantic is not as strong as 1177 the temporal relation (characterized by "what hap-1178 pens before/after" prompts), we still recognize the 1179 model as being self-consistent and reinforce its 1180 comprehension with such a symmetric structure. 1181

	Why	Result	Reason	Different	Opposite	Similar	Example	Before	After
well	1	0	0	0	0	0	0	0	0
race	0	0	0	0	0	0	0	0	0
finish	1	0	0	0	0	0	0	0	0
Sent: wiggins will race in front of a sell-out crowd at london's olympic velodrome. Sent2: the briton finished his team sky career at paris-roubaix last sunday. Q1: Why will wiggins race in front of a sell - out crowd at london 's olympic velodrome ? A1: the briton finished his team sky career									
Q2: Why did the briton finish his team sky career at paris - roubaix last sunday ? A2: wiggins will race in front of a sell-out crowd									

Figure 9: DISQM and Q&A pairs for self-contradiction case (**Topology 2**).

**Topology 2** (Self-contradiction): Selfcontradiction emerges in the DISQM in Figure 9. Two spans,  $s_1$  and  $s_2$  are extracting each other as the answer with the same prompt "*why*". It means the model believes  $s_1$  and  $s_2$  are reasons for each other. Such circular reasoning is considered self contradiction and demonstrates that the model has not fully understood the discourse.

	Why	Result	Reason	Different	Opposite	Similar	Example	Before	After
appealing	0	0	0	0	0	0	0	0	0
help	0	1	1	0	0	0	0	1	1
identify	0	1	1	0	0	0	1	1	1
robbed	1	1	0	0	0	0	1	1	1
made	0	0	0	0	0	0	0	0	0
Sent2: he made off with the dairy 's till and about \$ 1500 in cash.         Q1: Why did a man rob a christchurch dairy ?         A1: he made off with the dairy 's till and about \$ 1500 in cash         Q2: What is the result of robbing a christchurch dairy ?         A2: \$ 1500 in cash									
Q3: What is an example of robbing a christchurch dairy ? A3: the dairy 's till									
Q4: What happens after robbing a christchurch dairy ? A4: he made off with the dairy 's till and about \$ 1500 in cash									
Q5: What happens before robbing a christchurch dairy ? A5: the dairy 's till and about \$ 1500 in cash									

Figure 10: DISQM and Q&A pairs for selfcontradiction case (**Topology 2**) and hallucination (**Topology 4**).

**Topology 3 (Self-contradiction) and Topology 4** (**Hallucination**): Let's now focus on the fourth 1182

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Figure 11: Performance of BERT models on DISQ: We present the score of  $\hat{V}(R, p) - 1$ . A score > 0 is considered sensitive between R and p. There is a steady trend that sensitivity increases with model size increases (Tiny  $\rightarrow$  Base  $\rightarrow$  Large). Insertion of explicit connectivity (right) boosts the association for all models without connective (left).



Figure 12: Performance of RoBERTa on DISQ: We present the score of  $\hat{V}(R, p) - 1$ . A score > 0 is considered sensitive between R and p. A steady trend among Tiny, Base, Large model sizes can be observed for DISQ without connective (left), but the tread is not clear in DISQ with connective (right). The Y-axis is in the same scale as Figure 11.

row in the DISQM in Figure 10. We only show-1192 case DISQ's output given the span of "robbing a 1193 christchurch dairy". (1)Self-contradiction: We first 1194 find that both "why" and "result" extracts similar 1195 answers in the meantime, which is not logical. A 1196 similar case also happens in "before" and "after" 1197 question prompts, which is not logical because a 1198 fact cannot happen before and after another fact in 1199 the meantime. (2) Hallucination: Model responds 1200 to 5 out of 9 question prompts. Besides the illogical 1201 cases discussed already, the model also retrieves an 1202 incorrect Q&A pair using the "example" prompt. It might be explained by a conjecture that the model 1204 may not infer the discourse relation properly and 1205 decides whether many spans are related to each 1206 other. 1207

## E How do NLMs' different designs impact DISQ?

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We have walked through fine-grained studies for one model in Section 3, let's now compare different models' performance on DISQ. This is an interesting question because different models can lead to different performances on discourse tasks ((Chen et al., 2019)). To facilitate inter-model comparison, we simplify the measure of  $sen_n(R, p)$  by only considering  $p \in \mathcal{P}_R$ , for which we desire a high sensitivity (*i.e.*, those desired cells marked **as bolded**). That is to say, we approximate a column's result by only one cell (the desired cell marked **as bolded**). For example, in the column of "What is different from" question in Table 4, we approximate it by the cell of *Comparison* relation, which represents  $\hat{V}(R, p) = 2.232$ . In practice, we present  $\hat{V}(R, p) - 1$ , because a random baseline should also achieve a normalized V(R, p) of 1.

