### **000 001 002 003 004** EDIT: A LOCAL-SGD-BASED EFFICIENT DIS-TRIBUTED TRAINING METHOD FOR LARGE LAN-GUAGE MODELS

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## ABSTRACT

Distributed training methods are crucial for large language models (LLMs). However, existing distributed training methods often suffer from communication bottlenecks, stragglers, and limited elasticity, particularly in heterogeneous or largescale environments. Local SGD methods have been proposed to address these issues, but their effectiveness remains limited to small-scale training due to additional memory overhead and concerns on efficiency and stability. To tackle these issues, we propose EDiT, an innovative Efficient Distributed Training method that combines a tailored Local SGD approach with model sharding techniques to enhance large-scale training efficiency. EDiT performs layer-wise parameter synchronization during forward pass, reducing communication and memory overhead and enabling the overlap of computation and communication. Besides, EDiT employs a pseudo gradient penalty strategy to suppress loss spikes, which ensures training stability and improve performance. Additionally, we introduce A-EDiT, a fully asynchronous variant of EDiT that accommodates heterogeneous clusters. Building on EDiT/A-EDiT, we conduct a series of experiments to validate largescale asynchronous training for LLMs, accompanied by comprehensive analyses. Experimental results demonstrate the superior performance of EDiT/A-EDiT, establishing them as robust solutions for distributed LLM training in diverse computational ecosystems.

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## 1 INTRODUCTION

**034 035 036 037 038 039 040 041 042 043** Distributed training stands as the cornerstone for deep neural networks [\(Dean et al., 2012\)](#page-10-0). With the explosive growth of model scale and data volume [\(Touvron et al., 2023;](#page-11-0) [Bai et al., 2023\)](#page-10-1), techniques such as Zero Redundancy Optimizer (ZeRO) [\(Rajbhandari et al., 2020\)](#page-11-1) and 3D Parallelism [\(Narayanan et al., 2021\)](#page-11-2) are precipitated to address the challenges of GPU memory overflow. These approaches rely on synchronous paradigm, which introduces significant communication overhead during the training process [\(Douillard et al., 2023\)](#page-10-2). Besides, the synchronous paradigm also introduces the straggler problem, where faster workers are idle waiting for the slower ones to catch up. This issue is particularly prevalent in large/heterogeneous clusters [\(Lian et al., 2018\)](#page-10-3). Lastly, in resource-constrained clusters, there is a compelling need for elastic training [\(Li et al., 2023\)](#page-10-4). However, synchronous training paradigms struggle in elastic settings, where dynamic scaling of resources disrupts optimal hyperparameters and requires slow redistribution of model parameters.

**045 046 047 048 049 050 051 052 053** These challenges have spurred significant research into distributed optimization methods. A typical method is Local Stochastic Gradient Descent (a.k.a Local SGD or Local-Update SGD) [\(Zhang](#page-12-0) [et al., 2016\)](#page-12-0), where each worker independently executes multiple local optimization steps in parallel before averaging model parameters across all workers. Subsequent studies have improved upon this foundational paradigm to improve the performance [\(Lin et al., 2019;](#page-10-5) [Wang et al., 2019;](#page-12-1) [Douil](#page-10-2)[lard et al., 2023\)](#page-10-2). However, existing Local SGD methods are not easily applicable to the training of large language models (LLMs). These methods do not handle model sharding well, preventing their application to models larger than billions of parameters. Moreover, previous applications of Local SGD have focused on small-scale, highly curated datasets [\(Zhang et al., 2016;](#page-12-0) [Douillard](#page-10-2) [et al., 2023\)](#page-10-2), making their results less transferable to LLM training that relies on vast, noisy datasets where instability may be introduced during the training process. Although current Local SGD meth-

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Figure 1: The schematic illustration of our proposed EDiT method with 4 workers and a  $2 \times 2$  device mesh as an example. The left part shows the communication groups and parameter sharding, and the right part presents the detailed computation and communication flows within worker B.

**071 072 073 074 075 076 077** ods can improve overall training efficiency by reducing communication frequency and diminishing the impact of random stragglers, they still struggle with the presence of consistent stragglers within heterogeneous devices [\(Liu et al., 2024\)](#page-10-6). Additionally, because most existing Local SGD methods synchronize all parameters globally after some local optimizer updates, extra communication overhead are introduced [\(Sun et al., 2023\)](#page-11-3). Lastly, current Local SGD methods predominantly employ a uniform averaging strategy to synchronize the parameters, failing to fully capitalize on the inherent differences in training progress across diverse workers [\(Douillard et al., 2023\)](#page-10-2).

**078 079 080 081 082 083 084 085 086 087 088 089 090 091 092** To address these challenges, we propose a novel Efficient Distributed Training (EDiT) method for large language models. As illustrated in Figure [1,](#page-1-0) EDiT employs a hierarchical distribution strategy on a two-dimensional device mesh, where all workers are data parallel. Model parameters are fully sharded along the model shard dimension and synchronized along the model sync dimension. With the efficient communication links within the model shard groups and the low-frequency periodic synchronization strategy within the model sync groups, the impact of communication overhead and random stragglers is effectively alleviated. When synchronizing parameters, EDiT operates layer by layer during the forward pass and makes use of a prefetch strategy to overlap computation and communication, thereby reducing the additional communication and GPU memory overhead introduced by parameter synchronization. Additionally, EDiT employs a novel pseudo-gradient penalty method to address the instability caused by workers progressing differently due to the diverse large-scale corpus, and it leverages these differences among workers. Furthermore, we propose an asynchronous variant of the EDiT method named A-EDiT to deal with the consistent stragglers in heterogeneous clusters. We conducted a comprehensive evaluation of our proposed methods on LLM tasks, demon-strating its effectiveness compared to state-of-the-art methods. <sup>[1](#page-1-1)</sup>

- **093** Our primary contributions can be summarized as follows:
	- Engineering Innovation: We introduce EDiT, an efficient large-scale distributed training method that integrates Local SGD with the model sharding strategy. EDiT reduces the impact of stragglers and communication overhead and supports elastic training.
	- Algorithmic Novelty: EDiT performs layer-wise parameter sync during forward pass to reduce communication and memory overhead. With prefetch strategy, the parameter-sync communication can be further overlapped with computation. Besides, we propose a new pseudo gradient penalty method to improve the training stability and model performance. We also provide a fully asynchronous variant of EDiT, called A-EDiT, to address the challenges of consistent stragglers.
- **103 104 105 106 107** • Practical Contributions: We provide a large-scale verification of asynchronous pre-training for LLMs, along with an extensive analysis of convergence, generalization, acceleration, scalability, and stability. This work offers critical insights into optimizing asynchronous distributed LLM training at scale.

<span id="page-1-1"></span><sup>&</sup>lt;sup>1</sup>The core code is in the supplementary material, and all code will be released after the paper is accepted.

#### **108 109** 2 RELATED WORK

**110 111 112 113 114 115 116 117 118 119 120 121 122 123 124** One of the early works that proposed the concept of Local SGD was [Zhang et al.](#page-12-0) [\(2016\)](#page-12-0), establishing the paradigm of parallel multi-step training followed by periodic averaging. [Lin et al.](#page-10-5) [\(2019\)](#page-10-5) introduced the Post Local SGD method, which starts with standard synchronized training for warm-up before switching to the Local SGD mode. SlowMo [\(Wang et al., 2019\)](#page-12-1) utilizes a slow momentum to transform model averaging into moving average. DiLoCo [\(Douillard et al., 2023\)](#page-10-2) demonstrates that the Nesterov optimizer [\(Nesterov, 1983\)](#page-11-4) is suitable as an outer optimizer. Multi-Level Local SGD [\(Castiglia et al., 2020\)](#page-10-7) partition the network into disjoint sub-networks and hierarchically synchronizes the models. [Wang & Joshi](#page-12-2) [\(2019\)](#page-12-2) and [Balles et al.](#page-10-8) [\(2023\)](#page-10-8) have respectively explored the optimal hyperparameter settings for Local SGD. [Shen et al.](#page-11-5) [\(2021\)](#page-11-5) advocated for gradually increasing synchronization intervals while decreasing learning rates to optimize model performance. Extensive theoretical analyses of Local SGD have also emerged. [Yu et al.](#page-12-3) [\(2019\)](#page-12-3), [Khaled et al.](#page-10-9) [\(2020\)](#page-10-9), [Spiridonoff et al.](#page-11-6) [\(2020\)](#page-11-6), and [Deng et al.](#page-10-10) [\(2022\)](#page-10-10) examined convergence rates under various conditions. [Gu et al.](#page-10-11) [\(2022\)](#page-10-11) found that Local SGD improves generalization with a small learning rate and long training duration. [Pan & Song](#page-11-7) [\(2023\)](#page-11-7) demonstrated faster convergence by leveraging second-order information.

