## Inverse Reinforcement Learning with Switching Rewards and History Dependency for Characterizing Animal Behaviors

Jingyang Ke<sup>1</sup> Feiyang Wu<sup>1</sup> Jiyi Wang<sup>1</sup> Jeffrey E. Markowitz<sup>12</sup> Anqi Wu<sup>1</sup>

### Abstract

Traditional approaches to studying decisionmaking in neuroscience focus on simplified behavioral tasks where animals perform repetitive, stereotyped actions to receive explicit rewards. While informative, these methods constrain our understanding of decision-making to short timescale behaviors driven by explicit goals. In natural environments, animals exhibit more complex, long-term behaviors driven by intrinsic motivations that are often unobservable. Recent works in time-varying inverse reinforcement learning (IRL) aim to capture shifting motivations in long-term, freely moving behaviors. However, a crucial challenge remains: animals make decisions based on their history, not just their current state. To address this, we introduce SWIRL (SWitching IRL), a novel framework that extends traditional IRL by incorporating time-varying, history-dependent reward functions. SWIRL models long behavioral sequences as transitions between short-term decision-making processes, each governed by a unique reward function. SWIRL incorporates biologically plausible history dependency to capture how past decisions and environmental contexts shape behavior, offering a more accurate description of animal decision-making. We apply SWIRL to simulated and real-world animal behavior datasets and show that it outperforms models lacking history dependency, both quantitatively and qualitatively. This work presents the first IRL model to incorporate history-dependent policies and rewards to advance our understanding of complex, naturalistic decision-making in animals.

## 1. Introduction

Historically, decision making in neuroscience has been studied using simplified assays where animals perform repetitive, stereotyped actions (such as licks, nose pokes, or lever presses) in response to sensory stimuli to obtain an explicit reward. While this approach has its advantages, it has limited our understanding of decision making to scenarios where animals are instructed to achieve an explicit goal over brief timescales, usually no more than tens of seconds. In contrast, in natural environments, animals exhibit much more complex behaviors that are not confined to structured, stereotyped trials. For example, a freely moving mouse may immediately rush toward the scent of food when hungry, but after eating, it might seek out a quiet spot to rest for an extended period. Thus, real-world animal behaviors form long sequences composed of multiple decision-making processes. Each decision-making process involves a series of states and actions aimed at achieving a goal, and such decision switching is unlikely to occur on very short timescales in simplified assays. Additionally, many of the goals animals pursue in natural settings are generated by intrinsic motivations and thus unobservable. To truly understand animal's decision-making in a naturalistic context, we need methods to uncover animals' intrinsic motivations during multiple decision-making processes.

Inverse reinforcement learning (IRL), which infers agents' policies and intrinsic reward functions based on their interactions with the environment (Ng & Russell, 2000; Abbeel & Ng, 2004; Ziebart et al., 2008; 2010; Wu et al., 2024), has been shown to be effective in capturing animal decisionmaking intentions by learning reward functions from behavioral trajectories (Sezener et al., 2014; Yamaguchi et al., 2018; Pinsler et al., 2018; Hirakawa et al., 2018). However, traditional IRL assumes a single static reward function over time, limiting its ability to account for shifts in intrinsic motivations. To address this limitation, recent IRL variants have aimed to uncover heterogeneous and time-varying reward functions (Babes-Vroman et al., 2011; Surana & Srivastava, 2014; Nguyen et al., 2015; Ashwood et al., 2022a; Zhu et al., 2024). Despite these advancements, a significant challenge remains unaddressed: animals make decisions based on their history, not just their current state (Kennedy, 2022; Hattori

<sup>&</sup>lt;sup>1</sup>Georgia Institute of Technology, Atlanta, GA, USA <sup>2</sup>Emory University, Atlanta, GA, USA. Correspondence to: Anqi Wu <anqiwu@gatech.edu>.

Proceedings of the  $42^{nd}$  International Conference on Machine Learning, Vancouver, Canada. PMLR 267, 2025. Copyright 2025 by the author(s).

et al., 2019). For example, in perceptual decision-making tasks, mice are found to make new decision based on reward, state and decision history (Ashwood et al., 2022b). Incorporating historical context into the modeling could offer a more accurate representation of animal behavior.

To address the absence of history dependency in timevarying IRL models, we introduce a novel framework called SWitching IRL (SWIRL). Similar to Zhu et al. (2024), SWIRL models long recordings of animal behaviors as a sequence of short-term decision-making processes. Each decision-making process is treated as a Markov decision process (MDP) with a unique reward function that can be inferred using IRL. The segmentation of a long recording into switching decision-making processes is unknown; therefore, each process is regarded as being associated with a hidden mode that must also be inferred. Most importantly, SWIRL incorporates biologically plausible history dependency, drawing on insights from animal behavior. The history dependency is added at two levels: the transitions between decision-making processes (decision-level) and the actions taken to achieve a single goal within a decision-making Decision-level dependency is process (action-level). reflected in the transitions between decision-making processes over extended sequences of time bins, suggesting that an animal's current choice is shaped by its previous decisions and environmental feedback. Additionally, we posit that these transitions are influenced by the animal's location. For example, after a mouse drinks from a water port, if it stays nearby, it is more likely to seek another goal. Conversely, if it is far from the port, indicating it has been away for some time, it may become thirsty again and return to search for water. For action-level history dependency, we will model the policy and reward functions as dependent on trajectory history within each decision-making process, using a non-Markovian decision framework. Such a dependency has been studied by existing reinforcement learning research, which often characterizes exploration with reward functions based on historical states and actions (Houthooft et al., 2016; Sharafeldin et al., 2024). Importantly, SWIRL is the first to incorporate history-dependent policies and rewards into IRL.

One key aspect we want to highlight in this paper is that the proposed SWIRL model has intriguing connections to traditional behavioral analysis methods in the animal neuroscience literature. In Sec. 3.5, we will demonstrate that our SWIRL model offers a more generalized and principled approach to characterize animal behaviors compared to existing autoregressive dynamics models (Wiltschko et al., 2015; Mazzucato, 2022; Stone, 2023; Weinreb et al., 2024).

In the Results section, we will apply our SWIRL to a simulated dataset as well as two real-world animal behavior datasets. For both animal datasets, we will demonstrate that SWIRL outperforms alternative models when history dependency is not included, both quantitatively and qualitatively. This underscores the necessity of incorporating this biologically plausible element when modeling long-term behaviors. Additionally, for the first time, we will present the application of non-Markovian reward functions and stateaction reward functions to model freely-moving animals, contrasting with previous works that only assume a single state-based reward.

## 2. Related Work

IRL for animal behavior understanding. IRL has been widely used to infer animals' behavioral strategies and decision-making policies when the reward is unknown. For instance, Pinsler et al. (2018) applies IRL to uncover the unknown reward functions of pigeons, explains and reproduces their flock behavior, and introduces a method to learn a leader-follower hierarchy. Similarly, Hirakawa et al. (2018) uses IRL to learn reward functions from animal trajectories, identifies environmental features preferred by shearwaters, and demonstrates differences in male and female migration route preferences based on the estimated rewards. In another study, Yamaguchi et al. (2018) applies IRL to C. elegans thermotactic behavior, revealing distinct behavioral strategies for fed and unfed worms. Additionally, Sezener et al. (2014) maps reward functions for rats freely moving in a square area, showing how these rewards changed before and after training. While these studies demonstrate the utility of IRL in uncovering behavioral strategies of freely moving animals, they share a key limitation: they all assume a single reward function governs all animal behaviors, which does not account for the complexities of long-term decision-making.

Heterogeneous and time-varying IRL. Recent works have extended traditional IRL, which assumes a constant reward, to models with time-varying or multiple reward functions driving behavioral trajectories. For example, Babes-Vroman et al. (2011) introduced Multi-intention IRL, which infers multiple reward functions across different trajectories but still assumes a single reward function within each trajectory. On the other hand, the Dynamic IRL (DIRL) method (Ashwood et al., 2022a) models reward functions as a linear combination of feature maps with time-varying weights, addressing the issue of varying rewards within a trajectory. However, DIRL requires trajectories to be highly similar or clustered beforehand, significantly limiting its applicability. Moreover, it cannot capture switching decision-making processes over long-term periods where each process may vary in length. Additionally, BNP-IRL (Surana & Srivastava, 2014), locally consistent IRL (Nguyen et al., 2015) and multi-intention inverse Q-learning (IQL) (Zhu et al., 2024) all extended the multi-intention IRL framework to allow for changing reward functions within trajectories, making

them the closest models to our proposed SWIRL. However, all models do not account for both decision-level and action-level history dependency, an important biologically plausible factor that SWIRL incorporates to achieve more accurate behavior modeling. In our experiments, we will use multi-intention IQL and locally consistent IRL as baseline models, as they are special cases of SWIRL.

Dynamics-based behavior analysis in animal neuroscience. Traditional approaches to analyzing animal behavior in neuroscience often rely on autoregressive dynamics models. For instance, MoSeq and related works (Wiltschko et al., 2015; Weinreb et al., 2024) assume that animal behavior consists of multiple segments modeled by a hidden markov model (HMM), with each segment evolving through an autoregressive process. Stone (2023) introduces a switching linear dynamical system (SLDS), similar to an ARHMM, but with an additional layer of continuous latent states between the behavioral trajectories and the hidden states representing behavioral segments. We argue that if each segment lasts only a few seconds, it represents meaningful action motifs, such as grooming and sniffing. However, if a segment is significantly longer and reflects a decision-making process, traditional dynamics-based models may not be suitable for identifying these long-term segments. However, these dynamics-based models are not entirely independent of SWIRL. We will demonstrate that SWIRL generalizes purely dynamics-based models by relying on a more principled IRL framework to identify multiple decision-making processes. Our goal is to offer insights that bridge these traditional and new models for animal behavioral analysis.

