# Cache & Distil: Optimising API Calls to Large Language Models

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#### Abstract

 Large-scale deployment of generative AI tools often depends on costly API calls to a Large Language Model (LLM) to fulfil user queries. To curtail the frequency of these calls, one can employ a smaller language model – a *student* – which is continuously trained on the responses of the LLM. This student gradually gains profi- ciency in independently handling an increasing number of user requests, a process we term *neural caching*. The crucial element in neural caching is a policy that decides which requests should be processed by the student alone and which should be redirected to the LLM, subse- quently aiding the student's learning. In this study, we focus on classification tasks, and we **consider a range of classic Active Learning-** based selection criteria as the policy. Our ex- periments suggest that Margin Sampling and **Query by Committee bring consistent benefits**  over other policies and baselines across tasks and budgets.

## 022 1 **Introduction**

 Large Language Models (LLMs) offer unique capa- bilities in understanding and generating human-like text. They have gained widespread use in a wide range of applications, such as assistive tools and en- tertainment bots. However, large models are often very challenging for all but a few companies and [i](#page-10-0)nstitutions to run on their infrastructure [\(Schwartz](#page-10-0) [et al.,](#page-10-0) [2020\)](#page-10-0). Meanwhile, smaller models typi- cally under-perform in these applications, at least without additional fine-tuning on task-specific la- belled data. Consequently, many applications ac- cess LLMs via commercial APIs despite the costs involved and the exposure of their entire request stream to the API providers.

 To minimise the costs and data exposure asso- ciated with calling the API, we propose to train a smaller language model, which we refer to as *student*, on the LLM's predictions and, as the stu-dent gets more accurate, it handles an increasing

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Figure 1: Neural caching (one iteration): A student generates a response to a user request. The policy algorithm determines whether to rely on the student's response or to call an LLM. LLM responses are stored and used to re-train the student as more data becomes available.

number of requests. The knowledge of the LLM **042** gets continuously distilled into the smaller model. **043** We refer to this scenario as *neural caching* (see 044 Figure [1\)](#page-0-0), as the student can be thought of as a  $045$ smart cache. Note though that the student not only 046 remembers what the LLM predicted but also gen- **047** eralises beyond these examples. The goal of this **048** paper is to formalise the neural caching problem **049** and investigate simple ways of approaching it. **050**

The key element in the neural caching scenario is **051** the policy determining which requests the student **052** processes independently. A good policy should **053** weigh the expected immediate user benefit (i.e., 054 if the LLM is substantially more likely to make **055** a correct prediction than the student) and the an- **056** ticipated benefit for the student (i.e., whether the **057** LLM's prediction will aid in training the student). **058** The latter underscores its relationship with Active **059** Learning (AL, [Settles,](#page-10-1) [2009;](#page-10-1) [Zhan et al.,](#page-10-2) [2022\)](#page-10-2), **060** although AL is typically associated with solicit- **061** ing human annotations. In particular, there is a **062** similarity to online AL [\(Cacciarelli and Kulahci,](#page-8-0) 063 [2023\)](#page-8-0), where new unlabelled data points arrive in **064**

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 a stream and are discarded immediately or sent to an annotator. However, online AL tends to focus on maximising the accuracy of the final model (i.e. student in our terminology). In contrast, what mat- ters in neural caching is the accuracy of the joint 070 system (student, teacher, along with the policy) over its lifetime since this *online accuracy* reflects the average level of service offered to a user.

 Despite the aforementioned differences with AL, evaluating the existing AL algorithms – specifically the example selection criteria – remains valuable given the maturity of the AL field and the ease of implementation of some of the AL methods. This study aims to achieve this, as well as to investigate the potential shortcomings of these methods. For instance, will the AL methods end up selecting ex- amples that are too challenging even for the LLM? Would learning from these noisy examples be detri- mental to the student? Answering these questions can inform future research on this practically sig-nificant scenario.

 In this work, our focus is specifically on clas- sification tasks, as opposed to free text genera- tion. Many practical problems, such as routing user requests to relevant departments or answering questions about factual knowledge, can be framed as classification tasks. By confining our focus to classification, we can apply methods developed in AL without modification. This also allows us to circumvent additional challenges tied to the auto- [m](#page-8-1)atic evaluation of text generation [\(Celikyilmaz](#page-8-1) [et al.,](#page-8-1) [2020\)](#page-8-1).

 Our findings reveal the benefits of using AL- [b](#page-9-0)ased policies such as Margin Sampling [\(Scheffer](#page-9-0) [et al.,](#page-9-0) [2001\)](#page-9-0) and Query by Committee [\(Seung et al.,](#page-10-3) [1992\)](#page-10-3). Across datasets and budgets, these methods consistently outperform baselines, such as routing examples randomly or training the student at the very start. Our analysis also reveals that the stu- dent appears robust to the noise introduced by an LLM. We also analyse a simplified practical sce- nario where the student is not retrained and observe even greater improvements in online accuracy from using AL-based policies. We release our code to encourage further work on this problem.<sup>[1](#page-1-0)</sup>

**110** The key contributions of this work are:

**111** • We formulate the *neural caching* problem as **112** a powerful extension of using static caches. **113** In neural caching, LLM calls are optimised, while the student model is periodically retrained on the labels. We believe online **115** Knowledge Distillation could play a key role **116** in saving calls to expensive models. **117**

- We release a benchmark with LLM annota- **118** tions for classification tasks to facilitate future **119** research in this setup. **120**
- We evaluate and analyse different instance se- **121** lection criteria for the neural caching setup. **122**
- Our findings reveal that AL-based selection **123** criteria consistently improve performance **124** over baseline methods across various budgets **125** and datasets. **126**