**125 126 127 128 129 130 131 132 133 134** Researchers have also explored the combination of Local SGD with asynchronous training paradigms that decouple computation and communication. Early works were predominantly based on the federated learning framework [\(Xie et al., 2019\)](#page-12-4). FedBuff [\(Nguyen et al., 2022\)](#page-11-8) updates the server model only after accumulating a certain amount of pseudo gradients. DN-DyLN [\(Liu et al.,](#page-10-6) [2024\)](#page-10-6) improves the buffer mechanism to employ delayed Nesterov update. TimelyFL [\(Zhang et al.,](#page-12-5) [2023\)](#page-12-5) dynamically adjusts the local training workload according to the real-time resource situation. Subsequently, several works based on other architectures were also proposed. Gossip-PGA [\(Chen](#page-10-12) [et al., 2021\)](#page-10-12) incorporates periodic global averaging into the gossip SGD framework [\(Lian et al.,](#page-10-13) [2017\)](#page-10-13). CO2 [\(Sun et al., 2023\)](#page-11-3) utilizes Local SGD and asynchronous communication to hide the overhead. A key challenge for asynchronous training is the staled model problem, resulting in inferior performance compared to synchronous training methods [\(Liu et al., 2024\)](#page-10-6).

**135 136 137 138 139 140 141 142 143** Notably, current All-Reduce-based Local SGD methods [\(Lin et al., 2019;](#page-10-5) [Wang et al., 2019;](#page-12-1) [Sun](#page-11-3) [et al., 2023\)](#page-11-3) hold complete model parameters on each GPU, making it difficult to handle model sharding for LLM training. Although [Sun et al.](#page-11-3) [\(2023\)](#page-11-3) claims that they can combine CO2 with ZeRO series optimizers [\(Rajbhandari et al., 2020\)](#page-11-1), the additional communication introduced degrades CO2 to a synchronized mode, negating the performance gains from periodic synchronization and overlapped communication. Furthermore, the extra parameters and outer momentum further increase memory pressure, limiting their scalability to larger models. In contrast, our proposed EDiT and A-EDiT methods effectively utilize the characteristics of model sharding, leveraging device mesh, layer-wise parameter synchronization, prefetch strategy, and CPU offload to minimize communication and memory overhead, making it more suitable for LLM training.

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# 3 METHOD

**148** 3.1 OVERVIEW

**149 150 151 152 153 154 155 156 157 158 159** Our proposed EDiT method integrates model sharding with periodic synchronization to accelerate the training of LLMs. The detailed procedure of EDiT is illustrated in Figure [1](#page-1-0) and for-mally outlined in Algorithm [1](#page-13-0) in Appendix. To start with, EDiT builds an  $M \times N$  device mesh across K workers : M model sync groups  $\mathcal{G}^r = \{\mathcal{G}^r_1, \cdots, \mathcal{G}^r_M\}$  with each comprising N workers  $\mathcal{G}_i^r = \{ \mathcal{W}_{(i,1)}, \mathcal{W}_{(i,2)}, \cdots, \mathcal{W}_{(i,N)} \}$  $\mathcal{G}_i^r = \{ \mathcal{W}_{(i,1)}, \mathcal{W}_{(i,2)}, \cdots, \mathcal{W}_{(i,N)} \}$  $\mathcal{G}_i^r = \{ \mathcal{W}_{(i,1)}, \mathcal{W}_{(i,2)}, \cdots, \mathcal{W}_{(i,N)} \}$ <sup>2</sup>, and N model shard groups  $\mathcal{G}^s = \{ \mathcal{G}_1^s, \cdots, \mathcal{G}_N^s \}$  with each comprising M workers  $\mathcal{G}_i^s = \{ \mathcal{W}_{(1,i)}, \mathcal{W}_{(2,i)}, \cdots, \mathcal{W}_{(M,i)} \},$  where  $M \times N = K$ . This structured arrangement aims to tailor communication patterns to the diverse capabilities and network latencies inherent in the distributed system. For instance, in a multi-node GPU cluster where intra-node communication is significantly faster than inter-node communication, all GPUs within the same node can be connected as a model shard group, while GPUs of the same rank across different nodes can be connected as a model sync group. Model parameters are sharded uniformly in each model

<span id="page-2-0"></span><sup>&</sup>lt;sup>2</sup>The employment of double subscripts herein is merely a notational convenience to denote the relationship between workers and groups. Similar considerations apply to the cases discussed below.

**162 163 164 165 166 167 168 169 170** shard group and each worker  $W_i$  retains a fraction of each parameter for the complete L modules:  $\theta^{(i)} = \{\theta^{(i,1)}, \cdots, \theta^{(i,L)}\}$ . In this way, workers as a whole within a model shard group  $\mathcal{G}_i^s$  maintain a complete replica of model parameters:  $\theta = \text{Concat}(\{\theta^{(i)} : \theta^{(i)} \in \mathcal{G}_i^s\})$ , while workers within a model sync group  $G_i^r$  maintain an identical shard of the parameters. The EDiT method centralizes communication-intensive operations within the model shard groups and utilizes periodic synchronization to mitigate the communication overhead in the model sync groups, thereby achieving training acceleration. To enhance the stability of the initial training process, EDiT utilizes a two-phase training strategy. This begins with a warmup phase using standard mini-batch SGD, followed by a periodic synchronization phase utilizing Local SGD. More specifically,

- **171 172 173 174 175 176 177 178 179** 1. During the forward pass of the  $l$ -th module, if the current updated step requires model synchronization, *i.e.*,  $(t*\tau+p) > t_{warm}$  and  $p == 0$  where t is the outer step, p is the inner step,  $t_{warm}$  is the number of warmup steps and  $\tau$  is the synchronization interval, parameters are synced in model sync groups, as outlined in lines 7 to 9 in Algorithm [1.](#page-13-0) In practice, the communication overhead is minimal due to the large synchronization interval ( $\tau \gg 1$ ) and sharded parameters. Herein a novel pseudo gradient penalty strategy is introduced to enhance training stability that will be detailed. After that, each worker gathers the full module parameters through its model shard group for forward computations and promptly frees excess parameters to conserve memory.
- **180 181 182 183 184 185** 2. During the backward pass of the l-th module, workers again aggregate parameters via model shard groups for gradient calculations, followed by a *reduce-scatter* operation to average gradients across each model shard group. If the current step  $t$  is within the warmup phase, *i.e.*,  $t \leq t_{warm}$ , an additional *all-reduce* operation will be performed within each model sync group to synchronize gradients across all workers; otherwise this operation will be skipped (lines 19 to 21). Afterwards, each worker frees the excess parameters.
	- 3. Once all modules have completed one forward-backward iteration, the optimizer updates the local parameters of each worker. Note that to distinguish from the outer optimizer (OuterOpt) used in parameter synchronization, we refer to the optimizer for local updates as the inner optimizer (InnerOpt).

**190 191 192 193 194 195** Different from other Local SGD methodologies that synchronize parameters after optimizer update, EDiT performs layer-wise parameter synchronization during forward pass. In practice, we normally employ a prefetch strategy that aggregates parameters for the upcoming module concurrently with ongoing computations, with which communications within model sync groups can be effectively overlapped with forward computations. In this way, EDiT further diminishes the additional communication overhead introduced by parameter synchronization.

**196 197 198 199** It is also noteworthy that EDiT is compatible with most current large-scale distributed training frameworks. Although this manuscript mainly discusses its integration within ZeRO-3/FSDP framework [\(Rajbhandari et al., 2020\)](#page-11-1), it can be transposed with relative ease to other frameworks such as 3D parallelism [\(Shoeybi et al., 2019\)](#page-11-9).

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# <span id="page-3-0"></span>3.2 PSEUDO GRADIENT PENALTY

![](_page_3_Figure_9.jpeg)

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**212 213 214** Figure 2: Illustration of model synchronization and our proposed pseudo gradient penalty method, depicted with an example of four workers in a model sync group.