#### 3. Methods

#### 3.1. Hidden-Mode Markov Decision Process

A discounted Hidden-Mode Markov Decision Process (HM-MDP) is defined by the tuple  $\mathcal{M} = (\mathcal{Z}, \mathcal{S}, \mathcal{A}, \mathcal{P}, \mathcal{P}_z, r, \gamma)$ . Here,  $\mathcal{Z}$  represents a finite set of hidden modes z,  $\mathcal{S}$  denotes the finite state space, and  $\mathcal{A}$  indicates the finite action space.  $r_z$  represents the reward function r under hidden mode z. The discount factor  $\gamma$  is constrained to the interval [0,1]. Starting from an initial state  $s_0$ , the agent (animal) selects an action a based on its policy (behavioral strategy)  $\pi$  and subsequently receives a reward determined by  $r_z$ ,  $z \in \mathcal{Z} := \{z_1, z_2, \ldots, z_m\}$ , where m represents the total number of modes. The agent then transitions to the next state s' according to the transition kernel  $\mathcal{P}(s'|s, a)$ , while the agent's hidden mode also transitions to z' based on the transition probability  $\mathcal{P}_z(z'|z)$ .

#### 3.2. Inverse Reinforcement Learning

Inverse Reinforcement Learning (IRL) addresses the scenario where we have gathered multiple trajectories



*Figure 1.* **SWIRL graphical model.** Green dotted lines represent transitions of the hidden modes depend on the previous state (decision-level dependency). Blue dotted lines represent that polices depend on past states (action-level dependency).

from an expert agent  $\pi^*$ , comprising a set of state-action pairs  $\{(s_t^*, a_t^*)\}$ . The goal is to estimate the policy and reward that generated these state-action pairs, often referred to as expert demonstrations in IRL literature. We assume that we have collected N expert trajectories, denoted as  $\mathcal{D} = \{\xi_1, \xi_2, \ldots, \xi_N\}$ . Each trajectory consists of a sequence of state-action pairs, represented as  $\xi_n = \{(s_1^*, a_1^*), (s_2^*, a_2^*), \ldots\}$ , with  $T_n$  time steps, which may vary across trajectories.

#### 3.3. Switching Inverse Reinforcement learning

Our SWIRL model is built on the HM-MDP. Instead of explicitly knowing the reward for each mode, we will use IRL to infer these rewards. Mathematically, at each time step t, we represent the agent's internal reward function  $r_{z_t}$ with an additional dependency on the hidden mode  $z_t$ . This means that the agent receives a reward  $r_{z_t}$  based on its current hidden mode  $z_t$ , which indicates the decision-making state the animal is in (e.g., water seeking or home seeking), with  $r_{z_t}$  representing the corresponding intrinsic motivation. Consequently, the optimal policy  $\pi_t$  is determined by  $r_{z_t}$ . However, SWIRL goes beyond merely embedding IRL within HM-MDP: We also introduce two levels of history dependency into the model. The full graphical model is depicted in Fig. 1.

The decision-level dependency is characterized by the idea that animals make new decisions based on their previous choices. The transitions between decision-making processes already account for this decision-level dependency since  $\mathcal{P}_z(z_{t+1}|z_t)$ . However, the hidden modes with such a classical transition are generated through an open-loop process: the mode  $z_{t+1}$  depends solely on the preceding mode  $z_t$ , with  $z_{t+1}|z_t$  being independent of the observation state  $s_t$ . Consequently, if a discrete switch should occur when the animal enters a specific region of the state space, the classical transition will fail to capture this dependency. To address this, we extend the transition model to include the state  $s_t$  as a condition, resulting in  $\mathcal{P}_z(z_{t+1}|z_t, s_t)$ , which effectively captures the desired relationship between decisions and the animal's location.

For action-level history dependency, we treat both the re-

ward and policy under a hidden mode z as functions dependent on the previous L states, specifically  $r_z : S^L \times \mathcal{A} \to \mathbb{R}$  and  $\pi_z : S^L \to \mathcal{A}$ , where  $L \in \mathbb{N}$  and  $S^L$  denotes the cartesian product of L state spaces. To simplify the notation, we denote an element of  $S^L$  as  $s^L$ , so that  $r_z(s^L, a) := r_z(s^1, s^2, \ldots, s^L, a)$  and  $\pi_z(a|s^L) := \pi_z(a|s^1, s^2, \ldots, s^L)$ , and pad both functions with dummy variables if the current time step is less than L. While it is also possible to incorporate previous actions into the reward function, we focus on state-only rewards for simplicity, which is a common practice in IRL. Nonetheless, this framework naturally extends from a single-state dependency to a history of states.

Furthermore, we can view the decision process as being non-Markovian, meaning that the current decision or action depends not only on the current state but also on the history of previous states and actions. Noticeably, there are various approaches to address non-Markovian decision processes, including state augmentation (Sutton, 1991), recurrent neural networks (Bakker, 2001; Hausknecht & Stone, 2015), Neural Turing Machines (Parisotto & Salakhutdinov, 2017) and so forth. In this paper, we adopt the most common approach– state augmentation; however, the framework can also be implemented using more advanced and scalable methods.

#### 3.4. SWIRL Inference Procedure

The goal of inference is to learn the hidden modes z and the model parameters  $\theta = (\mathcal{P}_z, r_z, \pi_z, p(s_1), p(z_1))$  given the collected trajectories  $\mathcal{D}$ . Here,  $p(s_1)$  and  $p(z_1)$  represent the probabilities of the initial state and hidden mode, respectively. The variables  $r_z$  and  $\pi_z$  denote the reward and policy associated with the hidden mode z, while  $\mathcal{P}_z$  is the transition matrix between hidden modes. We can maximize the likelihood of the demonstration trajectories  $\mathcal{D}$  to learn the optimal  $\theta^*$ , such that  $\theta^* = \operatorname{argmax}_{\theta} \log P(\mathcal{D}|\theta)$  (MLE). However, achieving this objective requires marginalizing over the hidden modes z, which is intractable. To address this issue, we employ the Expectation-Maximization (EM) algorithm, alternating between inferring the posterior distributions of the hidden modes and updating the parameters with the following auxiliary function:

$$G(\theta, \hat{\theta}) = \log p(s_1) + \sum_{z} p(z_1|\xi, \hat{\theta}) \log p(z_1)$$
(1)

$$+\sum_{t=1}^{T-1} \log \mathcal{P}(s_{t+1}|s_t, a_t)$$
(2)

$$+\sum_{t=1}^{T}\sum_{z_{t}}p(z_{t}|\xi,\hat{\theta})\log\pi_{z_{t}}(a_{t}|s_{t}^{L};r_{z})$$
(3)

+ 
$$\sum_{t=1}^{T-1} \sum_{z_t, z_{t+1}} p(z_t, z_{t+1} | \xi, \hat{\theta}) \log \mathcal{P}_z(z_{t+1} | z_t, s_t).$$
 (4)

Detailed SWIRL algorithm and EM derivation are provided in Appendix A.1 & A.2.

It is worth noting that this EM derivation seeks to maximize the log-likelihood of policy  $\pi_{z_t}(a_t|s_t^L;r_z)$  given the posterior of  $z_t$  (Eq. 3). This procedure can be incorporated into the Maximum Entropy IRL (MaxEnt IRL) (Ziebart et al., 2008; 2010) framework, since optimizing the reward by maximizing  $\log \pi$  corresponds to the Lagrangian dual of the standard MaxEnt IRL approach (Zeng et al., 2022). As a result, SWIRL can leverage a variety of IRL methods within the MaxEnt IRL framework: SWIRL can be integrated with model-based methods to infer the policy used to optimize the reward, such as Soft-Q iteration (Haarnoja et al., 2017), or model-free methods, such as Soft-Q learning (Haarnoja et al., 2017) and Soft Actor-Critic (Haarnoja et al., 2018). Alternatively, we can also convert the MaxEnt IRL problem to a model-free inverse Q-learning problem, such as IQ-Learn (Garg et al., 2021). Although model-free methods are often more general and scalable, we find that the model-based Soft-Q iteration approach is more suitable for our behavioral neuroscience study setting, where environment sizes tend to be small, data availability is limited, and the accuracy requirement for reward recovery is high. Accordingly, we use the Soft-Q iteration approach in our main experiments. Nevertheless, in Appendix D.1 we also demonstrate that SWIRL can be integrated with the modelfree IQ-Learn to achieve solid performance, illustrating SWIRL's potential in broader applications.