## 2 Related Work **<sup>127</sup>**

Active Learning. Active Learning (AL) seeks **128** to reduce the amount of manual data annotation **129** needed. To accomplish this, it selects the most in- **130** formative examples from unannotated data. These **131** datapoints are then presented to an annotator and **132** the labels are subsequently used to train a model. **133** The most common scenario for AL is pool-based, **134** where a large unlabelled dataset is available from 135 the start and then a subset of examples is selected **136** for labelling. There has been extensive work on **137** applying pool-based techniques to NLP tasks, es- **138** pecially for classification problems [\(Settles,](#page-10-1) [2009;](#page-10-1) **139** [Zhan et al.,](#page-10-2) [2022;](#page-10-2) [Zhang et al.,](#page-10-4) [2022\)](#page-10-4). **140**

Online Active Learning. In single-pass online **141** AL [\(Cacciarelli and Kulahci,](#page-8-0) [2023\)](#page-8-0), access to a **142** large unlabelled dataset is not available. Instead, **143** we are given one unlabelled instance at a time and **144** need to decide at that time whether to request an- **145** notation. Online AL was initially motivated by **146** scenarios in which an instance would not be avail- **147** able for annotation at a later time, such as in defect **148** detection or medical applications, where an item **149** might get shipped or the patient becomes unavail- **150** able [\(Riquelme,](#page-9-1) [2017\)](#page-9-1). Online AL tends to focus **151** on the final accuracy of the model, rather than the **152** online accuracy of the student and teacher com- **153** bined, the measure more suitable for our scenario. **154**

Knowledge Distillation of LLMs. Knowledge **155** distillation (KD), i.e., training a smaller model to **156** mimic a larger one, has garnered substantial atten- **157** tion [\(Bucila et al.,](#page-8-2) [2006;](#page-8-2) [Hinton et al.,](#page-9-2) [2015\)](#page-9-2). The **158** class of methods most closely related to ours is ac- **159** [t](#page-9-3)ive KD, which effectively applies AL to KD [\(Liang](#page-9-3) **160**

<span id="page-1-0"></span><sup>1</sup> [https://anonymous.4open.science/r/neural-caching-](https://anonymous.4open.science/r/neural-caching-780F/README.md)[780F/README.md](https://anonymous.4open.science/r/neural-caching-780F/README.md)

 [et al.,](#page-9-3) [2021;](#page-9-3) [Xu et al.,](#page-10-5) [2023;](#page-10-5) [Baykal et al.,](#page-8-3) [2023\)](#page-8-3). Similar to AL, the emphasis is placed on the pool- based setting, as opposed to the online setting, with a particular focus on optimising the final accuracy of the student model, rather than online accuracy as needed for our use case.

 Optimisation of Commercial LLM API Calls. Due to the high cost of commercial LLM APIs, sev- eral works have explored methods to reduce or oth- erwise optimise the cost of API calls. GPTCache [\(Bang,](#page-8-4) [2023\)](#page-8-4) relies on a vector store of past query embeddings and retrieves their associated labels. It shares similarities with the Coreset version of our approach – which emerged as the weakest method in our experiments. FrugalGPT [\(Chen et al.,](#page-8-5) [2023\)](#page-8-5) implements a cascade of commercial LLMs, where bigger models are only called if the response from a cheaper model is deemed as too unreliable by a scorer that was trained with in-domain data. In contrast, in this work, we do not assume access to gold data to train a scorer. [Zhu et al.](#page-10-6) [\(2023\)](#page-10-6) present a method to allocate queries among multiple mod- els, together with traditional caching, in a scenario with highly repetitive queries. [Šakota et al.](#page-10-7) [\(2023\)](#page-10-7); [Shnitzer et al.](#page-10-8) [\(2023\)](#page-10-8) optimise routing calls through models by predicting their respective performance. Our work deviates from all these as we propose to use continuous KD in a student model.

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Concurrent work of [Stogiannidis et al.](#page-10-9) [\(2023\)](#page-10-9) [2](#page-2-0) also presents a calling strategy that leverages KD to reduce API calls to an LLM. Unlike our pa- per, which offers a systematic analysis of existing AL criteria, their work concentrates on a specific model design. This design resembles a hybrid of our Coreset and Prediction Entropy, which do not perform well in our experiments. Even more signif- icantly, their method's advantages are only shown in comparison to a scenario where no student model is used. This overlooks trivial baselines of front- loading and random allocation, both of which have shown hard to beat in our experiments. They also use very simple student models (kNN or a non- pretrained MLP versus our smaller pretrained LM), whose relative success may be attributed primarily to the simplicity of the two datasets in their study, which do not necessitate generalisation beyond the teacher model's predictions.

## <span id="page-2-0"></span><sup>2</sup>Made public on the same day as ours.

## <span id="page-2-1"></span>3 The Neural Caching Problem **<sup>208</sup>**

The objective of neural caching is to optimise the **209** usage of an LLM in a scenario where labels need **210** to be generated for a stream of inputs. As we get **211** more predictions from the LLM, a student model is **212** trained on them. Our goal is to achieve the highest **213** level of service possible within a set budget of LLM **214** calls; hence, calling the LLM serves both to attain **215** high accuracy for the incoming input as well as to **216** train a student model. **217**

To put it formally, our goal is to establish a map- **218** ping between elements in the input space  $\chi$  and the **219** corresponding labels in the space Y. We start with **220** a student model  $S_0$ , and we can access a teacher **221** model  $T$  on demand. Our task is to predict labels  $222$ for a sequence of *n* examples  $(x_1, \ldots, x_n) \stackrel{\text{iid}}{\sim} \mathcal{X}$ . 223

We retrain the student model on the labels ob- **224** tained from the LLM every *f* processed requests. **225** This simulates the situation where the number of re- **226** quests is uniform in time, and there is a set time to **227** retrain the model, e.g. at night. For simplicity and **228** to follow the convention in AL to retrain the model **229** from scratch [\(Ren et al.,](#page-9-4) [2022\)](#page-9-4), every time we re- **230** train the student model, we reset it to the original **231** pre-trained model and then use parameter-efficient **232** fine-tuning. Although continual learning methods **233** [c](#page-10-10)ould be employed [\(Biesialska et al.,](#page-8-6) [2020;](#page-8-6) [Zhou](#page-10-10) **234** [and Cao,](#page-10-10) [2021\)](#page-10-10), we believe this is largely orthogo- **235** nal to our primary focus on policies and resetting **236** enhances the reproducibility of our analysis. Im- **237** portantly, we do not assume access to ground truth **238** (or human annotation) at any point in learning to **239** simulate a fully automatic scenario. **240** 