**215** Despite diligent data cleaning efforts, there are still significant amount of low-quality data in the LLM pre-training corpora [\(Albalak et al., 2024\)](#page-10-14), resulting in training instability manifested as loss **216 217 218** spikes. This issue can be addressed by large batch sizes typical of synchronous training regimes, but becomes salient in Local SGD regimes where each worker operates on relatively smaller batches.

**219 220 221 222 223 224 225** To tackle this issue, we introduce a novel pseudo gradient penalty strategy at the parameter synchronization stage, as depicted in Figure [2](#page-3-0) and Algorithm [2](#page-14-0) in Appendix. This strategy consists of anomaly elimination, weighted averaging, and gradient clipping. To illustrate the idea, we use a model sync group  $\mathcal{G}_m^r = \{W_1, \cdots, W_N\}$  as an example. We begin by computing the pseudo gradients  $\Delta_t^{(i,l)}=\theta_{t,\tau}^{(i,l)}-\theta_t^{(i,l)}$  for each worker, where  $\theta_{t,\tau}^{(i,l)}$  is the sharded parameters of module  $l$  held by worker  $W_i$  at outer step t and inner step  $\tau$ , and  $\theta_t^{(i,l)}$  denotes the corresponding synchronized parameters at the beginning of outer step  $t$ .

**226 227 228 229 230 231 232 233 234 235 236 237** Anomaly elimination. We first eliminate the significantly anomalous workers to reduce their adverse impacts on the overall model performance. Since anomalies cause substantial parameter fluctuations and lead to large pseudo-gradient norms, we use the pseudo-gradient norm as the criterion. Here we utilize an Exponential Moving Average (EMA) z-test method for statistical analysis. Let  $G_t^{(i,l)} = \|\Delta_t^{(i,l)}\|_2$  denotes the pseudo gradient norm for the worker  $\mathcal{W}_i$ , then the EMA z-score can be calculated by  $z_t^{(i,l)} = \frac{G_t^{(i,l)} - \mu_t^{(i,l)}}{\sigma_t^{(i,l)}}$ , where  $\mu_t^{(i,l)}$  and  $\sigma_t^{(i,l)}$  are the EMA mean and standard deviation of  $G_t^{(i,l)}$ , respectively. A worker  $\mathcal{W}_i$  with  $z_t^{(i,l)} > \delta$  is identified as an anomaly and its  $G_t^{(i,l)}$ will be set to infinity, where  $\delta$  is a threshold, typically set to 3 in practice. Both  $\mu_t^{(i,l)}$  and  $\sigma_t^{(i,l)}$  are updated at each step using an exponential moving average to capture the convergence trend of the gradient norm during the training process:

<span id="page-4-0"></span>
$$
\mu_{t+1}^{(i,l)} = \alpha G_t^{(i,l)} + (1 - \alpha)\mu_t^{(i,l)}, \quad \sigma_{t+1}^{(i,l)} = \sqrt{(1 - \alpha)(\sigma_t^{(i,l)})^2 + \alpha(G_t^{(i,l)} - \mu_{t+1}^{(i,l)})^2},\tag{1}
$$

**239 240 241 242 243 244 245 246 247** where  $\alpha$  is a weighting coefficient, commonly assigned a value of 0.02 in practical applications. The update of Equation [1](#page-4-0) will be skipped if  $G_t^{(i,l)}$  is infinite. In the preliminary stage, a warm-up period is set to establish stable values for  $\mu_t^{(i,l)}$  and  $\sigma_t^{(i,l)}$ , during which no workers are flagged as anomalies. Notably, to maintain consistent updates within the same module, we compute the pseudo gradient norm for the entire module, and subsequently introduced gradient norm-related operations follow the same procedure. Because this process only introduces one scalar communication in the model shard groups, the overhead is negligible. If all workers are identified anomalous, all the parameters will be effectively rollbacked to the last synchronized parameters  $\pmb{\theta}_{t}^{(i,l)}.$ 

**248 249 250 251** Weighted averaging. Furthermore, considering that large pseudo gradients may still exert considerable impacts on the overall update direction, we propose to weigh the pseudo gradients of each worker based on the norms, which was similarly demonstrated in [Thakkar et al.](#page-11-10) [\(2023\)](#page-11-10). The weight assigned to the pseudo gradients corresponding to  $\mathcal{W}_i \in \mathcal{G}_m^r$  is calculated by

<span id="page-4-1"></span>
$$
w_{t,i} = \frac{\exp(-G_t^{(i,l)})}{\sum_j \exp(-G_t^{(j,l)})}.
$$
\n(2)

In this way, a larger pseudo gradient norm leads to stronger suppression, thereby allowing all workers to contribute equally to the update direction and thus increasing the likelihood to find the correct direction. Following that, by performing a weighted summation of all pseudo gradients in  $\mathcal{G}_m^r$ , we obtain the synchronized pseudo gradients:

∆¯

<span id="page-4-3"></span>
$$
\bar{\mathbf{\Delta}}_t^{(i,l)} = \sum_j w_{t,j} \mathbf{\Delta}_t^{(j,l)}, \forall \mathcal{W}_i \in \mathcal{G}_m^r. \tag{3}
$$

Gradient clip. We then adopt a gradient clip strategy to constrain the update step size. Let  $\bar{G}^{(i,l)}_t = \|\bar{\mathbf{\Delta}}_t^{(i,l)}\|_2$  denote the synchronized pseudo gradient norm and  $\phi$  denote the threshold, the clip coefficient is computed by

<span id="page-4-4"></span>
$$
\beta_t = \min(\phi/(\bar{G}_t^{(i,l)} + \epsilon), 1),\tag{4}
$$

**268** where  $\epsilon$  is a small positive constant to avoid division by zero. The pseudo gradients are clipped by

<span id="page-4-2"></span>
$$
\widehat{\mathbf{\Delta}}_t^{(i,l)} = \beta_t \bar{\mathbf{\Delta}}_t^{(i,l)}.
$$
\n(5)

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**270 271** Proceeding further, we update  $\theta_t^{(i,l)}$  by  $\theta_{t+1}^{(i,l)} = \text{OuterOpt}(\theta_t^{(i,l)}, \hat{\Delta}_t^{(i,l)})$  on each worker.

**272 273 274 275 276 277 278 279** In EDiT, the extra parameters and outer momentum on each worker are sharded in correspondence with the sharded parameters. Compared to previous methods that maintain full extra parameters and outer momentum on each worker, EDiT reduces the additional memory usage. Additionally, based on layer-wise synchronization and prefetch strategy, EDiT can further offload the extra parameters and outer momentum to the CPU and only transfer the corresponding layer's data to GPU as needed, thereby minimizing memory overhead. Since the data for each layer is relatively small, the GPU-CPU data transfer can be effectively overlapped with GPU computations and GPU-GPU communications, ensuring fast parameter synchronization.

# 3.3 ASYNCHRONOUS EDIT

<span id="page-5-0"></span>![](_page_5_Figure_4.jpeg)

Figure 3: A comparison of the synchronization scheme of EDiT and A-EDiT.

**292 293 294 295** EDiT requires periodic synchronization at every  $\tau$  inner iterations. However, the fastest worker idles awaiting the peers to finish  $\tau$  iterations even if it completes its own  $\tau$  iterations earlier. As a consequence, the overall training efficiency is pegged to the slowest worker. This issue becomes more pronounced in heterogeneous clusters, where nodes are equipped with diverse devices.

**296 297 298 299 300 301 302 303** Intuitively, it would be beneficial to allow different workers to train at their own pace and remove the constraint of fixed-step synchronization. Therefore, we propose an asynchronous variant of the EDiT method, named A-EDiT. The differences are depicted in Figure [3.](#page-5-0) Herein, we set a fixed time interval  $\tau_{time}$ , and let each worker update locally until surpassing this specified time threshold. Then, a parameter synchronization ensues. This modification enables faster workers to undertake more iterations in each inner loop. Theoretically, no worker will wait longer than the single step time of the slowest worker at each parameter synchronization. We empirically verified that A-EDiT achieves faster training in all scenarios with comparable model performance.

- **304 305** 4 EXPERIMENTS
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**307 308** 4.1 EXPERIMENTAL SETUPS

**309 310** Models We consider four different scales of Llama models [\(Touvron et al., 2023\)](#page-11-0) in our experiments: 350M, 1B, 3B, and 7B. Their specific configurations are detailed in Table [3](#page-14-1) in Appendix.