#### 3.5. Connection to Dynamics-based Behavior Methods

Traditional methods for analyzing animal behavior in neuroscience often use autoregressive dynamics models, with the autoregressive hidden Markov model (ARHMM) being the most prevalent (Wiltschko et al., 2015; Weinreb et al., 2024). ARHMMs assume that the animal behavior consists of multiple segments represented by a hidden Markov model, where each segment evolves through an autoregressive process. Using the notation established earlier, we denote hidden modes as  $z_t$  at time t, following the transition  $p(z_{t+1}|z_t)$ . At each time step t, the observation state  $s_t$  follows conditionally linear (or affine) dynamics, determined by the discrete mode  $z_t$ . This can be expressed as  $s_{t+1} = A_{z_t} s_t + v_t$ , where  $A_{z_t}$  is the linear dynamics associated with  $z_t$  and  $v_t$  represents Gaussian noise. If  $z_t$  changes, the linear dynamics will also change accordingly. More generally, we can represent the dynamics as  $p(s_{t+1}|s_t, z_t)$ . Consequently, the overall generative model for the ARHMM can be summarized as follows: (1)  $z_t \sim p(z_t|z_{t-1})$ , and (2)  $s_{t+1} \sim p(s_{t+1}|s_t, z_t)$ . Let's outline the generative model of SWIRL without history dependency: (1)  $z_t \sim p(z_t|z_{t-1})$ , and (2)  $s_{t+1} \sim \sum_{a_t} p(s_{t+1}|s_t, a_t) \pi(a_t|s_t, z_t)$ . The term  $\pi(a_t|s_t, z_t)$  arises because the policy is derived from  $r_{z_t}$ . Consequently, the primary distinction between ARHMM

and SWIRL lies in the dynamics used to generate  $s_{t+1}$ .

We can show that SWIRL is a more generalized version of ARHMM. In a deterministic MDP, where  $p(s_{t+1}|s_t, a_t)$  is a delta function and each action  $a_t$  uniquely determines  $s_{t+1}$ ,  $s_{t+1}$  directly implies  $a_t$ . Thus,  $\sum_{a_t} p(s_{t+1}|s_t, a_t)\pi(a_t|s_t, z_t) = \pi(a_t|s_t, z_t) = p(s_{t+1}|s_t, z_t)$ . This effectively reduces SWIRL to ARHMM. In the second real-world experiment (Sec. 4.3), the MDP setup satisfies these assumptions. In such a case, ARHMM can be seen as performing policy learning through behavioral cloning without learning a reward function, whereas SWIRL employs IRL to learn the policy.

Having established this connection, we can view SWIRL as a more generalized version of ARHMM, as it permits the MDP to be stochastic and allows multiple actions to result in the same preceding state. Additionally, explicitly modeling the policy introduces a reinforcement learning framework that better represents the decision-making processes of animals and reveals the underlying reward function. For SWIRL with history dependency, we can further connect it to the recurrent ARHMM (Linderman et al., 2016), which expands  $p(z_{t+1}|z_t)$  to  $p(z_{t+1}|z_t, s_t)$ .

Another advanced version of the ARHMM is the switching linear dynamical system (SLDS), which assumes that the state  $s_t$  is unobserved. Instead, the observed variable  $y_t$  is a linear transformation of  $s_t$ . Thus, the complete generative model for SLDS consists of: (1)  $z_t \sim p(z_t | z_{t-1})$ , (2)  $s_{t+1} \sim p(s_{t+1}|s_t, z_t)$ , and (3)  $y_{t+1} \sim p(y_{t+1}|s_{t+1})$ . This suggests that the representation  $s_t$  capturing the primary dynamics is, in fact, a latent representation of the observation  $y_t$ . Building on this concept, we can extend SWIRL into a latent variable model, where  $s_t$  serves as the latent representation of the true observation state  $y_t$ . This corresponds to the setup of Partial Observation Markov Decision Process (POMDP) in the literature. While SWIRL is not a POMDP method in the formal sense (e.g., modeling belief states or latent dynamics explicitly), it does address non-Markovian behavior by augmenting the state space with recent history (e.g., using  $s_t, s_{t-1}, s_{t-2}, \ldots$ ). This is a commonly used strategy to handle partial observability or non-Markovianity-similar in spirit to how LSTMs or memory-based policies are used in POMDP settings. Therefore, SWIRL leverages temporal context in a manner similar to methods designed for POMDPs. This extension will link SWIRL to representation learning in reinforcement learning, which can be explored further in future work.

Thus, we argue that SWIRL offers a more generalized and principled approach to studying animal behavior compared to commonly used dynamics-based models, as one can draw inspiration from the development of (latent) dynamics models to enhance advanced IRL methods for analyzing animal decision-making processes.

#### 4. Results

Throughout the experiment section, we use the following terminology to denote our proposed algorithms and the baseline models we compare:

• MaxEnt (Ziebart et al., 2008; 2010): Maximum Entropy IRL where the reward function is only a function of the current state and action. It is a single-mode IRL approach with a single reward function.

• **Multi-intention IQL** (Zhu et al., 2024): learns timevarying reward functions based on HM-MDP. It is a SWIRL model with no history dependency.

• Locally Consistent IRL (Nguyen et al., 2015): learns time-varying reward functions based on HM-MDP. It is a SWIRL model with no action-level history dependency.

• **ARHMM** (Wiltschko et al., 2015): learns the segmentation of animal behaviors using autoregressive dynamics combined with a hidden Markov model.

• **rARHMM** (Linderman et al., 2016): recurrent ARHMM whose transition probability of the hidden modes also relies on the state.

• I-1, I-2: the baseline variant of our proposed SWIRL method which assumes the transition kernel  $\mathcal{P}_z$  is **independent** of the state. The reward and policy depend either on the current state (in the case of I-1) or on both the current and previous states (in the case of I-2). Note that I-1 represents the simplest version of SWIRL, which corresponds to Multi-intention IQL. Thus, we use I-1 to denote Multi-intention IQL. The model can incorporate an arbitrary history length L for the policy and reward; in this paper, we use L = 1 and L = 2.

• S-1, S-2: our proposed SWIRL method where  $\mathcal{P}_z$  is state dependent. The suffix follows the same setup as above. S-1 corresponds to Locally Consistent IRL.

SWIRL code can be found at https://github.com/ BRAINML-GT/SWIRL.

#### 4.1. Application to a simulated gridworld environment

We begin by testing our method on simulated trajectories within a  $5 \times 5$  gridworld environment, where each state allows for five possible actions: up, down, left, right, and stay. The agent alternates between two reward maps: a home reward map and a water map (see Fig. 2A). Following the design of real animal experiments (Rosenberg et al., 2021), we assume that the water port provides water to the agent only once per visit. Therefore, under the water reward map, the agent receives a reward for (1) visiting the water state if it was not in the water state previously or (2) leaving the water state. The home reward map returns a reward at the home state. This leads to a non-Markovian reward function that relies on both the current state and the previous state. We employed soft-Q iteration to determine the optimal policy for each reward function and generated 200 trajecto-

Inverse Reinforcement Learning with Switching Rewards and History Dependency for Characterizing Animal Behaviors



Figure 2. Simulation experiment on a 5 × 5 gridworld. (A) Comparison between the true and discovered reward maps. The color scale represents reward values ranging from 0 to 1. The home reward is defined as  $r(s_t)$ , while the water reward depends on both the current and previous locations,  $r(s_t, s_{t-1})$ . To present the water reward, each location is divided into five groups, as detailed in the table on the far right. For example, the polygon in the first row represents the reward value when  $s_t$  is the current location and  $s_{t-1}$  is the location to the right. Light grey indicates an impossible transition where no reward exists. (B) Box plots illustrating the Pearson correlation between the true and recovered reward maps, test log-likelihood, and test segmentation accuracy over 10 runs. The x-axis represents the five different models. Outlier selection method is described in Appendix B.8.

ries based on the learned policy, using a history-dependent hidden-mode switching dynamic  $\mathcal{P}_z(z_{t+1}|z_t, s_t)$ . Accordingly, the agent is more likely to switch to the home map after visiting the water port and to switch to the water map after returning home. Each trajectory consists of 500 steps.

We then used SWIRL to learn the reward functions and the transition dynamics between them, based on 80% of the generated trajectories. As a baseline, we employed the Maximum Entropy IRL (MaxEnt) method and tested four variations of the SWIRL models (I-1, I-2, S-1, S-2), with I-1 representing multi-intention IQL. Fig. 2A displays a comparison between the true and discovered reward functions, while Fig. 2B presents boxplots showing the Pearson correlation between the true and recovered reward functions, along with the test log-likelihood (LL) and test segmentation accuracy (which measures the ability to predict the correct segments for home and water modes). The test performance was evaluated using the remaining 20% of the trajectories. Notably, accurate reward recovery was only achieved with the S-2 model. All four SWIRL variations outperformed MaxEnt, indicating the presence of more than one hidden model. Both the state dependency of hidden-mode transitions (decision-level dependency) and the history dependency reward function (action-level dependency) contributed to further improvements in test LL and segmentation accuracy. Specifically, only the state-dependent models (S-1, S-2) could accurately and robustly recover test segments, while the independent models (I-1, I-2) exhibited lower accuracy with higher variance. This is attributed to the non-Markovian reward design, where the agent can only receive water once per visit. Notably, S-2, the full SWIRL model incorporating both decision-level and action-level dependencies, demonstrated the best performance across all metrics.

To assess the robustness of SWIRL, in Appendix B.7, we evaluated the performance of SWIRL (S-2) under increasing levels of random perturbations in this gridworld dataset. We found that SWIRL can tolerate moderate levels of noise or incomplete data (with 30% of the states and actions in training data permuted), making it suitable for real-world animal behavior datasets where such challenges are common.