For every new input  $x_i$ , we use the student model 241  $S_{i/f}$  to obtain the predicted label  $\hat{y}_i^S$ . Then, we 242 have the option to request the label  $\hat{y}_i^{\mathcal{T}}$  from the **243** teacher model (LLM), which incurs a cost of  $c(x_i)$ . 244 Finally, we return the label  $\hat{y}_i$  for  $x_i$ : the teacher's 245 label if requested or the student's otherwise. **246**

The processing of the *n* examples is subject to 247 a budget constraint, where the total cost must not **248** exceed a fixed budget *b*. We assess the effective- **249** ness of our querying strategy based on the accuracy **250** of our predicted label  $\hat{y}_i$  compared to the actual 251 label *y<sup>i</sup>* (*online accuracy*) on the online examples. **<sup>252</sup>** Additionally, we measure the accuracy of the final **253** student model  $S_{n/f}$  on a test dataset (*final accu*-254 *racy*). Algorithm [1](#page-3-0) describes the process. **255**

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Algorithm 1: Pseudo-code for the neural caching algorithm with budget *b*, retraining frequency *f*, cost per query *c*, data from the LLM  $\mathcal{D}_{\text{LLM}}$  and an initial student  $\mathcal{S}_0$ 

<span id="page-3-0"></span> $\mathcal{D}_{\text{online}} = \emptyset$ for  $x_i$  in  $X_{\text{online}}$  do if  $i \mod f = 0$  then  $S_{i/f} = \text{Train}(\mathcal{D}_{\text{LLM}})$ end  $\hat{y}_i = \mathcal{S}_{i/f}(x_i)$ if Call\_LLM(*b*,  $x_i$ ,  $\hat{y}_i$ ) and  $b \ge c(x_i)$ then  $\hat{y}_i = \text{LLM}(x_i)$  $b = b - c(x_i)$  $\mathcal{D}_{\text{LLM}} = \mathcal{D}_{\text{LLM}} \cup \{\langle x_i, \hat{y}_i \rangle\}$ end  $\mathcal{D}_{\text{online}} = \mathcal{D}_{\text{online}} \cup \{\langle x_i, \hat{y}_i \rangle\}$ end  $\mathcal{D}_{\text{test}} = \{ \langle x_j, \mathcal{S}_{i/f}(x_j) \rangle \mid x_j \in X_{\text{test}} \}$  $Acc<sub>online</sub> = Evaluate(D<sub>online</sub>)$  $Acc<sub>final</sub> = Evaluate(D<sub>test</sub>)$ 

## **256** 3.1 Instance Selection Criteria

 We use classical instance selection criteria from AL for the neural caching problem. We use the term *selecting an instance* to denote using the LLM to annotate that example.

 Front-loading (FR) This simple approach in- volves using the entire budget initially by selecting all instances for LLM annotation. Once the bud- get is used up, subsequent requests are handled by the student model alone. As the examples are i.i.d. in our experiments, this strategy has the same expected *final accuracy* as random selection.

 Margin Sampling (MS) MS [\(Scheffer et al.,](#page-9-0) [2001;](#page-9-0) [Luo et al.,](#page-9-5) [2004\)](#page-9-5) selects examples with high margin between the top two predictions made by the student model

$$
\begin{aligned}\n\text{Margin}(x_i) &= \log P(y_i = k_1^* \mid x_i) \\
&\quad - \log P(y_i = k_2^* \mid x_i)\n\end{aligned}\n\tag{1}
$$

273 where  $k_1^*$  and  $k_2^*$  are the first and second most likely labels, respectively, according to the distribution  $P(y_i | x_i)$  computed by the student model. This [i](#page-9-6)s a popular selection criterion for AL [\(Roth and](#page-9-6) [Small,](#page-9-6) [2006;](#page-9-6) [Balcan et al.,](#page-8-7) [2007\)](#page-8-7). [Schröder et al.](#page-10-11) [\(2022\)](#page-10-11) evaluated different uncertainty-based strate- gies with Transformer models [\(Devlin et al.,](#page-8-8) [2019\)](#page-8-8) and found MS to be the best-performing one in an offline, pool-based setting. To adapt MS – as **281** well as the other criteria – to an online setting as **282** a selection policy, we define a threshold, and only **283** examples with a margin above this threshold are **284** selected until the budget is exhausted. We refer to **285** Appendix [A.1](#page-11-0) for more details. **286** 

[P](#page-10-12)rediction Entropy (PE) In PE [\(Schohn and](#page-10-12) **287** [Cohn,](#page-10-12) [2000;](#page-10-12) [Roy and McCallum,](#page-9-7) [2001\)](#page-9-7), we select **288** instances with high entropy of the output distribu- **289** tion: **290**

Entropy
$$
(x_i)
$$
 =  
 
$$
-\sum_j P(y_i = k_j^* | x_i) \log P(y_i = k_j^* | x_i)
$$
 (2)

(2) **291**

[Q](#page-10-3)uery by Committee (QBC) In QBC [\(Seung](#page-10-3) **292** [et al.,](#page-10-3) [1992;](#page-10-3) [Burbidge et al.,](#page-8-9) [2007\)](#page-8-9), we select in- **293** stances relying on the disagreement among a com- **294** mittee of models. Our committee is the set of  $d = 4$  295 previous student models plus the current – presum- **296** ably best – student. The disagreement is quantified **297** by computing the proportion of committee mem- **298** bers contradicting the current student. **299**