**311 312 313** Datasets We use a new large-scale open-source dataset, FineWeb-Edu [\(Lozhkov et al., 2024\)](#page-11-11) in our experiments. Additionally, we also utilize an in-house private out of production pre-training dataset, which we will refer to as in-house dataset below.

**314 315 316 317 318** Baselines We consider several state-of-the-art methods, including standard mini-batch (Baseline), Post Local SGD [\(Lin et al., 2019\)](#page-10-5), DiLoCo [\(Douillard et al., 2023\)](#page-10-2), and CO2/CO2\* [\(Sun et al.,](#page-11-3) [2023\)](#page-11-3). Here CO2\* is the memory-efficient version of CO2 that shards extra parameters and outer momentum across workers [\(Sun et al., 2023\)](#page-11-3).

**319 320 321 322 323** Training Following DiLoCo [\(Douillard et al., 2023\)](#page-10-2), we use AdamW [\(Loshchilov & Hutter, 2019\)](#page-11-12) as the inner optimizer and Nesterov momentum [\(Nesterov, 1983\)](#page-11-4) as the outer optimizer. The models are initialized with  $\mu$ P [\(Yang et al., 2021\)](#page-12-6) for efficient hyperparameter search. Synchronization intervals  $\tau$  and  $\tau_{time}$  are set to 128 and 600s, respectively. Experiments are conducted on eight Nvidia A100 GPU nodes with 64 GPUs and an  $8 \times 8$  device mesh.  $\phi$  is 10 for pseudo gradient clip.

For more detailed setups, please refer to the Appendix [A.2.](#page-14-2)

# 4.2 CONVERGENCE AND GENERALIZATION

<span id="page-6-1"></span>![](_page_6_Figure_2.jpeg)

Figure 4: The loss and PPL curves of different methods on the (a)  $\&$  (b) FineWeb-Edu dataset and  $(c)$  & (d) in-house dataset. The final values are marked, with the best ones in bold. Here we use the average of the last 10 values as results to prevent randomness. PLS is short for Post Local SGD.

<span id="page-6-2"></span>Table 1: The evaluation results for different methods on the public benchmarks [\(Fourrier et al., 2023;](#page-10-15) [OpenCompass Contributors, 2023\)](#page-11-13), with the best results in bold and second-best underlined. PLS is short for Post Local SGD.

![](_page_6_Picture_823.jpeg)

**352 353 354 355 356** We first applied different methods to train the Llama 1B model on the FineWeb-Edu dataset and in-house dataset separately. Here we only compared the best-performing methods, *i.e.*, Baseline, DiLoCo, EDiT, and A-EDiT, on the in-house dataset. The training loss  $(\downarrow)^3$  $(\downarrow)^3$  and validation PPL  $(\downarrow)$ results are shown in Figure [4.](#page-6-1)

**357 358 359 360 361 362 363** As can be seen, our proposed EDiT and A-EDiT both achieve consistently good performance. Specifically, EDiT achieves the lowest training loss on both datasets and achieves the lowest validation PPL on the FineWeb-Edu dataset, even surpassing the Baseline. A-EDiT marginally lags behind the sync version due to the lagging workers, but it still performs better than other methods in most scenarios. Because the in-house dataset contains diverse data types and lower-quality corpora, DiLoCo [\(Douillard et al., 2023\)](#page-10-2) experienced a noticeable decline in performance. In contrast, EDiT and A-EDiT filtered out low-quality data with the pseudo gradient penalty strategy, achieving results that were nearly comparable to the Baseline.

**364 365 366 367 368 369** We evaluated the trained models on public benchmarks [\(Fourrier et al., 2023;](#page-10-15) [OpenCompass Con](#page-11-13)[tributors, 2023\)](#page-11-13). Table [1](#page-6-2) presents the evaluation results. As can be seen, the models trained with EDiT both achieve the best average performance, and A-EDiT also performs well on the eight evaluation benchmarks. These results demonstrate that both EDiT and A-EDiT exhibit strong convergence and generalization capabilities.

**370 371 372** Besides, we additionally trained the Llama 350M, 3B, and 7B models on the FineWeb-Edu dataset using EDiT, the results in Figure [8](#page-16-0) and Table [5](#page-15-0) demonstrate that EDiT performs consistently well across different model scales.

**373 374** 4.3 ACCELERATION

**375 376 377** We measured the speeds of different methods when training Llama models of four different scales on two A100 nodes. The synchronization interval was set to 5, and the results are the average

<span id="page-6-0"></span><sup>&</sup>lt;sup>3</sup>In this manuscript the  $\uparrow$  means the bigger the better and the  $\downarrow$  means the smaller the better.

![](_page_7_Picture_450.jpeg)

<span id="page-7-0"></span>Table 2: The speeds of different methods on training models of various scales. The values in the table correspond to throughput (tokens/sec) and TFLOPS, respectively.

**388 389 390 391 392 393 394 396 398** throughput (tokens/sec) and TFLOPS over 100 steps. As shown in Table [2,](#page-7-0) all Local SGD-based methods achieved higher throughput than the Baseline. It should be noted that when training the Llama 1B model with DiLoCo, extra parameters and outer momentum were placed on CPUs to prevent out of memory (OOM), resulting in non-overlapped extra GPU-CPU data transfer overhead. While CO2 achieved the highest throughput on the smallest model, holding its extra parameters and outer momentum caused significant memory overhead preventing the method to be scaled beyond 350M model. CO2\* alleviates memory pressure by sharding extra parameters and outer momentum, but introduces additional non-overlapping communication, causing a throughput drop. Our proposed methods synchronize sharded parameters layer-by-layer during the forward pass, and utilize a prefetch strategy to overlap computation with communication, achieving nearly the same throughput as CO2 (−0.5%). We also performed a profiling analysis of the synchronization operations for different methods, and detailed results can be found in Appendix [A.3.2](#page-16-1) and Figure [9.](#page-17-0)

<span id="page-7-1"></span>![](_page_7_Figure_4.jpeg)

![](_page_7_Figure_5.jpeg)

**411 412 413 414 415 416** We further evaluated the training speed of our proposed EDiT and A-EDiT methods against the Baseline method in various more challenging training scenarios. Here we manually introduced stragglers and communication delays. Specifically, we simulated stragglers by pausing the training process of one selected node at each step, and simulated inter-node bandwidth constraints by artificially repeating inter-node communications. Experiments were conducted on the Llama 7B model. Detailed experimental results are presented in Figure [5](#page-7-1) and Table [6](#page-16-2) in Appendix.

**417 418 419 420 421 422 423 424 425 426 427** The results reveal a consistent trend where A-EDiT and EDiT outperforms the Baseline method. As anticipated, the Baseline's training speed declines rapidly with increased lag time or inter-node congestion. In the random straggler scenario, EDiT and A-EDiT experience only slight speed reductions. This is attributed to the periodic synchronization that ensures relatively uniform training speeds across workers. In the consistent straggler scenario, since the cumulative delay at a single node cannot be eliminated by periodic synchronization, the performance of EDiT declines visibly. A-EDiT, leveraging its asynchronous nature, maintains a high training speed. In the bandwidthconstrained scenario, both EDiT and A-EDiT are not affected. This is due to the large synchronization interval, which minimizes inter-node communication overhead. In summary, our proposed methods consistently demonstrate superior training speed compared to the Baseline method across various scenarios, and A-EDiT further effectively addresses the issue of consistent stragglers.

**428** 4.4 SCALABILITY

**430 431** Elastic training is the ability to dynamically adjust the resources in accordance with workload fluctuations. However, varying the resources alters the global batch size and requires additional learning rate tuning. Intuitively, the optimal learning rate of the Local SGD methods may be solely related to

![](_page_7_Figure_10.jpeg)

**429**

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**397**

<span id="page-8-0"></span>![](_page_8_Figure_1.jpeg)

Figure 6: (a)  $\&$  (b) The PPL results against learning rates ( $log 2$  scale) under different number of workers for the Baseline and EDiT methods. (c) The PPL curves in the simulated training scenarios.