## 4.2. Application to long, non-stereotyped mouse trajectories

We then applied SWIRL to the long, non-stereotyped trajectories of mice navigating a 127-node labyrinth environment with water restrictions (Rosenberg et al., 2021). In this experiment, a cohort of 10 water-deprived mice moved freely in the dark for 7 hours. A water reward was provided at an end node (Fig. 3A), but only once every 90 seconds at most. Similar to the simulated experiment, the 90-second condition forces the mice to leave the port after drinking water, leading to a non-Markovian internal reward function. For our analysis, we segmented the raw node visit data into 238 trajectories, each comprising 500 time points. This data format presents a considerably greater challenge compared to the same dataset processed with more handcrafted methods in previous IRL applications (Ashwood et al., 2022a; Zhu et al., 2024), which were limited to clustered, stereotyped trajectories of only 20 time points in length.

#### 4.2.1. SWIRL INFERRED INTERPRETABLE HISTORY-DEPENDENT REWARD MAPS

We applied SWIRL to 80% of the 238 mouse trajectories from the water-restricted labyrinth experiments. According to Rosenberg et al. (2021), mice quickly learned the labyrinth environment and began executing optimal paths

Inverse Reinforcement Learning with Switching Rewards and History Dependency for Characterizing Animal Behaviors



*Figure 3.* Water-restricted labyrinth experiment. (A) Setup for the labyrinth experiment. (B) Boxplot showing held-out test LL over 10 runs, with the x-axis representing the five different models. Outlier selection method is described in Appendix B.8. (C) History dependency inferred by SWIRL (S-2), as reflected in the reward map for the water mode. (D) Inferred reward maps from SWIRL (S-2) under three hidden modes: water, home, and explore. To enhance visualization, the inferred reward  $r(s_t, s_{t-1})$  was averaged over  $s_{t-1}$  to produce  $r(s_t)$ . (E) Segments of a trajectory from held-out test data, predicted by four SWIRL models. The orange dot indicates when the mouse visits the water port, while the red cross denotes the mouse's visit to state 0 (home) at that time. (F) Trajectories segmented into hidden modes based on SWIRL (S-2) predictions.

from the entrance to the water port within the first hour of the experiment. Therefore, we assume the mice acted optimally concerning the internal reward function guiding their behavior. We tested a number of hidden modes Z from 2 to 5 in Appendix B.6.1 and found Z = 3 to be the best fit. Fig. 3B displays the held-out test LL for MaxEnt and the SWIRL variations based on the remaining 20% of trajectories. The state dependency in hidden-mode switching dynamics and the history dependency in the reward function contributed to improved test performance. The final SWIRL model (S-2) successfully recovered a water reward map, a home reward map, and an explore reward map (Fig. 3D). For better visualization, we averaged the S-2-recovered history-dependent rewards across previous states and normalized the reward values to a range of (0, 1). In the water reward map, mice received a high reward for visiting the water port. In the home reward map, there was a high reward for visiting state 0 at the center of the labyrinth, which also served as the entrance and exit. Mice occasionally went to state 0 to enter or leave the labyrinth and sometimes passed by on their way to other nodes. In the explore reward map, mice received a high reward for exploring areas of the labyrinth other than state 0 and the water port.

Importantly, SWIRL recovered an interpretable historydependent reward map for the water port (Fig. 3C). It indicates that mice receive a high reward (1.0) for reaching the water port when their previous location was not the water port. If their prior location was the water port, there is still a reward (0.7) for staying there, but the reward for leaving the water port is even higher (0.9). This observation aligns with the water port design, as mice can only obtain water once every 90 seconds. Consequently, it makes sense that the mice would want to leave the water port after reaching it. Such insights would not be captured by a Markovian reward function that depends solely on the current state.

#### 4.2.2. SWIRL INFERRED INTERPRETABLE HISTORY-DEPENDENT HIDDEN-MODE SEGMENTS

We then visualized all mouse trajectories based on the hidden-mode segments predicted by SWIRL (S-2) (Fig. 3F). In segments classified as water mode, mice start from various locations in the labyrinth and move toward the water port. In segments identified as home mode, mice begin from distant nodes and head toward the center of the labyrinth (home). In segments categorized as explore mode, mice start from junction nodes or the water port and explore end nodes other than the water port. This result demonstrates that SWIRL can identify sub-trajectories of varying lengths from raw data spanning 500 time points, allowing us to visualize them together and reveal clustered behavioral strategies. This capability has not been achieved by previous studies on freely moving animal behavior over extended recording periods, and we conducted this analysis without prior knowledge of the locations of the water port or home.

We also provide a detailed visualization of the hidden-mode segments from an example trajectory in the held-out test data and compare the segmentation performance of the four SWIRL variations (Fig. 3E). In the S-2 segments, visits to the water port (indicated by orange dots) consistently occur at the end of a water mode segment, while visits to state 0 (home) (indicated by red crosses) typically happen

at the conclusion of a home mode segment. Notably, home mode segments that do not include a visit to state 0 can still be valid, as these segments may end at state 1 or 2 (see Appendix C.1). In contrast, the I-1, I-2, and S-1 segments exhibit instances of water segments that do not involve a visit to the water port, along with many home segments that lack clear interpretability. Overall, S-2 successfully identifies robust segments of reasonable length, avoiding the numerous rapid switches seen in the other variations. We attribute this to both the state dependency of hidden mode transitions and the history dependency in rewards. This suggests that mice are unlikely to make quick changes in their decisions; instead, they make choices based on their current location and take into account at least two locations while navigating the maze.

Furthermore, in Appendix B.6.2, we found S-3 and S-4 exhibited even higher test LL than S-2, suggesting the presence of longer action-level history dependency (L > 2) in this labyrinth dataset. This observation aligns with the partially observable nature of this 127-node labyrinth: The mouse may not know the whole environment, so it likely relies on a longer history of prior states to guide its decision-making. However, hidden mode predictions of S-3 and S-4 are very close to that of S-2, suggesting that S-2 is already powerful enough for hidden mode prediction.

# 4.3. Application to mouse spontaneous behavior trajectories

We also employed SWIRL on a dataset in which mice wandered an empty arena without explicit rewards (Markowitz et al., 2023). In this experiment, mouse behaviors were recorded via depth camera video, and dopamine fluctuations in the dorsolateral striatum were monitored. The dataset includes behavior "syllables" inferred by MoSeq (Wiltschko et al., 2015), which indicate the type of behavior exhibited by the mice during specific time periods (e.g., grooming, sniffing, etc.). Consequently, trajectories consist of behavioral syllables, with each time point representing a syllable. We selected 159 trajectories, each comprising 300 time points, by retaining only the 9 most frequent syllables and merging consecutive identical syllables into a single time point. This method, also used in previous reinforcement learning studies on this dataset (Markowitz et al., 2023), ensures that each syllable has sufficient data for learning and allows the model to concentrate on the transitions between different syllables.

The MDP for this experiment comprises 9 states and 9 actions, where the state represents the current syllable and the action signifies the next syllable. As mentioned in Sec. 3.5, the ARHMM can be viewed as a variant of SWIRL that learns the policy through behavior cloning. In other words, the policy for this MDP aligns with the emission probability of the ARHMM. This setup offers an excellent opportunity to compare the performance of SWIRL with ARHMM and its variant, rARHMM.

We applied SWIRL, rARHMM, ARHMM, and MaxEnt to 80% of the trajectories and assessed the held-out test LL on the remaining 20% (Fig. 4B). All four SWIRL models outperformed ARHMM and rARHMM on this dataset, indicating that learning rewards is more beneficial for behavior segmentation and explaining the behavior trajectories. Interestingly, the history dependency in the reward function resulted in lower test LL, as S-1 and I-1 demonstrated higher test LL than S-2 and I-2. We believe this is attributable to the merging of consecutive identical syllables and the selection of the top 9 syllables during the preprocessing phase for this dataset. As a result of these steps, the actual time interval between  $s_{t-1}$  and  $s_t$  may vary significantly, leading to a poorly defined time concept that complicates the model's ability to capture the history dependency in the reward function. However, we can use SWIRL with different variations as a hypothesis-testing tool. The variation yielding the highest test LL may be regarded as more accurately reflecting the dynamics and structure of the data. Consequently, these results suggest that the behavior trajectories exhibit only Markovian dependency rather than long-term non-Markovian dependency. Since S-1 remains higher than I-1, we conclude that the state dependency in the hidden mode transition contributes to explaining the data.

The best SWIRL model (S-1) recovered reward maps and hidden-mode segments provide insights into the variability of dopamine impacts on animal spontaneous behavior: As illustrated in Fig. 4A, the reward maps exhibit some similarities along with meaningful differences. For certain reward maps, there is a relatively high correlation (e.g., 0.40 and 0.48) with dopamine fluctuations during the corresponding modes. This suggests that dopamine fluctuations can reflect a certain extent of reward during hidden modes 1 and 4.