Coreset (CS) CS [\(Sener and Savarese,](#page-10-13) [2018\)](#page-10-13) **300** uses an encoder to obtain the embedding repre- **301** sentation of the new instance. Then, it calculates **302** the cosine similarity between the embedding of the **303** new input and the embeddings of past examples. **304** If the similarity with respect to the most similar **305** past instance  $x_i$  annotated by the LLM is below a  $306$ certain threshold *s*, then it requests further annota- **307** tion from the LLM. To obtain the embeddings, we **308** average the encoder representation across tokens, **309** as this has been proven effective in sentence em- **310** bedding benchmarks [\(Ni et al.,](#page-9-8) [2022\)](#page-9-8). Similarity **311** with previous examples has been employed in AL 312 to encourage diversity and coverage [\(Kim et al.,](#page-9-9) **313** [2006;](#page-9-9) [Zeng et al.,](#page-10-14) [2019\)](#page-10-14). GPTCache [\(Bang,](#page-8-4) [2023\)](#page-8-4) **314** also uses the embedding representations to decide **315** whether an incoming instance should be labelled. 316

## **4 Experimental Setup** 317

#### 4.1 Datasets **318**

We study the proposed setup on four classification 319 tasks. The first two tasks have been commonly **320** studied in AL for NLP: ISEAR [\(Shao et al.,](#page-10-15) [2015\)](#page-10-15) **321** and RT-Polarity [\(Pang and Lee,](#page-9-10) [2005\)](#page-9-10). The remain- **322** ing two tasks showcase harder problems where **323** factual knowledge acquired during pre-training **324** of an LLM could be highly beneficial: the fact- **325** checking dataset FEVER [\(Thorne et al.,](#page-10-16) [2018\)](#page-10-16) **326**

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		<b>ISEAR RT-Polarity FEVER Openbook</b>		
Accuracy, T5+LoRA (100 gold labels)	0.51	0.85	0.53	0.23
Accuracy, T5+LoRA (5000 gold labels)	0.67	0.90	0.74	0.68
Accuracy, LLM	0.68	0.91	0.78	0.80
Average margin (LLM labels)	10.0	15.4	9.2	10.3
Average margin when wrong (LLM labels)	4.2	10.3	69	5.3

Table 1: The accuracy of the LLM is similar to training the simple model with 5000 gold labels.

 [a](#page-9-11)nd the question-answering dataset Openbook [\(Mi-](#page-9-11) [haylov et al.,](#page-9-11) [2018\)](#page-9-11). We split all datasets into online and test portions (80%-20%, except for Openbook, as it has fewer samples). The datasets are balanced.

**331 ISEAR [\(Shao et al.,](#page-10-15) [2015\)](#page-10-15)** annotates personal **332** reports for emotion (classes: *joy*, *fear*, *shame*, *sad-***333** *ness*, *guilt*, *disgust*, *anger*; 7666 examples).

**334** RT-Polarity [\(Pang and Lee,](#page-9-10) [2005\)](#page-9-10) provides sen-**335** timent polarity labels for movie reviews (classes: **336** *positive*, *negative*; 10662 examples).

 **FEVER [\(Thorne et al.,](#page-10-16) [2018\)](#page-10-16)** is a fact-checking dataset (classes: *true*, *false*; 6612 examples) with claims that can be checked with 1-3 sentences from Wikipedia.

 Openbook [\(Mihaylov et al.,](#page-9-11) [2018\)](#page-9-11) is a challeng- ing question-answering dataset modelled after open book exams for assessing human understanding of a subject. Each instance consists of a multiple choice question (classes: *A*, *B*, *C*, *D*) and includes one fact that can help answer it. The full dataset consists of 5957 data points; we selected 5457 for the online set and 500 for testing.

## **349** 4.2 Annotation by LLM

 While we are interested in the online caching sce- nario, to facilitate comparisons between our meth- ods and ensure replicability in future work, we create a dataset in which we obtain LLM predic- tions for all data points; this dataset is then used to simulate the online setup.

 We generate soft labels using OpenAI's text-davinci-003, an InstructGPT-based model [\(Zhan et al.,](#page-10-2) [2022\)](#page-10-2). For each task, we design a prompt that describes the task and the possible classes. Our prompts do not contain any in-context examples (zero-shot), but we use a small part of the dataset (up to 10 examples) for prompt engineering.

On all datasets, we observe that the LLM **364** achieves better accuracy than the smaller model **365** trained on 5000 gold labels, suggesting that KD **366** would be useful in these datasets (Table [1\)](#page-4-0). In our **367** benchmark, we store the log-probabilities of the **368** labels. We note that the average margin for the **369** generated labels is substantially lower when the **370** predicted label is wrong; we observe with addi- **371** tional experiments that the LLM annotations are **372** well calibrated (Figure [4\)](#page-6-0). We release our bench- **373** mark with the generated labels to encourage further **374** work on the neural caching problem. **375** 

#### 4.3 Experiment Details **376**

We run all our experiments with three random  $377$ seeds, which also determine the ordering of ex- **378** amples; we present the average scores. For sim- **379** plicity, we use a retraining frequency  $f = 1000$  380 and a constant cost per query  $c(x_i) = 1$ . To avoid 381 a cold-start, we train the initial student model  $S_0$  382 with  $N = 100$  (ISEAR, RT-Polarity) or  $N = 1000$  383 (FEVER, Openbook) data points from the LLM; **384** we choose *N* so that  $S_0$  is better than random 385 [c](#page-9-12)hoice. For the student model, we use *T*5*base* [\(Raf-](#page-9-12) **<sup>386</sup>** [fel et al.,](#page-9-12) [2020\)](#page-9-12) as the backbone model; we freeze **387** the model weights and add LoRA adapter layers for **388** a parameter-efficient fine-tuning [\(Hu et al.,](#page-9-13) [2022\)](#page-9-13). **389**

We fine-tune the student model with the cross- **390** entropy loss using the log-probabilities assigned by **391** the teacher to each class. Using hard labels seems **392** to work almost as well (Table [9\)](#page-13-0). We split the **393** accumulated data from the LLM into training and **394** validation sets, and train each student from scratch **395** for 30 epochs with early stopping with patience of **396** five epochs. The rest of the hyperparameters can **397** be found in Appendix [A.](#page-11-1) **398**

## 5 Experiments **<sup>399</sup>**

We first present our results and then their analysis. 400 To report accuracy across budgets, we use the cor- **401** responding Area Under the Curve (AUC) divided **402**

<span id="page-5-0"></span>

	<b>ISEAR</b>	<b>RT-Polarity</b>	FEVER	<b>Openbook</b>	Average
Random	0.640	0.886	0.704	0.662	0.723
Margin Sampling	0.666	0.896	0.725	0.703	0.748
<b>Ouery by Committee</b>	0.656	0.889	0.725	0.687	0.739

Table 2: Online accuracy (AUC) for neural caching with no student retraining.