**445 446 447 448 449 450 451 452 453 454 455 456** the per-worker batch size, which has not been extensively studied in prior research. To validate this hypothesis, we conducted experiments on the Llama 350M model to investigate the optimal learning rate shift for the Baseline method and EDiT method under different worker numbers, fixing the batch size per worker at 128. The validation PPL results are shown in Figure [6a](#page-8-0) and Figure [6b,](#page-8-0) and the detailed training losses are shown in Figure [10](#page-18-0) in Appendix. It can be seen that as the worker number increases, the optimal learning rate for Baseline gradually increases, whereas that for EDiT consistently remains at 1.5e-4. These results validate our hypothesis. The scalability of EDiT makes it suitable for elastic training scenarios. Besides, this property enables us to economize resources by initially tuning the learning rate on a single worker before scaling up to hundreds of workers. We also note that the training loss for EDiT is more stable than that of the Baseline method across different worker numbers and learning rates, as shown in Figure [10.](#page-18-0) This not only demonstrates the robustness of EDiT but also highlights its potential to maintain consistent performance across diverse training configurations.

**457 458 459 460 461 462 463 464** We further simulated a realistic elastic training scenario. We conducted experiments on the Llama 1B model, setting the batch size per worker to 128 and fixing the learning rate at 1.5e-4. We systematically scaled the worker number upwards (1-2-4-8) and downwards (8-4-2-1), training for 25,000 steps at each worker number, and observed the validation PPL for both the Baseline and EDiT methods. As illustrated in Figure [6c,](#page-8-0) although the Baseline method initially decreases faster than EDiT, EDiT maintains a significant decline rate in the later stages and achieves the optimal PPL values in both scaling scenarios, yielding a 4.5% and 2.6% improvement, respectively. These findings affirm the EDiT's viability and advantage in real-world, elastic training scenarios.

<span id="page-8-1"></span>4.5 ABLATION STUDY

**465 466 467**

**477 478 479**

![](_page_8_Figure_6.jpeg)

Figure 7: (a) The validation PPL curves of different versions of EDiT with the final PPL values marked. (b)  $\&$  (c) The training loss curves for DiLoCo and EDiT, respectively.

**480 481 482 483 484 485** We conducted ablation studies on the pseudo gradient penalty strategy to better understand its capabilities. In this experiment, we employ the in-house dataset as it is of higher diversity and thus serves as an ideal testbed. We individually removed anomaly elimination (w/o AE), weighted averaging (w/o WA), and gradient clip (w/o GC) from EDiT, as well as all three components simultaneously (w/o ALL). The validation PPL results are shown in Figure [7a.](#page-8-1) It can be observed that without the pseudo gradient penalty strategy (w/o ALL), the PPL curve exhibits noticeable spikes and deviates considerably from the Baseline. Individually removing anomaly elimination, weighted averaging,

**486 487 488 489 490 491 492** or gradient clip each adversely affects stability and validation PPL, demonstrating that every component of the pseudo gradient penalty strategy is effective. We further investigated the training losses across eight different workers. As depicted in Figure [7b](#page-8-1) and Figure [7c,](#page-8-1) all workers in DiLoCo simultaneously encounter loss spikes and take a long time to recover. In contrast, EDiT can swiftly rectify deviations in individual workers. Even when all workers experience abnormal losses, they can promptly revert to normal loss levels through the rollback strategy. These results demonstrate the effectiveness of the pseudo gradient penalty strategy.

**493 494 495**

5 THEORETICAL ANALYSIS

In this section, we choose SGD [\(Robbins & Monro, 1951\)](#page-11-14) as the inner optimizer and the outer optimizer for simplicity. Under the framework developed in [Wang et al.](#page-12-1) [\(2019\)](#page-12-1), we have the following convergence theorem.

Theorem 1. *Suppose that the following assumptions are satisfied:*

*1.*  $\mathcal L$  *is differential and lower bounded, i.e.,*  $\mathcal L(\theta^*) > -\infty$  *where*  $\theta^*$  *is an optimal solution.*  $\mathcal L$  *is* also L-smooth, i.e.,  $\forall u,v\in\mathbb{R}^n$ , we have  $\mathcal{L}(\boldsymbol{u})\leq\mathcal{L}(\boldsymbol{v})+\langle\nabla\mathcal{L}(\boldsymbol{v}),\boldsymbol{u}-\boldsymbol{v}\rangle+\frac{L}{2}\|\boldsymbol{u}-\boldsymbol{v}\|^2.$ 

*2.* At the outer step t and inner step p,  $\forall W_i \in \mathcal{G}_m^r$ ,  $m \in 1, \cdots, M$ , the algorithm can access a *bounded noisy gradient and the true gradient is bounded, i.e.,*  $\|g^{(i)}_{t,p}\|_\infty \leq G_\infty, \|\mathbb{E}[g^{(i)}_{t,p}]\|_\infty \leq$  $G_{\infty}$ ,  $\forall t \in [T-1] := \{0, \cdots, T-1\}, \forall p \in [\tau-1] := \{0, \cdots, \tau-1\}.$ 

3. The noisy gradient is unbiased and the noise is independent, i.e.,  $\bm{g}_{t,p}^{(i)} = \mathbb{E}[\bm{g}_{t,p}^{(i)}] + \bm{\zeta}_{t,p}^{(i)}, \mathbb{E}[\bm{\zeta}_{t,p}^{(i)}] =$ **0** and  $\zeta_{t,p}^{(i)}$  is independent of  $\zeta_{t',p}^{(i)}$  $t^{(i)}_{t',p'}$  if  $t \neq t'$  or  $p \neq p'.$ 

4. The learning rate of the inner optimizer is  $\eta_{t,p} = \eta/\sqrt{t\tau + p + 1}$ , and the learning rate of the *outer optimizer is* ν*.*

*Then Algorithm [1](#page-13-0) yields*

<span id="page-9-0"></span>
$$
\min_{t \in [T-1], p \in [\tau-1]} \mathbb{E}[\|\nabla \mathcal{L}(\theta_{t,p})\|^2]
$$
\n
$$
\leq \frac{1}{2\sqrt{\tau}\eta(\sqrt{T}-1)} \left( \frac{\mathcal{L}(\theta_{0,0})}{\nu} + \frac{LnG_{\infty}^2 \tau \phi \eta^2 (1 + \ln(\tau T))}{\epsilon} + \frac{L\nu n G_{\infty}^2 \phi^2 \eta^2 (1 + \ln(\tau T))}{2\epsilon^2} \right).
$$
\n(6)

*where the meaning of n,*  $\phi$  *and*  $\epsilon$  *are listed in Table [7](#page-19-0) of Appendix [A.4.](#page-19-1)* 

The proof of Theorem [1](#page-9-0) is presented in Appendix [A.4.](#page-19-1) Therefore, the convergence (to the stationary point) rate of EDiT is  $O(\log(T)/\sqrt{T})$ .

## 6 CONCLUSION

**526 527 528 529 530 531 532 533 534 535** In this work, we investigate the challenge of training LLMs on large-scale clusters. We analyze the fundamental characteristics of large scale clusters and the limitations of the existing Local SGD-type methods. On this basis, we propose a novel Efficient Distributed Training method for LLMs called EDiT. This method effectively integrates model sharding strategies with tailored Local SGD mechanisms. We propose layer-wise synchronization to achieve overlap of computation and communication and reduce communication and memory overhead. We enhance the convergence and stability of EDiT by introducing a pseudo gradient penalty strategy. We also present an asynchronous variant of EDiT (A-EDiT) to tackle the problem of consistent stragglers in heterogeneous clusters. Extensive experimental results demonstrate the superior capabilities of our proposed methods across multiple dimensions, and the convergence analysis provides a theoretical foundation for our method.

**536 537 538 539** Several potential avenues for future research are identified. First, for the A-EDiT, the stragglers negatively impact the overall performance. Mitigating the impact of these stragglers warrants further investigation. Second, our simulation of elastic training currently entails halting and restarting the training process upon node addition or subtraction. We look forward to a truly elastic framework that can swiftly adjust training resources without disrupting the ongoing training process.

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<span id="page-11-15"></span><span id="page-11-13"></span><span id="page-11-12"></span><span id="page-11-11"></span><span id="page-11-8"></span><span id="page-11-7"></span><span id="page-11-4"></span><span id="page-11-2"></span><span id="page-11-1"></span>![](_page_11_Picture_379.jpeg)

<span id="page-11-16"></span><span id="page-11-14"></span><span id="page-11-10"></span><span id="page-11-9"></span><span id="page-11-6"></span><span id="page-11-5"></span><span id="page-11-3"></span><span id="page-11-0"></span>tion and fine-tuned chat models. *arXiv preprint arXiv:2307.09288*, 2023.