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We first present how BERT models ((Devlin et al., 2019)) of different sizes perform on DISQ. We have obtained the following findings: (1) Clearly all models demonstrate association between R and p. It is a strong result for BERT models to comprehend discourse by reasoning over spans and identifying the relations among them. The prompts for Comparison and Temporal rela-

tions are performing better, which is in line with 1235 our discovery in Section 3. (2) Figure 11 exhibits a 1236 clear correlation between performance and model 1237 sizes. The Tiny model (blue) tends to be least sen-1238 sitive, the Base model (green) the medium, and the Large model (grey) the most sensitive. This trend is 1240 steady w.r.t. different question prompts. (3) Inser-1241 tion of explicit connective also brings steady boosts 1242 to almost all models and all questions. Interesting, 1243 there is a big variance w.r.t. the boost to different 1244 questions. For example, "What is different from" 1245 questions are much higher than "What is similar to" 1246 questions. This might be due to the frequency of 1247 keywords in pre-training data or fine-tuning data 1248 ((Razeghi et al., 2022)). 1249

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We then perform the same set of experiments on RoBERTa models ((Liu et al., 2019)). We have the following findings: (1) RoBERTa models also have a good performance on DISQ. As we can see in Figure 12, most sensitivity scores are positive values, and only a small portion of them have slightly negative values. It is a strong result for RoBERTa, because it has removed the Next Sentence Prediction (NSP) training objective which is believed to be useful for modeling over longer contexts. It means RoBERTa has implicitly constructed discourse-level understanding through other training objectives; (2) We find the trend among Tiny, Base, and Large is steady for DISQ without connective (left), but not steady for DISQ with connective (right). For example, the Base model achieves better V(R, p) than the Large model in "Different" and "Opposite" questions in the right figure. We leave the exploration of this interesting phenomenon for future work.

#### F Reproducibility

#### F.1 Neural Language Models (NLMs)

We have applied DISQ to examine NLMs' capacity for discourse understanding. We follow Choudhury et al. (2022) to study BERT family (Devlin et al., 2019; Liu et al., 2019).

To enable NLMs to perform QA, we choose models fine-tined on SQuAD 2.0 dataset (Rajpurkar et al., 2018). Specifically, we use a set of offthe-shelf models shared through the Hugging Face community. This is because these models are very popular in the community and many applications have been built on top of them. We hope our findings generated with DISQ can help the users of these models diagnose the discourse capacity for

Model	Configurations	URL
BERT <sub>tiny</sub>	67M parame-	https://huggingface.co
	ters, 6l, 768d	/deepset/tinybert-61-
		768d-squad2
BERT <sub>base</sub>	110M parame-	https://huggingface.co
	ters, 12l, 768d	/deepset/bert-base-
		uncased-squad2
BERT <sub>large</sub>	340M parame-	https://huggingface.co/
_	ters, 24l, 1024d	deepset/bert-large-
		uncased-whole-word-
		masking-squad2
RoBERTatiny	76M parame-	https://huggingface.co/
	ters, 6l, 768d	deepset/tinyroberta-
		squad2
RoBERTabase	125M parame-	https://huggingface.co/
	ters, 12l, 768d	deepset/roberta-base-
		squad2
RoBERTalarge	355M parame-	https://huggingface.co/
	ters, 24 <i>l</i> , 1024 <i>d</i>	deepset/roberta-large-
		squad2

Table 13: We examine BERT family with different configurations. Please refer to the URL for model details.

these models. These models also come with MIT or CC BY 4.0 licenses. Detailed model cards can be found in the URLs. 1285

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#### F.2 Computational Costs

DISQ is an unsupervised interpretative measure, 1289 hence no training is required. We directly deploy 1290 the off-the-shelf NLMs and do not tune any parame-1291 ters of it. As for the evaluation of the PDTB dataset 1292 (around 12k discourse instances), the computation 1293 costs around 3 hours, 6 hours, and 10 hours for 1294 tiny, base, and large models respectively on a sin-1295 gle NVIDIA V100 GPU. As for the evaluation of 1296 the SummEval dataset (1700 summaries), the com-1297 putation costs around 5 hours, 10 hours, and 17 1298 hours for tiny, base, and large models respectively on a single NVIDIA V100 GPU. 1300

#### F.3 Packages

We use AllenNLP's toolkit for semantic role labeling <sup>4</sup> for question generation and use spaCy model<sup>5</sup> to perform sentence segmentation for the summaries in the SummEval dataset.

<sup>&</sup>lt;sup>4</sup>https://storage.googleapis.com/allennlp-publicmodels/structured-prediction-srl-bert.2020.12.15.tar.gz

<sup>&</sup>lt;sup>5</sup>https://github.com/explosion/spacy-models/releases/tag/ en\_core\_web\_sm-3.4.0