**403** by the budget range, thus obtaining an average ac-**404** curacy.

## <span id="page-5-1"></span>**405** 5.1 Neural Caching without Student **406** Retraining

 We first study a simplified version of neural caching, where the student model is not retrained on new data points. This is a practical scenario, as retraining creates extra overhead for the application provider (e.g., consider a setting where the student is run on a portable device, which is not powerful enough to support retraining).

 We adapt the AL instance selection criteria in the following way. Given a criterion *C*, we calculate the respective values from the previous outputs of the student and call this list the history  $\hat{C}$ . If we have a remaining budget *b* and *n* remaining online instances, we use as a threshold for an incoming **instance the**  $\frac{b}{n}$ **-th percentile of the history**  $\hat{C}$ **. The**  best possible scenario would imply having oracle threshold values for each budget (i.e. as if we had access to the full dataset offline). However, in additional experiments, we found that the above rule yields very similar scores.

 To use QBC in this setup, we simulate that we have four previous students trained on subsets of the data. For example, if the student is trained **on**  $N = 1000$  examples, the previous students are trained on 900, 800, 700, and 600 data points, respectively. We find that MS yields results very similar to PE and that Coreset is similar to Random. To ease visualising the results, here we omit PE and **434** Coreset.

 Table [2](#page-5-0) and Figure [2](#page-6-1) contain the results when 436 we train the initial student with  $N = 1000$  dat- apoints annotated by the LLM. Our experiments with different initial budgets *N* yield similar re- sults (Table [8](#page-12-0) in Appendix), and Coreset performs poorly even with different encoders.

 We find that MS and PE are the best-performing methods on all datasets and across all the initial student models, followed by QBC, which outper- forms the baseline of random selection. Given the simplicity of these methods, these results make a strong case for using AL-based selection methods, **446** especially MS. Unlike QBC, MS does not require **447** storing multiple models and performing inference **448** with each of them.

### <span id="page-5-2"></span>5.2 Neural Caching with Student Retraining **450**

We now turn to the complete setup proposed in  $451$ Section [3,](#page-2-1) in which the selected instances are used **452** to retrain a student model with some periodicity. **453** This creates the incentive to spend the budget early **454** to get a more proficient student model as soon as **455** possible. To observe this effect, we include a ran- **456** dom baseline with a uniform sampling rate. This **457** suggests waiting longer for informative examples **458** to arrive counterweights the benefits of getting a **459** strong student as quickly as possible. We select 460 thresholds to encourage spending more of the bud- **461** get early on (see Appendix [A.1\)](#page-11-0). **462**

We show the results averaged across all datasets **463** in Figure [3](#page-6-2) and per-dataset in Figure [5.](#page-13-1) We observe **464** that both MS and QBC substantially outperform the **465** other methods. Coreset (embedding-based) does **466** badly in all the studied setups and encoders (Ta- **467** ble [11\)](#page-14-0). Table [3](#page-6-3) summarises the results. **468**

### 5.3 Analysis **469**

Hard examples with noisy labels. We have ob- **470** served in our experiments that prioritising harder **471** instances for teacher annotation leads to clear gains **472** in online accuracy. However, as discussed in the **473** introduction, LLM accuracy may be significantly **474** affected by the increased 'complexity' of an ex- **475** ample, which can inflate the proportion of noisy **476** annotations in the data on which the student is **477** trained (see Figure [4\)](#page-6-0). This problem is known in **478** [K](#page-9-14)D as *confirmation bias* [\(Arazo et al.,](#page-8-10) [2020;](#page-8-10) [Liu](#page-9-14) **479** [and Tan,](#page-9-14) [2021\)](#page-9-14). Previous results from offline KD **480** suggest that this type of confirmation bias can be **481** [m](#page-8-3)itigated by avoiding the hardest instances [\(Baykal](#page-8-3) **482** [et al.,](#page-8-3) [2023\)](#page-8-3), improving the chances that the teacher **483** model makes a correct prediction. However, we **484** observe that the most significant advantage of the **485** LLM with respect to the student in terms of accu- **486** racy lies in these samples that are deemed hard by **487** the student (leftmost part of the plot in Figure [4\)](#page-6-0); **488** since we are optimising the online accuracy, the **489** trade-off between providing hard or correct labels **490** may be different in our online case than in the of- **491** fline scenario. Given the above, we hypothesise **492** that MS and QBC would be more negatively af- **493** fected by the confirmation bias than front-loading, **494** which does not prioritise hard examples. To test 495

<span id="page-6-1"></span>

ISEAR RT-Polarity FEVER Openbook Average Random 0.614 0.872 0.723 0.703 0.728 Front-loading 0.637 0.879 0.734 0.731 0.745 Coreset 0.637 0.878 0.715 0.726 0.739 Entropy 0.657 0.886 0.728 0.693 0.741 Margin Sampling 0.658 0.889 0.753 0.726 0.757 Query by Committee 0.650 0.887 0.748 0.737 0.755

<span id="page-6-3"></span>Figure 2: Accuracy curve with respect to budgets for neural caching without student retraining.

Table 3: Online accuracy (AUC) for neural caching with student retraining.

<span id="page-6-2"></span>

Figure 3: Accuracy curve with respect to budgets, in the neural caching problem with student retraining. Error lines indicate variance.