<span id="page-12-6"></span>

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### **702 703** A APPENDIX

### **704 705** A.1 METHOD

**706 707 708** Here we provide the formal descriptions of EDiT method and model synchronization with pseudo gradient penalty strategy in Algorithm [1](#page-13-0) and Algorithm [2,](#page-14-0) respectively, to help readers better understand our work.

<span id="page-13-0"></span>![](_page_13_Picture_1152.jpeg)

<span id="page-14-0"></span>![](_page_14_Picture_822.jpeg)

## <span id="page-14-2"></span>A.2 EXPERIMENTAL SETUPS

**782 783 784** Here we provide a more detailed description of the experimental setups to facilitate readers in reproducing the experimental results of this paper.

**785 786 787 788** Models We consider four different scales of Llama models [\(Touvron et al., 2023\)](#page-11-0) in our experiments: 350M, 1B, 3B, and 7B. Their specific configurations are detailed in Table [3.](#page-14-1) We configure the models to have the same number of layers and head dimensions, which facilitates the utilization of  $\mu$ P [\(Yang et al., 2021\)](#page-12-6) for hyperparameter search.

Table 3: Configurations for the four scales of Llama models.

<span id="page-14-1"></span>![](_page_14_Picture_823.jpeg)

**799 800**

**779 780 781**

**801 802 803 804 805** Datasets Departing from small language datasets used in prior works [\(Douillard et al., 2023\)](#page-10-2), we employ a new large-scale open-source dataset, FineWeb-Edu [\(Lozhkov et al., 2024\)](#page-11-11) in our experiments. This dataset comprises 1.3T tokens of premium educational web pages filtered from the extensive FineWeb repository [\(Penedo et al., 2024\)](#page-11-15). Additionally, we also utilize an in-house private pre-training dataset, which consists of a diverse collection of corpus of varying quality.

**806 807 808 809** Baselines We compare the proposed EDiT and A-EDiT method against several state-of-theart methods, including standard mini-batch (Baseline), Post Local SGD [\(Lin et al., 2019\)](#page-10-5), DiLoCo [\(Douillard et al., 2023\)](#page-10-2), and CO2/CO2<sup>\*</sup> [\(Sun et al., 2023\)](#page-11-3). Here CO2<sup>\*</sup> is the memoryefficient version of CO2 that shards extra parameters and outer momentum across workers [\(Sun](#page-11-3) [et al., 2023\)](#page-11-3). Since Parallel SGD [\(Zhang et al., 2016\)](#page-12-0) and SlowMo [\(Wang et al., 2019\)](#page-12-1) are equiva**810 811 812** lent to Post Local SGD [\(Lin et al., 2019\)](#page-10-5) and DiLoCo [\(Douillard et al., 2023\)](#page-10-2), respectively, we do not include them in comparisons.

**813 814 815 816 817 818 819 820 821 822 823 824 825 826 Training** Follow DiLoCo [\(Douillard et al., 2023\)](#page-10-2), we use AdamW [\(Loshchilov & Hutter, 2019\)](#page-11-12) as the inner optimizer and Nesterov momentum [\(Sutskever et al., 2013\)](#page-11-16) as the outer optimizer. The models are initialized with  $\mu$ P [\(Yang et al., 2021\)](#page-12-6), enabling the hyperparameters transfer from the smallest scale model (350M) to models of larger magnitude. To balance efficiency and performance, the synchronization interval  $\tau$  and  $\tau_{time}$  are set to 128 and 600s, respectively. Across all experiments, a context length of 4,096 tokens and a cosine learning rate decay schedule are consistently applied. For the FineWeb-Edu dataset [\(Lozhkov et al., 2024\)](#page-11-11), the total batch size is set to 1,024 and the training step is set to 100,000 (∼420B tokens). The learning rate for Baseline, inner learning rate, outer learning rate, and outer momentum are set to 3e-4, 1.5e-4, 0.8, and 0.85, respectively. For the in-house dataset, the total batch size is set to 1,536 and the training step is set to 150,000 (∼950B tokens). The learning rate for Baseline, inner learning rate, outer learning rate, and outer momentum are set to 6e-4, 6e-4, 1.0, and 0.8, respectively. We list the searched hyperparameters in detail in Table [4.](#page-15-1) The experimental infrastructure comprised eight Nvidia A100 GPU nodes with 64 GPUs and an  $8 \times 8$  device mesh. For the hyperparameters in the pseudo gradient penalty strategy, we set  $\phi = 10$ .

<span id="page-15-1"></span>Table 4: The hyperparameters searched in the experiments.

![](_page_15_Picture_464.jpeg)

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**838 839**

# A.3 ADDITIONAL EXPERIMENTAL RESULTS

A.3.1 CONVERGENCE AND GENERALIZATION

**840 841 842 843 844 845 846 847 848 849** In the main text, we present the performance of EDiT and other Local SGD methods in training the Llama 1B model in Figure [4](#page-6-1) and Table [1.](#page-6-2) To demonstrate that EDiT performs consistently well across different model scales, we additionally trained Llama 350M, 3B, and 7B models using EDiT on the FineWeb-Edu dataset, each with a total of 420B tokens. The corresponding training loss, validation PPL, and evaluation results are shown in Figure [8](#page-16-0) and Table [5.](#page-15-0) It can be observed that EDiT is robust across various model scales. Besides, to our knowledge, this is the first time to train a 7B model on a large-scale dataset with a Local SGD-related method. Although CO2 [\(Sun et al.,](#page-11-3) [2023\)](#page-11-3) also claimed that they trained a 7B model, they only used about 50B tokens and provided only the final validation PPL results. The models trained with EDiT will be open-sourced upon the acceptance of this paper.

<span id="page-15-0"></span>Table 5: The evaluation results on the public benchmarks [\(Fourrier et al., 2023;](#page-10-15) [OpenCompass](#page-11-13) [Contributors, 2023\)](#page-11-13) for the 350M, 1B, 3B, and 7B models trained with the EDiT method.

![](_page_15_Picture_465.jpeg)

<span id="page-16-0"></span>![](_page_16_Figure_1.jpeg)

Figure 8: The training loss and validation PPL curves for the 350M, 1B, 3B, and 7B models trained with the EDiT method on the FineWeb-Edu dataset. The final loss and PPL values are marked in the figures, which are the average values of the last 10 values to prevent randomness.

#### <span id="page-16-1"></span>**881** A.3.2 ACCELERATION

**882**

**883 884 885 886 887 888 889 890 891 892 893 894 895** In the main text, we analyzed the throughput and TFLOPS of different acceleration methods. Here, we further profile the synchronization operations of different methods when training the Llama 1B model. As shown in Figure [9,](#page-17-0) Post Local SGD introduces a significant additional communication overhead of 160ms during model synchronization. Although CO2\* successfully overlaps model synchronization communication with the forward computation of the next step, it incurs two segments of non-overlapping communication overhead to deal with the sharded extra parameters and outer momentum, causing a delay of approximately 300ms. This delay negates the acceleration benefits gained from overlapped parameter synchronization. However, without the memory-efficient mode, the complete copies of model parameters and outer momentum in CO2 lead to severe memory usage, resulting in OOM in this scenario. In contrast, EDiT synchronizes sharded parameters layer-by-layer during the forward pass, reducing communication volume and overlapping computation with communication through a prefetch strategy. It achieves the same performance as CO2 without introducing additional communication burdens or memory overhead. As a result, EDiT only introduces 19ms delay in this scenario.

<span id="page-16-2"></span>Besides, we provide the detailed TFLOPS corresponding to the Figure [5](#page-7-1) in Table [6.](#page-16-2)

Table 6: The TFLOPS of different methods under different training scenarios.

![](_page_16_Picture_421.jpeg)

A.3.3 SCALABILITY

Here we provide the detailed training loss curves of the Baseline and EDiT methods under different numbers of workers and distinct learning rates, which correspond to the Figure [6](#page-8-0) in the main text.

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<span id="page-17-0"></span>![](_page_17_Figure_1.jpeg)

Figure 9: The profiling results of Baseline, Post Local SGD, CO2, and EDiT during synchronization while training the Llama 1B model. The parts corresponding to model synchronization and computation are highlighted with red boxes.

<span id="page-18-0"></span>![](_page_18_Figure_1.jpeg)

**1024 1025** Figure 10: The training loss curves of the Baseline and EDiT methods under different numbers of workers and distinct learning rates.