Furthermore, the plot of hidden mode segments across all trajectories (Fig. 4C) shows how each spontaneous behavior trajectory is temporally segmented into distinct latent modes, each governed by one of the five learned reward functions (h1-h5). Early in the trajectories, we observe a higher prevalence of h1, h2, and h4, while h3 and h5 increasingly dominate toward the later stages. This temporal pattern aligns well with the findings from prior work (Markowitz et al., 2023), which reported that mice exhibit greater activity at the beginning of spontaneous behavior sequences and progressively slow down and disengage over time. The reward maps provide mechanistic insight into these transitions: h1 encourages selective transitions into pause while still supporting other state transitions, representing a modulated rest phase; h2 discourages passivity, with low reward for transitions into pause and strong suppression



*Figure 4.* **Mouse spontaneous behavior experiment.** (A) SWIRL (S-1) inferred reward maps for five hidden modes. h1 denotes hidden mode 1, and so on. For better visualization, reward values are normalized to a range of (0, 1). DA corr represents the Pearson correlation between the inferred reward map and the averaged dopamine fluctuation levels. (B) Held-out test LL for each model across different number of hidden modes over 10 runs. The shaded area represents the total area that falls between one standard deviation above and below the mean. (C) Inferred hidden-mode segments for all trajectories, with each row representing a trajectory.

of grooming; and h4 favors transitions into sniffing, reflecting exploratory drive. In contrast, h3 and h5 strongly reward transitions into pause and suppress departures from it, indicating globally suppressive states that enforce behavioral quiescence. The increasing expression of h3 and h5 over time reflects the mice's natural progression from active to inactive states, supporting the interpretation that the learned rewards capture underlying behavioral structure consistent with known temporal dynamics.

While the non-Markovian action-level history dependency introduced by SWIRL does not demonstrate superior performance in this particular experiment, the findings showcase SWIRL's unique contribution to neuroscience research. Specifically, SWIRL serves as a powerful tool for hypothesis testing in behavioral datasets, enabling researchers to validate or challenge hypotheses regarding decision-level dependency as well as non-Markovian action-level dependency. This versatility further confirms SWIRL's great potential in advancing our understanding of complex behaviors.

#### 5. Discussion

We introduce SWIRL, a novel IRL framework designed to capture history-dependent switching reward functions in complex animal behaviors. Our framework can infer interpretable switching reward functions from lengthy, nonstereotyped behavioral tasks, achieving reasonable hiddenmode segmentation—a feat that, to the best of our knowledge, has not been accomplished previously. Those abilities, combined with its connection to traditional dynamics-based behavior analysis methods in neuroscience, make SWIRL well-suited for behavioral neuroscience applications. Future extensions of SWIRL to partially observable Markov decision processes (POMDPs) could further broaden its utility, offering enhanced insight into complex and nuanced animal behaviors.

Beyond its relevance to neuroscience study, SWIRL also benefits the broader machine learning community. It offers a flexible framework with history-dependent switching reward functions that can be integrated with various model-free IRL algorithms. For example, in Appendix D.1, we highlight SWIRL's potential to be integrated with IQ-Learn, a state-of-the-art scalable model-free IRL method that has been employed in training large language models (Wulfmeier et al., 2024). Future development of SWIRL that emphasizes scalability, such as incorporating RNNs or transformer-based policy model will be particularly valuable for areas such as robotics and large language models, where adaptable IRL strategies are increasingly in demand.

## **Impact Statement**

SWIRL has the potential to advance neuroscience research by helping uncover connections between complex animal decision-making and corresponding brain activities. In a broader context, SWIRL's capacity to learn multiple historydependent switching reward functions can also enable enhanced policy learning and explainability in fields such as robotics and large language models. However, as with all methods that analyze complex behaviors, careful consideration of data privacy, fairness, and responsible deployment is imperative to ensure ethical use.

## Acknowledgements

This work was supported by National Science Foundation NSF2336055 (AW), a Career Award at the Scientific Interface from the Burroughs Wellcome Fund (JEM), the David and Lucille Packard Foundation (JEM), and the Sloan Foundation (AW & JEM).

## References

- Abbeel, P. and Ng, A. Y. Apprenticeship learning via inverse reinforcement learning. In *Proceedings of the Twenty-First International Conference on Machine Learning*, ICML '04, pp. 1, New York, NY, USA, 2004. Association for Computing Machinery. ISBN 1581138385. doi: 10.1145/1015330.1015430. URL https://doi. org/10.1145/1015330.1015430.
- Ashwood, Z., Jha, A., and Pillow, J. W. Dynamic inverse reinforcement learning for characterizing animal behavior. In Oh, A. H., Agarwal, A., Belgrave, D., and Cho, K. (eds.), *Advances in Neural Information Processing Systems*, 2022a. URL https://openreview.net/ forum?id=nosngu5XwY9.
- Ashwood, Z. C., Roy, N. A., Stone, I. R., Urai, A. E., Churchland, A. K., Pouget, A., Pillow, J. W., and Laboratory, T. I. B. Mice alternate between discrete strategies during perceptual decision-making. *Nature Neuroscience*, 25(2):201–212, Feb 2022b. ISSN 1546-1726. doi: 10.1038/s41593-021-01007-z. URL https:// doi.org/10.1038/s41593-021-01007-z.
- Babes-Vroman, M., Marivate, V., Subramanian, K., and Littman, M. L. Apprenticeship learning about multiple intentions. In *International Conference on Machine Learning*, 2011. URL https://api. semanticscholar.org/CorpusID:9737656.
- Bakker, B. Reinforcement learning with lstm in nonmarkovian tasks with longterm dependencies. *Memory*, pp. 1–18, 2001.

- Garg, D., Chakraborty, S., Cundy, C., Song, J., and Ermon, S. Iq-learn: Inverse soft-q learning for imitation. In Ranzato, M., Beygelzimer, A., Dauphin, Y., Liang, P., and Vaughan, J. W. (eds.), *Advances in Neural Information Processing Systems*, volume 34, pp. 4028–4039. Curran Associates, Inc., 2021.
- Haarnoja, T., Tang, H., Abbeel, P., and Levine, S. Reinforcement learning with deep energy-based policies. In *International conference on machine learning*, pp. 1352– 1361. PMLR, 2017.
- Haarnoja, T., Zhou, A., Abbeel, P., and Levine, S. Soft actorcritic: Off-policy maximum entropy deep reinforcement learning with a stochastic actor. In Dy, J. and Krause, A. (eds.), Proceedings of the 35th International Conference on Machine Learning, volume 80 of Proceedings of Machine Learning Research, pp. 1861–1870. PMLR, 10–15 Jul 2018. URL https://proceedings.mlr. press/v80/haarnoja18b.html.
- Hattori, R., Danskin, B., Babic, Z., Mlynaryk, N., and Komiyama, T. Area-specificity and plasticity of history-dependent value coding during learning. *Cell*, 177(7):1858–1872.e15, 2019. ISSN 0092-8674. doi: https://doi.org/10.1016/j.cell.2019.04. 027. URL https://www.sciencedirect.com/ science/article/pii/S0092867419304465.
- Hausknecht, M. and Stone, P. Deep recurrent q-learning for partially observable mdps. In *AAAI 2015 Fall Symposium*, 2015.
- Hirakawa, T., Yamashita, T., Tamaki, T., Fujiyoshi, H., Umezu, Y., Takeuchi, I., Matsumoto, S., and Yoda, K. Can ai predict animal movements? filling gaps in animal trajectories using inverse reinforcement learning. *Eco-sphere*, 9(10):e02447, 2018.
- Houthooft, R., Chen, X., Duan, Y., Schulman, J., De Turck, F., and Abbeel, P. Vime: Variational information maximizing exploration. *Advances in neural information* processing systems, 29, 2016.
- Kennedy, A. The what, how, and why of naturalistic behavior. Current Opinion in Neurobiology, 74:102549, 2022. ISSN 0959-4388. doi: https://doi.org/10.1016/j.conb.2022.102549. URL https://www.sciencedirect.com/science/article/pii/S0959438822000435.
- Linderman, S. W., Miller, A. C., Adams, R. P., Blei, D. M., Paninski, L., and Johnson, M. J. Recurrent switching linear dynamical systems. *arXiv preprint arXiv:1610.08466*, 2016.

- Markowitz, J. E., Gillis, W. F., Jay, M., Wood, J., Harris, R. W., Cieszkowski, R., Scott, R., Brann, D., Koveal, D., Kula, T., Weinreb, C., Osman, M. A. M., Pinto, S. R., Uchida, N., Linderman, S. W., Sabatini, B. L., and Datta, S. R. Spontaneous behaviour is structured by reinforcement without explicit reward. *Nature*, 614(7946):108– 117, January 2023.
- Mazzucato, L. Neural mechanisms underlying the temporal organization of naturalistic animal behavior. *Elife*, 11: e76577, 2022.
- Ng, A. Y. and Russell, S. J. Algorithms for inverse reinforcement learning. In *Proceedings of the Seventeenth International Conference on Machine Learning*, ICML '00, pp. 663–670, San Francisco, CA, USA, 2000. Morgan Kaufmann Publishers Inc. ISBN 1558607072.
- Nguyen, Q. P., Low, K. H., and Jaillet, P. Inverse reinforcement learning with locally consistent reward functions. In *Neural Information Processing Systems*, 2015.
- Parisotto, E. and Salakhutdinov, R. Neural map: Structured memory for deep reinforcement learning. arXiv preprint arXiv:1702.08360, 2017.
- Pinsler, R., Maag, M., Arenz, O., and Neumann, G. Inverse reinforcement learning of bird flocking behavior. In *ICRA Swarms Workshop*, 2018.
- Rosenberg, M., Zhang, T., Perona, P., and Meister, M. Mice in a labyrinth show rapid learning, sudden insight, and efficient exploration. *eLife*, 10:e66175, jul 2021. ISSN 2050-084X. doi: 10.7554/eLife.66175. URL https: //doi.org/10.7554/eLife.66175.
- Sezener, C. E., Uchibe, E., and Doya, K. Obtaining reward functions of rats using inverse reinforcement learning. In *Türkiye Autonomous Robots Conference*, 2014.
- Sharafeldin, A., Imam, N., and Choi, H. Active sensing with predictive coding and uncertainty minimization. *Patterns*, 5(6), Jun 2024. ISSN 2666-3899. doi: 10.1016/j.patter. 2024.100983. URL https://doi.org/10.1016/ j.patter.2024.100983.
- Stone, I. R. Latent Variable Models for Characterizing the Dynamic Structure Underlying Complex Behaviors. PhD thesis, Princeton University, 2023.
- Surana, A. and Srivastava, K. Bayesian nonparametric inverse reinforcement learning for switched markov decision processes. In 2014 13th International Conference on Machine Learning and Applications, pp. 47–54. IEEE, 2014.
- Sutton, R. S. Dyna, an integrated architecture for learning, planning, and reacting. ACM Sigart Bulletin, 2(4):160– 163, 1991.