<span id="page-6-0"></span>

Figure 4: On the left, we order data points by their margin and plot the accuracy of their respective labels generated by the student and teacher. We observe that the greatest advantage of using the labels from the teacher comes from examples with small margins. On the right, the accuracy of the labels generated by the LLM calls in neural caching with no student retraining. We observe that MS and QBC are more likely to generate wrong labels. We focus on Openbook for both plots.

this hypothesis, we designed an experiment to put **496** an upper bound on the effect of wrong LLM annota- **497** tions. For each strategy, we only retrain the student **498** model on correct labels, simulating an oracle that **499** discards incorrect examples. Table [5](#page-7-0) shows the **500** absolute improvements in the online and final accu- **501** racy with respect to the values obtained without the **502** oracle (Table [3](#page-6-3) and [4\)](#page-7-1). We observe moderate abso- **503** lute improvements, but surprisingly MS and QBC **504** do not seem to improve more than front-loading, **505** suggesting that the hypothesis is wrong and that the **506** impact of confirmation bias is somewhat limited **507** and - what is surprising - similar across strategies. **508**

As an additional test, we analyse the subset of 509 test examples where the teacher is incorrect. If **510** confirmation bias is a major issue for MS and QBC **511** than for front-loading, we would expect that they **512** are more prone to reproducing the teacher's errors. **513** Again, we do not find any substantial differences **514** between these two strategies vs front-loading (Ta- **515** ble [10\)](#page-14-1). 516

**Online accuracy vs. final accuracy.** Taking a 517 look at the accuracy of the final student (Table [4\)](#page-7-1), **518** we observe that it is generally consistent with the  $519$ online accuracy (Table [3\)](#page-6-3). However, MS has a low **520** *final* accuracy on FEVER while having the best **521** *online* accuracy on that dataset, confirming that in **522** some tasks, calling the LLM to obtain labels for **523** hard examples may improve the online accuracy **524** while not necessarily improving the student. This  $525$ result emphasises the differences between our set- **526**

<span id="page-7-1"></span>

	<b>ISEAR</b>	<b>RT-Polarity</b>	<b>FEVER</b>	<b>Openbook</b>	Average
Front-loading	0.598	0.879	0.686	0.647	0.702
Coreset	0.599	0.879	0.680	0.641	0.700
Entropy	0.608	0.885	0.682	0.647	0.705
<b>Margin Sampling</b>	0.609	0.884	0.678	0.634	0.701
Query by Committee	0.609	0.882	0.687	0.646	0.706

Table 4: Final accuracy (AUC) of the last student model for neural caching with student retraining.

<span id="page-7-0"></span>

	$\Delta$ Online $\Delta$ Final	
Front-loading	0.009	0.019
<b>Margin Sampling</b>	0.008	0.022
Query by Committee	0.008	0.018

Table 5: Absolute improvements for the online and final accuracy using an oracle that allows us to discard instances with wrong labels from the LLM, averaged across datasets. The improvements are with respect to values from Table [3](#page-6-3) and [4.](#page-7-1)

<span id="page-7-2"></span>

	<b>Openbook</b>			<b>FEVER</b>		
		$N=1000$ $N=2000$ $N=3000$ $N=500$ $N=1000$ $N=1500$				
Front-loading	0.731	0.769	0.751	0.716	0.734	0.734
Margin Sampling	0.726	0.777	0.764	0.718	0.753	0.751
<b>Ouery by Committee</b>	0.737	0.786	0.779	0.722	0.748	0.755

Table 6: Online accuracy (AUC) of different selection criteria with different initial student models  $S_0$ .

**527** up and the setting normally studied in AL.

#### **528** 5.4 Robustness of the Findings

**Vary initial training**  $(S_0)$ **.** We study the effect of the quantity of LLM-annotated data on which the first student model is trained, focusing on the setup with retraining (Table [6\)](#page-7-2). We consider the two more challenging tasks, FEVER and Openbook. We find that QBC performs best overall, and the performance of MS is more sensitive to the initial budget. This observation suggests that better deci- sion criteria for transitioning from a front-loading regime to MS can be beneficial; we leave this for future exploration.

 Higher retraining frequency *f*. We repeat neu- ral caching experiments, setting this time a higher frequency of retraining  $f = 100$ ; this results in much longer runs as the student model has been retrained an order of magnitude more times. Ta- ble [7](#page-7-3) shows the results. We observe that results are consistent and very similar to those with a lower frequency of retraining (Table [3\)](#page-6-3).

<span id="page-7-3"></span>

Table 7: Online accuracy (AUC) for neural caching with retraining frequency  $f = 100$ .

### 6 Conclusions **<sup>548</sup>**

In this work, we have studied how instance selec- **549** tion criteria from AL behave when they are used **550** to decide in real time whether we should perform **551** an LLM call or use a student model that has been **552** trained on previous LLM predictions. In the sce- **553** nario where we are not retraining the student model, **554** Margin Sampling performs the best, across differ- **555** ent datasets. In the scenario where we retrain the **556** student model with some time periodicity, Query **557** by Committee is the most robust option. In our ex- **558** periments we observe that, while Margin Sampling **559** outperforms the front-loading baseline on harder **560** tasks, it is more sensitive to the initial budget spent **561** to train the student model  $S_0$ .  $562$ 

We find that the embedding-based strategy (Core- **563** set) consistently performs poorly across different **564** encoders; it is the only LLM caching approach **565** which is known to be adopted by practitioners (e.g., 566 GPTCache [\(Bang,](#page-8-4) [2023\)](#page-8-4)). We believe these types **567** of strategies could be useful in certain contexts, e.g. **568** multiple near-identical calls to an LLM, a scenario 569 which has not been the focus of this work.<sup>[3](#page-7-4)</sup>

Our results suggest that (i) there is room for **571** smart LLM query allocation in the context of con- **572** tinuously distilling an LLM into a student model **573** and (ii) previous literature in Active Learning can **574** transfer well to this setup. We believe that online **575** Knowledge Distillation could play a key role in **576** caching LLMs and saving unnecessary calls to ex- **577** pensive models. **578**

**570**

<span id="page-7-4"></span><sup>&</sup>lt;sup>3</sup>FEVER does contain paraphrases or statements entailing each other but these constitute only a small fraction of the dataset.