#### <span id="page-19-1"></span>**1026 1027** A.4 PROOF OF THEOREM [1](#page-9-0)

<span id="page-19-0"></span>**1028**

![](_page_19_Picture_944.jpeg)

Table 7: The hyperparameters of Theorem [1.](#page-9-0)

*Proof.* Since the inner and outer optimizer are both SGD, 
$$
\forall W_i \in \mathcal{G}_m^r, m \in \{1, \dots, M\}
$$
, we have

<span id="page-19-4"></span><span id="page-19-3"></span>
$$
\boldsymbol{\theta}_{t,0}^{(i)} = \boldsymbol{\theta}_t^{(i)},\tag{7}
$$

$$
\boldsymbol{\theta}_{t,p+1}^{(i)} = \boldsymbol{\theta}_{t,p}^{(i)} - \eta_{t,p} \boldsymbol{g}_{t,p}^{(i)},
$$
\n(8)

<span id="page-19-2"></span>
$$
\boldsymbol{\theta}_{t+1} = \boldsymbol{\theta}_t - \nu \widehat{\boldsymbol{\Delta}}_t,\tag{9}
$$

where  $\eta_{t,p}$  and  $\nu$  are the inner optimizer learning rate and the outer optimizer learning rate, respectively. Here, we omit the superscripts of variables in Equation [9,](#page-19-2) as they remain identical across all workers in  $\mathcal{G}_m^r$ . The following proof will also adopt this simplified notation without risk of confusion. Hence, by the Equations [2,](#page-4-1) [3,](#page-4-3) [4,](#page-4-4) [5,](#page-4-2) [7](#page-19-3) and [8,](#page-19-4) we have

<span id="page-19-5"></span>
$$
\widehat{\mathbf{\Delta}}_t = \beta_t \overline{\mathbf{\Delta}}_t = \beta_t \sum_j w_{t,j} \mathbf{\Delta}_t^{(j)} = \beta_t \sum_j w_{t,j} (\theta_{t,\tau}^{(j)} - \theta_{t,0}^{(j)}) \n= \beta_t \sum_j w_{t,j} (\eta_{t,p} \mathbf{g}_{t,\tau-1}^{(j)} + \theta_{t-1,\tau}^{(j)} - \theta_{t,0}^{(j)}) = \beta_t \sum_j w_{t,j} \sum_{p=0}^{\tau-1} \eta_{t,p} \mathbf{g}_{t,p}^{(j)}.
$$
\n(10)

**1059 1060** Let

**1061**

**1064**

**1067 1068 1069**

<span id="page-19-6"></span>
$$
\boldsymbol{h}_{t,p} = \beta_t \sum_j w_{t,j} \boldsymbol{g}_{t,p}^{(j)},
$$
\n(11)

**1062 1063** then

<span id="page-19-7"></span>
$$
\mathbb{E}[\boldsymbol{h}_{t,p}] = \mathbb{E}[\beta_t \sum_j w_{t,j} \boldsymbol{g}_{t,p}^{(j)}] = \beta_t \mathbb{E}[\boldsymbol{g}_{t,p}].
$$
\n(12)

**1065 1066** Combining Equation [7,](#page-19-3) Equation [10](#page-19-5) and Equation [11](#page-19-6) into Equation [9,](#page-19-2) we have

$$
\theta_{t+1,0} - \theta_{t,0} = -\nu \sum_{p=0}^{\tau-1} \eta_{t,p} h_{t,p}.
$$
\n(13)

**1070 1071** For proving the convergence of  $\{\theta_{t,p}^{(i)}\}$ , we need to define the auxiliary sequence  $\{\psi_{t,p}\}$ . Denote

1072  
\n1073  
\n1074  
\n
$$
\begin{cases}\n\psi_{0,0} = \mathbf{\theta}_{0,0}, \\
\psi_{t+1,0} = \psi_{t,0} - \nu \sum_{p=0}^{\tau-1} \eta_{t,p} \mathbf{h}_{t,p}, \\
\psi_{t,p+1} = \psi_{t,p} - \nu \eta_{t,p} \mathbf{h}_{t,p}.\n\end{cases}
$$

**1075 1076** It is easy to prove  $\psi_{t+1,0} = \psi_{t,\tau}$ . Then we have

<span id="page-19-8"></span>1077  
1078 
$$
\mathbb{E}[\psi_{t,p}] - \mathbb{E}[\theta_{t,p}] = \mathbb{E}[\psi_{t,0} - \nu \sum_{k=0}^{p-1} \eta_{t,k} \mathbf{h}_{t,k}] - \mathbb{E}[\theta_{t,0} - \sum_{k=0}^{p-1} \eta_{t,k} g_{t,k}] = (1 - \nu \beta_t) \sum_{k=0}^{p-1} \eta_{t,k} \mathbb{E}[g_{t,k}]
$$
(14)

**1080 1081** By assumption 1, we have

**1082 1083**

 $\mathcal{L}(\psi_{t,p+1}) \leq \mathcal{L}(\psi_{t,p}) + \langle \nabla \mathcal{L}(\psi_{t,p}), \psi_{t,p+1} - \psi_{t,p} \rangle + \frac{L}{2}.$  $\frac{L}{2}\|\psi_{t,p+1}-\psi_{t,p}\|^2$  $= \mathcal{L}(\bm{\psi}_{t,p}) - \nu \eta_{t,p} \left\langle \nabla \mathcal{L}(\bm{\psi}_{t,p}), \bm{h}_{t,p} \right\rangle +$  $L\nu^2\eta_{t,p}^2$  $\frac{\eta_{t,p}}{2}\|\boldsymbol{h}_{t,p}\|^2$  $={\cal L}(\bm{\psi}_{t,p}) - \nu \eta_{t,p} \,\Big\langle$  $\nabla \mathcal{L}(\boldsymbol{\psi}_{t,p}) - \nabla \mathcal{L}(\boldsymbol{\theta})$  $t_{t,p}^{(i)}), \boldsymbol{h}_{t,p}\Big\rangle$  $-\nu \eta_{t,p} \left\langle \nabla \mathcal{L}(\pmb{\theta}_{t,p}^{(i)}), \pmb{h}_{t,p} \right\rangle$  $\nabla \mathcal{L}(\bm{\theta}$ +

<span id="page-20-0"></span>
$$
= \mathcal{L}(\psi_{t,p}) - \nu \eta_{t,p} \left\langle \nabla \mathcal{L}(\psi_{t,p}) - \nabla \mathcal{L}(\boldsymbol{\theta}_{t,p}^{(i)}), \boldsymbol{h}_{t,p} \right\rangle - \nu \eta_{t,p} \left\langle \nabla \mathcal{L}(\boldsymbol{\theta}_{t,p}^{(i)}), \boldsymbol{h}_{t,p} \right\rangle + \frac{L\nu^2 \eta_{t,p}^2}{2} \|\boldsymbol{h}_{t,p}\|^2
$$
  

$$
\leq \mathcal{L}(\psi_{t,p}) + \nu \eta_{t,p} L \|\psi_{t,p} - \boldsymbol{\theta}_{t,p}^{(i)}\| \|\boldsymbol{h}_{t,p}\| - \nu \eta_{t,p} \left\langle \nabla \mathcal{L}(\boldsymbol{\theta}_{t,p}^{(i)}), \boldsymbol{h}_{t,p} \right\rangle + \frac{L\nu^2 \eta_{t,p}^2}{2} \|\boldsymbol{h}_{t,p}\|^2.
$$
 (15)

**1091 1092** Rearranging Equation [15](#page-20-0) and taking expectation both sides, by assumption 2, assumption 3, Equation [12](#page-19-7) and Equation [14,](#page-19-8) we get

<span id="page-20-1"></span>1093 
$$
\nu \eta_{t,p} \beta_t \mathbb{E}[\|\nabla \mathcal{L}(\boldsymbol{\theta}_{t,p})\|^2]
$$
  