- Weinreb, C., Pearl, J. E., Lin, S., Osman, M. A. M., Zhang, L., Annapragada, S., Conlin, E., Hoffmann, R., Makowska, S., Gillis, W. F., et al. Keypoint-moseq: parsing behavior by linking point tracking to pose dynamics. *Nature Methods*, 21(7):1329–1339, 2024.
- Wiltschko, A. B., Johnson, M. J., Iurilli, G., Peterson, R. E., Katon, J. M., Pashkovski, S. L., Abraira, V. E., Adams, R. P., and Datta, S. R. Mapping sub-second structure in mouse behavior. *Neuron*, 88(6):1121–1135, 2015.
- Wu, F., Ke, J., and Wu, A. Inverse reinforcement learning with the average reward criterion. Advances in Neural Information Processing Systems, 36, 2024.
- Wulfmeier, M., Bloesch, M., Vieillard, N., Ahuja, A., Bornschein, J., Huang, S., Sokolov, A., Barnes, M., Desjardins, G., Bewley, A., Bechtle, S. M. E., Springenberg, J. T., Momchev, N., Bachem, O., Geist, M., and Riedmiller, M. Imitating language via scalable inverse reinforcement learning. In *The Thirty-eighth Annual Conference on Neural Information Processing Systems*, 2024. URL https: //openreview.net/forum?id=5d2eScRiRC.
- Yamaguchi, S., Naoki, H., Ikeda, M., Tsukada, Y., Nakano, S., Mori, I., and Ishii, S. Identification of animal behavioral strategies by inverse reinforcement learning. *PLoS computational biology*, 14(5):e1006122, 2018.
- Zeng, S., Li, C., Garcia, A., and Hong, M. Maximumlikelihood inverse reinforcement learning with finite-time guarantees. In Koyejo, S., Mohamed, S., Agarwal, A., Belgrave, D., Cho, K., and Oh, A. (eds.), *Advances in Neural Information Processing Systems*, volume 35, pp. 10122–10135. Curran Associates, Inc., 2022.
- Zhu, H., Crompe, B. D. L., Kalweit, G., Schneider, A., Kalweit, M., Diester, I., and Boedecker, J. Multiintention inverse q-learning for interpretable behavior representation. *Transactions on Machine Learning Research*, 2024. ISSN 2835-8856. URL https:// openreview.net/forum?id=hrKHkmLUFk.
- Ziebart, B. D., Maas, A., Bagnell, J. A., and Dey, A. K. Maximum entropy inverse reinforcement learning. In *Proceedings of the 23rd National Conference on Artificial Intelligence - Volume 3*, AAAI'08, pp. 1433–1438. AAAI Press, 2008. ISBN 9781577353683.
- Ziebart, B. D., Bagnell, J. A., and Dey, A. K. Modeling interaction via the principle of maximum causal entropy. In *Proceedings of the 27th International Conference on International Conference on Machine Learning*, ICML'10, pp. 1255–1262, Madison, WI, USA, 2010. Omnipress. ISBN 9781605589077.

#### A. Appendix A

#### A.1. The SWIRL algorithm

Following the EM update scheme, we derive the auxiliary function for the *n*-th trajectory during the E-step, where n = 1, 2, ..., N:

$$G_n(\theta, \hat{\theta}) = \log p(s_{n,1}) + \sum_z p(z_{n,1}|\xi_n, \hat{\theta}) \log p(z_{n,1}) + \sum_{t=1}^{T_n - 1} \log \mathcal{P}(s_{n,t+1}|s_{n,t}, a_{n,t})$$
(5)

$$+\sum_{t=1}^{T_n} \sum_{z_{n,t}} p(z_{n,t}|\xi_n, \hat{\theta}) \log \pi_{z_{n,t}}(a_{n,t}|s_{n,t}^L; r_z)$$
(6)

$$+\sum_{t=1}^{T_n-1}\sum_{z_{n,t},z_{n,t+1}} p(z_{n,t},z_{n,t+1}|\xi_n,\hat{\theta}) \log \mathcal{P}_z(z_{n,t+1}|z_{n,t},s_{n,t}).$$
(7)

Here are some remarks: (I) We incorporate state dependency into the hidden mode transition  $\mathcal{P}_z$ , such that  $z_{t+1}$  depends not only on the previous hidden mode  $z_t$  but also on the current state  $s_t$ . This modification results in longer segments of hidden modes with reduced fast-switching phenomena. (II) We can perform MaxEnt IRL based on the policy term  $\pi_{z_{n,t}}(a_{n,t}|s_{n,t}^L;r_z)$  in Eq. 6, as discussed in Sec. 3.4. (III) If we have estimated the current policy  $\pi_{z_n}$  based on the current reward estimate  $r_z$ , we can apply any inference method to estimate the posterior probabilities  $p(z_{n,t}|\xi_n, \hat{\theta})$  and  $p(z_{n,t}, z_{n,t+1}|\xi_n, \hat{\theta})$ . In this work, we use the standard forward-backward message-passing algorithm. (IV) It is important to note that  $\mathcal{P}(s_{n,t+1}|s_{n,t}, a_{n,t})$  represents the environment transition and is not involved in the optimization process.

In the M-step, to maximize the auxiliary function G, we update all parameters in  $\theta$  by performing gradient descent on G. The inference procedure alternates between the E-step and M-step until convergence or a predetermined number of iterations. The algorithm is summarized in Algorithm 1.

#### Algorithm 1 The SWIRL Algorithm

**Data:** Expert demonstrations  $\mathcal{D} = \{\xi_1, \xi_2, \dots, \xi_N\}$ 

**Result:** Posterior probabilities of hidden modes z, rewards  $r_z$  for each mode, and other parameters in  $\theta$ 

Initialize parameters  $\theta^0$ for  $k = 1, 2, \dots, K$  do

E-step

For each hidden mode z and corresponding reward  $r_z^k$ , infer the optimal soft Q-function  $Q_z^{k^*}$  using a RL method. Compute the policy with the Boltzmann distribution:

$$\pi_z(a|s) = \frac{\exp\{Q_z^{k^*}(s,a)/\alpha\}}{\sum_{a'\in\mathcal{A}} \exp\{Q_z^{k^*}(s,a')/\alpha\}}$$

to obtain  $\pi_z^k(a|s^L; r_z^k), \forall s \in S. \alpha$  is a predefined temperature parameter.

For each trajectory  $\xi_n$ , use forward-backward message passing to calculate  $p(z_{n,t}|\xi_n, \theta^k)$  and  $p(z_{n,t}, z_{n,t+1}|\xi_n, \theta^k)$ . Use the posteriors,  $\pi_z^k(a|s^L; r_z^k)$ , and  $\theta^k$  to compute the auxiliary function G (Eqs. 5-7).

end M-step

Update parameters  $\theta$  using gradient descent on the auxiliary function G with learning rate  $\eta_k$ :

$$\theta^{k+1} \leftarrow \theta^k - \eta_k \nabla_\theta G(\theta, \theta^k).$$

end

end

#### A.2. Detailed derivation of SWIRL objectives by EM algorithm

Here we need to learn  $\theta \triangleq (r_z, \mathcal{P}_z, p(s_1), p(z_1))$ . Note that the total probability for a sequence  $\{(s_t, a_t, z_t)\}_{t=1:T}$  is

$$\log p(z, s, a) = \log p(z_1) p(s_1) \pi_{z_1}(a_1 | s_1; r_z) \prod_{t=2}^T \mathcal{P}(s_t | s_{t-1}, a_{t-1}) \mathcal{P}_z(z_t | z_{t-1}, s_{t-1}) \pi_{z_t}(a_t | s_t^L; r_z).$$

The expectation across all possible sequences is given by

$$\mathbb{E}[\log p(z, s, a)] = \sum_{n=1}^{N} \log p(s_{n,1}) + \sum_{n=1}^{N} p(z_{n,1}|s_1, a_1) \log p(z_{n,1}) \\ + \sum_{n=1}^{N} \sum_{t=2}^{T} \log \mathcal{P}(s_{n,t}|s_{n,t-1}, a_{n,t-1}) \\ + \sum_{n=1}^{N} \sum_{t=2}^{T} p(z_{n,t}, z_{n,t-1}|\xi_n) \log \mathcal{P}_z(z_{n,t}|z_{n,t-1}, s_{n,t-1}) \\ + \sum_{n=1}^{N} \sum_{t=1}^{T} p(z_{n,t}|\xi_n) \log \pi_{z_{n,t}}(a_{n,t}|s_{n,t}^L; r_z).$$