# **<sup>579</sup>** Limitations

 Our experiments assume that there is no develop- ment set available for each task, which could help improve the results of non-baseline methods by in- troducing a task-specific hyperparameter for thresh-**584** olds.

 Our experiments refer to a particular configura- tion with one student model and one LLM. We leave for future work configurations with other models. We also leave for future work experiments on text generation, which would require using text-based AL criteria.

 In this work, we focused on a stationary (i.i.d.) stream of requests. In practice, the distribution of [r](#page-8-0)equests is likely to change over time [\(Cacciarelli](#page-8-0) [and Kulahci,](#page-8-0) [2023\)](#page-8-0). As suggested by the online AL literature [\(Bifet and Gavaldà,](#page-8-11) [2007\)](#page-8-11), this should further increase the gap between the AL-based ap- proaches and static strategies, e.g., front-loading. In those cases, we would expect improvements in both online and final accuracy.

 Ethics statement We anticipate that our pro- posed approach will be advantageous for smaller companies and will enhance user privacy by limit- ing the amount of data shared with API providers. However, we recognise the potential for misuse of this technology. For instance, it might contravene the service policies of API providers and poten- tially could decrease the revenue of creators if they are compensated for the usage of their content by the API provider. Furthermore, while the original model provided through the API may have been fine-tuned to diminish harmful biases and tailored for fairness across diverse user groups, there is a possibility that the student model derived through our process may not inherit these qualities.

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<span id="page-11-1"></span>

# **901 A** Experimental details and **<sup>902</sup>** hyperparameters

 Student model We use the T5 implementation from Huggingface's transformers library. We use LoRA adapters [\(Hu et al.,](#page-9-13) [2022\)](#page-9-13), as they have been considered one of the most parameter-efficient architectures in few-shot settings [\(Liu et al.,](#page-9-15) [2022\)](#page-9-15). Following [Ponti et al.](#page-9-16) [\(2023\)](#page-9-16), we add a LoRA adapter to the query, key, value and output weights in each self-attention layer of T5. We set the LoRA 911 rank to  $r = 16$ , and the scaling to  $\alpha = 0.25$ . **We use learning rate**  $\eta = 5 \cdot 10^{-4}$ , training batch 913 size  $m = 16$  and weight decay  $\lambda = 0.01$ . We validate this hyperparameter choice based on ex-

916 **Adaptation of strategies** For Entropy, we nor-**917** malise before computing it by applying a softmax **918** over the classes.

**915** periments using the soft labels from the teacher.

 **Reporting of results** In order to report accuracy across budgets, we use the corresponding Area Un- der the Curve (AUC) divided by the budget range. By budget range, we refer to the biggest budget minus the smallest one for that task. Intuitively, this gives us an average accuracy across budgets.

 Normalisation, pre-processing and evaluation We do not apply normalisation or pre-processing before using the T5 tokeniser. This can be con-sulted in our code.

# <span id="page-11-0"></span>**929** A.1 Threshold values

 To encourage an early expense of the budgets in the setting with student retraining, we have selected threshold values to ensure initially a higher propor-933 tion of calls for LLM annotation (PE=0.5, MS=5, **QBC=4, CS=0.9); we have selected these values**  so that the first student model selects at least 50% of instances for LLM annotation on RT-Polarity. However, we observe very similar results when we use the empirical threshold from Section [5.1.](#page-5-1)

# **939** A.2 Labels from the LLM

 We use a budget for LLM annotation of \$200. All the labels are obtained during May 2023. Since the OpenAI API can only return up to the five most 943 likely tokens, we add a bias  $b = 100$  to the tokens that represent each class:

- **945** ISEAR: ' *joy*', ' *fear*', ' *anger*', ' *sadness*', ' **946** *disgust*', ' *shame*', ' *guilt*'
- **947** RT-POLARITY: ' *positive*', ' *negative*'
- FEVER: ' *true*', ' *false*' **948**
- OPENBOOK: ' *A*', ' *B*', ' *C*', ' *D*' **949**

If a class is not among the five most likely tokens, **950** it gets assigned in our experiments a log probability **951** of -100. **952**

## A.3 Computational resources **953**

*T*5*base* has 220 million parameters. We addition- **<sup>954</sup>** ally added LoRA modules, which comprise 3.5 mil- **955** lion parameters. Only LoRA modules are trained, **956** making it a lightweight student overall. For our ex- **957** periments, we used clusters with NVIDIA Tesla **958** V100-SXM2-16GB and NVIDIA A100-SXM4- **959** 40GB. Runs with frequency *f*=100 take between 1 **960** and 4 hours to run.

# **B** Additional results **962**

# B.1 Neural caching with no student retraining **963**

We observe that Margin Sampling is the best- **964** performing method on all datasets and across all **965** the initial student models, followed by Query by **966** Committee and outperforming the baseline of ran- **967** dom selection (Table [8\)](#page-12-0). The gap between Margin **968** Sampling and the baseline widens as we have a **969** better initial student. 970

# **B.2 Neural caching with retraining <b>971**

Figure [5](#page-13-1) shows the online accuracy per-dataset in **972** the setup with retraining of the student. **973**

# **B.3** Soft labels **974**

We conduct experiments to study the effect of us- **975** ing soft labels (using the logprobabilities for each **976** class from the LLM) or hard labels (only using the **977** first class from the LLM). To do this, we train a **978** student model on multiple budgets and obtain the **979** final accuracy. We observe this has some gains in **980** FEVER (Table [9\)](#page-13-0). **981**

# B.4 Effect of confirmation bias in neural **982 caching with retraining <b>983**

To study the confirmation bias, we select the sam- **984** ples from the test dataset where the LLM produces **985** a wrong answer. If the model performance is **986** affected by the noise of the labels it was trained **987** on, it is expected it will reproduce the mistakes **988** of the LLM; therefore, we would expect that it **989** will have a lower score in this subset of the test **990** dataset. We do not find that Margin Sampling and **991** Query by Committee have lower performance **992**