\n1094  $\leq \mathbb{E}[\mathcal{L}(\boldsymbol{\psi}_{t,p}) - \mathcal{L}(\boldsymbol{\psi}_{t,p+1})] + \nu \eta_{t,p} L \mathbb{E}[\|\boldsymbol{\psi}_{t,p} - \boldsymbol{\theta}_{t,p}\|\|\boldsymbol{h}_{t,p}\|] + \frac{L\nu^2 \eta_{t,p}^2}{2} \mathbb{E}[\|\boldsymbol{h}_{t,p}\|^2]$   
\n1096  $\leq \mathbb{E}[\mathcal{L}(\boldsymbol{\psi}_{t,p}) - \mathcal{L}(\boldsymbol{\psi}_{t,p+1})] + \nu \eta_{t,p} L \beta_t \sqrt{n} G_{\infty} \mathbb{E}[\|\boldsymbol{\psi}_{t,p} - \boldsymbol{\theta}_{t,p}\|] + \frac{L\nu^2 \eta_{t,p}^2 \beta_t^2 n G_{\infty}^2}{2}$   
\n1099  $= \mathbb{E}[\mathcal{L}(\boldsymbol{\psi}_{t,p}) - \mathcal{L}(\boldsymbol{\psi}_{t,p+1})] + \nu \eta_{t,p} L \beta_t \sqrt{n} G_{\infty} (1 - \nu \beta_t) \sum_{k=0}^{p-1} \eta_{t,k} \mathbb{E}[\|\boldsymbol{g}_{t,k}\|] + \frac{L\nu^2 \eta_{t,p}^2 \beta_t^2 n G_{\infty}^2}{2}$   
\n1101  $\leq \mathbb{E}[\mathcal{L}(\boldsymbol{\psi}_{t,p}) - \mathcal{L}(\boldsymbol{\psi}_{t,p+1})] + \nu \eta_{t,0}^2 L \beta_t n G_{\infty}^2 \tau + \frac{L\nu^2 \eta_{t,p}^2 \beta_t^2 n G_{\infty}^2}{2}$   
\n1104  $\leq \mathbb{E}[\mathcal{L}(\boldsymbol{\psi}_{t,p}) - \mathcal{L}(\boldsymbol{\psi}_{t,p+1})] + \nu \eta_{t,0}^2 L \beta_t n G_{\infty}^2 \tau + \frac{L\nu^2 \eta_{t,p}^2 \beta_t^2 n G_{\infty}^2}{2}$   
\n1104 **Telescoping Equation 16 for**  $p = 0$  **to**  $\tau - 1$  **and**

Telescoping Equation [16](#page-20-1) for  $p = 0$  to  $\tau - 1$  and  $t = 0$  to  $T - 1$ , we have

$$
\sum_{t=0}^{T-1} \sum_{p=0}^{\tau-1} \nu \eta_{t,p} \beta_t \mathbb{E}[\|\nabla \mathcal{L}(\boldsymbol{\theta}_{t,p})\|^2]
$$
\n
$$
\leq \mathbb{E}[\mathcal{L}(\psi_{0,0}) - \mathcal{L}(\psi_{T-1,\tau})] + \nu LnG_{\infty}^2 \tau^2 \sum_{t=0}^{T-1} \beta_t \eta_{t,0}^2 + \frac{L\nu^2 n G_{\infty}^2}{2} \sum_{t=0}^{T-1} \sum_{p=0}^{\tau-1} \beta_t^2 \eta_{t,p}^2 \qquad (17)
$$
\n
$$
\leq \mathcal{L}(\boldsymbol{\theta}_{0,0}) + \nu LnG_{\infty}^2 \tau^2 \sum_{t=0}^{T-1} \beta_t \eta_{t,0}^2 + \frac{L\nu^2 n G_{\infty}^2}{2} \sum_{t=0}^{T-1} \sum_{t=0}^{\tau-1} \beta_t^2 \eta_{t,n}^2.
$$

<span id="page-20-2"></span>
$$
\leq \mathcal{L}(\boldsymbol{\theta}_{0,0}) + \nu LnG_{\infty}^{2} \tau^{2} \sum_{t=0}^{T-1} \beta_{t} \eta_{t,0}^{2} + \frac{L\nu^{2} n G_{\infty}^{2}}{2} \sum_{t=0}^{T-1} \sum_{p=0}^{T-1} \beta_{t}^{2} \eta_{t,p}^{2}.
$$

 $\sum^{T-1}$  $t=0$ 

**1115 1116** Since from Equation [4,](#page-4-4) we have  $1 \leq \beta_t \leq \frac{\phi}{\epsilon}$ . Combining with Equation [17,](#page-20-2) we can get

$$
\sum_{t=0}^{T-1} \sum_{p=0}^{\tau-1} \eta_{t,p} \mathbb{E}[\|\nabla \mathcal{L}(\boldsymbol{\theta}_{t,p})\|^2] \le \frac{\mathcal{L}(\boldsymbol{\theta}_{0,0})}{\nu} + \frac{Ln G_{\infty}^2 \tau^2 \phi}{\epsilon} \sum_{t=0}^{T-1} \eta_{t,0}^2 + \frac{L \nu n G_{\infty}^2 \phi^2}{2\epsilon^2} \sum_{t=0}^{T-1} \sum_{p=0}^{\tau-1} \eta_{t,p}^2. \tag{18}
$$

1

 $\frac{1}{\sqrt{s}}ds$ 

 $\frac{1}{\sqrt{t+1}}$ 

**1119 1120** Since

> $\sum^{T-1}$  $t=0$

 $\sum^{T-1}$  $p=0$ 

 $\eta_{t,p} \geq \tau$ 

 $\sum^{T-1}$  $t=0$ 

$$
\begin{array}{c} 1121 \\ 1122 \\ 1123 \\ 1124 \end{array}
$$

**1117 1118**

$$
\begin{array}{c}\n 1124 \\
 1125 \\
 1126\n \end{array}
$$

<span id="page-20-3"></span>
$$
= \sqrt{\tau} \eta \left( \int_1^2 \frac{1}{\sqrt{1}} ds + \dots + \int_T^{T+1} \frac{1}{\sqrt{T}} ds \right) \ge \sqrt{\tau} \eta \int_1^{T+1}
$$
  
=  $2\sqrt{\tau} \eta (\sqrt{T+1} - 1) \ge 2\sqrt{\tau} \eta (\sqrt{T} - 1),$ 

 $\eta_{t,\tau-1} = \sqrt{\tau} \eta$ 

**1127 1128 1129 1130 1131 1132 1133** T X−1 t=0 τX−1 p=0 η 2 t,p ≤ τ T X−1 t=0 η 2 t,<sup>0</sup> = η 2 T X−1 t=0 1 t + 1 τ = η 2 1 + <sup>Z</sup> <sup>1</sup> 0 1 1 + <sup>1</sup> τ ds + · · · + Z <sup>T</sup> <sup>−</sup><sup>1</sup> T −2 1 T − 1 + <sup>1</sup> τ ds! ≤ η 2 1 + <sup>Z</sup> <sup>T</sup> <sup>−</sup><sup>1</sup> 0 1 s + 1 τ ds! = η 2 (1 + ln(τT − τ + 1)) ≤ η 2 (1 + ln(τT)), (19)

 substituting Equation [19](#page-20-3) into Equation [17,](#page-20-2) we have  $\min_{t\in[T-1],p\in[\tau-1]}\mathbb{E}[\|\nabla \mathcal{L}(\boldsymbol{\theta}_{t,p})\|^2]$  $\leq \frac{1}{\sqrt{T-1}}$  $\frac{1}{\sum_{t=0}^{T-1}\sum_{p=0}^{\tau-1}\eta_{t,p}}\Bigg(\frac{\mathcal{L}(\bm{\theta}_{0,0})}{\nu}$  $\frac{\partial \theta_{0,0}}{\nu} + \frac{Ln G_{\infty}^2 \tau^2 \phi}{\epsilon}$  $\epsilon$  $\sum^{T-1}$  $t=0$  $\eta_{t,0}^2 +$  $L\nu n G_{\infty}^2 \phi^2$  $2\epsilon^2$  $\sum^{T-1}$  $t=0$  $\sum^{T-1}$  $p=0$  $\eta_{t,p}^2\bigg)$  $\leq \frac{1}{\sqrt{1-\frac{1}{2}}}$  $\frac{1}{2\sqrt{\tau}\eta(1-\tau)}$  $\frac{1}{\sqrt{T}-1)}\left(\frac{\mathcal{L}(\bm{\theta}_{0,0})}{\nu}\right)$  $\frac{\partial \Theta_{0,0}}{\partial \nu} + \frac{LnG_{\infty}^2 \tau \phi \eta^2 (1 + \ln(\tau T))}{\epsilon}$  $\frac{(1 + \ln(\tau T))}{\epsilon} + \frac{L\nu n G_{\infty}^2 \phi^2 \eta^2 (1 + \ln(\tau T))}{2\epsilon^2}$  $2\epsilon^2$  $\big).$  $\begin{matrix} (20) \\ \Box \end{matrix}$ This completes the proof.