Now we use Expectation-Maximization to find  $\theta$ . E step:

$$\begin{aligned} G(\theta, \hat{\theta}) &= \sum_{z} p(z|\xi_{1:N}, \hat{\theta}) \log p(z, \xi_{1:N}, |\hat{\theta}) \\ &= \sum_{z} \left( \prod_{n=1}^{N} p(z_{n,1:T}|\xi_n, \hat{\theta}_n) \right) \\ &\sum_{n=1}^{N} \left\{ \log p(s_{n,1}) + \log p(z_{n,1}) + \sum_{t=1}^{T_n} (\log \pi_{z_{n,t}}(a_{n,t}|s_{n,t}^L; r_z)) + \sum_{t=1}^{T_{n-1}} (\log \mathcal{P}(s_{n,t+1}|s_{n,t}, a_{n,t}) + \log \mathcal{P}_z(z_{n,t+1}|z_{n,t}, s_{n,t})) \right\} \end{aligned}$$

$$= \sum_{n=1}^{N} \log p(s_{n,1}) + \sum_{n=1}^{N} \sum_{z} p(z_{n,1} = z | \xi_n, \hat{\theta}) \log p(z_{n,1}) + \sum_{n=1}^{N} \sum_{t=1}^{T_n} \sum_{z} p(z_{n,t} = z | \xi_n, \hat{\theta}) \log \pi_{z_{n,t}}(a_{n,t} | s_{n,t}^L; r_z) + \sum_{n=1}^{N} \sum_{t=1}^{T_n-1} \sum_{z} \sum_{z'} p(z_{n,t} = z, z_{n,t+1} = z' | \xi_n, \hat{\theta}) \log \mathcal{P}_z(z_{n,t+1} | z_{n,t}, s_{n,t}) + \sum_{n=1}^{N} \sum_{t=1}^{T_n-1} \log \mathcal{P}(s_{n,t+1} | s_{n,t}, a_{n,t}).$$

M step:

$$\theta^{k+1} = \arg\max_{\theta} G(\theta, \theta^k).$$

For notational simplicity, we only consider a specific trajectory n. To compute  $G(\theta, \theta^k)$ , we need to estimate

$$p(z_t|s_{1:T}, a_{1:T}, \hat{\theta})$$

and

$$p(z_t = z, z_{t+1} = z' | s_{1:T}, a_{1:T}, \hat{\theta}).$$

Thus we can use message passing algorithm, where we define the forward-backward variables  $\alpha$  and  $\beta$ . Forward variables  $\alpha_{t,z}$ , for  $t = 1, \ldots, T$ :

$$\begin{aligned} \alpha_{1,z} &= p(z_1 = z | \hat{\theta}), \\ \alpha_{t,z} &= p(s_{1:t}, a_{1:t}, z_t = z | \hat{\theta}) \\ &= \sum_{z'} p(s_{1:t-1}, a_{1:t-1}, z_{t-1} = z' | \hat{\theta}) \mathcal{P}_z(z_t = z | s_{t-1}, z_{t-1} = z') p(s_t | s_{t-1}, a_{t-1}) \pi_{z_t}(a_t | s_t^L; r_z) \\ &= \sum_{z'} \alpha_{t-1,z'} \mathcal{P}_z(z_t = z | s_{t-1}, z_{t-1} = z') p(s_t | s_{t-1}, a_{t-1}) \pi_{z_t}(a_t | s_t^L; r_z). \end{aligned}$$

Backward variables  $\beta_{t,z}$ , for  $t = 1, \ldots, T$ :

$$\begin{split} \beta_{T,z} &= 1, \\ \beta_{t,z} &= p(s_{t+1:T}, a_{t+1:T} | s_t, a_t, z_t = z, \hat{\theta}) \\ &= \sum_{z'} \beta_{t+1,z'} p(s_{t+1} | s_t, a_t) \pi_{z'}(a_t | s_t^L; r_z) \mathcal{P}_z(z_{t+1} = z' | z_t = z, s_{t+1}), \\ \beta_{1,z} &= p(s_{1:T}, a_{1:T} | z_1 = z, \hat{\theta}) \\ &= \sum_{z'} \beta_{1,z'} p(s_1) \pi_{z'}(a_1 | s_1^L; r_z) \mathcal{P}_z(z_1 = z' | z_0 = z, s_1). \end{split}$$

Therefore,

$$\begin{split} p(z_t &= z | \xi, \hat{\theta}) \\ &= p(z_t = z, \xi | \hat{\theta}) / p(\xi | \hat{\theta}) \\ &= p(s_{1:t}, a_{1:t}, z_t = z | \hat{\theta}) p(s_{t+1:T}, a_{t+1:T} | s_t, a_t, z_t = z, \hat{\theta}) / p(\xi | \hat{\theta}) \\ &= \alpha_{t,z} \beta_{t,z} / p(\xi | \hat{\theta}). \end{split}$$

Furthermore,

$$\begin{split} p(z_{t-1}, s_{t-1}, z_t | \xi, \hat{\theta}) &= p(z_{t-1}, s_{t-1}, z_t, \xi | \hat{\theta}) / p(\xi | \hat{\theta}) \\ &= p(s_{1:t-1}, a_{1:t-1}, z_{t-1}) p(z_t | z_{t-1}, s_{t-1}) p(s_t, a_t | s_{t-1}, a_{t-1}, z_t) p(s_{t+1:T}, a_{t+1:T} | z_t, s_t, a_t) / p(\xi | \hat{\theta}) \\ &= \frac{p(s_{1:t-1}, a_{1:t-1}, z_{t-1}) p(z_t | z_{t-1}, s_{t-1}) p(s_t | s_{t-1}, a_{t-1}) p(a_t | s_t, z_t) p(s_{t+1:T}, a_{t+1:T} | z_t, s_t, a_t)}{p(\xi | \hat{\theta})} \\ &= \frac{\alpha_{t-1, z_{t-1}} \mathcal{P}_z(z_t | z_{t-1}, s_{t-1}) \mathcal{P}_z(s_t | s_{t-1}, a_{t-1}) \pi_{z_t}(a_t | s_t^L; r_z) \beta_{t, z_t}}{p(\xi | \hat{\theta})}. \end{split}$$

And finally,

$$p(\xi|\hat{\theta}) = \sum_{z} \alpha_{T,z} = \sum_{z} \alpha_{1,z} \beta_{1,z}.$$

## **B.** Appendix B

## **B.1. Implementation details**

We developed our SWIRL framework in JAX, leveraging its automatic differentiation and parallelization features to efficiently handle the computational demands of our algorithm. During each M-step update, we performed gradient descent to optimize the model parameters. We employed the adam optimizer from Optax (5x5 Gridworld & Spontaneous Behavior) or the BFGS optimizer from jax.scipy (Labyrinth) for learning the reward function  $r_z$ , using a learning rate of  $5 \times 10^{-3}$  and momentum coefficients of (0.9, 0.999) (adam) or a tolerance of  $1 \times 10^{-4}$  (BFGS). We backpropagated the gradient for the reward function from the policy term in loss function through 100 Soft-Q iterations. For optimizing the hidden mode transition  $\mathcal{P}_z(z_{t+1} \mid z_t, s_t)$ , we used the LBFGS optimizer from JAXopt with the tolerance set to  $1 \times 10^{-4}$ .

## **B.2.** Empirical runtime

Our SWIRL implementation leverages the advantages of JAX, including just-in-time (JIT) compilation and vectorization, to achieve high computational efficiency. For S-2 experiments across all three datasets (gridworld, labyrinth, and spontaneous behavior), SWIRL converges within 15–30 minutes on a V100 GPU, which takes 50–100 EM iterations. For longer L, a S-4 experiment on labyrinth with 50 EM iterations take 2-3 hours to finish on a L40S GPU.

## **B.3.** Evaluation metrics

The test log-likelihood is computed from the forward variable  $\alpha$ , where  $\log p(s_{1:T}, a_{1:T}) = \log \sum_{z} \alpha_{T,z}$ . Detail of the forward variable  $\alpha$  computation is described in Appendix A.2. For test hidden mode segmentation accuracy, we use the Viterbi algorithm to predict the hidden mode of each timepoint and compute the percentage of correct hidden mode prediction compared to ground truth data. For reward correlation, we compute the Pearson correlation between learnt reward and ground truth reward or dopamine fluctuation levels.

## **B.4.** Environment setup

5x5 Gridworld: State space: Discrete(25); Action space: Discrete(5). The 5 actions are 'up', 'left', 'down', 'right', 'stay'.

**Labyrinth:** State space: Discrete(127); Action space: Discrete(4). The labyrinth has a binary-tree structure and the 4 actions are 'move in left', 'move out left', 'move out left', 'move out right'.

**Spontaneous Behavior:** State space: Discrete(9); Action space: Discrete(9). Each state is a MoSeq syllable that defines a behavior motif. Each action represents a next state that the agent transfers into.