<span id="page-12-0"></span>

$\overline{N}$			<b>ISEAR RT-Polarity FEVER Openbook Average</b>			
	Random	0.629	0.882	0.679	0.567	0.689
	<b>Margin Sampling</b>	0.656	0.895	0.698	0.587	0.709
	Query by Committee	0.644	0.887	0.693	0.568	0.698
500	Entropy	0.657	0.895	0.698	0.586	0.709
	Coreset (T5)	0.633	0.886	0.669	0.570	0.689
	Coreset (SimCSE)	0.636	0.887	0.682	0.569	0.694
	Coreset (MPNet)	0.632	0.886	0.675	0.566	0.690
	Random	0.640	0.886	0.704	0.662	0.723
	<b>Margin Sampling</b>	0.666	0.896	0.725	0.703	0.748
	Query by Committee	0.656	0.889	0.725	0.687	0.739
	1000 Entropy	0.665	0.895	0.726	0.700	0.747
	Coreset (T5)	0.643	0.887	0.699	0.665	0.724
	Coreset (SimCSE)	0.646	0.888	0.704	0.661	0.725
	Coreset (MPNet)	0.641	0.888	0.704	0.661	0.724
	Random	0.652	0.884	0.724	0.729	0.747
	<b>Margin Sampling</b>	0.673	0.896	0.751	0.764	0.771
	Query by Committee	0.667	0.891	0.745	0.760	0.766
	2000 Entropy	0.672	0.893	0.747	0.756	0.767
	Coreset (T5)	0.656	0.886	0.719	0.733	0.749
	Coreset (SimCSE)	0.657	0.888	0.725	0.728	0.750
	Coreset (MPNet)	0.655	0.888	0.724	0.727	0.749
	Random	0.648	0.885	0.738	0.734	0.752
	<b>Margin Sampling</b>	0.669	0.895	0.757	0.767	0.772
	Query by Committee	0.665	0.890	0.758	0.773	0.771
3000	Entropy	0.664	0.893	0.752	0.760	0.767
	Coreset (T5)	0.651	0.885	0.733	0.740	0.752
	Coreset (SimCSE)	0.652	0.885	0.735	0.736	0.752
	Coreset (MPNet)	0.653	0.885	0.735	0.732	0.751

Table 8: Online accuracy (AUC) for neural caching without retraining.

**993** than front-loading in this subset of the dataset **994** (Table [10\)](#page-14-1).

## **996 B.5** Experiments with different encoders

**995**

 To test the validity of results for Coreset, we repeat experiments from Section [5.2](#page-5-2) with encoders SimCSE [\(Gao et al.,](#page-9-17) [2021\)](#page-9-17) and MP- Net [\(Song et al.,](#page-10-17) [2020\)](#page-10-17). For SimCSE, we use sup-simcse-bert-base-uncased from 1002 the project repository.<sup>[4](#page-12-1)</sup> For MPNet, we use sentence-transformers/all-mpnet-base-v2 from Huggingface. We use threshold = 0.9 for all 1005 the methods and retraining frequency  $f = 100$ .

**1006** We show our results in Table [11.](#page-14-0) We observe that **1007** front-loading outperforms Coreset with the three encoders. **1008**

## C Prompts used **<sup>1009</sup>**

The following are the prompts we used when call- **1010** ing the LLM. We have marked in blue one example, **1011** and in red the expected answer. **1012** 

- **ISEAR:** This is an emotion classification task. 1013 Only answer one of: 'joy', 'fear', 'anger', 1014 'sadness', 'disgust', 'shame', 'guilt'. **1015 INPUT:** During the period of falling in love, 1016 each time that we met and especially when we **1017** had not met for a long time. **1018 OUTPUT:** joy 1019
- RT-Polarity: This is a sentiment classification **1020** task for movie reviews. Only answer either **1021** 'positive' or 'negative'. **1022**

<span id="page-12-1"></span><sup>4</sup> <https://github.com/princeton-nlp/SimCSE>

<span id="page-13-1"></span>

Figure 5: Accuracy curve with respect to budgets, in the neural caching problem with student retraining. Error lines indicate variance.

	<b>ISEAR RT-Polarity Openbook FEVER Average</b>			
Soft labels 0.598	0.880	0.617	0.670	0.691
Hard labels 0.598	0.879	0.616	0.659	0.688

<span id="page-13-0"></span>Table 9: Final accuracy (AUC) of the last student model, taking either soft or hard labels from the LLM.

<span id="page-14-1"></span>

Table 10: Accuracy (AUC) over the subset of the test dataset where the LLM produces wrong labels for the last student model for neural caching with student retraining.

<span id="page-14-0"></span>

		<b>FEVER Openbook</b>
Front-loading	0.734	0.731
Coreset (SimCSE)	0.707	0.726
Coreset (MPNet)	0.716	0.724
Coreset (T5)	0.715	0.726

Table 11: Online accuracy (AUC) for neural caching with student retraining.



# **1045 D Additional information about <sup>1046</sup>** datasets

 Datasets used RT-Polarity, FEVER and Openbook were relased as NLP benchmarks for classification. While ISEAR was orig- inally released as part of a psychological study on emotion across cultures, it has been

used as an Active Learning benchmark in the **1052** past [\(Ein-Dor et al.,](#page-9-18) [2020;](#page-9-18) [Bastos and Kaul,](#page-8-12) **1053** [2021\)](#page-8-12). **1054**

We did not check if these datasets contain any 1055 information that names or uniquely identifies **1056** individual people or offensive content because **1057** the data we use comes from established clas- **1058** sification/multiple choice benchmarks. A cus- 1059 tom filtering or modification of the data would **1060** hamper comparability with other works using 1061 these benchmarks. **1062**

Dataset generated We release the soft la- **1063** bels from the LLM under the CC BY 4.0 **1064** DEED license. We refer to the original data **1065** sources for documentation such as coverage **1066** of domains, languages or linguistic phenom- **1067** ena. **1068**