## B.5. Discussion on discount factor $\gamma$ and temperature $\alpha$

We set the discount factor  $\gamma = 0.95$ , a standard choice in RL and IRL literature. For the mouse spontaneous behavior dataset, we also tested a smaller  $\gamma = 0.7$ , as previous literature Markowitz et al. (2023) suggested this value as optimal for the dataset. However, we observed that the results learned by SWIRL were highly similar for both discount factors, indicating that the choice of  $\gamma$  had minimal impact on performance in this case.

We searched for the optimal temperature  $\alpha$  in {0.01, 0.1, 0.5, 1}. For the labyrinth dataset, smaller values of  $\alpha$  led to better results for certain hidden modes. This observation aligns with the deterministic nature of behaviors in the labyrinth's tree-like structure. On the contrary, for the spontaneous behavior dataset, where animals exhibit more stochastic behavior patterns, we found higher values of  $\alpha$  were more appropriate.

## B.6. Discussion on the number of hidden modes Z and history length L

In this section, we discuss the selection and impact of the number of hidden modes  $Z = |\mathcal{Z}|$  and action-level history length L.

## B.6.1. Z in Labyrinth experiment

We evaluated the test LL of SWIRL models on Z from 2 to 5 and found that the best model (S-2) plateaus beyond Z = 4 (Fig. 5A). However, Z = 4 result does not differ much from the Z = 3 result: Z = 4 result mainly segments the explore



Figure 5. Water-restricted labyrinth experiment with different number of hidden modes Z. (A) Held-out test LL for each model across different number of hidden modes over 10 runs. The shaded area represents the total area that falls between one standard deviation above and below the mean. (B) Segments of a trajectory from held-out test data, predicted by SWIRL (S-2) with Z = 3 and Z = 4. The orange dot indicates when the mouse visits the water port, while the red cross denotes the mouse's visit to state 0 (home) at that time. (C) Inferred reward maps from SWIRL (S-2) with Z = 4: water, home, and two explore maps. To enhance visualization, the inferred reward  $r(s_t, s_{t-1})$  was averaged over  $s_{t-1}$  to produce  $r(s_t)$ .

mode of Z = 3 into two explore modes with similar reward maps (Fig. 5BC). As a result, we still present Z = 3 as the primary result for simplicity.

#### B.6.2. L in Labyrinth experiment

With Z = 3, we evaluated the test LL of SWIRL models on L from 1 to 4 and found that the L = 4 (S-4) provides the best test LL (Fig. 6A). L = 3 and L = 4 provide similar hidden segments and reward maps (when averaged over  $(s_{t-1}, ..., s_{t-L+1})$  to produce  $r(s_t)$ ) as L = 2 (Fig. 6BC). In the main paper, we present L = 2 (S-2) as the primary result as it has effectively demonstrated the benefits of incorporating non-Markovian action-level history dependency into SWIRL. However, we note that the test LL results in Fig. 6A suggest the presence of longer action-level history dependency (L > 2) in this labyrinth dataset. This observation aligns with the partially observable nature of this 127-node labyrinth: The mouse may not know the whole environment, so it likely relies on a longer history of prior states to guide its decision-making.

#### B.6.3. Z and L in mouse spontaneous behavior experiment

In the mouse spontaneous behavior experiment, we find that L = 1 (S-1) is the optimal choice, as L = 1 (S-1) consistently provides higher test log-likelihood (LL) compared to L = 2 (S-2) (Fig. 4B). Additionally, we select Z = 5 for the number of hidden modes since the test LL plateaus at Z = 5 (Fig. 4B).

#### **B.7. Robustness of SWIRL**

To assess the robustness of SWIRL, we evaluated the performance of SWIRL (S-2) under increasing levels of random perturbations in the simulated gridworld dataset.

Specifically, we introduced random permutations to a percentage of the states and actions in the training data, ranging from 0% to 50%. As expected, performance decreased as the level of permutation increased (Fig. 7). The model maintained high accuracy with less than 10% permutation. Between 10% and 30%, SWIRL demonstrated stable performance, achieving reasonable reward correlations and hidden mode segmentation accuracy despite the noise. Permutation beyond 30% led to very noisy data and it became hard for the model to maintain high performance.

These results suggest that SWIRL can tolerate moderate levels of noise or incomplete data, making it suitable for real-world



Figure 6. Water-restricted labyrinth experiment with different action-level history length L. (A) Boxplot showing held-out test LL over 10 runs, with the x-axis representing the four different models from L = 1 to L = 4. Outlier selection method is described in Appendix B.8. (B) Segments of a trajectory from held-out test data, predicted by the four SWIRL models. The orange dot indicates when the mouse visits the water port, while the red cross denotes the mouse's visit to state 0 (home) at that time. (C) Inferred reward maps from SWIRL (S-4): water, home, and explore. To enhance visualization, the inferred reward  $r(s_t, s_{t-1}, s_{t-2}, s_{t-3})$  was averaged over  $(s_{t-1}, s_{t-2}, s_{t-3})$  to produce  $r(s_t)$ .

animal behavior datasets where such challenges are common.



*Figure 7.* **SWIRL (S-2) experiment on 5 × 5 gridworld dataset with ten random permutations.** Box plots illustrating the Pearson correlation between the true and recovered reward maps, test log-likelihood, and test segmentation accuracy. The x-axis represents the percentage of states and actions permuted in the training data. Outlier selection method is described in Appendix B.8.

#### **B.8.** Outlier selection in box plot

All box plots in this paper are drawn by seaborn.boxplot() with its default outlier selection method. Specifically, the upper quartile (Q3), lower quartile (Q1), and interquartile range (IQR) are calculated. Values greater than Q3+1.5IQR or less than Q1-1.5IQR are considered as outliers.

## C. Appendix C

C.1. An example labyrinth trajectory



*Figure 8.* **Hidden mode segments in a labyrinth trajectory.** (A) Segments of a trajectory from held-out test data, predicted by SWIRL (S-2). The orange dot indicates when the mouse visits the water port, while the red cross denotes the mouse's visit to state 0 (home) at that time. (B) The segments of the trajectory shown in (A) are plotted within the labyrinth.

To further explore the hidden mode segments of the trajectory from held-out test data presented in Fig. 3E, we visualized the segments corresponding to each hidden mode in this trajectory in detail (Fig. 8B). The visualization reveals that "home" segments can remain valid even without a visit to state 0, as these segments often instead terminate at state 1 or state 2, which are next to state 0.

### **D.** Appendix D



D.1. Model-free SWIRL on a simulated gridworld environment

Figure 9. True and discovered reward maps in model-free SWIRL (S-2) simulation experiment. The color scale represents reward values ranging from 0 to 1. The home reward is defined as  $r(s_t)$ , while the water reward depends on both the current and previous locations,  $r(s_t, s_{t-1})$ . To present the water reward, each location is divided into five groups, as detailed in the table on the far right. For example, the polygon in the first row represents the reward value when  $s_t$  is the current location and  $s_{t-1}$  is the location to the right. Light grey indicates an impossible transition where no reward exists.

To demonstrate that SWIRL also supports model-free IRL, we replaced the model-based soft-Q iteration IRL approach used in main experiments with a model-free IRL method IQ-Learn (Garg et al., 2021). Garg et al. (2021) shows that we can convert the MaxEnt IRL objective  $L(\pi, r)$  with a convex reward regularizer to an offline inverse Q-learning objective:

$$\max_{Q} \mathcal{J}(Q) = \mathbb{E}_{(s,a,s') \sim \xi} [\phi(Q(s,a) - \gamma V(s'))] - \mathbb{E}_{(s,a,s') \sim \xi} [V(s) - \gamma V(s')]$$

with  $V(s) = \log \sum_{a} \exp Q(s, a)$ .  $\phi$  is the concave function from a convex conjugate. When using  $\chi^2$ -divergence,  $\phi(x) = x - \frac{x^2}{4}$ . The reward can be obtained as  $r(s, a) = Q(s, a) - \gamma \mathbb{E}_{s' \sim \mathcal{P}(\cdot|s, a)}[\log \sum_{a'} \exp Q(s', a')]$ . By marginalizing over actions, one can similarly obtain a state-only reward r(s).

Since optimizing the reward by maximizing  $\log \pi$  corresponds to the Lagrangian dual of the standard MaxEnt IRL approach (Zeng et al., 2022), we can maximize the IQ-Learn objective J(Q) instead of the  $\log \pi$  term in SWIRL EM auxiliary function (Eq. 3). Therefore, for a trajectory  $\xi$ , SWIRL can perform IRL with the following objective:

$$\max_{Q} \sum_{t=1}^{T} \sum_{z_{t}} p(z_{t}|\xi, \hat{\theta}) \left( \left[ \phi(Q_{z_{t}}(s_{t}^{L}, a_{t}) - \gamma V_{z_{t}}(s_{t+1}^{L})) \right] - \left[ V_{z_{t}}(s_{t}^{L}) - \gamma V_{z_{t}}(s_{t+1}^{L}) \right] \right)$$

with  $V_{z_t}(s^L) = \log \sum_a \exp Q_{z_t}(s^L, a)$ .

We tested this IQ-Learn-based, model-free SWIRL (S-2) on simulated trajectories in the same 5x5 gridworld environment as Sec. 4.1. The recovered reward maps achieved a Pearson correlation of 0.737 relative to the true reward maps. Although the model-free SWIRL recovered reward maps (Fig. 9) appear noisier than those from the model-based approach in Sec. 4.1 (Fig. 2A), they still accurately capture the critical high-reward regions.